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# Electron pre-acceleration through Stochastic Shock Drift Acceleration at shocks in merging galaxy clusters

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# Introduction

- supersonic flows of baryonic matter induced during large-scale structure formation of the Universe produce shocks in hot intracluster (ICM) medium with high plasma beta ( $\beta \gg 1$ )
- merger shocks are observed in radio and X-rays as so-called **radio relics**; their synchrotron emission indicates CR electron acceleration to high energies
- most energetic merger shocks have low Mach numbers ( $M_s < 5$ ,  $M_A < 10$ )
- Diffusive Shock Acceleration (DSA) assumed to operate at these shocks but mechanism of **electron injection** that regulates the efficiency of CR acceleration is poorly known for galaxy cluster conditions

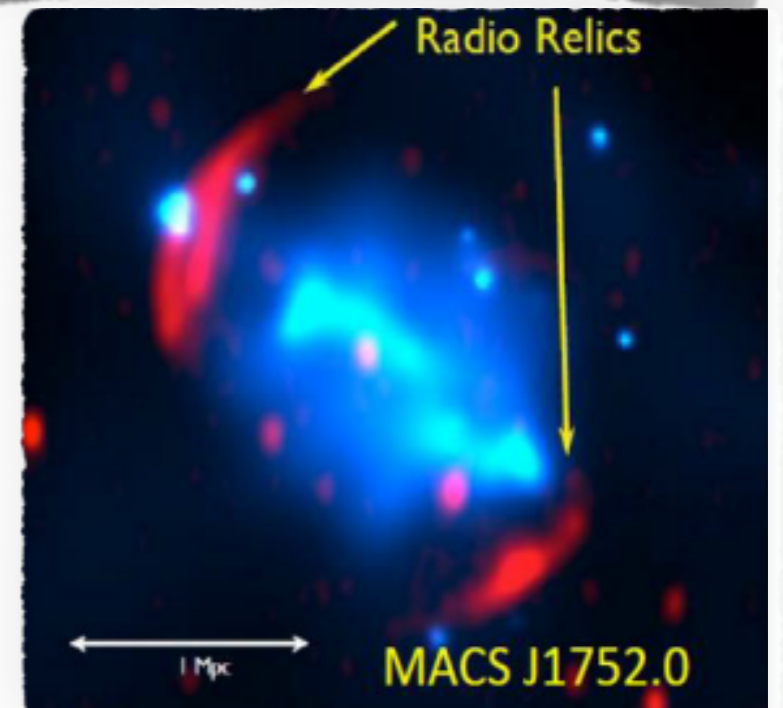
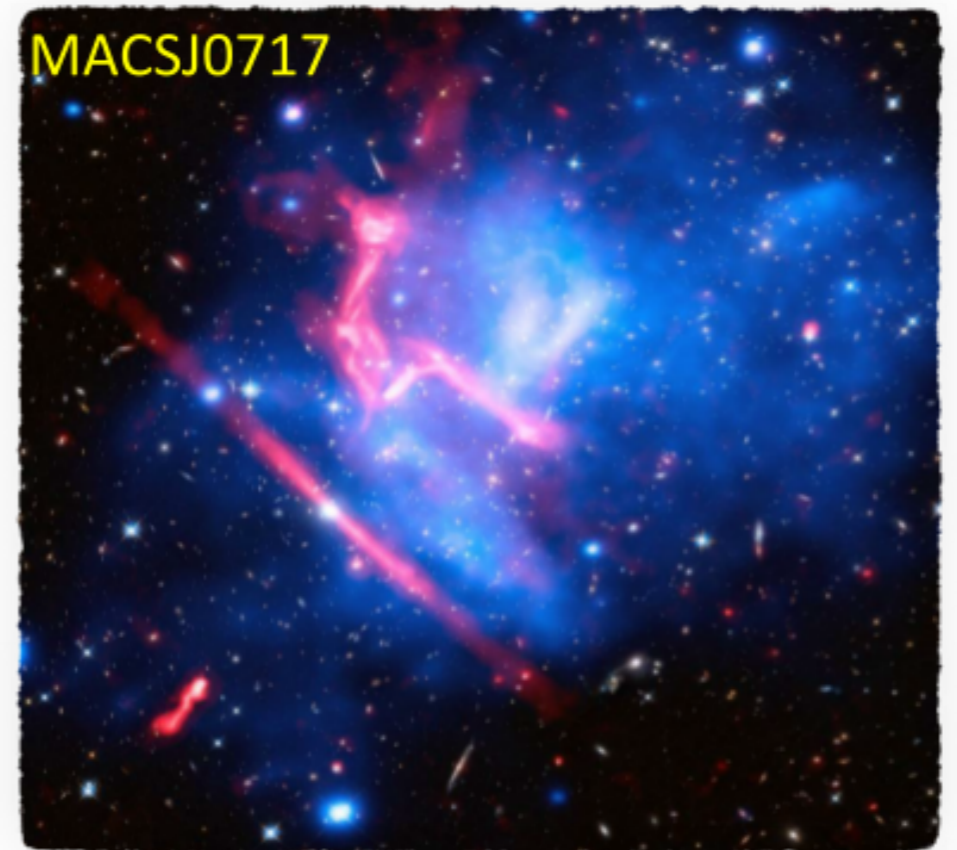
Alfvenic Mach number:  $M_A = \frac{v_{sh}}{v_A}$

Sonic Mach number:  $M_s = \frac{v_{sh}}{c_s}$

Plasma beta:  $\beta = p_{th}/p_{mag}$

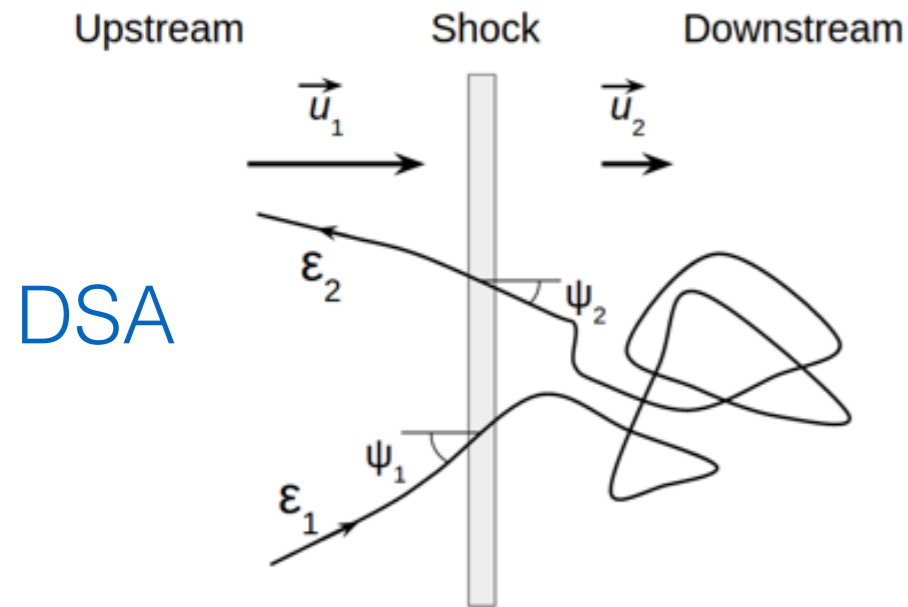
$$v_A = \frac{B_0}{\sqrt{\mu_0(N_e m_e + N_i m_i)}}$$

$$c_s = \sqrt{2\Gamma k_B T_i / m_i}$$



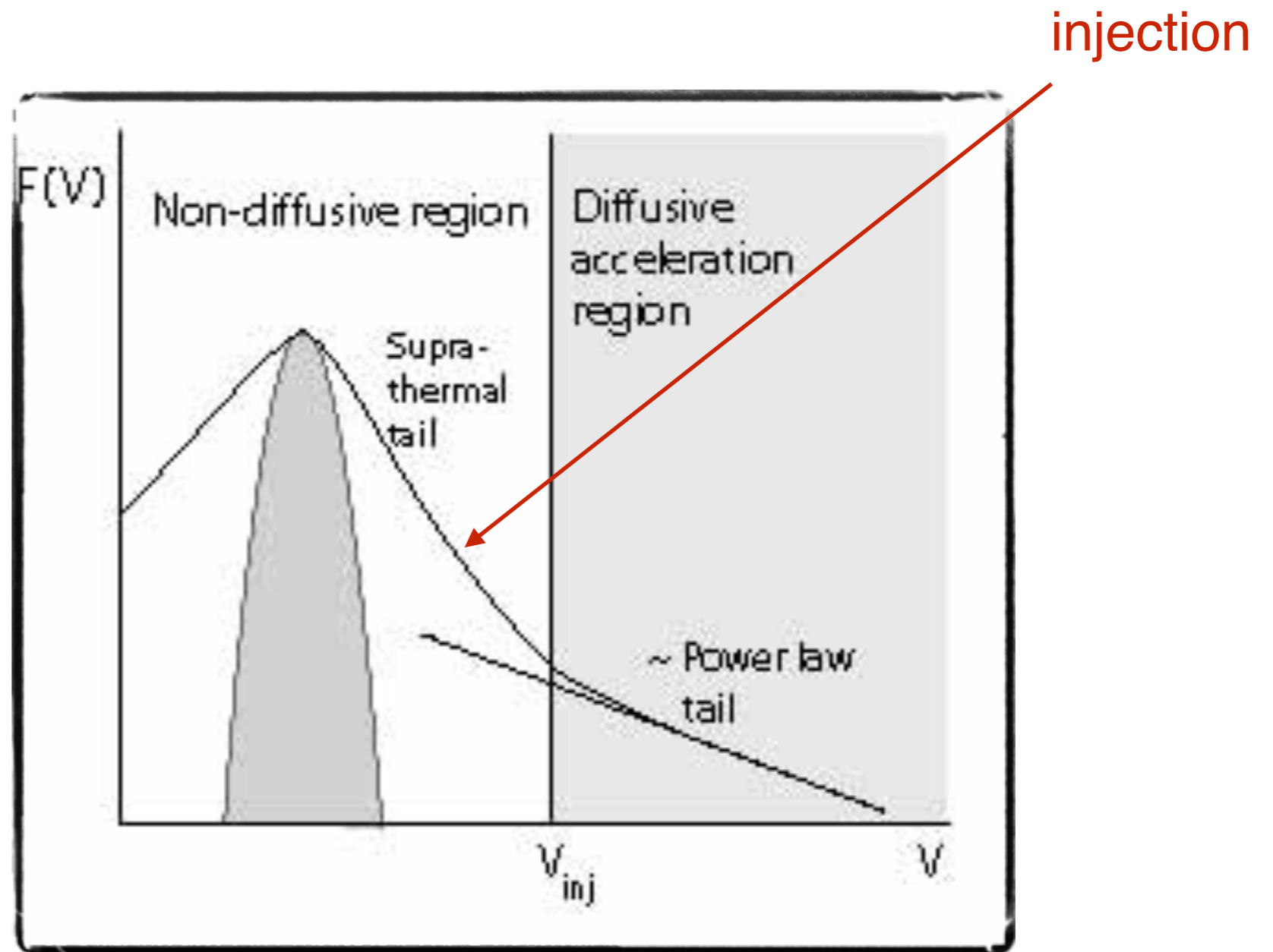
White - optical (Hubble)  
 Blue - X-ray (Chandra)  
 Red - radio (VLA)

# Particle injection (pre-acceleration) to DSA

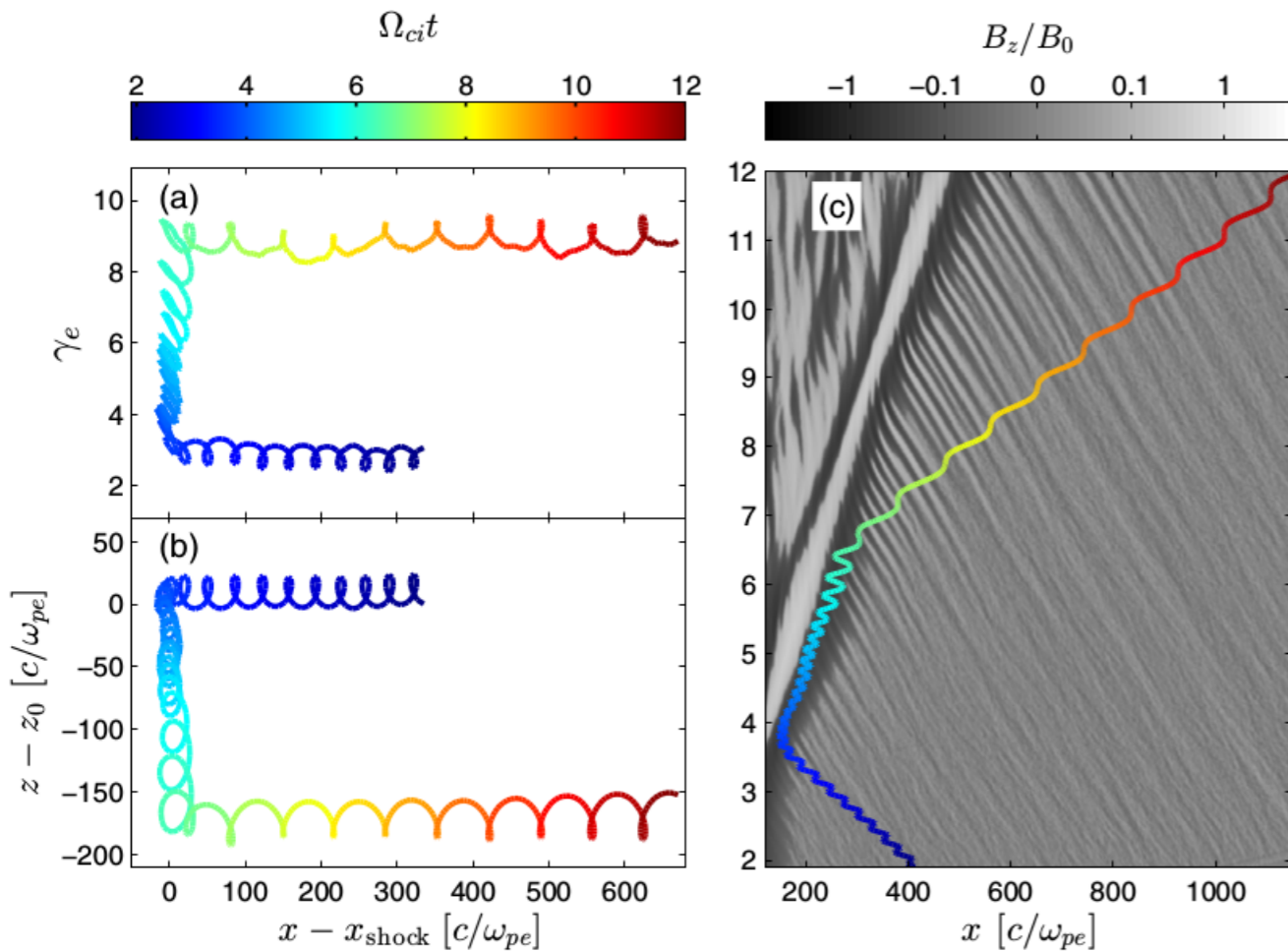


$$d_{\text{sh}} \sim (1-100) \lambda_{\text{gi}}$$

$$r_g(\epsilon_{\text{inj}}) > d_{\text{sh}}$$



# Electron injection at shocks in high beta plasmas: Shock Drift Acceleration (SDA)



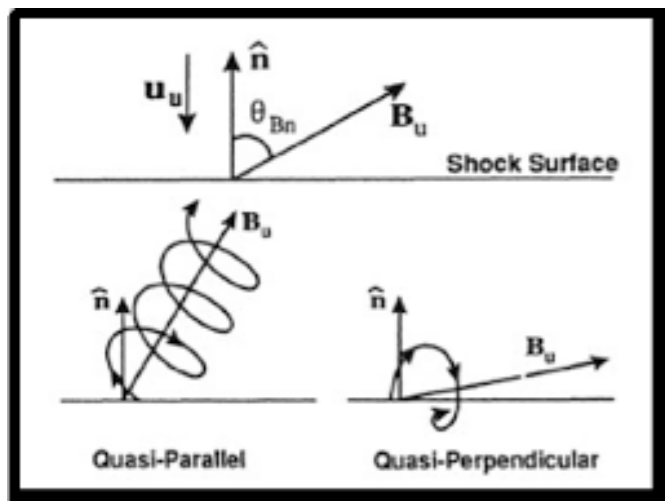
Guo et al. 2014 (2D)

- particles gain energies from the motional electric field while drifting along the shock surface due to the magnetic field gradient
- some particles can be reflected from the shock back upstream (magnetic mirror effect) and form non-thermal upstream plasma component
- works at subluminal shocks:  $v_t \leq c$
- acceleration time:  $\sim \Omega_i^{-1}$
- energy gain:

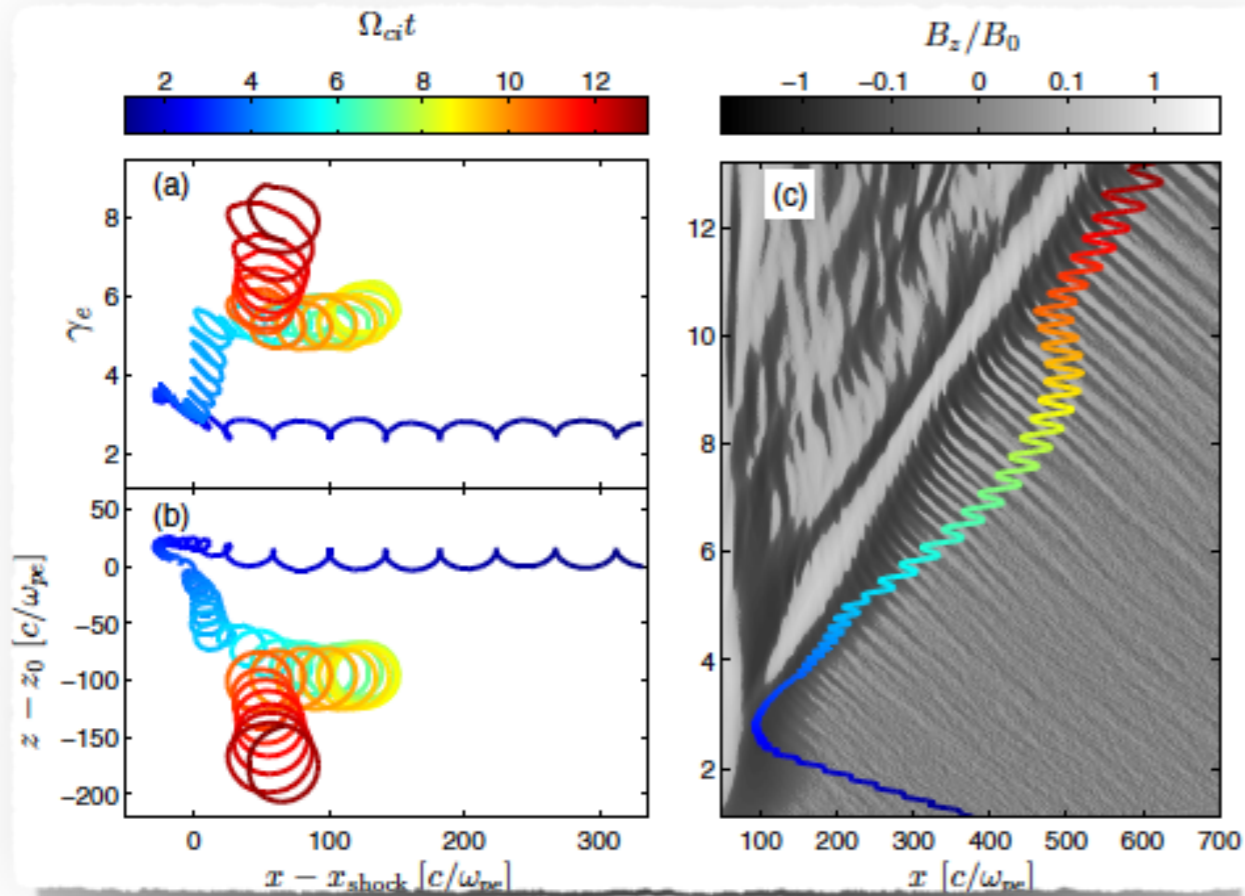
$$\Delta\gamma_{\text{SDA}} = \frac{-e}{m_e c^2} \int E_z dz$$

de Hoffman-Teller velocity:

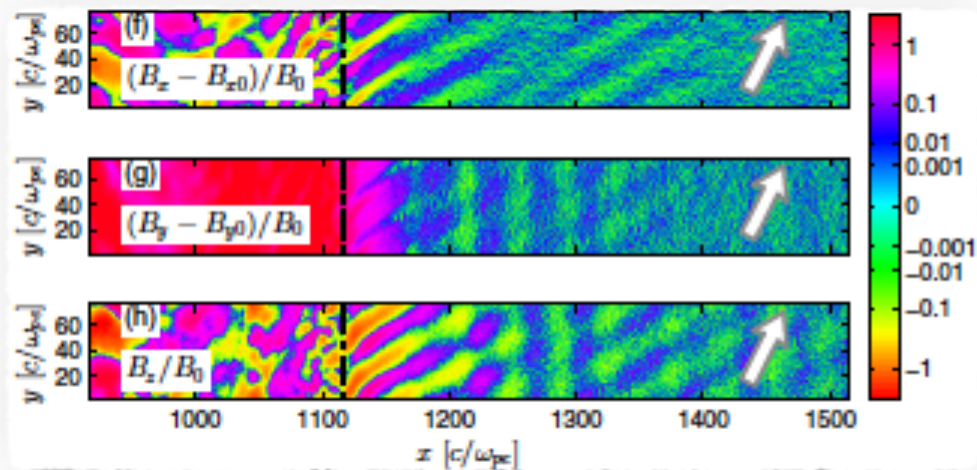
$$v_t = u_{\text{sh}}^{\text{up}} / \cos \theta_{Bn}$$



# Previous work: multiple Shock Drift Acceleration cycles at quasi-perpendicular shocks

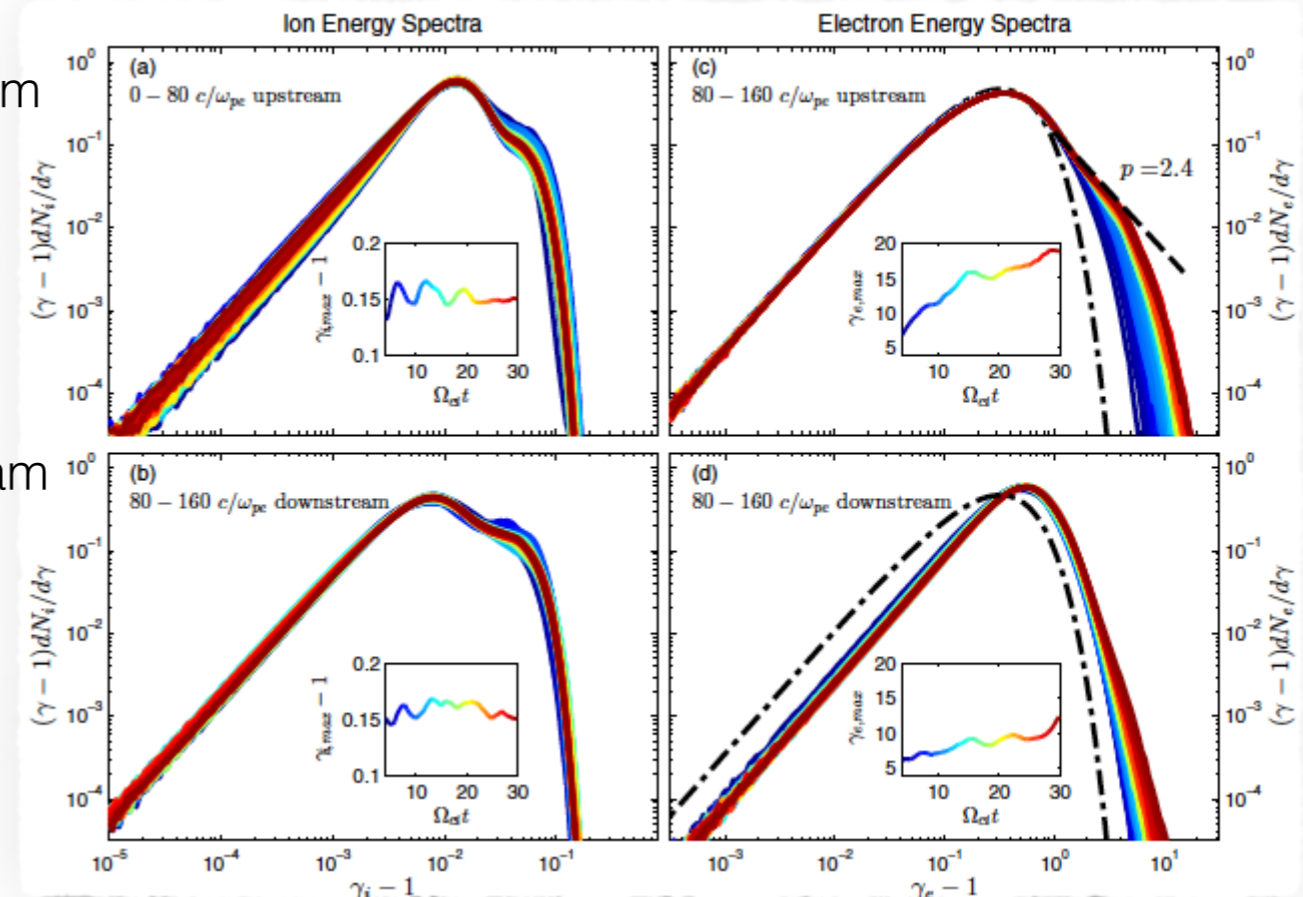


- SDA-reflected electrons scattered back towards shock by upstream self-generated waves - **DSA-like process**
- formation of **upstream** power-law spectra (and steep downstream spectra)
- more effective at high  $\beta$
- $\gamma_{\max} \ll \gamma_{\text{inj}}$ ?



upstream

downstream



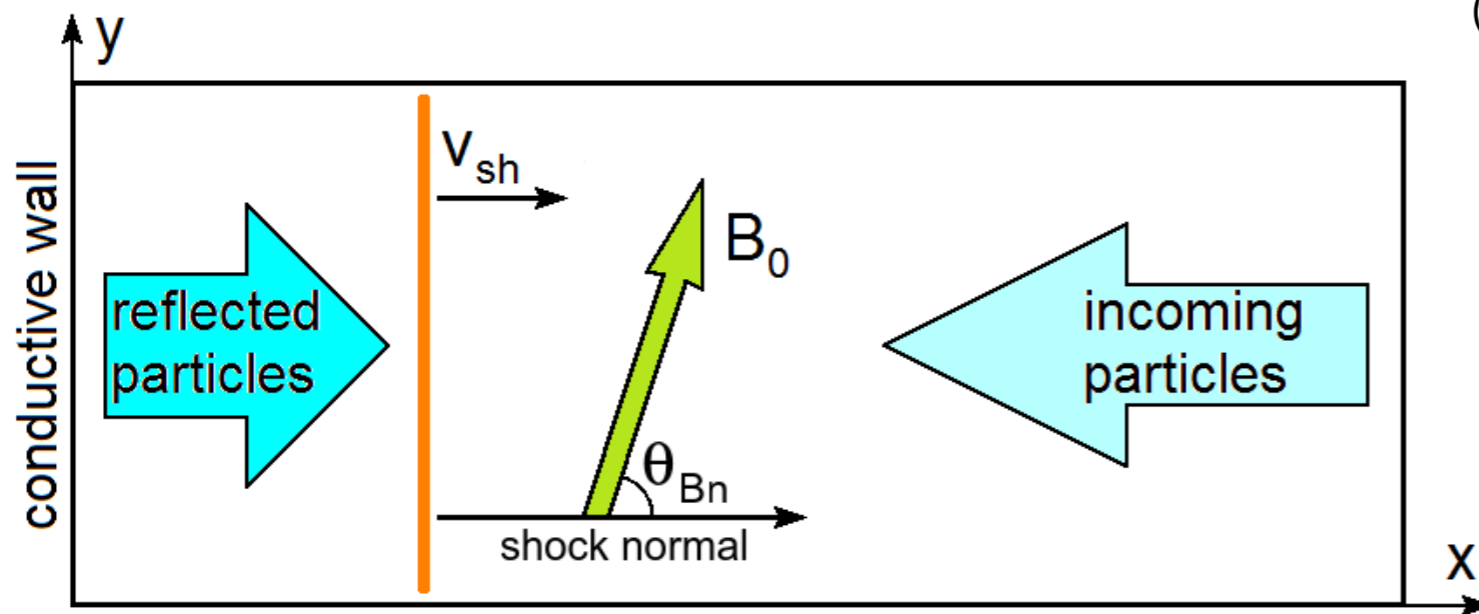
Matsukiyo et al. 2011 (1D)  
 Guo et al. 2014 (2D)  
 Kang et al. 2019 (2D)

# *This work:* investigate the effects of the shock rippling on electron pre-acceleration

Kobzar O., et al., ApJ 2021

Fułat K., M.Sc. thesis (2021)

(see also Matsukiyo & Matsumoto 2015)



Large-scale 2D3V Particle-In-Cell (PIC) simulations

- $M_s=3$ ,  $m_i/m_e=100$ ,  $v_0=0.1c$ ,  $\beta=5, 10, 20, 30$  (plasma temperature  $k_B T \approx 40$  keV)
- subluminal shocks:  $\vartheta_{Bn}=75^\circ, 78^\circ$  ( $\vartheta_{cr} \approx 81,4^\circ$ )
- conditions of inefficient EFI mode driving in the laminar shock phase:

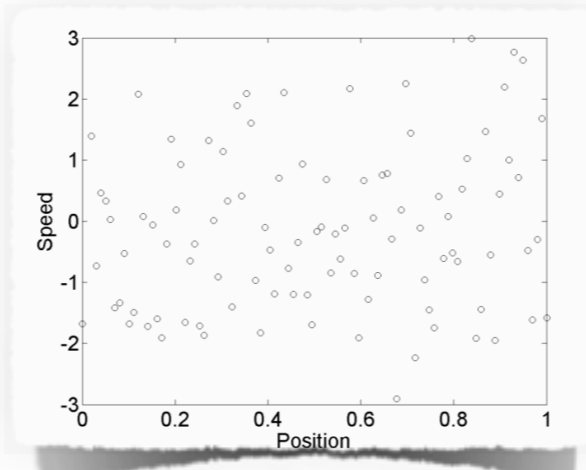
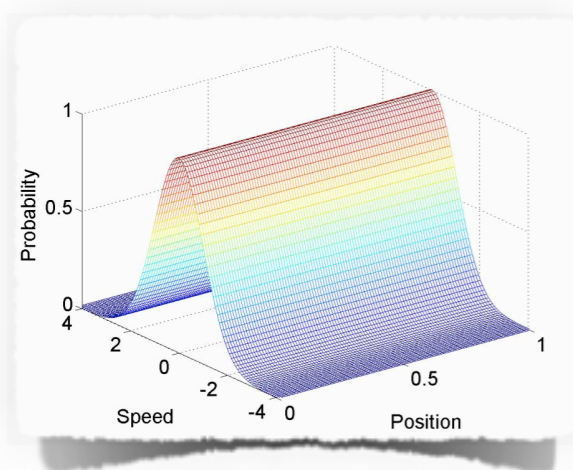
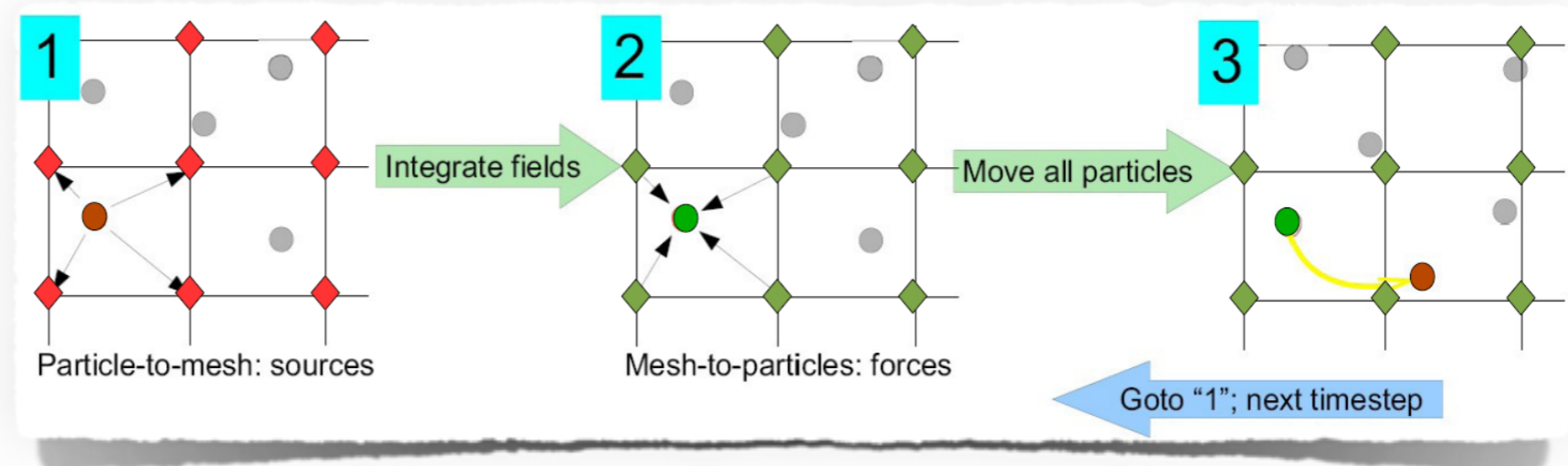
$$v_t \approx 1.5v_{th,e} \quad (\theta_{Bn} = 75^\circ)$$

