



Muon g-2 at Fermilab: Current status and outlook

Dominika Vasilkova (on behalf of the Muon g-2 collaboration)
Lake Louise Winter Institute
2023

The magnetic moment of the muon

- Charged particle in B field interacts via intrinsic magnetic moment:

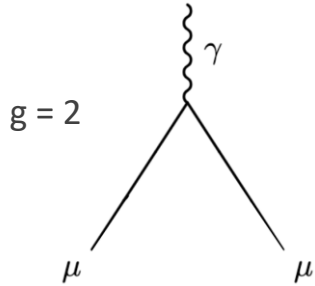
$$\vec{\mu} = g \frac{q}{2m} \vec{S}$$

- Dirac equation predicts $g = 2$ for spin $\frac{1}{2}$ particles, but virtual particles in loops lead to corrections: **$g > 2$** .
- Unique indirect way to test precision of SM!

- We define the 'anomalous magnetic moment' and measure that:

$$a_{\mu} = \frac{g - 2}{2}$$

Theoretical predictions

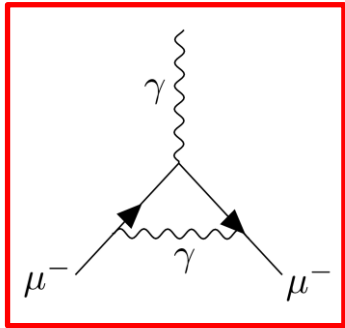


1st Order QED
(Schwinger)

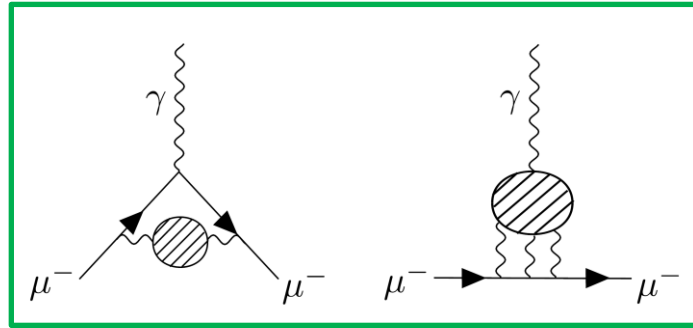
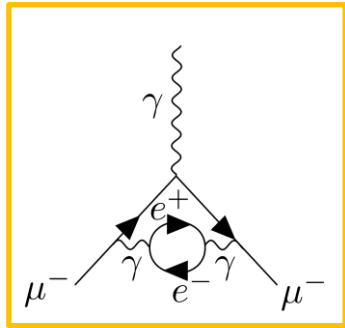
Higher order
QED (Vacuum
polarization)

$$a_\mu (\text{SM}) = 116591810(43) \times 10^{-11}$$

(Muon g-2 theory initiative: WP2020)

