

# Fully Differential Study of Post-Collision Effects in Ionization of H<sub>2</sub> by Proton Impact

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**Quantum-mechanical few-body problem one of the most fundamentally important, unsolved problems in Physics!**

**Schrödinger equation not solvable for more than two particles, even when underlying forces are precisely known**

**Dynamic few-body systems like fragmentation processes**

**Atomic fragmentation particularly suitable because:**

- **underlying interaction** (electromagnetic) understood
- can select systems with small particle number ( $\approx 3 - 5$ )  $\Rightarrow$  **kinematically complete experiments**

# Ionization of H<sub>2</sub> by p impact

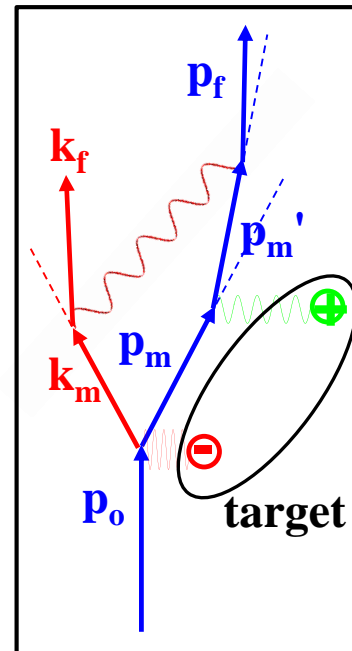
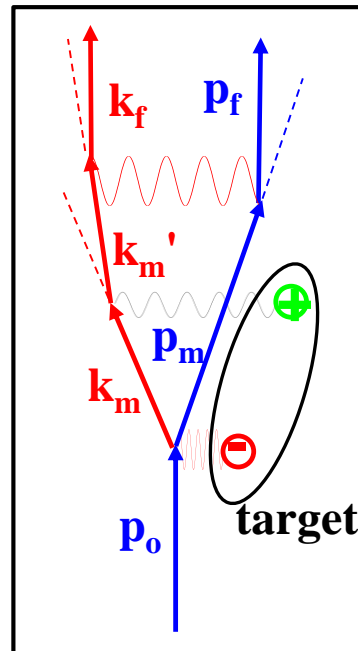
Perturbative treatment: expand T in powers of interaction potential V (Born series)

$$T = \langle e^{ik_f r} \varphi_f | V | e^{ik_i r} \varphi_i \rangle + \langle e^{ik_f r} \varphi_f | V G_0 V | e^{ik_i r} \varphi_i \rangle + \langle e^{ik_f r} \varphi_f | V G_0 V G_0 V | e^{ik_i r} \varphi_i \rangle + \dots$$

In perturbation theory **understanding few-body dynamics** means describing relative contributions of **higher- vs first-order terms**

Particularly important higher-order process: **PCI**

**PE** – **ET** – **PE**  
sequence

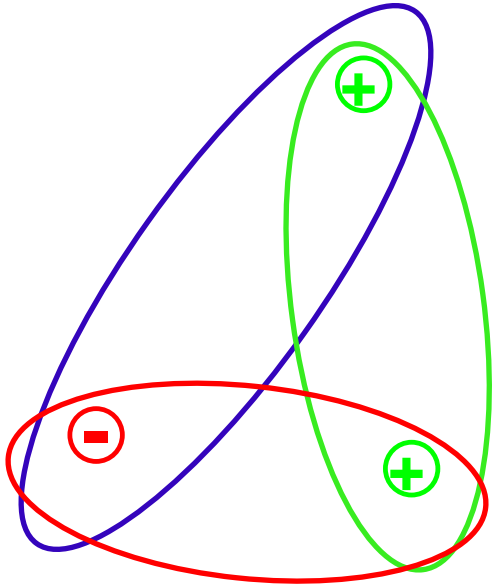


**PE** – **PT** – **PE**  
sequence

## Alternative to Born Series: Distorted wave methods

Higher-order contributions treated in wavefunction of system

Break up three-body system into **3 two-body systems**:



