

**Short range nucleon correlations
studied with electron and photon probes**

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Short range nucleon correlations studied with electron and photon probes

- ◆ Introduction: Why short range correlations are important
- ◆ Low energy (γ, pN) experiments at Mainz
- ◆ High energy (e, e') experiments at Jefferson Lab
- ◆ Exclusive 3-nucleon knockout experiments
- ◆ Summary and conclusions

This talk will give a selective overview of investigations of few-body nucleon interactions using electromagnetic probes, with an emphasis on experiments carried out at Mainz and Jefferson Lab in the A2, CLAS and CLAS12 collaborations.

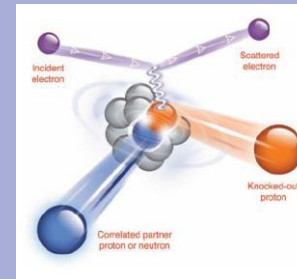
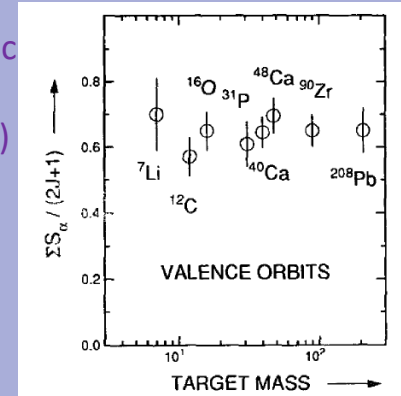
SRC and electromagnetic interactions

- **1N** knockout reactions
 - ⇒ missing single particle strength observed in (e,e'p) reactions
 - ⇒ Attributed to **2N** correlations

- ⇒ Investigate with **2N** knockout reactions
- ⇒ Residual nucleus is spectator
- ⇒ Look for strength at high p_m , corresponding to short **NN** separations

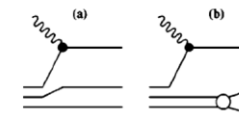
- ⇒ **3N** correlations take this a stage further.
- ⇒ Energy and momentum given to three nucleons.
- ⇒ Expect effects at even higher p_m , higher excitation energies and even shorter distances
- ⇒ Expect magnitude of **3N** effects to be small (~10% **2N** strength)
- ⇒ Enhance with kinematic selection
- ⇒ Information on nuclear physics at high nucleon densities (cold dense nuclear matter).

Missing Spectroscopic Strength, Lapikas, NPA 553 (1993) 297c)

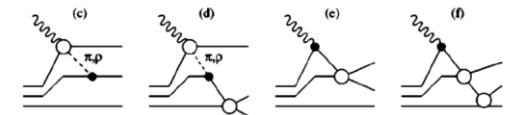


2N knockout reactions, Subedi et al, Science 1476 (2008) 8

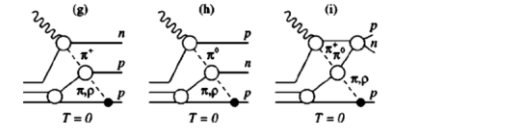
1N



2N



3N



Laget calculations of **1N**, **2N** and **3N** mechanisms, Nicolai et al, PRC 70 (2004) 064003

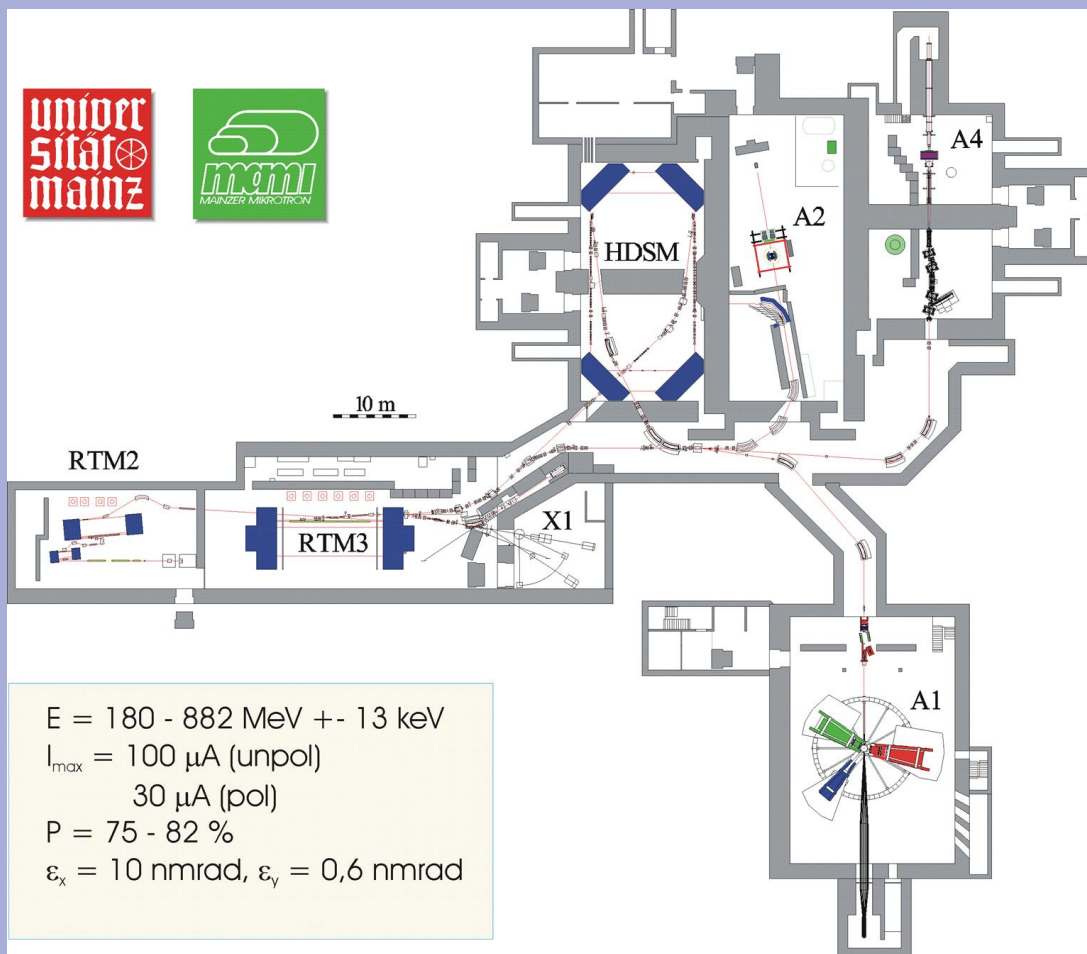
The MAMI Racetrack Microtron Facility at Mainz



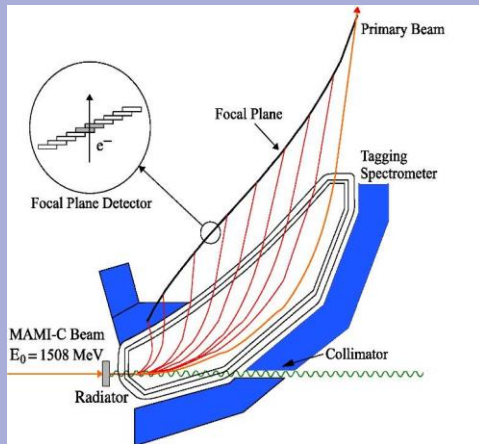
A2 (Real Photon) Collaboration



RTM3



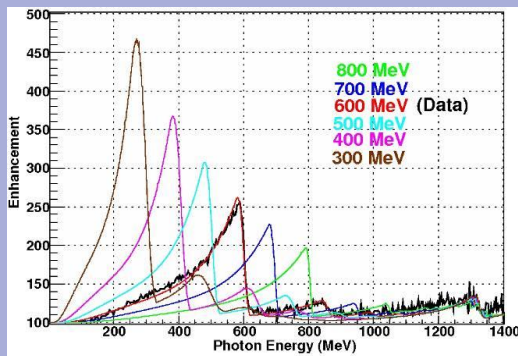
Glasgow Tagged Photon Spectrometer



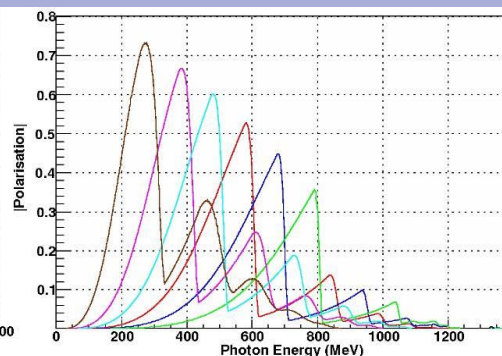
- ◆ Photon Energy: $E_\gamma = E_e - E_{e'}$
- ◆ Resolution: 2-4 MeV
- ◆ Circ. pol. γ from long. pol. e^- (up to 85%)
- ◆ Lin. pol. γ from diamond radiator (up to 70%)

Glasgow Tagged Photon Spectrometer
I Anthony et al, NIM 301 (1991) 230

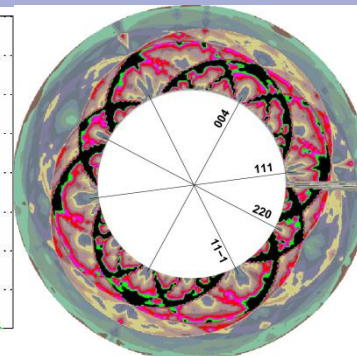
Linear Photon Polarisation from Coherent Bremsstrahlung



Yield Enhancement



Polarisation



Stonehenge crystal alignment technique,
K Livingston,
NIM A 603 (2009) 205

Photon-induced 2N-knockout reactions

At low E_m only 2 nucleons participate, but at higher missing energies contributions from 3N forces are possible.