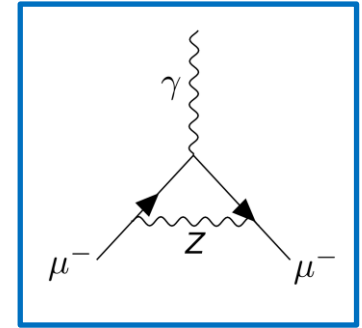


Uncertainties: $\sim 0.1 \times 10^{-11}$



HVP: $\sim 40 \times 10^{-11}$

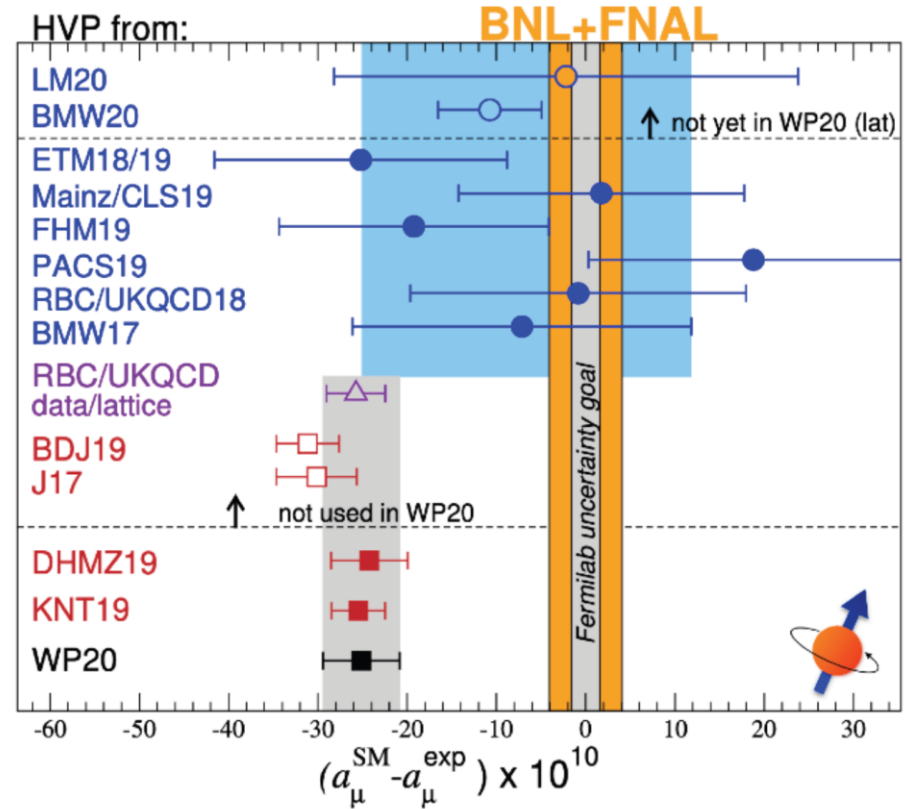
HLBL: $\sim 19 \times 10^{-11}$



$\sim 1 \times 10^{-11}$

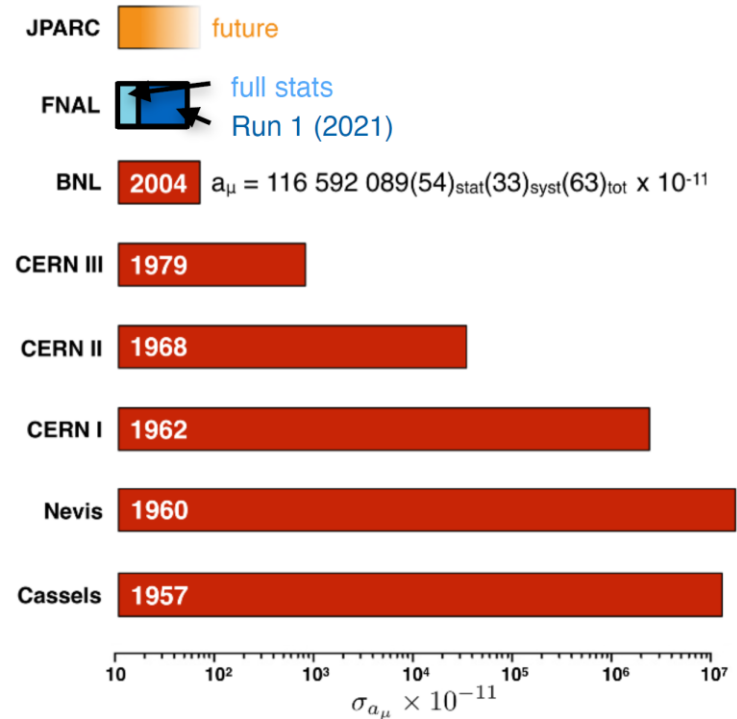
Theoretical predictions

- Uncertainty dominated by HVP.
- Two methods to get this – dispersive methods, and lattice.
- Growing tension between the two – allows for a 3-way comparison.



Experimental measurements

- Previous best measurement at Brookhaven National Laboratory – 3.7σ discrepancy with SM.
- Aim at FNAL is to redo measurement with 4x better precision (140ppb).
- Future measurement also planned at JPARC.



Measuring a_μ in a storage ring

- Beam of polarized muons in a storage ring, 1.45 T vertical B field.
- Two oscillations: cyclotron frequency and spin precession. Measure the difference:

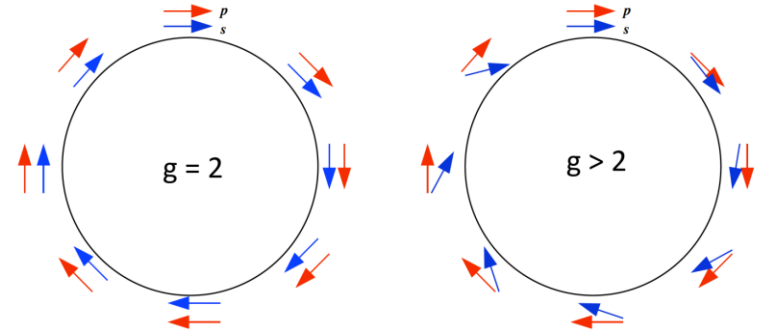
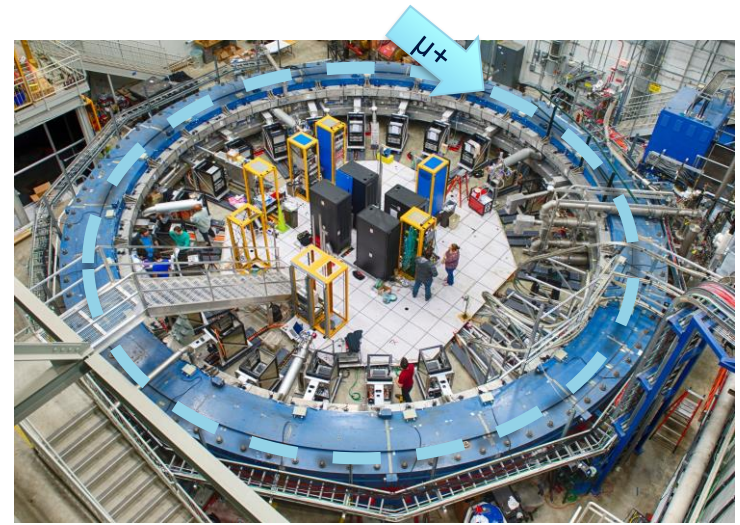
$$\omega_a = \omega_S - \omega_P \cong a_\mu \frac{eB}{m_\mu}$$

- If we also measure the field to high precision: can extract a_μ .

$$a_\mu = \frac{\omega_a}{\tilde{\omega}_p} \frac{g_e \mu_p m_\mu}{2 \mu_e m_e}$$