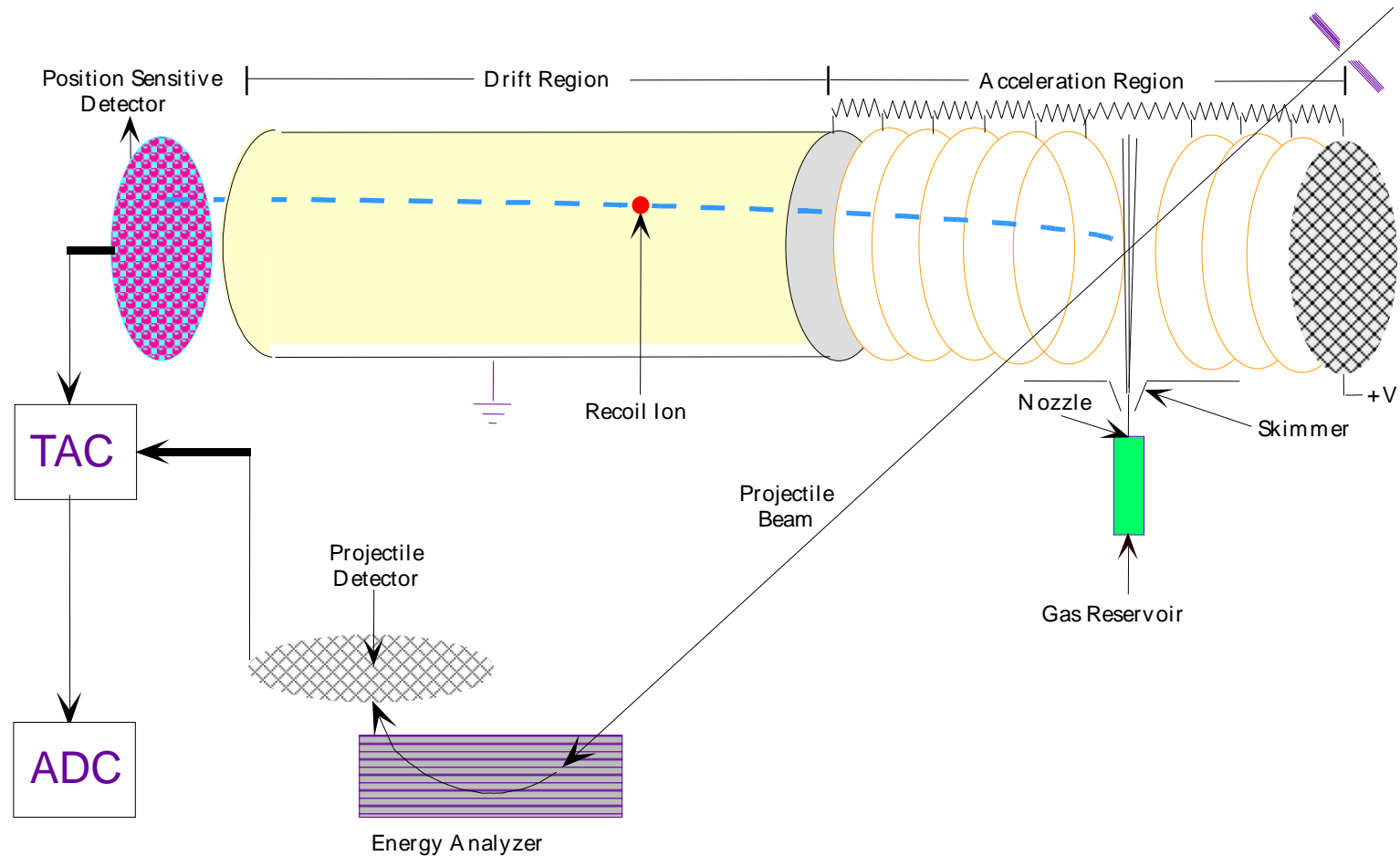
The continuum eigenstate of each two-body subsystem is a (distorted) **Coulomb-wave**. Approximation: Represent total wavefunction as product of three Coulomb-waves

$$\Psi_f = C_{Pe} C_{PT} C_{Te}$$

Conceptually, **all interactions treated to all orders**, but 3C wavefunction **ignores correlations between particle pairs**  $\Rightarrow$  only accurate if one particle far from other two  $\Rightarrow$  at small distances **none of higher-order terms described accurately**

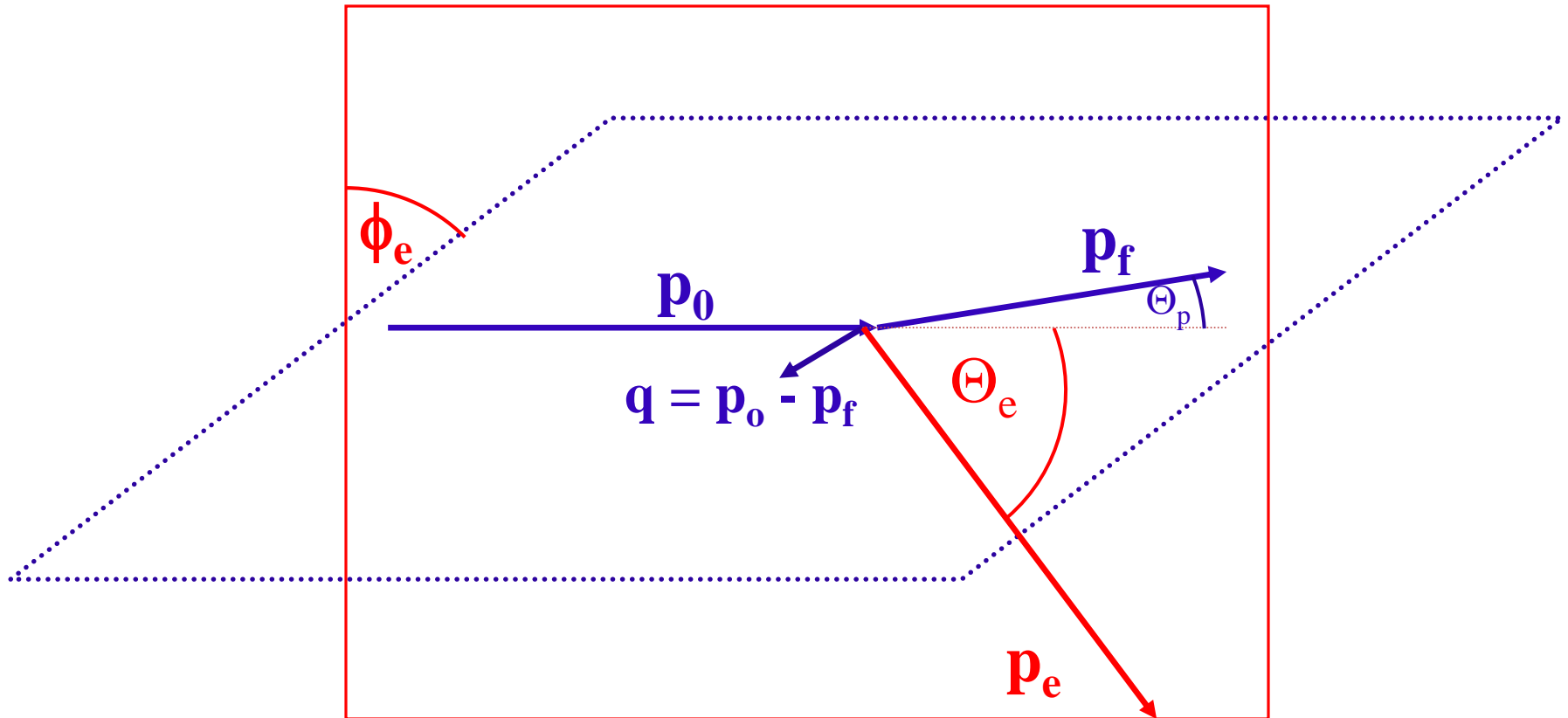
PCI maximizes for  $v_{e1} = v_p$ , **no kinematically complete data available!**

