

Few-Nucleon System Dynamics Studied

via

Deuteron-Deuteron Collisions at 160 MeV



Outline:

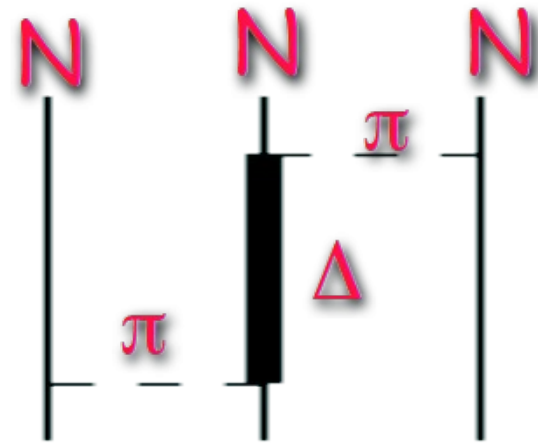
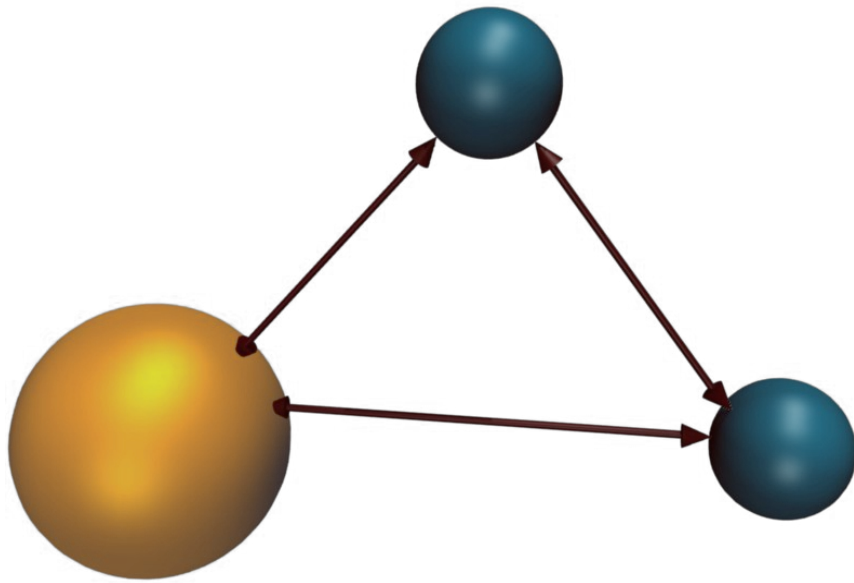
1. Goals and motivations,
2. 3N systems question marks,
3. 4N systems - theory,
4. Experiment dd@ 160 MeV (BINA@ KVI) and results on elastic scattering, proton transfer and breakup,
5. Outlook: dd@ 350MeV (WASA@ COSY).

Motivations

- Tremendous progress in the solution of numerical exact *ab initio* calculations of observables involving 4N reactions, below and above breakup threshold,
- Studies of 4N systems are much more difficult from the computational point of view than 3N,
- **Challenges**: a number of resonances (in the low energy region), many input and output channels, isospin dependence, ...
- Higher sensitivity to 3NF effects, “rich” structure of 4N observables (maxima and minima) important for testing interaction models,
- **Recent accurate calculations** for $p\text{-}^3\text{He}$ and $n\text{-}^3\text{H}$ (AGS, FY, HH),
- Complete knowledge of the 3N interaction

Very few datasets exist to test recent calculations, especially for breakup: @ 130, 160 MeV (KVI Groningen), better situation for transfer channels and elastic scattering

Additional Part of the System Dynamics: **3N Force**



Fujita-Miyazawa 3NF

Prog. Theor. Phys. 17(1957) 360

$$H = -\sum_{i=1}^3 \frac{\hbar^2}{2m_i} + \sum_{i>j=1}^3 v_{ij} + V$$

3NF models

2NF input:

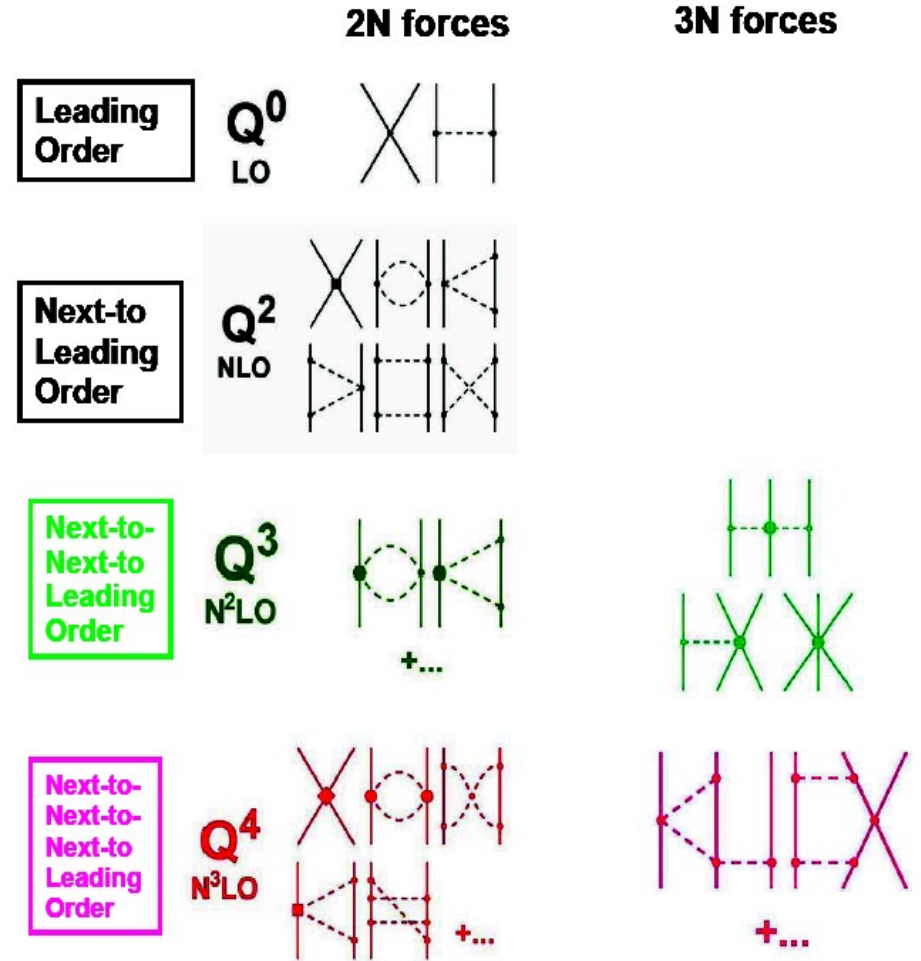
- × CD Bonn
- × Argonne V18
- × Nijmegen I, II
- ×



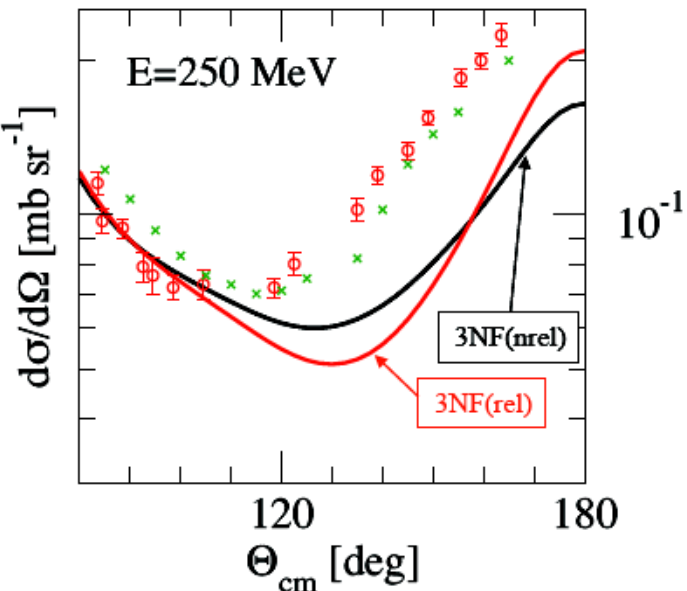
3NF input:

- × Tucson-Melbourne TM99
- × Urbana IX
- ×

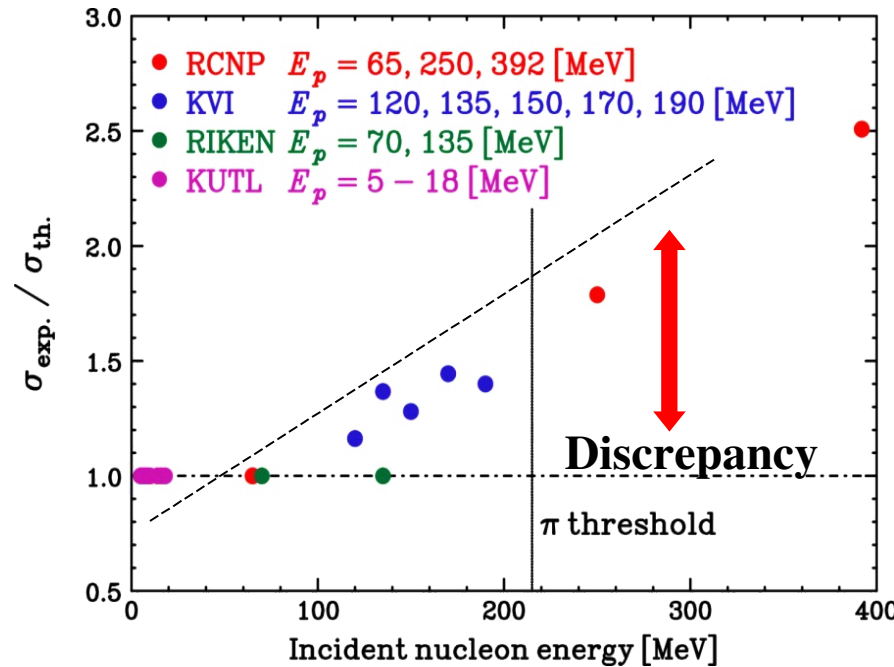
Chiral Forces



Elastic scattering & 3NF effects



$\pi\rho$ 3NF ?
 $\rho\rho$ 3NF ?
 relativity ?
 others ?



