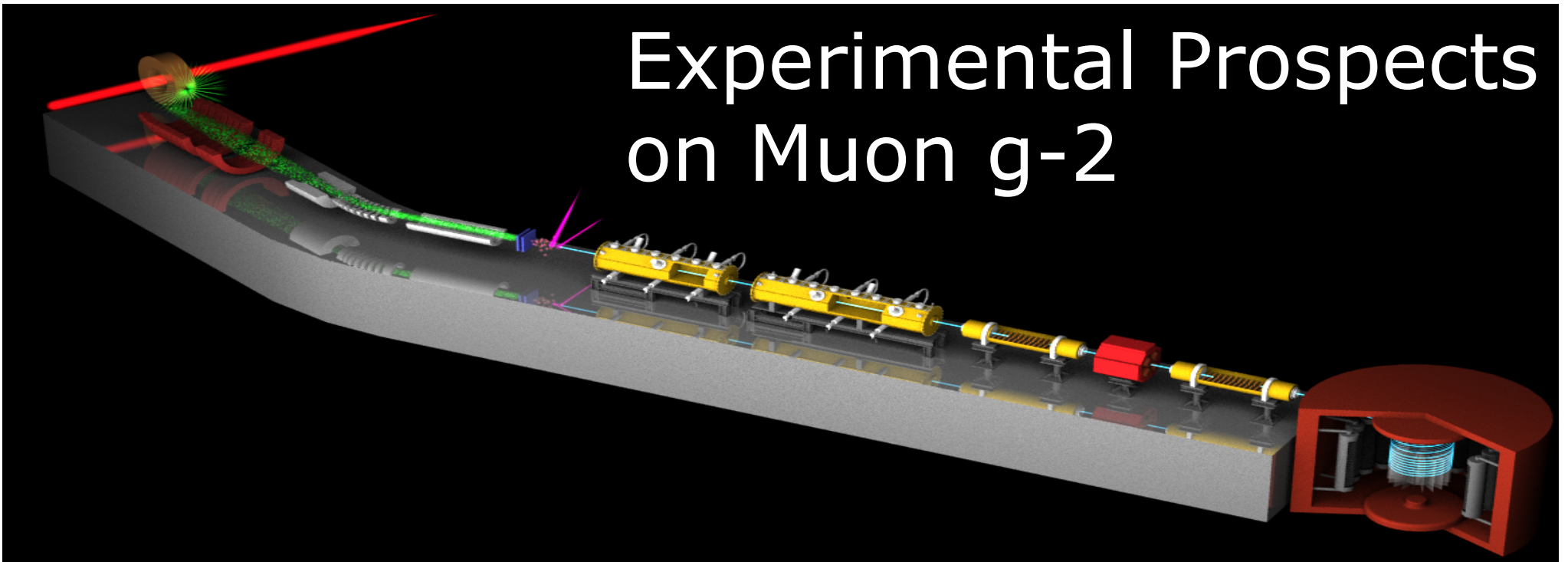


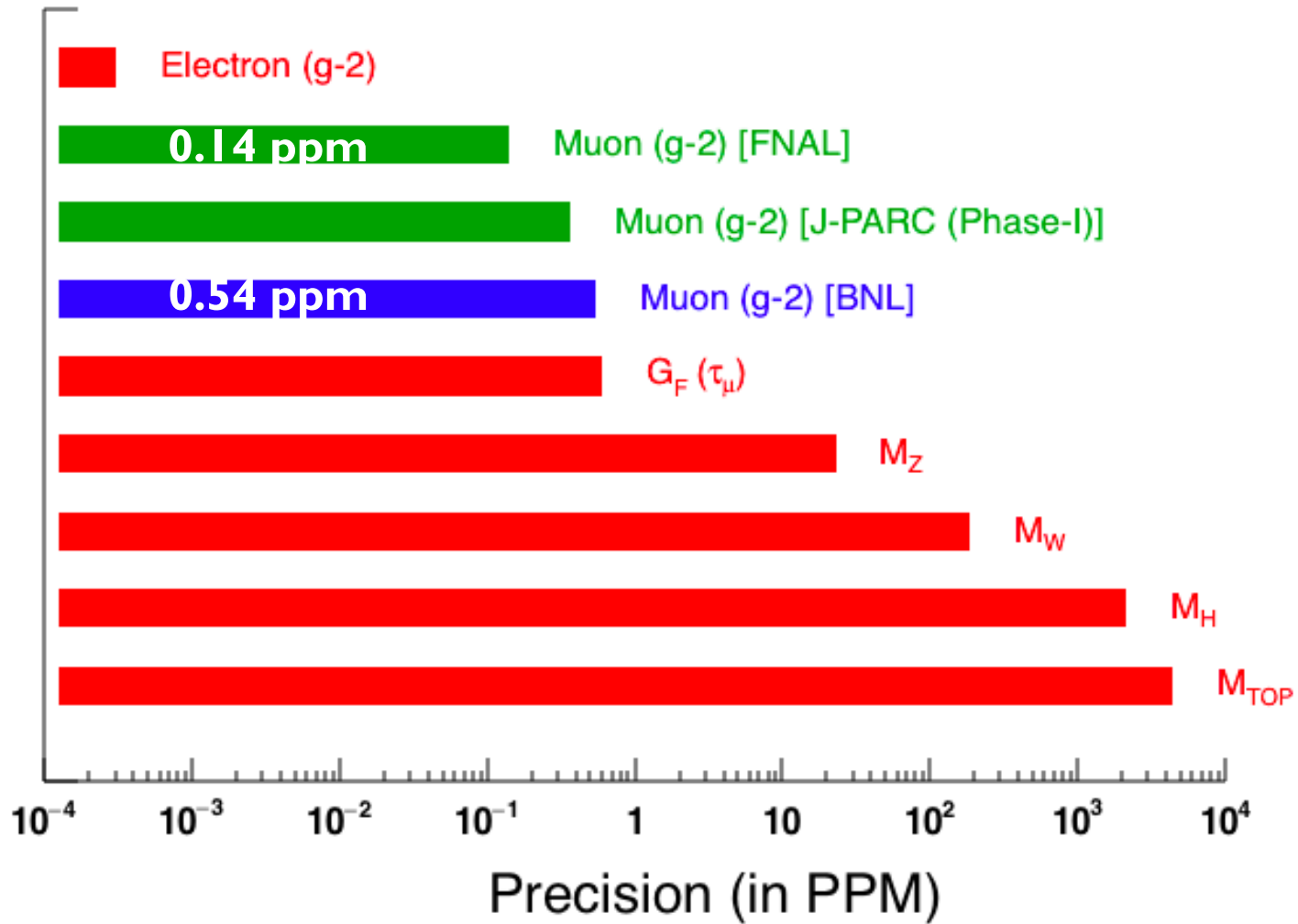
# Experimental Prospects on Muon $g-2$



Mark Lancaster

University College London







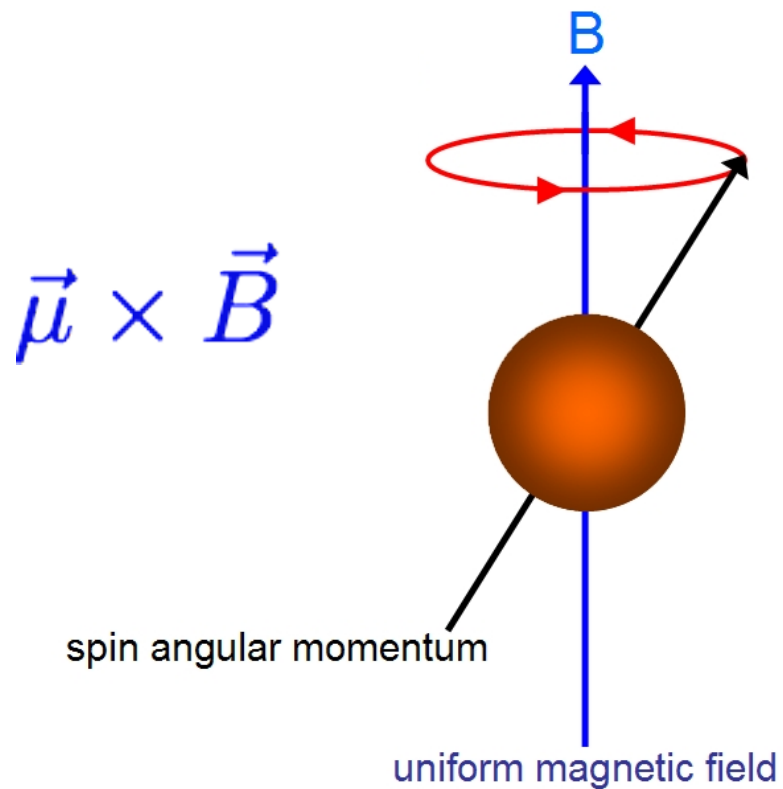


**“Never measure anything but frequency”**

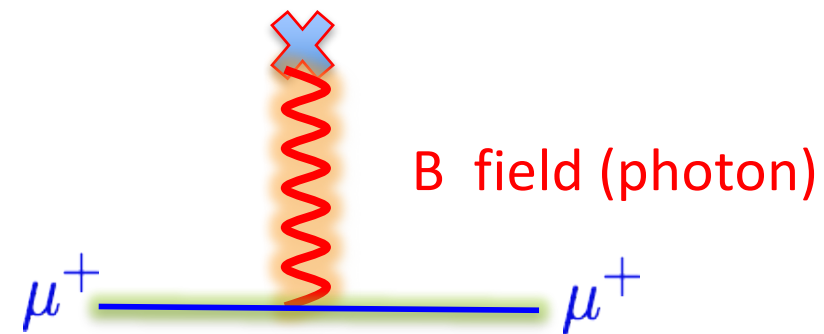
*I. Rabi*

$$\vec{\mu} = g \frac{Qe}{2m} \vec{s}$$

Interaction between magnetic moment (spin) with B-field.



Spin precesses around B at a frequency determined by “g”



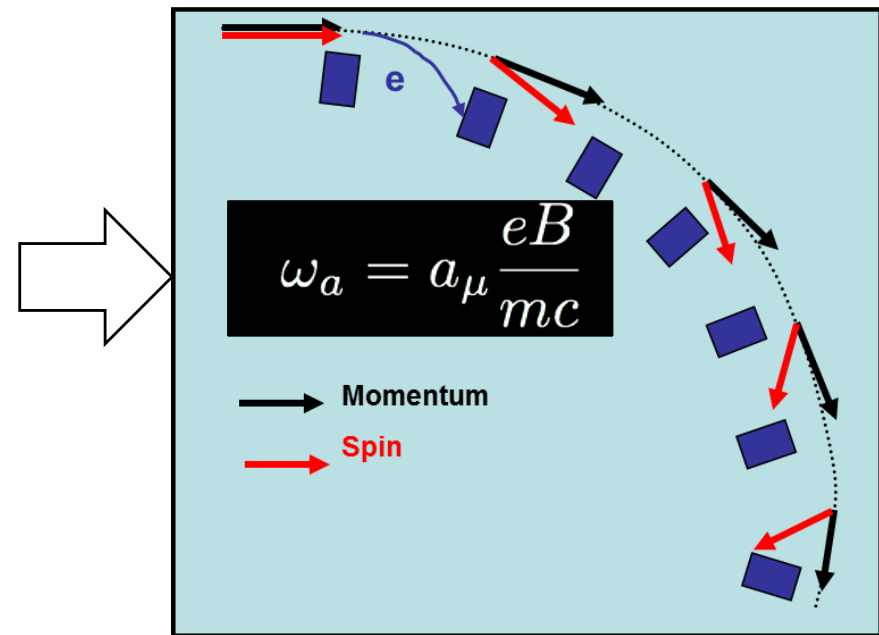
Particle in a circular storage ring (B-field): two frequencies:

$$\omega_S = \frac{g e B}{2 m c} + (1 - \gamma) \frac{e B}{\gamma m c} \qquad \omega_C = \frac{e B}{m c \gamma}$$

Spin vector of muon rotates slightly quicker than Momentum vector.  
 For a 1.5T field spin rotates in 144ns and momentum in 149ns.

$$\begin{aligned} \omega_a &= \omega_S - \omega_C \\ &= \left( \frac{g - 2}{2} \right) \frac{e B}{m c} = a \frac{e B}{m c} \end{aligned}$$

$$f_a = 228 \text{ kHz}$$



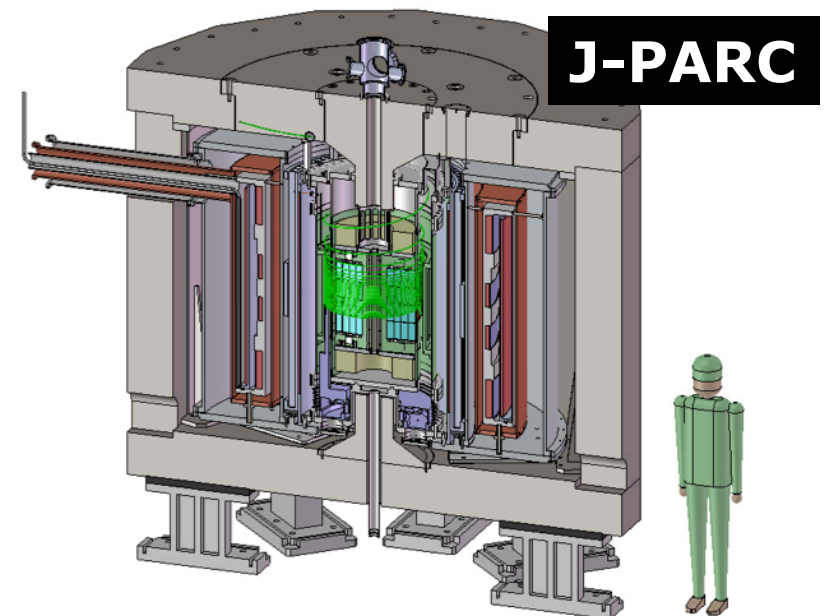


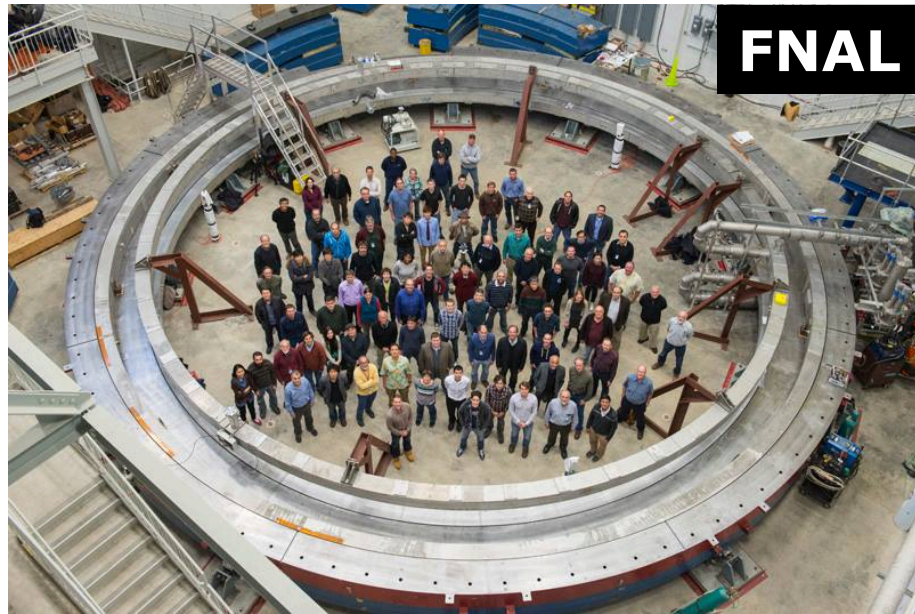
But real beams are not all on the same perfect circular orbit and can have a (small) transverse velocity component.

**These imperfection causes beam to diverge vertically.**

Two approaches:

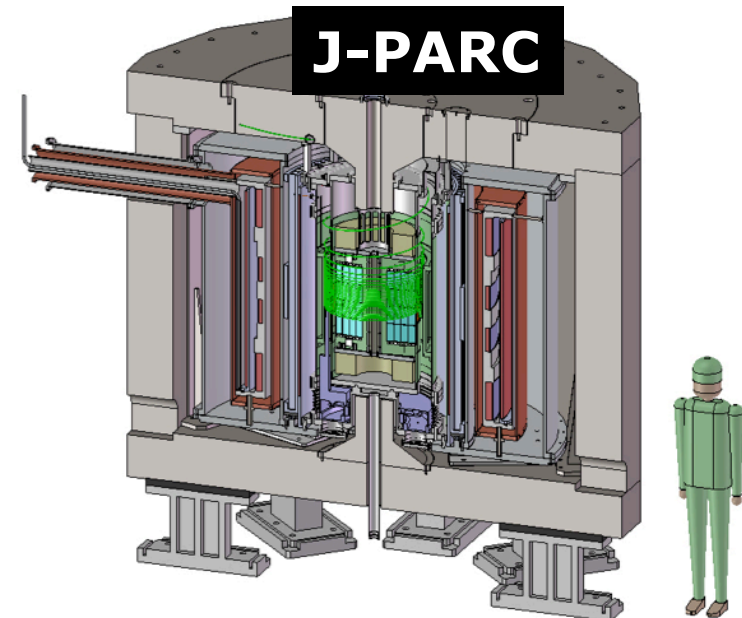
- cancel the divergence with an electric quadrupole field (CERN, BNL, FNAL)
- minimise the divergence by reducing the beam  $p_T$  (J-PARC)





3.094 GeV muons  
1.45 T, 14m bespoke magnet  
Focussing quadrupoles  
Kicker magnets  
Emittance: 1000pimm

0.3 GeV muons  
3T, 66cm MRI magnet  
 $\Delta p_T/p_T = 1e-5$



Apparatus and hence systematics are very different

$$\omega_a = -\frac{e}{m} \left[ a_\mu \vec{B} - \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

**FNAL: MAKE ZERO BY CHOOSING "MAGIC"  $\gamma$**

**J-PARC: MAKE ZERO BY HAVING  $E=0$**

$$a_\mu = \frac{\omega_a m B}{e}$$

Both expts need to measure two quantities

- B field
- $\omega_a$

**To better than 0.1 ppm**

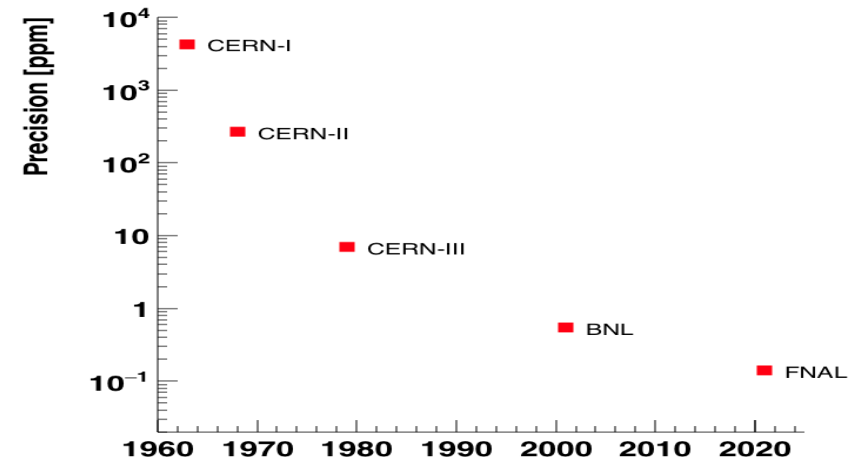
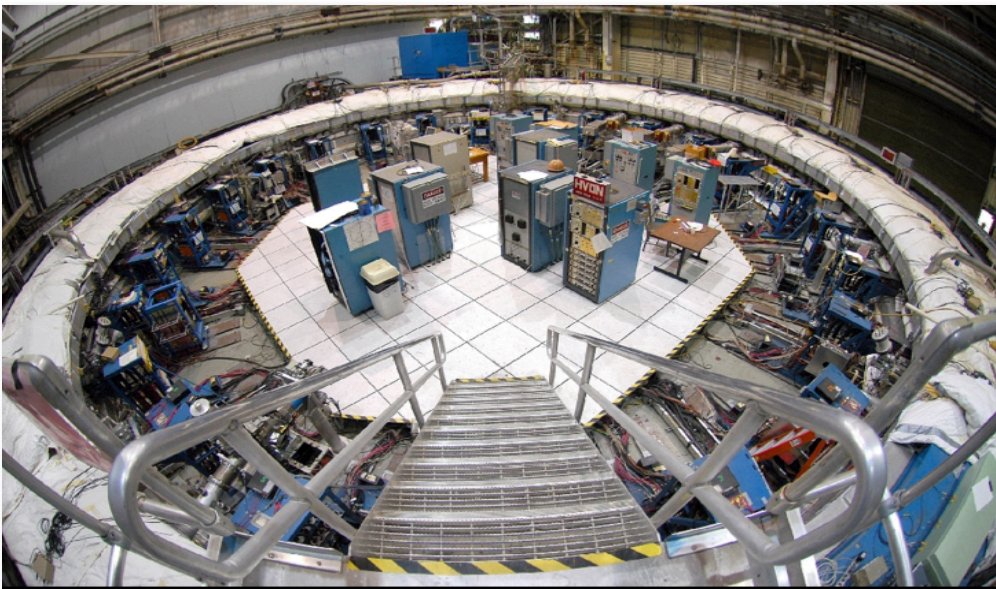
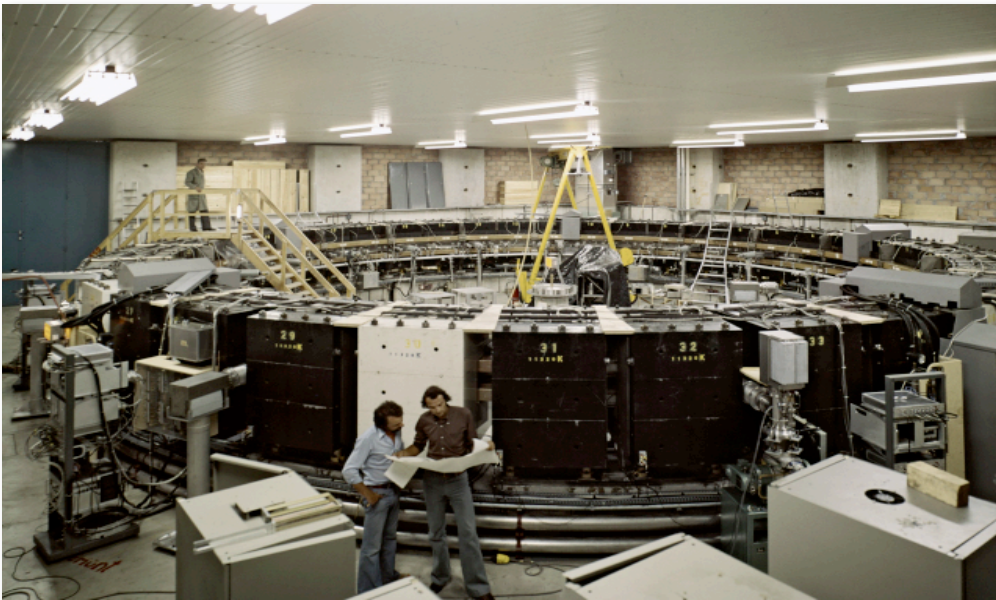


