

*In collaboration with Riccardo Catena, Timon Emken, Nicola Spaldin, Marek Matas*

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# General Dark Matter Electron Interactions in Detector Materials

*With a focus on Graphene and Carbon Nanotubes, Materials of Novel Experiments*

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Einar Urdshals  
PhD student at Chalmers Technical  
University, Gothenburg, Sweden



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# Outline

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- ❖ Dark Matter (DM) distribution in our galaxy
- ❖ Directional detection of DM
- ❖ DM induced electron ejections in graphene and carbon nanotubes
- ❖ Potential for discovering smoking gun signals from DM in graphene and carbon nanotubes based detectors.



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# The Standard Halo Model

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Credits: ESO/L Calçada



# The Standard Halo Model

- ❖ DM density  $\rho_\chi \approx 0.4 \text{ GeV}/\text{cm}^3$



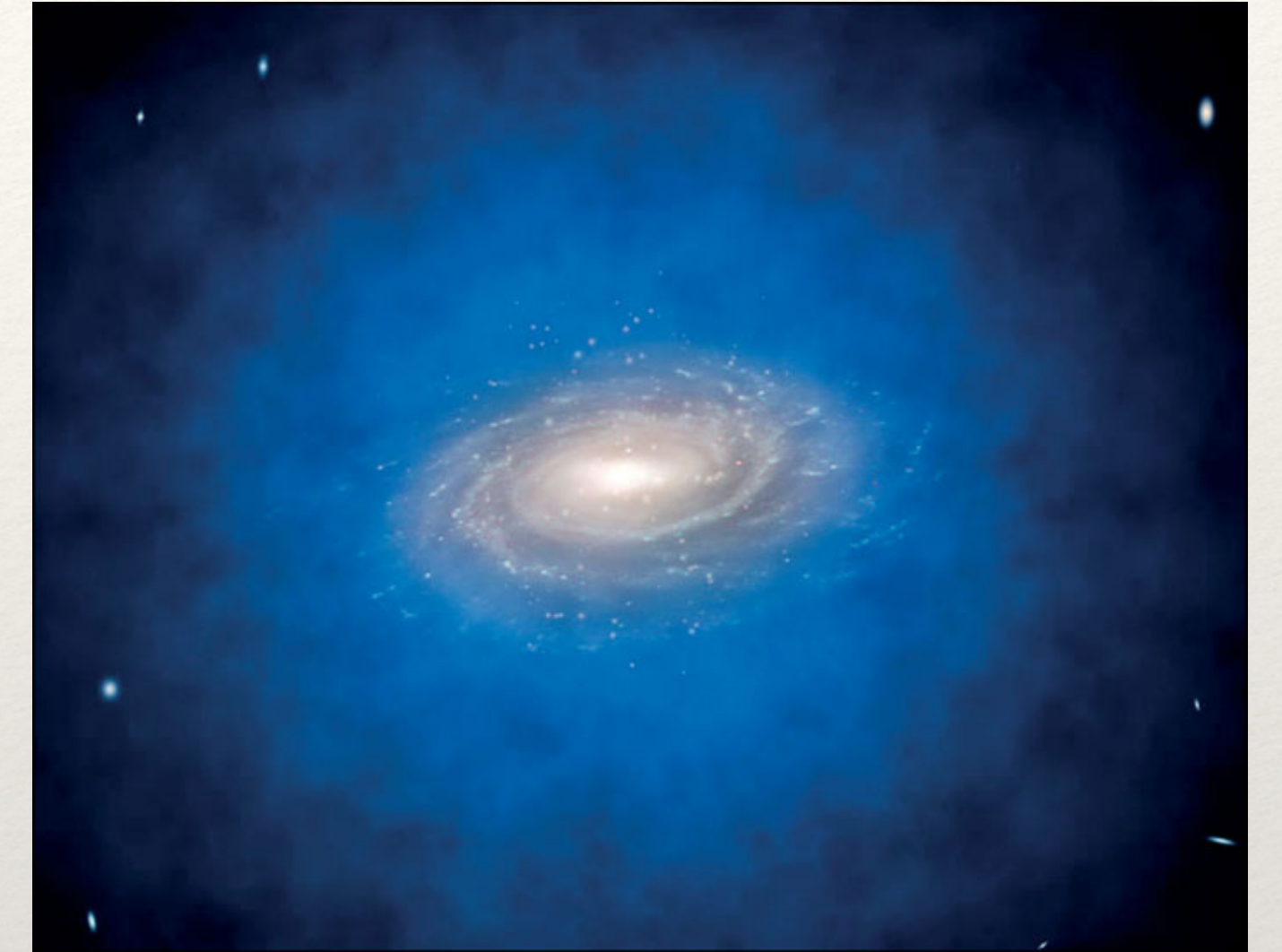
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- ❖ DM velocity is Boltzmann distributed,  $\mathbf{v} \sim e^{\frac{-v^2}{v_0^2}}$



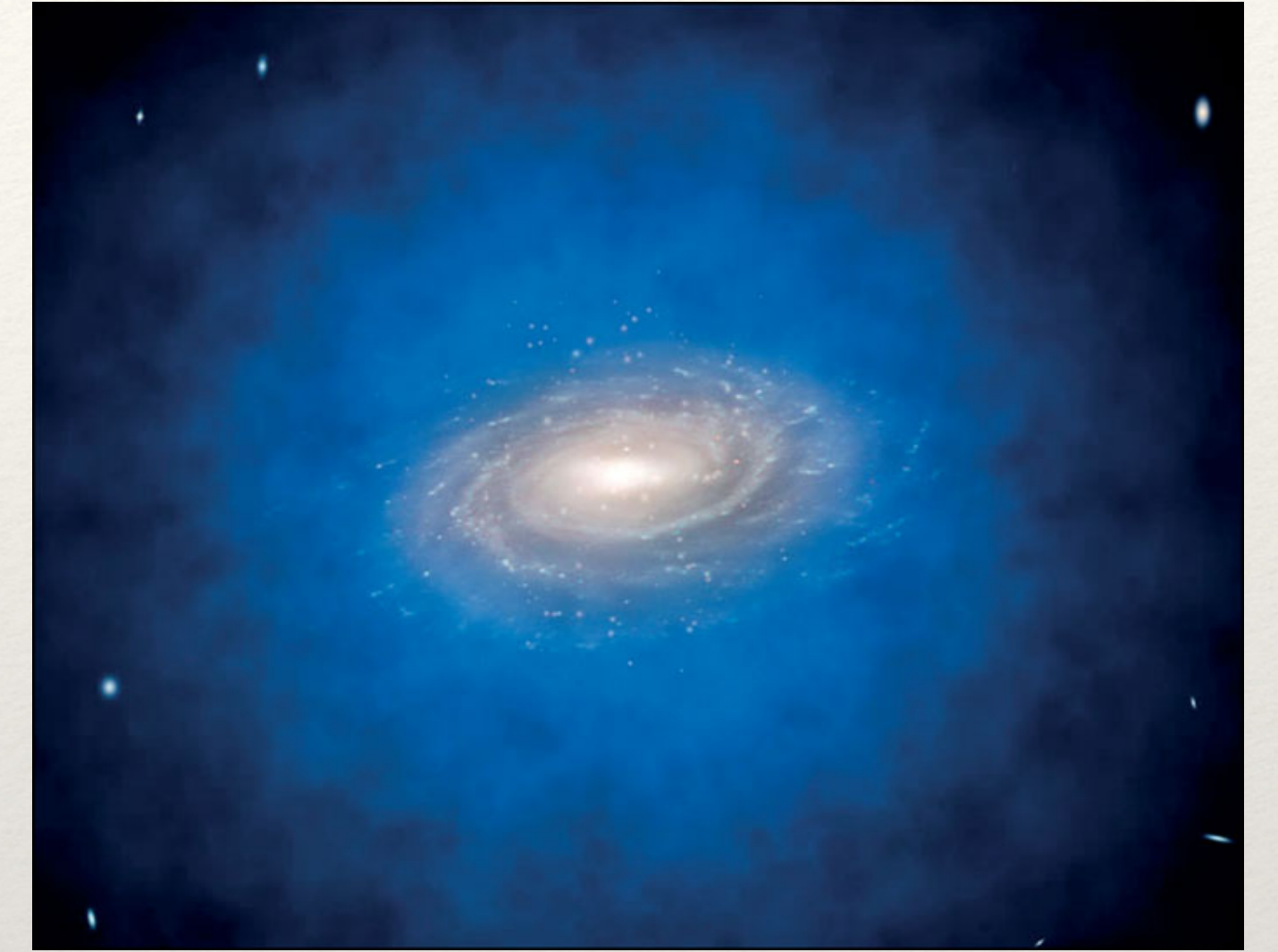
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- ❖  $v_0 \approx 238 \text{ km/s}$  and  $v_e \approx 250 \text{ km/s}$ , so  $v \ll c$

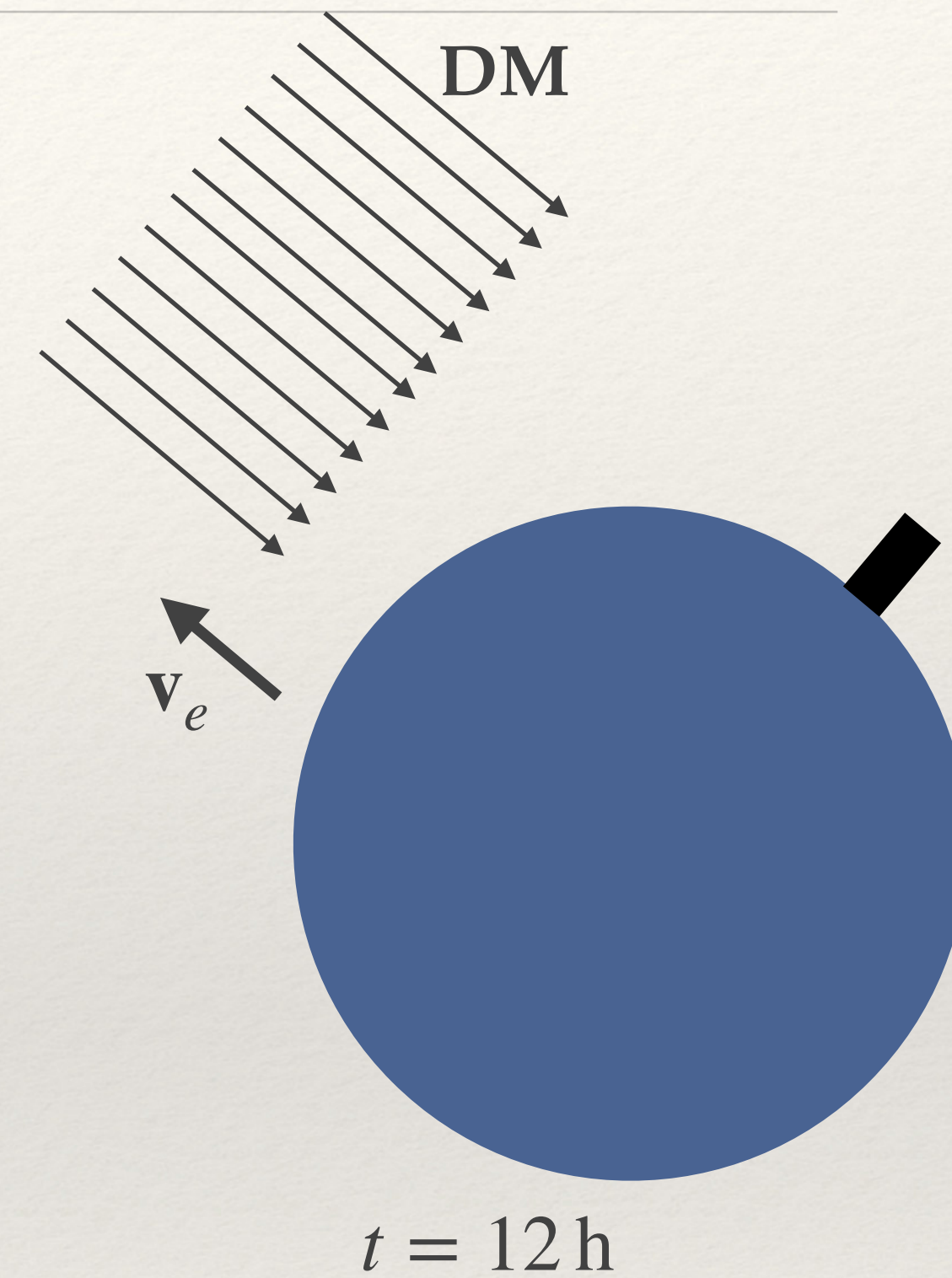
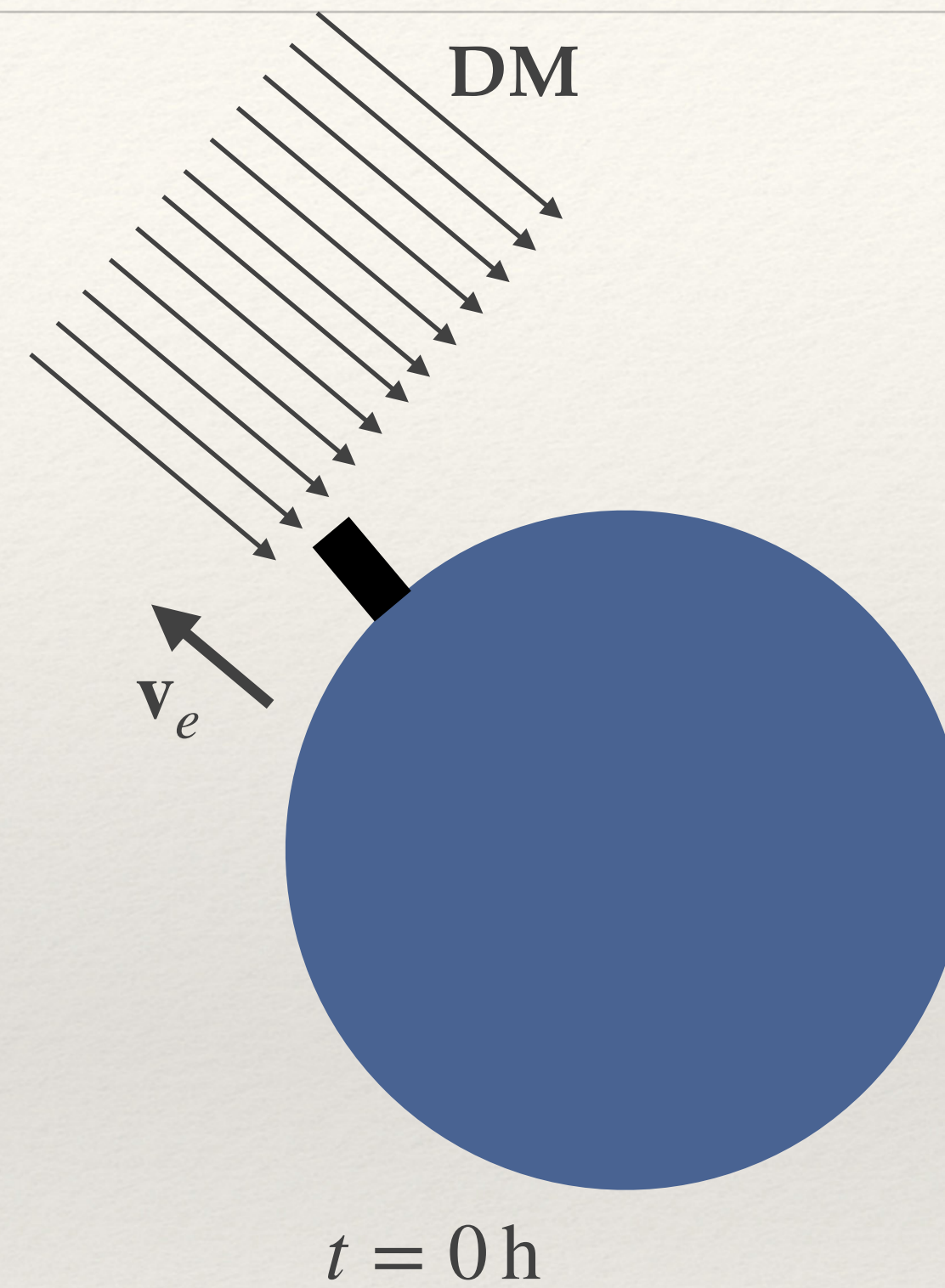


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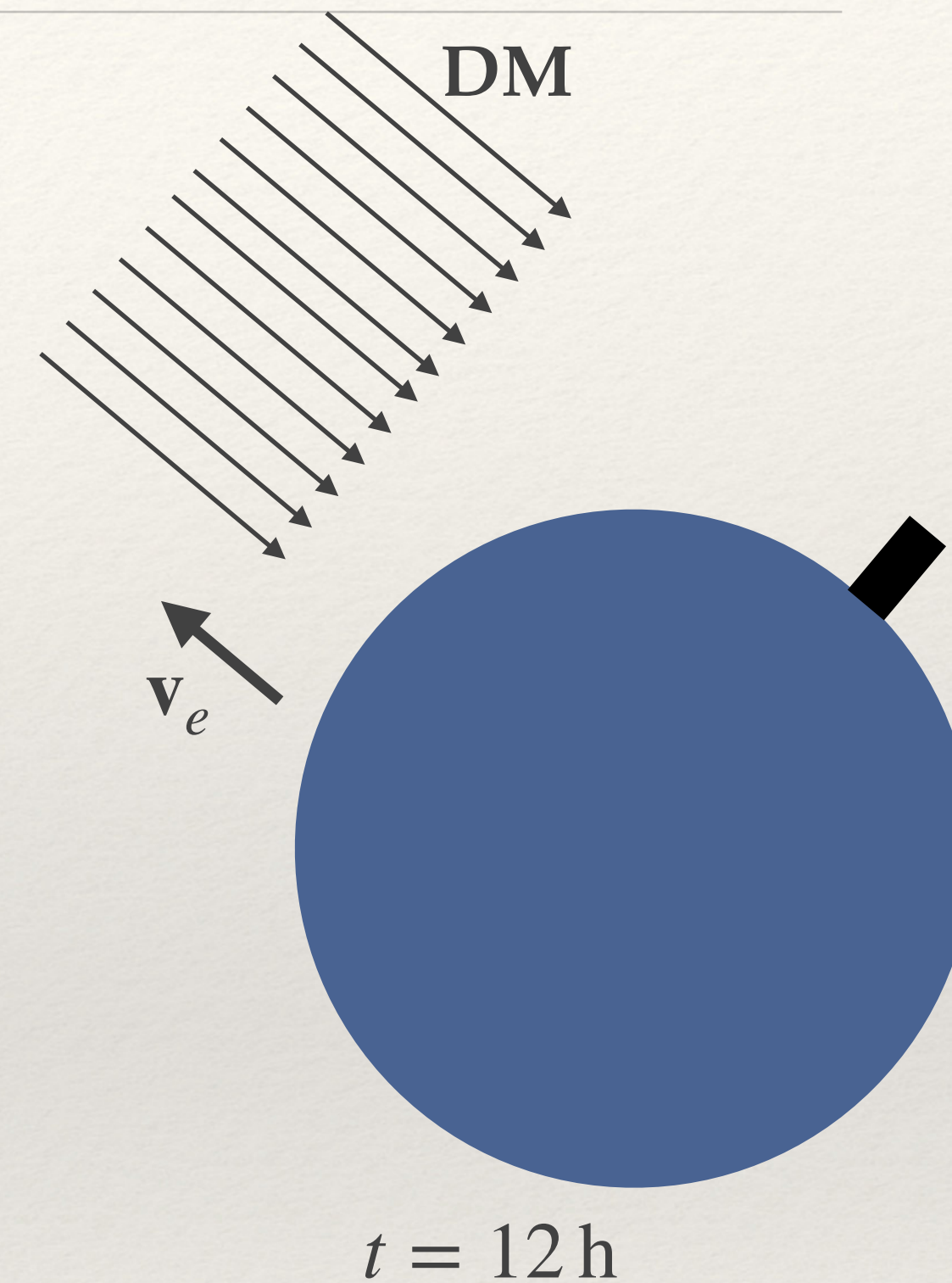
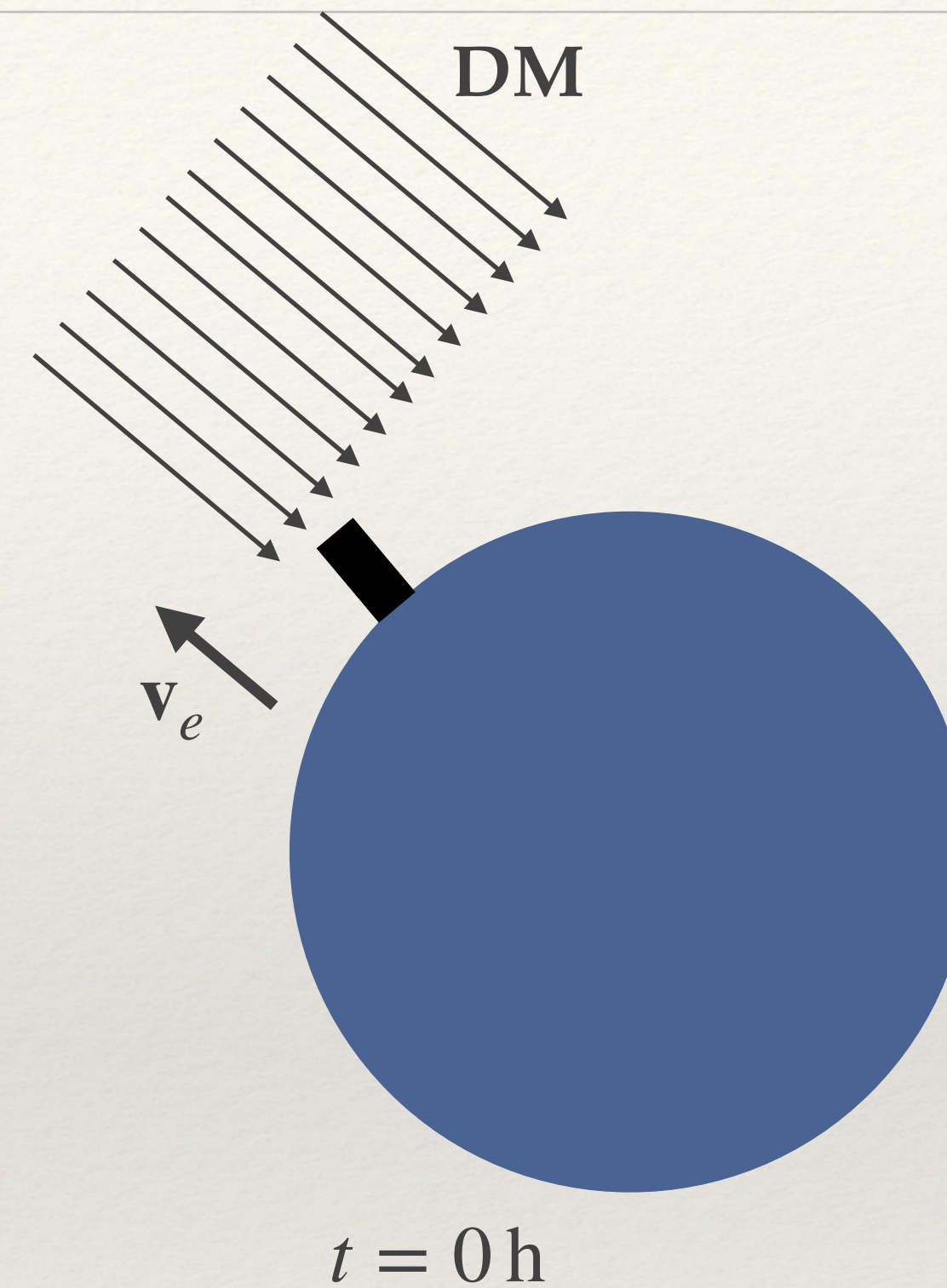
# Directional Detection of DM