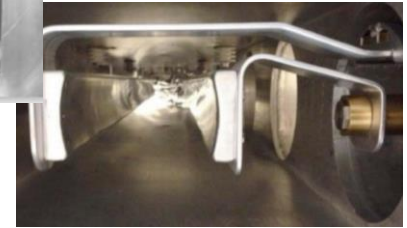
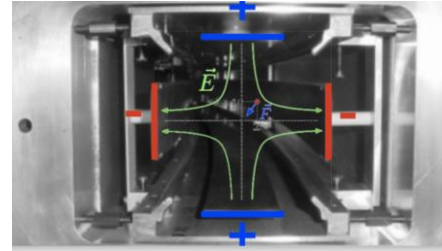
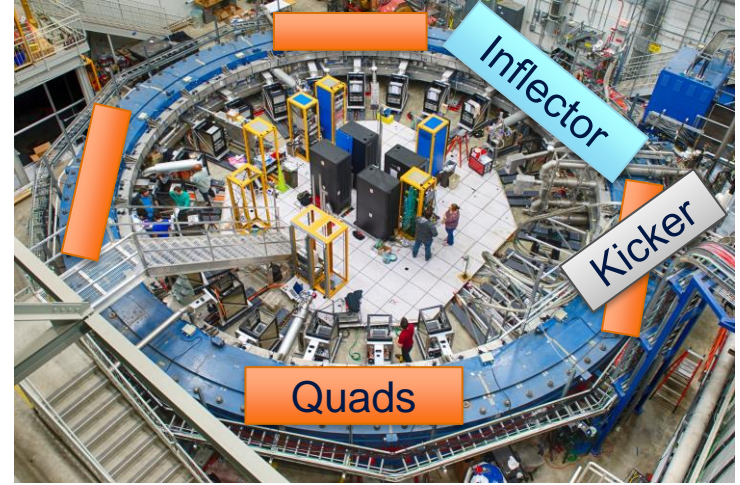
Measured by us

Measured by other experiments



Storage

- Magnet: Radial focusing.
- Inflector: Prevents large beam deflections.
- Kicker: Pushes incoming beam onto equilibrium orbit.
- Electrostatic quadrupoles: vertical focusing.



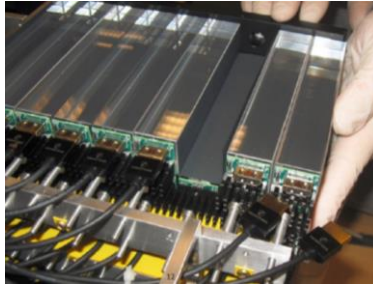
~~$$\vec{\omega}_a = \frac{e}{m} \left[a_\mu \vec{B} - a_\mu \frac{\gamma}{\gamma+1} (\vec{\beta} \cdot \vec{B}) \vec{\beta} - \left(a_\mu - \frac{1}{\gamma^2-1} \right) \vec{\beta} \times \vec{E} \right]$$~~

0 when in a flat plane

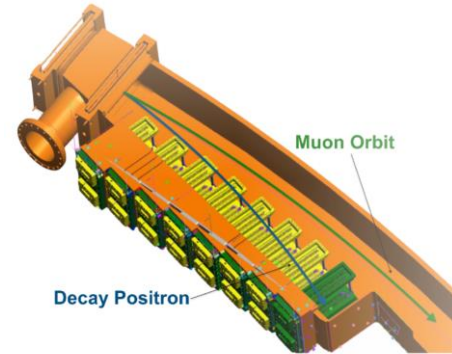
0 at the 'magic momentum' = 3.094 GeV

Measurements

- 24 PbF_2 calorimeters around inside of ring
 - 54 crystals read by SiPMs
 - Laser calibration



- 2 straw tracker stations
 - 8 modules per station, 4 x 32 straws $\text{Ar}:\text{C}_2\text{H}_6$
 - Beam dynamics and muon distribution
 - Bonus analyses: e.g. muon EDM



Our 'master formula'

blinding factor precession beam dynamics corrections

$$\frac{\omega_a}{\tilde{\omega}'_p} \approx \frac{f_{\text{clock}} \omega_a^{\text{meas}} \left(1 + C_e + C_p + C_{ml} + C_{pa}\right)}{f_{\text{calib}} \left\langle \omega'_p(x, y, \phi) \times M(x, y, \phi) \right\rangle \left(1 + B_K + B_Q\right)}$$

absolute field
calibration

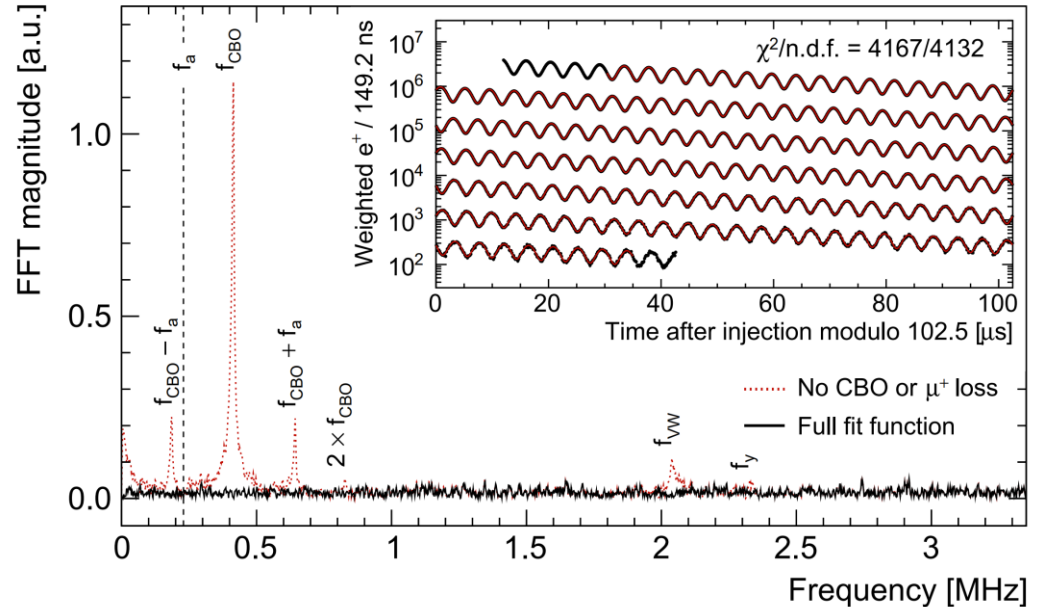
magnetic field sampled
by the muon distribution

Magnetic transients
corrections

Blinding, extracting ω_a

- To avoid bias, we blind the frequency at a hardware and software level.
- Parity violating decay – high E e^+ emitted preferentially along spin direction.
- ω_a extracted from the wiggler plot using a 22-parameter fit.