B is measured using NMR in terms of the proton Larmor frequency :  $\omega_p$

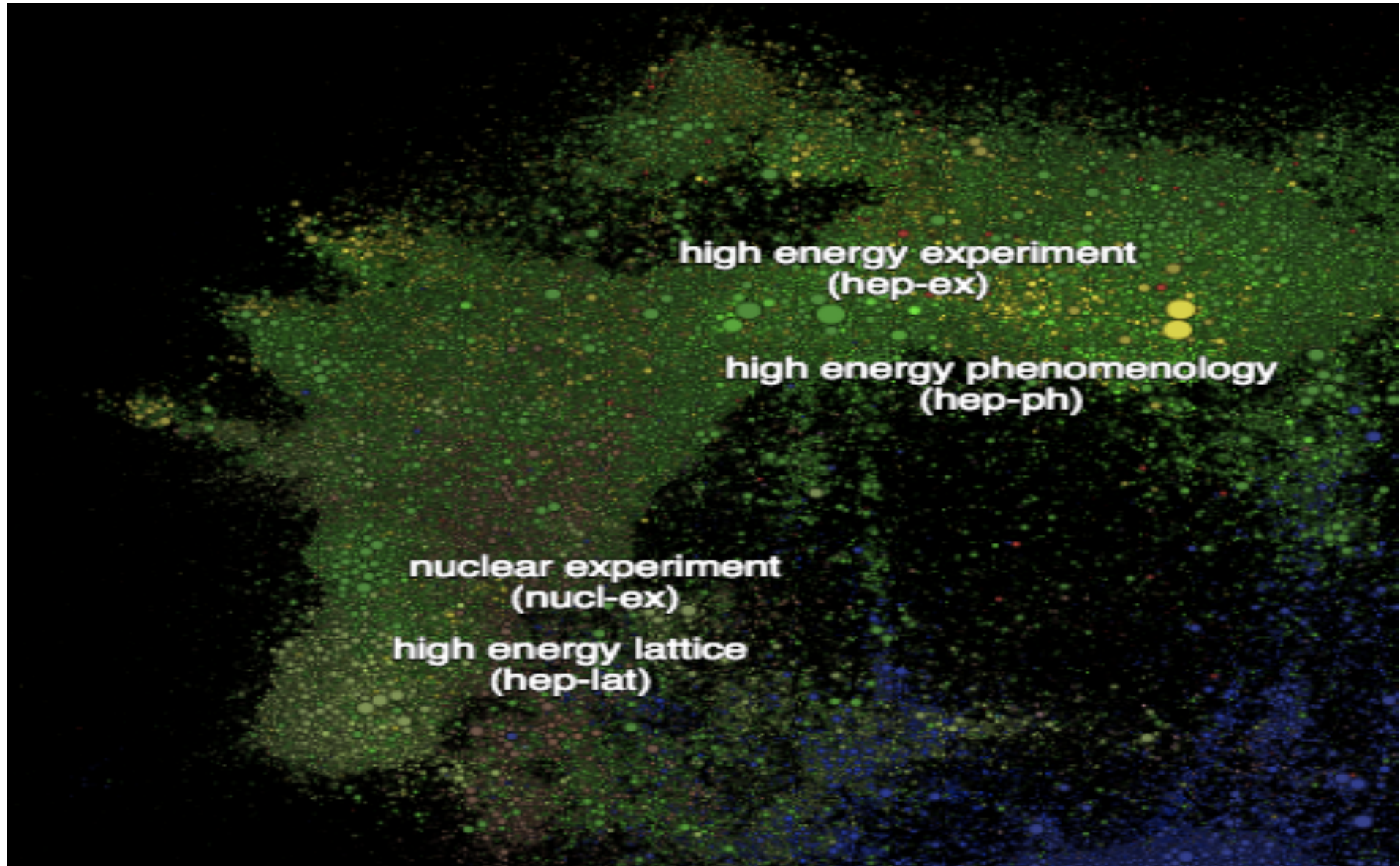
$$a_\mu = \frac{\omega_a/\omega_p}{\lambda_+ - \omega_a/\omega_p} ; \lambda_+ = \mu_{\mu^+}/\mu_p$$

$\lambda_+$  measured from muonium hyperfine structure

Uncertainty in  $a_\mu$  determined by precision of  $\omega_p$  and  $\omega_a$  measurements







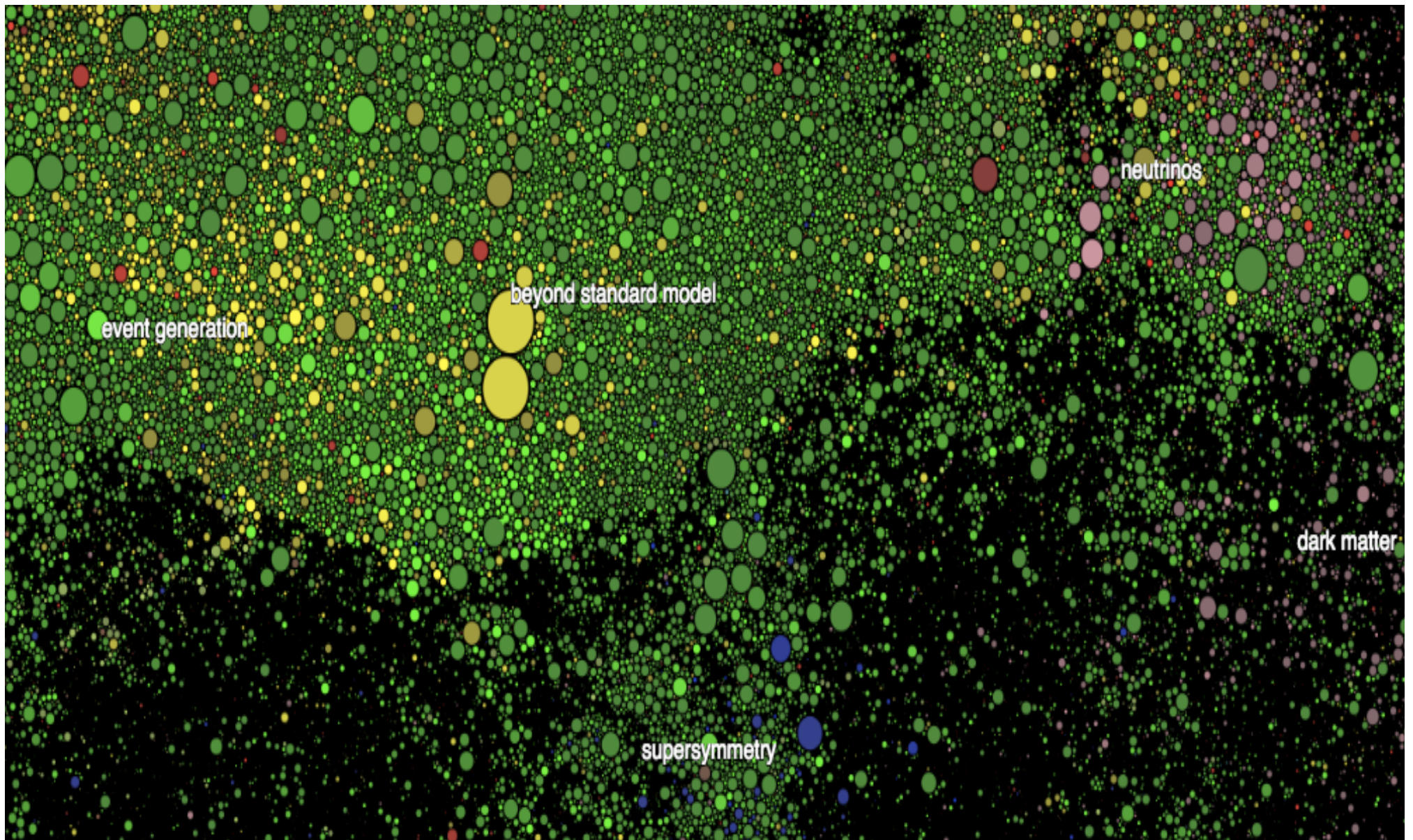
high energy experiment  
(hep-ex)

high energy phenomenology  
(hep-ph)

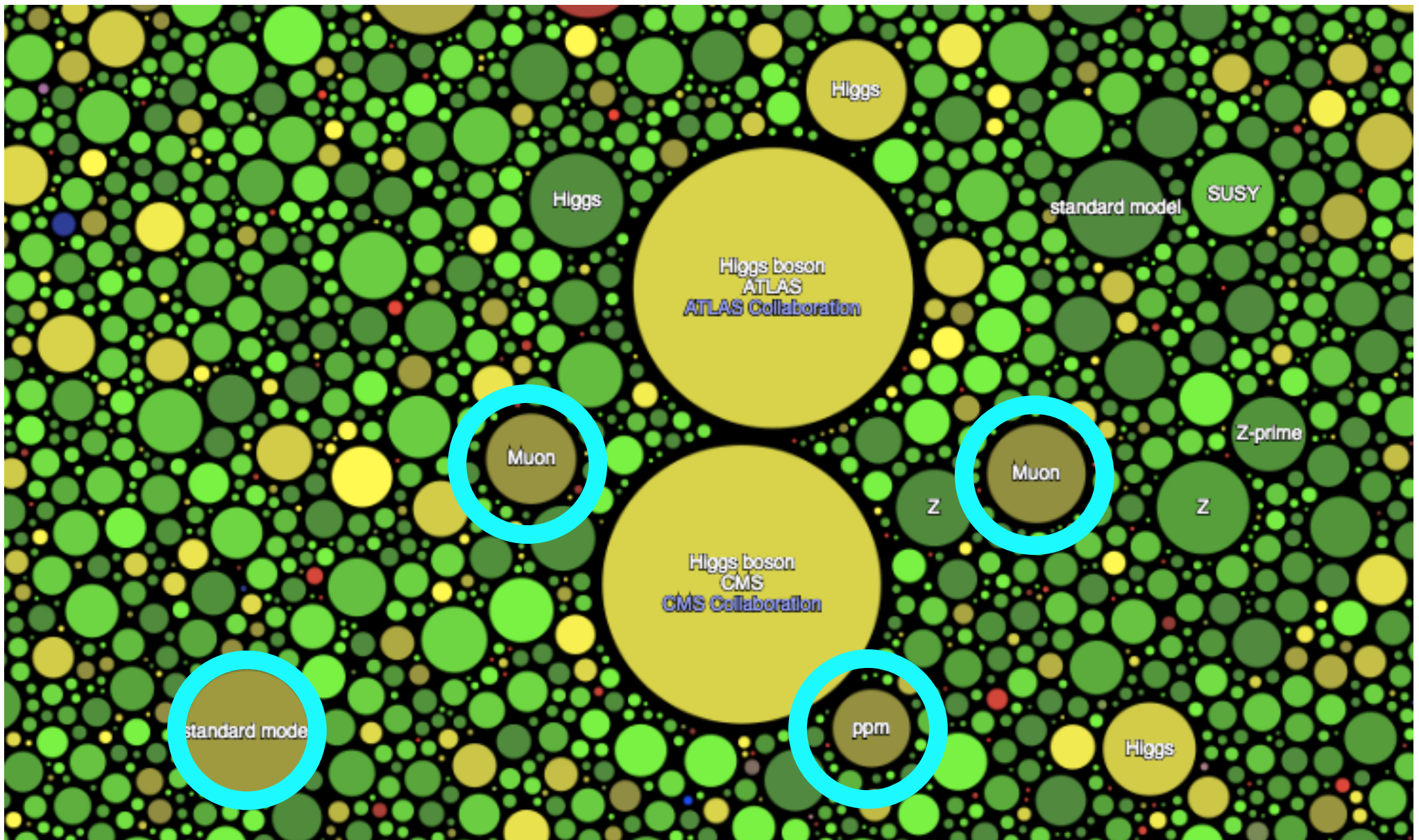
nuclear experiment  
(nucl-ex)

high energy lattice  
(hep-lat)



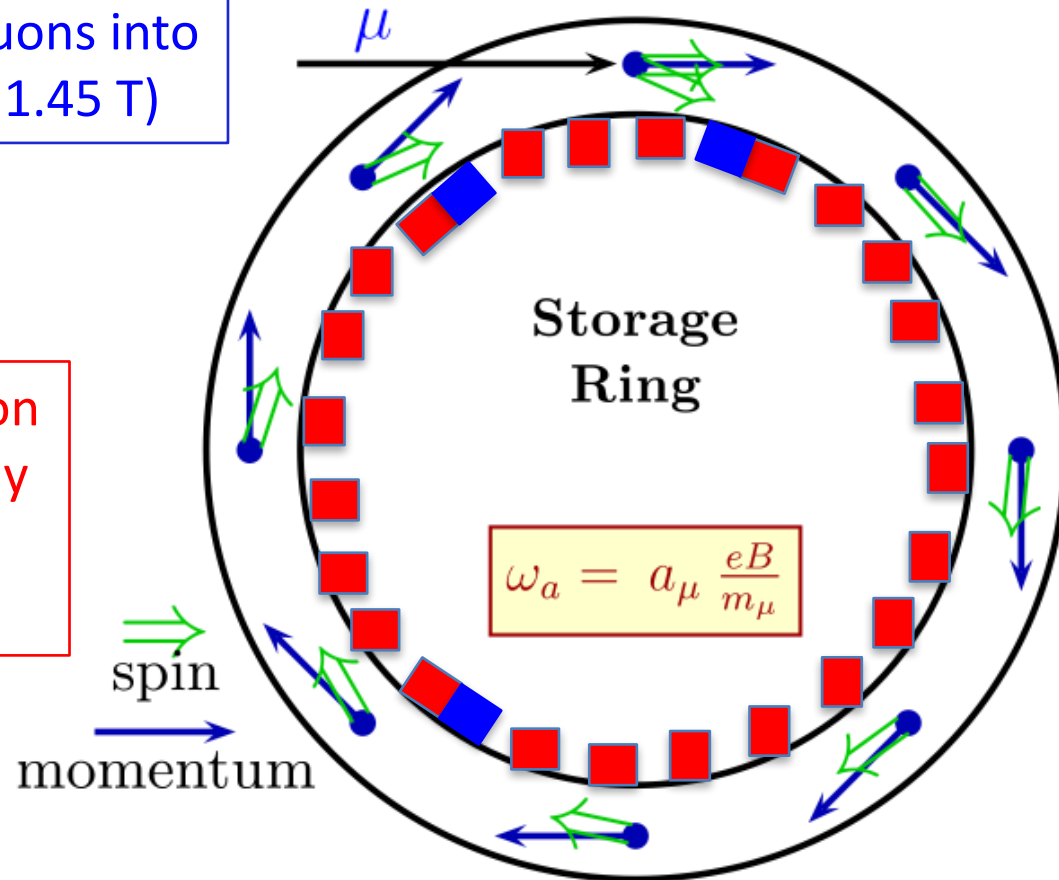






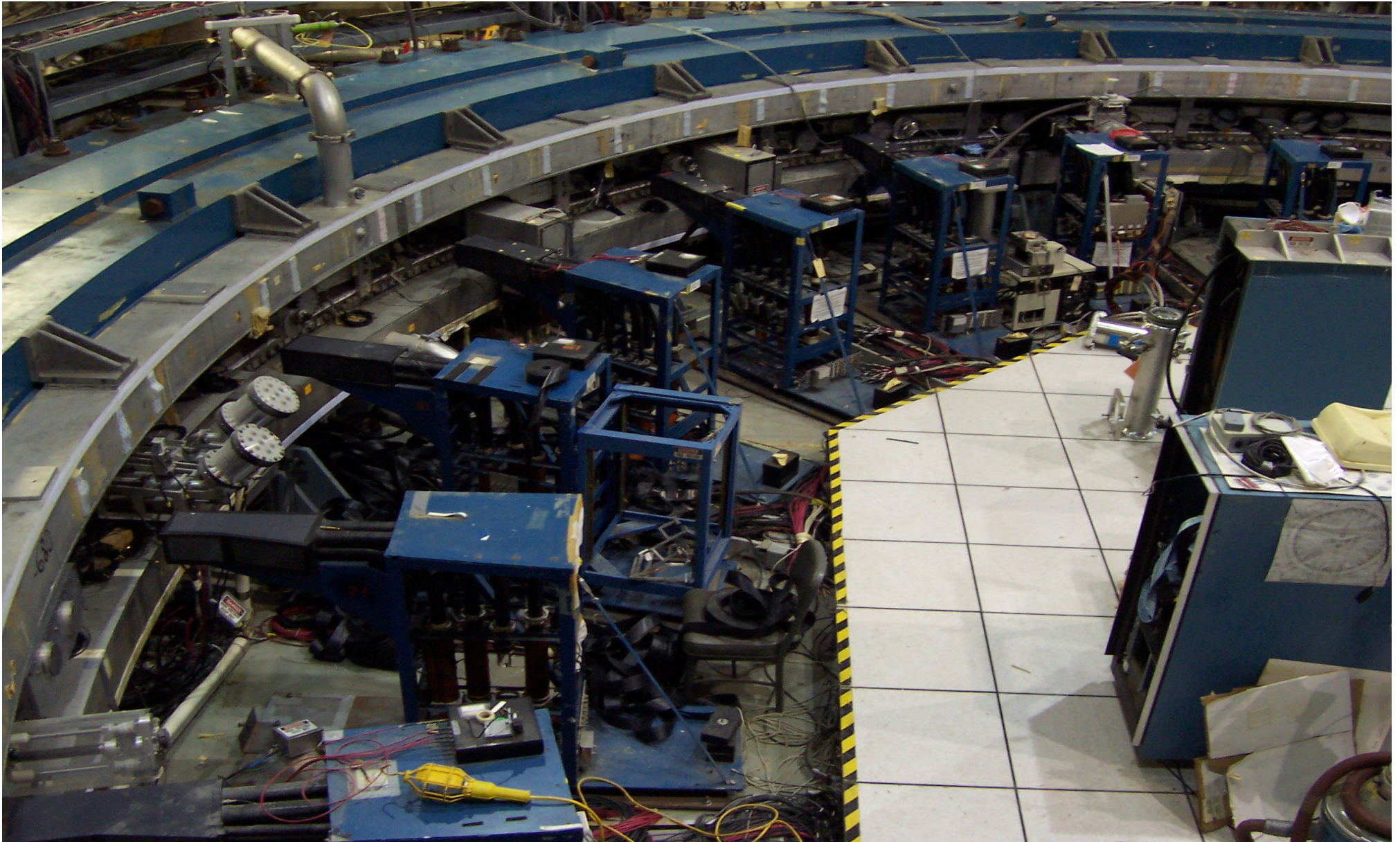
Inject 3.09 GeV muons into a storage ring (B = 1.45 T)

Exploit property that direction of  $e^+$  from  $\mu^+$  decay is strongly correlated with  $\mu^+$  spin for highest energy  $e^+$



24 calorimeters and 3 straw trackers measure  $e^+$  for  $O(1 \text{ ms})$  for spills separated by 10ms.  
 16,000 stored 3.09 GeV muons from  $10^{12}$  protons per spill.



