

Experimental status and prospects of light pionic atoms

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for the PIONIC HYDROGEN COLLABORATION

HC2NP 2016

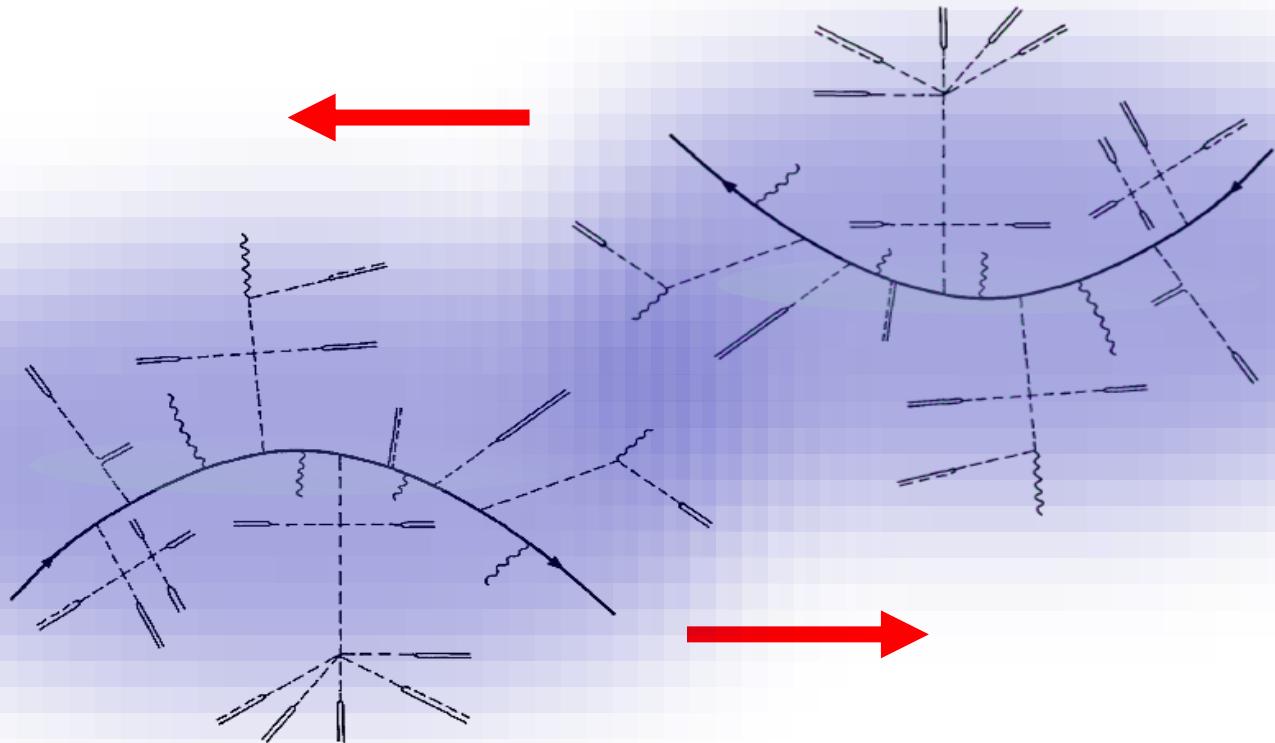
Puerto de la Cruz, September 26, 2016

- **WHY PIONIC HYDROGEN & ... ?**
- **EXPERIMENTAL APPROACH**
- **ANALYSIS**
- **RESULTS**
- **CONCLUSIONS**

PIONS, NUCLEONS - INTERACTION in terms of QCD

$$N \Leftrightarrow N$$

$$\pi N \Leftrightarrow \pi N$$



J. Gasser et al., *Nucleons with chiral loops*, Nucl. Phys. B307, 779 (1988)

Fig. 1. A typical term in the expansion (3.7) of the nucleon propagator. ——— nucleon; - - - pions; ~~~~ vector current; = = = axial vector current; - - - pseudoscalar density; —— scalar density.

CHIRAL PERTURBATION THEORY (χ PT), ...

- **WHY PIONIC HYDROGEN & ... ?**
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- CONCLUSIONS

Strong - interaction effects in X-ray transitions



$$\begin{aligned}\pi H: \varepsilon_{1s} &\propto a_{\pi^- p \rightarrow \pi^- p} + \dots \\ \Gamma_{1s} &\propto (a_{\pi^- p \rightarrow \pi^0 n})^2 + \dots \\ \pi D: \varepsilon_{1s} &\propto a_{\pi^- p \rightarrow \pi^- p} + a_{\pi^- n \rightarrow \pi^- n} + \dots\end{aligned}$$

$$\begin{aligned}\pi D: \Gamma_{1s} &\propto g_1(\pi^- d \rightarrow nn) \\ &\propto \alpha(p p \rightarrow \pi^+ d) \\ &\text{detailed balance \& charge symmetry}\end{aligned}$$

*strong interaction
attractive*



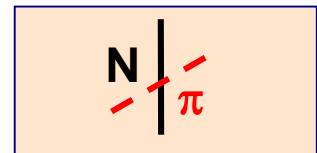
$$\begin{aligned}\Gamma_{1s} &\text{ broadening } \Gamma_{1s} \\ \varepsilon_{1s} &\text{ shift } \varepsilon_{1s}\end{aligned}$$

*strong interaction
repulsive*

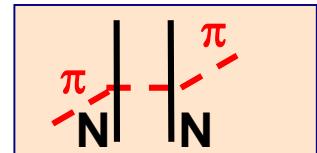
$$\varepsilon, \Gamma = \text{few eV}$$

πH & πD - origin of ε_{1s}

πH elastic scattering $\pi^- p \rightarrow \pi^- p \dots$



πD coherent sum $\pi^- p \rightarrow \pi^- p + \pi^- n \dots$



πH & πD - origin of Γ_{1s}

πH scattering $\pi^- p \rightarrow \pi^0 n + n\gamma$

CEX = charge exchange

CEX scattering



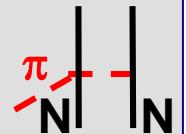
radiative capture



BR well known from experiment

πD absorption $\pi^- d \rightarrow nn + n\gamma\gamma$

„true“ absorption



PION-NUCLEON SCATTERING LENGTHS

$$\pi \otimes N \text{ isospin} \quad 1 \otimes 1/2 = 1/2 \oplus 3/2$$

$$a^\pm \equiv \frac{1}{2}(a_{\pi^- p} \pm a_{\pi^+ p})$$

$$a_{\pi^- p} = \frac{1}{3}(2a_{1/2} + a_{3/2}) = a^+ + a^-$$

$$a_{\pi^- p \rightarrow \pi^0 n} = -\frac{\sqrt{2}}{3}(a_{1/2} - a_{3/2}) = -\sqrt{2} a^-$$

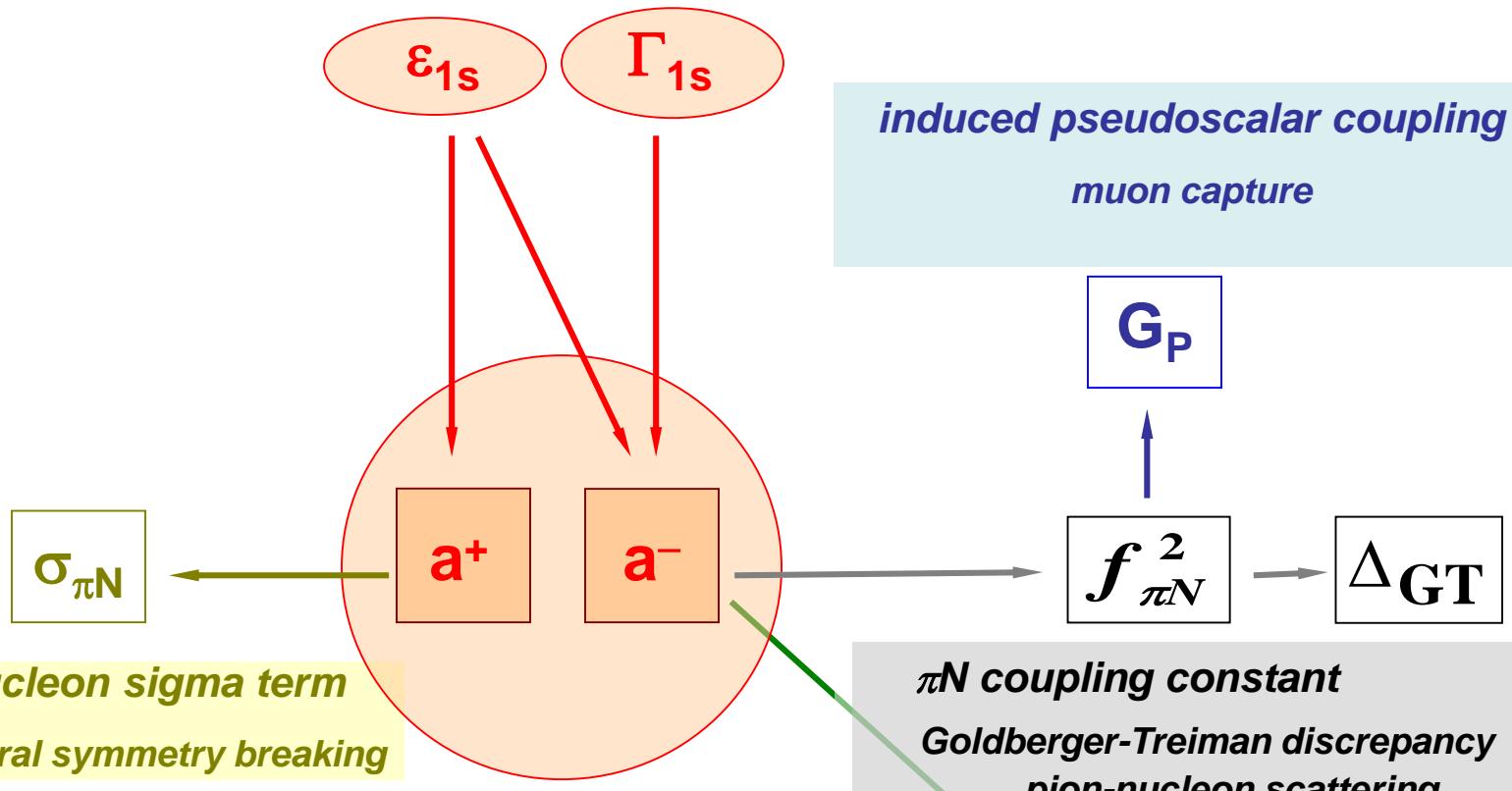
$$a_{\pi^+ p} = a_{\pi^- n} = a_{3/2} = a^+ - a^-$$

$$\begin{aligned} \chi \text{PT} \quad a^+ &\rightarrow a^+ + \Delta a^+ \\ a^- &\rightarrow a^- + \Delta a^- \end{aligned}$$

review theory: J. Gasser, V.E. Lyubovitskij, A. Rusetsky, Phys. Rep. 456, 167 (2008)

PION-NUCLEON SCATTERING LENGTHS

related quantities

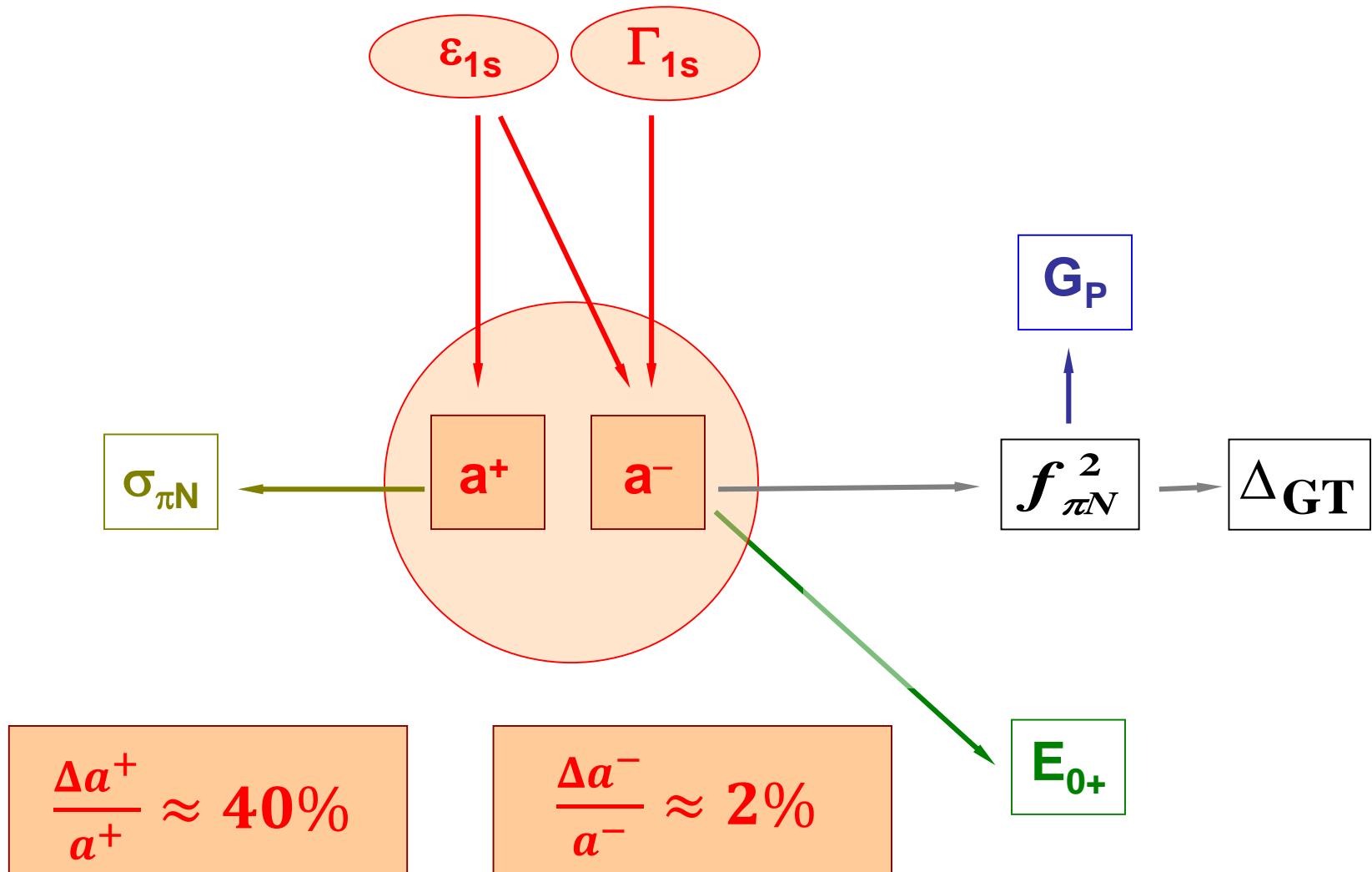


THEORETICAL FRAME WORK
CHIRAL PERTURBATION THEORY

electric dipole amplitude
threshold pion photo production

PION-NUCLEON SCATTERING LENGTHS

present accuracy



WHICH SCATTERING LENGTH ?

$$\epsilon_{1s} = -2\alpha^3 \mu_c^2 \mathcal{A} (1 - 2\alpha \mu_c (\ln \alpha - 1) \mathcal{A}) + \dots$$

analogue Trueman expansion, 1961

analogue for Γ_{1s}

$$\begin{aligned}
 \mathcal{A} &= a_{0+}^+ + a_{0+}^- + \epsilon \quad \text{purely hadronic } \pi^- p \text{ scattering length} \\
 &= \frac{1}{8\pi(m_p + M_{\pi^+})F_\pi^2} \\
 &\times \left\{ m_p M_{\pi^+} - \frac{g_A^2 m_p M_{\pi^+}^2}{m_n + m_p + M_{\pi^+}} \right. \\
 &+ m_p (-8c_1 M_{\pi^0}^2 + 4(c_2 + c_3)M_{\pi^+}^2 \\
 &\quad \left. - 4e^2 [f_1] - e^2 [f_2] \right\} \quad + \quad O(\delta^3) \dots
 \end{aligned}$$