# Experimental Setup, 75 keV p + H<sub>2</sub>



**Complete projectile and recoil-ion moment measured. Electron momentum from conservation laws  $\Rightarrow$  kinematically complete  $\Rightarrow$  FDCS**

# Three-Dimensional Fully Differential Single Ionization Data



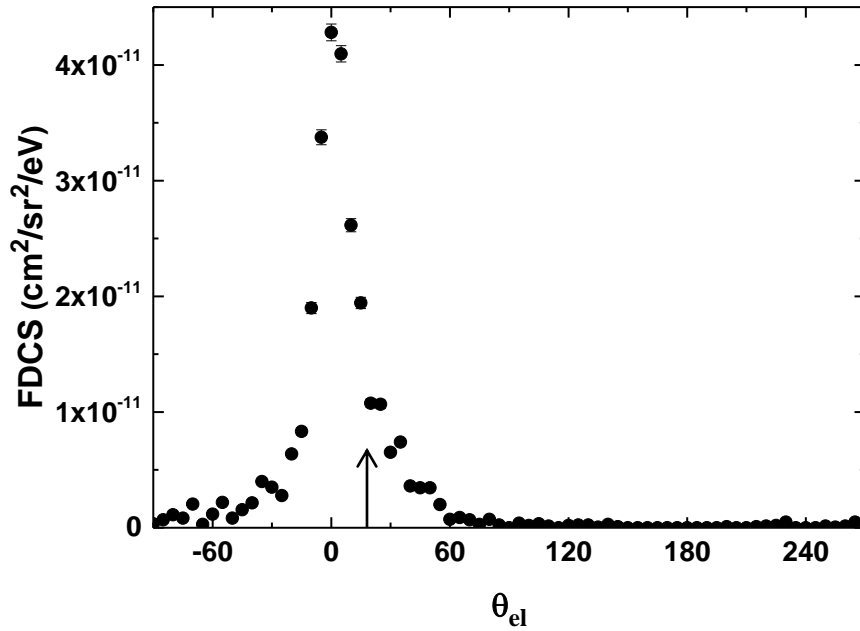
**Blue:** Scattering plane  
defined by  $\mathbf{p}_0$  and  $\mathbf{p}_f$

**Red:** electron emission plane  
defined by  $\mathbf{p}_0$  and  $\mathbf{p}_e$

**Quantities fixed:**  $\phi_p = 0$ ,  $\mathbf{q}$ ,  $\phi_e = 0$ , and  $\mathbf{E}_e$ , spectra plotted as a fct. of  $\Theta_e$

# Results: FDCS 75 keV p + H<sub>2</sub>

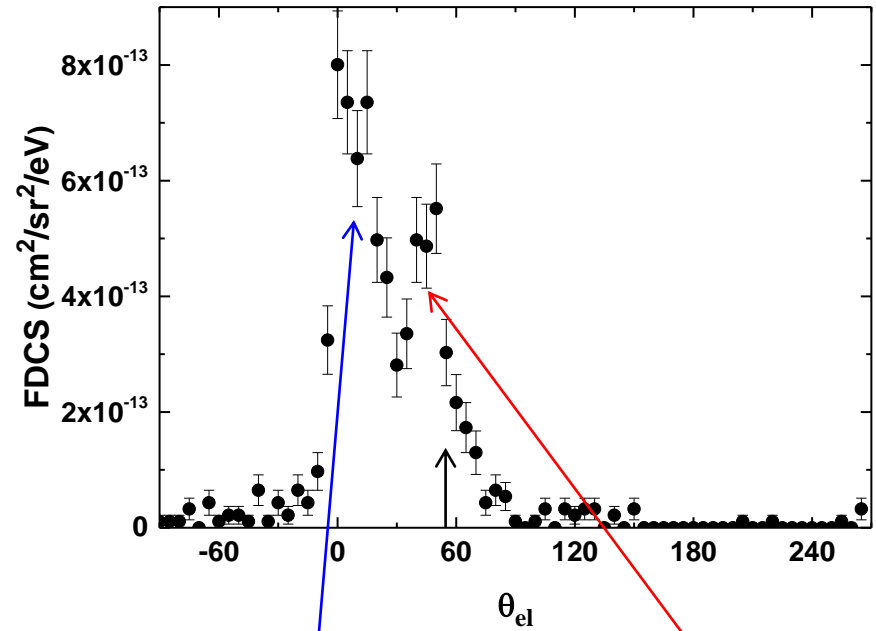
$\varepsilon = 53$  eV,  $\theta_p = 0.1$  mrad



small  $\theta_p$ :