pictures from K. Sagara

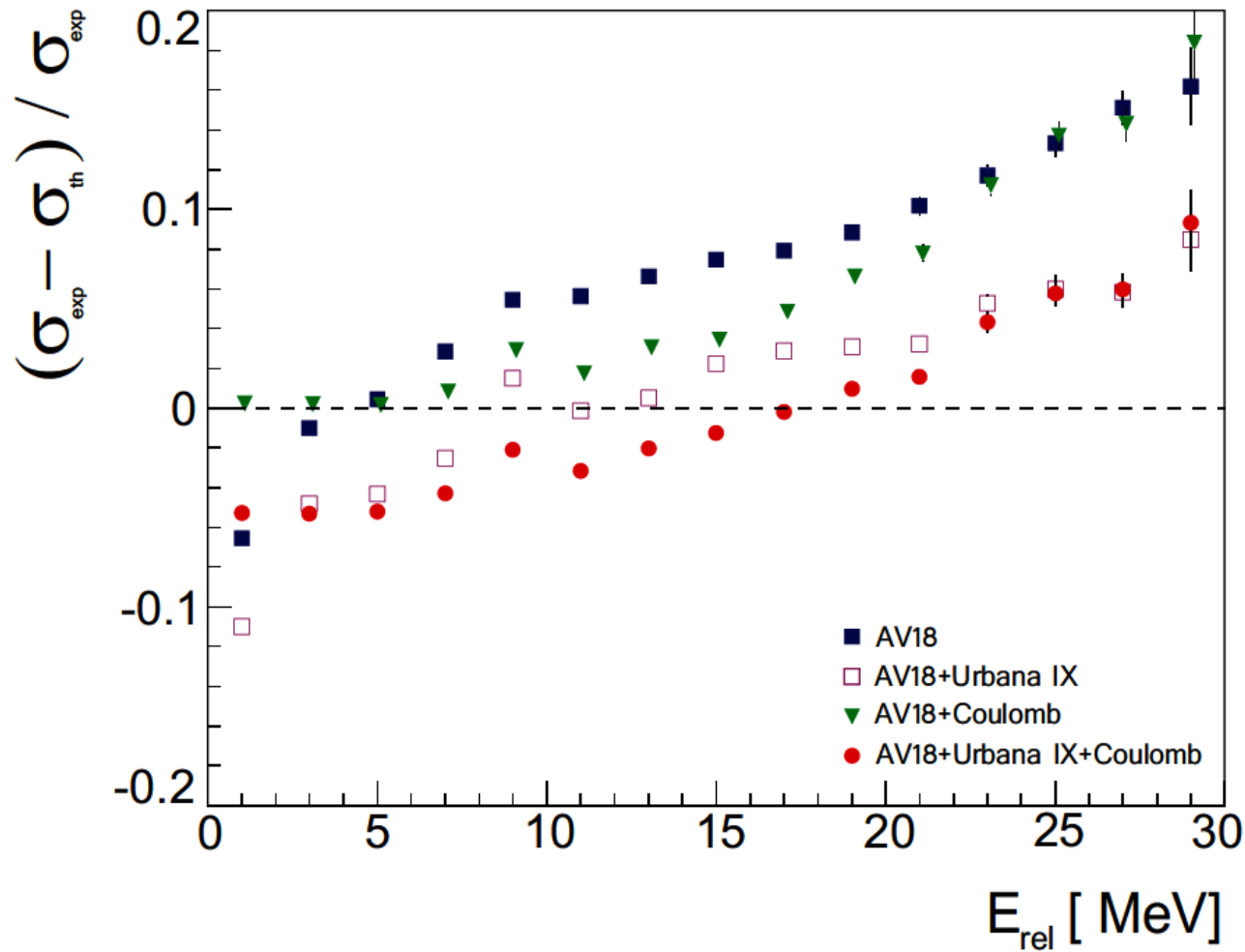
H. Witala et al,
Phys. Rev. C 83, 044001 (2011)

**The spin part of 3NF
 is still not under
 control in theory**

At lower energies:

- A_y puzzle (NN P-waves)
- Space Star anomaly

dp breakup @ 130 MeV: Coulomb force & 3NF


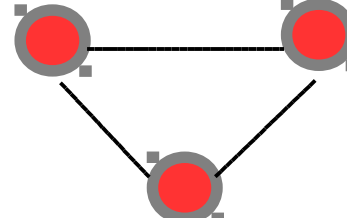
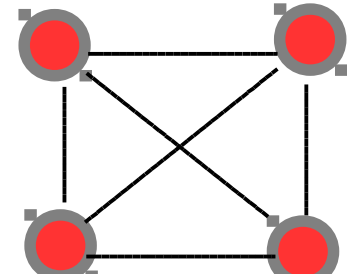


Coulomb force + 3NF gives much better agreement with the data !

4N - a new quality in nuclear forces studies

4N systems studies

- ◆ many input and output channels (resonances),
- ◆ higher sensitivity (in comparison to 3N) for 3NF,
- ◆ chance for investigation of isospin dependencies,
- ◆ extra sensitivity to NN force models (isospin symmetry of NN P-waves),
- ◆ role of 4NF.

	2NF	3NF	4NF
	1		
	3	1	
	6	4	1

2NF >> 3NF >> 4NF

$\langle V_{NN} \rangle \sim 20 \text{ MeV/pair}$

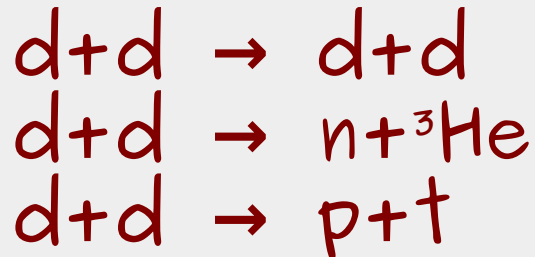
$\langle V_{3NF} \rangle \sim 1 \text{ MeV/triplet}$

$\langle V_{4NF} \rangle < 0.1 \text{ MeV/quartet}$

1
3
2
3

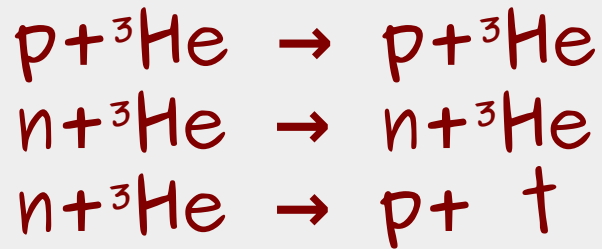
x2

4N calculations - summary



calculations above the 4N breakup threshold (10, 12.3 and 25 MeV)

*A. Deltuva, A. C. Fonseca,
Phys. Let. B 742, 285, (2015)*



calculations above the 4N breakup threshold (up to 35 MeV)

*A. Deltuva, A. C. Fonseca,
Phys. Rev. C 95, 024003 (2017)*



calculations near QFS @ 130, 160 MeV
Single Scattering Approximation (SSA)

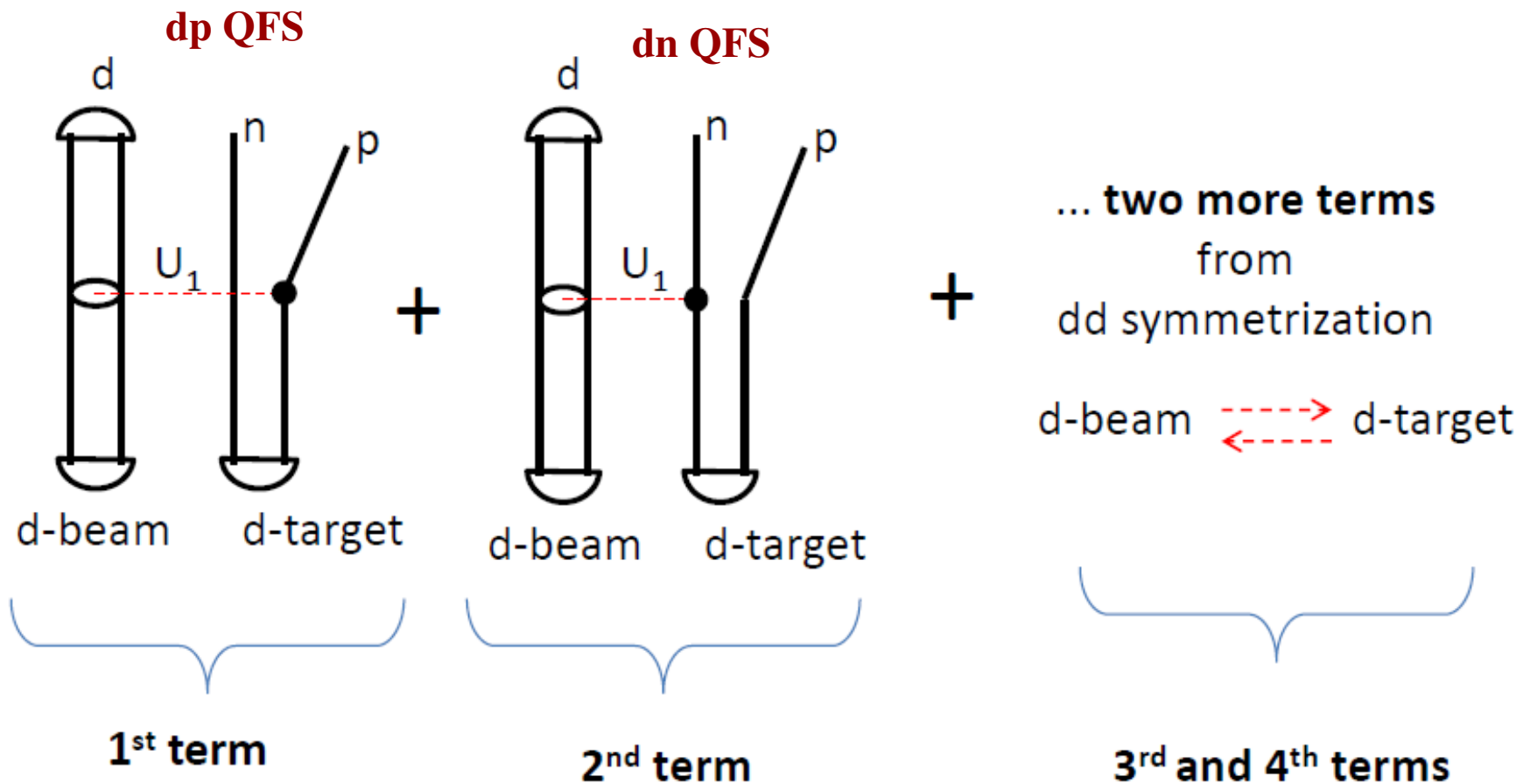
*A. Deltuva, A. C. Fonseca
Phys. Rev. C93, 044001 (2016)*

4N systems – Single Scattering Approximation (SSA)

estimate of d-d breakup cross sections at **higher energies**:

first term in the Neumann series expansion of AGS 3-cluster

breakup operator (taken from exact solution of the AGS 3-nucleon equations)