LECs f_1, f_2, c_1 contribute to isospin breaking in $O(\delta^2)$

review: J. Gasser, V.E. Lyubovitskij, A. Rusetsky, Phys. Rep. 456 (2008) 167

RELATIONS simplified

scattering lengths

LO: current algebra

Weinberg,Tomozawa:
chiral limit $m_{\text{quark}} \rightarrow 0$

Goldberger-Treiman relation

πN coupling constant $f_{\pi N}^2$

$$\begin{aligned} \mathbf{a}^+ &= 0 \\ \mathbf{a}^- &= -0.079 / m_\pi \\ \mathbf{f}_{\pi N}^2 &= \frac{m_\pi^2}{4} \frac{\mathbf{g}_A^2}{\mathbf{F}_\pi^2} = 0.072 \end{aligned} \quad \left. \right\} + \text{higher orders } \chi\text{PT}$$

Sigma term

explicit chiral symmetry breaking

$$\sigma_{\pi N} = \frac{\mathbf{m}_u + \mathbf{m}_d}{4M} \langle \mathbf{p} | \bar{u}u + \bar{d}d | \mathbf{p} \rangle \leftrightarrow \langle \mathbf{p} | \bar{s}s | \mathbf{p} \rangle \text{ contents}$$

πN sigma-term σ_N

$$(1 + \frac{m_\pi}{M}) \boxed{a^+} = \frac{m_\pi^2}{4\pi f_\pi^2} \cdot \left(\frac{\sigma_{\pi N}}{m_\pi^2} + d - \frac{g_A^2}{4M_N} \right)$$

πN coupling constant $f_{\pi N}$

$$(1 + \frac{m_\pi}{M}) \boxed{a^-} = \frac{2f_{\pi N}^2}{m_\pi^2 - (m_\pi^2/2M)^2} + \frac{1}{2\pi^2} \int_0^\infty \frac{\sigma_{\pi^- p}^{tot}(k_\pi) - \sigma_{\pi^+ p}^{tot}(k_\pi)}{2\omega(k_\pi)} dk_\pi$$

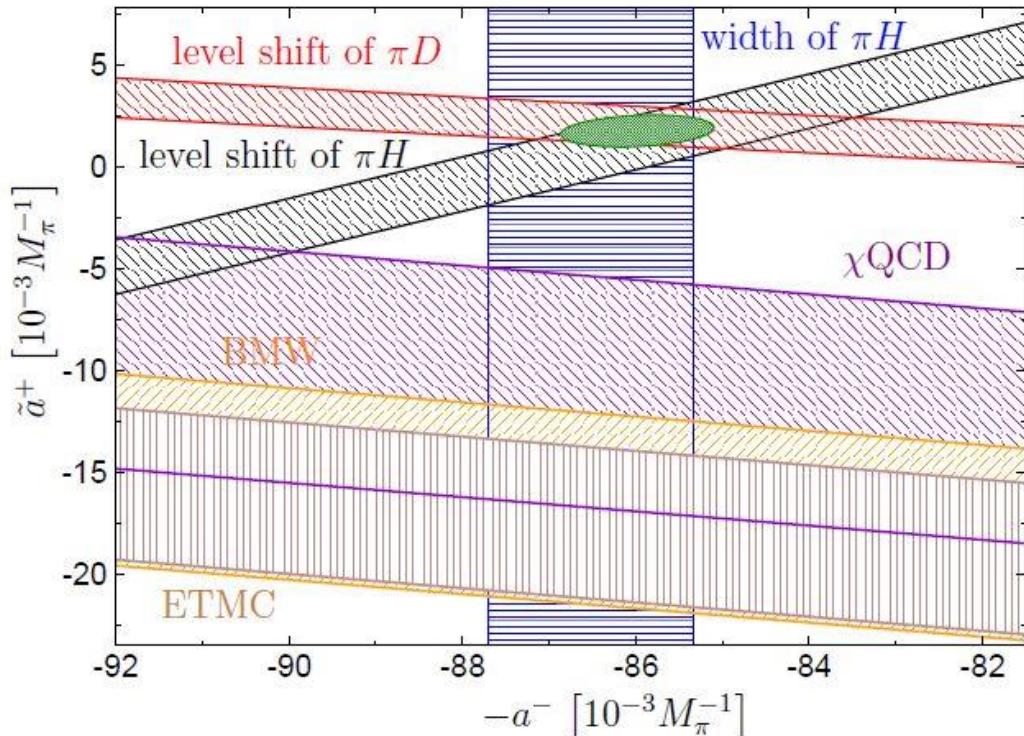
Goldberger- Miyazawa-Oehme

(GMO)

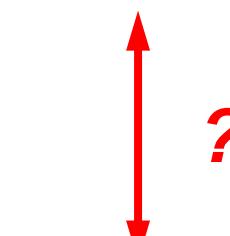
sum rule

$$\Delta f_{\pi N} \approx 1\%$$

$\sigma_{\pi N} \Leftrightarrow$ WIMP – nucleon scattering



← pionic atoms analysis

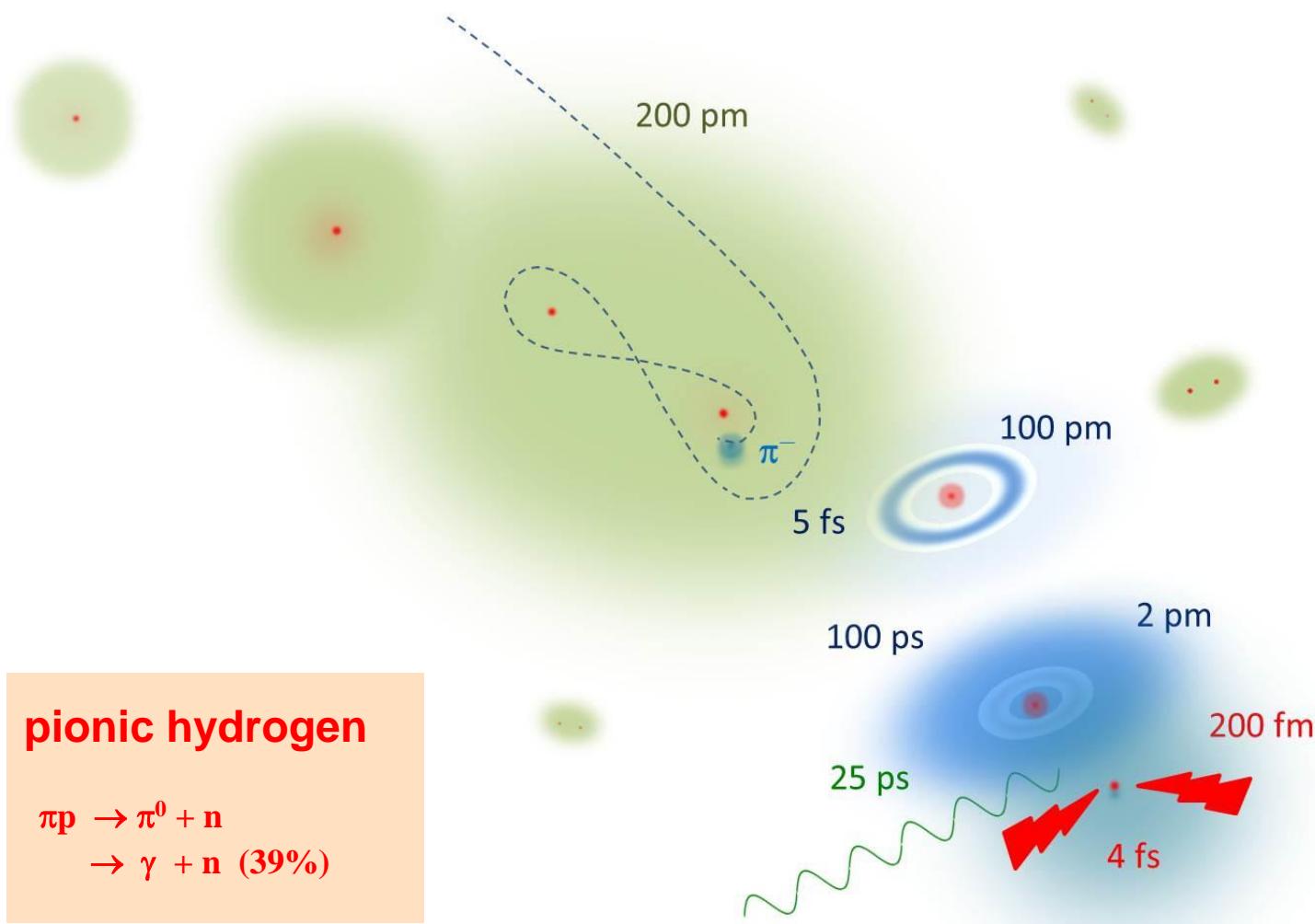


← lattice

Figure 1: Constraints on the πN scattering lengths from pionic atoms (black: level shift in πH , blue: width of πH ground state, red: level shift in πD) and from lattice σ -terms (orange: BMW [20], violet: χ QCD [21], brown: ETMC [22]).

Hoferichter et al., arXiv: 1602.07688v2
 Crivellin et al., Phys. Rev. D 89, 054021 (2014)
 Ellis et al., Phys. Rev D, 065026 (2008)
 ...

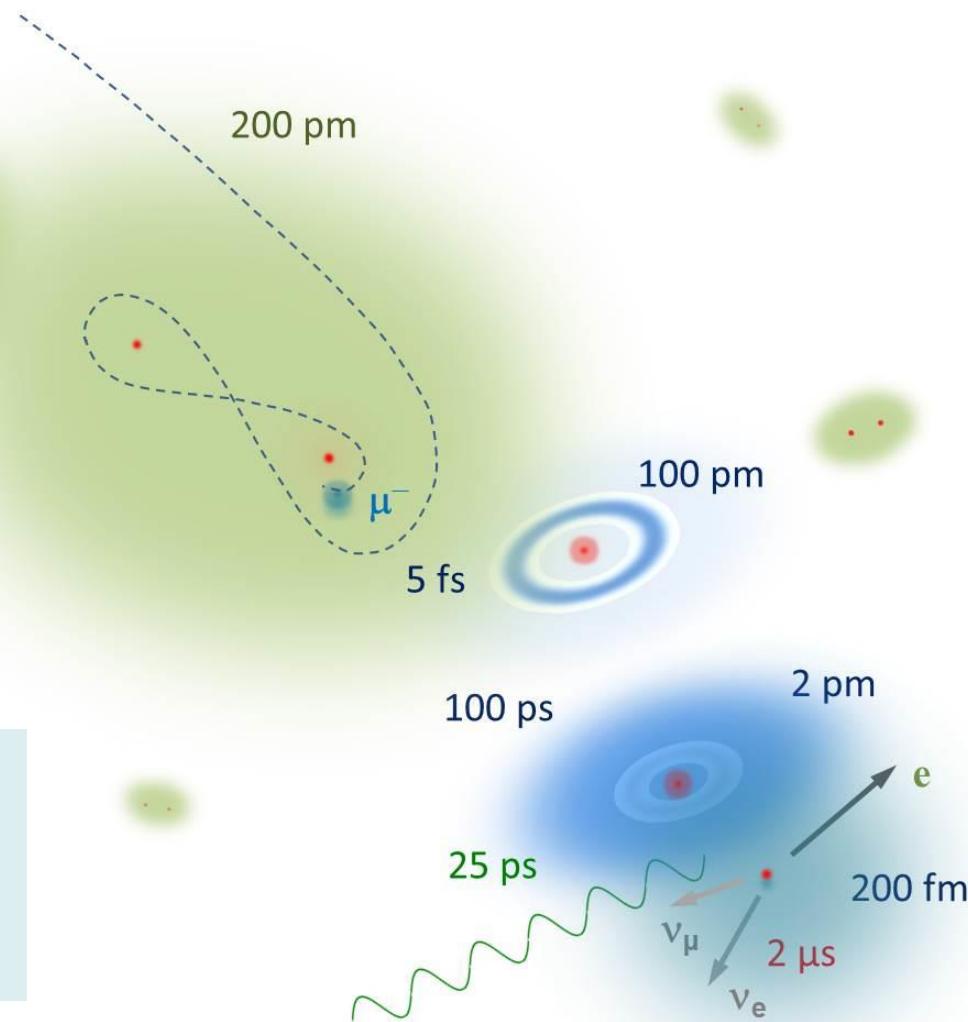
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muonic hydrogen

$\mu p \rightarrow e \bar{\nu} + p$

$\mu p \rightarrow \nu + n$ (0.1%)



DE-EXCITATION CASCADE and COLLISIONAL EFFECTS

target density > 0

πH or μH are NOT ISOLATED SYSTEMS !

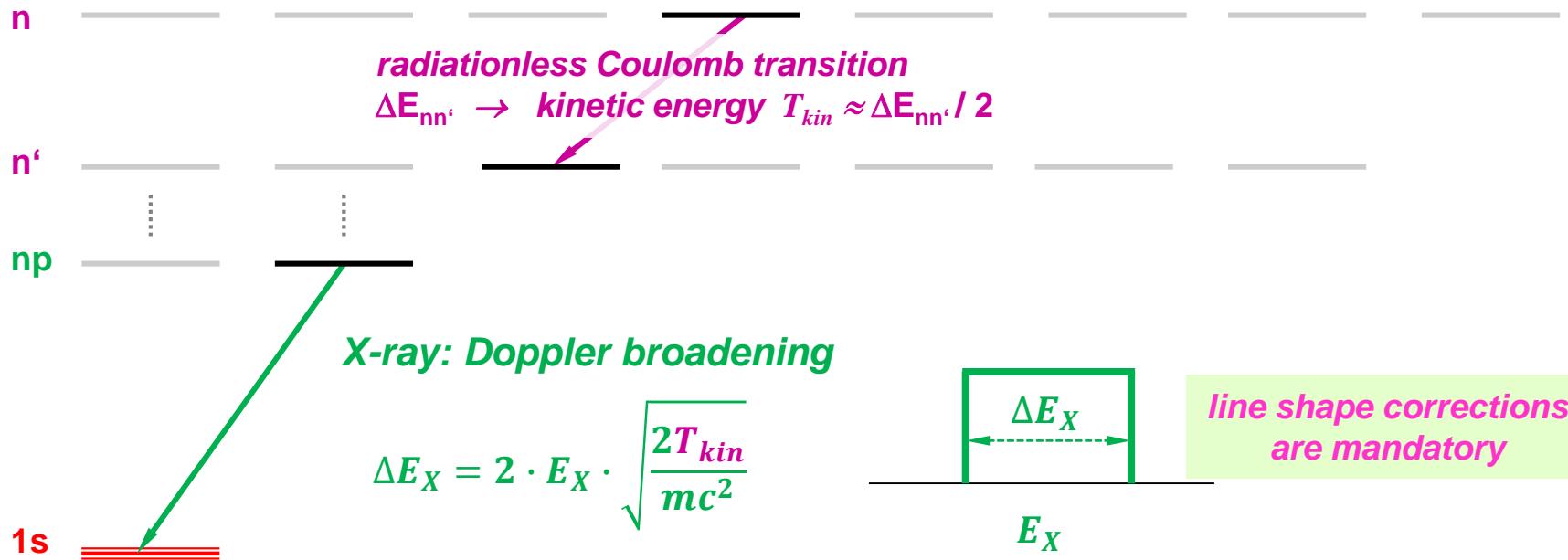
density dependent effects on line energy and/or width ?

