



Instituto de Estructura de la Materia – Consejo Superior de Investigaciones Científicas

## Single particle versus collectivity, shapes of exotic nuclei

Andrea Jungclaus

*Instituto de Estructura de la Materia, CSIC – Madrid, Spain*

**Rewriting Nuclear Physics textbooks  
30 years with Radioactive Ion Beam Physics**

Pisa (Italy), July 20<sup>th</sup> – 24<sup>th</sup>, 2015



Photo copyright Robert Charity 2014

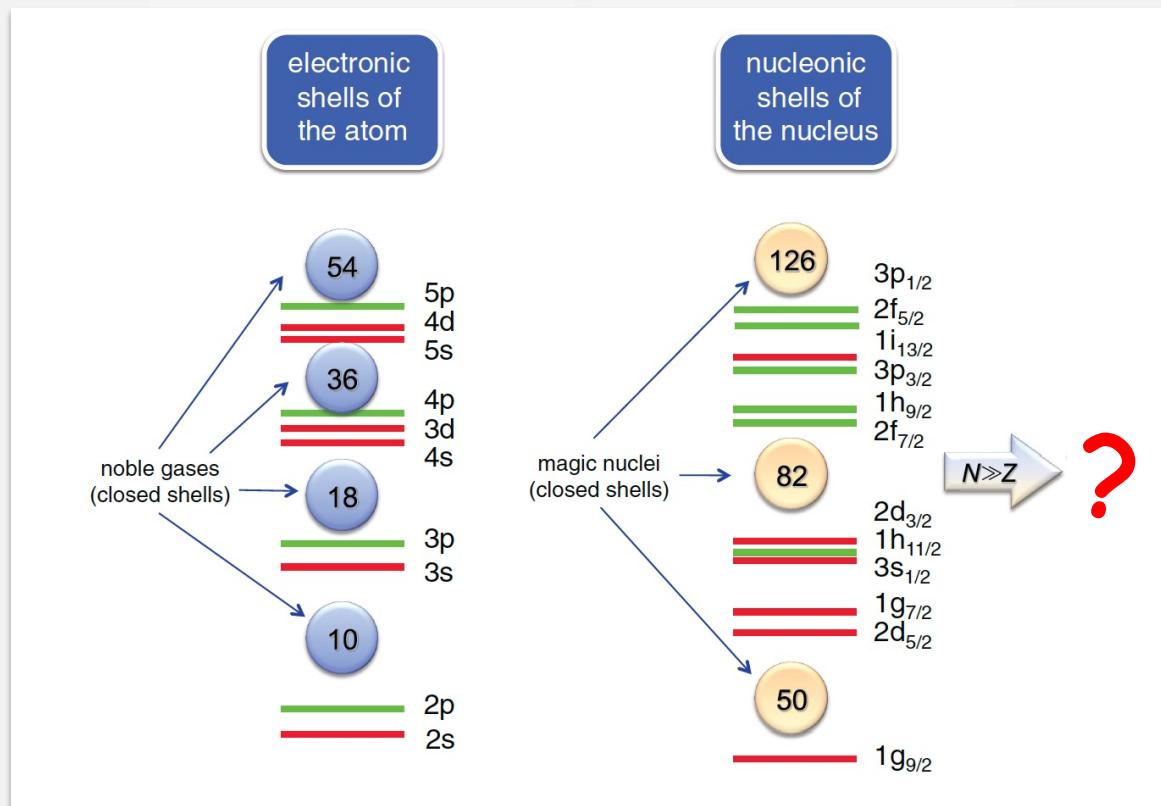
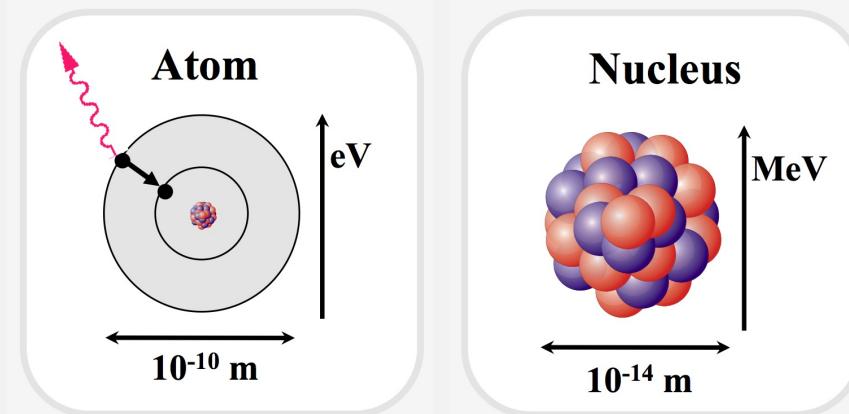
# Single particle versus collectivity, shapes of exotic nuclei

- What a title ! A bit of everything ...
- Start with some reminders of “classical” nuclear physics
- What’s new over the last 30 years ?  
From the perspective of an observer of the field since 1989 ...  
(pure experimentalist,  $\gamma$ -ray spectroscopist interested in  $A > 70$  nuclei)

**Rewriting Nuclear Physics textbooks  
30 years with Radioactive Ion Beam Physics**

- Radioactive ion beams are an important part, but not the whole story !
- Small selection of examples – only limited time ...
- I will simplify (hopefully without getting things wrong), omit, not always show latest etc.
- Try to avoid topics which others may already have shown

# The shell structure of atomic nuclei



Remember:  
Two independent parameters  
in atomic nuclei,  $Z$  and  $N$  !

"Shell evolution":  
Next part of my talk ...

# The shell structure of atomic nuclei

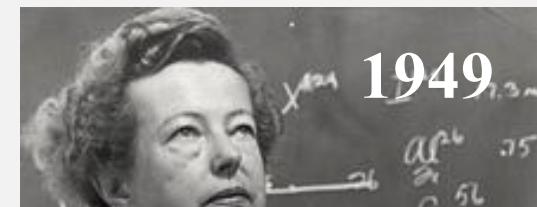
Atom



Nucleus



1949



Nobel Prize in Physics 1963



Eugene Paul Wigner  
Prize share: 1/2

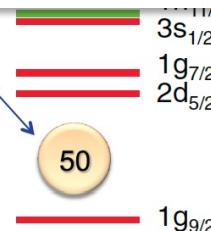
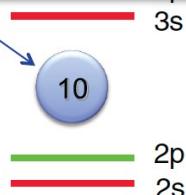


Maria Goeppert  
Mayer  
Prize share: 1/4



J. Hans D. Jensen  
Prize share: 1/4

noble gases  
(closed shells)



gent parameters  
ei, Z and N !

"Shell evolution":  
Next part of my talk ...

# The birth of the collective models in 1952

## Interpretation of Isomeric Transitions of Electr

AAGE BOHR  
*Institute for Theore*  
(Receiv

IN the recent classificat  
electric quadrupole  
examples of lifetimes ap  
basis of the shell model. I  
more than a factor of a h  
we have here the effect  
motion.<sup>1</sup>

A natural interpretation  
model describing the nucl  
motion and nuclear surf  
model, the low-lying state  
of the particle structure  
the surface, or by an exci  
the particle quantum nun  
states are of the former ch  
means of the shell model.  
however, that transition

## Rotational States in Even-Even Nuclei

AAGE BOHR AND BEN R. MOTTELSON\*  
*Institute for Theoretical Physics, Copenhagen, Denmark*  
(Received March 24, 1953)

IN a recent note,<sup>1</sup> an interpretation of the short-lived  $E2$  iso  
mers has been suggested in terms of rotational states of the  
deformed nucleus. Empirical evidence is rapidly accumulating on  
the low energy spectra of even-even nuclei;<sup>2-4</sup> the purpose of the  
present note is to call attention to the extensive support which  
exists in these data for the above interpretation, and to suggest  
its usefulness in the analysis of decay schemes.

In the model describing the nucleus in terms of the coupled  
particle motion and surface oscillations, low-lying rotational states  
are associated with the large deformations expected in regions with  
many particles outside of closed shells. In such regions, the rota  
tional spectrum is expected to be given rather accurately by the  
simple expression<sup>1</sup>

$$E_I = \frac{\hbar^2}{2g} I(I+1), \quad I=0, 2, 4, 6, \quad (1)$$

even parity

Nov. 1952

March 1953

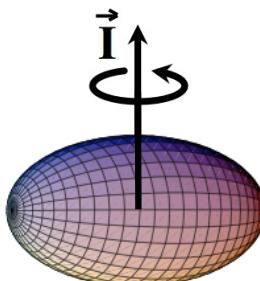
# First observation of rotational bands

Three examples from 1953:

Fine structure in  $\alpha$  decay

Nobel Prize in Physics 1975

rotations -



even-even  
nucleus



Aage Niels Bohr



Ben Roy Mottelson



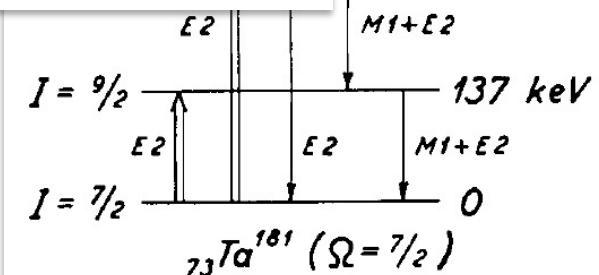
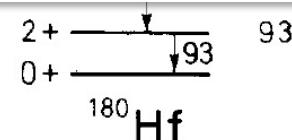
Leo James Rainwater

— 146  
— 43  
—

experiment

303 keV

$$E(4^+)/E(2^+) \sim 3.3$$



Bohr Nobel Lecture

# The problem of the “wrong” moment of inertia

Det Kongelige Danske Videnskabernes Selskab

Matematisk-fysiske Meddelelser, bind 30, nr. 1

Dan. Mat. Fys. Medd. 30, no. 1 (1955)

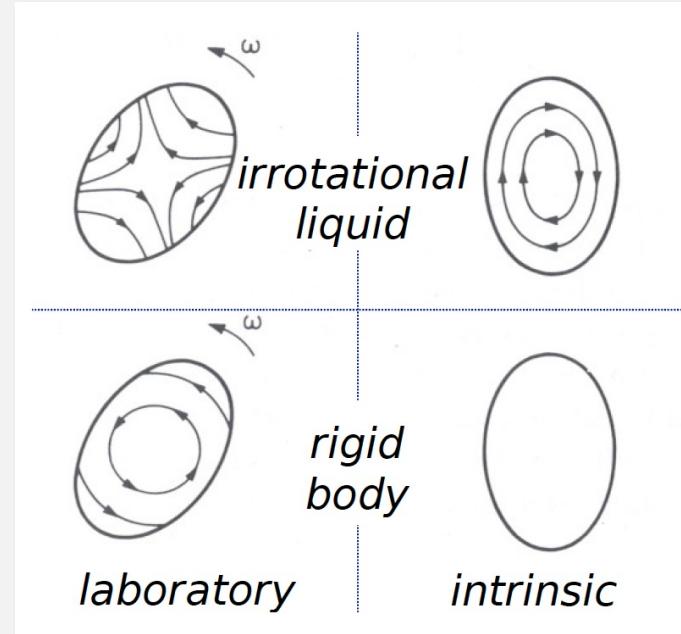
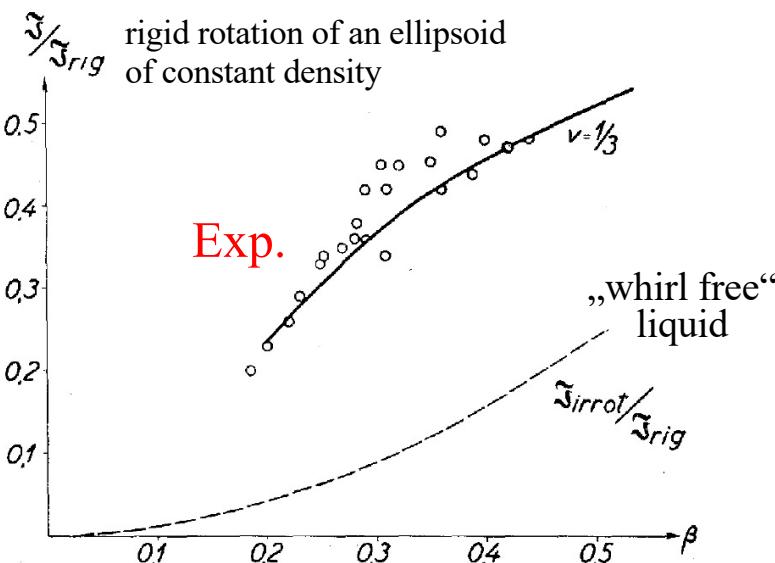
DEDICATED TO PROFESSOR NIELS BOHR ON THE  
OCCASION OF HIS 70TH BIRTHDAY

1955

## MOMENTS OF INERTIA OF ROTATING NUCLEI

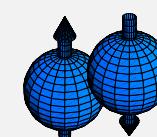
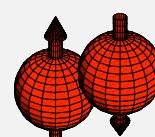
BY

AAGE BOHR AND BEN MOTTELSON

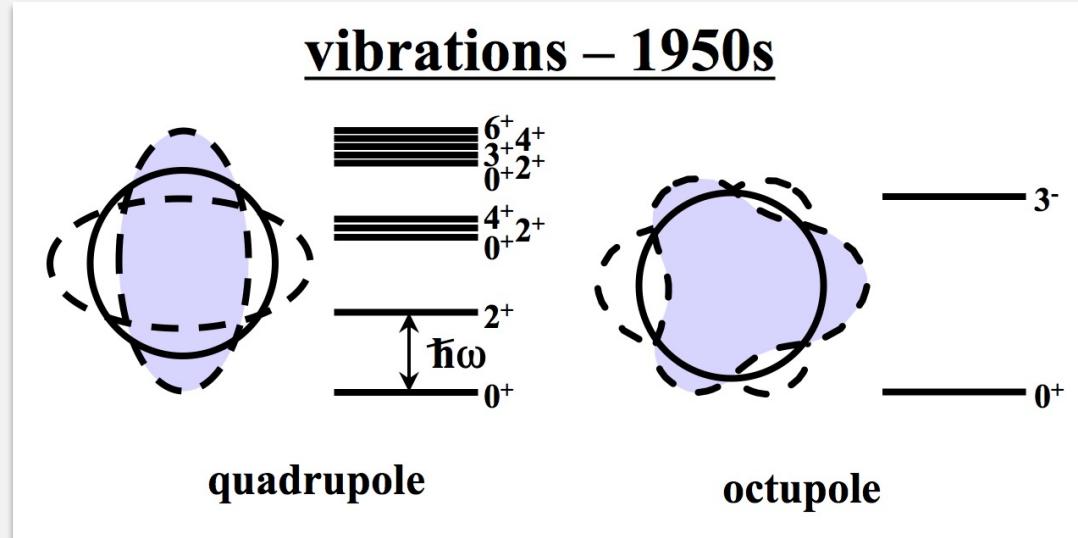
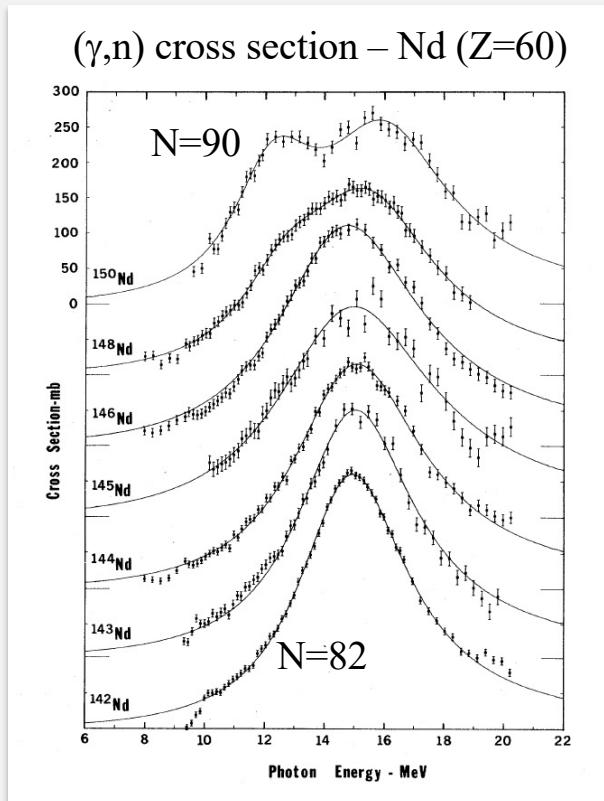


„Nuclei are like egg shells which are filled with a mixture of a normal and a superconducting liquid !“

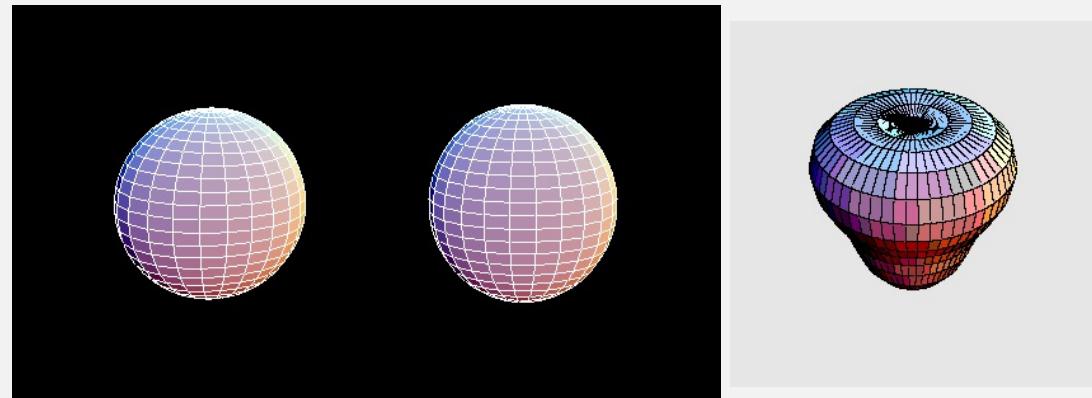
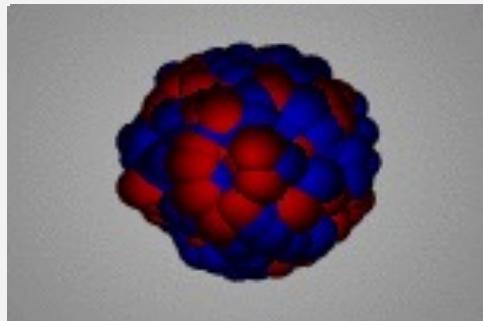
Super conductivity due to **pairing forces** in analogy to the Cooper pairs (electrons) in superconductors.



