

Dark Matter

Ken Van Tilburg

CCPP @ New York University | CCA @ Flatiron Institute

Lake Louise Winter Institute — Feb 21, 2022

[Hubble Ultra Deep Field]

Dark Matter

A vast field of galaxies, including spirals, ellipticals, and irregular shapes, scattered across a dark cosmic background. The galaxies are in various colors, including yellow, blue, and purple, and some show prominent spiral arms.

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Not The Outline

Every dark matter theory and experiment

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“... a wealth of information creates a poverty of attention.” —Herbert A Simon

Not The Outline

Every dark matter theory and experiment

“... a wealth of information creates a poverty of attention.” —Herbert A Simon (1971)

The Outline

Almost no dark matter theory nor experiment

The Outline

The Outline

How does dark matter fit into theoretical particle physics?

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How does dark matter fit into theoretical particle physics?

↳ a serious question mark

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How does dark matter fit into theoretical particle physics?

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The evidence for dark matter!

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General principles of precision-frontier dark matter detection

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How does dark matter fit into theoretical particle physics?

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The evidence for dark matter!

↳ not a question mark

A motivation “metric” for dark matter theories

↳ a guide for the first question

General principles of precision-frontier dark matter detection

↳ something I know something about

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The Central “Problem” of Fundamental Physics

Standard Model of cosmology and particle physics accurately describes* every known experiment and observation to the measured and calculated precision

theoretical frontiers:

mathematical structures | theory breakdown | parametric puzzles | computational precision

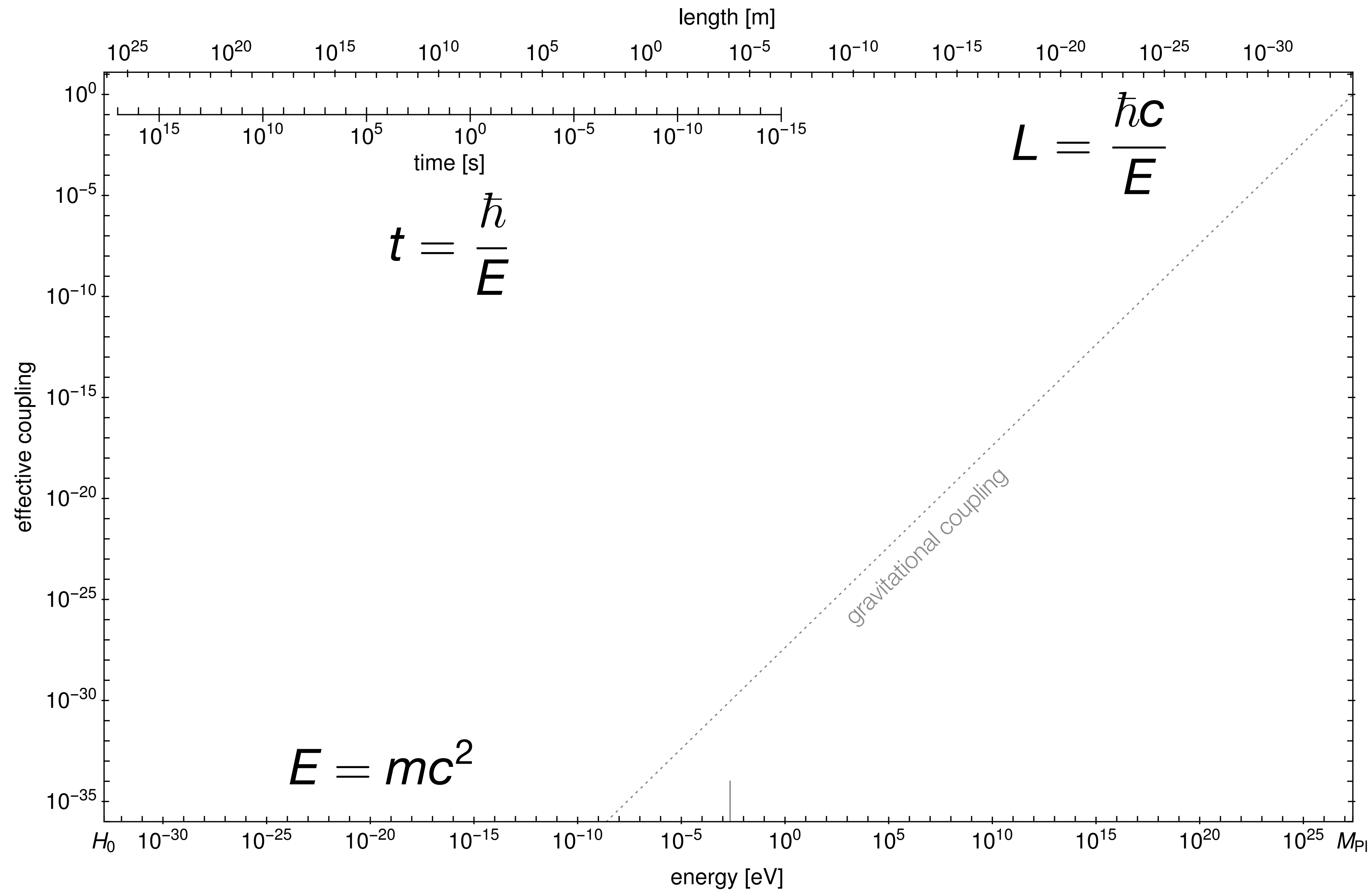
experimental frontiers:

high-energy | cosmic | intensity | precision

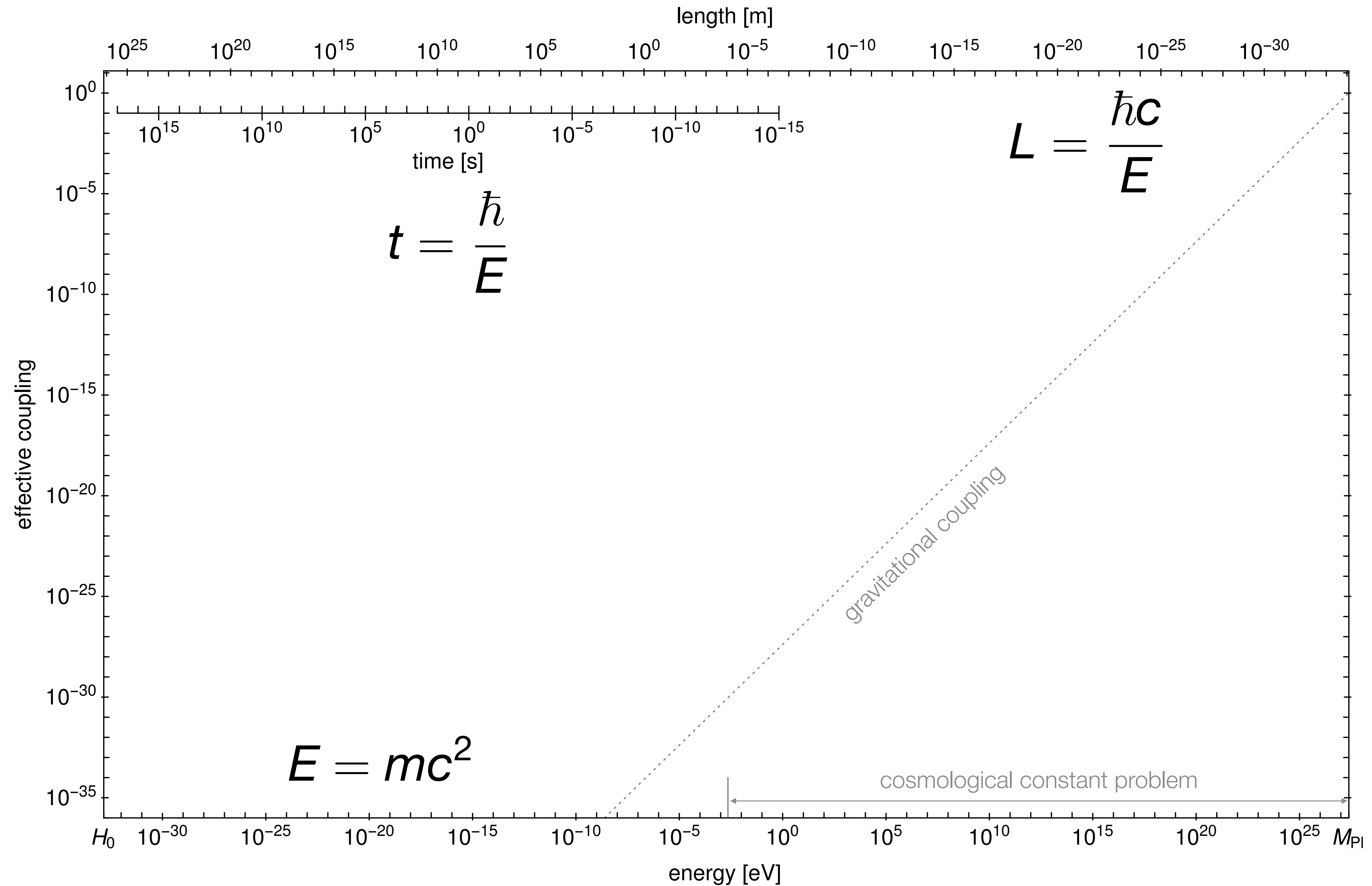
*parametrized unknowns:

dark matter | neutrino masses | baryon asymmetry | inflation

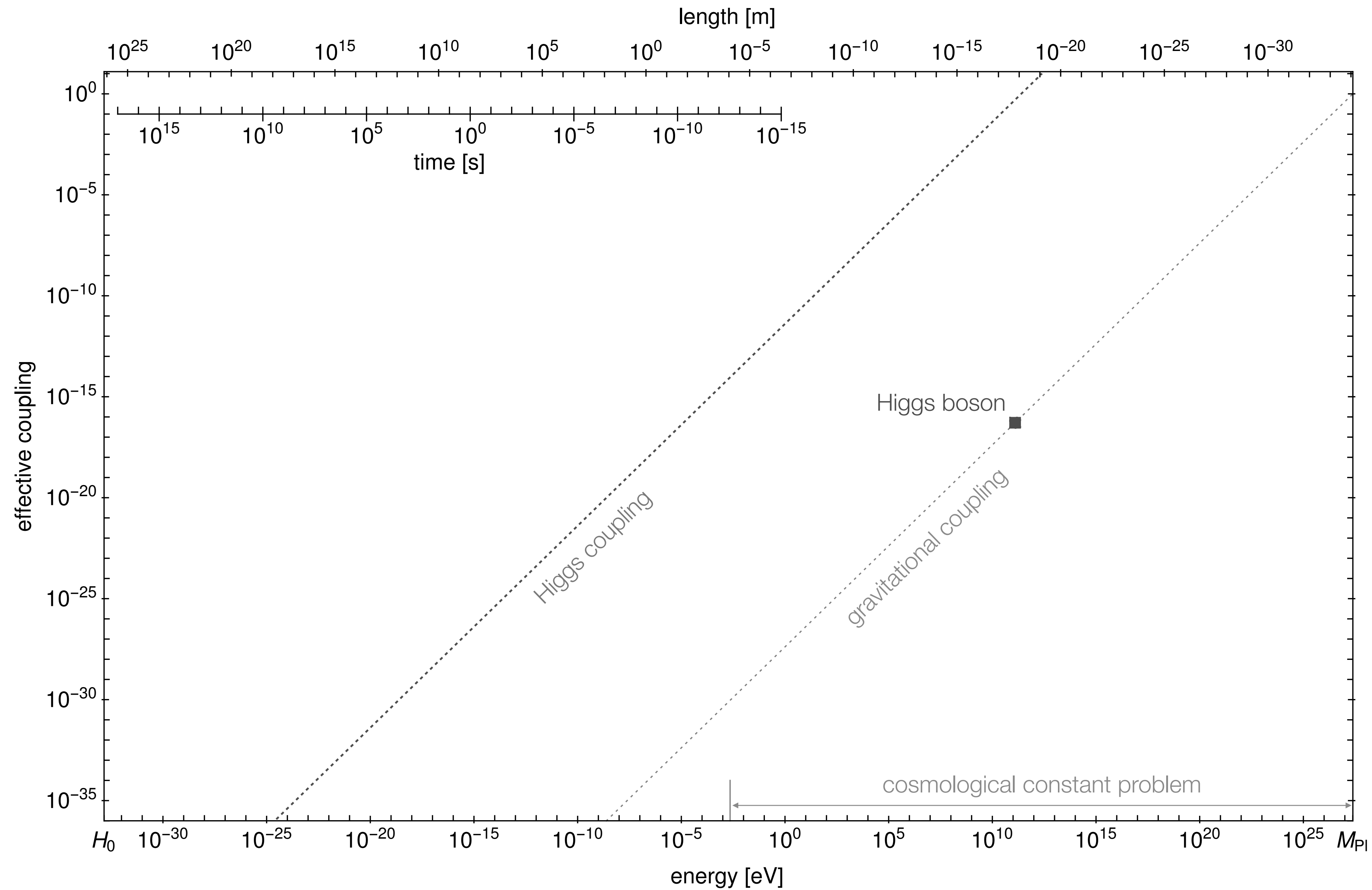
Scales in the Standard Model and Beyond



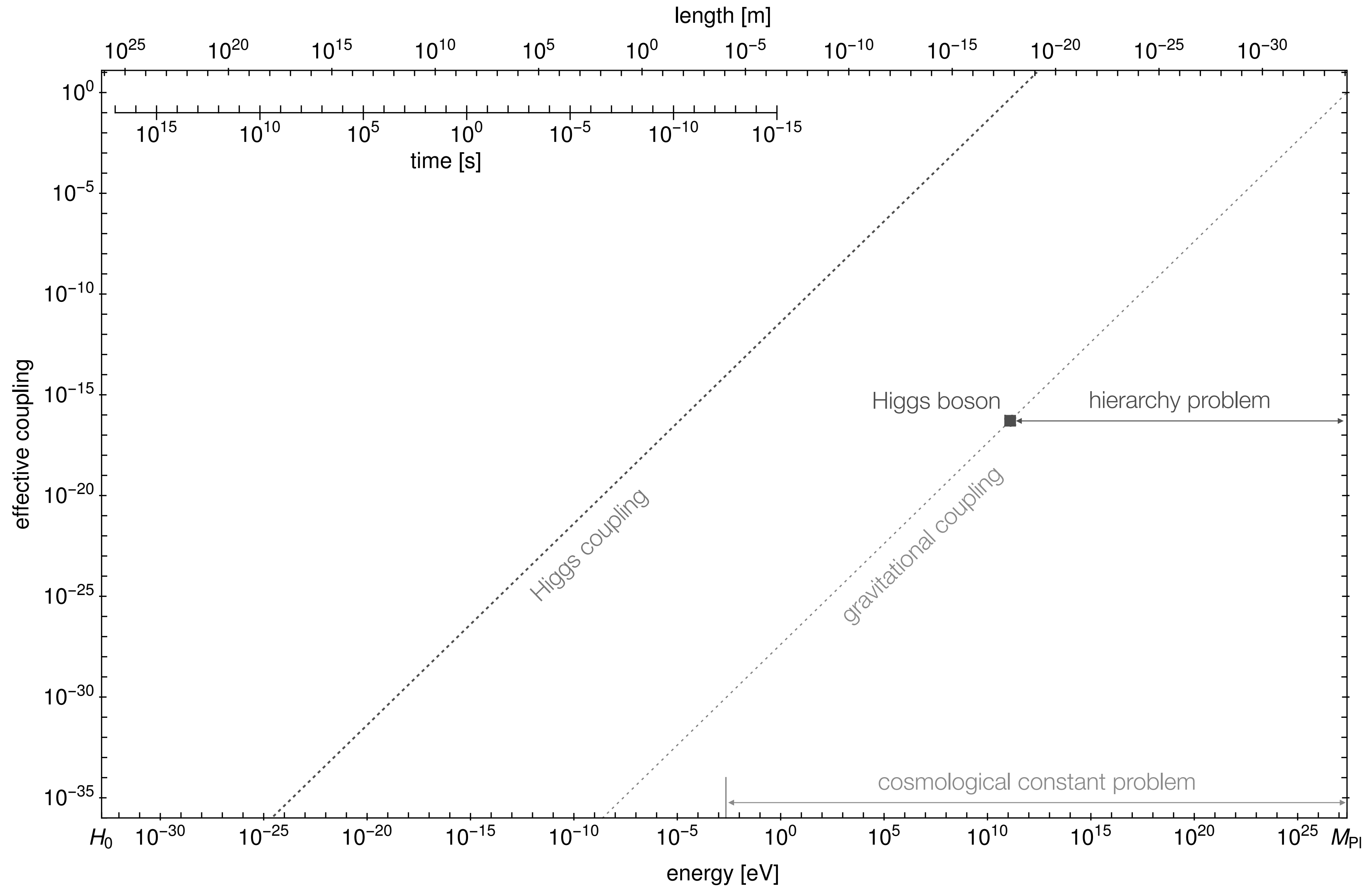
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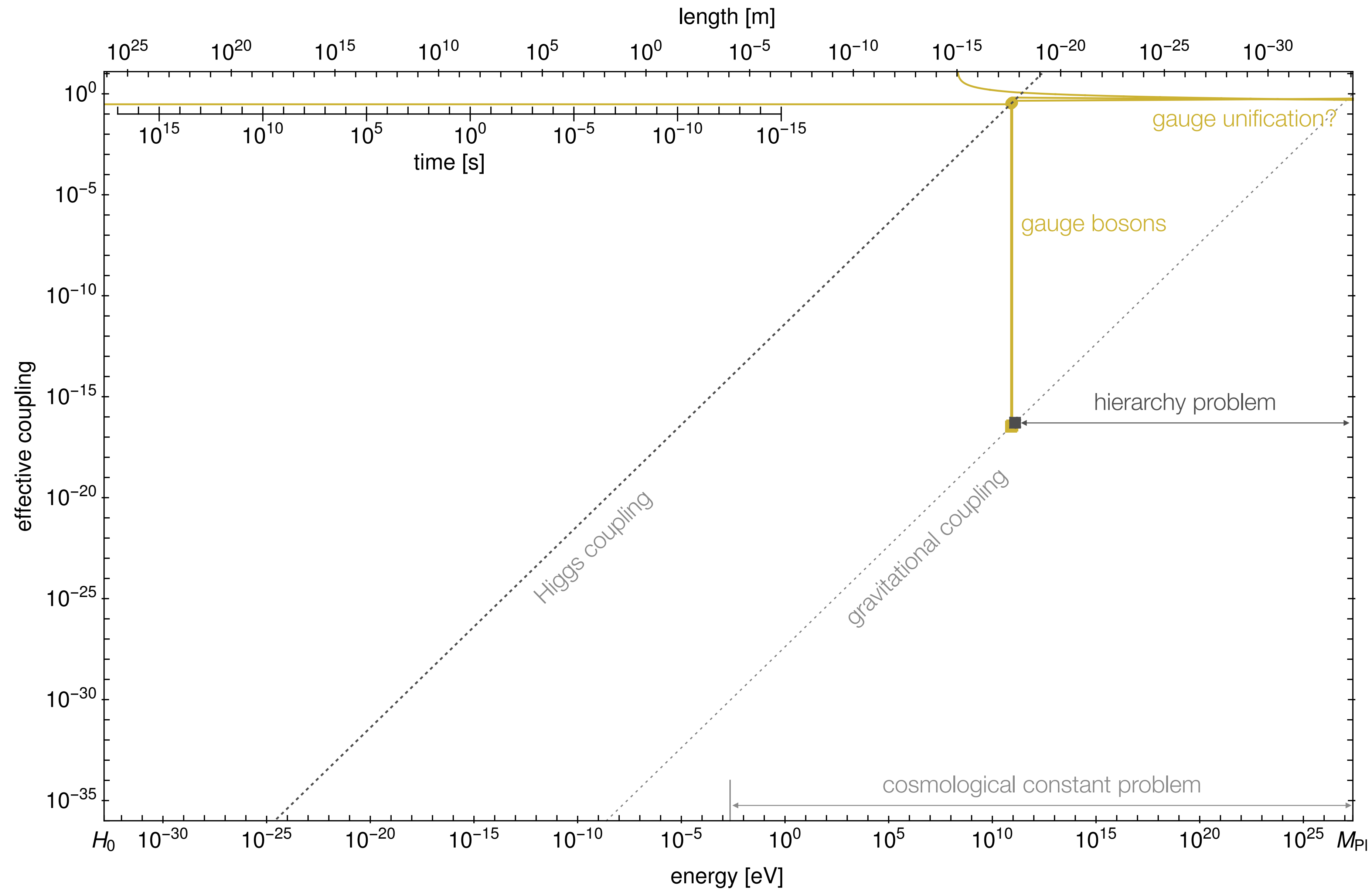
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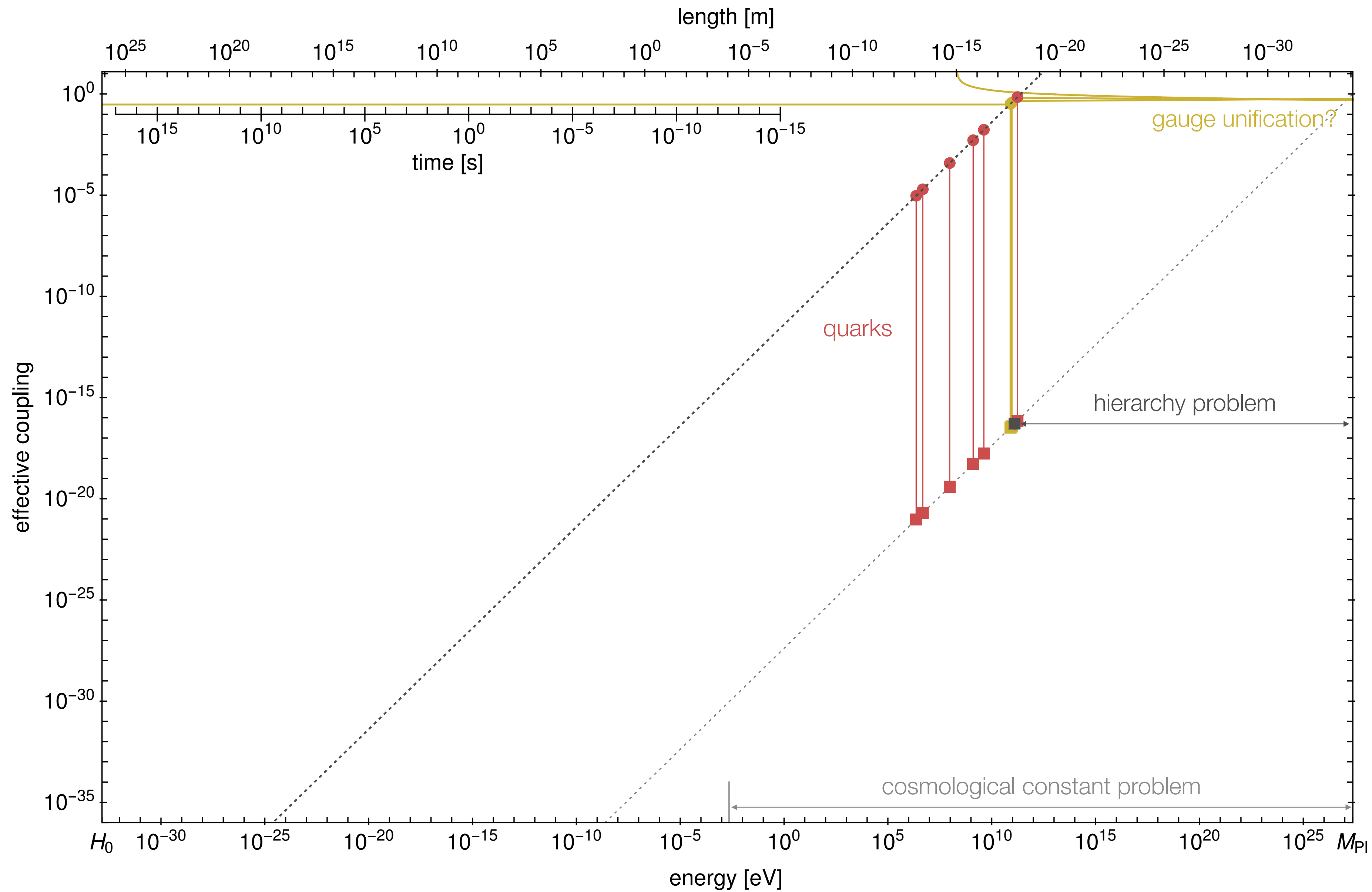
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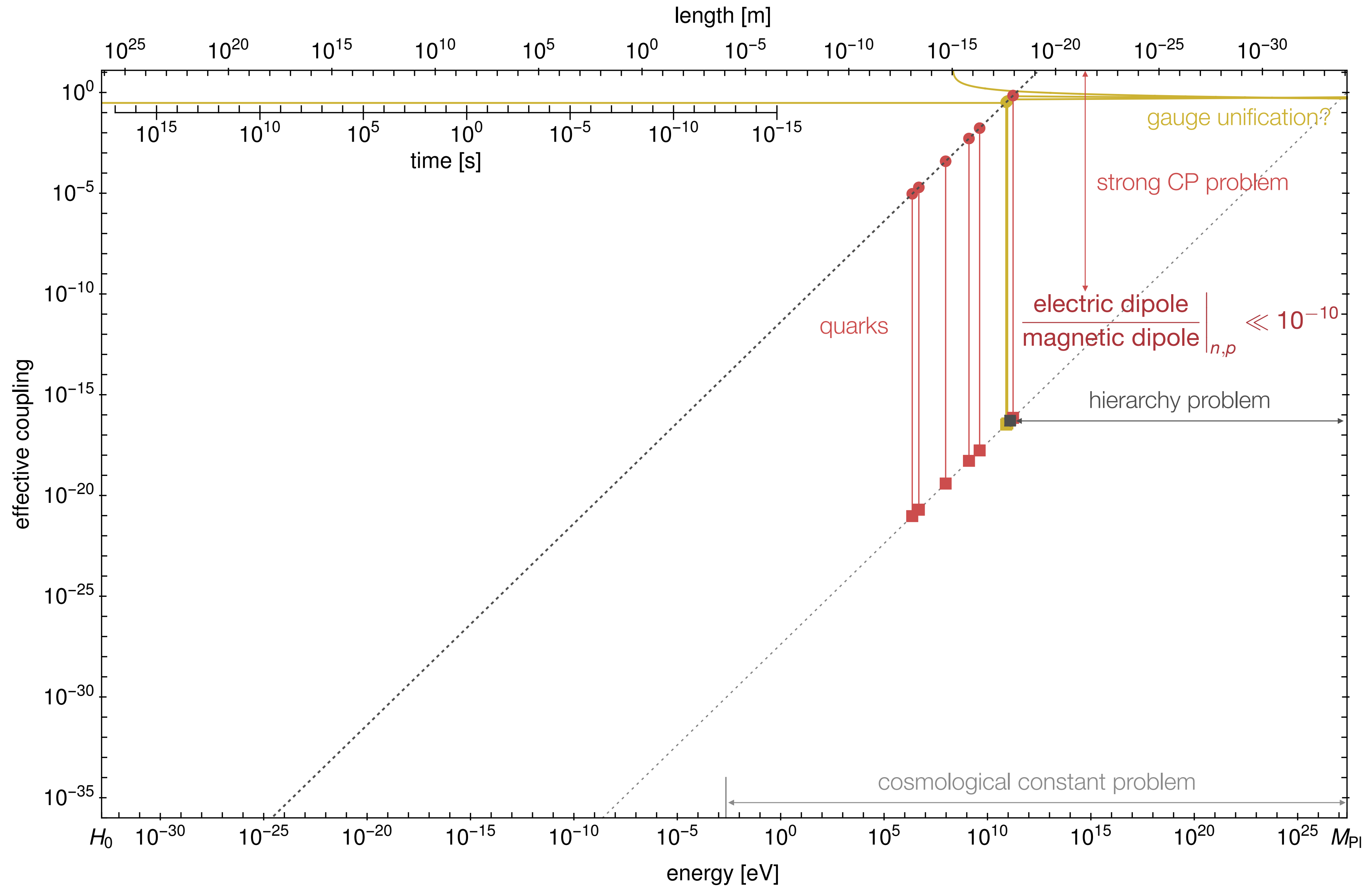
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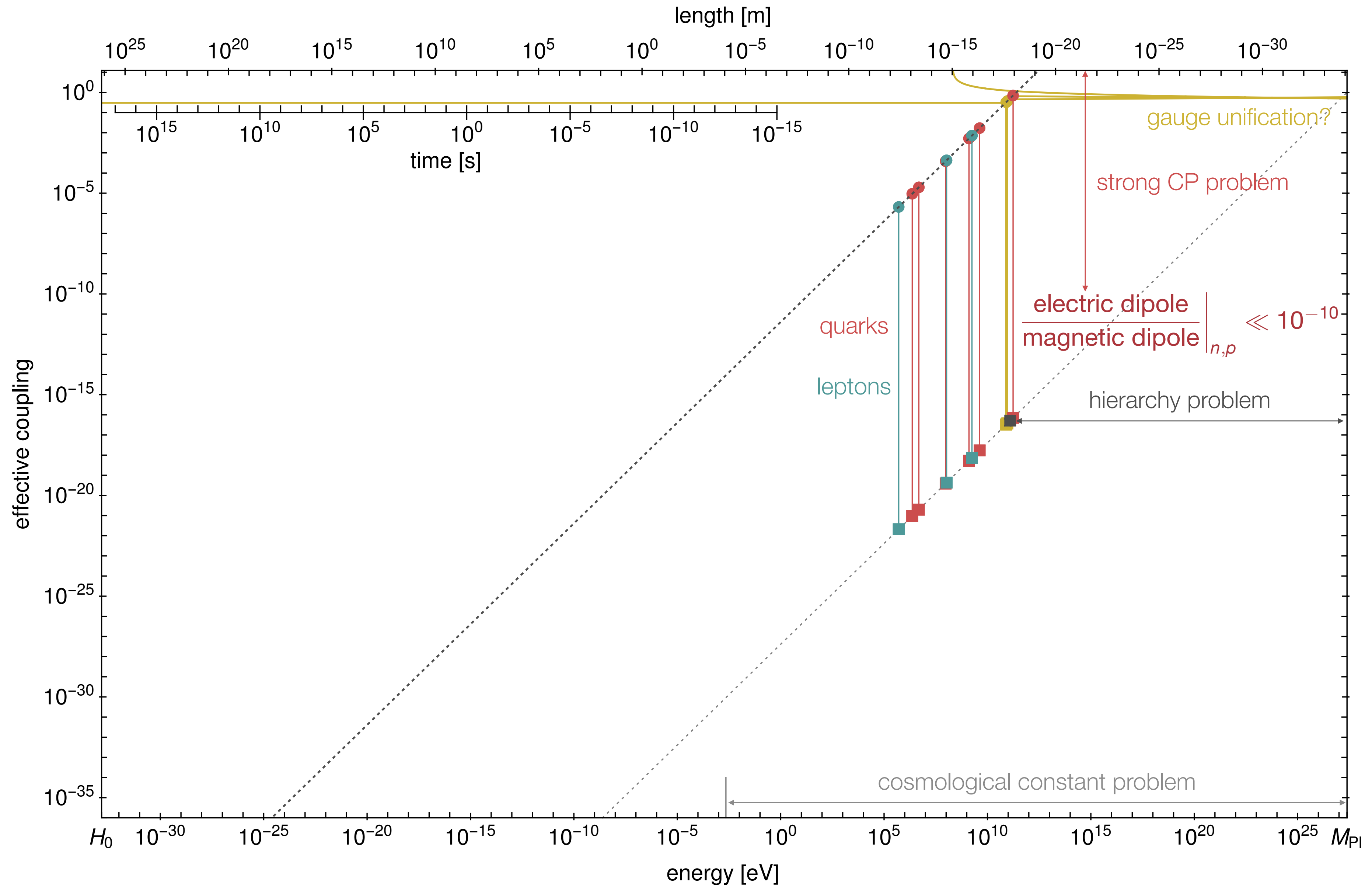
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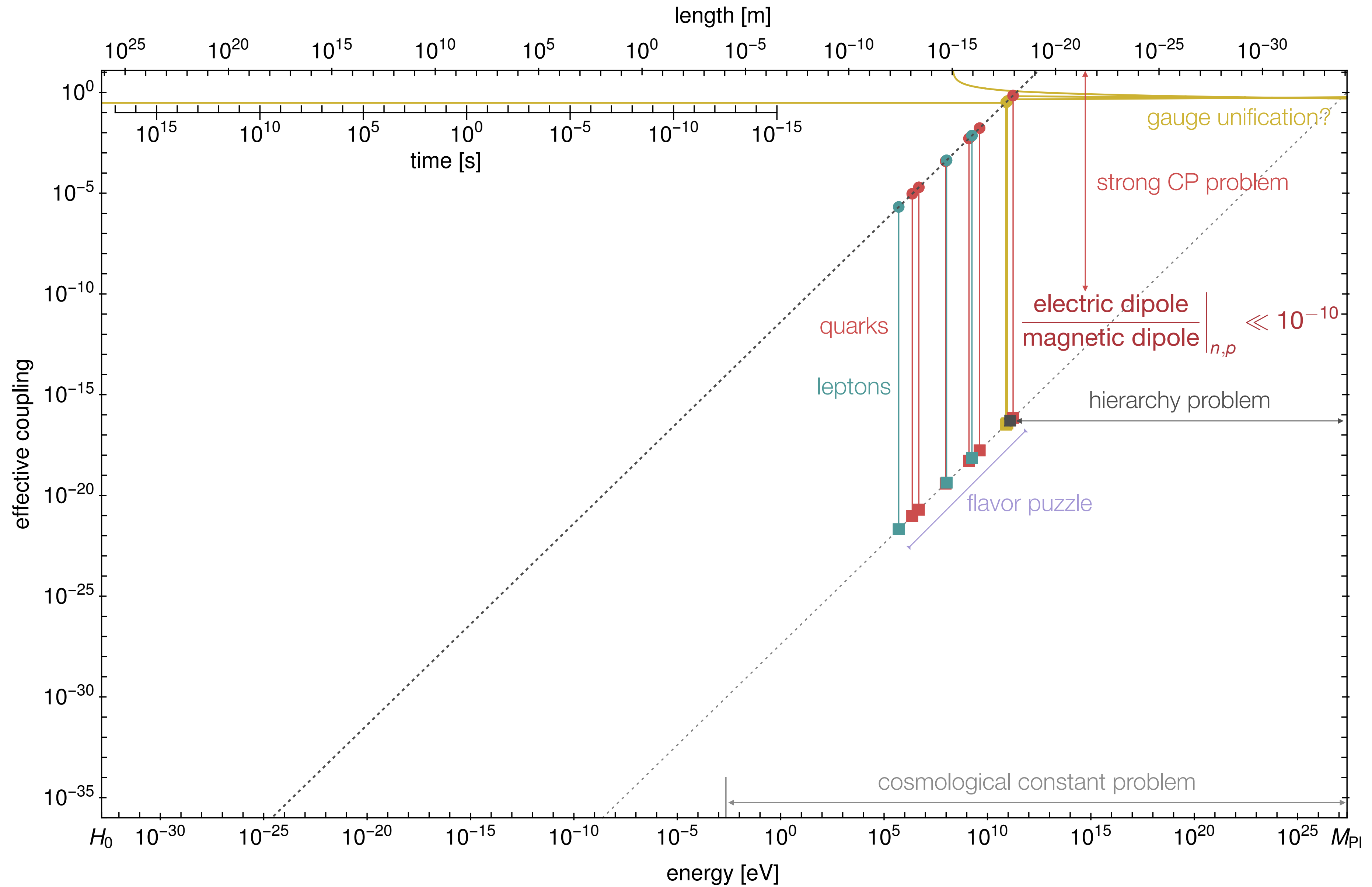
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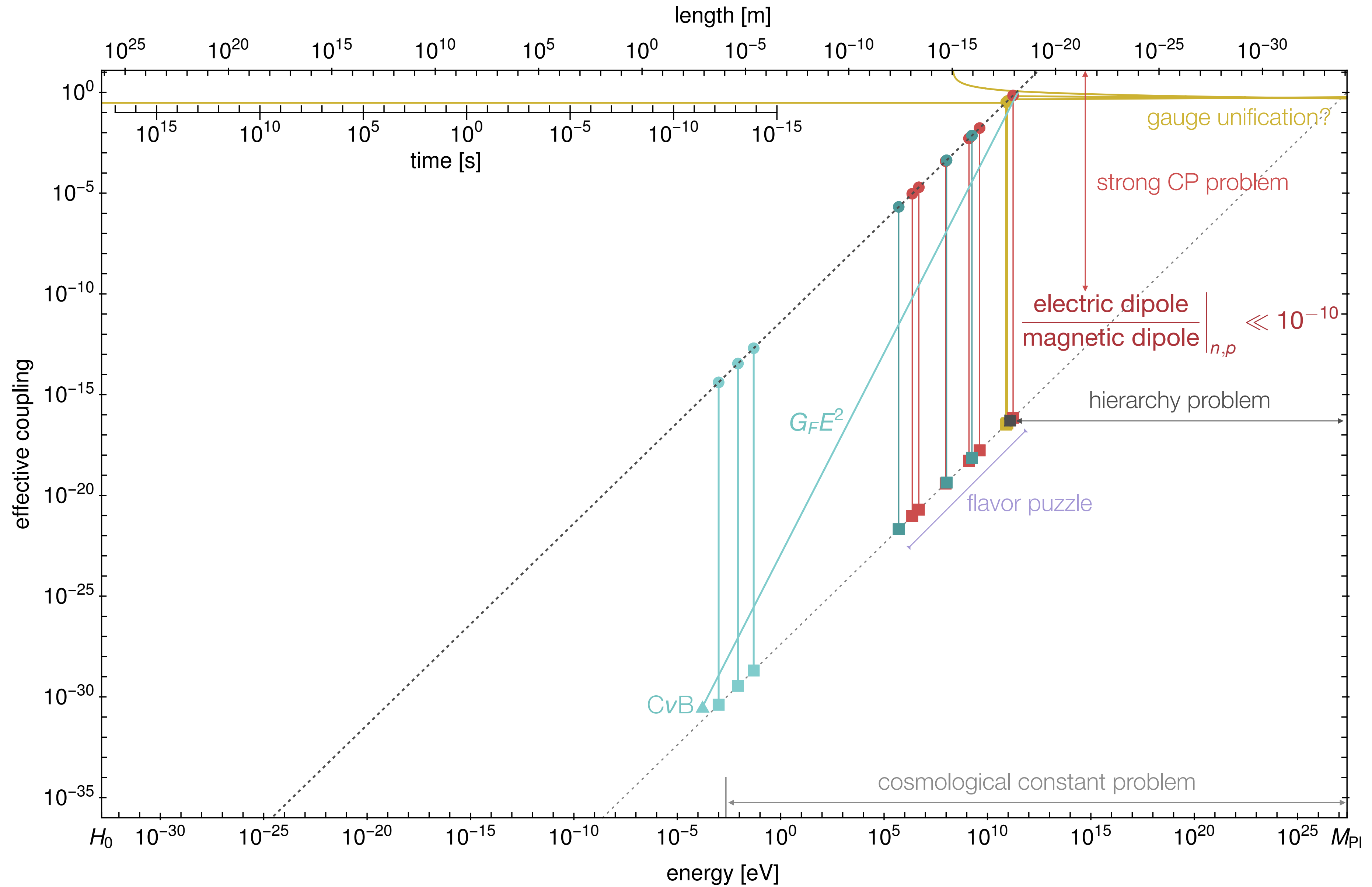
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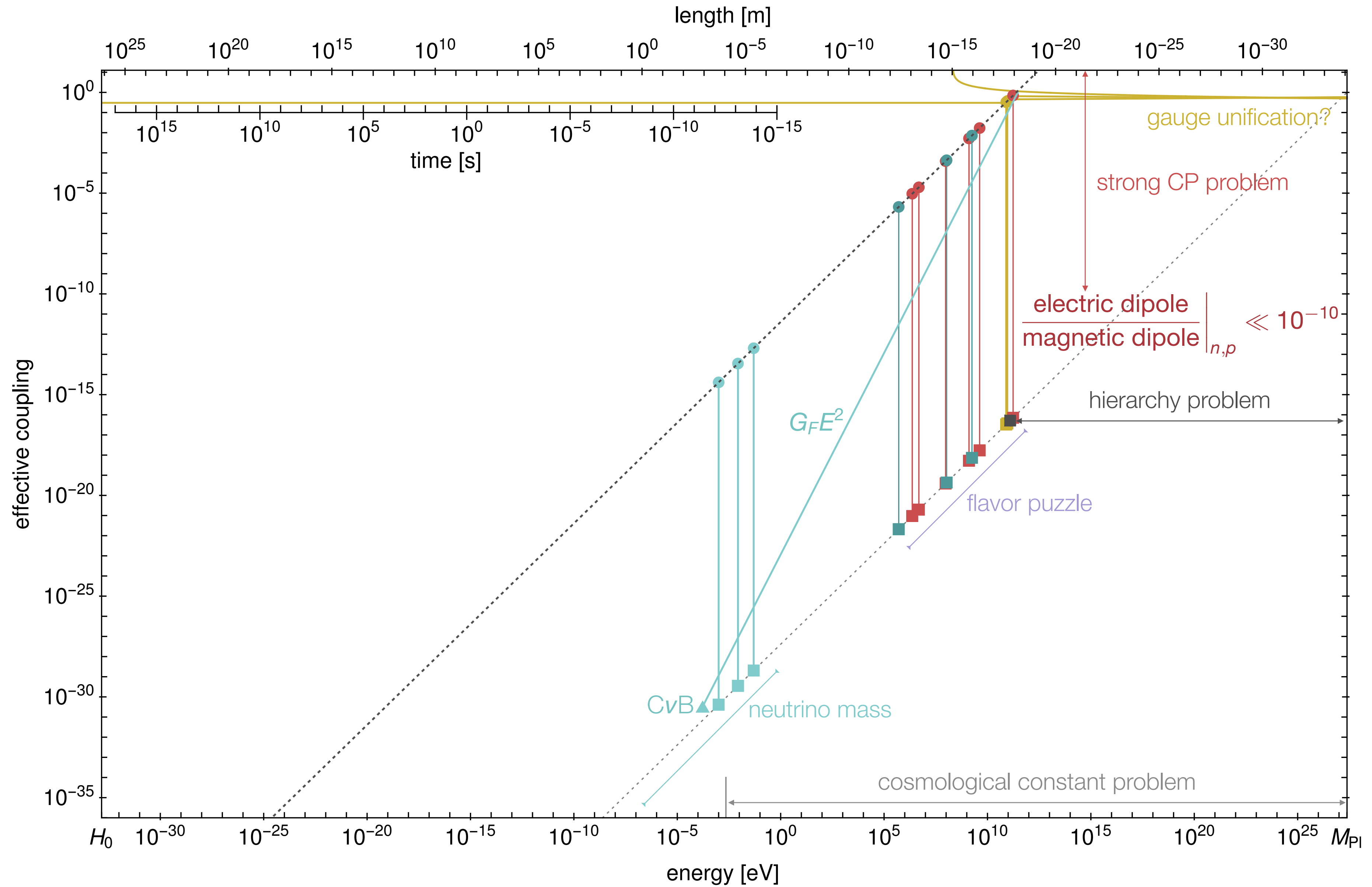
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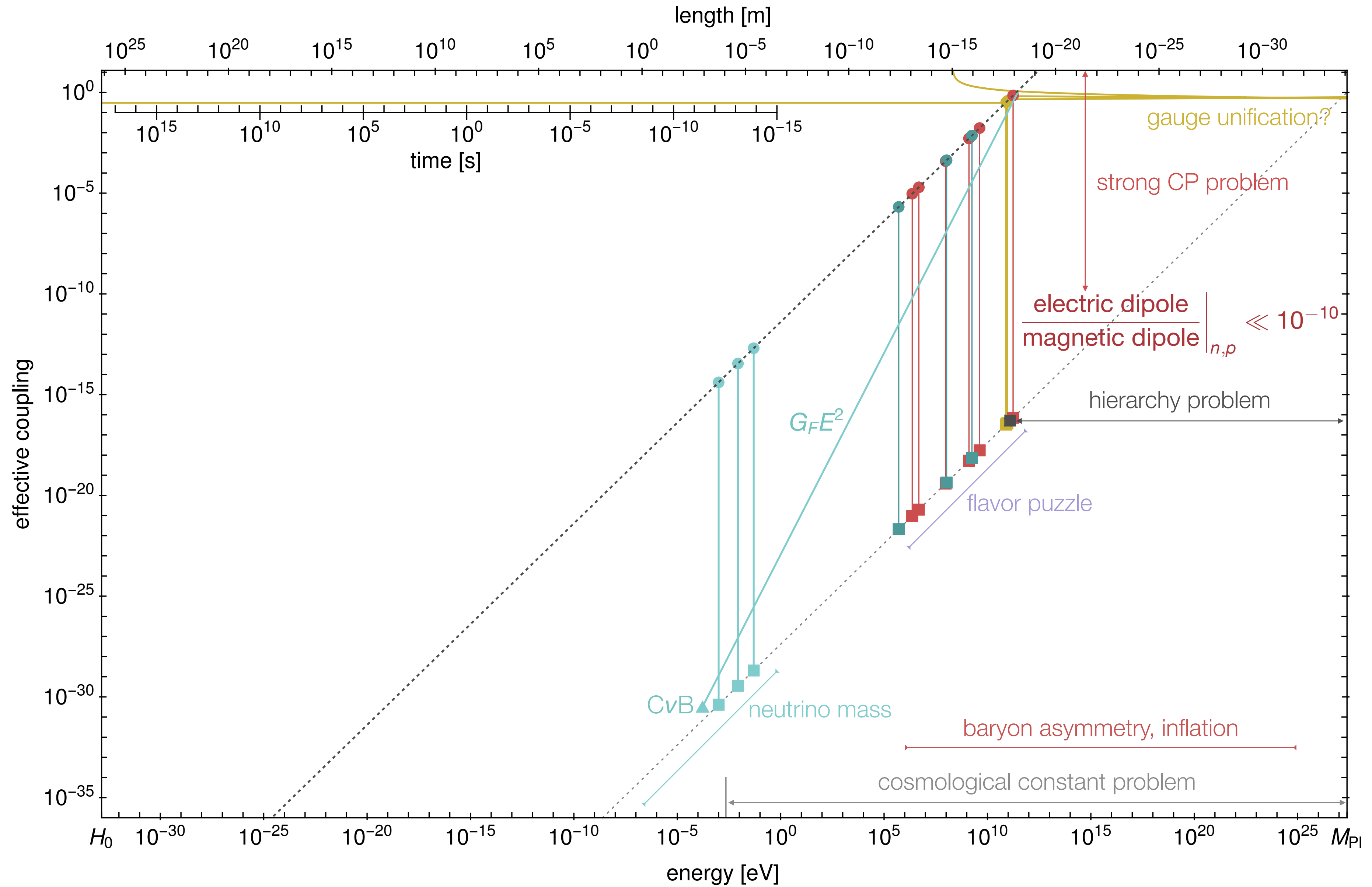
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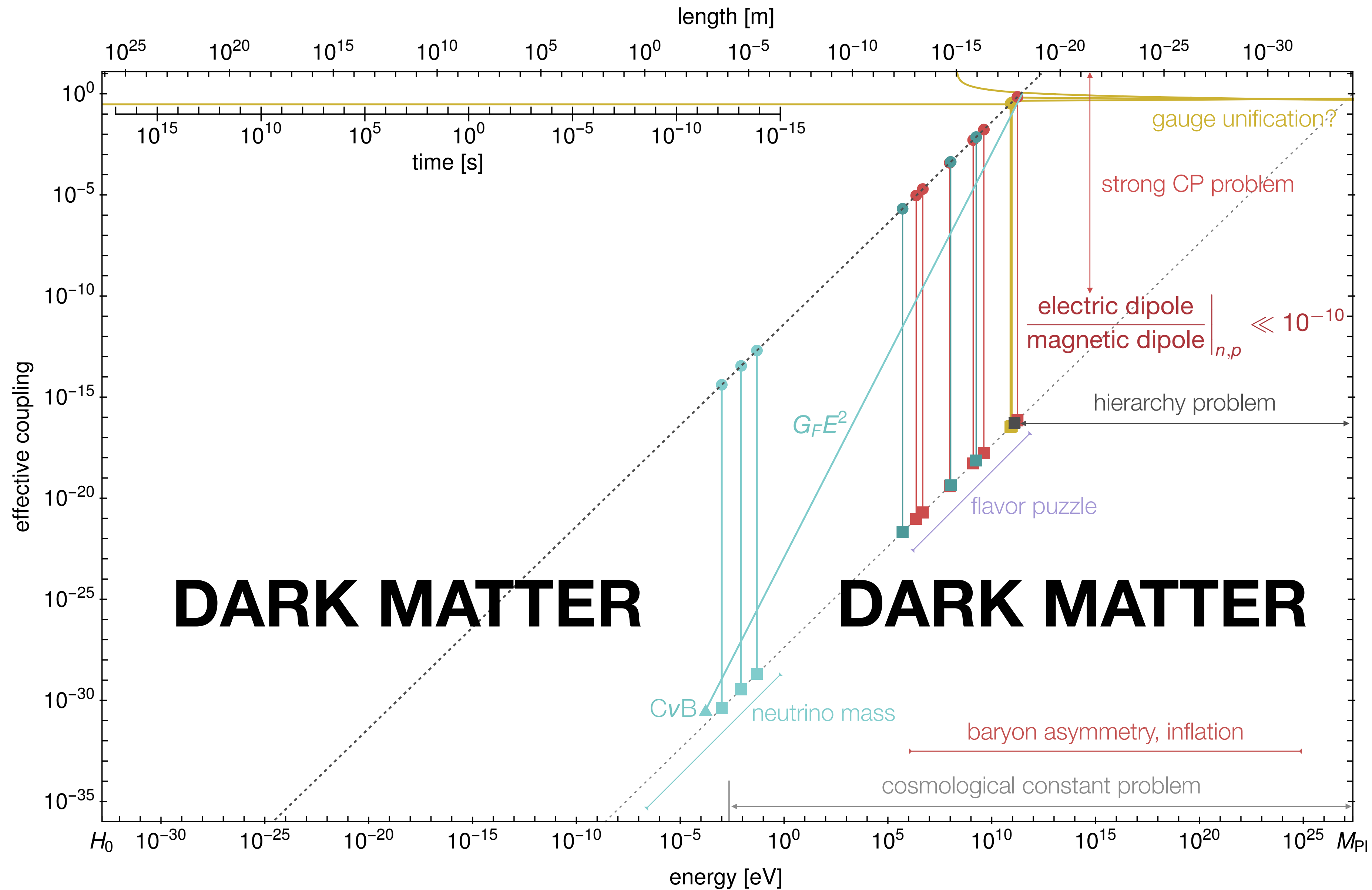
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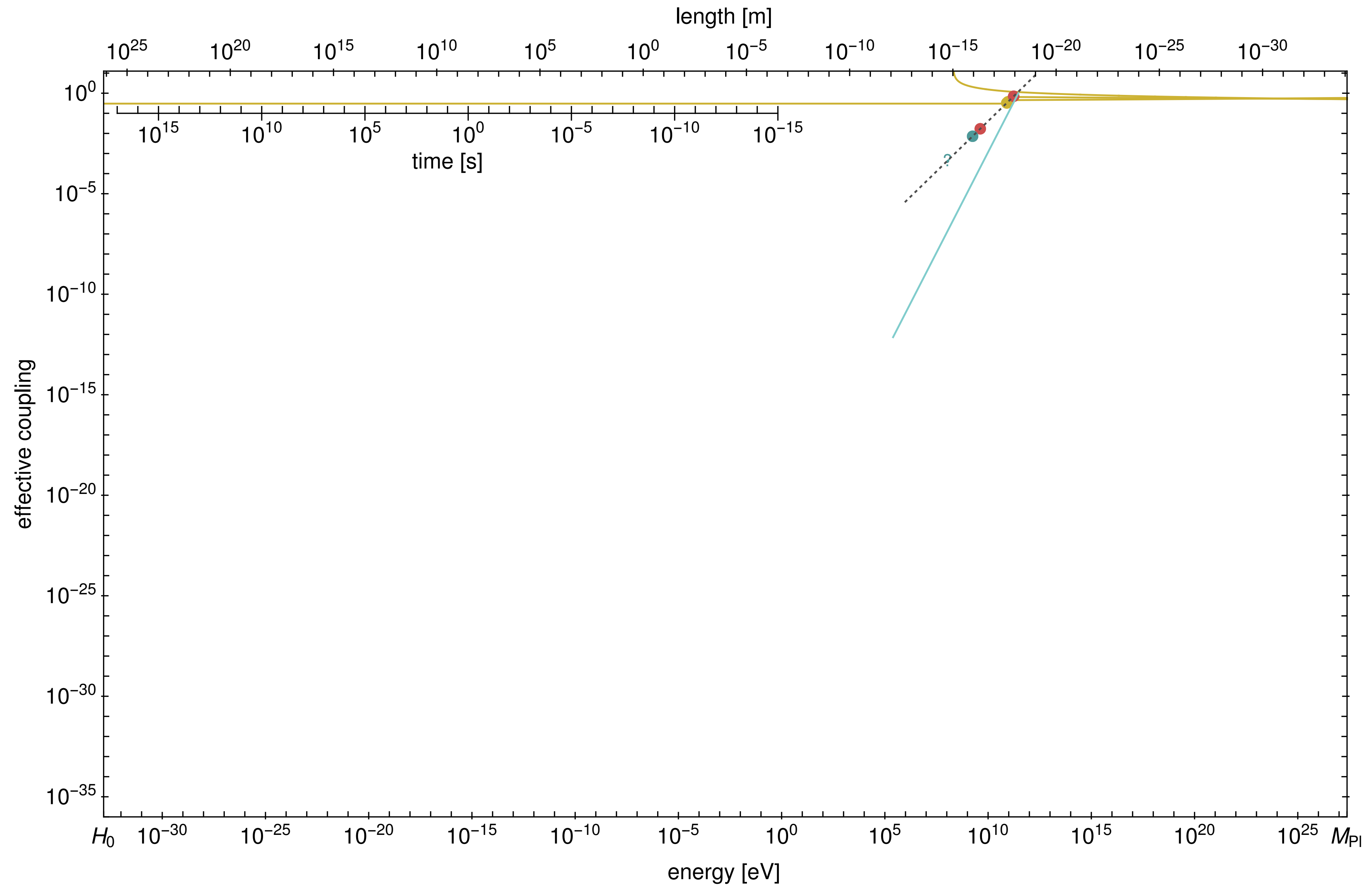
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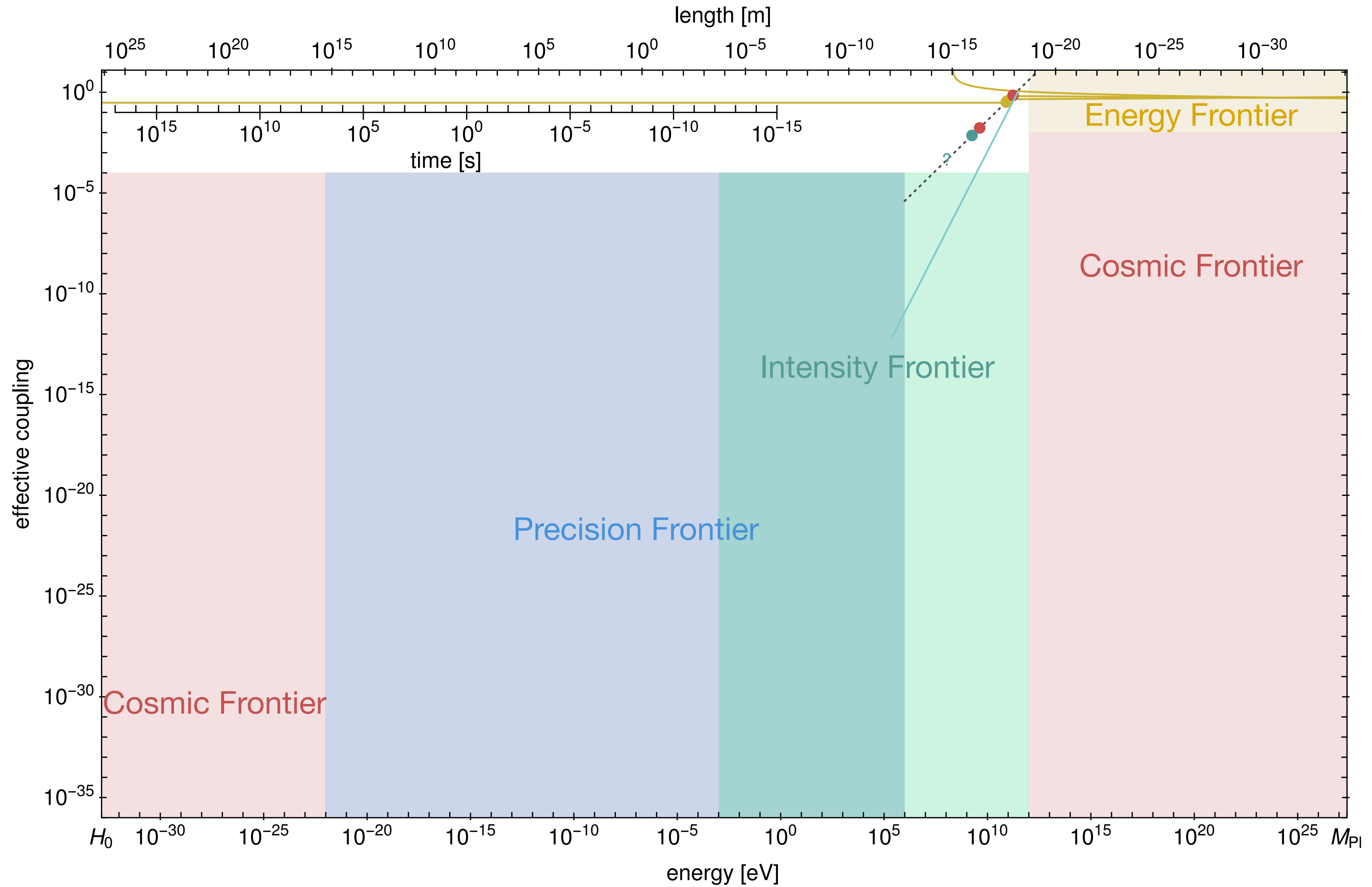
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New Physics Frontiers



New Physics Frontiers



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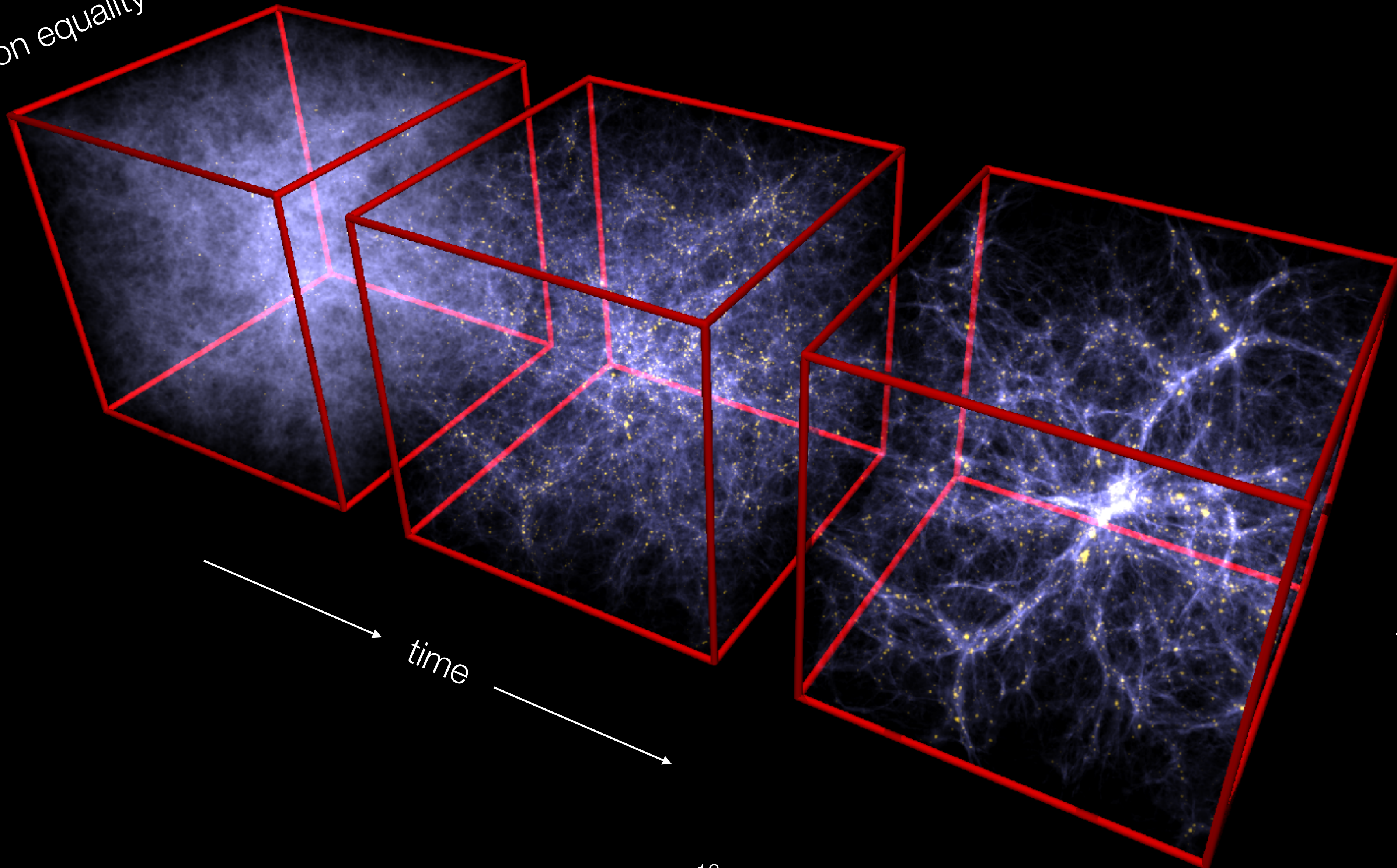
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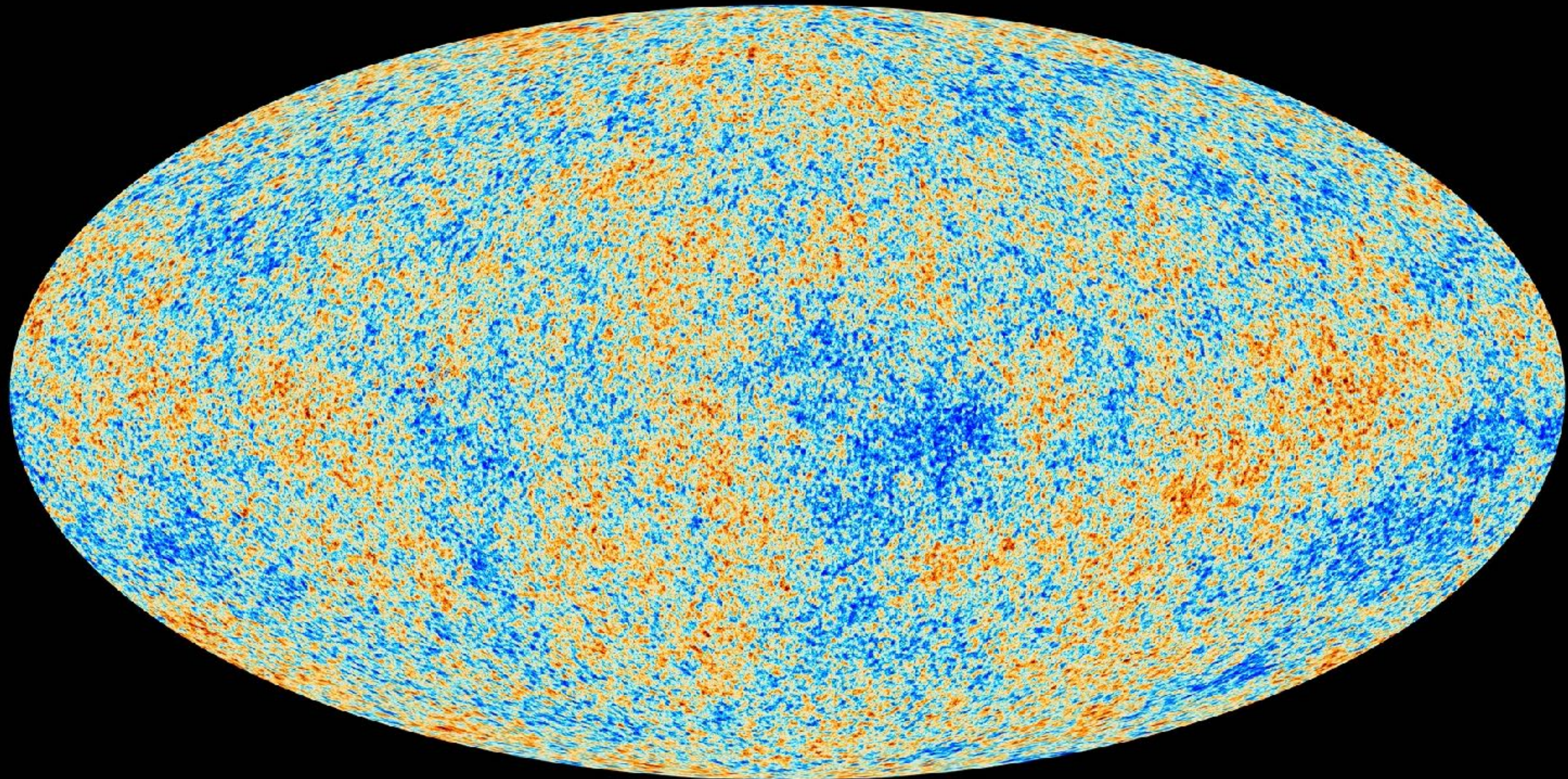
Growth of Dark Matter Density Fluctuations

matter-radiation equality

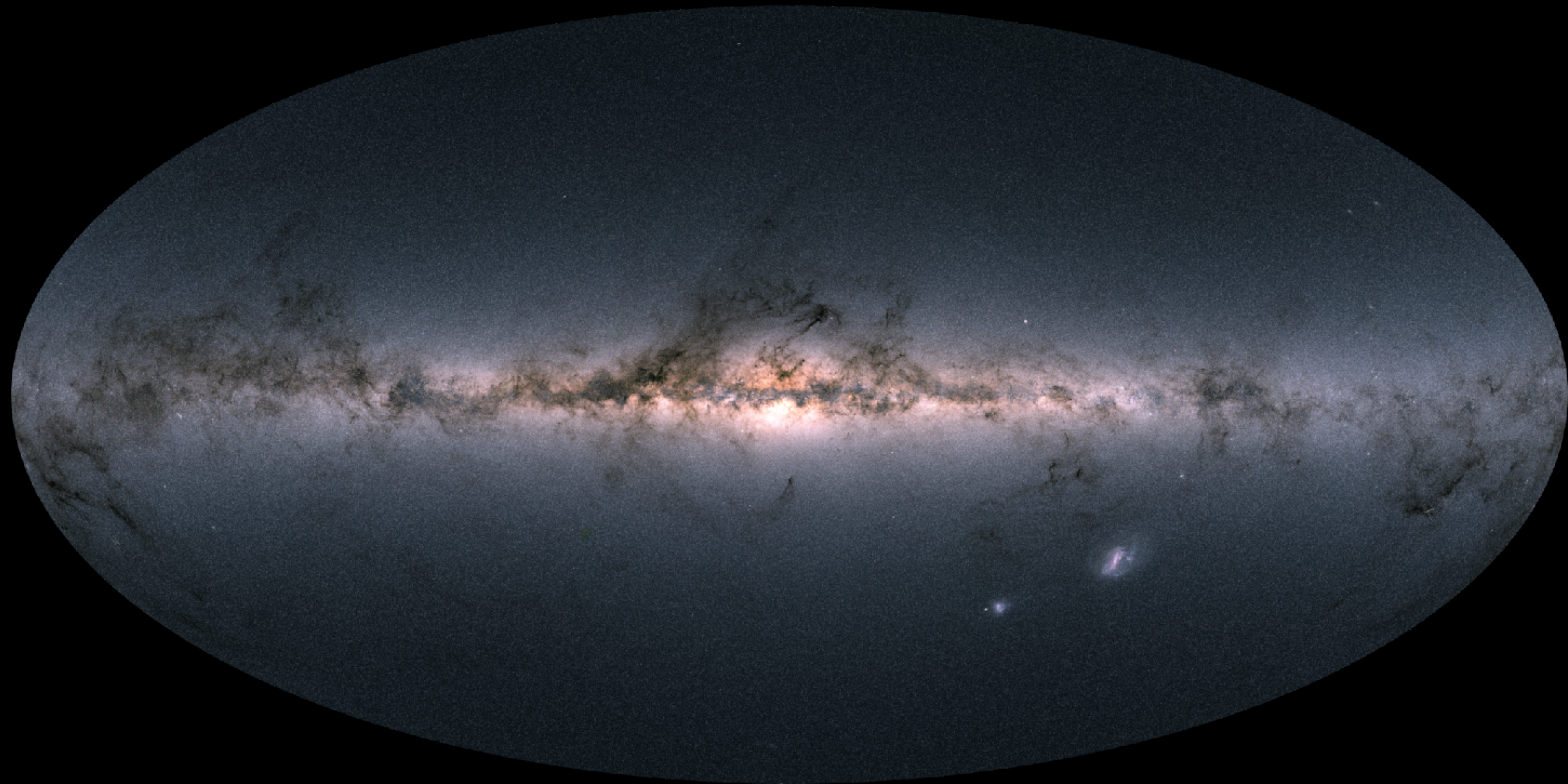


today

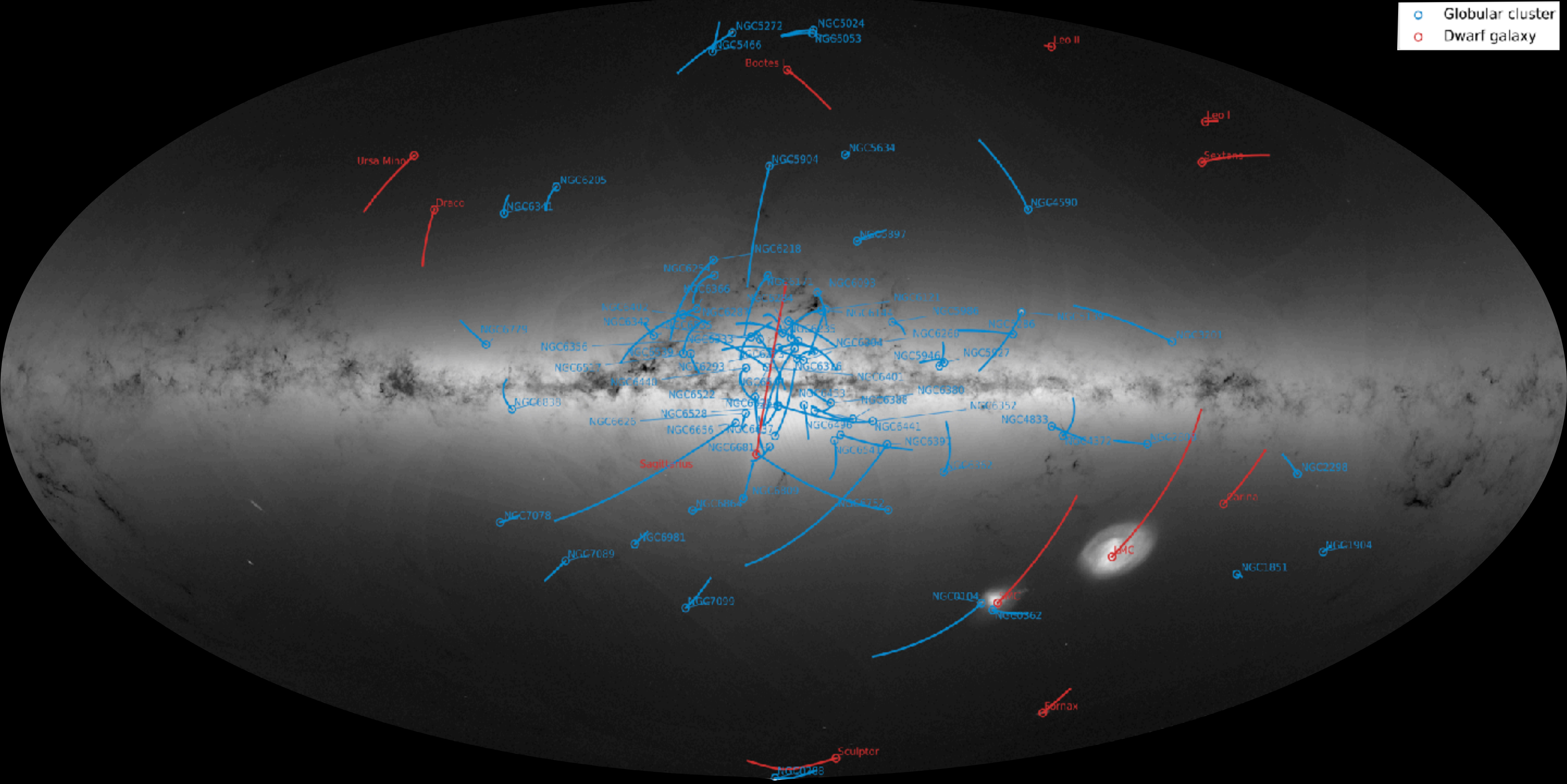
Large-Scale Dark Matter Density Fluctuations