COULOMB DE-EXCITATION

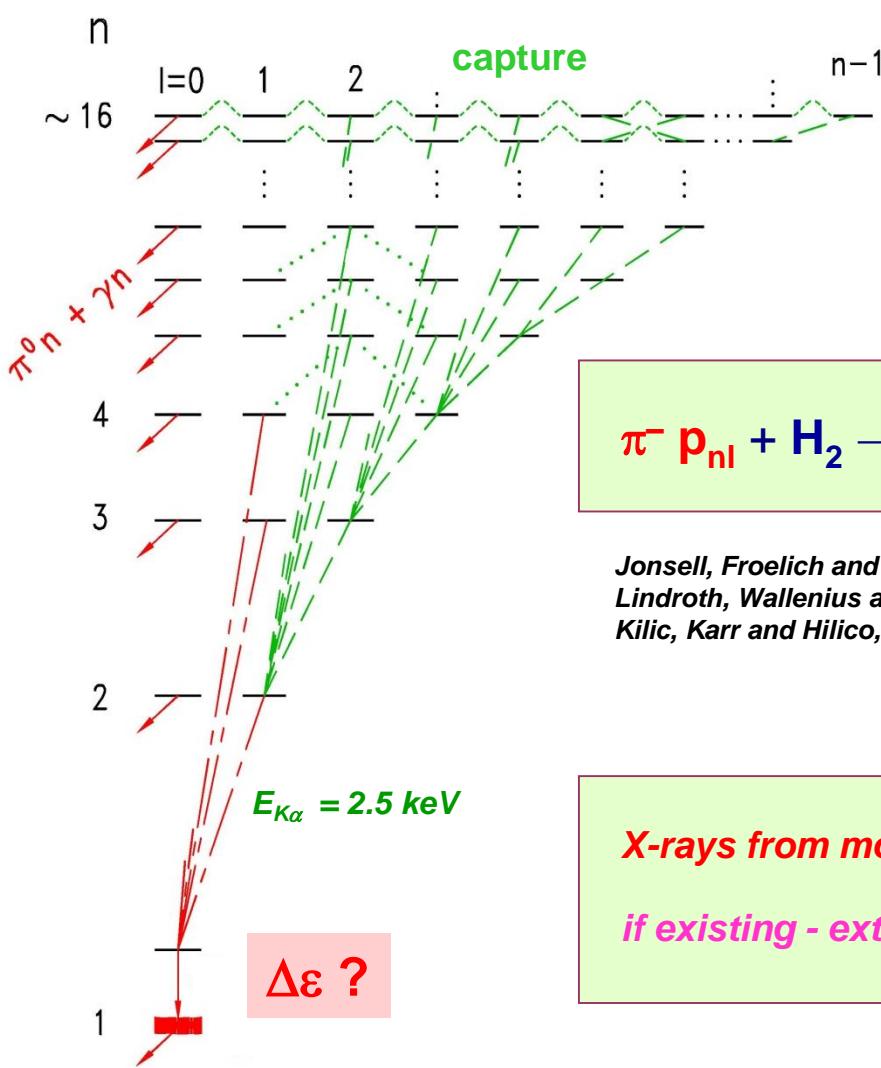
first observed from NEUTRON - TOF

J.B. Czirr et al., Phys. Rev. 130, 341 (1963)

A. Badertscher et al., Eur. Phys. Lett. 54 (2001) 313 (status)

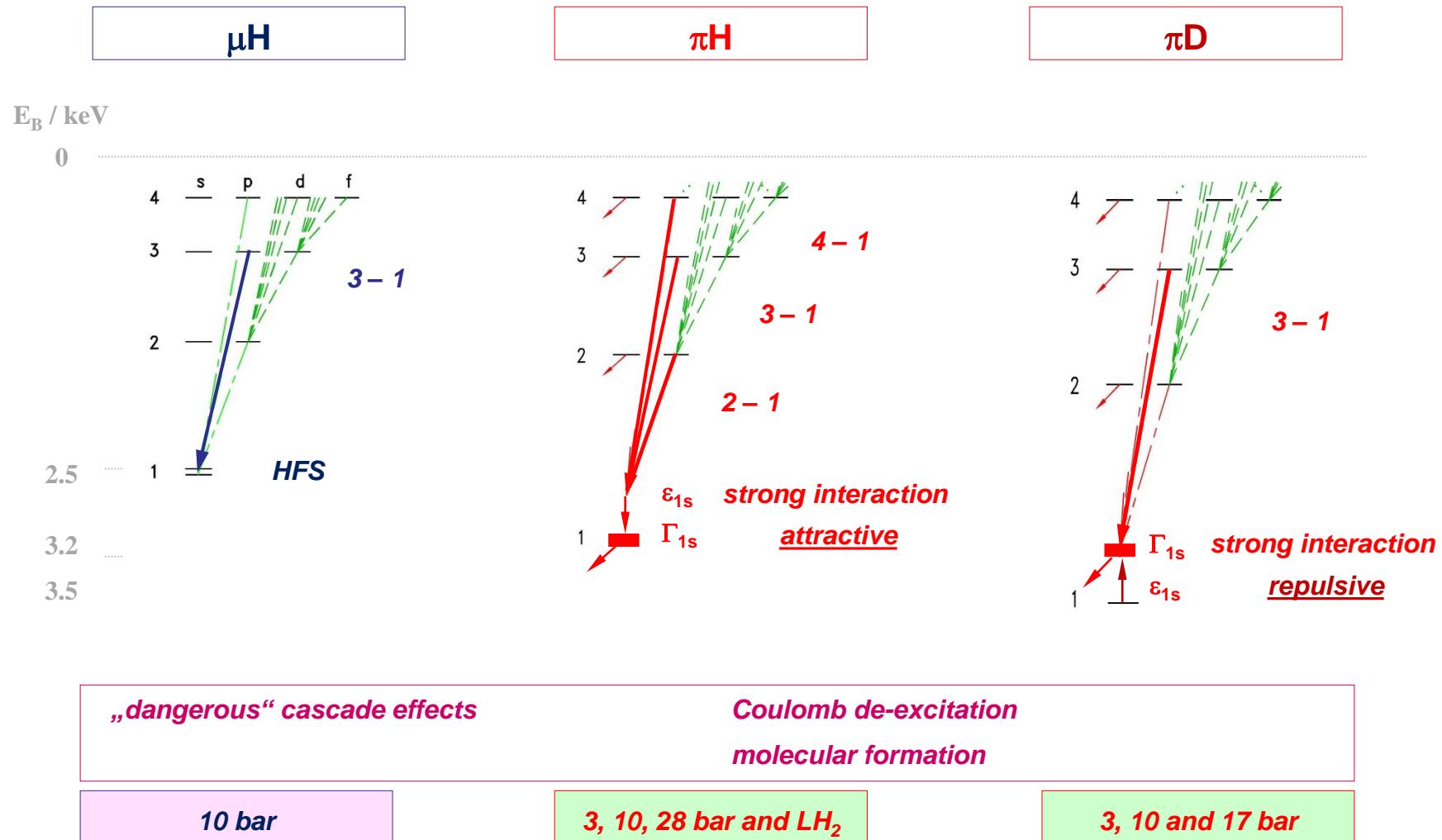


MOLECULAR FORMATION



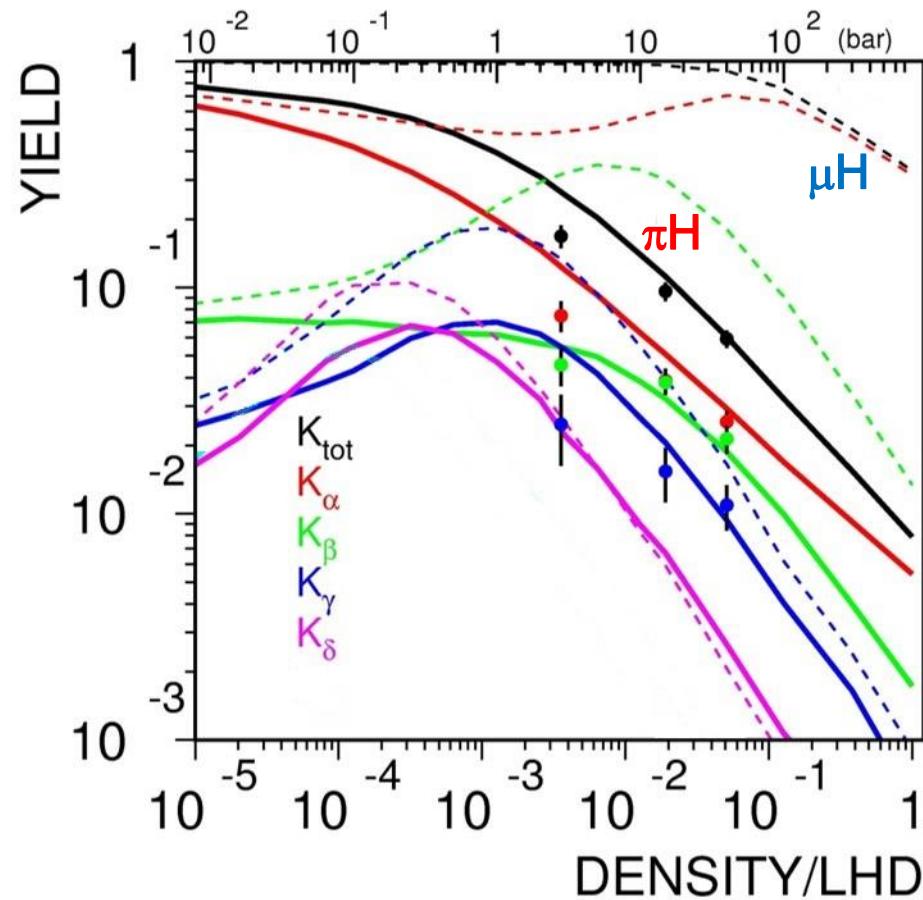
- known to exist from muon-catalysed fusion
- μH experiment quenching of μp_{2s} via $[(\mu pp)p]ee$ formation
R. Pohl et al., Phys. Rev. Lett. 97 (2006) 193402

