

# QCD at the LHC

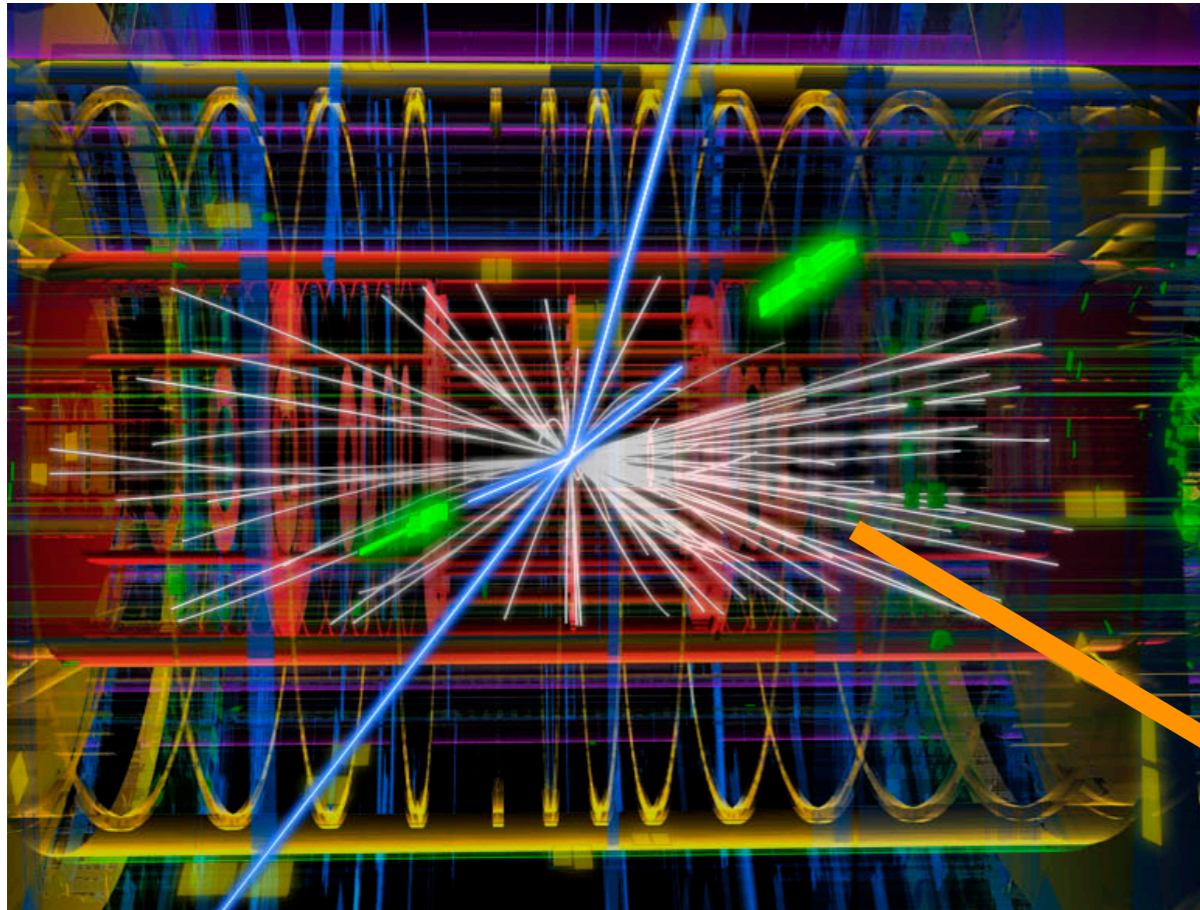
Fabrizio Caola

Rudolf Peierls Centre for Theoretical Physics & Wadham College

Lake Louise Winter Institute, February 25, 2022



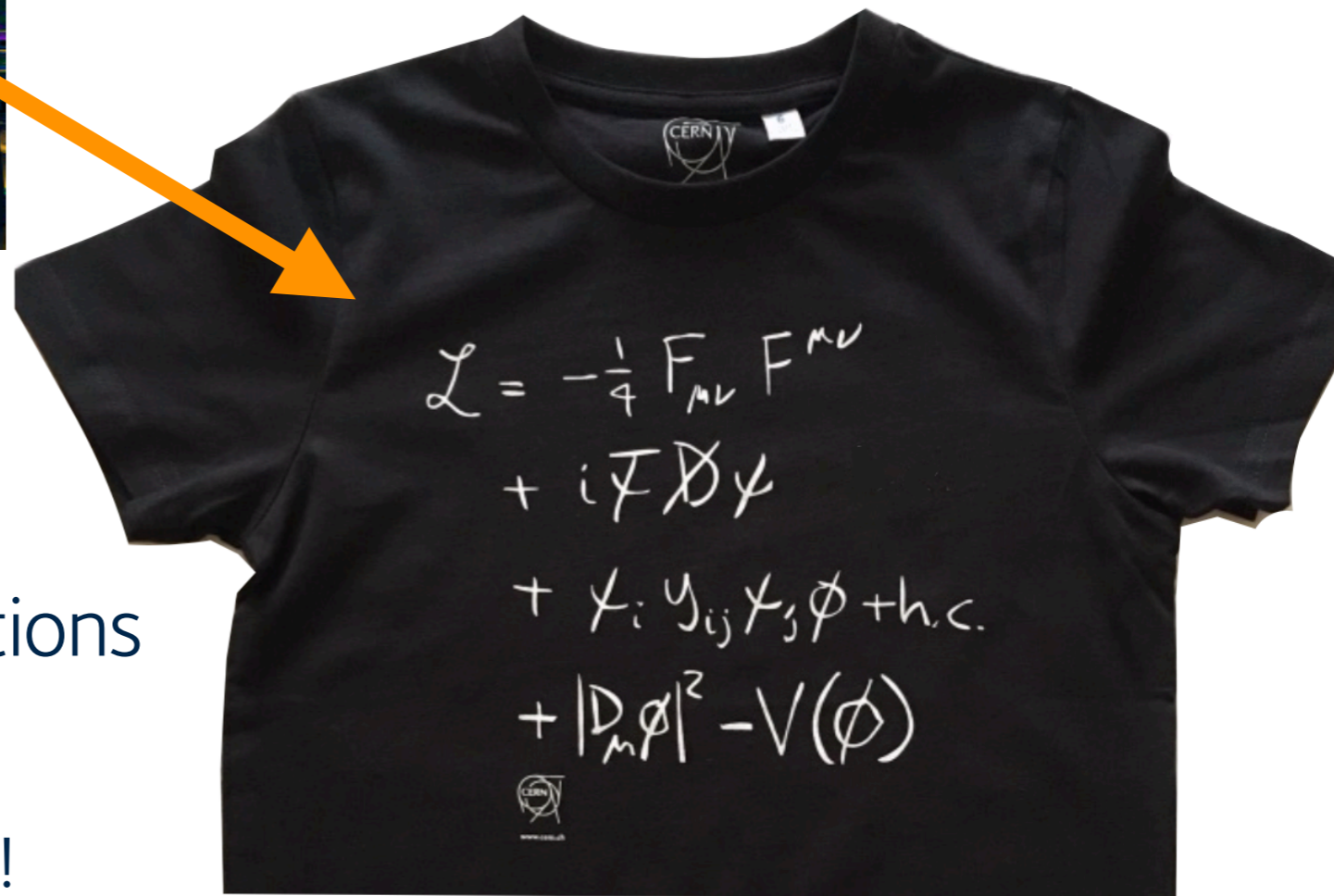
# QCD at the LHC: the big goal



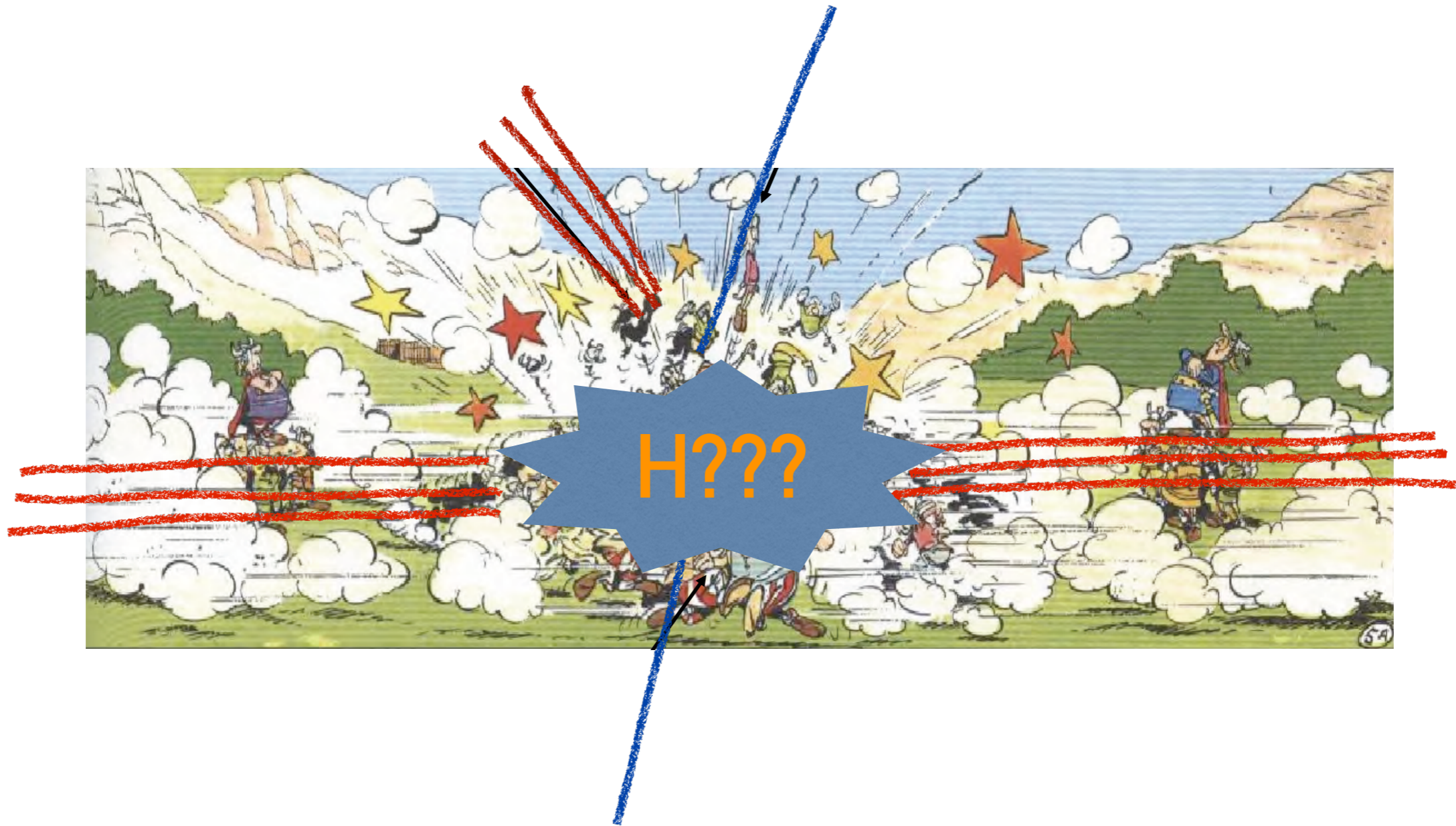
Extract information from a highly-complex environment, from first principles...

... and use it to constraint fundamental particles and interactions

Bonus: QCD is a very interesting theory!

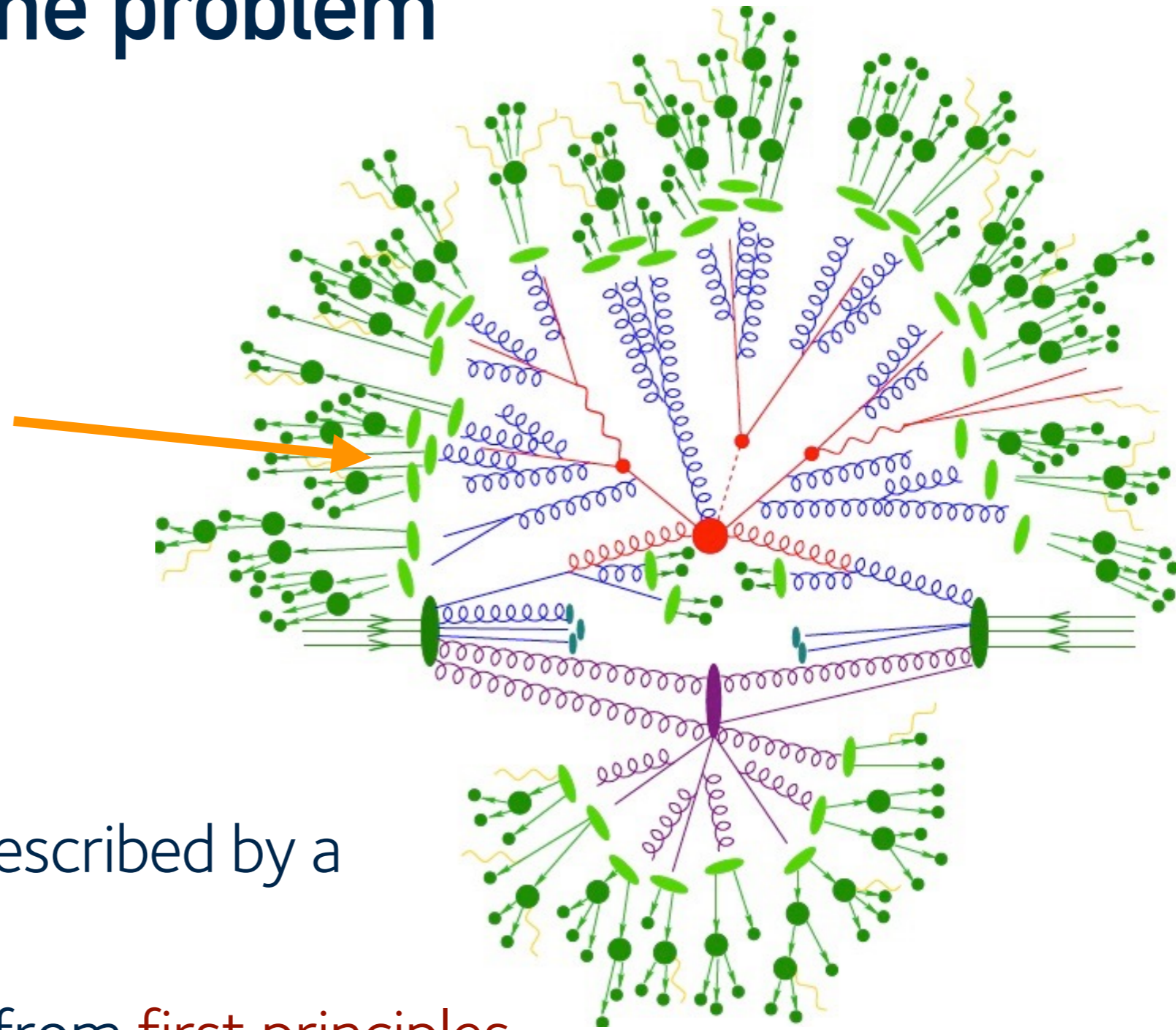
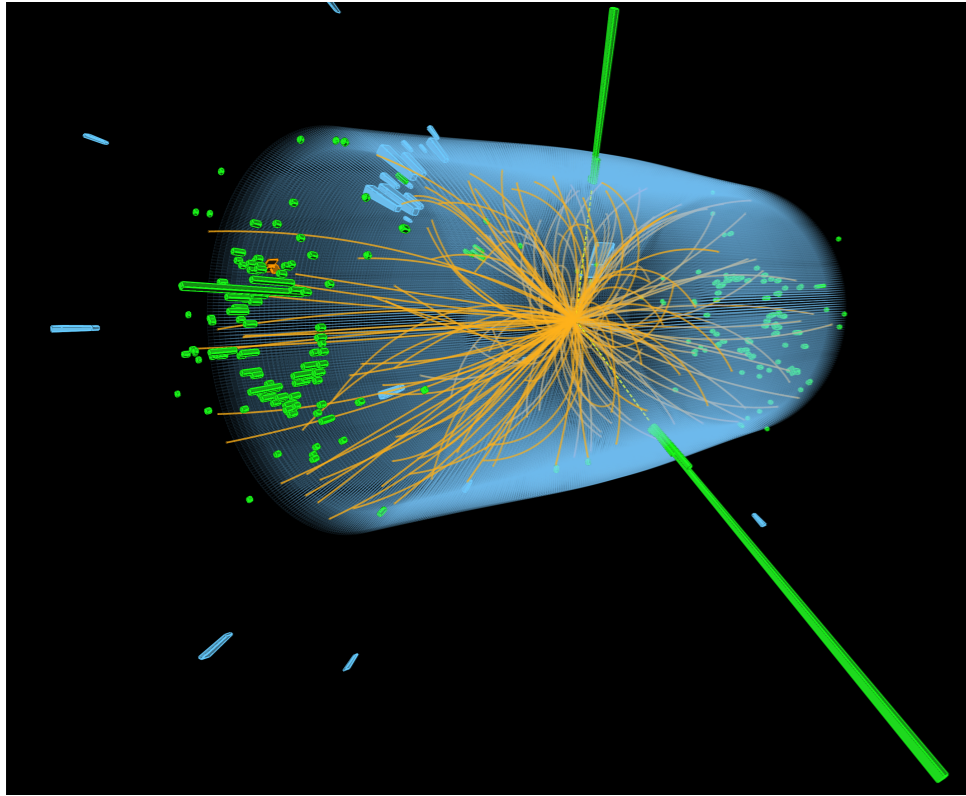


# QCD at the LHC: the big goal



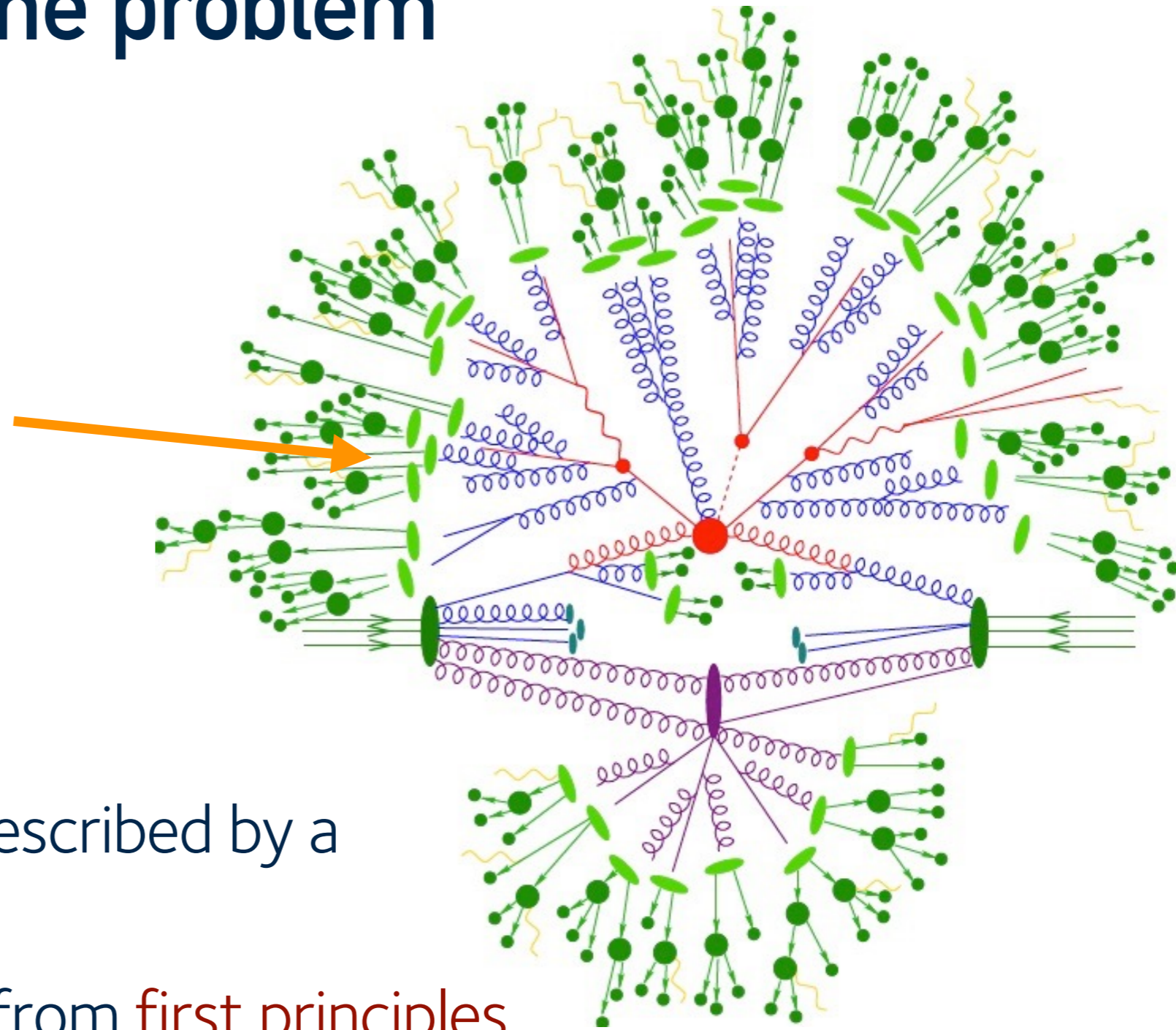
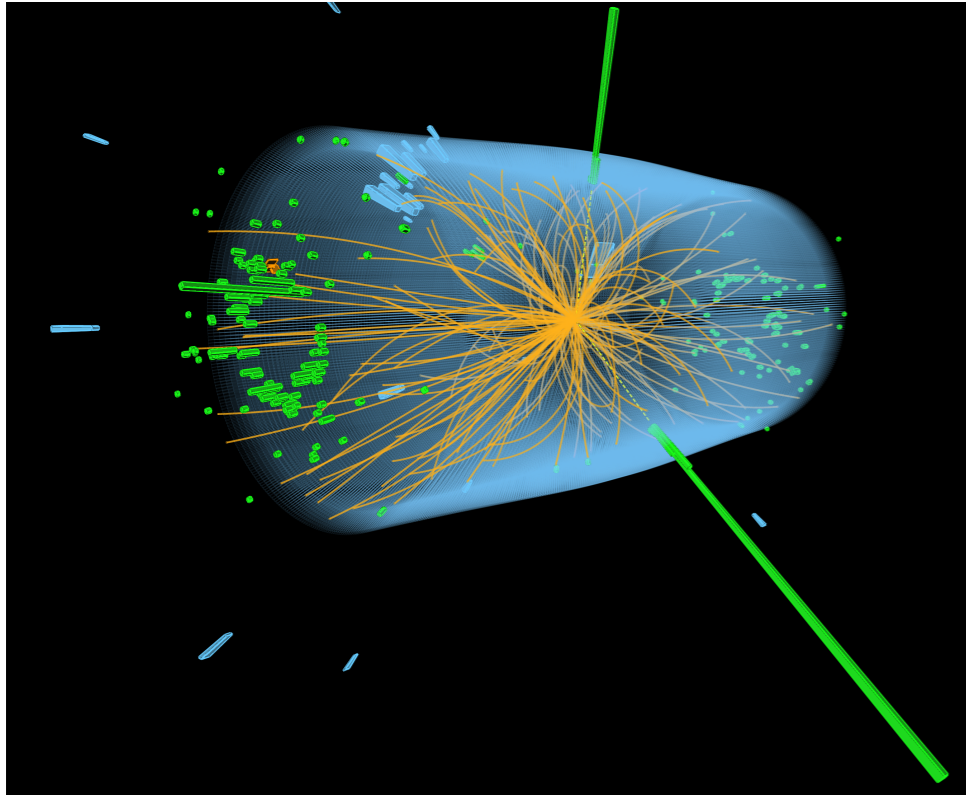
“It’s like try to learn how a Swiss watch works by taking a bunch of them, smashing against each other and see what comes out”

# The problem



- A **complex environment**, described by a strongly coupled theory
- We want to understand it from **first principles**