# The vibrational degree of freedom



Giant Dipole Resonance



# Deformed nuclei in the Nilsson model

Det Kongelige Danske Videnskabernes Selskab

Matematisk-fysiske Meddelelser, bind 29, nr 16

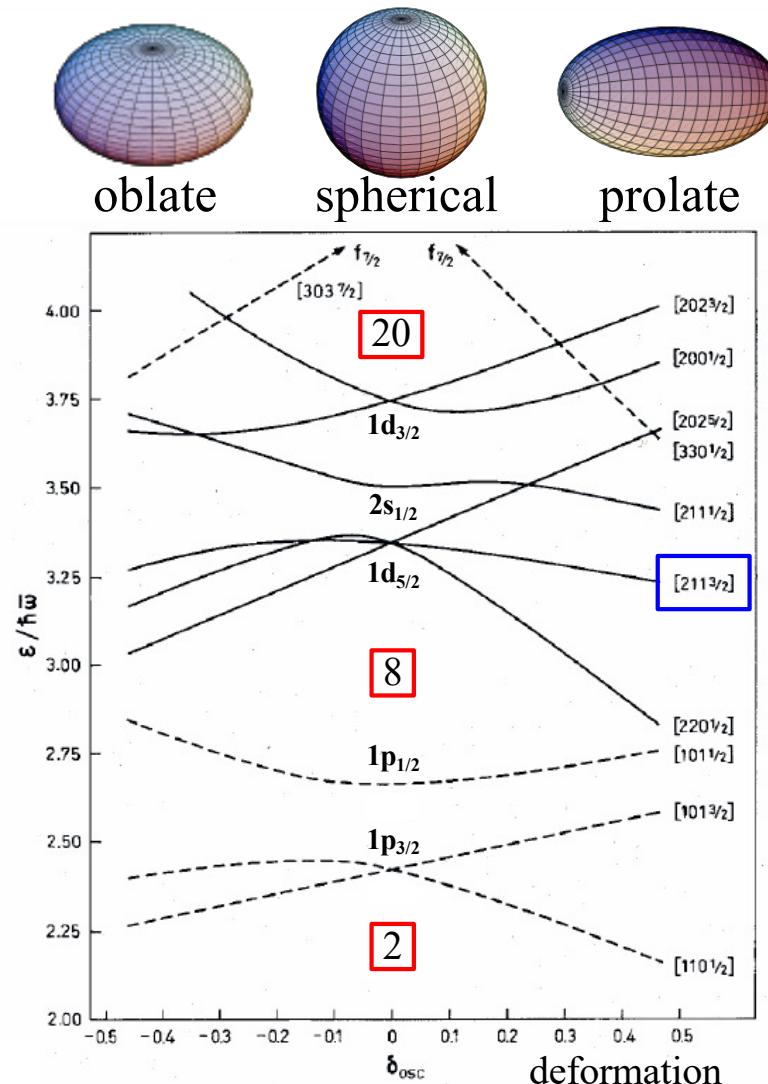
Dan Mat Fys Medd 29, no 16 (1955)

1955

## BINDING STATES OF INDIVIDUAL NUCLEONS IN STRONGLY DEFORMED NUCLEI

BY

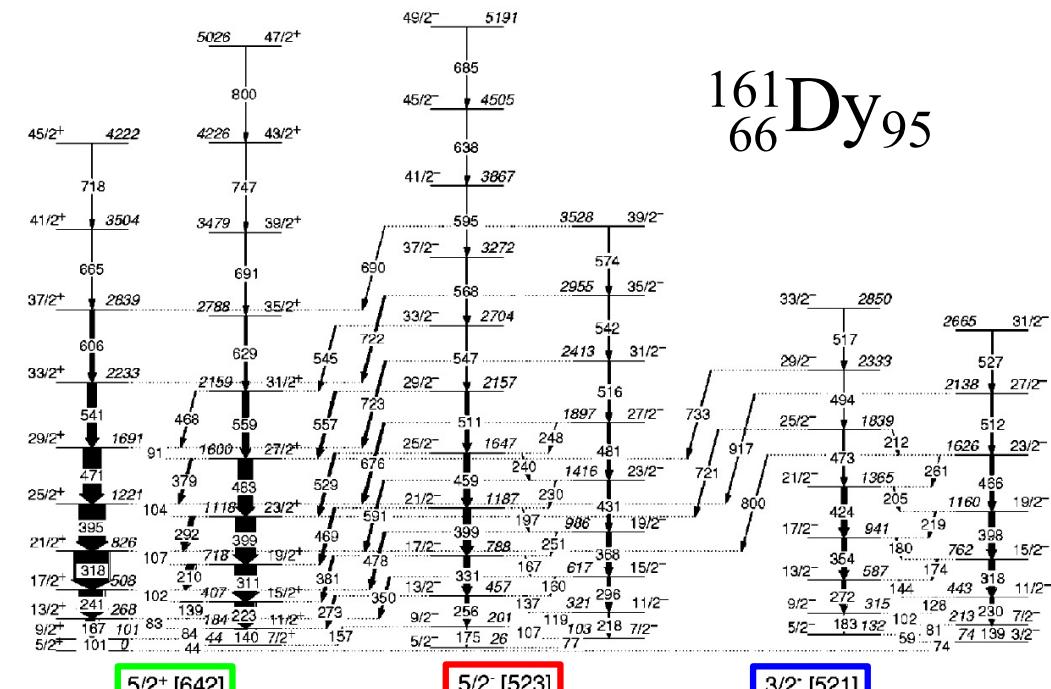
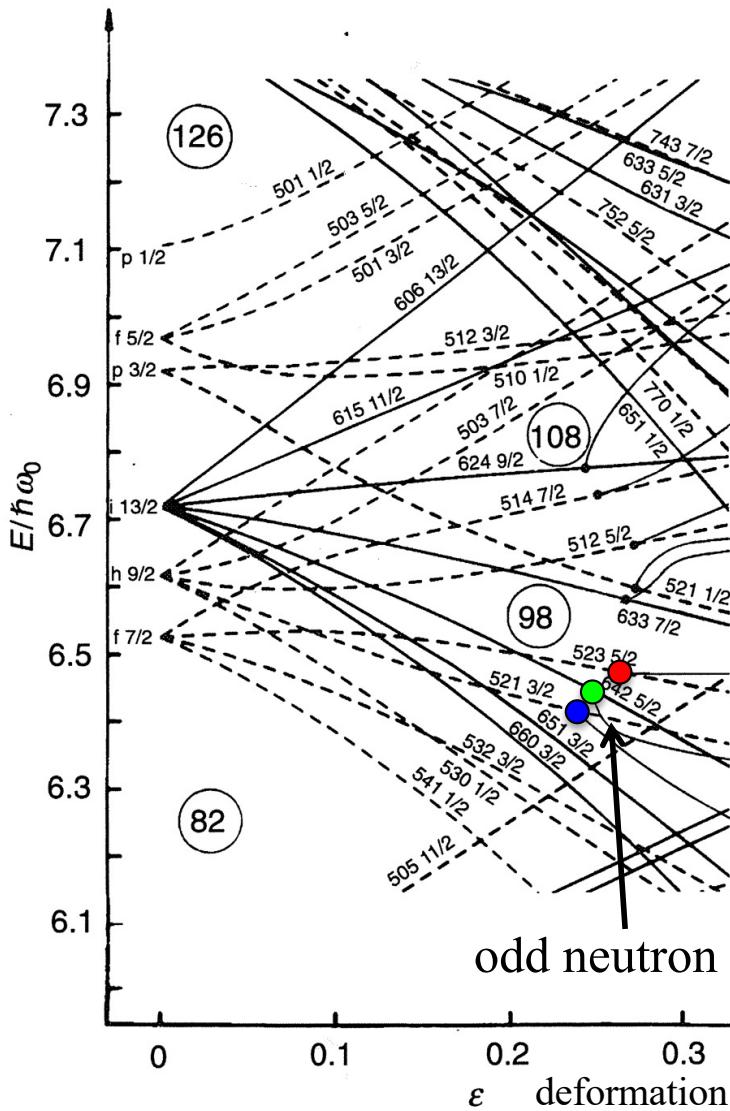
SVEN GÖSTA NILSSON



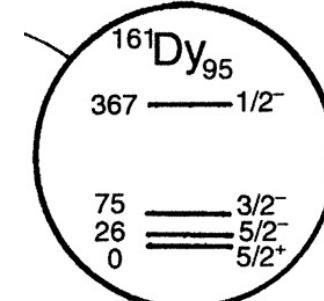
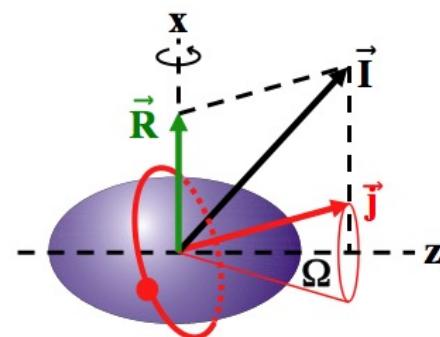
new asymptotic  
quantum numbers

$2j+1$ -fold degeneration is removed,  
states with  $+m$  and  $-m$  still degenerate !

# Single-particle motion in a deformed field

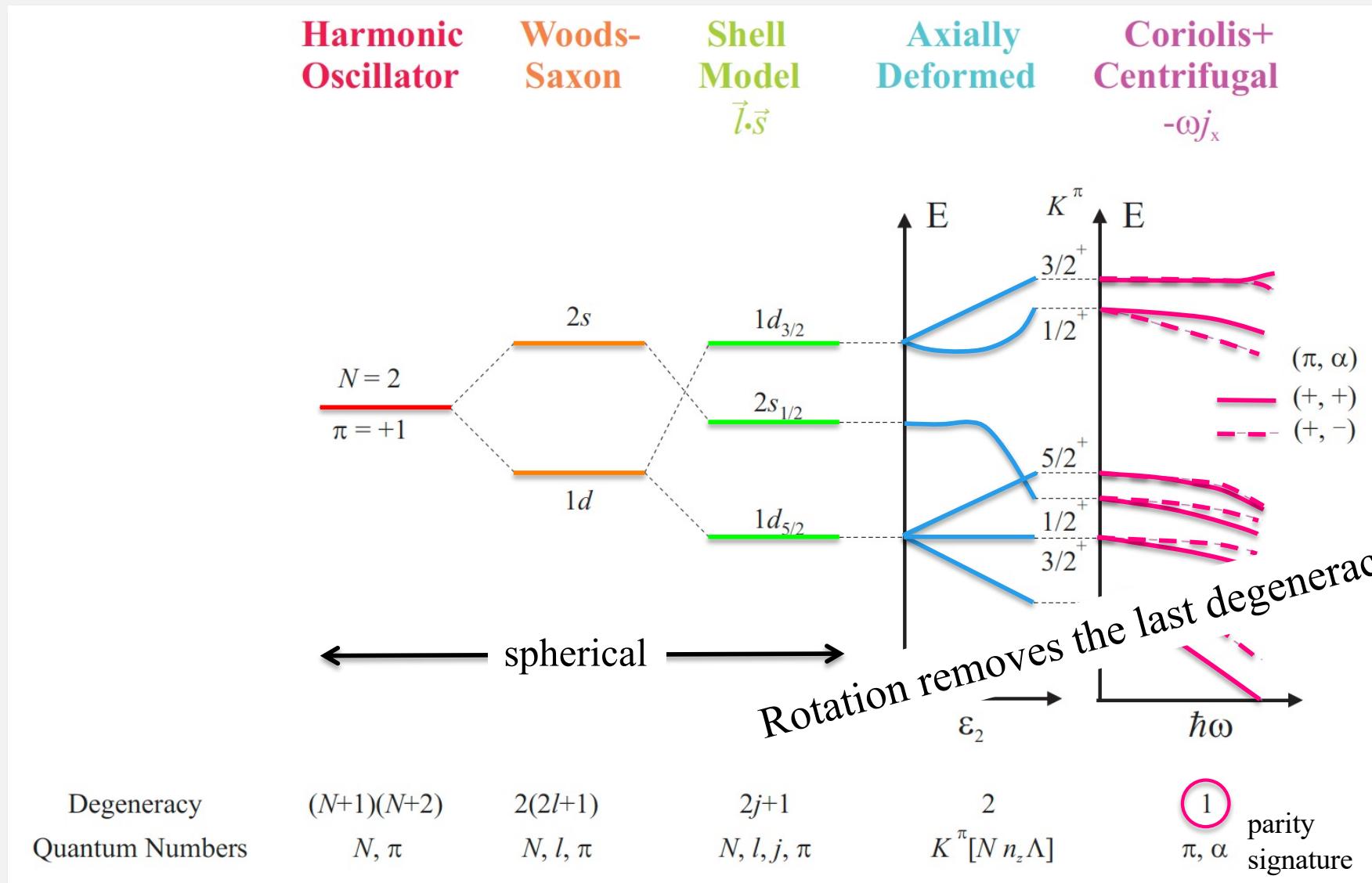


A. Jungclaus et al., Phys. Rev. C67, 034302 (2003)



Three rotational band heads within 75 keV!

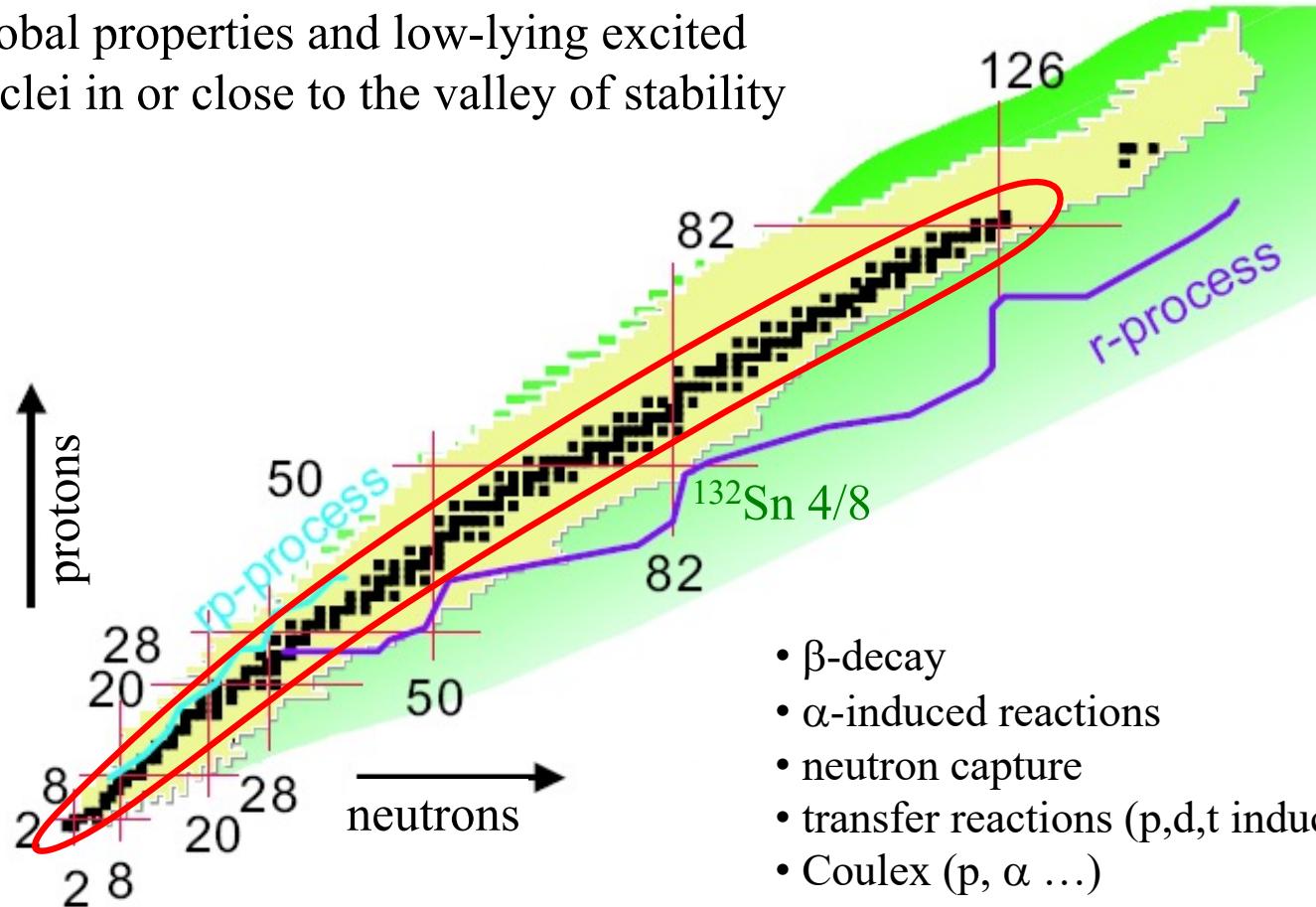
# Single-particle motion in a rotating deformed field



Single-particle energies depend on deformation and rotational frequency !

## Over the next twenty years ...

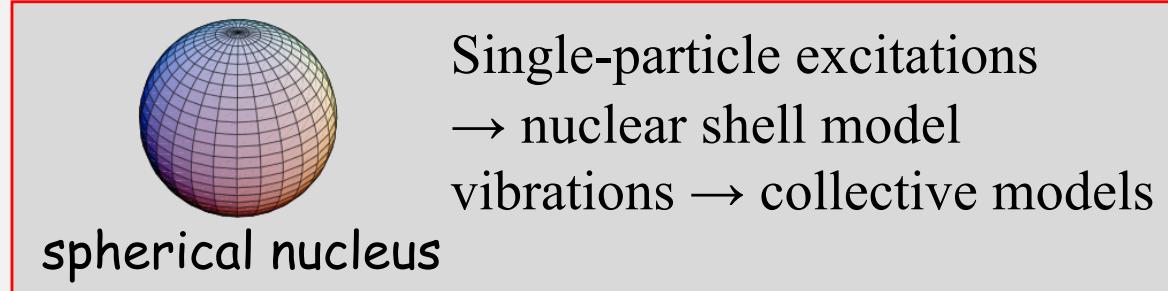
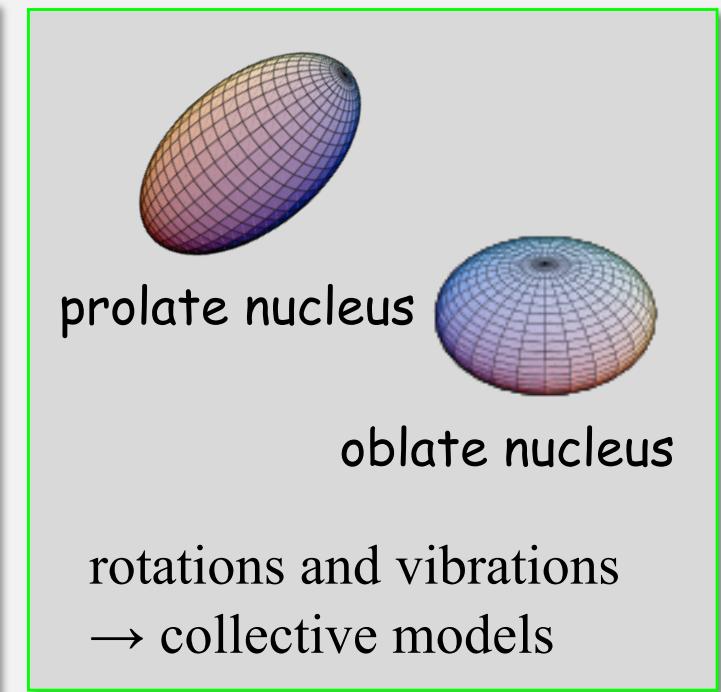
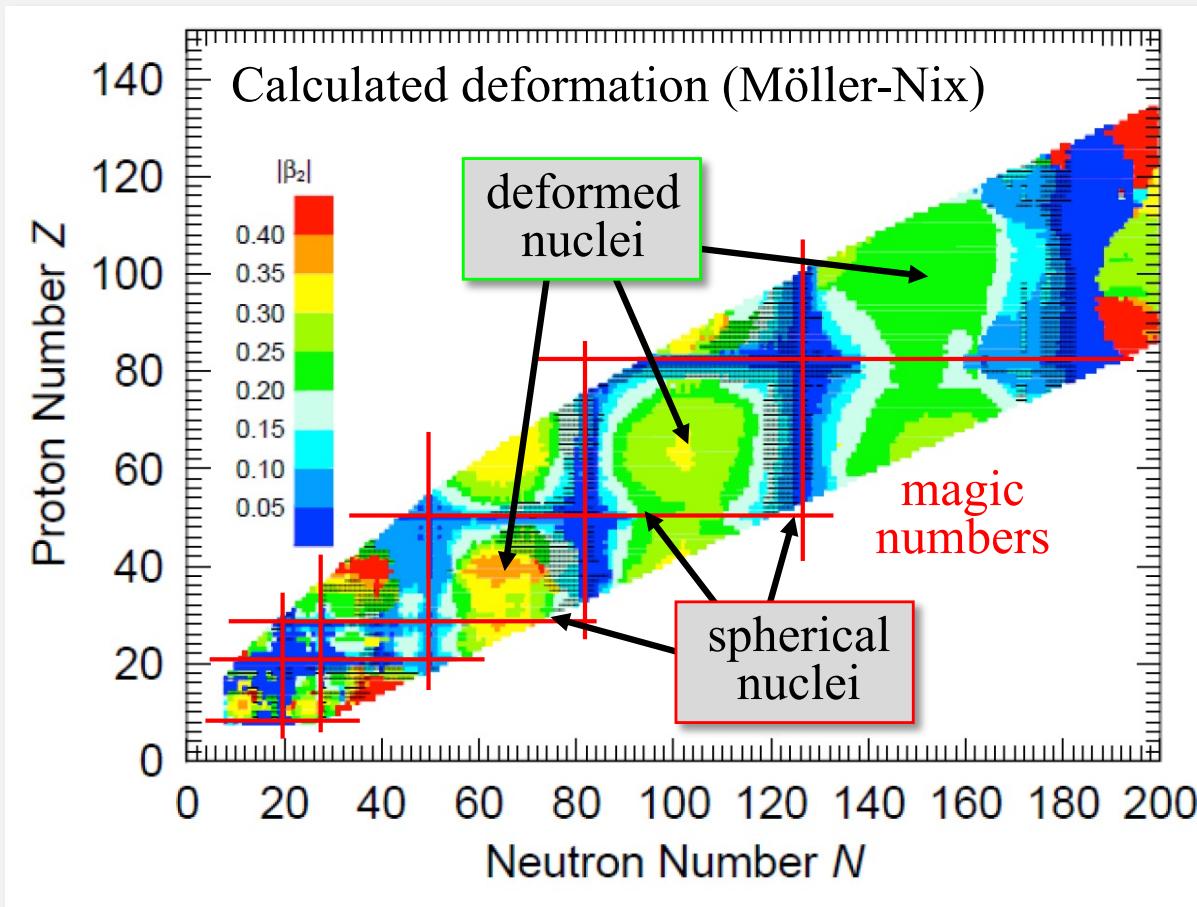
Study of global properties and low-lying excited states of nuclei in or close to the valley of stability