STRATEGY – VARY TRANSITION + VARY DENSITY



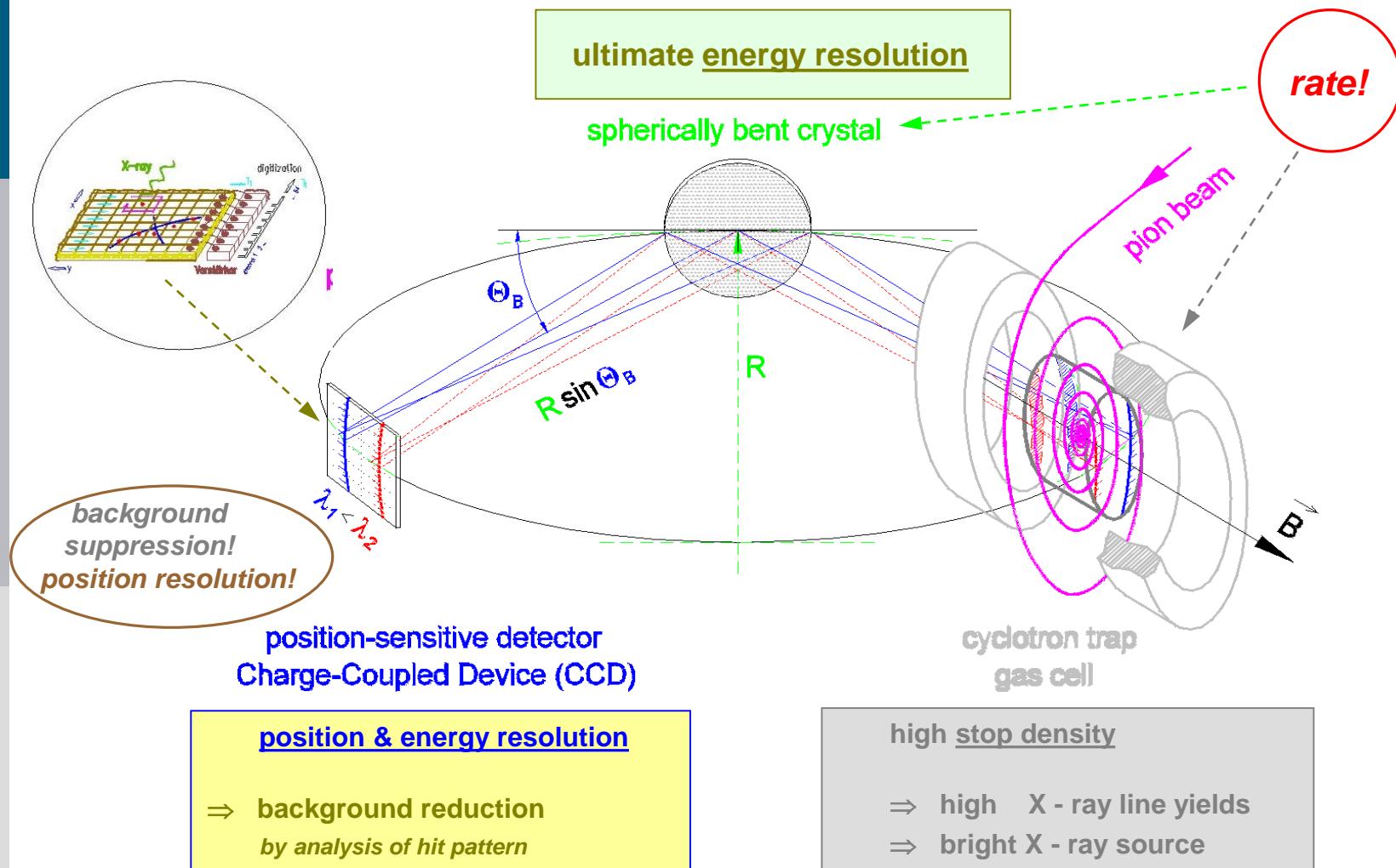
X-RAY YIELDS

πH
 μH
Lyman series



cascade calculation: V. E. Markushin, PSI

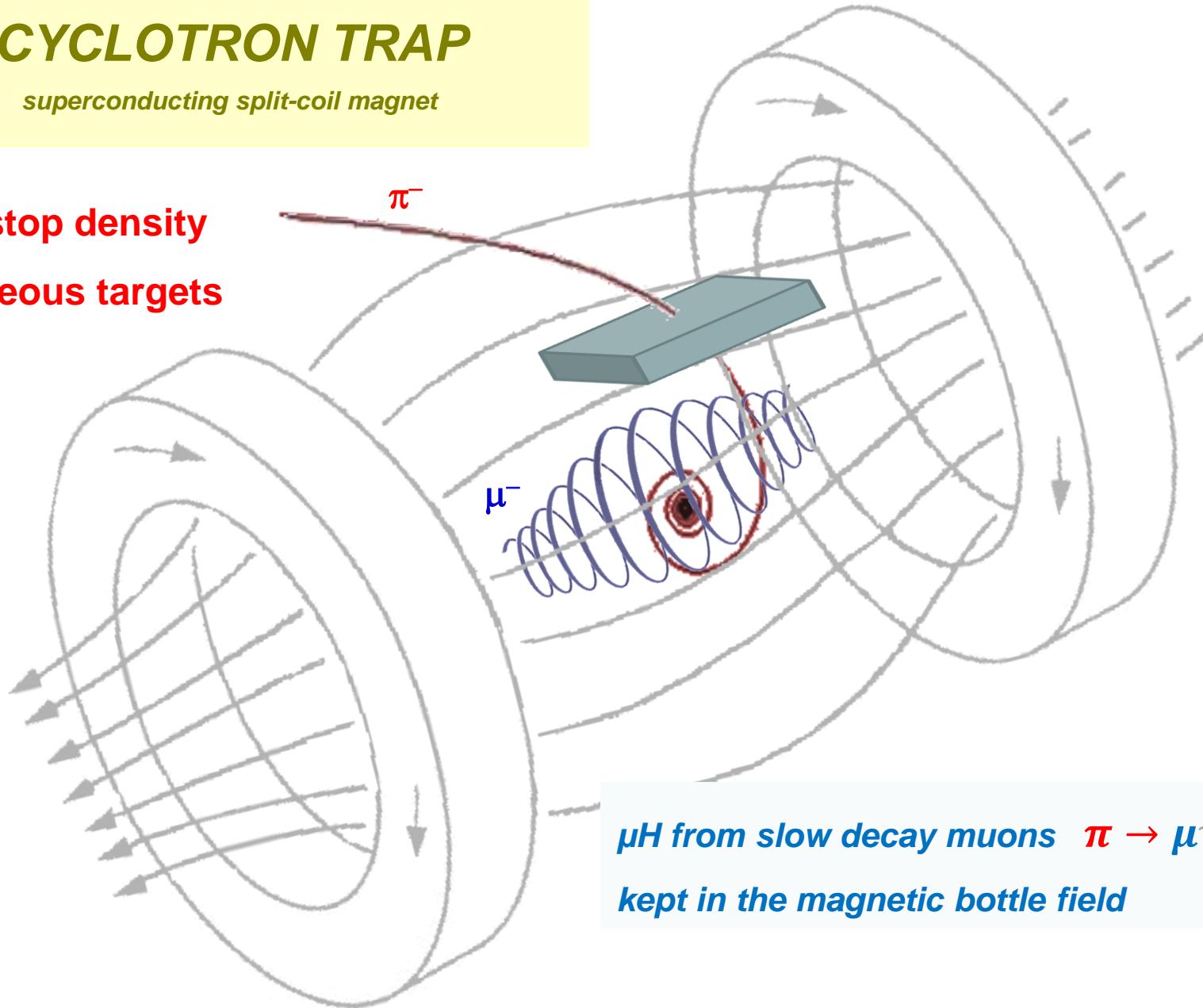
Johann-type SET-UP



CYCLOTRON TRAP

superconducting split-coil magnet

high stop density
in gaseous targets

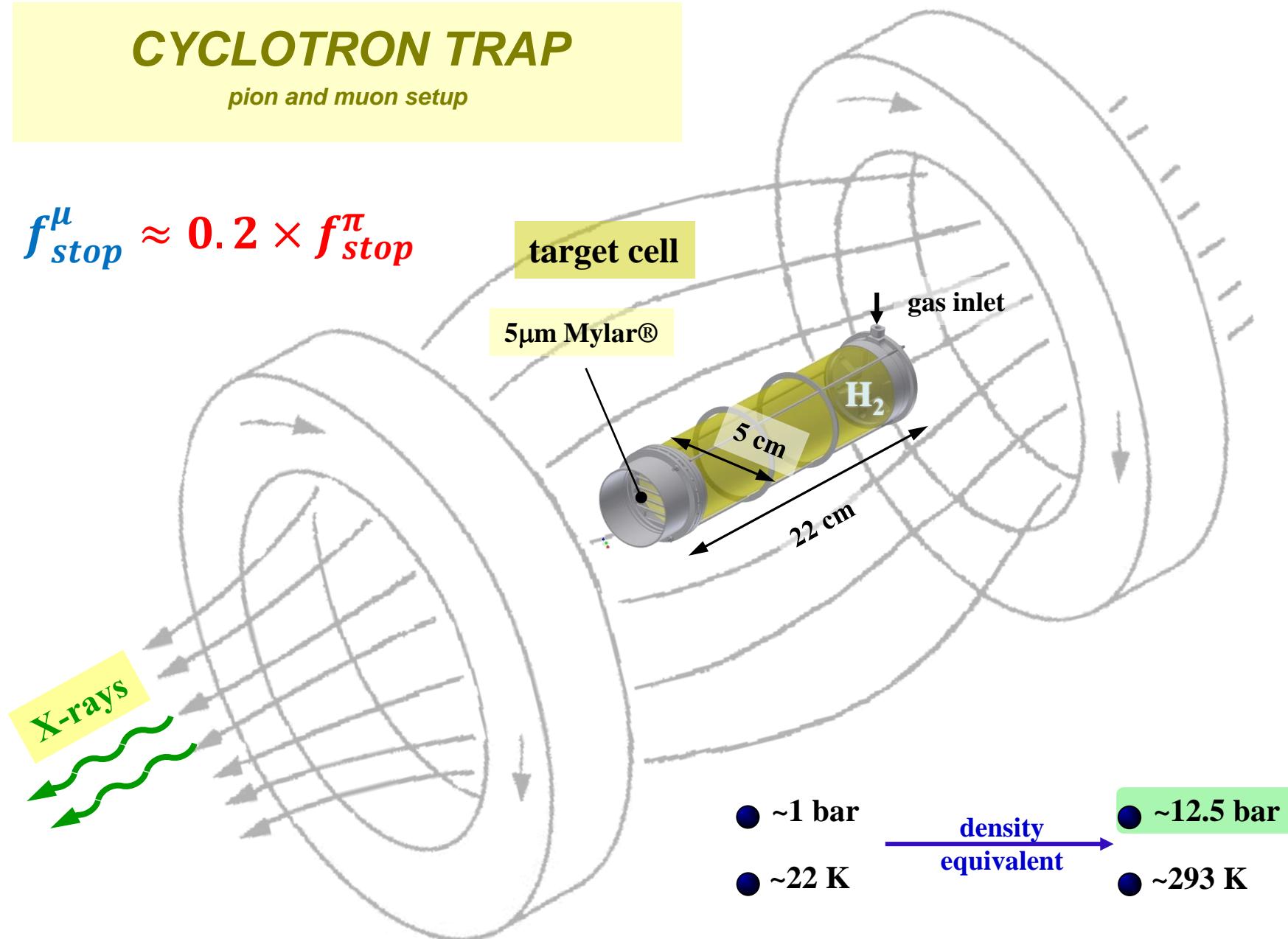


μH from slow decay muons $\pi \rightarrow \mu\nu$
kept in the magnetic bottle field

CYCLOTRON TRAP

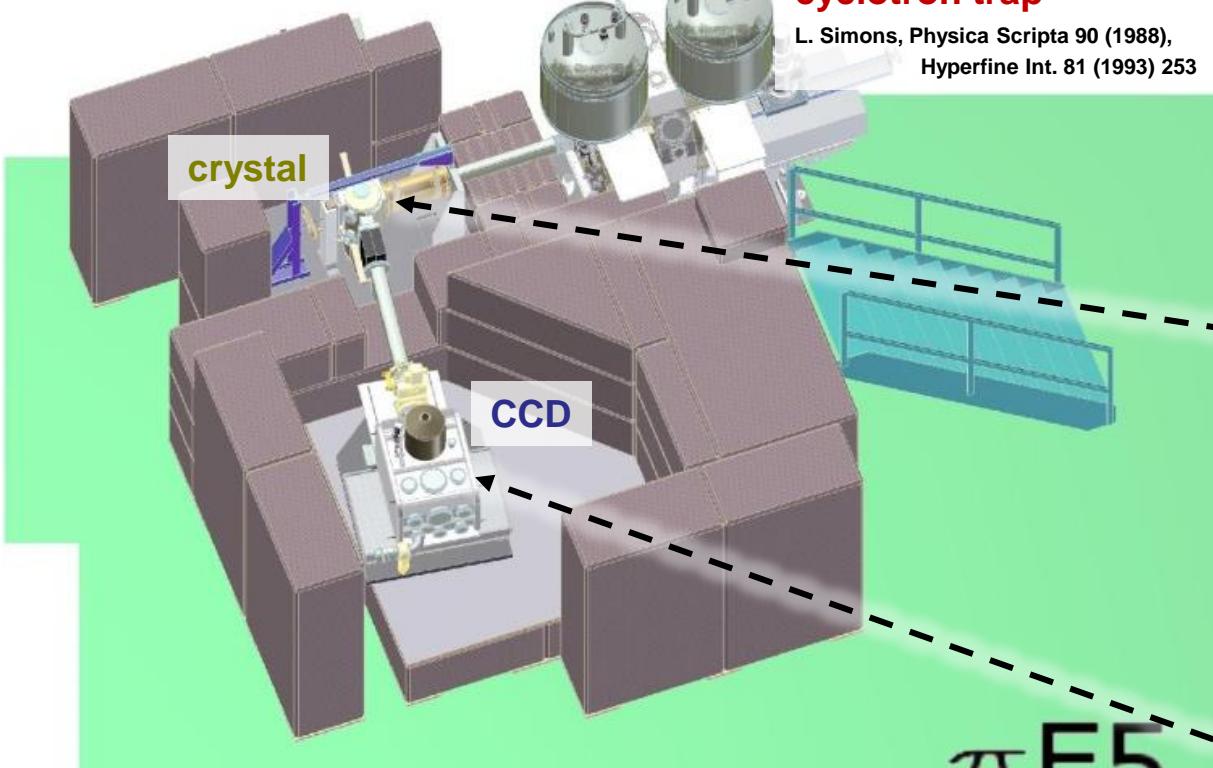
pion and muon setup

$$f_{stop}^{\mu} \approx 0.2 \times f_{stop}^{\pi}$$



TYPICAL SET-UP at PSI

pion stops in gas: few % of 10^8 /s
 ≈ 5 neutrons / π^-

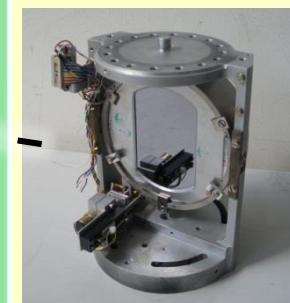


crystal spectrometer setup

$\pi H(4-1)$ and $\pi D(3-1)$ $\Theta_{Bragg} \approx 40^\circ$

PSI experiments R-98.01 and R-06.03

BRAGG CRYSTAL Si, quartz

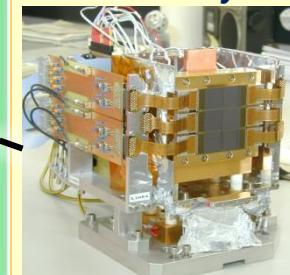


spherically
bent

$R = 3\text{ m}$
 $\Phi = 10\text{ cm}$

FOCAL PLANE DETECTOR

3x2 CCD array

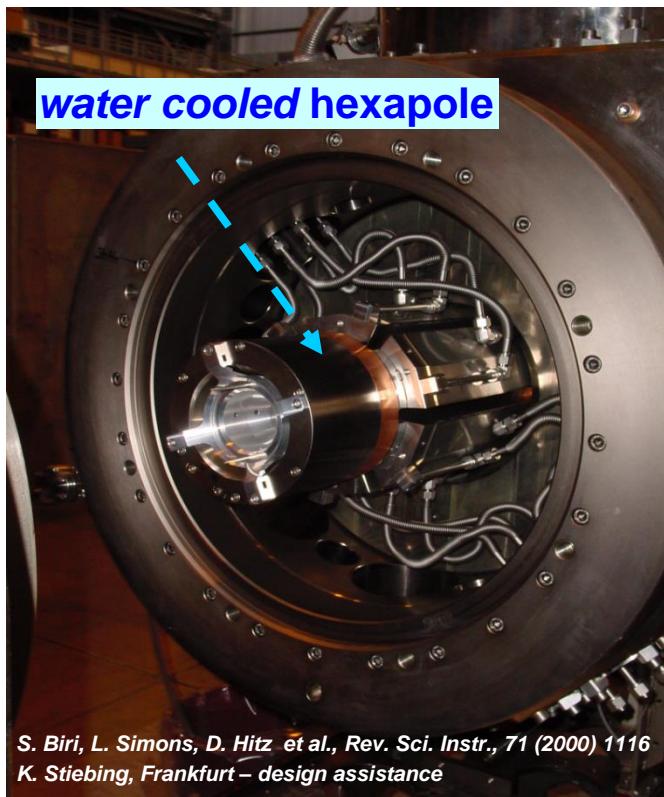
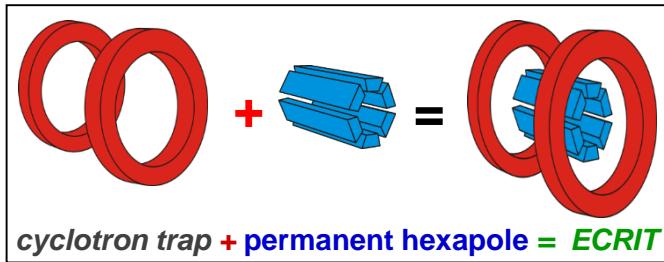


pixel size
 $40\text{ }\mu\text{m} \times 40\text{ }\mu\text{m}$

N. Nelms et al. Nucl. Instr. Meth. A484 (2002) 419

SPECTROMETER RESPONSE

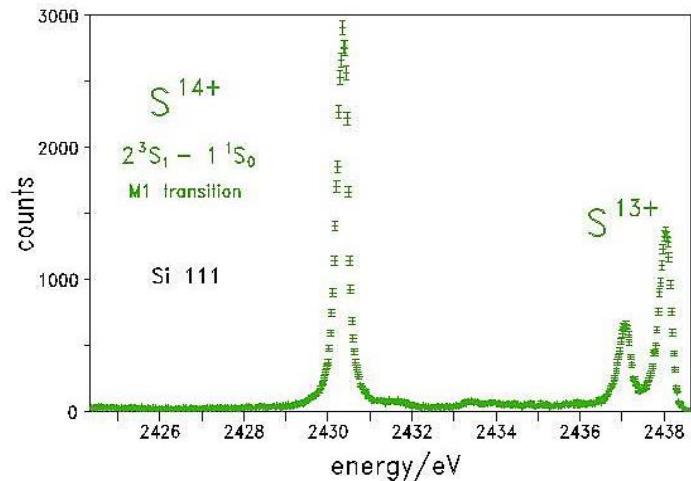
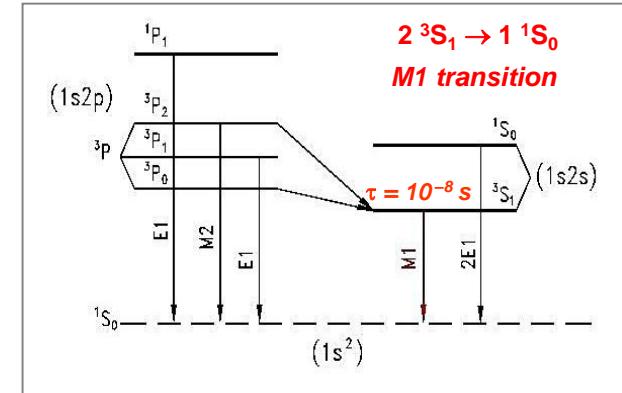
*new approach
Electron Cyclotron Resonance Ion Trap*



He - like

- S** $\leftrightarrow \pi\text{H}(2\text{p}-1\text{s})$
- Cl** $\leftrightarrow \pi\text{H}(3\text{p}-1\text{s})$
- Ar** $\leftrightarrow \pi\text{H}(4\text{p}-1\text{s})$

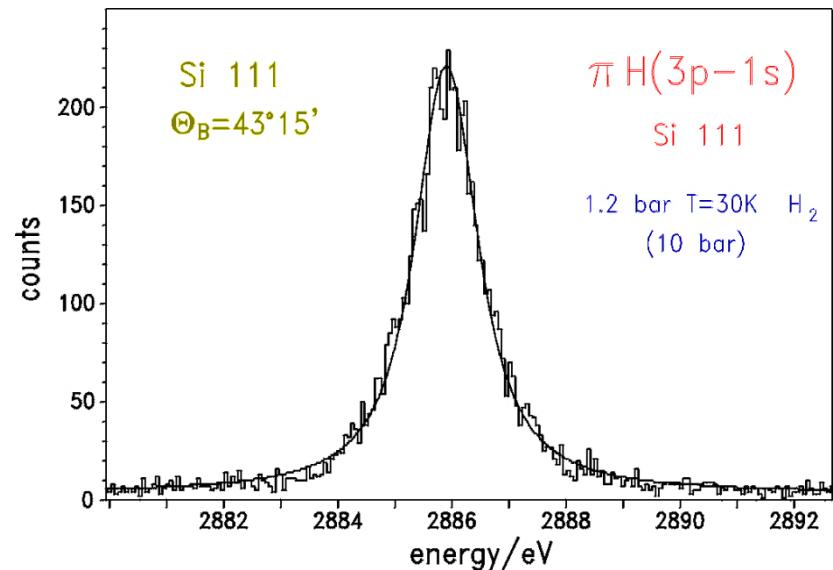
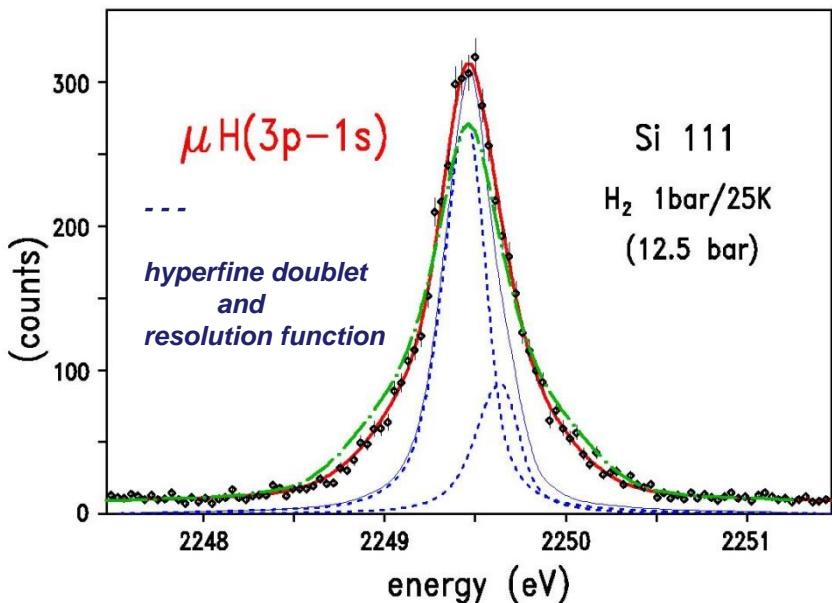
**30000 events
in M1 line (3 h)**



D.F.Anagnostopoulos et al., Nucl. Instr. Meth. B 205 (2003) 9
D.F.Anagnostopoulos et al., Nucl. Instr. Meth. A 545 (2005) 217