Small-Scale Dark Matter Density Fluctuations



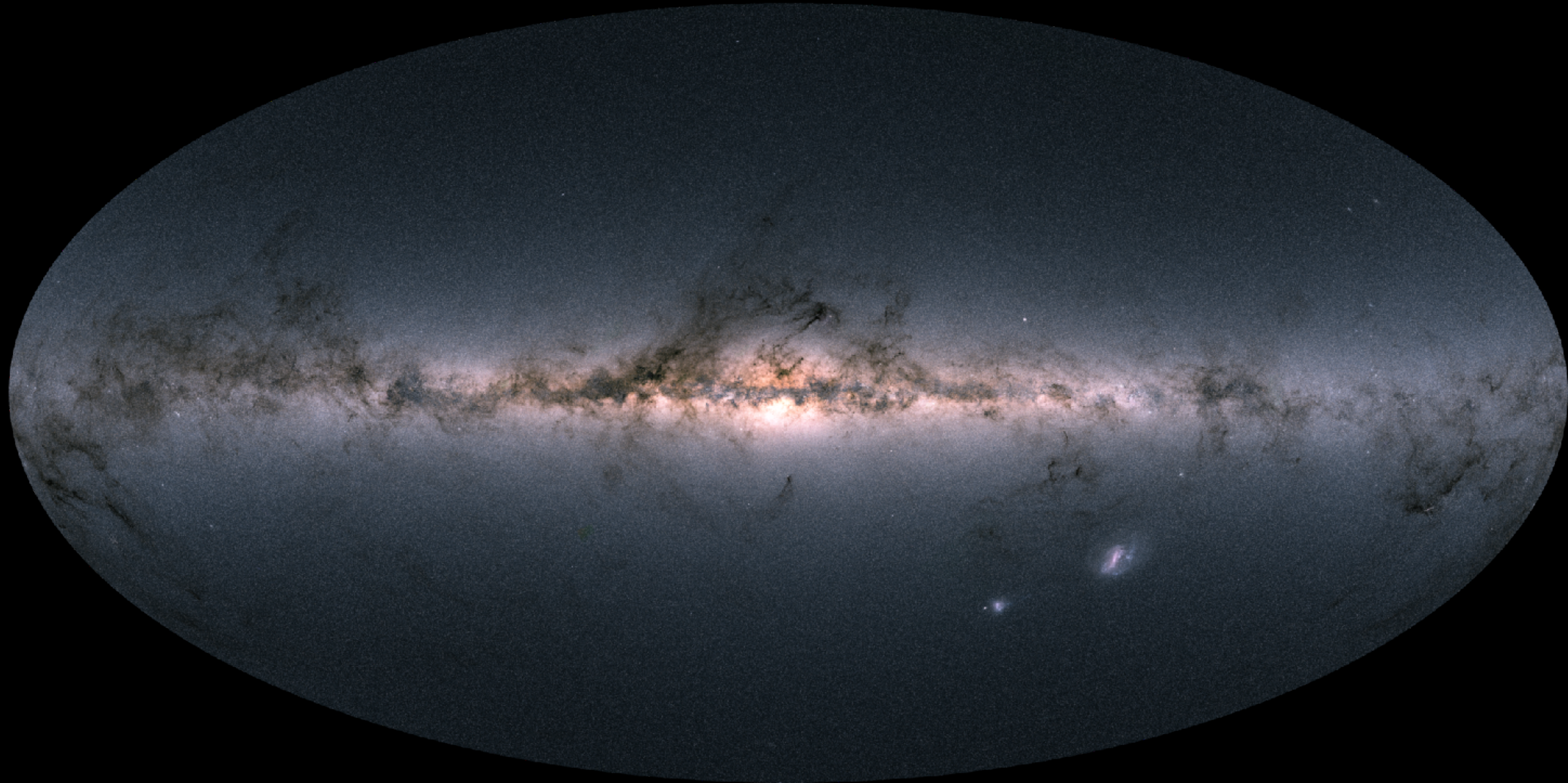
Small-Scale Dark Matter Density Fluctuations



Small-Scale Dark Matter Density Fluctuations

Theory: primordial fluctuations & DM microphysics

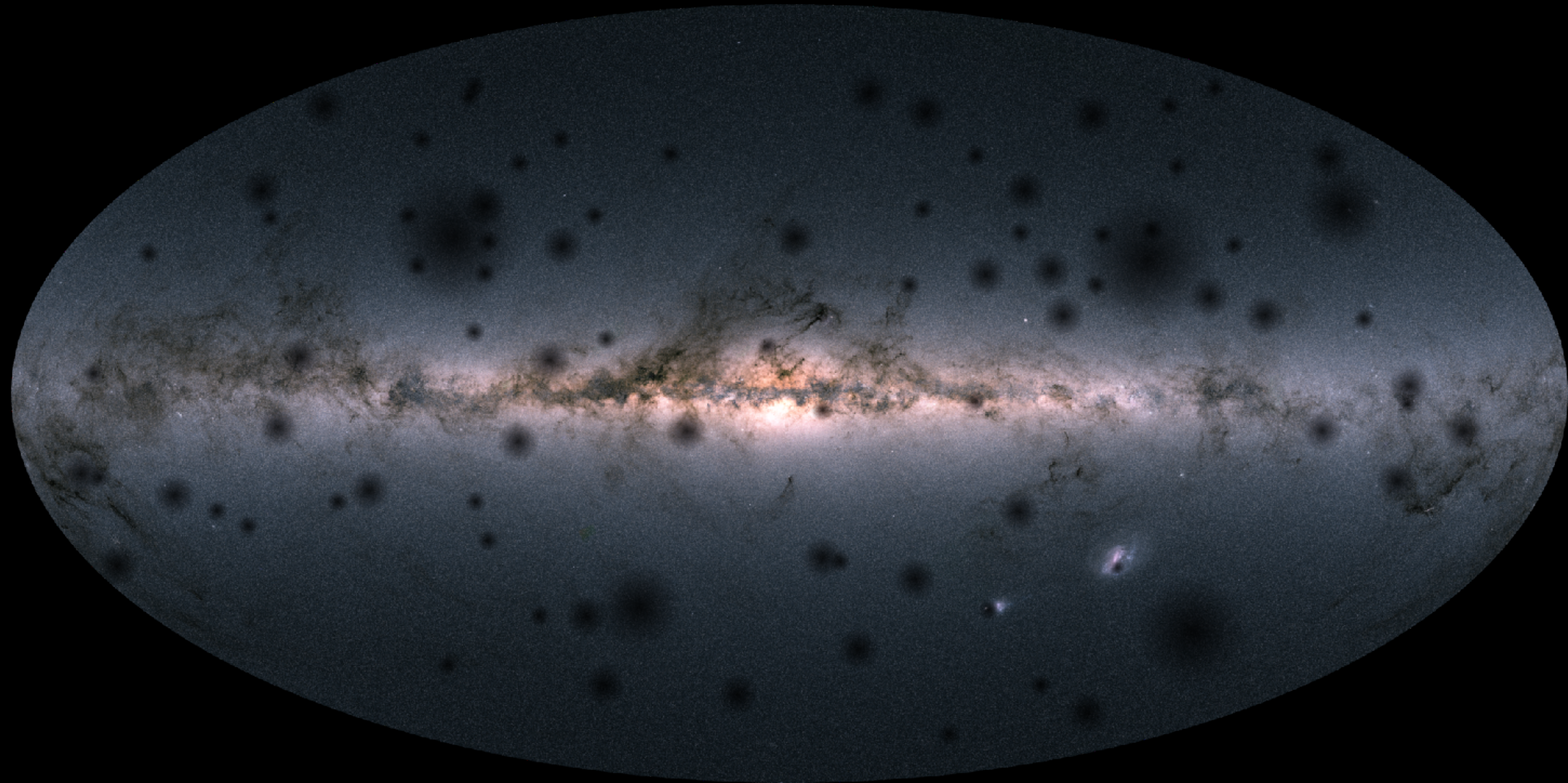
Observation: local & global



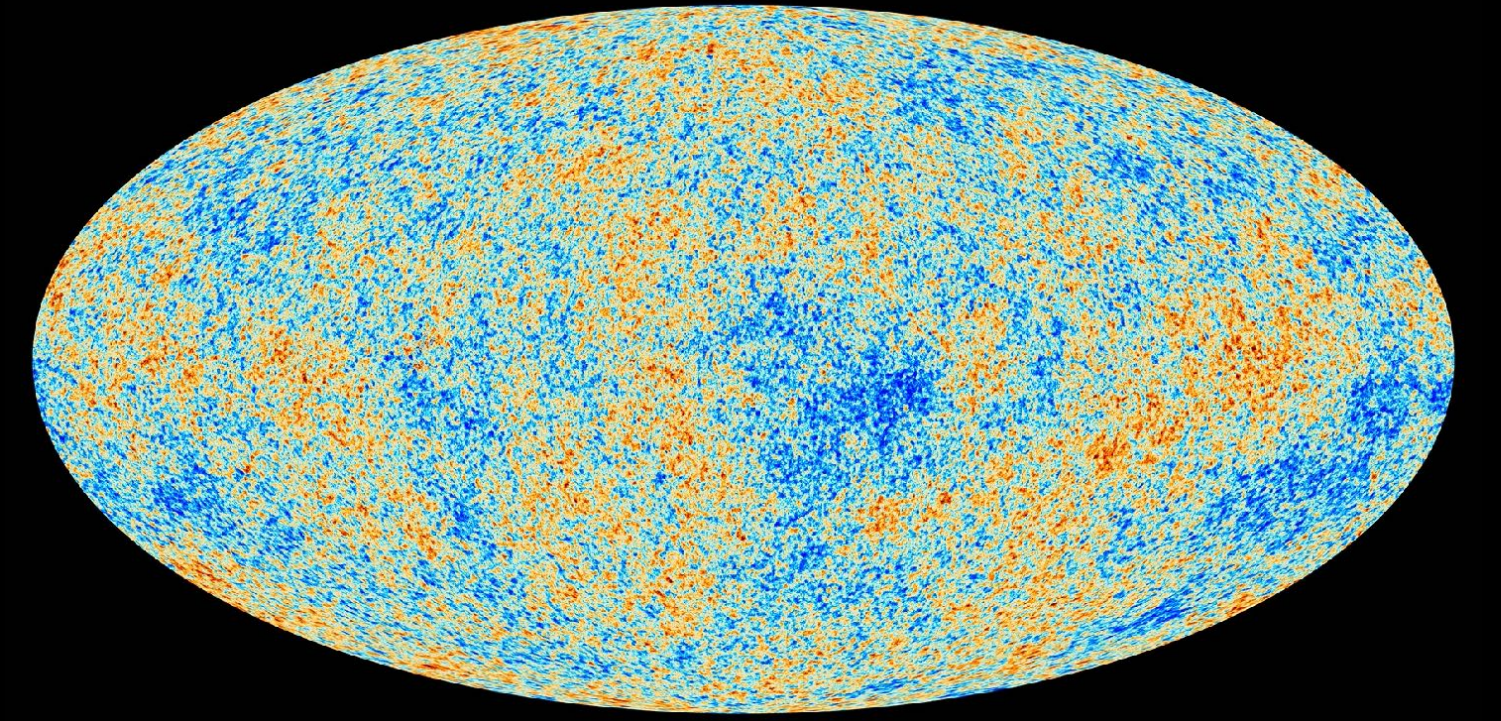
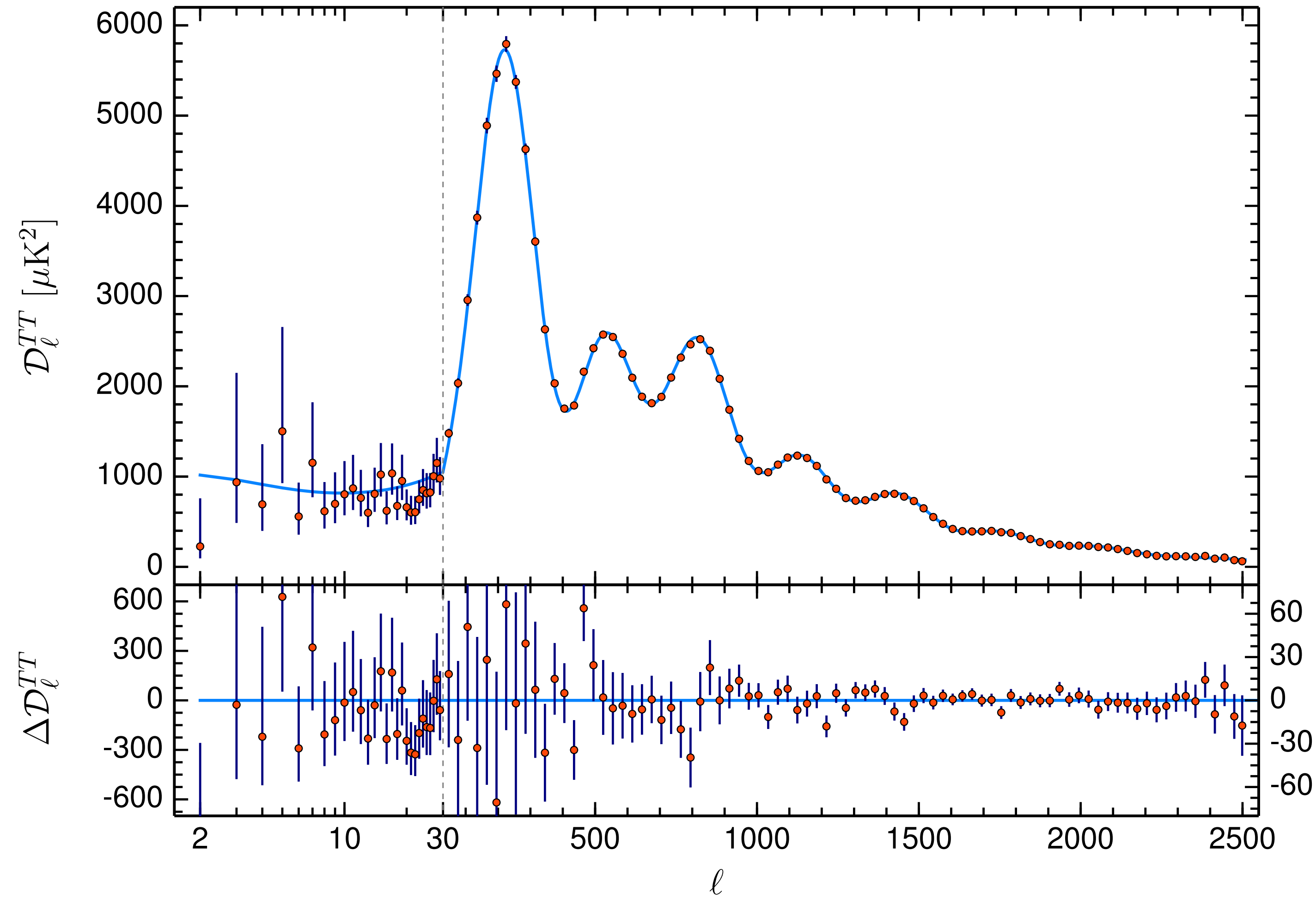
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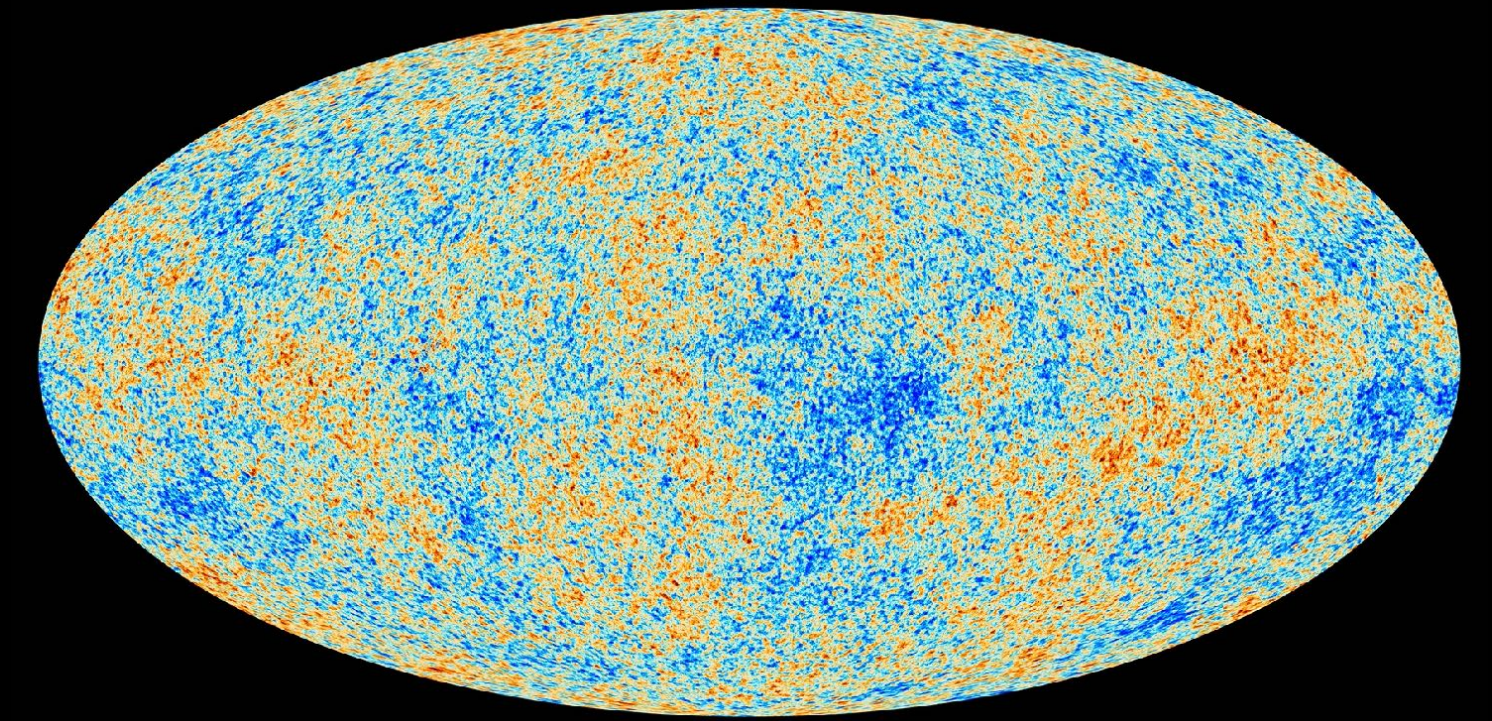
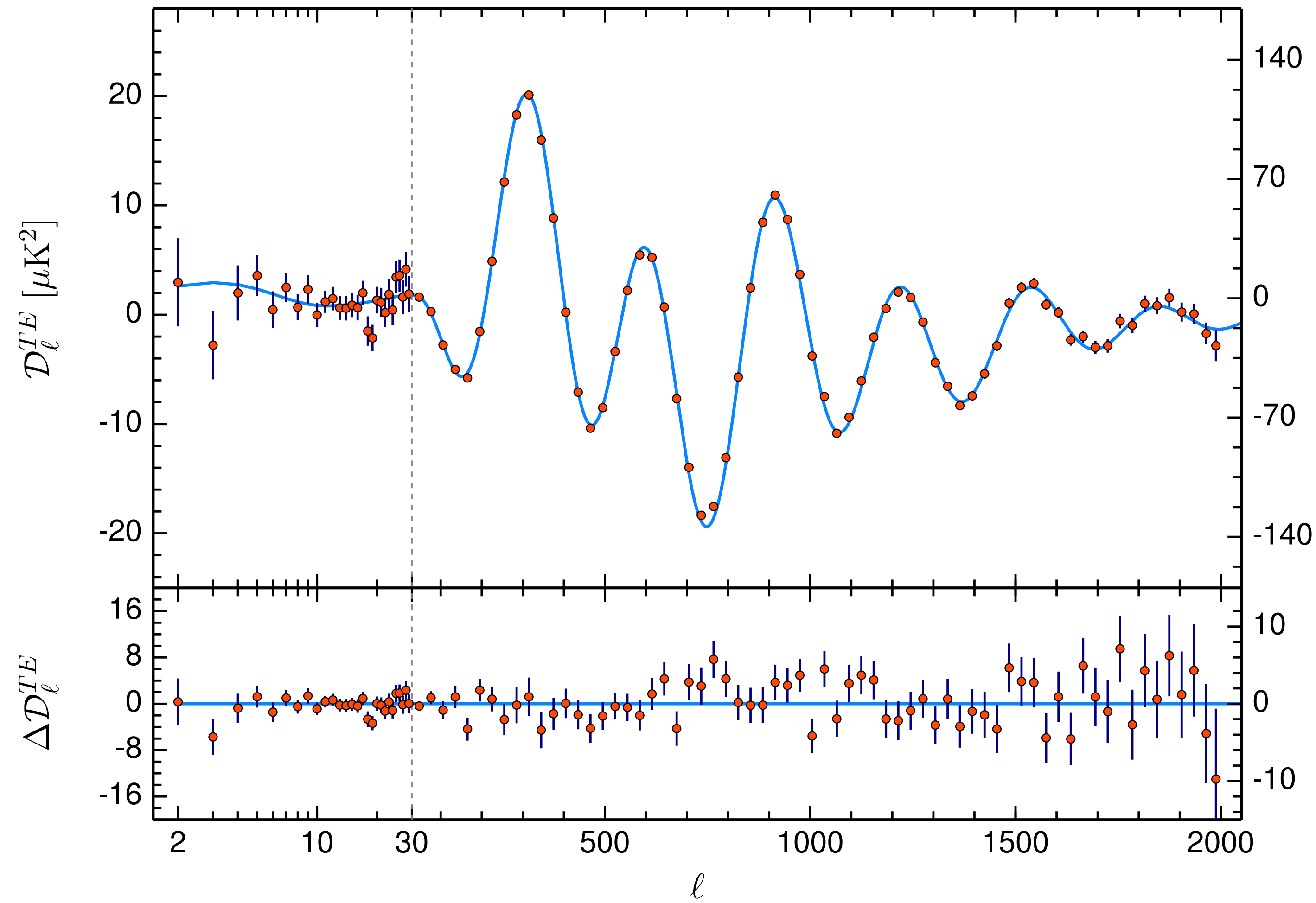
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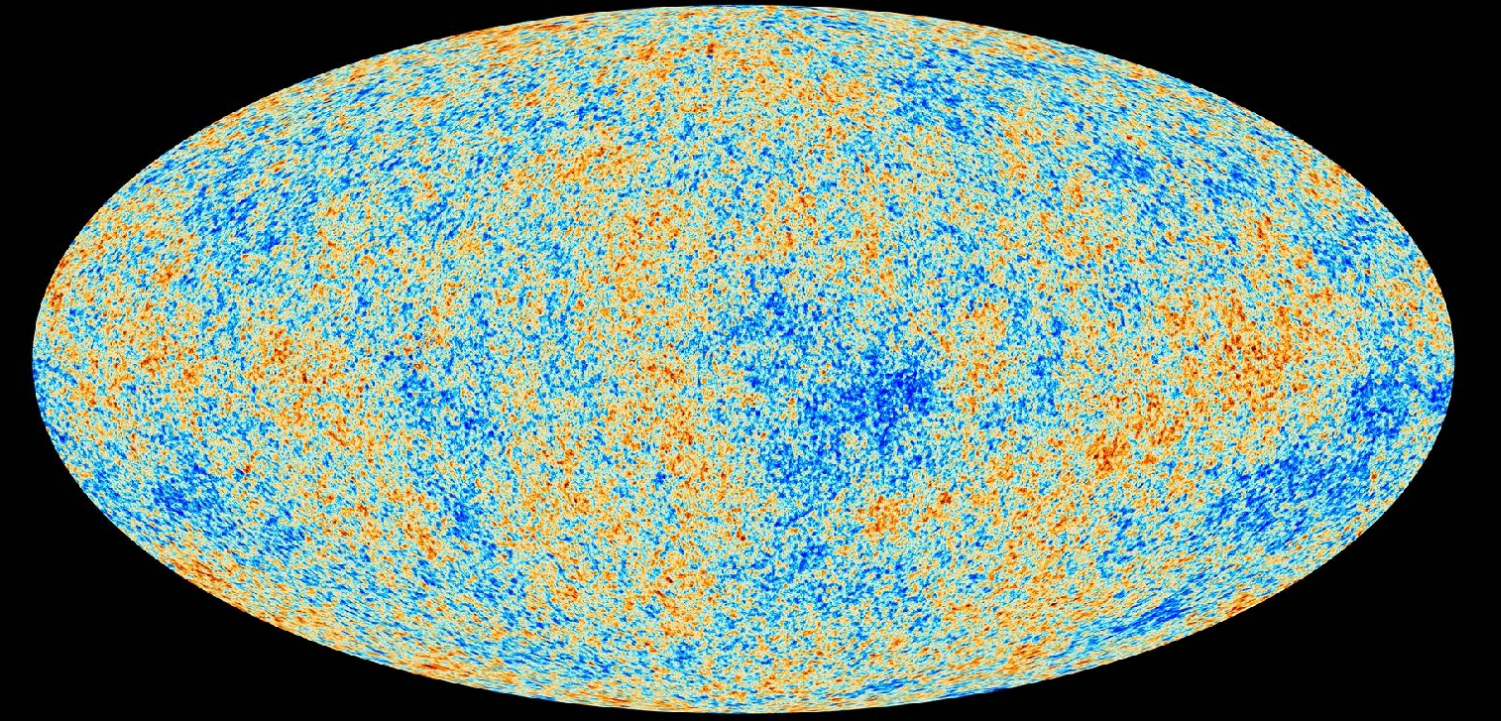
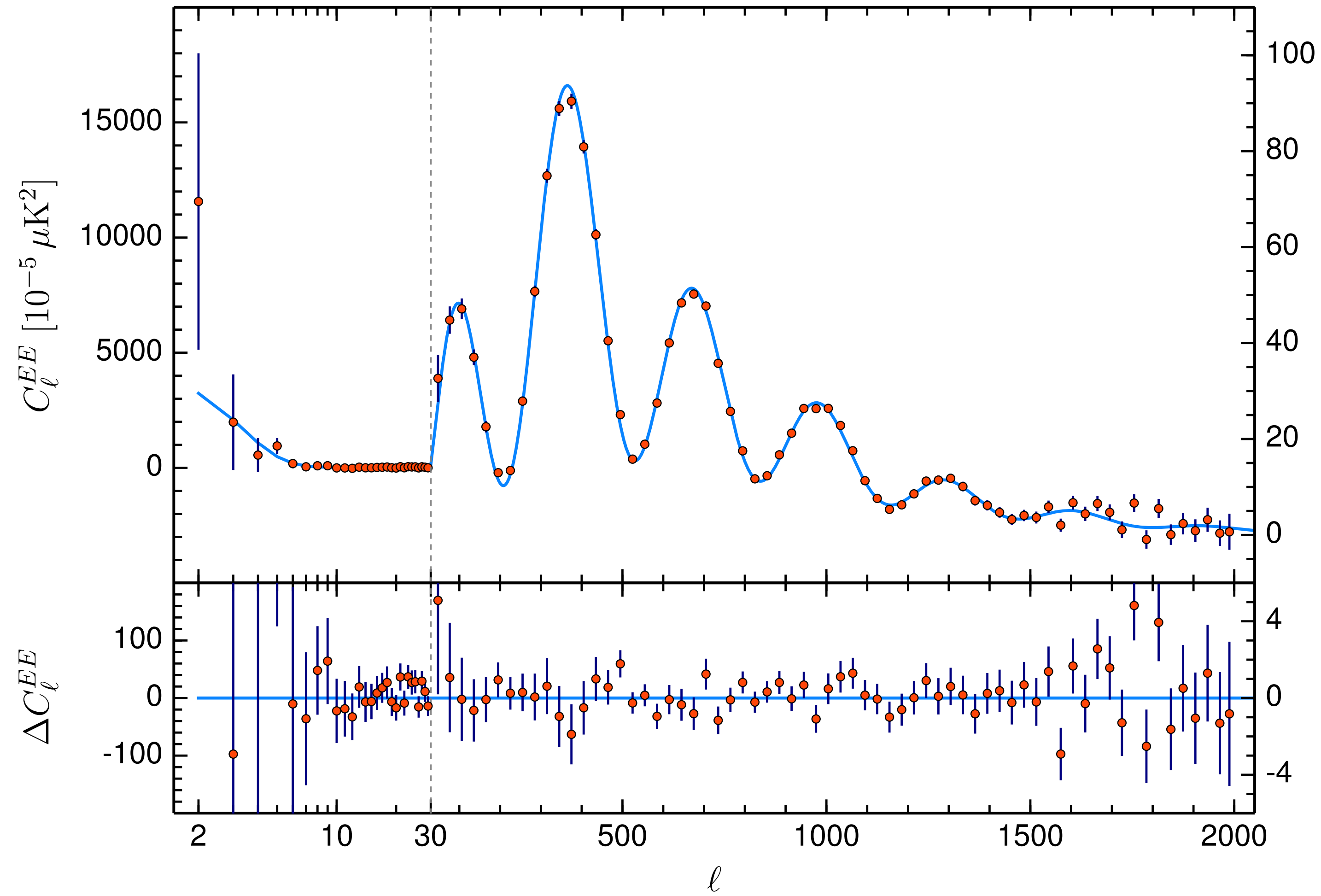
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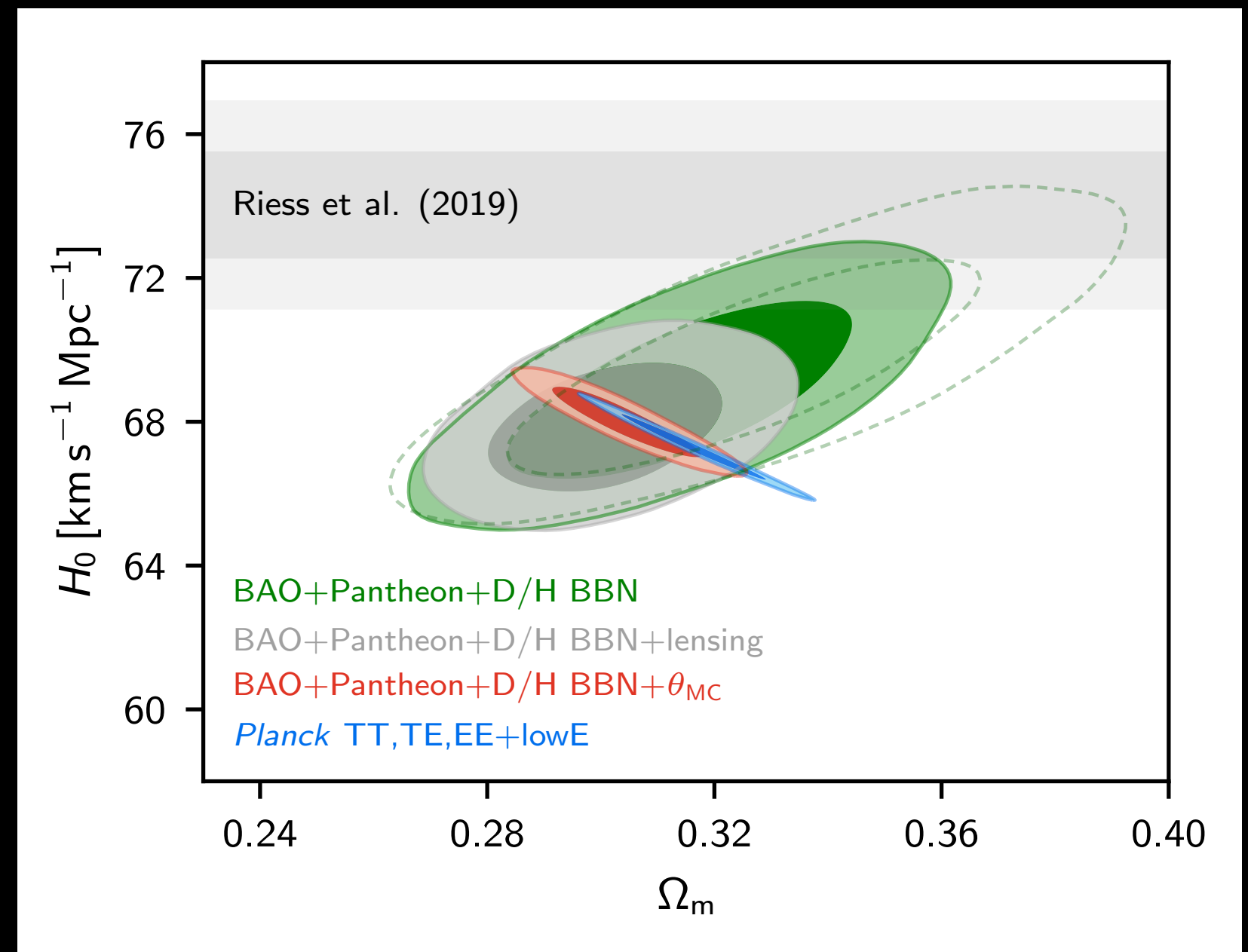
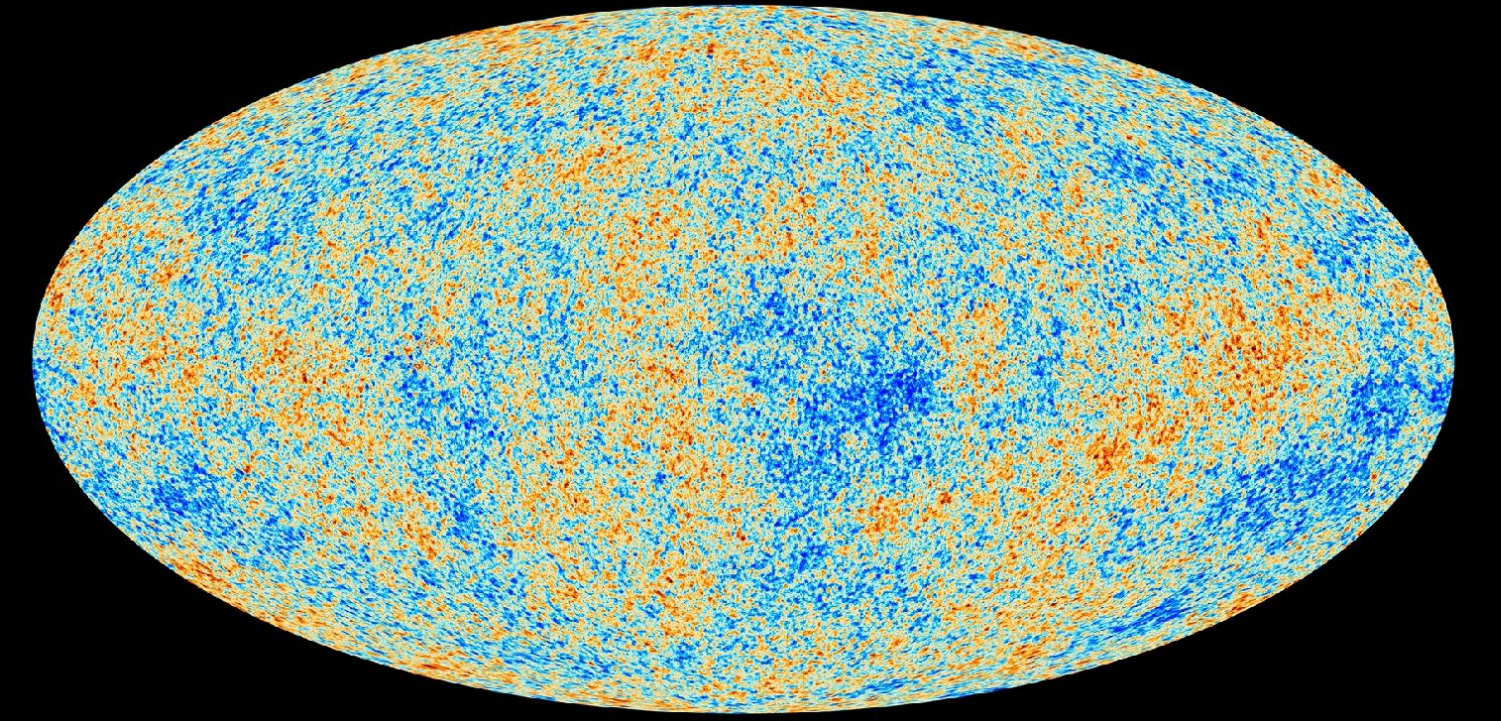
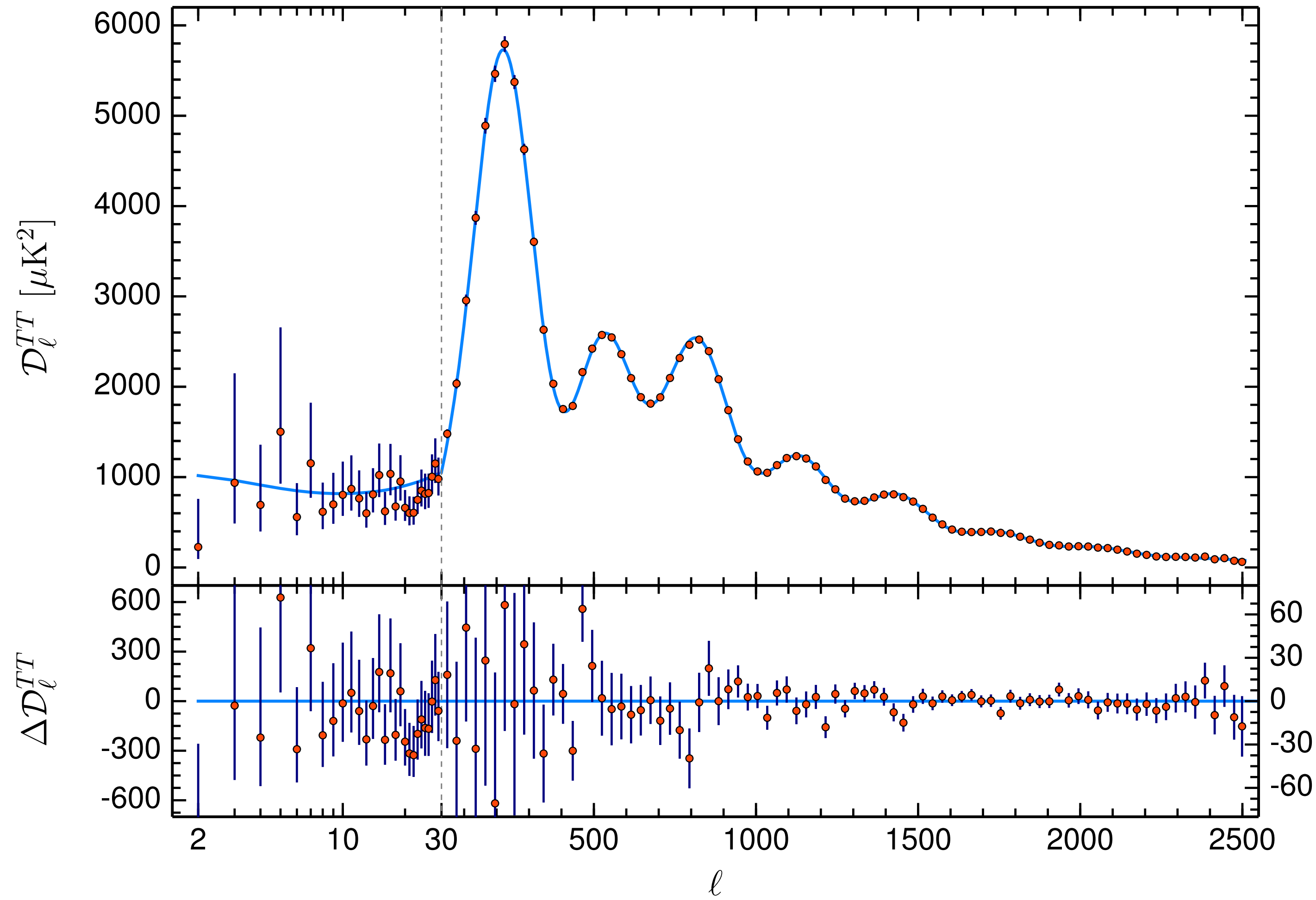
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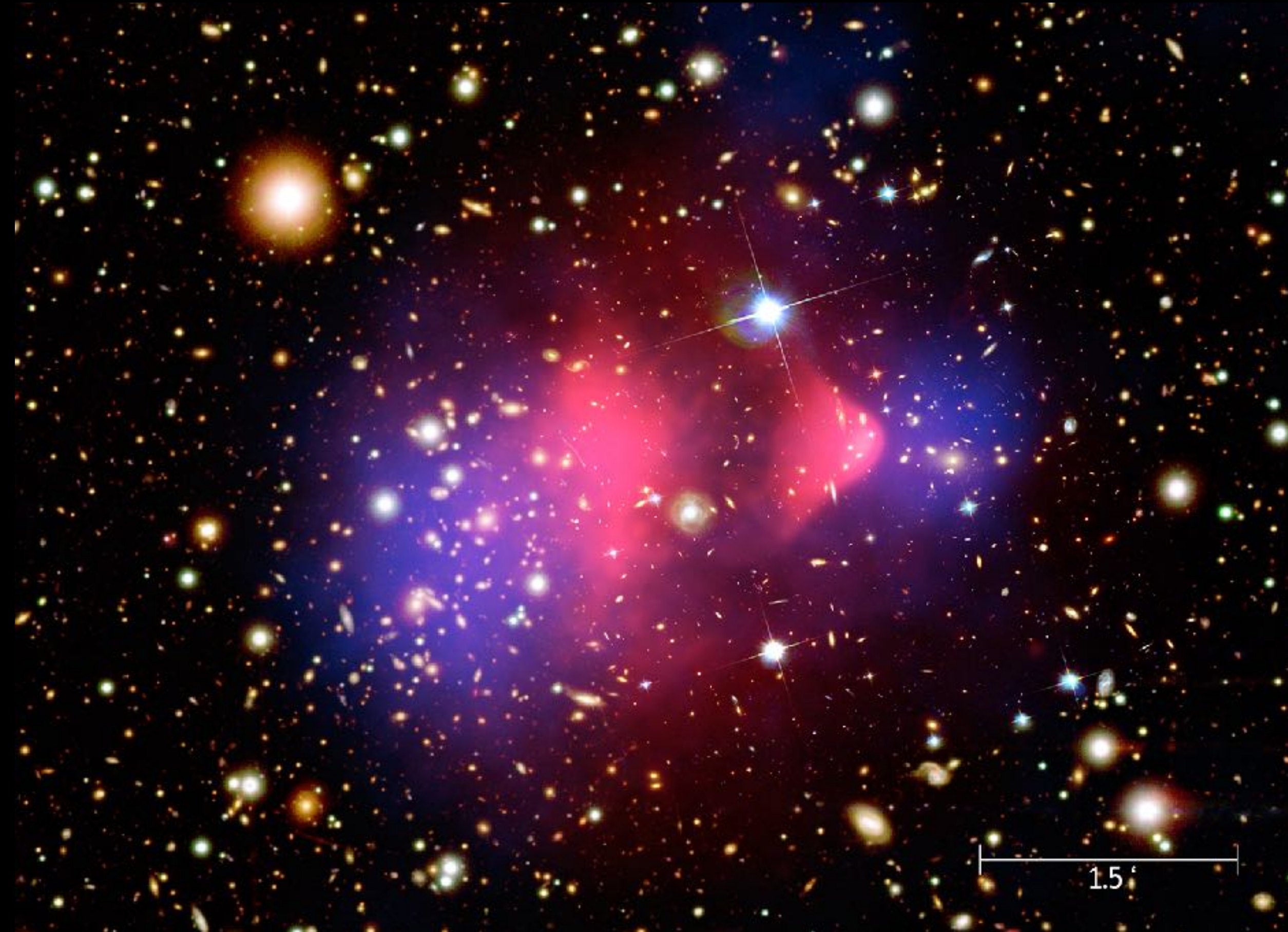
Large-Scale Dark Matter Density Fluctuations