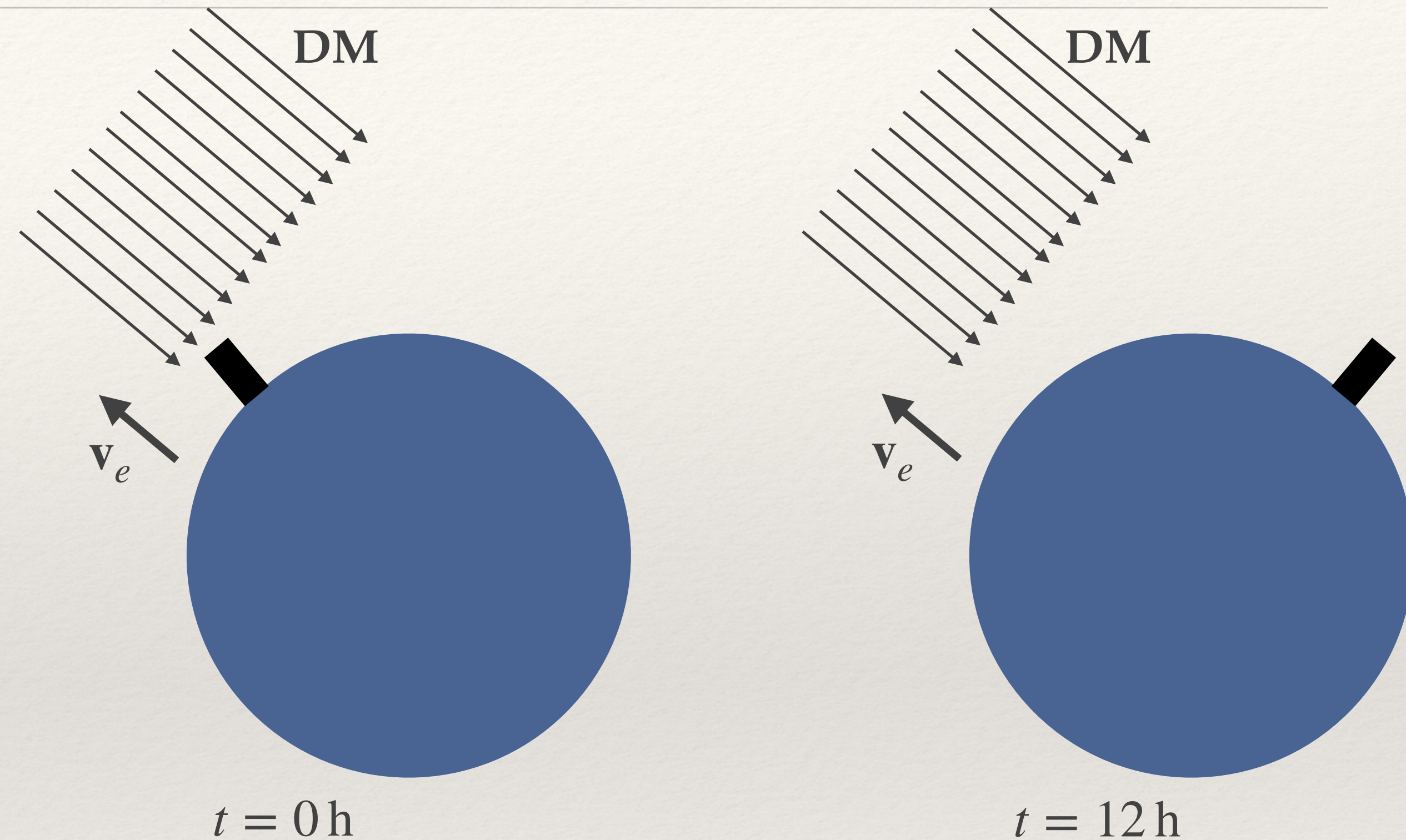
# Directional Detection of DM

- ❖ Direction of DM wind changes throughout the day



# Directional Detection of DM

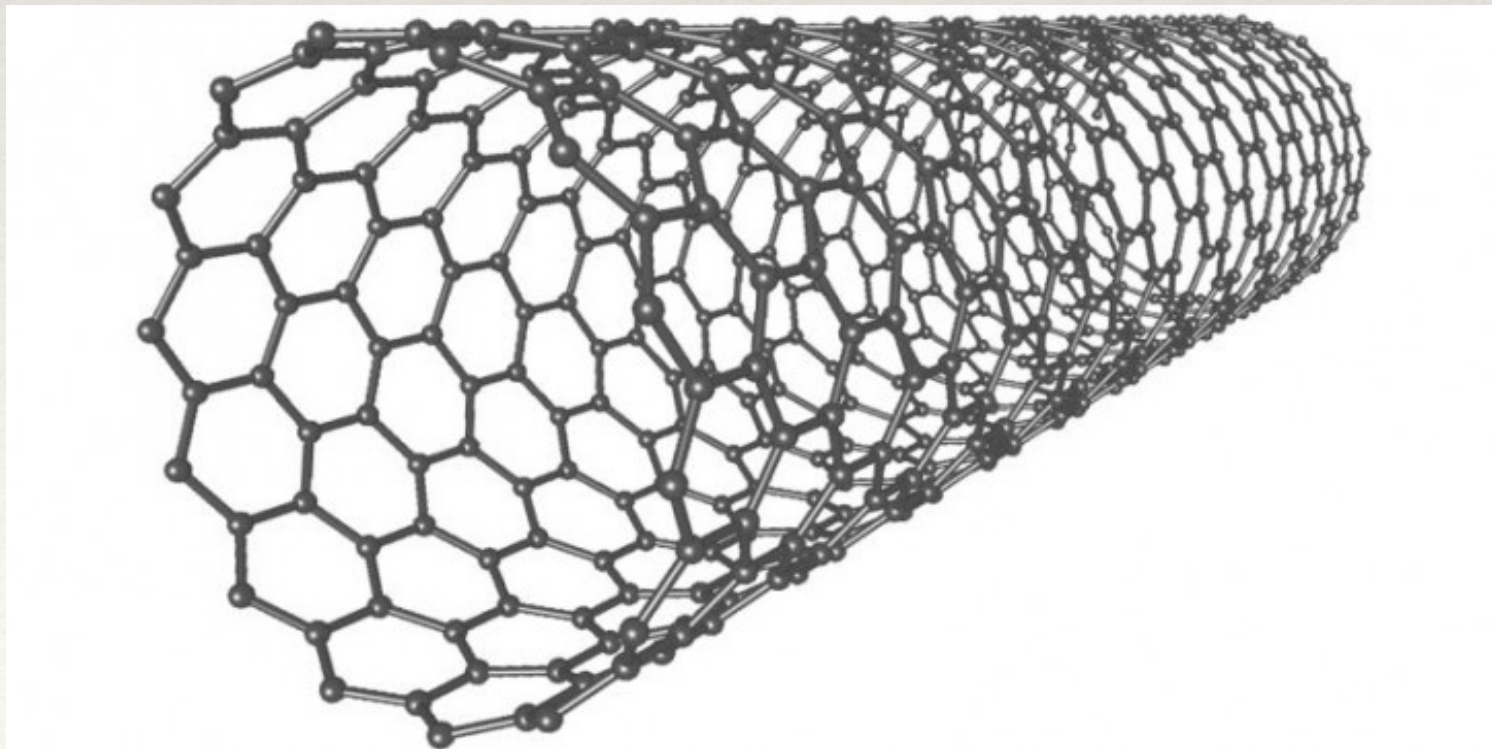
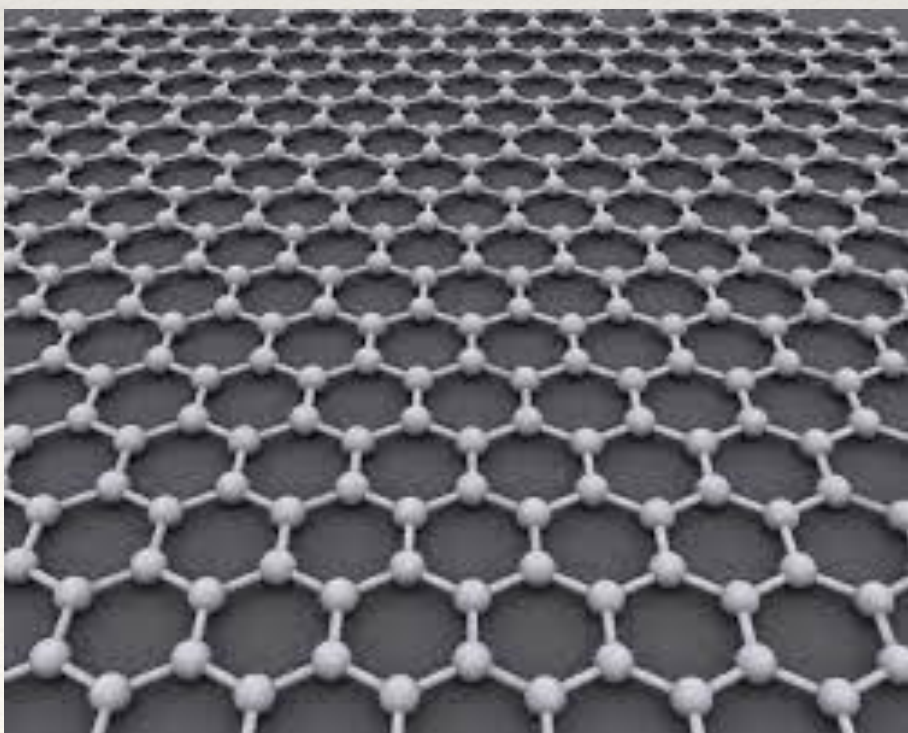
- ❖ Direction of DM wind changes throughout the day
- ❖ Experiments sensitive to directionality can discriminate signal from background



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# DM induced electron ejections from graphene and nanotubes

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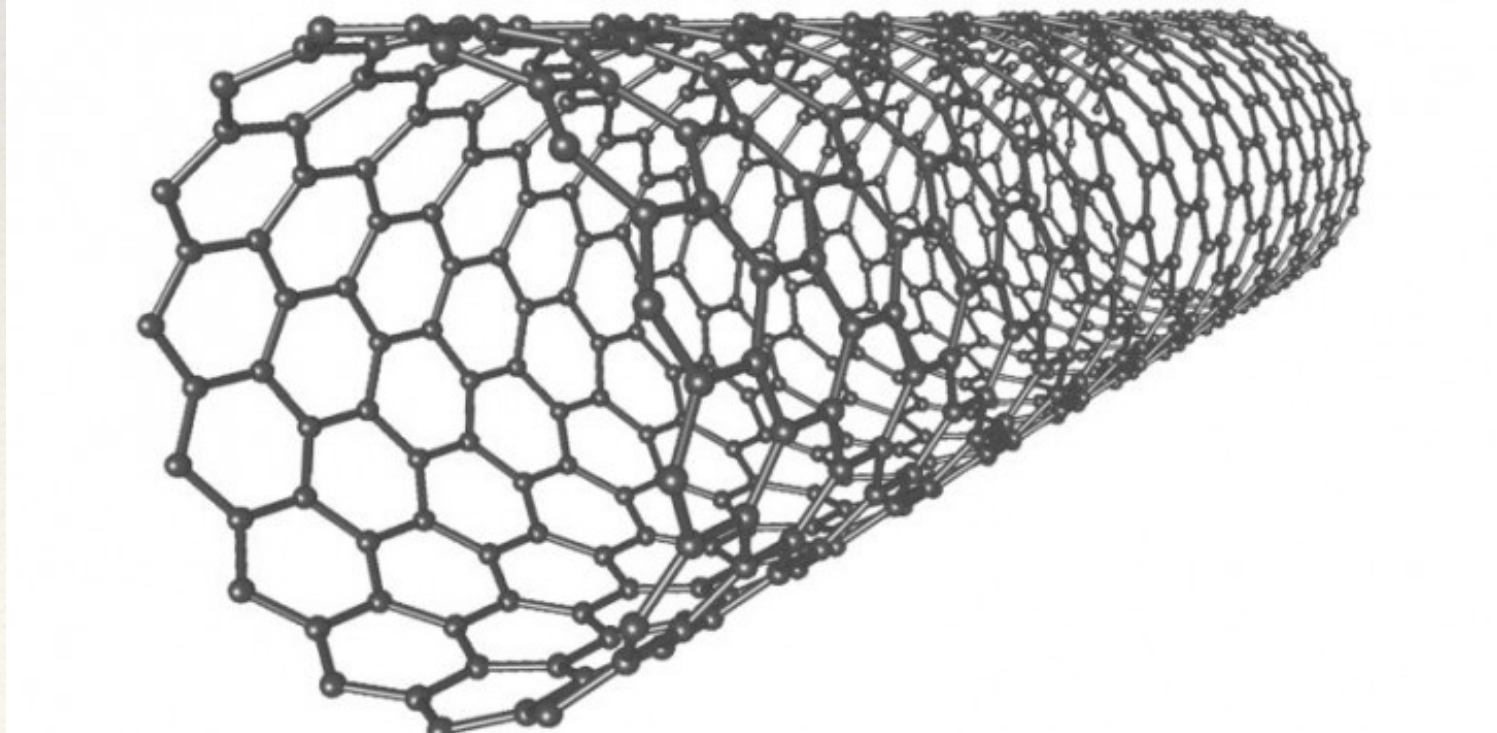
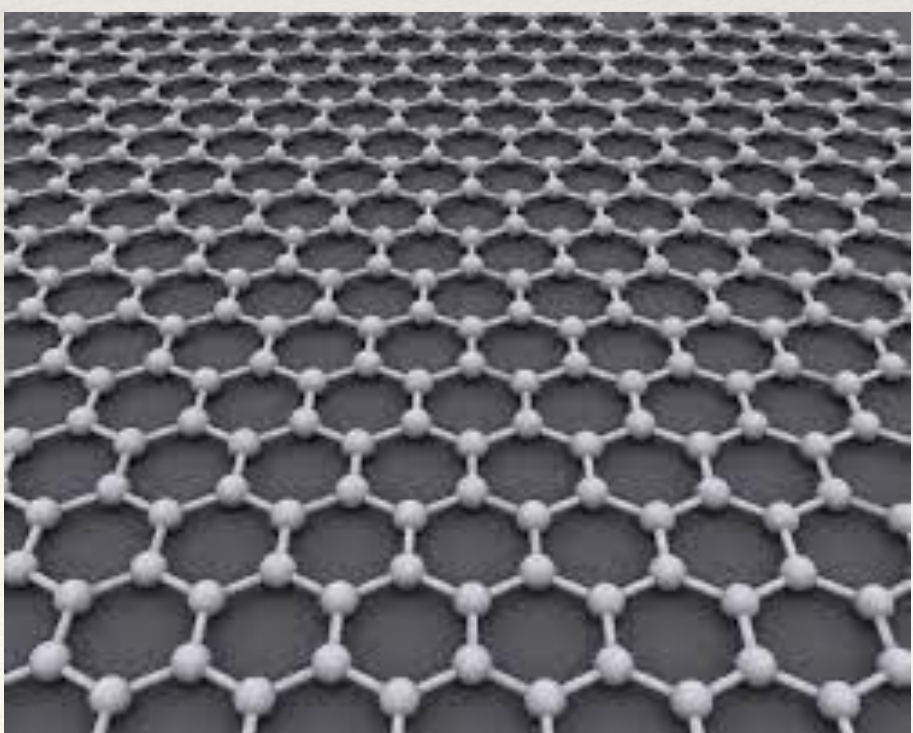


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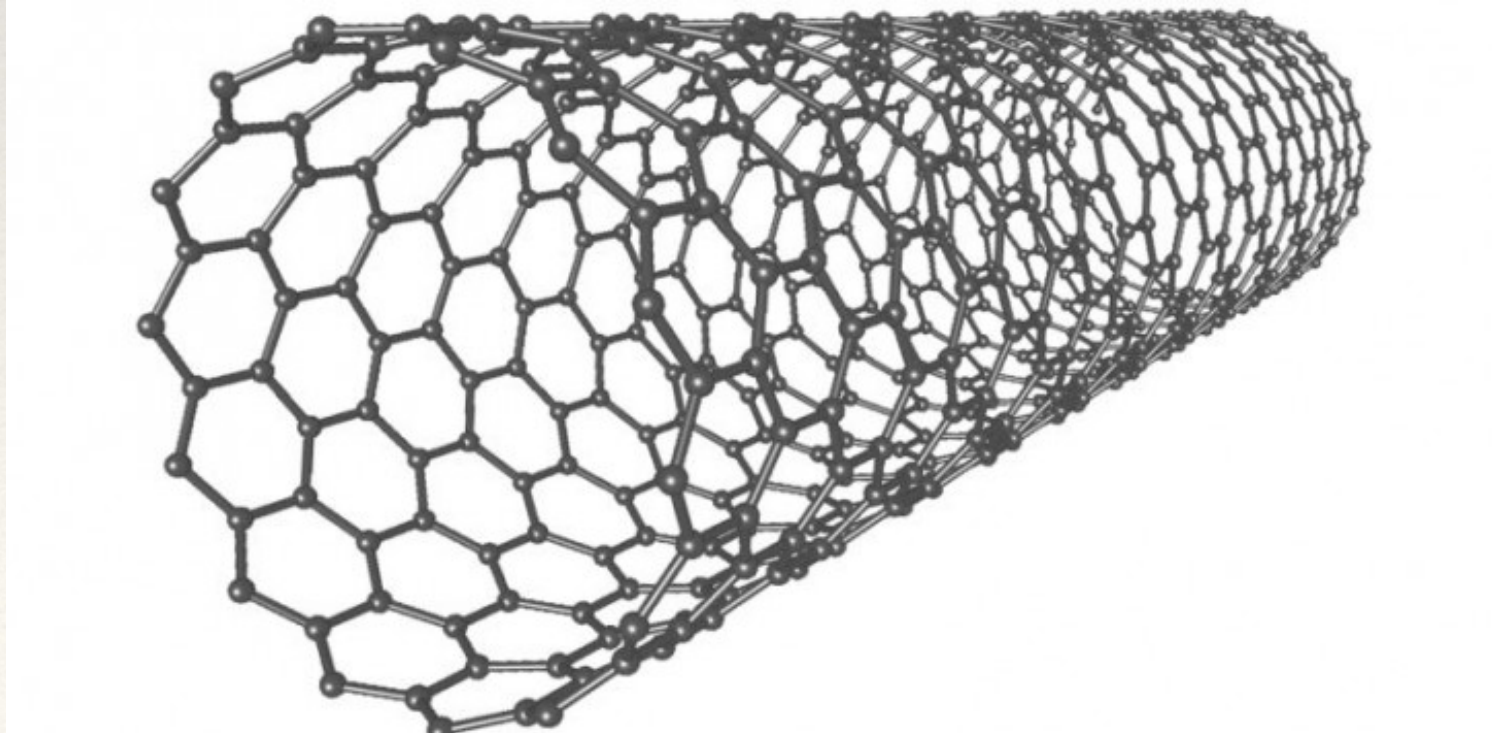
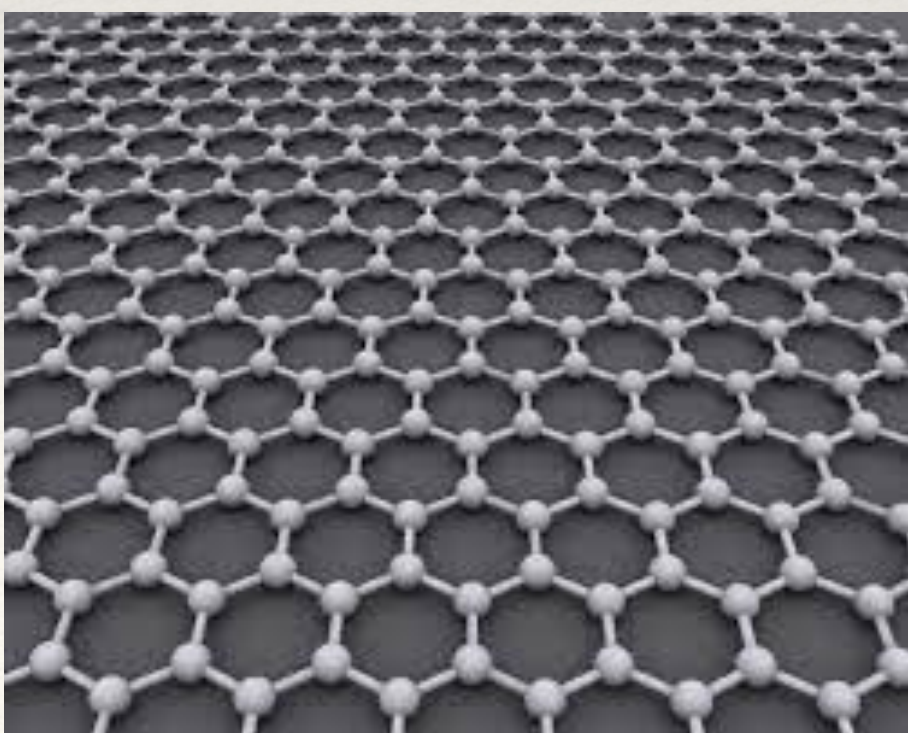
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- ❖ The materials have asymmetric electron momentum distributions