- WHY PIONIC HYDROGEN & ... ?
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TYPICAL SPECTRA - parameter space



position

intensity

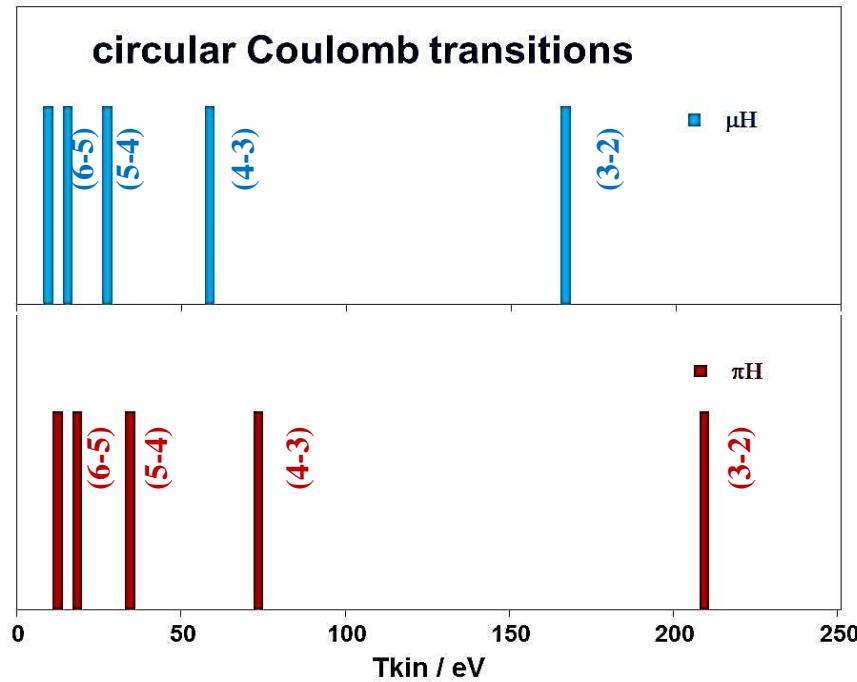
*background
(response)*

T/S ratio
(HFS)

Γ_{hadronic}

kinetic energy distribution

STRATEGY I - *model independent approach*



$$\Delta E_{X,max} = 1,5 \text{ eV} \quad \mu H(3p - 1s)$$

$$\Delta E_{X,max} = 3,0 \text{ eV} \quad \pi H(2p - 1s)$$

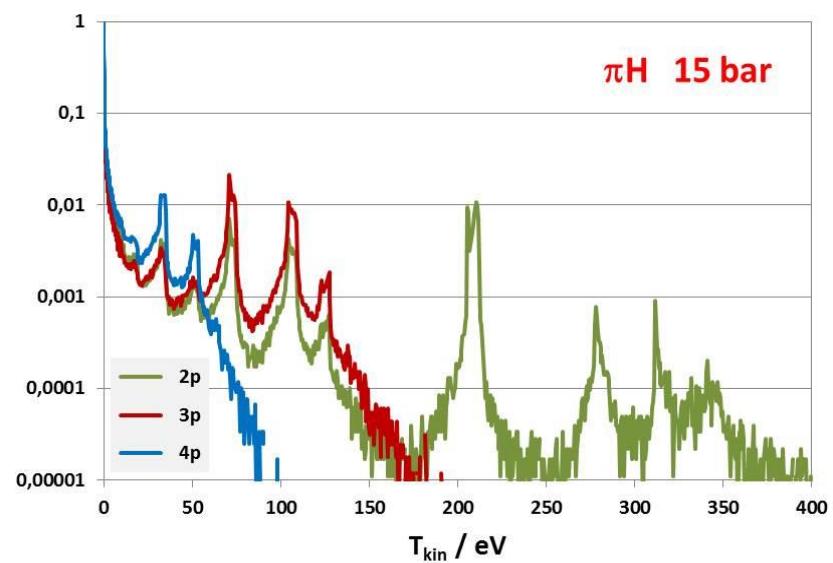
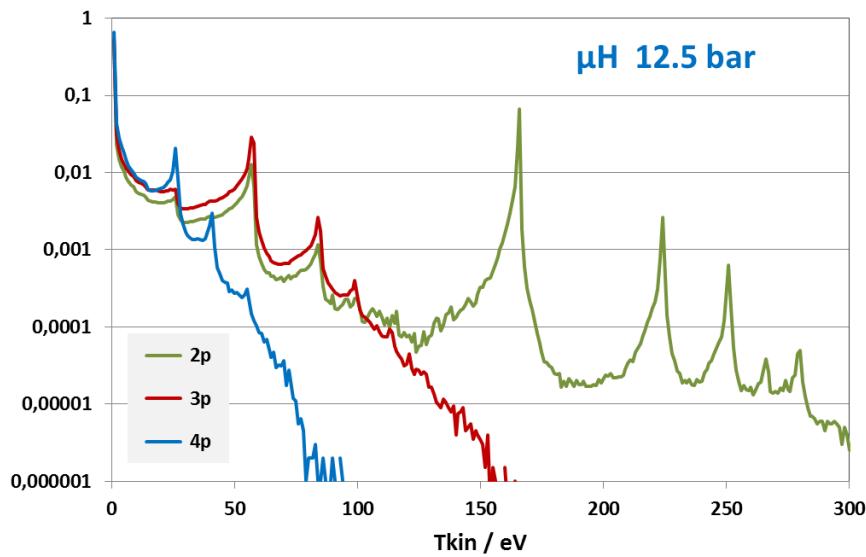
$$\Delta E_{X,max} = 2,1 \text{ eV} \quad \pi H(3p - 1s)$$

$$\Delta E_{X,max} = 1,5 \text{ eV} \quad \pi H(3p - 1s)$$

neglected here: possible $\Delta n=2$ Coulomb transitions

STRATEGY II - *input from cascade theory*

ESCM (extended standard cascade model) model follows development of kinetic energy



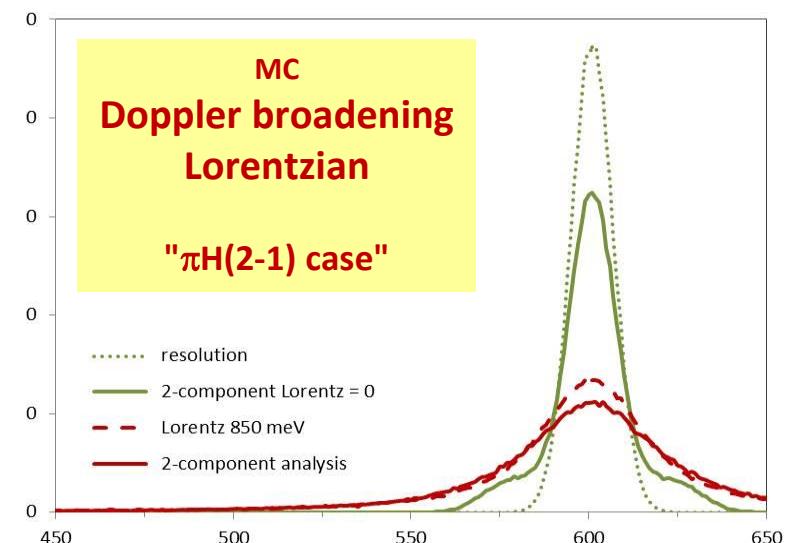
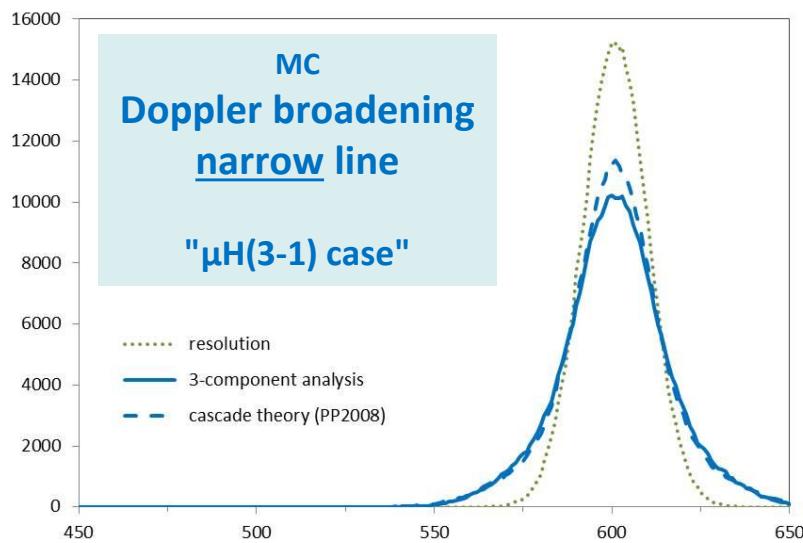
T.Jensen and V.Markushin

introduction of ESCM

V.N. Pomerantsev and V.P. Popov

new collision cross sections

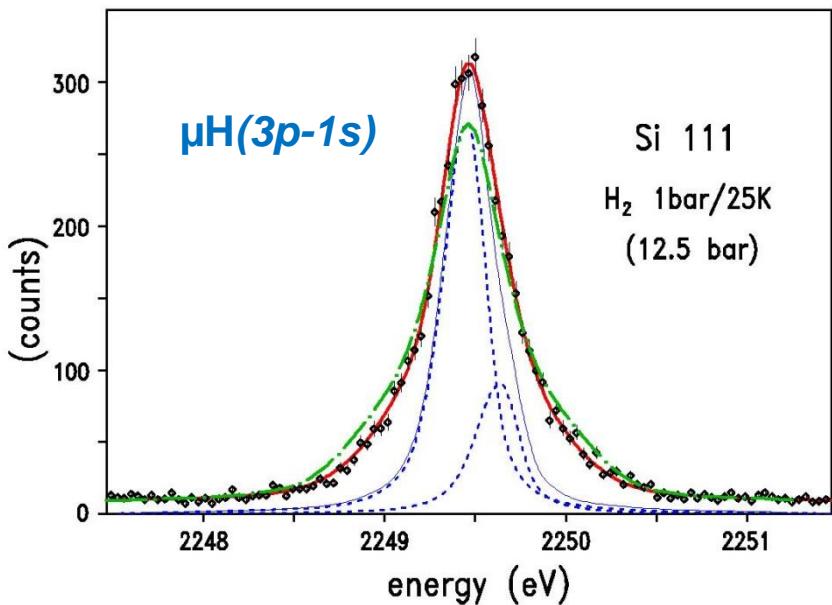
EXEMPLIFICATION



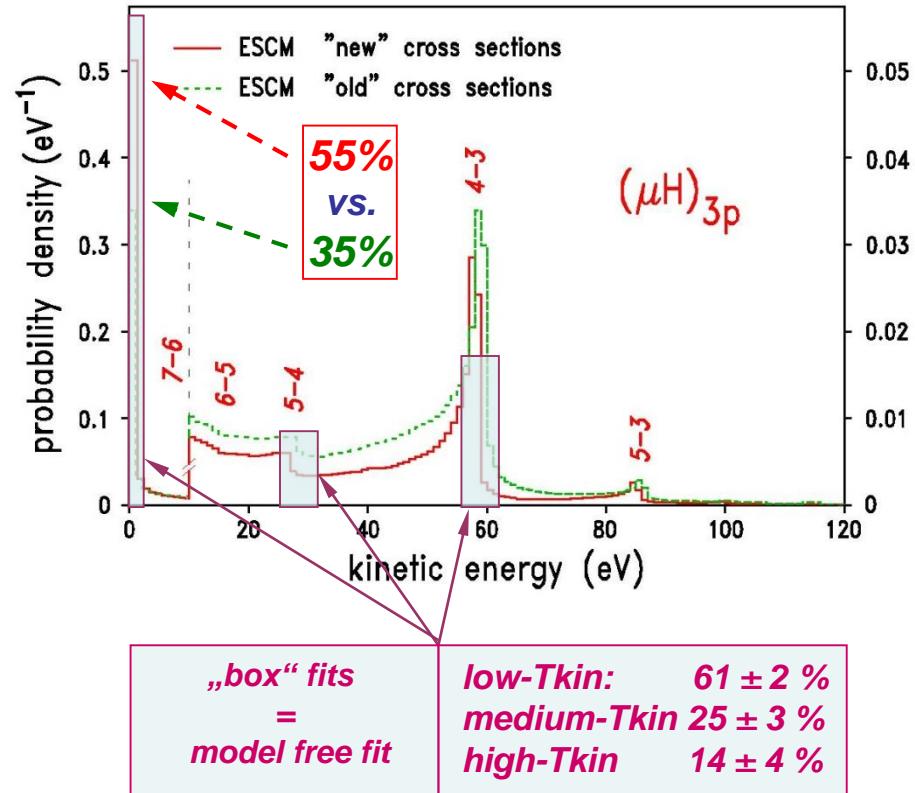
typical resolution (FWHM)
272 meV

390 meV

ANALYSIS - $\mu\text{H}(3p - 1s)$ I



re-calculation of cross sections



ESCM:

extended standard cascade calculation and cross sections

T.S.Jensen and V.E.Markushin, Eur. Phys. J. D 19, 165 (2002); *ibid.D* 21,261 (2002); *ibid.D* 21,271 (2002)

new cross sections

G.Ya. Koreman, V.N. Pomerantsev and V.P. Popov, JETP. Lett. 81, 543 (2005)

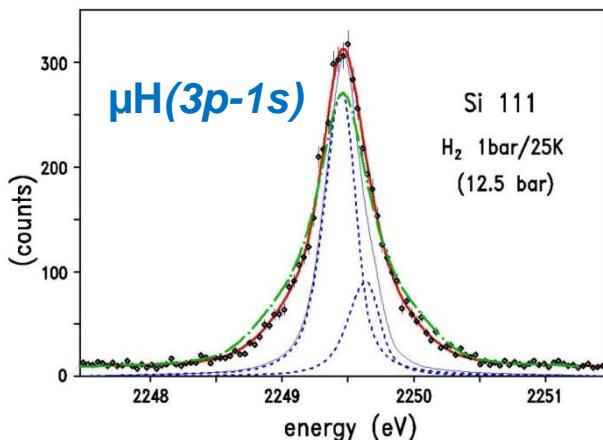
V.N. Pomerantsev and V.P. Popov, Phys. Rev A 73, 040501 (2006)

V.P. Popov and V.N. Pomerantsev, arXiv:0712.3111v1[nucl-th] (2007)

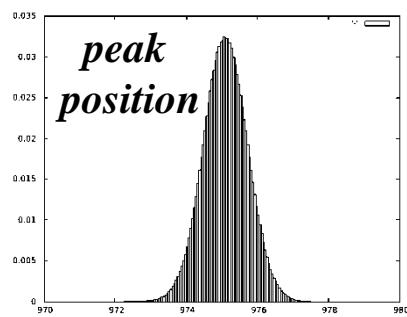
V.P. Popov and V.N. Pomerantsev, Phys. Rev A 86, 052520 (2012)