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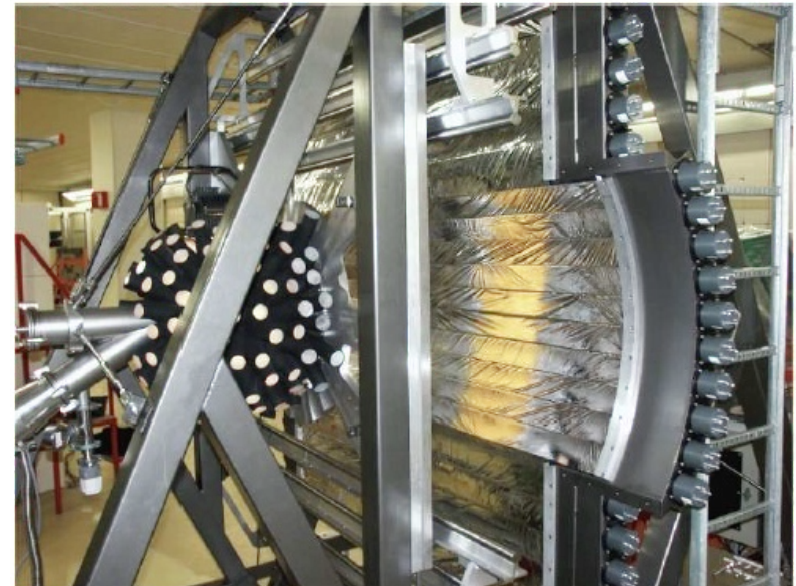
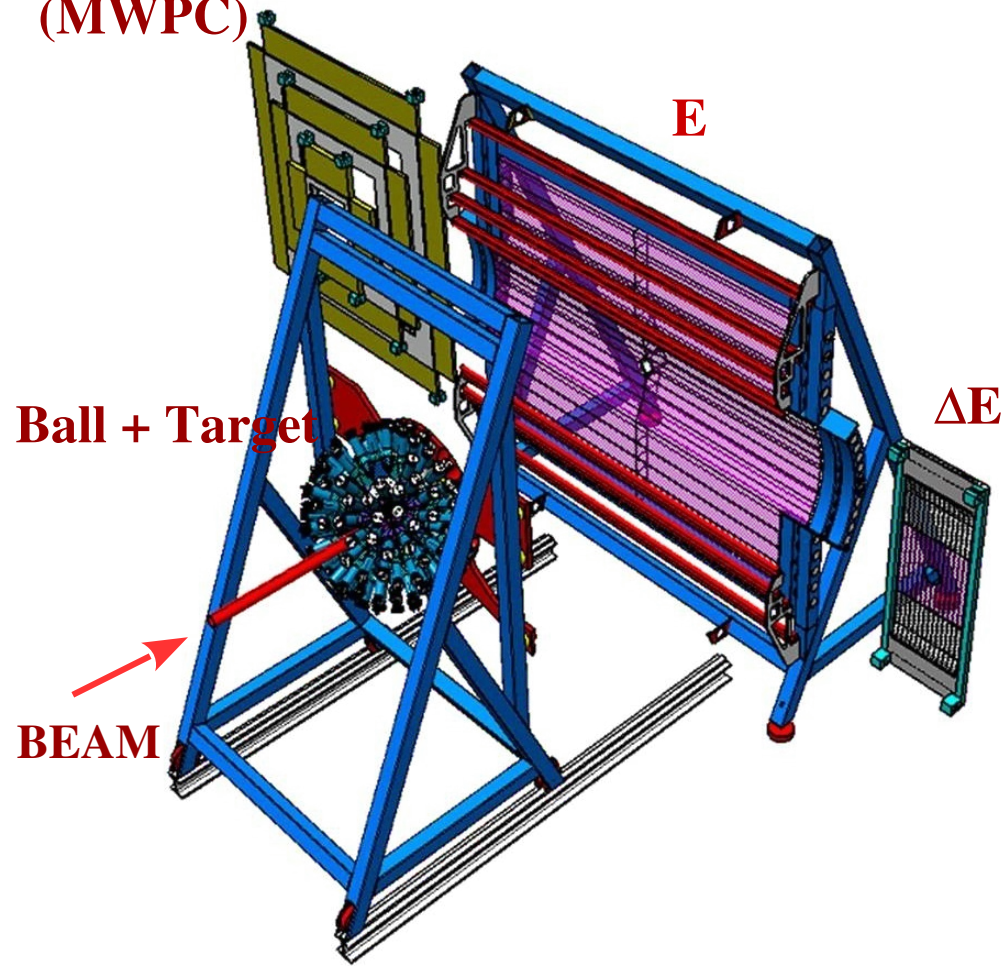
Simplified reaction mechanism → calculations are reliable:

1. high enough beam energy,
2. $E_n \sim 0$,
3. high relative n - d and n - p energy

BINA-Big Instrument for Nuclear-polarisation Analysis



Wire chamber
(MWPC)



Experiment @ 160 MeV

- experiment performed at **KVI** with **BINA**,
- beam: deuteron,
- energy: 160 MeV,
- target: Liquid Deuterium.

d+d – even more complicated system

d+d → d+d elastic scattering

d+d → d+p+n 3-body breakup

d+d → p+p+n+n 4-body breakup

used for the data normalization

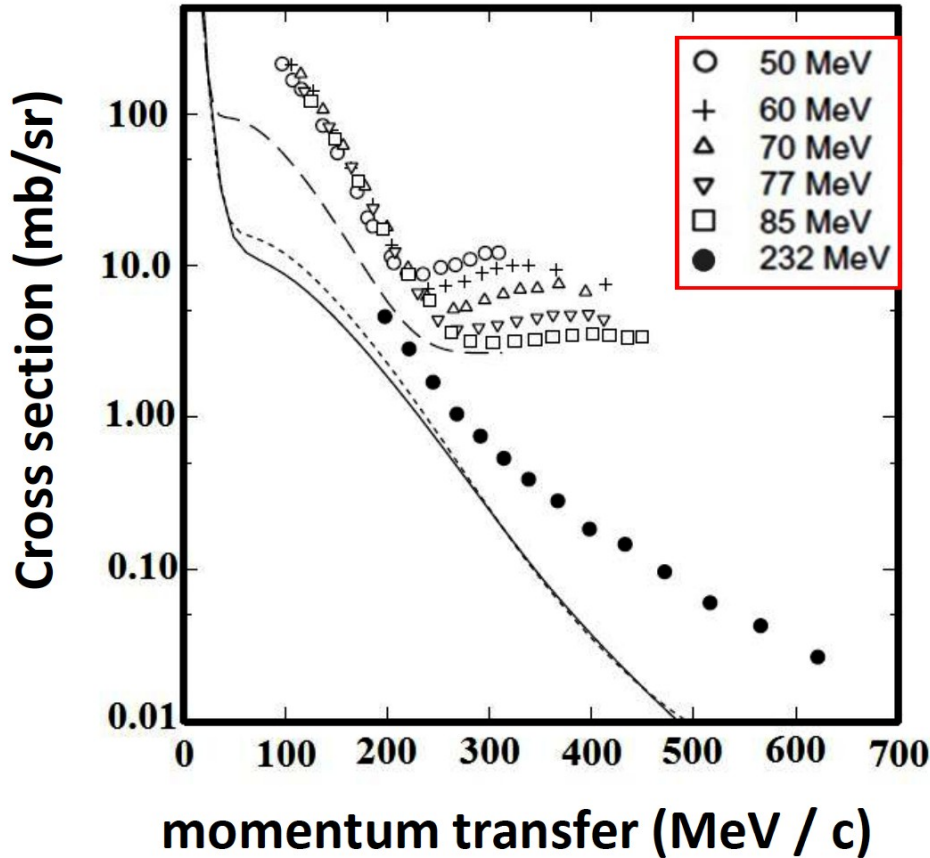
d+d → d+p+(n_{spec}) QFS

d+d → p+p+(2n_{spec}) double QFS

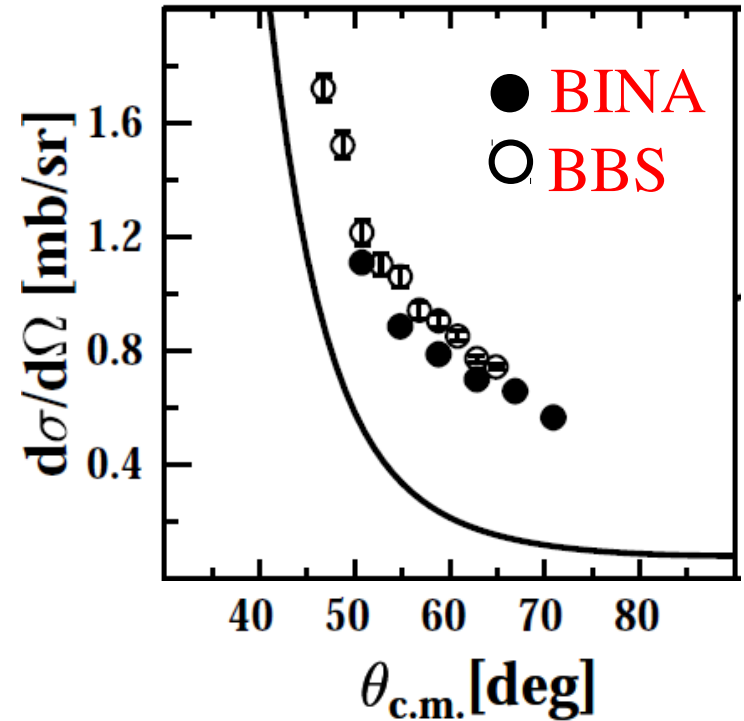
d+d → n+³He proton transfer

d+d → p+³H neutron transfer

d-d elastic scattering: theory vs data

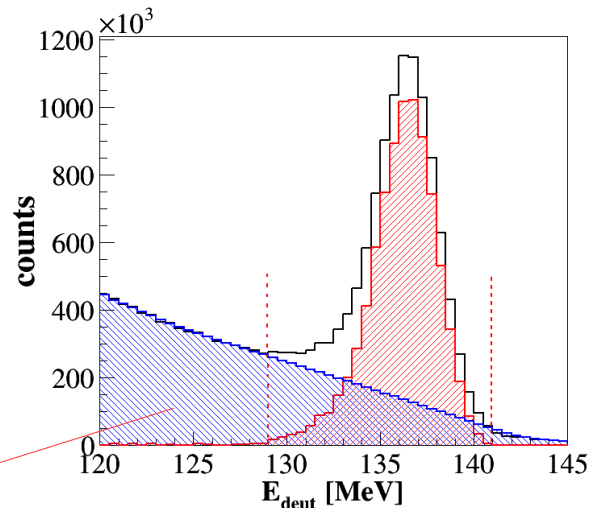
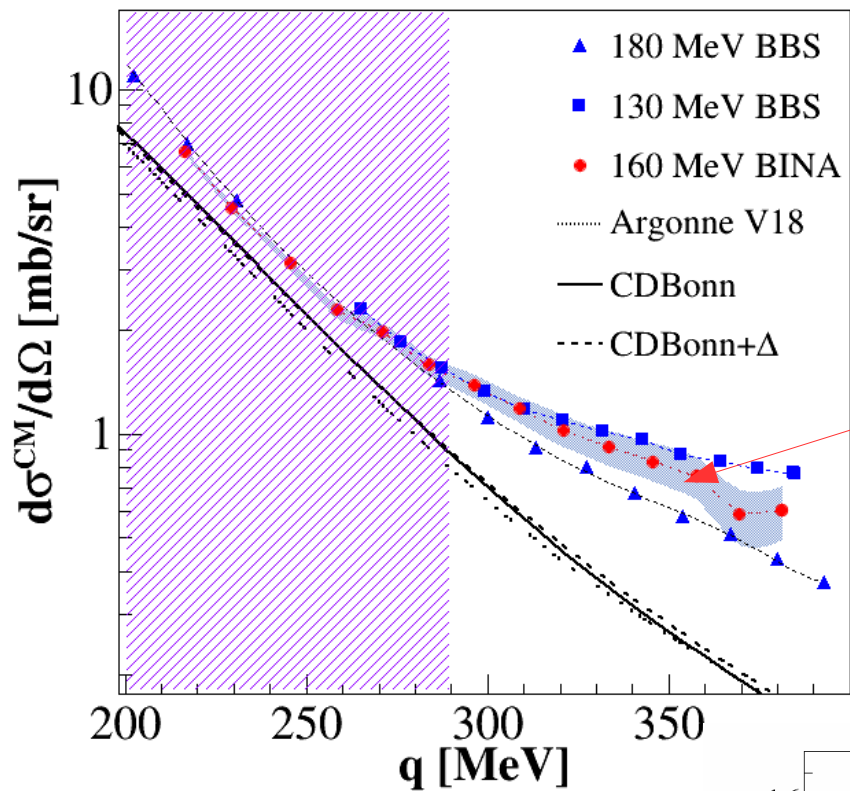


data @ 130 MeV

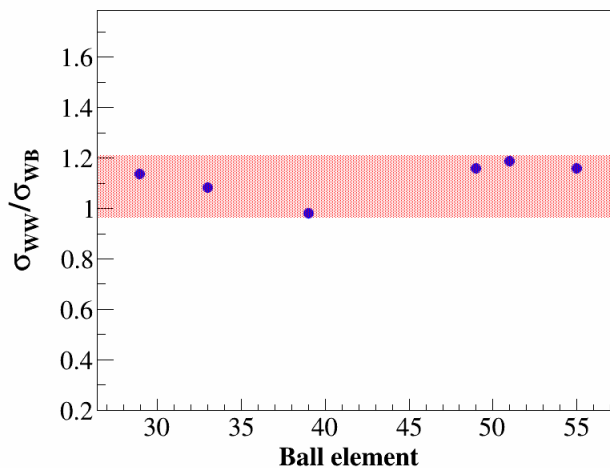
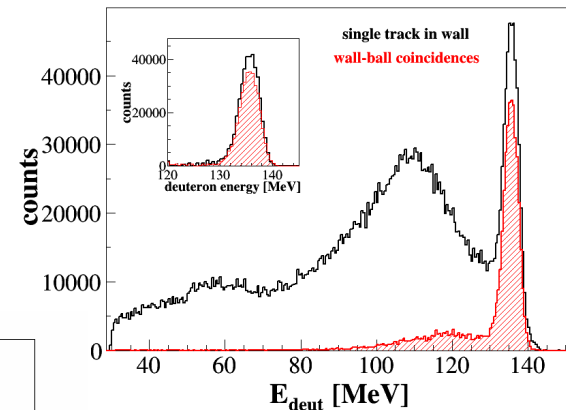