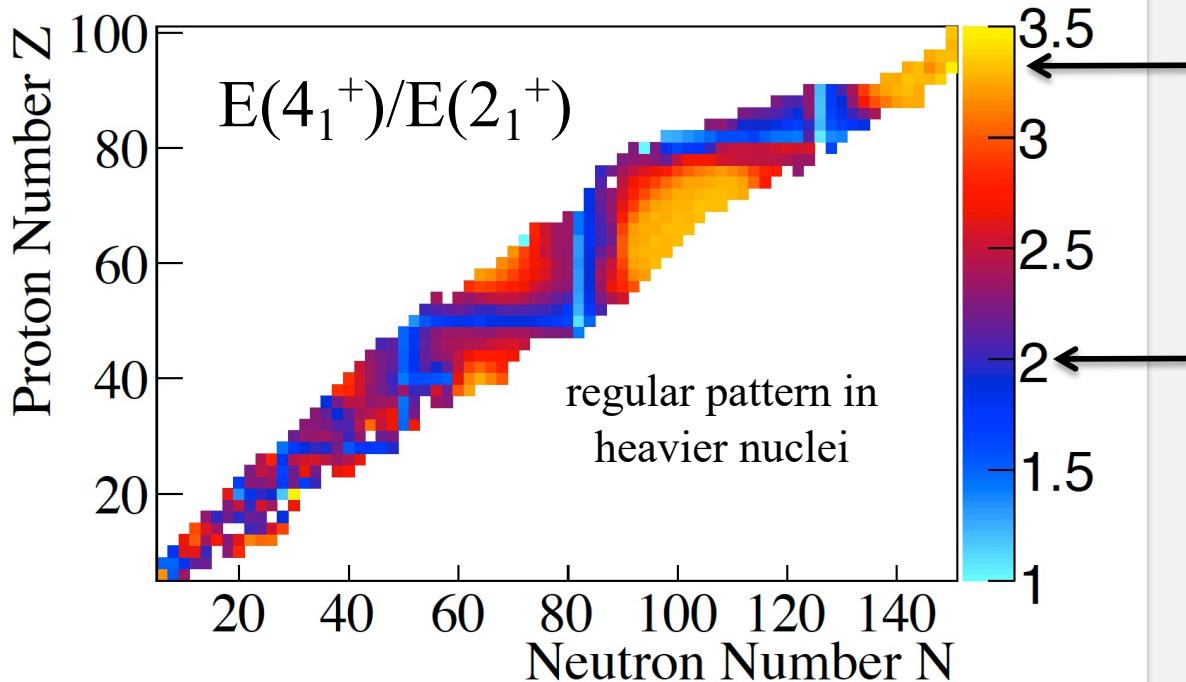
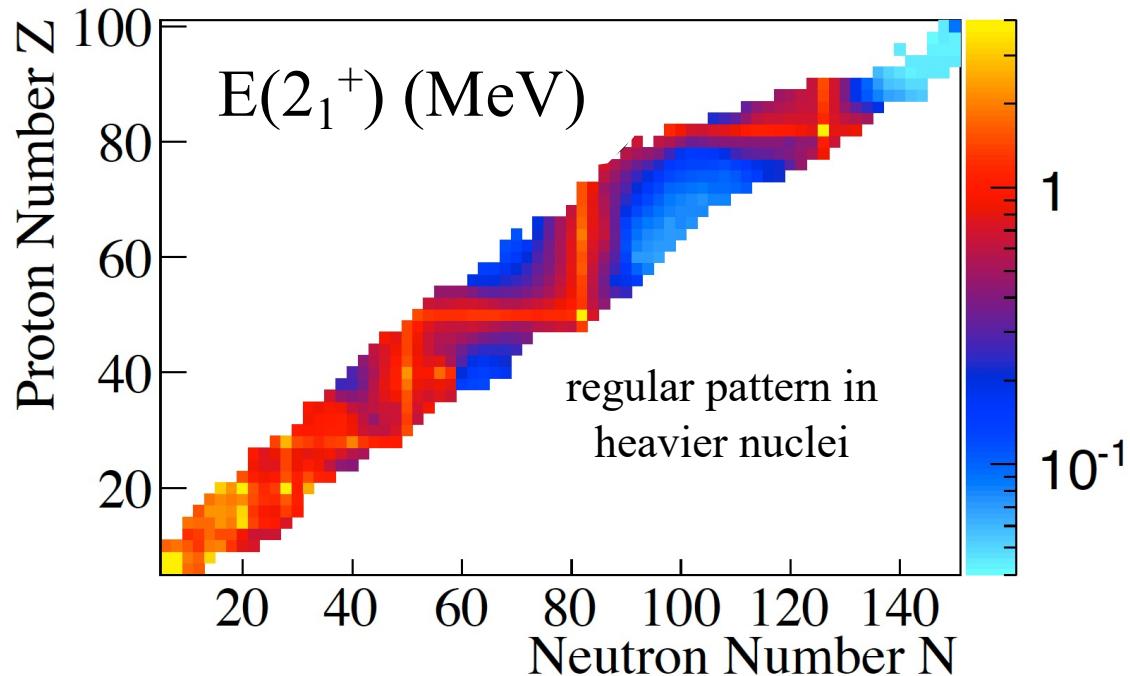


- $\beta$ -decay
  - $\alpha$ -induced reactions
  - neutron capture
  - transfer reactions ( $p, d, t$  induced)
  - Coulex ( $p, \alpha \dots$ )
  - $\gamma$ -induced neutron emission
- scattering experiments ( $e, p \dots$ )

Radii and density distributions !

# „Classical“ nuclear physics





$E(2^+)$  and  $E(4^+)/E(2^+)$  as global indicators in even-even nuclei

Rotations

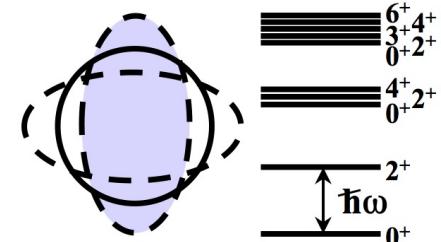
- $8^+$
- $6^+$
- $4^+$
- $2^+$
- $0^+$

$$E_x = I(I+1) \frac{\hbar^2}{2J}$$

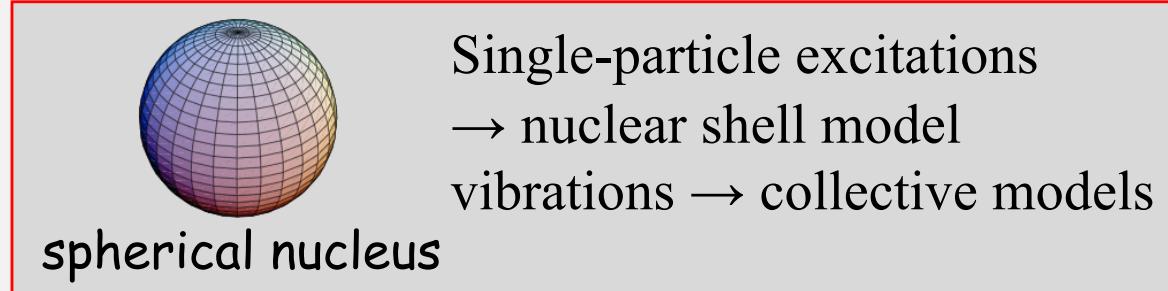
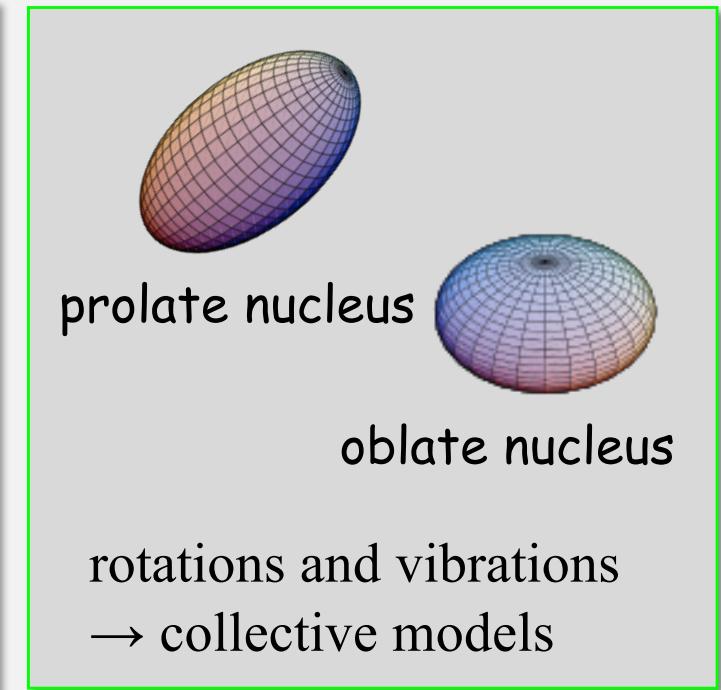
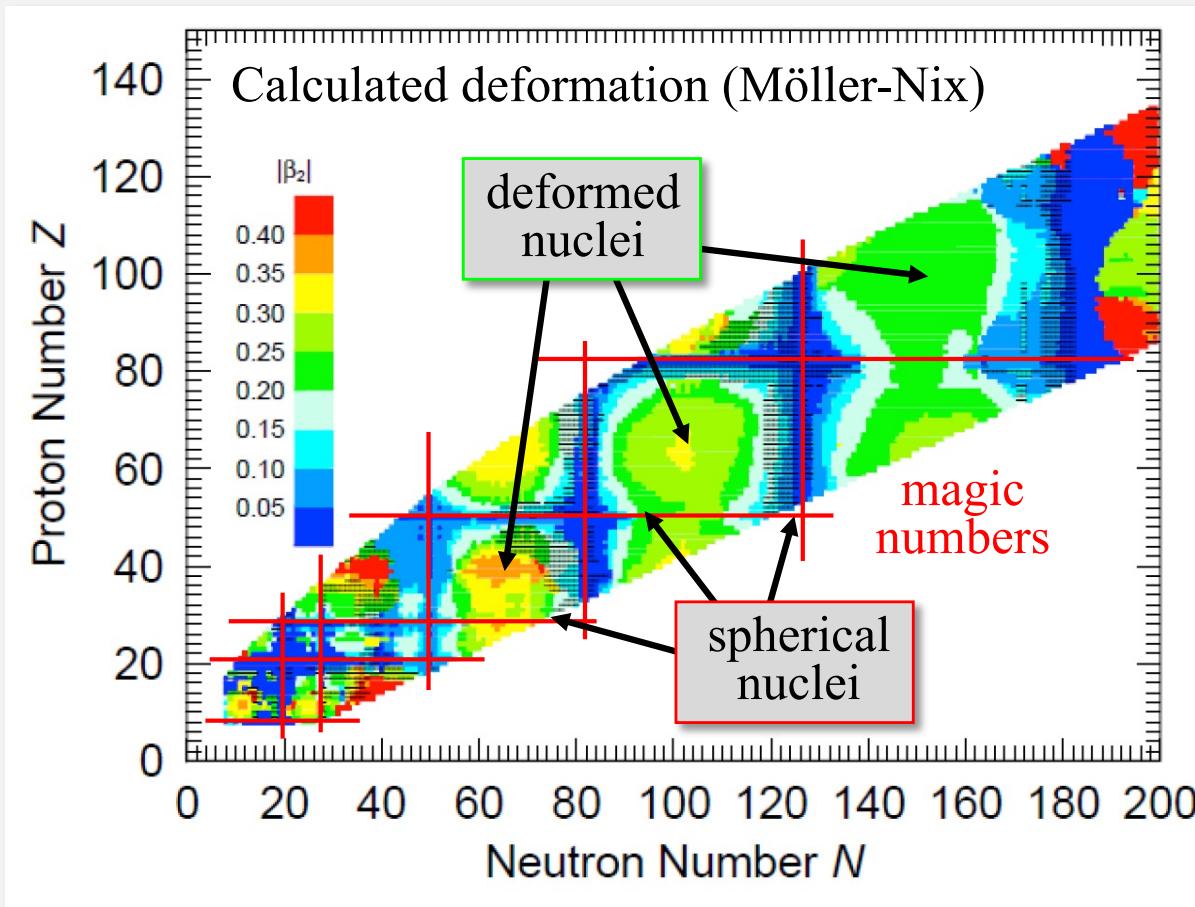
$$\begin{aligned} E(4_1^+)/E(2_1^+) \\ =(4^*/5)/(2^*3) \\ =20/6=3.3 \end{aligned}$$

$$\begin{aligned} E(4_1^+)/E(2_1^+) \\ =2\hbar\omega/\hbar\omega=2 \end{aligned}$$

Quadrupole vibrations



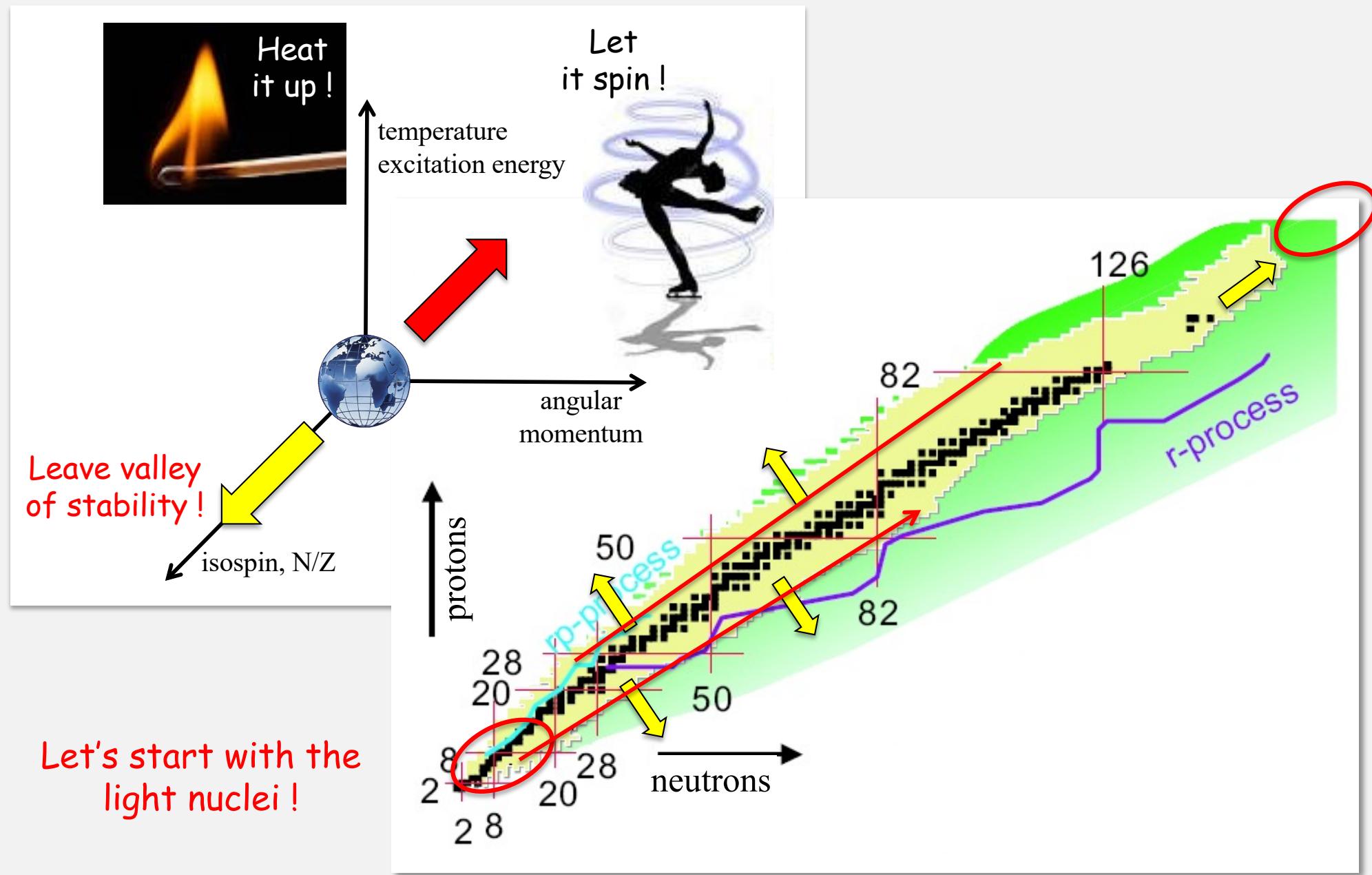
# „Classical“ nuclear physics



Is that already  
the full story ?