# DM induced electron ejections from graphene and nanotubes

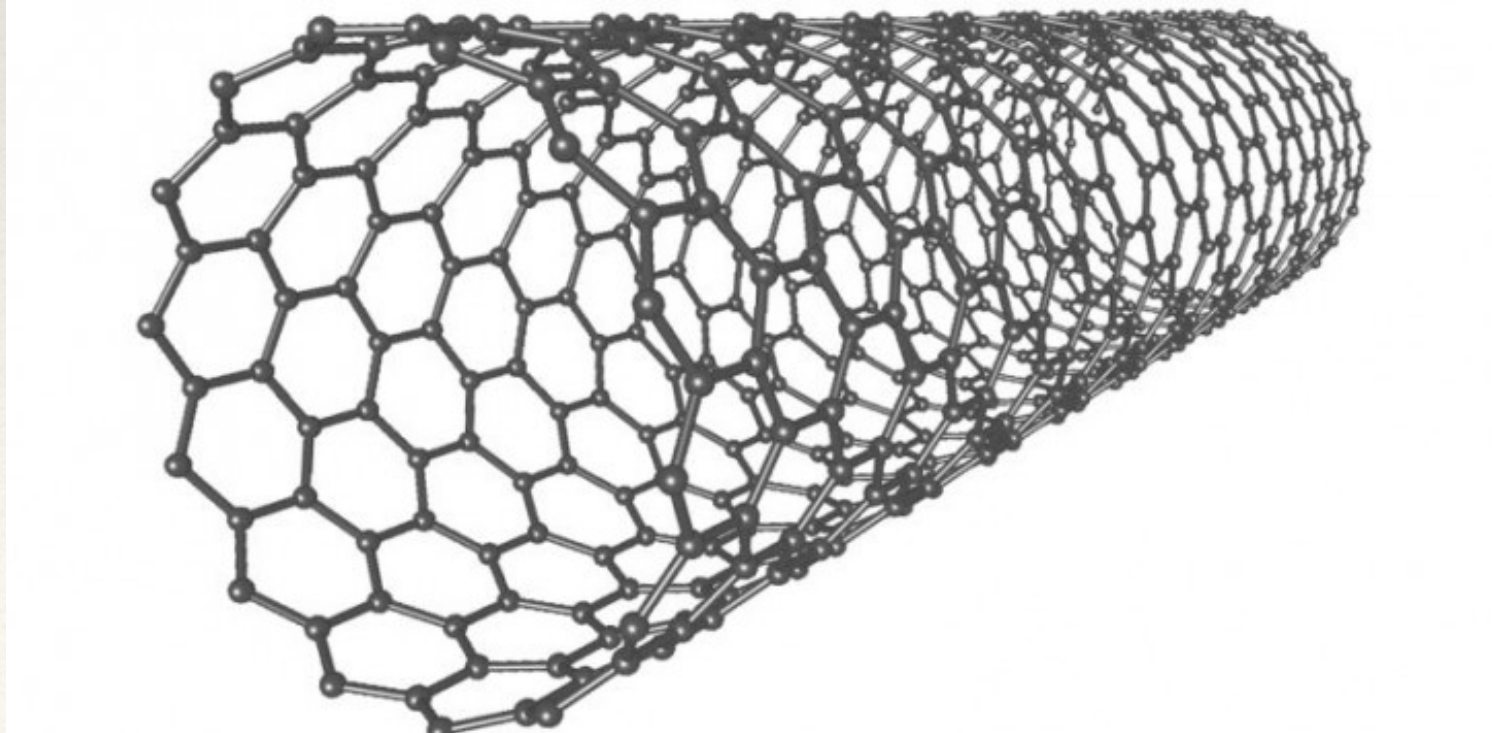
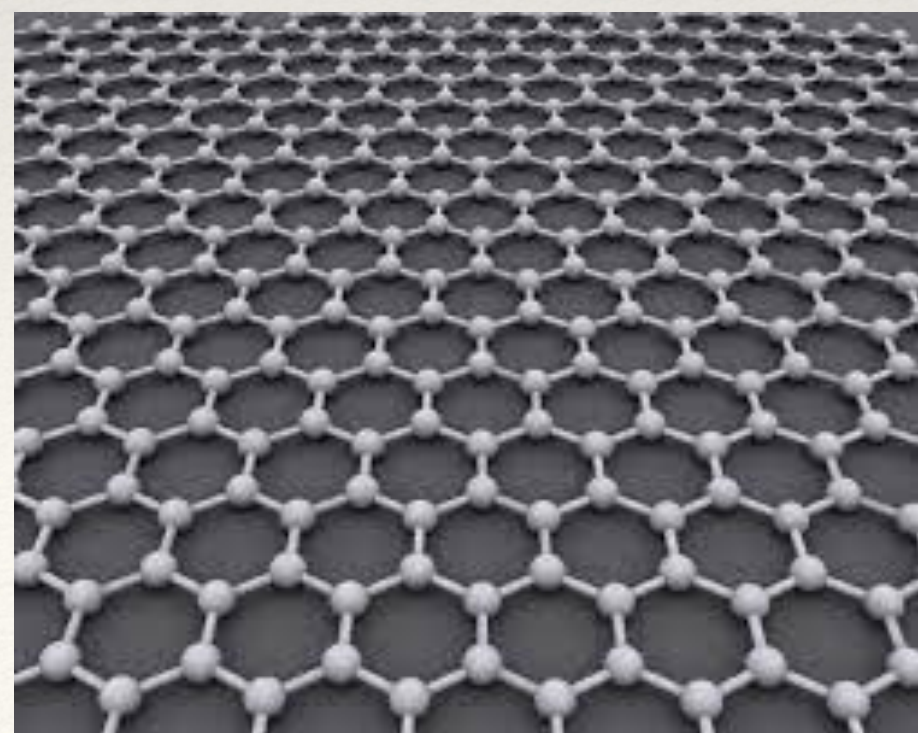
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- ❖ Electron scatterings are sensitive to DM masses down to a couple MeV



# DM induced electron ejections from graphene and nanotubes

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- ❖ Electron scatterings are sensitive to DM masses down to a couple MeV
- ❖ Using NR-EFT to model arbitrary DM electron interactions, we find

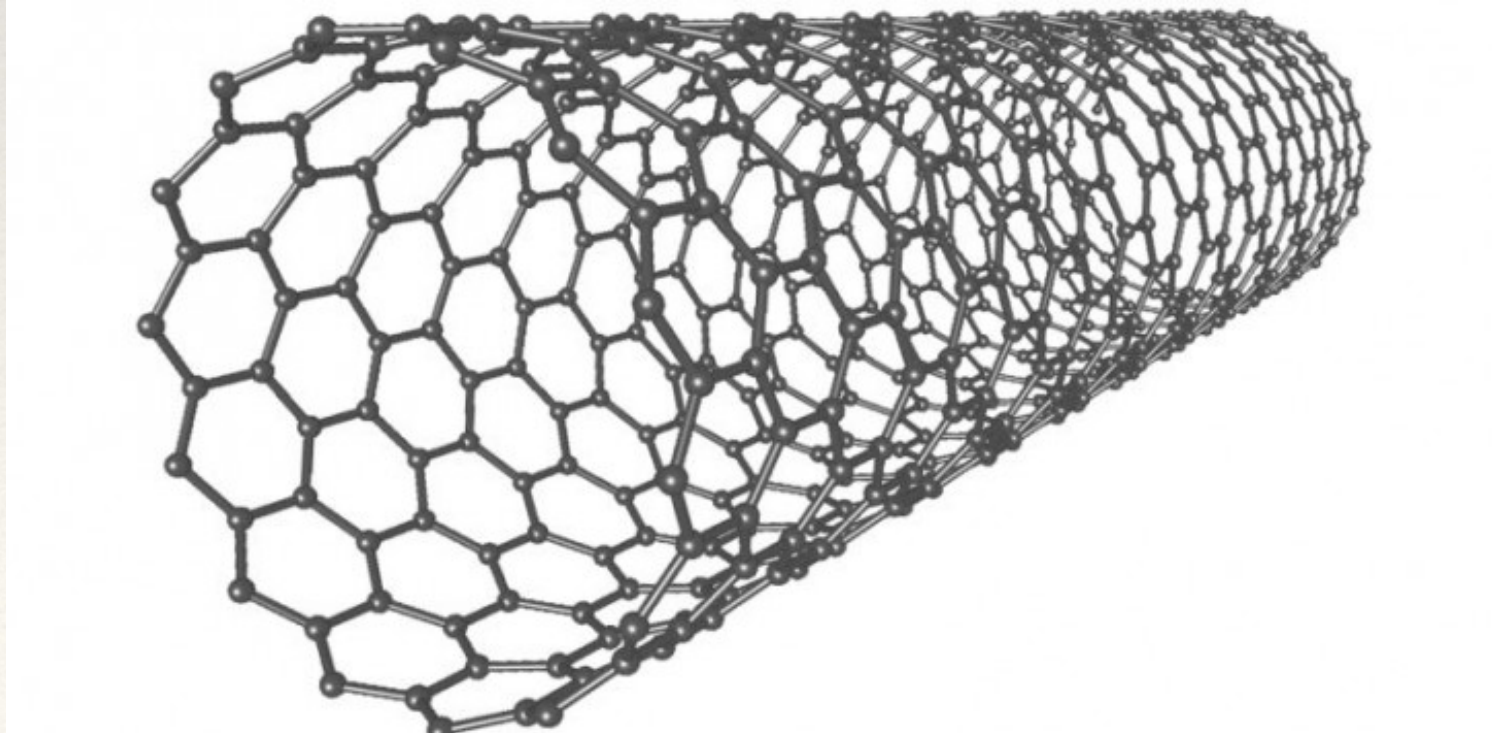
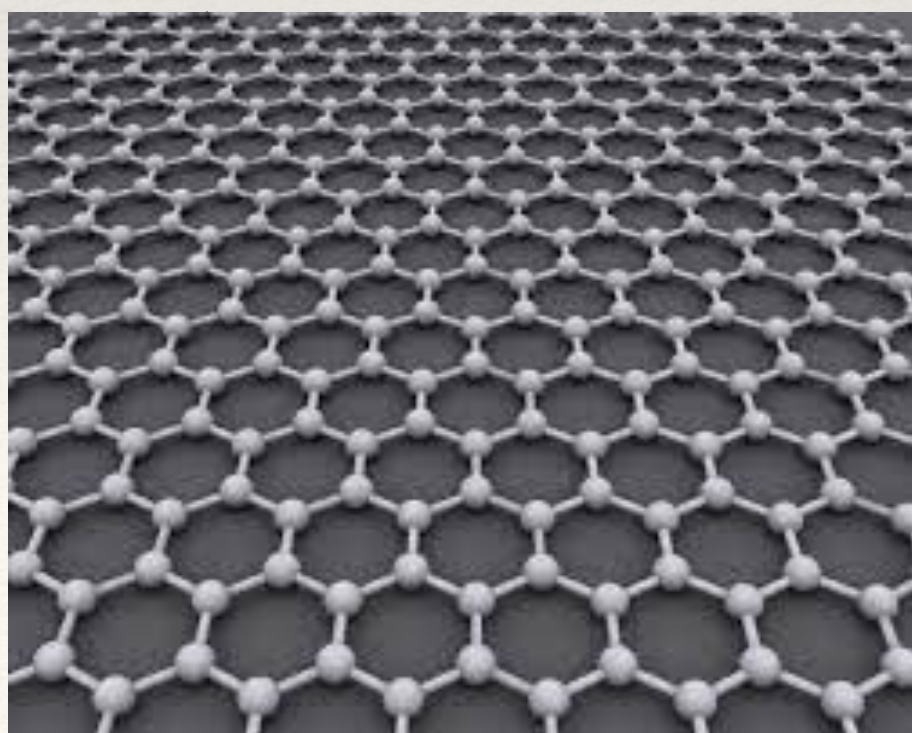
$$\left| \mathcal{M}_{1 \rightarrow 2} \right|^2 = \underbrace{R_{\text{free}}(\mathbf{k}', \mathbf{q}, \mathbf{v})}_{\text{DM particle physics}} \times \frac{1}{V} \underbrace{\left| \widetilde{\psi}_1(\mathbf{k}' - \mathbf{q}) \right|^2}_{\text{target properties}}$$



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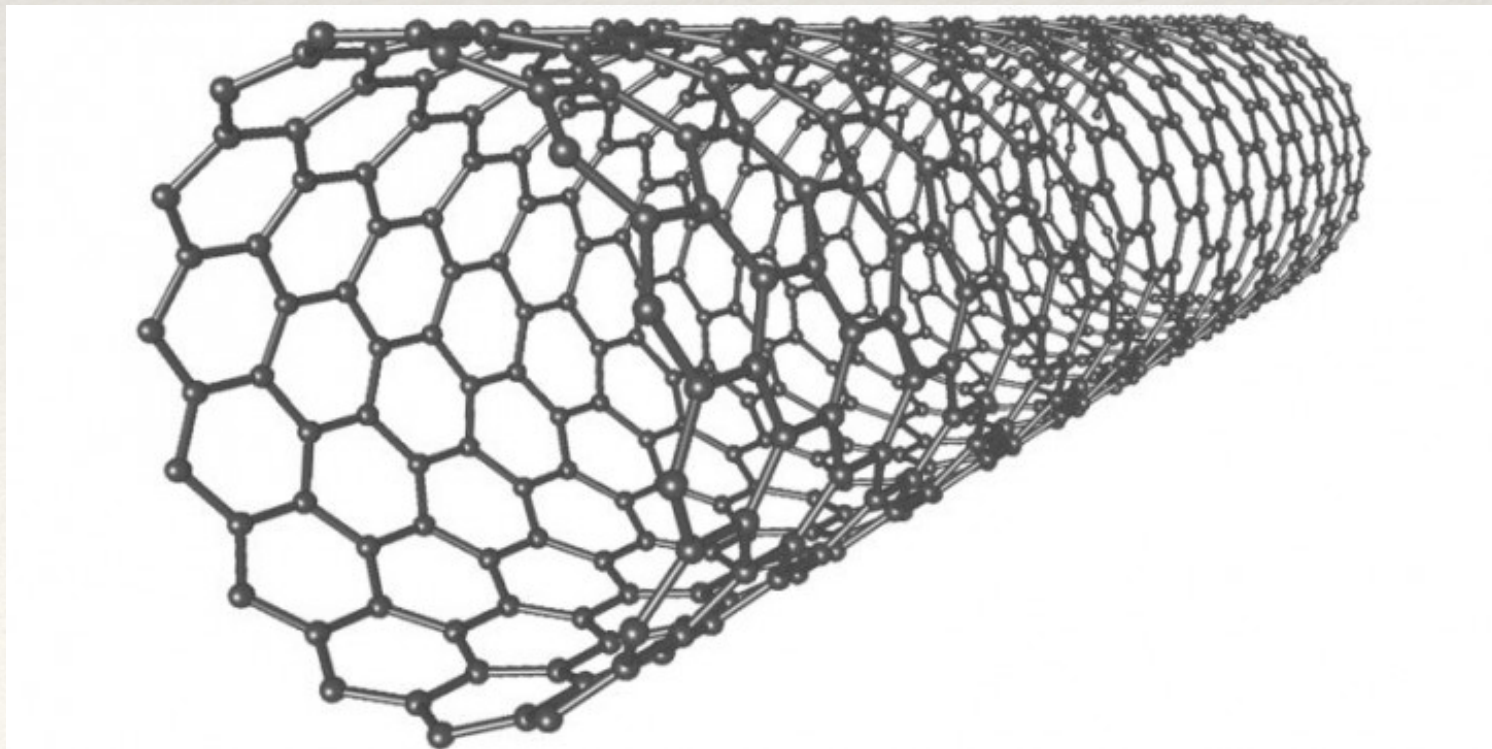
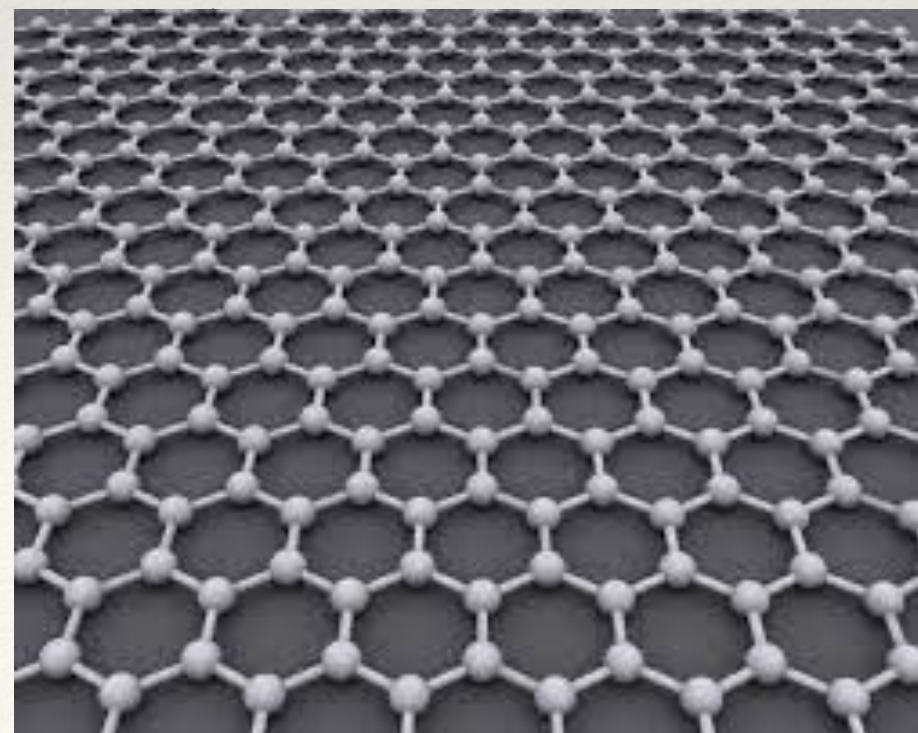


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Catena, Emken, Matas, Spaldin, EU: Work in progress



$$\mathcal{O}_1 = \mathbb{1}_{\chi e}$$

$$\mathcal{O}_3 = i\mathbf{S}_e \cdot \left( \frac{\mathbf{q}}{m_e} \times \mathbf{v}_{\text{el}}^\perp \right)$$

$$\mathcal{O}_4 = \mathbf{S}_\chi \cdot \mathbf{S}_e$$

$$\mathcal{O}_5 = i\mathbf{S}_\chi \cdot \left( \frac{\mathbf{q}}{m_e} \times \mathbf{v}_{\text{el}}^\perp \right)$$

$$\mathcal{O}_6 = \left( \mathbf{S}_\chi \cdot \frac{\mathbf{q}}{m_e} \right) \left( \mathbf{S}_e \cdot \frac{\mathbf{q}}{m_e} \right)$$

$$\mathcal{O}_7 = \mathbf{S}_e \cdot \mathbf{v}_{\text{el}}^\perp$$

$$\mathcal{O}_8 = \mathbf{S}_\chi \cdot \mathbf{v}_{\text{el}}^\perp$$

$$\mathcal{O}_9 = i\mathbf{S}_\chi \cdot \left( \mathbf{S}_e \times \frac{\mathbf{q}}{m_e} \right)$$

$$\mathcal{O}_{10} = i\mathbf{S}_e \cdot \frac{\mathbf{q}}{m_e}$$

$$\mathcal{O}_{11} = i\mathbf{S}_\chi \cdot \frac{\mathbf{q}}{m_e}$$

$$\mathcal{O}_{12} = \mathbf{S}_\chi \cdot \left( \mathbf{S}_e \times \mathbf{v}_{\text{el}}^\perp \right)$$

$$\mathcal{O}_{13} = i \left( \mathbf{S}_\chi \cdot \mathbf{v}_{\text{el}}^\perp \right) \left( \mathbf{S}_e \cdot \frac{\mathbf{q}}{m_e} \right)$$