$^{12}\text{C}(\gamma, pN)$ Reactions at Mainz

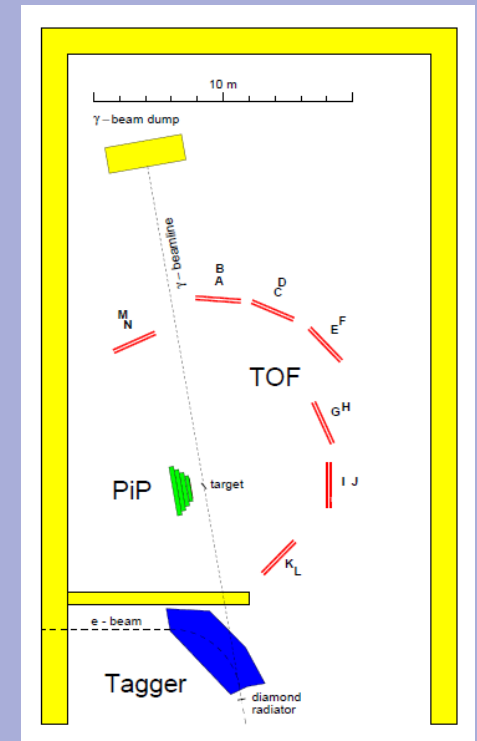
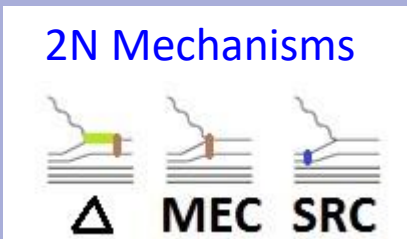
◆ There are many possible contributions to two nucleon knockout e.g. Δ excitation, MEC, 2N SRC, 3N SRC, FSI etc.

◆ Experimentally separate processes can't be distinguished.

Rather, selection of kinematics is used to enhance contribution of particular processes, prior to comparison with models.

◆ $^{12}\text{C}(\gamma, pN)$ cross sections measured and compared with predictions of the Valencia Model (VM) Carrasco et al, NPA 570 (1994) 701

◆ The VM simplifies the nuclear many-body problem using a Fermi-gas model and a local density approximation. It incorporates all of the expected major mechanisms and calculates FSI, treating propagation of produced particles semi-classically.



Missing Energy spectra

Lamparter et al, ZPA 355 (1996) 1

◆ At low E_γ $^{12}\text{C}(\gamma, pn)$ has sharp peak at low E_m , indicating only two nucleons involved

◆ At higher E_γ more complex processes involving more nucleons occur at higher E_m

◆ The $^{12}\text{C}(\gamma, pp)$ reaction is a factor of ~ 30 weaker than $^{12}\text{C}(\gamma, pn)$ at low E_m

◆ It has no discernible peak at low E_m , but has a broader distribution, indicating stronger FSI

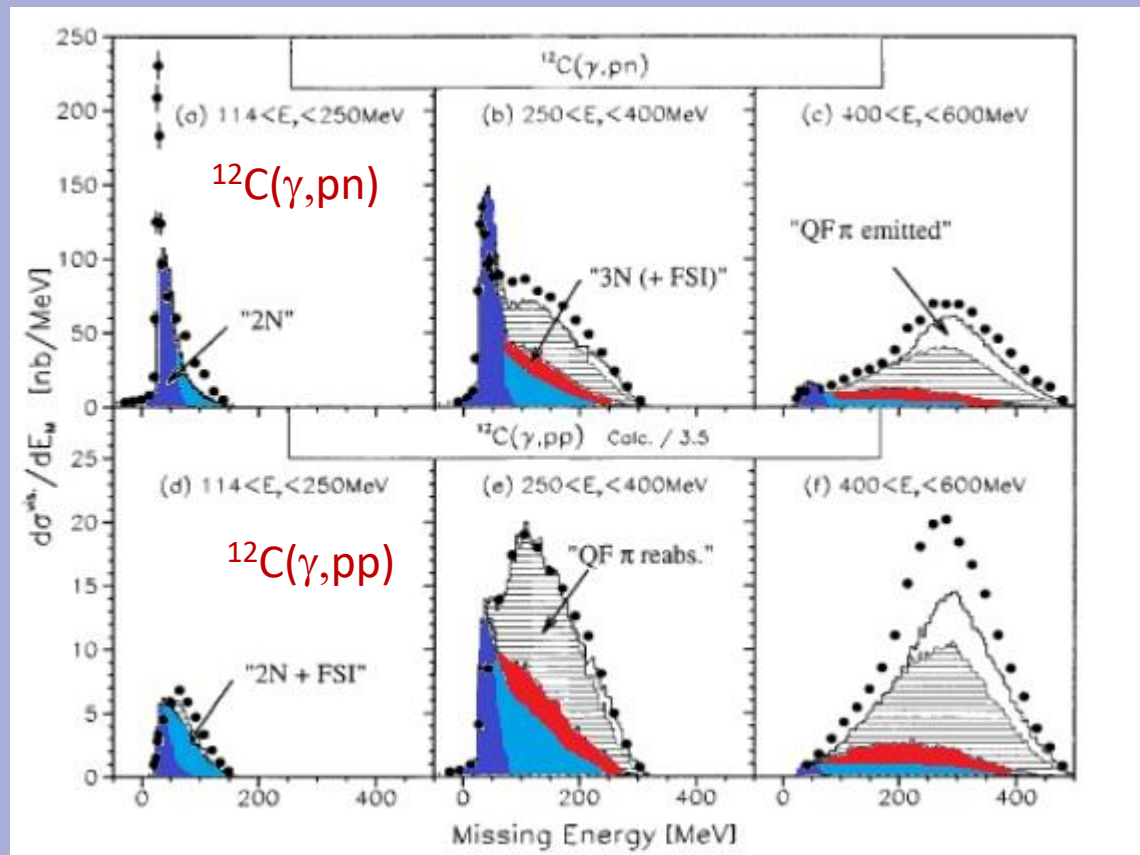


Table 1. Calculated mean multiplicities of nucleons emitted in pn/pp events

E_m /MeV	2N	2N + FSI	3N(+ FSI)	QF π reabs.	QF π emitted	Total
27 - 80	2.0/2.0	2.9/3.0	3.1/3.1	3.2/3.1	- / -	2.2/2.5
100 - 200	- / -	3.6/3.7	3.8/3.9	4.0/4.0	2.1/2.2	3.9/3.9
300 - 500	- / -	4.9/5.0	5.3/5.4	5.8/5.9	3.6/3.8	5.3/5.5
27 - 500	2.0/2.0	3.5/3.6	4.1/4.2	4.8/4.7	3.1/3.3	3.8/4.2

Interpretation

- ◆ The $^{12}\text{C}(\gamma, pn)$ E_m spectra agree reasonably in shape and magnitude with the VM predictions
- ◆ The VM calculations give the correct shape for the $^{12}\text{C}(\gamma, pp)$ E_m spectra but over-predict the strength by a factor 3.5
- ◆ 2N and 2N+FSI processes occur at low E_m
- ◆ 3N and 3N +FSI processes contribute to both channels at $E_m > 60$ MeV and $E_\gamma > 250$ MeV
- ◆ Relative contribution of 3N and 3N + FSI is similar in both channels

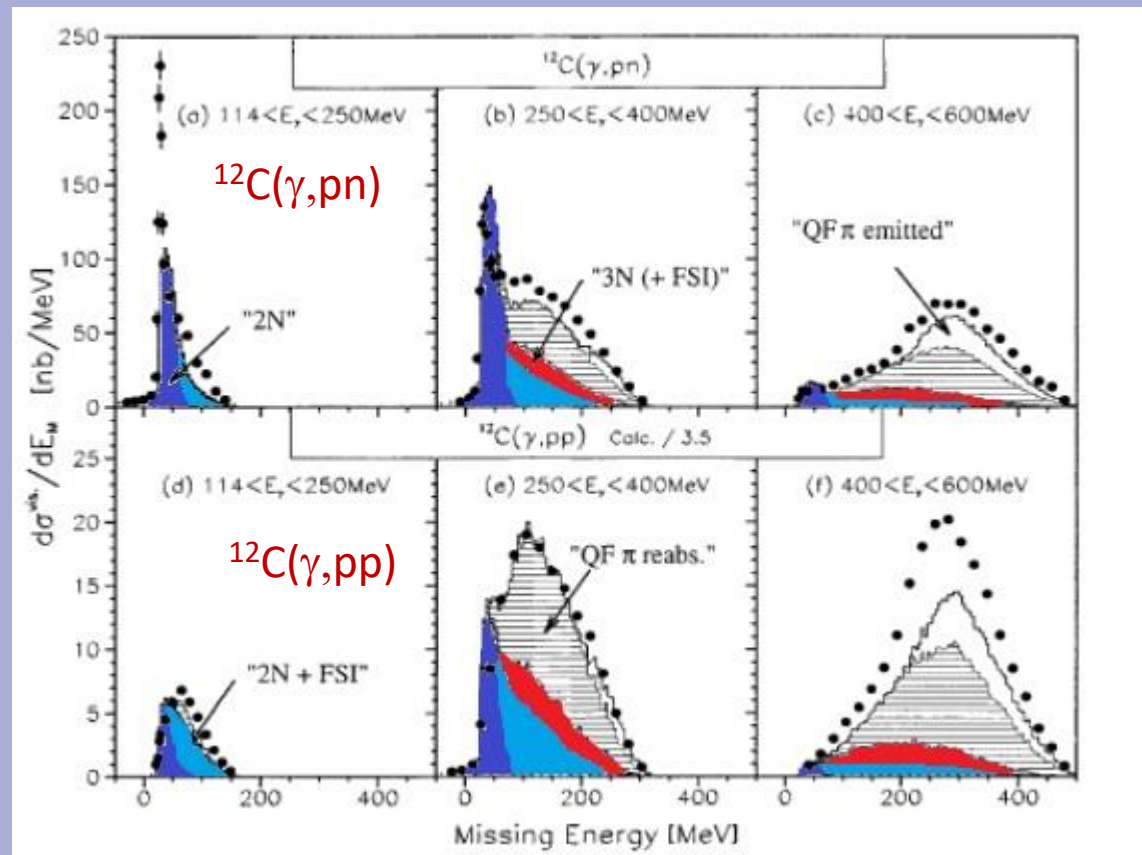
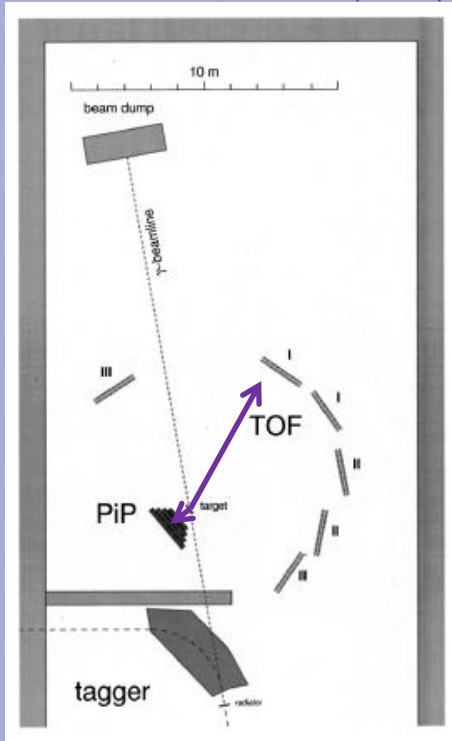