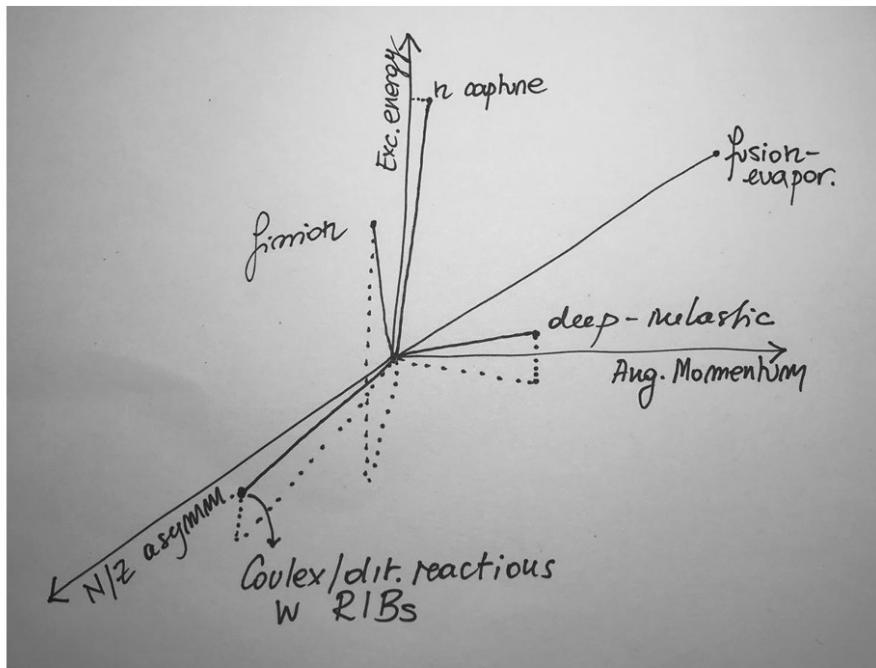
No !!!!!!!!

# Let's play with all degrees of freedom



# Three main “research axes”

To study nuclear structure under “extreme conditions”



Each production mechanism is characterised by :

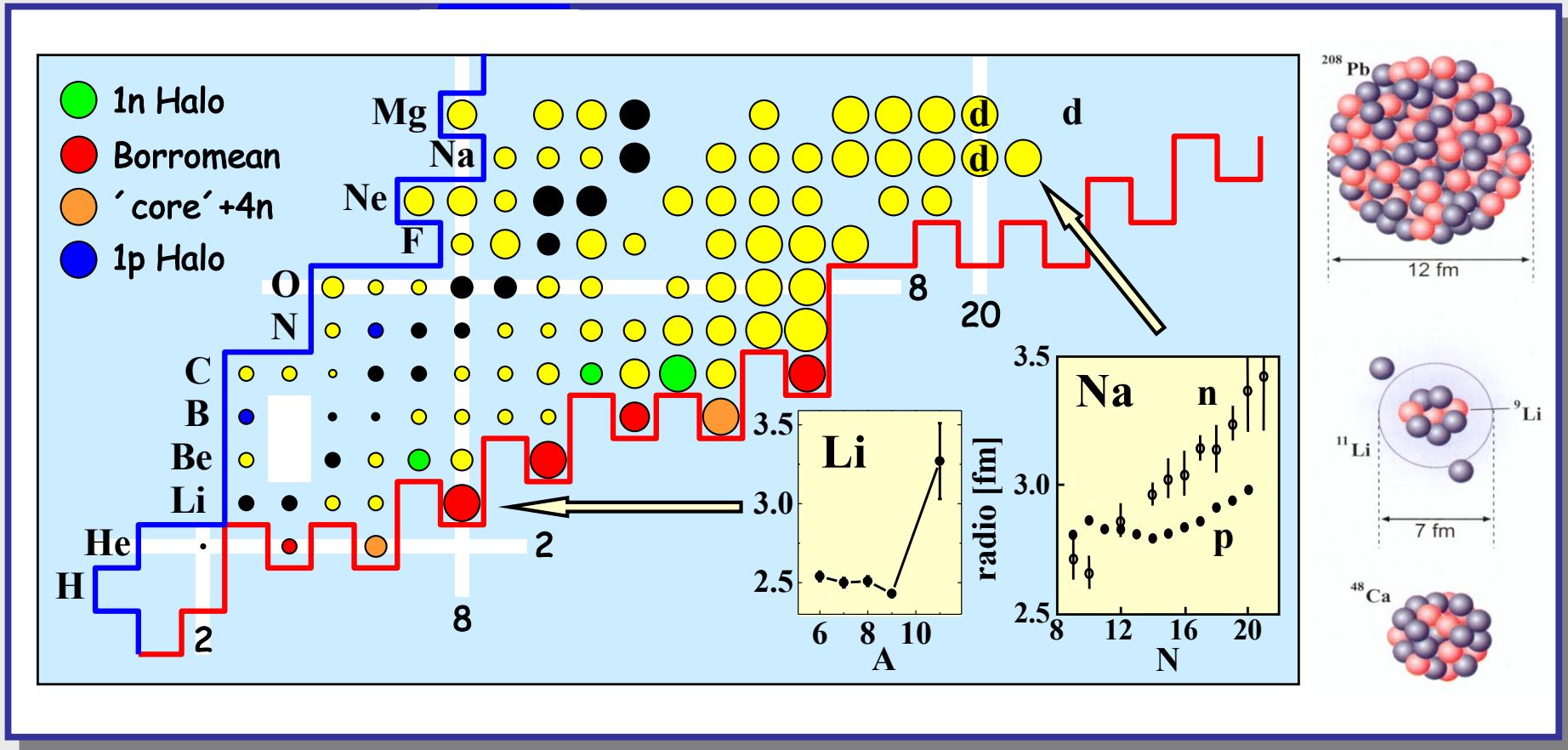
- (max) angular momentum, excitation energy and N/Z asymmetry
- Different cross sections (few mbarn for fusion-evaporation, up to  $10^5$  barn for neutron capture)
- Different recoil velocities ( $\beta \sim 0$  for n capture reactions, up to 50% for RIBs from fragmentation)
- Different needs for channel selectivity (ancillary detectors – charged particle detectors, mass separators...)

THE EUROPEAN NEUTRON SOURCE



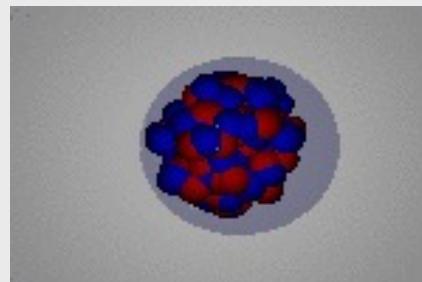
Caterina Michelagnoli, 1. Lecture

# Nuclear radii - halos and neutron skins



Remember:

- $R = r_0 \cdot A^{1/3}$        $r_0 = 1.1\text{-}1.2 \text{ fm}$
- The thickness  $t$  of the nuclear surface is constant.
- Protons and neutrons are uniformly mixed.

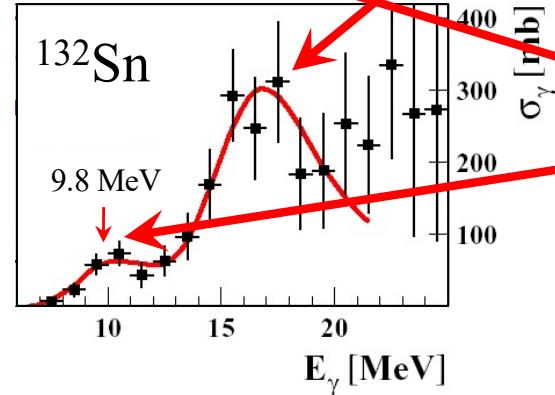
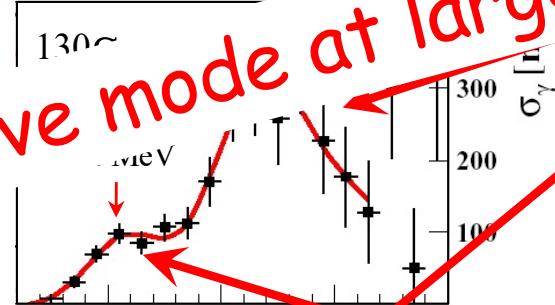
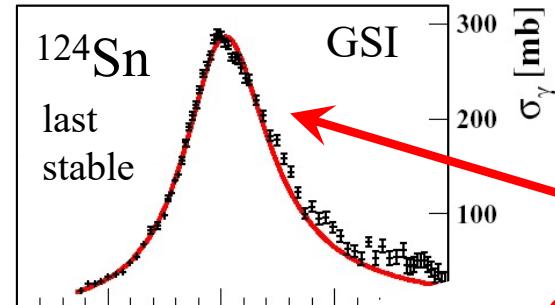


# The Pygmy resonance in neutron-rich Sn isotopes

neutron number  
N ↓  
82  
74

A new collective mode at large isospin!

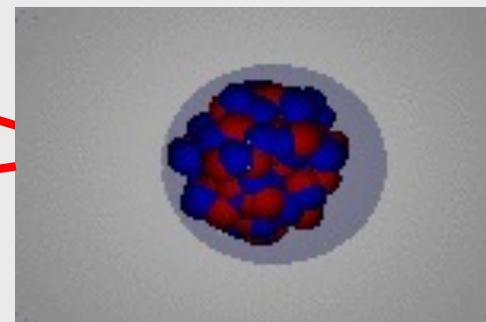
photo-neutron cross section



Giant Dipole Resonance

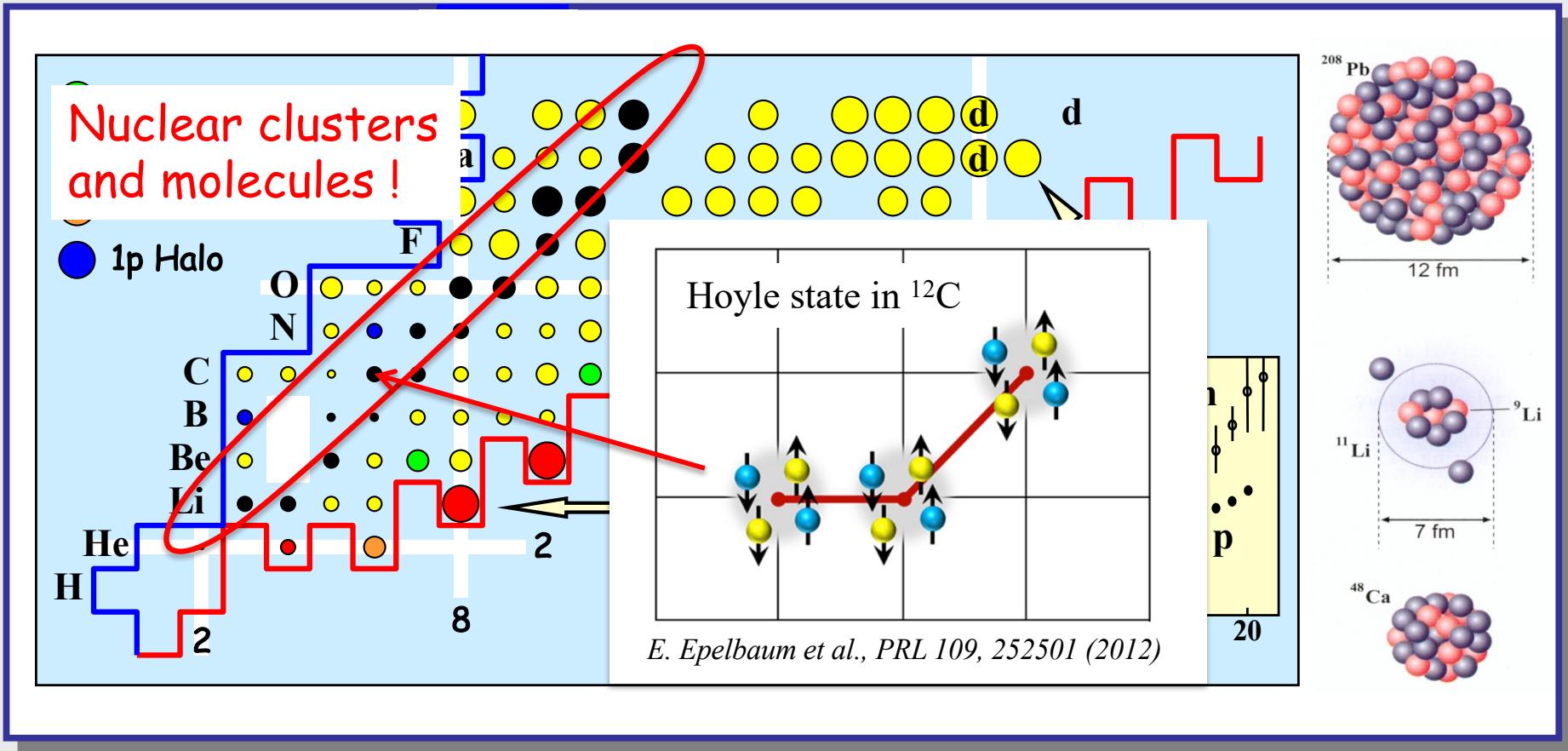


Pygmy Resonance



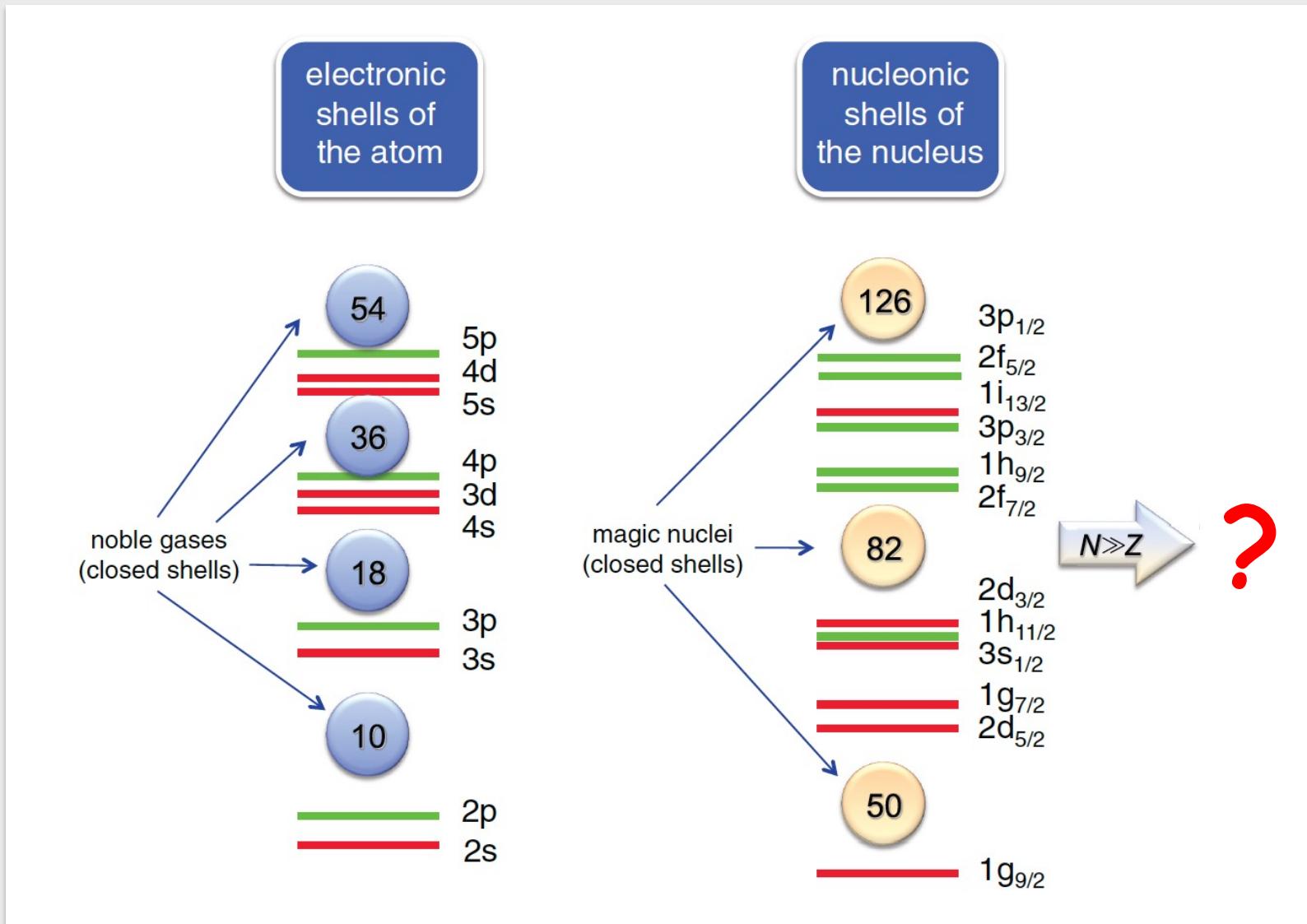
P. Adrich et al.  
*Phys. Rev. Lett.* 95 (2005) 132501

# Nuclear radii - halos and neutron skins



Light nuclei are indeed a rich playground !