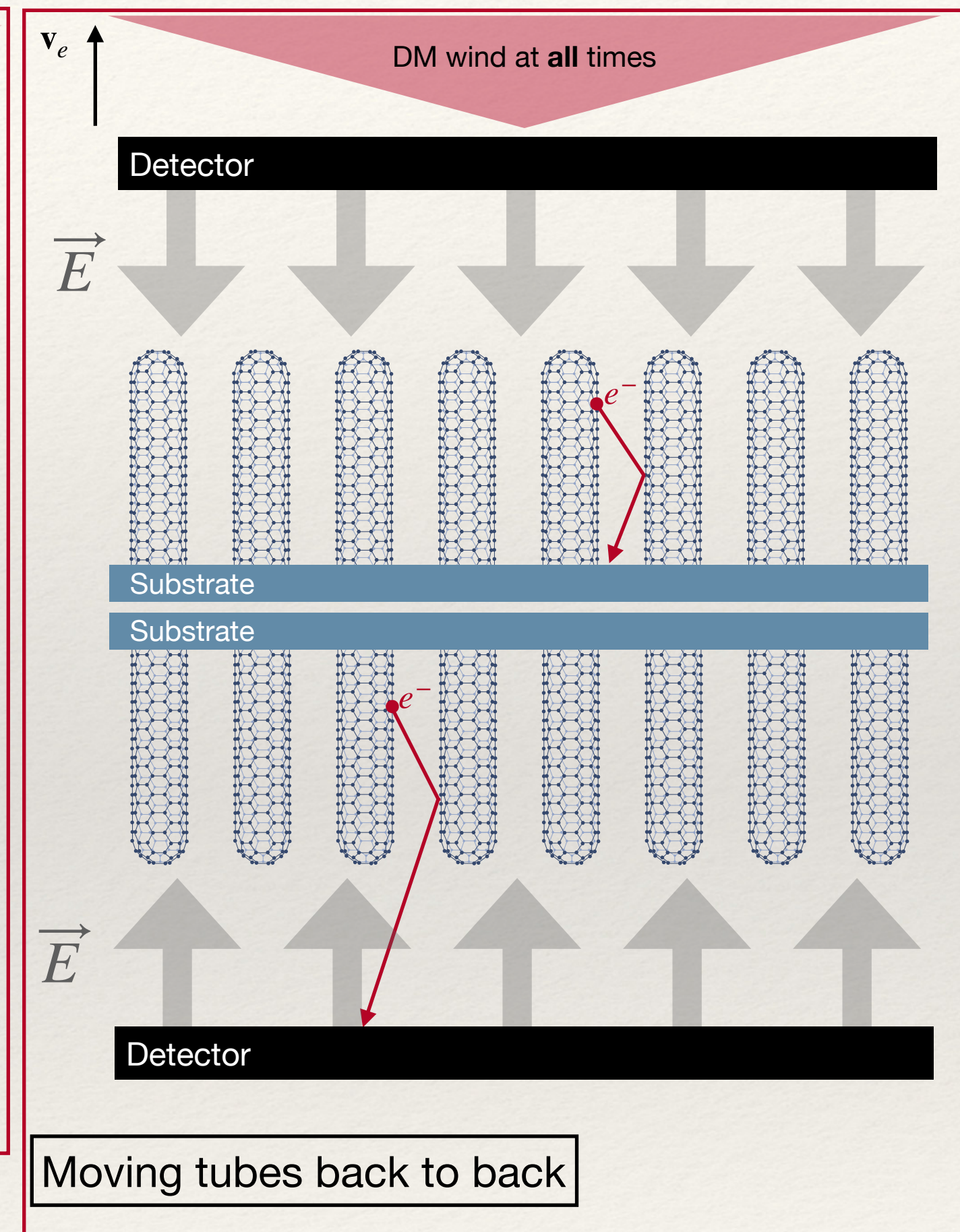
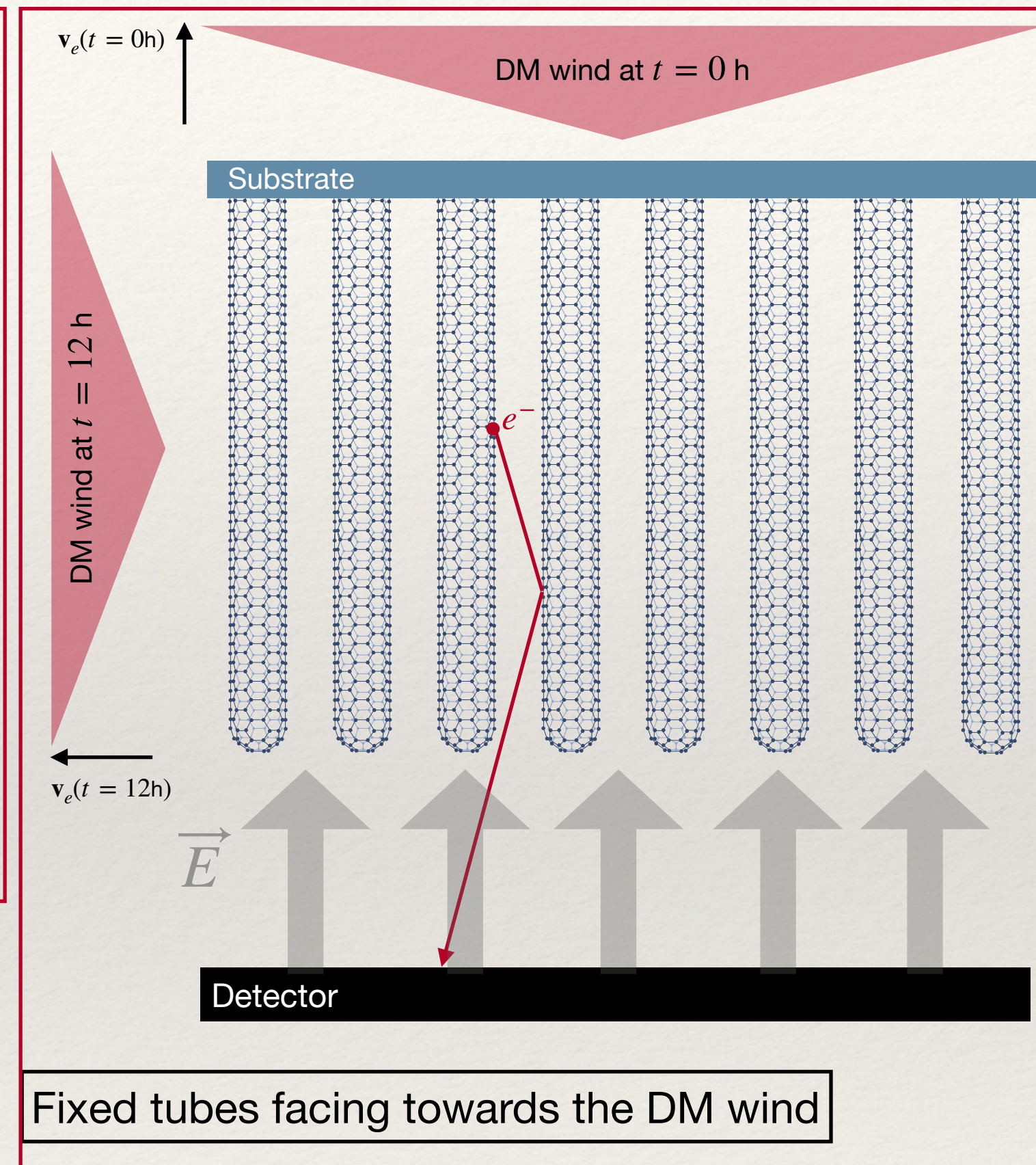
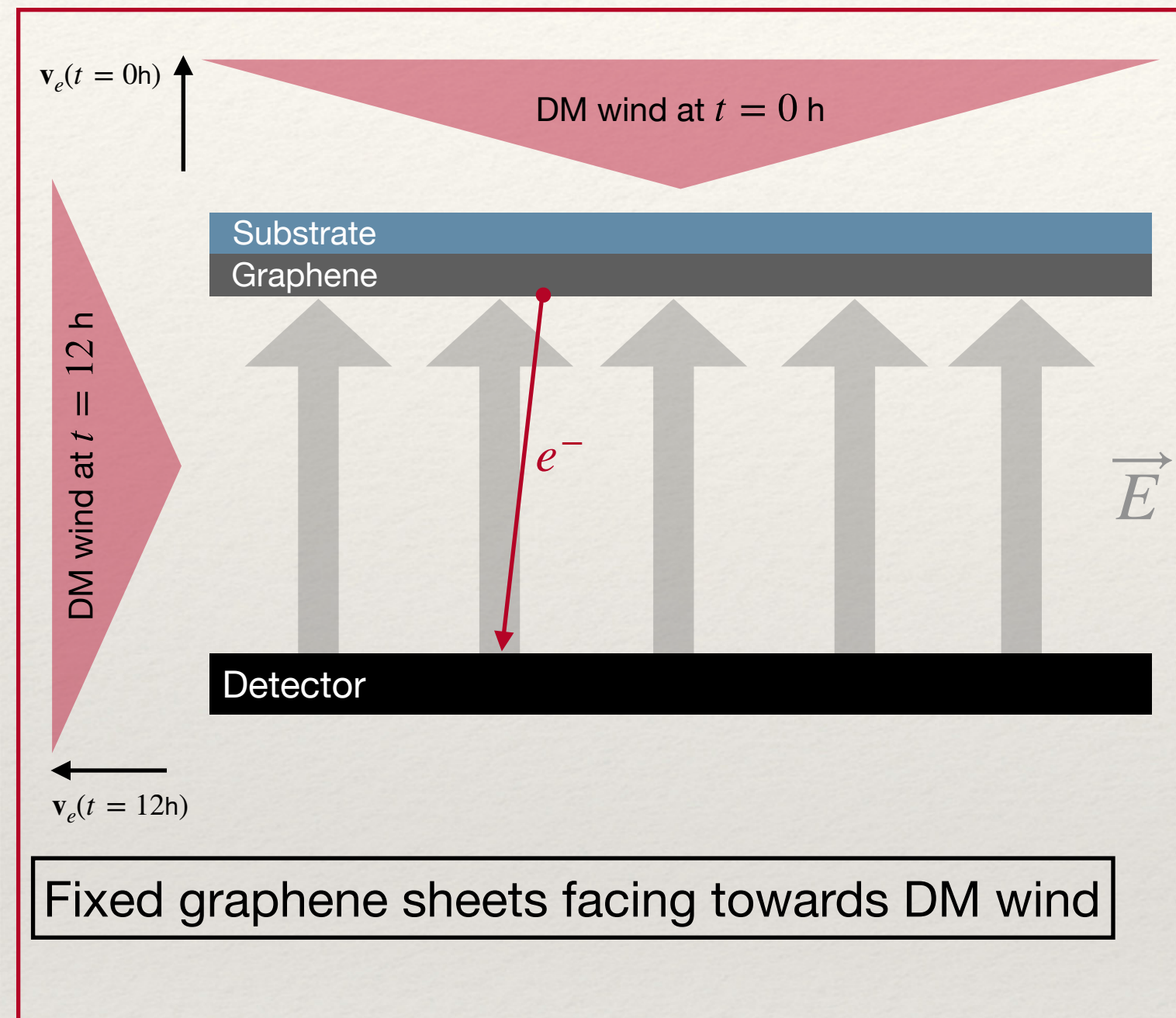
$$\mathcal{O}_{14} = i \left( \mathbf{S}_\chi \cdot \frac{\mathbf{q}}{m_e} \right) \left( \mathbf{S}_e \cdot \mathbf{v}_{\text{el}}^\perp \right)$$

$$\mathcal{O}_{15} = i\mathcal{O}_{11} \left[ \left( \mathbf{S}_e \times \mathbf{v}_{\text{el}}^\perp \right) \cdot \frac{\mathbf{q}}{m_e} \right]$$

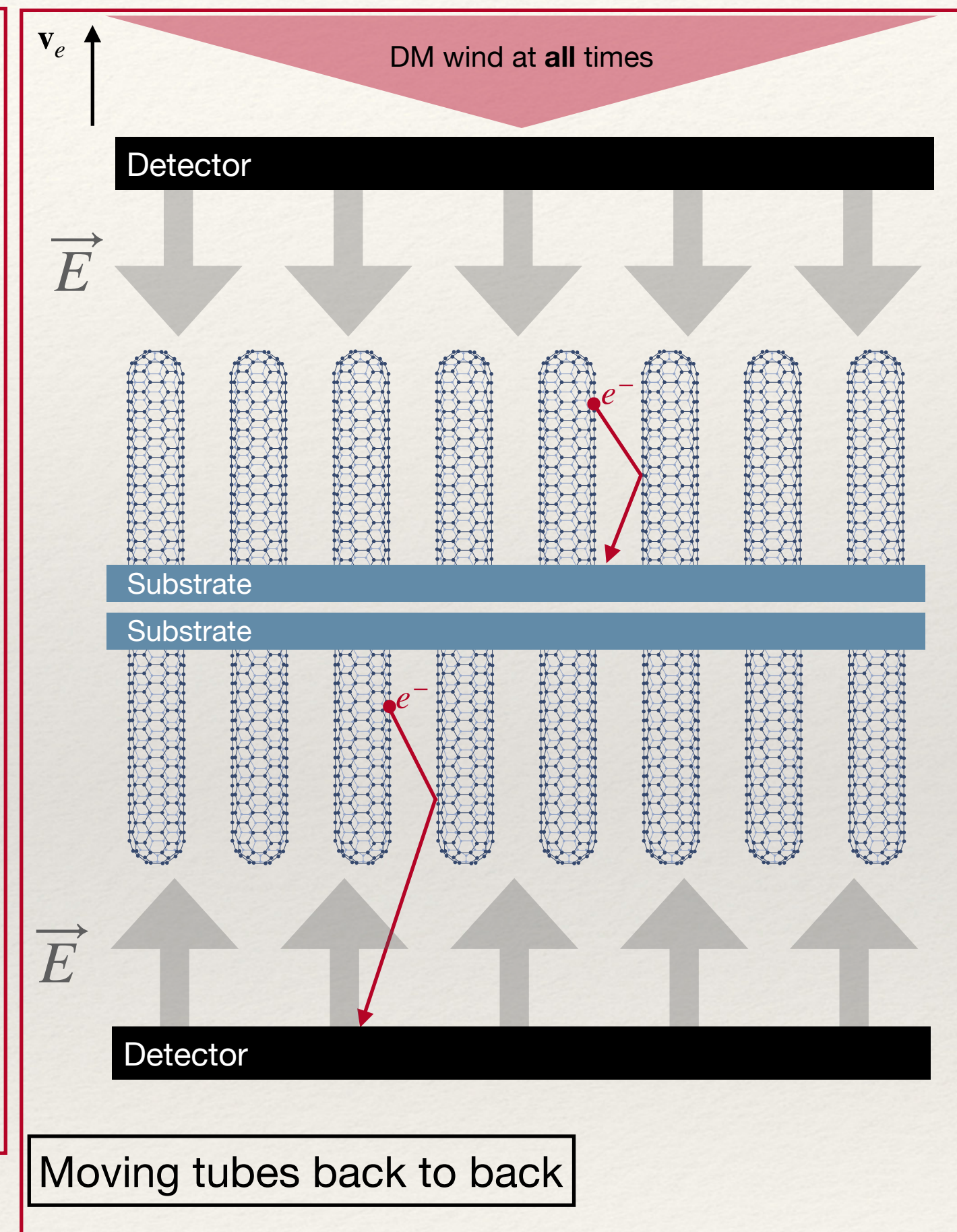
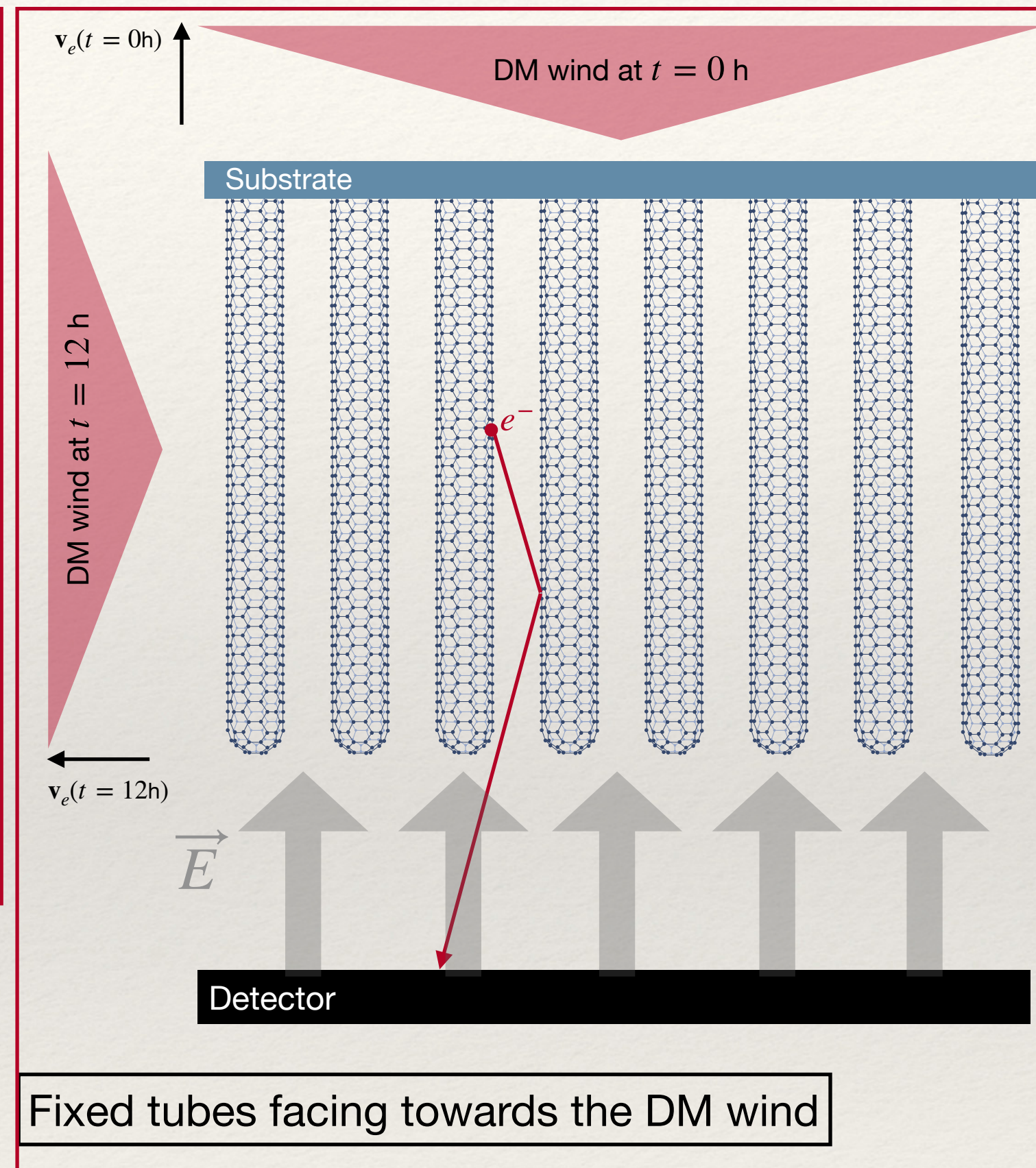
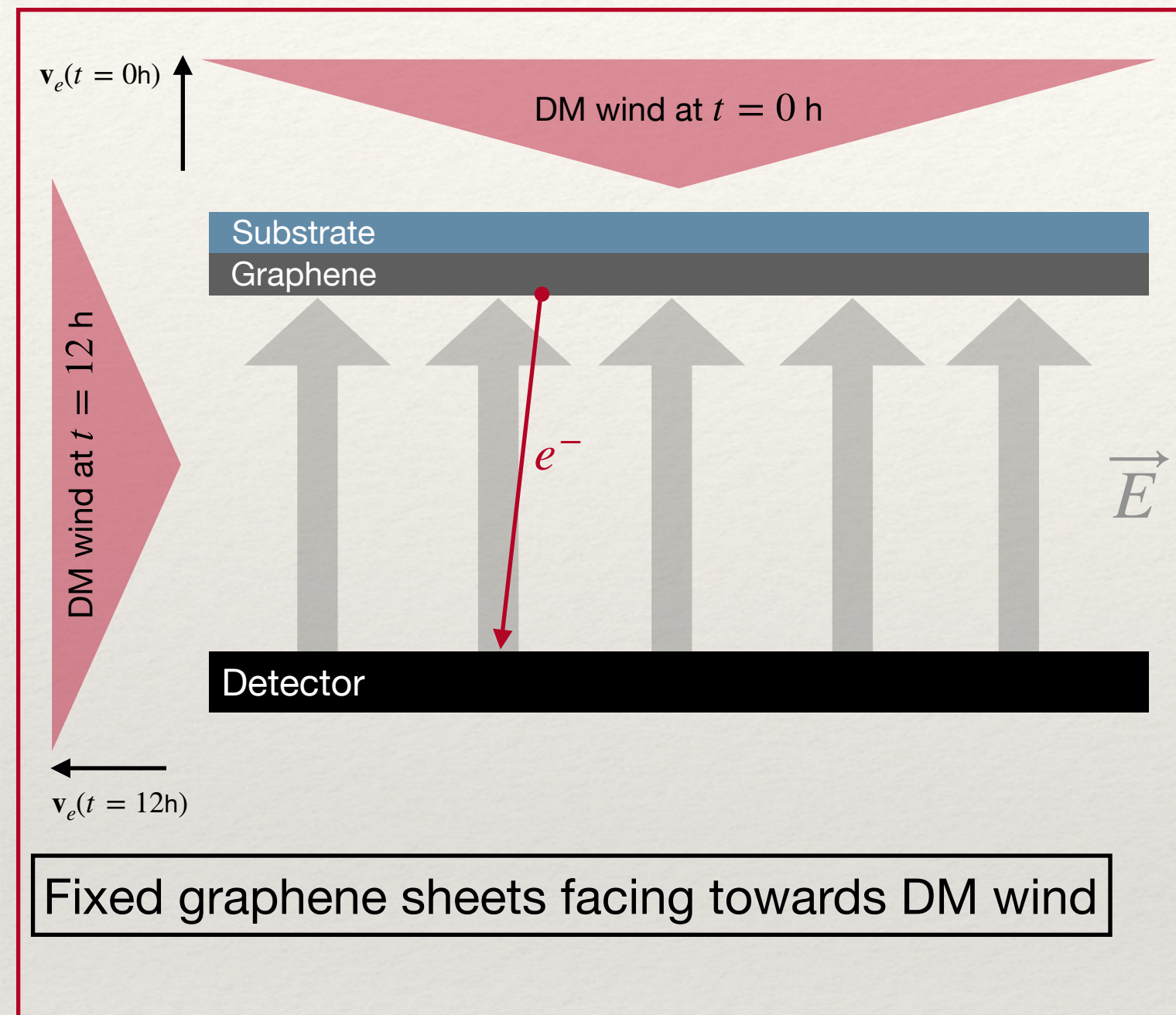




# Experimental setups



# Experimental setups



Setup considered  
by ANDROMEDA



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# Expected Sensitivity at 90% Confidence level

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- ❖ Record two numbers of events,  $N_{\max}$  and  $N_{\min}$  with the same expectation value if the signal is time or space symmetric.



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❖  $\chi^2 = \frac{(N_{\max} - N_{\min})^2}{N_{\max} + N_{\min} + N_b} > 2.71$  means we expect to be at least 90 % sure that  $N_{\max}$  and  $N_{\min}$  are not drawn from the same distribution.