- a) direction of  $q$  much closer to  $\theta_{el} = 0$
  - b) binary peak much weaker
- $\Rightarrow$  only single peak

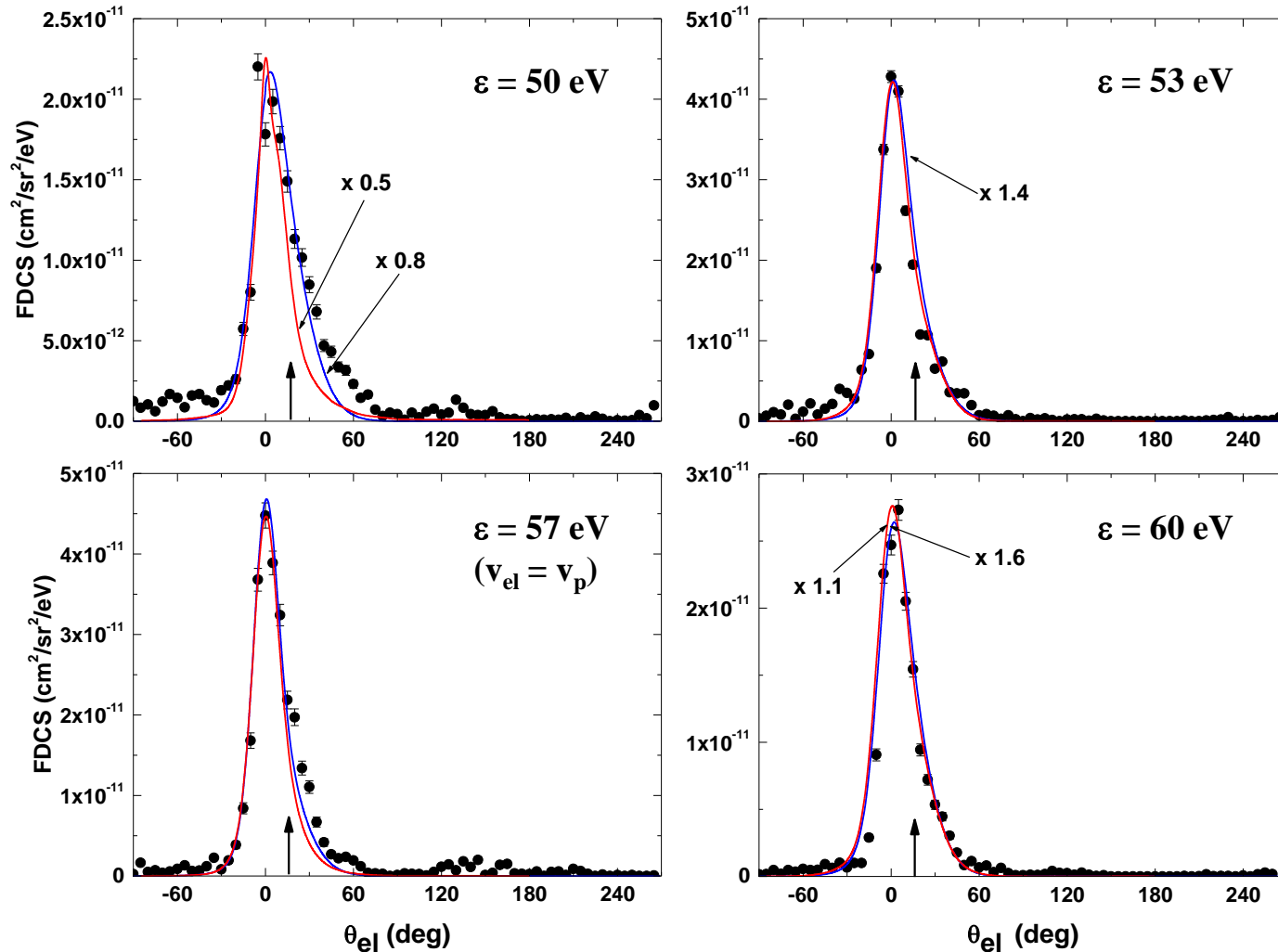
$\varepsilon = 60$  eV,  $\theta_p = 0.55$  mrad



„forward peak“  
signature of PCI  
projectile and  
electron attract  
each other  
towards beam  
axis

„binary peak“  
signature of 1<sup>st</sup>  
order process  
momentum  
conservation:  
near  $\theta_q$