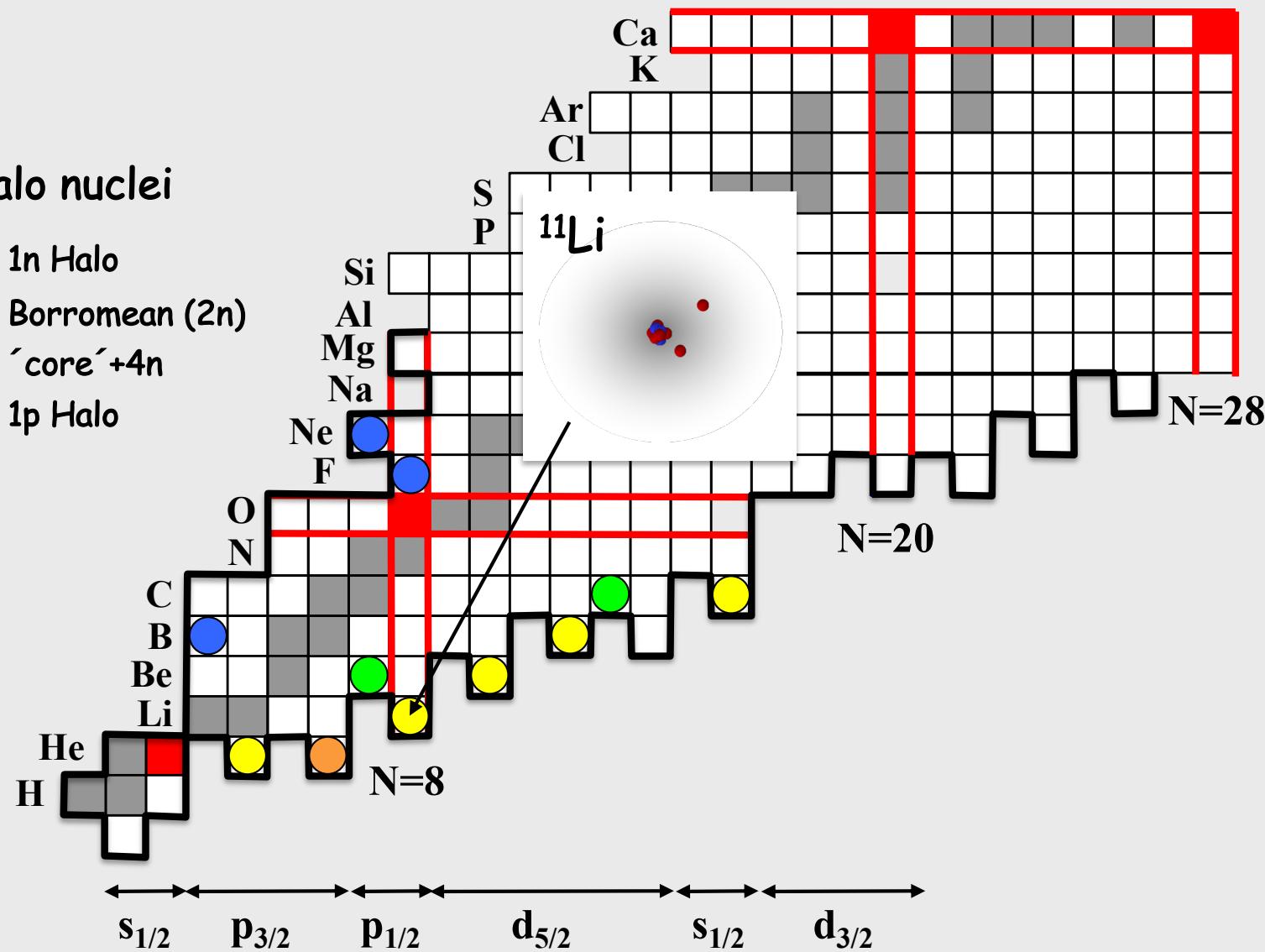
# "Shell evolution" on the neutron-rich side



# Neutron halos and the N=8 shell closure

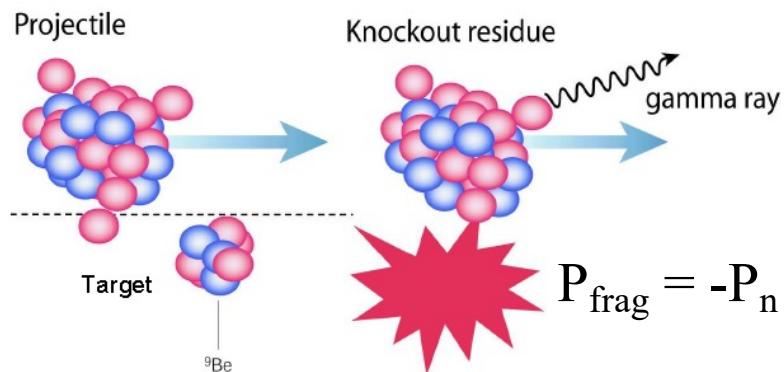
Halo nuclei

- 1n Halo
- Borromean (2n)
- 'core' +4n
- 1p Halo



# Knockout reactions at relativistic energies

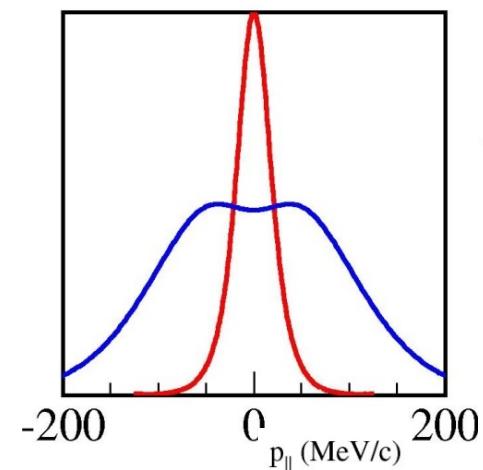
## knockout reaction



$$P_{\text{frag}} = -P_n$$

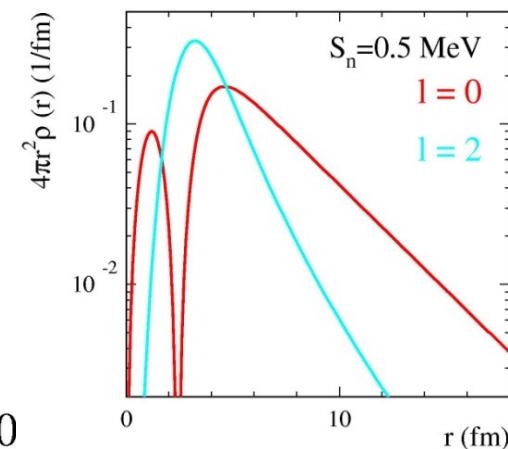
Heisenberg's uncertainty principle

momentum distribution



narrow momentum distribution

density distribution



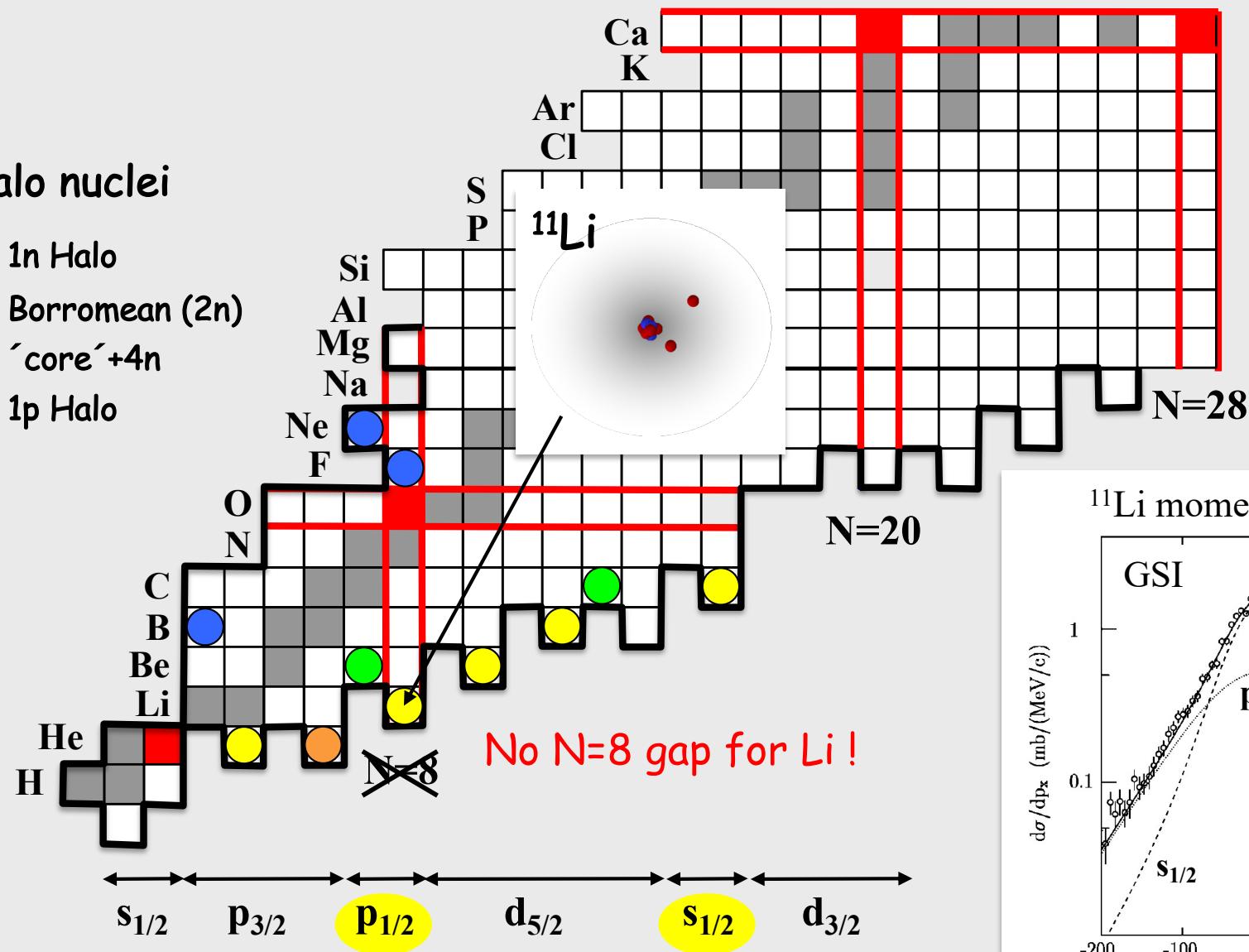
extended wavefunction

→ angular momentum  $\ell$  of the removed nucleon

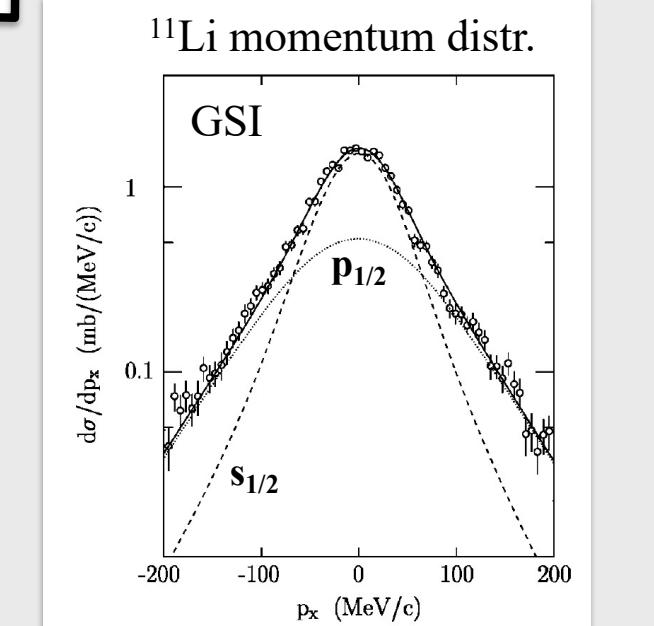
# Neutron halos and the N=8 shell closure

Halo nuclei

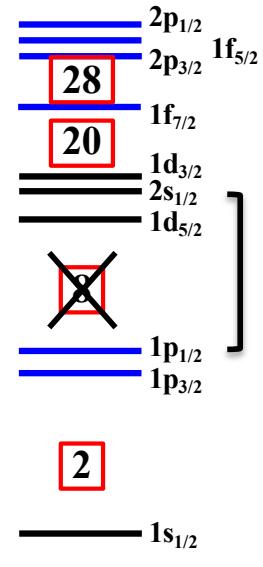
- 1n Halo
- Borromean (2n)
- 'core' + 4n
- 1p Halo



strong s-wave admixture



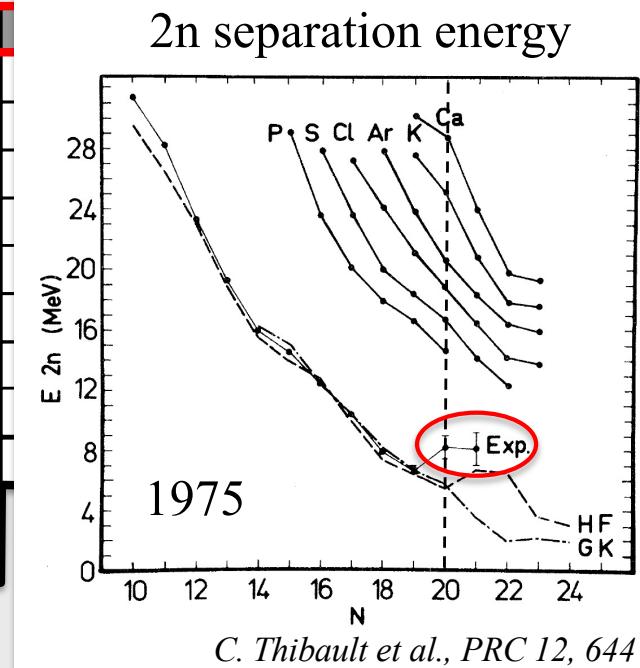
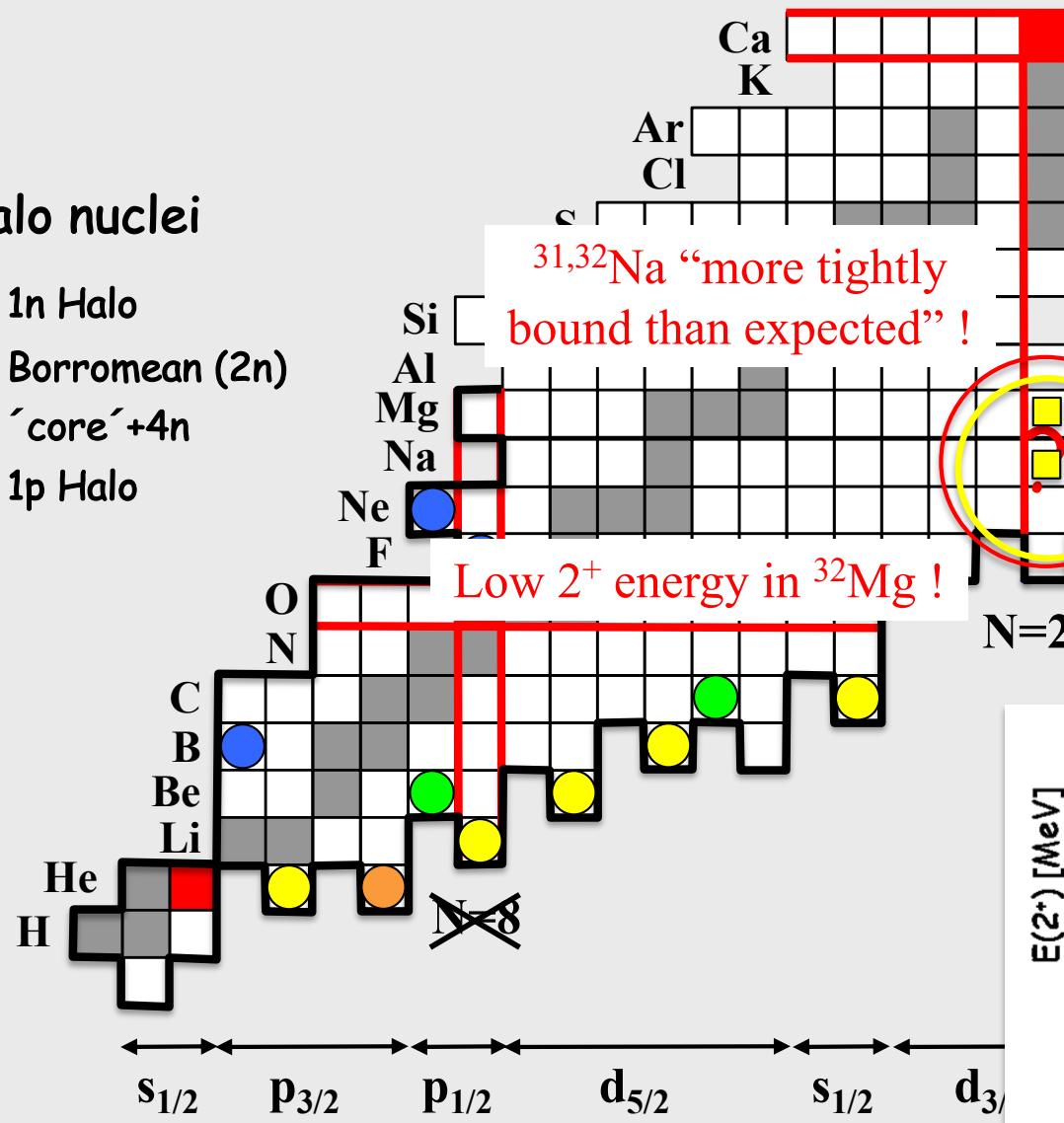
*H. Simon et al., Phys. Rev. Lett. 83, 496 (1999)*



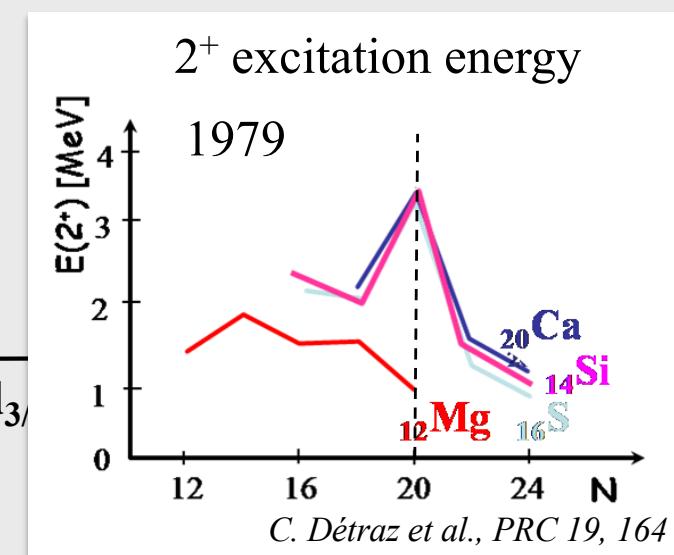
# What about the N=20 shell closure ?