$$\frac{\omega_a}{\tilde{\omega}'_p} \approx \frac{f_{\text{clock}} \omega_a^{\text{meas}} (1 + C_e + C_p + C_{ml} + C_{pa})}{f_{\text{calib}} \langle \omega'_p(x, y, \phi) \times M(x, y, \phi) \rangle (1 + B_K + B_Q)}$$



Beam dynamics corrections

$$\frac{\omega_a}{\tilde{\omega}'_p} \approx \frac{f_{\text{clock}} \omega_a^{\text{meas}} \left(1 + C_e + C_p + C_{ml} + C_{pa} \right)}{f_{\text{calib}} \left\langle \omega'_p(x, y, \phi) \times M(x, y, \phi) \right\rangle \left(1 + B_K + B_Q \right)}$$

- E-field correction (C_e) and pitch correction (C_p):

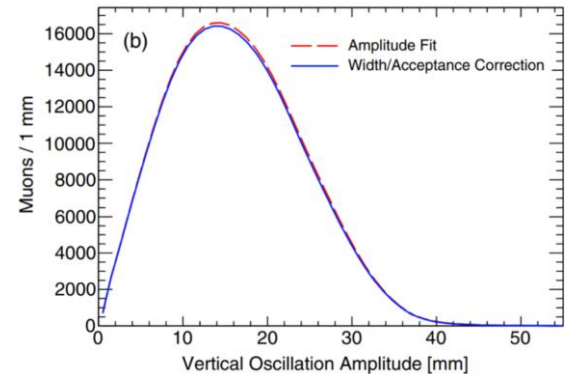
$$\vec{\omega}_a = \frac{e}{m} \left[a_\mu \vec{B} - a_\mu \frac{\gamma}{\gamma + 1} (\vec{\beta} \cdot \vec{B}) \vec{\beta} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \vec{\beta} \times \vec{E} \right]$$

0 when in a flat plane

0 at the 'magic momentum' = 3.094 GeV

Spread in muon momentum values, vertical betatron oscillations make these not exactly 0

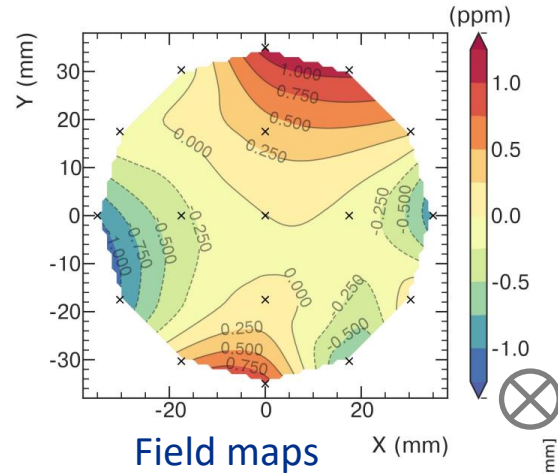
- Muon loss (C_{ml}) and Phase acceptance (C_{pa}).
Lost muons have a different phase, any time dependence in phase can bias ω_a
- Quantify these using tracker data/MC simulation.



Field measurements

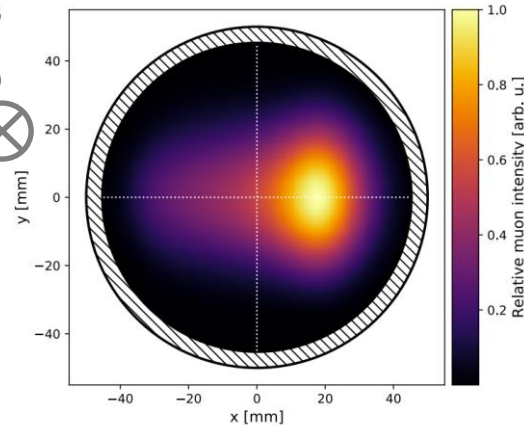
- Field calibrations with external H₂O probe.
- Trolley measures field maps, then fixed probes monitor in between trolley runs.
- Need to know what field the muon beam sees: so convolute with the muon beam from the trackers.

$$\frac{\omega_a}{\tilde{\omega}'_p} \approx \frac{f_{\text{clock}} \omega_a^{\text{meas}} (1 + C_e + C_p + C_{ml} + C_{pa})}{f_{\text{calib}} \langle \omega'_p(x, y, \phi) \times M(x, y, \phi) \rangle (1 + B_K + B_Q)}$$