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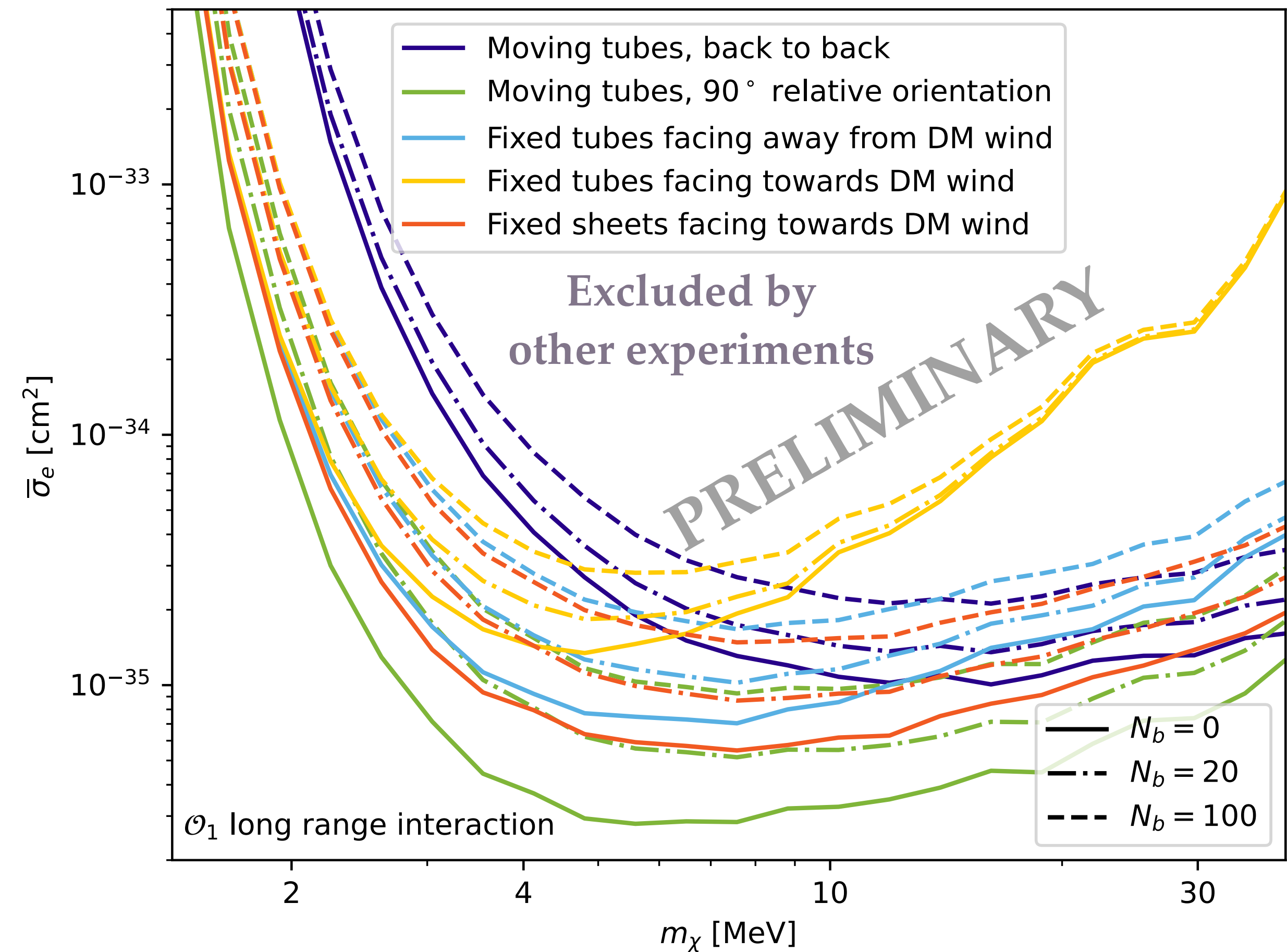
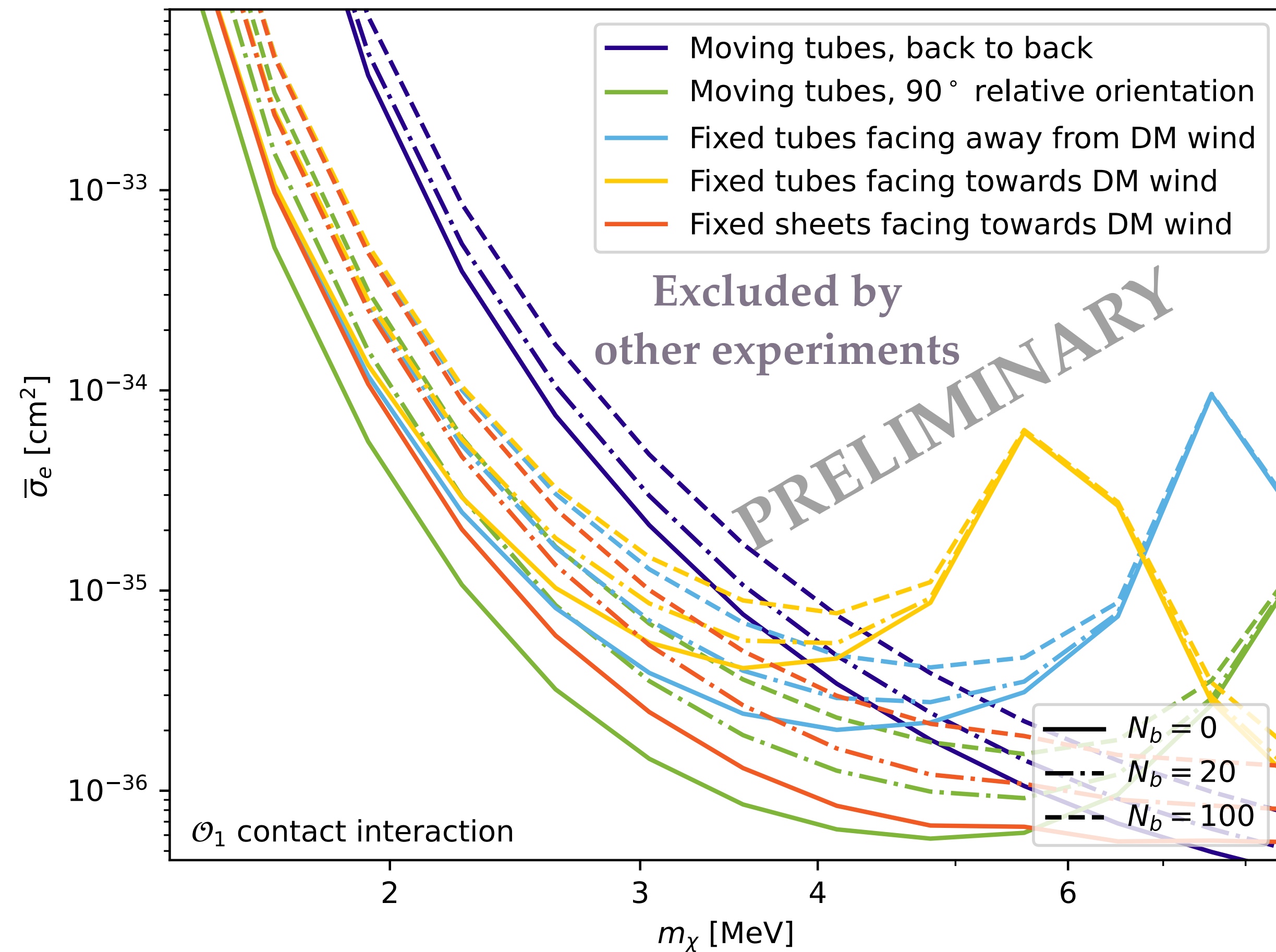
[Geilhufe, Kahlhoefer, Winkler: 1910.02091]



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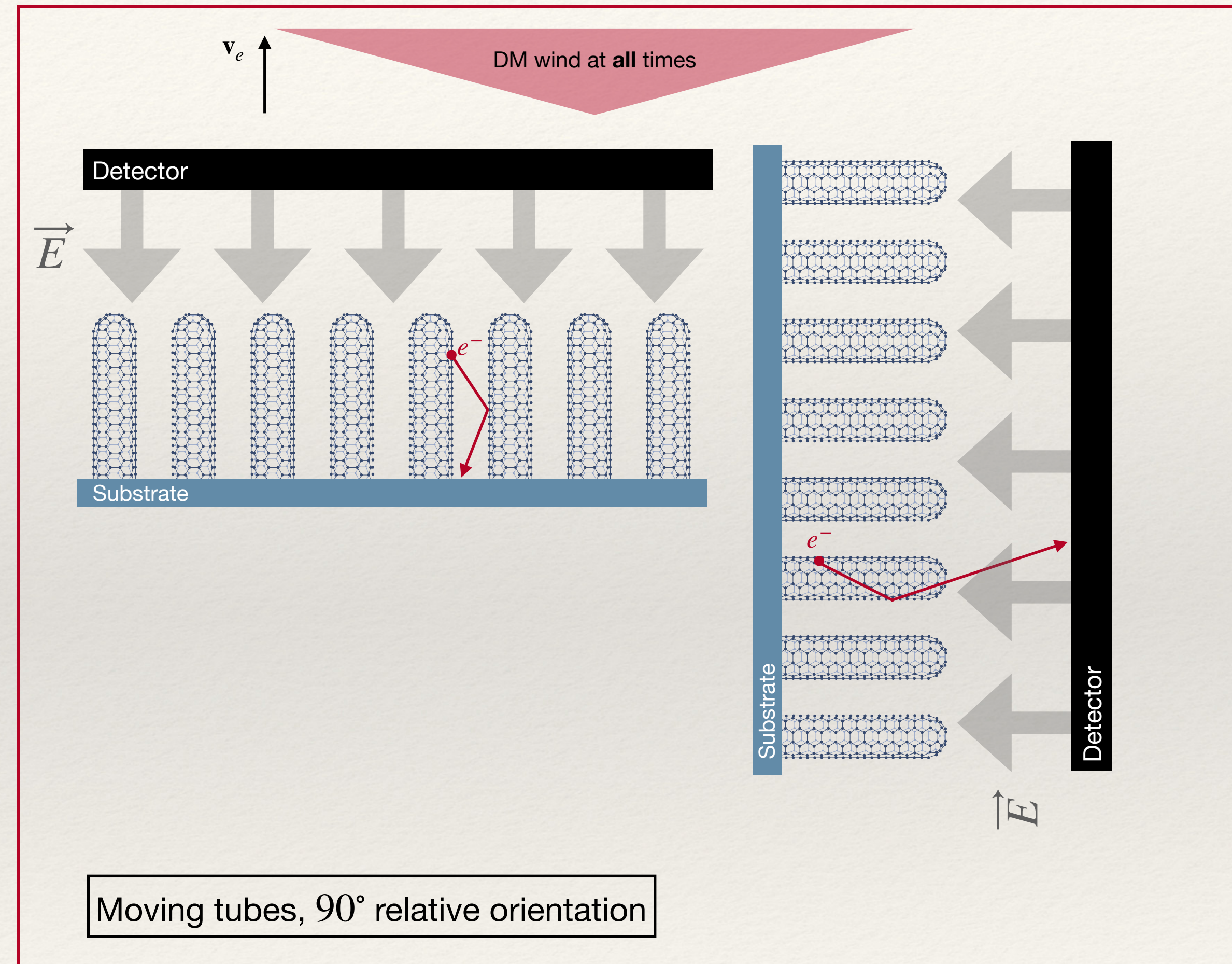
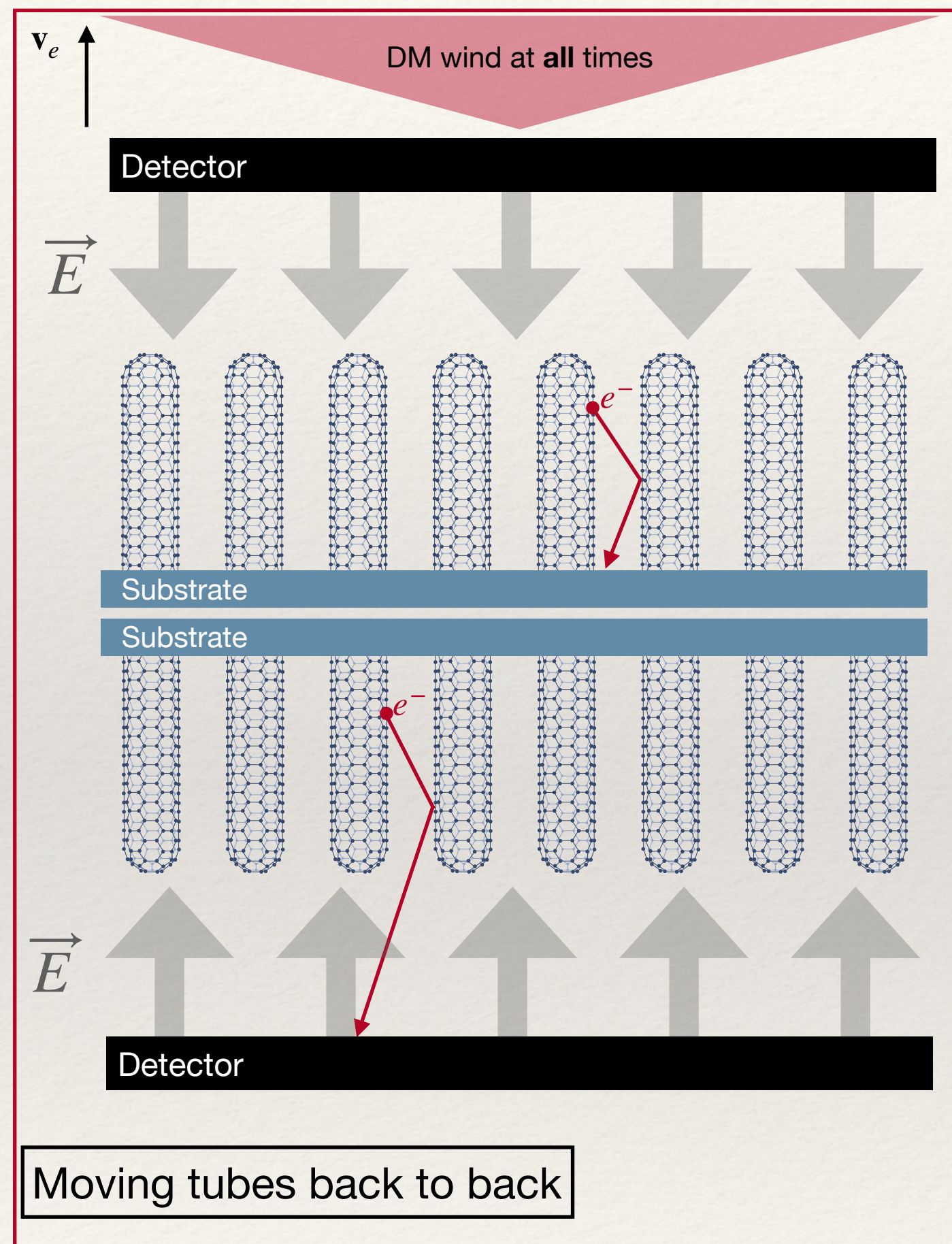


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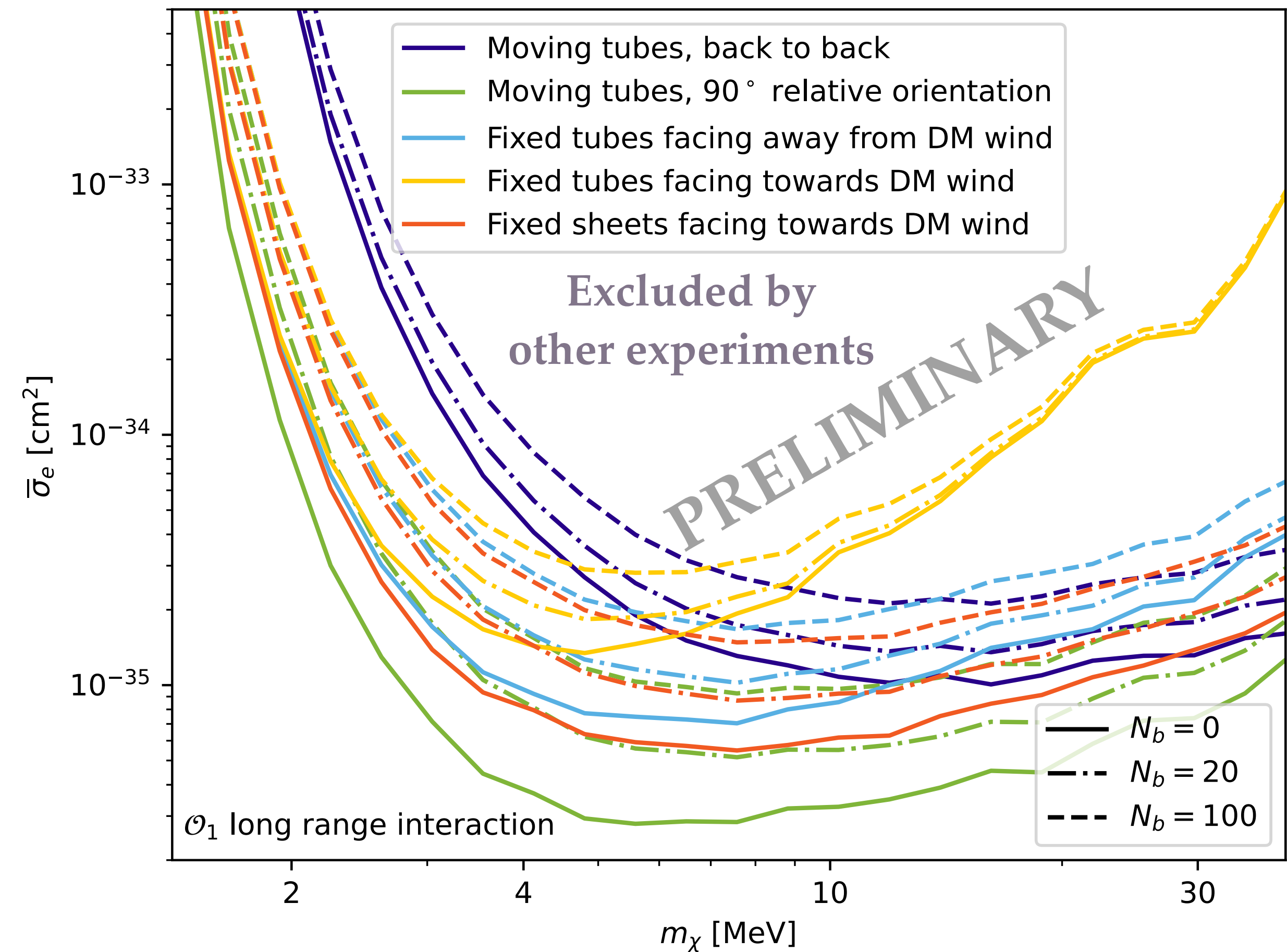
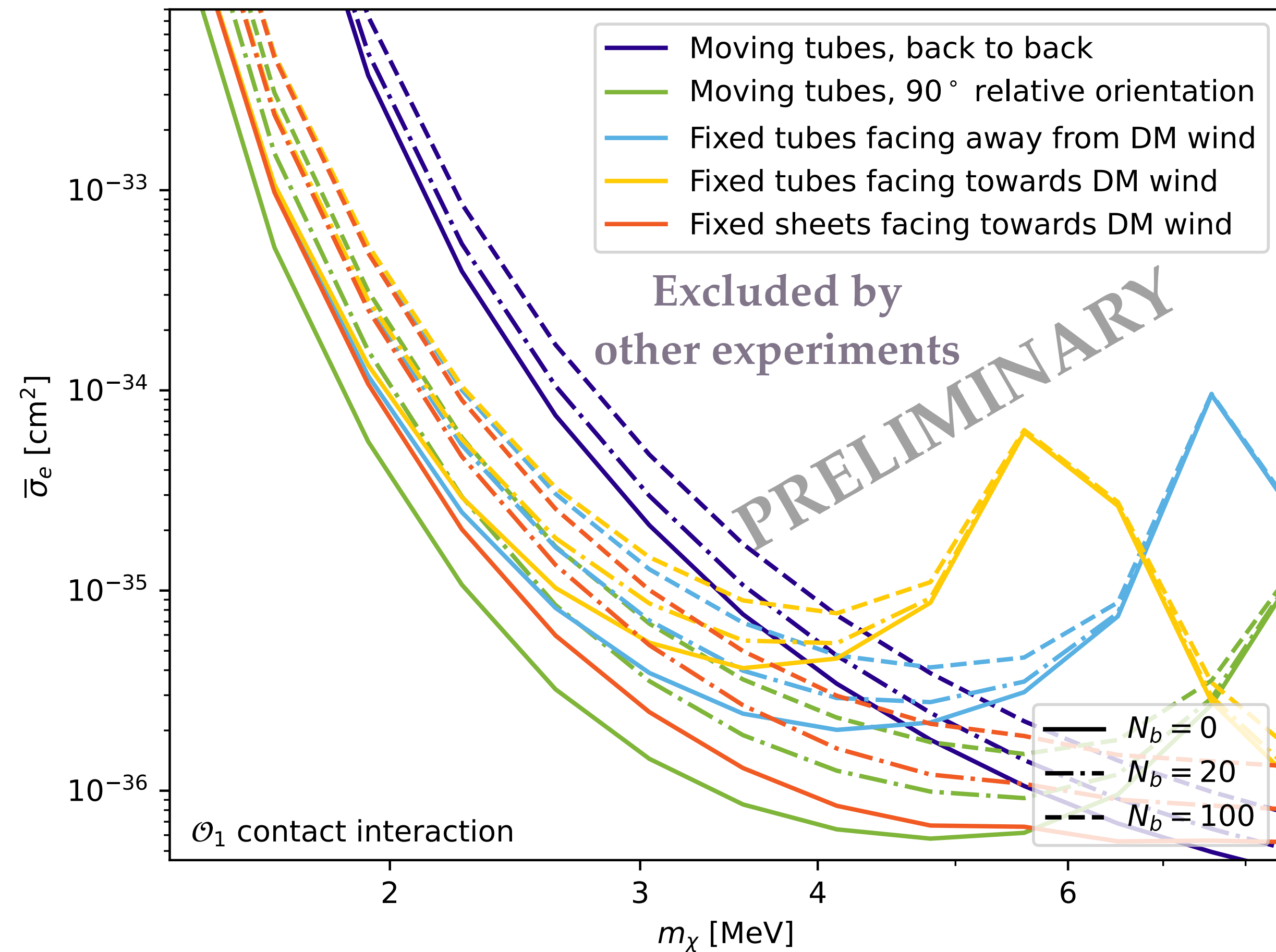