Halo nuclei

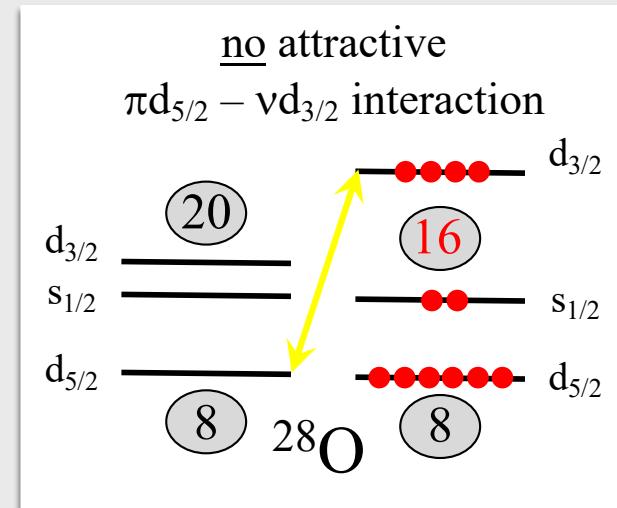
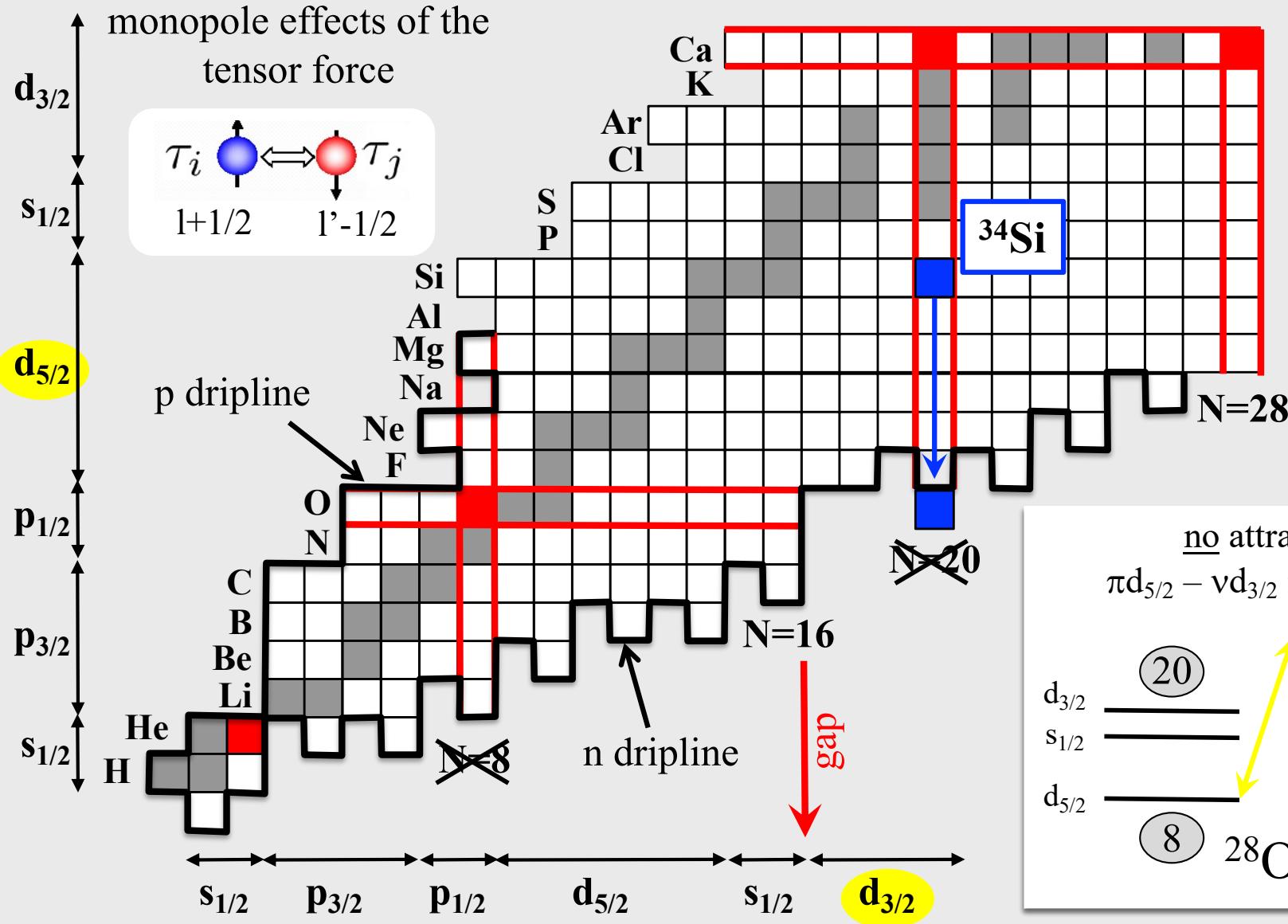
- 1n Halo
- Borromean (2n)
- 'core' +4n
- 1p Halo

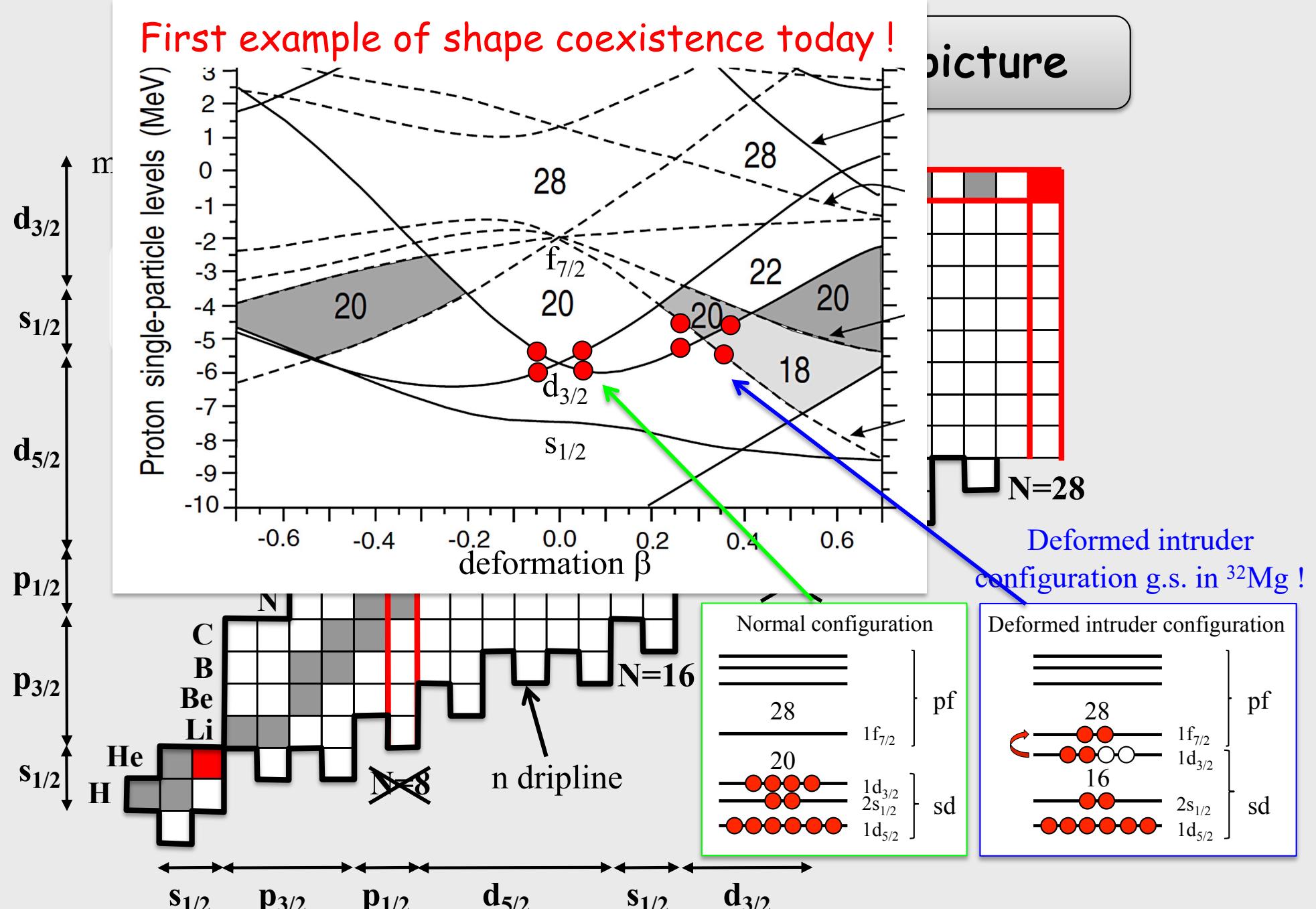


Since then a wealth of information in this region



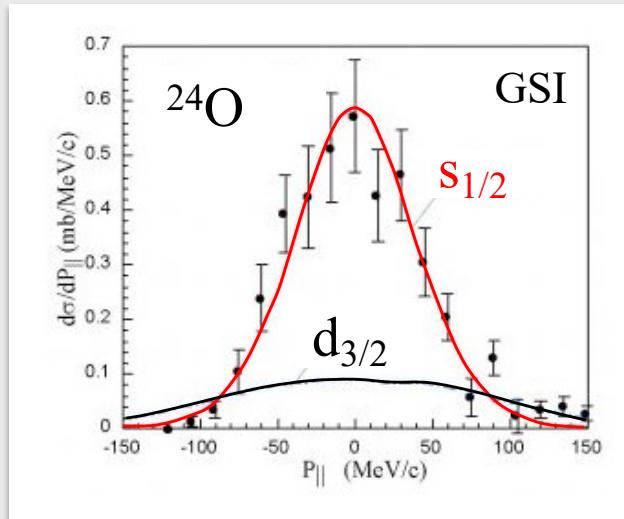
# Explanation within the shell model picture





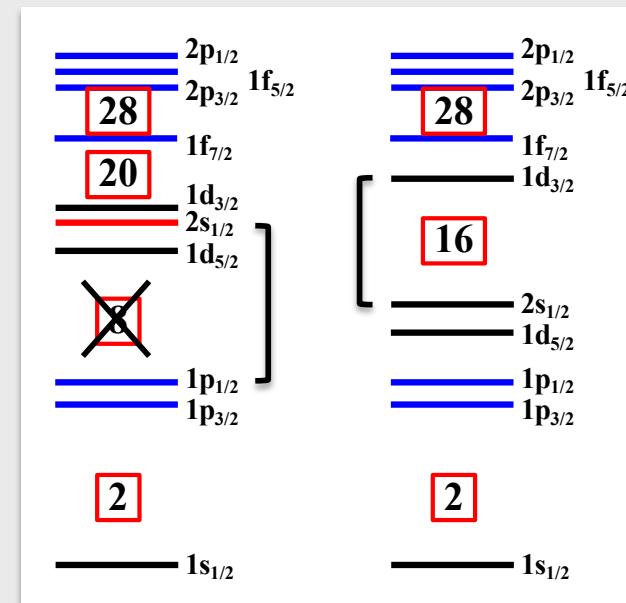
T. Otsuka et al., Phys. Rev. Lett. 87, 082502 (2001); Phys. Rev. Lett. 95, 232502 (2005)

# Momentum distributions in $^{23,24}\text{O}$



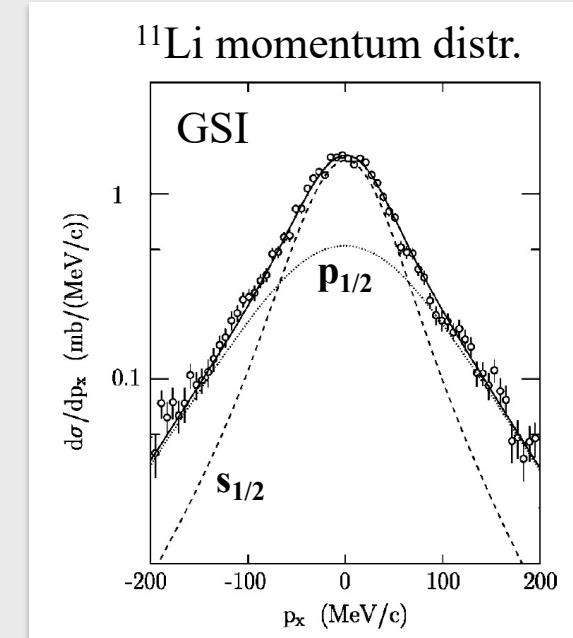
R. Kanungo et al., PRL 102, 152501 (2009)

Last neutron occupies  $\textcolor{red}{s}_{1/2}$  orbital, no  $\textcolor{blue}{d}_{3/2}$  component !

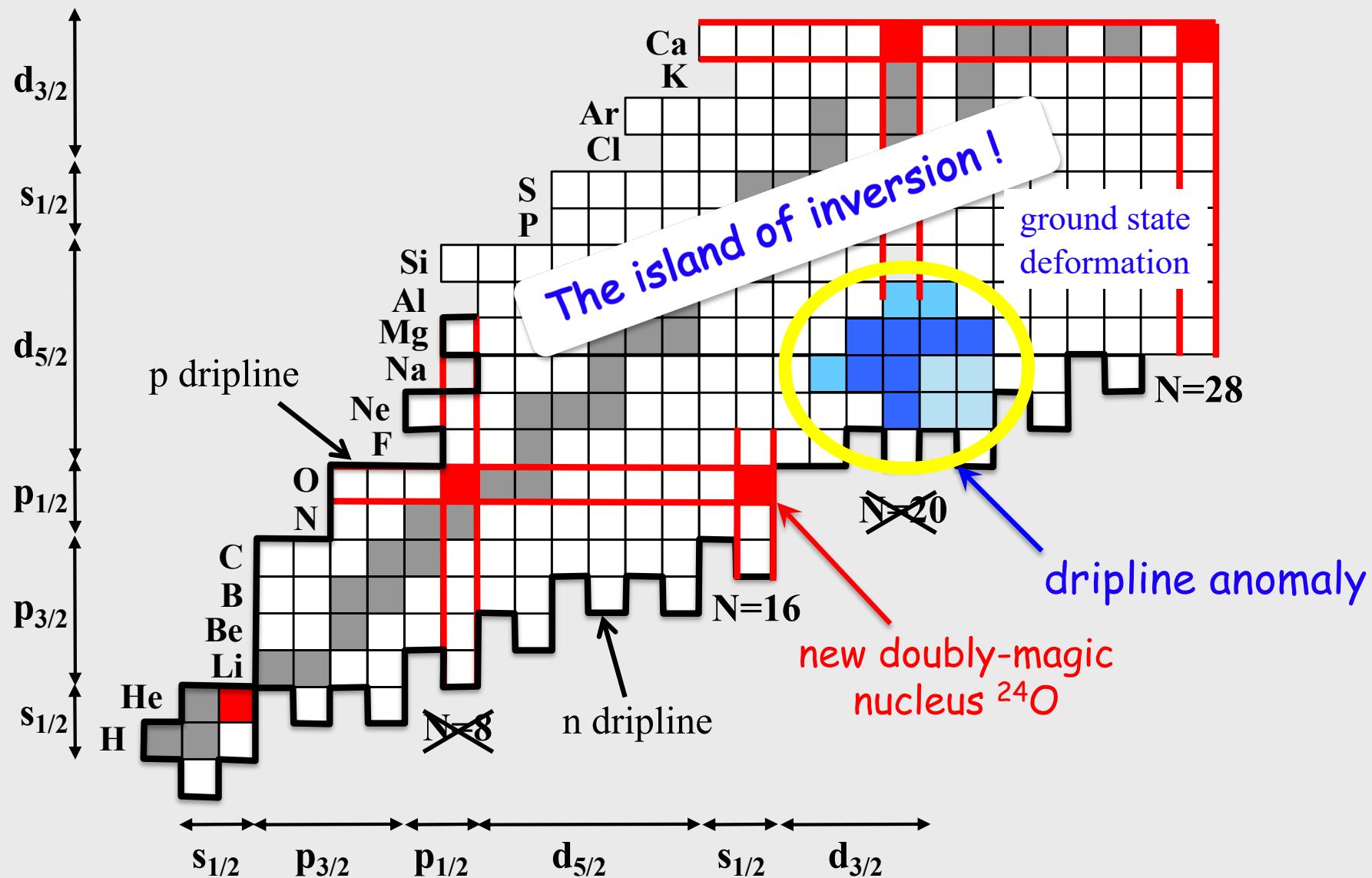


Spherical magic number at N=16,  
 $^{24}\text{O}$  doubly magic !

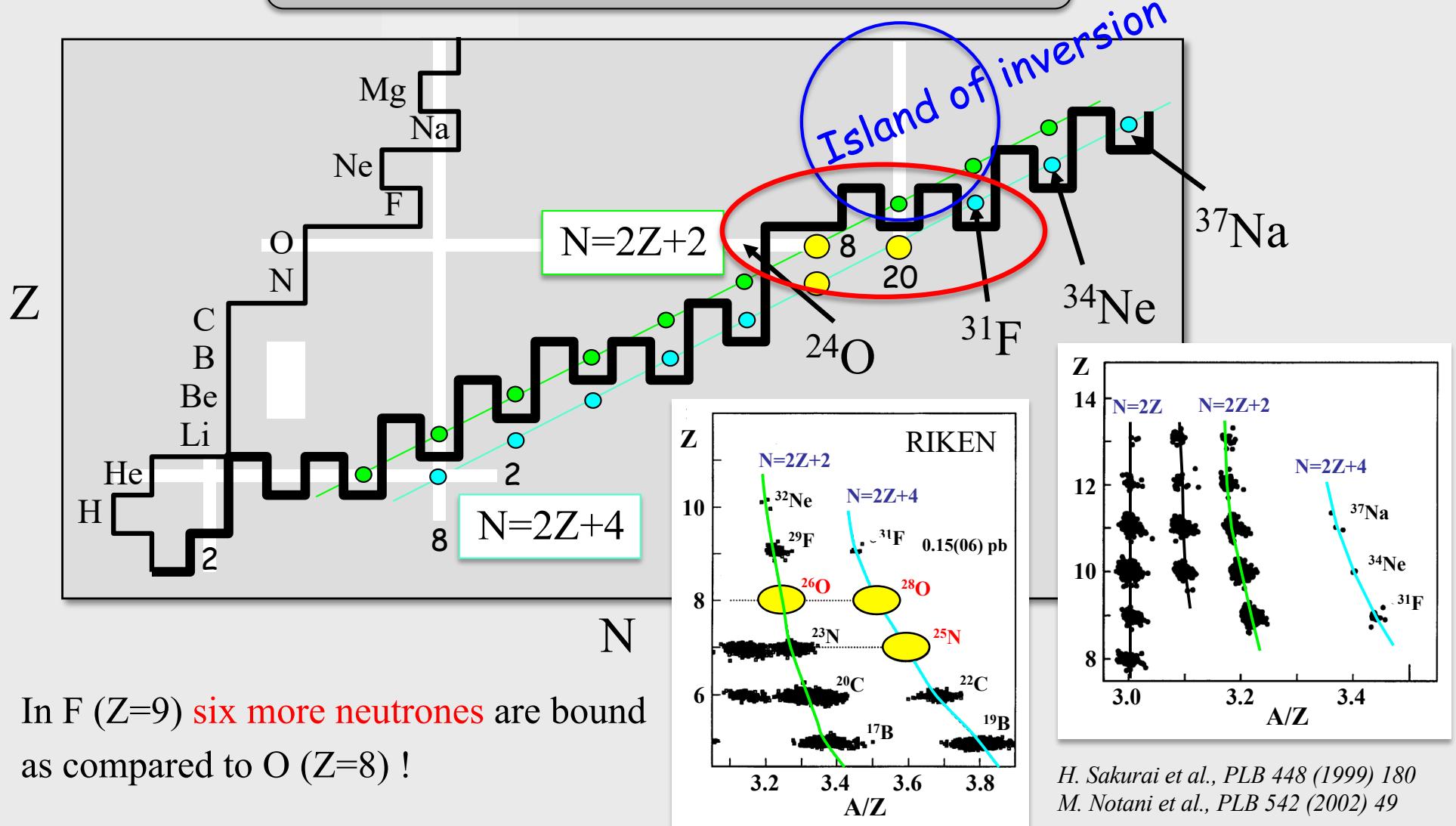
$\textcolor{red}{s}_{1/2}$  and  $\textcolor{blue}{d}_{3/2}$  close in energy,  
mixing to be expected  
No mixing  $\rightarrow$  N=16 gap !