<i>calculations by A. C. Fonseca :</i>	---	52 MeV
	191 MeV
	—	232 MeV

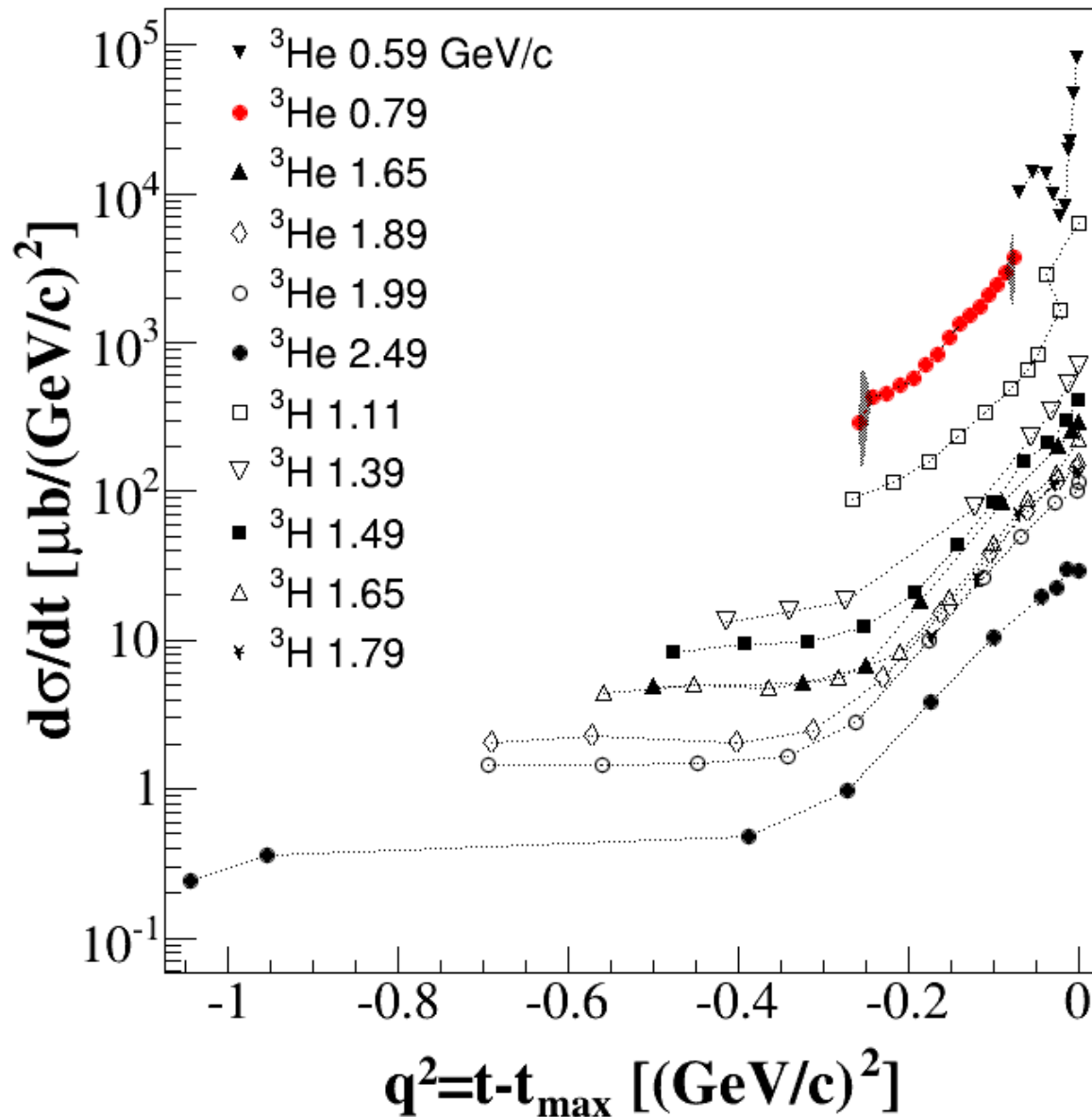
d-d elastic scattering @ 160 MeV



singles vs
coincidences



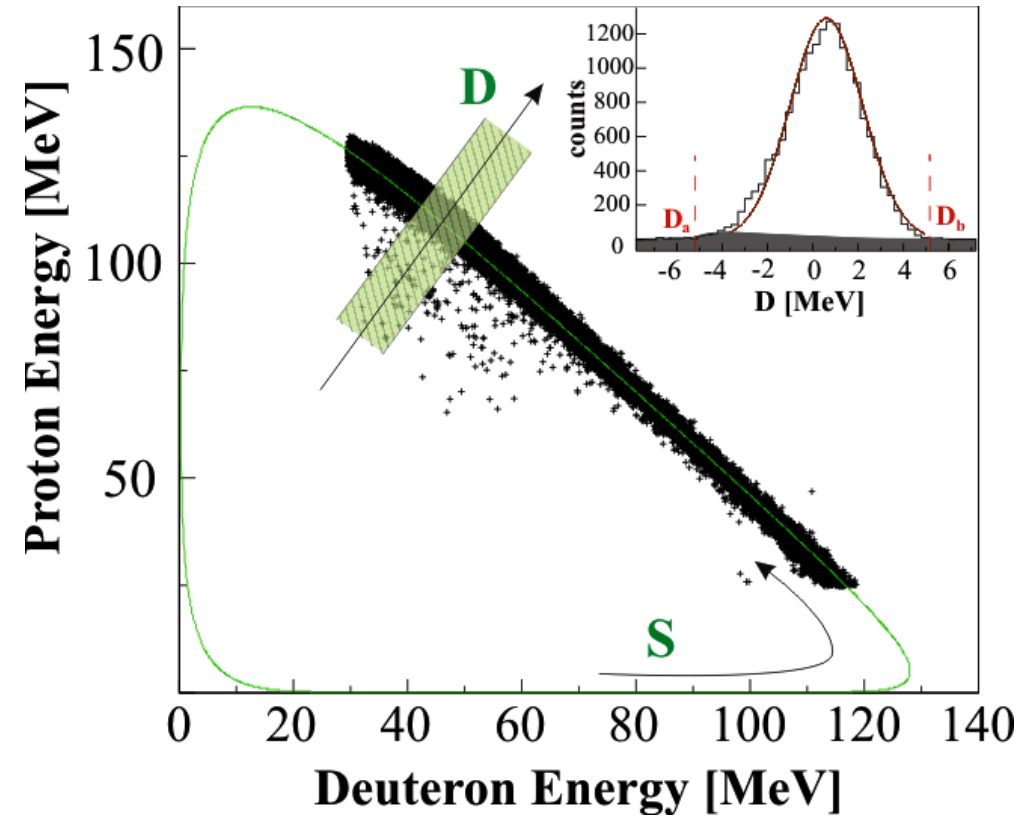
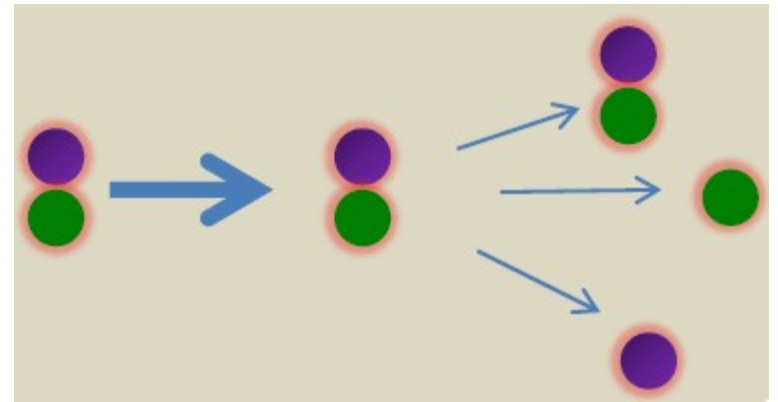
$d+d \rightarrow n+{}^3\text{He}$ @ 160 MeV



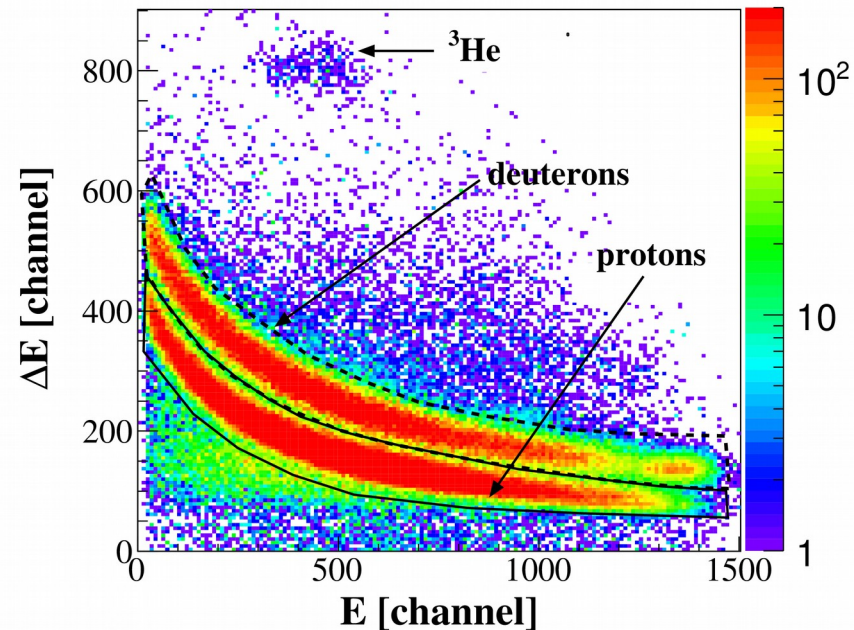
*I. Ciepał et al.,
Phys. Rev. C 99, 014620 (2019)*