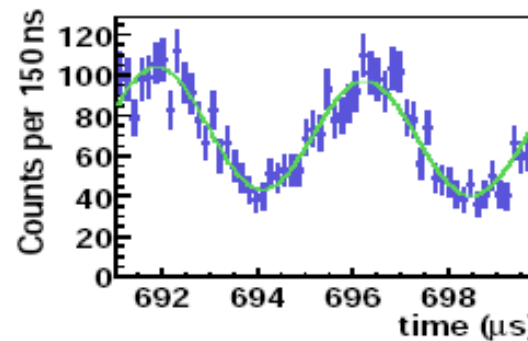
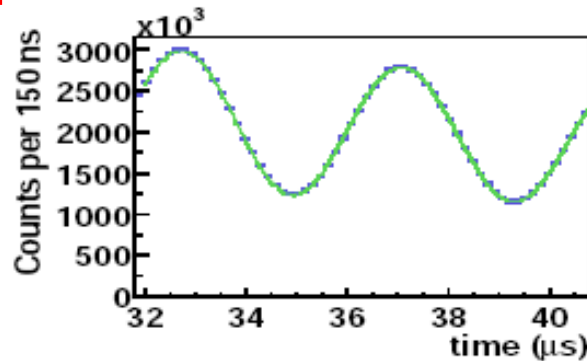
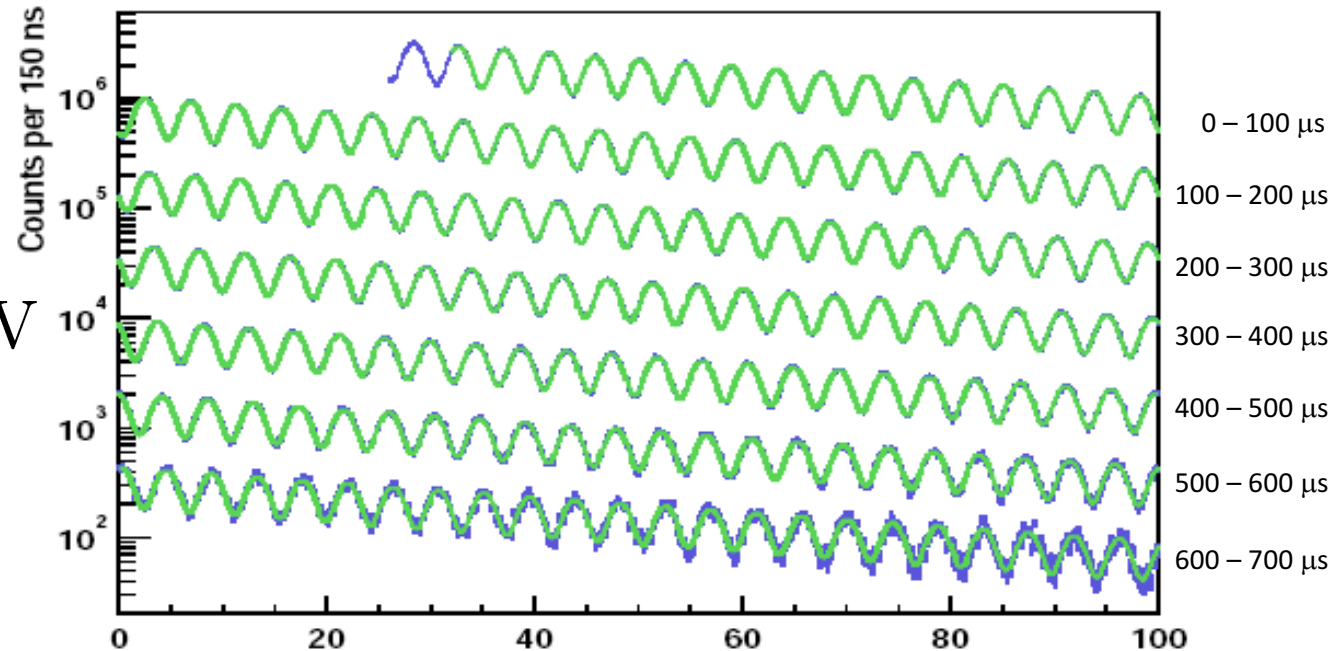


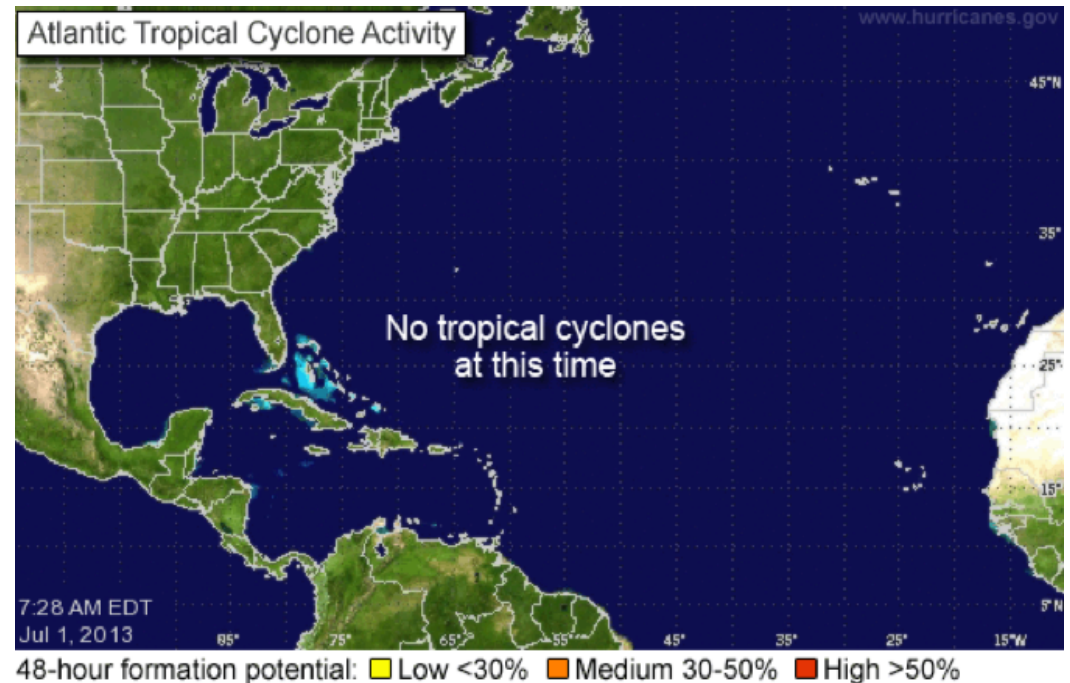
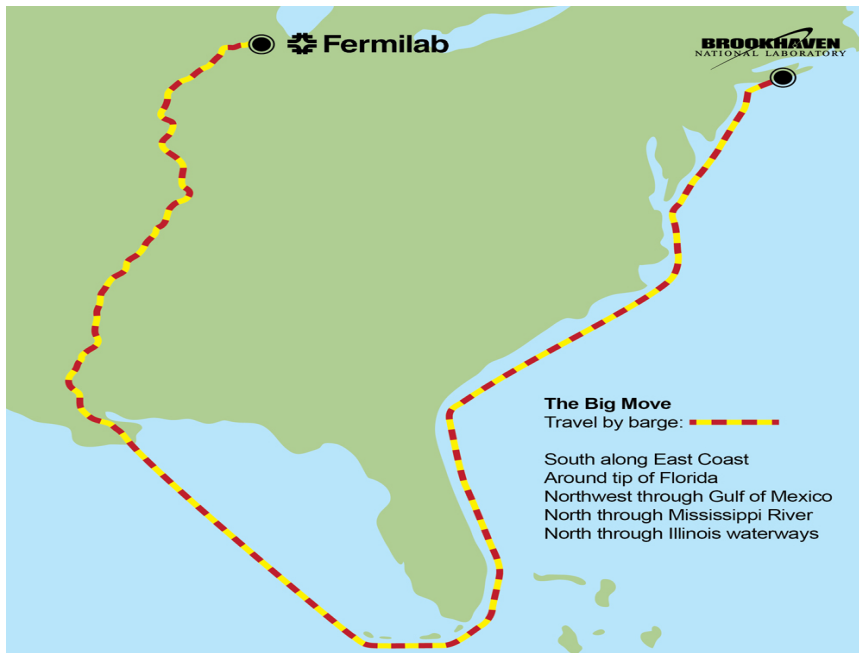
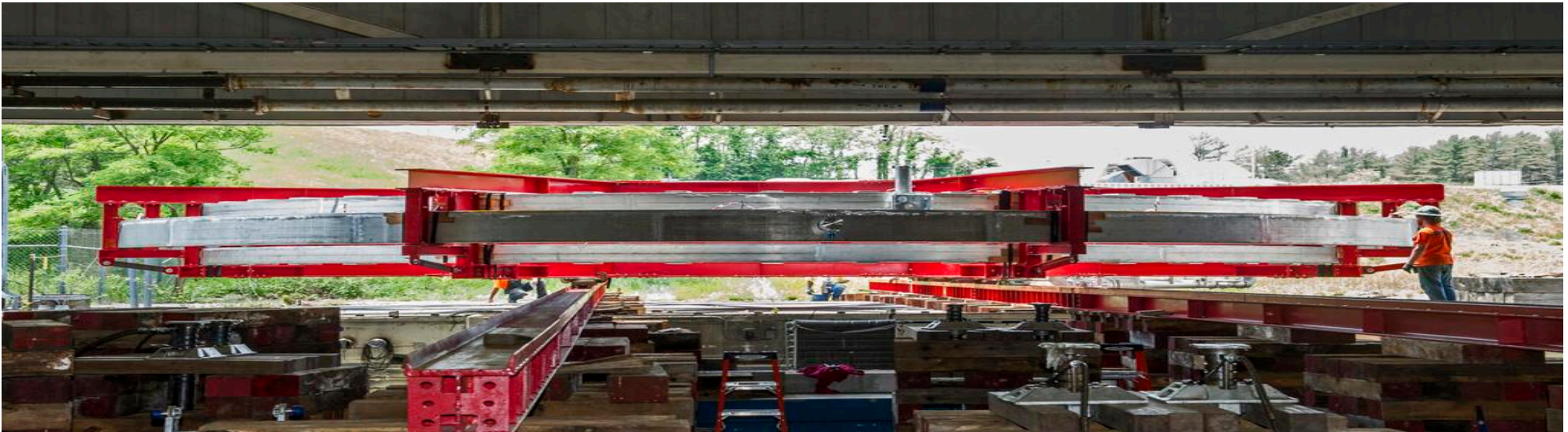


$$N_e(t) \simeq N_0 e^{-\frac{t}{\gamma\tau}} [1 - A \cos(\omega_a t + \phi_a)]$$

$E_{e^+} > 1.8 \text{ GeV}$

Need approx  
100B muons !





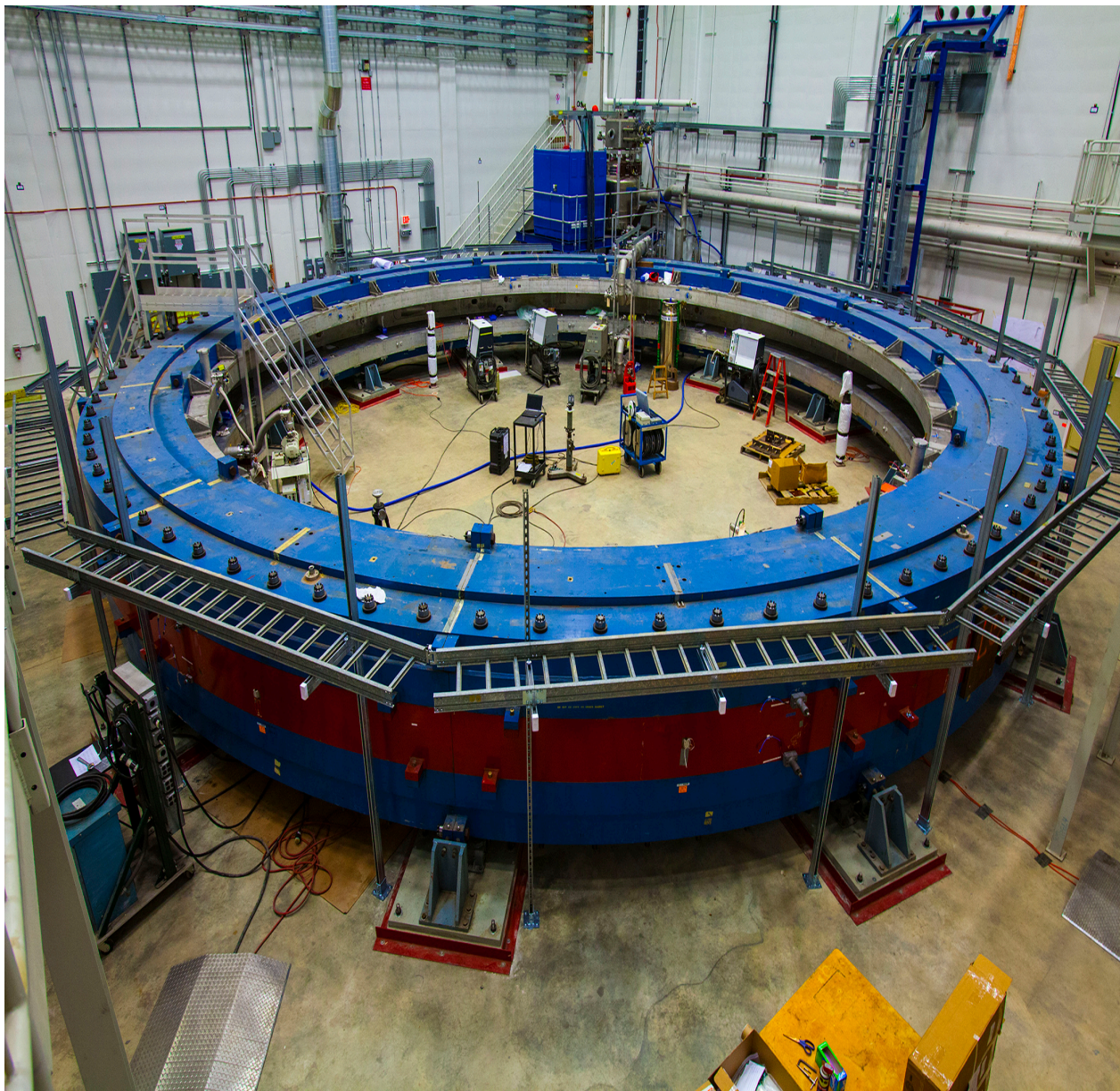




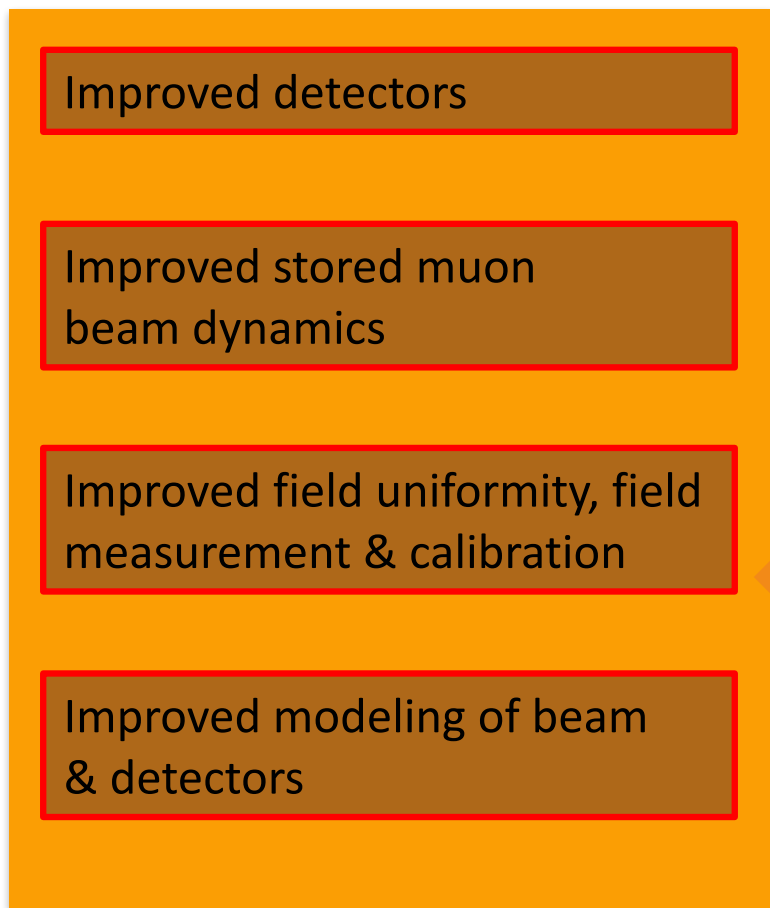
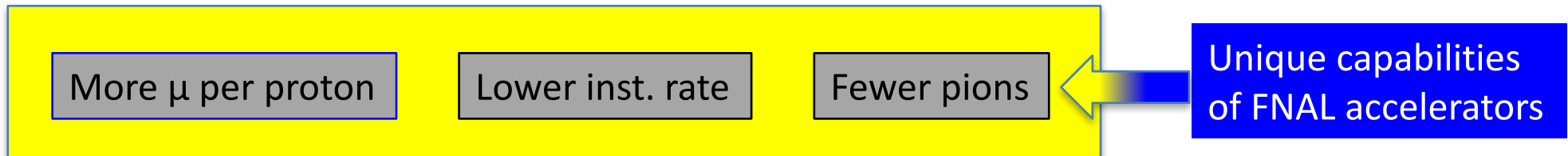