Assuming graphene / carbon nanotube exposure of 1g year

# Moving experimental setups



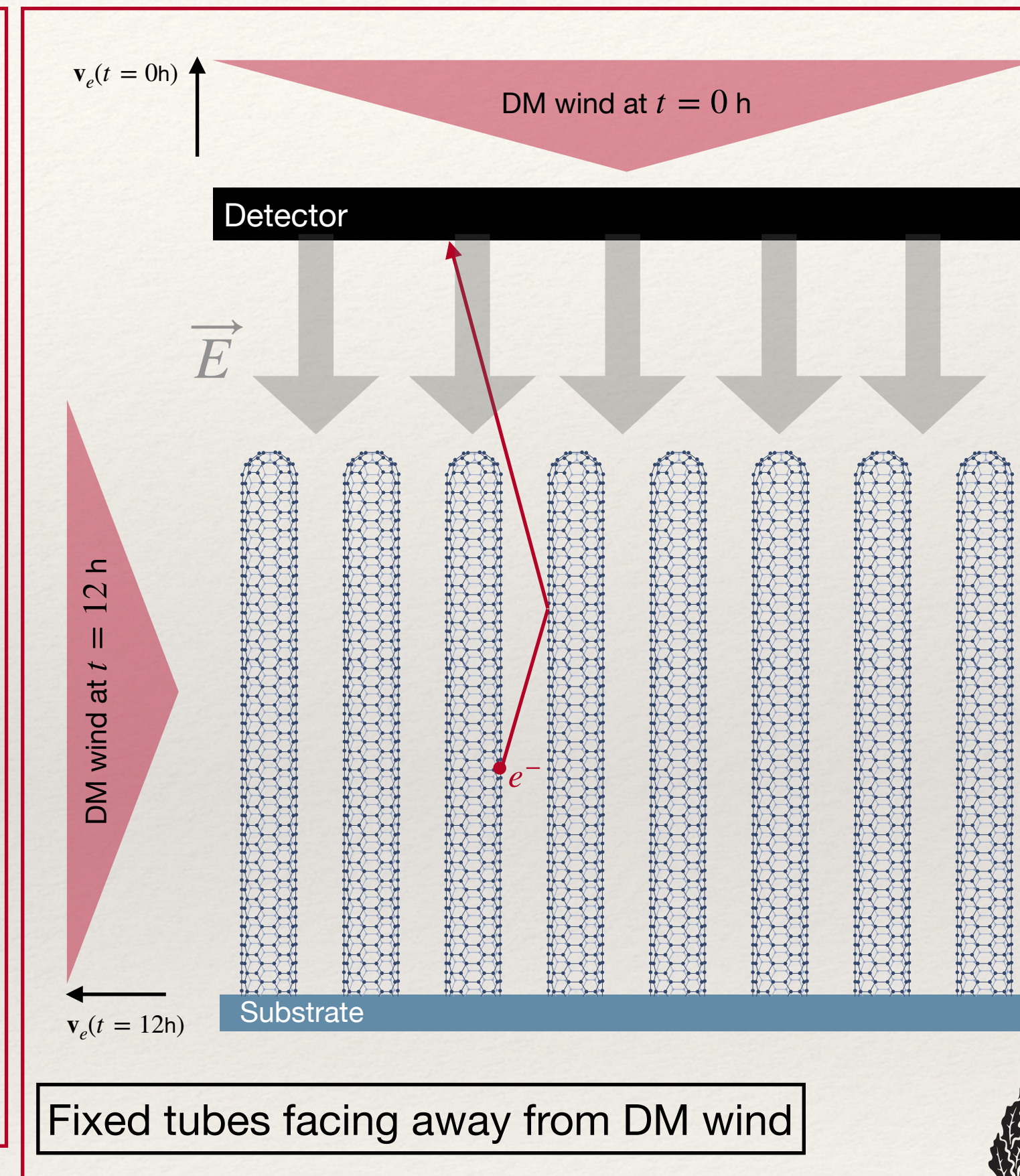
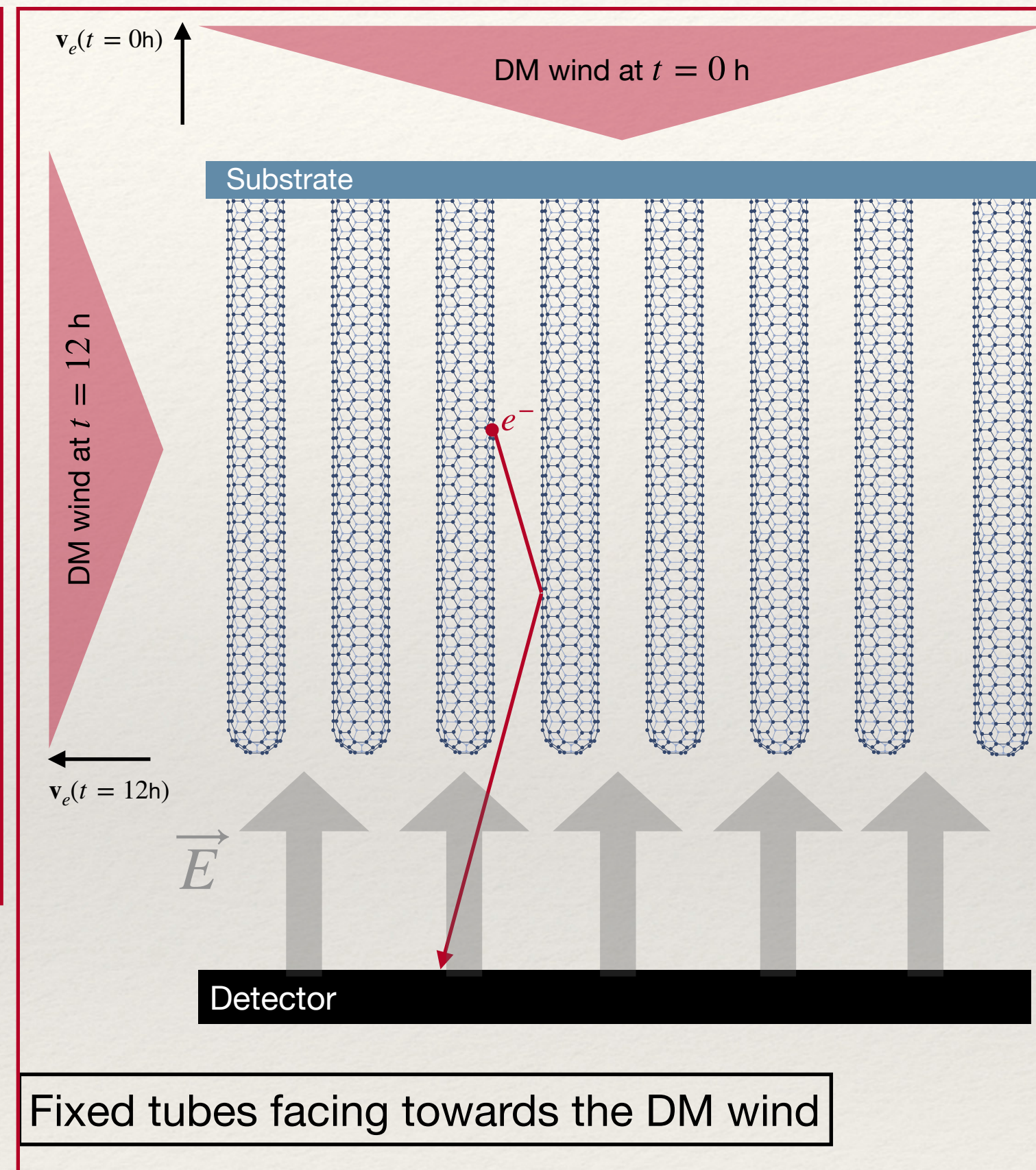
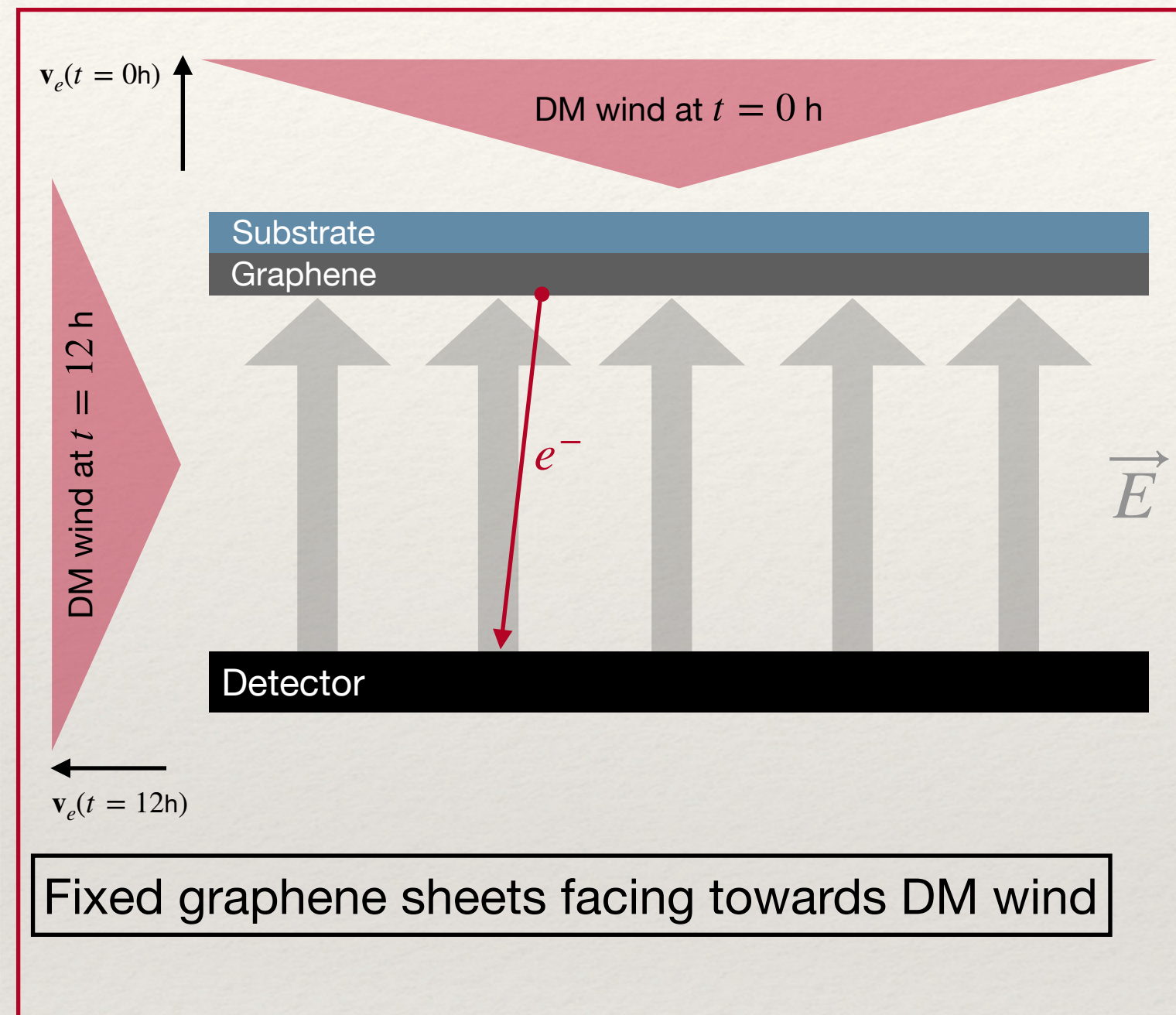
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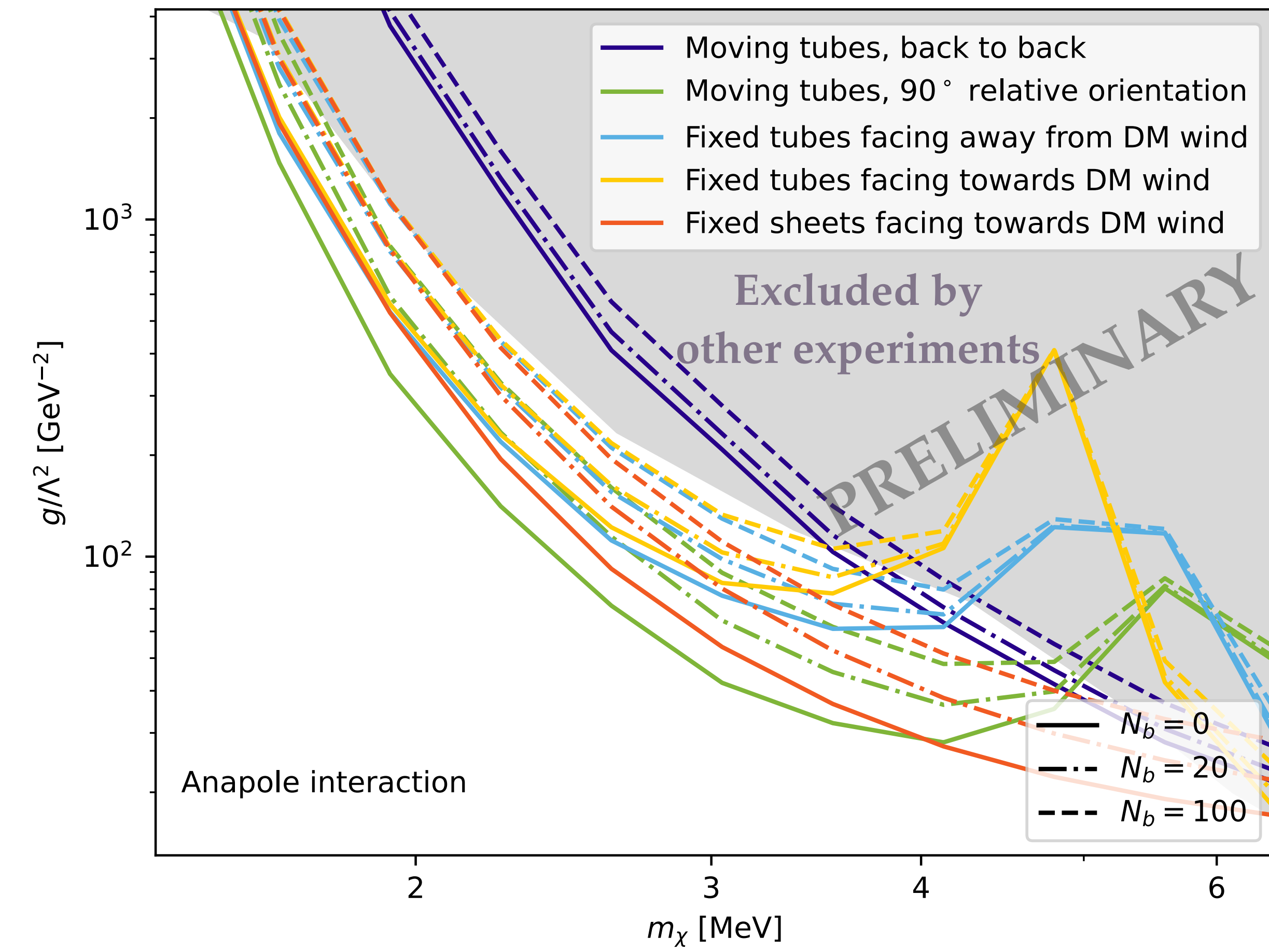
Assuming graphene / carbon nanotube exposure of 1g year



# Fixed experimental setups



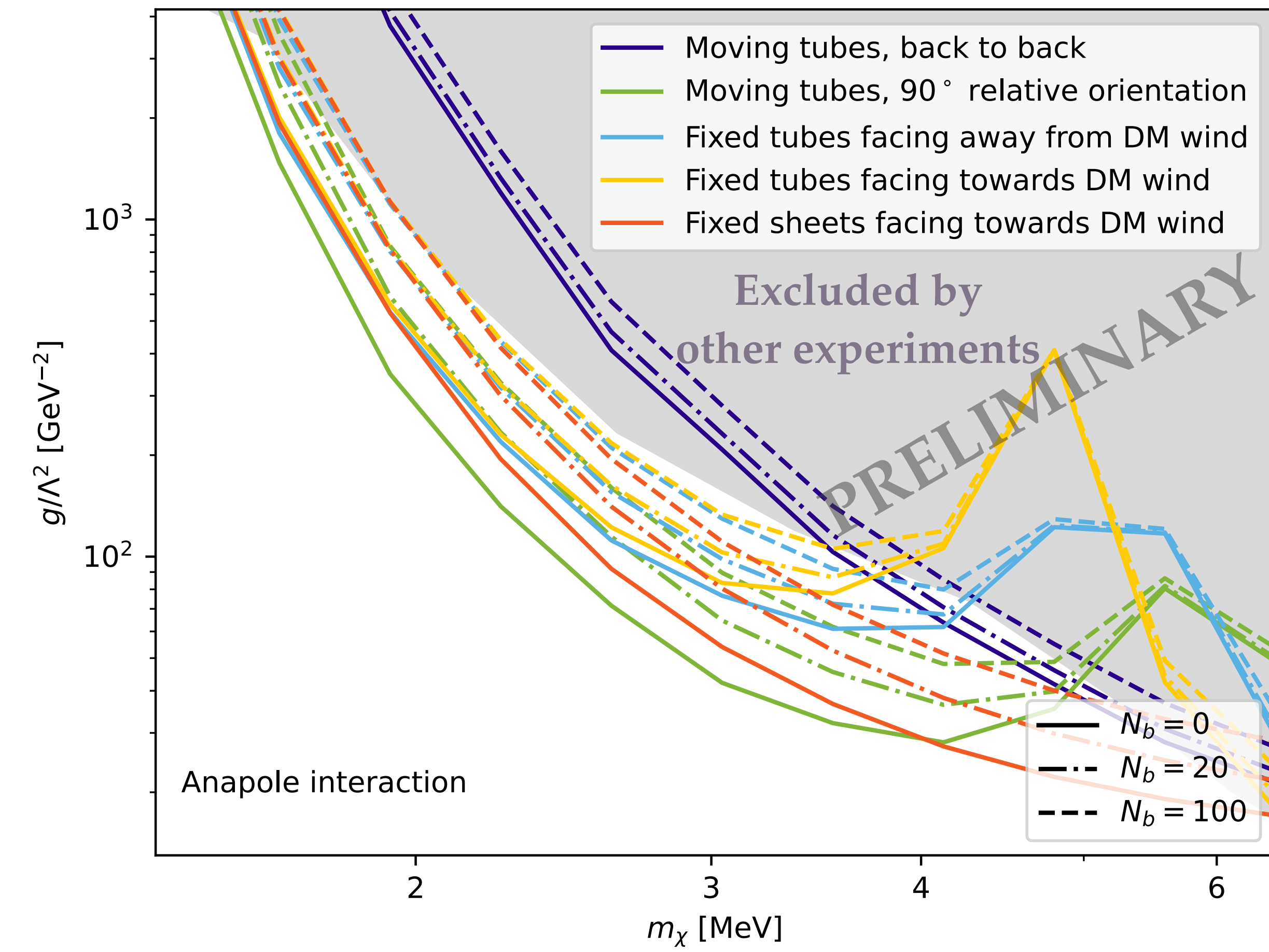
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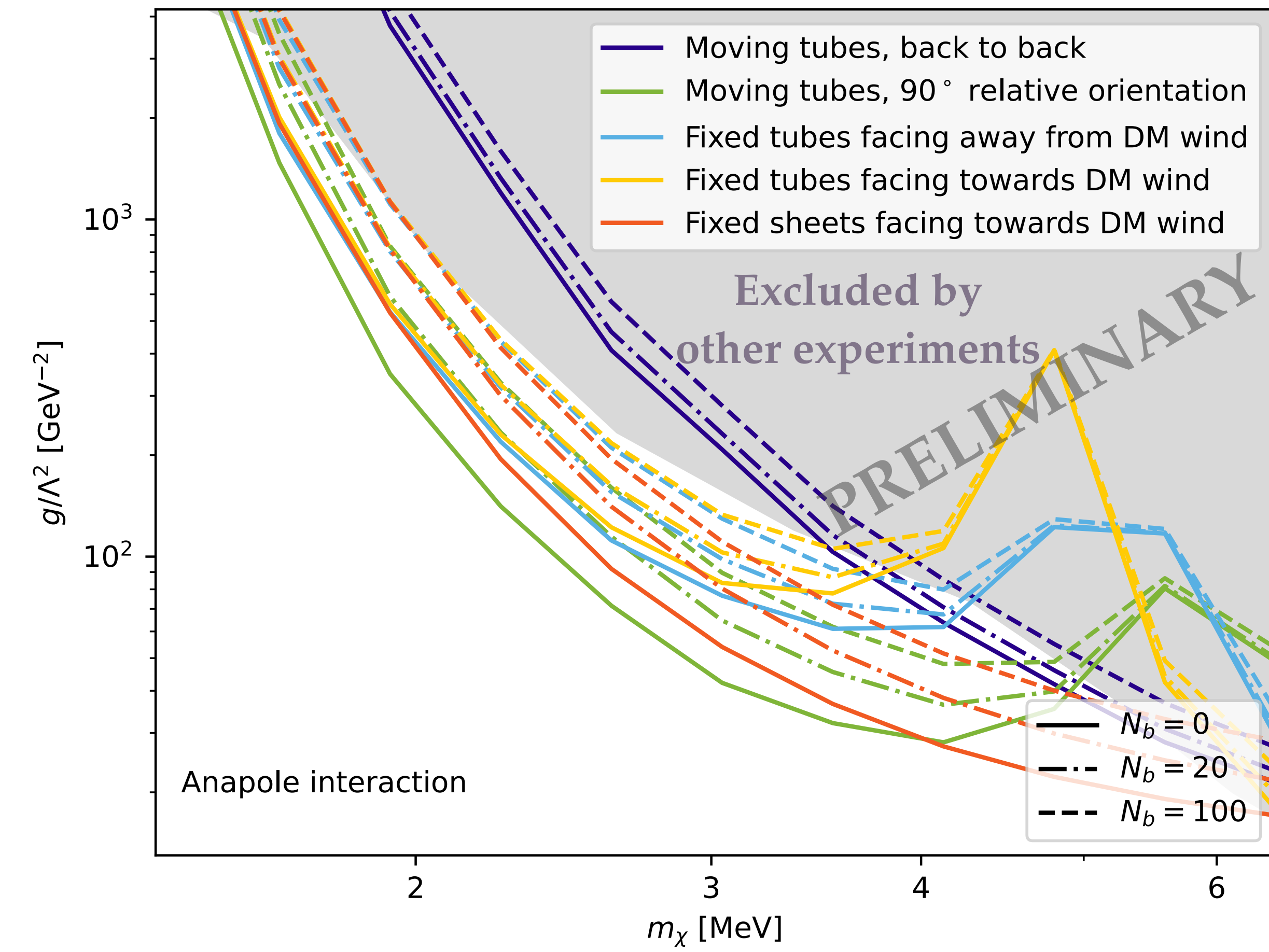
❖ Anapole interaction,

$$\mathcal{L}_{\text{int}} = \frac{g}{2\Lambda^2} \bar{\chi} \gamma^\mu \gamma^5 \chi \partial^\nu F_{\mu\nu}$$

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Assuming graphene / carbon nanotube exposure of 1g year