Data included into EXFOR:
<https://www-nds.iaea.org/exfor/>

$d+d \rightarrow d+p+n$ @ 160 MeV



Particle Identification



$d+d \rightarrow d+p+n$ @ 160 MeV around QFS

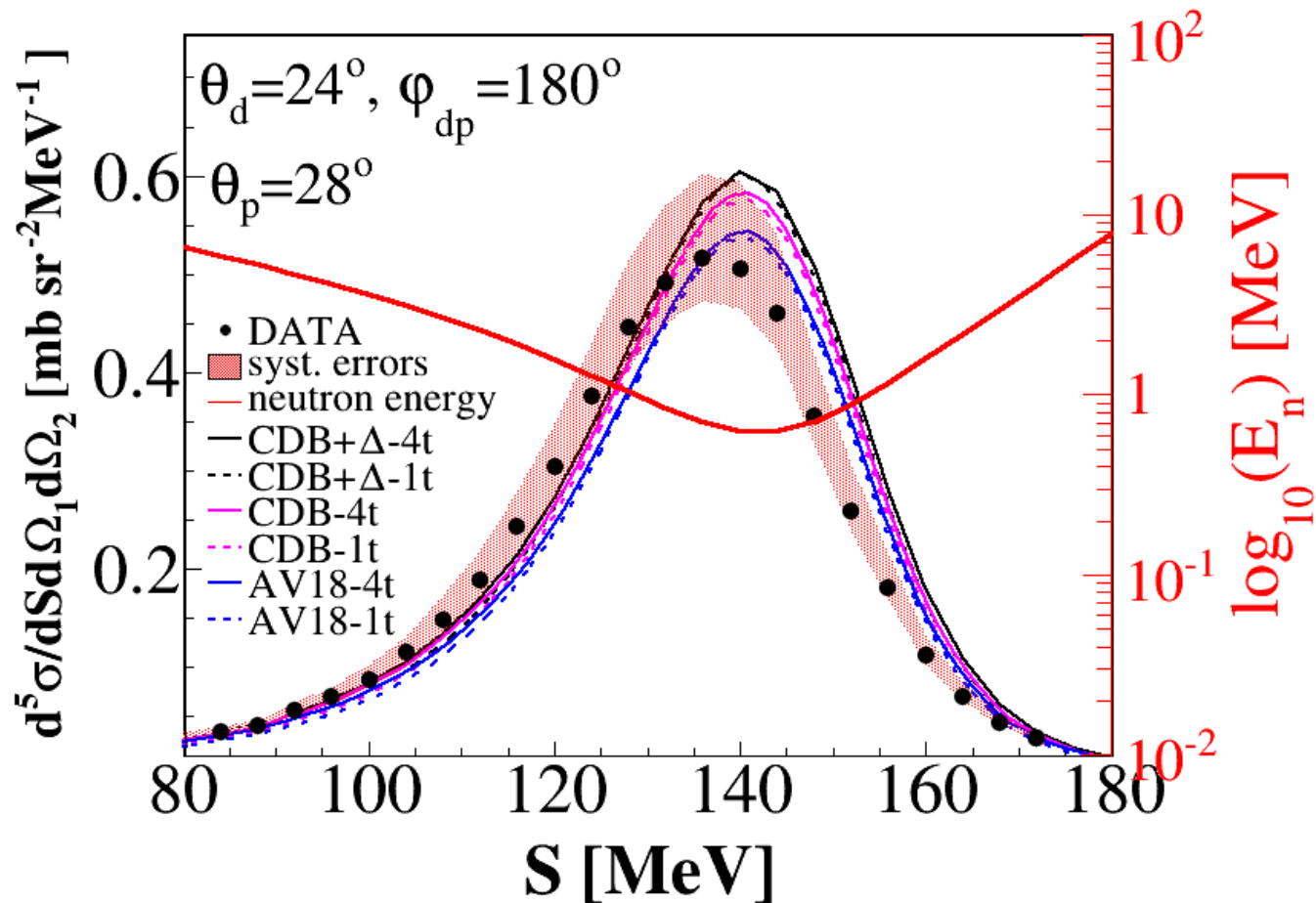
I. Ciepał et al.,

Phys. Rev. C 100, 024003 (2019)

I. Ciepał et al.,

Few-Body Syst 60, 44 (2019)

SSA calculations by Arnas Deltuva



$d+d \rightarrow d+p+n$ @ 160 MeV around QFS

I. Ciepał et al.,

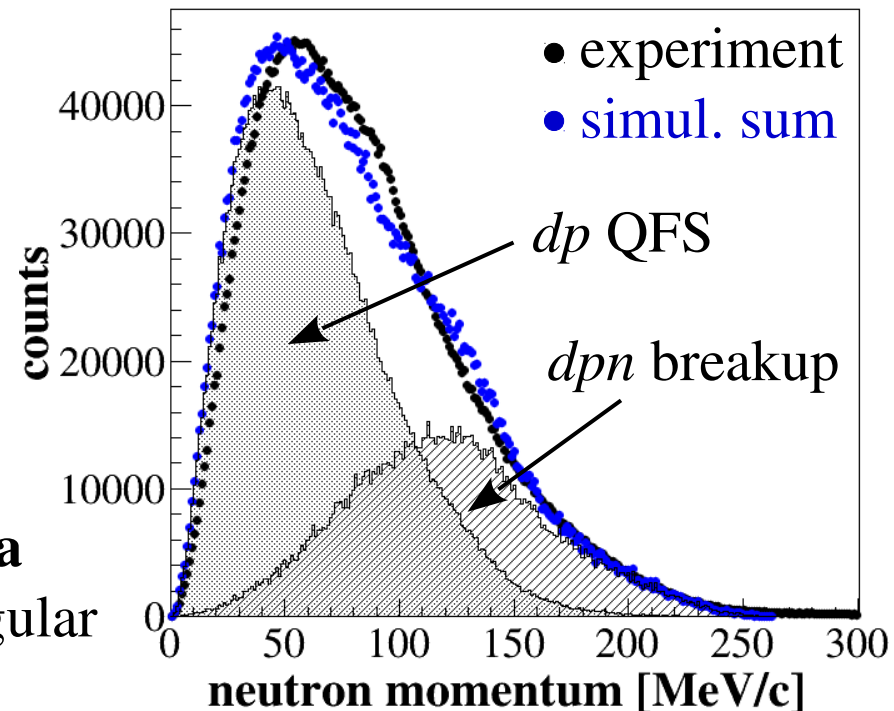
Phys. Rev. C 100, 024003 (2019)

around QFS = we analyze the data under conditions:

- detector acceptance ($\theta_d, \theta_p: 15^\circ-29^\circ$) \rightarrow target breakup,
- neutron from deuteron target (Fermi momentum ~ 80 MeV/c)
 \rightarrow spectator,
- $\varphi_{dp}: 135^\circ-185^\circ$,
- the data were sorted according to the neutron energy E_n ,

PLUTO simulations vs. data

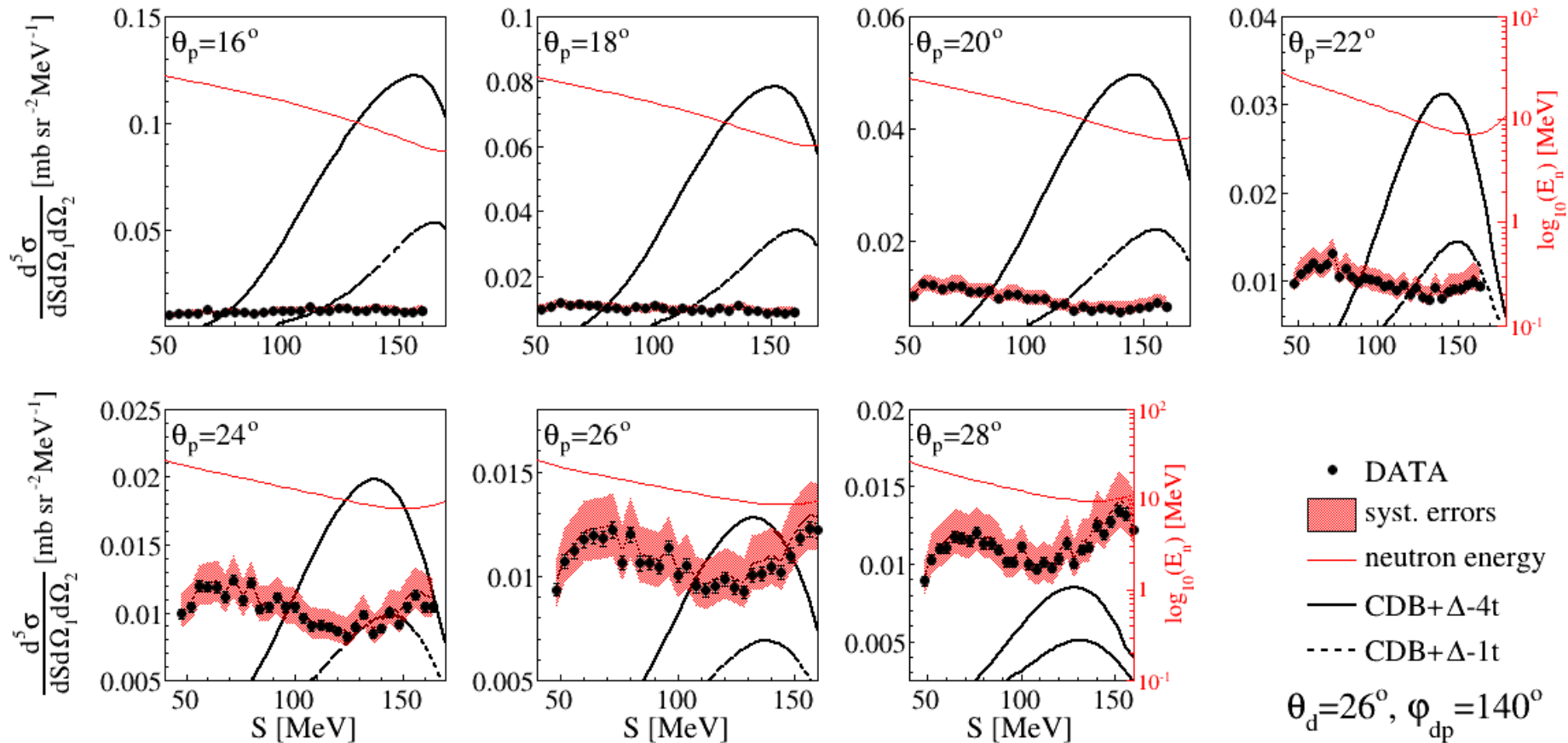
sensitivity of the selected angular range to the QFS kinematics