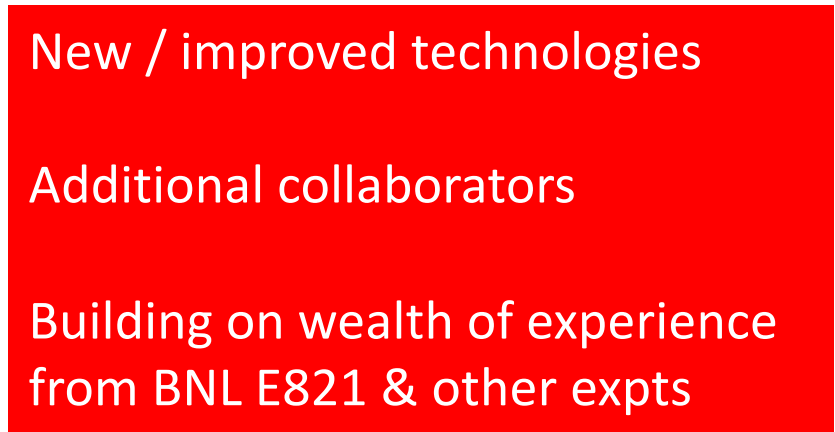




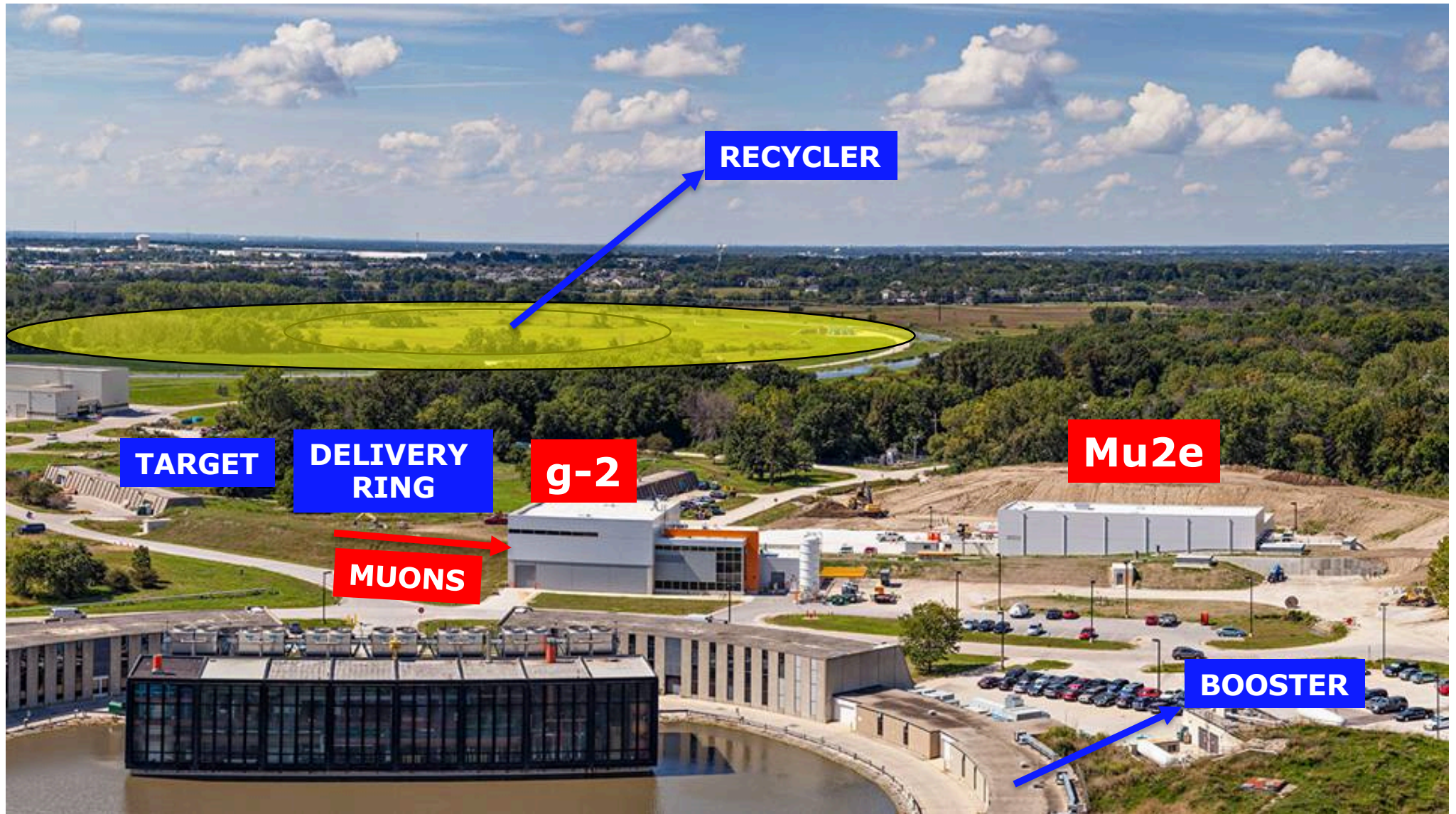




BNL  $\rightarrow$  FNAL  
[54 (stat.)  $\oplus$  33 (syst.)  $\rightarrow$  11 (stat.)  $\oplus$  11 (syst.)]  $\times 10^{-11}$   
0.54 ppm  $\rightarrow$  0.14 ppm



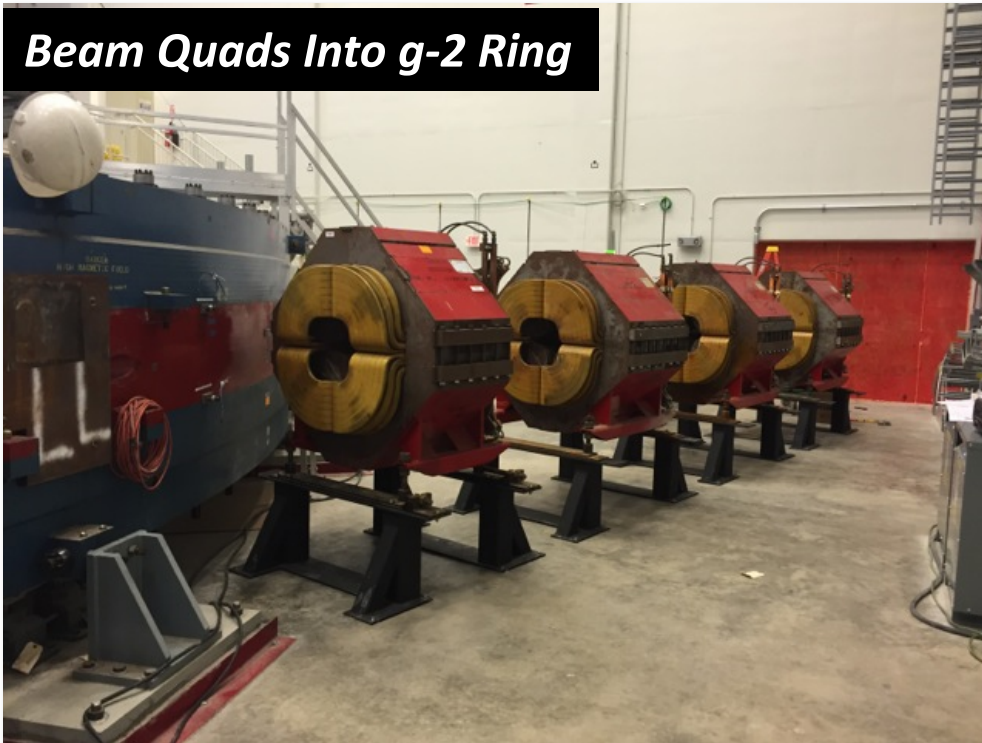






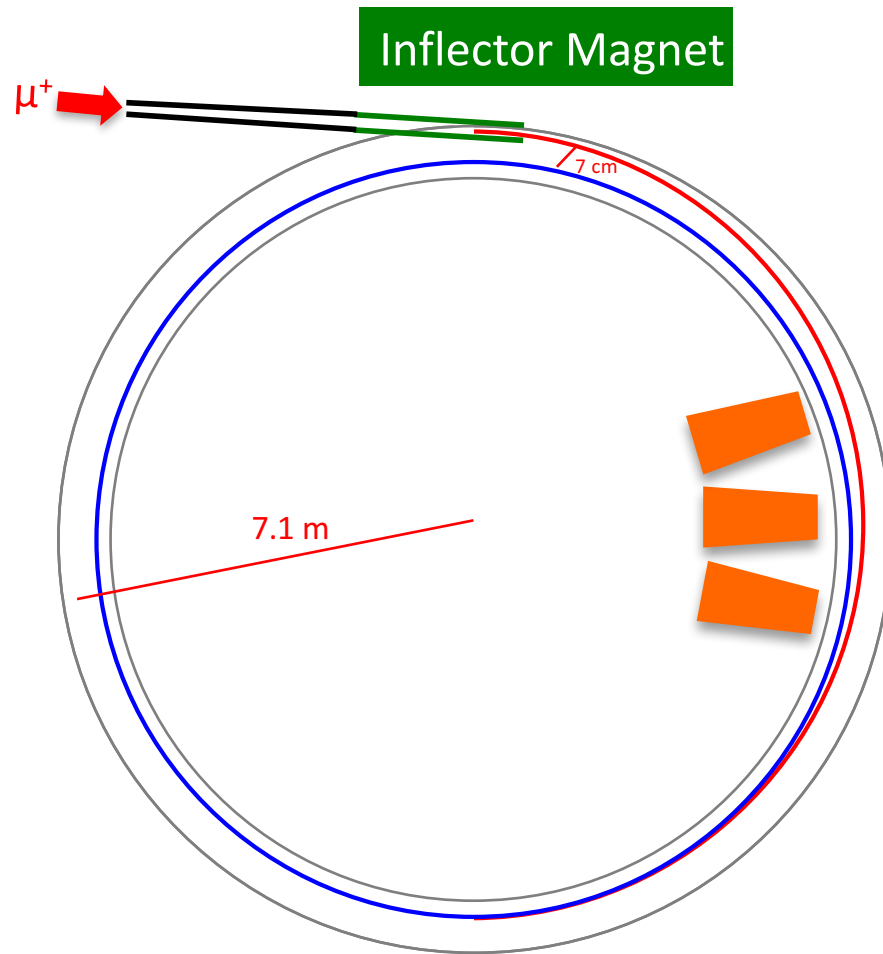
Beam infrastructure 90% complete  
First beams (low muon intensity) from April 2017

**Beam Quads Into g-2 Ring**



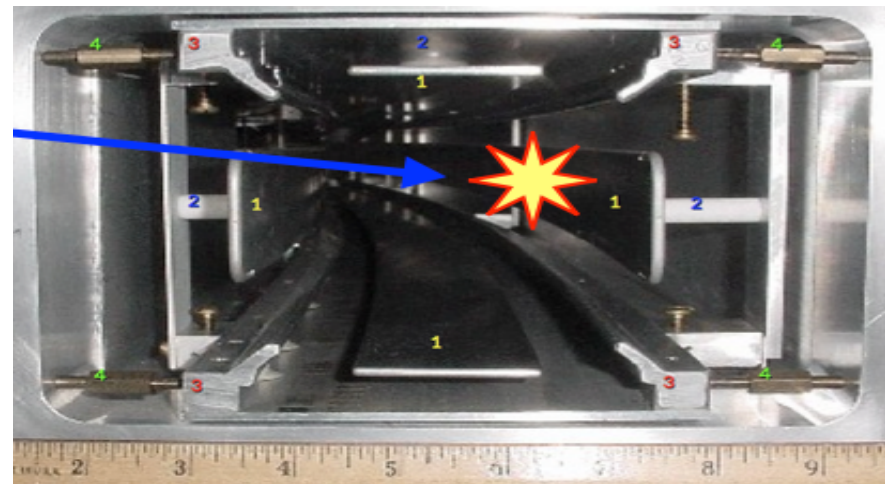
**AP30 Delivery Beamline**



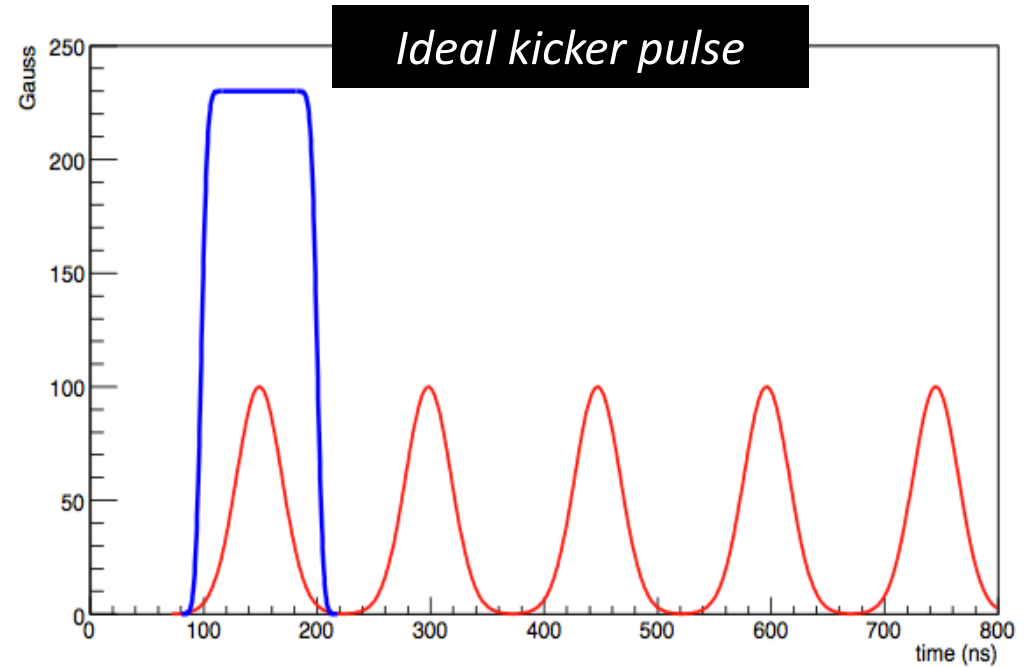
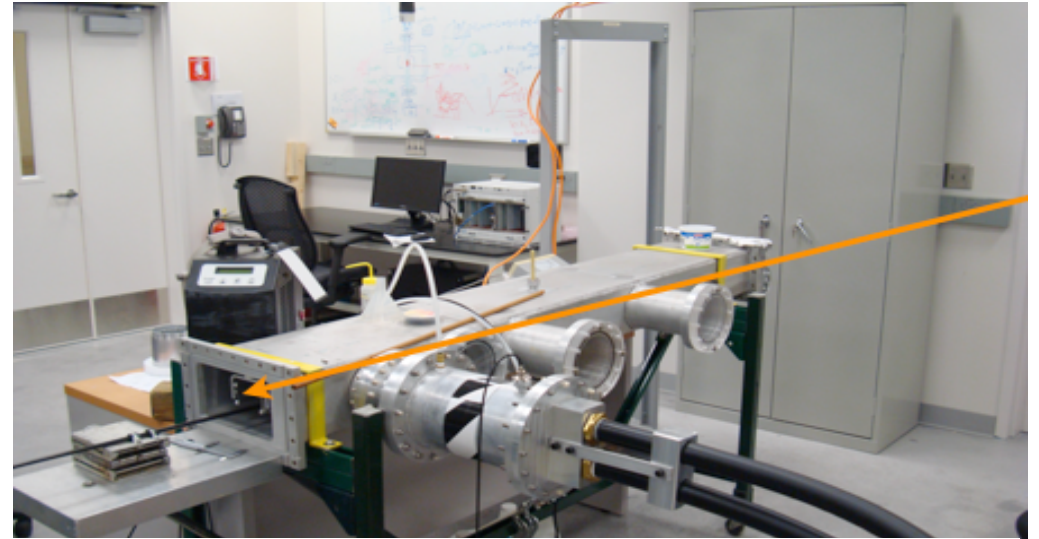
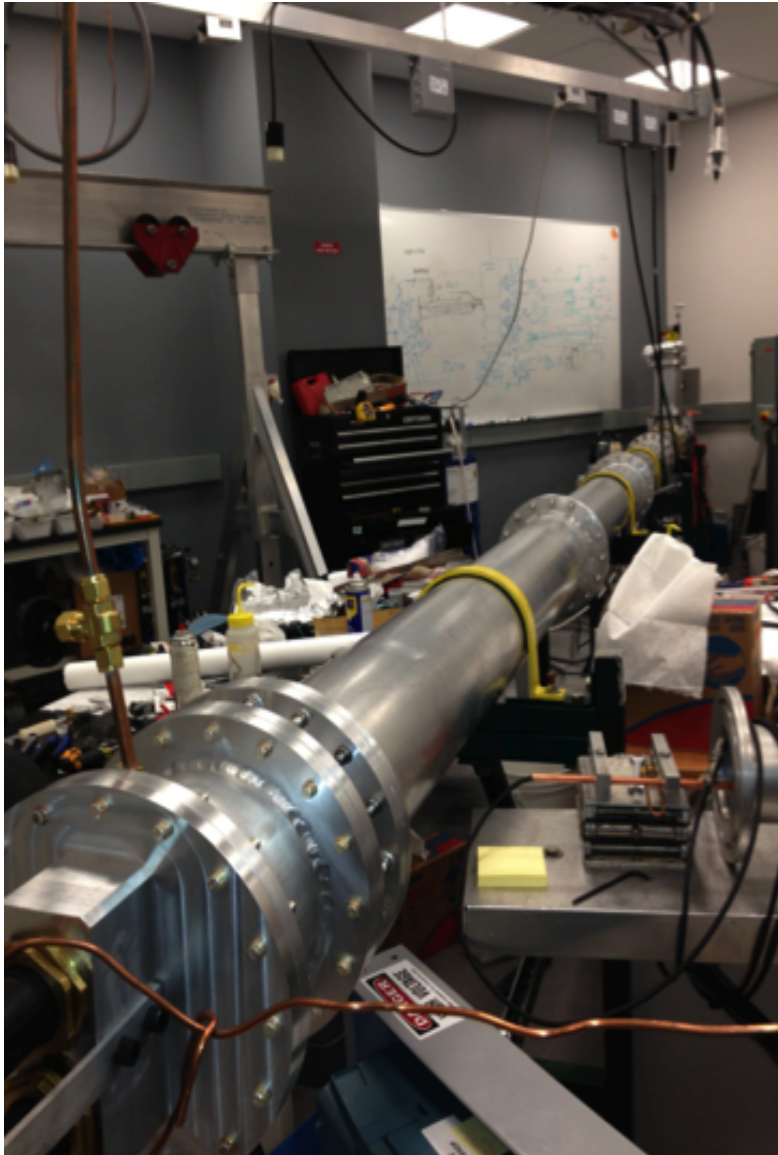


Beam doesn't enter on the correct orbit and needs a kick to get there !