$$v_t \approx 1.9v_{th,e} \quad (\theta_{Bn} = 78^\circ)$$

$$v_t \gtrsim v_{th,e} \quad (v_t = u_{sh}^{up} / \cos \theta_{Bn})$$

# Method of Particle-In-Cell Simulations

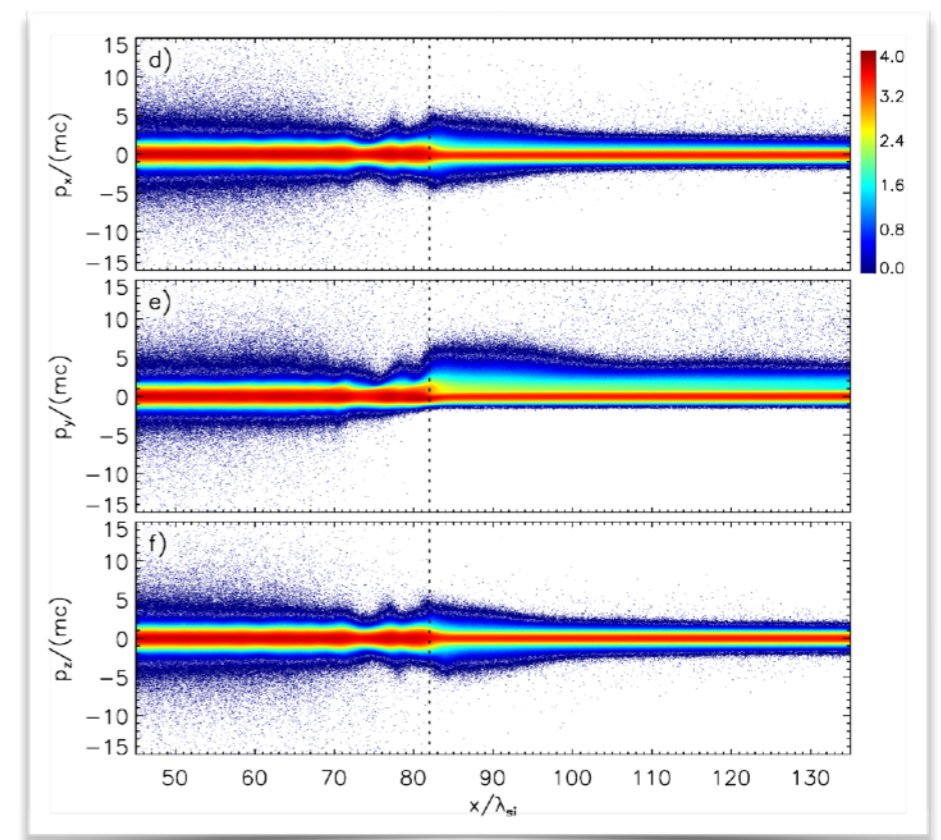
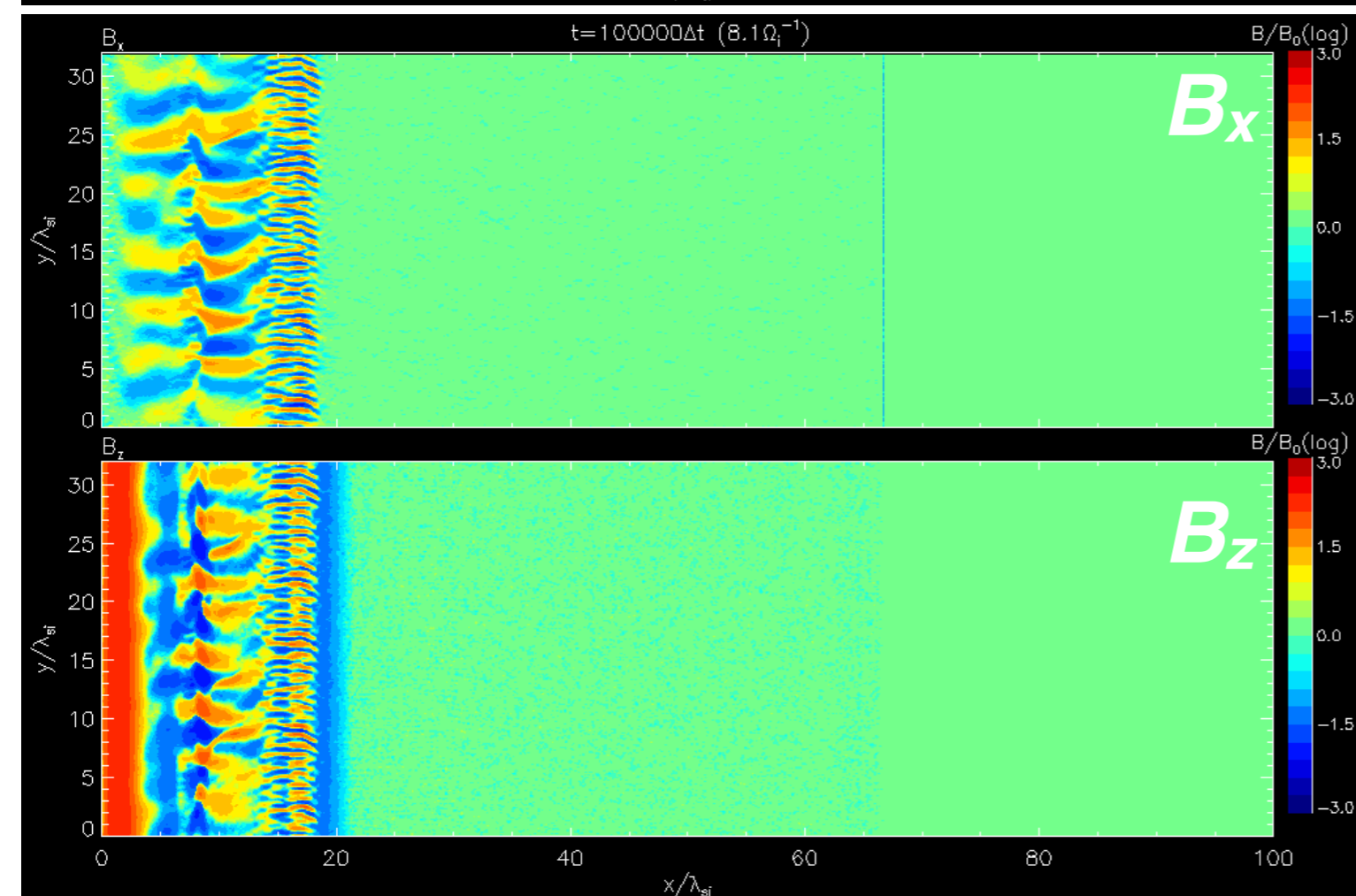
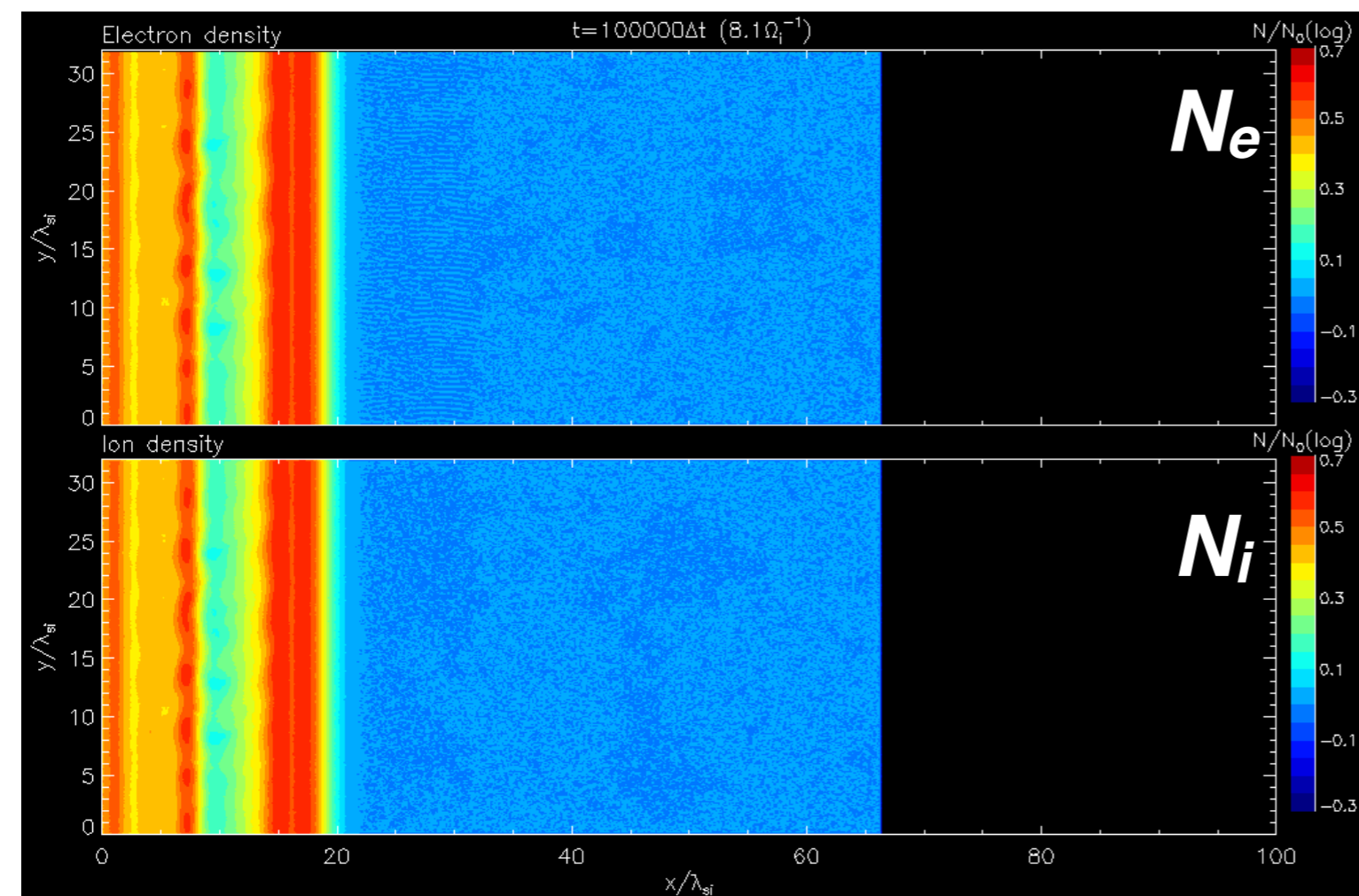
- Fully self-consistent description of collisionless plasma:
  - Vlasov equation (kinetic theory; **time evolution of particle distribution function**  $f(\mathbf{x}, \mathbf{v}, t)$  in phase-space) + Maxwell's equations
- **Particle-In-Cell** modeling - an *ab-initio* method of Vlasov equation solution through:
  - integration of Maxwell's equations on a numerical grid
  - integration of relativistic particle equations of motion in collective self-consistent EM field



Particle distribution function represented by **macroparticles** on a numerical grid.  
(Macroparticles represent a small volume of particle phase-space; equations of motion as for realistic particles)

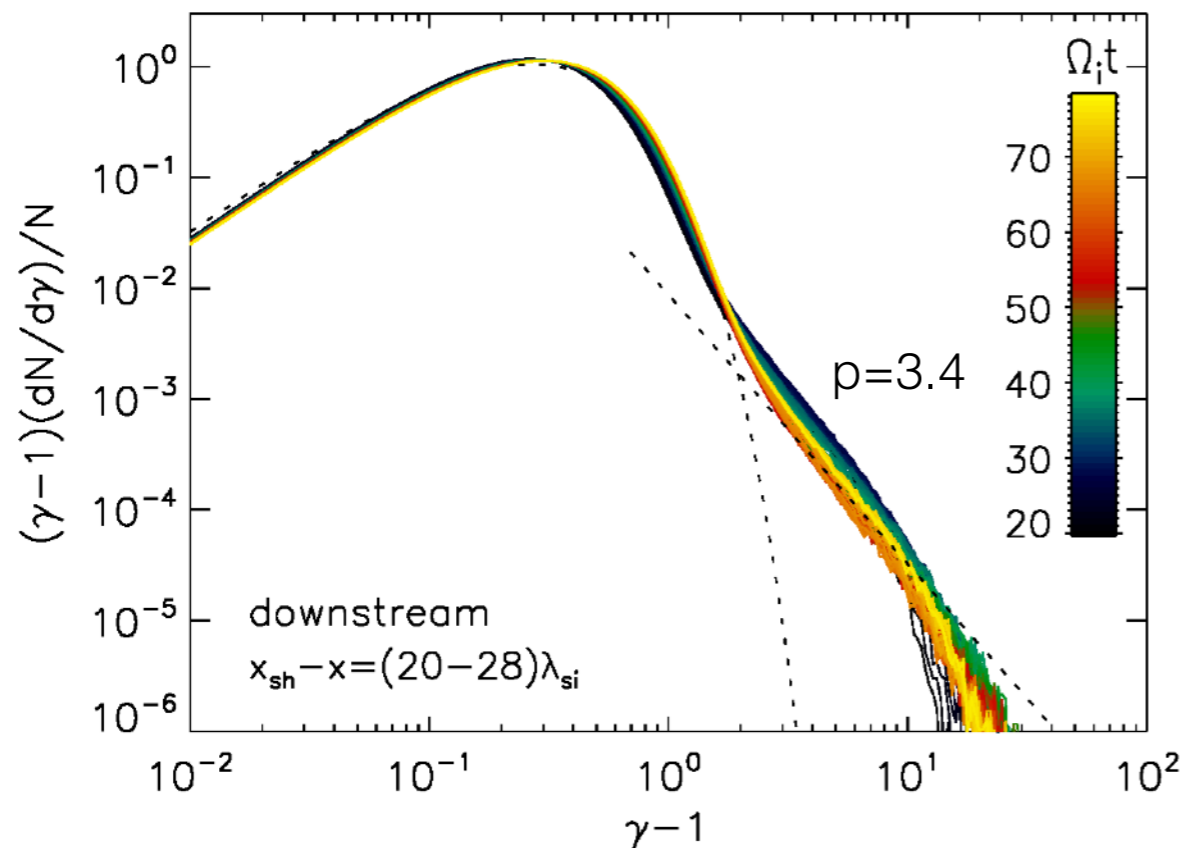
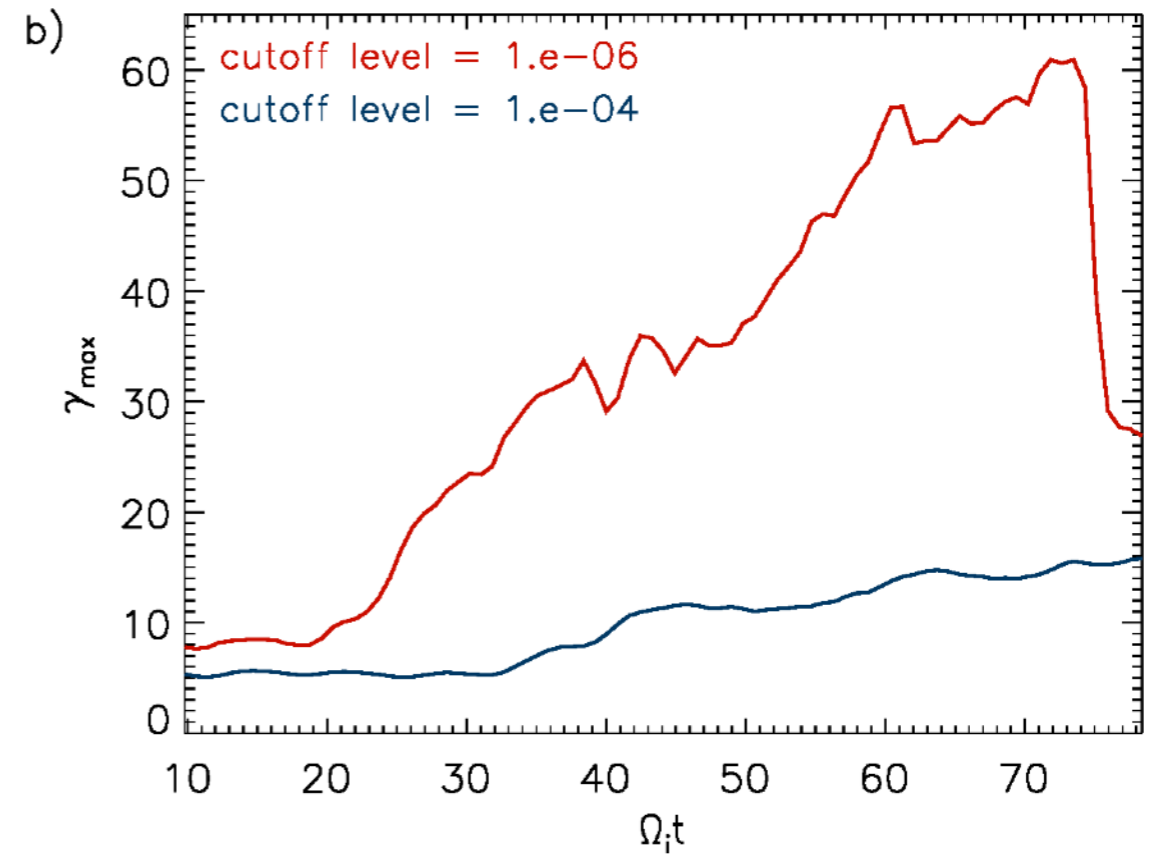
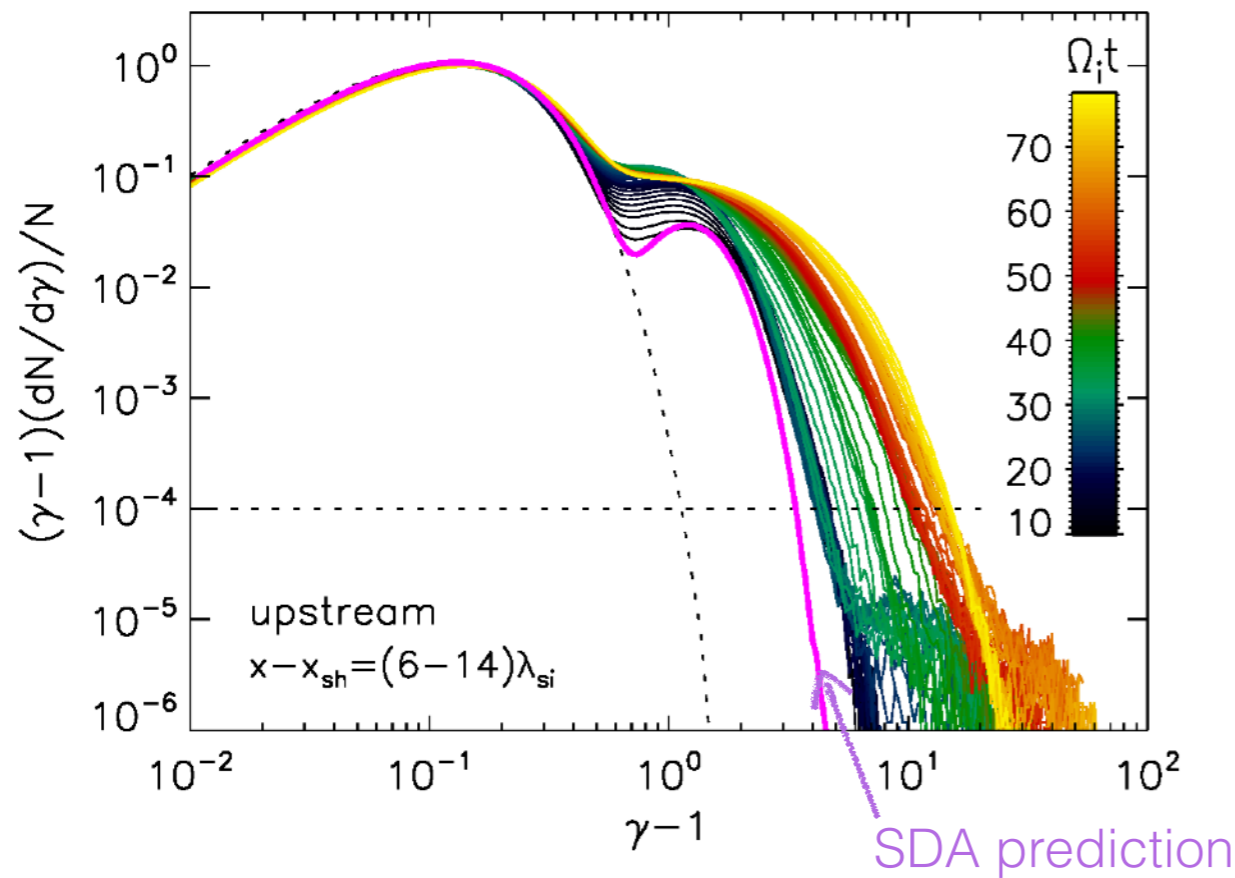
# Global shock structure: multi-scale turbulence ( $\beta=5$ , $\vartheta_{Bn}=75^\circ$ )