Large-Scale Dark Matter Overdensities

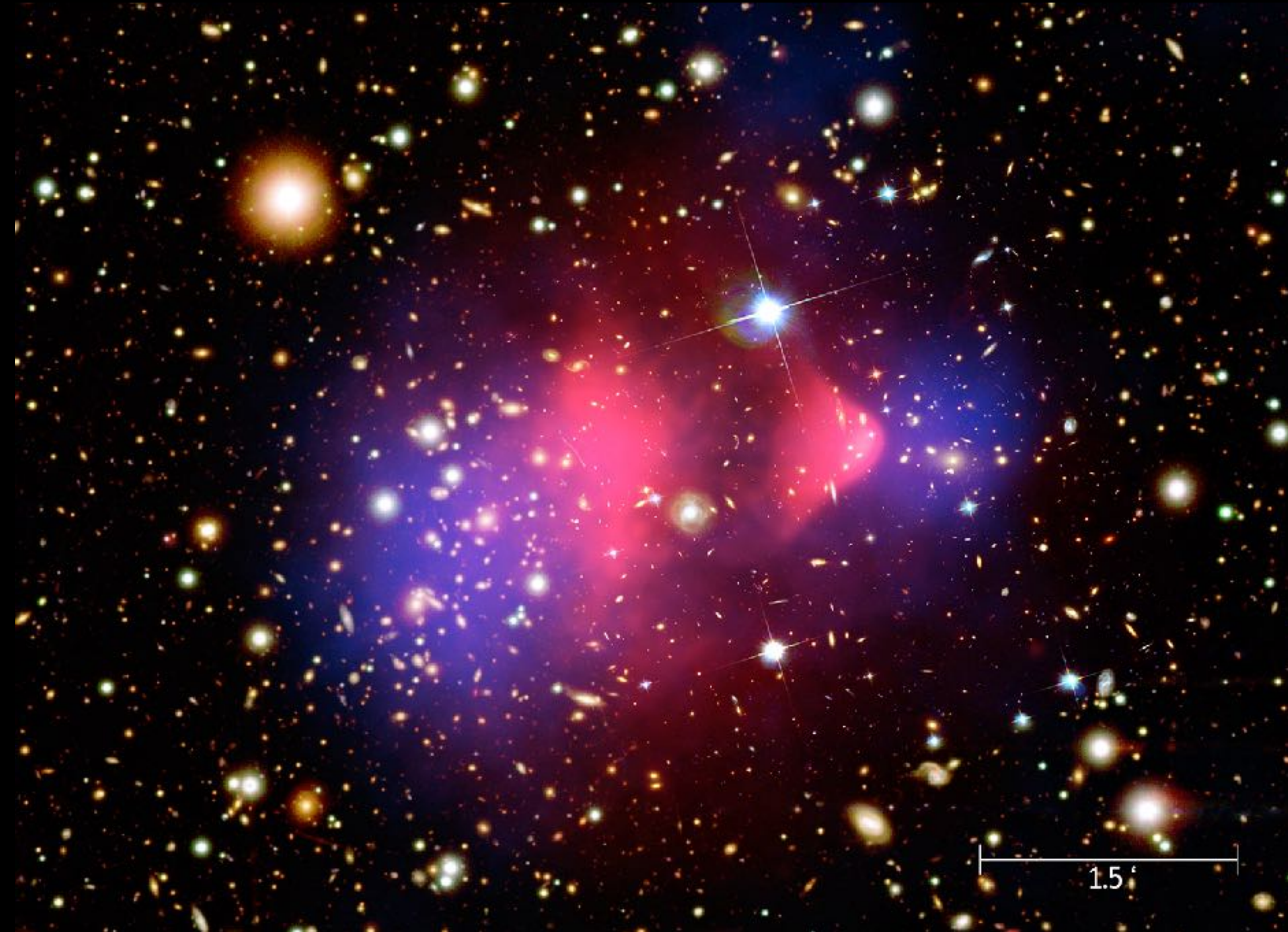
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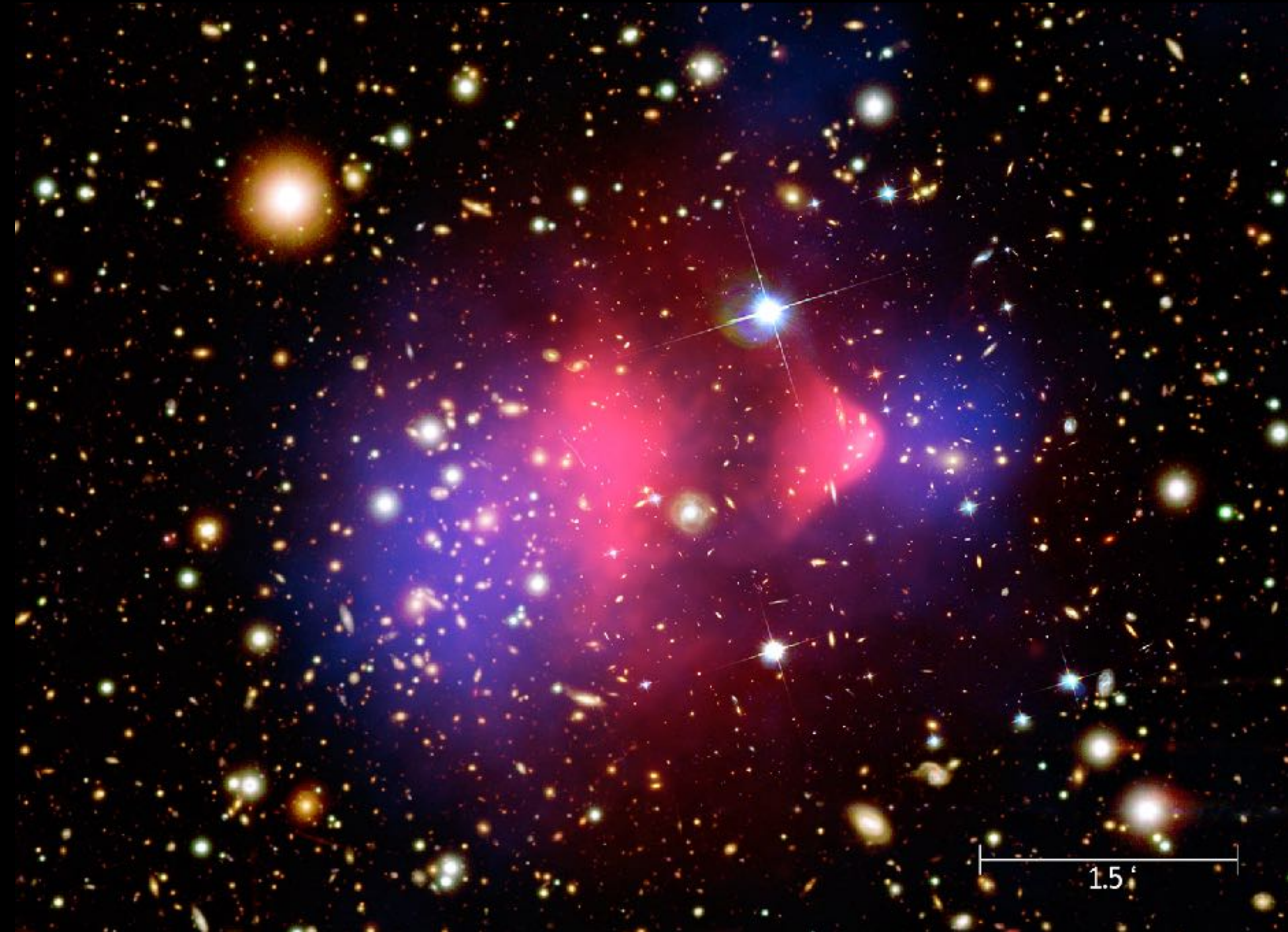
Large-Scale Dark Matter Overdensities



abundance, location, kinematics

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Large-Scale Dark Matter Overdensities



abundance, location, kinematics



mass, spin, non-gravitational interactions

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Enumerable Dark Matter Candidates

something else?

Weakly Interacting Massive Particle

stable by symmetry

thermal production: freeze-out, freeze-in

motivated by hierarchy problem

mass > keV

mass < keV

Super Weakly Interacting Light Boson

meta-stable by lightness

non-thermal production: misalignment, inflationary fluctuation

motivated by strong CP problem, string theory, origin of SM masses and couplings

- ! allowed
- ! consistent
- ! produced
- ✓ testable
- ✓ anomaly, puzzle
- ✓ natural

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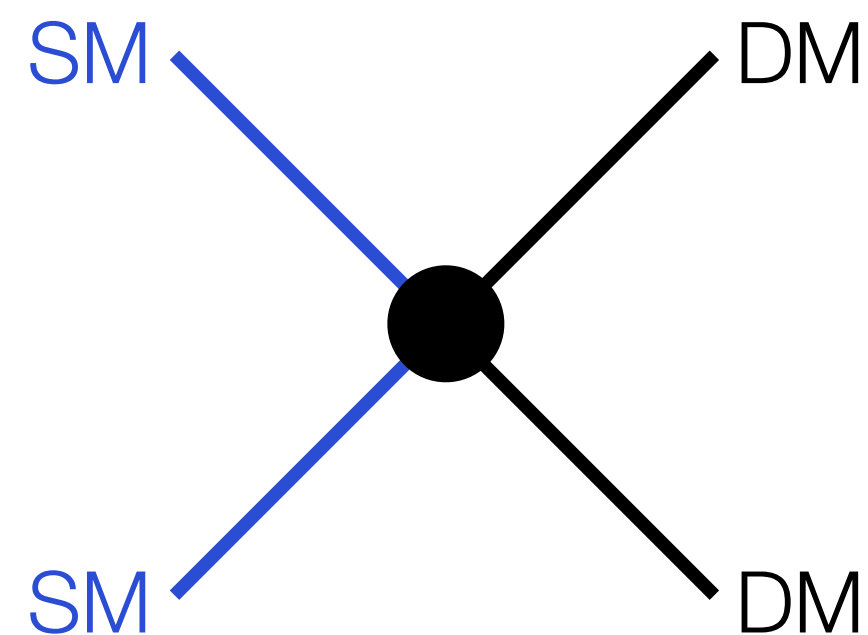
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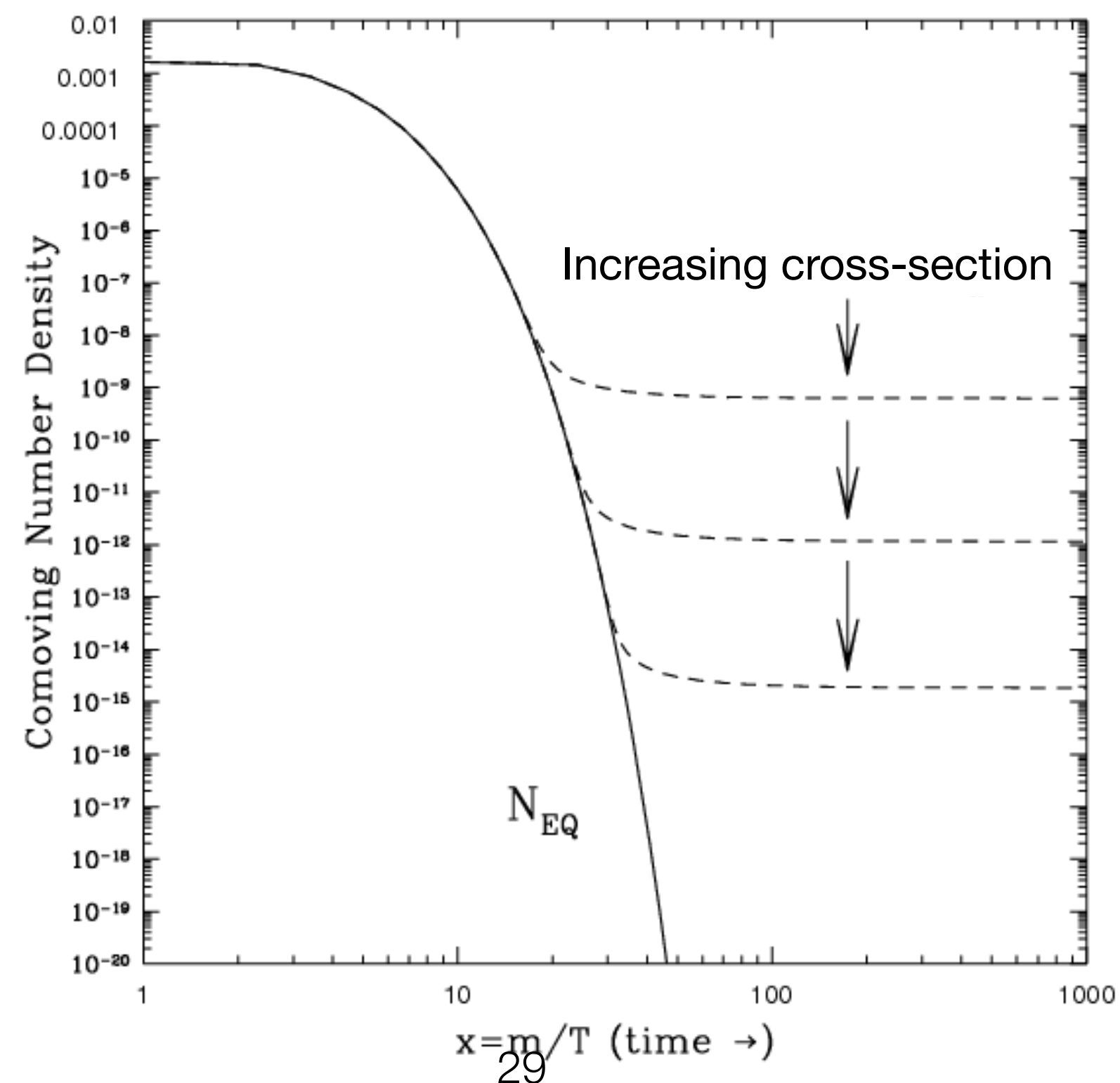


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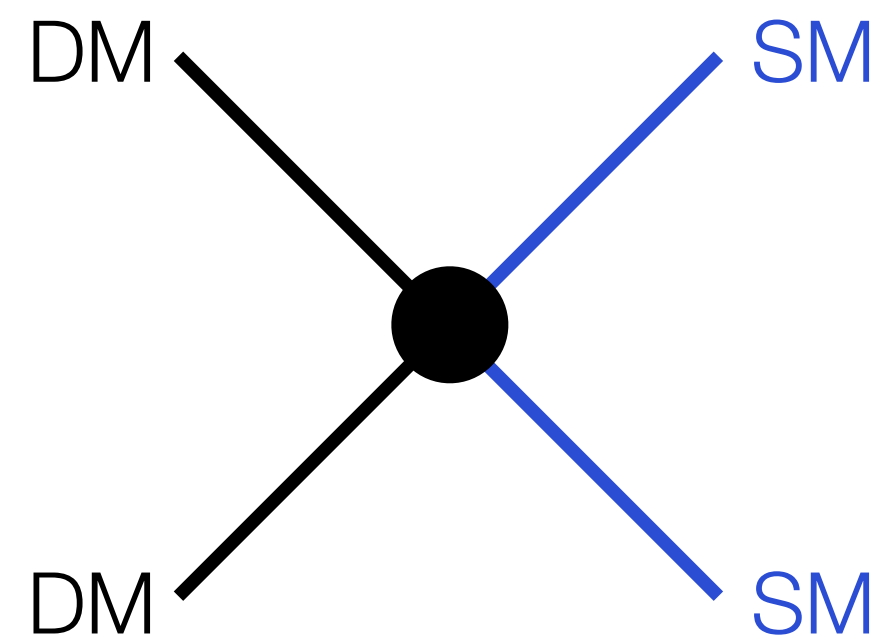
motivated by hierarchy problem



$$\frac{\Omega_{\text{WIMP}}}{\Omega_m} \propto \frac{1}{\sigma_{\text{annihilation}}} \approx \frac{1}{(20 \text{ TeV})^{-2}}$$

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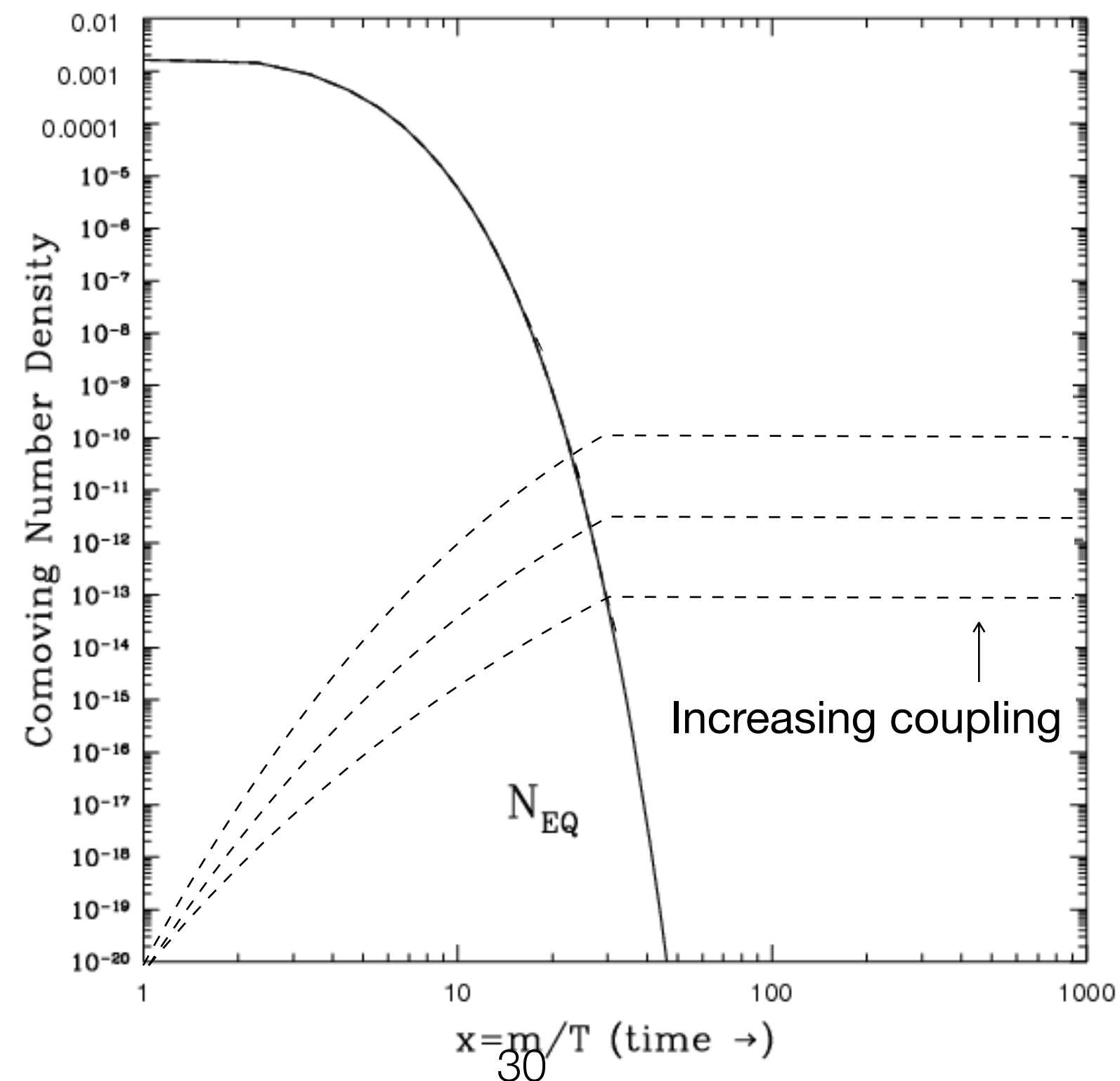


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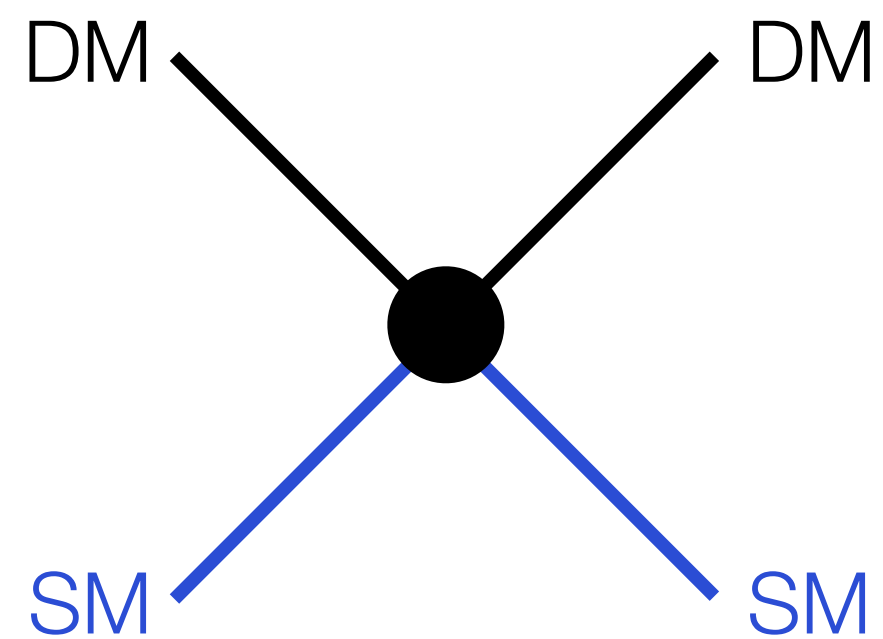


$$\frac{\Omega_{\text{WIMP}}}{\Omega_m} \propto \frac{(\text{coupling})^2}{\text{mass}}$$

$$\approx \left(\frac{\text{coupling}}{10^{-12}} \right)^2 \frac{\text{GeV}}{\text{mass}}$$

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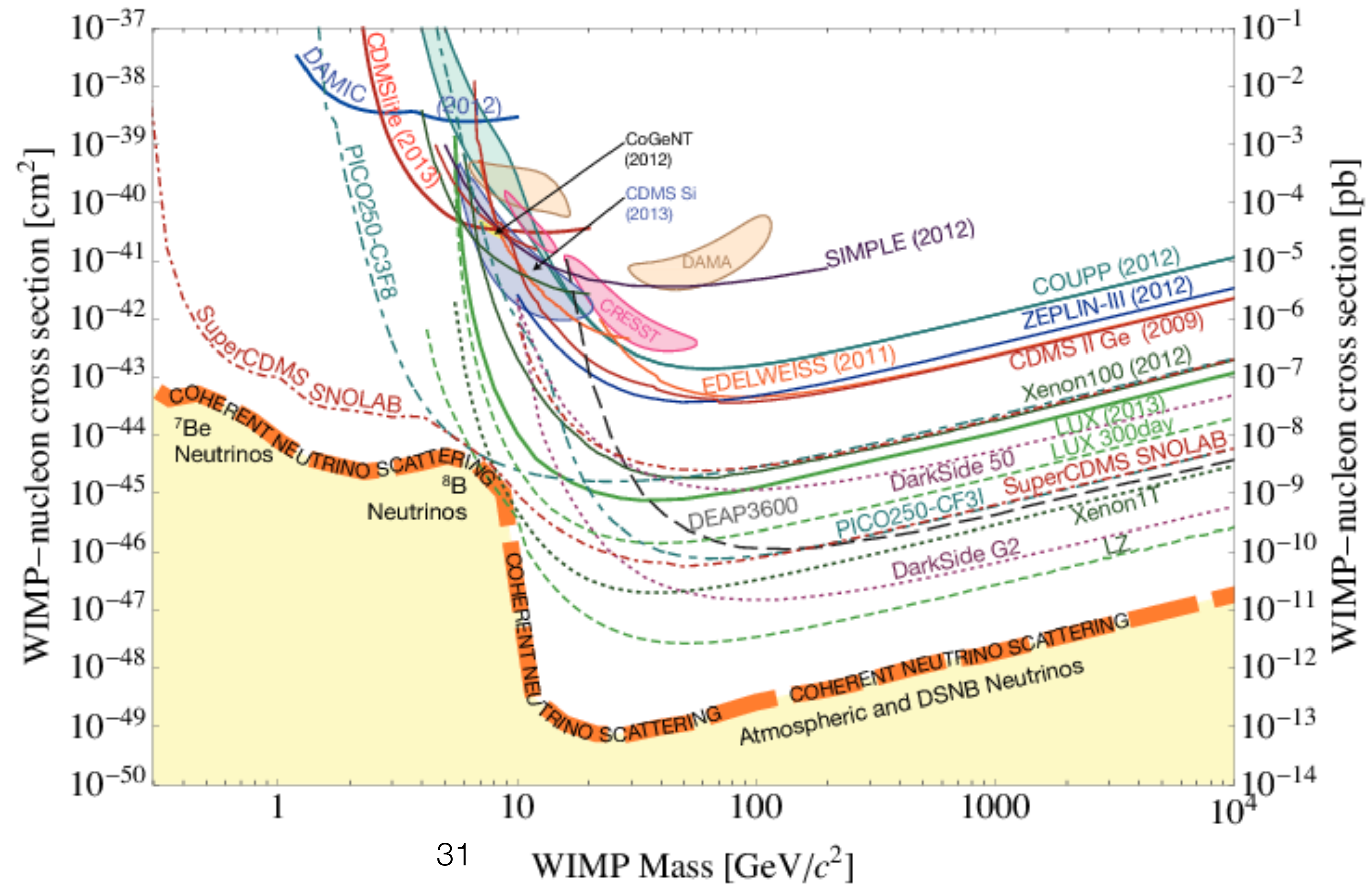