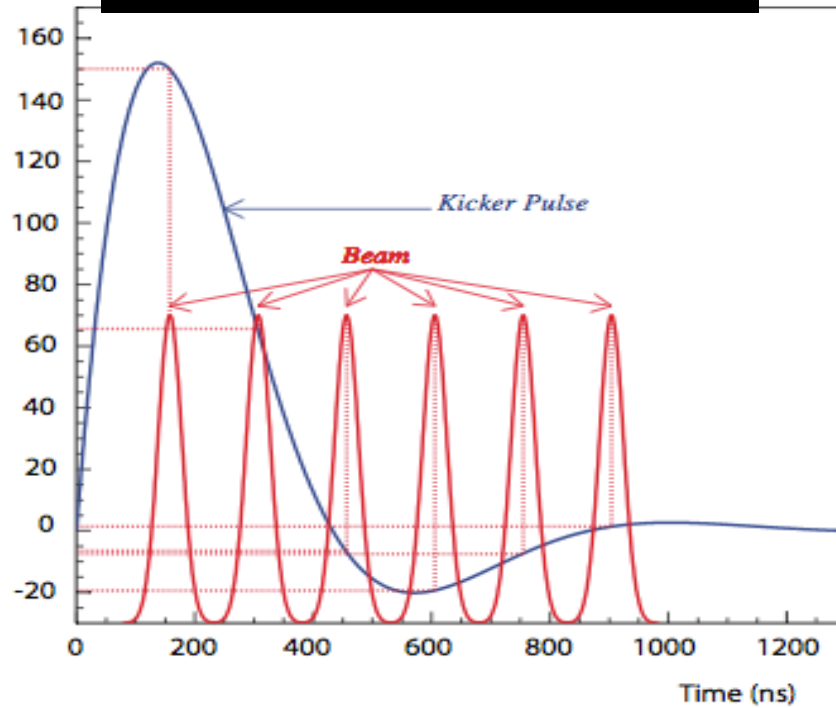
Kicker magnets



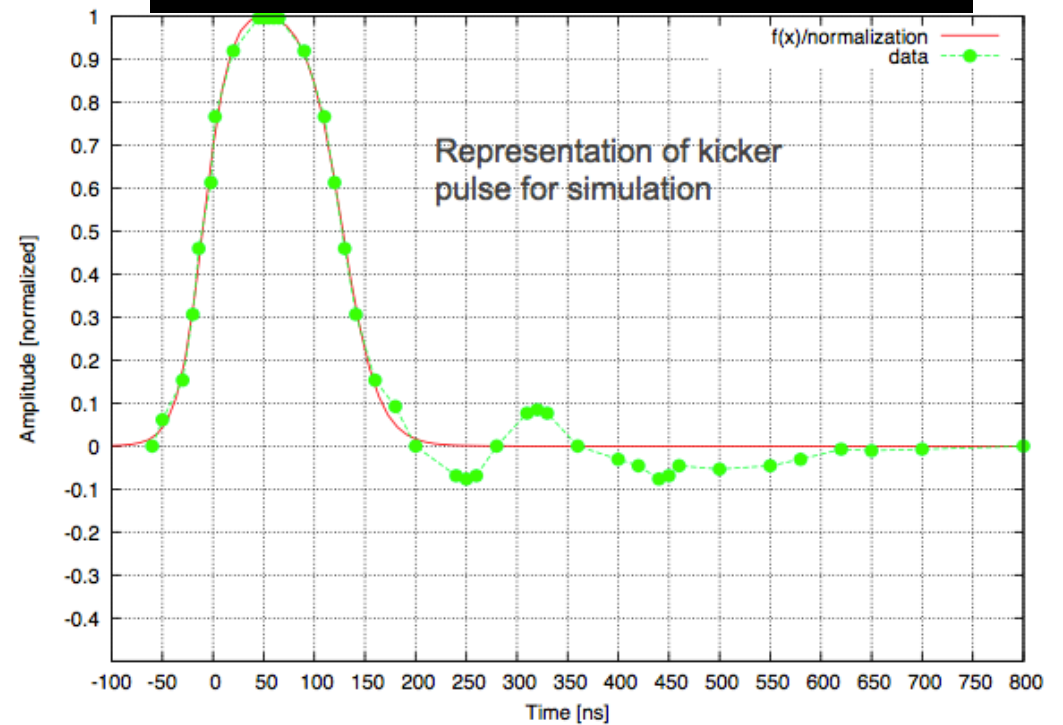


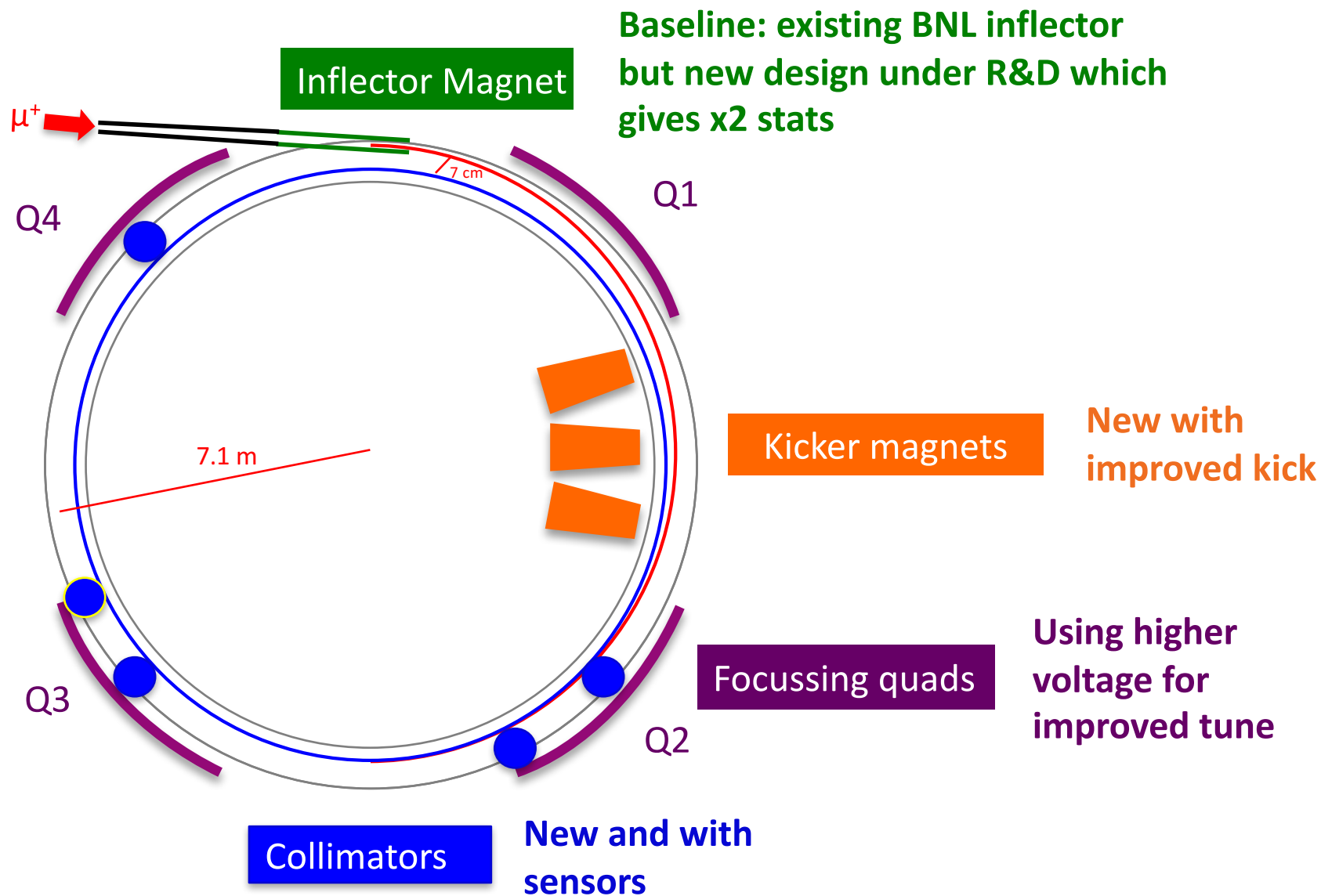


*BNL kicker pulse*

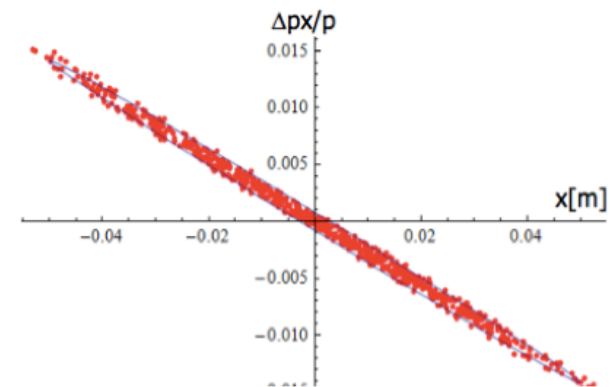
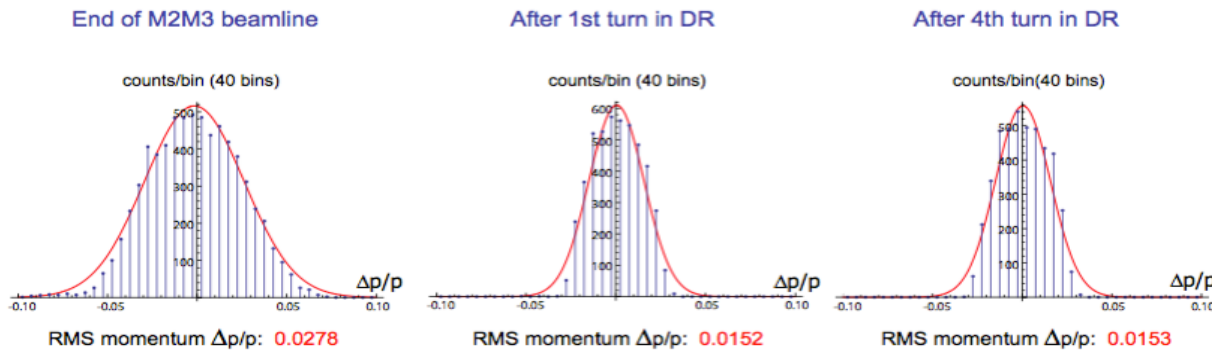
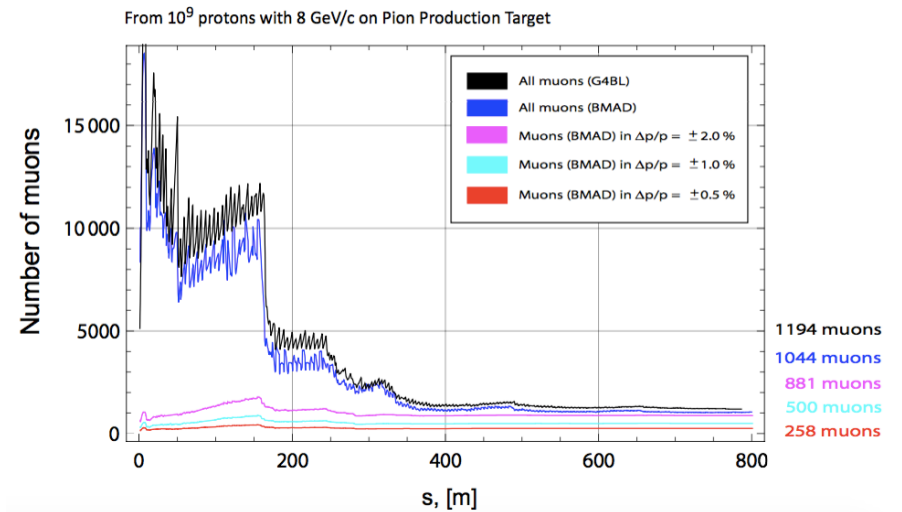


*New FNAL (Cornell) kicker pulse*









72 pole pieces

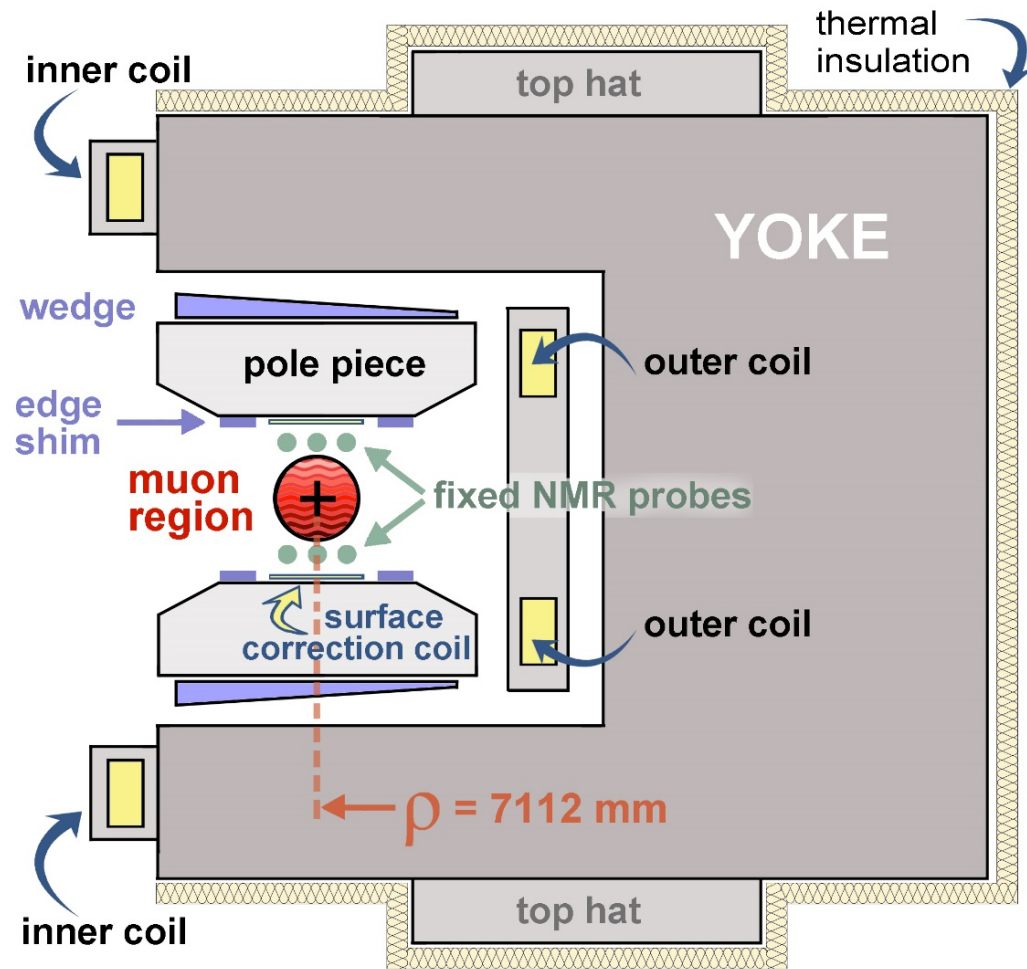
864 wedges

48 iron "top hats"

144 edge shims

8000 surface iron foils

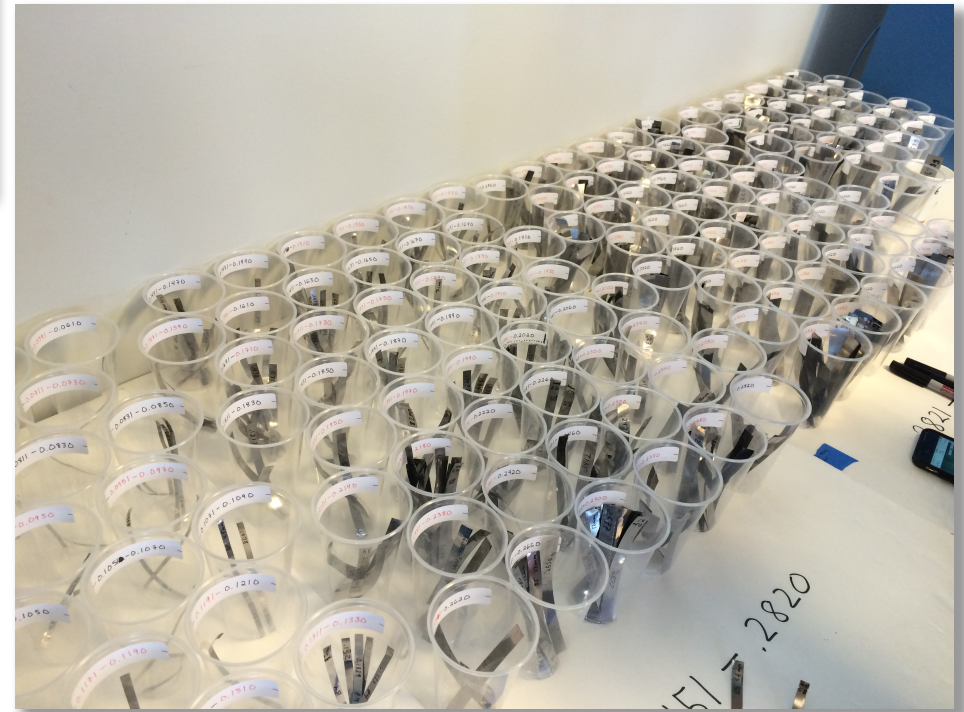
100 active surface coils

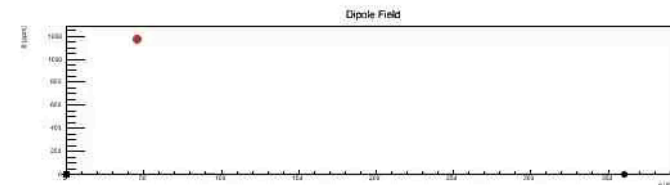
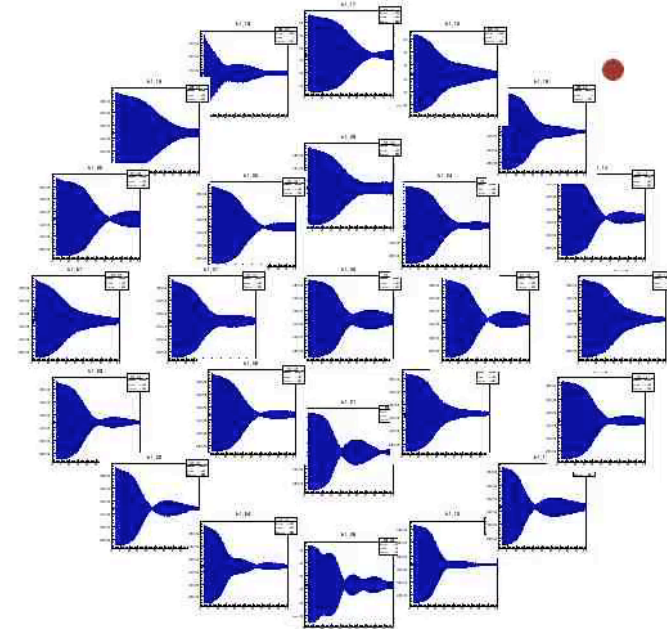
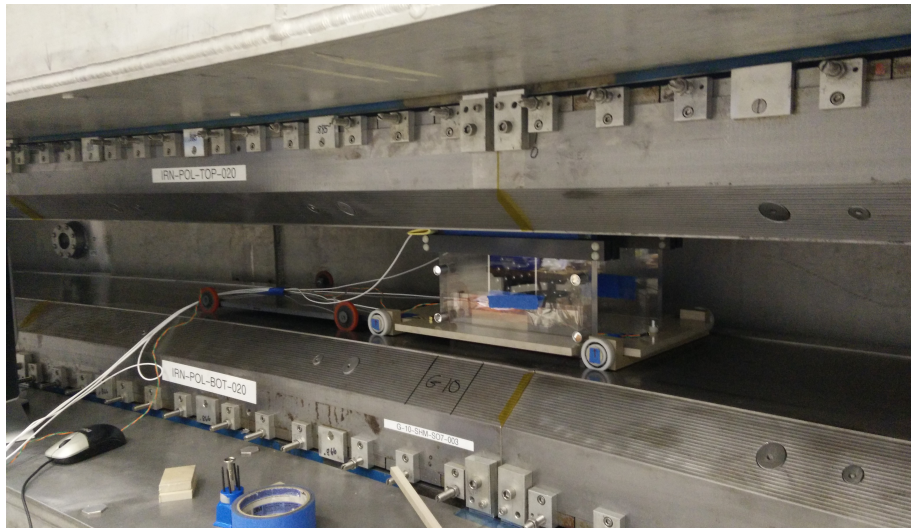


Yoke : 26 tons to 125 microns....