- **rippling** in the shock transition on different scales (overshoot-undershoot-2nd overshoot) - AIC and mirror modes
- short-scale **whistler waves** in the overshoot
- oblique and perpendicular modes of the **electron firehose instability** in the upstream, enhanced and modulated by the ripples





# Electron spectra – time evolution ( $\beta=5$ , $\vartheta_{Bn}=75^\circ$ )



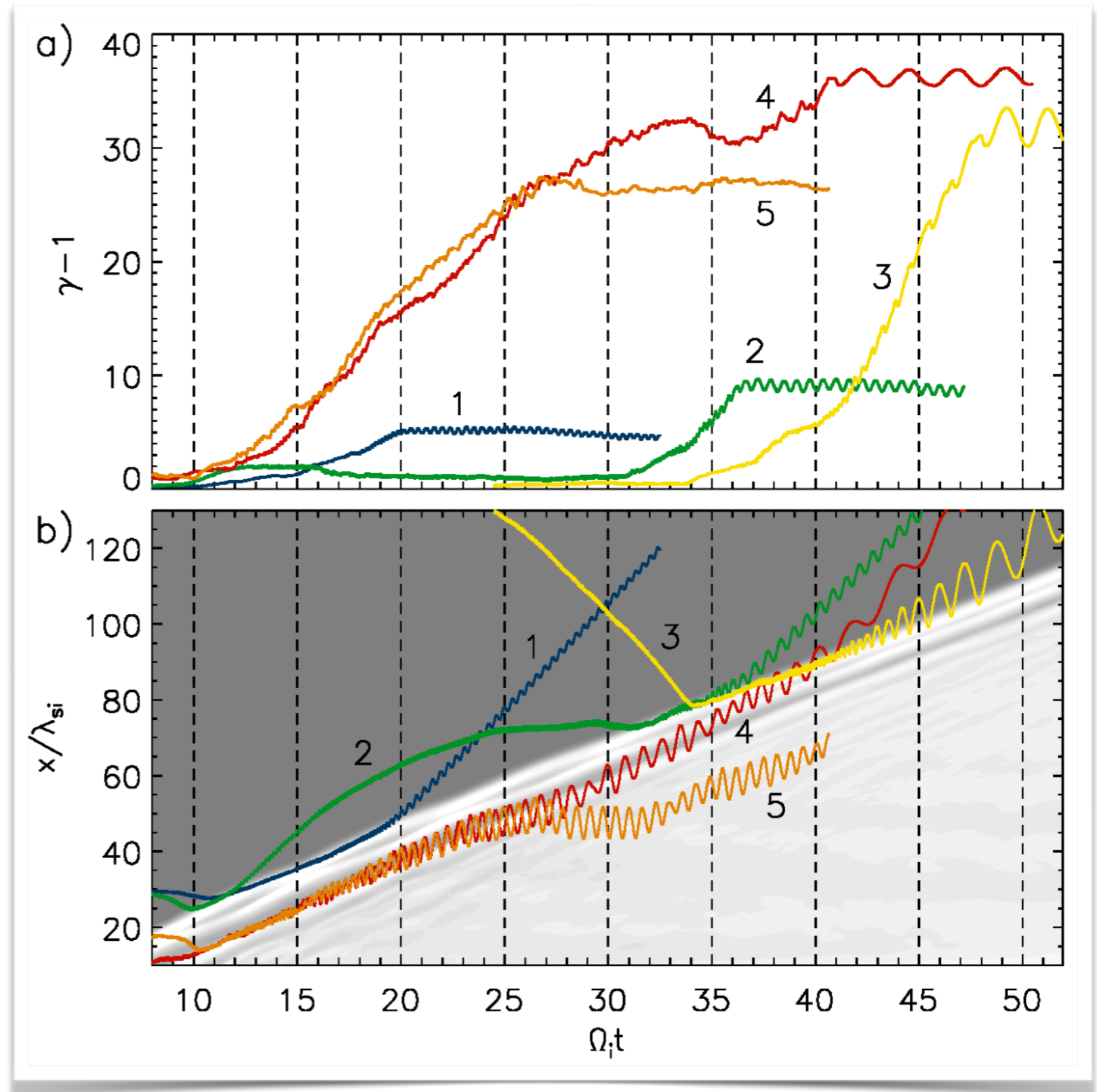
- substantial increase in non-thermal tail production efficiency coincident with the onset of the shock rippling at  $\Omega_{ci}t \approx 25$
- maximum electron energy sufficient for injection to DSA:  $\gamma_{inj} \approx 25$  ( $p_{inj} \sim 3p_{th,i}$ )

$$\gamma_{max,up} \approx 40 - 60$$

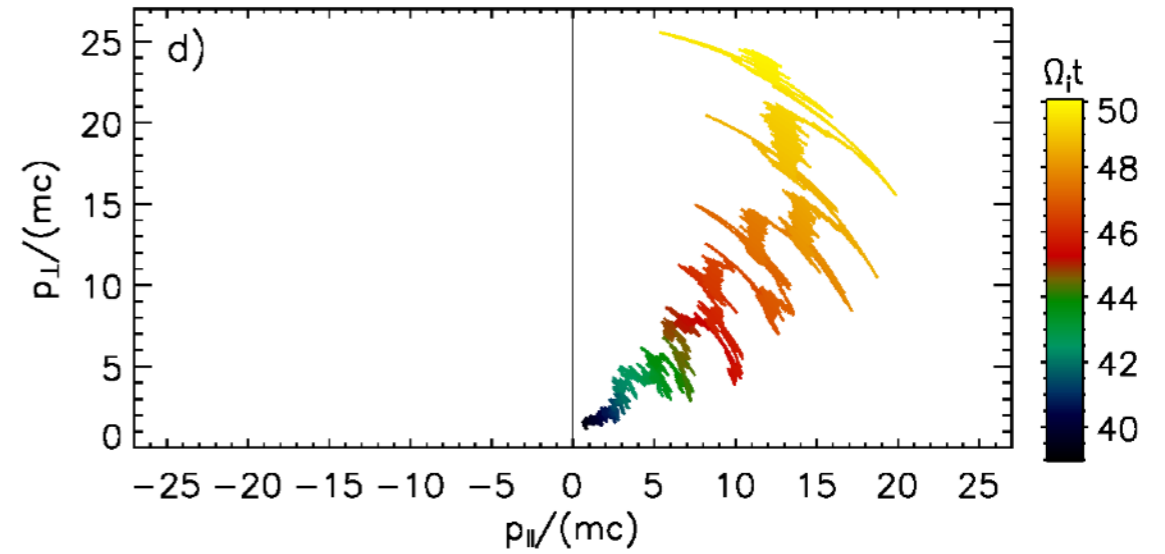
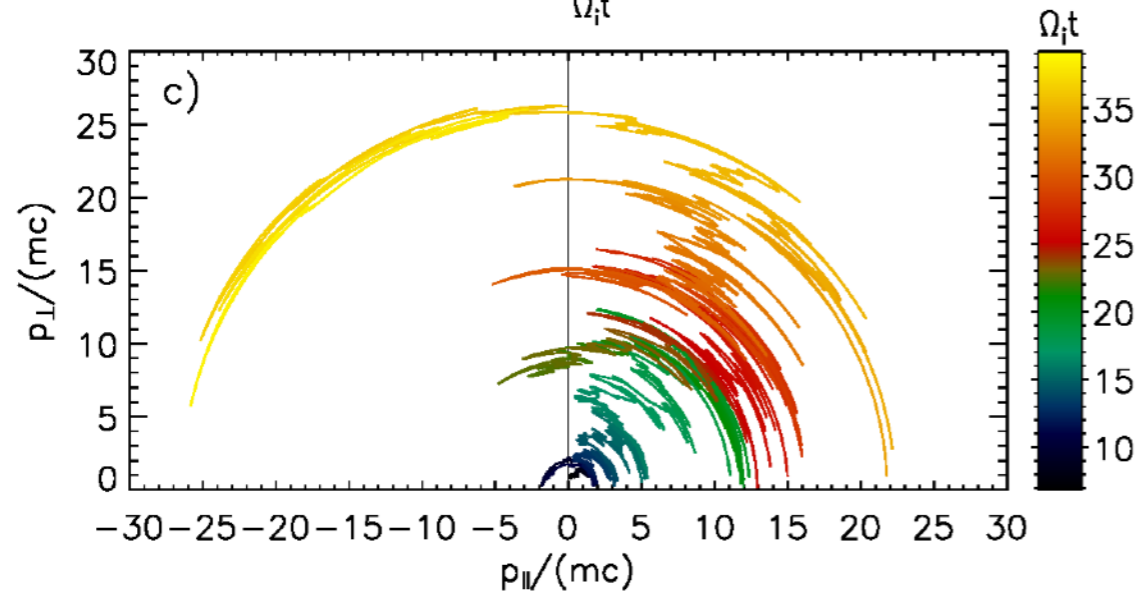
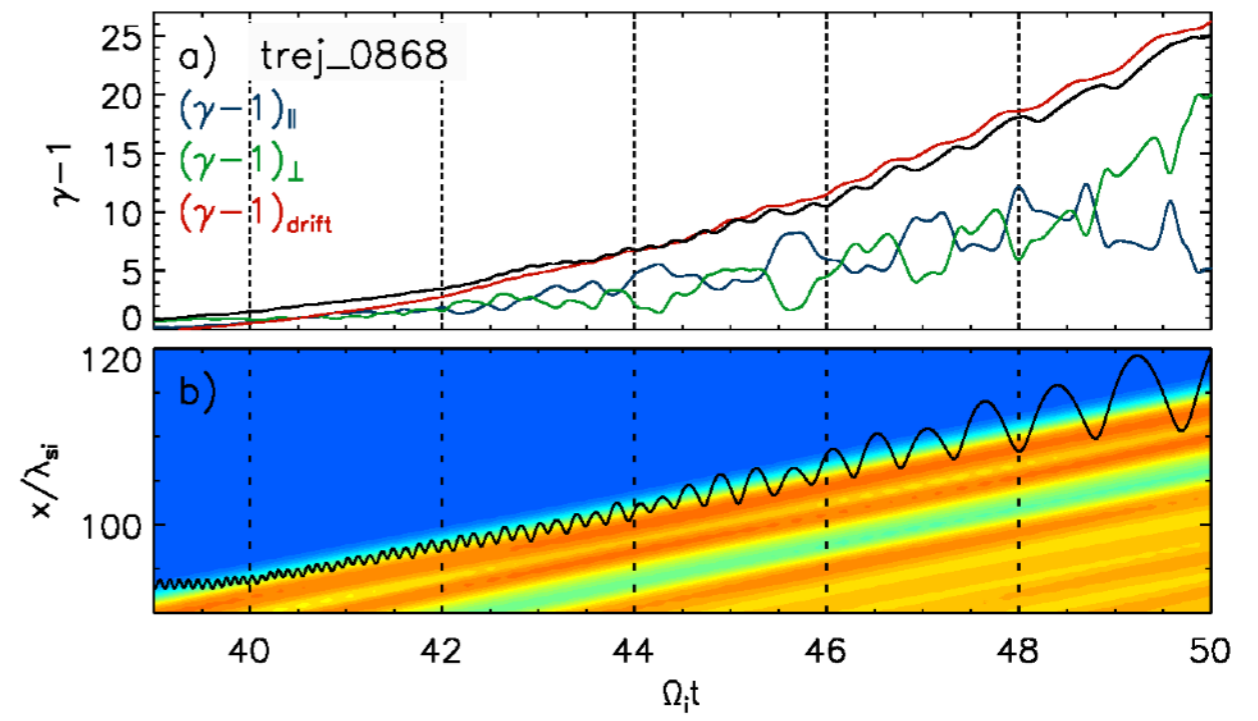
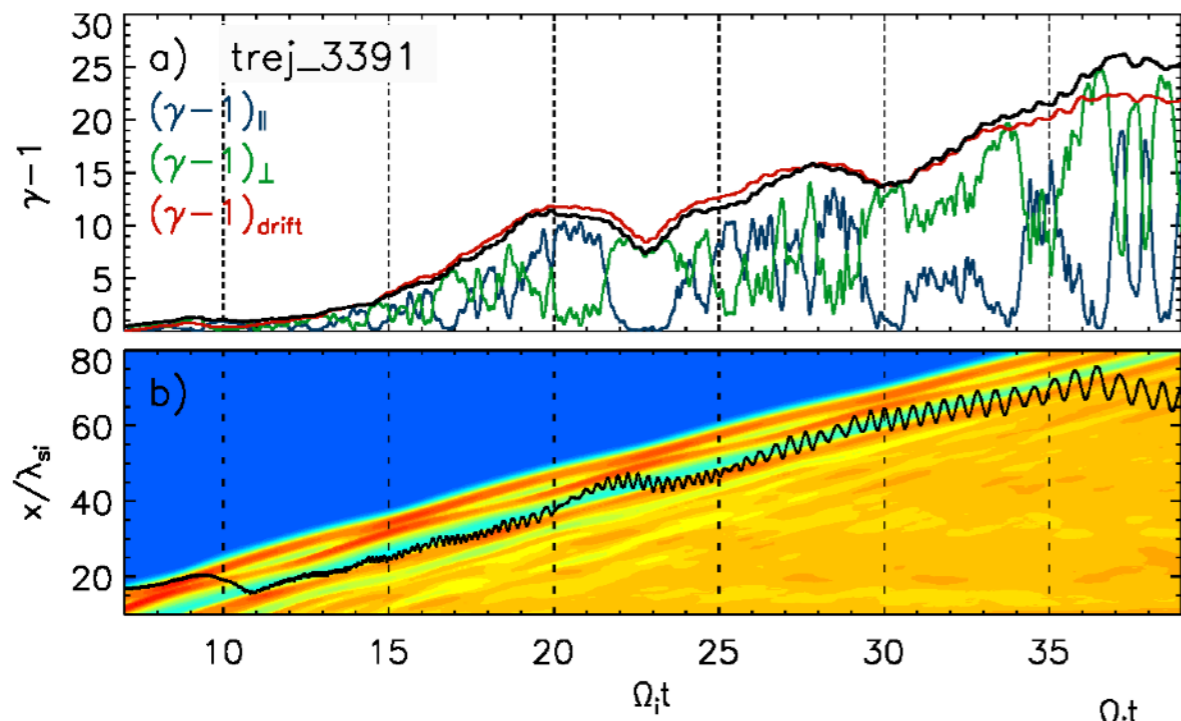
- limited-range power-law spectra  
downstream