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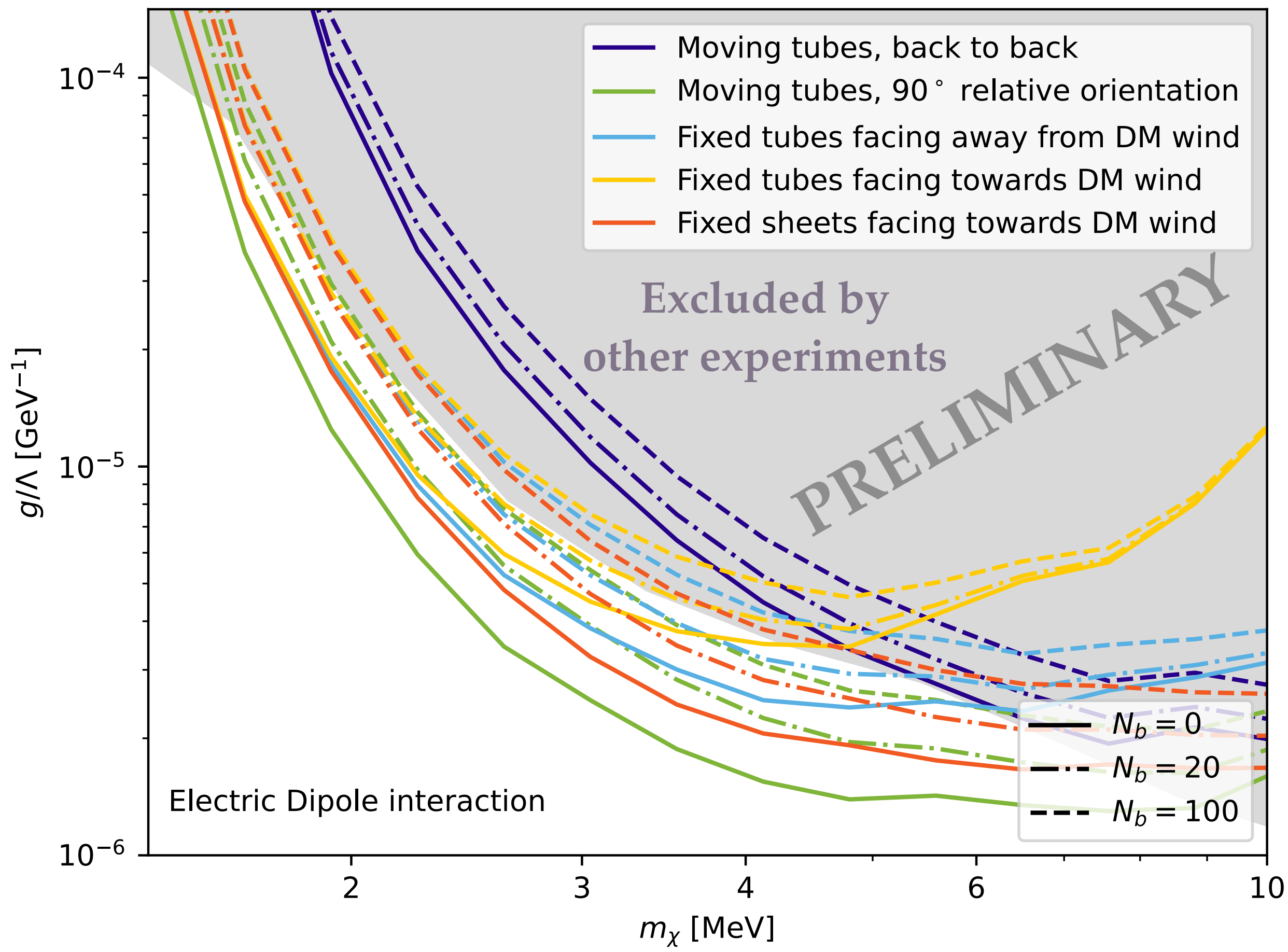
$$\mathcal{L}_{\text{int}} = \frac{g}{2\Lambda^2} \bar{\chi} \gamma^\mu \gamma^5 \chi \partial^\nu F_{\mu\nu}$$

- ❖ Gives contact interactions with  $\mathcal{O}_8$  and  $\mathcal{O}_9$  contributing with coupling strengths

$$c_8 = 8em_e m_\chi \frac{g}{\Lambda^2} \text{ and } c_9 = -8em_e m_\chi \frac{g}{\Lambda^2}$$



# Expected Sensitivity at 90% Confidence level

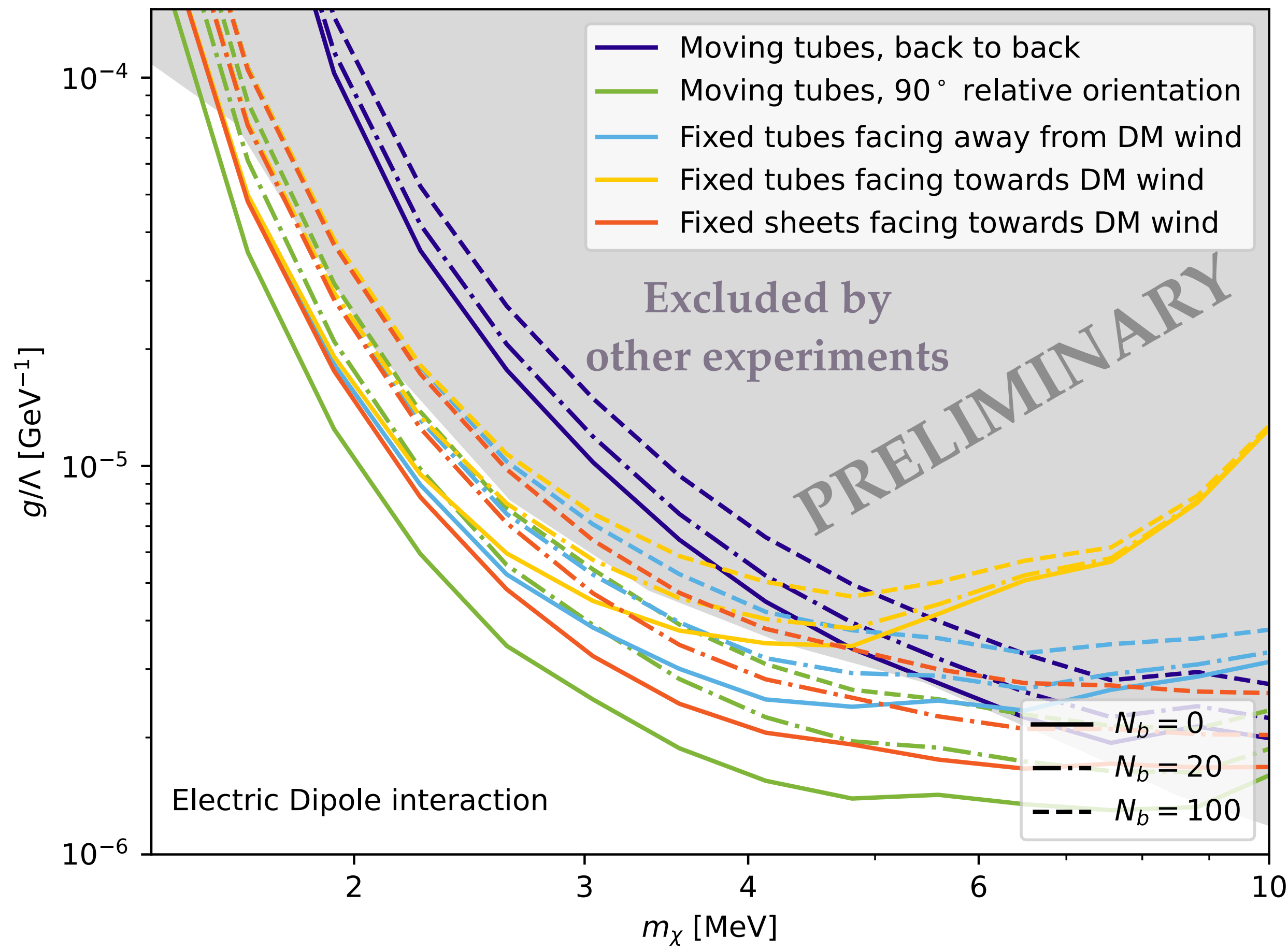


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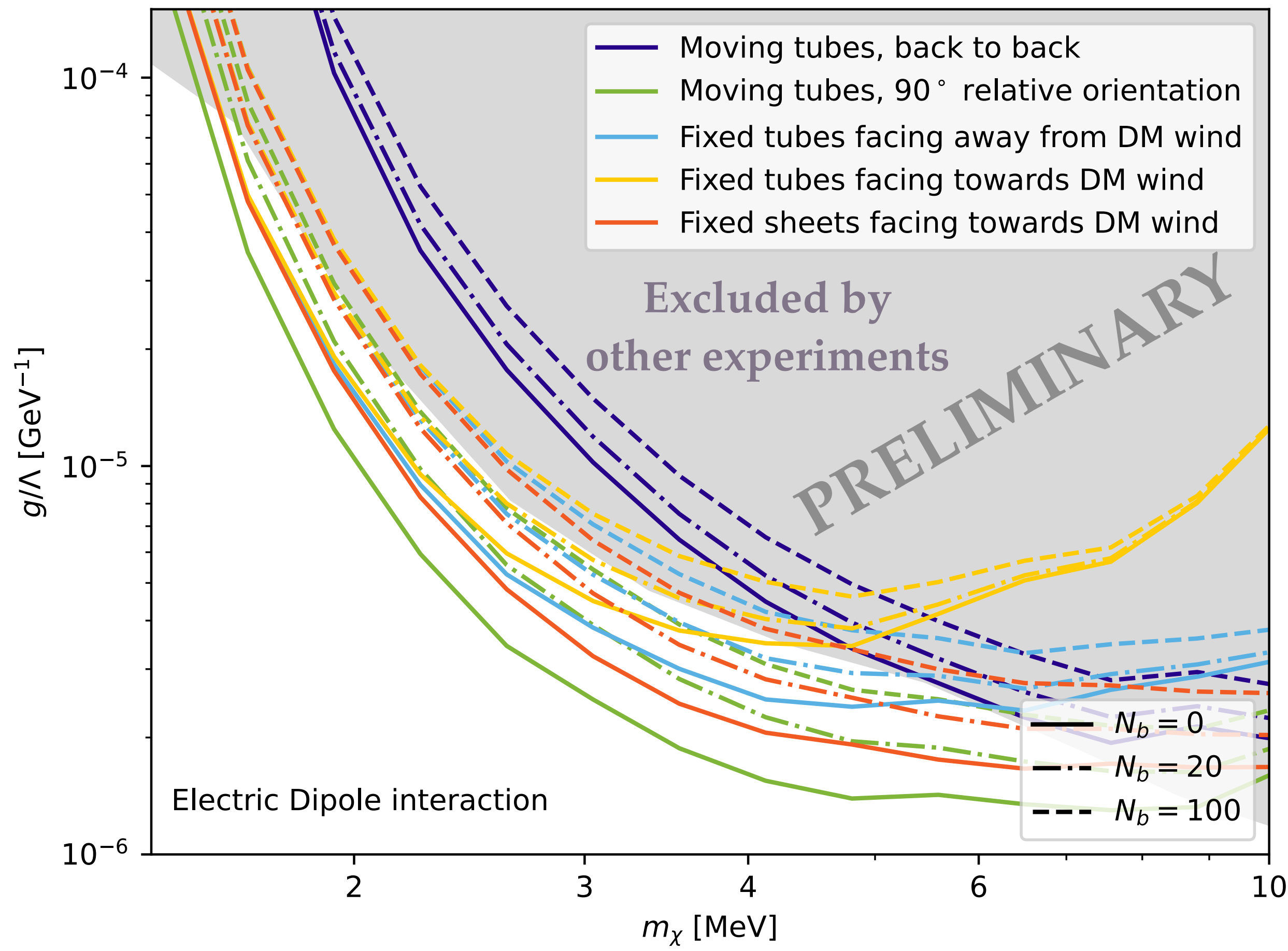
❖ Electric dipole interaction,

$$\mathcal{L}_{\text{int}} = \frac{g}{\Lambda} i\bar{\chi}\sigma^{\mu\nu}\gamma^5\chi F_{\mu\nu}$$

Assuming graphene / carbon nanotube exposure of 1g year



# Expected Sensitivity at 90% Confidence level



Assuming graphene / carbon nanotube exposure of 1g year

- ❖ Electric dipole interaction,

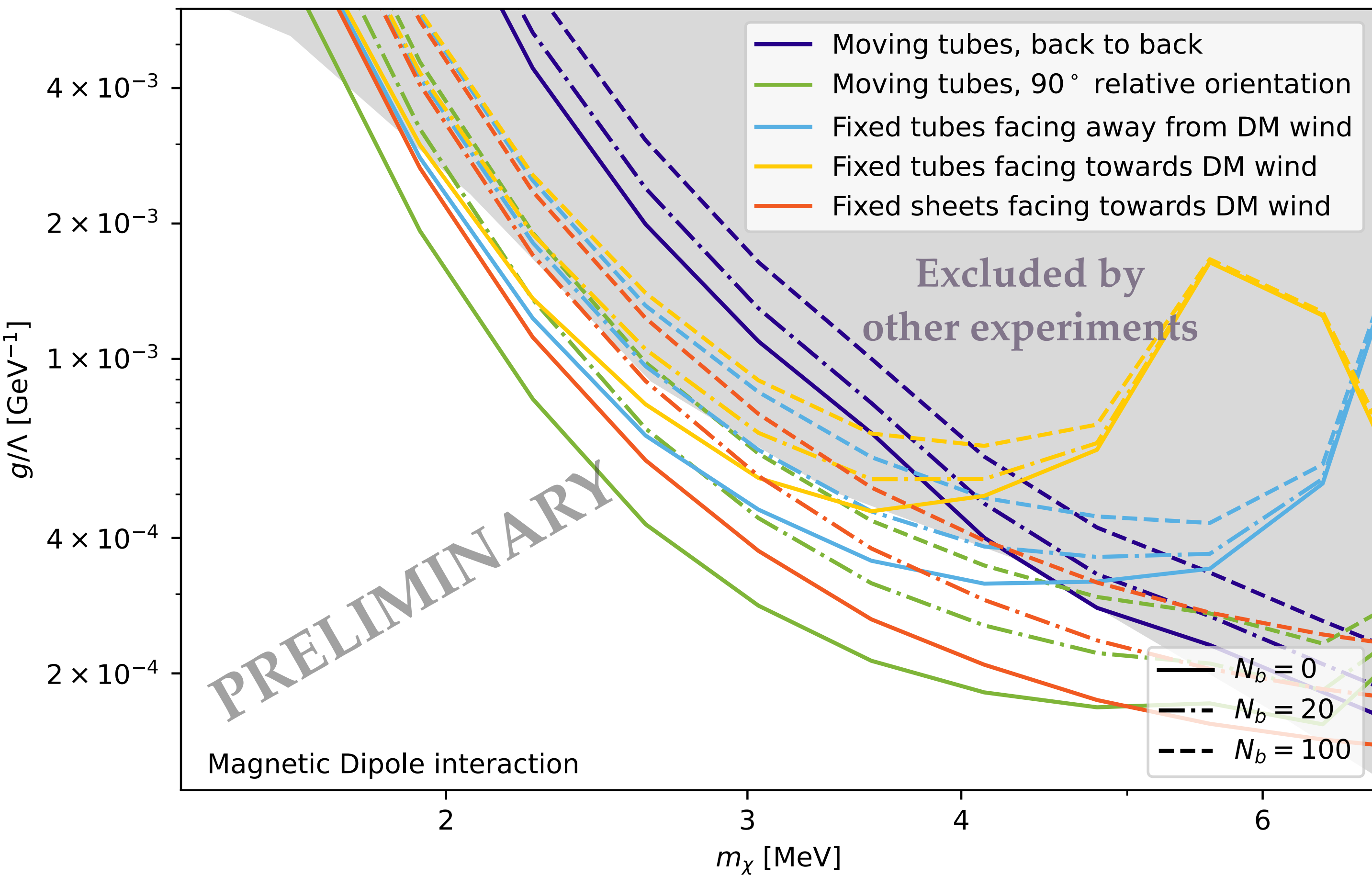
$$\mathcal{L}_{\text{int}} = \frac{g}{\Lambda} i\bar{\chi}\sigma^{\mu\nu}\gamma^5\chi F_{\mu\nu}$$

- ❖ Gives long range interactions with  $\mathcal{O}_{11}$  contributing with coupling strength

$$c_{11} = \frac{16em_{\chi}m_e^2}{q_{\text{ref}}^2} \frac{g}{\Lambda}$$



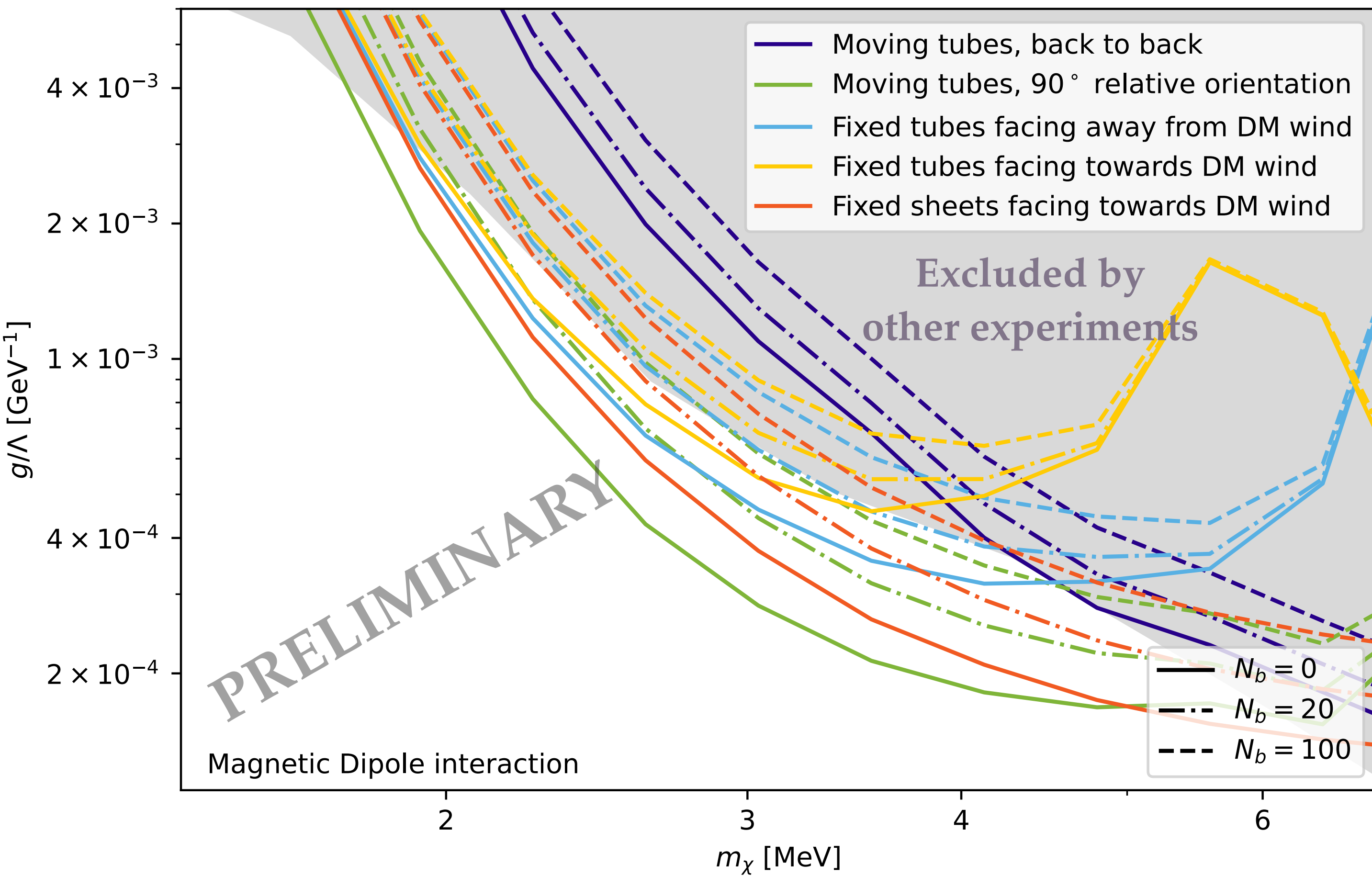
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Assuming graphene / carbon nanotube exposure of 1g year



# Expected Sensitivity at 90% Confidence level



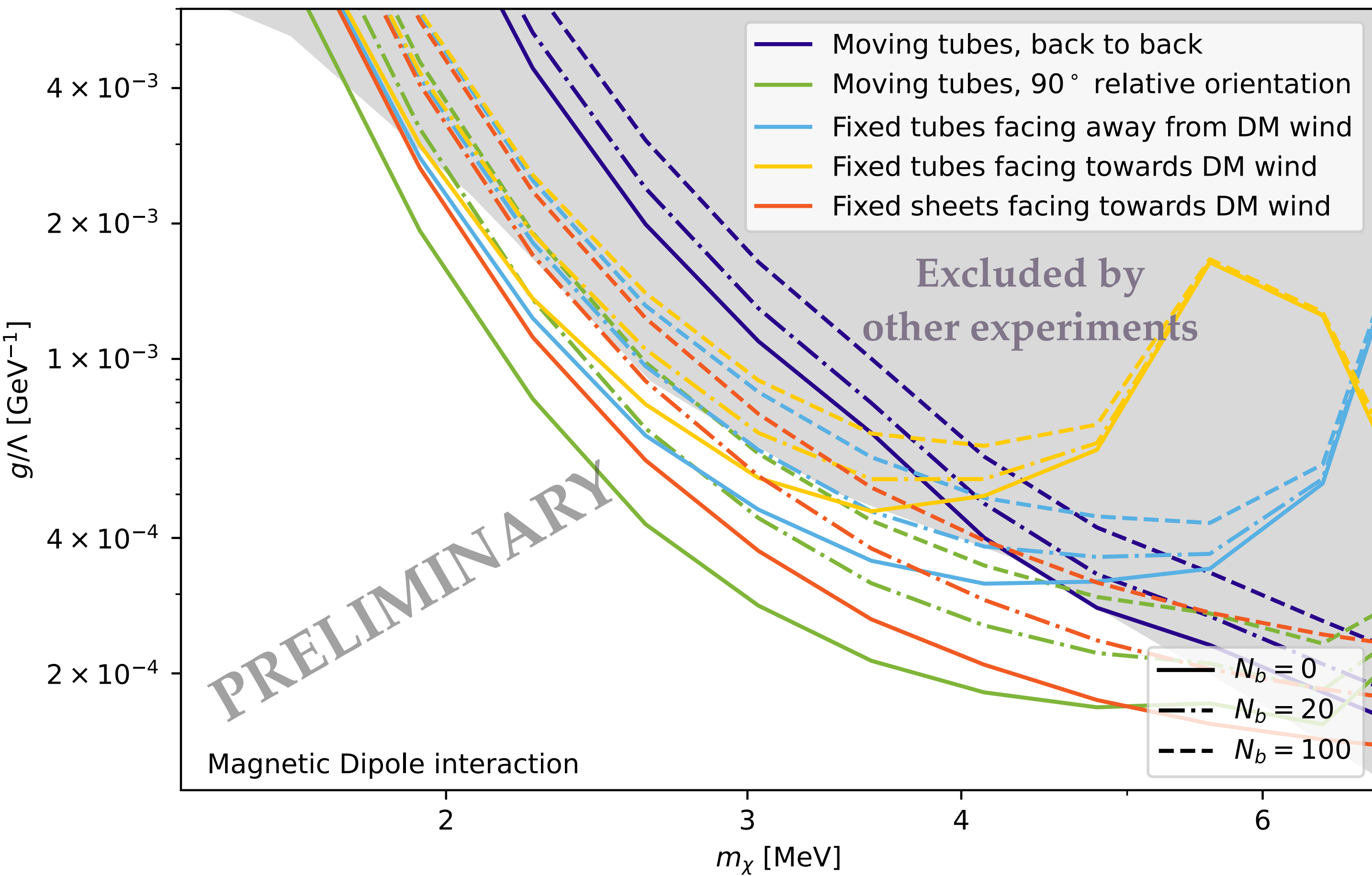
❖ Magnetic dipole interaction,

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Assuming graphene / carbon nanotube exposure of 1g year