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Variation of kinematics to enhance 3N contributions

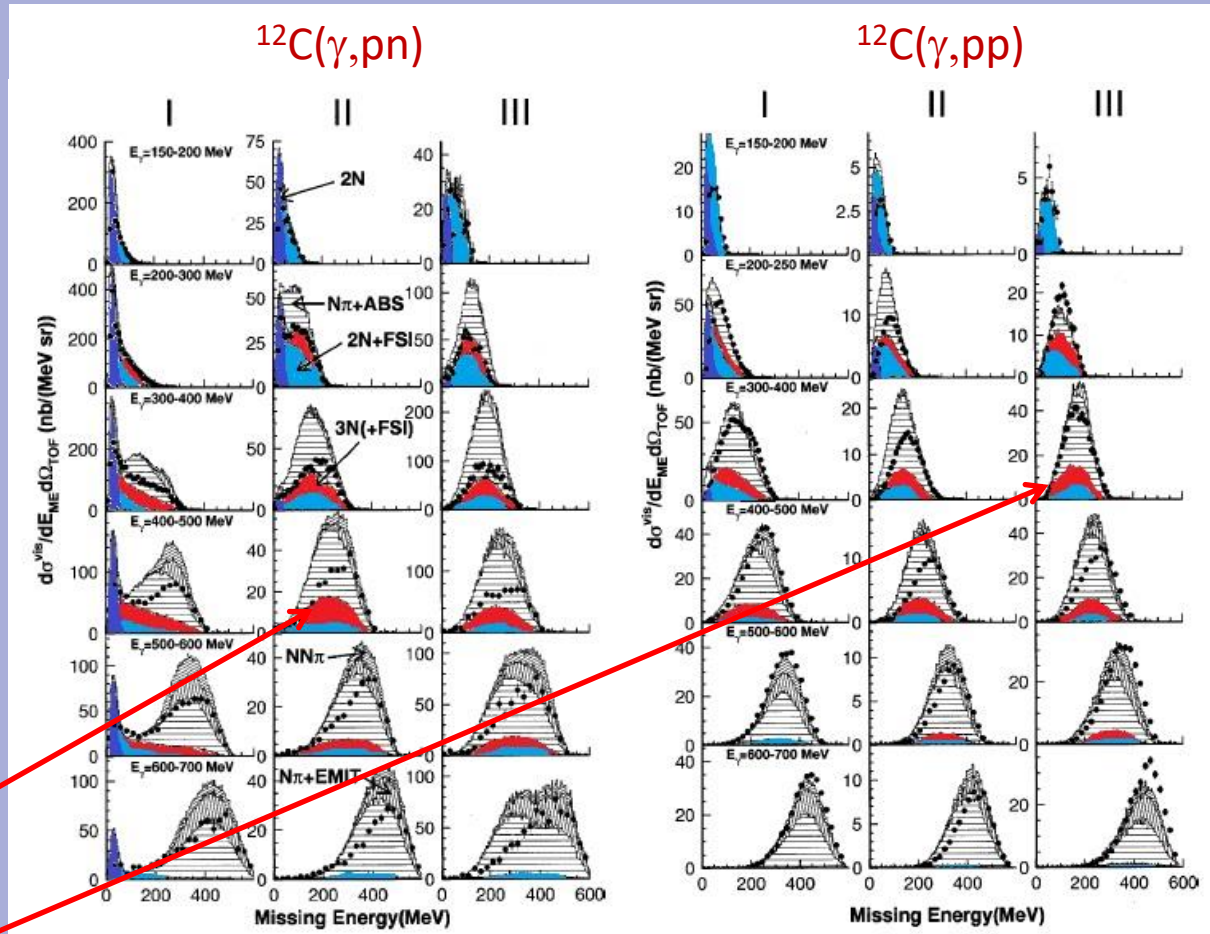
Watts et al, PRC 62 (2000) 014616



Region I: back-to-back,
suppresses 2N FSI

Region II: large opening angles,
enhances 3N

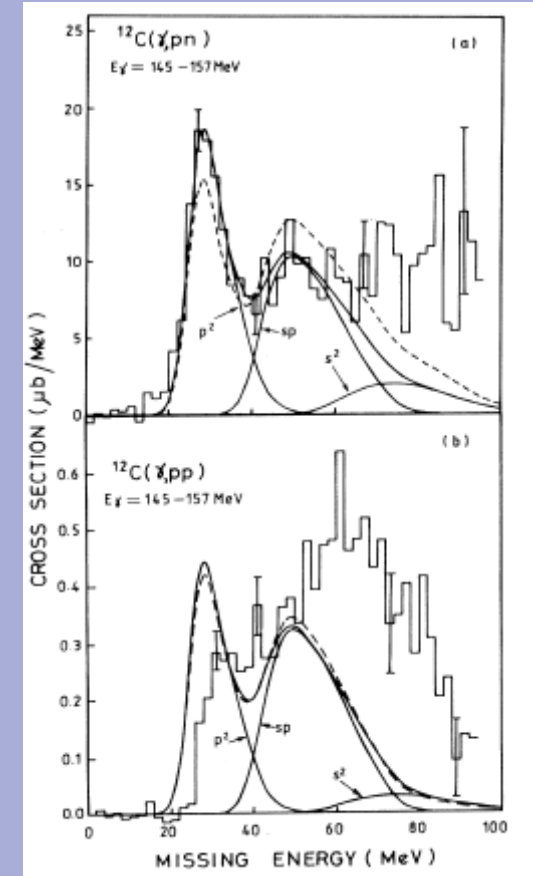
Region III: extreme kinematics, both nucleons on same side of photon beam line,
enhances 3N



$^{12}\text{C}(\gamma, pn)$ Missing Energy

McGeorge et al, PRC 51 (1995) 1967

- ◆ E_m spectra modelled by folding together two $(e, e'p)$ spectra, together with 7 MeV detector resolution
- ◆ Gives a good account of shape of E_m spectra for $^{12}\text{C}(\gamma, pn)$
- ◆ Strength of $(1p)^2$ and $(1p)(1s)$ emission determined from number of $(1p)^2$ and $(1p)(1s)$ pairs
- ◆ $^{12}\text{C}(\gamma, pp)$ shape not so well reproduced, perhaps suggesting other processes, such as $2N+FSI$ are important
- ◆ For $E_m < 40$ MeV the $^{12}\text{C}(\gamma, pp)$ strength is $<2\%$ of the $^{12}\text{C}(\gamma, pn)$ cross section