# Acceleration processes - typical particle trajectories

- most particles gain their energies in a **single** interaction with the shock
- acceleration time much longer than predicted by SDA ( $\sim 1/\Omega_i$ )
- highest-energy electrons produced at the shock front via interactions with long-wave ripples
- bulk of high-energy electrons accelerated deep in the shock transition



$$(\beta=5, \vartheta_{Bn}=75^\circ)$$



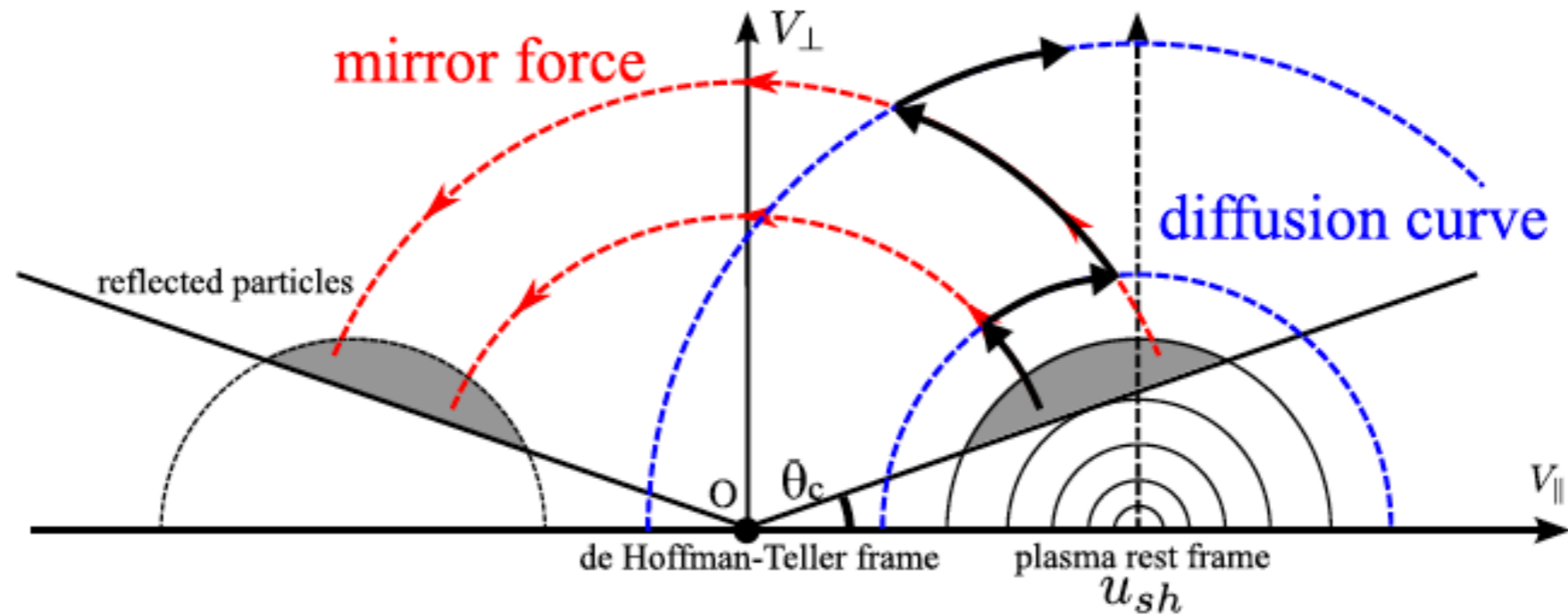
- most accelerations associated with an increase in  $p_{\perp}$
- strong **pitch-angle scattering** (arcs in  $p_{\parallel}$ - $p_{\perp}$  momentum space)
- energy gain mostly through the drift along motional electric field:

$$\Delta\gamma_{\text{drift}} = (-e/m_e c^2) \int E_z dz$$

→ Stochastic Shock-Drift Acceleration (SSDA)

# Stochastic Shock Drift Acceleration (SSDA)

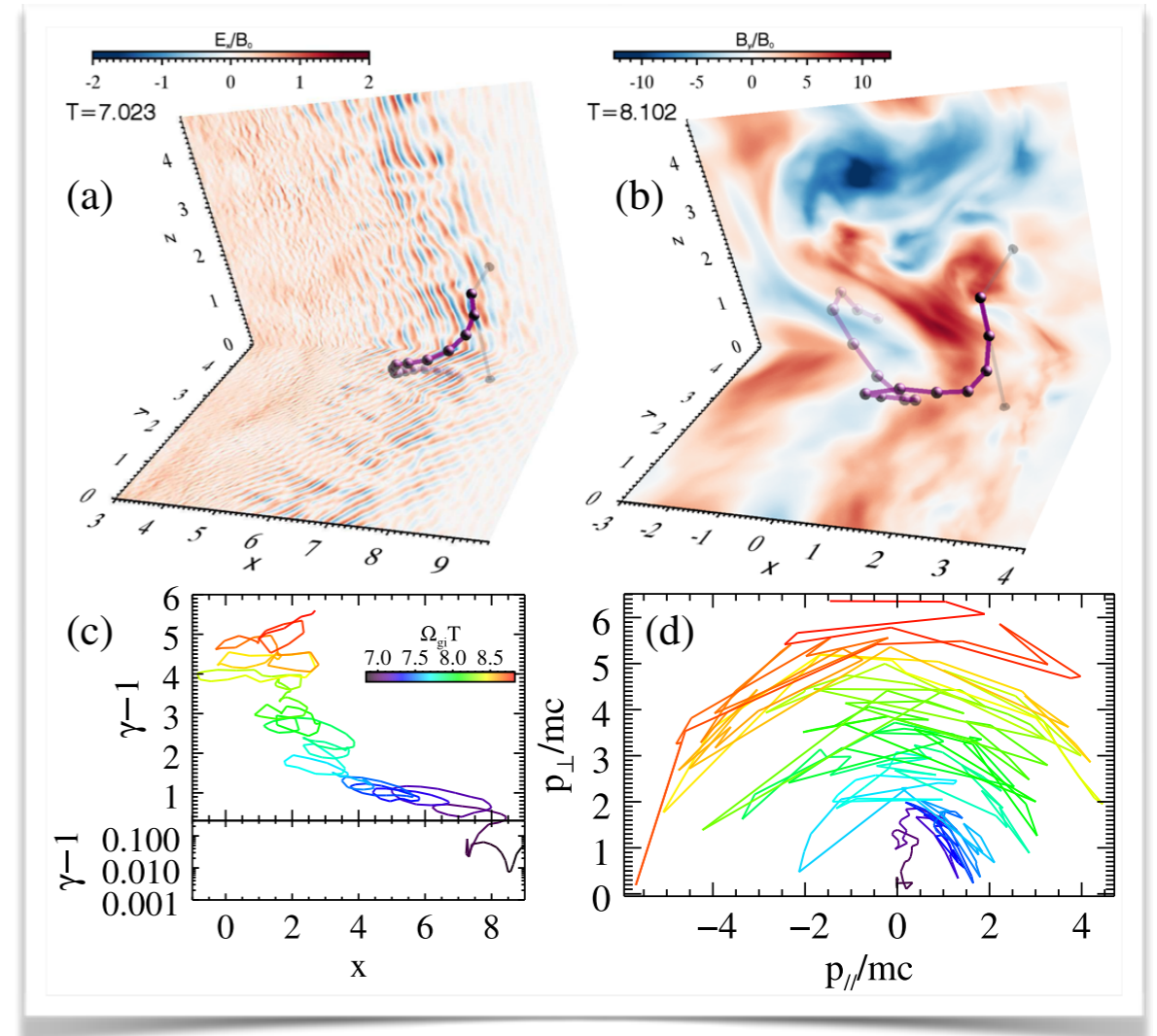
Katou & Amano (2019)



- adiabatic mirror reflection in the HTF
- elastic scattering (diffusion) in the plasma rest frame

- electrons are confined in the shock transition region by stochastic pitch-angle scattering off magnetic turbulence and gain energy through SDA (non-adiabatic acceleration)
- longer particle confinement increases energy gains and enables more efficient acceleration than standard SDA

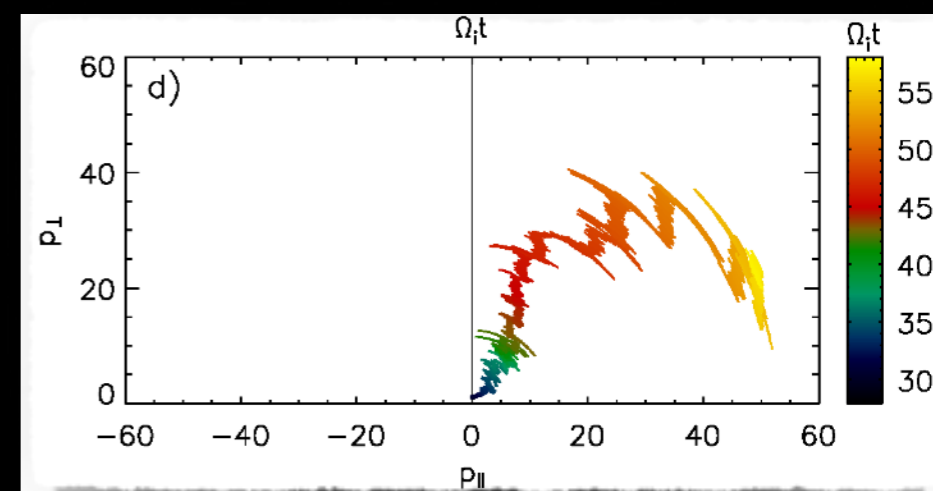
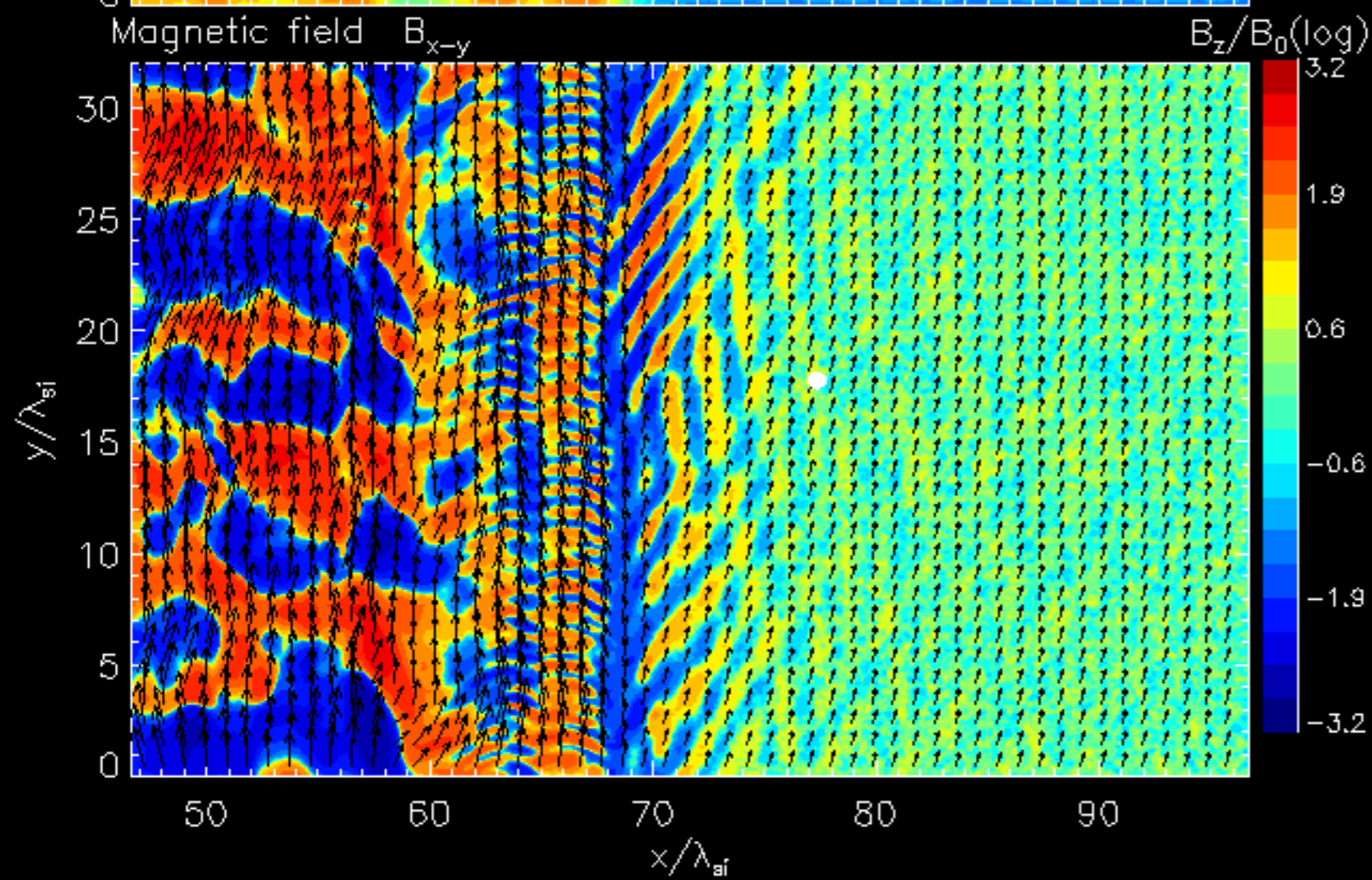
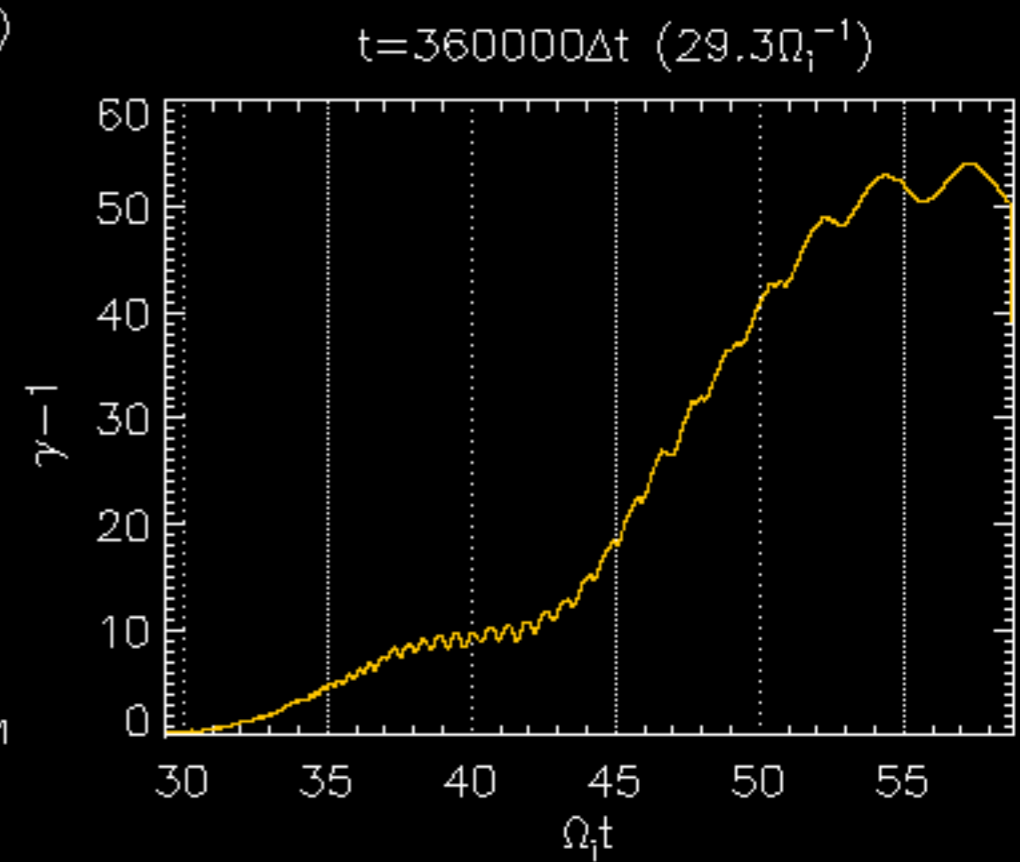
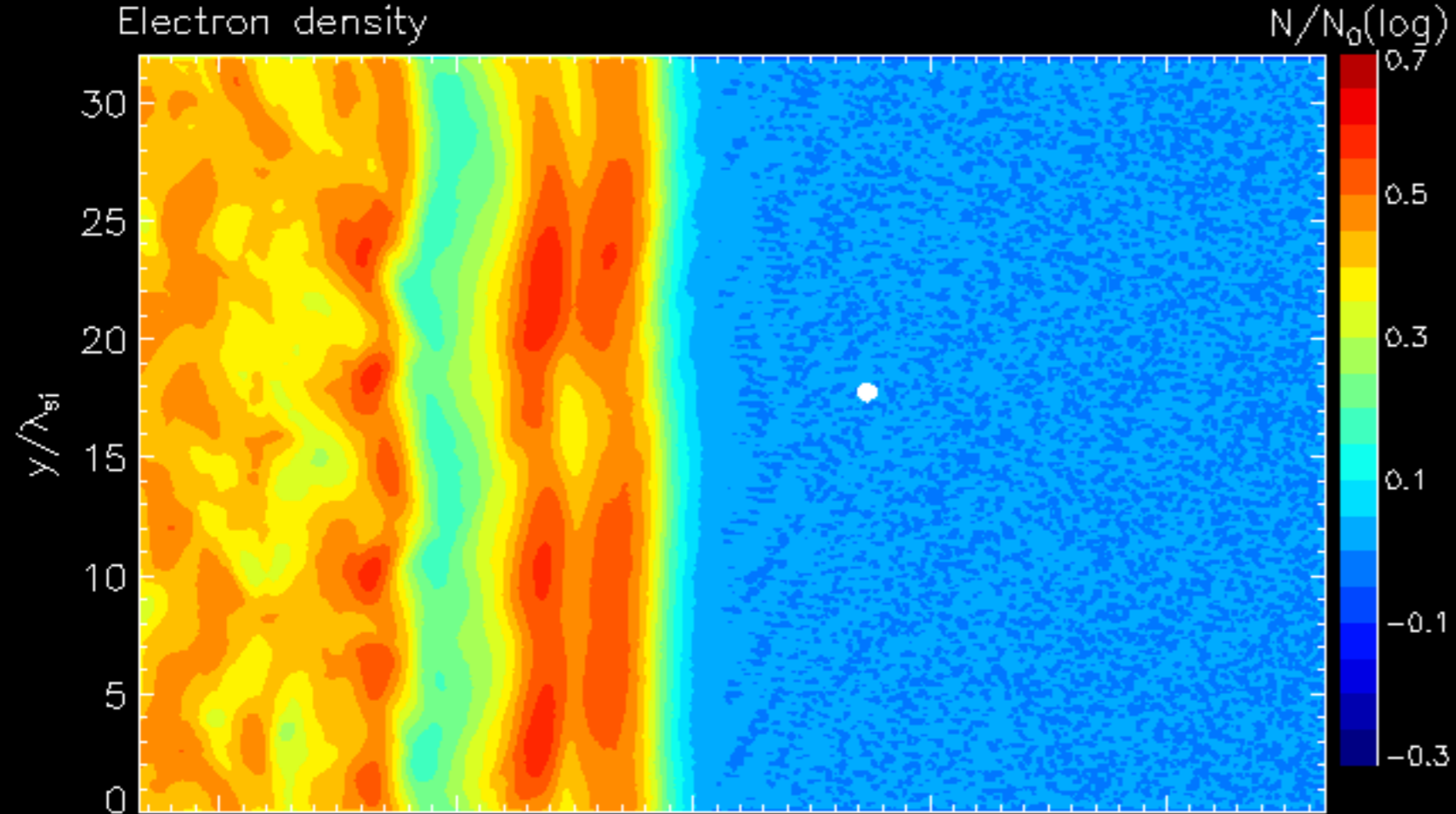
- observational evidence for electron injection via SSDA at the Earth's bow shock recently provided by Magnetospheric Multiscale mission (Oka et al. 2017, Amano et al. 2020) - **high-frequency whistlers**
- SSDA observed in 3D PIC simulations of quasi-perpendicular high Mach number shocks of young supernova remnants ( $M_s=22.8$ ,  $\beta=1$ ; Matsumoto et al. 2017) - **Weibel instability modes at the shock foot**
- also observed in hybrid PIC and test-particle studies of solar wind shocks ( $M_s=6.6$ ,  $\beta=1$ ; Trotta & Burgess 2019) - **shock-surface fluctuations**