# The problem



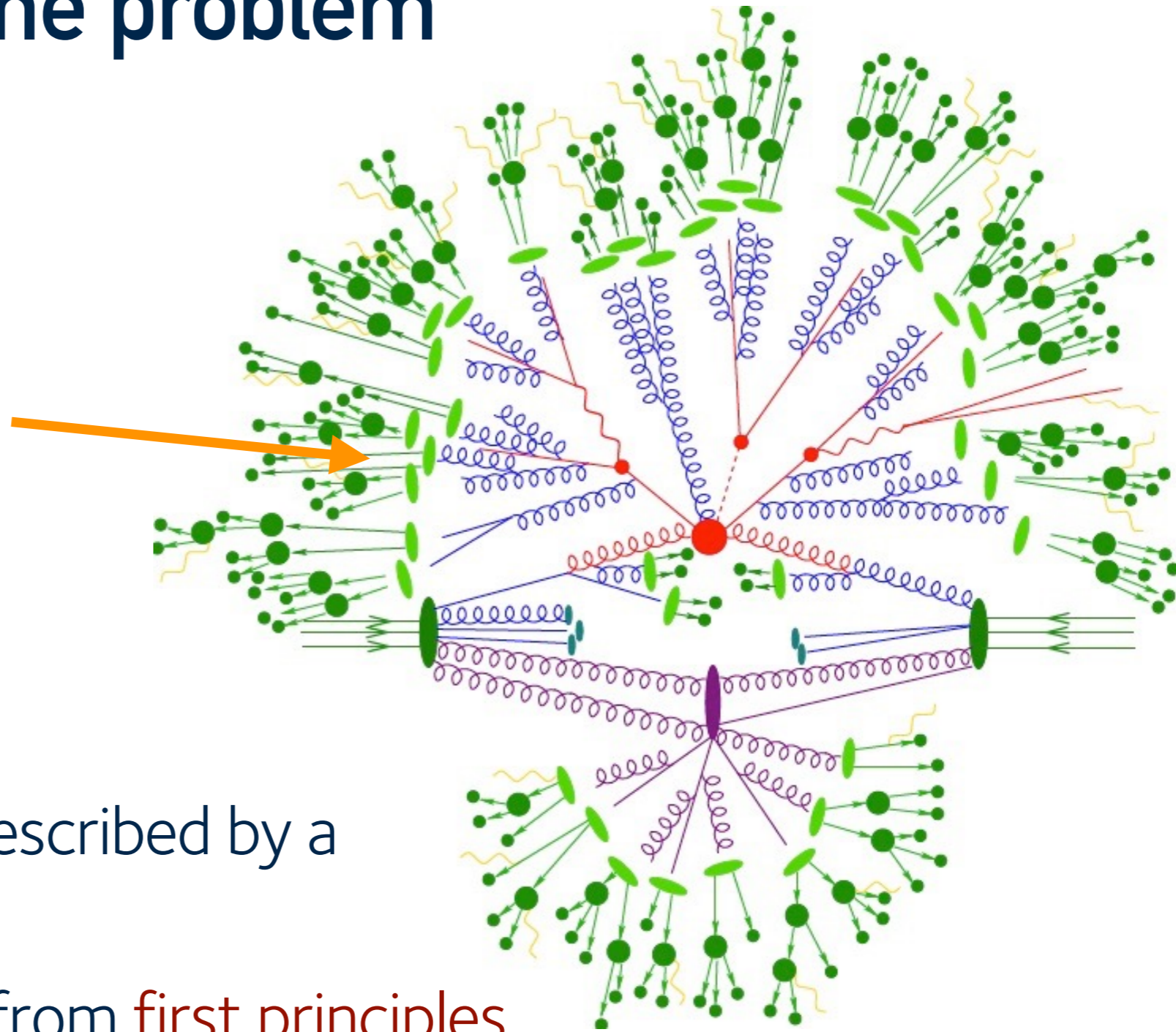
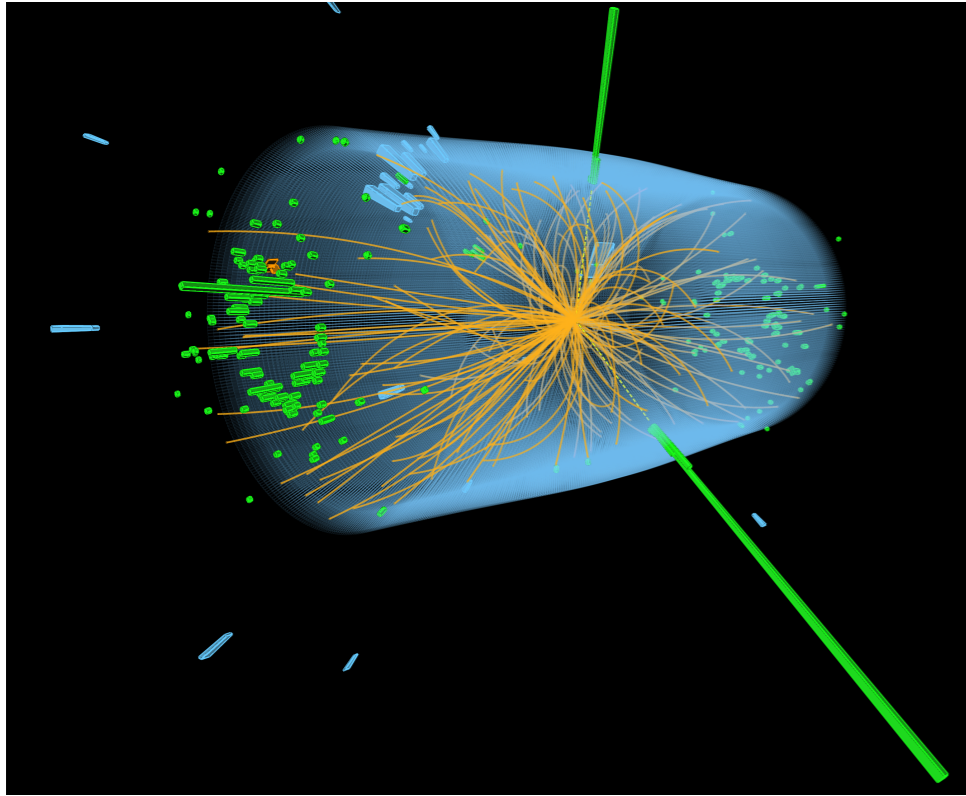
- A **complex environment**, described by a strongly coupled theory
- We want to understand it from **first principles**

## Lattice?

- Resolve the full event  $\rightarrow 2 \text{ TeV} \sim 10^{-4} \text{ fm}$
- Hadronic scale  $\sim 1 \text{ fm}$ , boost factor  $\sim 100 \rightarrow 10^4 \text{ fm}$

$10^{32}$  nodes

# The problem



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- We want to understand it from **first principles**

Lattice?

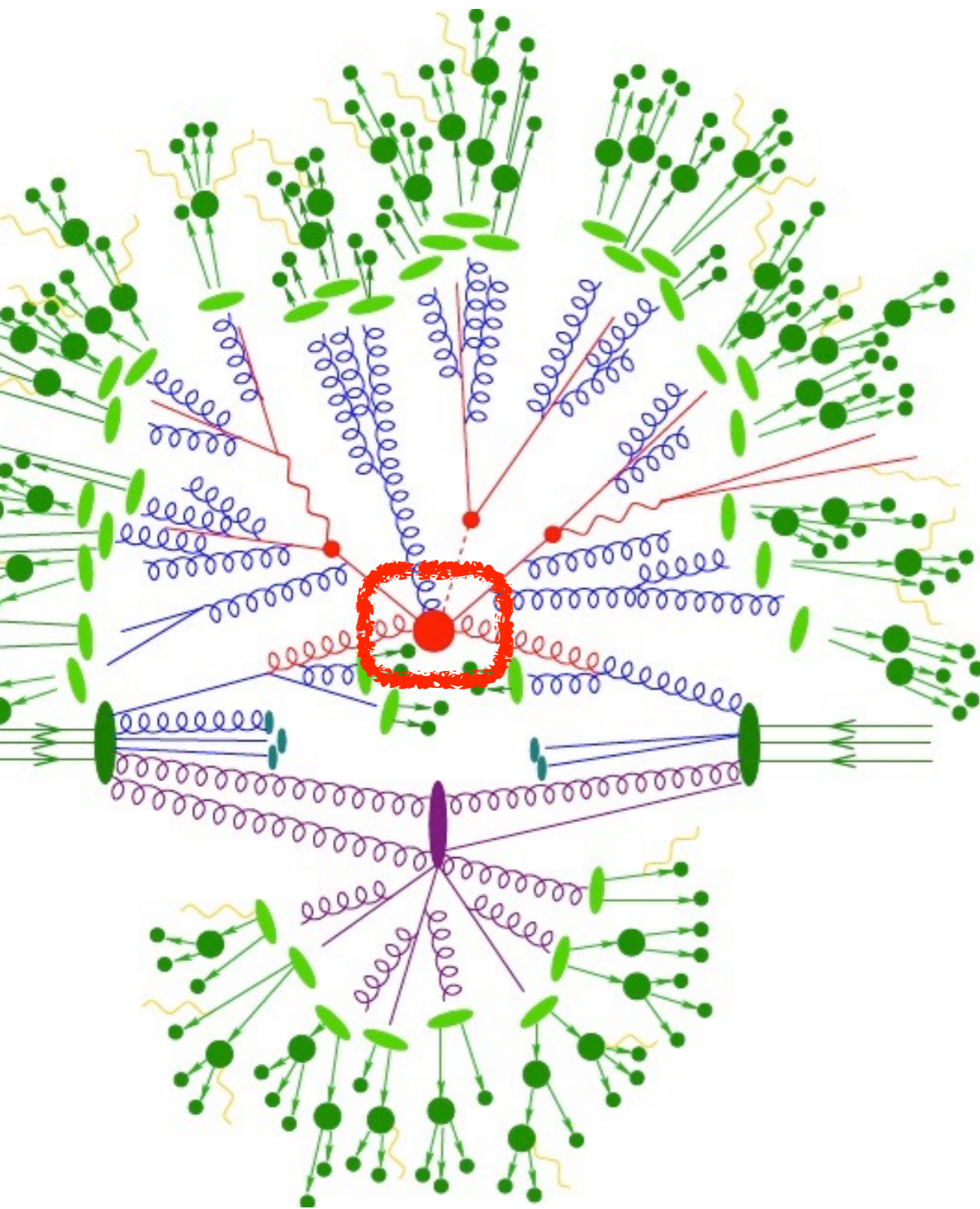
- Resolve the full
- Hadronic

Quantum computing?

$10^{52}$  nodes

cost factor  $\sim 100 \rightarrow 10^4$  fm

# The solution: factorisation



The “interesting”  
short distance physics

$Q \approx 100 \text{ GeV}$

The experimental world:  
hadrons/jets in the detector

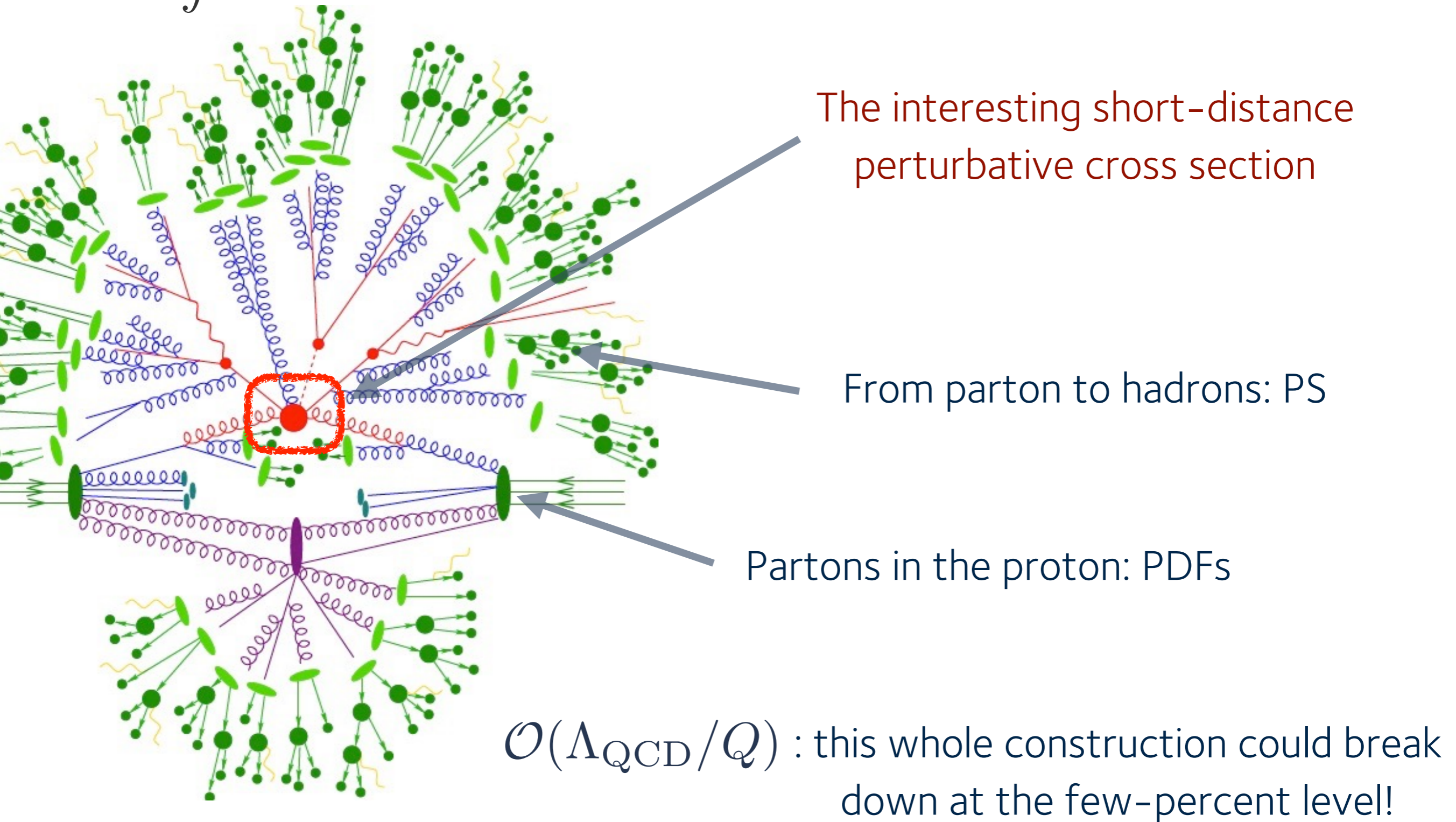
$Q \sim 1 \text{ GeV}$

Partons from proton

Different physics at very different scales, can be TREATED SEPARATELY

# The solution: factorisation

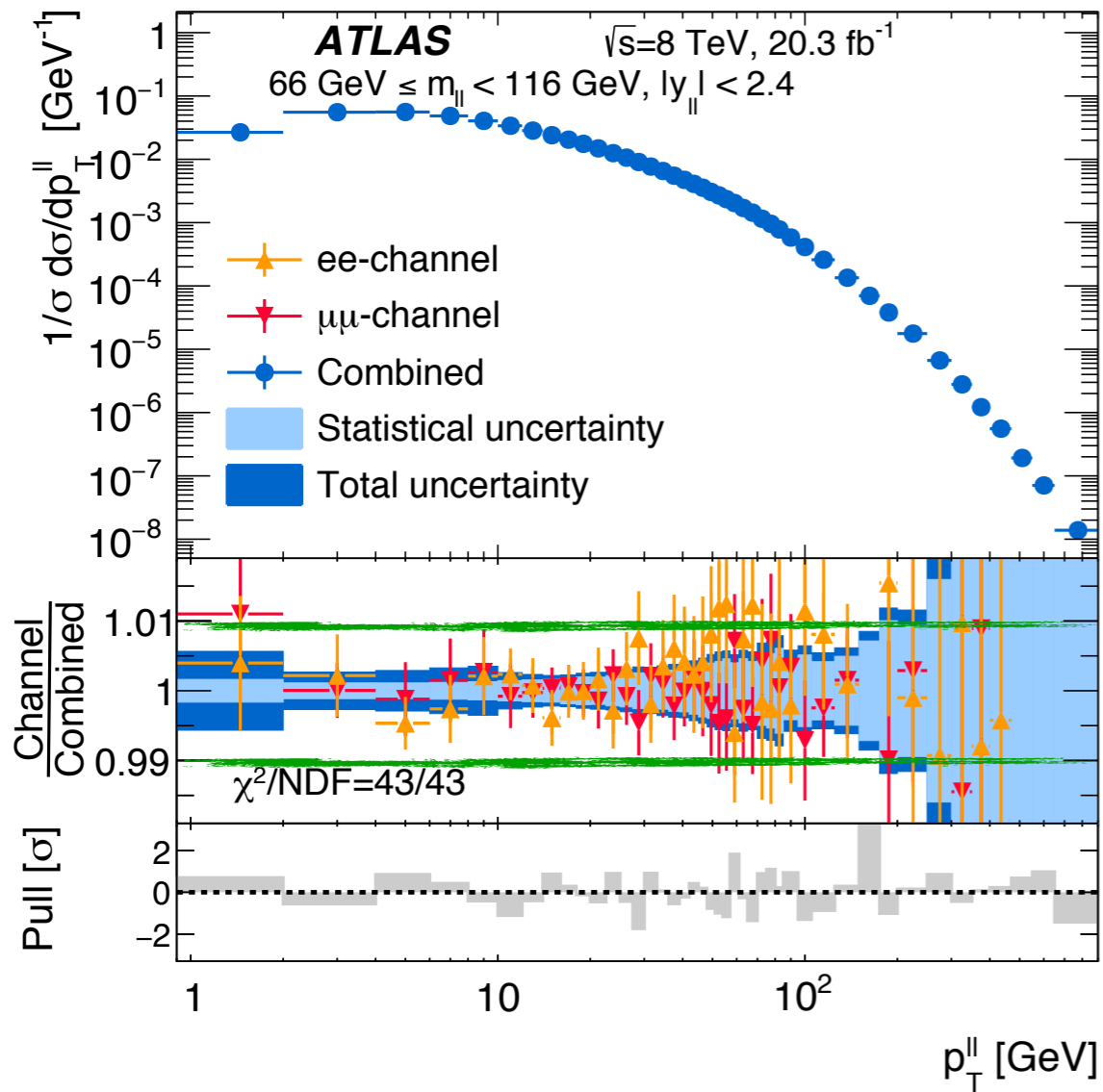
$$d\sigma = \int dx_1 dx_2 f(x_1) f(x_2) d\sigma_{\text{part}}(x_1, x_2) F_J (1 + \mathcal{O}(\Lambda_{\text{QCD}}/Q))$$



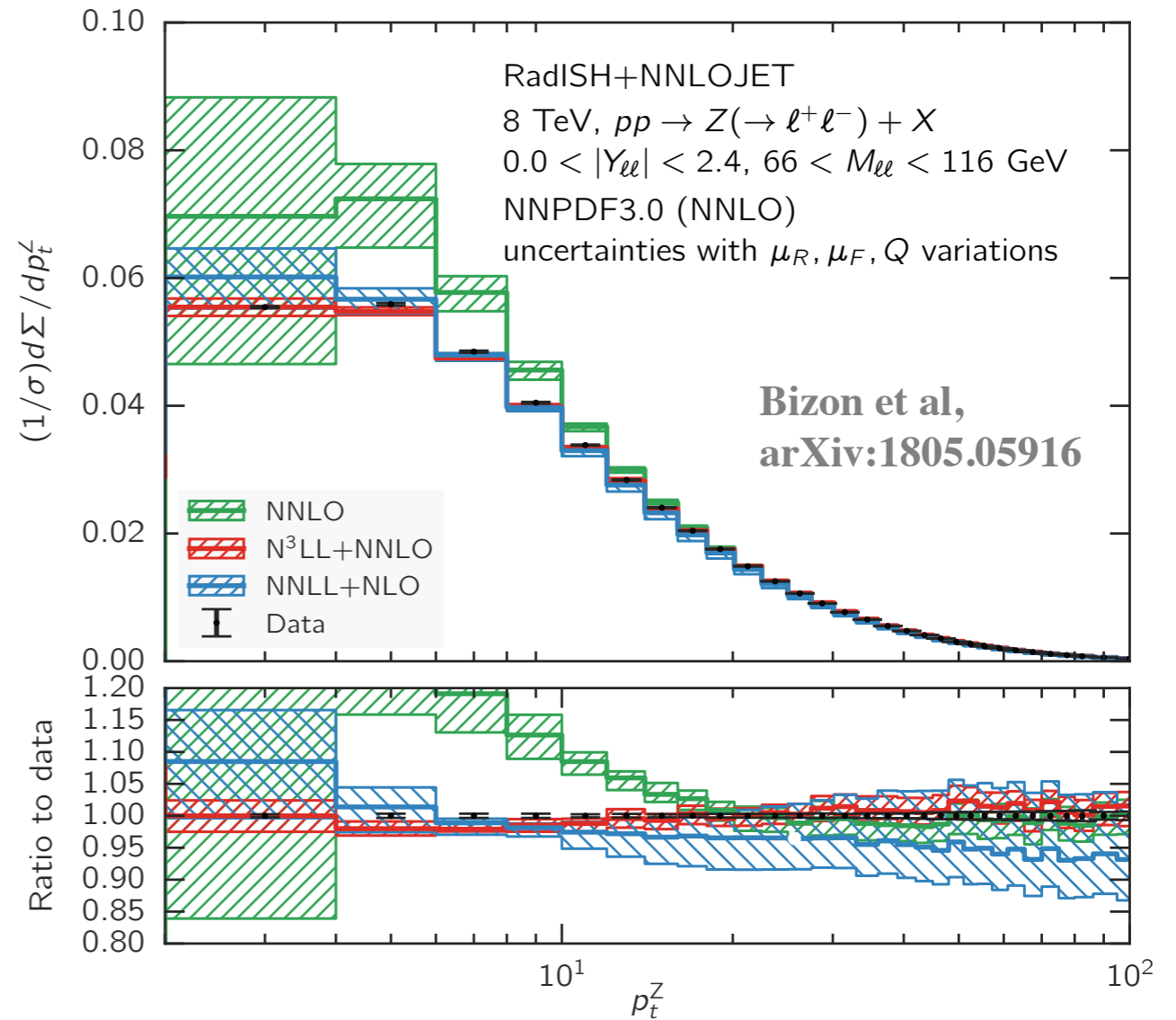


# Precision goals

## Drell-Yan



Data: per-mill



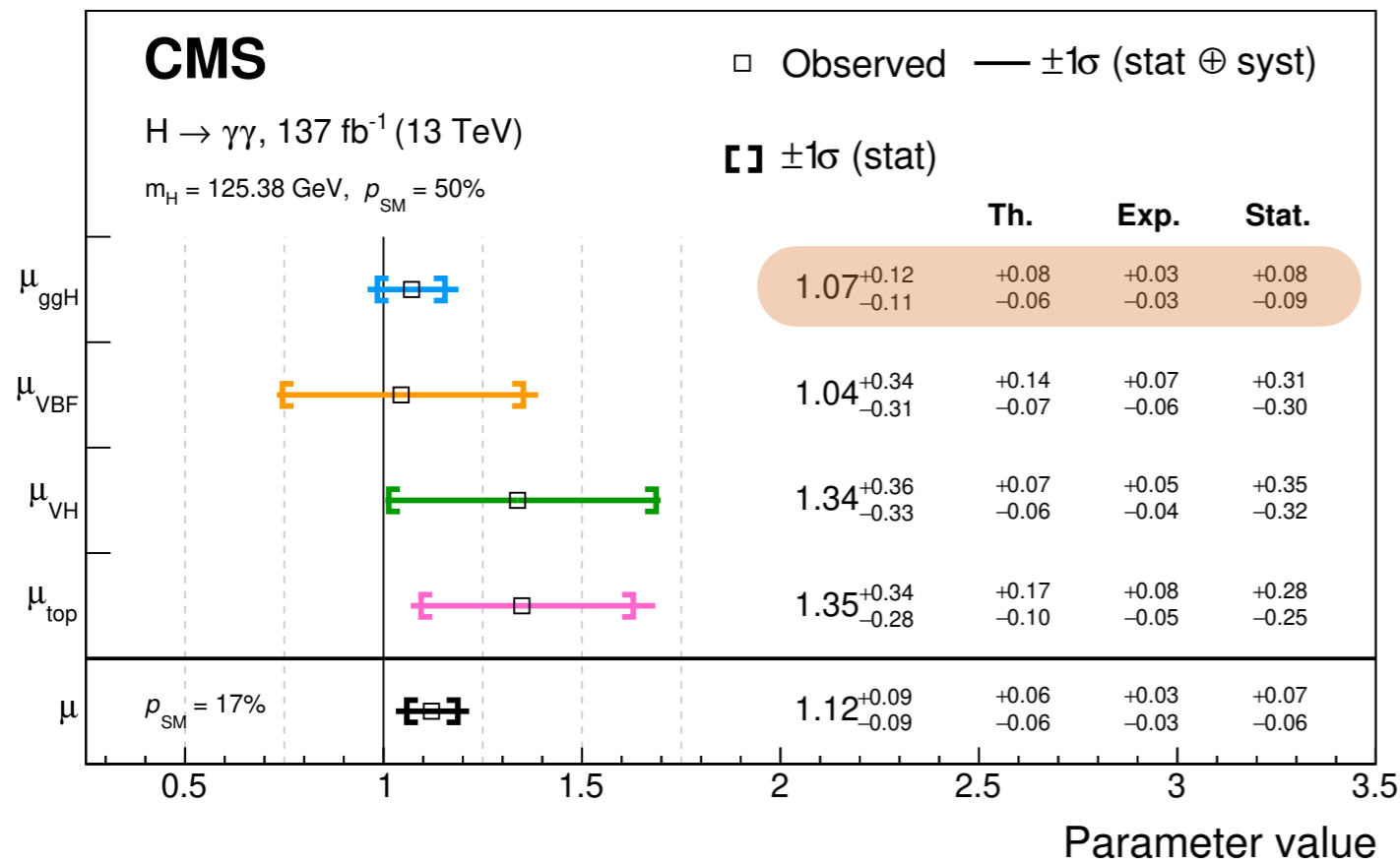
Theory: few percent

# Precision goals

## Higgs

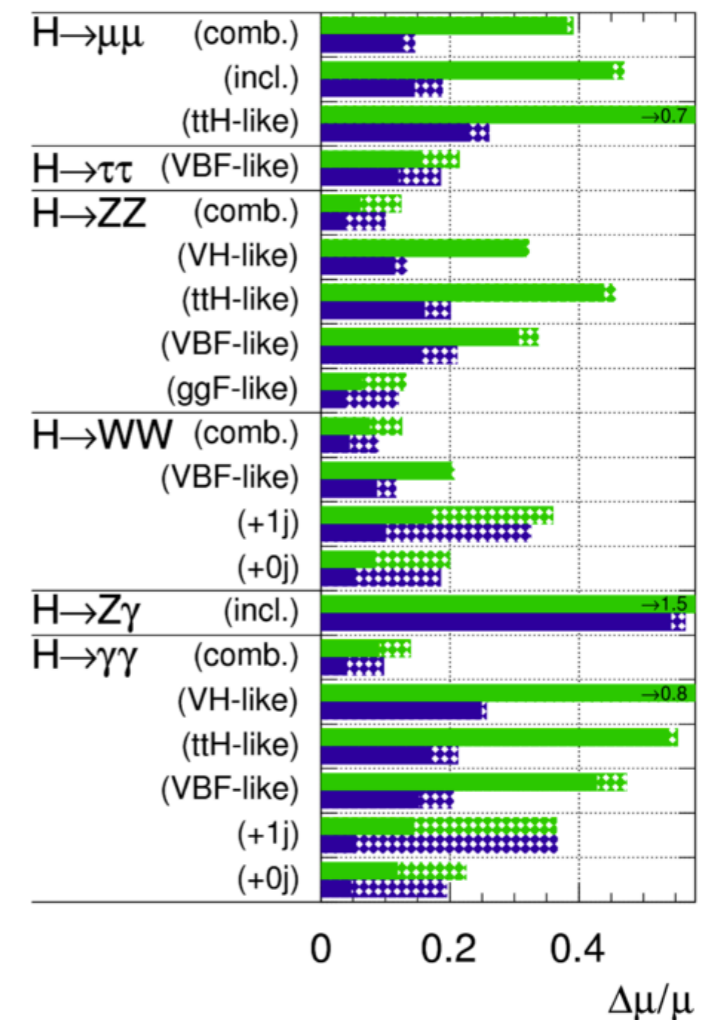
ggF Higgs, now

Higgs couplings, HL-LHC



**ATLAS Simulation Preliminary**

$\sqrt{s} = 14 \text{ TeV}$ :  $\int L dt = 300 \text{ fb}^{-1}$  ;  $\int L dt = 3000 \text{ fb}^{-1}$



In many interesting cases, physics at the few-percent possible

# What does precision buy you

$\Lambda_{\text{NP}}$

direct  
searches

SM  $\sim$  v.e.v.