$d+d \rightarrow d+p+n$ @ 160 MeV around QFS

I. Ciepał et al.,

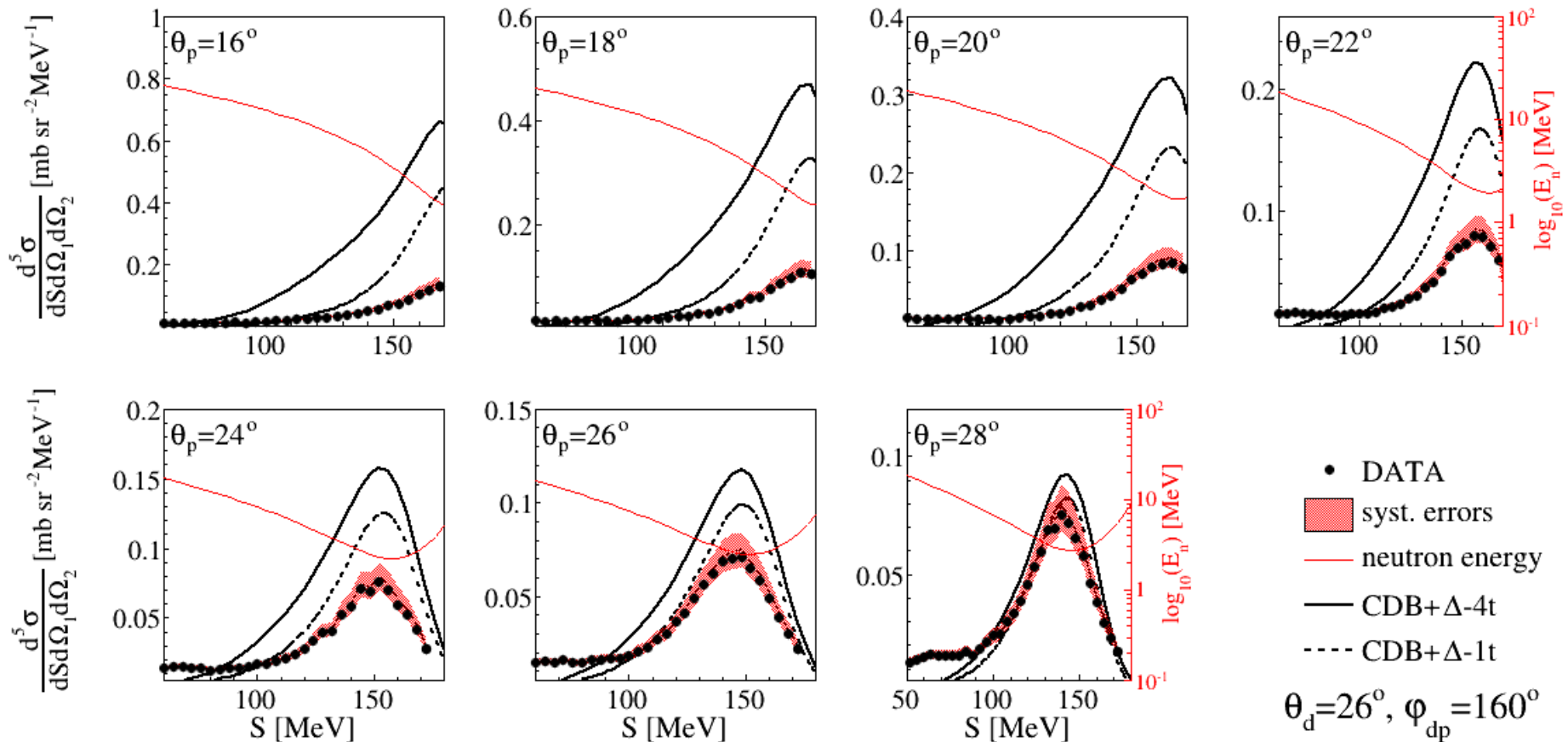
Phys. Rev. C 100, 024003 (2019)



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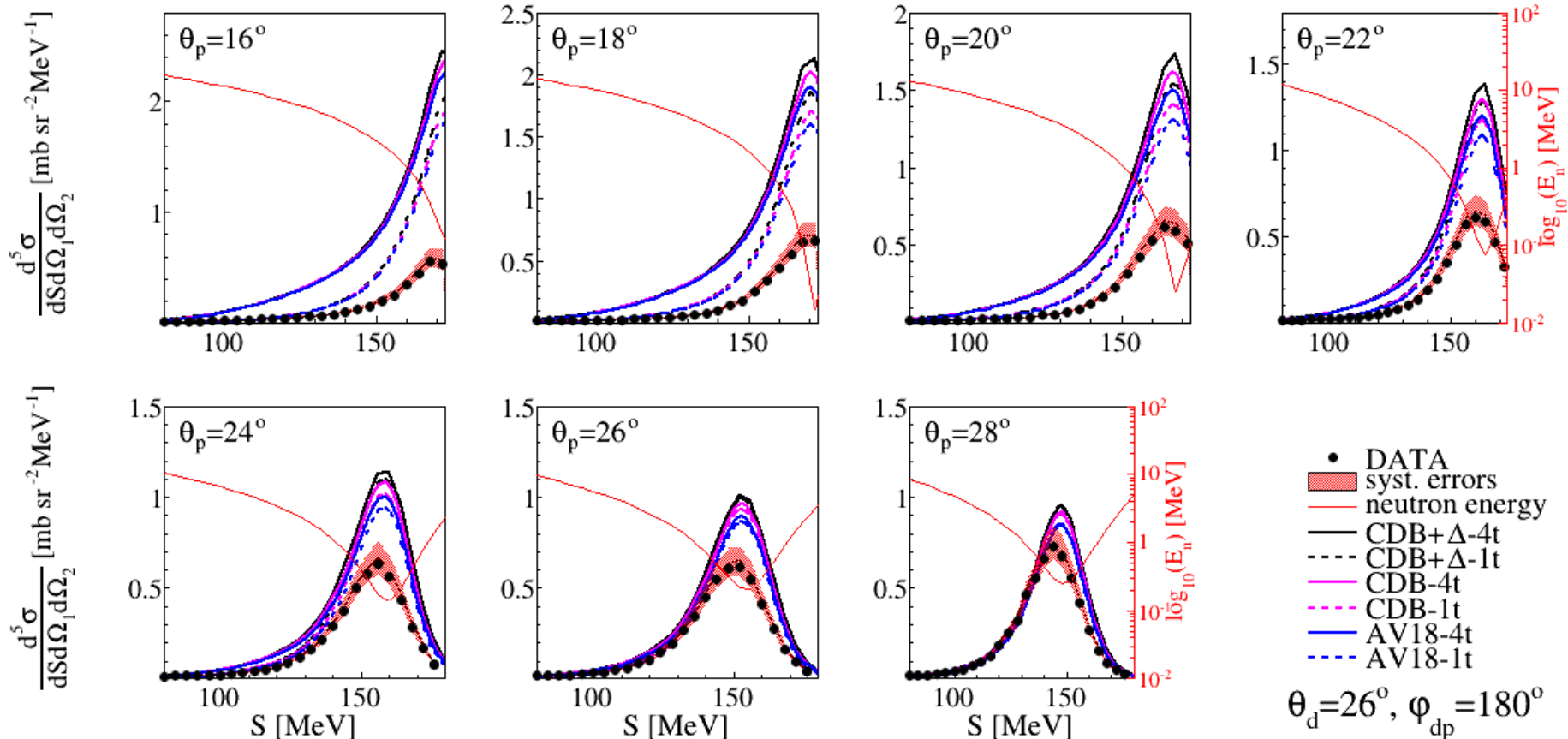
Phys. Rev. C 100, 024003 (2019)



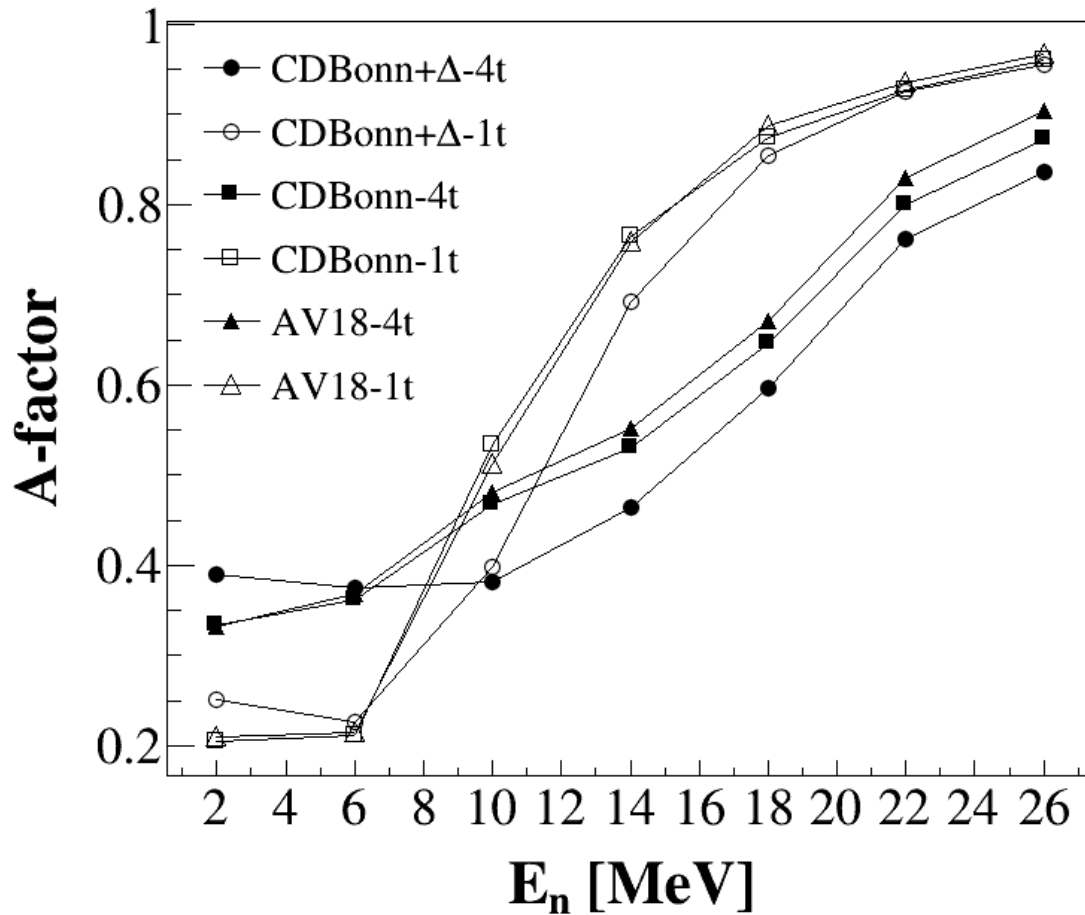
$d+d \rightarrow d+p+n$ @ 160 MeV around QFS

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Phys. Rev. C 100, 024003 (2019)