Missing Momenta

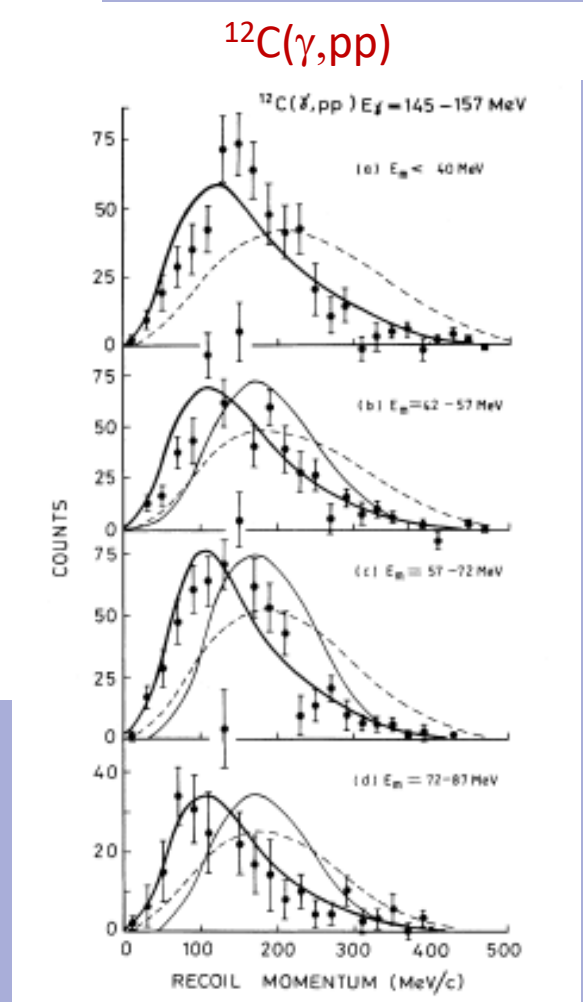
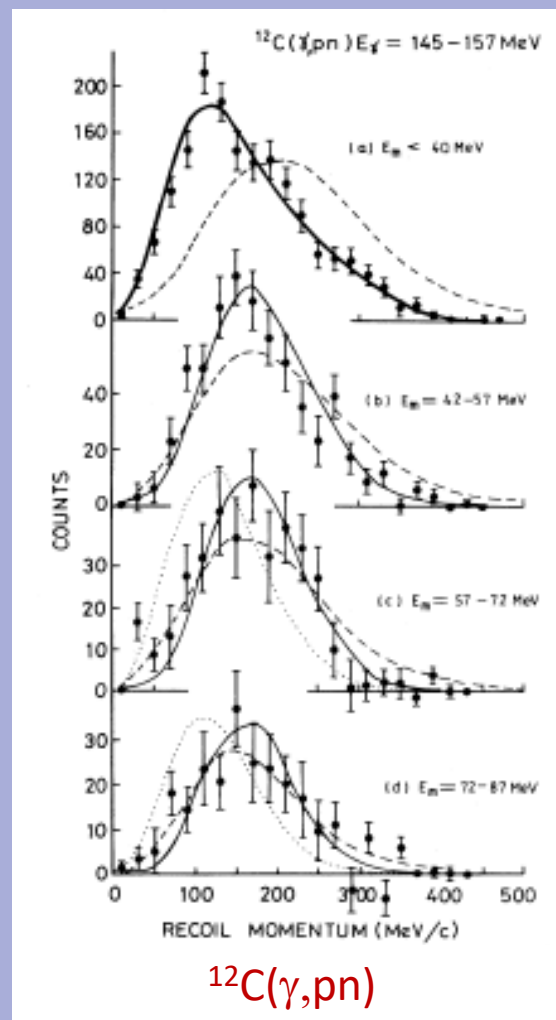
- ◆ The initial pair momentum:

$$P_{\text{pair}} = -P_{\gamma} + P_{N1} + P_{N2}$$

- ◆ For $^{12}\text{C}(\gamma, pn)$ spectrum shape agrees well with simple model folding momentum wavefunctions of two nucleons, for a range of E_m

- ◆ For $^{12}\text{C}(\gamma, pp)$ shapes also agree

- ◆ Confirms both 2-nucleon knockout reactions are described by 2N and 2N+FSI processes



Polarised Photons I

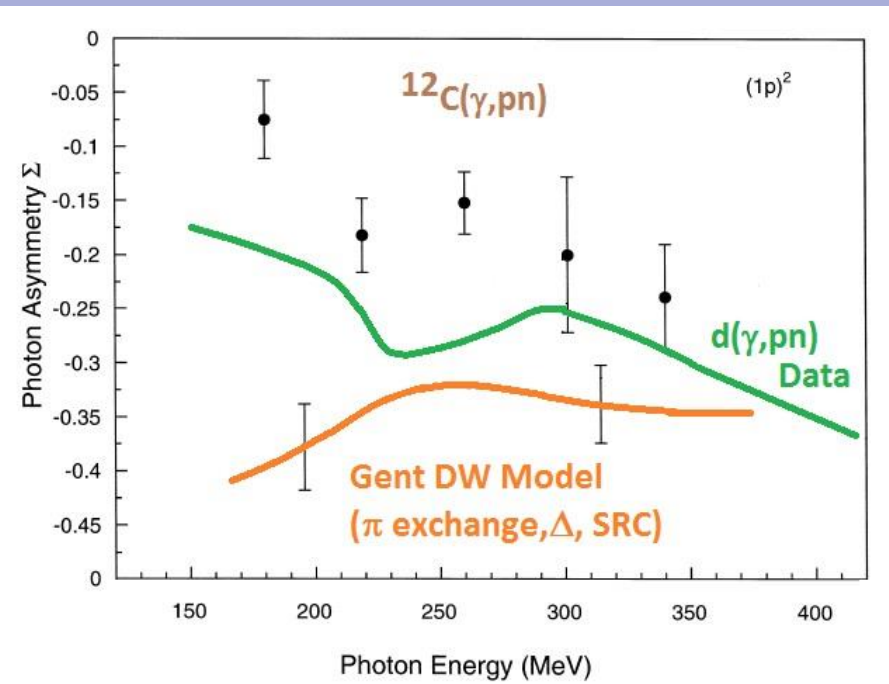
Franczuk et al, PLB 450 (1999) 332

- ◆ The photon asymmetry is defined by

$$\Sigma = \frac{\sigma_{\parallel} - \sigma_{\perp}}{\sigma_{\parallel} + \sigma_{\perp}}$$

where σ_{\parallel} is the cross section parallel to the linearly polarised photon and σ_{\perp} is the perpendicular cross section

- ◆ For $^{12}\text{C}(\gamma, pn)$ Σ for $E_m < 40$ MeV is negative, but not as strong as $d(\gamma, pn)$



- ◆ Comparison with a detailed Gent model, including π -meson in flight, π -seagull, Δ terms and SRC, averaged over our detector acceptance, is a poor fit to the data.
- ◆ Theoretical approximations limit these calculations to photon energies of a few hundred MeV
- ◆ There is a need for improved calculations, before detailed information on the strength of each contributing mechanism can be extracted.

Polarised Photons II

Powrie et al, PRC 64 (2001) 034602

- ◆ The photon asymmetry is defined by

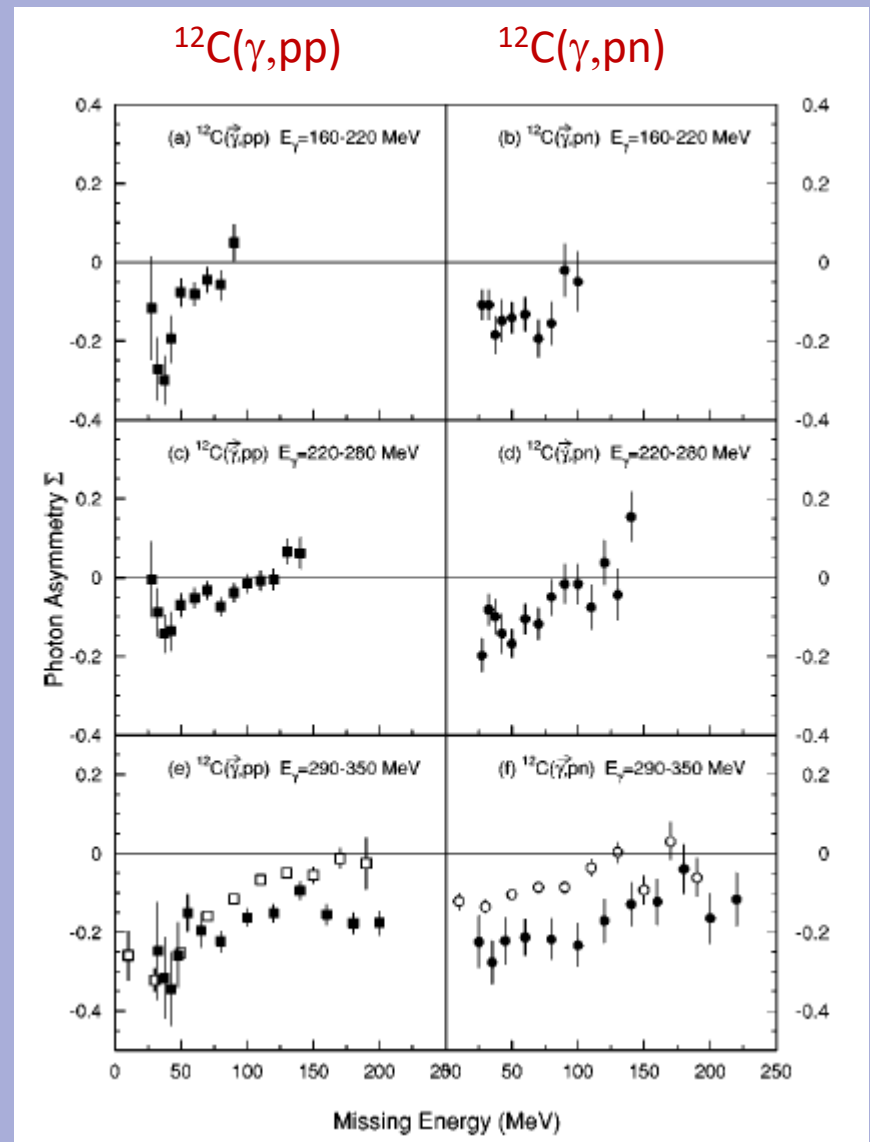
$$\Sigma = \frac{\sigma_{\parallel} - \sigma_{\perp}}{\sigma_{\parallel} + \sigma_{\perp}}$$

where σ_{\parallel} is the cross section parallel to the linearly polarised photon and σ_{\perp} is the perpendicular cross section