Imagine to have new physics at a  
(heavish) scale  $\Lambda_{\text{NP}}$

Typical modification to observable w.r.t.  
standard model prediction:

$$\delta O \sim Q^2 / \Lambda_{\text{NP}}^2$$

Search strategies:

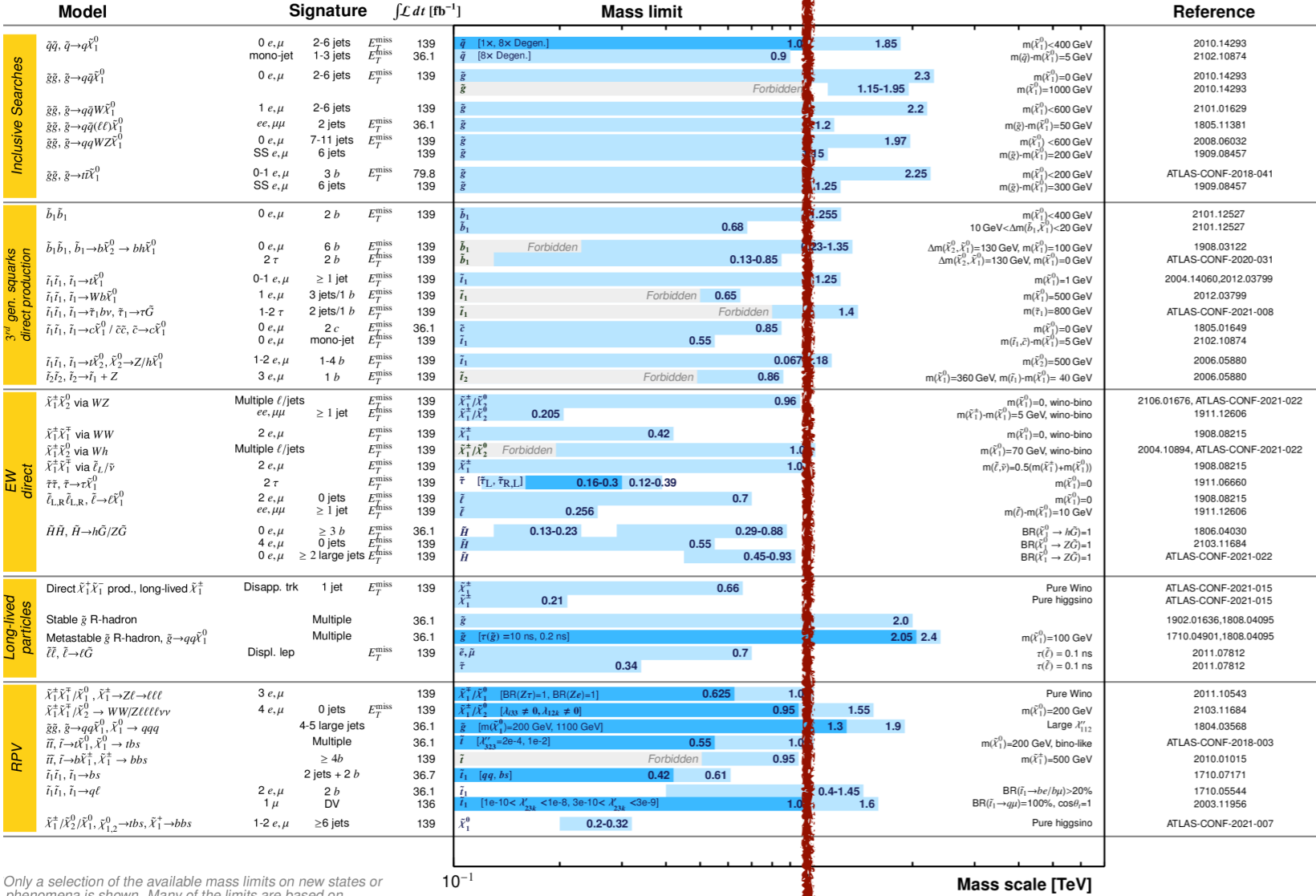
- Direct searches: energy-limited
- Indirect searches: precision-limited,  
long-run game

# What does precision buy you

## 1 TeV

ATLAS SUSY Searches\* - 95% CL Lower Limits  
June 2021

ATLAS Preliminary  
 $\sqrt{s} = 13$  TeV



Direct searches:  
probing the TeV  
scale, already now

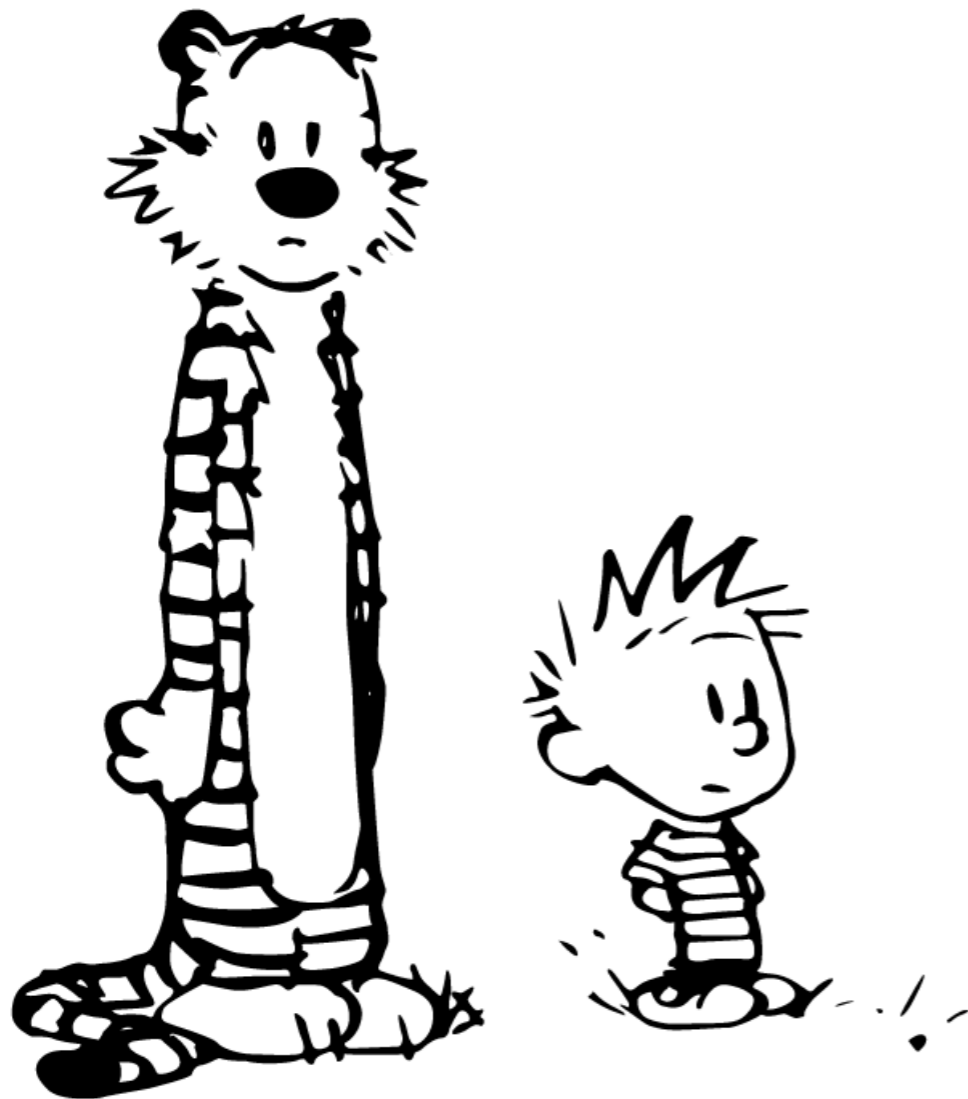
To be competitive:  
 $\delta = Q^2/\Lambda^2, \Lambda \gtrsim 1 \text{ TeV}$

- $\delta$ :  $\sim$  few percent in the bulk ( $\sim 100 \text{ GeV}$ )
- $\delta$ :  $\sim 10\%, 20\%$  in the tails ( $\sim 500 \text{ GeV}$ )

Only a selection of the available mass limits on new states or phenomena is shown. Many of the limits are based on

# Precision QCD: an oxymoron?

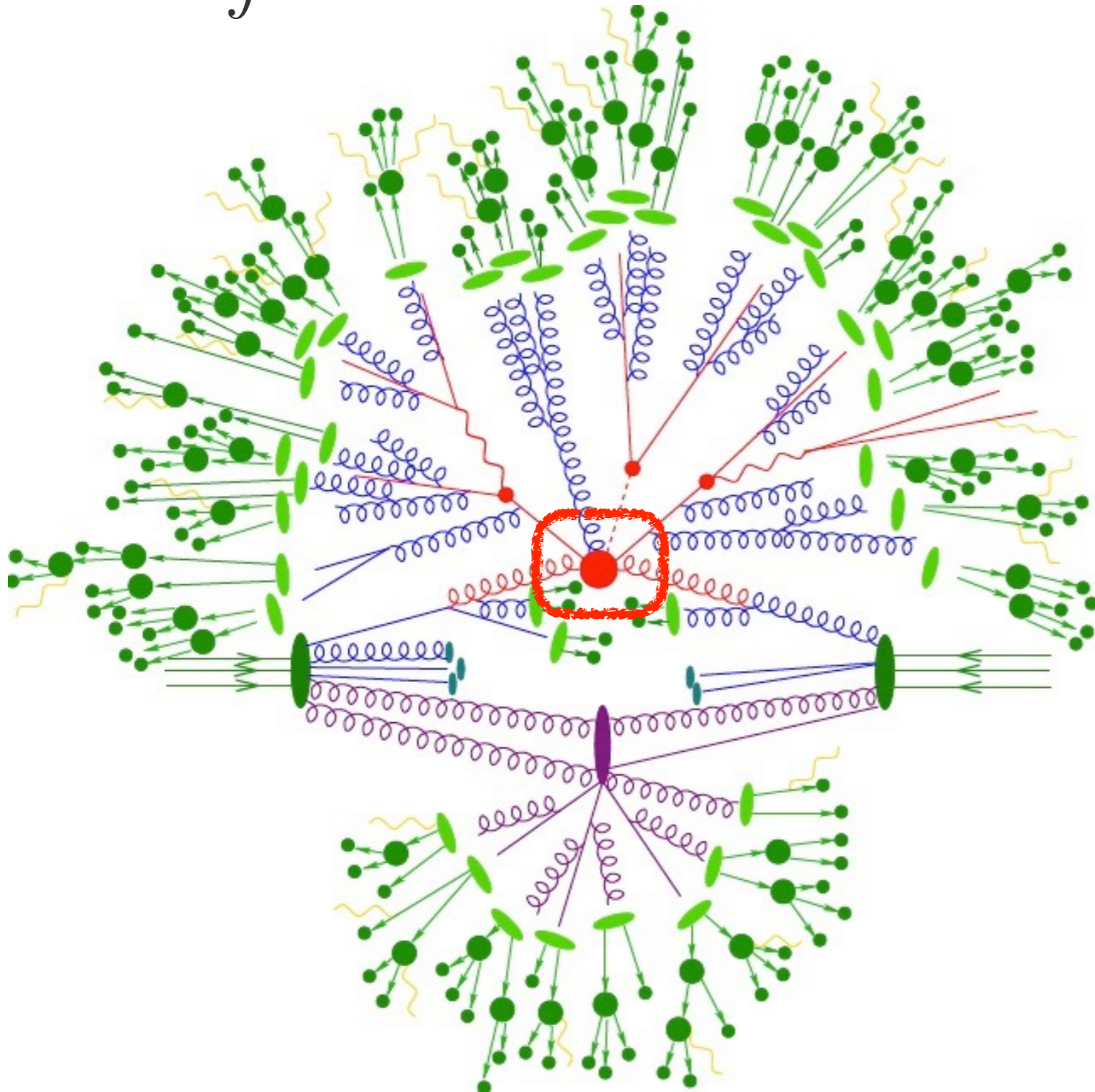
A motivational speech from an old distinguished professor, who pioneered the development of quantum field theory and the Standard Model



- And what about you young man, what are you working on?
- Perturbative QCD
- My dear boy, you should change topic: QCD was established decades ago!
- But we don't want to establish it, we want to use it to extract precision information from the LHC
- Hadron colliders are messy, you cannot do precision physics there

# Physics at the few percent

$$d\sigma = \int dx_1 dx_2 f(x_1) f(x_2) d\sigma_{\text{part}}(x_1, x_2) F_J (1 + \mathcal{O}(\Lambda_{\text{QCD}}/Q))$$



Need control over

Input parameters (PDFs,  $\alpha_s$ )

Hard process  $\rightarrow$  th predictions

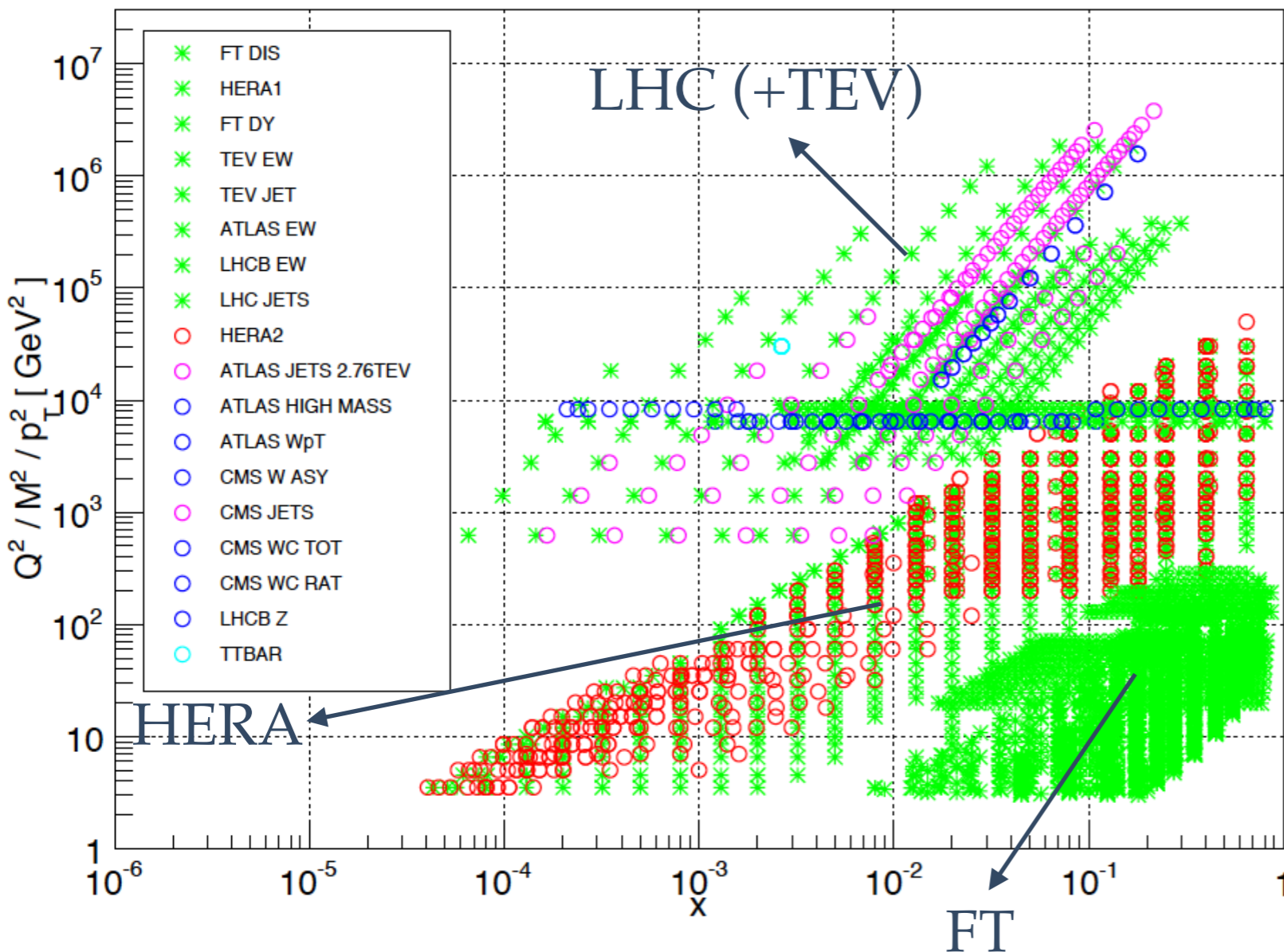
Framework

Non-trivial...

# Input parameters: PDFs in the LHC era

- Parton content of the proton  
non pert → fitted to data
- Data at different scales related by first-principle computable AP evolution → universality

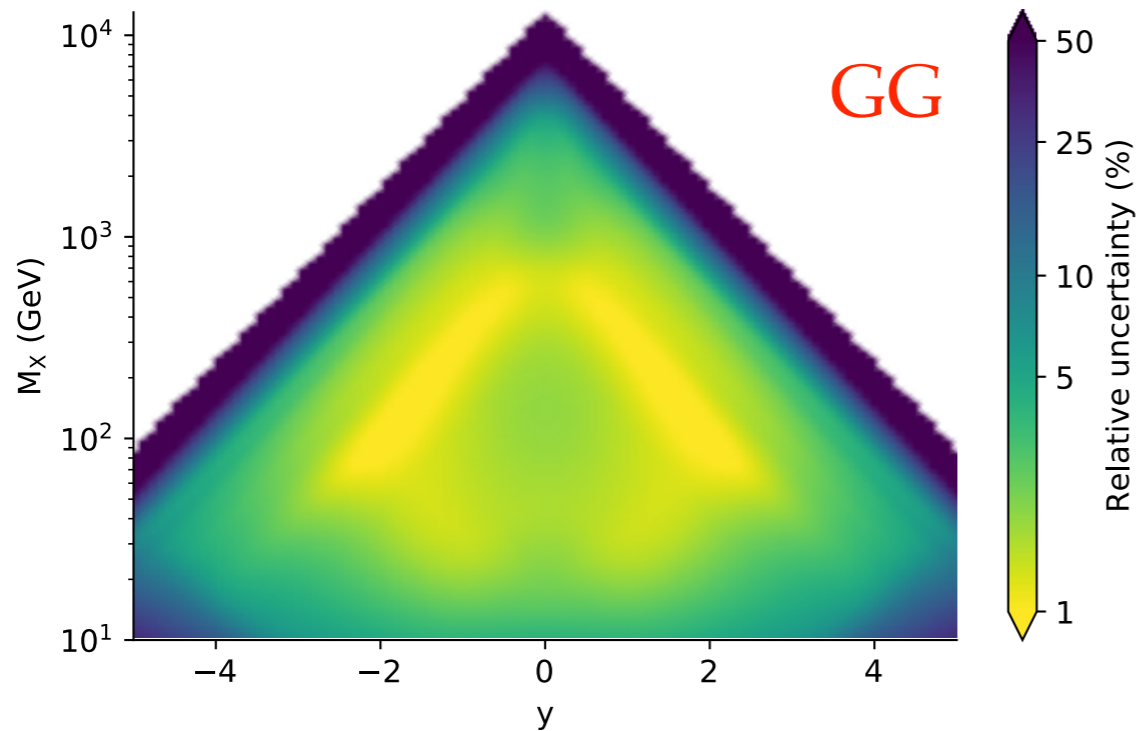
$$\frac{\partial f(x, Q^2)}{\partial \log Q^2} = \alpha_s \int_x^1 \frac{dy}{y} P\left(\frac{x}{y}\right) f(y, Q^2) + \mathcal{O}(\alpha_s^2)$$



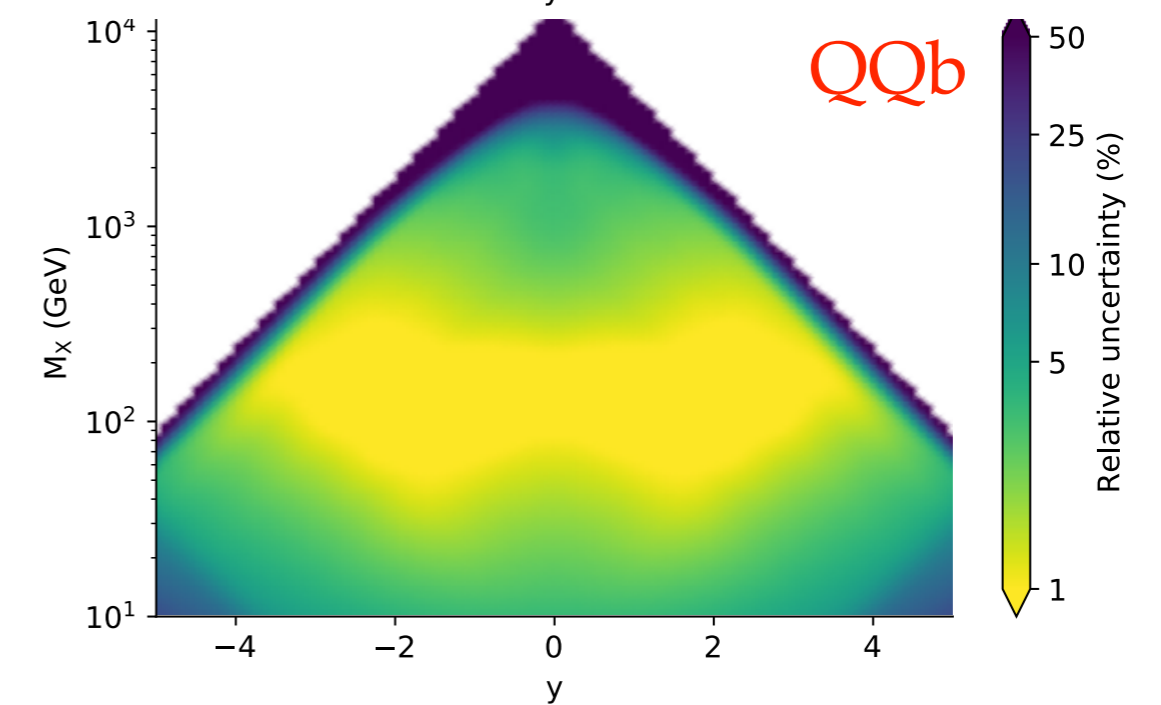
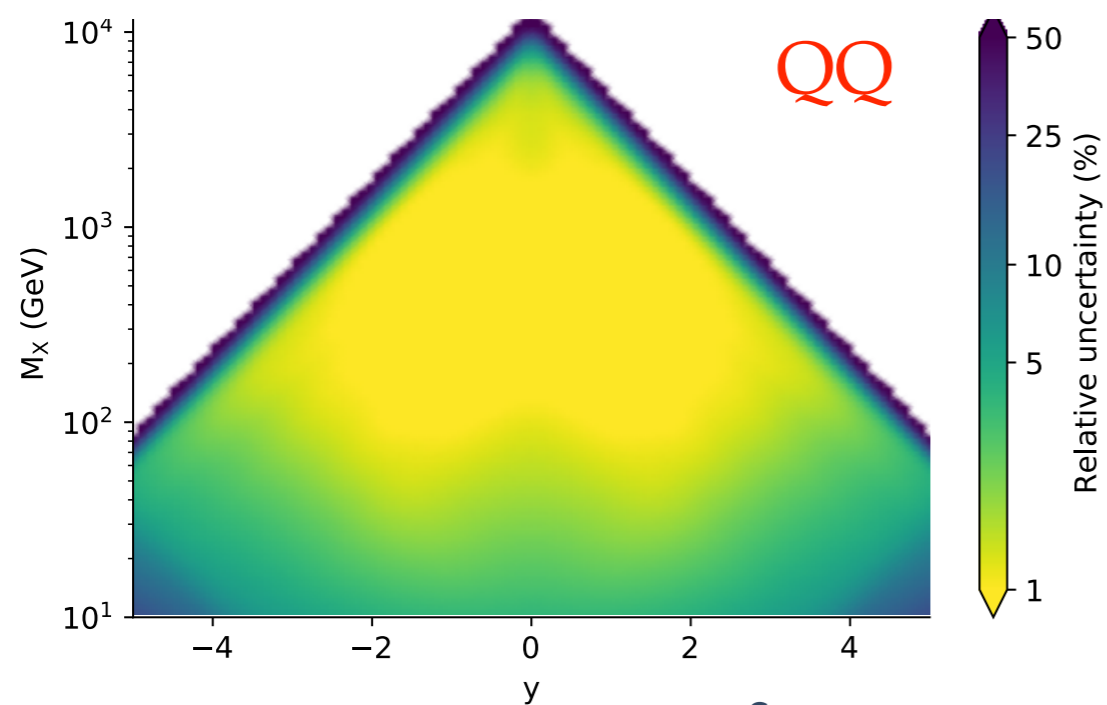
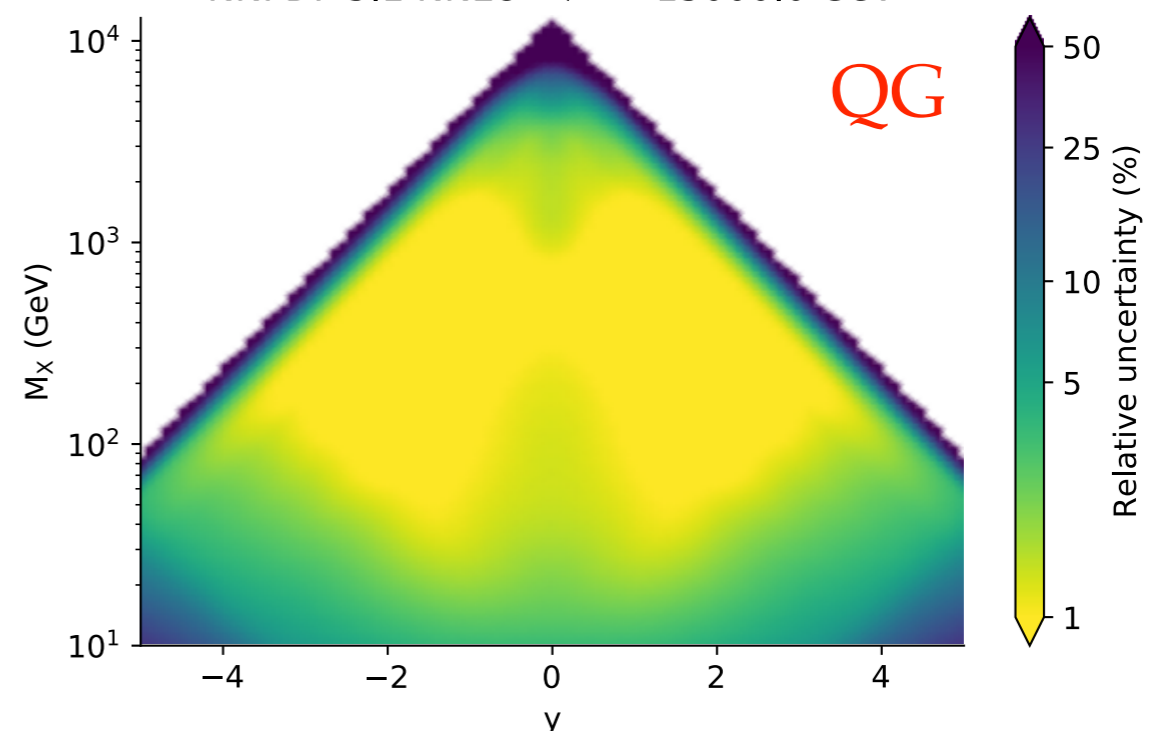
- Results consistent over many orders of magnitude → great test of pQCD
- A lot of precise data from the LHC are already now having great impact (tt, jj, Z/W...)
- We may soon discard 'old' low-Q data with limited theoretical control (nuclear corrections...)
- SOLID, ROBUST AND 'CLEAN' DETERMINATIONS