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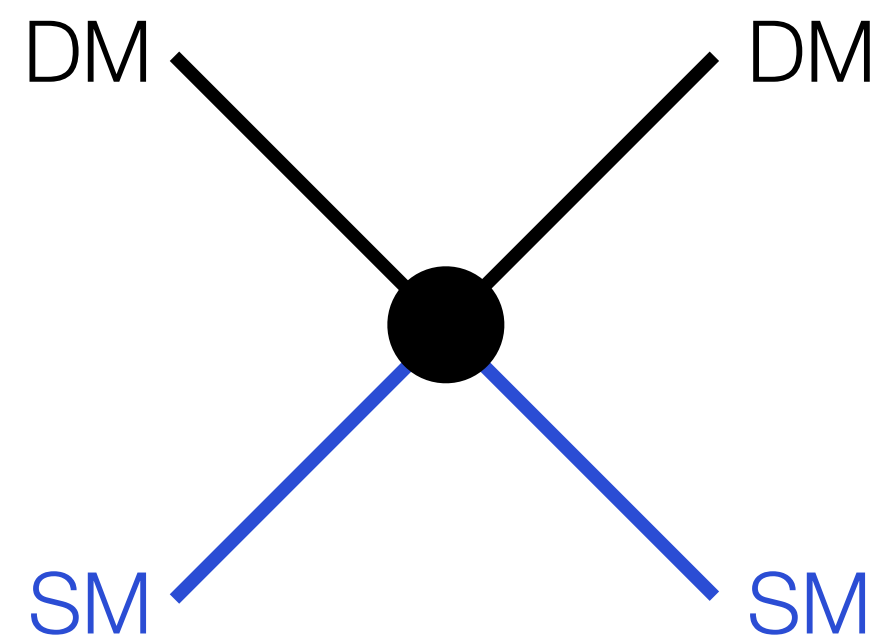
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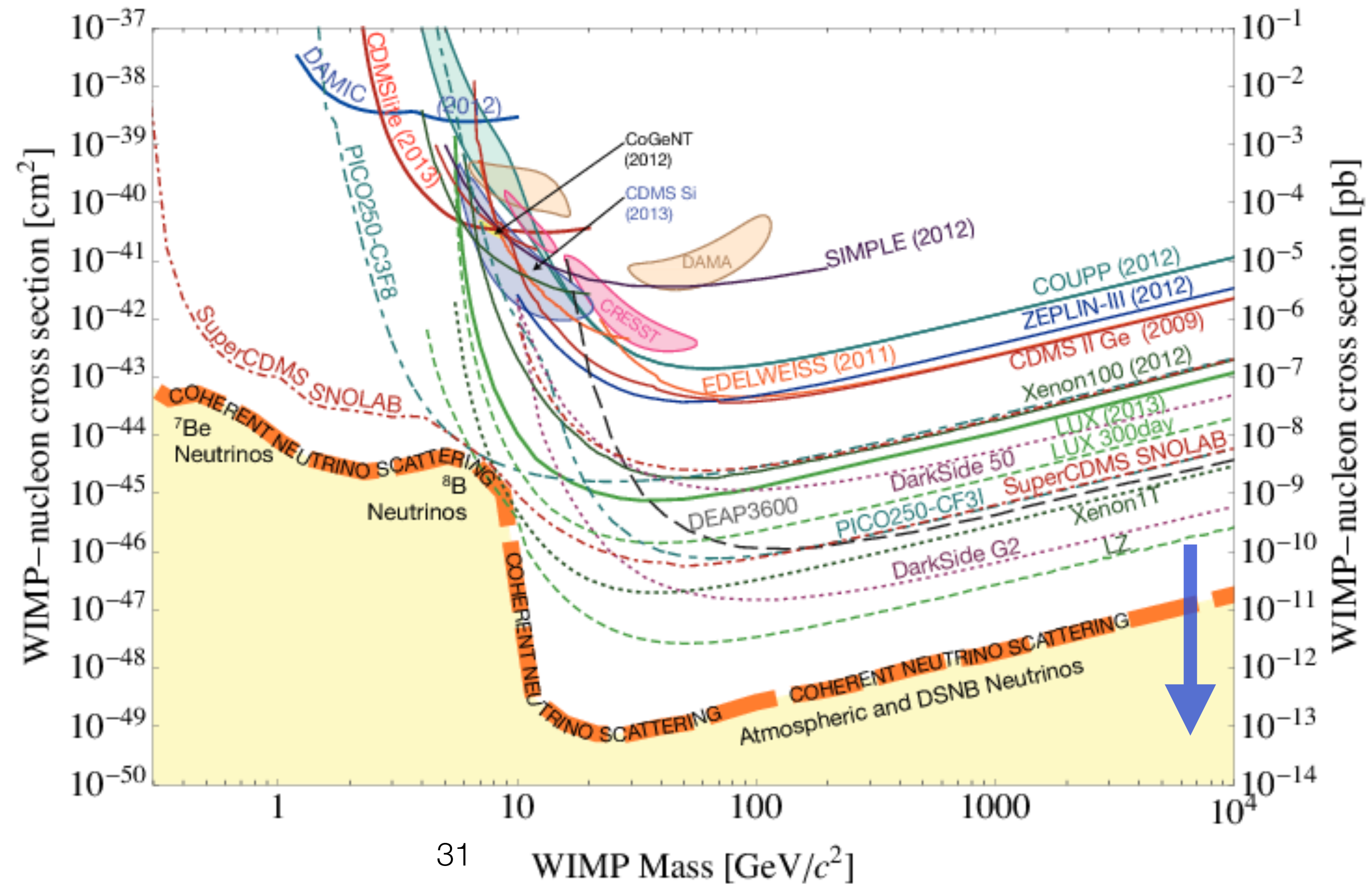


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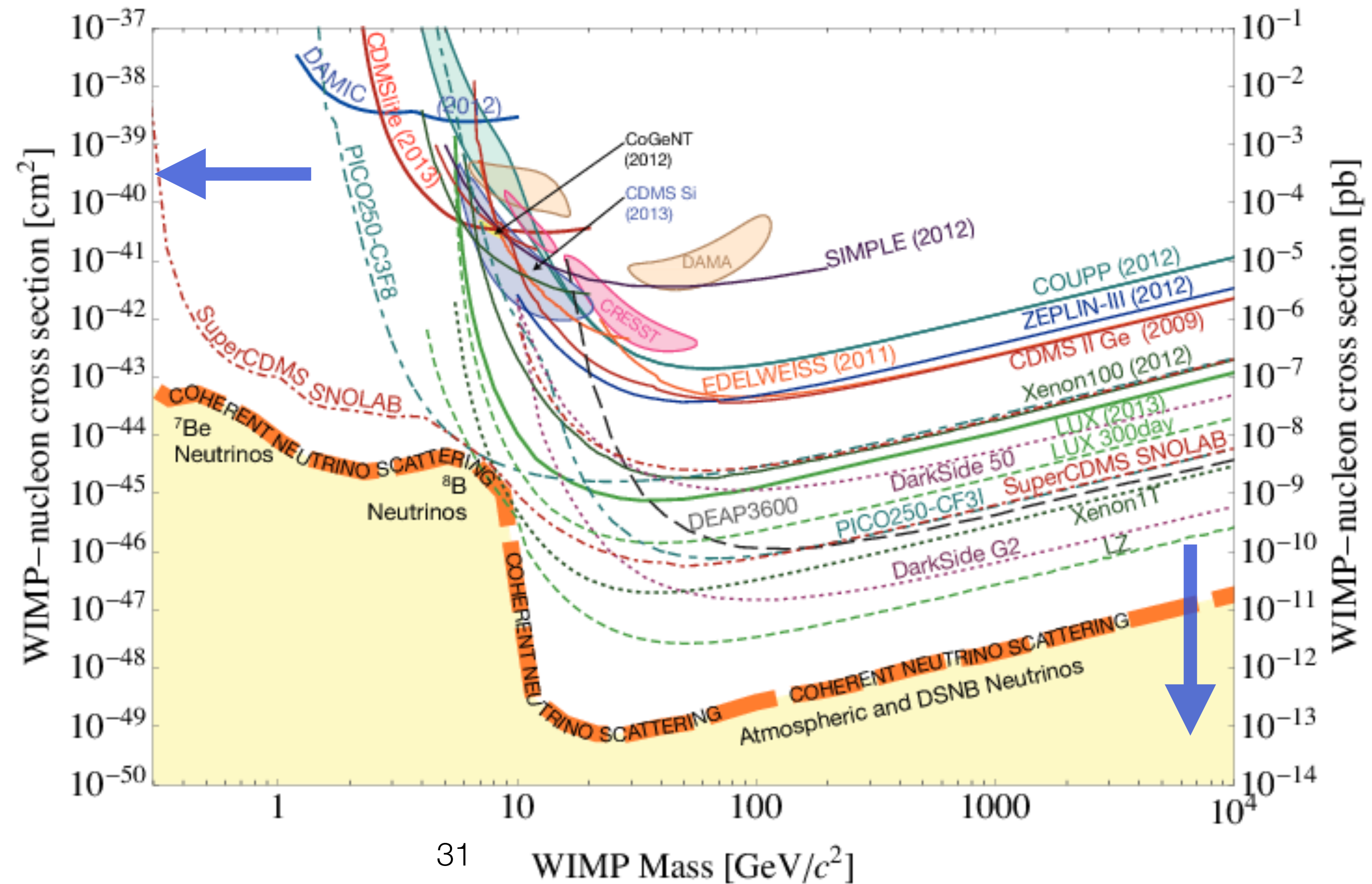
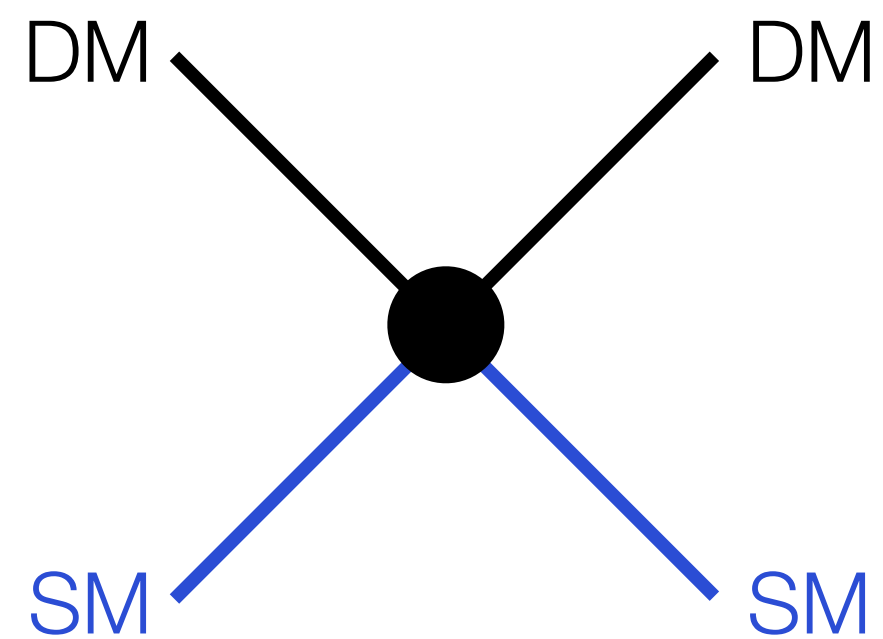
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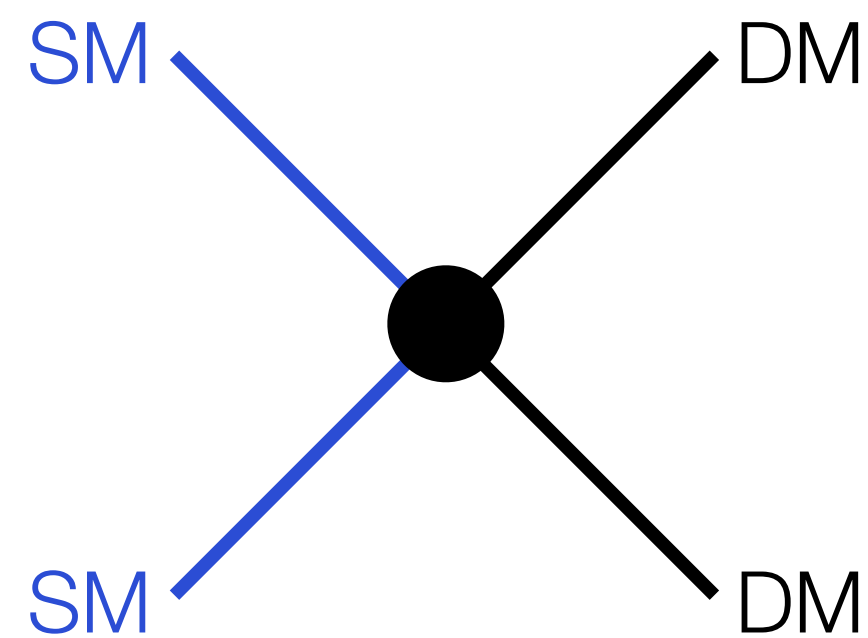
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Enumerable Bosonic Dark Matter Candidates

- | | |
|---|-----------------|
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Super Weakly Interacting Light Boson

meta-stable by lightness

non-thermal production: misalignment, inflationary fluctuations

motivated by strong CP problem, string theory, origin of masses/couplings

Scalar

$$\phi \bar{e}e \quad \phi \bar{q}q$$

$$\phi F^2 \quad \phi G^2$$

Pseudoscalar

$$a \bar{e}i\gamma_5 e \quad a \bar{q}i\gamma_5 q$$

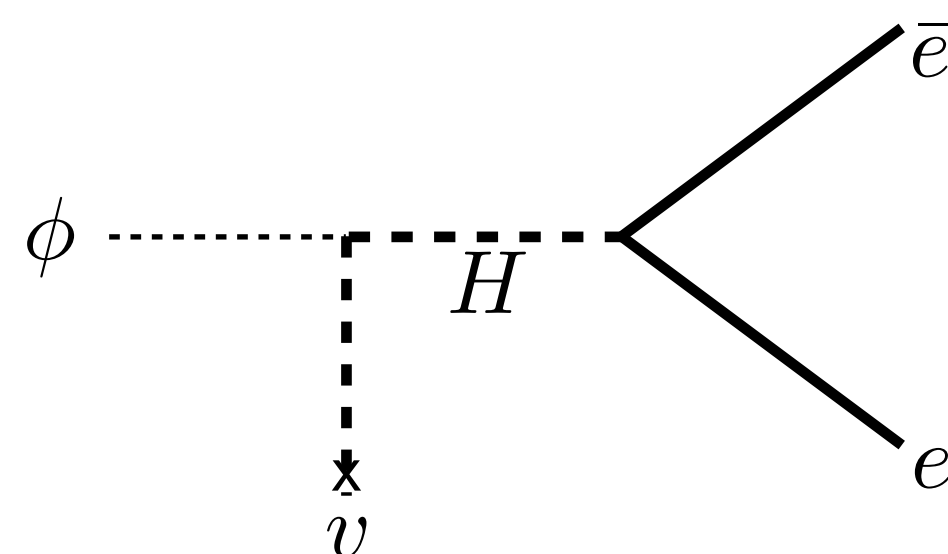
$$a F \tilde{F} \quad a G \tilde{G}$$

Vector

$$\epsilon A'_\mu J_{EM}^\mu$$

$$g A'_\mu J_{B-L}^\mu$$

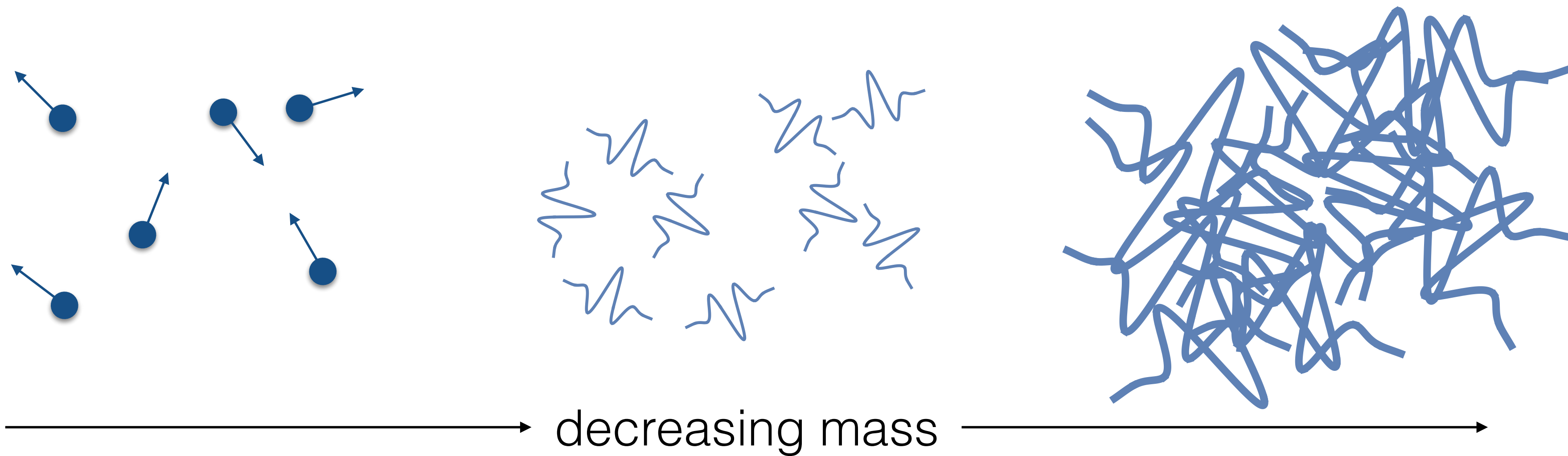
Higgs portal $A\phi|H|^2$



QCD axion

Light Bosonic Dark Matter as Classical Waves

$$\mathcal{L} = \frac{(\partial\phi)^2}{2} - \frac{m^2\phi^2}{2}$$



large occupation number:

$$\frac{\rho_{\text{DM}}}{m^4\sigma_v^3} \sim 10^4 \left(\frac{\text{eV}}{m}\right)^4$$

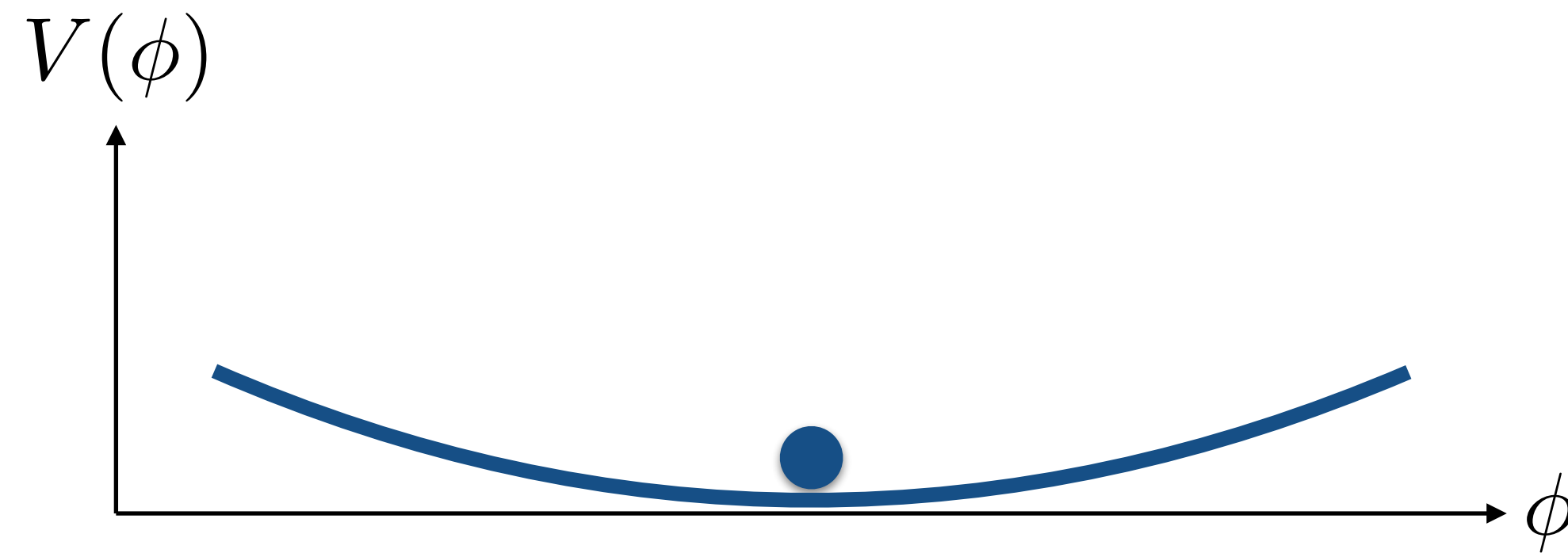
large field amplitude:

$$\phi(t, \mathbf{x}) \simeq \underbrace{\frac{\sqrt{2\rho_{\text{DM}}}}{m}}_{10^{-15} M_{\text{Pl}} \left(\frac{10^{-15} \text{ eV}}{m}\right)} \cos(mt - m\mathbf{v} \cdot \mathbf{x} + \alpha) + \dots$$

Scalar Dark Matter Production in the early Universe

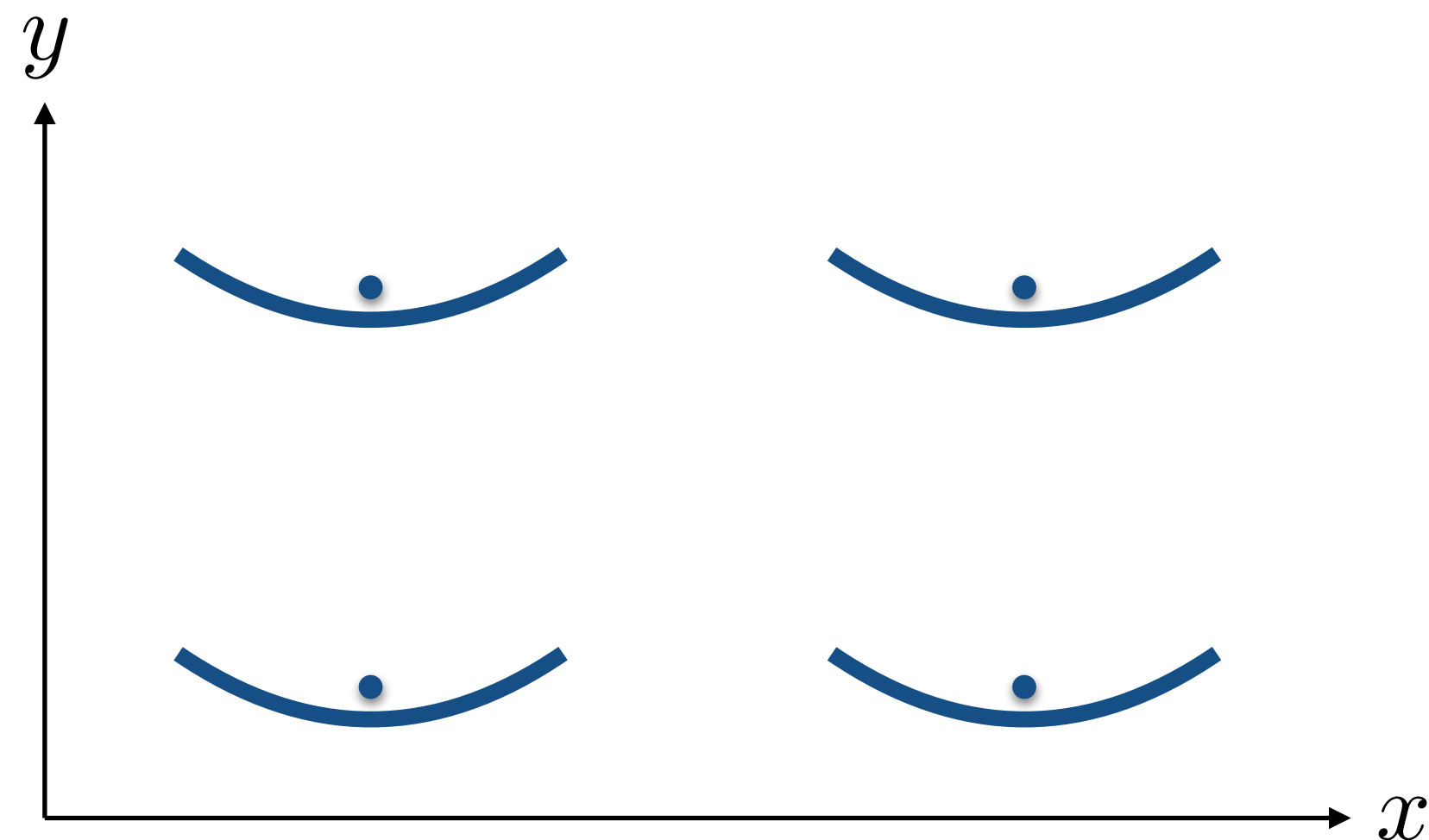
$$\mathcal{L} = \frac{1}{2}(\partial_\mu\phi)^2 - \frac{1}{2}m^2\phi^2$$

$$\ddot{\phi} + 3H\dot{\phi} + m^2\phi = 0$$



dissipation \longleftrightarrow fluctuation

during inflation: misalignment



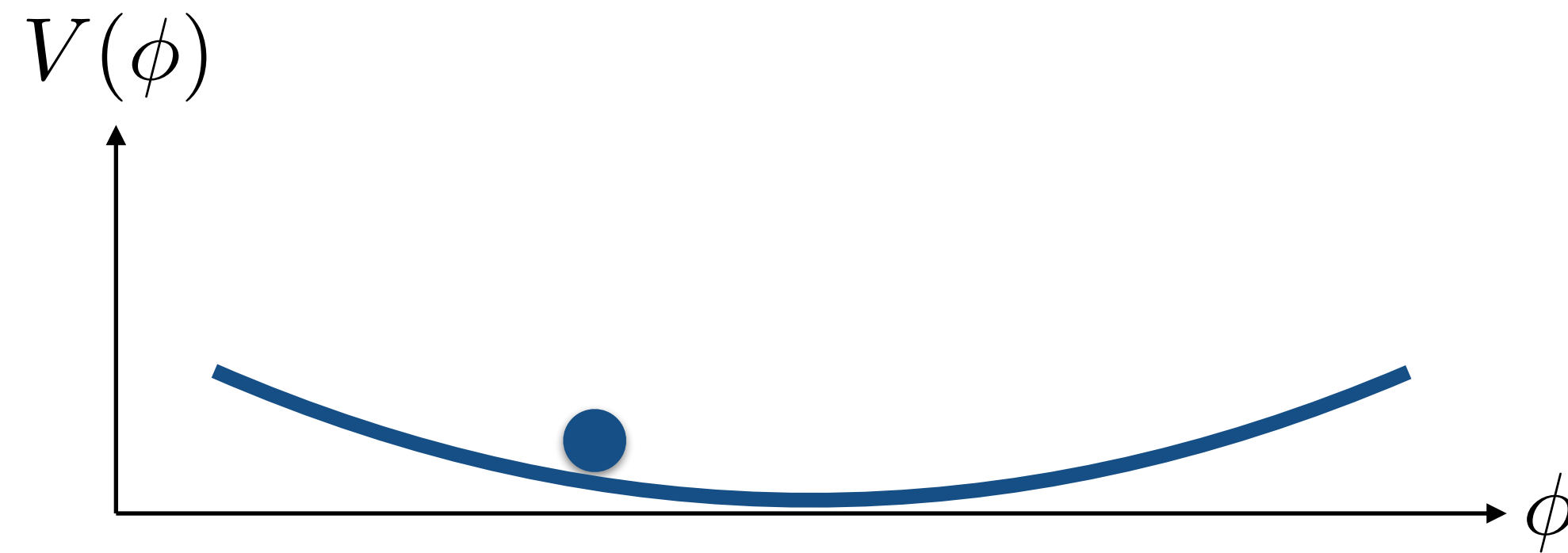
$$\phi_i \sim 10^{-2} M_{\text{Pl}} \left(\frac{10^{-20} \text{ eV}}{m} \right)^{1/4}$$

(for free scalar field)