- ◆ For $^{12}\text{C}(\gamma,pp)$ Σ shows a strong signal at low E_m

- ◆ This is stronger than for $^{12}\text{C}(\gamma,pn)$ indicating a distinct 2N process (FSI will reduce $|\Sigma|$)

- ◆ Confirms both 2-nucleon knockout reactions are described by 2N and 2N+FSI processes

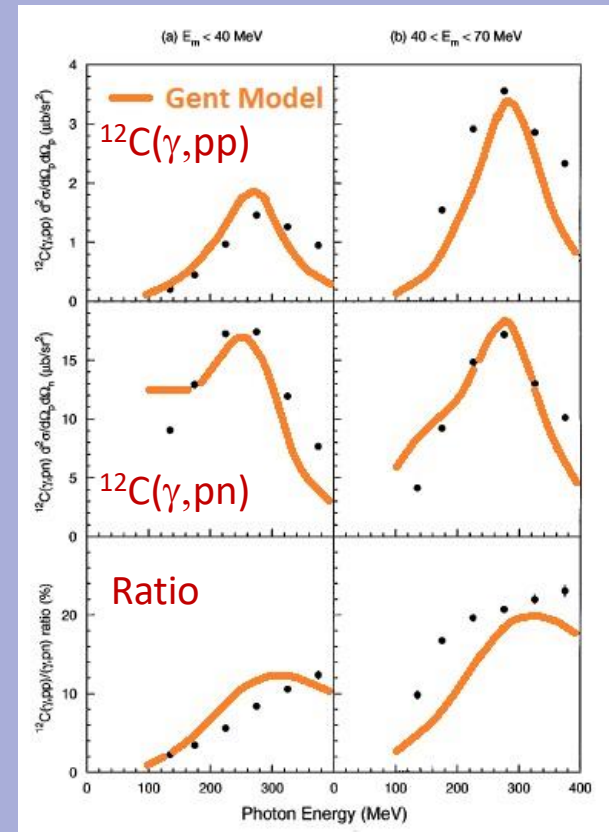
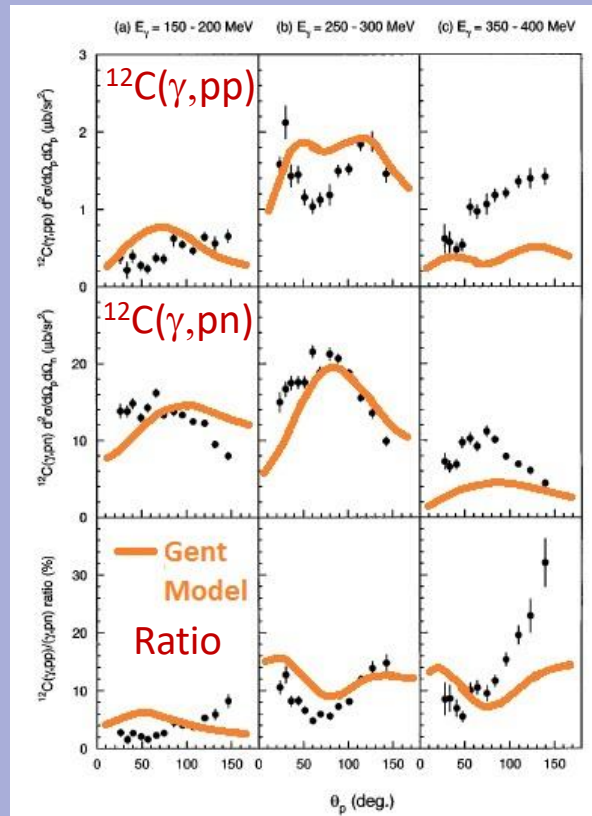


Further studies of 2-nucleon knockout

MacGregor et al, PRL 80 (1998) 245

◆ Further studies of

- i) the E_γ dependence of the 2N cross section
- ii) The $^{12}\text{C}(\gamma,pp)$ to $^{12}\text{C}(\gamma,pn)$ ratio
- iii) The differential cross section



- ◆ Both $^{12}\text{C}(\gamma,pp)$ to $^{12}\text{C}(\gamma,pn)$ cross sections peak in the Δ -resonance region
- ◆ The $^{12}\text{C}(\gamma,pp) / ^{12}\text{C}(\gamma,pn)$ ratio increases strongly with photon energy
- ◆ The angular distributions of both channels are very different and do not agree with Gent Model

Summary of low energy (γ ,pN) reactions

- ◆ Both $^{12}\text{C}(\gamma,\text{pn})$ and (γ,pp) reactions show clear evidence of 2N and $2\text{N} + \text{FSI}$ photon absorption at low E_m . (Similar results seen in other light nuclei: ^4He , ^6Li , ^{16}O)
- ◆ Clean reaction with the rest of the nucleus acting as a spectator
- ◆ There is evidence of a strong Δ -excitation mechanism
- ◆ Comparison of angular distributions with models indicates significant MEC in (γ,pn)
- ◆ The strength of the (γ,pp) reaction is very much less than (γ,pn) and varies with photon energy, emission angle and missing energy
- ◆ Note that (γ,pp) has fewer MEC channels available and has no Tensor contribution
- ◆ The mechanisms have a strong angular variation, which differs between (γ,pn) and (γ,pp)
- ◆ The reactions have a strong photon asymmetry Σ , which is stronger for (γ,pp) than (γ,pn)
- ◆ Exclusive (γ,pN) measurements require comparison with detailed calculations to identify specific contributions from SRC – Current comparisons are not sufficiently good enough for this
- ◆ 3N and other absorption processes occur at higher E_m

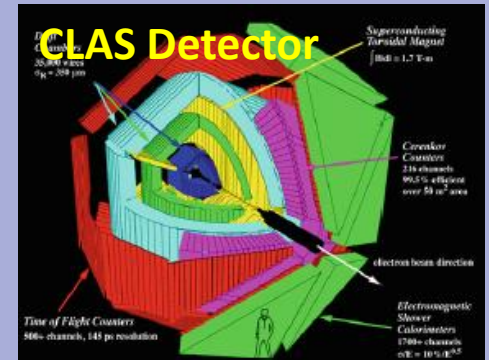
Inclusive (e,e') measurements (CLAS)

Egiyan et al, PRL 96 (2006) 082501

- ◆ Inclusive electron scattering at **high Q^2** and **high x_B** is able to transfer very high energies and momenta to the nucleus
- ◆ The cross section is sensitive to not just **2N** but also **3N** and higher correlations:

$$\sigma_A = A (a_1\sigma_1 + a_2\sigma_2/2 + a_3\sigma_3/3 + \dots)$$

- ◆ σ_j is the cross section for electron interaction with a j-nucleon correlation and a_j is the ratio of the probabilities for a given nucleon to belong to correlation j in nucleus A to correlation j in a nucleus of j nucleons
- ◆ It is expected that interaction with **2N SRC** will dominate for $1 < x_B < 2$ and **3N SRC** for $2 < x_B < 3$
- ◆ As cross sections drop rapidly with x_B , the **key** is *not* to look at the absolute cross sections, but to look at ratios for different nuclei, incorporating the elementary cross sections.



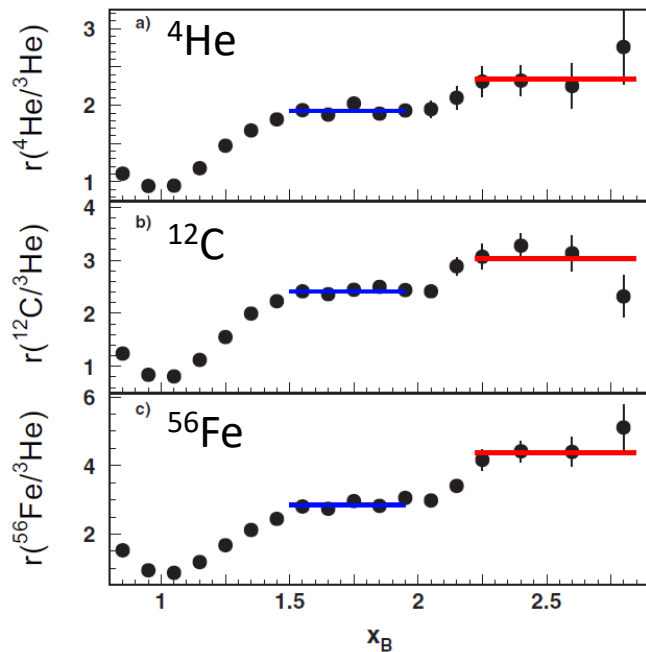


TABLE I. $a_j(A/{}^3\text{He})$ and $a_{jN}(A)$ ($j = 2, 3$) are the per nucleon relative (to ${}^3\text{He}$) and absolute probabilities of (jN) SRC, respectively. Errors shown are statistical and systematic for a_j and are combined (but systematic dominated) for a_{jN} . The systematic uncertainties due to the Coulomb interaction and SRC c.m. motion are not included. For the ${}^{56}\text{Fe}/{}^3\text{He}$ ratio they are expected to be $<2\%$ – 6% and $<20\%$, respectively, and are somewhat smaller for ${}^{12}\text{C}/{}^3\text{He}$ and smaller still for ${}^4\text{He}/{}^3\text{He}$ ratios.