# PDFs: the overall precision

Relative uncertainty for gg-luminosity  
NNPDF 3.1 NNLO -  $\sqrt{s} = 13000.0$  GeV



Relative uncertainty for qq-luminosity  
NNPDF 3.1 NNLO -  $\sqrt{s} = 13000.0$  GeV



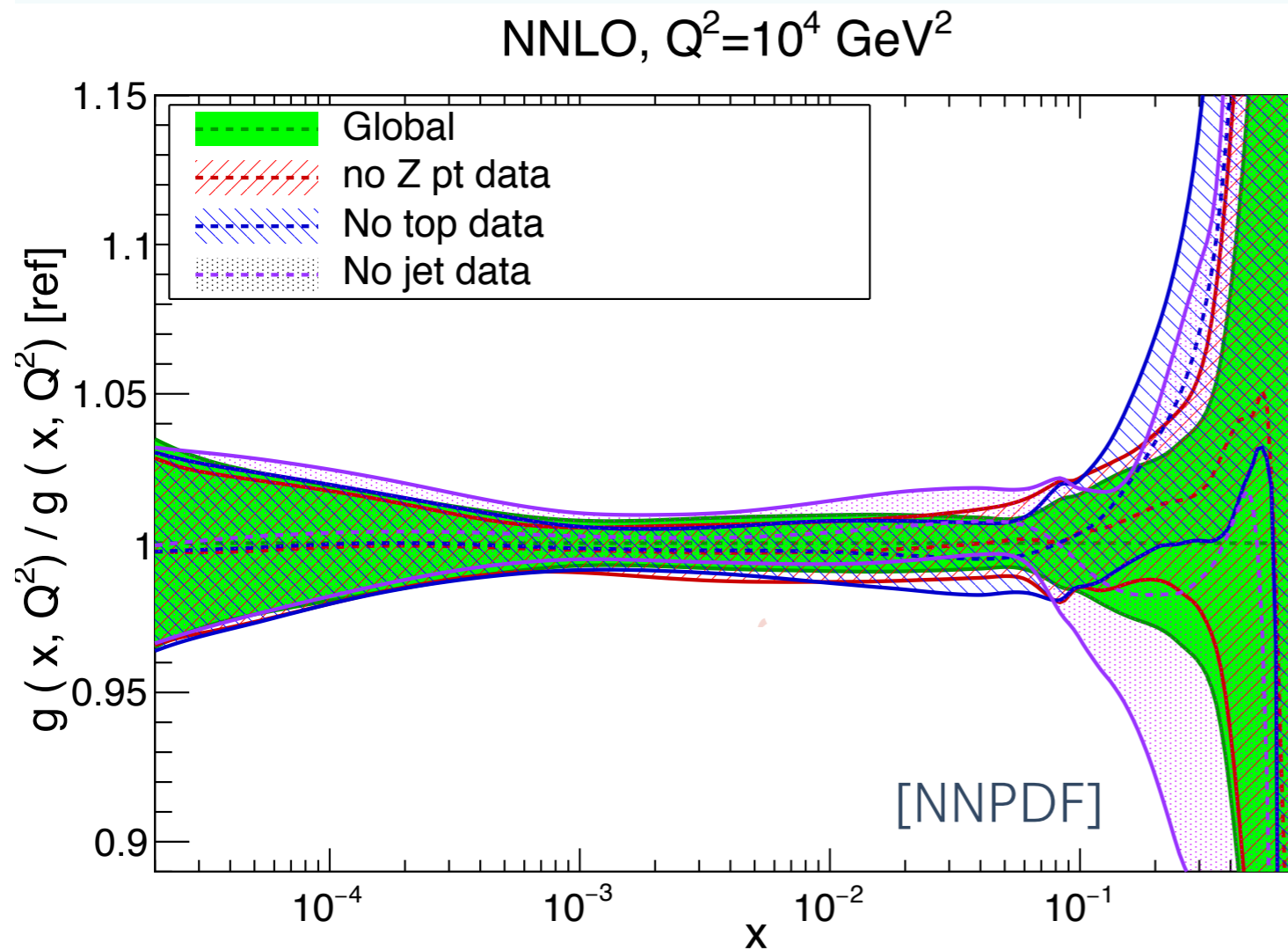
[NNPDF31]

- Big improvement w.r.t. few years ago
- FOR CENTRAL EW PRODUCTION: PERCENT PRECISION
- Although be careful to take these uncertainties at face value



# PDFs: sanity check

How do we make sure we are not fitting new physics away?

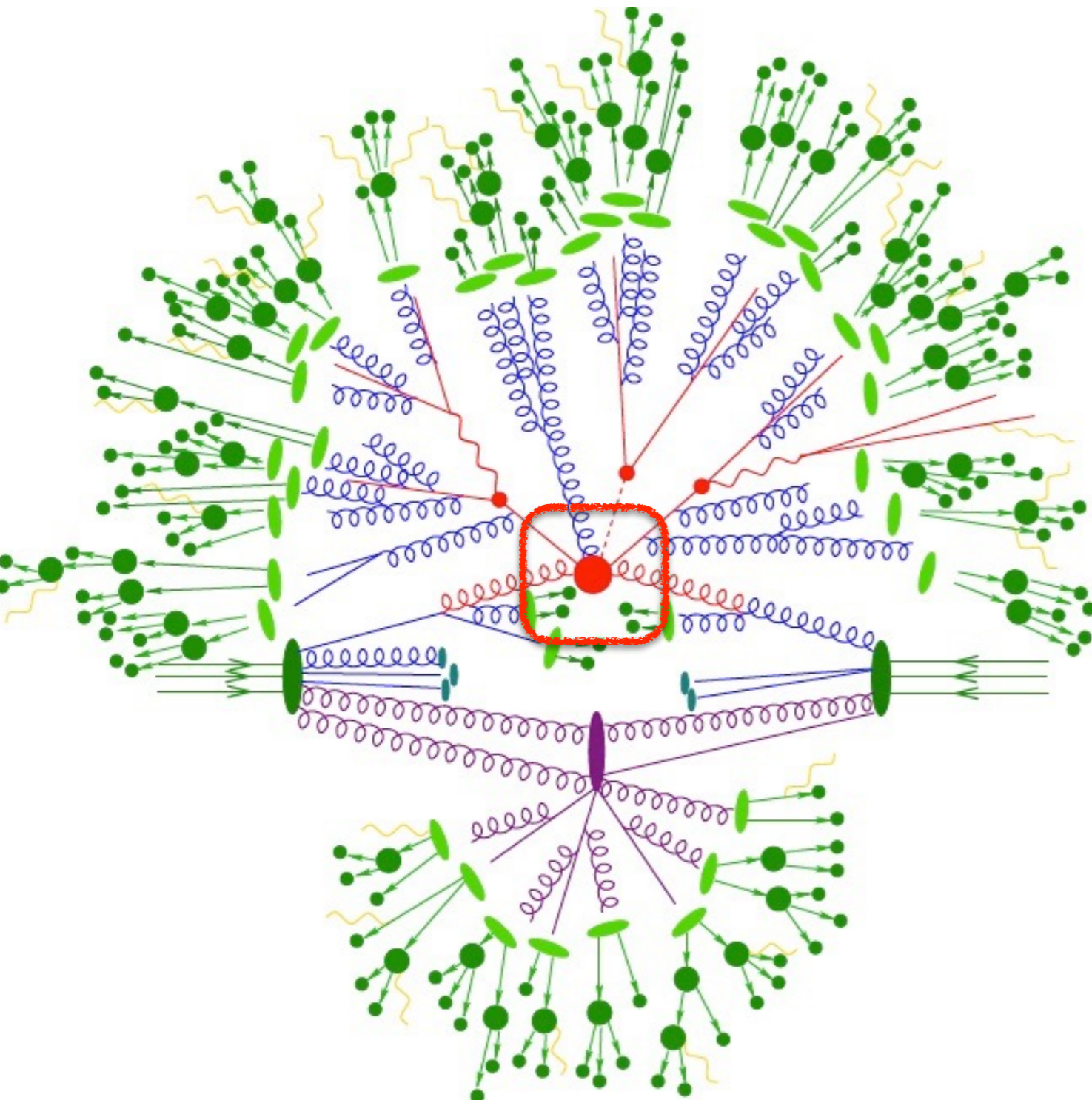


- Fits are stable under inclusion/exclusion of extra data-set
- Effect of new data: mostly reduction in uncertainty, small change in the central value

- With more and more data, can also try to fit “safest” PDFs from kinematic regions which should be free from BSM contaminations (e.g. forward jets...)

# The hard process: precision calculations

$$d\sigma = \int dx_1 dx_2 f(x_1) f(x_2) d\sigma_{\text{part}}(x_1, x_2) F_J (1 + \mathcal{O}(\Lambda_{\text{QCD}}/Q))$$



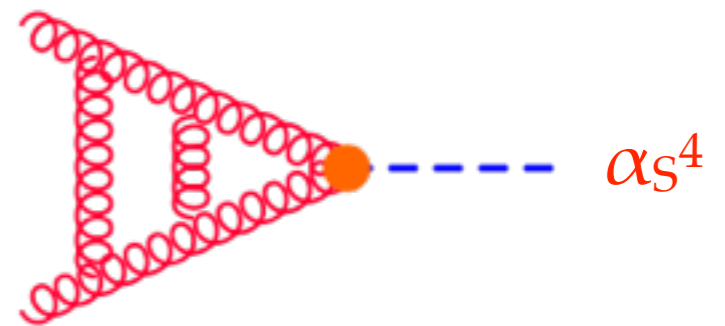
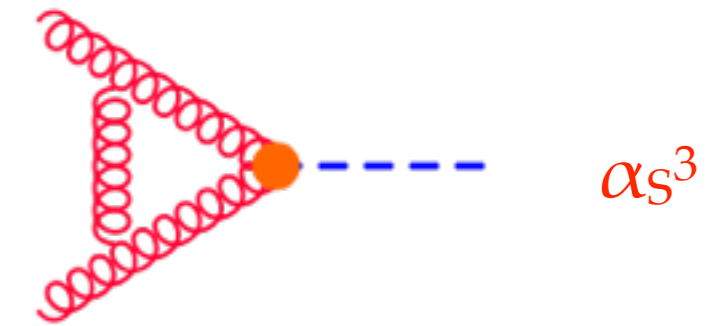
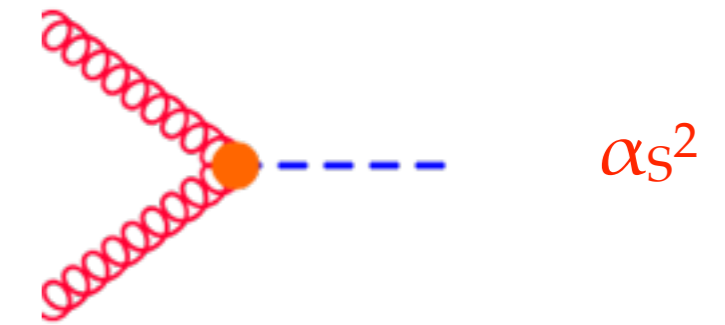
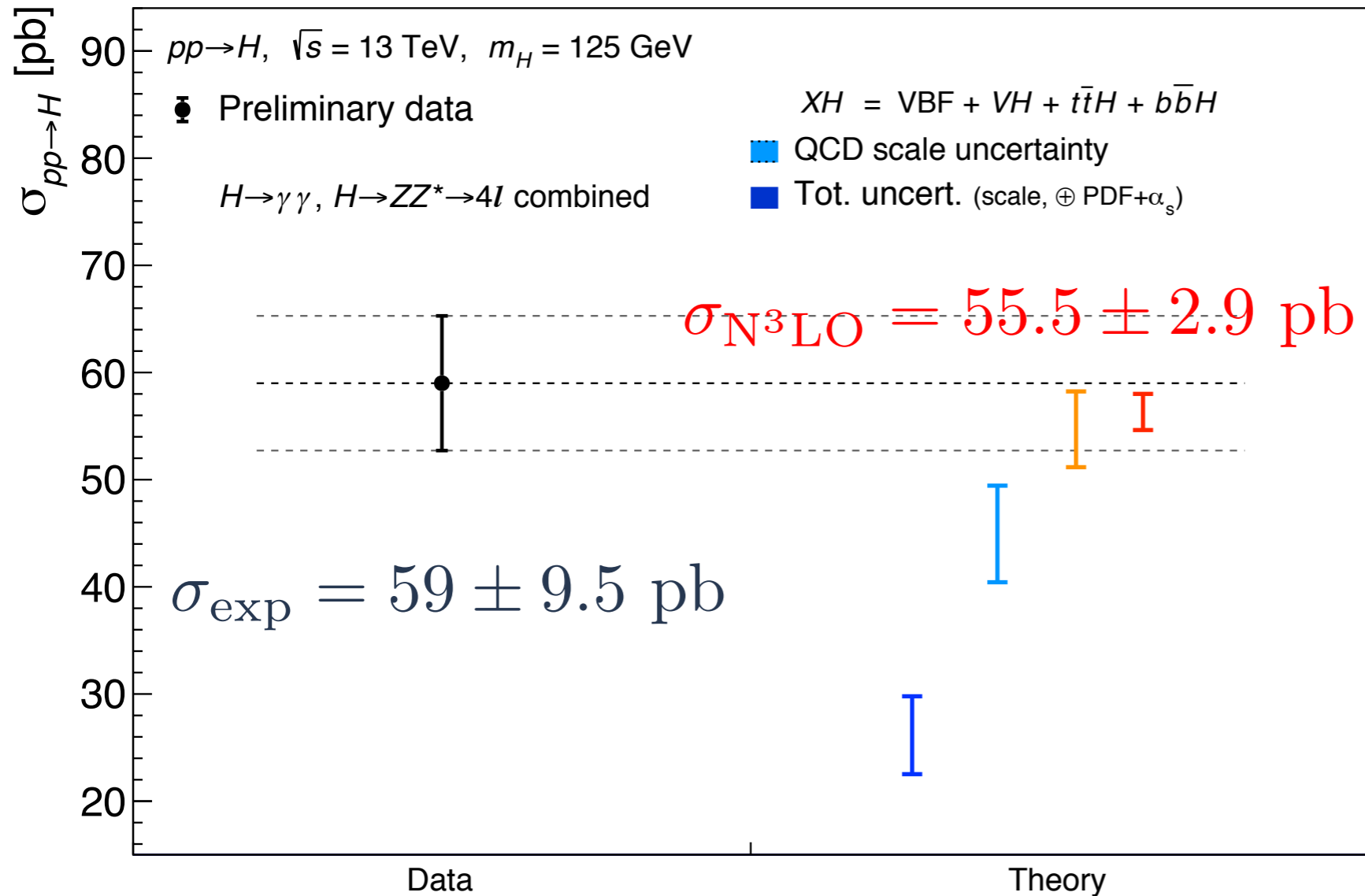
## THE “INTERESTING” SHORT DISTANCE CROSS-SECTION

- Asymptotic freedom  $\rightarrow$  at high scale QCD is perturbative
- Still, for typical EW scales  $\alpha_s \sim 0.1$
- The path to precision:  
NLO  $\sim 10\%$ , NNLO  $\sim 1\%$ .  
Gluonic processes (e.g. Higgs):  
large color charges  $\alpha_s C_A \sim 0.3$ .  
Even higher orders may be required (N<sup>3</sup>LO...)

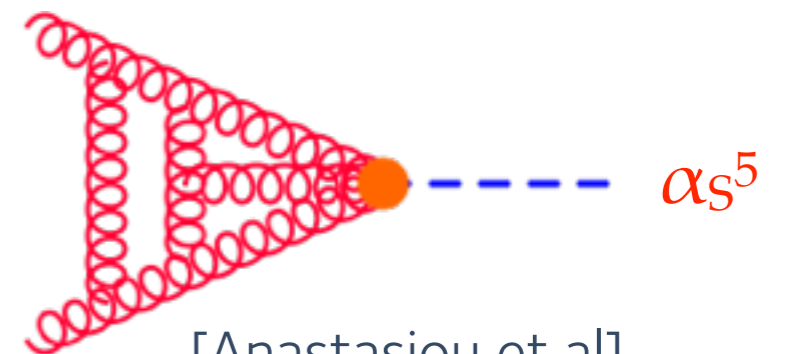
# The hard process: an ideal world

- In a perfect world (= large luminosities, good S/B control, large energy coverages):
  - find simple high-Q observables, where contamination by IR physics is minimal
  - “cut-and-count” like analysis, in the fiducial region → very clean data / theory comparison
- Whenever this is possible: very good theoretical control on our predictions. If the process is simple enough, we can obtain very accurate reliable results via **Higher Order Perturbative Computations**
- Fixed order (differential) computations:
  - very solid framework
  - they give direct access to the actual fiducial region (i.e. we can put cuts on the final state)

# The need for higher orders: Higgs



[Anastasiou, Melnikov;  
Harlander, Kilgore]

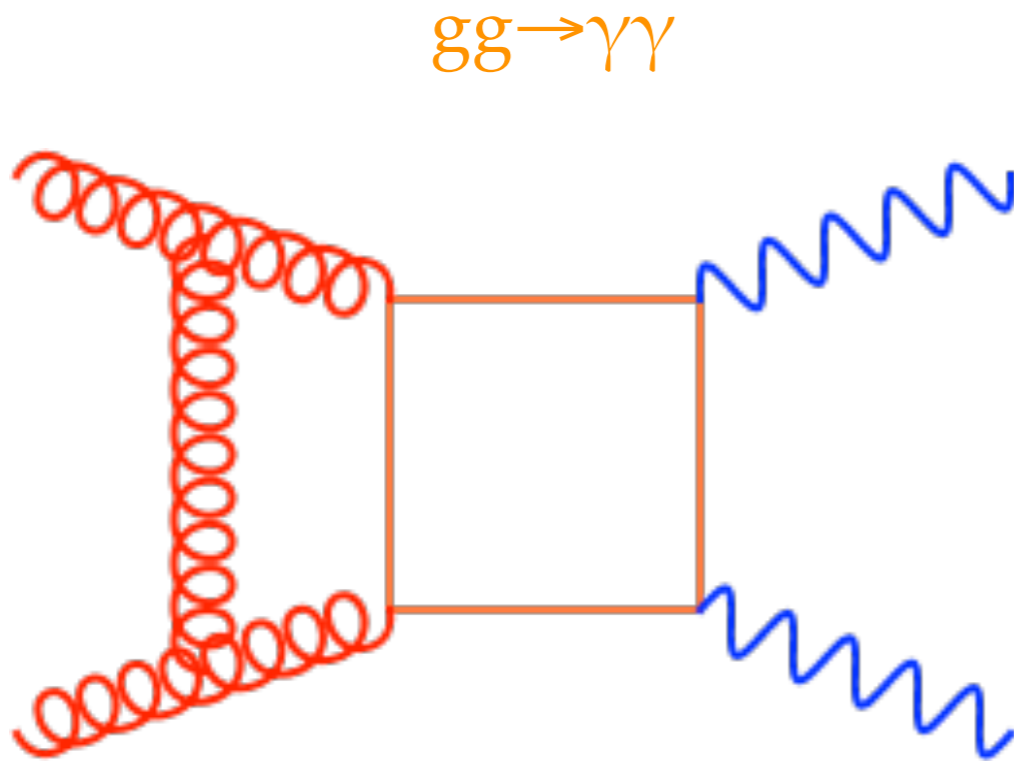


N<sup>3</sup>LO results needed to establish perturbative convergence / reduce residual theoretical uncertainty

# Higher order calculations: amplitudes

A crucial ingredient: multi-loop scattering amplitudes

The problem: complexity grows very fast with number of scales (#legs/masses)



$$\begin{aligned}
 F_{--++}^L &= -(x^2 + y^2) \left[ 4\text{Li}_4(-x) + \frac{1}{48} Z_+^4 \right. \\
 &\quad \left. + (\tilde{Y} - 3\tilde{X})\text{Li}_3(-x) + \Xi\text{Li}_2(-x) \right. \\
 &\quad \left. + i\frac{\pi}{12} Z_+^3 + i\frac{\pi^3}{2} X - \frac{\pi^2}{12} X^2 - \frac{109}{720} \pi^4 \right] \\
 &\quad + \frac{1}{2} x(1 - 3y) \left[ \text{Li}_3(-x/y) - Z_- \text{Li}_2(-x/y) \right. \\
 &\quad \left. - \zeta_3 + \frac{1}{2} Y \tilde{Z} \right] + \frac{1}{8} \left( 14(x - y) - \frac{8}{y} + \frac{9}{y^2} \right) \Xi \\
 &\quad + \frac{1}{16} (38xy - 13) \tilde{Z} - \frac{\pi^2}{12} - \frac{9}{4} \left( \frac{1}{y} + 2x \right) \tilde{X} \\
 &\quad + \frac{1}{4} x^2 \left[ Z_-^3 + 3\tilde{Y} \tilde{Z} \right] + \frac{1}{4} + \{t \leftrightarrow u\},
 \end{aligned}$$

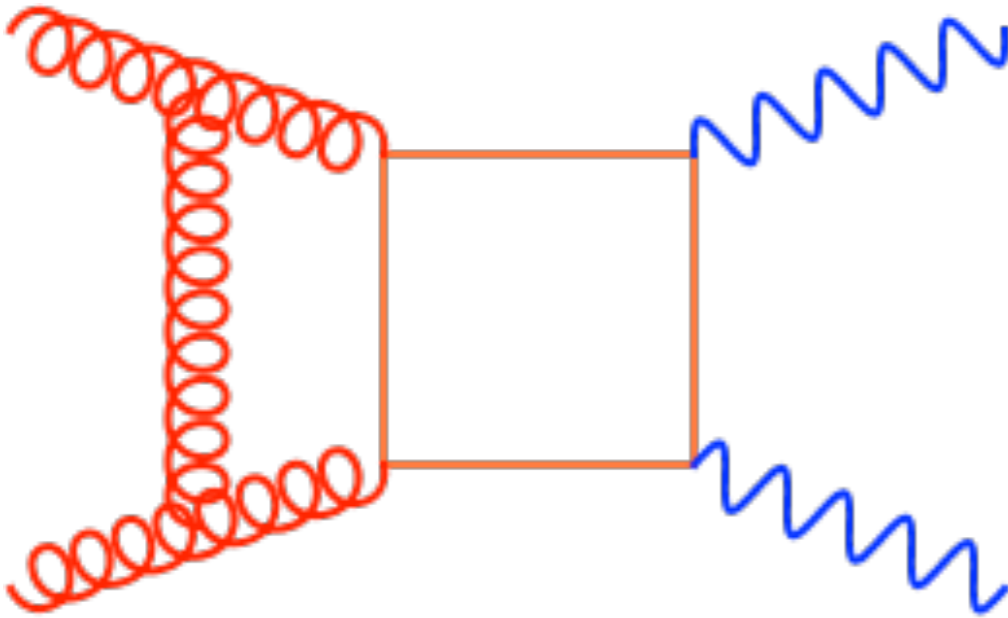
[Bern, De Freitas, Dixon (2002)]

# Higher order calculations: amplitudes

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$gg \rightarrow ZZ$



```
[766]+n(-13,2)*r[771]+n(19,2)*r[772]+n(43,2)*r[773];  
r[12412] = n(-23,2)*r[750]+n(-12)*r[754]+n(2)*r[758]+n(-11,4)*r[759]+n(-11,4)*r[  
760]+n(17,2)*r[761]+n(-11,4)*r[765]+n(-11,4)*r[766];  
r[12413] = n(-1,4)*r[750]+n(-2)*r[760]+n(2)*r[766]+r[771]+n(-1)*r[772]+n(-2)*r[8  
19]+n(5)*r[820]+n(2)*r[821];  
r[12414] = n(3,2)*r[750]+n(3,2)*r[984]+n(-3)*r[1333]+n(3)*r[1350]+n(3)*r[1351]+n  
(3)*r[1356]+n(3)*r[1520]+n(3)*r[1529];  
r[12415] = n(5)*r[750]+n(1,2)*r[759]+n(-1,2)*r[760]+n(-7,2)*r[765]+n(-5,2)*r[766  
]+n(7,2)*r[771]+n(-1,2)*r[772]+n(3,2)*r[773];  
r[12416] = n(34)*r[750]+n(-5,2)*r[759]+n(-5,2)*r[760]+n(-89,2)*r[765]+n(-89,2)*r  
[766]+n(59,2)*r[771]+n(35,2)*r[772]+n(59,2)*r[773];  
r[12417] = n(-4)*r[753]+n(-3,2)*r[759]+n(-3,2)*r[760]+n(17,2)*r[762]+n(-3,2)*r[7  
65]+n(-3,2)*r[766]+n(-17,2)*r[768]+n(3,2)*r[771];  
r[12418] = n(-1)*r[755]+n(115,12)*r[759]+n(-81,4)*r[760]+n(17,2)*r[764]+n(-13,12  
) *r[765]+n(71,4)*r[766]+n(-17,2)*r[770]+n(25,4)*r[771];  
r[12419] = n(-2,3)*r[755]+n(-605,12)*r[759]+n(15,4)*r[760]+n(-17,2)*r[764]+n(59,  
12)*r[765]+n(-161,4)*r[766]+n(17,2)*r[770]+n(73,4)*r[771];  
r[12420] = n(-1)*r[756]+n(-565,24)*r[759]+n(7,24)*r[760]+n(17,2)*r[762]+n(347,24  
) *r[765]+n(-83,8)*r[766]+n(-17,2)*r[768]+n(721,24)*r[771];  
1
```