Field maps

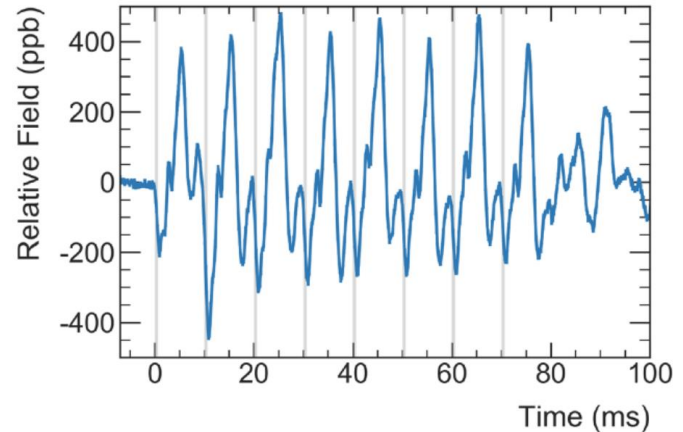
Muon distribution



Field transients

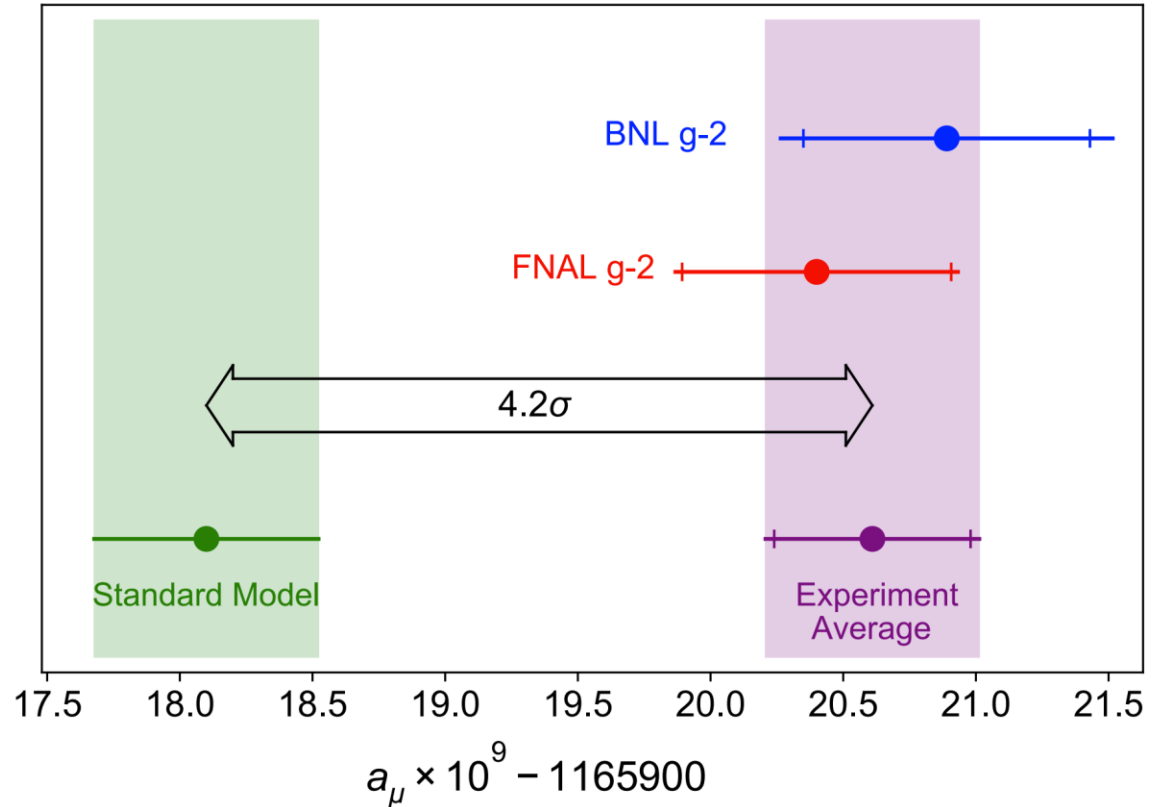
$$\frac{\omega_a}{\tilde{\omega}'_p} \approx \frac{f_{\text{clock}} \omega_a^{\text{meas}} (1 + C_e + C_p + C_{ml} + C_{pa})}{f_{\text{calib}} \langle \omega'_p(x, y, \phi) \times M(x, y, \phi) \rangle (1 + B_K + B_Q)}$$

- Kickers and Quadrupoles both perturb the field:
 - Quads introduce a mechanical vibration when charging/discharging
 - Kickers cause eddy currents
- Quad transient very important in Run 1:



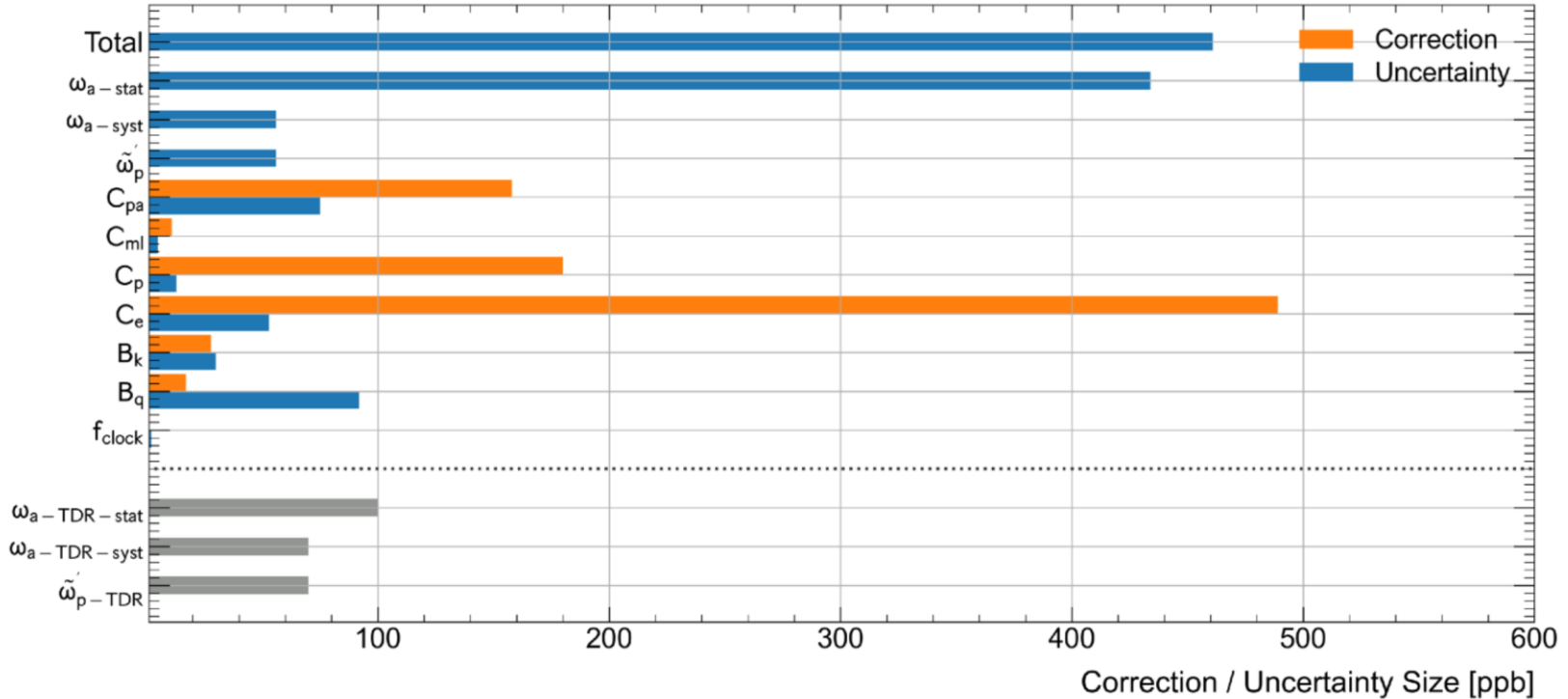
The Run 1 result

- First 6% of our data.
- 1st FNAL result is consistent with BNL measurement!
- Discrepancy between SM (WP2020) and experiment rises to 4.2σ .

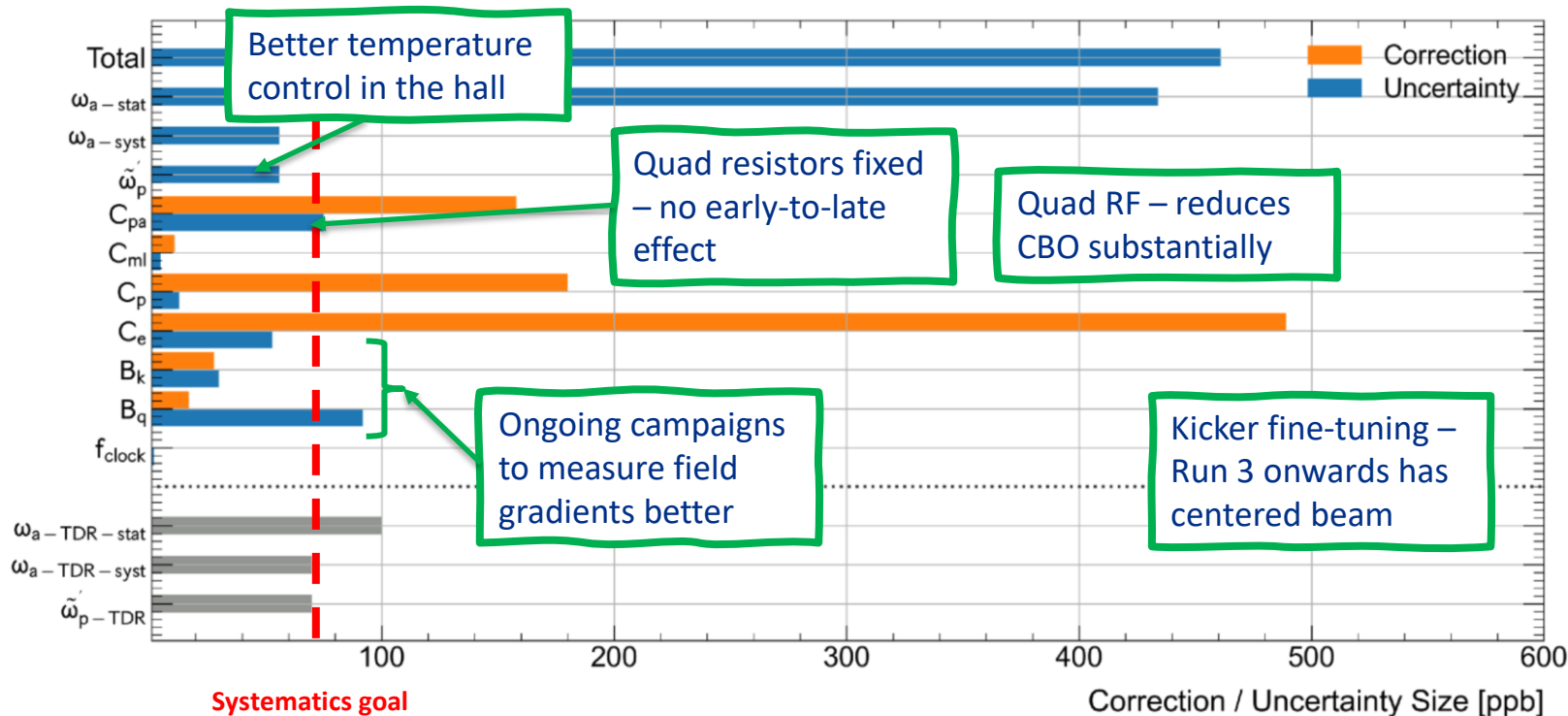


Everything measured to excruciating detail!

- Run 1 is statistically limited, but important to fully understand systematics.