	$a_2(A/{}^3\text{He})$	$a_{2N}(A)$ (%)	$a_3(A/{}^3\text{He})$	$a_{3N}(A)$ (%)
${}^3\text{He}$	1	8.0 ± 1.6	1	0.18 ± 0.06
${}^4\text{He}$	$1.93 \pm 0.02 \pm 0.14$	15.4 ± 3.3	$2.33 \pm 0.12 \pm 0.19$	0.42 ± 0.14
${}^{12}\text{C}$	$2.41 \pm 0.02 \pm 0.17$	19.3 ± 4.1	$3.05 \pm 0.14 \pm 0.21$	0.55 ± 0.17
${}^{56}\text{Fe}$	$2.83 \pm 0.03 \pm 0.18$	22.7 ± 4.7	$4.38 \pm 0.19 \pm 0.33$	0.79 ± 0.25

Observed ratios

Per nucleon probabilities

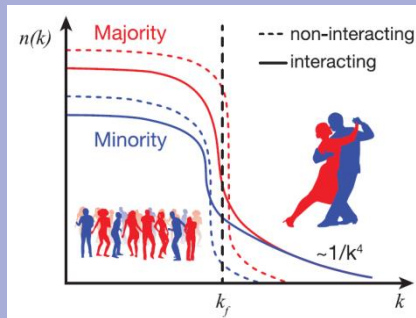
- ◆ Ratios of cross sections plotted for ${}^4\text{He}/{}^3\text{He}$, ${}^{12}\text{C}/{}^3\text{He}$ and ${}^{56}\text{Fe}/{}^3\text{He}$
- ◆ In each cases plateaus are seen for $1.5 < x_B < 2.0$ and $2.3 < x_B < 2.6$, although statistics become poorer at high x_B
- ◆ The lower x_B region is an indication of the universality of **2N** correlations and the higher x_B region is a signal of **3N** correlations

High Momentum Protons and Neutrons

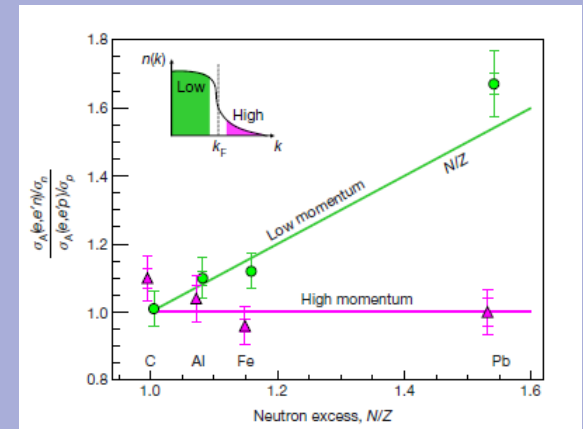
Hen et al, Science 436 (2014) 614, CLAS

Duer et al, Nature 560 (2018) 617, CLAS

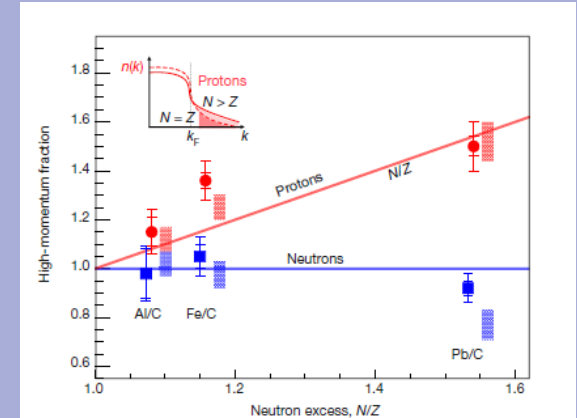
- ◆ SRC produce high momentum nucleons and the interaction between np pairs is stronger than between pp or nn pairs.
- ◆ How does this affect momentum distribution of protons and neutrons in heavy nuclei, such as Pb?
- ◆ Due to the neutron excess, on average each proton undergoes more SRC than the average neutron



- ◆ In a dancing analogy, the protons get more dances, and a greater fraction end up with high momenta
- ◆ Confirmed by $(e,e'p)$ and $(e,e'n)$ cross section measurements measured in CLAS data mining experiments



- ◆ In Pb there are fewer high momentum neutrons than low momentum neutrons.



- ◆ In Pb there are fewer high momentum neutrons than high momentum protons

SRC possible connection to EMC?

Smookler et al, Nature 566 (2019) 354, CLAS

- ◆ Neutrons and protons are composite objects
- ◆ Deep Inelastic Scattering (DIS) probes internal quark structure
- ◆ DIS cross sections are larger in heavy nuclei than in light nuclei
- ◆ i.e. The distributions of quark properties is affected by the nuclear environment (EMC effect)
 - ◆ SRC enhance the high momentum components of nucleons
 - ◆ In particular, proton high momentum fraction is increased in heavy nuclei
 - ◆ Could SRC affect the internal structure of nucleons?
 - ◆ Measure DIS and quasi-elastic cross sections simultaneously at CLAS

SRC possible connection to EMC?

Smookler et al, Nature 566 (2019) 354

- ◆ EMC effect is measured by slope of ratio of per nucleon F_2 structure function in nucleus A to F_2 in deuterium
- ◆ Write F_2^A in terms of interaction with uncorrelated protons and neutrons and with SRC pairs

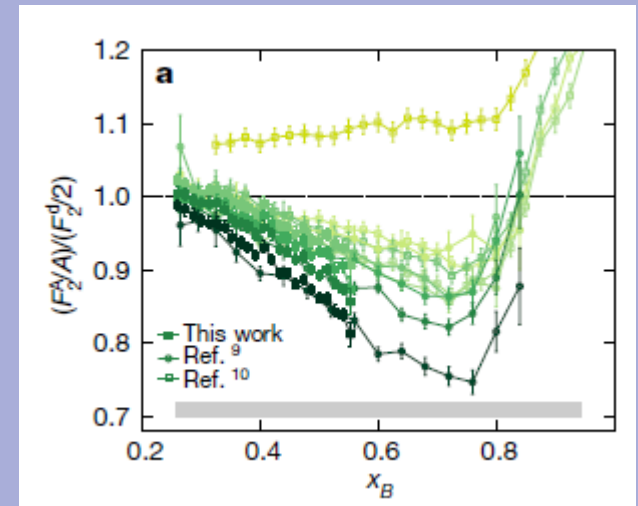
$$F_2^A = (Z - n_{\text{SRC}}^A) F_2^p + (N - n_{\text{SRC}}^A) F_2^n + n_{\text{SRC}}^A (F_2^{p*} + F_2^{n*})$$

- ◆ F_2^n is obtained from deuterium $F_2^d - F_2^p - n_{\text{SRC}}^d (\Delta F_2^p + \Delta F_2^n)$

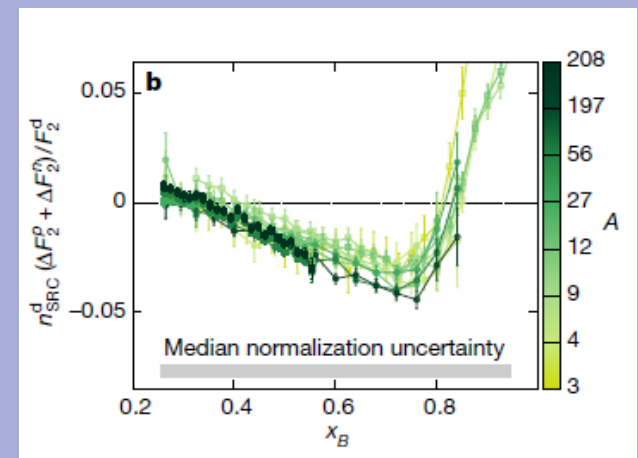
- ◆ This allows a nucleus-independent ratio to be extracted

$$\frac{n_{\text{SRC}}^d (\Delta F_2^p + \Delta F_2^n)}{F_2^d} = \frac{\frac{F_2^A}{F_2^d} - (Z - N) \frac{F_2^p}{F_2^d} - N}{(A/2) a_2 - N}$$

- ◆ The universality of the response strongly suggests a connection between SRC and the EMC effect in nuclei



EMC Effect: Uncorrected slope of $(F_2^A/A) / (F_2^D/2)$ for range of nuclei



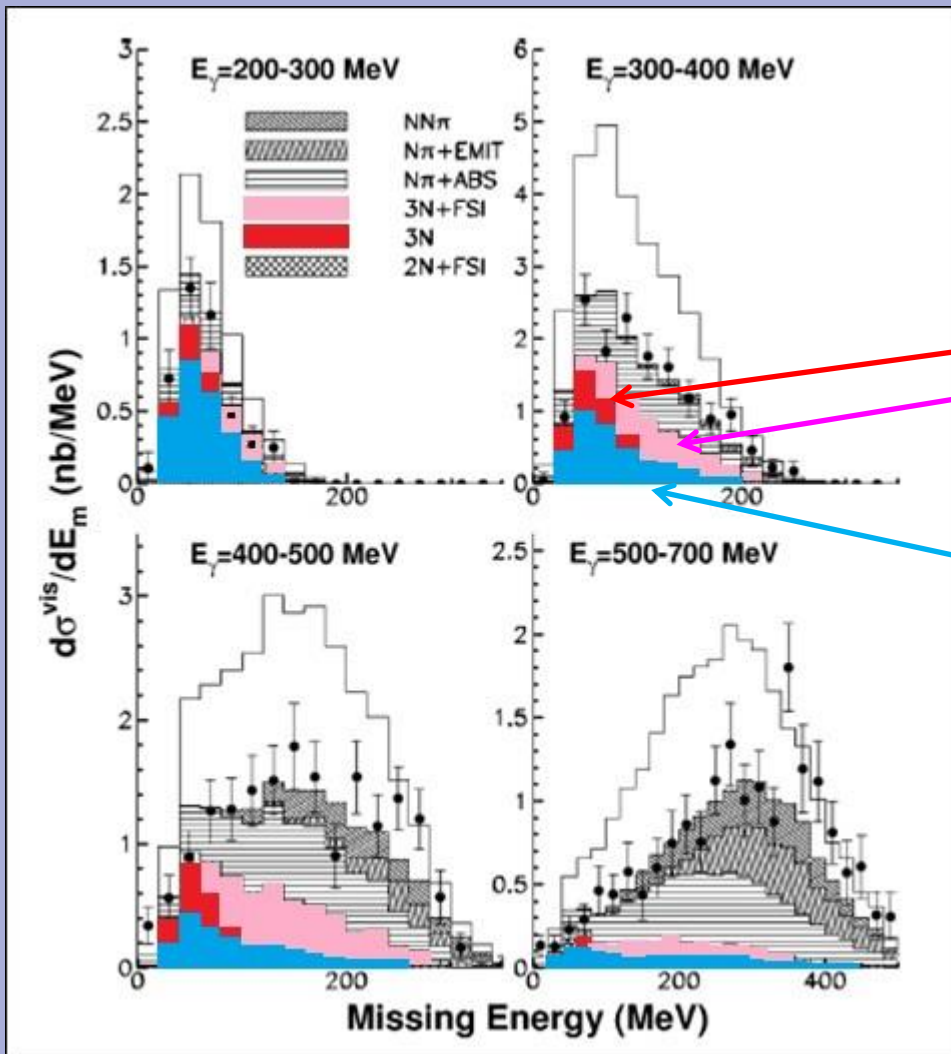
Universal ratio $n_{\text{SRC}}^d (\Delta F_2^p + \Delta F_2^n) / F_2^d$ for same range of nuclei