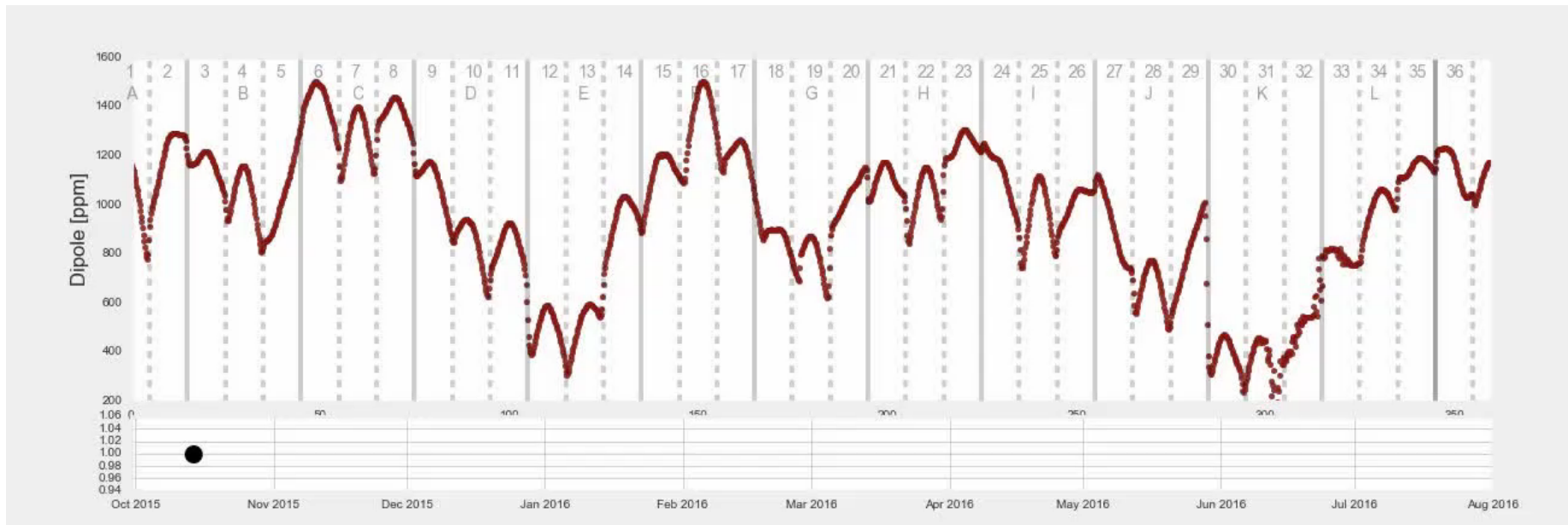


# The laminators !

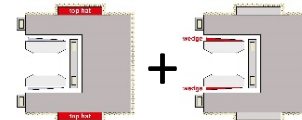




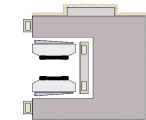




Poles

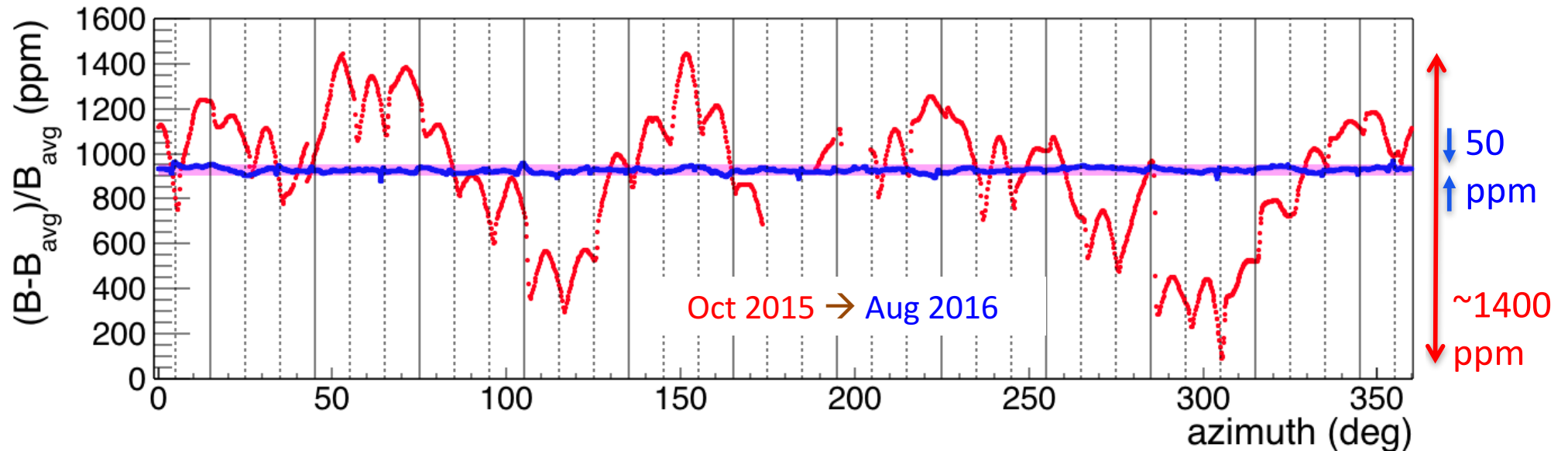


Top hats & wedges

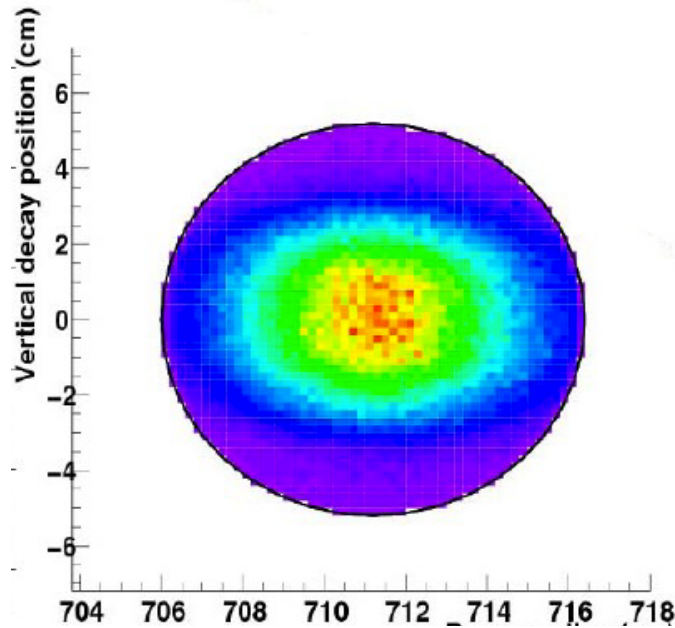


Surface foils

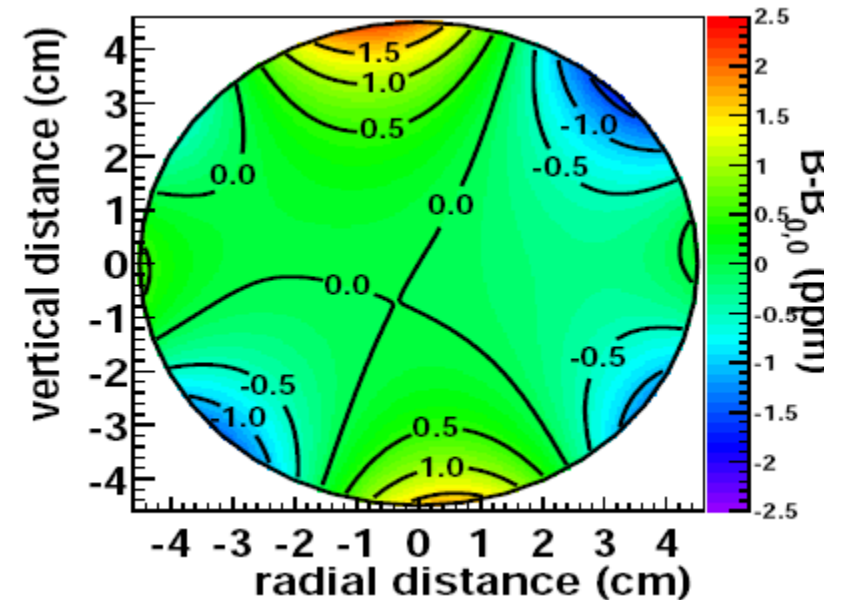
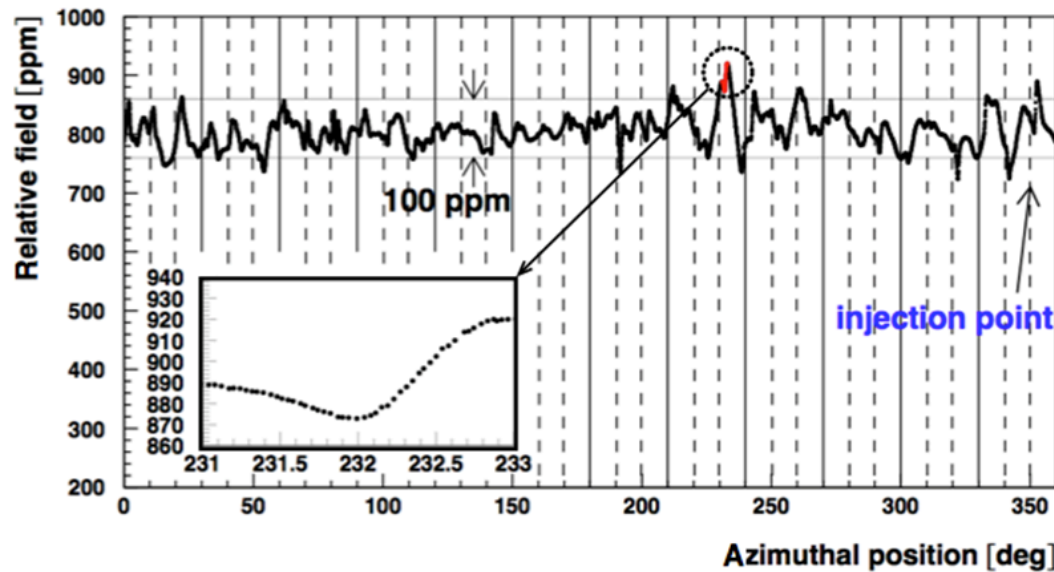
Field uniformity x30 improved in a year and now x4 better than achieved at BNL after first shimming round.







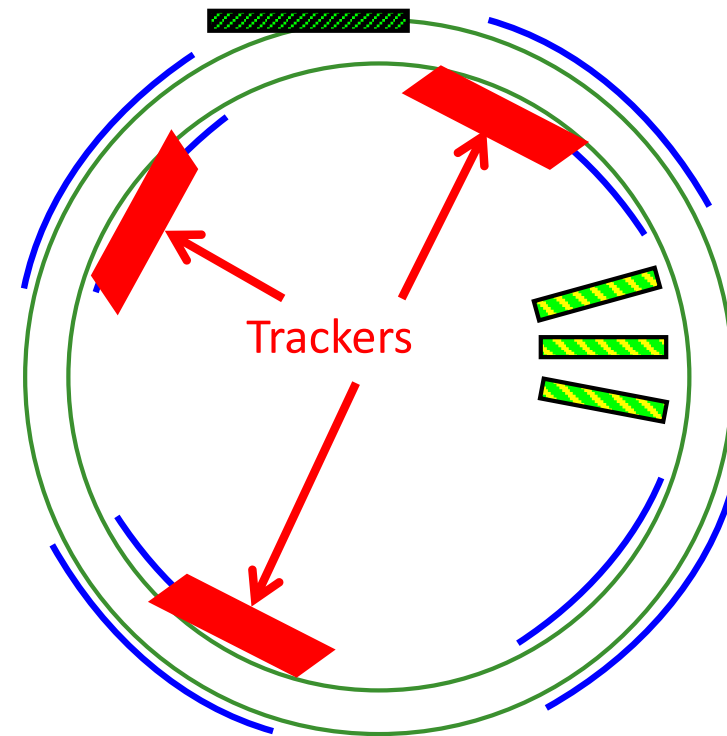
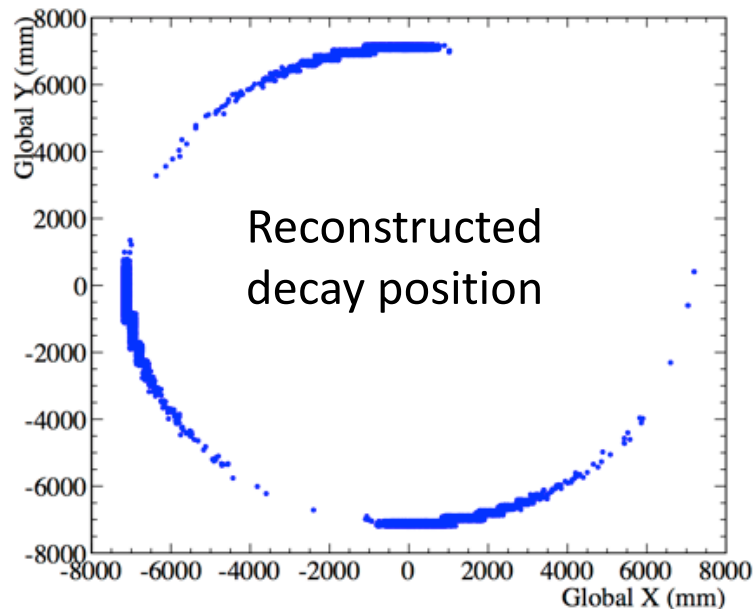
Muons are distributed over storage volume  
B-field is not uniform over this volume  
Need to convolute the two.



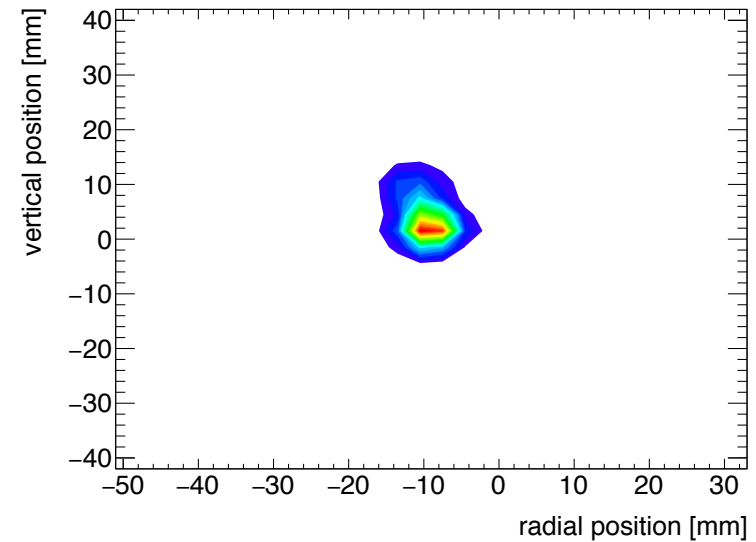
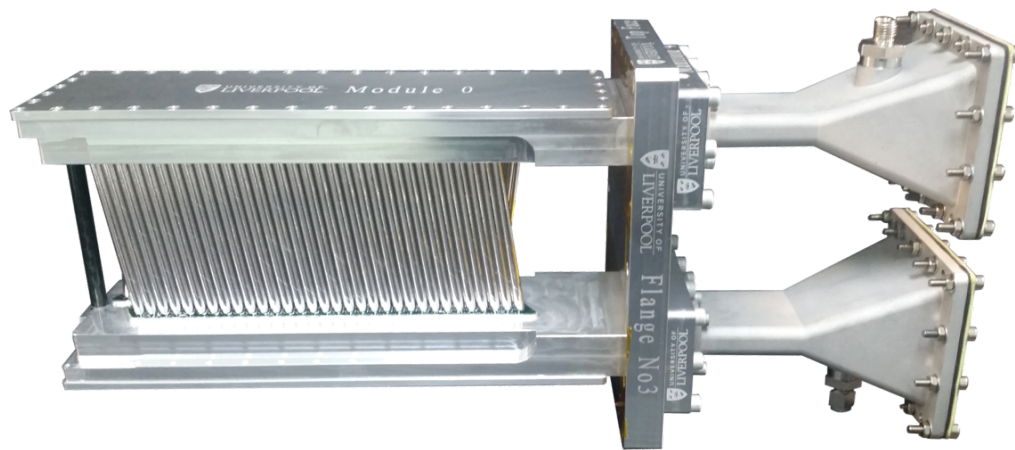
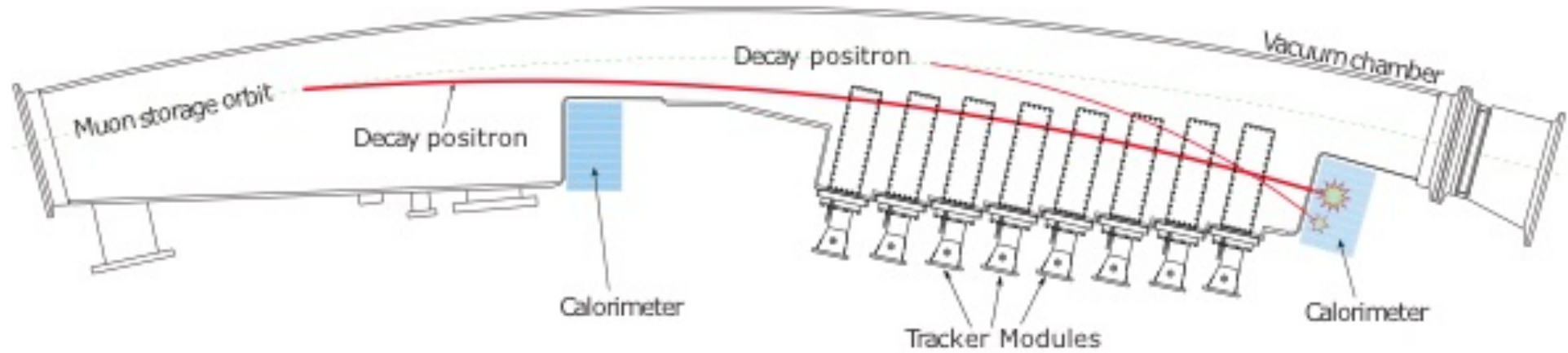
Measure beam profile

Identify pileup and muons lost from beam

Measure EDM



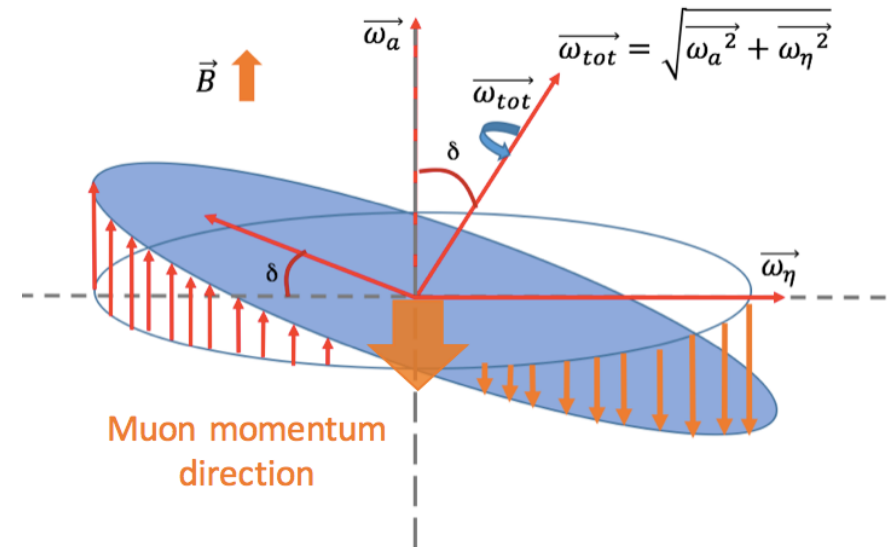
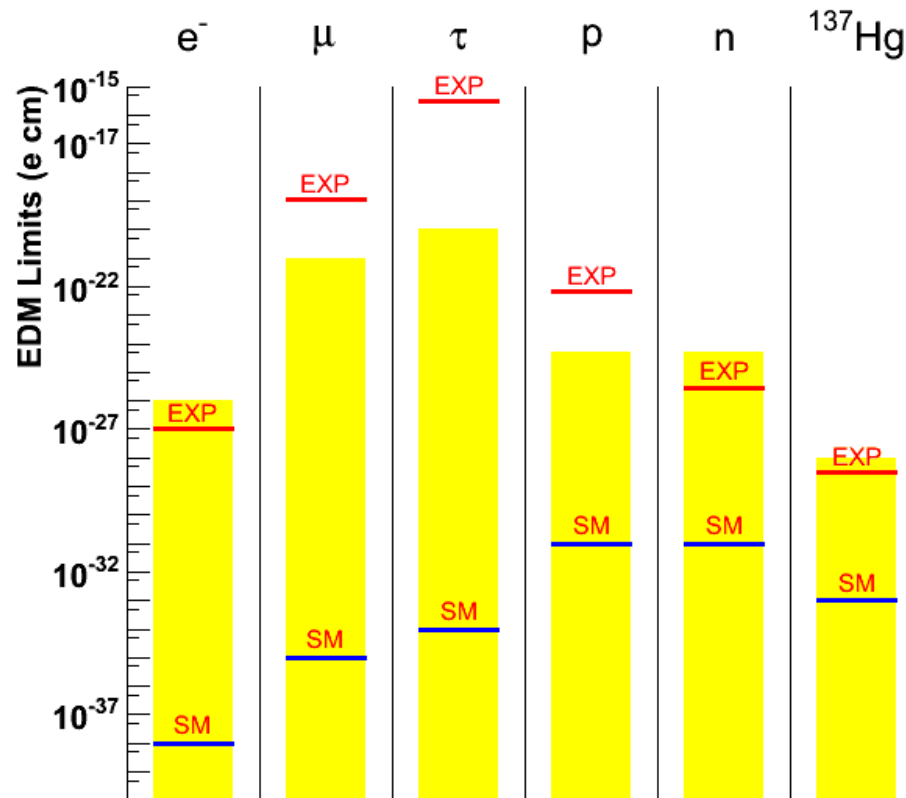








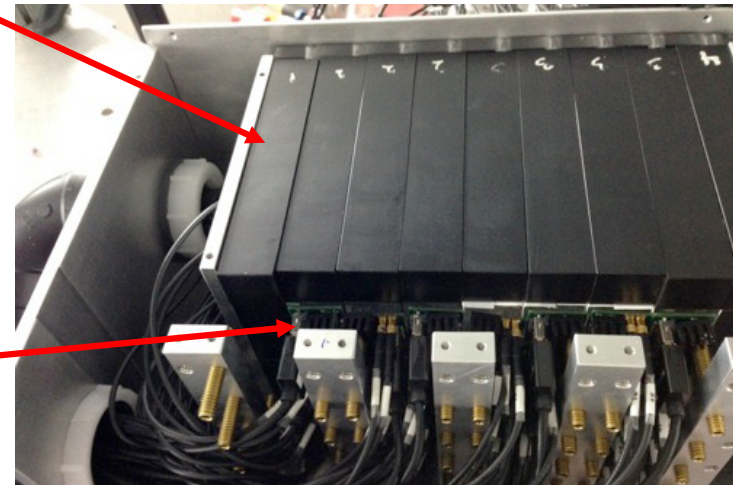
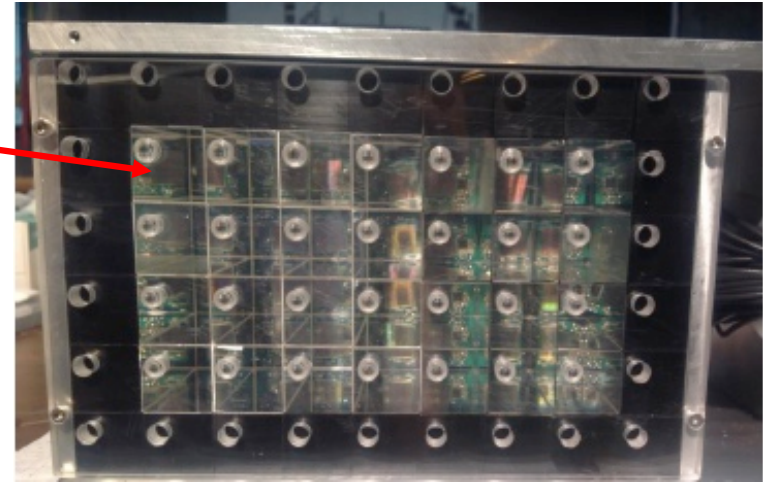
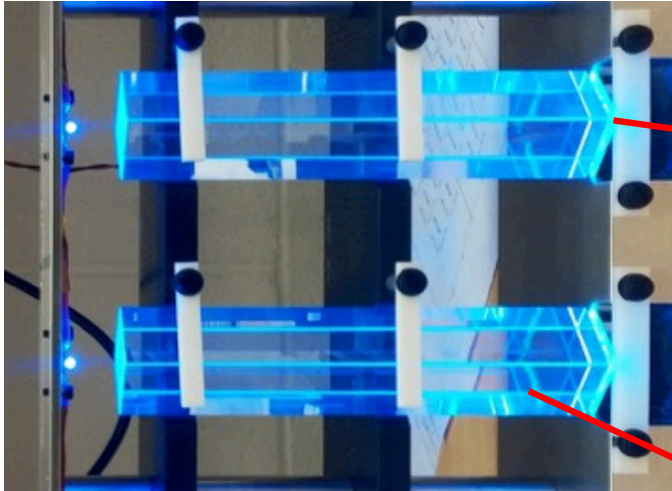
Essentially zero in SM : any observation is new physics



Expect several billion events in the trackers and so reach  $10^{-21}$  vs  $2 \times 10^{-19}$  at BNL

Needs non mass-scaling BSM effects to be in expt's reach given  $e^-$  EDM limit

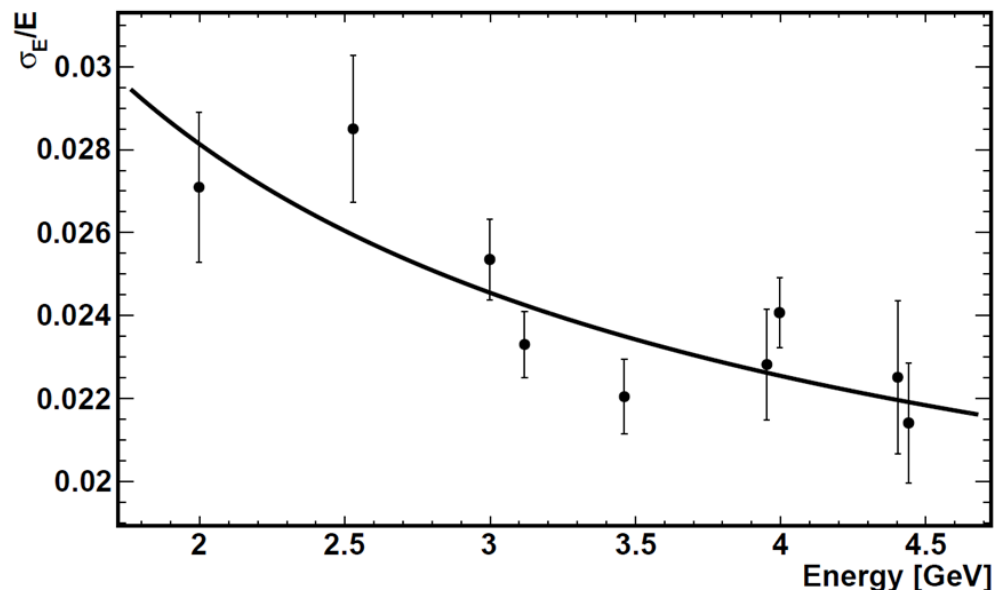
50 MeV resolution at 2 GeV and pulse separation < 5ns.