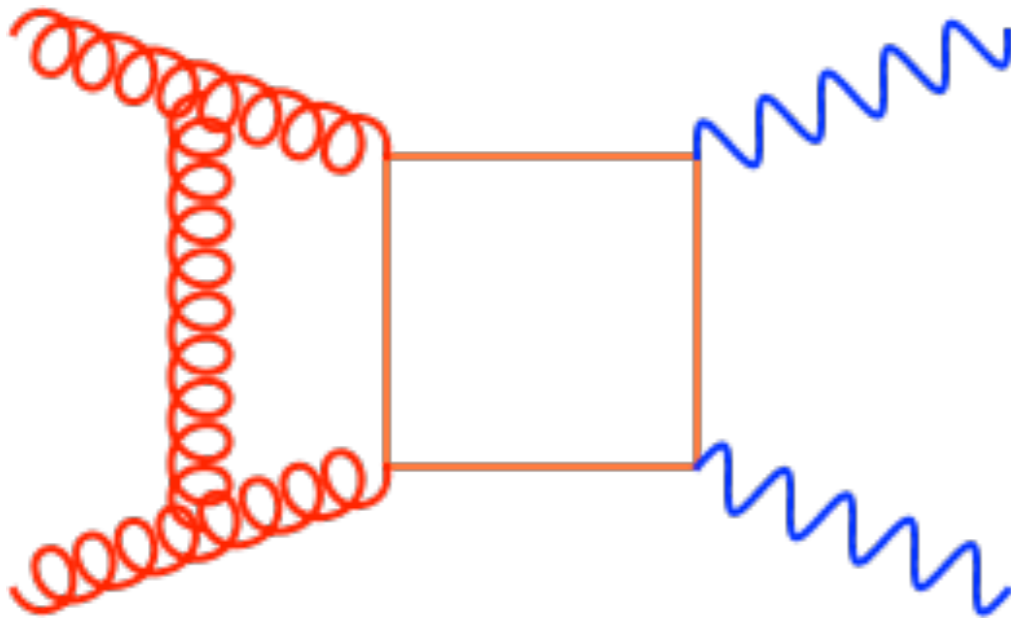
[FC, Henn, Melnikov, Smirnov<sup>2</sup>; Tancredi,  
von Manteuffel, Weihs, Gehrmann (2015)]