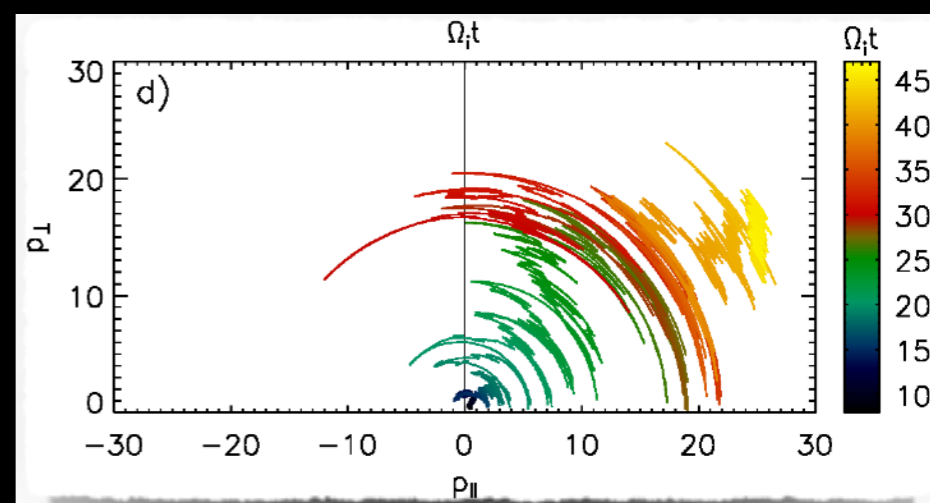
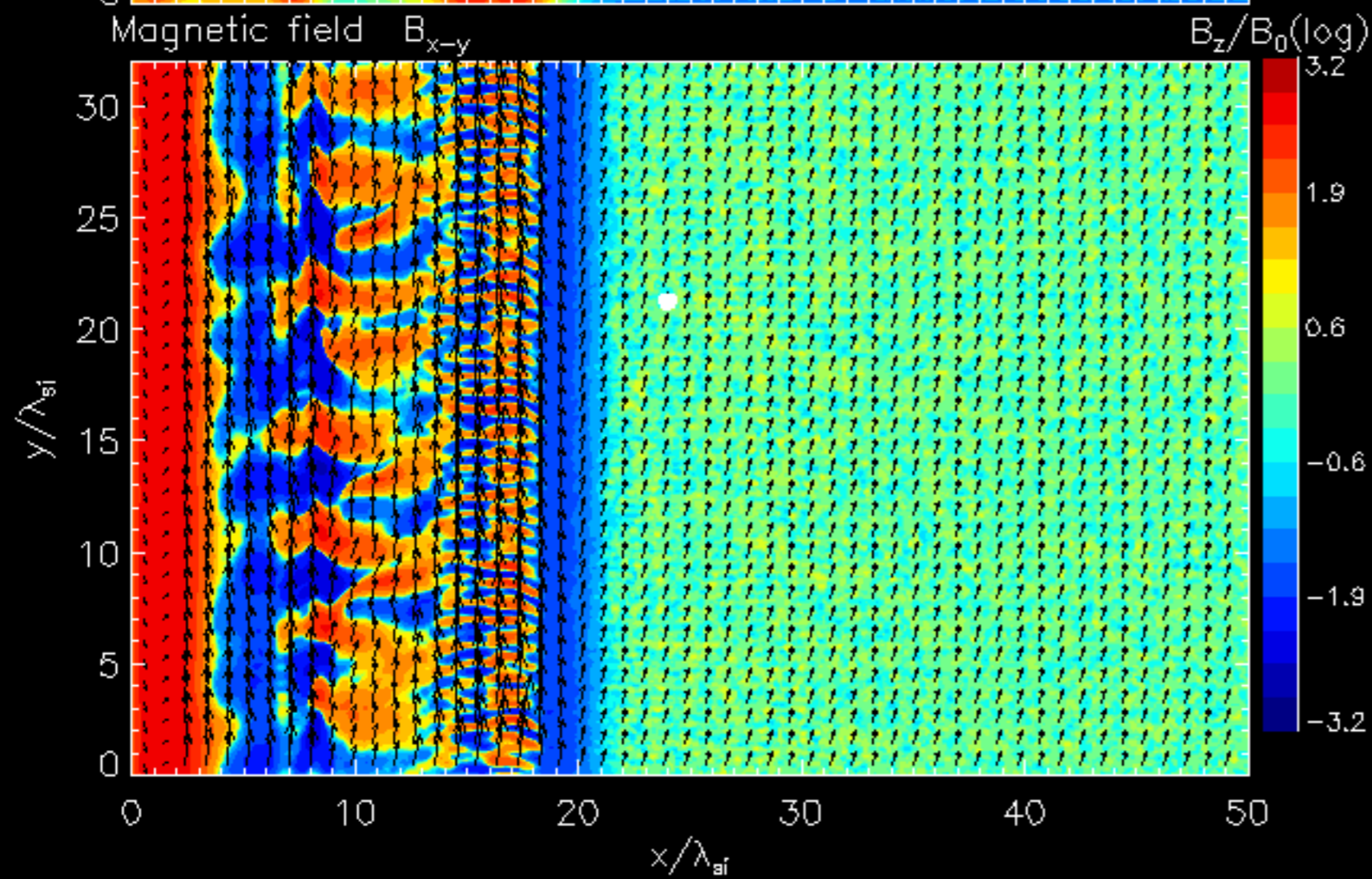
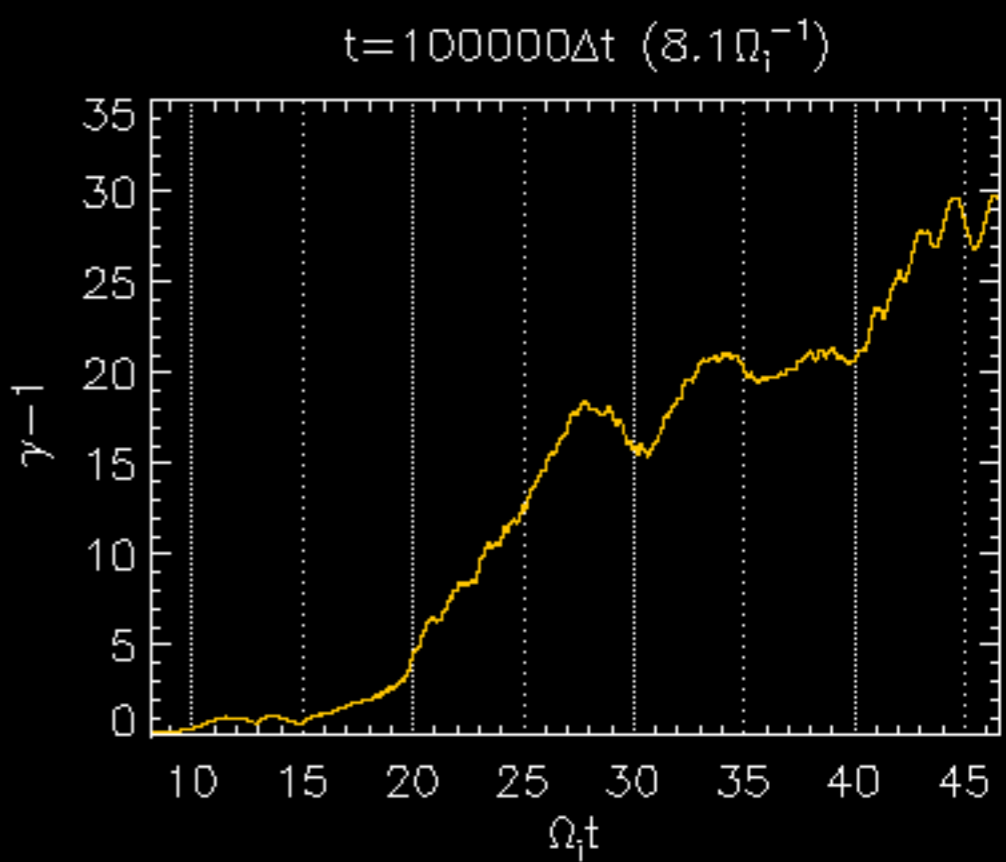
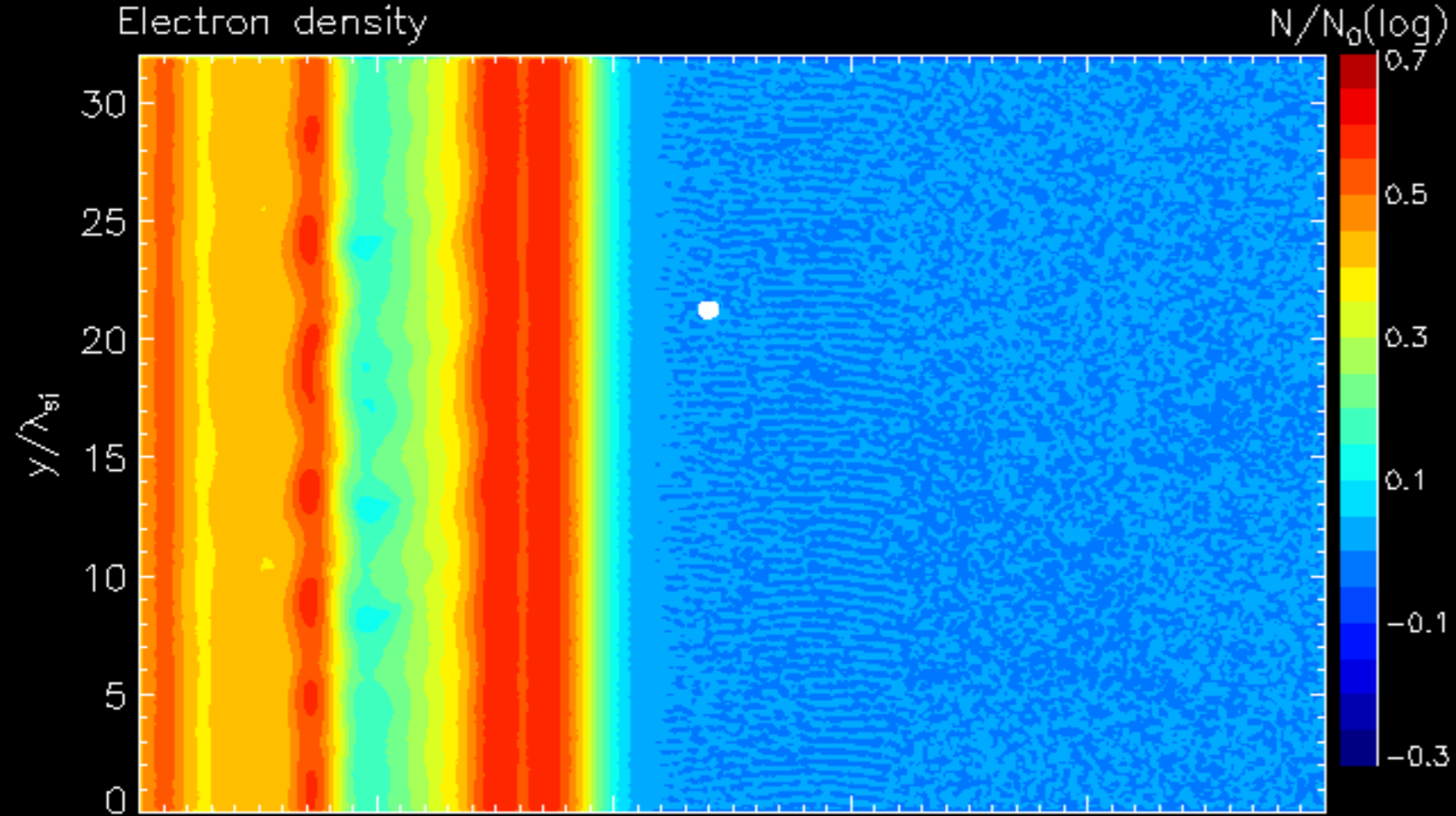


Matsumoto et al. (2017)