# FDCS for $\theta_p = 0.1$ mrad

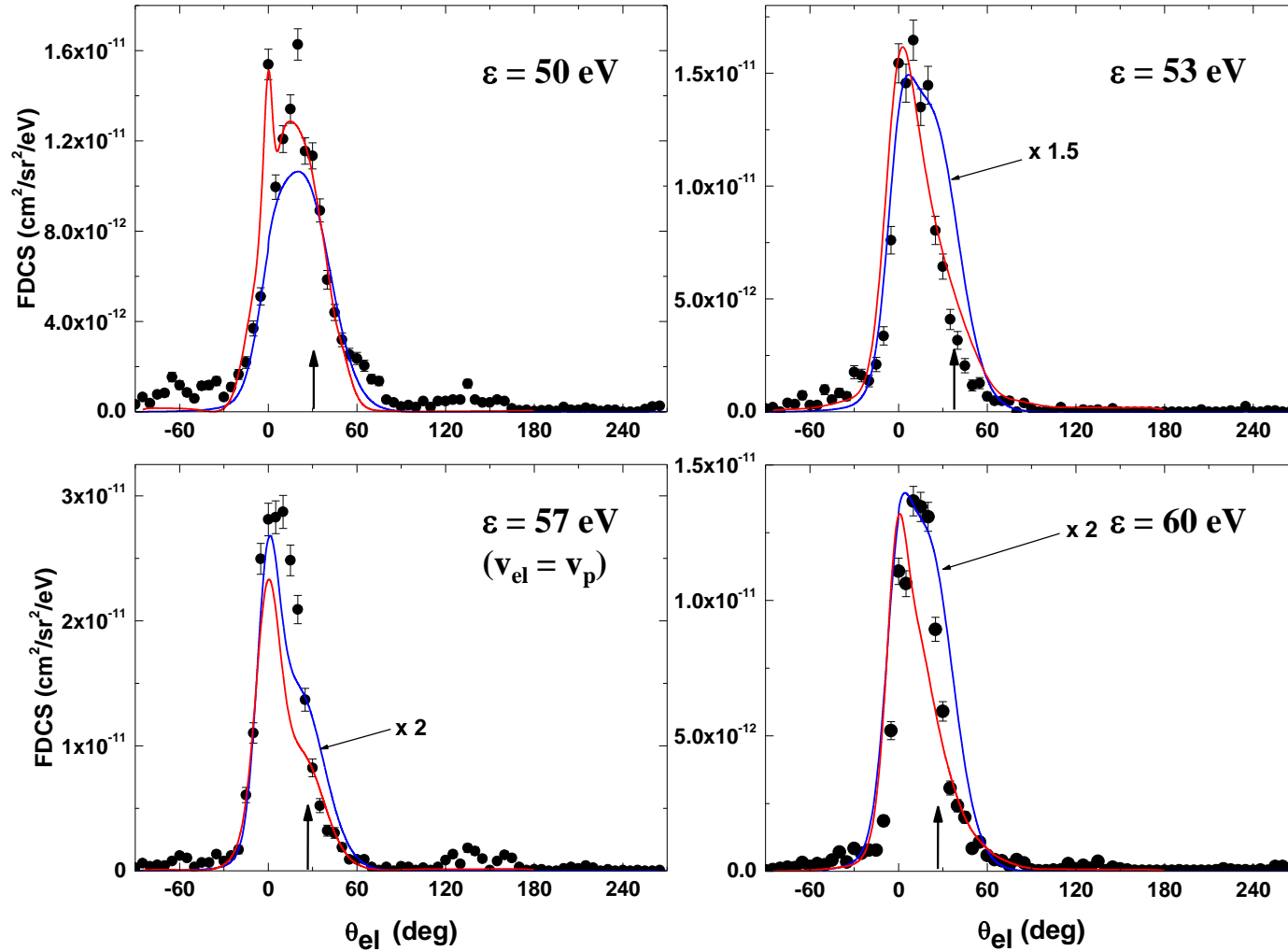


**Red curves: 3DW model**

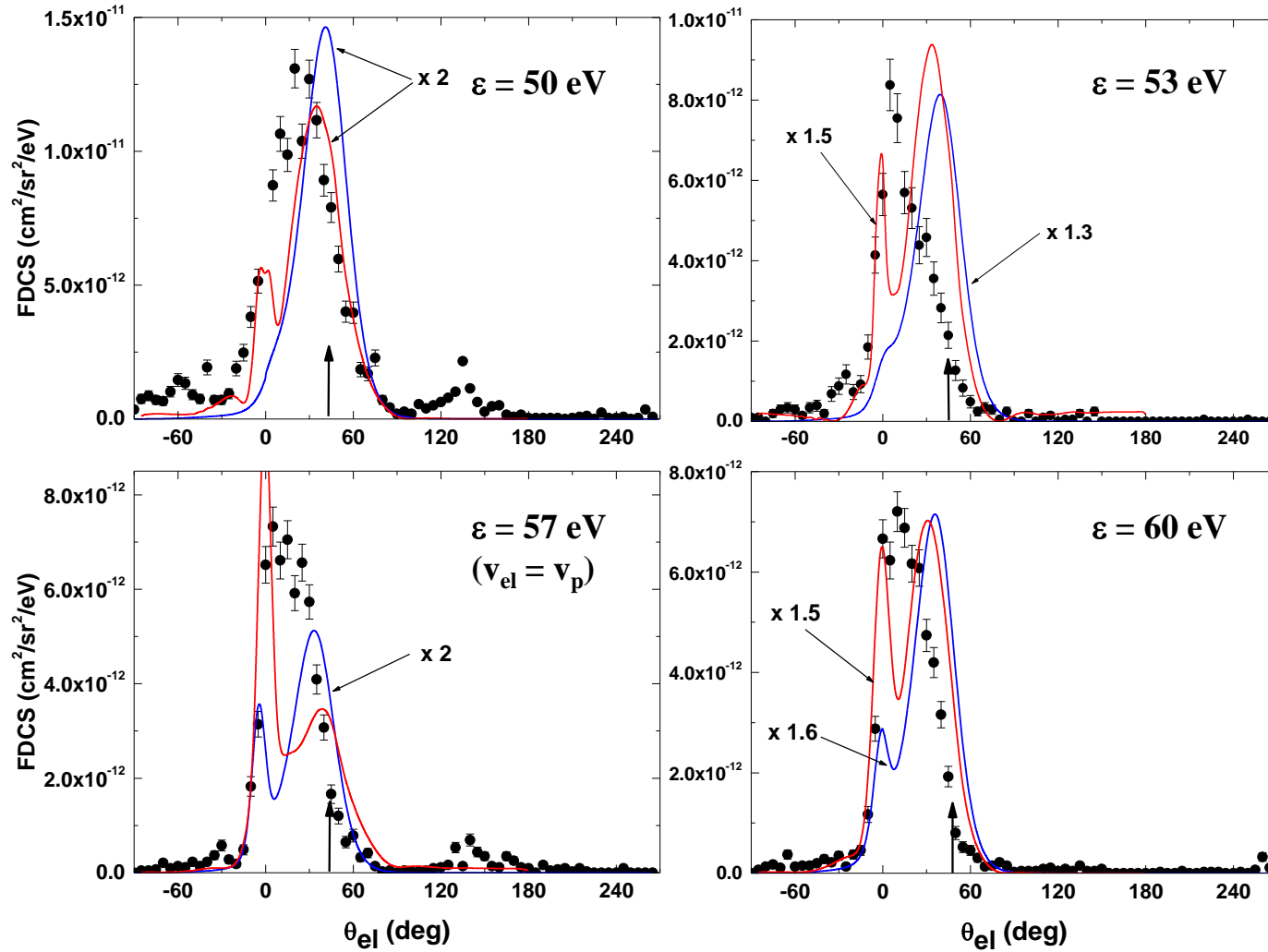
**Blue curves: CDW-EIS model**



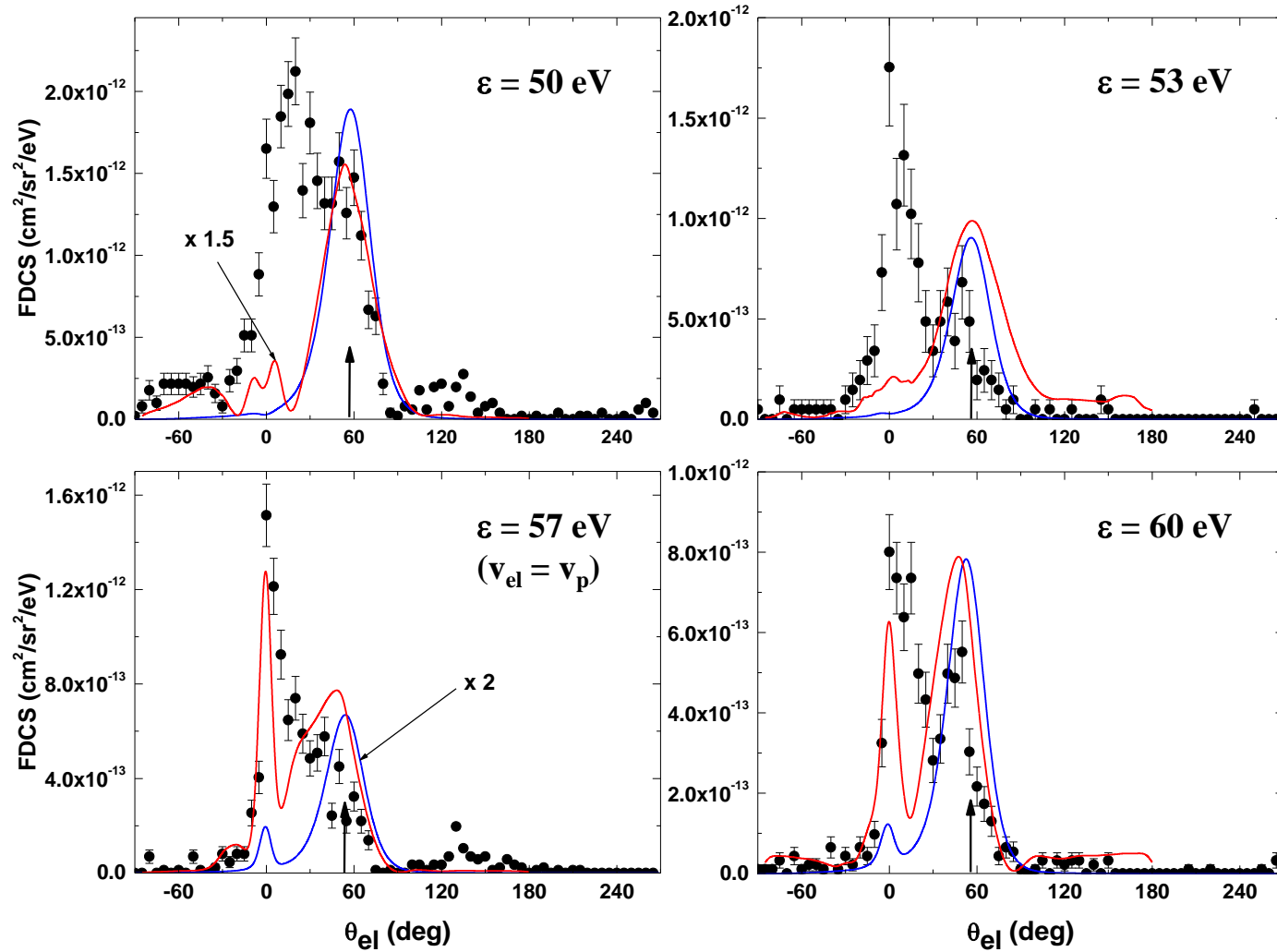
$$\theta_p = 0.2 \text{ mrad}$$



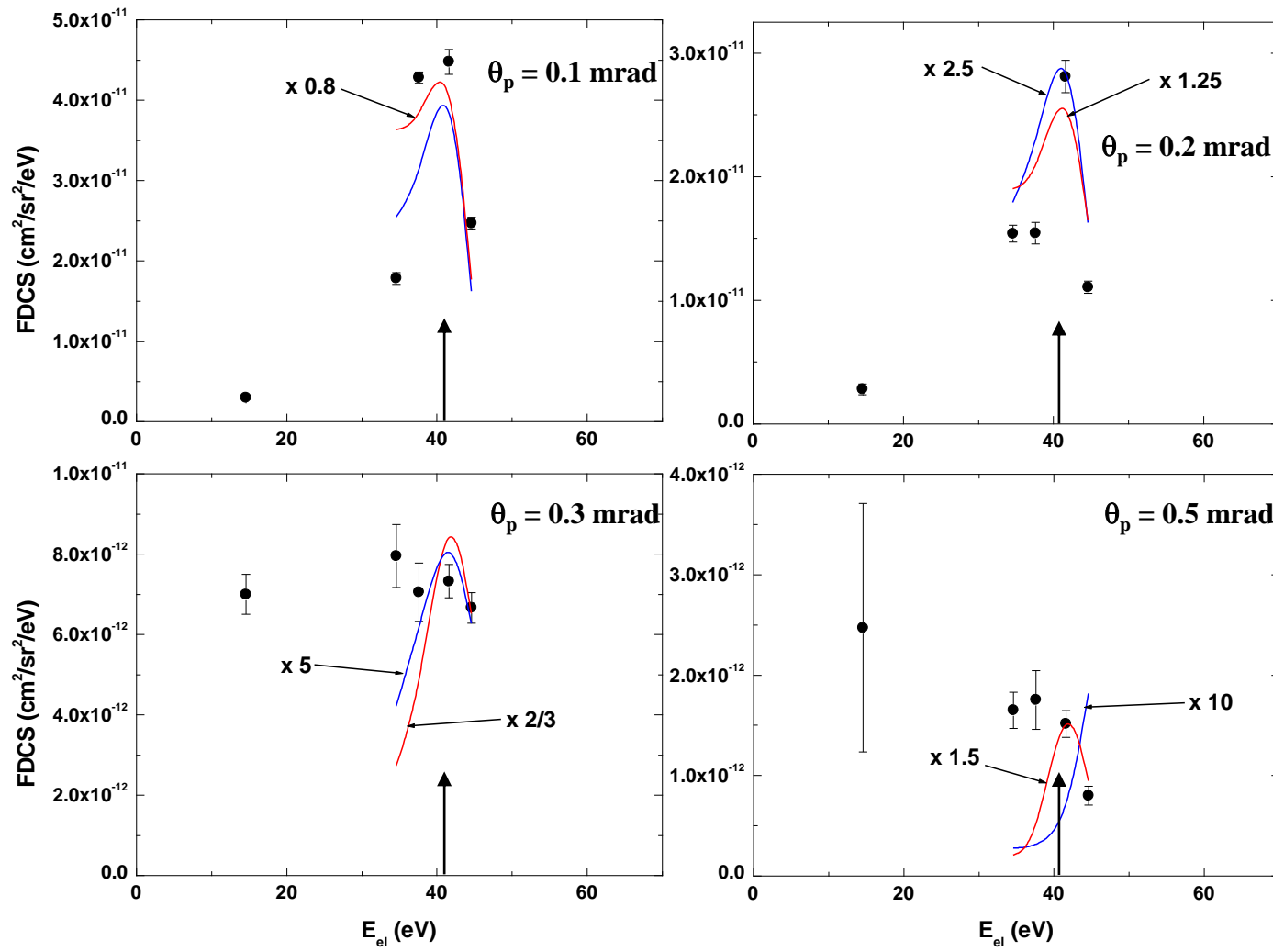
$$\theta_p = 0.325 \text{ mrad}$$



$$\theta_p = 0.55 \text{ mrad}$$



# Energy-dependence of FDCS for $\theta_e = 0^\circ$



⇒ Large discrepancies between experiment and **between two conceptually very similar theoretical models!**

At small electron energies much smaller discrepancies and theories agree with each other ⇒ **at velocity matching FDCS particularly sensitive to details of few-body dynamics!**

Possible causes for discrepancies:

- a) **PT interaction not accurate** in theory  