ANALYSIS - $\mu\text{H}(3p - 1s)$ //

comparison: 3-component model



„obvious“ parameters
look like Gaussian



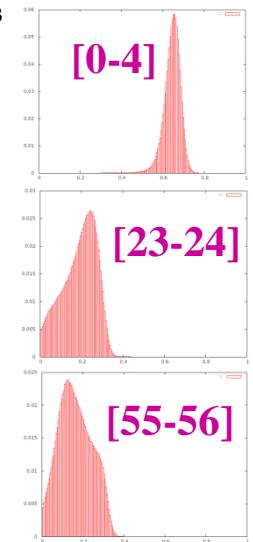
χ^2 analysis

[0-2]	61 ± 2
[24-27]	25 ± 3
[57-58]	14 ± 4

Bayesian approach

M.Theisen, Diploma thesis FZJ 2013

[0-4]	65^{+3}_{-4}
[23-24]	24^{+4}_{-10}
[55-56]	16^{+10}_{-4}



HFS free 211 ± 19

T/S 3.6 ± 0.6

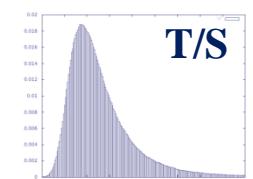
HFS fixed

T/S 2.9 ± 0.2

212^{+23}_{-21}

$3.2^{+1.6}_{-0.7}$

$2.5^{+1.1}_{-0.5}$

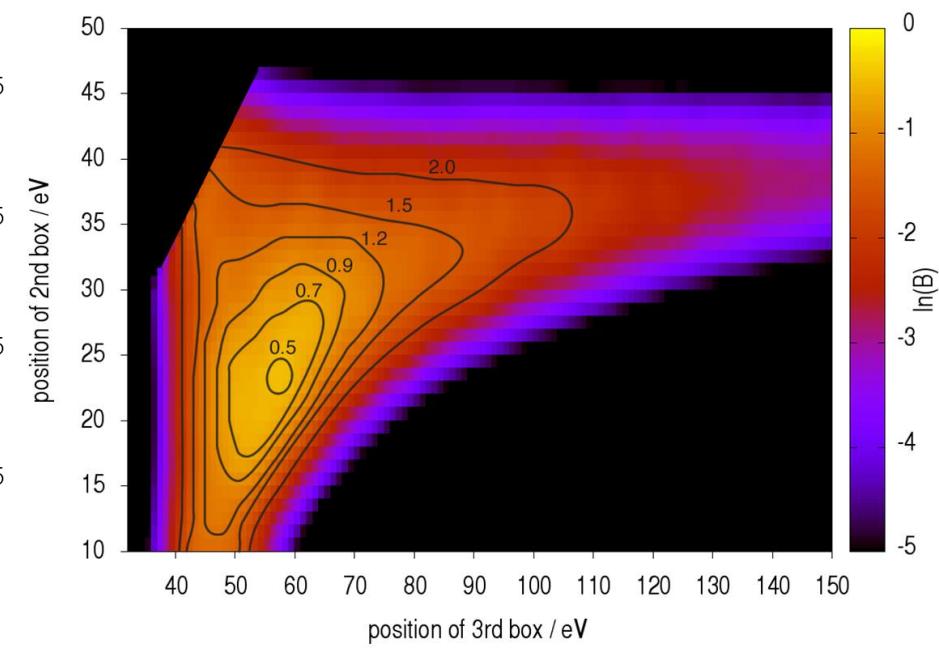
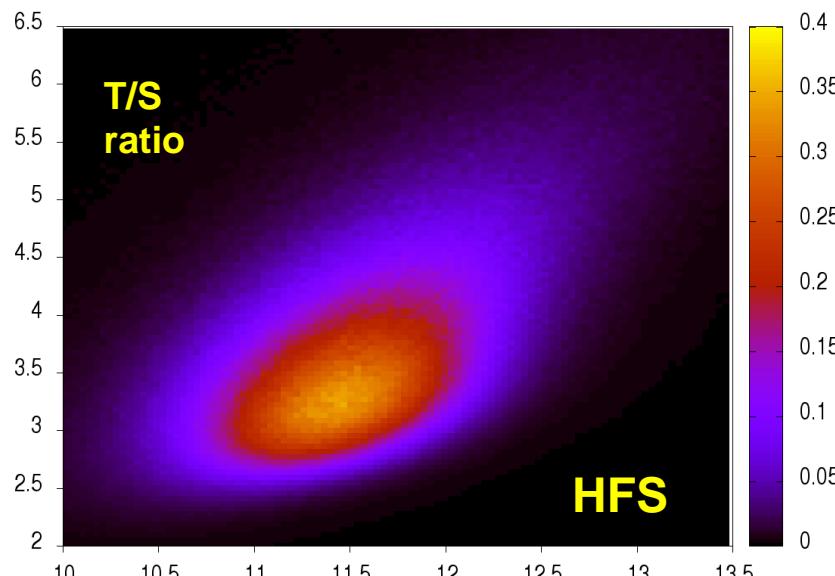


ANALYSIS - $\mu\text{H}(3p - 1s)$ III

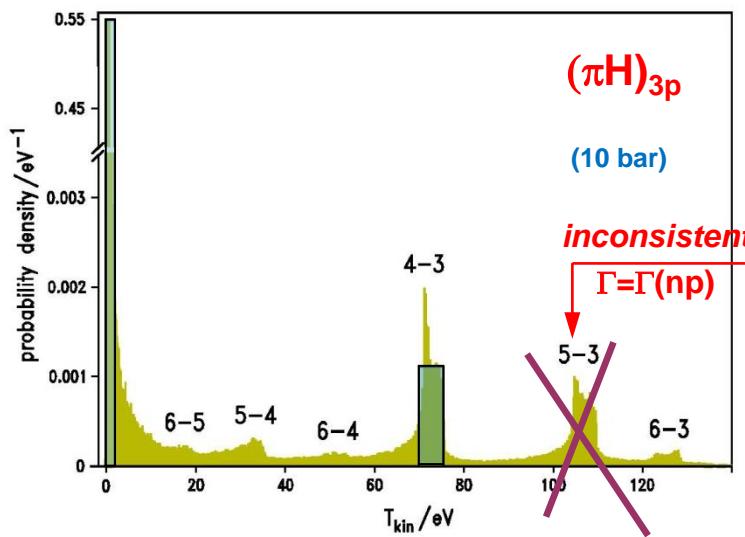
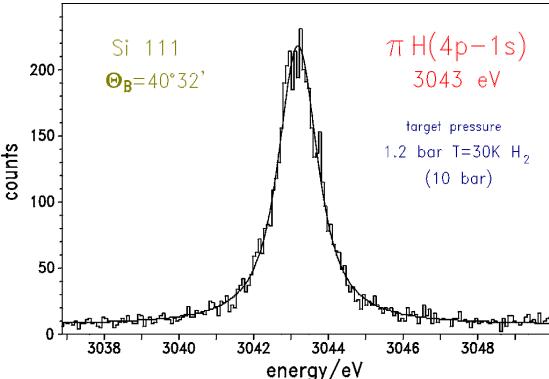
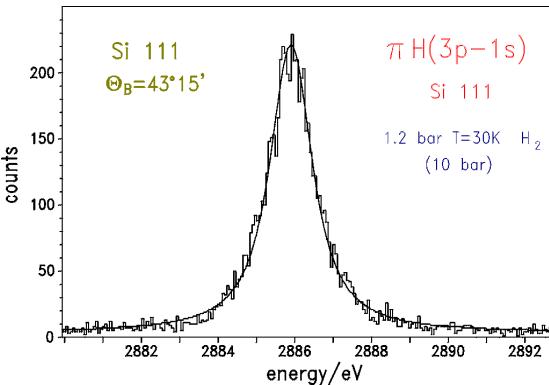
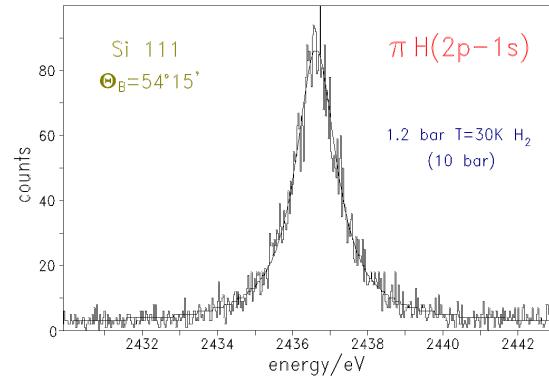
two-dimensional posterior probability

HFS free **212** $^{+23}_{-21}$
T/S **3.2** $^{+1.6}_{-0.7}$

High-energy components



ANALYSIS - $\pi H(np - 1s)$ I



Coulomb transition

low-energy $\approx 50\%$

5-4 ---

6-4 ---

4-3 $\approx 50\%$

3-2 ?

low-energy $\approx 55\%$

5-4 ---

6-4 ---

4-3 $\approx 45\%$

5-3 ---

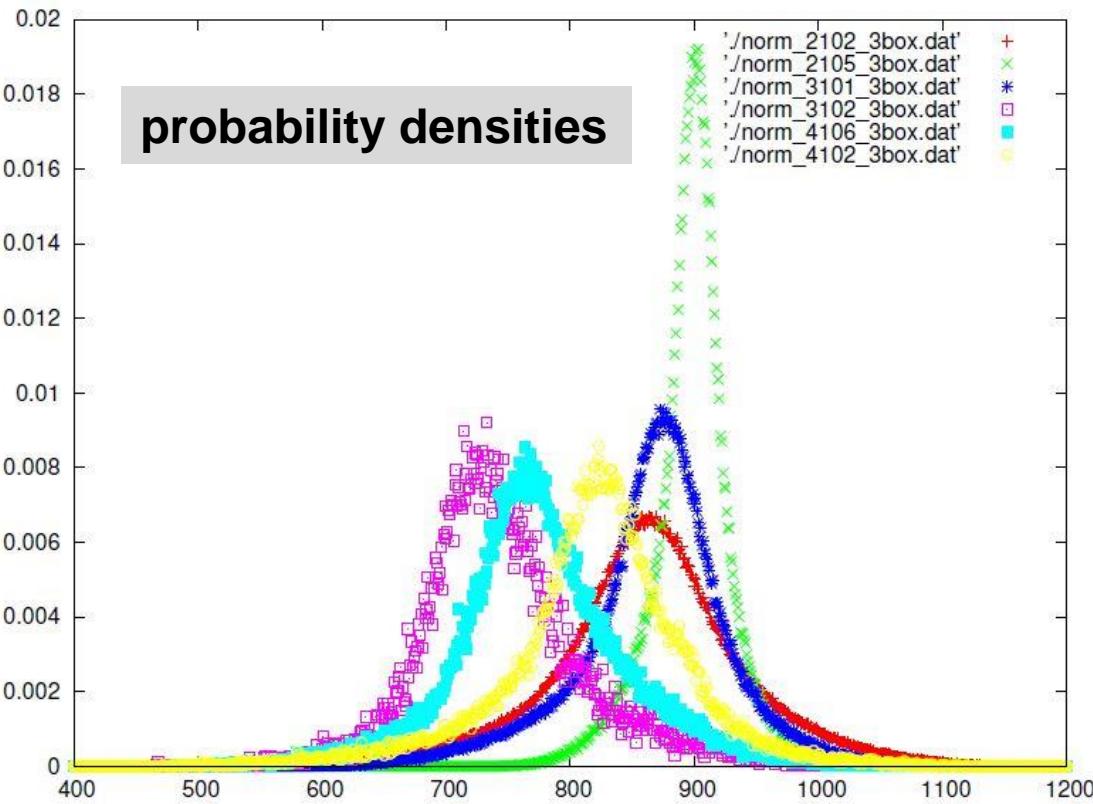
low-energy $\approx 50\%$

6-5 ---

5-4 $\approx 50\%$

6-4 ---

ANALYSIS - $\pi\text{H}(np - 1s)$ Γ_{1s} //



model-independent

approach

3-component model

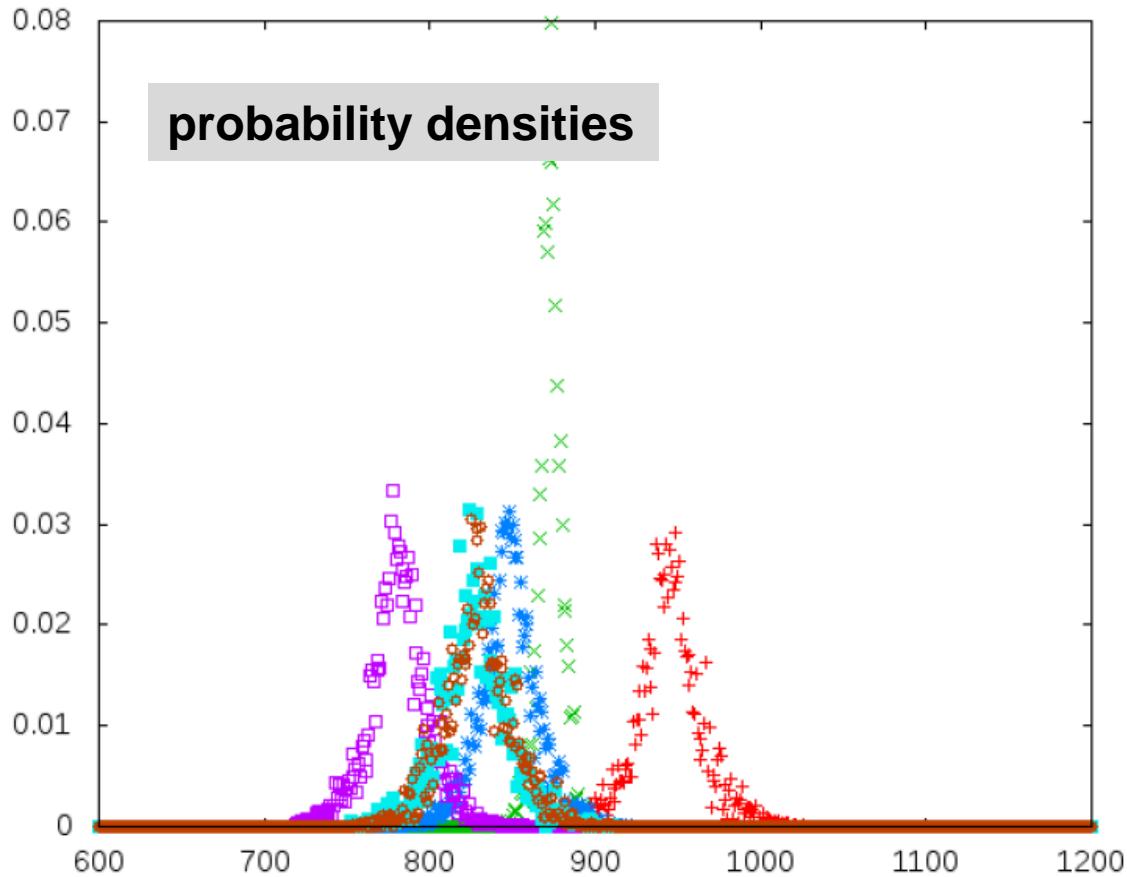
6 individual measurements

$2 \times \pi\text{H}(2p-1s)$

$2 \times \pi\text{H}(3p-1s)$

$2 \times \pi\text{H}(4p-1s)$

ANALYSIS - $\pi H(np - 1s) \Gamma_{1s}$ III

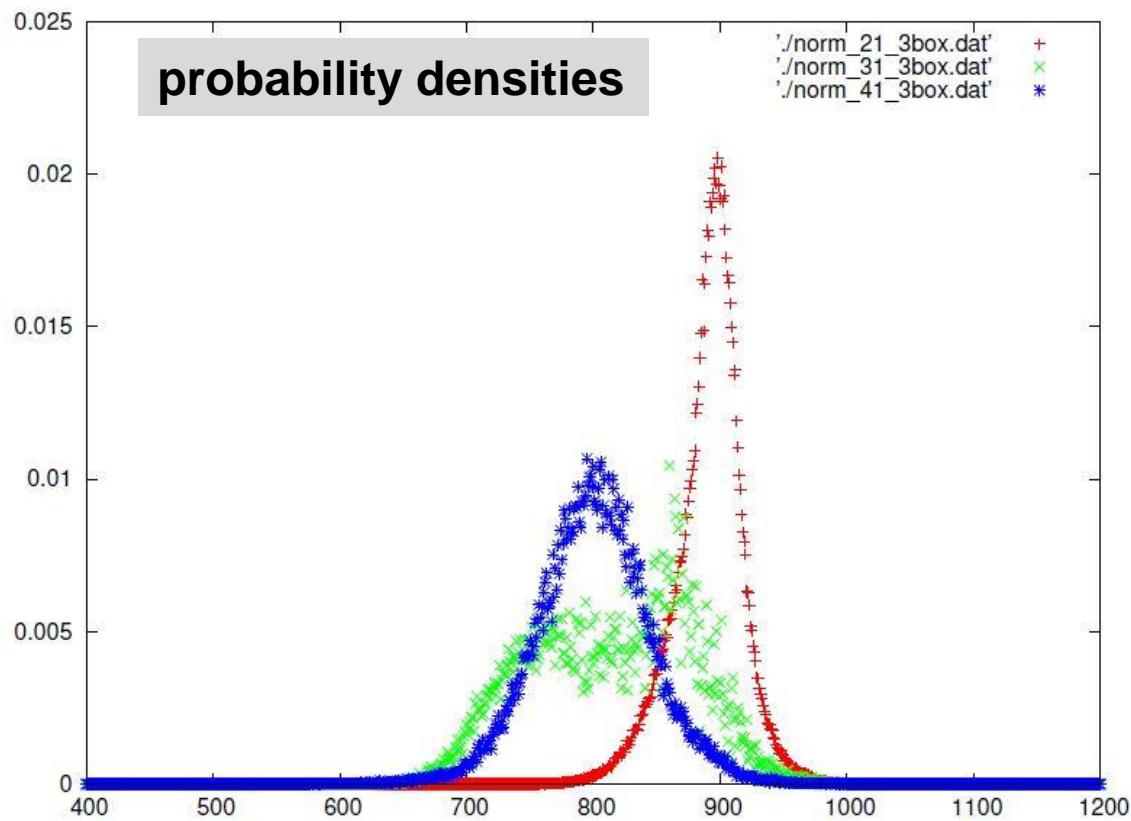


using
kinetic energy distribution
from cascade theory
6 individual measurements
 $2 \times \pi H(2p-1s)$
 $2 \times \pi H(3p-1s)$
 $2 \times \pi H(4p-1s)$

cascade calculation

V.N. Pomerantsev and V.P. Popov

ANALYSIS - $\pi H(np - 1s) \Gamma_{1s}$ IV



model-independent

approach

3-component model

individual transitions

$\pi H(2p-1s)$

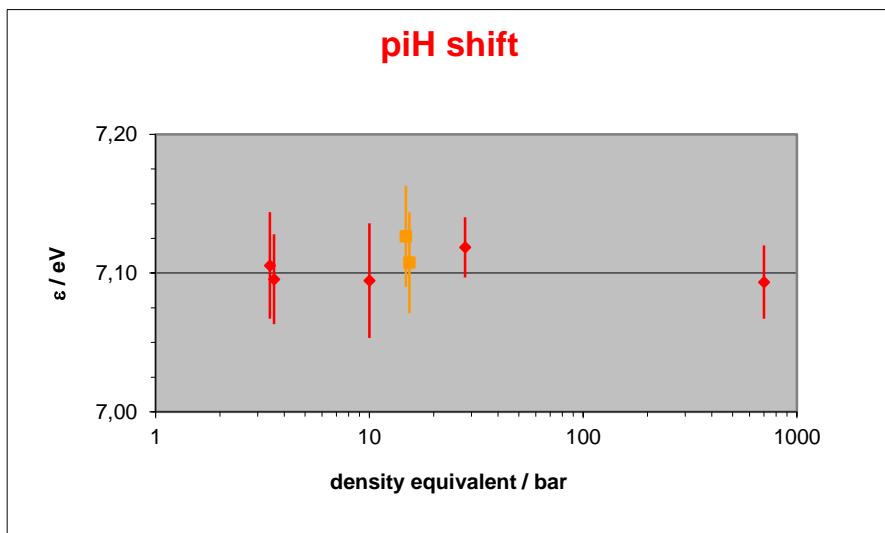
$\pi H(3p-1s)$

$\pi H(4p-1s)$

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- ANALYSIS
- **RESULTS**
- CONCLUSIONS