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$gg \rightarrow ZZ$



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760]+n(17,2)*r[761]+n(-11,4)*r[765]+n(-11,4)*r[766];
r[12413] = n(-1,4)*r[750]+n(-2)*r[760]+n(2)*r[766]+r[771]+n(-1)*r[772]+n(-2)*r[8
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r[12414] = n(3,2)*r[750]+n(3,2)*r[984]+n(-3)*r[1333]+n(3)*r[1350]+n(3)*r[1351]+n
(3)*r[1356]+n(3)*r[1520]+n(3)*r[1529];
r[12415] = n(5)*r[750]+n(1,2)*r[759]+n(-1,2)*r[760]+n(-7,2)*r[765]+n(-5,2)*r[766
]+n(7,2)*r[771]+n(-1,2)*r[772]+n(3,2)*r[773];
r[12416] = n(34)*r[750]+n(-5,2)*r[759]+n(-5,2)*r[760]+n(-89,2)*r[765]+n(-89,2)*r
[766]+n(59,2)*r[771]+n(35,2)*r[772]+n(59,2)*r[773];
r[12417] = n(-4)*r[753]+n(-3,2)*r[759]+n(-3,2)*r[760]+n(17,2)*r[762]+n(-3,2)*r[7
65]+n(-3,2)*r[766]+n(-17,2)*r[768]+n(3,2)*r[771];
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r[12419] = n(-2,3)*r[755]+n(-605,12)*r[759]+n(15,4)*r[760]+n(-17,2)*r[764]+n(59,
12)*r[765]+n(-161,4)*r[766]+n(17,2)*r[770]+n(73,4)*r[771];
r[12420] = n(-1)*r[756]+n(-565,24)*r[759]+n(7,24)*r[760]+n(17,2)*r[762]+n(347,24
)*r[765]+n(-83,8)*r[766]+n(-17,2)*r[768]+n(721,24)*r[771];
```

[FC, Henn, Melnikov, Smirnov<sup>2</sup>; Tancredi,  
von Manteuffel, Weihs, Gehrmann (2015)]

10 MB expression, complex transcendental functions

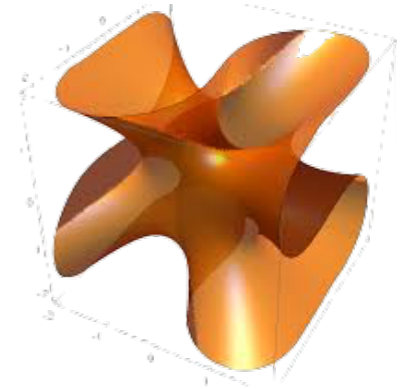
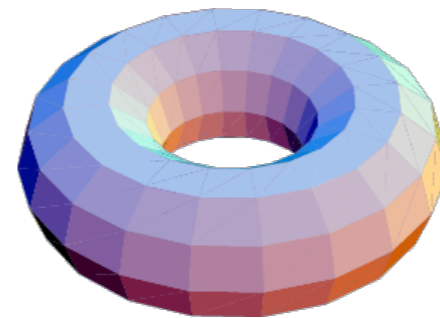
Massive tops (crucial for high energy): only known numerically

# Amplitudes: a lot of recent progress

[Abreu, Badger, Brønnum-Hansen, Bargiela, Borowka, Buccioni, FC, Chawdhry, Chen, Chicherin, Czakon, de Laurentis, Dormans, Duhr, Dunbar, Febres-Cordero, Frellesvig, Gambuti, Gehrmann, Hartanto, Heinrich, Henn, Ita, Jones, Jehu, Liu, Lo Presti, Manteuffel, Ma, Maître, Mitev, Mitov, Page, Peraro, Perkins, Poncelet, Schabinger, Sotnikov, Tancredi, Wasser, Weinzierl, Zhang...]

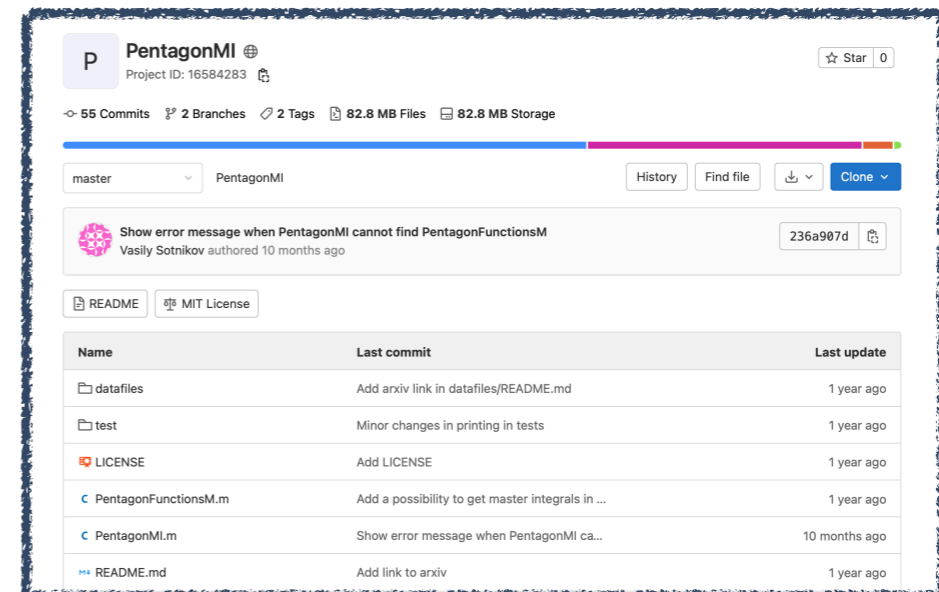
## Analytical / theoretical investigations:

- New structures / symmetries
- Interesting mathematical objects



## Numerical / implementation:

- Finite-field reconstruction
- Fast numerical evaluation



State of the art:  $2 \rightarrow 2@2L$ , some  $2 \rightarrow 3@2L$ , first results for  $2 \rightarrow 2@3L$

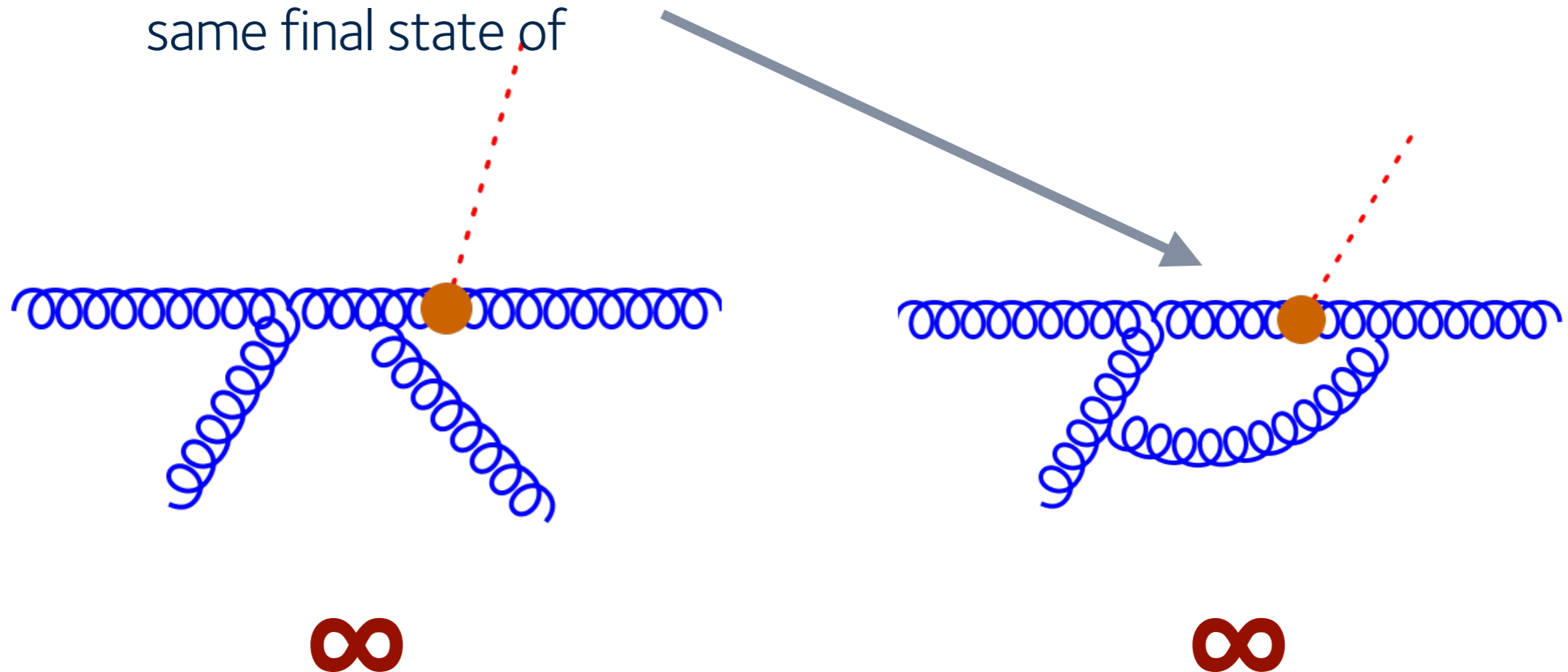


# From amplitudes to physics

Quantum mechanics: you should only deal with observables

If 2nd gluon soft/collinear:

same final state of



Only the sum is well-defined. Proper regulation / combination of the IR effects very complicated

# From amplitudes to physics

--"Local analytic" [Magnea, Maina, Pelliccioli, Signorile-Signorile, Torrielli]

--"qt" [Catani, Grazzini]

--"Antenna" [Gehrmann-de Ridder, Gehrmann, Glover]

--"N-jettiness" [Boughezal et al, Gaunt et al]

--"Sector decomposition+FKS" [Binoth, Heinrich; Anastasiou, Melnikov, Petriello; Czakon; Czakon, Heymes; Asteriadis, FC, Melnikov, Röntsch]

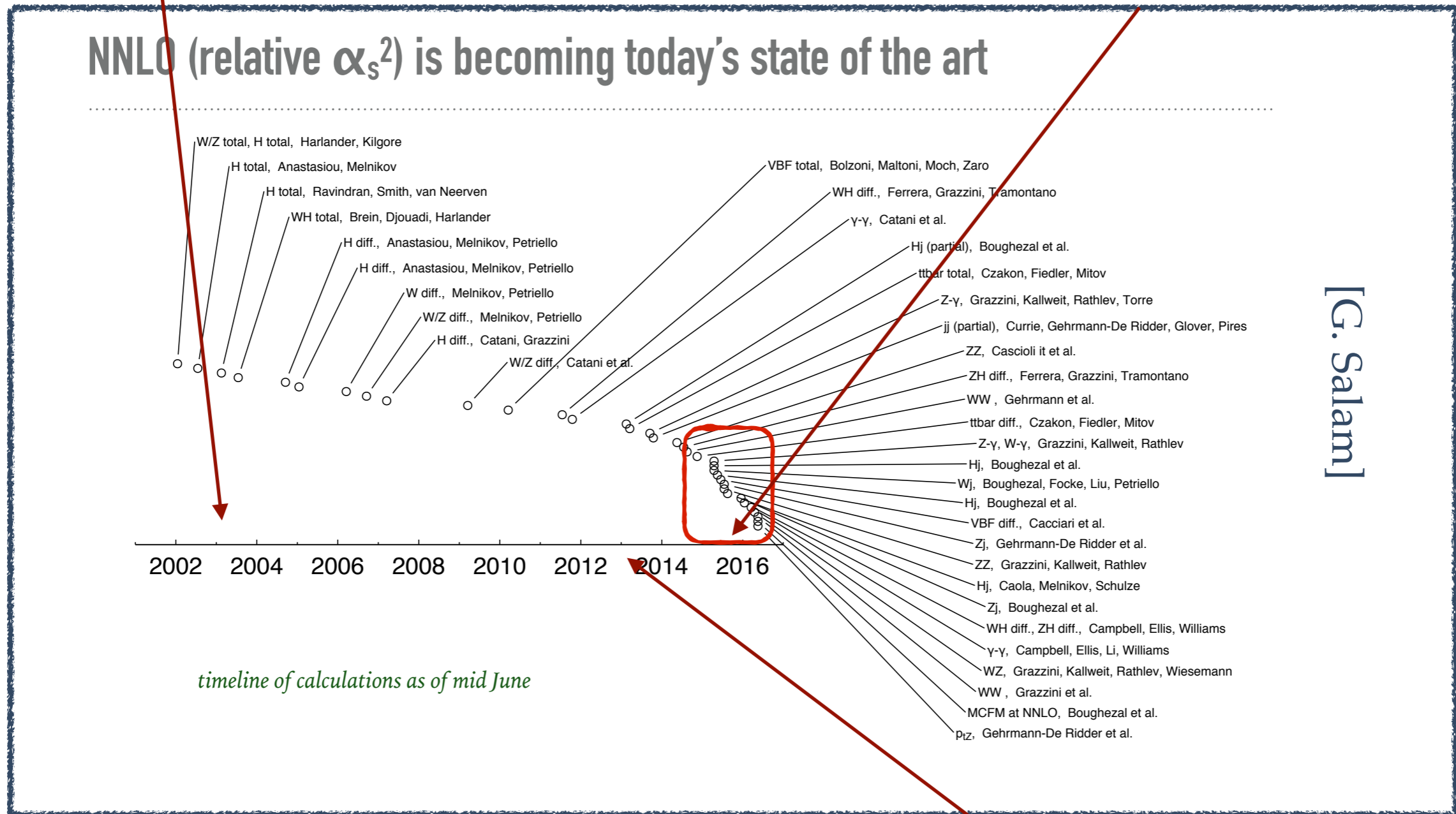
--"Projection to Born" [Cacciari, Dreyer, Karlberg, Zanderighi, Salam]

--"Colorful NNLO" [Del Duca, Duhr, Kardos, Somogyi, Trocsanyi]

# The NNLO timeline

1st 2L amplitudes

new ideas/techniques for multi-loop amplitude calculation

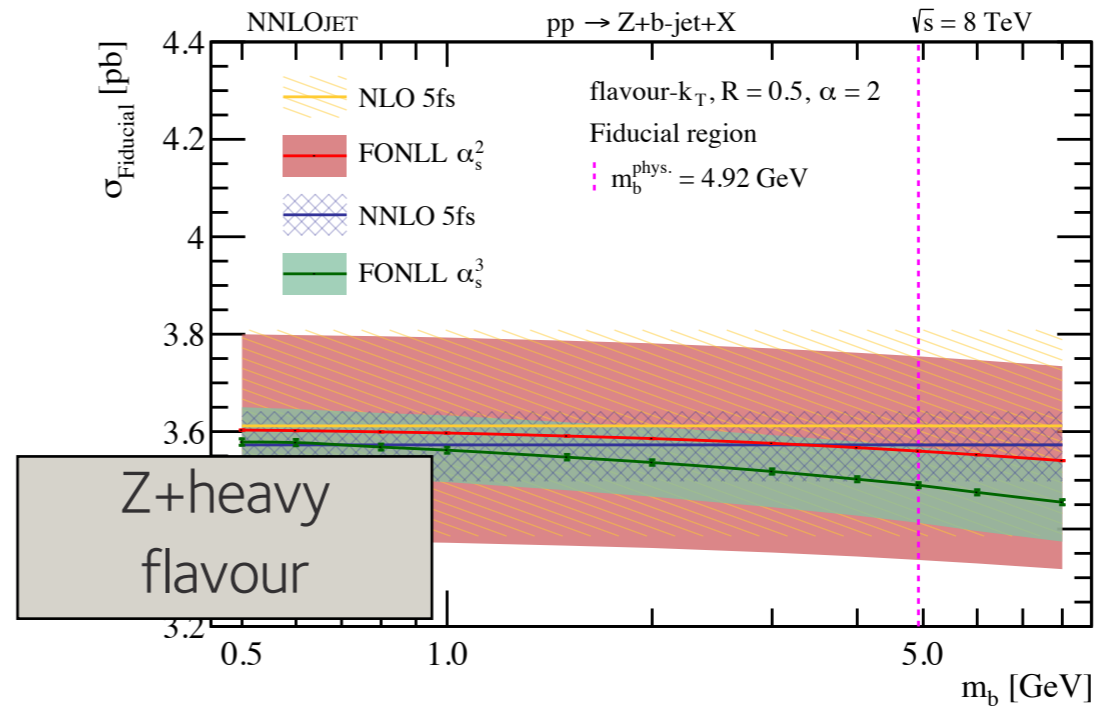
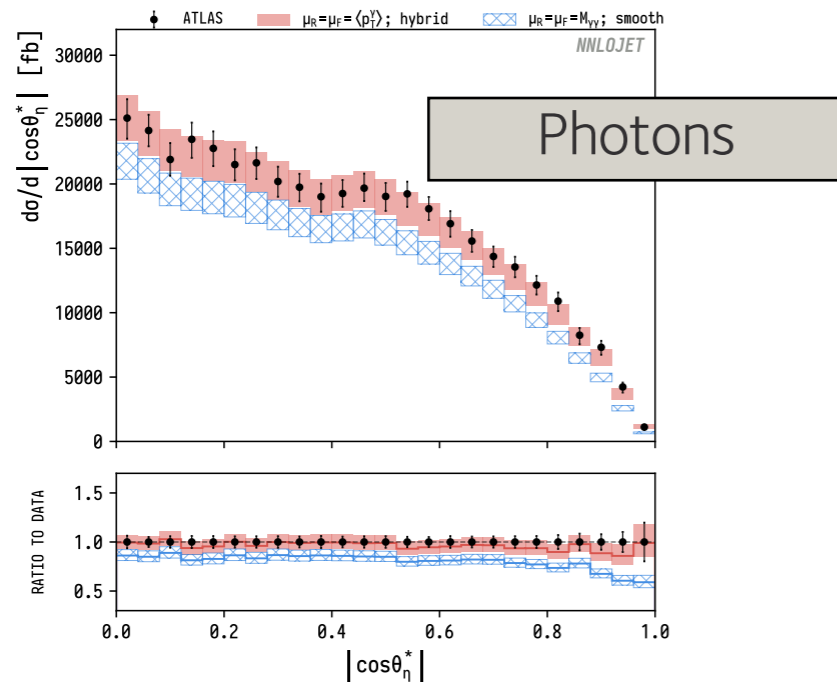


IR organisation for arbitrary processes

# Physics: 2→2 NNLO is well-understood

## NNLO: from proof of concept to detailed phenomenology

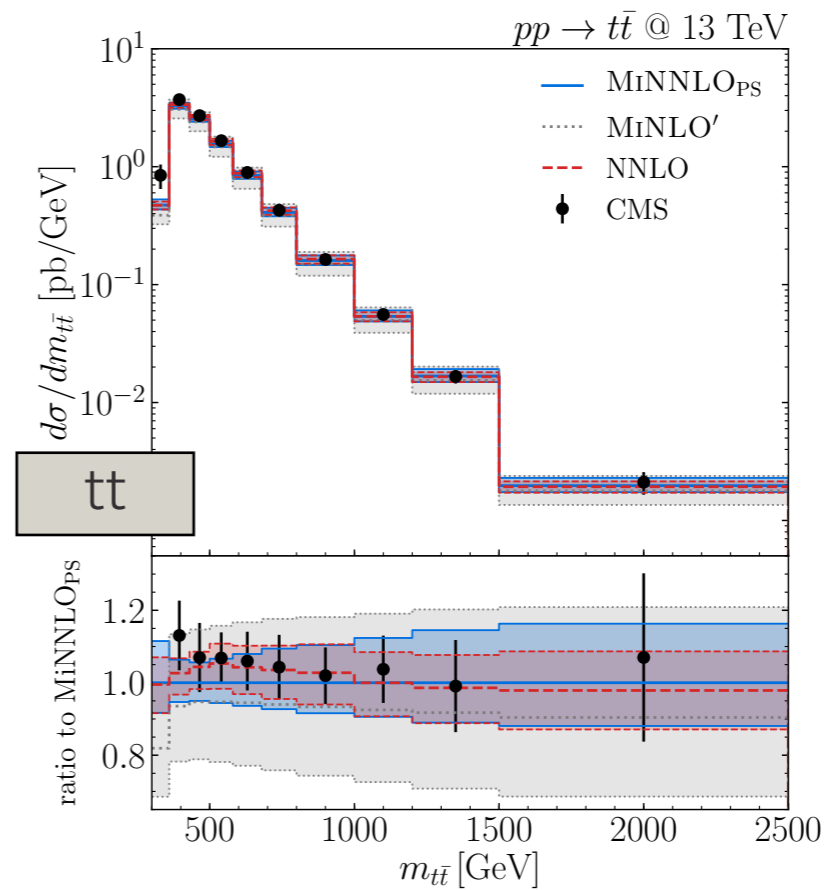
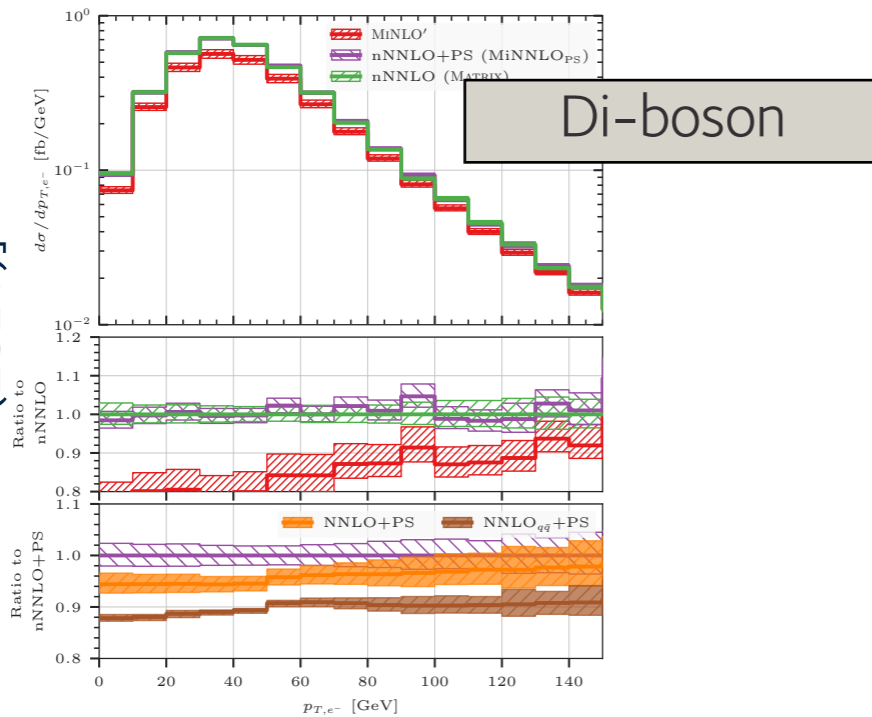
[Gehrmann, Glover, Huss, Whitehead (2020)]



[Gauld, Gehrmann-de Ridder, Glover, Huss, Majer (2020)]

## NNLLO + PS becoming a reality

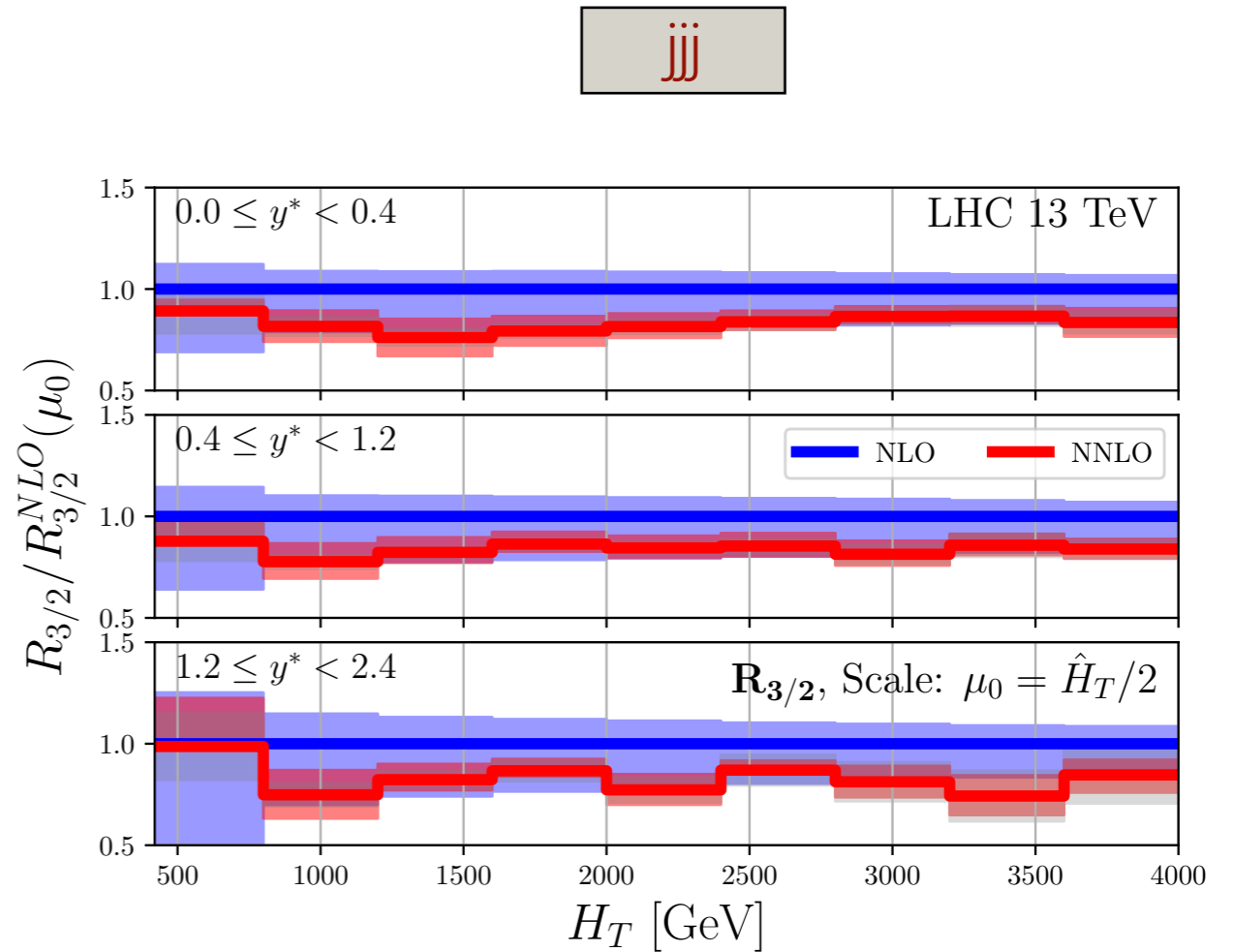
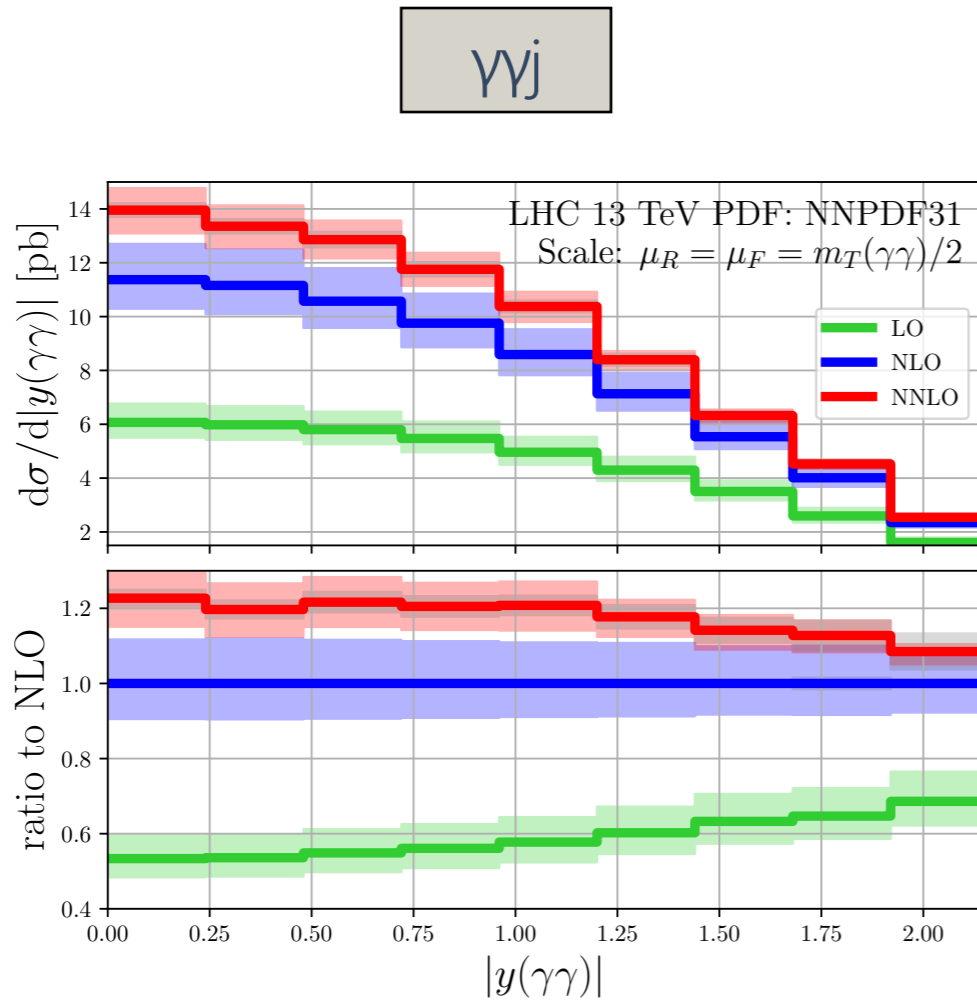
[Buonocore, Koole, Lombardi, Rottoli, Wieseemann, Zanderighi (2021)]



[Mazzitelli, Monni, Nason, Re, Wieseemann, Zanderighi (2021)]

# First steps toward more complex processes

[Chawdhry, Czakon,  
Mitov, Poncelet (2021)]

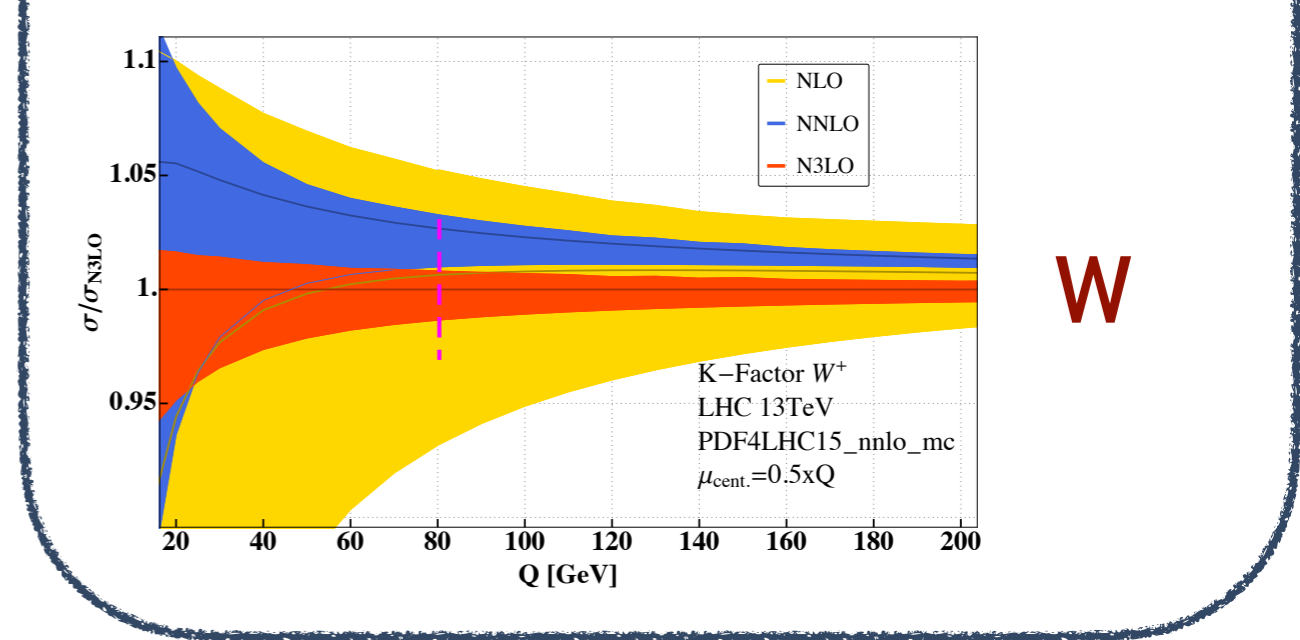
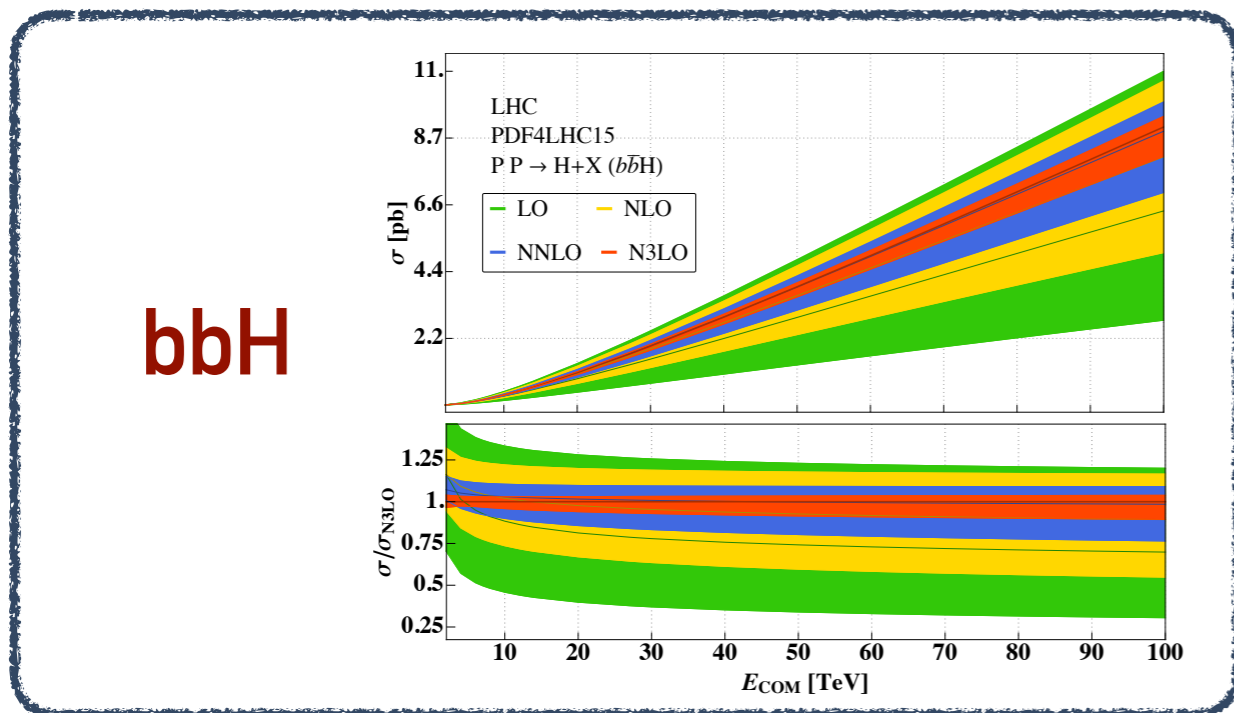
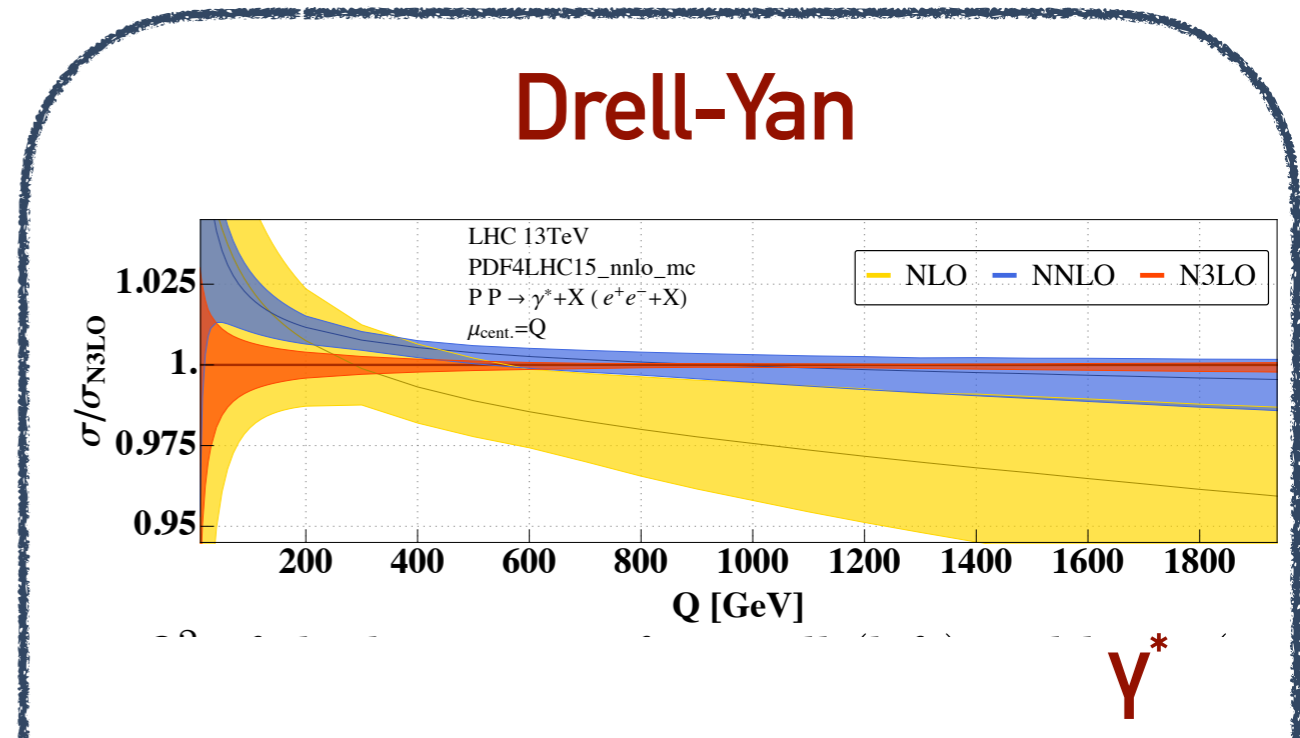
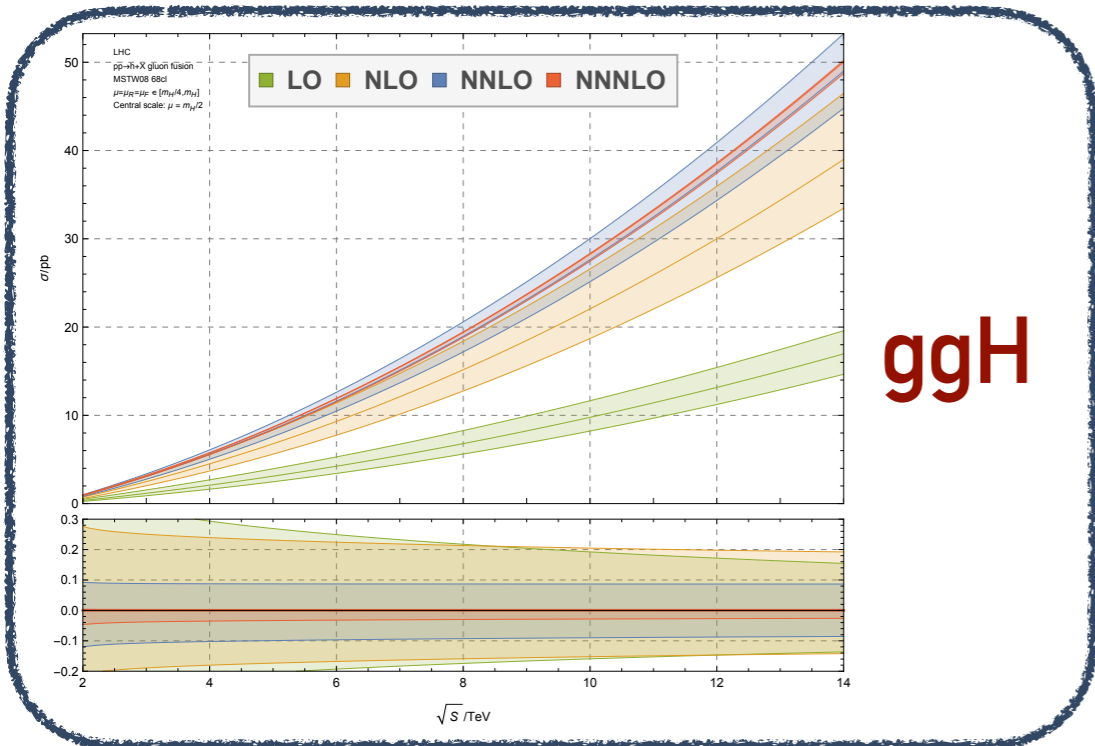


[Czakon, Mitov, Poncelet (2021)]

- $j\bar{j}j$ : “Tour de force in QCD”.
- still very much in the exploratory phase
- Gives access e.g. to  $\alpha_s$  in the TeV region

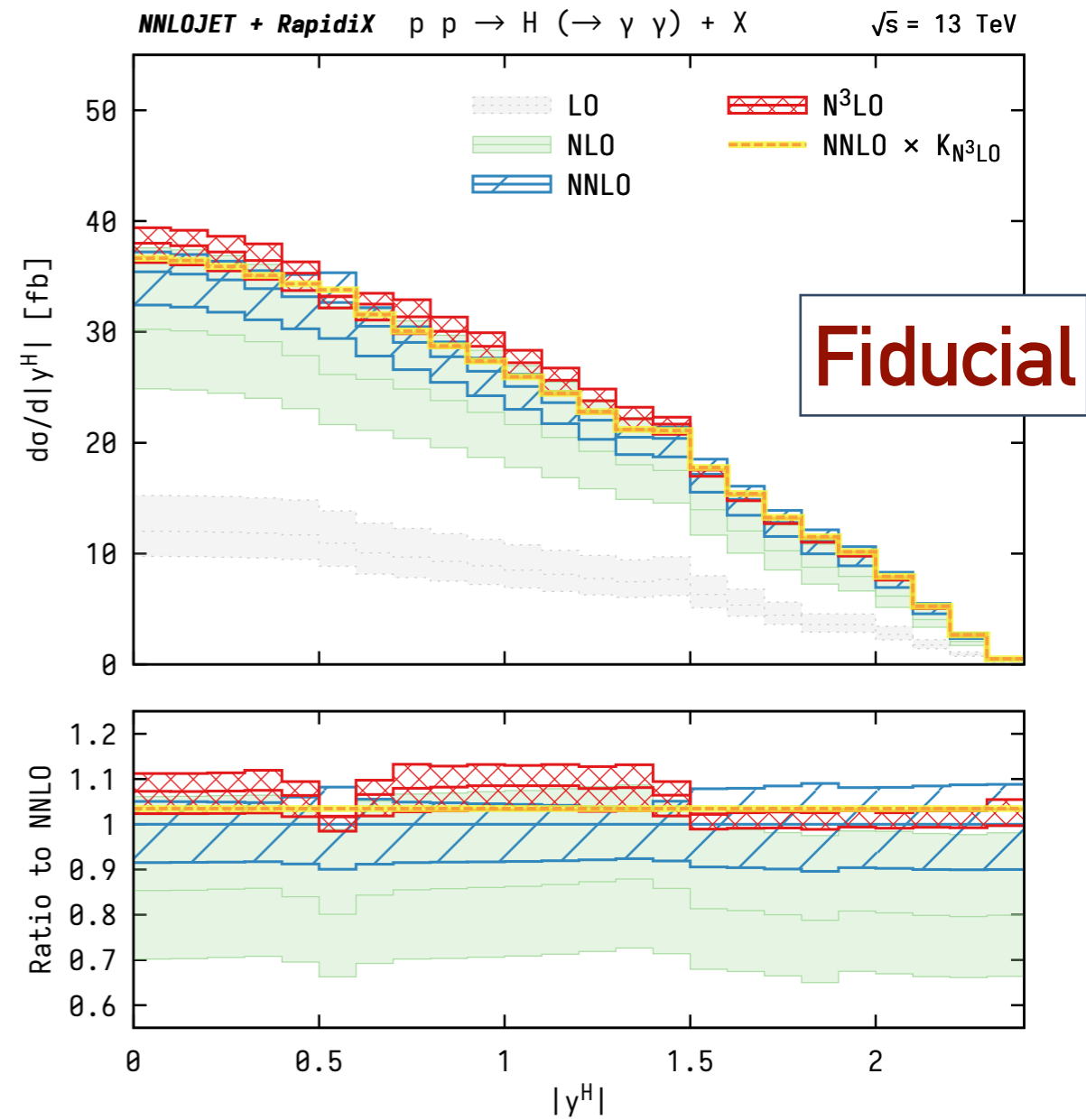
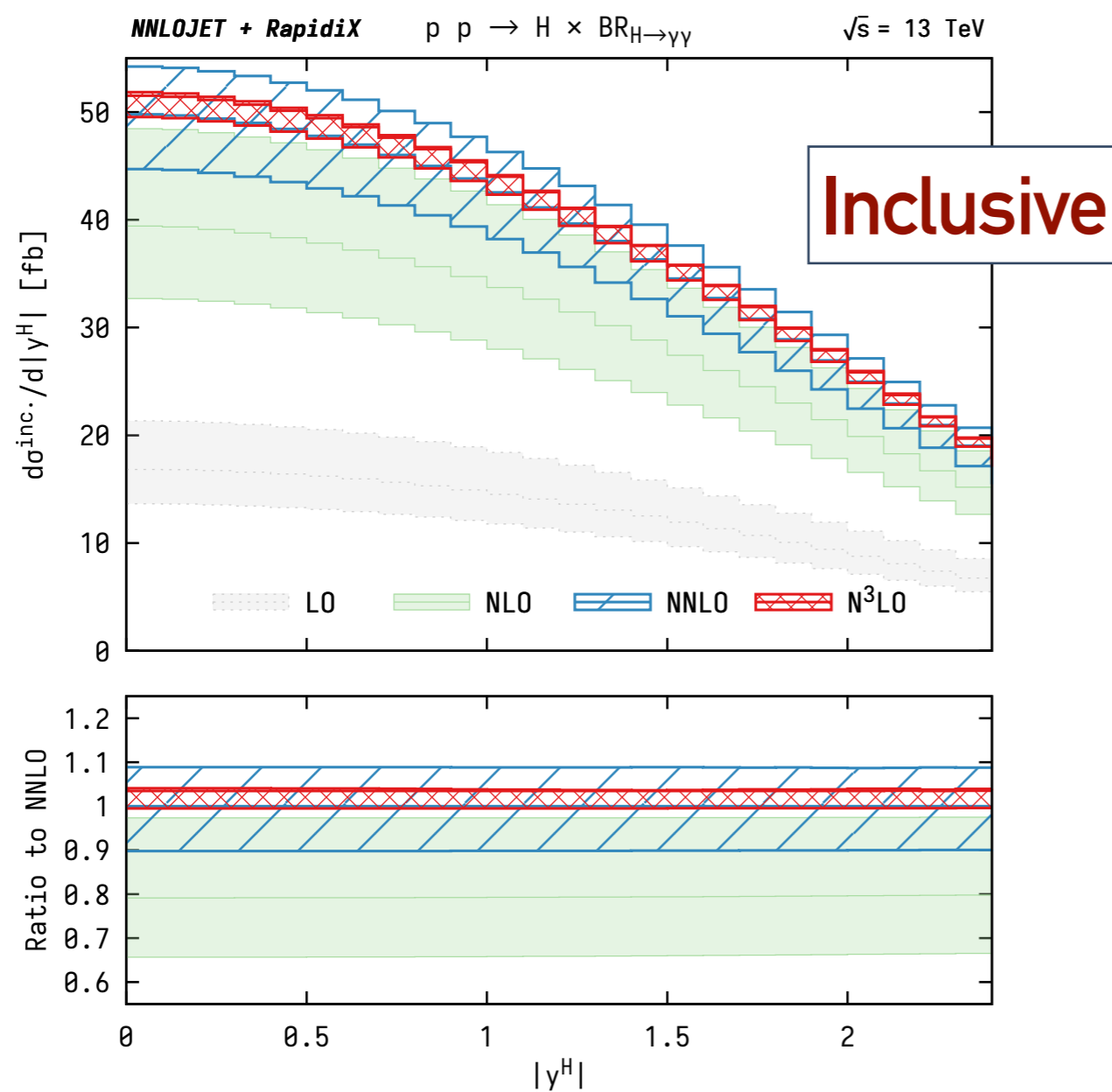