# New magic number and the island of inversion



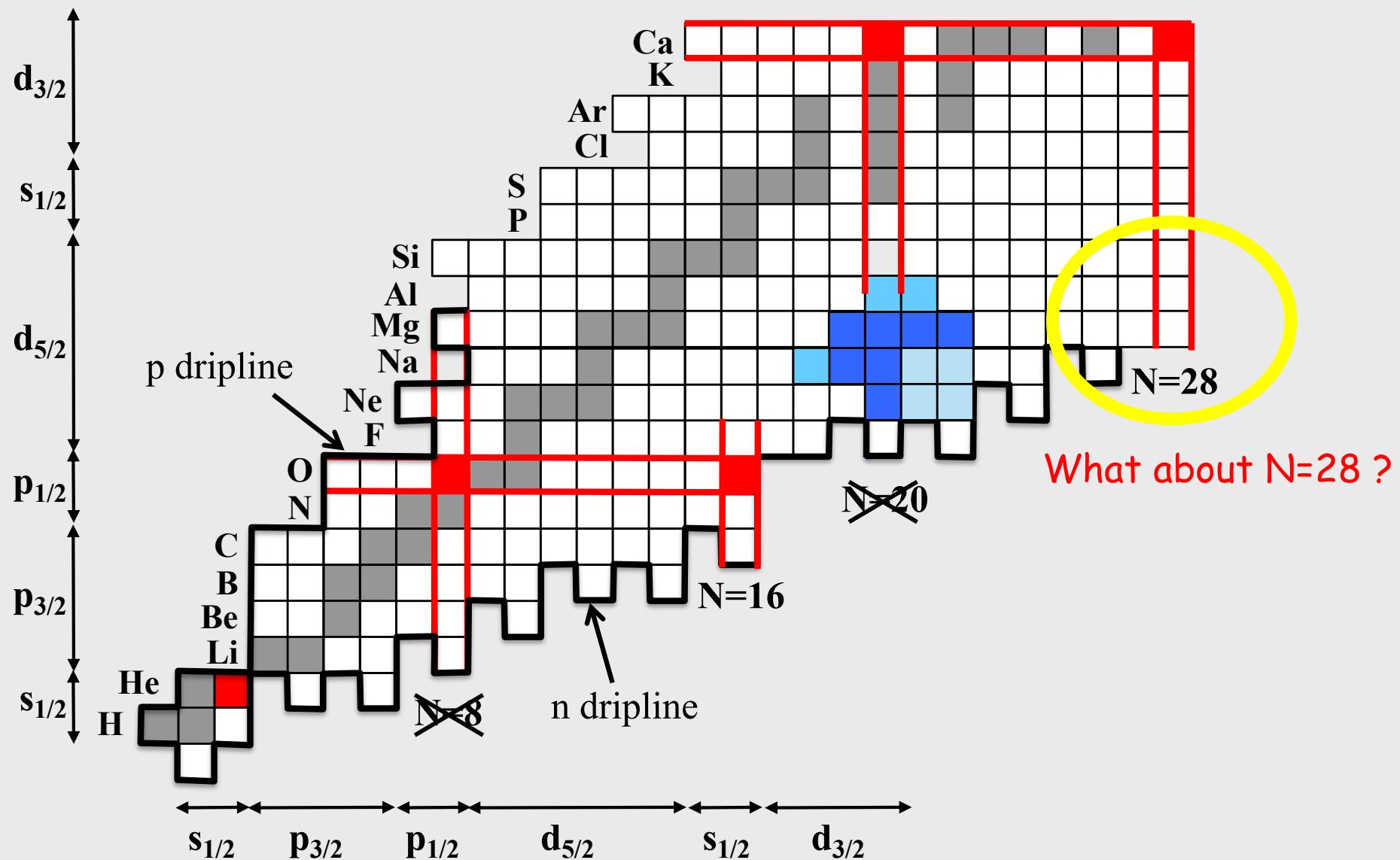
# The neutron dripline up to Na



Additional binding due to deformation !!!

The mere existence of a nucleus already tells us something ...

# New magic number and the island of inversion

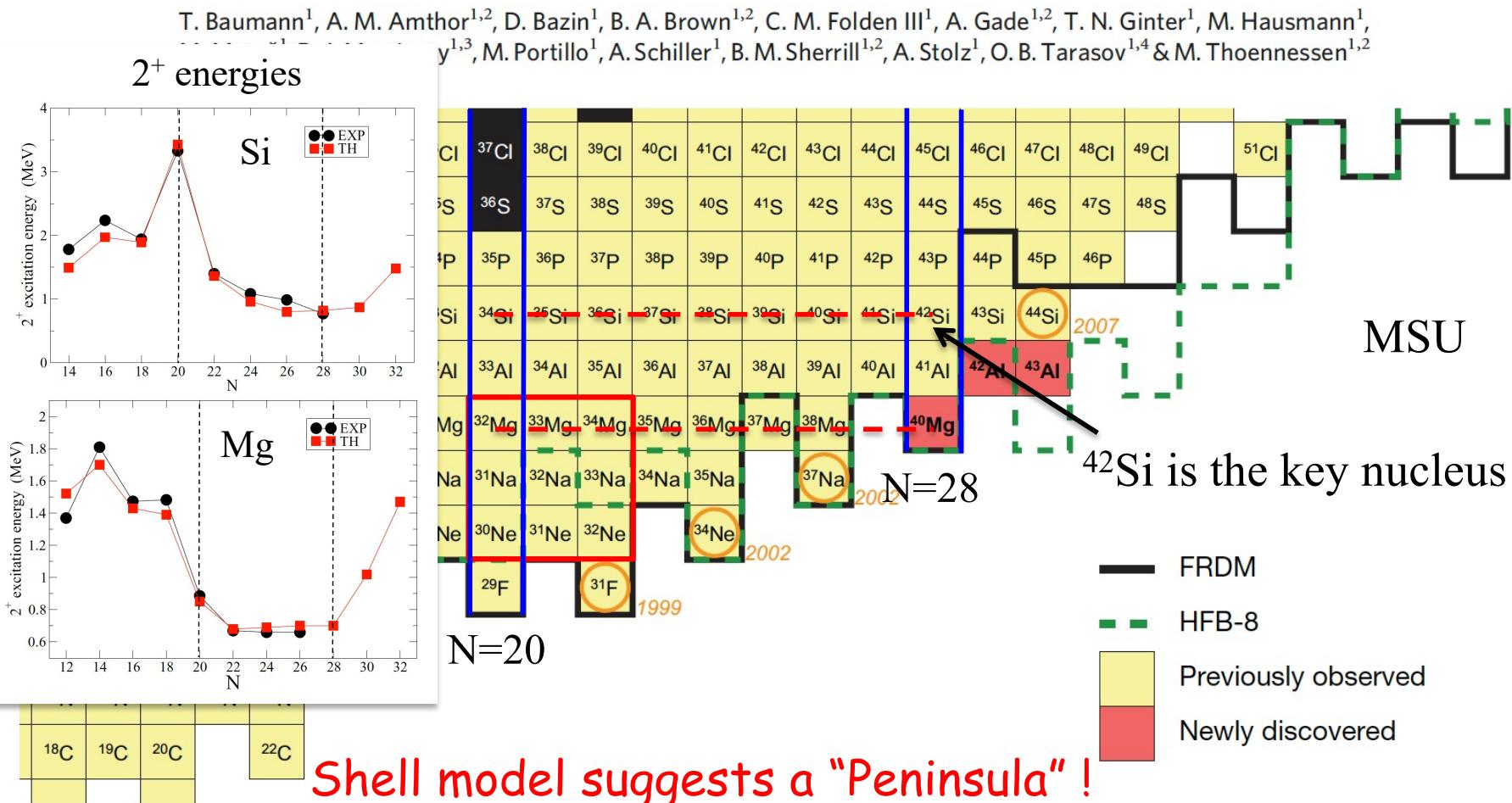


## LETTERS

A second "island of inversion" at N=28 ?

## Discovery of $^{40}\text{Mg}$ and $^{42}\text{Al}$ suggests neutron drip-line slant towards heavier isotopes

2007



# What about the N=28 shell closure ?

More complete experimental information needed !

nature

Vol 435 | 16 June 2005 | doi:10.1038/nature03619

LETTERS

2005

## 'Magic' nucleus $^{42}\text{Si}$

J. Fridmann<sup>1</sup>, I. Wiedenhöver<sup>1</sup>, A. Gade<sup>2</sup>, L. T. Baby<sup>1</sup>, D. Bazin<sup>2</sup>, B. A. Brown<sup>2</sup>, C. M. Campbell<sup>2</sup>, J. M. Cook<sup>2</sup>, P. D. Cottle<sup>1</sup>, E. Diffenderfer<sup>1</sup>, D.-C. Dinca<sup>2</sup>, T. Glasmacher<sup>2</sup>, P. G. Hansen<sup>2</sup>, K. W. Kemper<sup>1</sup>, J. L. Lecouey<sup>2</sup>, W. F. Mueller<sup>2</sup>, H. Olliver<sup>2</sup>, E. Rodriguez-Vieitez<sup>3</sup>, J. R. Terry<sup>2</sup>, J. A. Tostevin<sup>4</sup> & K. Yoneda<sup>2</sup>

PRL 99, 022503 (2007)

PHYSICAL REVIEW LETTERS

week ending  
13 JULY 2007

2007

## Collapse of the $N = 28$ Shell Closure in $^{42}\text{Si}$

B. Bastin,<sup>2</sup> S. Grévy,<sup>1,\*</sup> D. Sohler,<sup>3</sup> O. Sorlin,<sup>1</sup>  
D. Baiborodin,<sup>5</sup> R. Borcea,<sup>6</sup> C. Bourgeois,<sup>4</sup> A. Buta,<sup>6</sup>  
Z. Elekes,<sup>3</sup> S. Fransoo,<sup>4</sup> S. Iacob,<sup>6</sup> B. Laurent,<sup>2</sup> M.  
N. A. Orr,<sup>2</sup> Y. Penionzhkevich,<sup>10</sup> Z.  
M. G. Saint-Laur



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Physics Letters B 649 (2007) 43–48

PHYSICS LETTERS B

[www.elsevier.com/locate/physletb](http://www.elsevier.com/locate/physletb)

2007

## Mass measurements of neutron-rich nuclei near the $N = 20$ and 28 shell closures

PRL 109, 182501 (2012)

PHYSICAL REVIEW LETTERS

week ending  
2 NOVEMBER 2012

2012

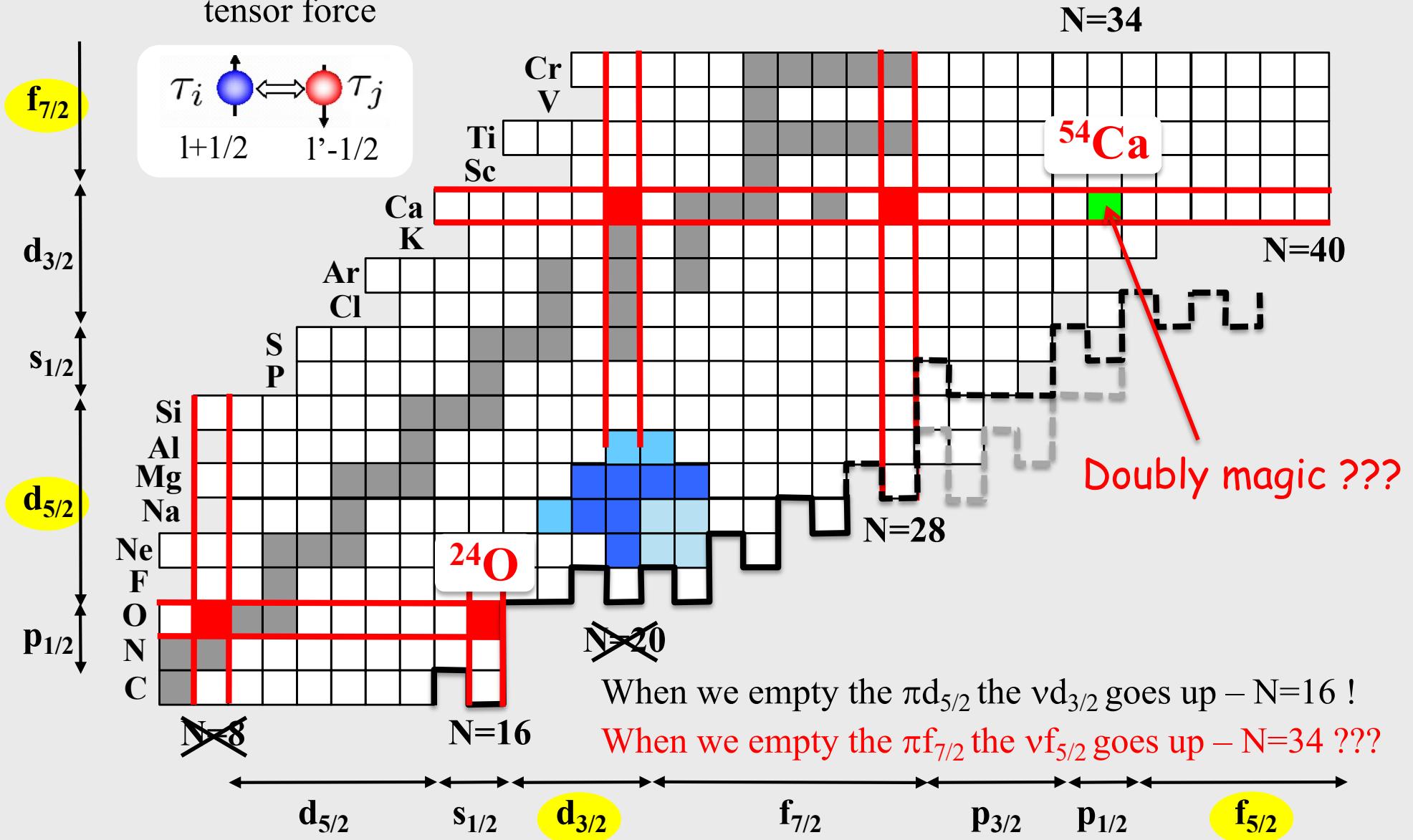
## Well Developed Deformation in $^{42}\text{Si}$

S. Takeuchi,<sup>1,\*</sup> M. Matsushita,<sup>1,2,†</sup> N. Aoi,<sup>1,‡</sup> P. Doornenbal,<sup>1</sup> K. Li,<sup>1,3</sup> T. Motobayashi,<sup>1</sup> H. Scheit,<sup>1,§</sup> D. Steppenbeck,<sup>1,†</sup>  
H. Wang,<sup>1,3</sup> H. Baba,<sup>1</sup> D. Bazin,<sup>4</sup> L. Cáceres,<sup>5</sup> H. Crawford,<sup>6</sup> P. Fallon,<sup>6</sup> R. Gernhäuser,<sup>7</sup> J. Gibelin,<sup>8</sup> S. Go,<sup>9</sup> S. Grévy,<sup>5</sup>  
C. Hinke,<sup>7</sup> C. R. Hoffman,<sup>10</sup> R. Hughes,<sup>11</sup> E. Ideguchi,<sup>9,‡</sup> D. Jenkins,<sup>12</sup> N. Kobayashi,<sup>13</sup> Y. Kondo,<sup>13</sup> R. Krücken,<sup>7,||</sup>  
T. Le Bleis,<sup>14,15,¶</sup> J. Lee,<sup>1</sup> G. Lee,<sup>13</sup> A. Matta,<sup>16</sup> S. Michimasa,<sup>9</sup> T. Nakamura,<sup>13</sup> S. Ota,<sup>9</sup> M. Petri,<sup>6,§</sup> T. Sako,<sup>13</sup> H. Sakurai,<sup>1</sup>  
S. Shimoura,<sup>9</sup> K. Steiger,<sup>7</sup> K. Takahashi,<sup>13</sup> M. Takechi,<sup>1,\*\*\*</sup> Y. Togano,<sup>1,\*\*\*</sup> R. Winkler,<sup>4,††</sup> and K. Yoneda<sup>1</sup>

homaz<sup>a</sup>, D. Baiborodin<sup>c</sup>,  
ibert<sup>f</sup>, L. Giot<sup>a</sup>, A. Khouaja<sup>a</sup>,  
n<sup>h</sup>, S. Pita<sup>a</sup>, M. Rousseau<sup>a</sup>,

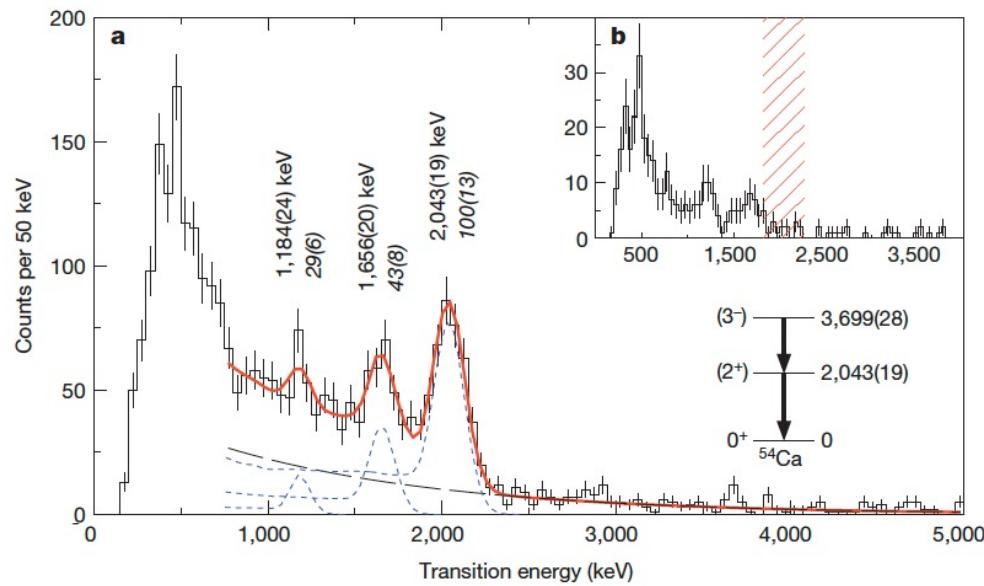
# Is N=34 a new magic number far-off stability ?

monopole effects of the tensor force



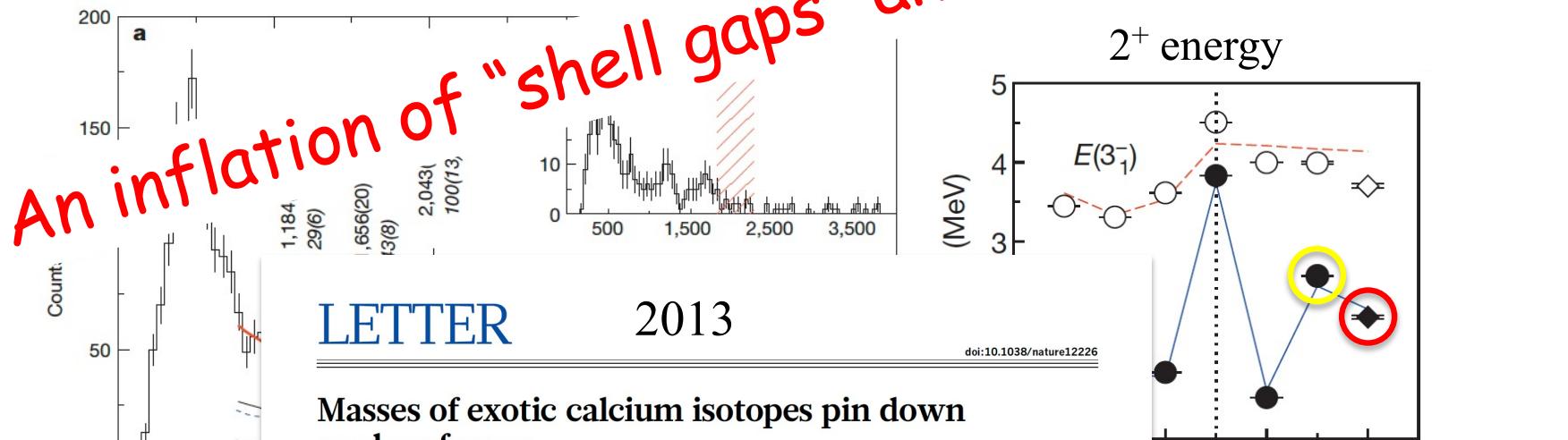
## Evidence for a new nuclear ‘magic number’ from the level structure of $^{54}\text{Ca}$