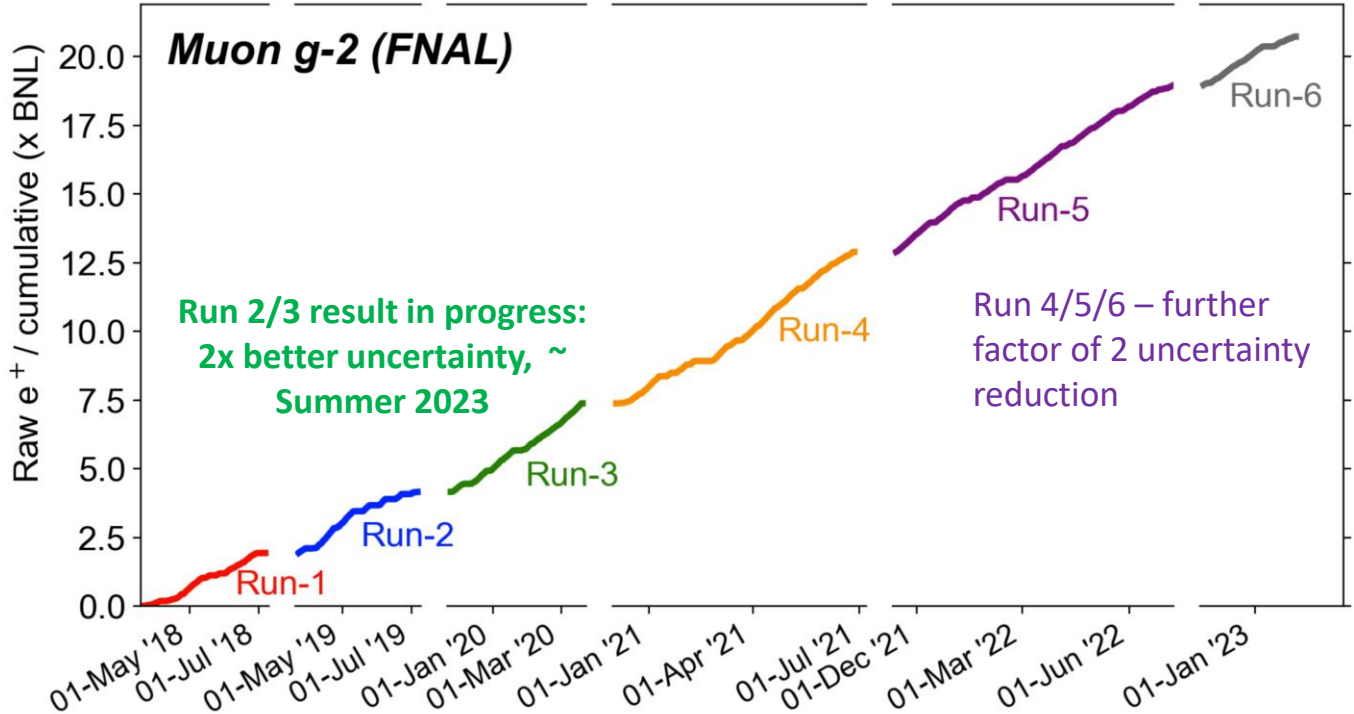
Improvements for Run 2/3 onwards



Looking to the future: Run 2/3 and beyond

Run 6 data collection ongoing:
nearly at 21 x BNL target - μ^+

Last update: 2023-02-11 10:09 ; Total = 20.7 (xBNL)





Thank you!

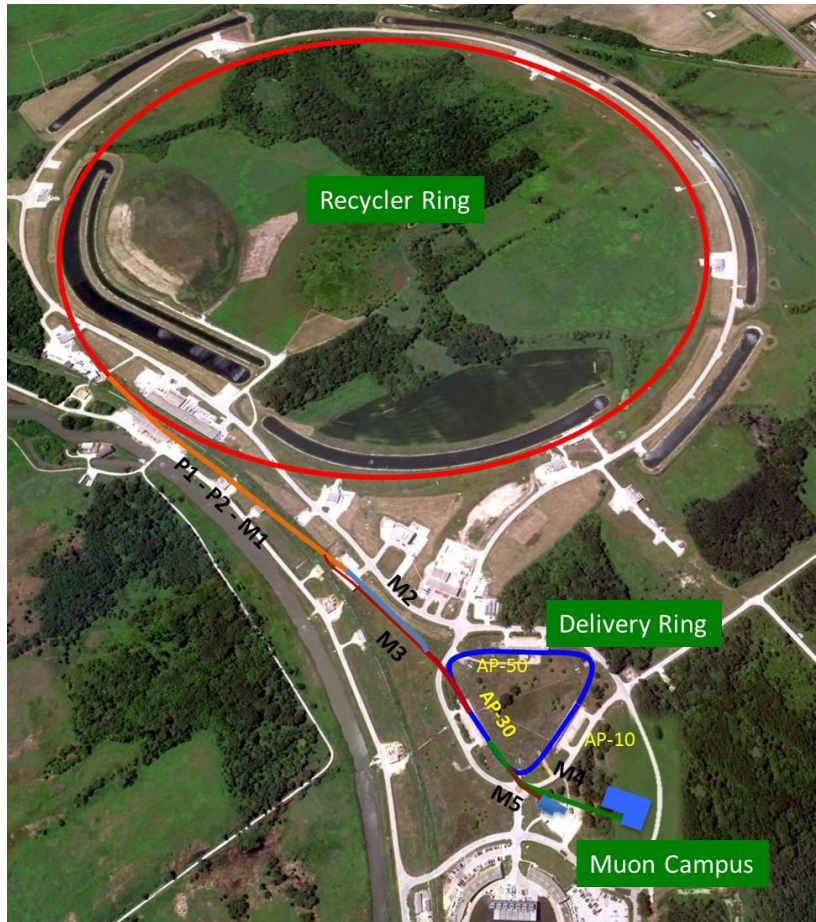
dominika@fnal.gov



Bonus slides

The muon campus beamline

- Protons incident on a target make pions.
- Pions are stored in the delivery ring until they decay into muons.
- Muons injected into our ring.



Where do all the parts come from?