Scalar Dark Matter Production in the early Universe

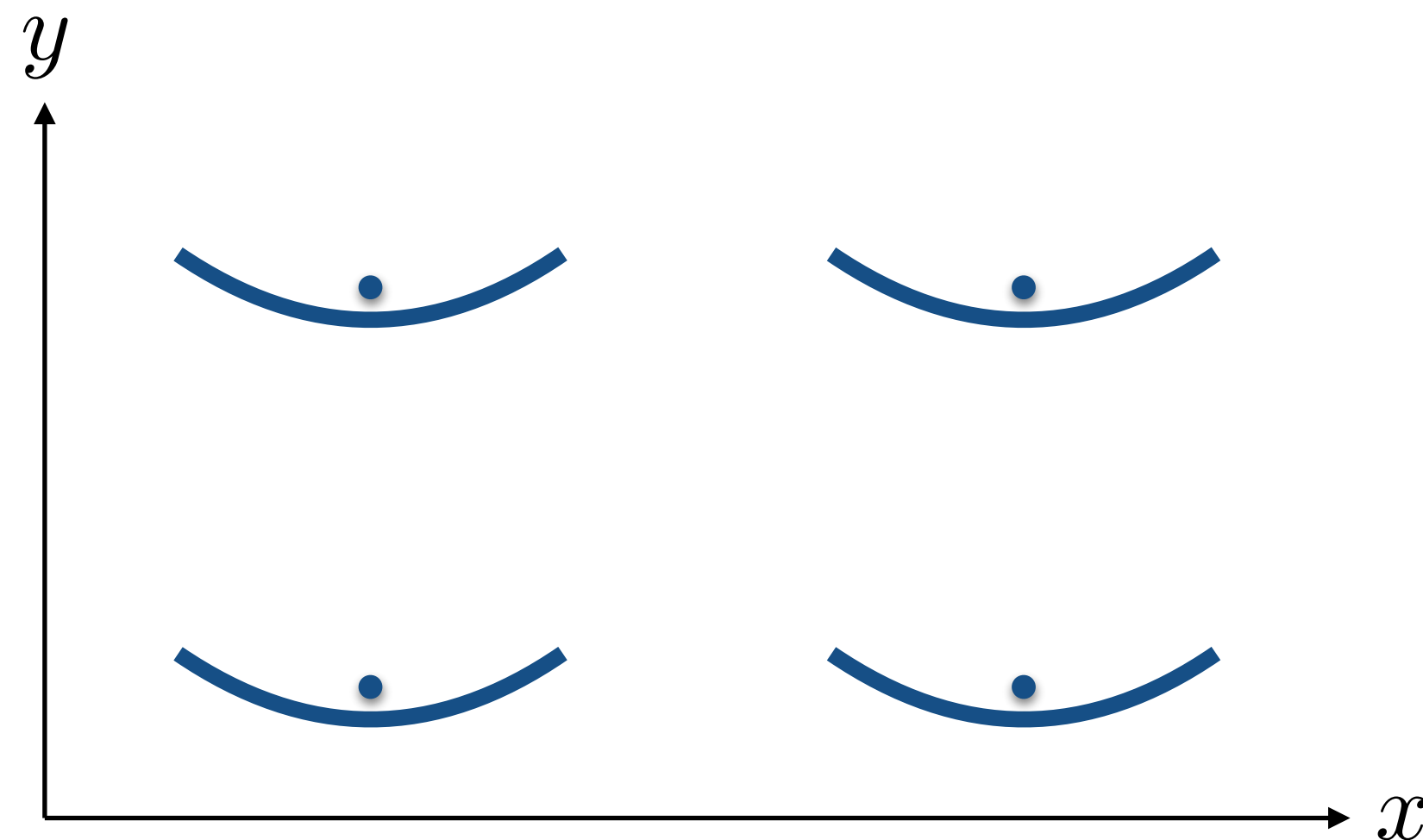
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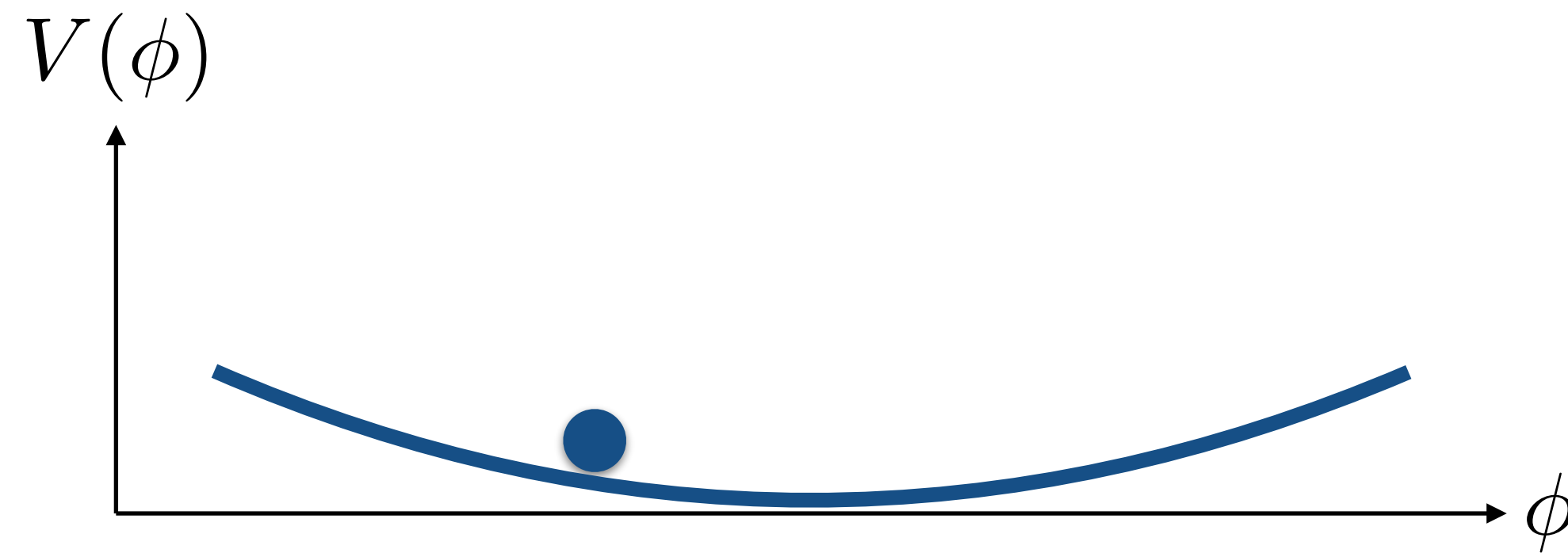
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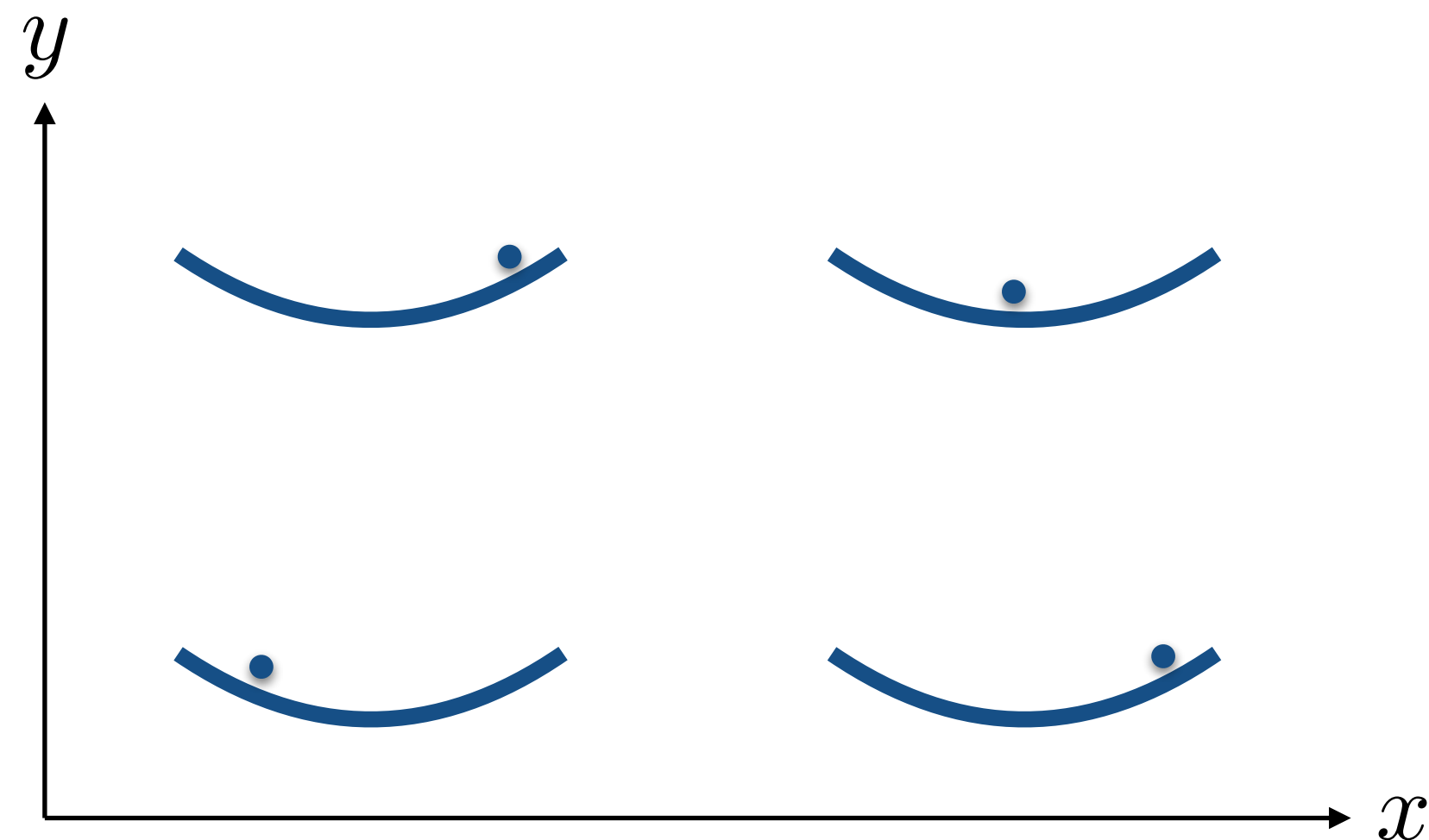
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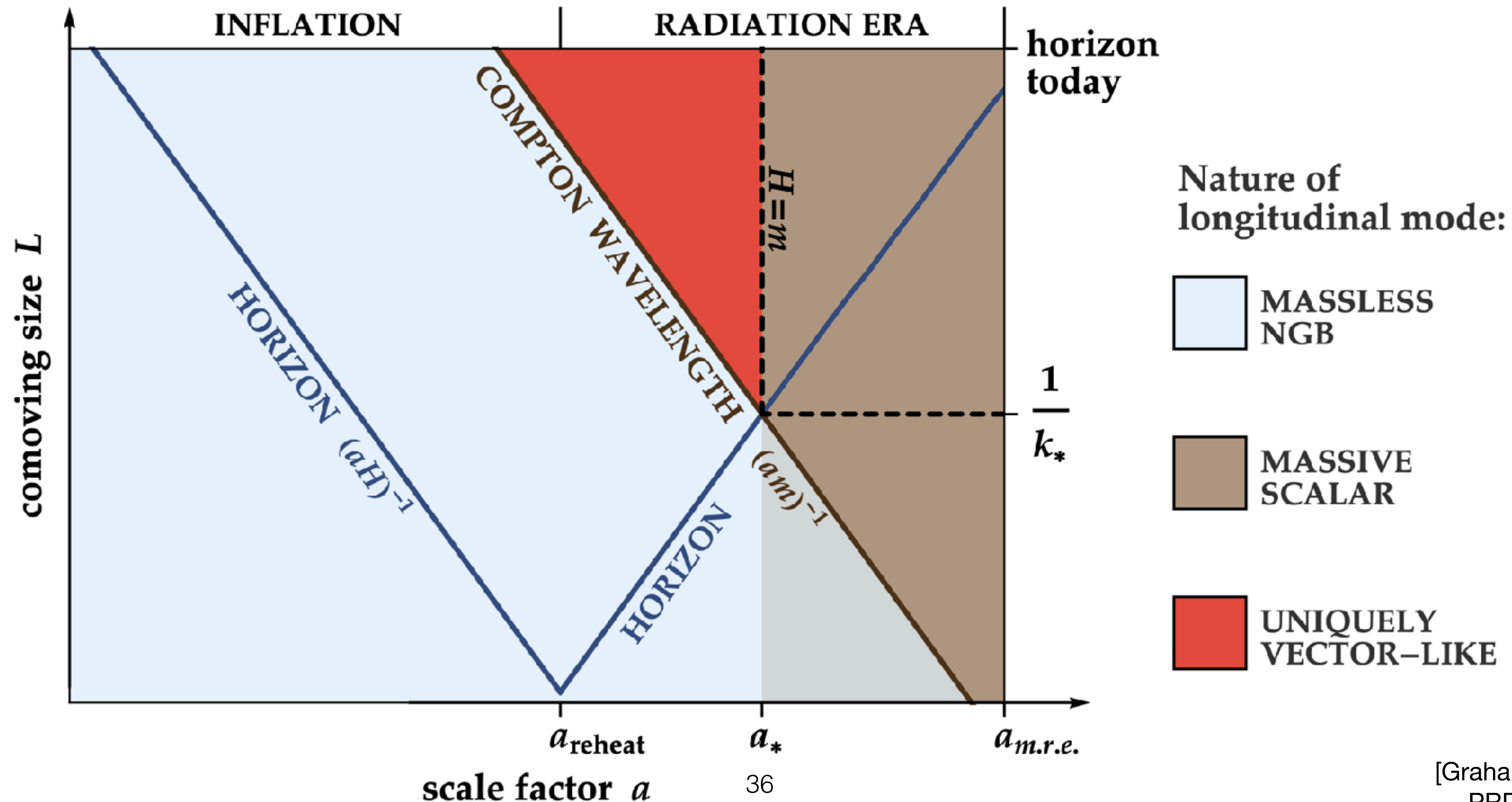


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(for free scalar field)

Vector Dark Matter Production in the early Universe

$$\mathcal{L} = -\frac{1}{4}F^{\mu\nu}F_{\mu\nu} - \frac{m^2}{2}A^\mu A_\nu \quad \frac{\Omega_{\text{vector}}}{\Omega_m} = \sqrt{\frac{m}{6 \times 10^{-6} \text{ eV}}} \left(\frac{H_I}{10^{14} \text{ GeV}} \right)^2$$



Motivation “Metric” for Dark Matter Theories

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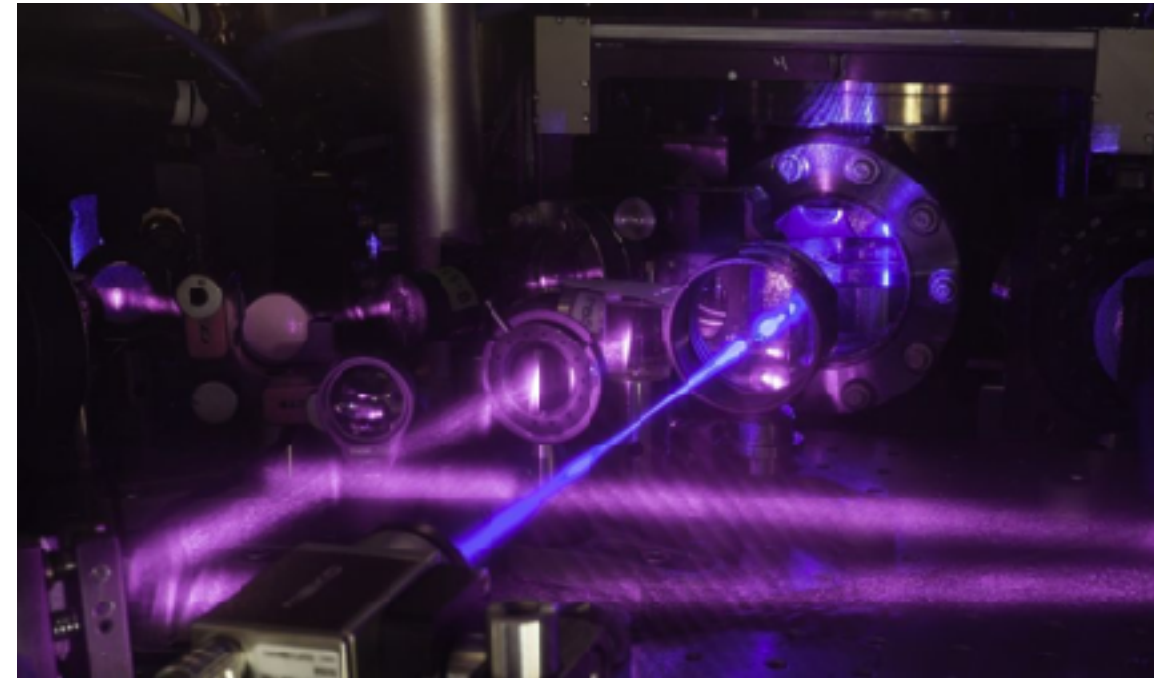
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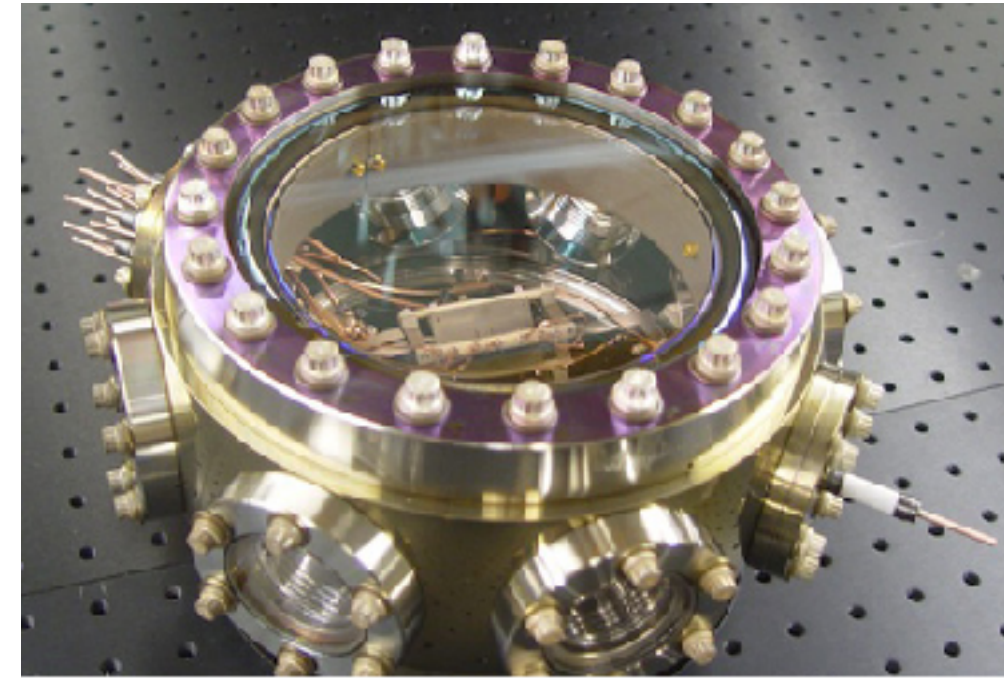
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Innumerable Probes

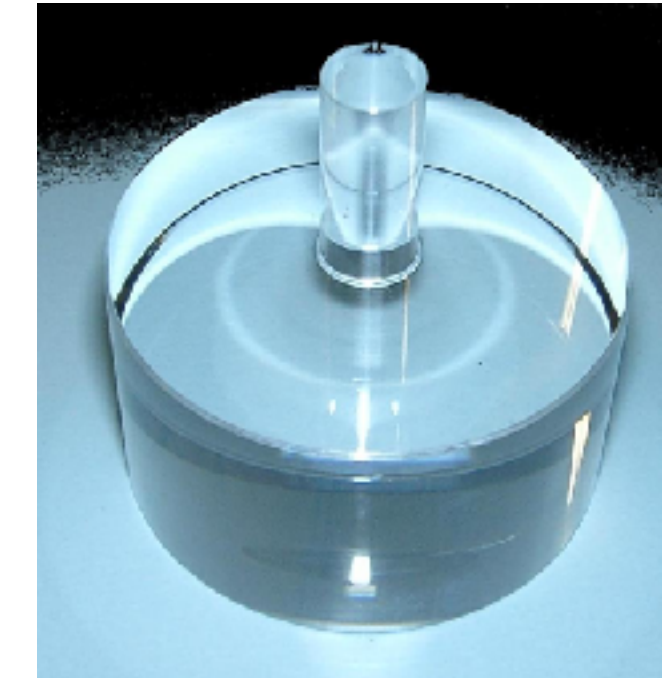
Atomic Clocks



Nuclear Clock



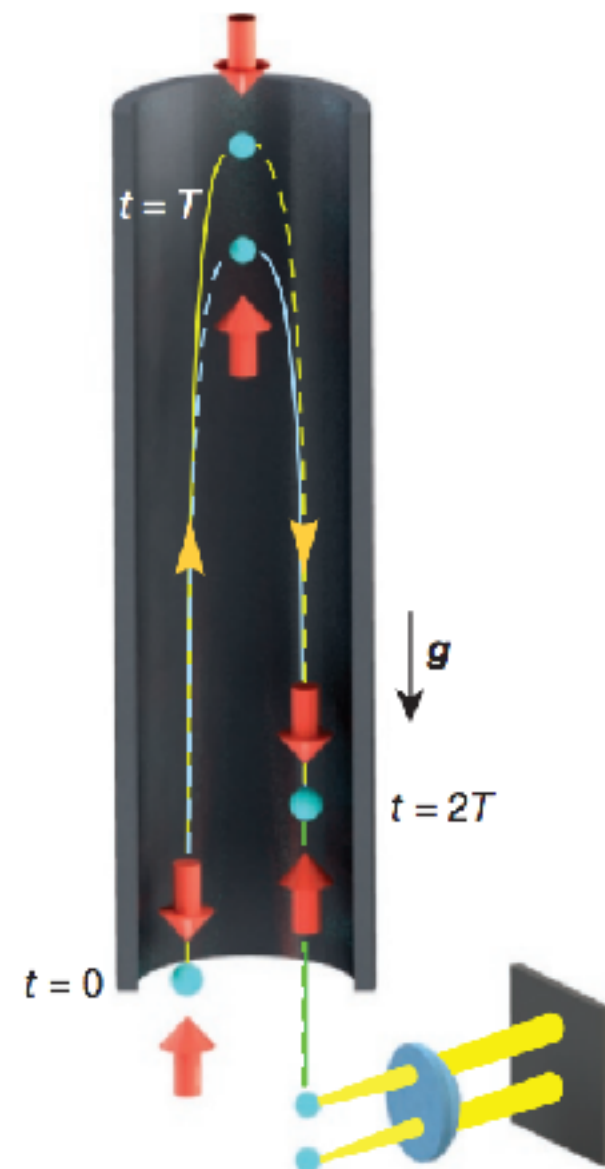
Acoustic Resonators



Molecular Resonators



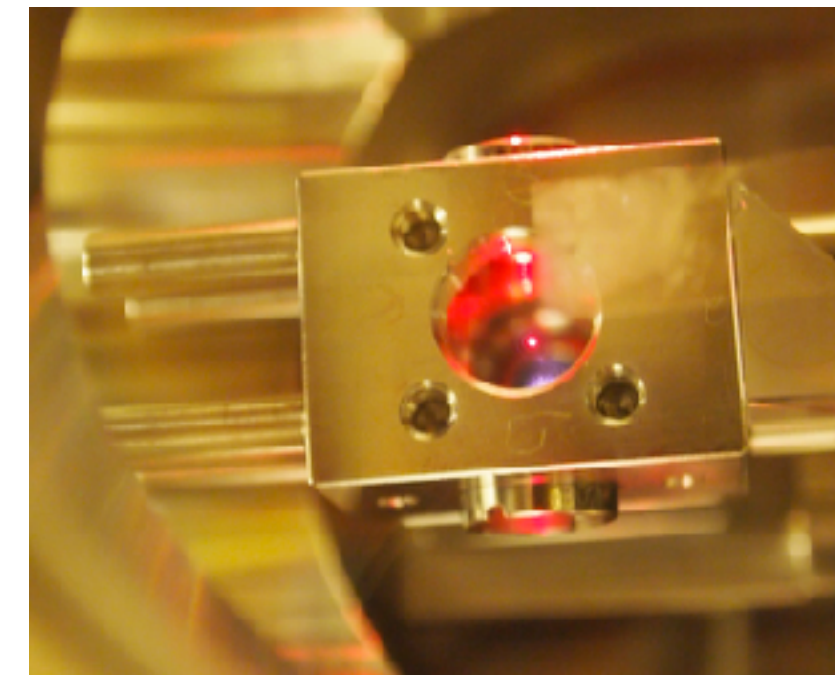
Atom Interferometry



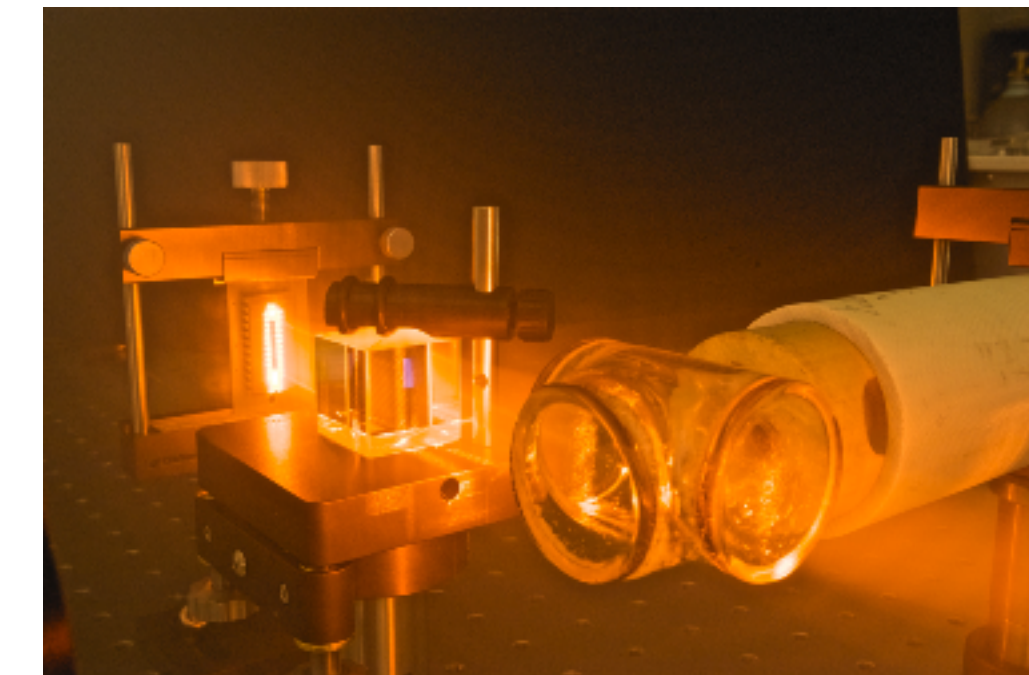
Laser Interferometry



Accelerometers

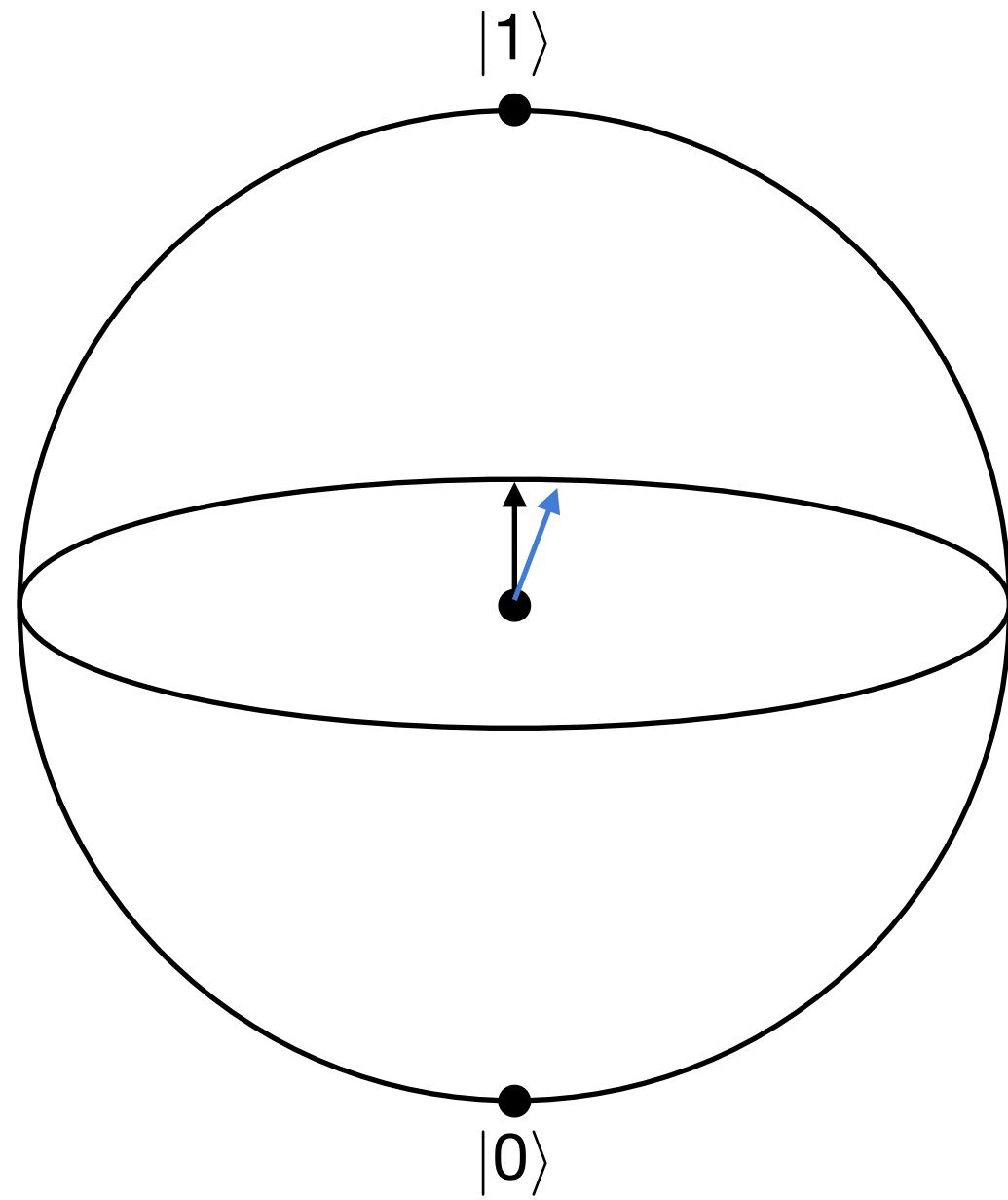


Spin Resonators

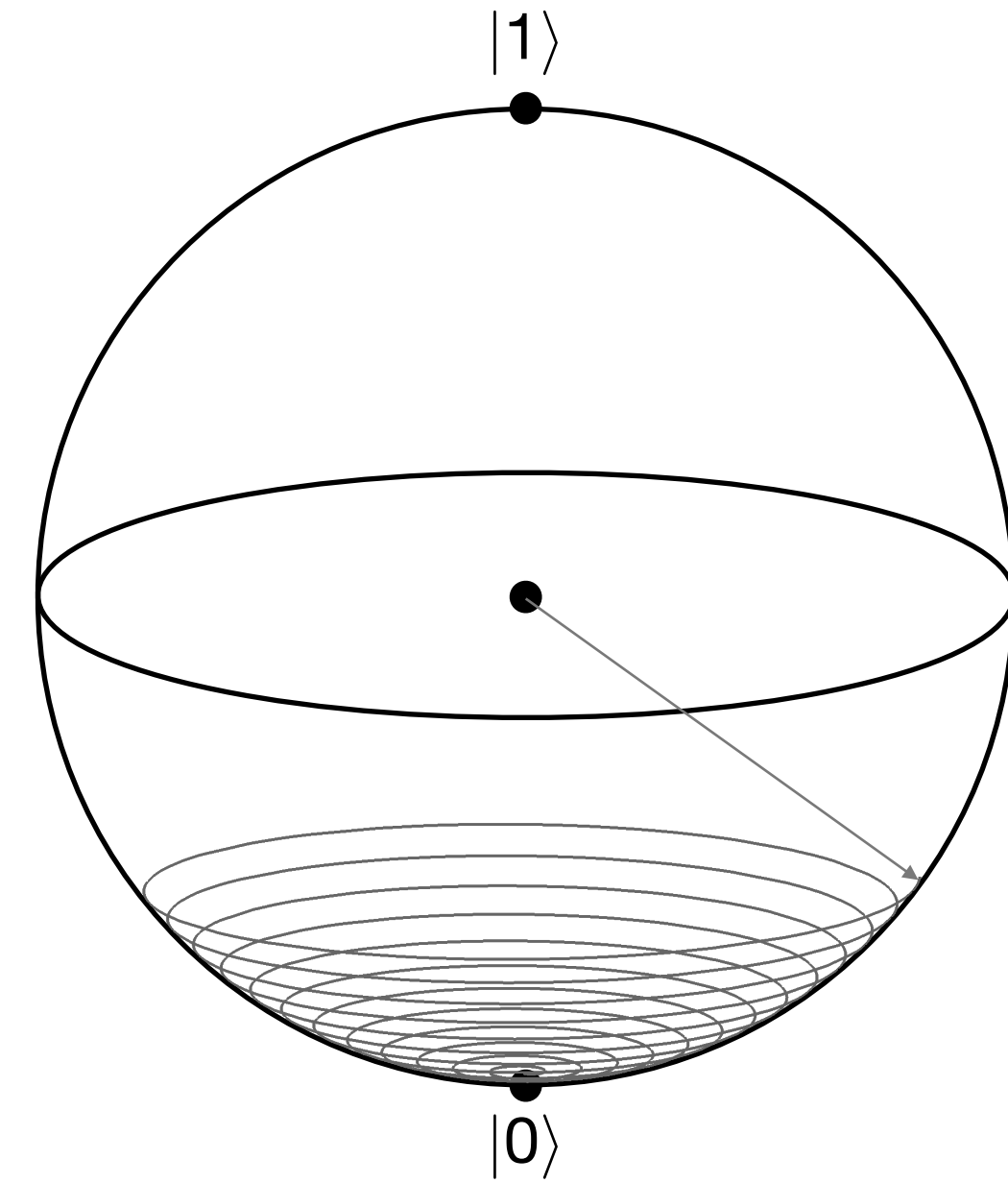
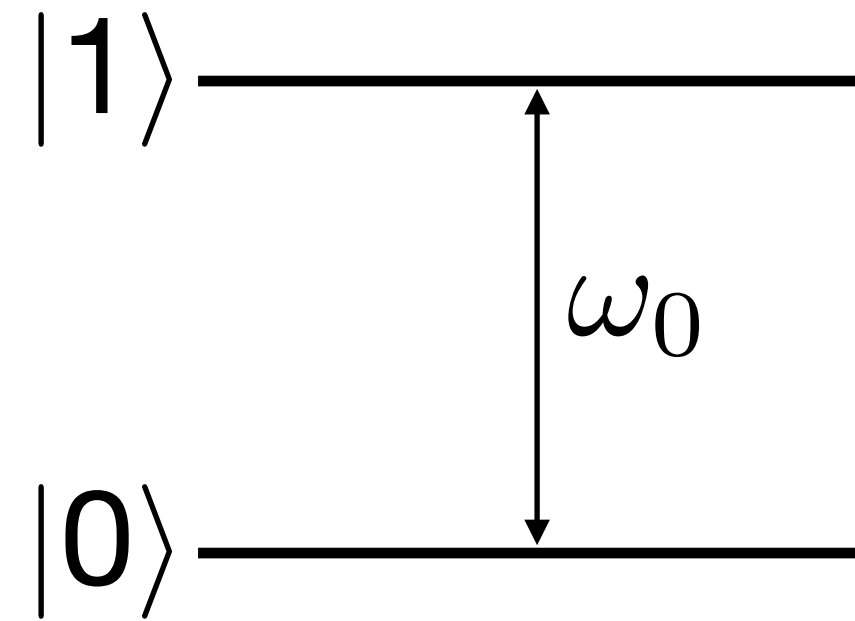