3C wavefunction only accurate if at least 1 particle far from other 2. **PE – PT – PE** sequence selects events where all 3 particles are close to each other
- b) **Capture channel not included** in theory ⇒ due to unitarity capture is erroneously counted as ionization in transition amplitude
- c) Projectiles treated as fully coherent waves, but in reality due to intrinsic momentum spread **coherence length is finite**

⇒ What type of theory is needed?

- a) **non-perturbative** because slow projectiles cannot be regarded as small perturbation ⇒ large basis set needed
- b) should incorporate **two-center basis set** including bound projectile states to account for **capture**
- c) projectiles should be described by **wave packet** with a width reflecting the **coherence length**

Non-perturbative models with two-center basis sets for ion impact have been developed recently (Kadyrov et al., Walters et al., Pindzola et al.). First results on FDCS for H<sub>2</sub> can be expected soon.

Incorporating wave packets in such models very challenging

# Conclusions

- Fully differential cross sections for ionization in 75 keV p + H<sub>2</sub> measured.
- Major discrepancies between experiment and theory and between two conceptually very similar models.
- At matching velocity **FDCS very sensitive to details of few-body dynamics.**
- Potential problems with **perturbative** methods:
  - a) capture not included
  - b) 3C wavefunction not accurate when all particles close
  - c) projectile coherence not realistically described
- What is needed: **non-perturbative calculations** with two-center basis set and wave packet describing projectile.