$\pi\text{H}(3p - 1s) \quad \varepsilon_{1s} \quad \text{final}$

no density dependence identified \Rightarrow “no” X-ray transitions from molecular states



previous experiment – Ar K α
ETHZ-PSI H.-Ch.Schröder et al.
Eur.Phys.J.C 1(2001)473

new calculation $\pi\text{H} \Rightarrow \Delta E_{QED} = \pm 0.001 \text{ eV} !$

P. Indelicato, priv. comm.

mainly pion mass $\Delta E_{QED} = \pm 0.006 \text{ eV} !$

cancels mainly using πO calibration* \downarrow

new QED value available since 2011: - 22 meV!

S. Schlessler et al. Phys. Rev. C 84 (2011) 015211

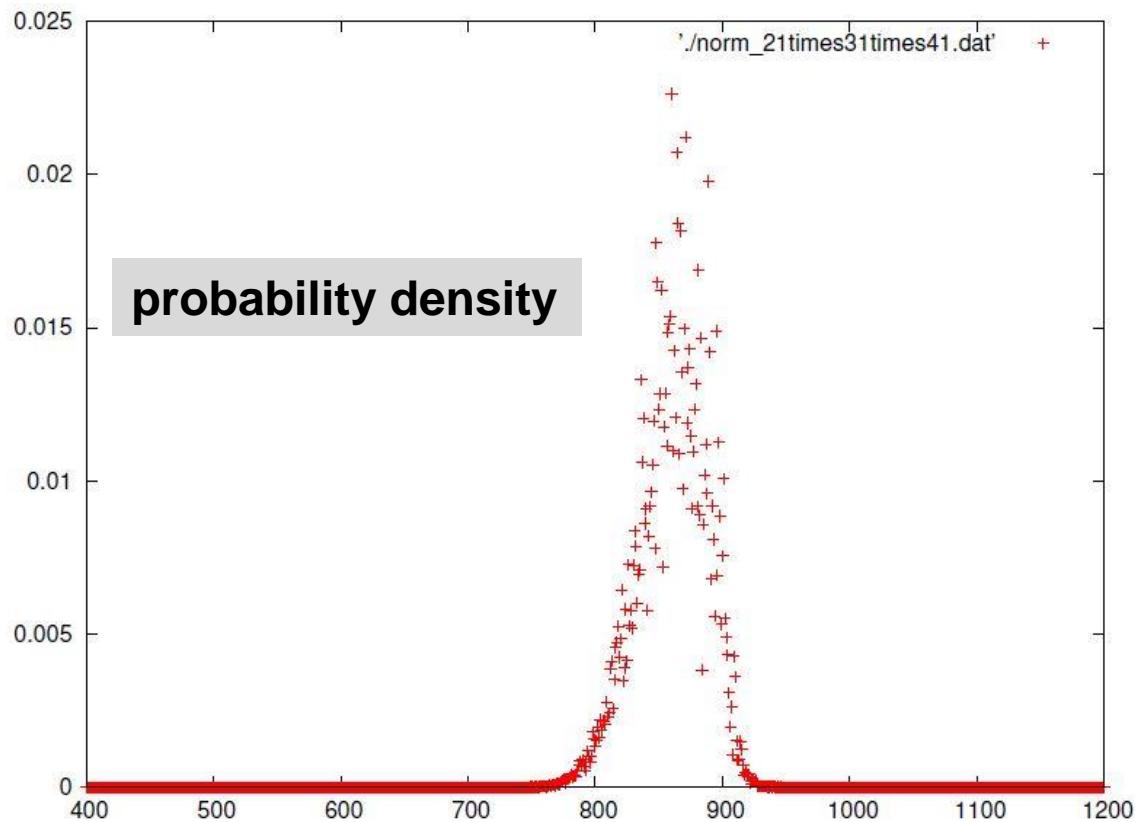
new mass measurement $\pm 1.3\text{ppm}$

M. Trassinelli et al., Phys. Lett. B 759 (2016) 583

$$\varepsilon_{1s} = + 7.087 \pm 0.009 \text{ eV} (\pm 0.13\%)$$

$$a_{\pi^- p} = (85.26 \pm 0.12) \cdot 10^{-3} m_\pi^{-1}$$

M. Hennebach, PhD thesis, Cologne 2003
M. Hennebach et al., Eur. Phys. J. A 50 (2014) 190



model-independent

approach

3-component model

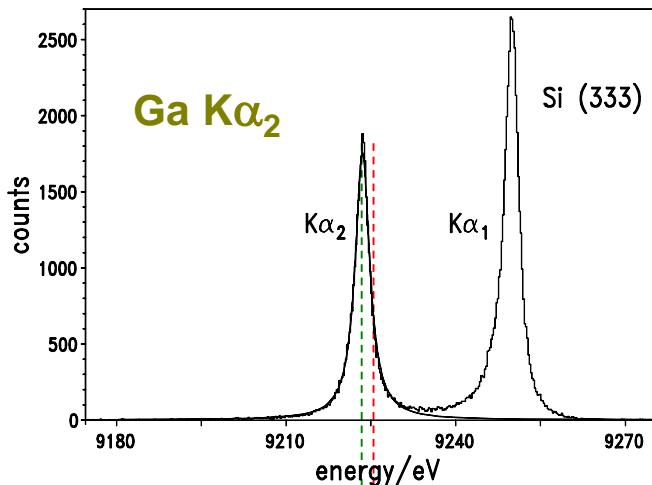
all measurements

$$\Gamma_{1s} = (0.85 \pm 0.04) \text{ eV}$$

$$a_{\pi^- p \rightarrow \pi^0 n} = (124 \pm 3) \cdot 10^{-3} \text{ m}_\pi^{-1}$$

$\pi D(3p - 1s)$ ε_{1s} final

energy calibration

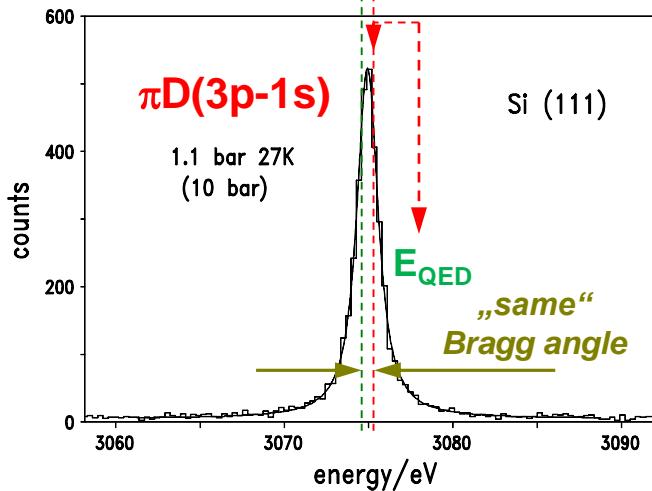
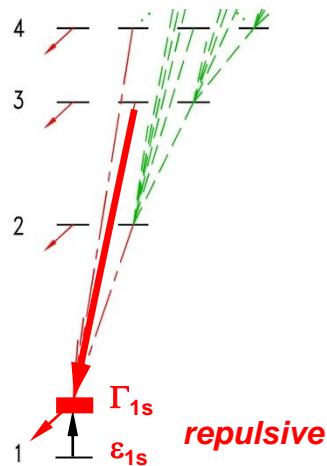


3 bar
10 bar
22 bar } no molecule formation seen

error budget

± 27 meV	$Ga K\alpha_2$
± 10 meV	statistics
± 8 meV	pion mass
± 5 meV	systematics
± 2 meV	QED

strong interaction



$$\varepsilon_{1s} = (-2.356 \pm 0.031) \text{ eV} (\pm 1.3\%)$$

$$\Re a_{\pi^- d} = (25.0 \pm 0.3) \cdot 10^{-3} m_\pi^{-1}$$

PhD thesis: Th. Strauch, Cologne 2009
Th. Strauch et al., Phys. Rev. Lett. 104 (2010) 142503; Eur. Phys. J. A 47 (2011) 88

πN ISOSPIN SCATTERING LENGTHS a^+ and a^-

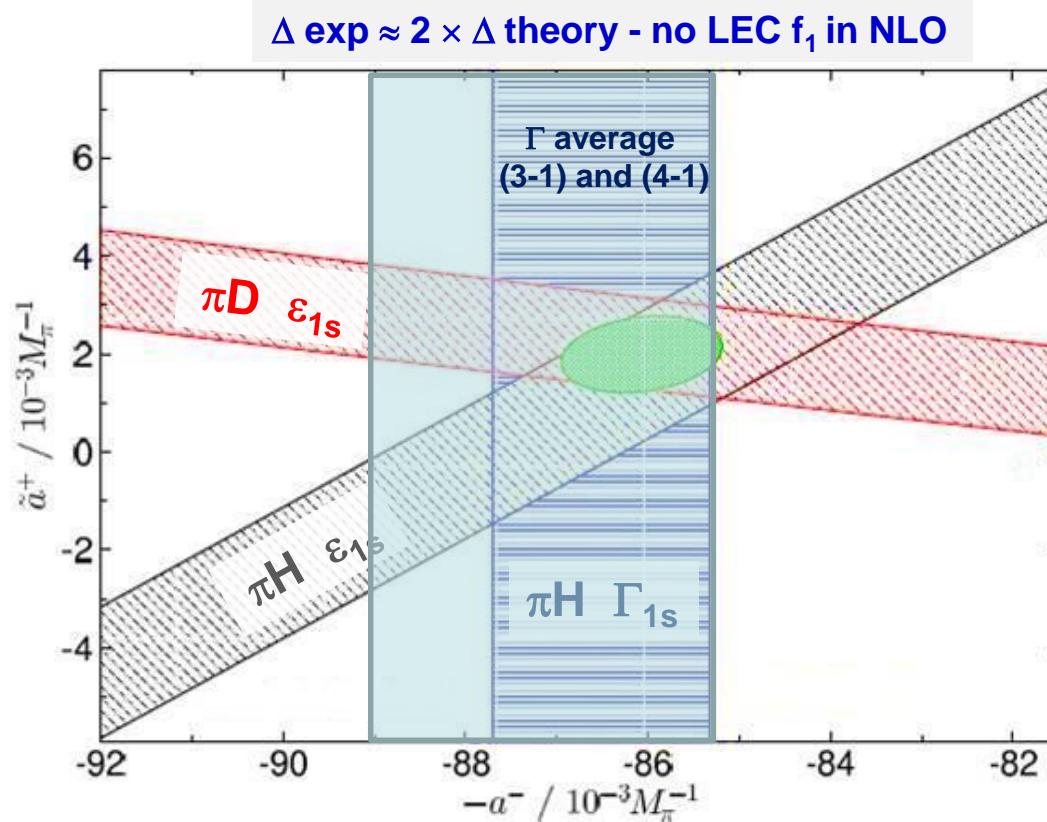


FIG. 2: Combined constraints in the $\tilde{a}^+ - a^-$ plane from data on the width and energy shift of πH , as well as the πD energy shift.

χPT : J. Gasser et al., Phys. Rep. 456 (2008) 167

M. Hoferichter et al., Phys. Lett. B 678 (2009) 65

V. Baru, C. Hanhart, M. Hoferichter, B. Kubis, A. Nogga, and D. R. Phillips, Phys. Lett. B 694 (2011) 473

data: πH - R-98.01 : D. Gotta et al., Lect. Notes Phys. 745 (2008) 165

M. Hennebach et al., Eur. Phys. J. A 50 (2014) 190

πD - R-06.03 : Th. Strauch et al., Eur. Phys. J. A 47 (2011) 88

- consistency ✓
- πD decisive
- $a^+ > 0 !$

NN $\Leftrightarrow \pi$ NN threshold parameter α

$$\Gamma_{1s} = (1.171 \pm 0.023) \text{ eV } (+2\%) \text{ } (-4\%) \text{ final}$$

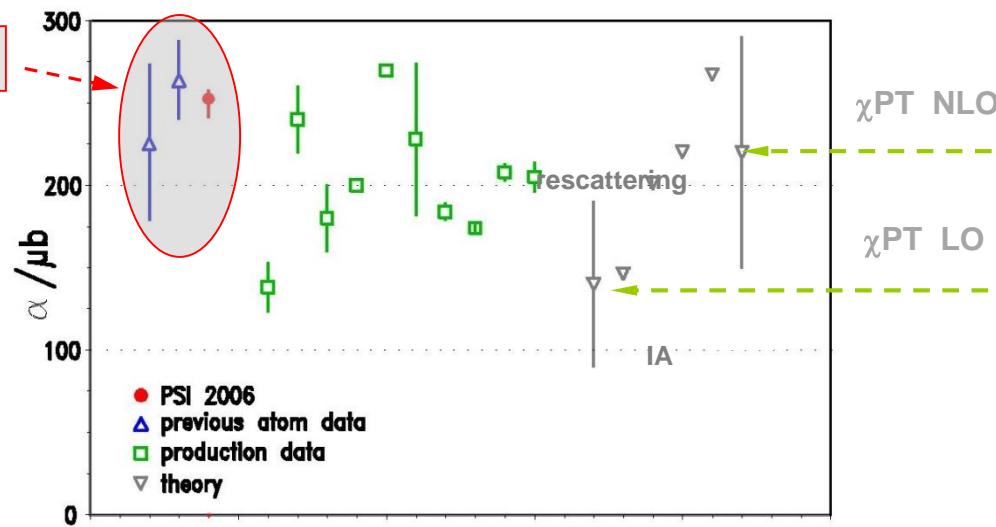
$$\Im a_{\pi^- d} \propto \alpha(pp \rightarrow \pi^+ d) = (251 \pm 5) \mu b$$

exotic-atom results

Th. Strauch,
PhD thesis, Cologne 2009

Th. Strauch et al.,
Phys. Rev. Lett. 104 (2010) 142503

Th. Strauch et al.,
Eur. J. Phys. 47 (2011) 88



χ PT
at present
 $\Delta\alpha/\alpha \approx 30\%$
 \rightarrow few % !?