# Even more precise: N<sup>3</sup>LO for standard candles

[Anastasiou, Duhr, Dulat, Furlan, Gehrmann, Herzog, Lazopoulos, Mistlberger (2016-...);  
Duhr, Dulat, Mistlberger (2020-21)]



# Precision studies: lessons learned

Higgs fiducial:  $p_{t,\gamma 1} > 0.35 m_H$ ,  $p_{t,\gamma 2} > 0.25 m_H$ ,



- Inclusive: flat K-factor (as for inclusive), tiny error, no structure
- Fiducial: large corrections, large error, non-trivial shapes



# The hard process: an ideal world

- In a perfect world (= large luminosities, good S/B control, large energy coverages):
  - find simple high-Q observables, where contamination by IR physics is minimal
  - “cut-and-count” like analysis, in the fiducial region → very clean data / theory comparison
- Whenever this is possible: very good theoretical control on our predictions. If the process is simple enough, we can obtain very accurate reliable results via Higher Order Perturbative Computations
- Fixed order (differential) computations:
  - very solid framework
  - they give direct access to the actual fiducial region (i.e. we can put cuts on the final state)

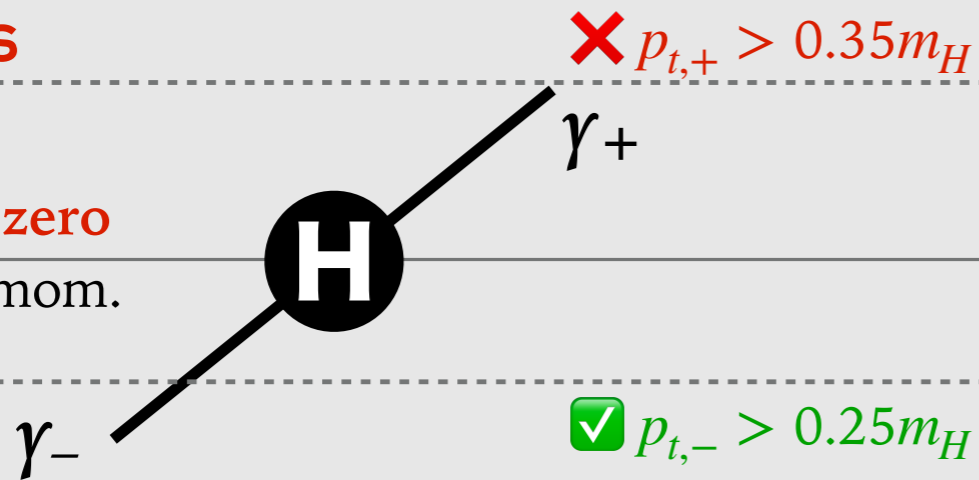


# Precision studies: lessons learned

Higgs fiducial:  $p_{t,\gamma_1} > 0.35 m_H$ ,  $p_{t,\gamma_2} > 0.25 m_H$ ,

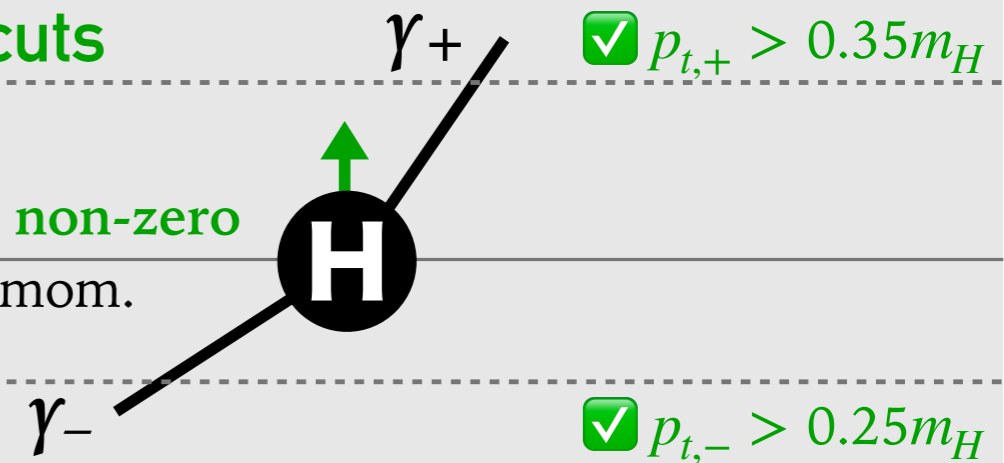
**Fails cuts**

Higgs with **zero**  
transverse mom.



**Passes cuts**

Higgs with **non-zero**  
transverse mom.



**Sensitive to IR physics** [Salam, Slade; Billis, Dehnadi, Ebert, Michel, Tackmann (2021)]

$$\frac{\sigma_{\text{asym}} - f_0 \sigma_{\text{inc}}}{\sigma_0 f_0} \simeq 0.15 \alpha_s - 0.29 \alpha_s^2 + 0.71 \alpha_s^3 - 2.39 \alpha_s^4 + 10.31 \alpha_s^5 + \dots \simeq 0.06$$

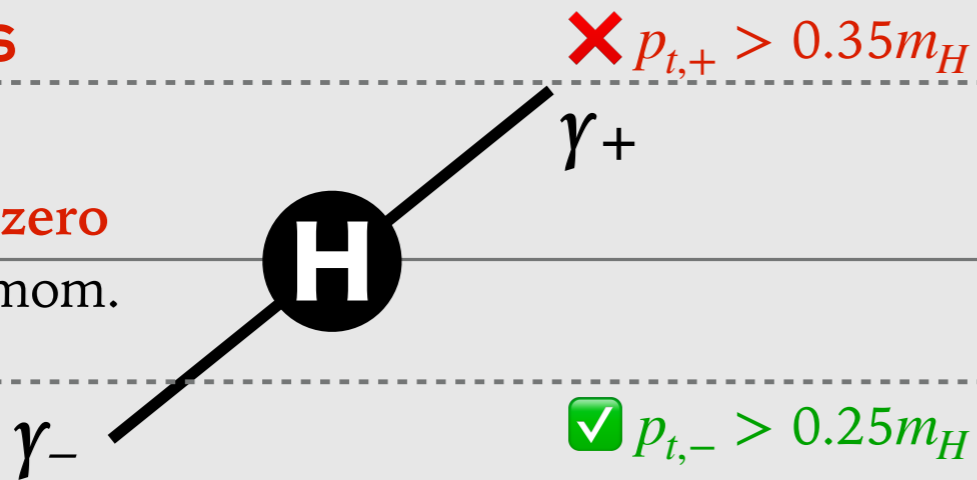
IR-sensitivity makes the perturbative expansion factorially divergent →  
**the more you compute, the worse it gets** [Salam, Slade]

# Precision studies: lessons learned

Higgs fiducial:  $p_{t,\gamma_1} > 0.35 m_H$ ,  $p_{t,\gamma_2} > 0.25 m_H$ ,

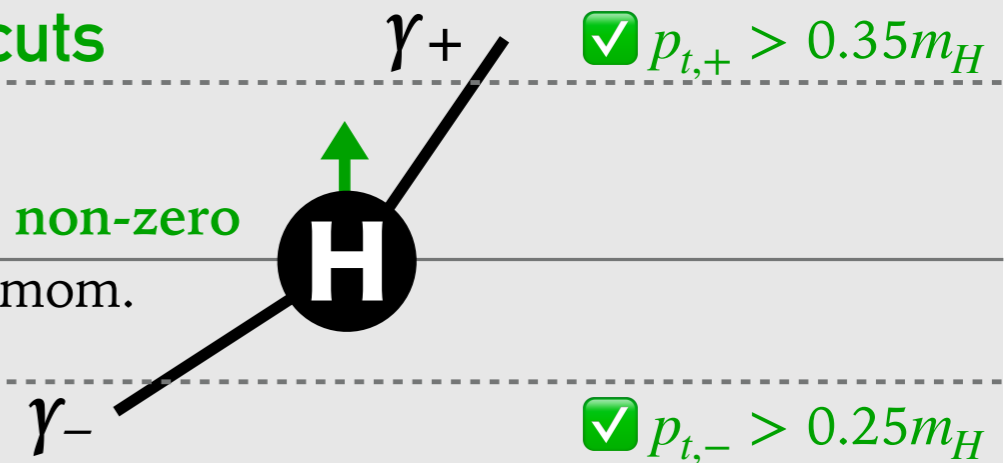
**Fails cuts**

Higgs with **zero**  
transverse mom.



**Passes cuts**

Higgs with **non-zero**  
transverse mom.



**Sensitive to IR physics** [Salam, Slade; Billis, Dehnadi, Ebert, Michel, Tackmann (2021)]

Way out:

- Resum all-order IR effects [Billis, Dehnadi, Ebert, Michel, Tackmann (2021)]
- Design cuts/observables that are insensitive to IR physics, while retaining good S/B ratio [Salam, Slade]

# Precision studies: lessons learned

Higgs fit:  $\mu = 0.95$   $\mu = 0.95$

Fails

As we get more and more precise, and explore the TeV region: careful analysis of common practice become crucial

$35m_H$

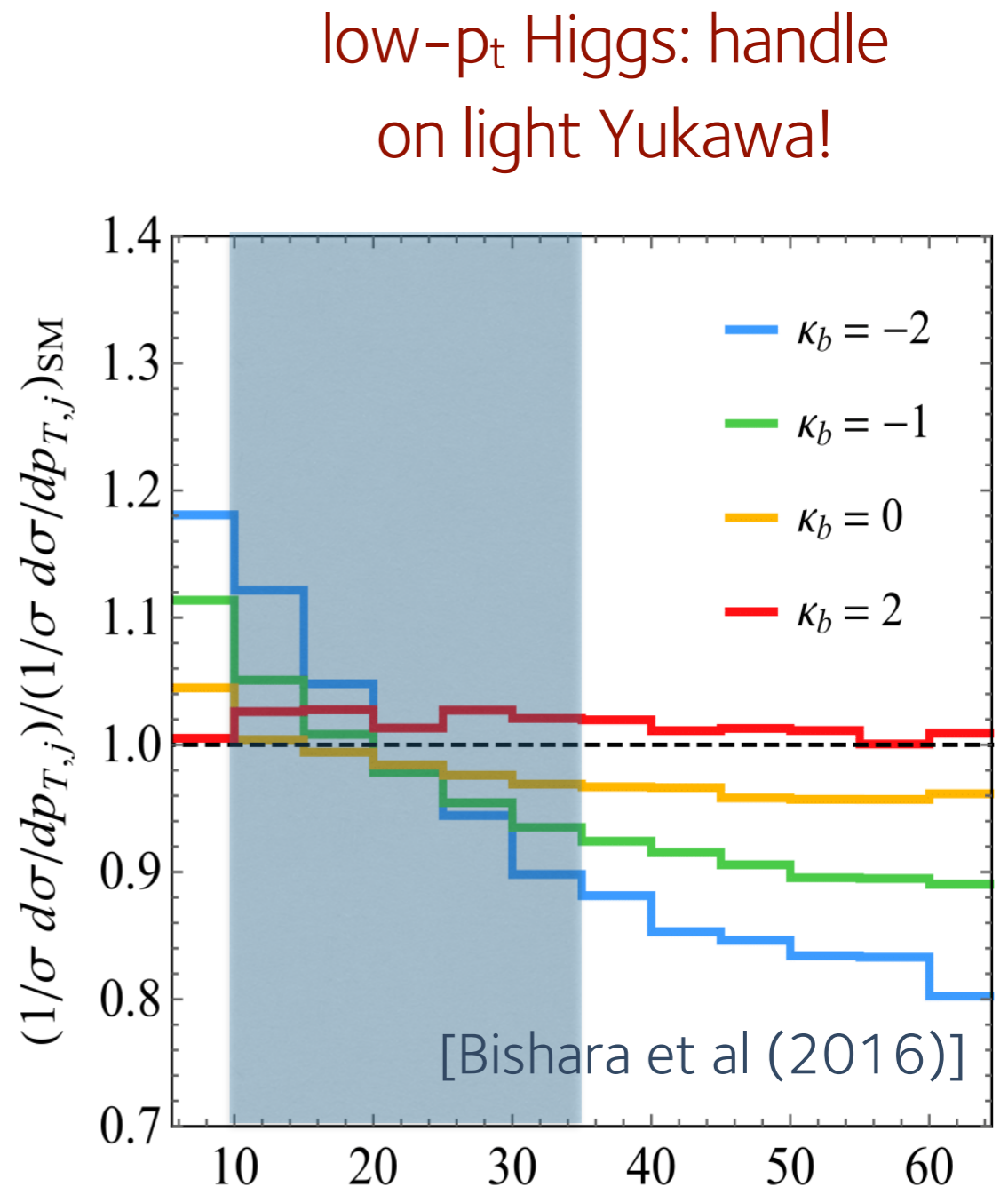
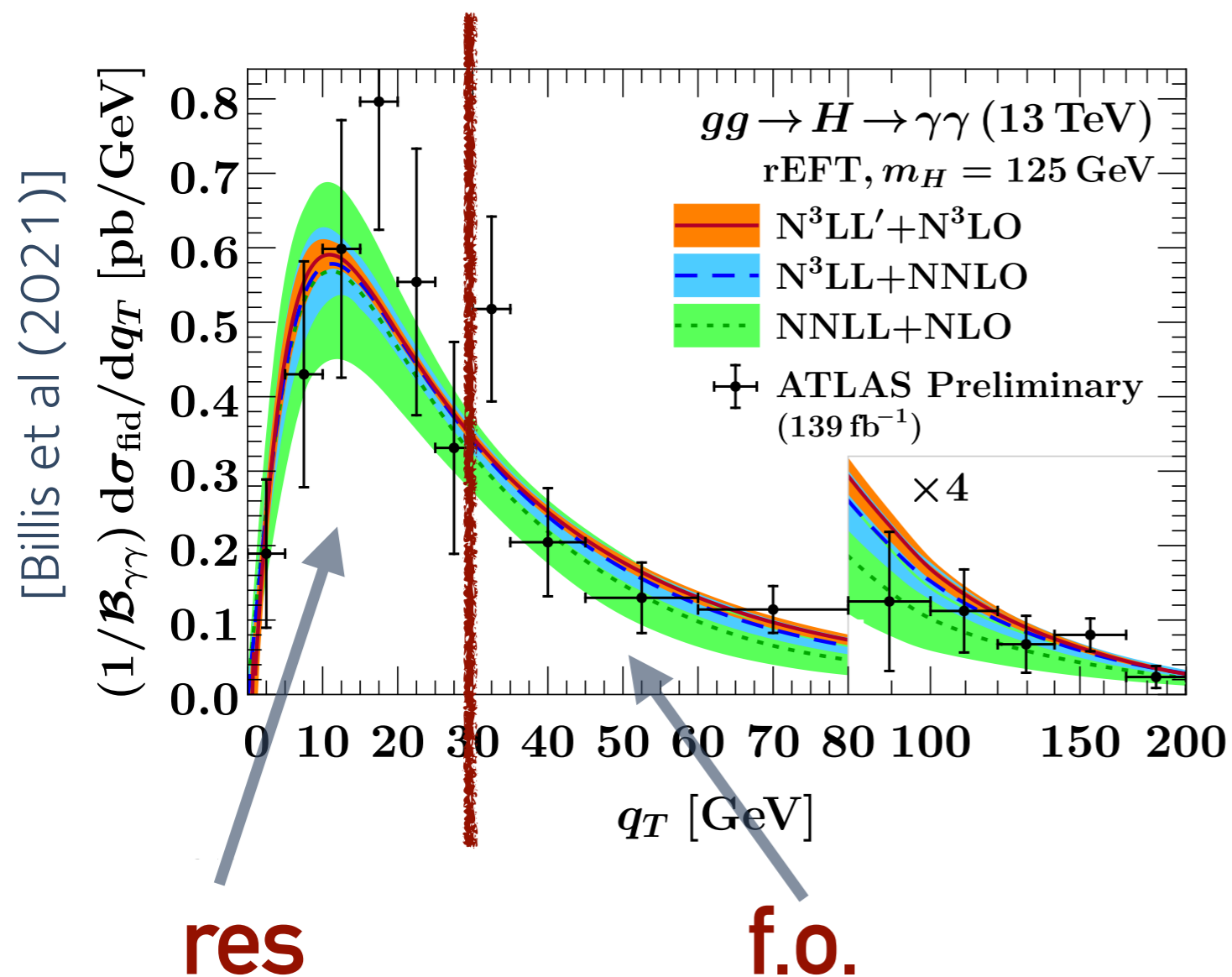
Higgs  
transv

$25m_H$

Problems (and in some cases tentative solutions) already known for energetic tops (high-invariant mass tops are IR-sensitive) and heavy flavour

# Taming IR physics: all-order resummation

In some cases, we can extend the range of validity of the perturbative approach by doing RGE-improved perturbation theory  $\rightarrow$  resum large class of soft/collinear terms

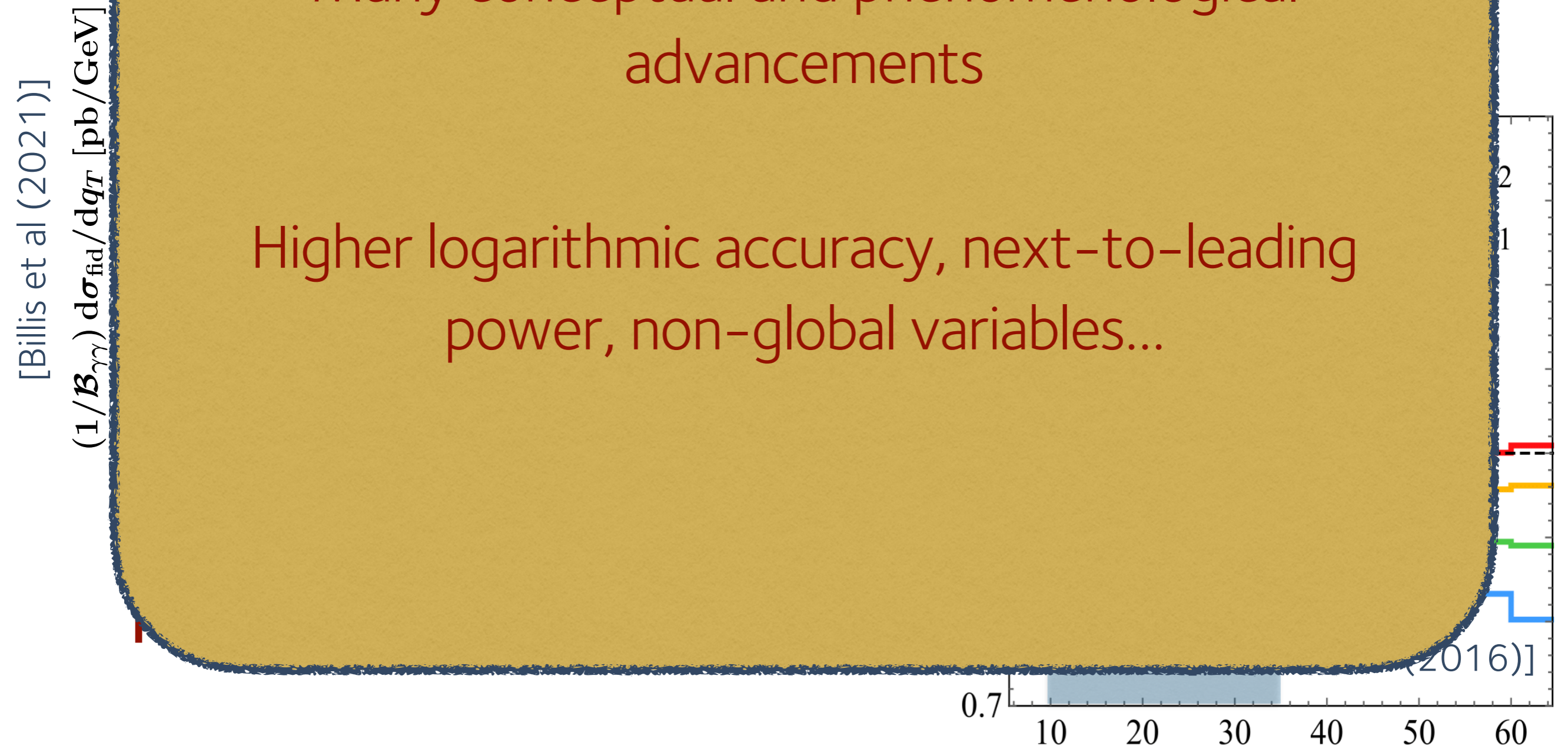


# Taming IR physics: all-order resummation

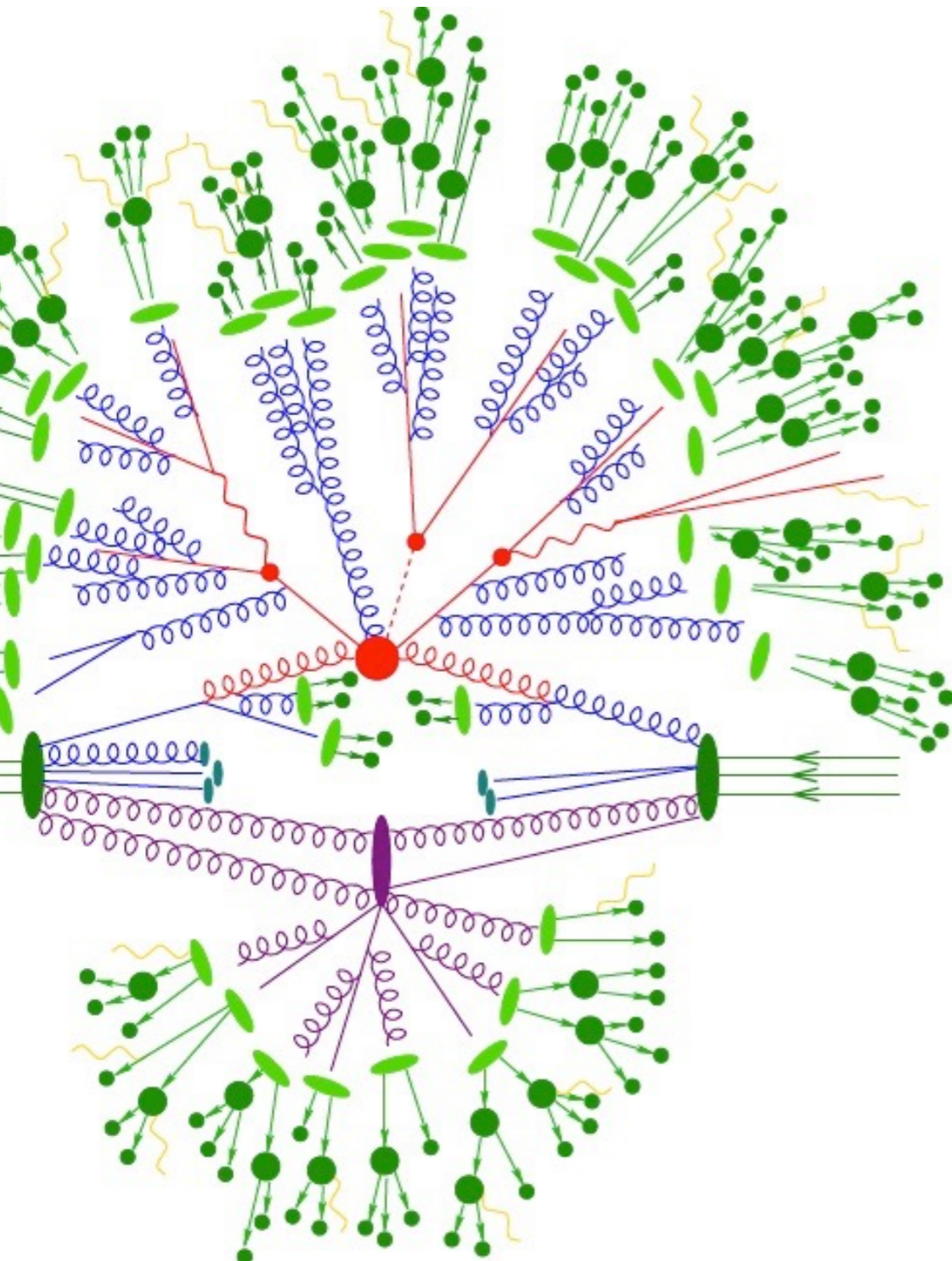
In some cases, we can extend the range of validity of the perturbative approach by doing  $\dots$  terms

Many conceptual and phenomenological advancements

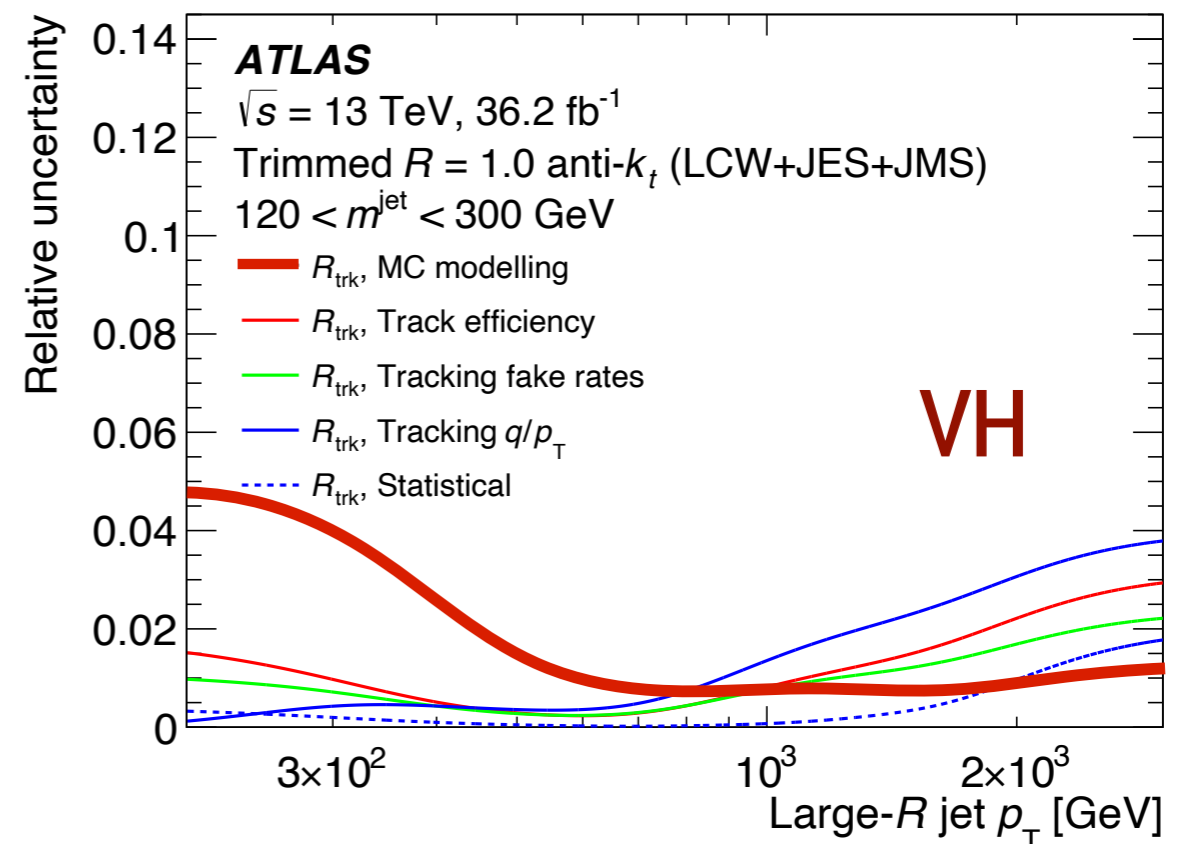
Higher logarithmic accuracy, next-to-leading power, non-global variables...



# From parton to hadrons: parton showers

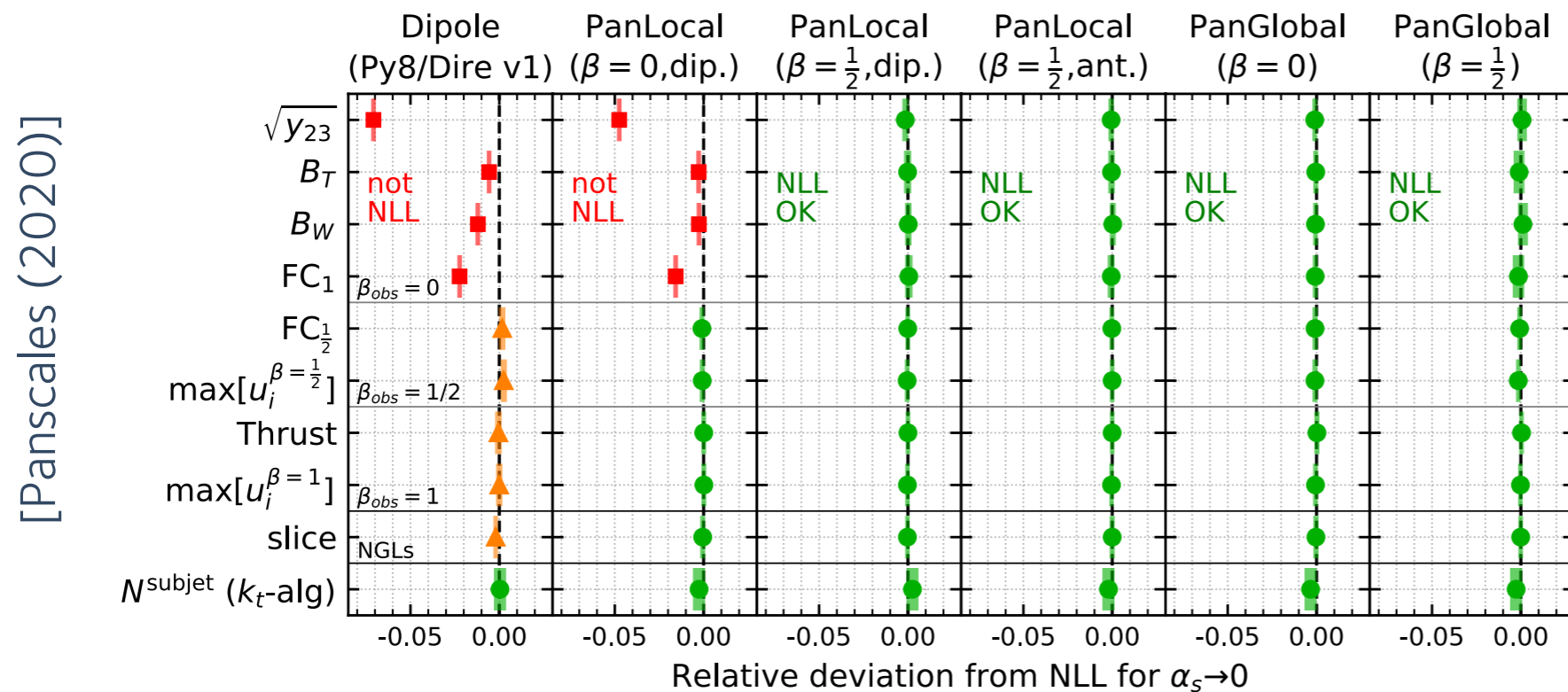


- In many cases, we need to connect high-energy scattering to detector reality
- Parton-shower MC, approximate treatment of many-body processes
  - -: lose precision
  - +: gain flexibility
- In many cases: leading TH systematics...



# From parton to hadrons: parton showers

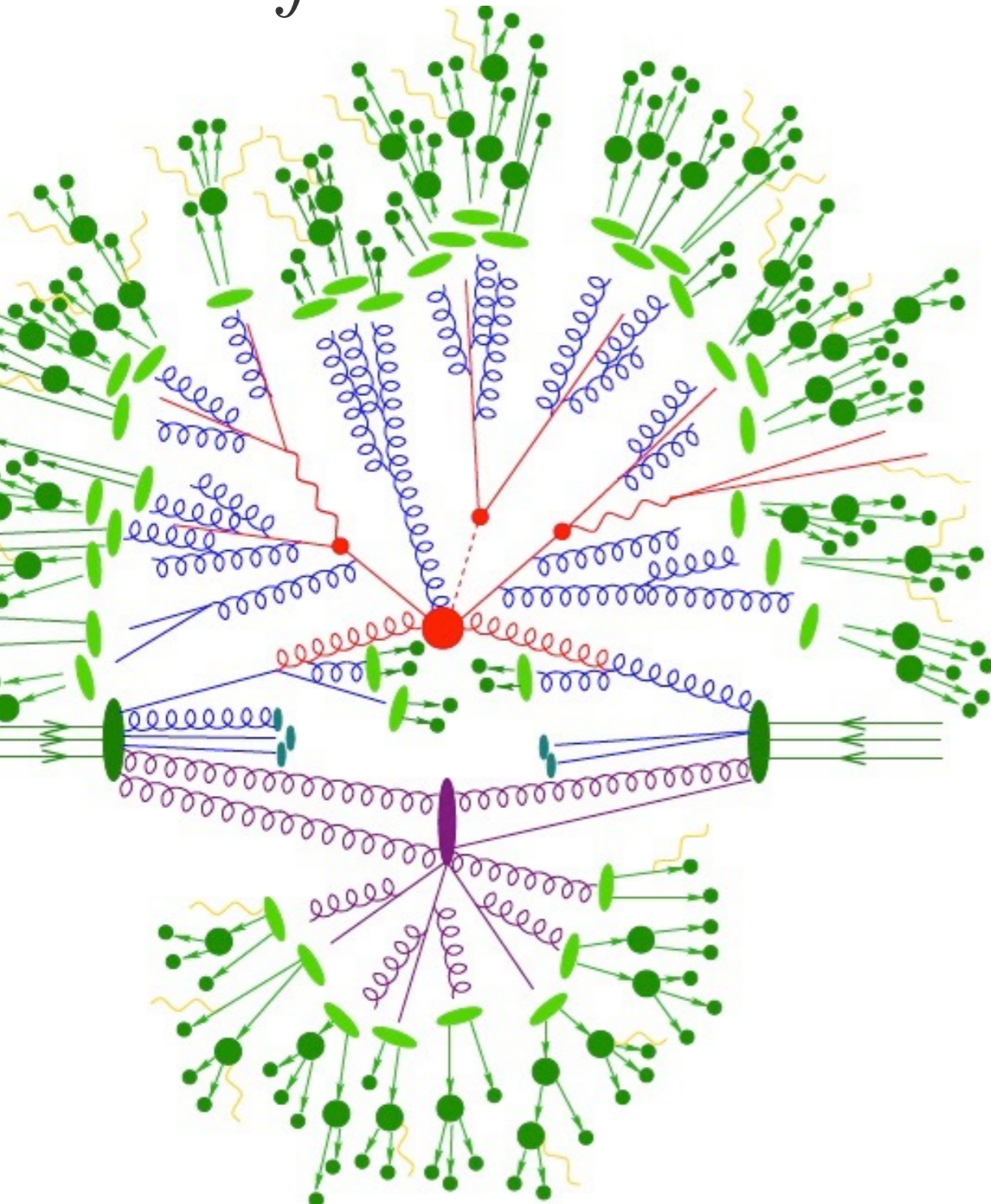
- Parton showers have two identities
  - Black boxes with enough handles, to accommodate for data features
  - Predictive tools
- Predictive tool: need to be reliable
  - Especially crucial in the ML world: virtually all the ML algorithms trained on PS
- Recent past: first attempts at making PS under theoretical control and systematically improvable!