Summary of high energy (e,e') measurements

- ◆ Inclusive (e,e') experiments at high Q and high x_B transfer large quantities of energy and momentum to the nucleus
- ◆ Virtual photons are absorbed on single nucleons as well as correlated **2N pairs** and **3N triples**
- ◆ JLab data show strong evidence of **2N SRC** and **3N SRC** in both light and heavy nuclei
- ◆ Studies of the isospin dependence show that the neutron excess in heavy nuclei results in the protons having a larger high-momentum fraction than the neutrons
- ◆ Recent work has suggested a connection between SRC and the EMC effect

$^{12}\text{C}(\gamma, \text{ppn})$ experiments at Mainz

Watts *et al.* PLB 553 (2003) 25



◆ 3-nucleon knockout is a natural reaction to investigate **3N** forces

◆ Use VM to identify the processes

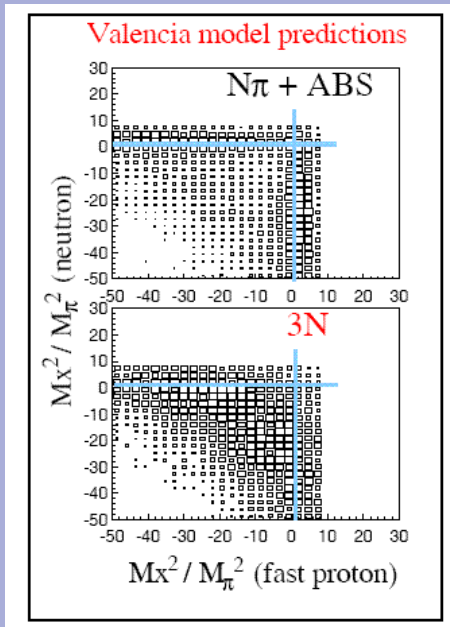
◆ **3N** and **3N+FSI** are small part of cross section

◆ There are also contributions from **2N+FSI**, $N\pi + \pi\text{ABS}$, etc

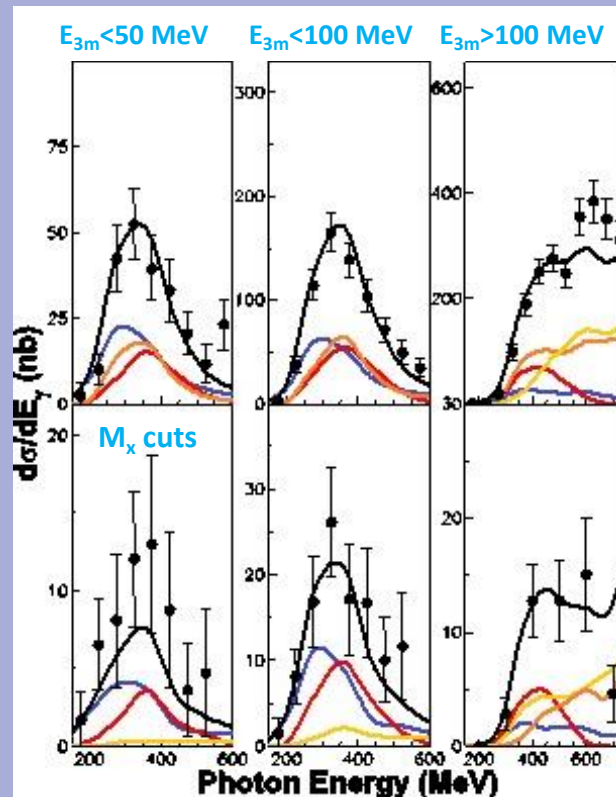
◆ **3N** strength concentrated at low missing energy $E_{3m} < 100$ MeV

◆ **3N+FSI** extends to higher E_{3m}

$^{12}\text{C}(\gamma,ppn)$ Kinematic selection to enhance **3N** contribution



- ◆ Cut $E_{3m} < 100$ MeV enhances **3N (+FSI)** contribution
- ◆ For $\gamma + N \rightarrow N + X$ process, followed by absorption of X on two more nucleons, $M_X^2 = (E_\gamma + m_N - E_N)^2 - (\mathbf{p}_\gamma - \mathbf{p}_N)^2$
- ◆ Cut on invariant mass $(M_X / M_\pi)^2 < -1.5$ to suppress **$N\pi + \pi\text{ABS}$**
- ◆ Can find regions where **3N (+FSI)** contributes $\sim 40\%$ of total strength.

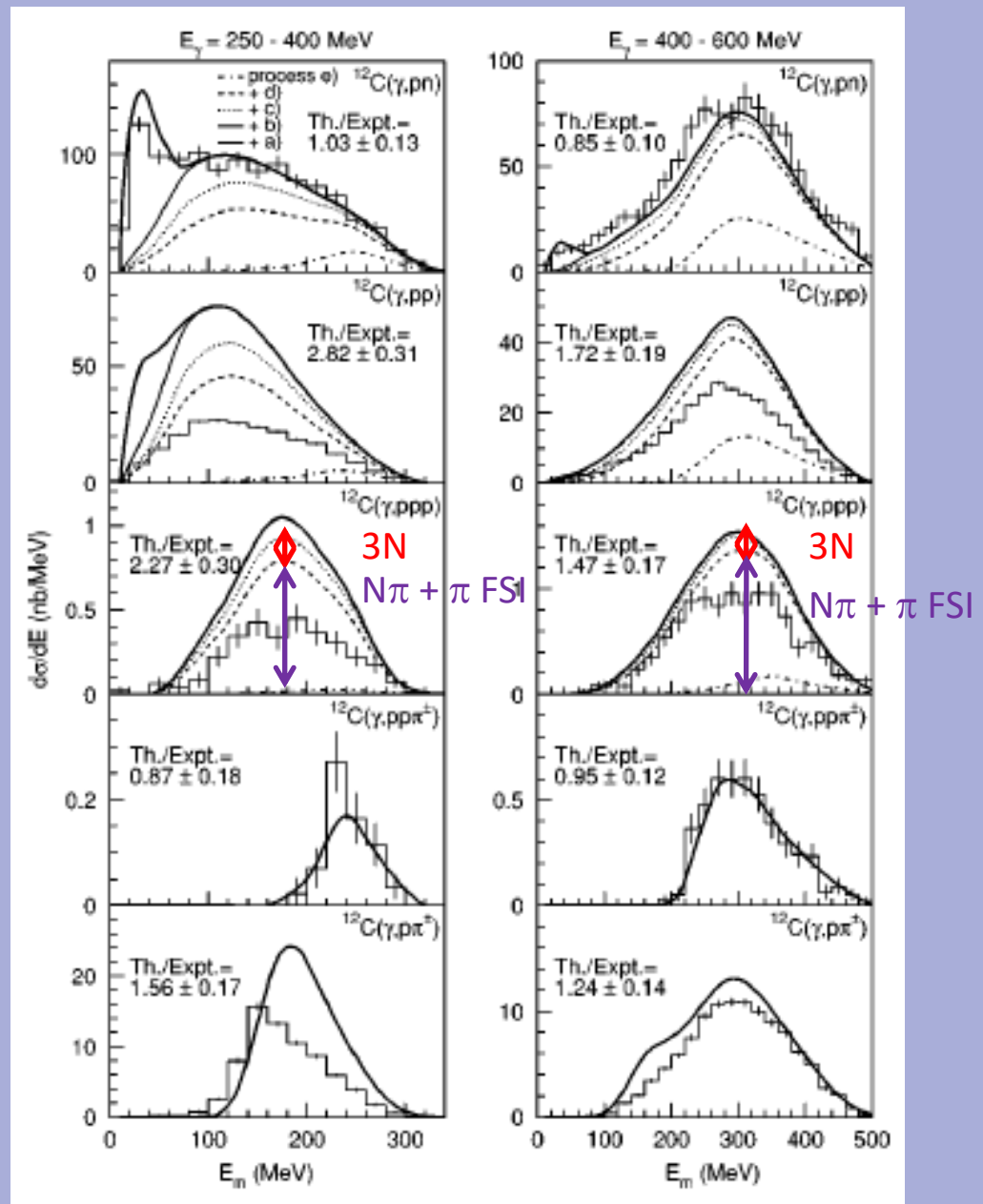


- VM total
- 3N (+FSI)
- 2N (+FSI)
- $N\pi + \pi\text{ABS (reduced)}$
- $N\pi = \pi\text{EMIT}$