# Expected Sensitivity at 90% Confidence level



Assuming graphene / carbon nanotube exposure of 1g year

❖ Magnetic dipole interaction,

$$\mathcal{L}_{\text{int}} = \frac{g}{\Lambda} \bar{\chi} \sigma^{\mu\nu} \chi F_{\mu\nu}$$

❖ Long range interaction with  $\mathcal{O}_5$  and  $\mathcal{O}_6$  with coupling strengths

$$c_5 = \frac{16em_e^2 m_\chi}{q_{\text{ref}}^2} \frac{g}{\Lambda} \text{ and } c_6 = -\frac{16em_e^2 m_\chi}{q_{\text{ref}}^2} \frac{g}{\Lambda}$$

Contact interaction with  $\mathcal{O}_1$  and  $\mathcal{O}_4$  with coupling strengths

$$c_1 = 4em_e \frac{g}{\Lambda} \text{ and } c_4 = 16em_\chi \frac{g}{\Lambda}$$



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# Take Home Message

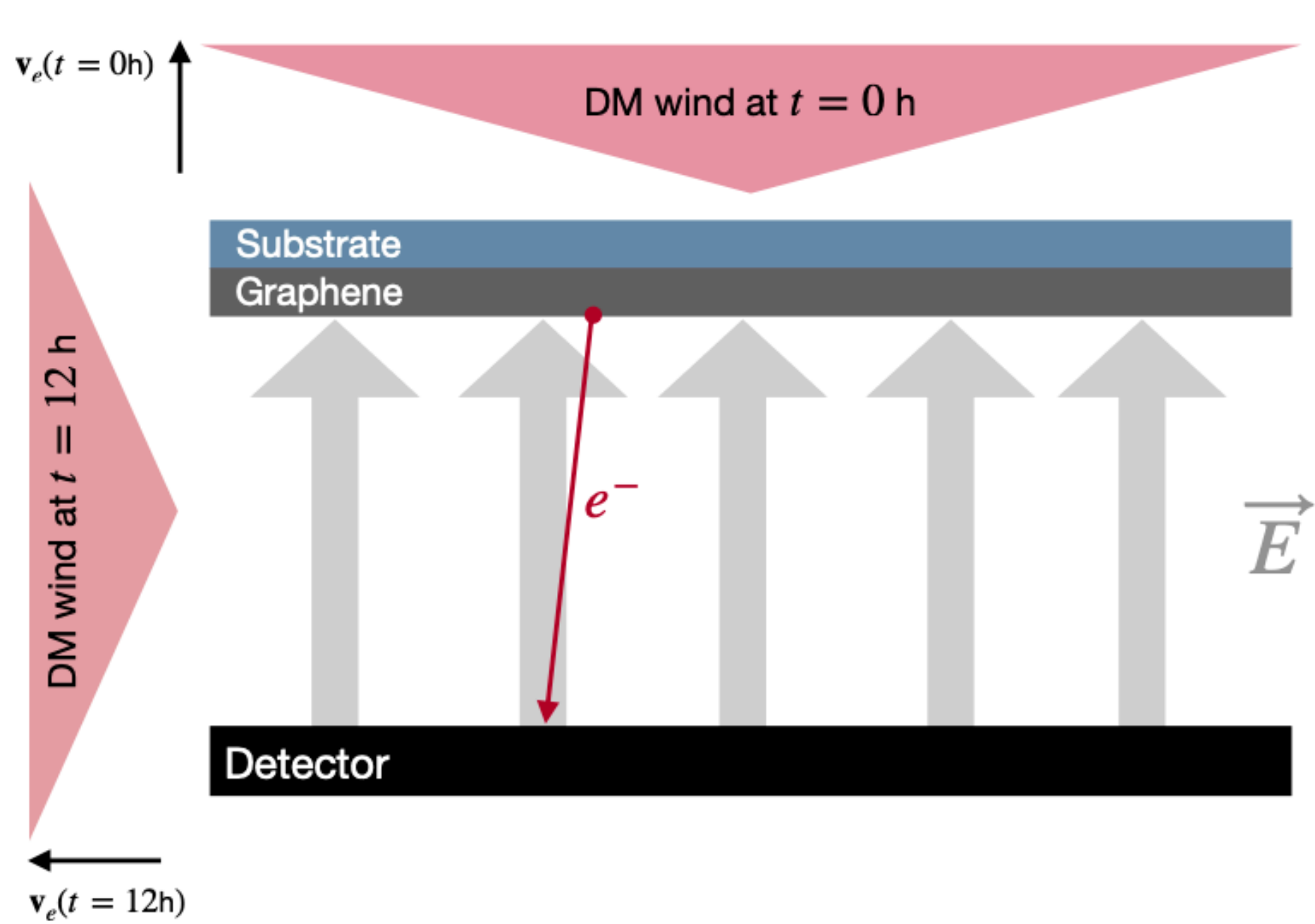
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- ❖ For plane wave final state electrons, the physics of general non-relativistic dark matter electron interactions factorises into the product of a single free particle response function and the norm of the momentum space initial state electron wave-function.
- ❖ Graphene and carbon nanotubes can be used to detect a smoking gun signals from DM.
- ❖ For DM masses of a few MeV both carbon nanotube and graphene based experiments are sensitive to yet viable parameter space for a range of DM models with an exposure of 1g year.

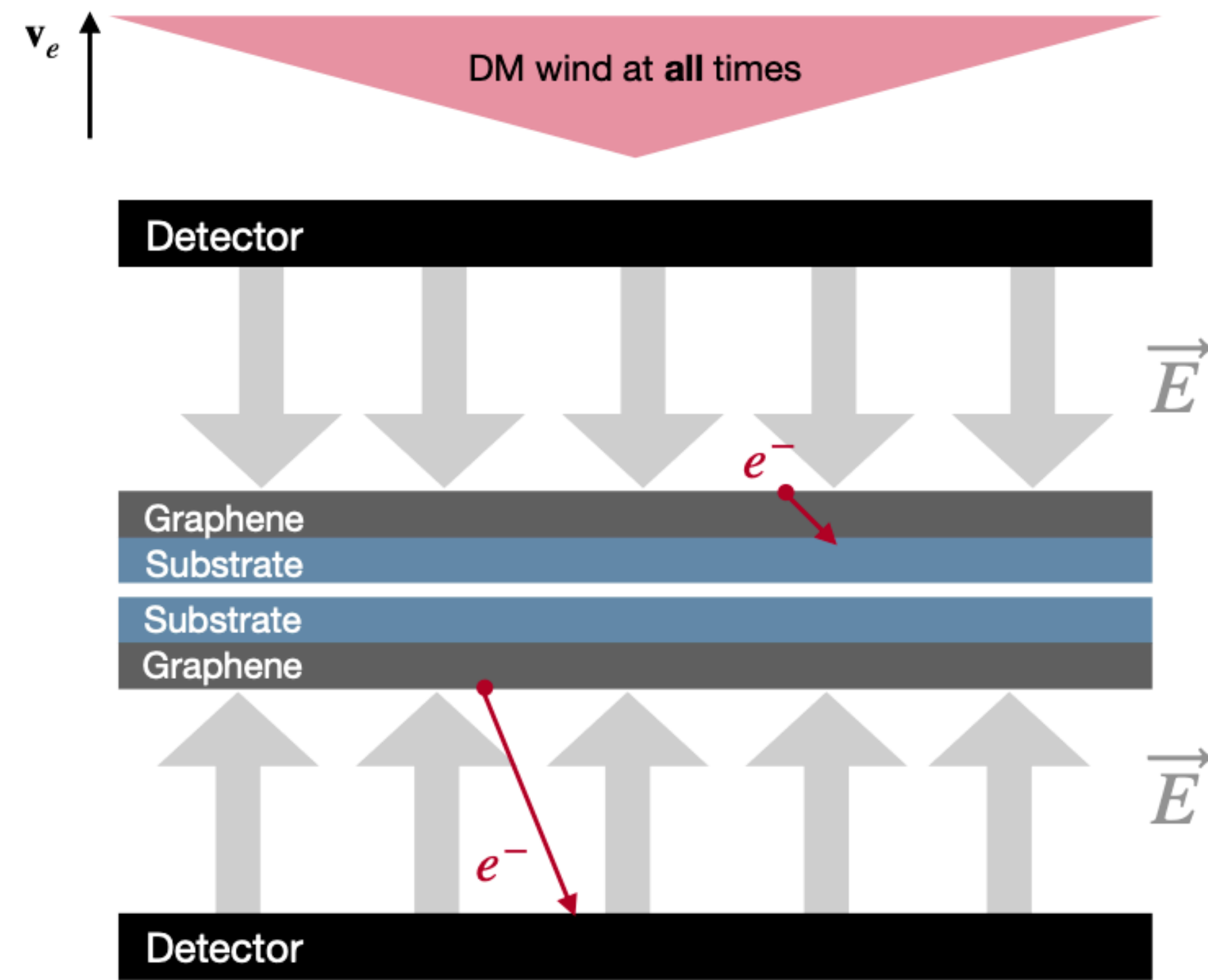


# Backup slides

# Experimental setups: Graphene



I. Fixed graphene sheets

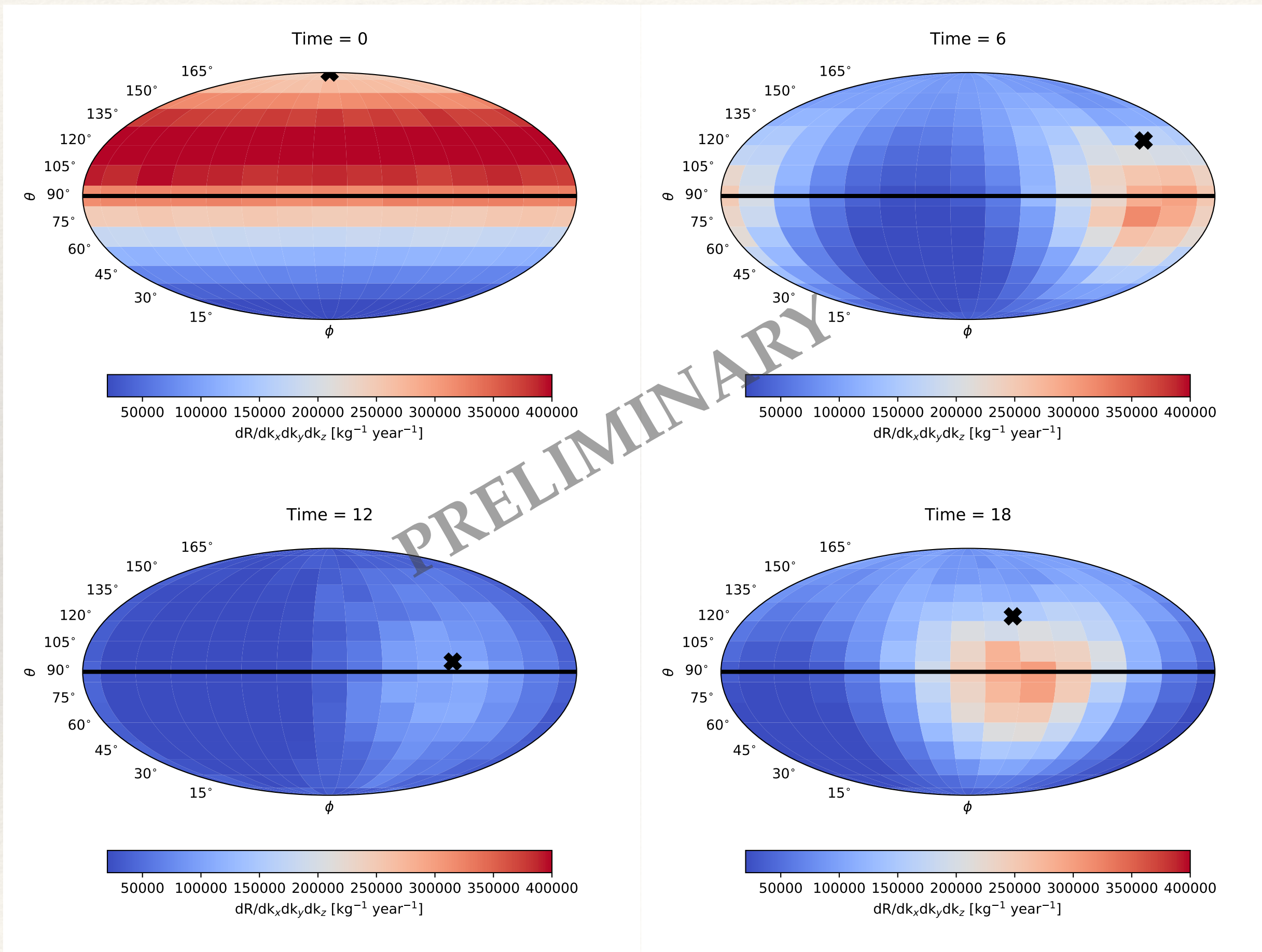


II. Moving graphene sheets





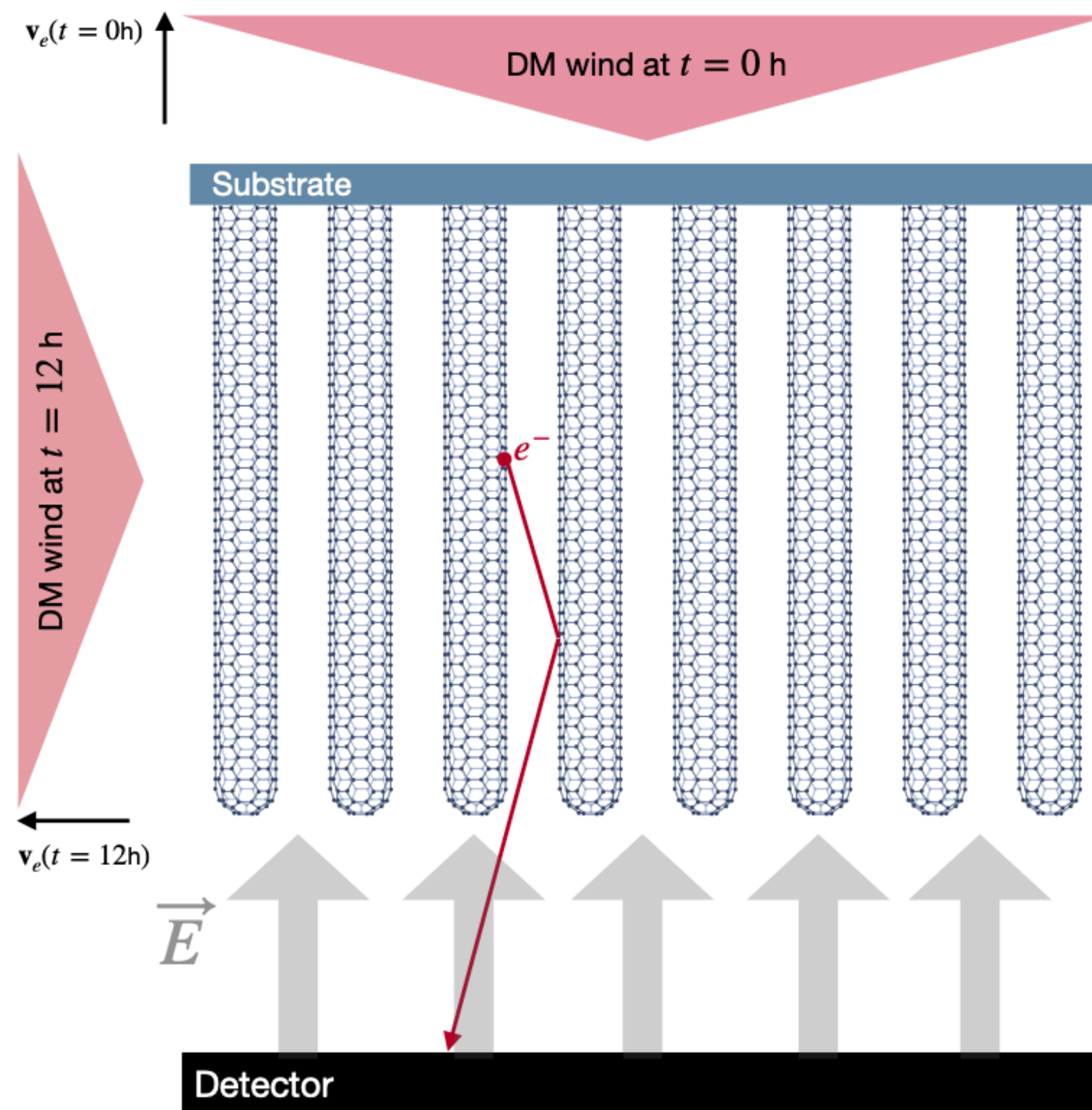
# Daily Modulation in Fixed Graphene Experiments



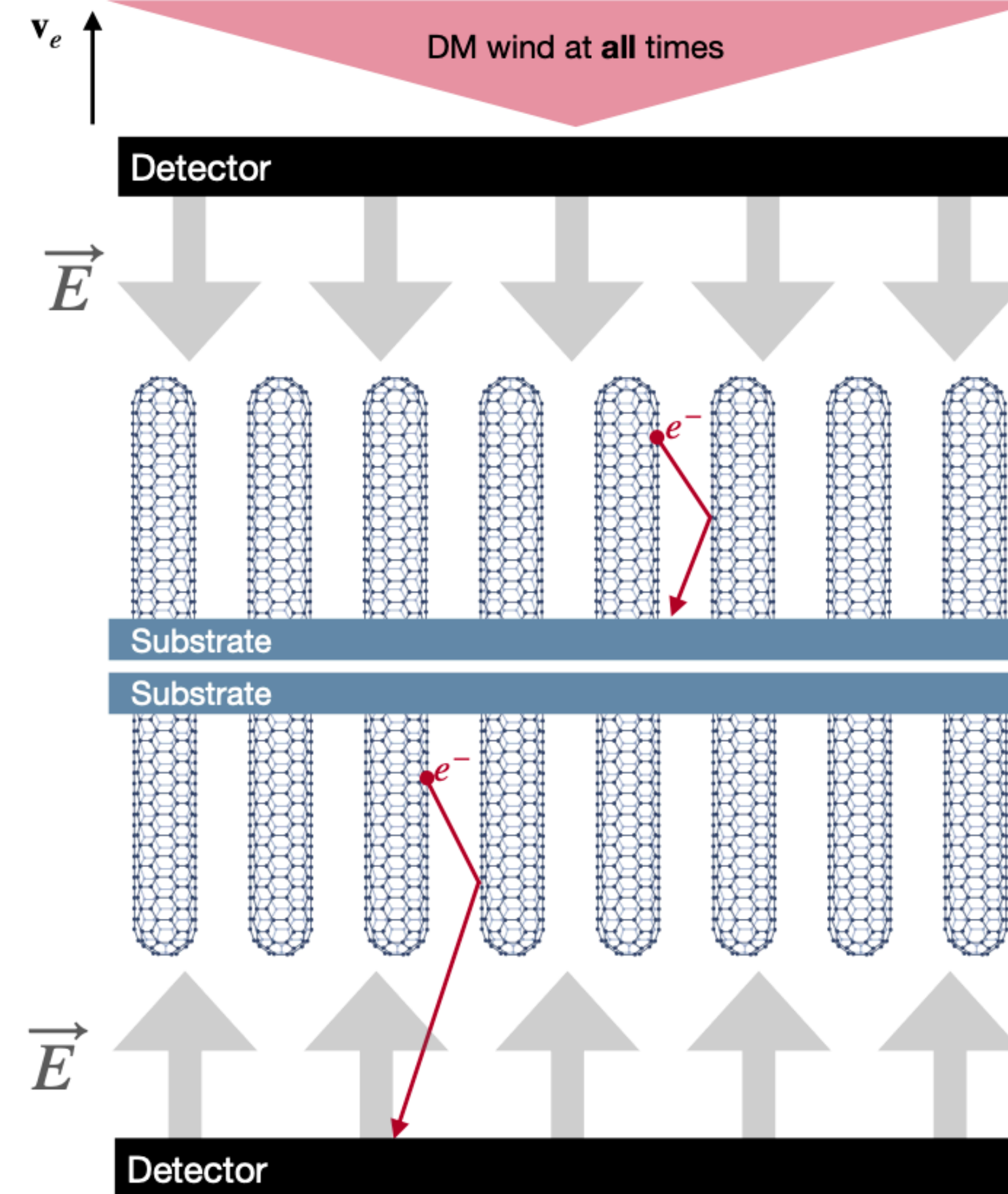
$$\mathcal{O}_5 = i\mathbf{S}_\chi \cdot \left( \frac{\mathbf{q}}{m_e} \times \mathbf{v} \right)$$



# Experimental setups: Carbon Nanotubes



III. Fixed CNTs



IV. Moving CNTs

To be built by  
ANDROMEDA



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