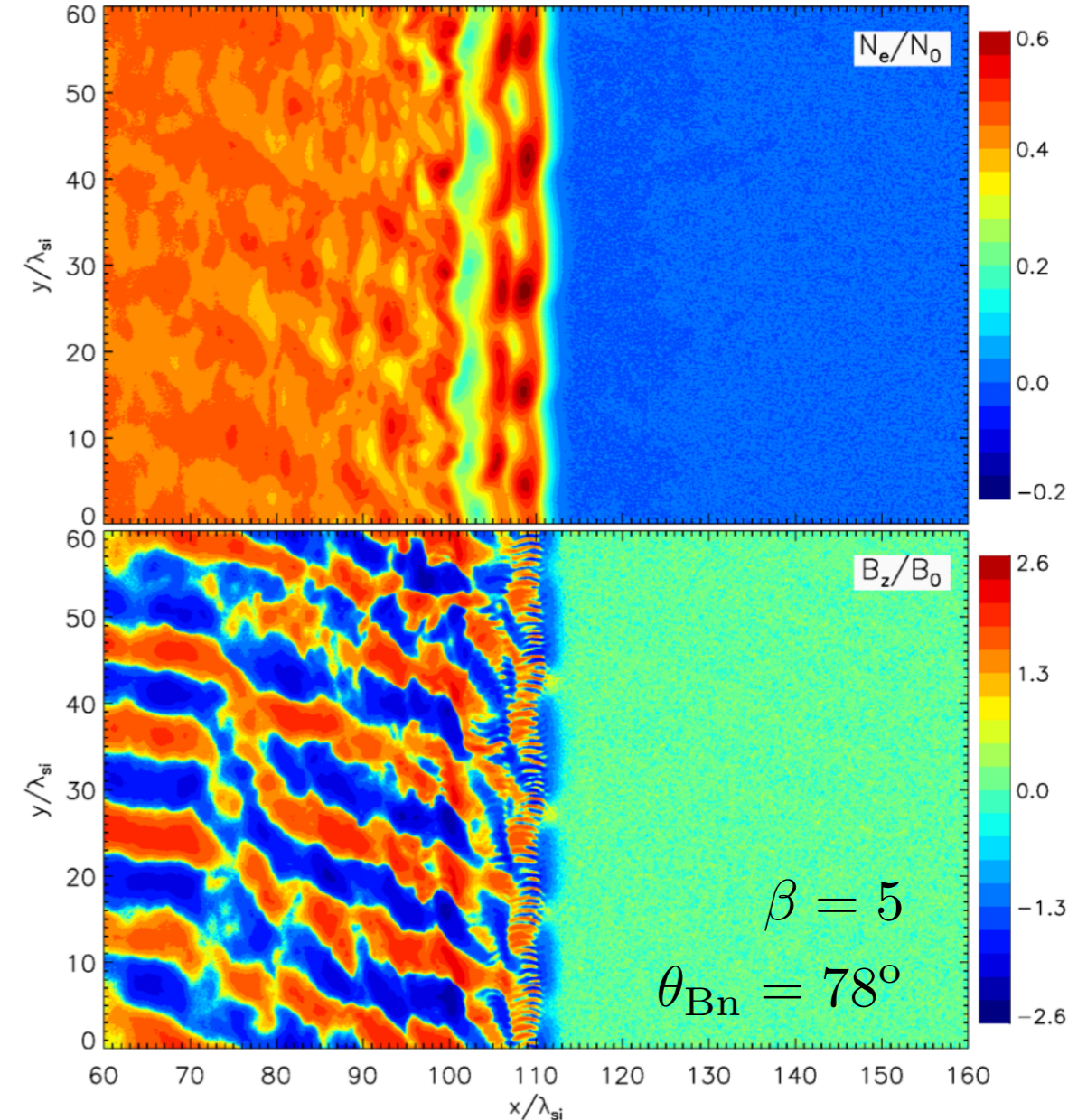
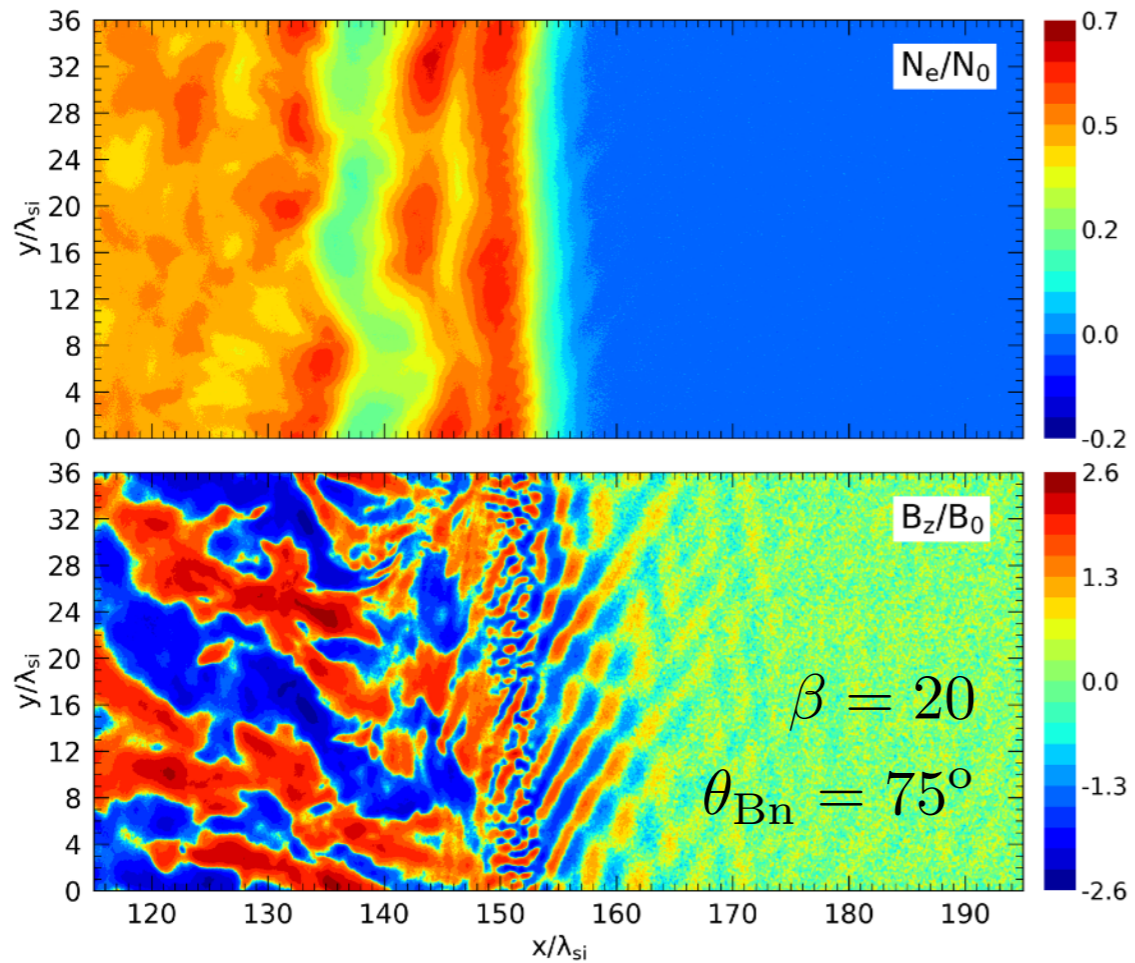
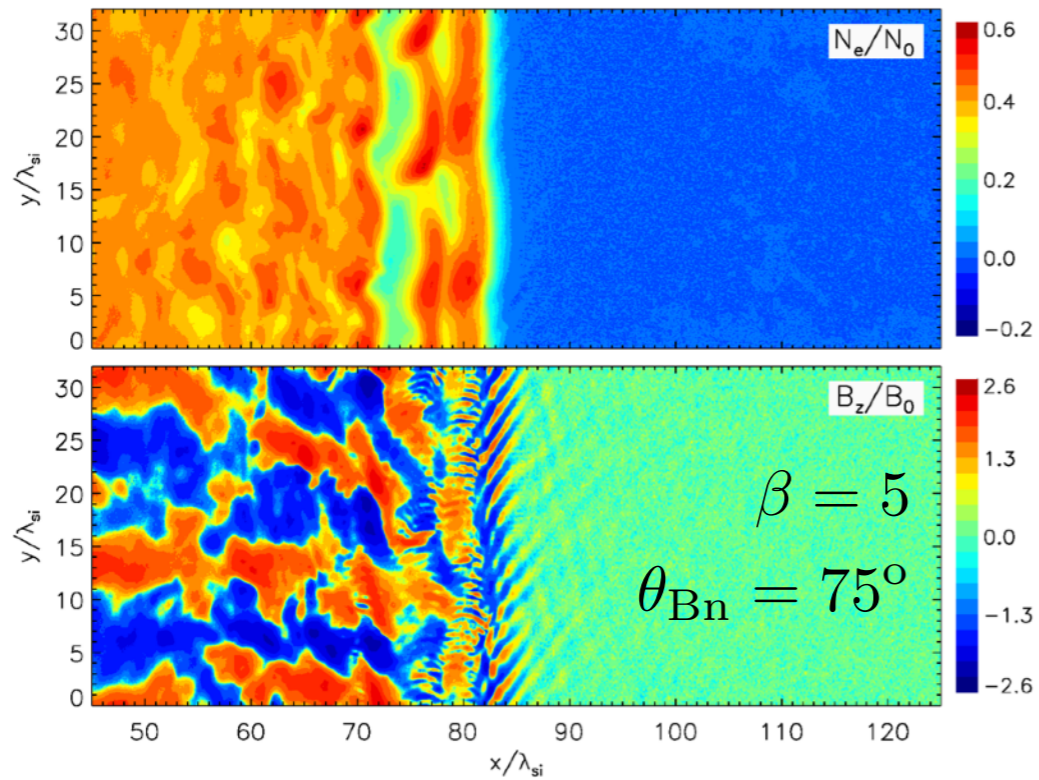
**3D**,  $M_A=20.8$ ,  $M_s=22.8$ ,  $\vartheta=74.3^\circ$ ,  $m_i/m_e=64$ ,  $\beta=1$

- results for shocks with  $\beta=5$  and  $\vartheta_{Bn}=75^\circ$  show that the electron scattering can be due to **multi-scale** (broad-band) **turbulence in the entire shock transition**





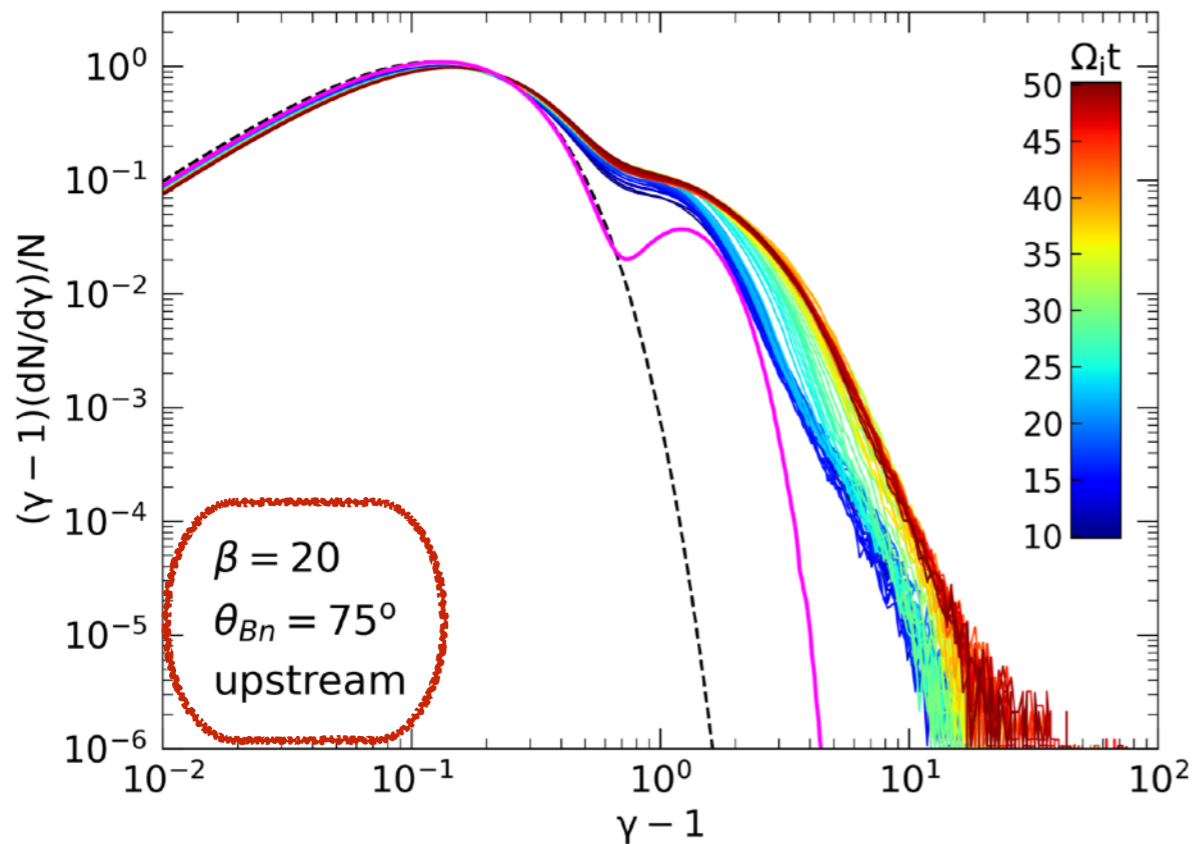
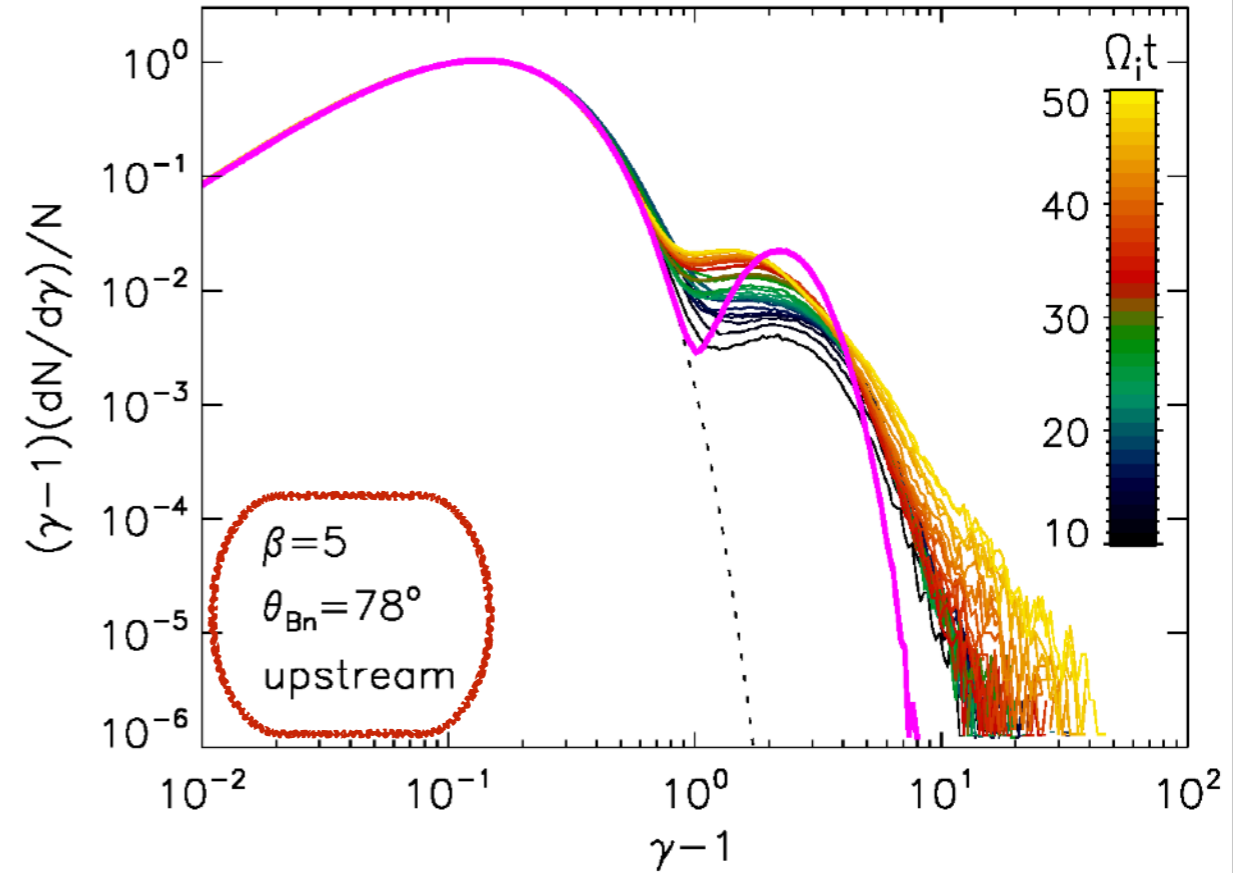
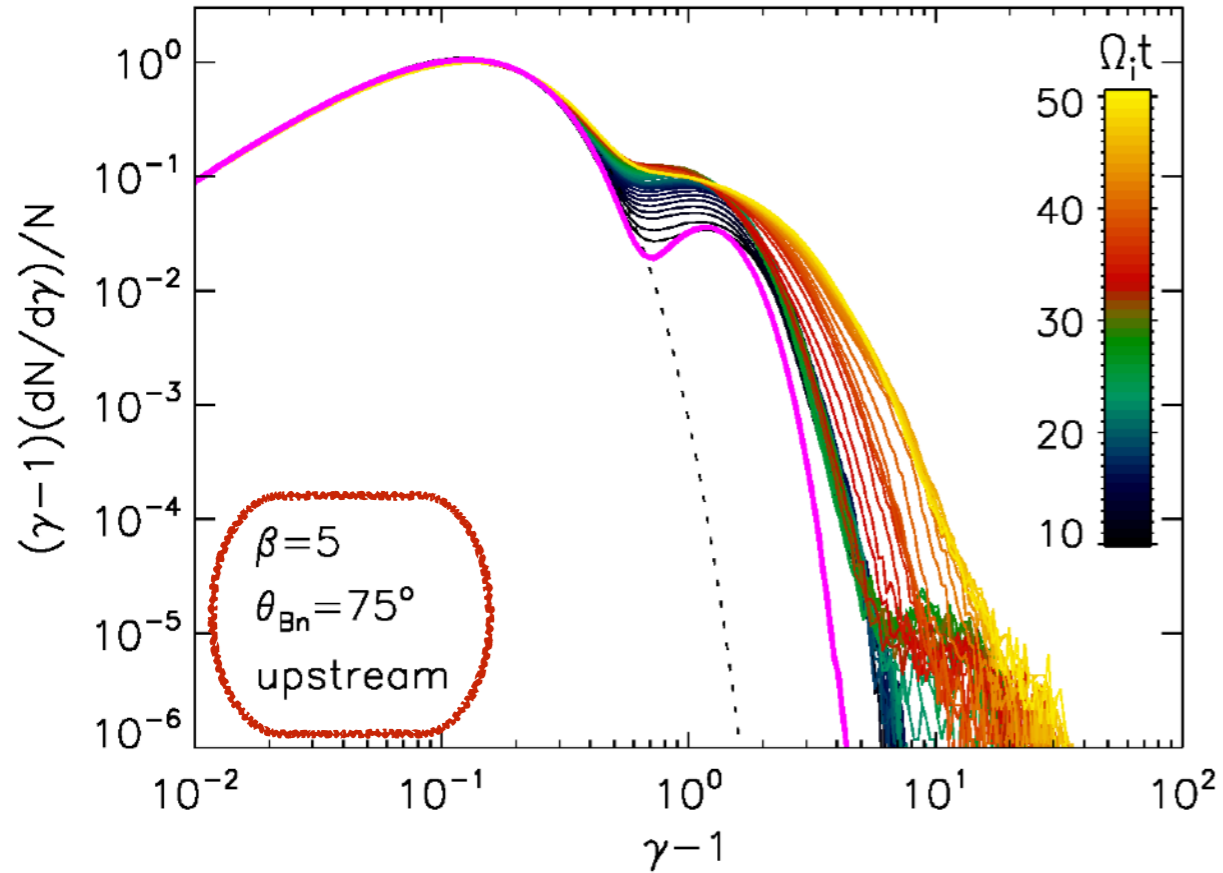
# Parameter dependence - multi-scale turbulence