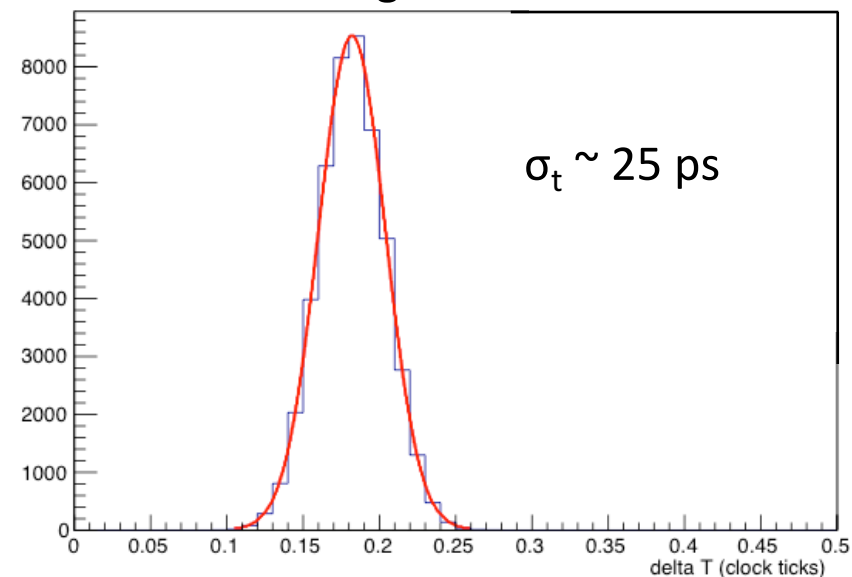


### Energy Resolution

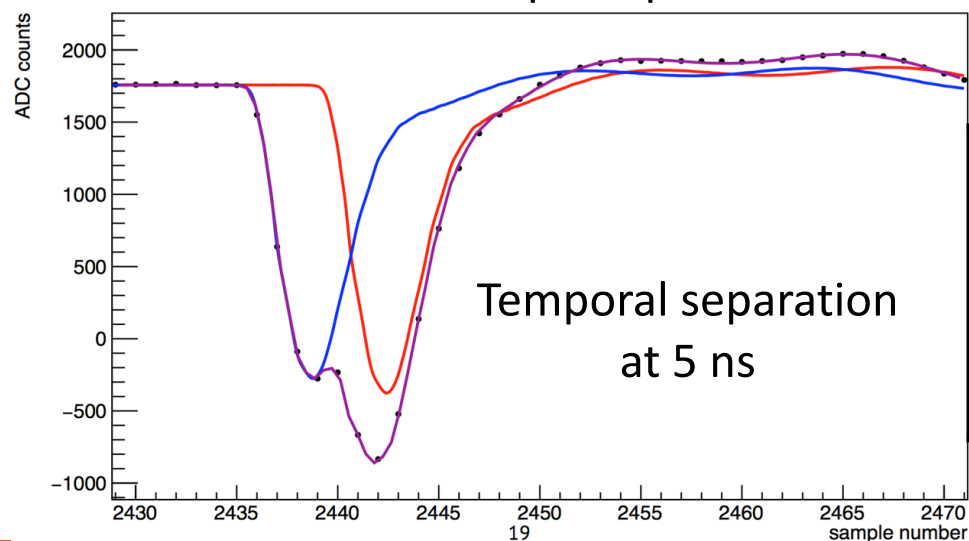
[NIM A 783 \(2015\)](#),



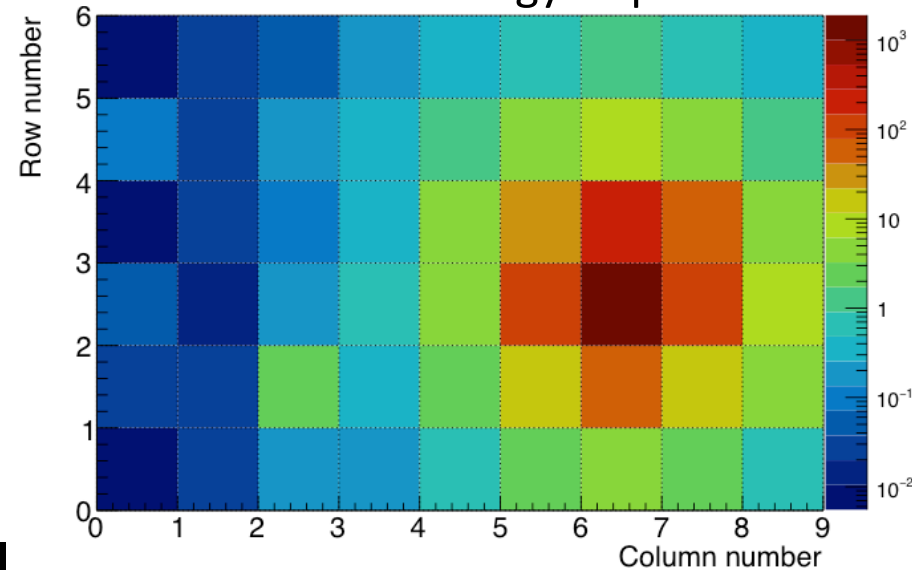
### Timing Resolution



### Electron pile-up



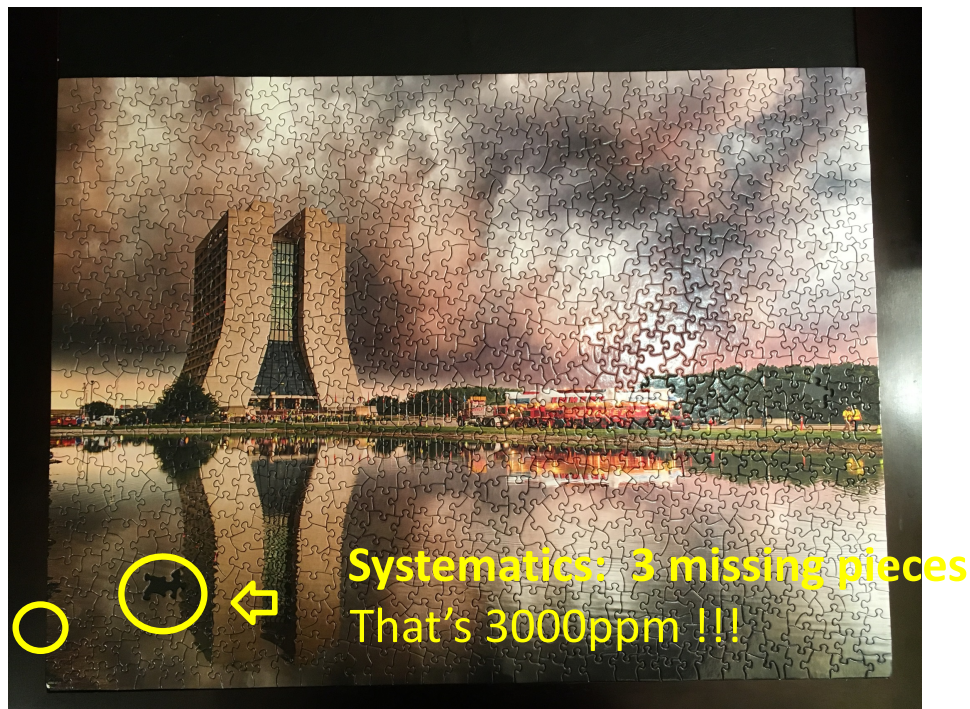
### Position from Energy Deposit



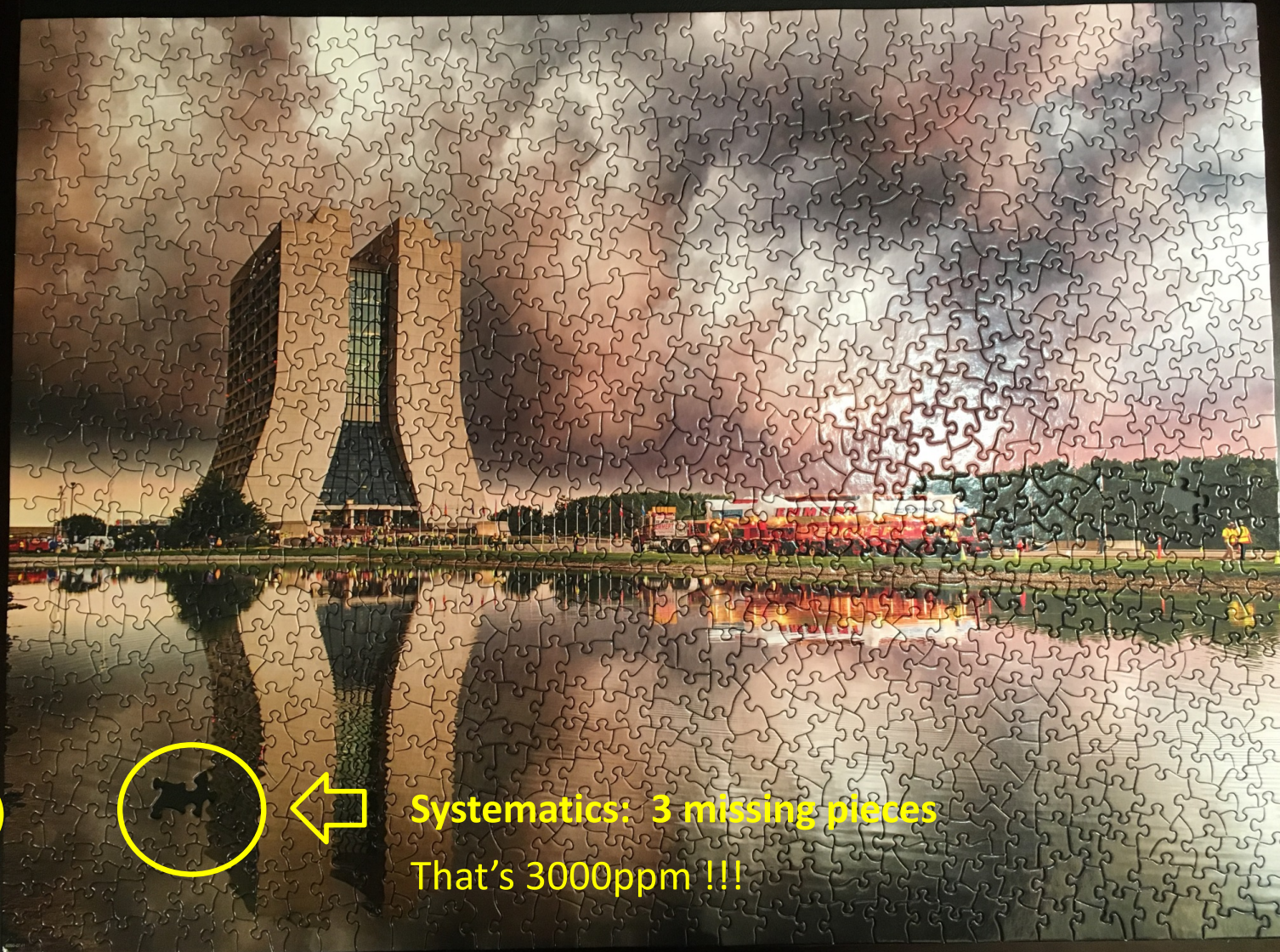
1st beam is expected in April with first muon data to be accumulated towards the end of 2017.