Precision Probe Classification

Two-Level System

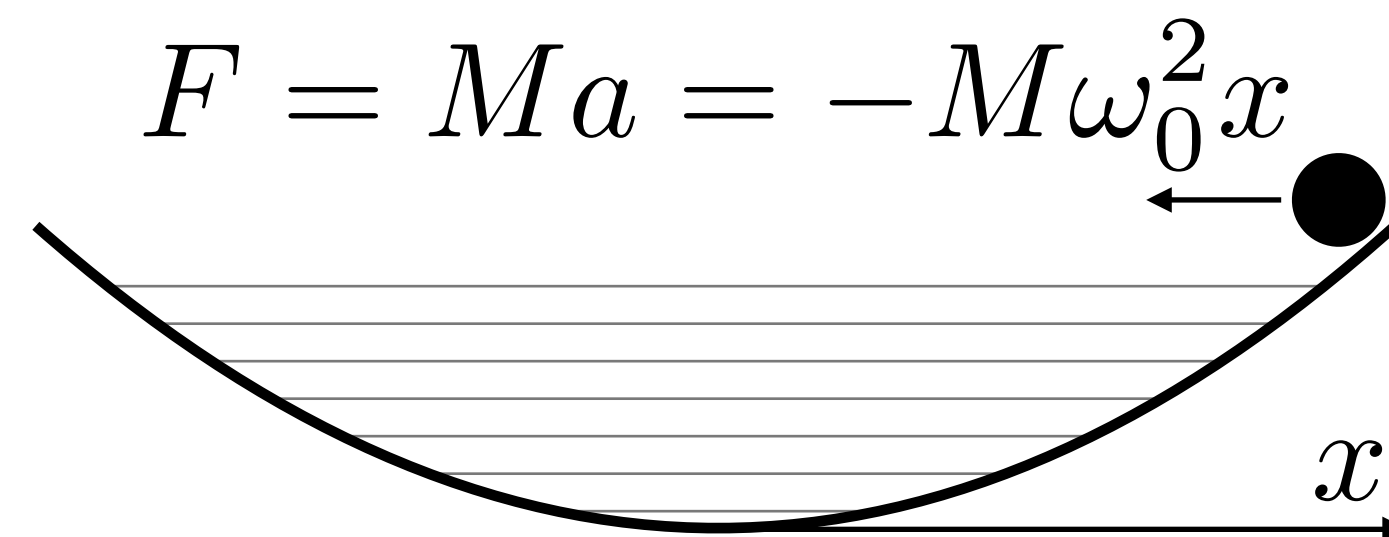


Interferometer

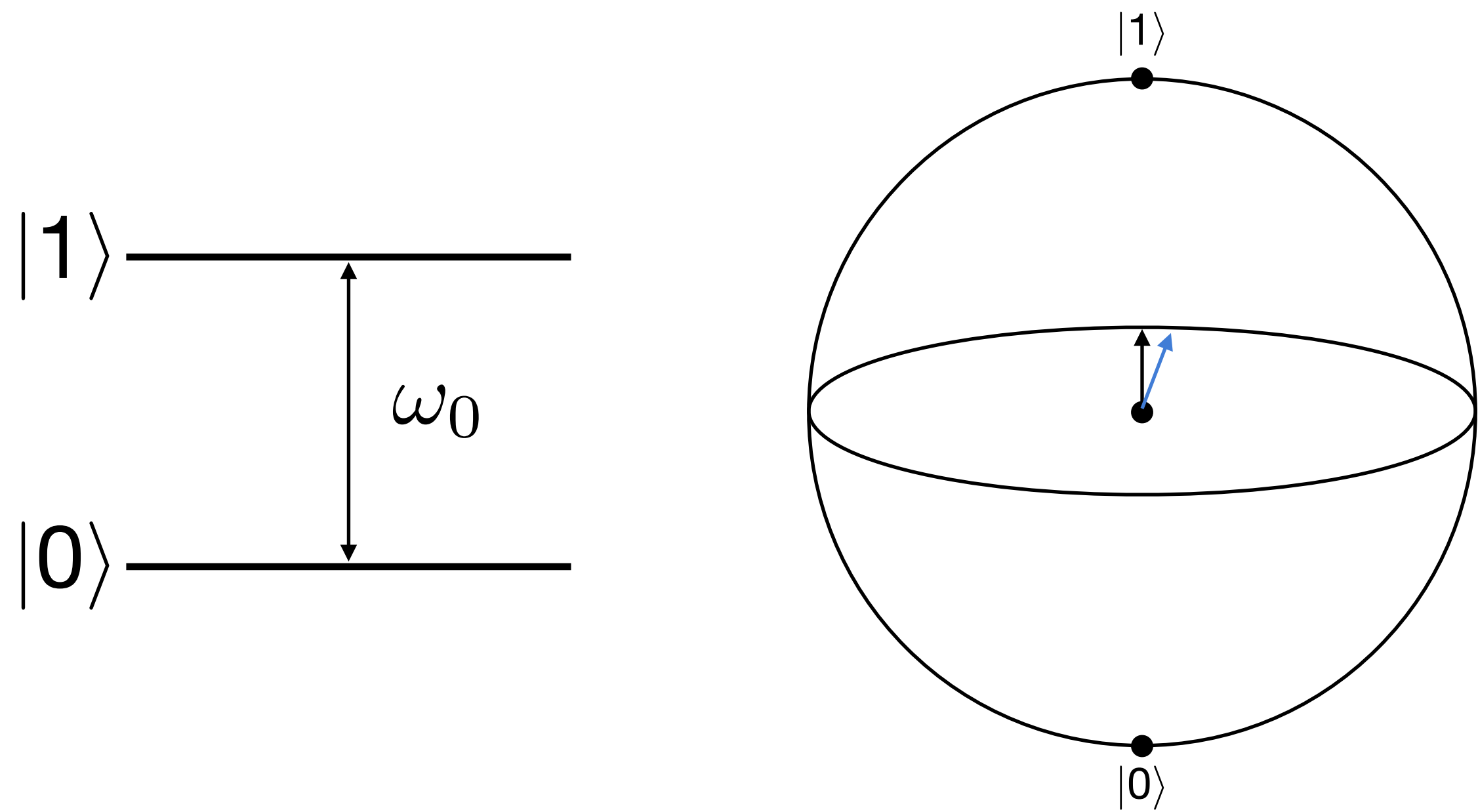


Resonator

Generalized Harmonic Oscillator



Two-Level Interferometer

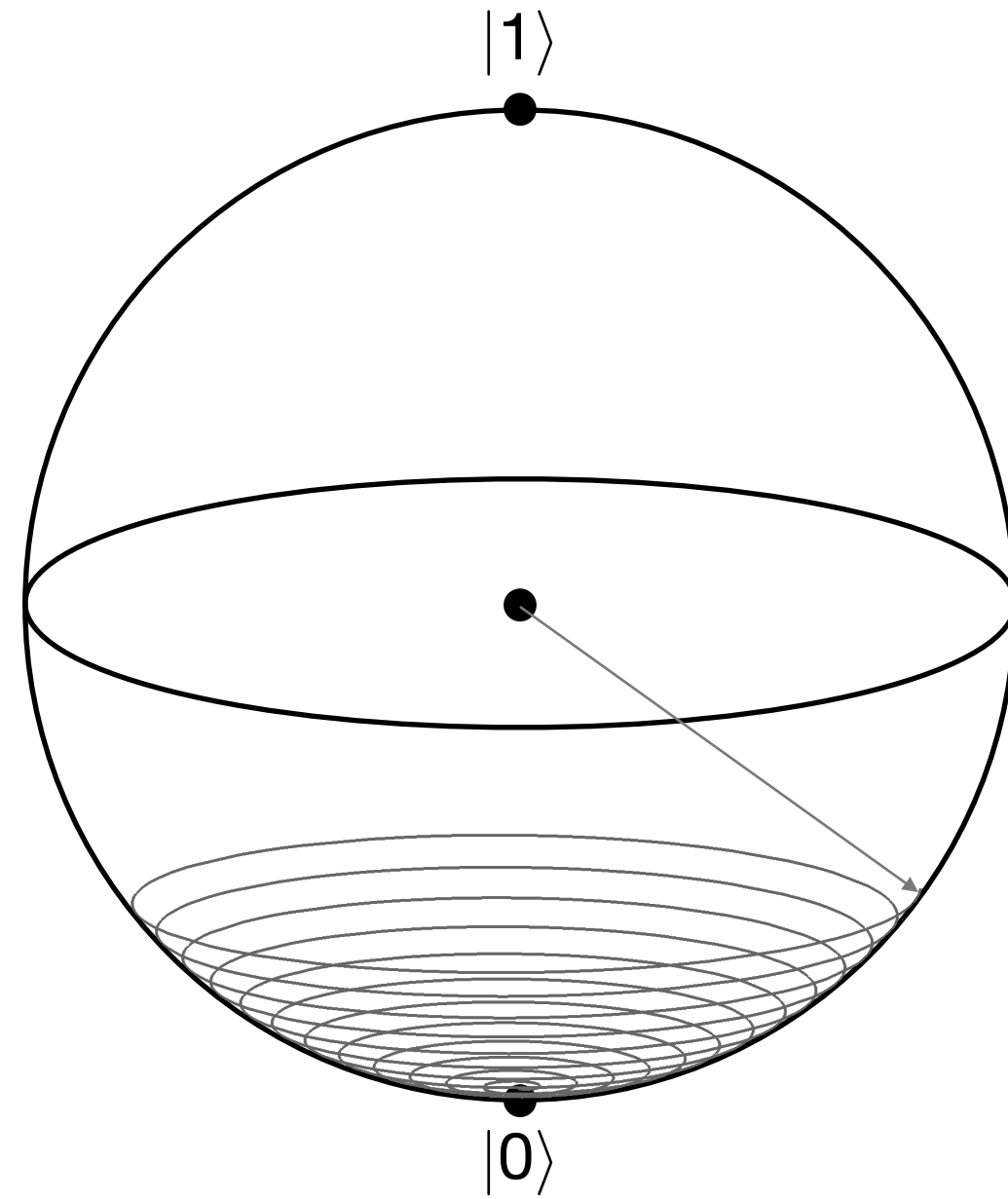
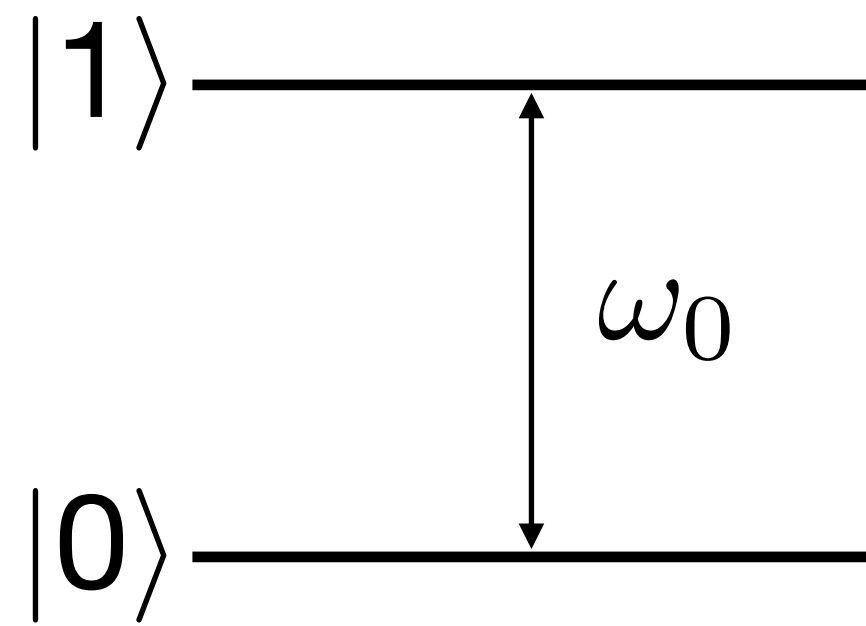


$$\left(|0\rangle + e^{i(\varphi + \Delta\varphi)} |1\rangle \right)^{\otimes N} \quad \sigma_\varphi = \frac{1}{\sqrt{N}}$$

$$\text{LIGO: } \Delta\varphi = h_{\text{strain}} k_\gamma L \quad \sigma_{h_{\text{strain}}} = \frac{1}{\sqrt{N}} \frac{1}{k_\gamma L}$$

$$\text{Clock: } \Delta\varphi = (\omega_0 - \omega) \tau \quad \sigma_{\frac{\Delta\omega_0}{\omega_0}} = \frac{1}{\sqrt{N}} \frac{1}{\omega_0 \tau}$$

Two-Level Resonator



Width: $\frac{\omega_0}{Q}$

On resonance: $|0\rangle - (i\langle\Delta H\rangle t)e^{i\omega_0 t}|1\rangle$

Transverse readout:

$$\langle 0| + \langle 1|$$

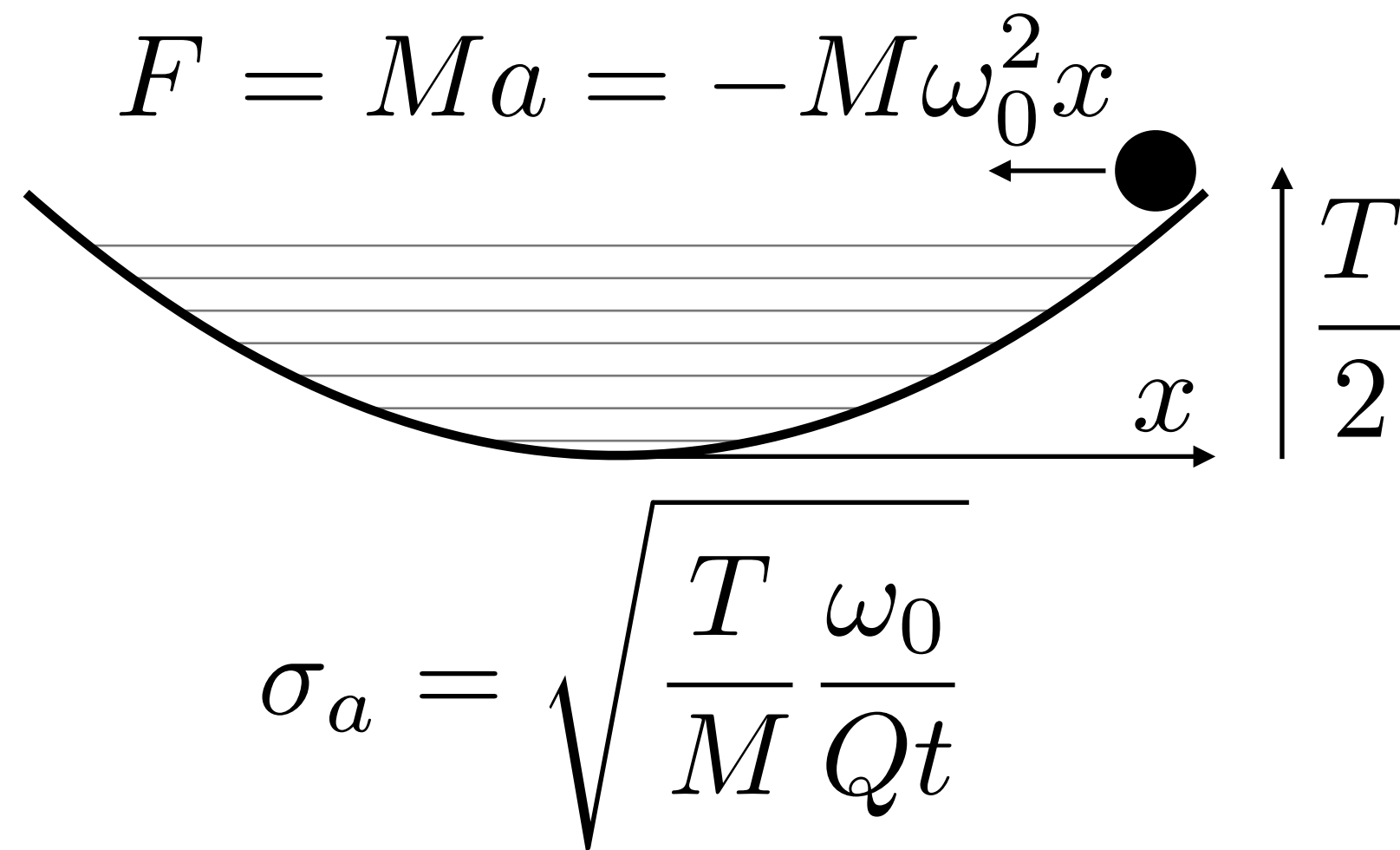
$$\sigma_{\Delta H} = \frac{\omega_0}{Q\sqrt{N}}$$

Absorption:

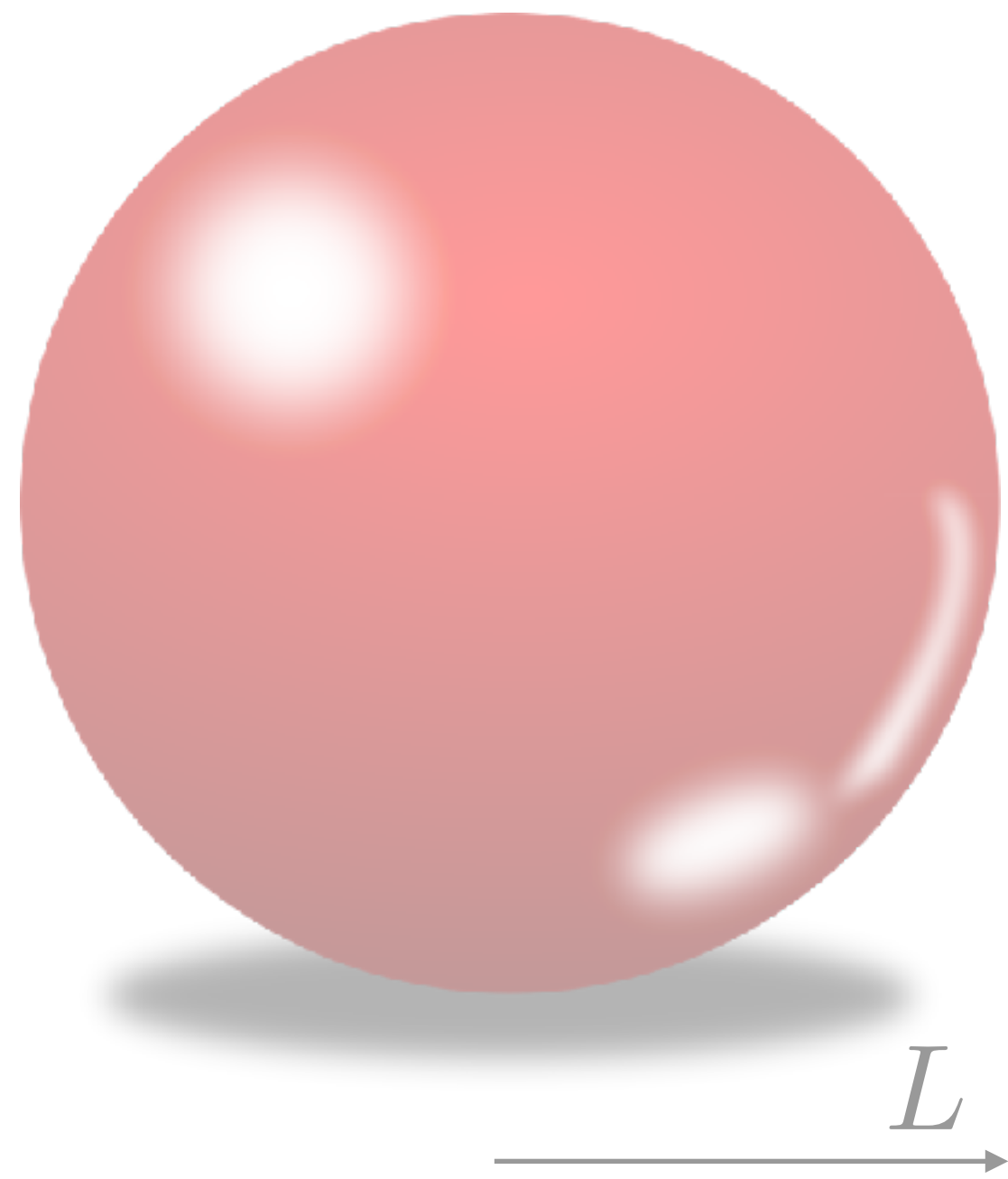
$$\Gamma_{\text{absorption}} = \frac{Q|\langle\Delta H\rangle|^2}{\omega_0}$$

$$\sigma_{\Delta H} = \sqrt{\frac{\omega_0\sigma_{\Gamma}}{QN}}$$

Generalized Harmonic Oscillator



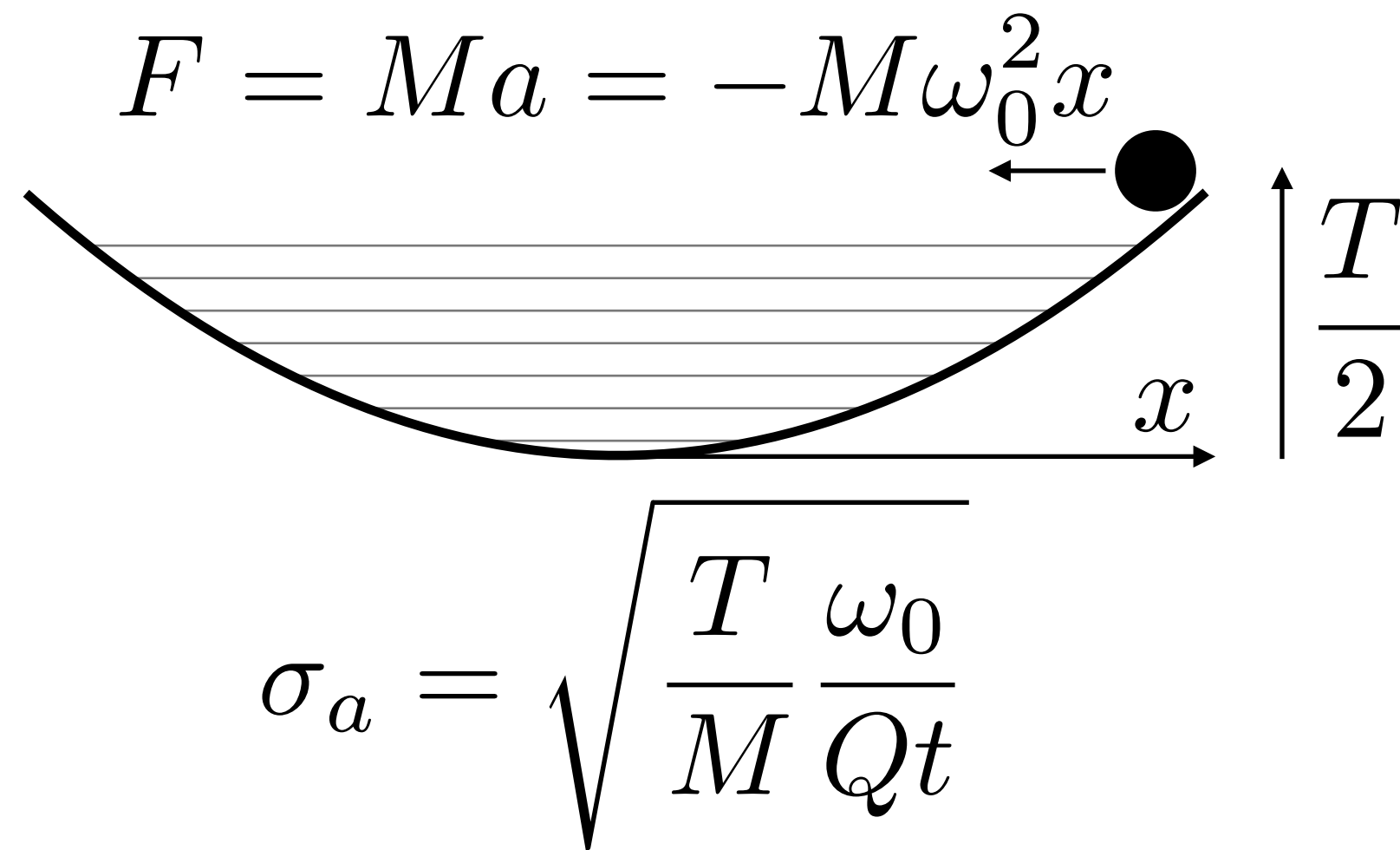
general for *any* linear system



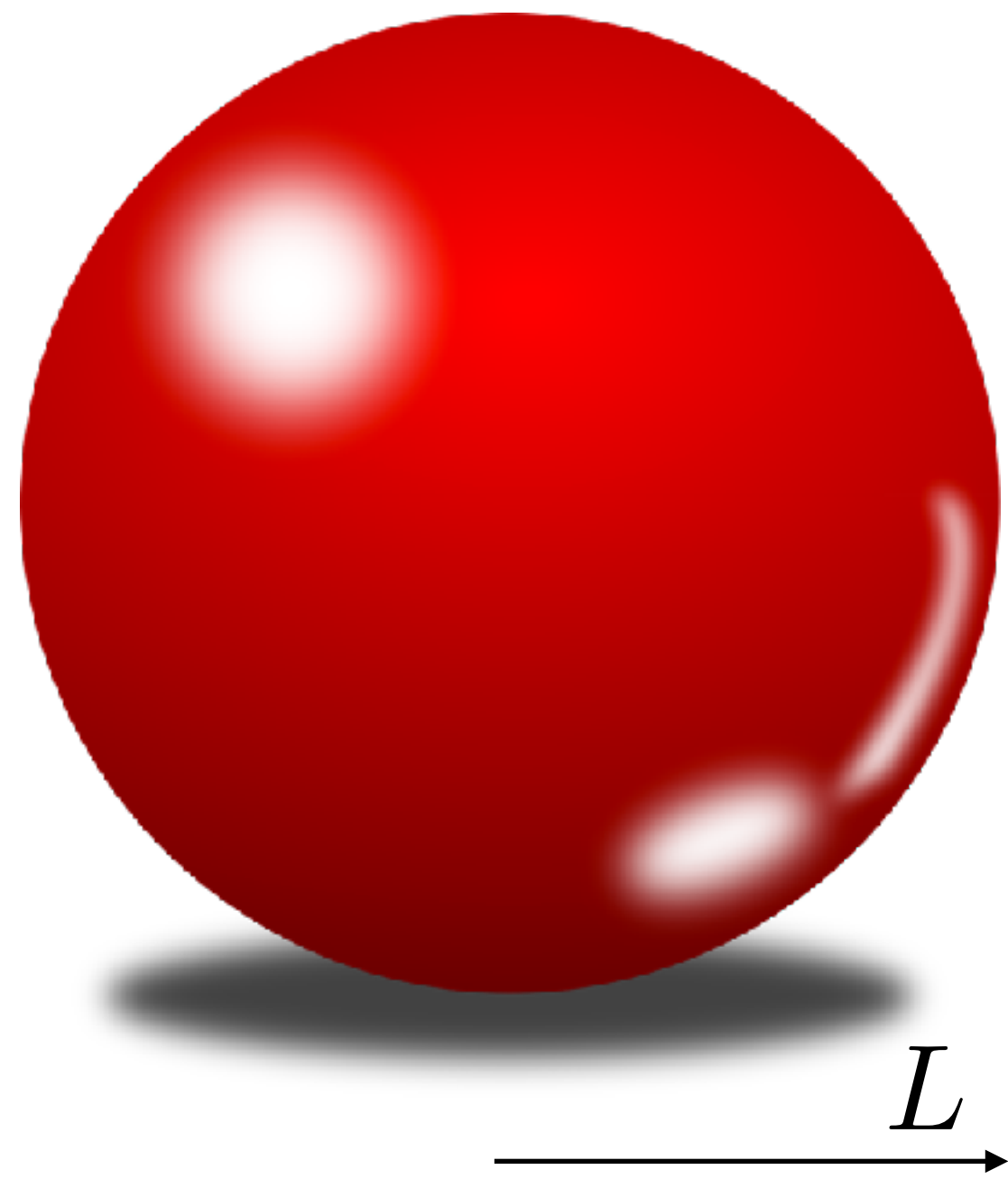
$$a = h_{\text{strain}} \omega^2 L \quad \omega_0 = \frac{c_s}{L}$$

$$\sigma_{h_{\text{strain}}} = \sqrt{\frac{T}{M} \frac{1}{Q c_s^2} \frac{\omega_0^4}{\omega^4} \frac{1}{\omega_0 t}}$$

Generalized Harmonic Oscillator



general for *any* linear system



$$a = h_{\text{strain}} \omega^2 L \quad \omega_0 = \frac{c_s}{L}$$

$$\sigma_{h_{\text{strain}}} = \sqrt{\frac{T}{M} \frac{1}{Q c_s^2} \frac{\omega_0^4}{\omega^4} \frac{1}{\omega_0 t}}$$

Where is the Precision?

Spacetime coherence

$$\lambda_{\text{coh}} \sim \frac{1}{m\sigma_v} \quad \tau_{\text{coh}} \sim \frac{1}{m\sigma_v^2}$$

Small dimensionless numbers

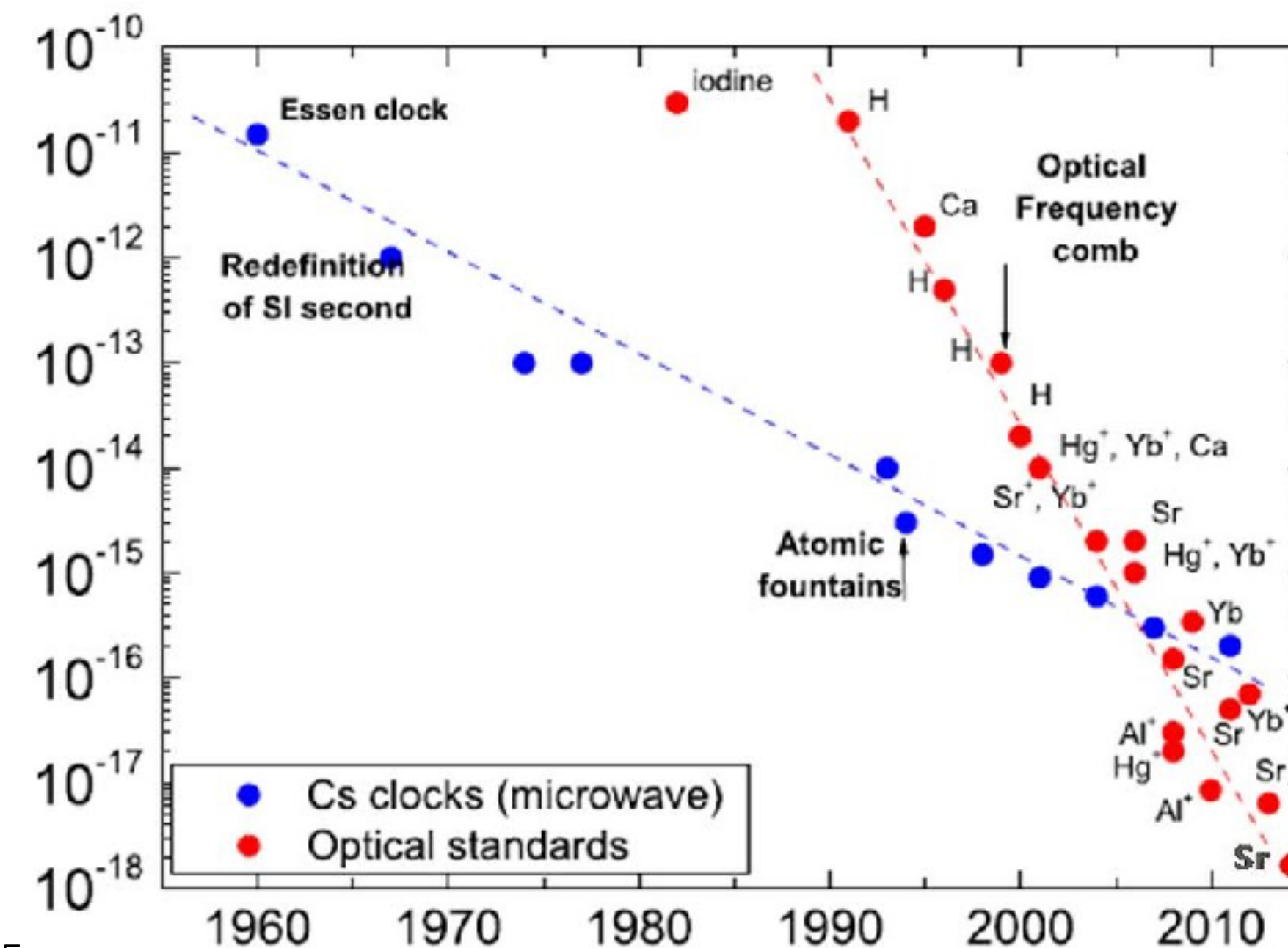
$$\frac{1}{\sqrt{N}} \quad \frac{1}{N} \quad \frac{1}{Q} \quad \frac{T}{M}$$