V. Lensky et al.,
Eur. Phys. J. A 27 (2006) 37

- WHY PIONIC HYDROGEN & ... ?
- EXPERIMENTAL APPROACH
- ANALYSIS
- RESULTS
- CONCLUSIONS

πA INTERACTION – ADDITIONAL ACCESS TO a^\pm ?

$$a_{\pi^-A} = \left(\frac{\mu_{\pi A}}{\mu_{\pi N}} \right) \cdot (A \cdot a^+ + T_3^A \cdot a^-) + IV + \text{few-body}$$

S. Baru et al.,
Eur. Phys. J. A 16 (2003) 437

S. Liebig et al.,
Eur. Phys. J. A 47 (2011) 69

$$a_{\pi^-p} \propto (a^+ + a^-) + (9\pm 4)\%$$

$$a_{\pi^-n} \propto (a^+ - a^-) + (9\pm 4)\%$$

$$\Re e a_{\pi^-D} \propto (2a^+ + 0) + \dots + 80\%$$

$$\Re e a_{\pi^-T} \propto (3a^+ - a^-) + \dots + 25\%$$

$$\Re e a_{\pi^- {}^3He} \propto (3a^+ + a^-) + \dots + 40\%$$

$$\Re e a_{\pi^- {}^4He} \propto (4a^+ + 0) + \dots + 80\%$$

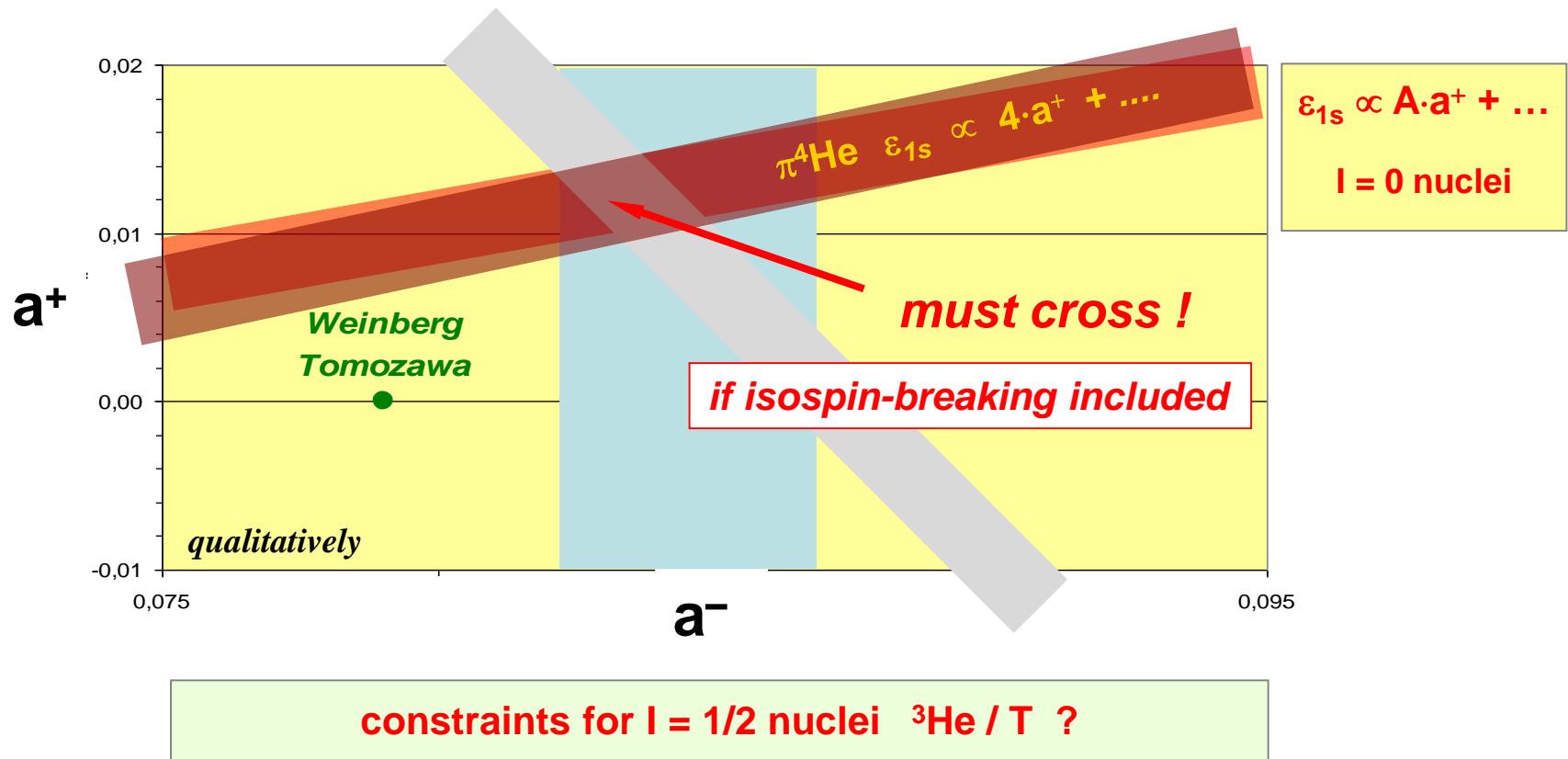
$\Re e a_{\pi^- A} / m_\pi^{-1}$

	<i>experiment</i>	<i>theory</i>
<i>p</i>	+ 0.0853 ± 0.0001	
<i>d</i>	- 0.0250 ± 0.0003	
<i>n</i>	- 0.0907 ± 0.0016*	
<i>T</i>	<i>unpopular</i>	
^3He	+ 0.047 ± 0.009**	+ 0.062 ± 0.008
^4He	- 0.098 ± 0.003**	- 0.055 ± 0.005

* *opt. potential*

** *new data to be analysed*

a⁺ vs. a⁻



Theory C.Werntz and H. S.Valk, Phys. Rev. C 37, 724 (1988). $\Gamma(\pi T)$ predicted from radiative capture $\pi T \rightarrow \gamma nnn$
Baru, Haidenbauer, Hanhart, Niskanen, Eur. Phys. J. A 16 (2003) 437, $T / {}^3\text{He}$ comparison:
.... more coming

Experiment ${}^3\text{He}/{}^4\text{He}$ new data for ε_{1s} at $\approx 3\%$ level available - analysis still preliminary



- πN scattering length: bands cross
- S - wave π - production strength
- μH – singlet / triplet
 - ΔE_{HFS}
 - cascade theory \approx line shape



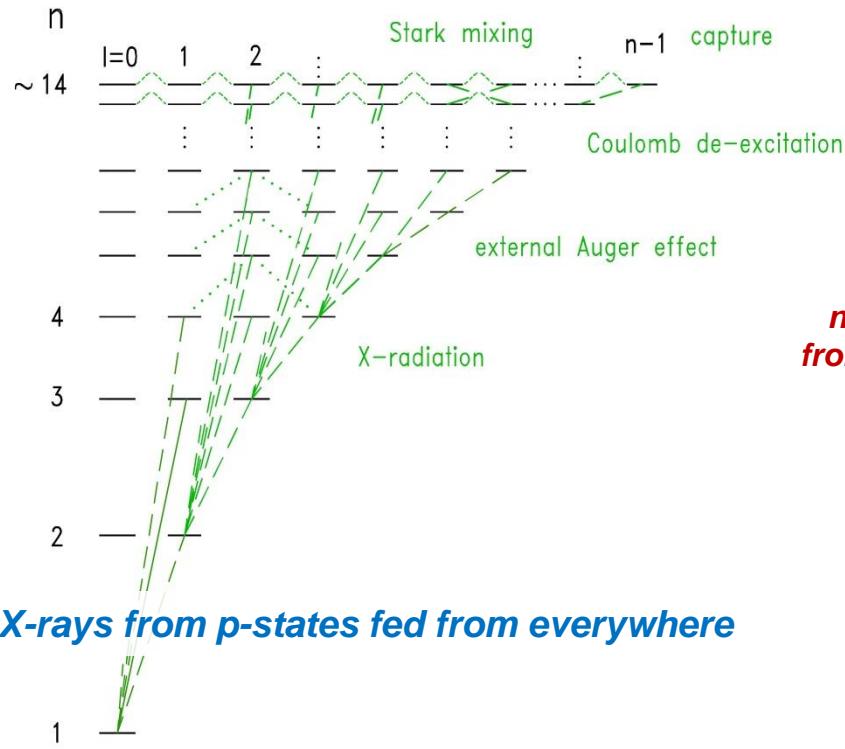
- πH – spreading of Γ_{1s} unsatisfactory
 - origin unknown* - cascade ?
 - analysis ?
 - experiment ?
- πD – Coulomb de-excitation ?

WHERE DO THEY GO ?

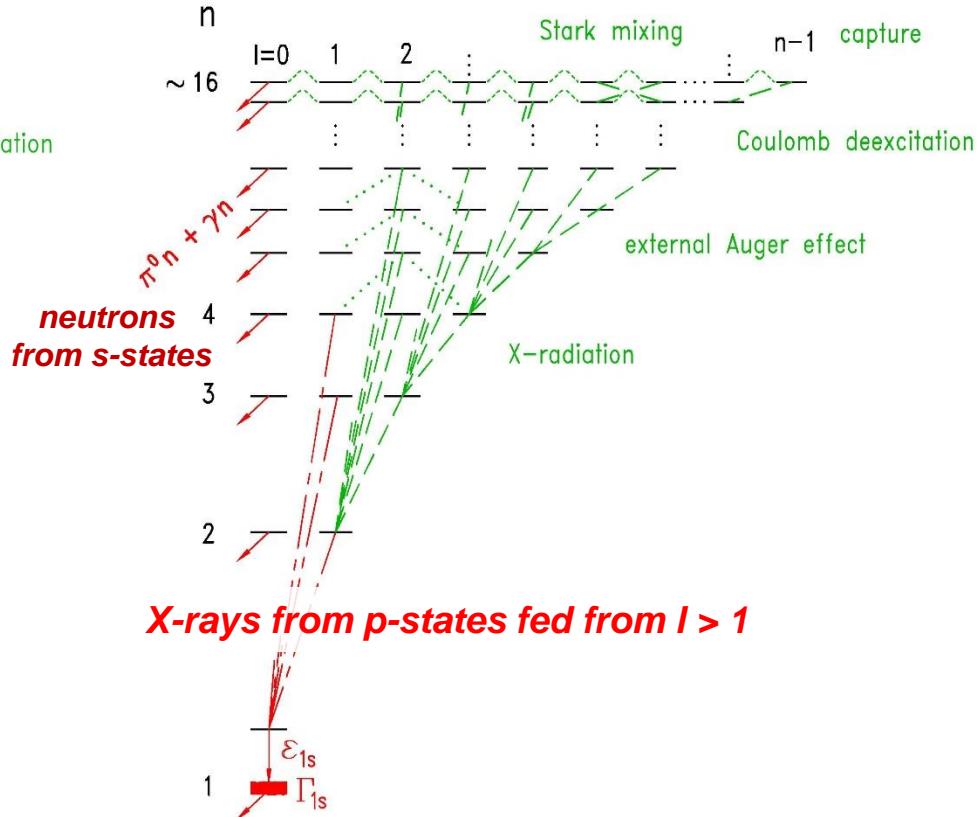
μH

πH

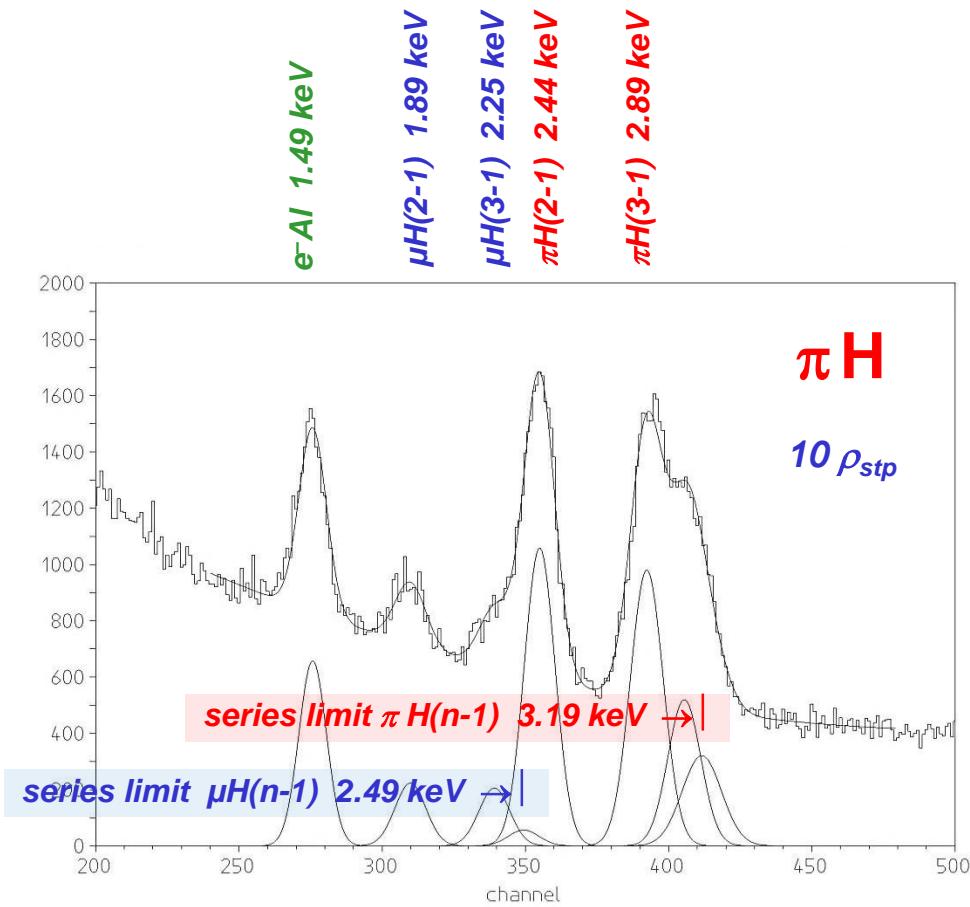
X-rays from p-states fed from everywhere



X-rays from p-states fed from $l > 1$



CASCADE - MORE INSIGHT ?



crystal spectrometer

$$n_{max} \approx \sqrt[3]{\frac{2n_f^2}{(\Delta E/E_{\infty-n_f})}}$$

$n_{max} \approx 25$ for $\Delta E = 400$ meV

n_{max} : resolvable state

n_f : final state

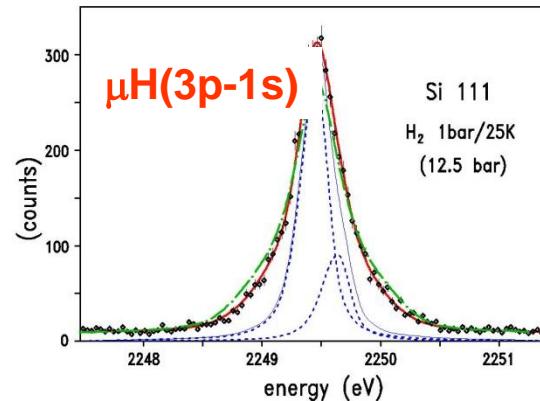
ΔE : energy resolution

$E_{\infty-n_f}$: transition energy from series limit

IS SOMETHING MISSING ?

?

X-ray satellites from
molecular formation
- none seen in πD -

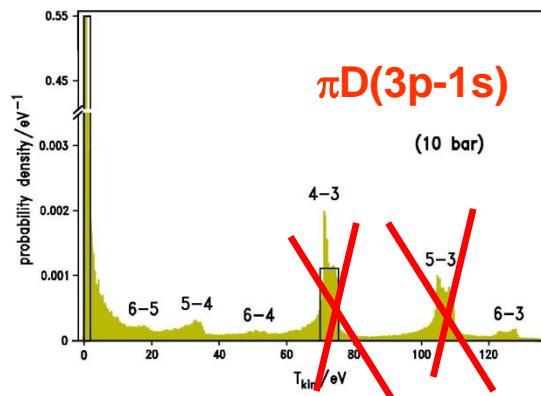


0-2 eV	61 ± 2 %
5-4	25 ± 3 %
4-3	14 ± 4 %

≈ πH

?

high-energy components
- no cascade calculation yet -



?

does cascade theory improve for πH as for μH - if yes: $\Delta\Gamma \rightarrow \Delta\Gamma /2$

μD

cross sections

WHAT TO DO?

$\Gamma_{1s} \rightarrow 1\%$

minimize Coulomb de-excitation

$\pi H(4p-1s)$

$\pi H(5p-1s)$?

set-up

increase resolution

quartz 10-2

cascade

understand better
kinetic energy distribution

$\mu H, \mu D$

exploit higher pion fluxes at PSI

PIONIC HYDROGEN collaboration

PSI experiments R-98.01 and R-06.03

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Cascade theory

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→ Diploma and PhD thesis ←

THANK YOU