BNL-level statistics by mid-2018 and by 2020 x20 the statistics

Expectation is to publish 3 results with 100%, 50% and 25% of BNL precision



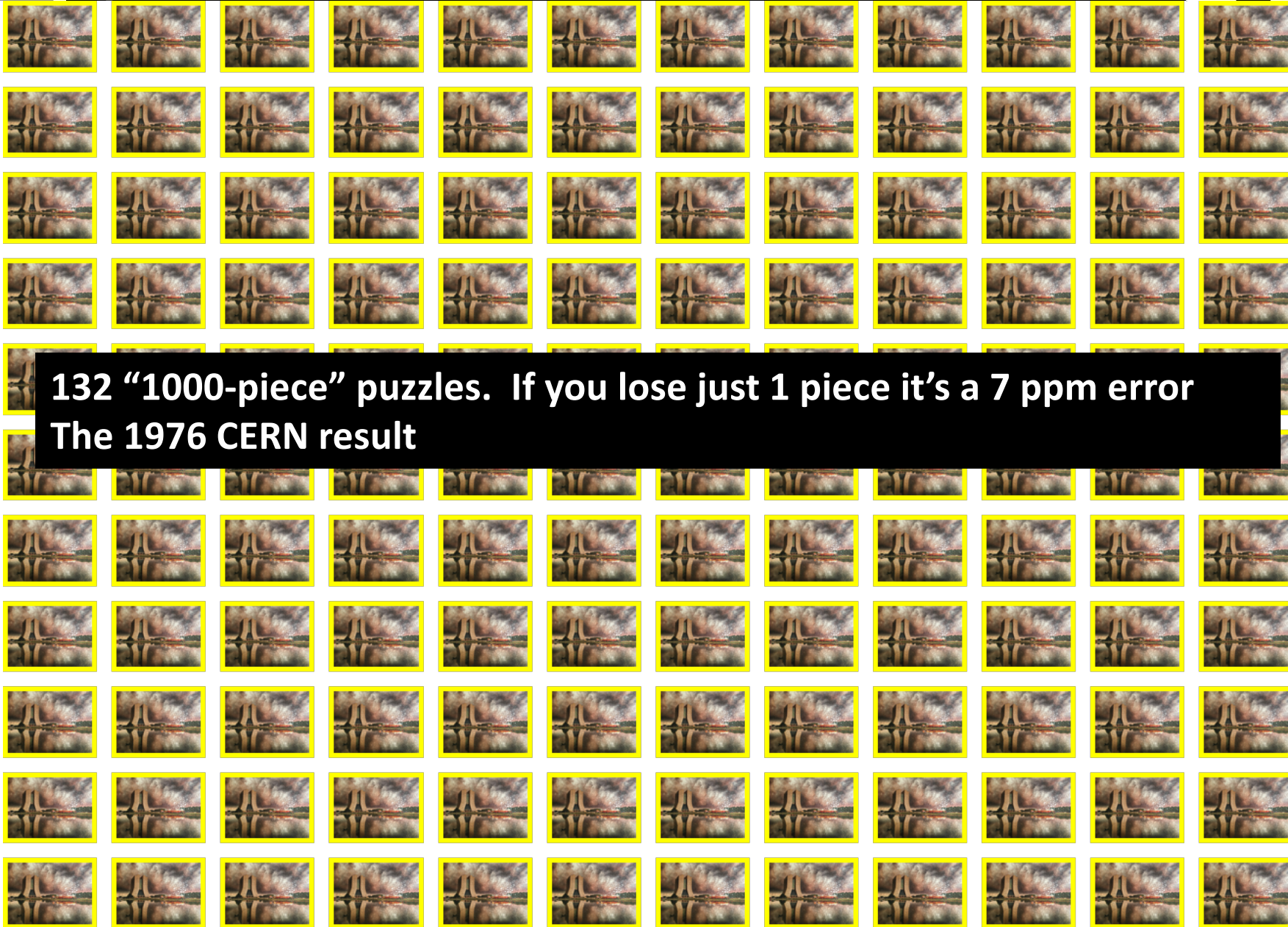




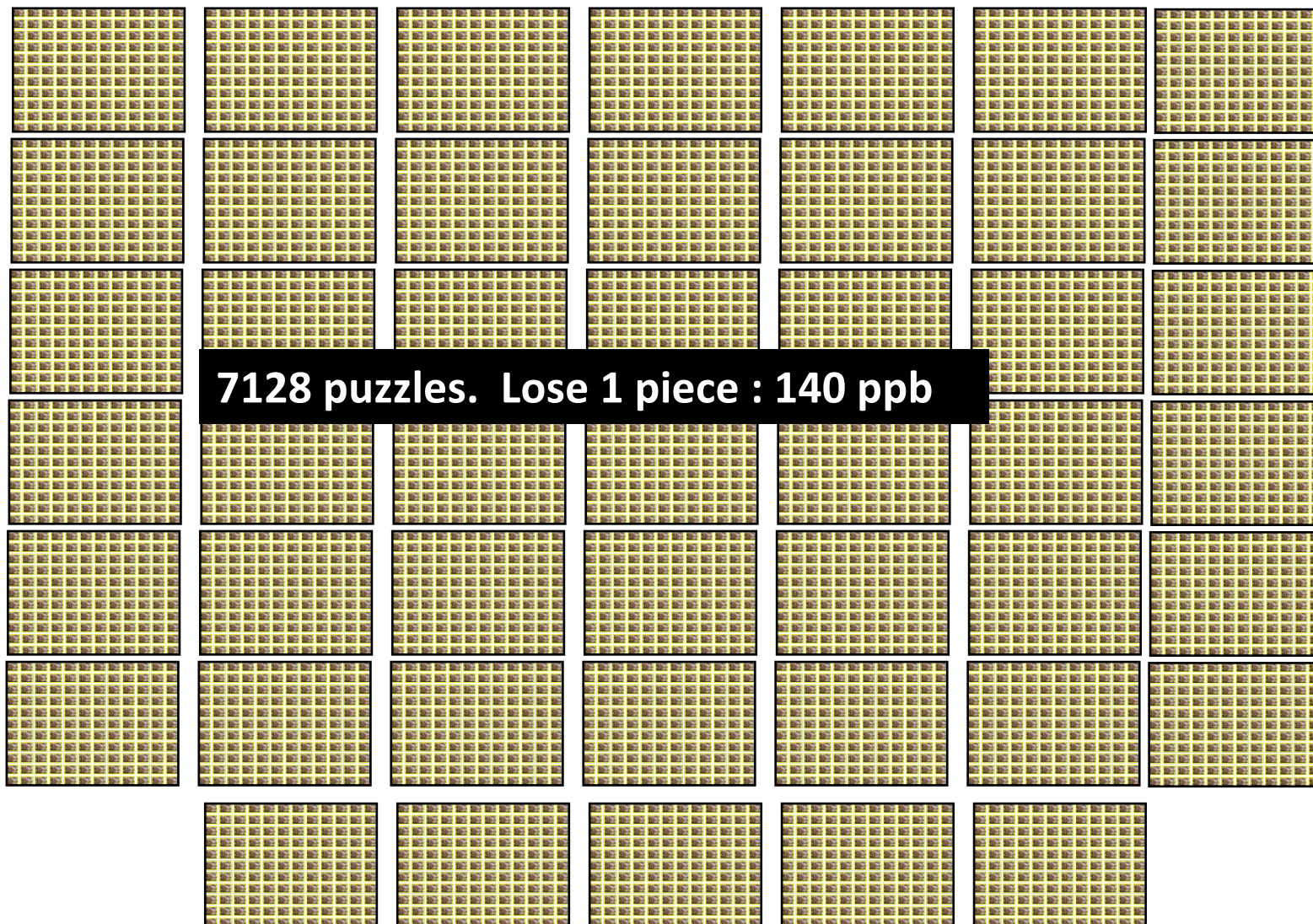
**Systematics: 3 missing pieces**

**That's 3000ppm !!!**

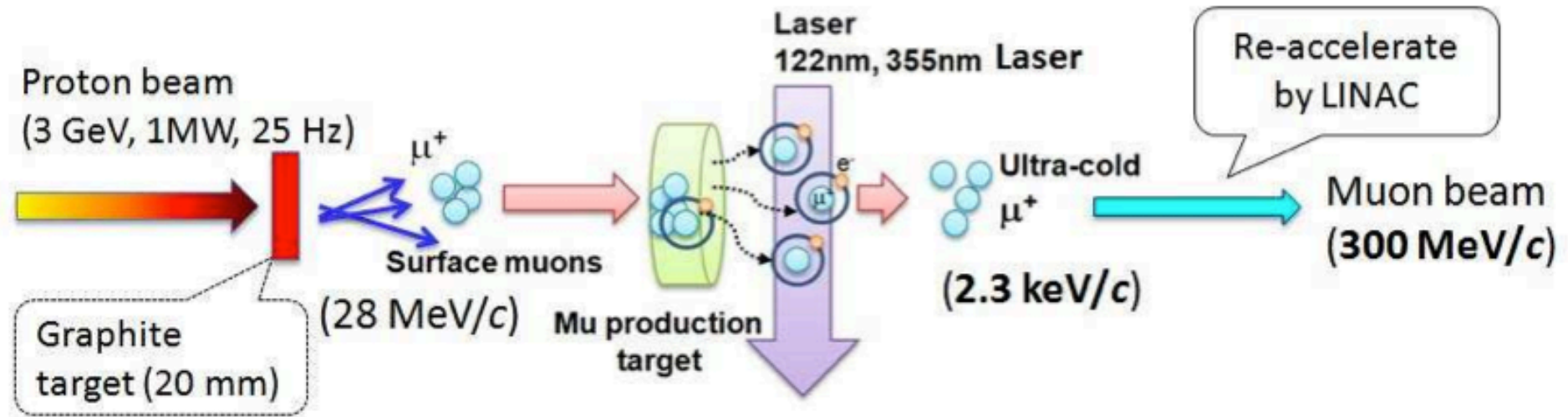




**132 “1000-piece” puzzles. If you lose just 1 piece it’s a 7 ppm error  
The 1976 CERN result**

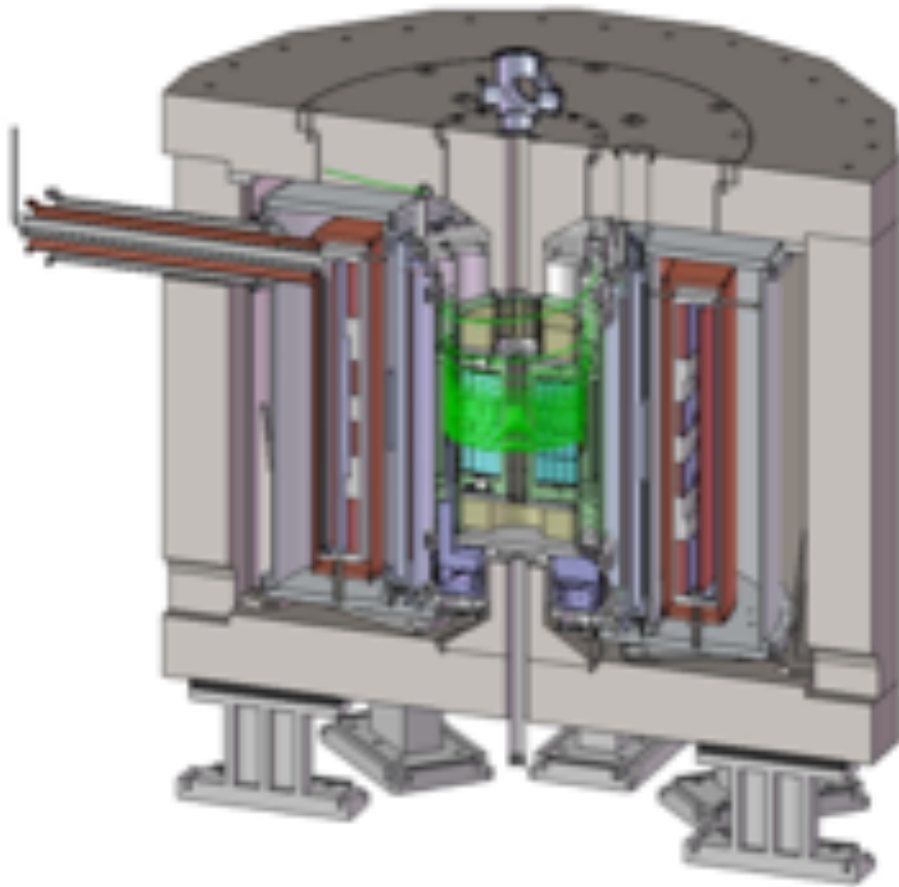






Requires several innovations to achieve  $10^6$  muons/sec

- production of sufficient muonium using special materials
- pulsed 100  $\mu$ J VUV lasers to ionise muonium
- muon linac keeping  $\Delta p_T/p_T < 1e-5$  : world's 1<sup>st</sup> muon accelerator !



Very precise tracking using  
Si detectors

Very uniform field (MRI magnet)

Spiral 3D beam injection !



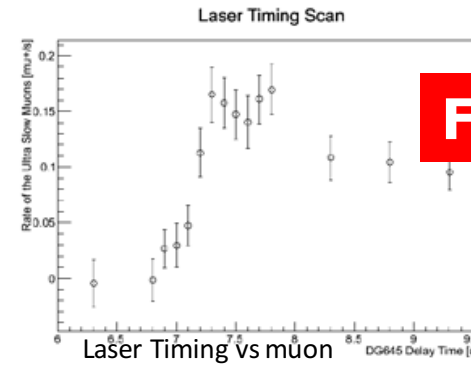
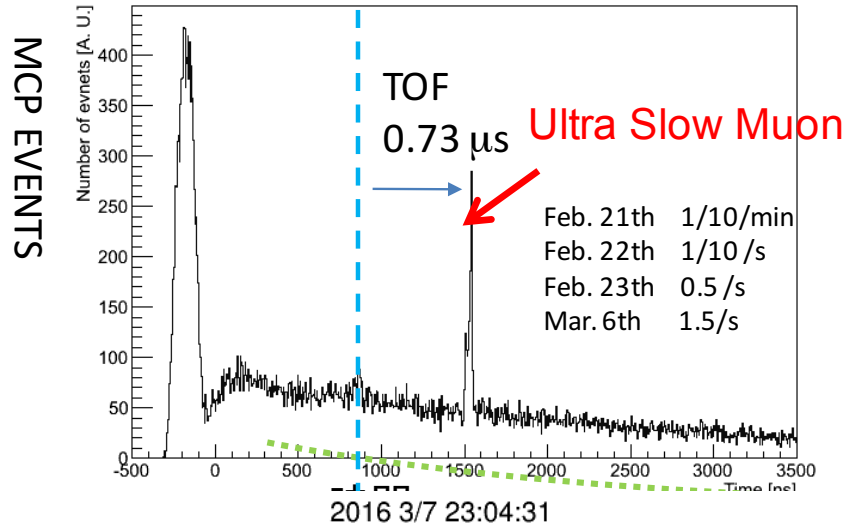


## Observation of Ultra Slow Muons @U-Line

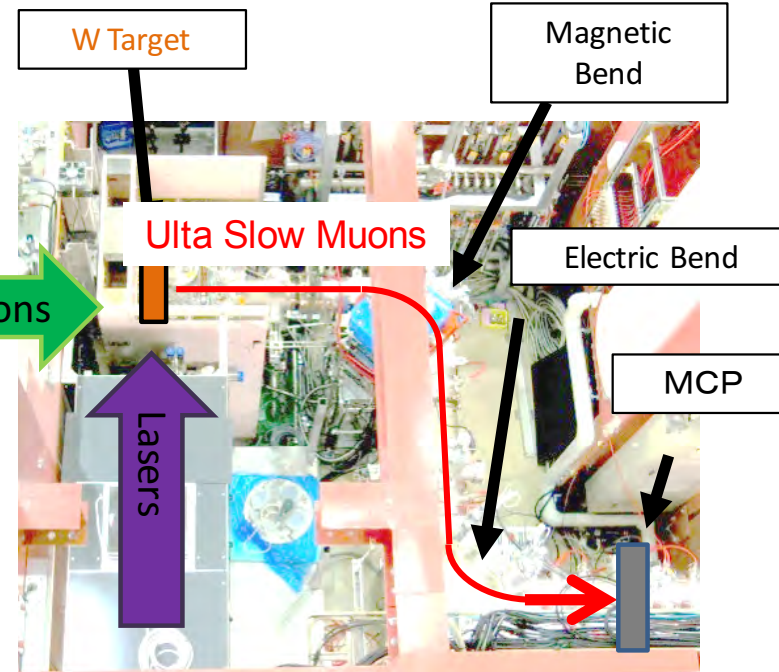
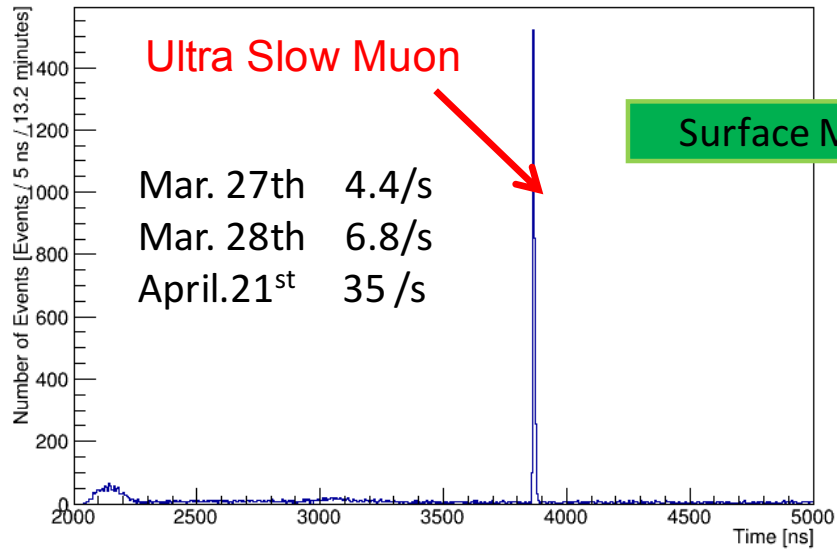
ULTRASLOW  
MUON  
MICROSCOPE



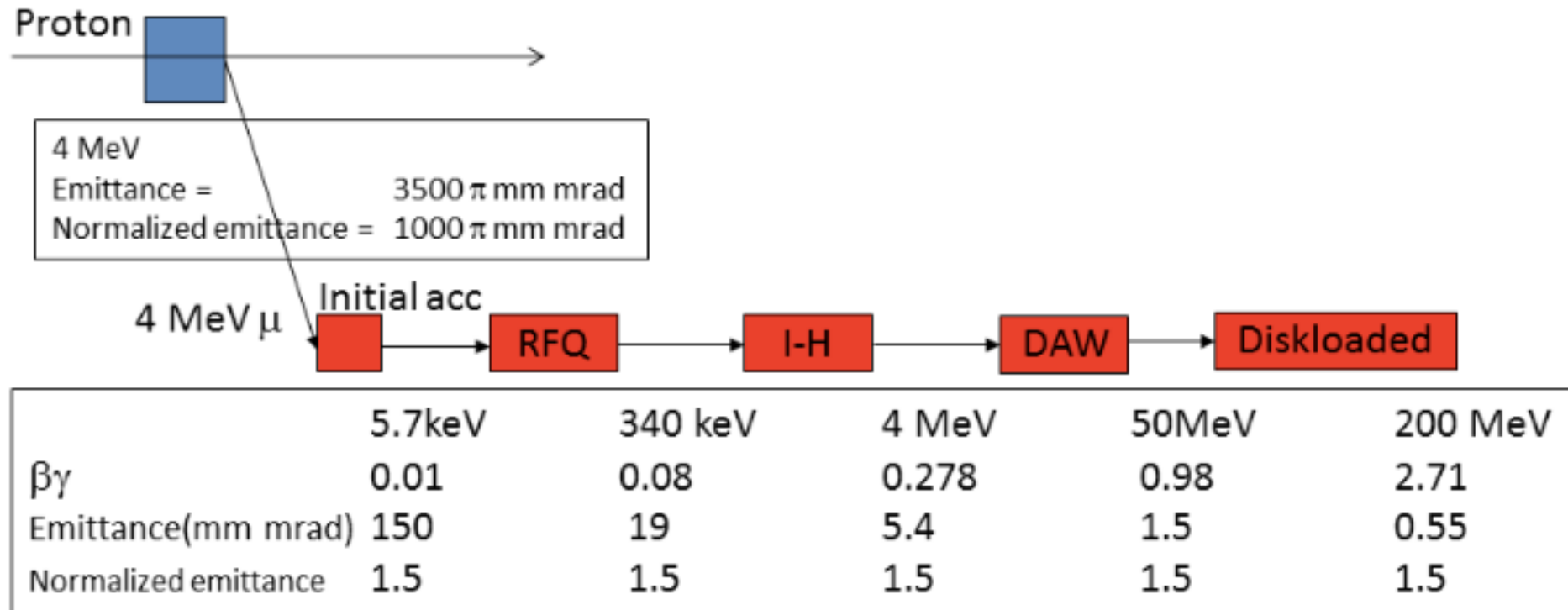
Events of the MCP



**Feb 2016**

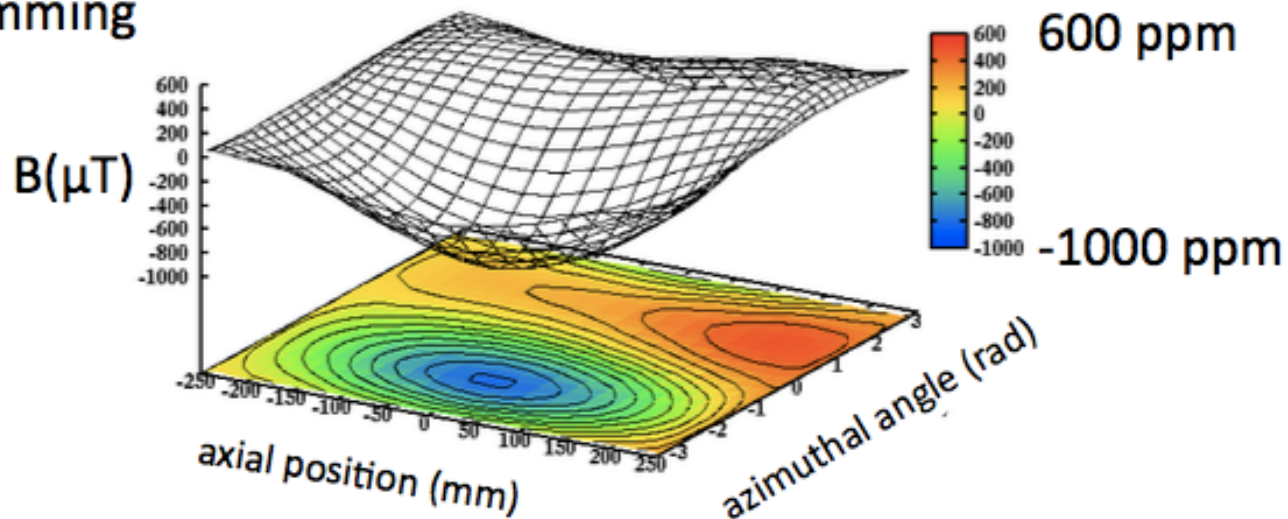


Topview of U-Line

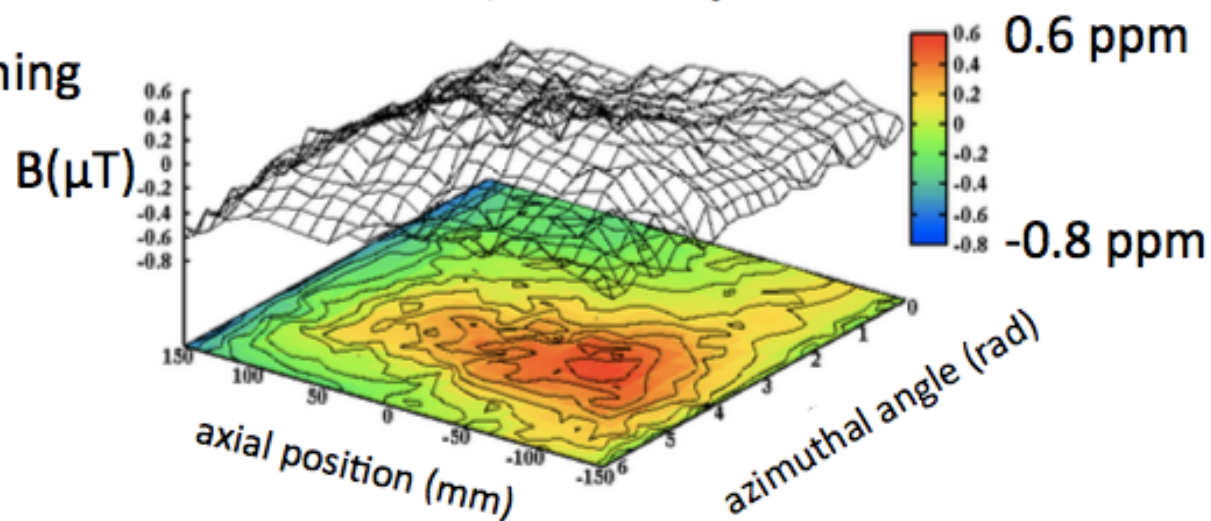


Tests of 1<sup>st</sup> two acceleration stages completed.

Before shimming



After shimming



$r = 140 \text{ mm}$



R&D phase being completed in next year

Funds for most of construction are secured.

Expect data taking to begin after FNAL g-2 i.e. 2020.

Initial sensitivity at 0.37 ppm (stat) reducing to 0.1 ppm (stat)  
i.e. similar to FNAL 0.1 ppm (stat) [0.1 ppm (syst)]

This will provide a crucial measurement with completely different systematic effects compared to the FNAL measurement.

“If you enjoy doing difficult experiments, you can do them, but it is a waste of time and effort because the result is already known” : **Pauli**



"No experiment is so dumb, that it should not be tried" : **Gerlach**





E821 Error	Size [ppm]	Plan for the E989 $g - 2$ Experiment	Goal [ppm]
Absolute field calibrations	0.05	Special 1.45 T calibration magnet with thermal enclosure; additional probes; better electronics	0.035
Trolley probe calibrations	0.09	Absolute cal probes that can calibrate off-central probes; better position accuracy by physical stops and/or optical survey; more frequent calibrations	0.03
Trolley measurements of $B_0$	0.05	Reduced rail irregularities; reduced position uncertainty by factor of 2; stabilized magnet field during measurements; smaller field gradients	0.03
Fixed probe interpolation	0.07	More frequent trolley runs; more fixed probes; better temperature stability of the magnet	0.03
Muon distribution	0.03	Additional probes at larger radii; improved field uniformity; improved muon tracking	0.01
Time-dependent external B fields	–	Direct measurement of external fields; simulations of impact; active feedback	0.005
Others	0.10	Improved trolley power supply; trolley probes extended to larger radii; reduced temperature effects on trolley; measure kicker field transients	0.05
Total	0.17		0.07

E821 Error	Size [ppm]	Plan for the E989 $g - 2$ Experiment	Goal [ppm]
Gain changes	0.12	Better laser calibration; low-energy threshold; temperature stability; segmentation to lower rates; no hadronic flash	0.02
Lost muons	0.09	Running at higher $n$ -value to reduce losses; less scattering due to material at injection; muons reconstructed by calorimeters; tracking simulation	0.02
Pileup	0.08	Low-energy samples recorded; calorimeter segmentation; Cherenkov; improved analysis techniques; straw trackers cross-calibrate pileup efficiency	0.04
CBO	0.07	Higher $n$ -value; straw trackers determine parameters	0.03
E-Field/Pitch	0.06	Straw trackers reconstruct muon distribution; better collimator alignment; tracking simulation; better kick	0.03
Diff. Decay	0.05 <sup>1</sup>	better kicker; tracking simulation; apply correction	0.02
Total	0.20		0.07