# SBA-2C:

Black: FBA

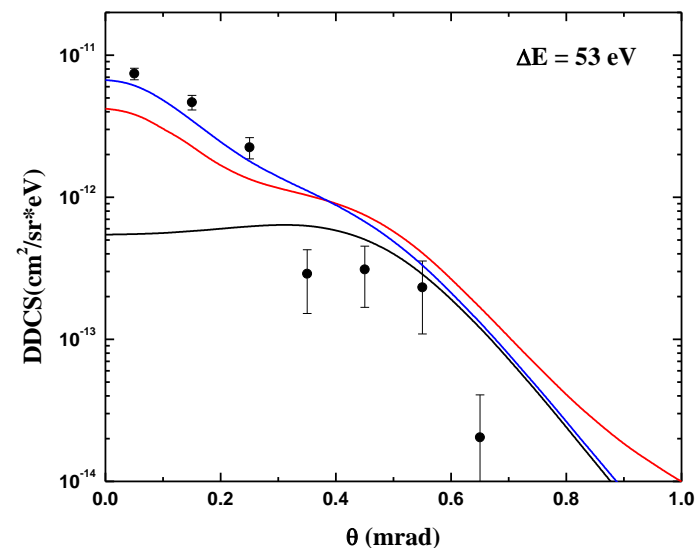
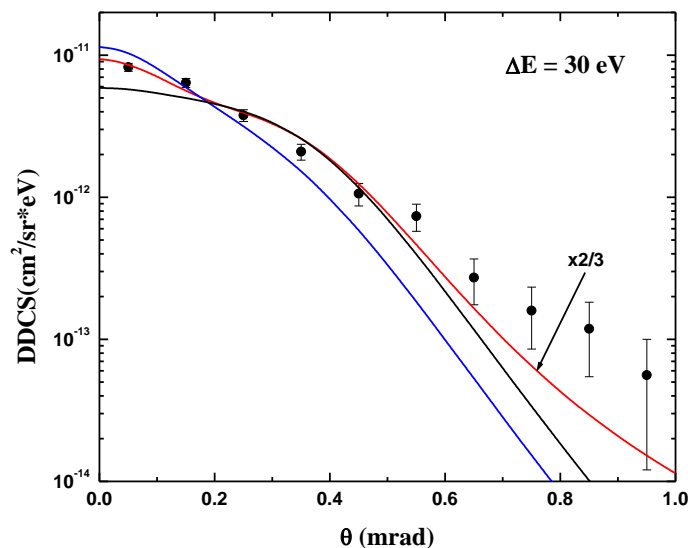
no PCI

Blue:

only PE-ET-PE

Red: PE-ET-PE

and PE-PT-PE



$\Rightarrow$  PE – ET – PE sequence dominant PCI channel in SBA-2C

# CDW-EIS:

Black: FBA

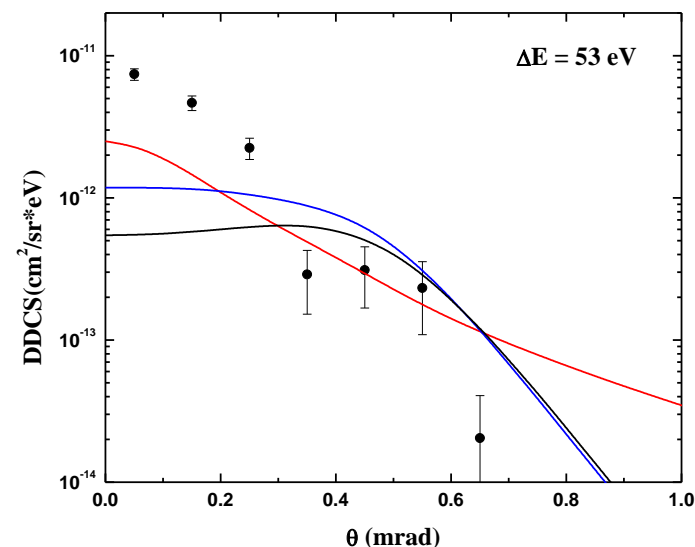
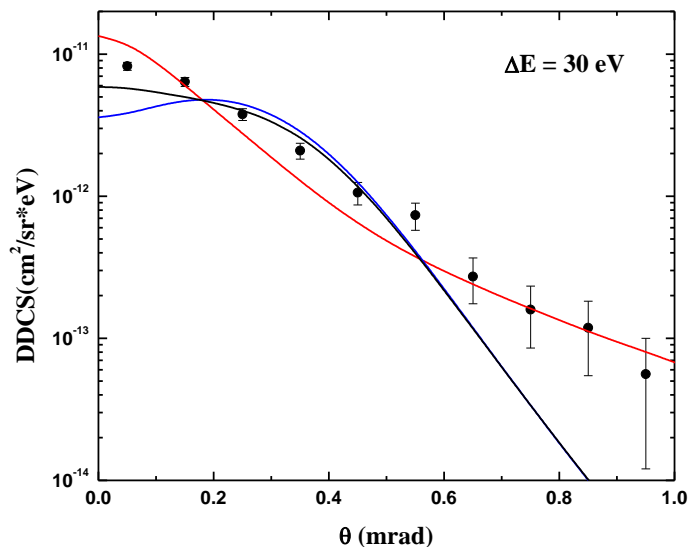
no PCI

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Red: PE-ET-PE

and PE-PT-PE



$\Rightarrow$  PE – PT – PE sequence dominant PCI channel in CDW-EIS