Global comparison



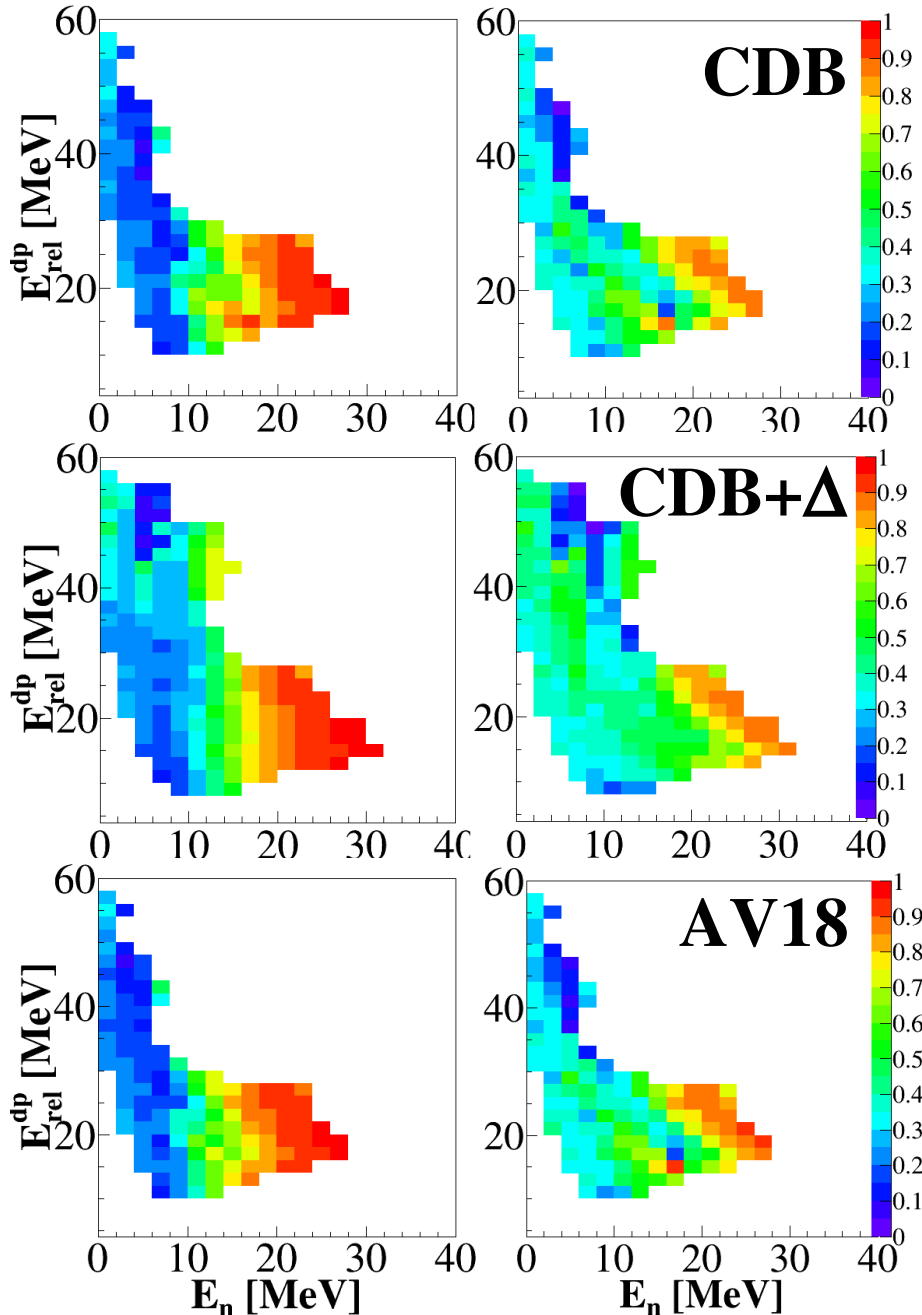
A-factor (instead of χ^2) on z-axis:

$$A \equiv \frac{1}{N} \sum_{i=1}^N \frac{|\sigma_i^{exp} - \sigma_i^{th}|}{\sigma_i^{exp} + \sigma_i^{th}}$$

A [0,1]

1-term

4-term



E_{rel}^{dp} vs E_n

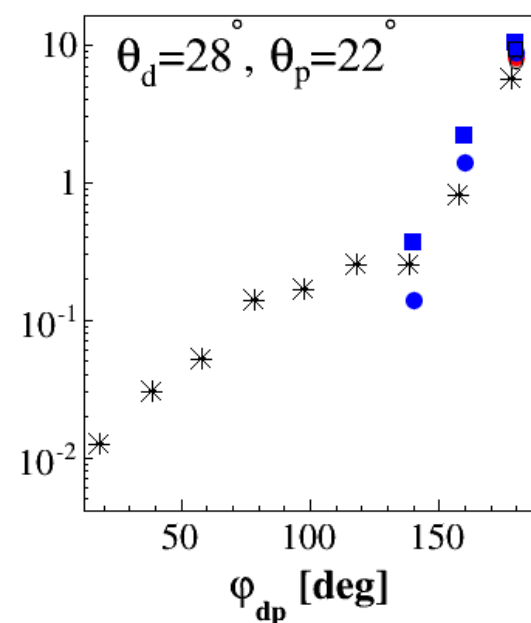
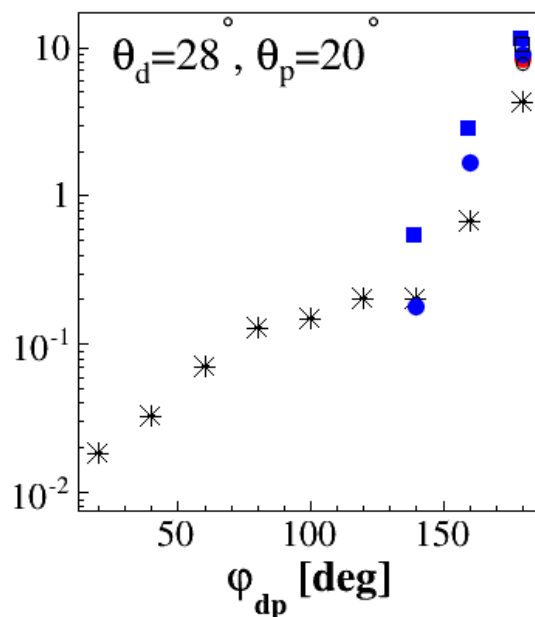
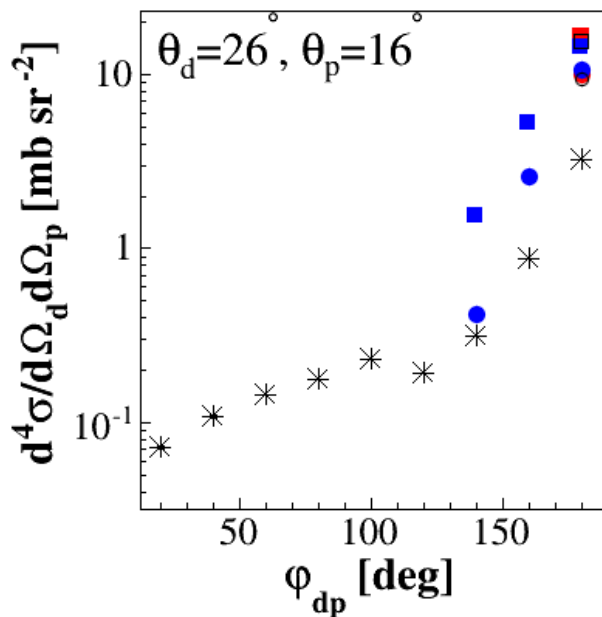
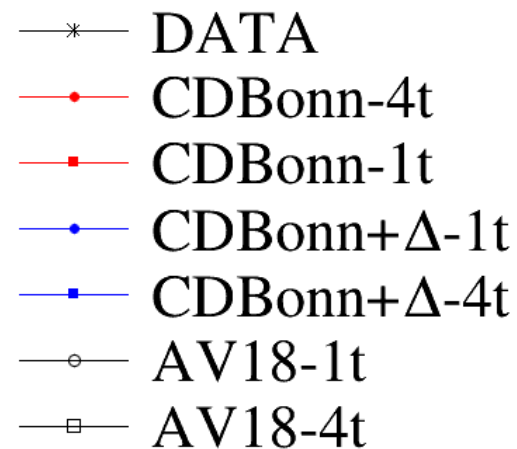
A-factor on z-axis

- 1t performs better
- deuteron beam energy of 160 MeV is too low to meet the SSA assumptions

d+d → d+p+n @ 160 MeV

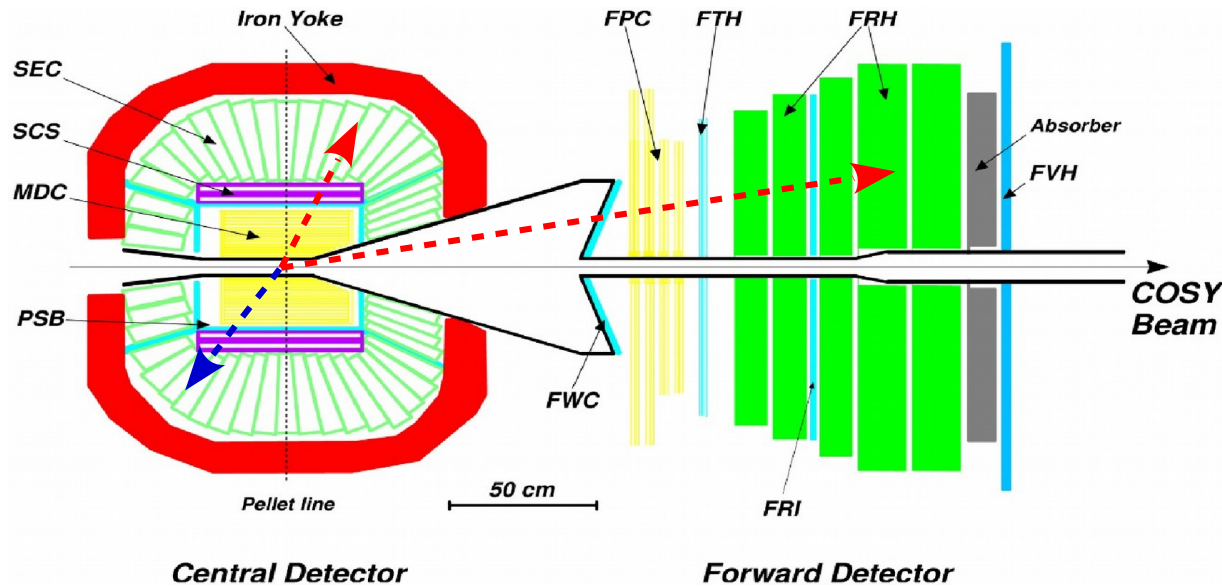
I. Ciepał et al.,
Few-Body Syst 60, 44 (2019)

- cross sections obtained also for $\varphi_{dp} < 135^\circ$,
- no theory available so far