First demonstrably  
“higher order” showers  
starting to appear

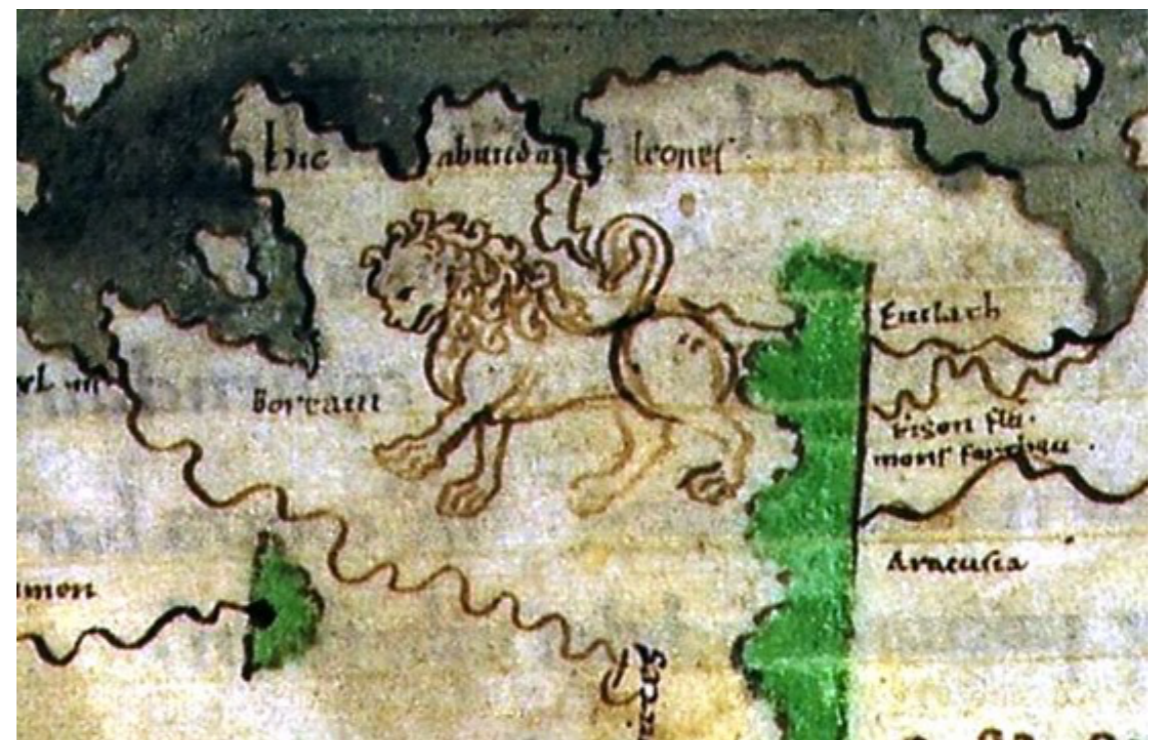
# Can we trust factorisation?

$$d\sigma = \int dx_1 dx_2 f(x_1) f(x_2) d\sigma_{\text{part}}(x_1, x_2) F_J (1 + \mathcal{O}(\Lambda_{\text{QCD}}/Q))$$



At the end, we cannot escape some contamination from soft physics

- $\Lambda_{\text{QCD}} \sim \text{GeV}$ ,  $Q \sim 100 \text{ GeV} \rightarrow$  can be 1% effect!
- Non-perturbative  $\rightarrow$  out of control





# Can we trust factorisation?

$$d\sigma = \int dx_1 dx_2 f(x_1) f(x_2) d\sigma_{\text{part}}(x_1, x_2) F_J (1 + \mathcal{O}(\Lambda_{\text{QCD}}^p / Q^p))$$

Can we at least establish the scaling?

In practice, a very big difference between  $p=1$  (problem) and  $p > 1$  (irrelevant)

- $e^+e^- \rightarrow$  hadrons:  $p \geq 4$
- For DIS: solid proof that  $p \geq 2$
- Hadron colliders:
  - for inclusive quantities (e.g. DY total xsec): leading NP corrections should have  $p=2$  (non-trivial!)
  - For more exclusive quantities: potential sources of linear power corrections.
  - Top, Jets are known to have linear power corrections. What about colour singlet?

# Can we trust factorisation?

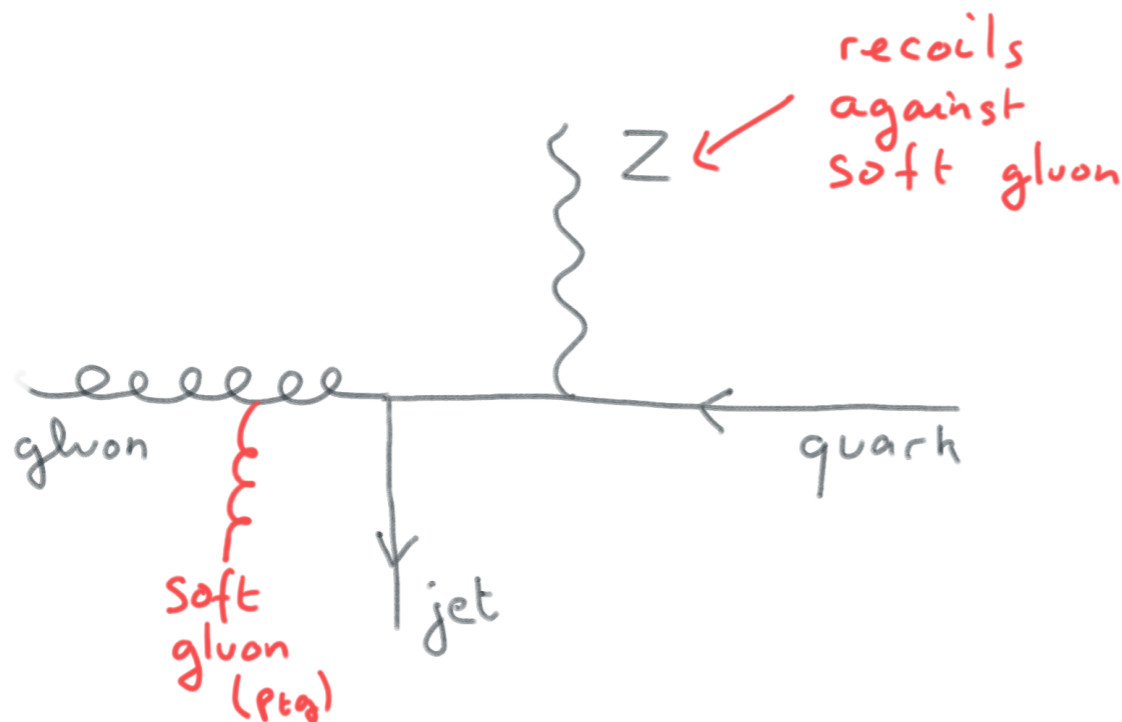
Mechanisms that could generate linear power corrections are there...

QCD power corrections  $\leftrightarrow$  sensitivity to IR physics

Basic idea: find good “probe” of the IR, and ask “can we generate  $p=1$  terms?”

E.g.: Z transverse momentum distribution (example from G.P. Salam)

[G.P. Salam]



$$\sigma \sim \int \frac{dp_{\perp}}{p_{\perp}} \alpha_s(p_{\perp})$$

Because of azimuthally asymmetric color flow: linear terms could be generated

Integrate over soft d.o.f.  $\rightarrow$  NP

# Beyond pQCD

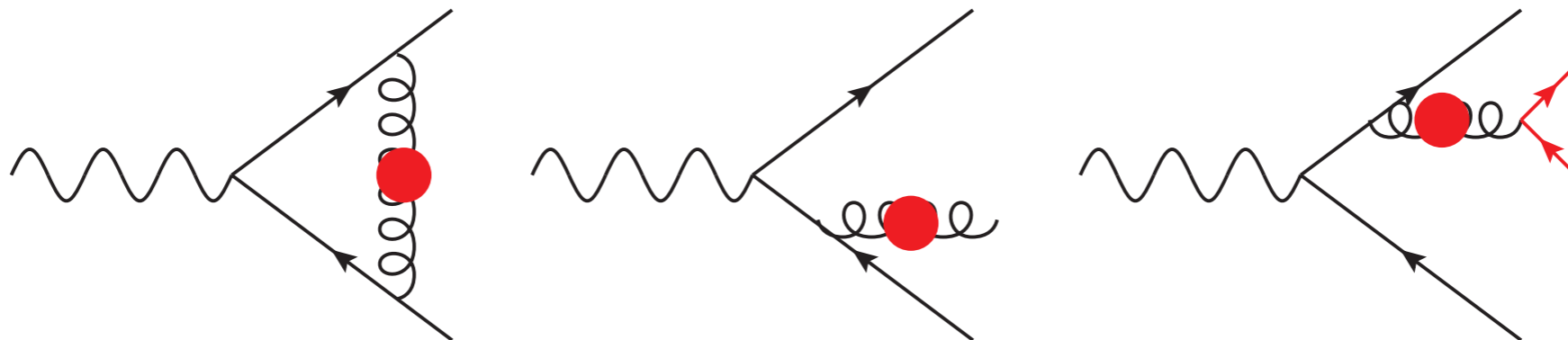
The obvious problem: at colliders, we cannot deal with QCD non-perturbatively

However: we know one source of NP that “creeps” into perturbative results.

When integrating over soft momenta  $\rightarrow$  Landau pole ambiguity

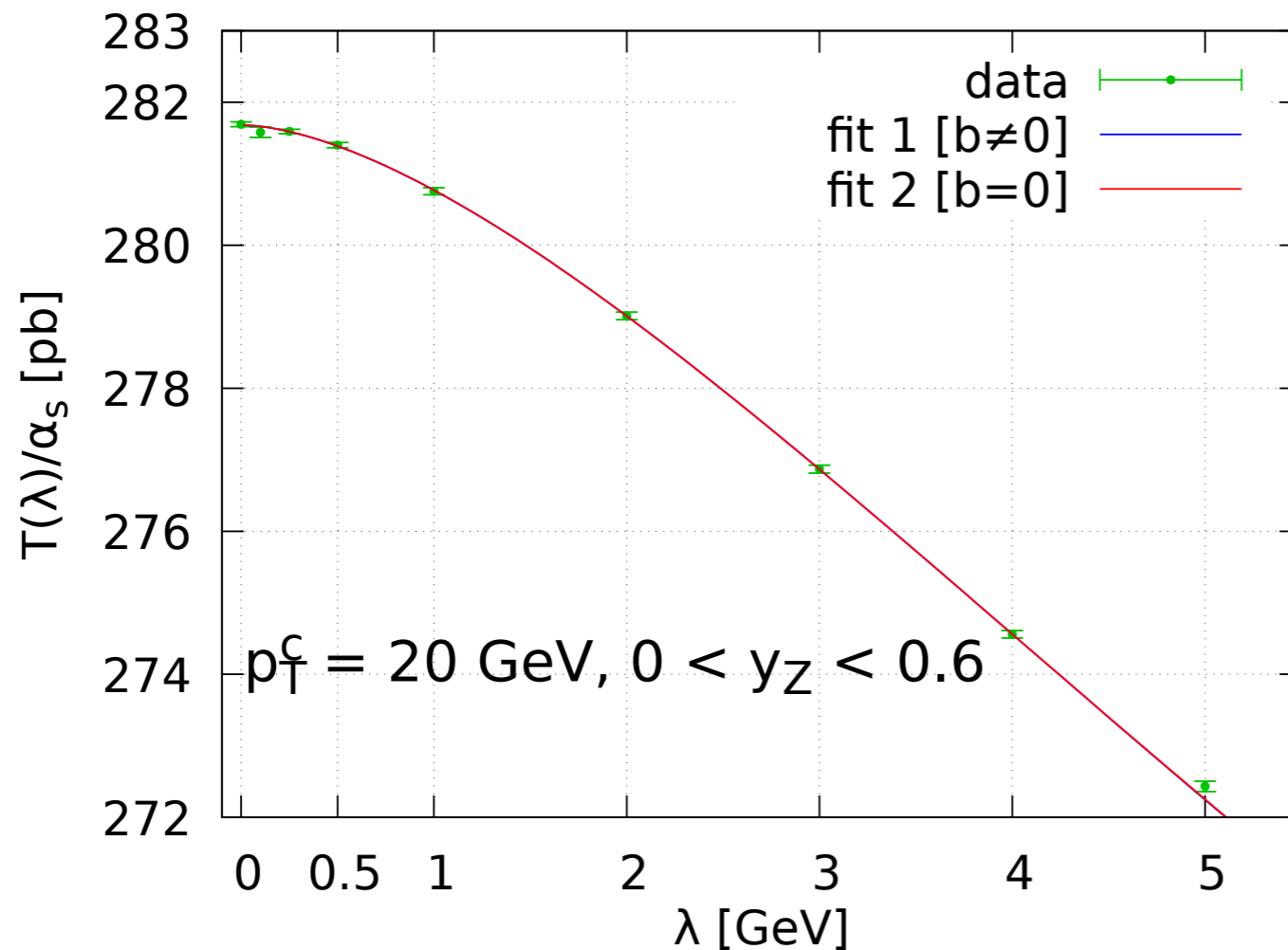
Lead to divergent behaviour of perturbative expansion  $\rightarrow$  can get info from PT theory itself!

Renormalons, calculations in the  $n_f \rightarrow -\infty$  limit



# Z $p_t$ and linear renormalons

[Ferrario Ravasio, Limatola, Nason (2020)]: Numerical study based on renormalon calculus



Compute Z  $p_t$  with massive gluons, and extrapolate to

$$m_g \rightarrow 0$$

$$f(\lambda) = a \left[ 1 + b \left( \frac{\lambda}{p_T^c} \right) + c \left( \frac{\lambda}{p_T^c} \right)^2 \log^2 \left( \frac{\lambda}{p_T^c} \right) + d \left( \frac{\lambda}{p_T^c} \right)^2 \log \left( \frac{\lambda}{p_T^c} \right) \right]$$

Fit consistent with  $b=0 \rightarrow$  no linear power corrections

# $Z_{p_t}$ and linear renormalons

[Ferrario Ravasio, Limatola, Nason (2020)]: Numerical study based on renormalon calculus

Very recently: towards a theoretical understanding.

“No linear power corrections for observables inclusive w.r.t. QCD radiation”

Towards strong foundations for the precision program

[FC, Ferrario Ravasio, Limatola, Melnikov, Nason (2021)]

is consistent with  $\mathcal{O}(1)$  no linear power corrections

# Conclusions and outlook

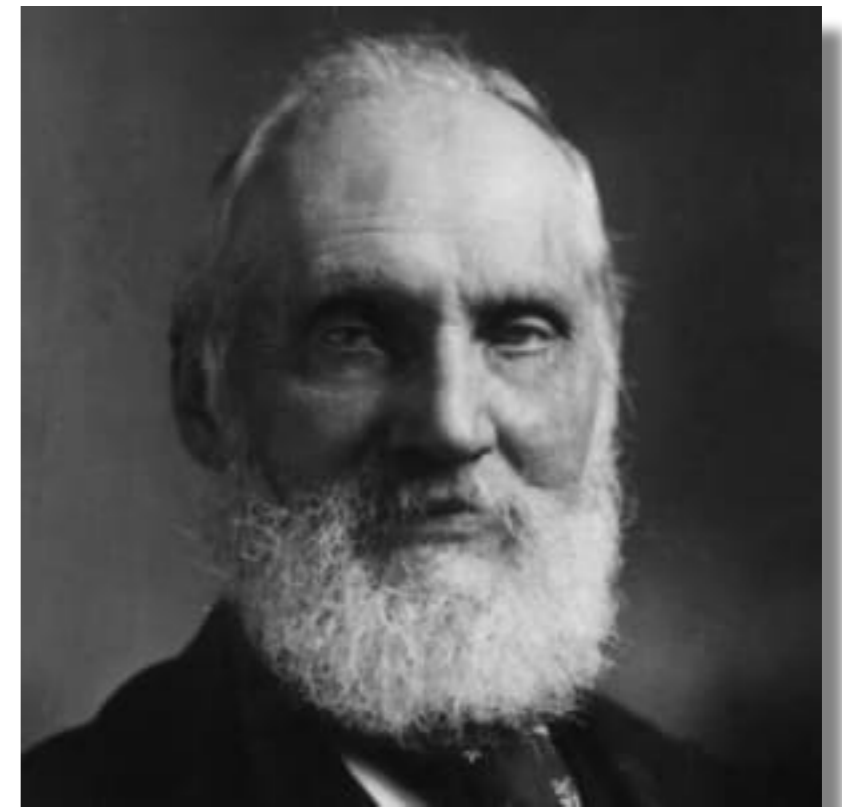
- Progress in precision QCD phenomenology keeps proceeding at a remarkable pace
  - ❖  $N^3$ LO, complex NNLO, QCD-EW, EW...
  - ❖ More and more elaborate resummations
  - ❖ Parton shower...
  - ❖ Computational tools ( $\rightarrow$  ingredients for  $N^3$ LL resummation)
  - ❖ SM/BSM interplay: EFTs...
  - ❖ ML to extract the most from data
- This is necessary but not sufficient for physics at the few percent. Many unexpected issues that keep popping up
- A better understanding of NP corrections may be required
- Future ahead: not only computations. Very interesting analysis, from hardcore pheno to subtle QFT...

# Precision physics at the LHC and beyond

With the Higgs, the Standard Model may be a complete theory. What is the point of looking at the next decimal digit?

“physics is complete, all we need to do is to measure some known quantities to a great degree of precision”

Lord Kelvin, ca 1900



5 years later: special relativity.

Less than 30 years later: quantum mechanics, general relativity



Thank you very much for your attention!