- features of multi-scale turbulence similar in all cases
- longer-wavelength ripples with growing  $\beta$
- absence of EFI waves for higher  $\theta_{Bn}$
- stronger and longer-wavelength EFI modes with increasing  $\beta$  (after amplification in rippled shocks)

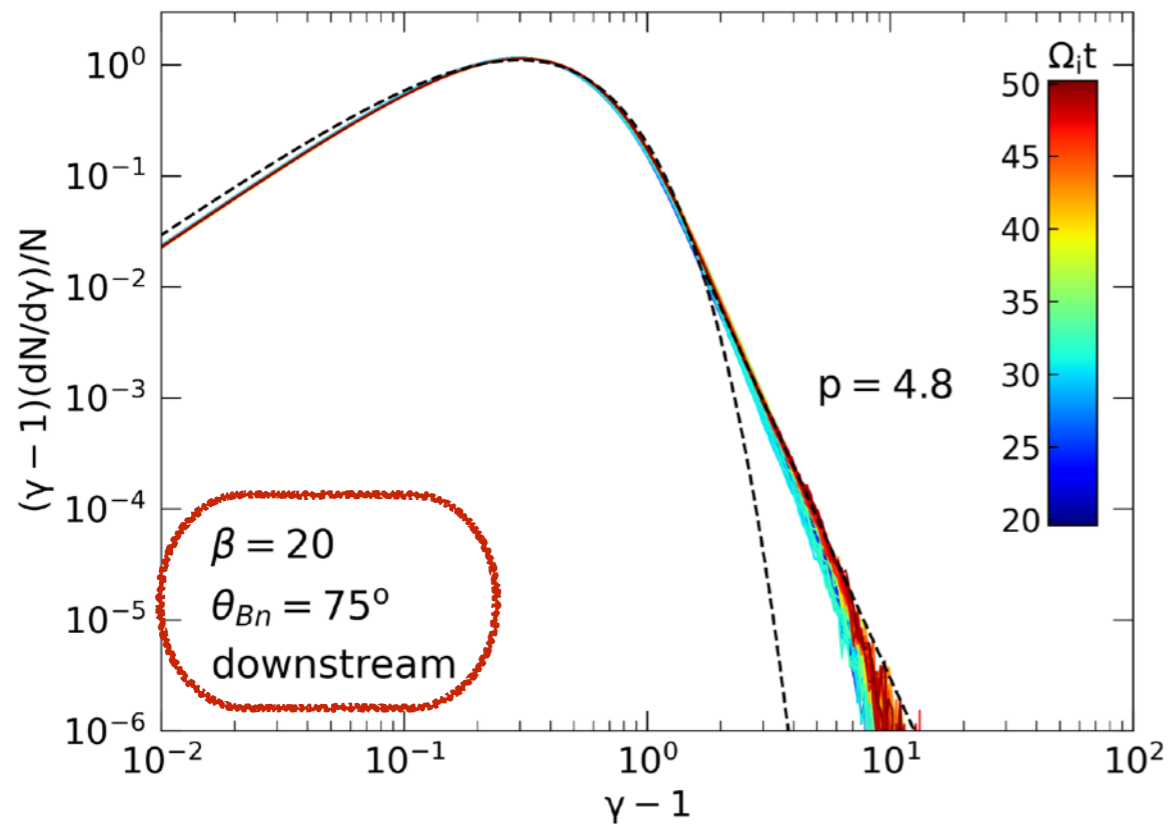
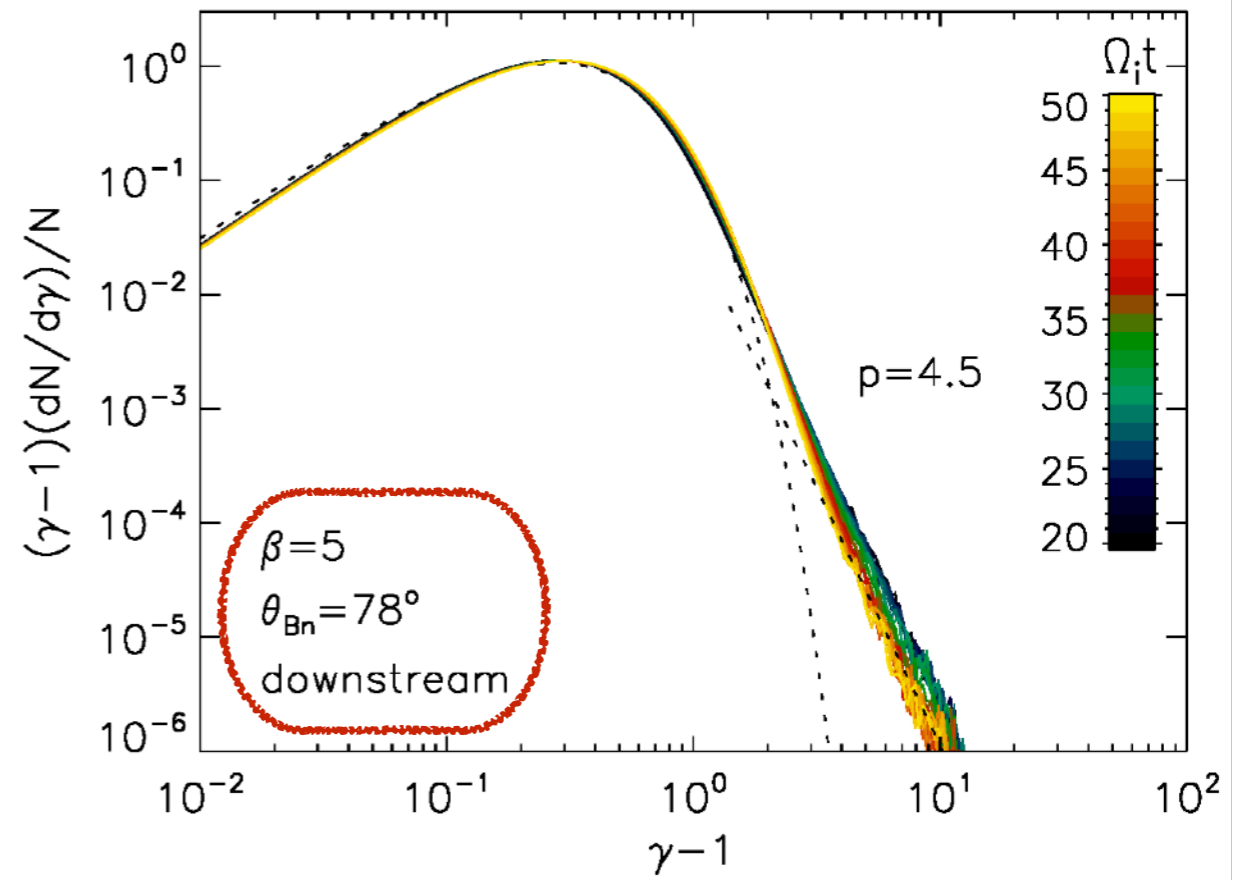
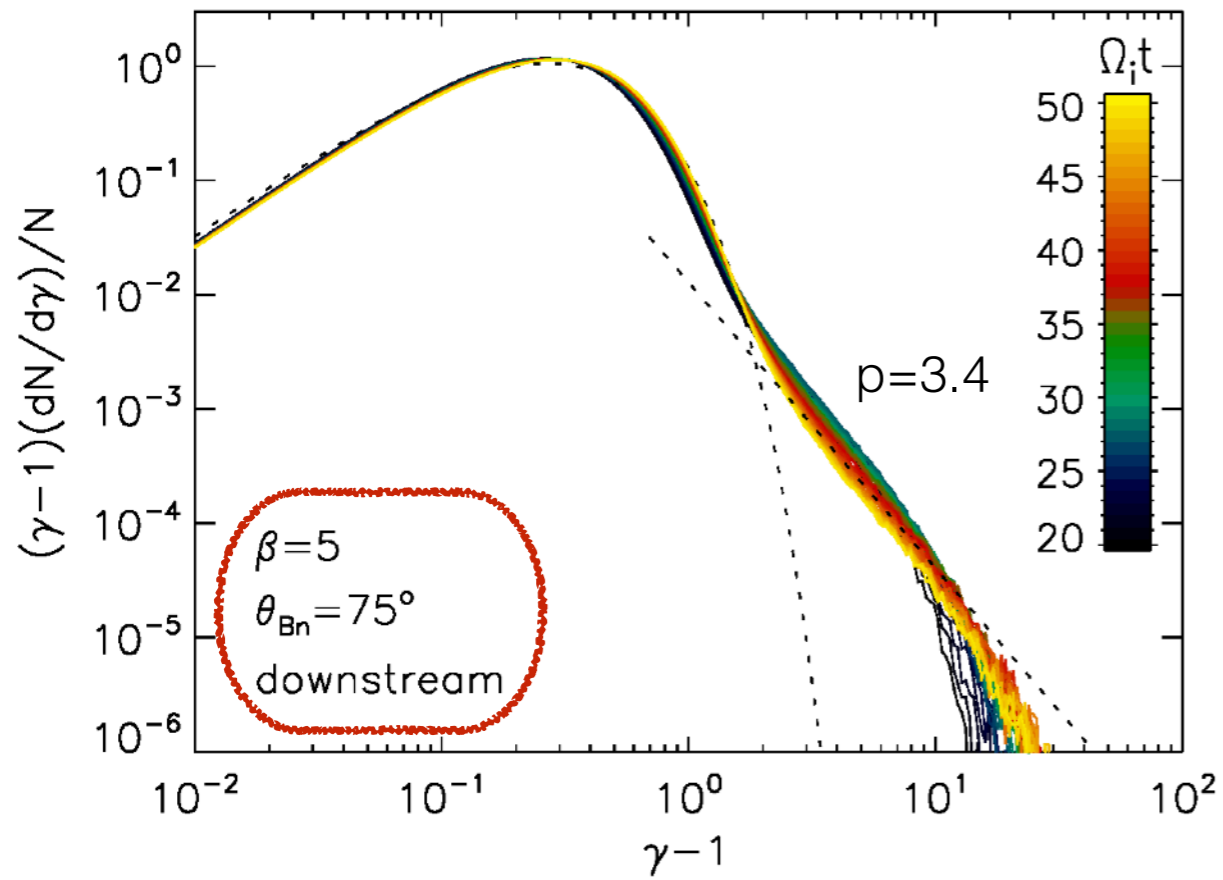


# Parameter dependence - upstream spectra



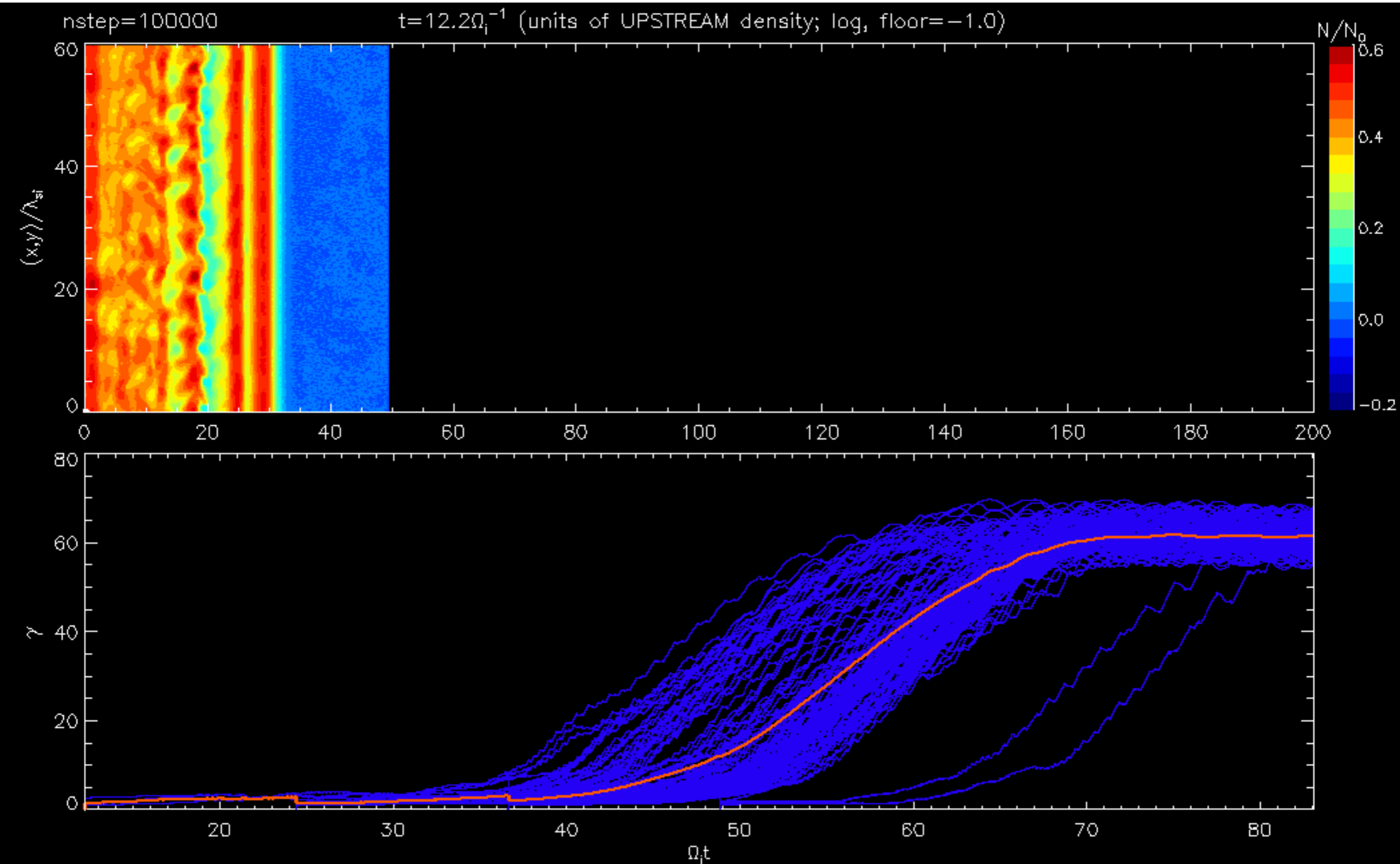
- SSDA in rippled shocks provides electron acceleration also for higher  $\beta=10-30$  (up to  $\beta=100$  - Ha et al. 2021)
- upstream spectra depend weakly on  $\beta$
- maximum energies  $\gamma_{max} \sim 30-40 > \gamma_{inj}$
- multiple-cycle SDA is not critical for injection but may contribute to electron acceleration in high- $\beta$  plasmas

# Parameter dependence - downstream spectra



- downstream spectra steepen with increasing  $\beta$  and  $\theta_{Bn}$

Sample trajectories of electrons with  $\gamma_{max} \sim 55-70$ ;  $\vartheta_{Bn} = 78^\circ$



- gradual formation of supra-thermal tails
- electrons accelerated exclusively at the shock front - superluminal cond. at 2nd overshoot
- some of them diffuse downstream

# Summary and conclusions

- kinetic modeling of particle acceleration at low Mach number shocks in high-beta plasmas requires multi-dimensional and large-scale effects to be taken into account
- the presence of multi-scale turbulence, including ion-scale shock rippling modes, is critical for efficient electron acceleration
- electrons can be injected to DSA at quasi-perpendicular sub-luminal ICM shocks that develop multi-scale turbulence
- electron injection proceeds mainly through the stochastic SDA process, effects of multi-SDA cycles can also occur
- pre-acceleration to high energies feasible, at which DSA starts to operate in the presence of long-wave (MHD) upstream turbulence