$^{12}\text{C}(\gamma, \text{ppp})$ reaction

Harty et al, PRC 57 (1998) 123

- ◆ Study of 3-nucleon final states in $^{12}\text{C}(\gamma, \text{ppp})$ reaction
- ◆ E_m spectra to VM
- ◆ VM gets shapes right but not absolute magnitude
- ◆ 3N contribution is significant, but not the dominant process
- ◆ Pion production + reabsorption $N\pi + \pi$ FSI is much larger



$^{12}\text{C}(\gamma, \text{pd})$ Reaction at Mainz

McAllister et al, PRC 60 (1999) 0044610

Watts et al, PLB 647 (2007) 88

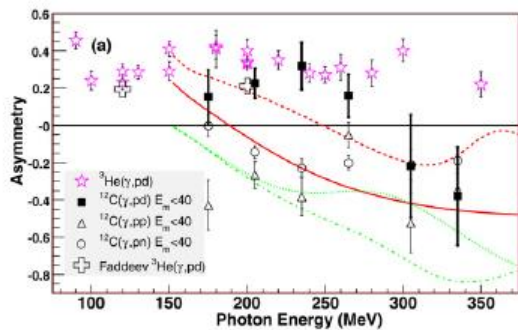
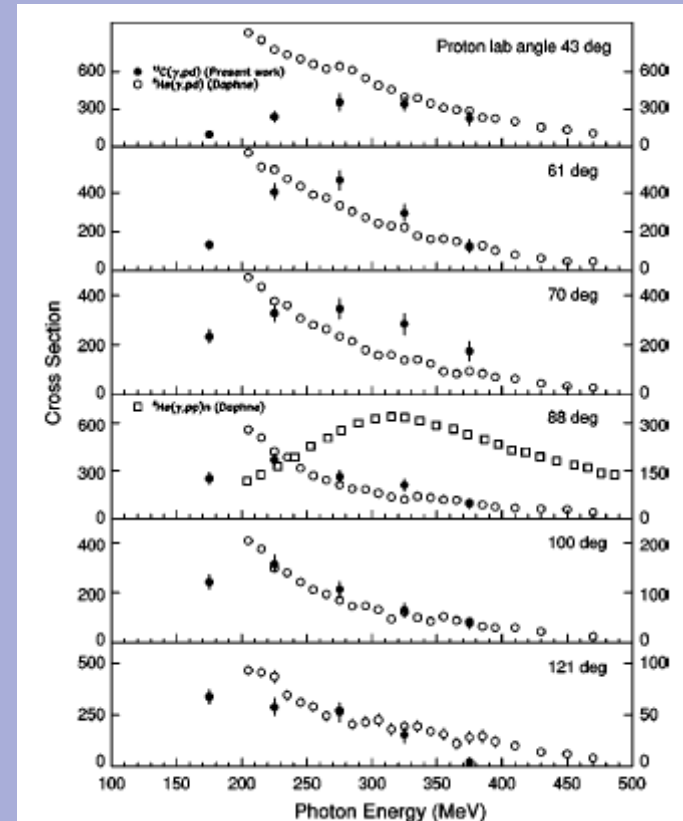
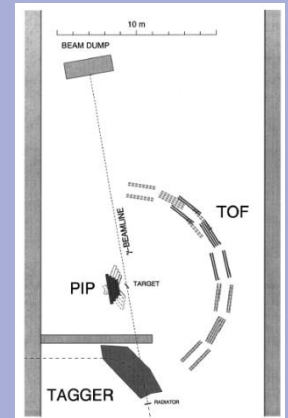
Reaction measured in back-to-back kinematics in three settings covering forward, central and backward proton angles

Comparison of $^{12}\text{C}(\gamma, \text{pd})$ and $^3\text{He}(\gamma, \text{pd})$

The photon energy dependence of the $^{12}\text{C}(\gamma, \text{pd})$ cross section For $E_m < 44$ MeV is compared to that from $^3\text{He}(\gamma, \text{pd})$

Above 300 MeV both have a similar shape with no influence from the Δ -resonance.

There are further similarities between both reactions when the photon asymmetry is considered.



Black squares: $^{12}\text{C}(\gamma, \text{pd})$ for $E_m < 40$ MeV

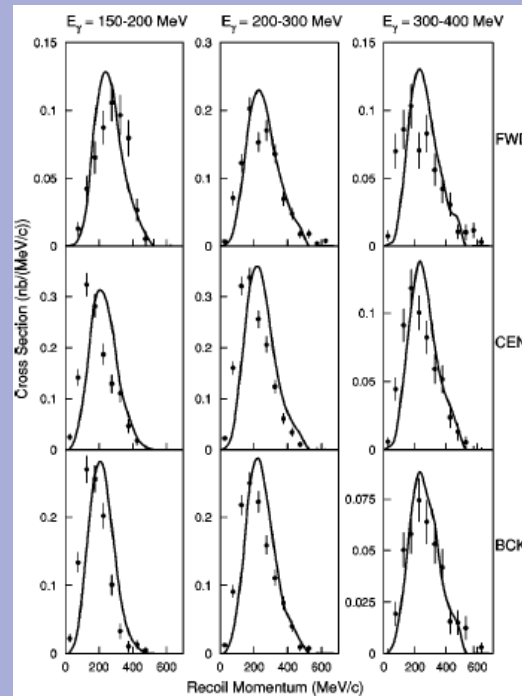
Pink stars: $^3\text{He}(\gamma, \text{pd})$

Belyaev et al, JETP Lett. 40 (1984) 1275

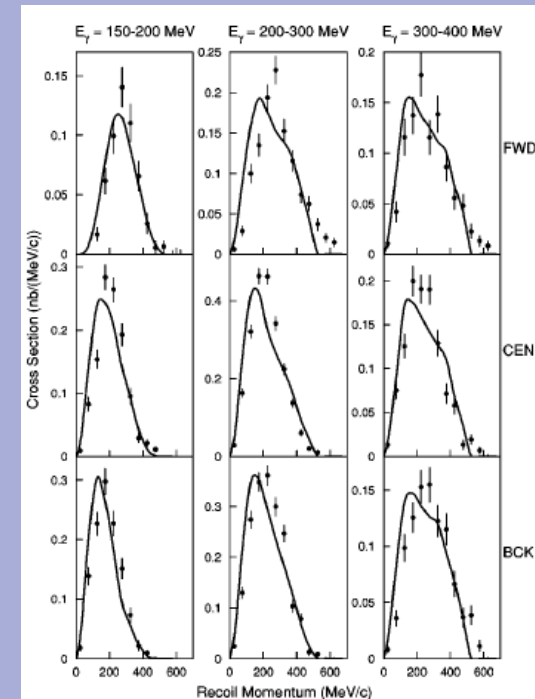
Recoil momentum distributions

- ◆ Data are split into two E_m regions $E_m < 44$ MeV and $44 < E_m < 70$ MeV
- ◆ Distributions are compared with a **3 nucleon plus spectator model** folding together 3 Elton-Swift nucleon wavefunctions in a relative S state.
- ◆ Data agree surprisingly well with calculations and support interpretation of 3 active nucleons.
- ◆ However, this is not a theoretical calculation of **3N** processes

$E_m < 44$ MeV



$44 < E_m < 70$ MeV



Summary and Conclusions I

- ◆ Electromagnetically induced 2- and 3-nucleon knockout reactions have contributions from many processes, including **2N**, **2N+FSI**, **3N**, and **3N+FSI**
- ◆ **2N** mechanisms occur at low E_m in both (γ, pn) and (γ, pp) reactions, with FSI extending strength to higher E_m
- ◆ **2N** mechanisms include Δ -excitation, MEC as well as SRC
- ◆ Kinematic selection can enhance the **2N** contribution, but cannot experimentally separate SRC from Δ -excitation and MEC
- ◆ Strength of each component can only be deduced by comparison with theoretical models
- ◆ State-of-the-art calculations are needed to compare with each experiment, but have to be filtered through the detector acceptances

Summary and Conclusions II

- ◆ **3N** interactions tend to take place at somewhat shorter ranges than **2N** processes due to the involvement of an additional nucleon
- ◆ **3N** and **3N+FSI** occur in (γ, pn) and (γ, pp) reactions at high E_m
- ◆ **3N** processes also occur at low E_m in 3-nucleon knockout reactions
- ◆ Kinematic selection can be used in each reaction to enhance the relative **3N** contribution
- ◆ However, **3N** and **3N+FSI** processes generally remain a small part of the cross section
- ◆ Estimating the strength of each component requires comparison with detailed theoretical models

Summary and Conclusions III

- ◆ Inclusive (e,e') experiments at high Q and high x_B transfer large quantities of energy and momentum to the nucleus
- ◆ Virtual photons are absorbed on single nucleons as well as correlated **2N pairs** and **3N triples**
- ◆ JLab data show strong evidence of **2N SRC** and **3N SRC** in a range of light and heavy nuclei
- ◆ Studies of the isospin dependence show that the neutron excess in heavy nuclei results in the protons having a larger high-momentum fraction than the neutrons
- ◆ Recent work has also suggested a connection between SRC and the EMC effect

Acknowledgements

- ◆ The work reported in this talk is the output of efforts made by many colleagues, past and present, over a large number of years
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