Single trapped electron measurements
(0.28ppt)

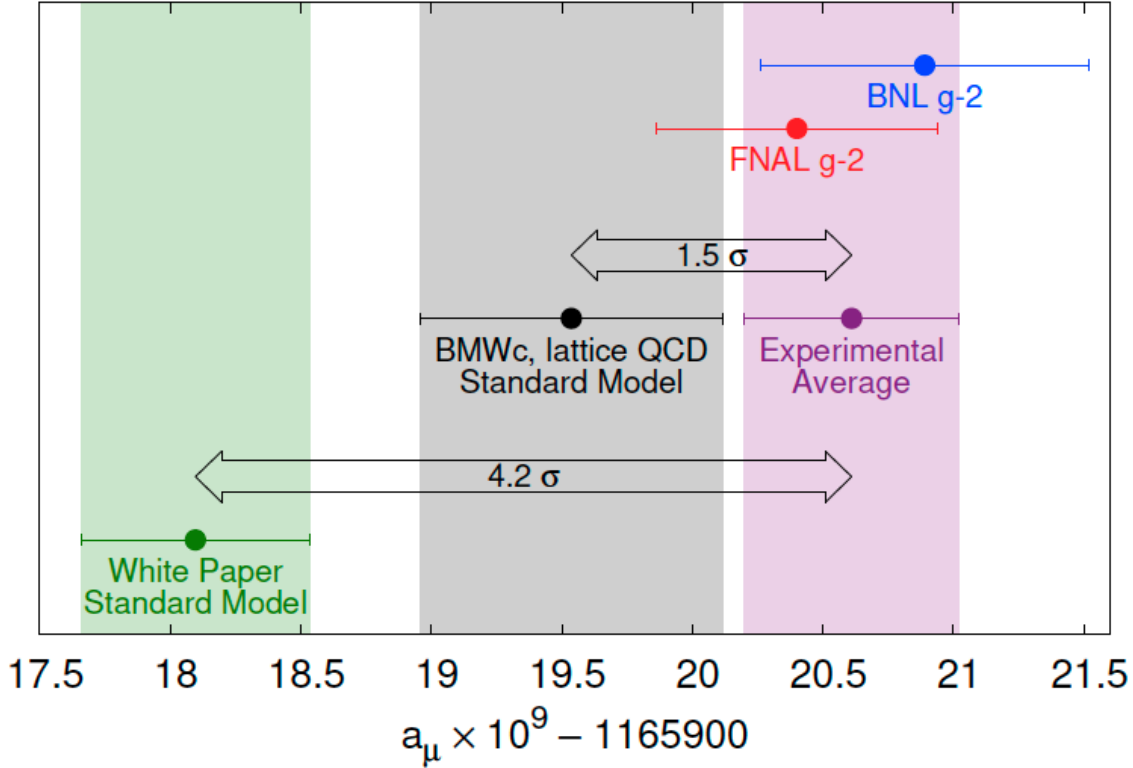
Hydrogen maser measurements (11ppb)

$$a_{\mu} = \frac{\omega_a}{\tilde{\omega}_p} \frac{g_e \mu_p m_{\mu}}{2 \mu_e m_e}$$

QED calculations (exact)

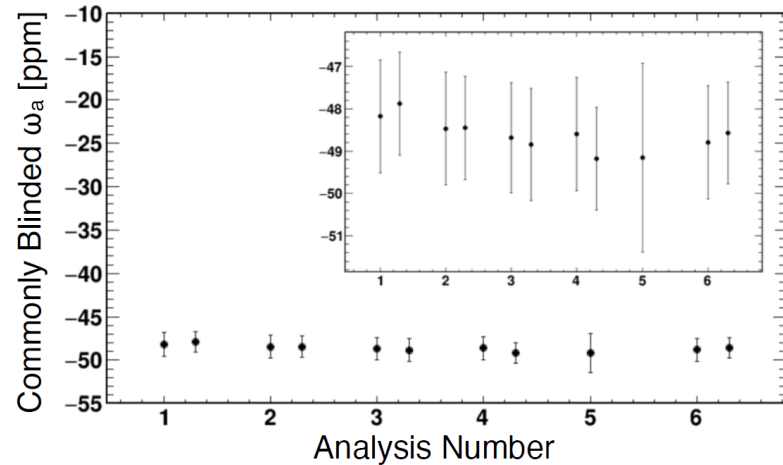
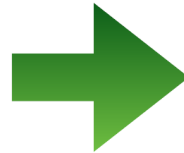
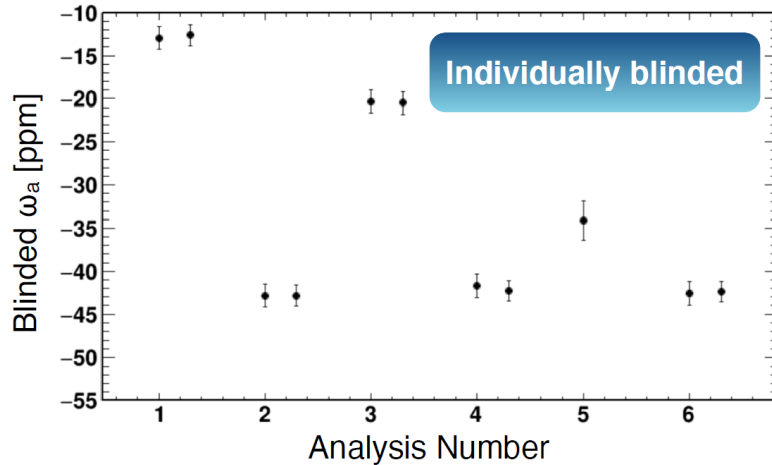
Muonium hyperfine splitting (22ppb)

Run 1 with three-way comparison



Blinding

- Both blinding methods shift the frequency by some unknown factor.
- Software blinding can be undone as a consistency check before hardware is unblinded.
- Run 1 example:



The bad resistors

- 2/32 resistors on quad plates faulty – took a longer time to stabilize
- Therefore, they impact things after the start time cut of 30 μs
- Fixed from run 2 onwards