D. Steffenbeck<sup>1</sup>, S. Takeuchi<sup>2</sup>, N. Aoi<sup>3</sup>, P. Doornenbal<sup>2</sup>, M. Matsushita<sup>1</sup>, H. Wang<sup>2</sup>, H. Baba<sup>2</sup>, N. Fukuda<sup>2</sup>, S. Go<sup>1</sup>, M. Honma<sup>4</sup>, J. Lee<sup>2</sup>, K. Matsui<sup>5</sup>, S. Michimasa<sup>1</sup>, T. Motobayashi<sup>2</sup>, D. Nishimura<sup>6</sup>, T. Otsuka<sup>1,5</sup>, H. Sakurai<sup>2,5</sup>, Y. Shiga<sup>7</sup>, P.-A. Söderström<sup>2</sup>, T. Sumikama<sup>8</sup>, H. Suzuki<sup>2</sup>, R. Taniuchi<sup>5</sup>, Y. Utsuno<sup>9</sup>, J. J. Valiente-Dobón<sup>10</sup> & K. Yoneda<sup>2</sup>



## Evidence for a new nuclear ‘magic number’ from $^{+1}$ level structure of $^{54}\text{Ca}$

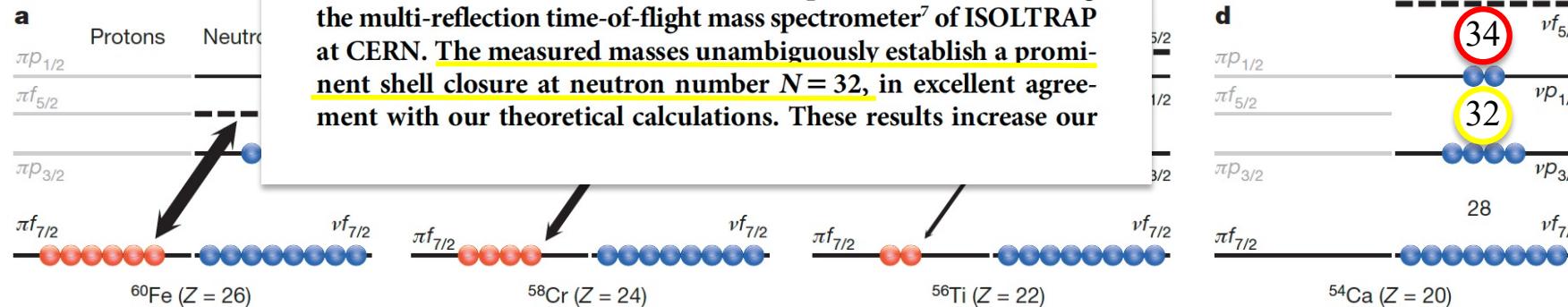
D. Stepenbeck<sup>1</sup>, S. Takeuchi<sup>2</sup>, N. Aoi<sup>3</sup>, P. Doornenbal<sup>2</sup>, M. Matsushita<sup>1</sup>,  
J. Lee<sup>2</sup>, K. Matsui<sup>5</sup>, S. Michimasa<sup>1</sup>, T. Motobayashi<sup>2</sup>, D. Nishimura<sup>1</sup>,  
T. Sumikama<sup>8</sup>, H. Suzuki<sup>2</sup>, R. Taniuchi<sup>5</sup>, Y. Utsuno<sup>9</sup>,  
L. Jöderström<sup>2</sup>,  
S. Goriely<sup>10</sup>,  
A. J. K. Stoks<sup>11</sup>,  
M. Watanabe<sup>12</sup>,  
Y. Yamamoto<sup>13</sup>,  
K. Yoshida<sup>14</sup>



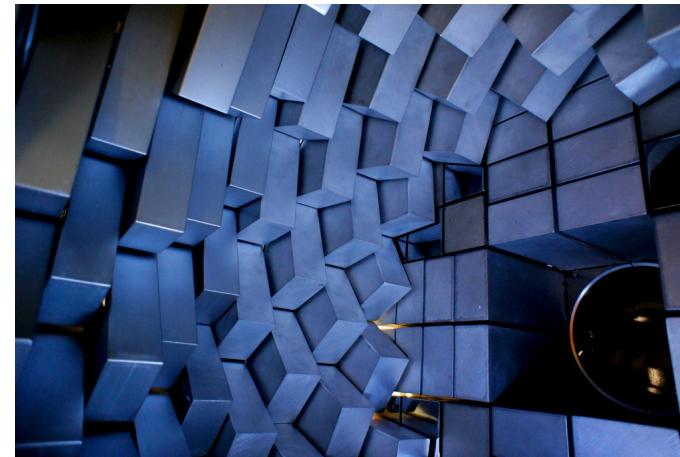
## Masses of exotic calcium isotopes pin down nuclear forces

F. Wienholz<sup>1</sup>, D. Beck<sup>2</sup>, K. Blaum<sup>3</sup>, Ch. Borgmann<sup>3</sup>, M. Breitenfeldt<sup>4</sup>, R. B. Cakirli<sup>3,5</sup>, S. George<sup>1</sup>, F. Herfurth<sup>2</sup>, J. D. Holt<sup>6,7</sup>,  
M. Kowalska<sup>8</sup>, S. Kreim<sup>3,8</sup>, D. Lunney<sup>9</sup>, V. Manea<sup>9</sup>, J. Menéndez<sup>6,7</sup>, D. Neidherr<sup>2</sup>, M. Rosenbusch<sup>1</sup>, L. Schweikhard<sup>1</sup>,  
A. Schwenk<sup>7,6</sup>, J. Simons<sup>6,7</sup>, J. Stanja<sup>10</sup>, R. N. Wolf<sup>1</sup> & K. Zuber<sup>10</sup>

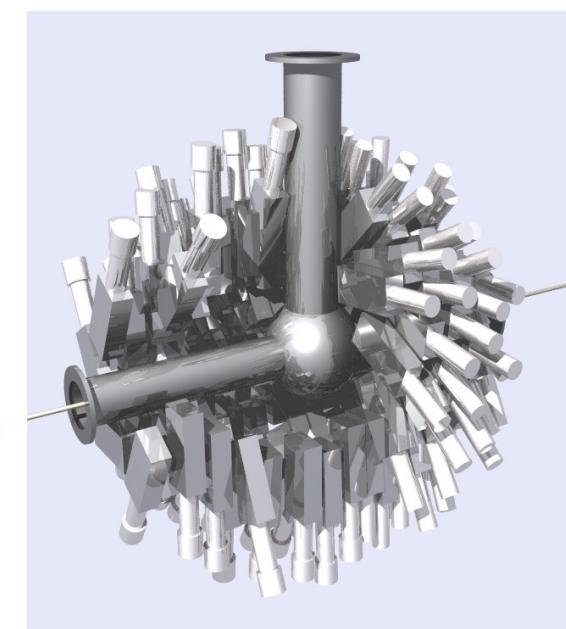
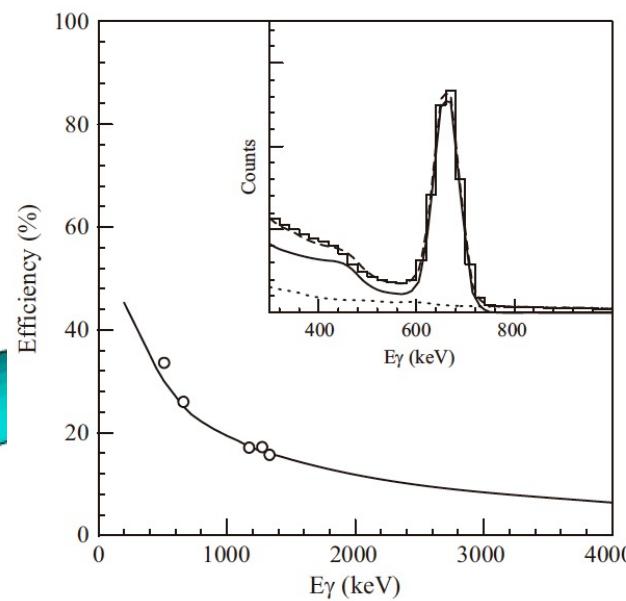
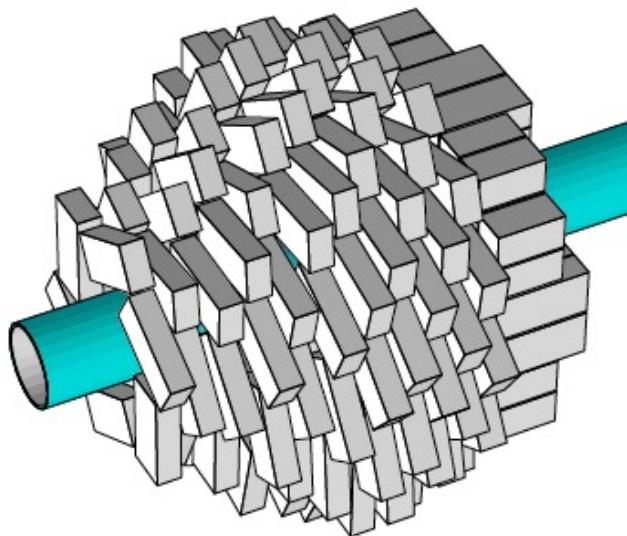
masses evolve for heavier calcium isotopes. Here we report the mass determination of the exotic calcium isotopes  $^{53}\text{Ca}$  and  $^{54}\text{Ca}$ , using the multi-reflection time-of-flight mass spectrometer<sup>7</sup> of ISOLTRAP at CERN. The measured masses unambiguously establish a prominent shell closure at neutron number  $N=32$ , in excellent agreement with our theoretical calculations. These results increase our



# The $\gamma$ -ray spectrometer DALI2 at RIKEN

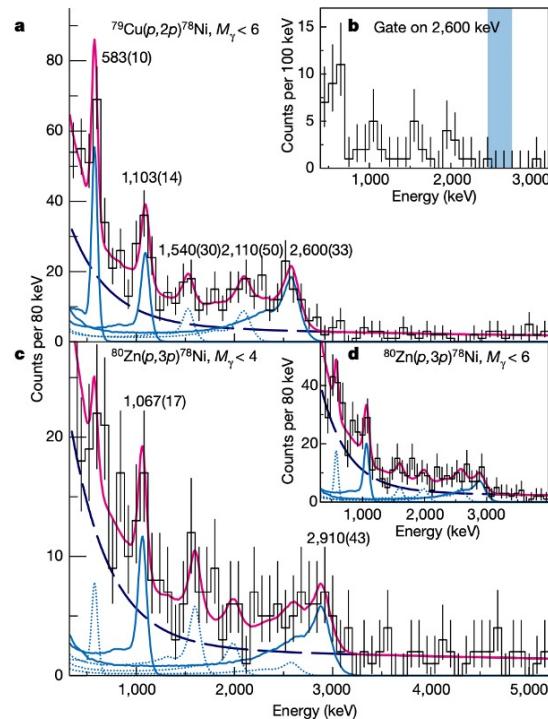


186 NaI (Tl)  
scintillators



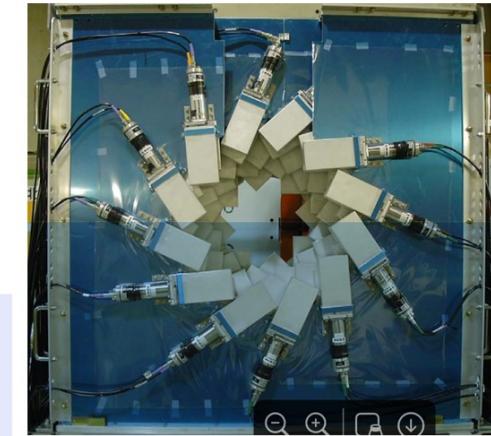
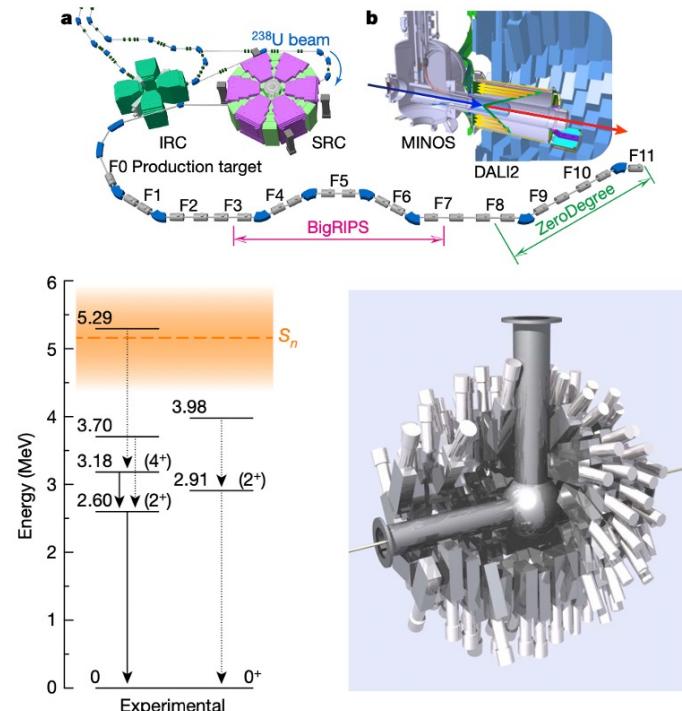
# "Low-resolution" $\gamma$ spectroscopy

BUT high efficiency and high granularity – DALI2 @ RIKEN, the first  $\gamma$  spectrum of  $^{78}\text{Ni}$



R. Taniuchi et al., Nature, 569 (2019) 53–58

S. Takeuchi et al., NIMA 763 (2014) 596



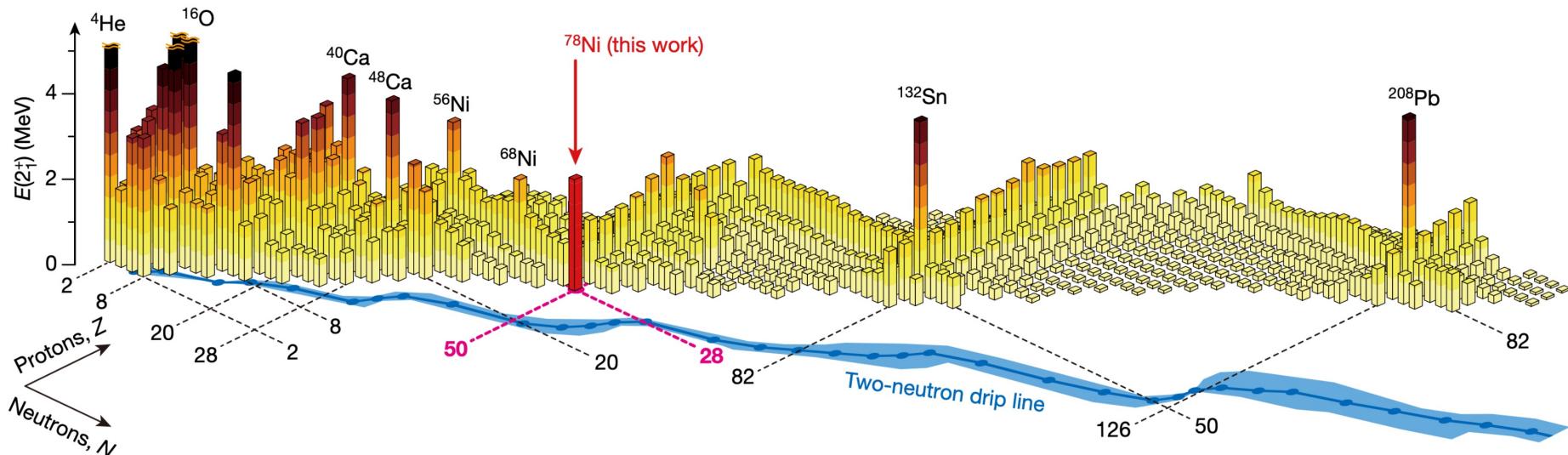
160  $\text{NaI}(\text{Tl})$  detectors  
-  $4.5 \times 8 \times 16 (\text{cm}^3)$   
- resol. 9% @ 662keV

16 layers, 6-14 dets per layer

## Caterina Michelagnoli, 1. Lecture

# $^{78}\text{Ni}$ revealed as a doubly magic stronghold against nuclear deformation

R. Taniuchi<sup>1,2</sup>, C. Santamaría<sup>2,3</sup>, P. Doornenbal<sup>2\*</sup>, A. Obertelli<sup>2,3,4</sup>, K. Yoneda<sup>2</sup>, G. Authelet<sup>3</sup>, H. Baba<sup>2</sup>, D. Calvet<sup>3</sup>, F. Château<sup>3</sup>, A. Corsi<sup>3</sup>, A. Delbart<sup>3</sup>, J.-M. Gheller<sup>3</sup>, A. Gillibert<sup>3</sup>, J. D. Holt<sup>5</sup>, T. Isobe<sup>2</sup>, V. Lapoux<sup>3</sup>, M. Matsushita<sup>6</sup>, J. Menéndez<sup>6</sup>, S. Momiyama<sup>1,2</sup>, T. Motobayashi<sup>2</sup>, M. Niikura<sup>1</sup>, F. Nowacki<sup>7</sup>, K. Ogata<sup>8,9</sup>, H. Otsu<sup>2</sup>, T. Otsuka<sup>1,2,6</sup>, C. Péron<sup>3</sup>, S. Péru<sup>10</sup>, A. Peyaud<sup>3</sup>, E. C. Pollacco<sup>3</sup>, A. Poves<sup>11</sup>, J.-Y. Rousse<sup>3</sup>, H. Sakurai<sup>1,9</sup>, A. Schwenk<sup>4,12,13</sup>, Y. Shiga<sup>2,14</sup>, J. Simonis<sup>4,12,15</sup>, S. R. Stroberg<sup>5,16</sup>, S. Takeuchi<sup>2</sup>, Y. Tsunoda<sup>6</sup>, T. Uesaka<sup>2</sup>, H. Wang<sup>2</sup>, F. Browne<sup>17</sup>, L. X. Chung<sup>18</sup>, Z. Dombradi<sup>19</sup>, S. Franschoo<sup>20</sup>, F. Giacoppo<sup>2</sup>, A. Gottardo<sup>20</sup>, K. Hadyńska-Klęk<sup>21</sup>, Z. Korkulu<sup>19</sup>, S. Koyama<sup>1,2</sup>, Y. Kubota<sup>2,6</sup>, J. Lee<sup>22</sup>, M. Lettmann<sup>4</sup>, C. Louchart<sup>4</sup>, R. Lozeva<sup>7,23</sup>, K. Matsui<sup>1,2</sup>, T. Miyazaki<sup>1,2</sup>, S. Nishimura<sup>2</sup>, L. Olivier<sup>20</sup>, S. Ota<sup>6</sup>, Z. Patel<sup>24</sup>, E. Sahin<sup>21</sup>, C. Shand<sup>24</sup>, P.-A. Söderström<sup>2</sup>, I. Stefan<sup>20</sup>, D. Steppenbeck<sup>6</sup>, T. Sumikama<sup>25</sup>, D. Suzuki<sup>20</sup>, Z. Vajta<sup>19</sup>, V. Werner<sup>4</sup>, J. Wu<sup>2,26</sup> & Z. Y. Xu<sup>22</sup>



**Fig. 1 | Experimental  $E(2_1^+)$  systematics of the even–even nuclear landscape.** Shown are known  $E(2_1^+)$  of even–even isotopes<sup>40</sup> and the value for  $^{78}\text{Ni}$  obtained in the present study. Canonical magic numbers are indicated by dashed lines and doubly magic nuclei are labelled.  $^{68}\text{Ni}$ , for

which the number of neutrons,  $N = 40$ , matches the harmonic-oscillator shell closure, is also marked. The predicted two-neutron drip line and its uncertainties<sup>3</sup> are shown in blue.

## The heavier neutron-rich region

Single-particle energies (and consequently shell gaps) change with isospin - as they do with deformation (and rotation) !