OUTLOOK

WASA@ COSY d+d @ 350 MeV



$$d+d \rightarrow d(\text{FD}) + p(\text{FD})+n$$

$$d+d \rightarrow d(\text{FD}) + p(\text{CD})+n$$

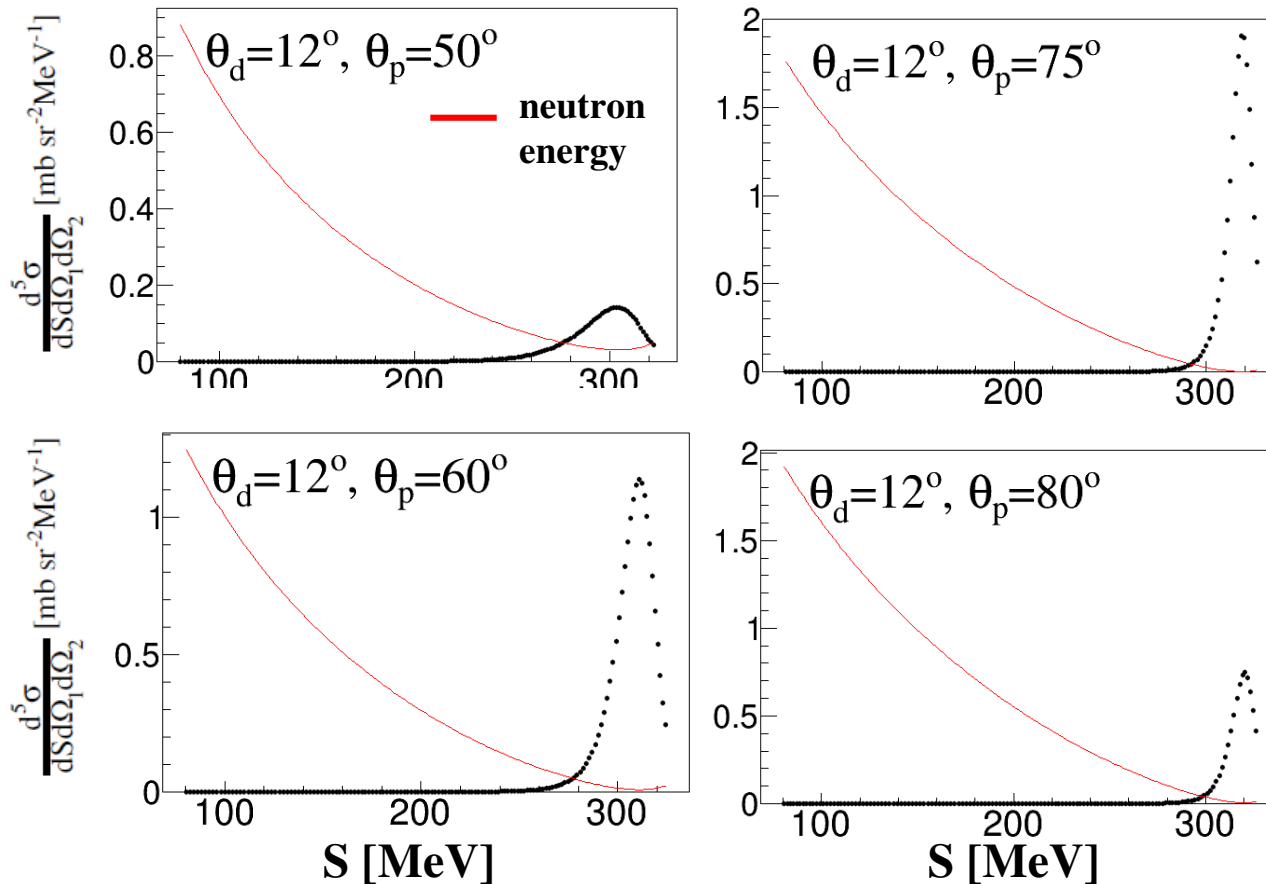
$$d+d \rightarrow d+p+n(\text{CD})$$

OUTLOOK

WASA@ COSY d+d @ 350 MeV

$d+d \rightarrow d(\text{FD}) + p(\text{CD})+n$

SSA calculations by Arnas Deltuva

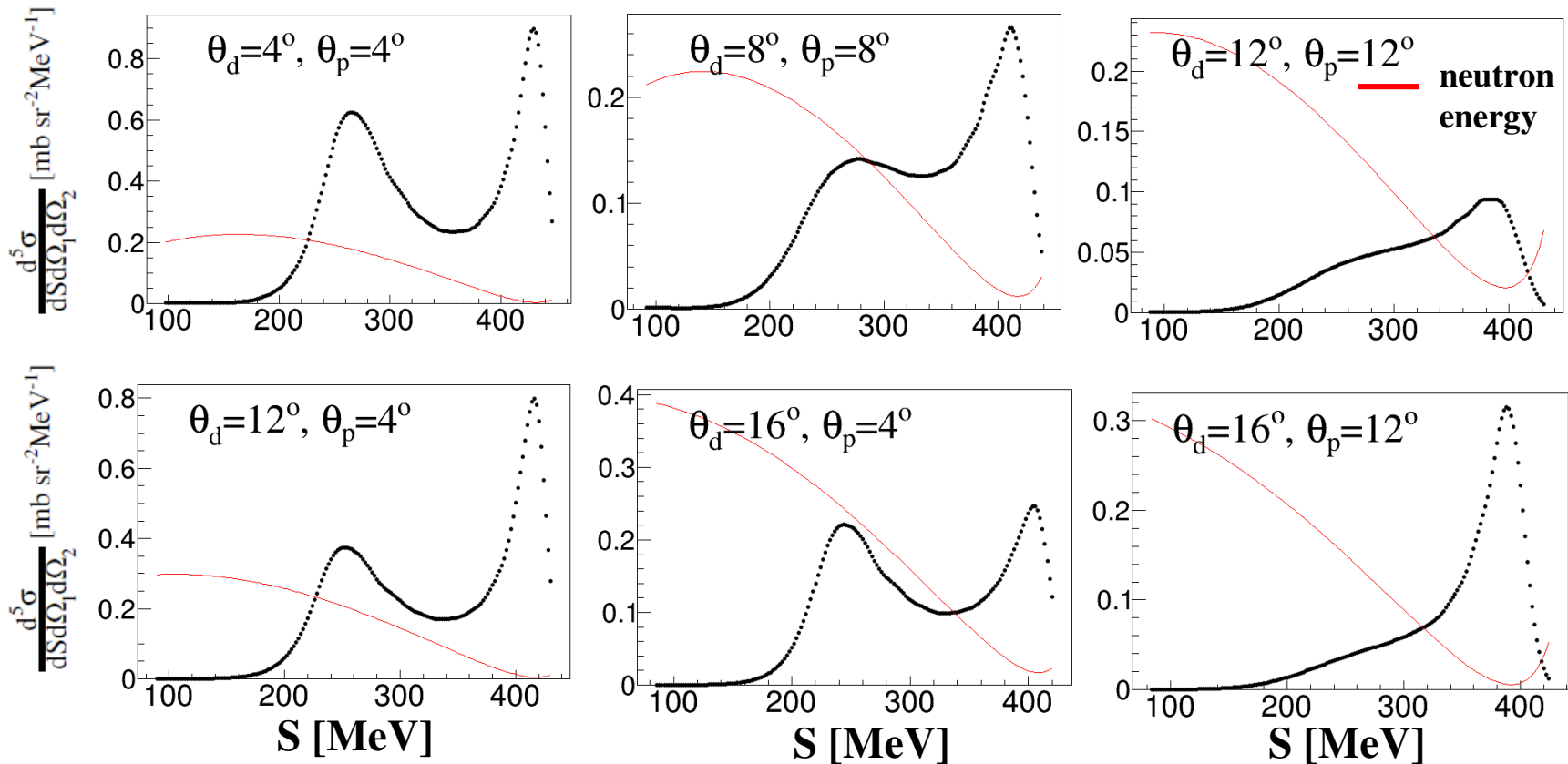


OUTLOOK

WASA@ COSY d+d @ 350 MeV

d+d → d(FD) + p(FD)+n

SSA calculations by Arnás Deltuva



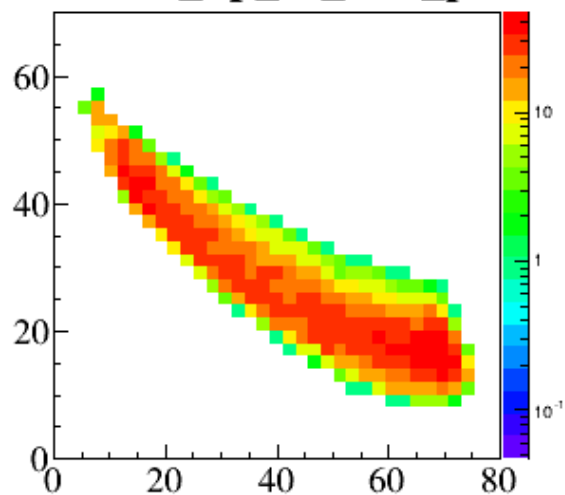
Summary

- ✗ Theoretical calculations exist for dd , $p+{}^3\text{He}$, $n+{}^3\text{He}$ for elastic scattering and transfer channels, but still for small energies < 35 MeV
 - ✗ **rapid progress in calculations for 4N systems.**
- ✗ Differential cross section for $dd \rightarrow n{}^3\text{He}$ @160MeV was obtained,
- ✗ Set of cross sections for the three body breakup around QFS and away from QFS has been evaluated and compared to the recent SSA calculations \rightarrow energy too low to fulfill the SSA assumptions,
- ✗ dd @ 350 MeV data measured with WASA@ COSY can also be used to evaluate the SSA predictions.

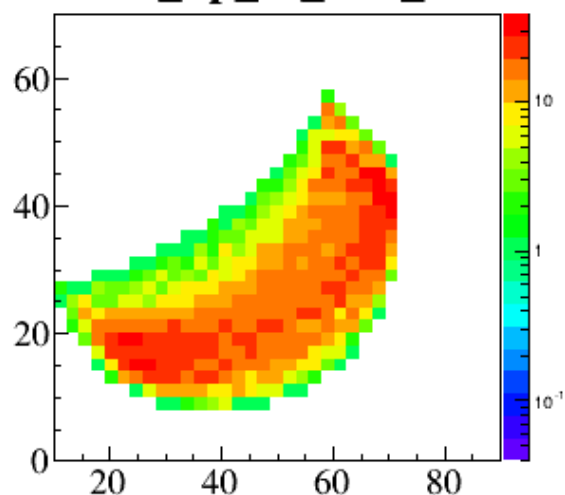


**THANK YOU
FOR
YOUR ATTENTION !**

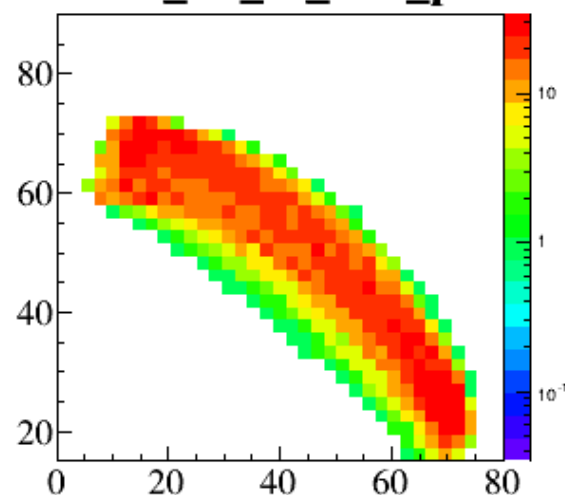
herel_dp_vs_erep_pn



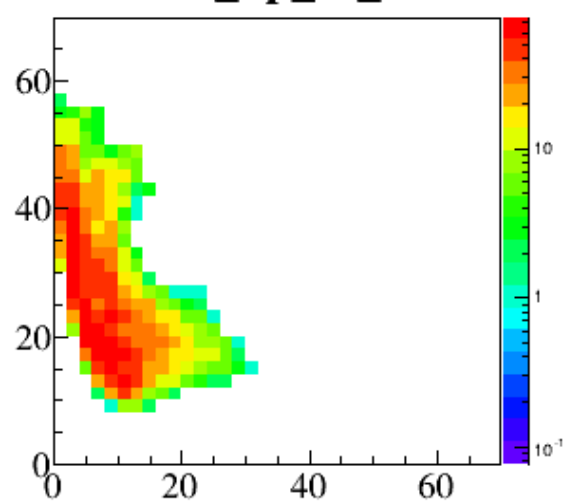
herel_dp_vs_erep_dn



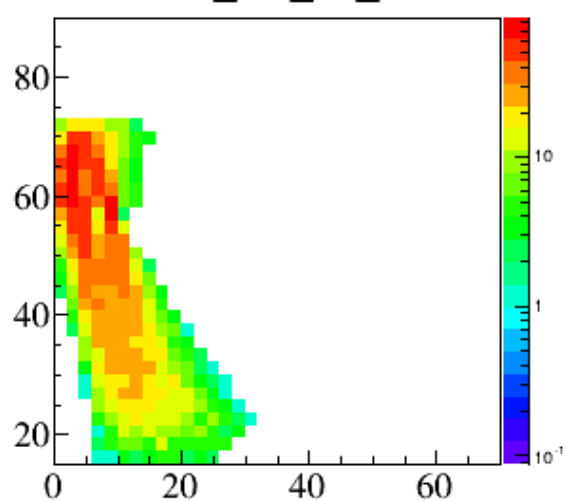
herel_dn_vs_erep_pn



herel_dp_vs_en



herel_dn_vs_en



herel_pn_vs_en