Large dimensionless charges

$$\frac{M}{m_N} \quad k_\gamma L \quad \omega_0 \tau \quad eBA$$

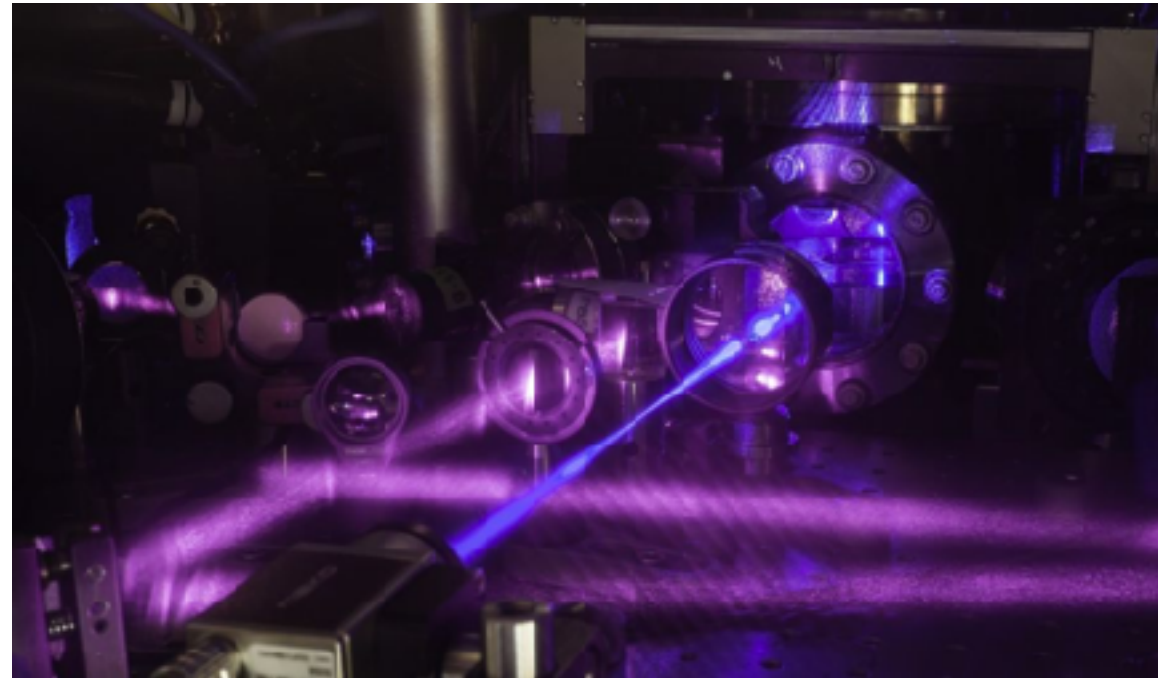
$$\frac{\rho_{\text{DM}}}{m^4}$$

Engineering marvel

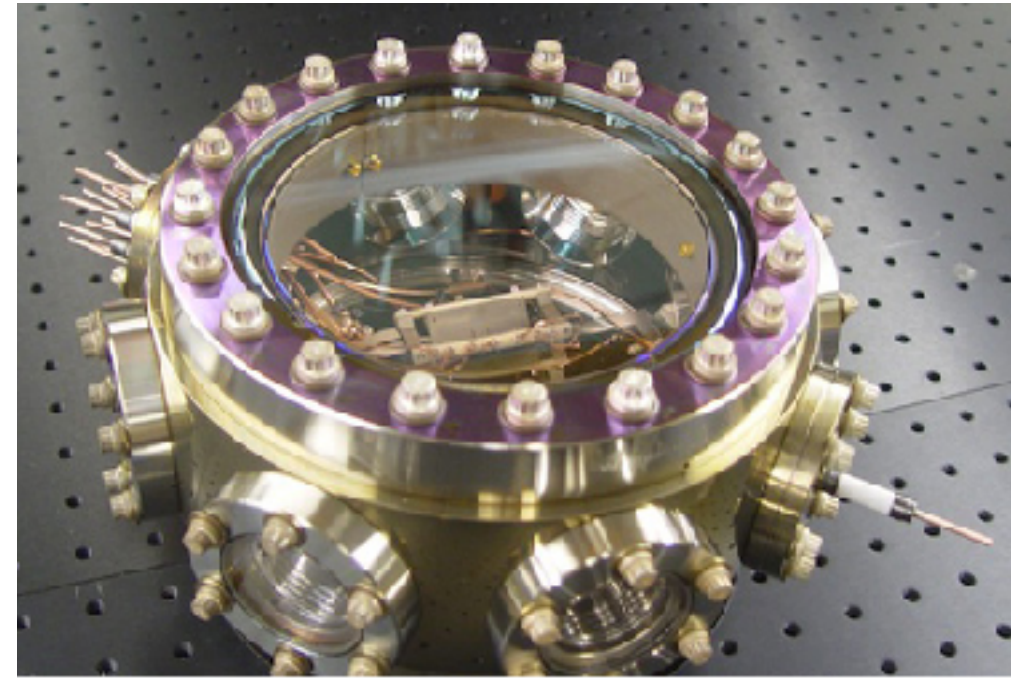


Innumerable Probes

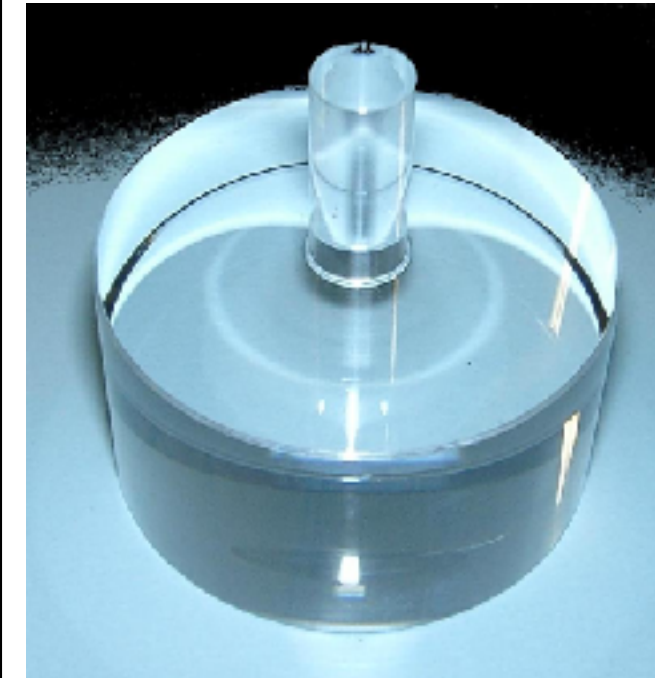
Atomic Clocks



Nuclear Clock



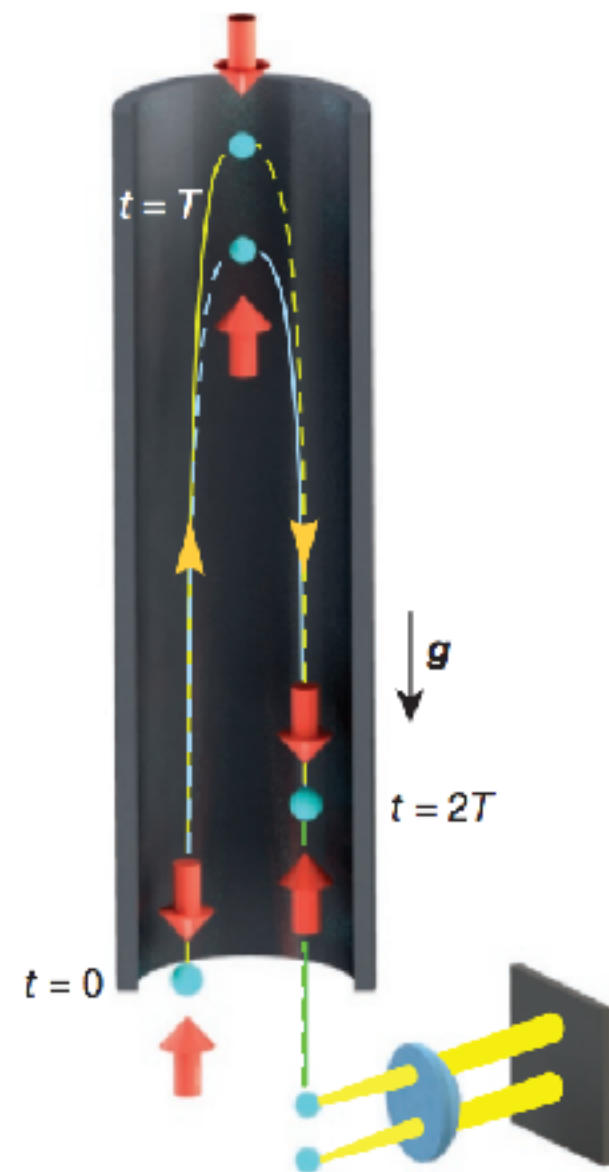
Acoustic Resonators



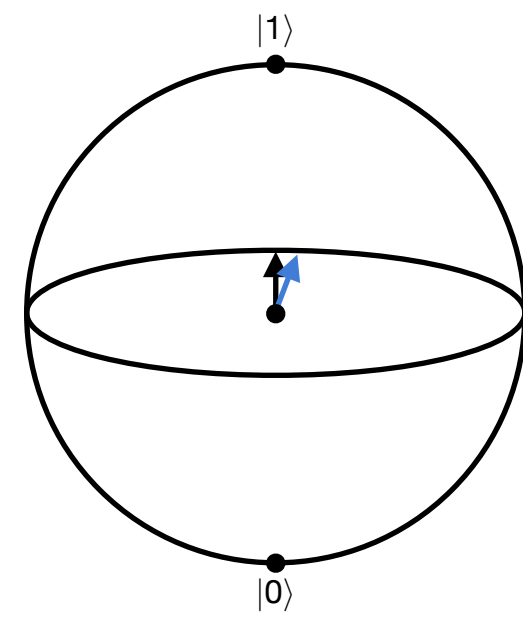
Molecular Resonators



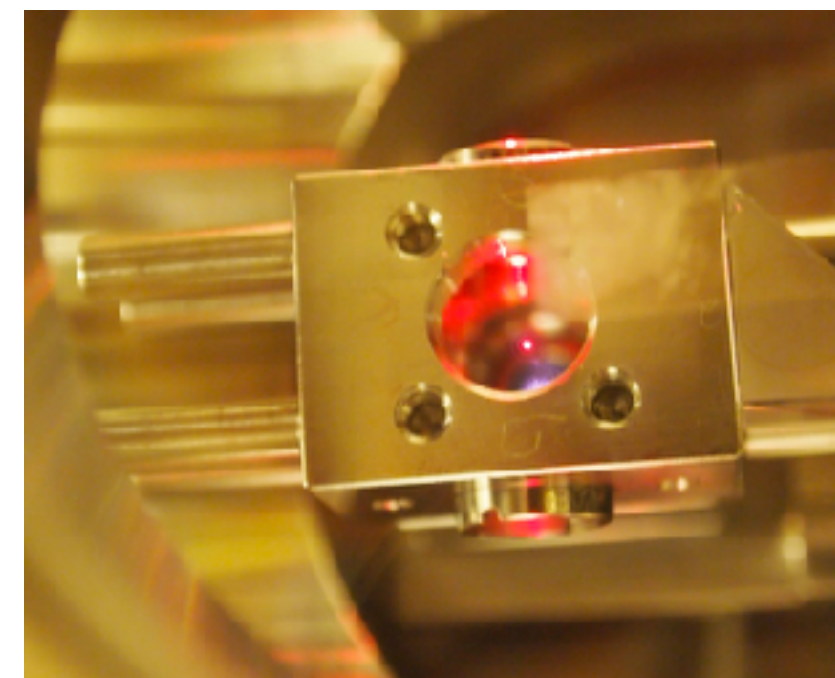
Atom Interferometry



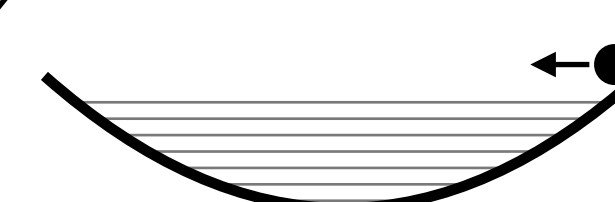
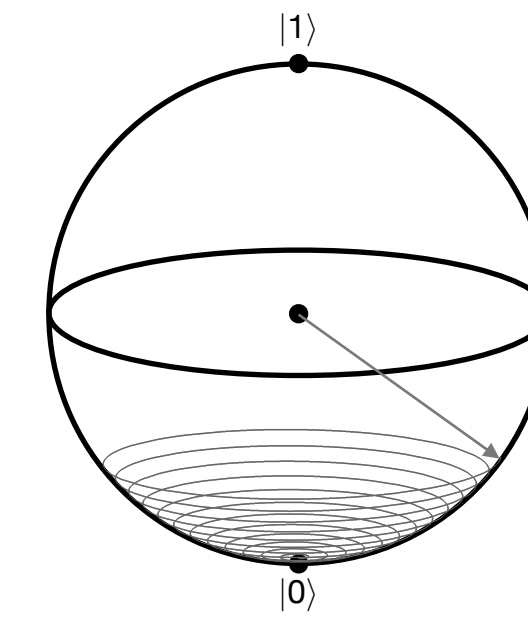
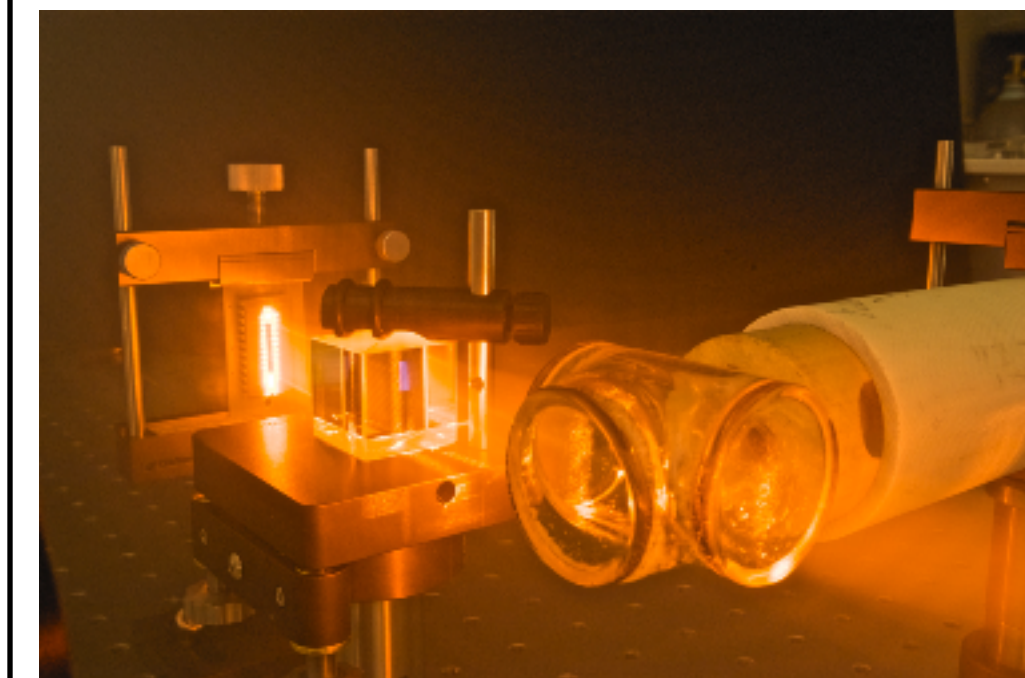
Laser Interferometry



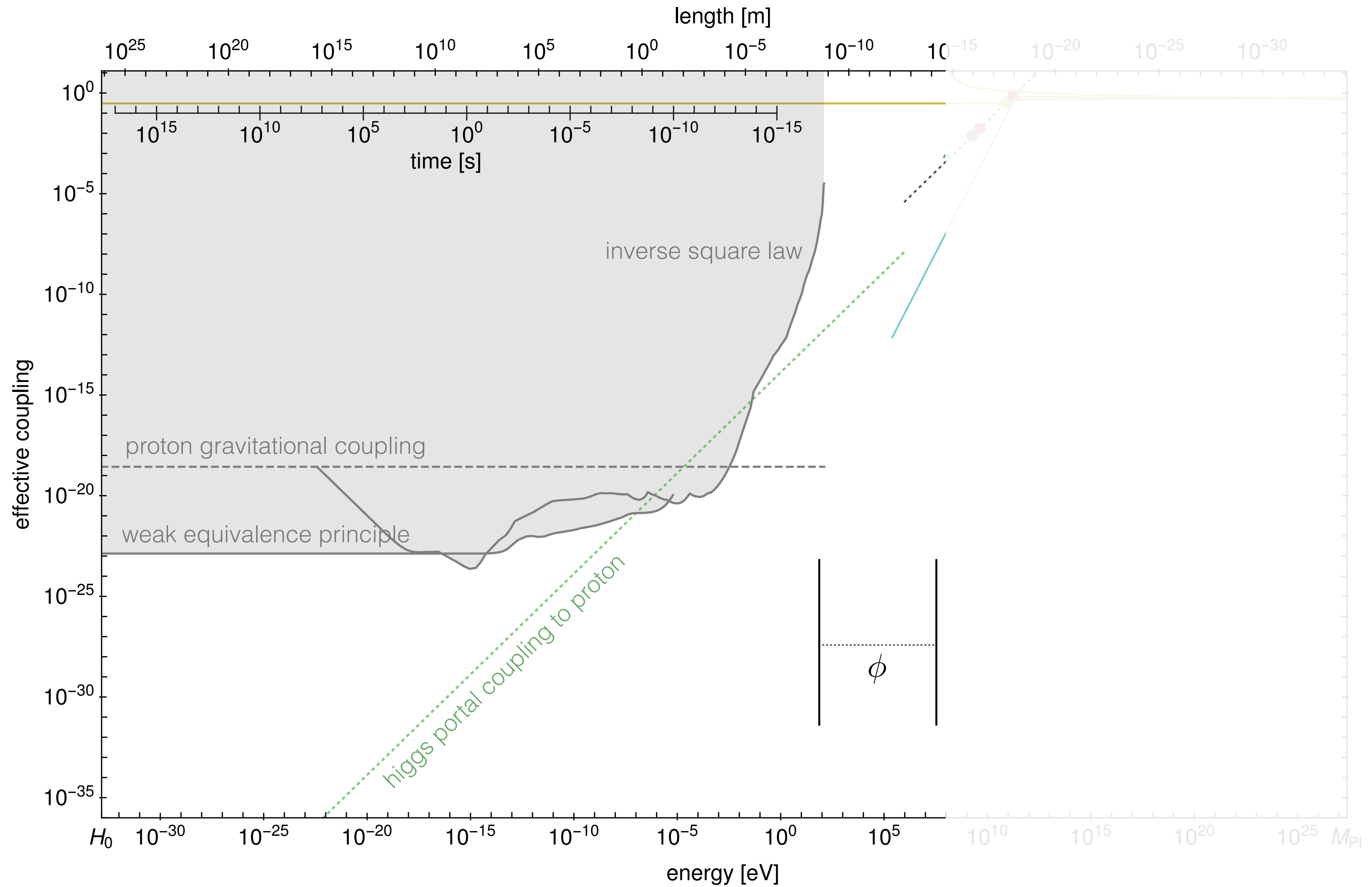
Accelerometers



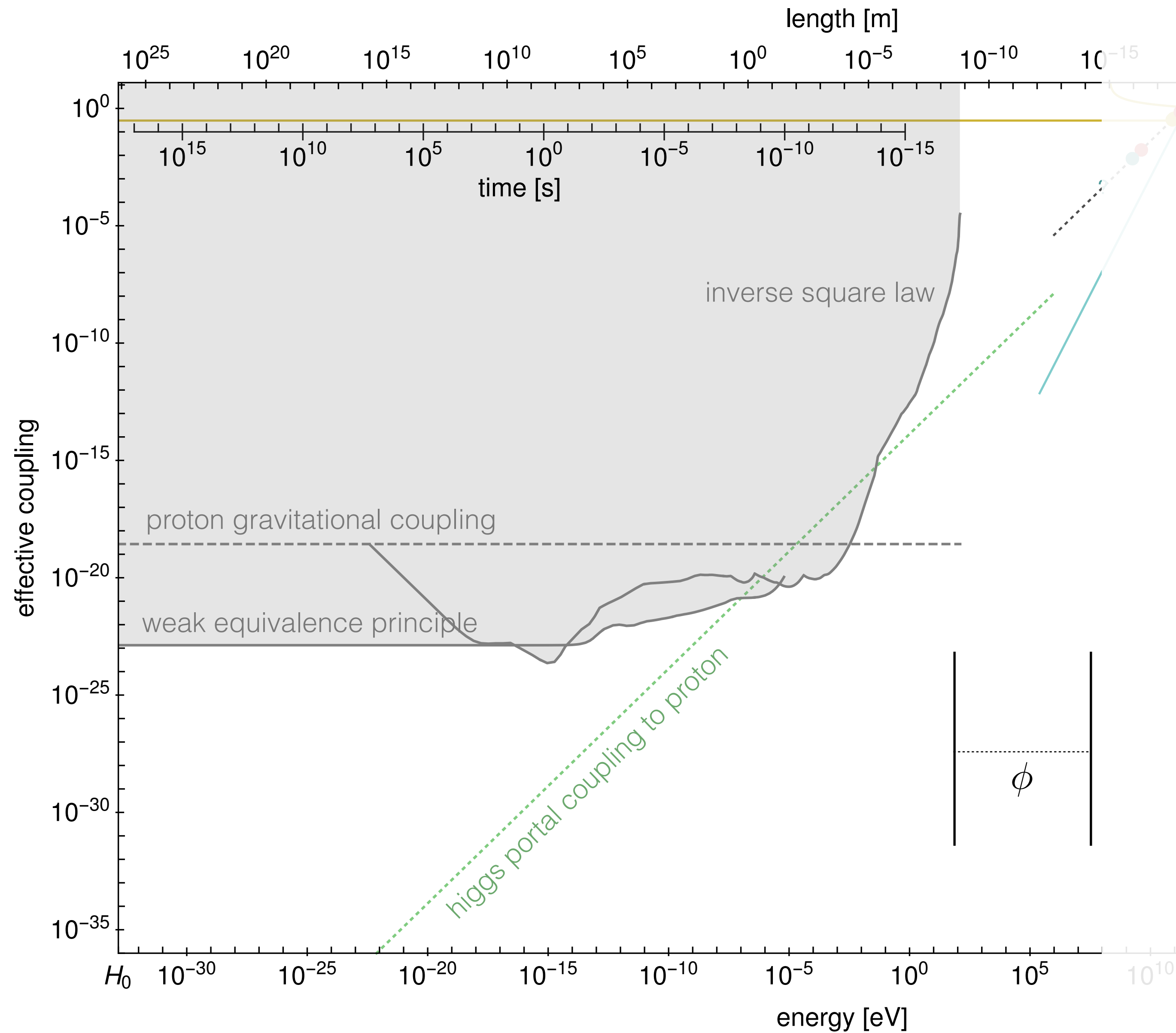
Spin Resonators



Tests of Gravity



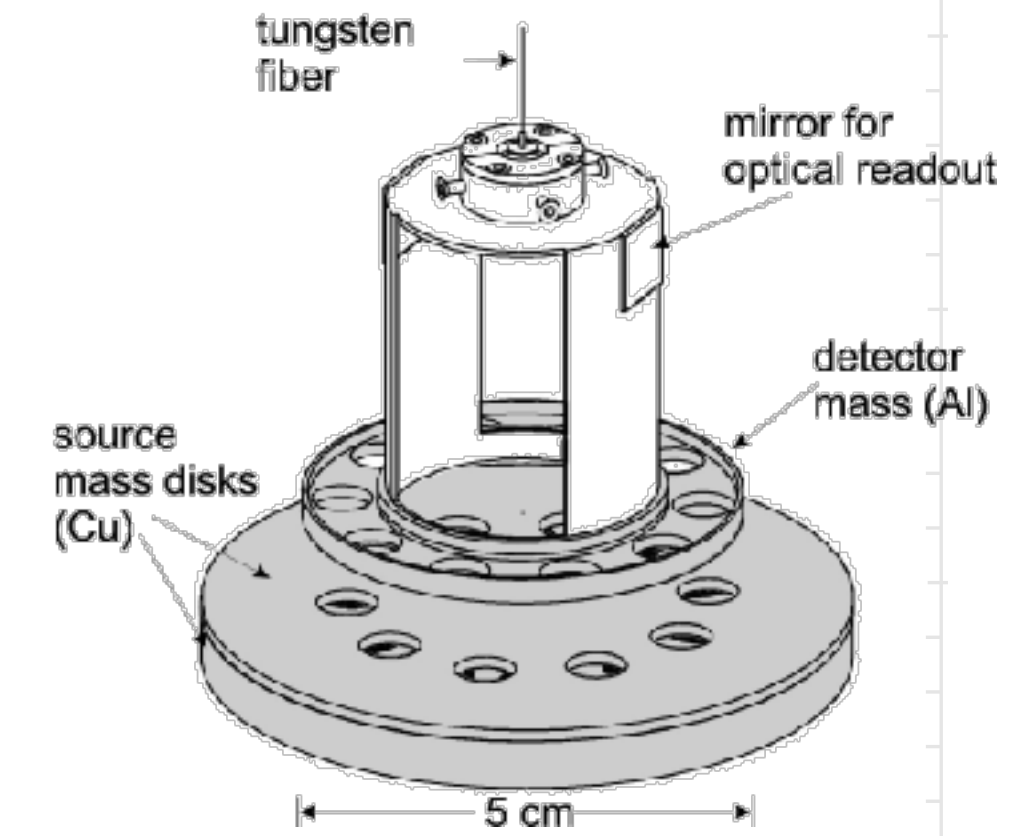
Tests of Gravity



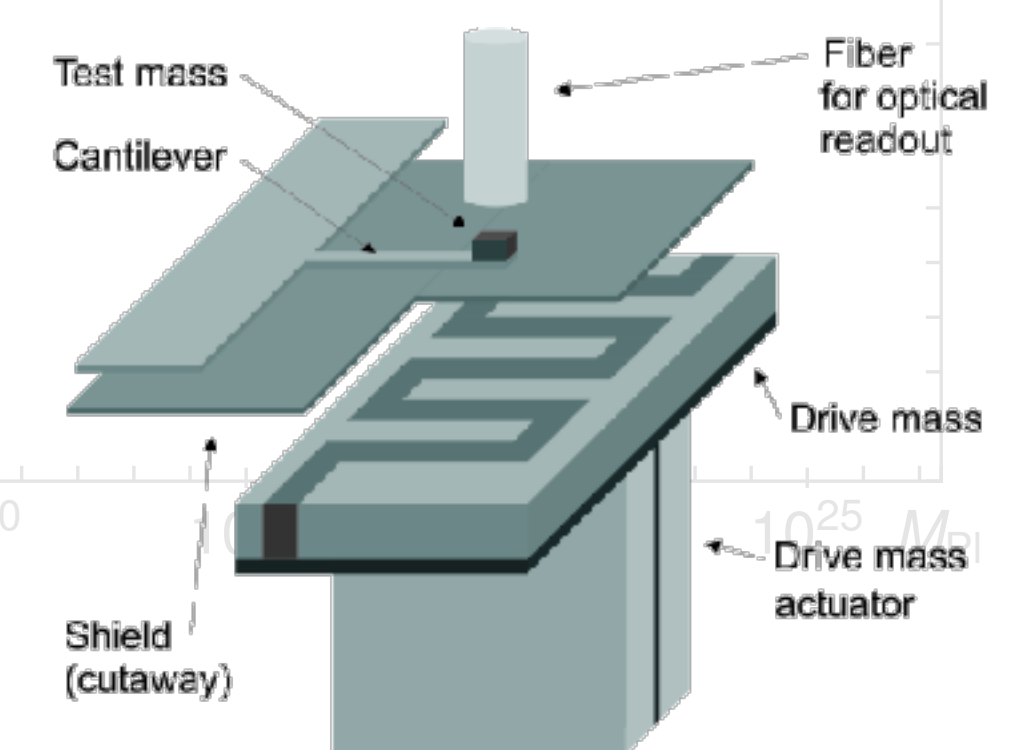
Lunar Laser Ranging



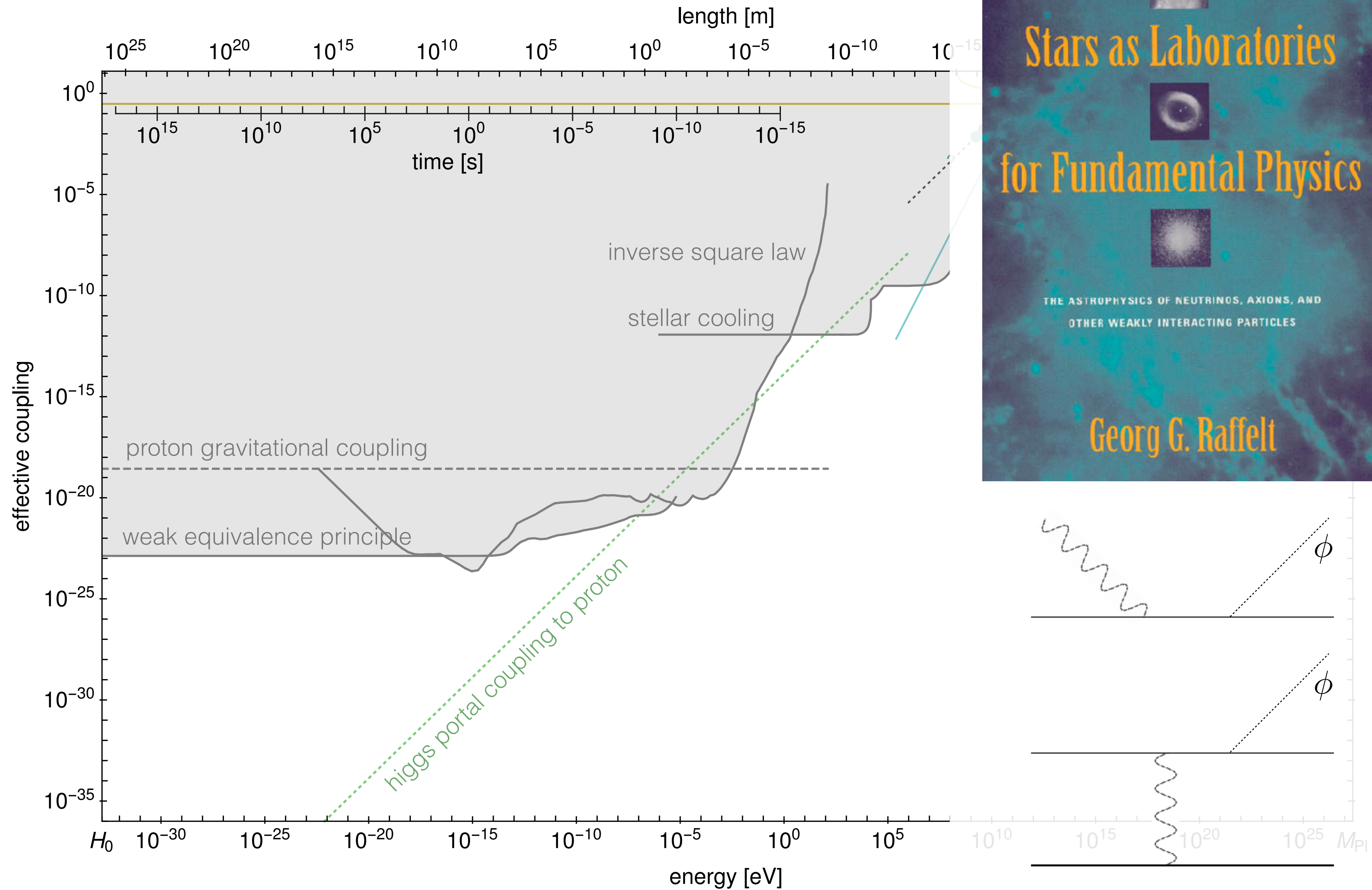
Torsion Balance



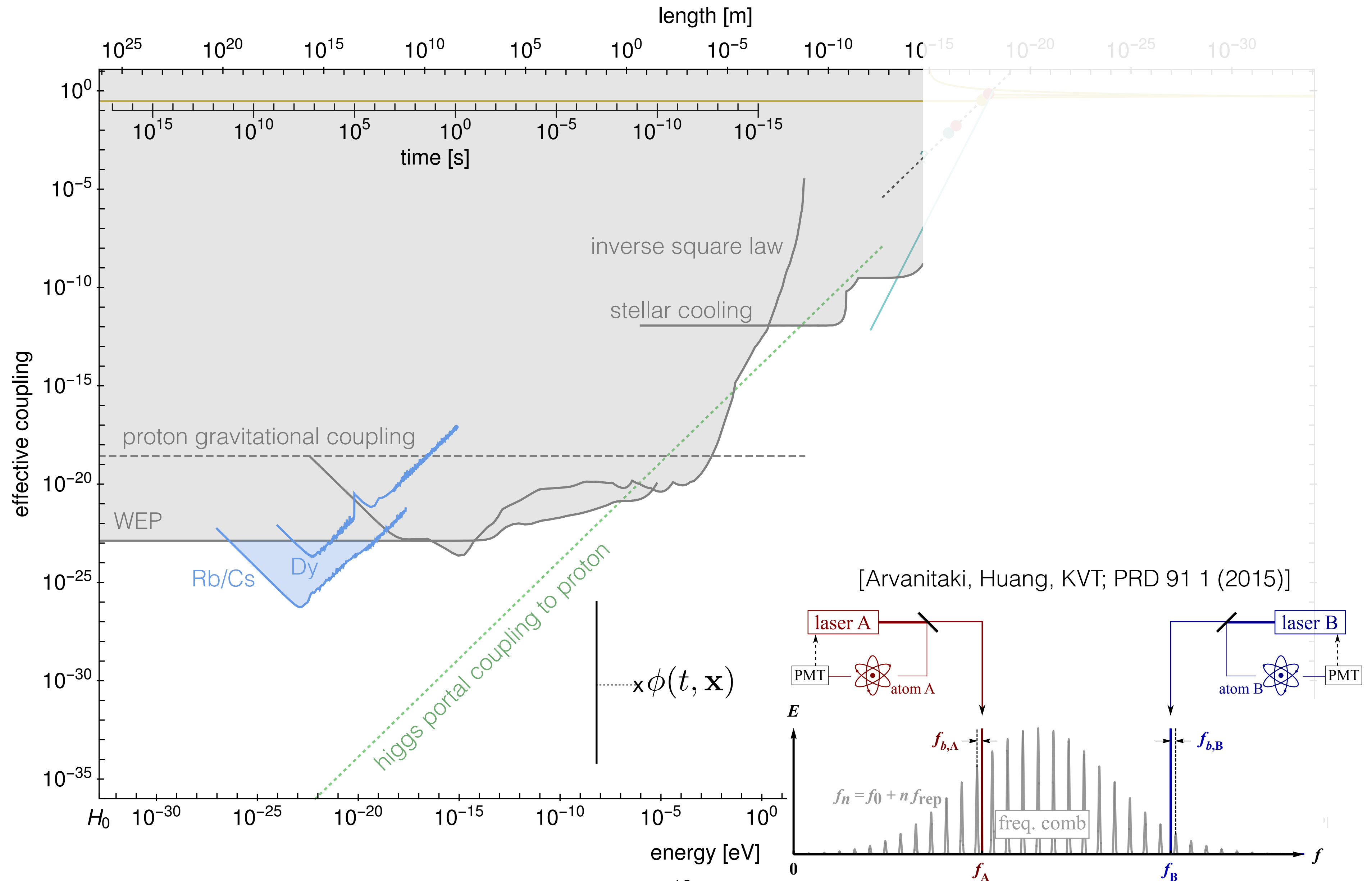
Cantilever



Stellar Cooling



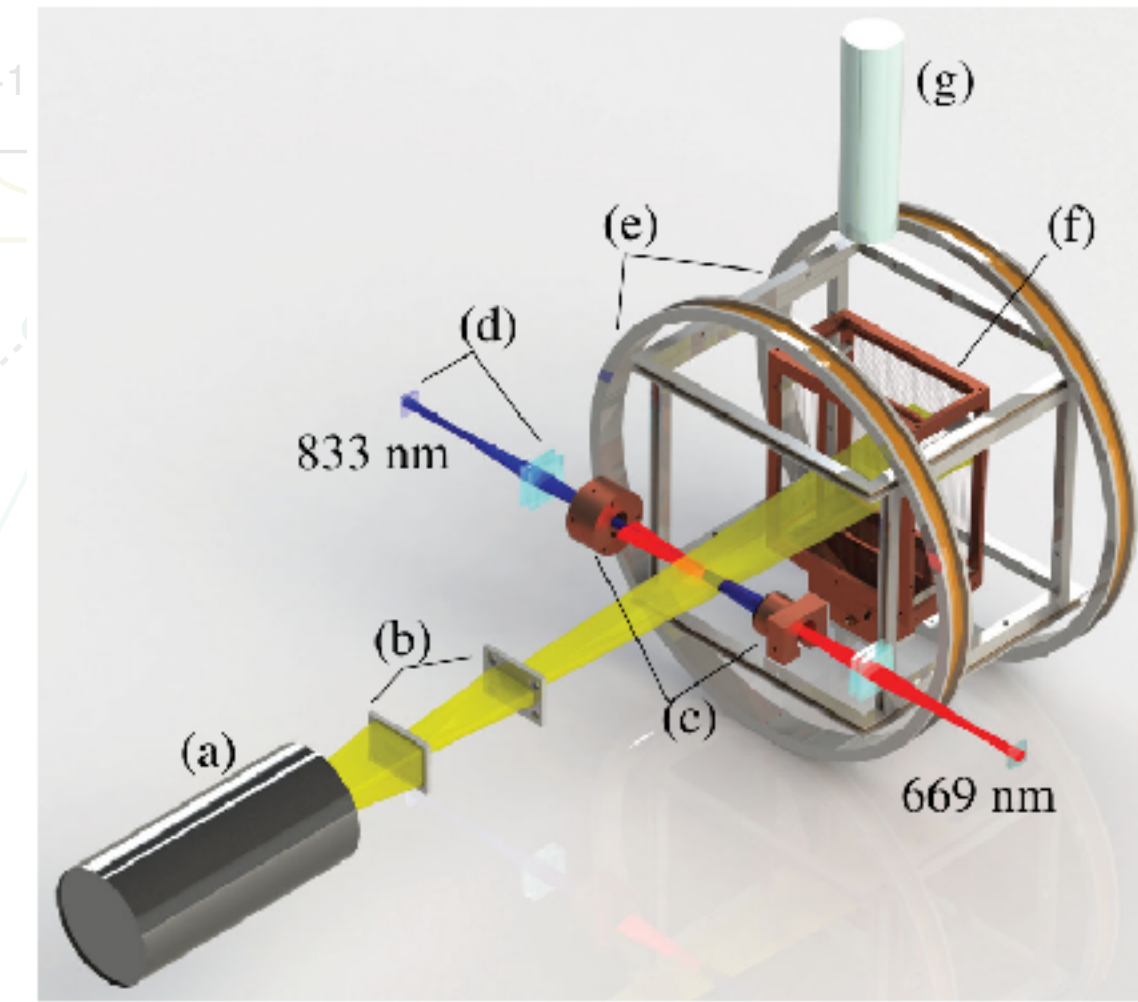
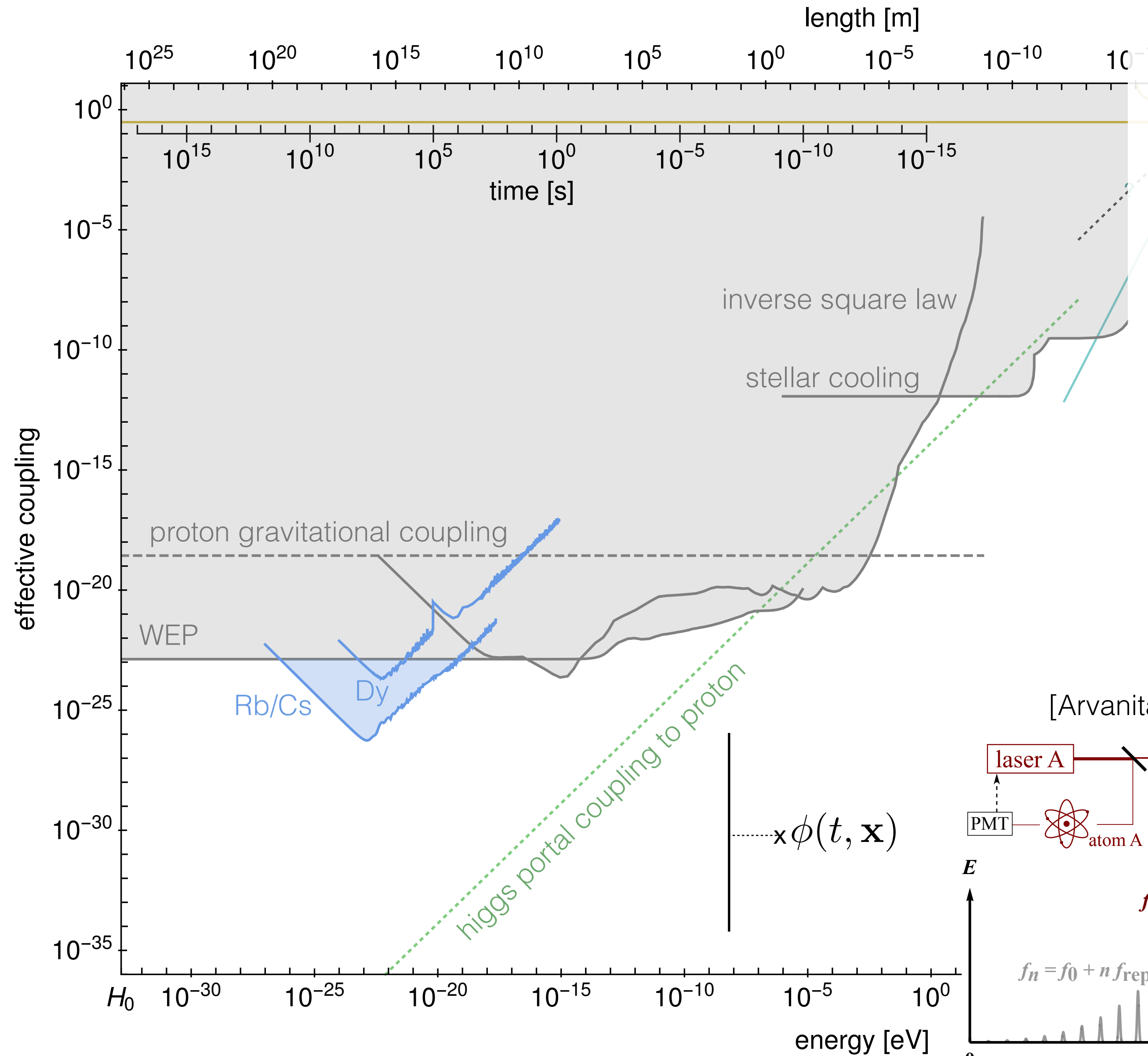
Atomic Clocks



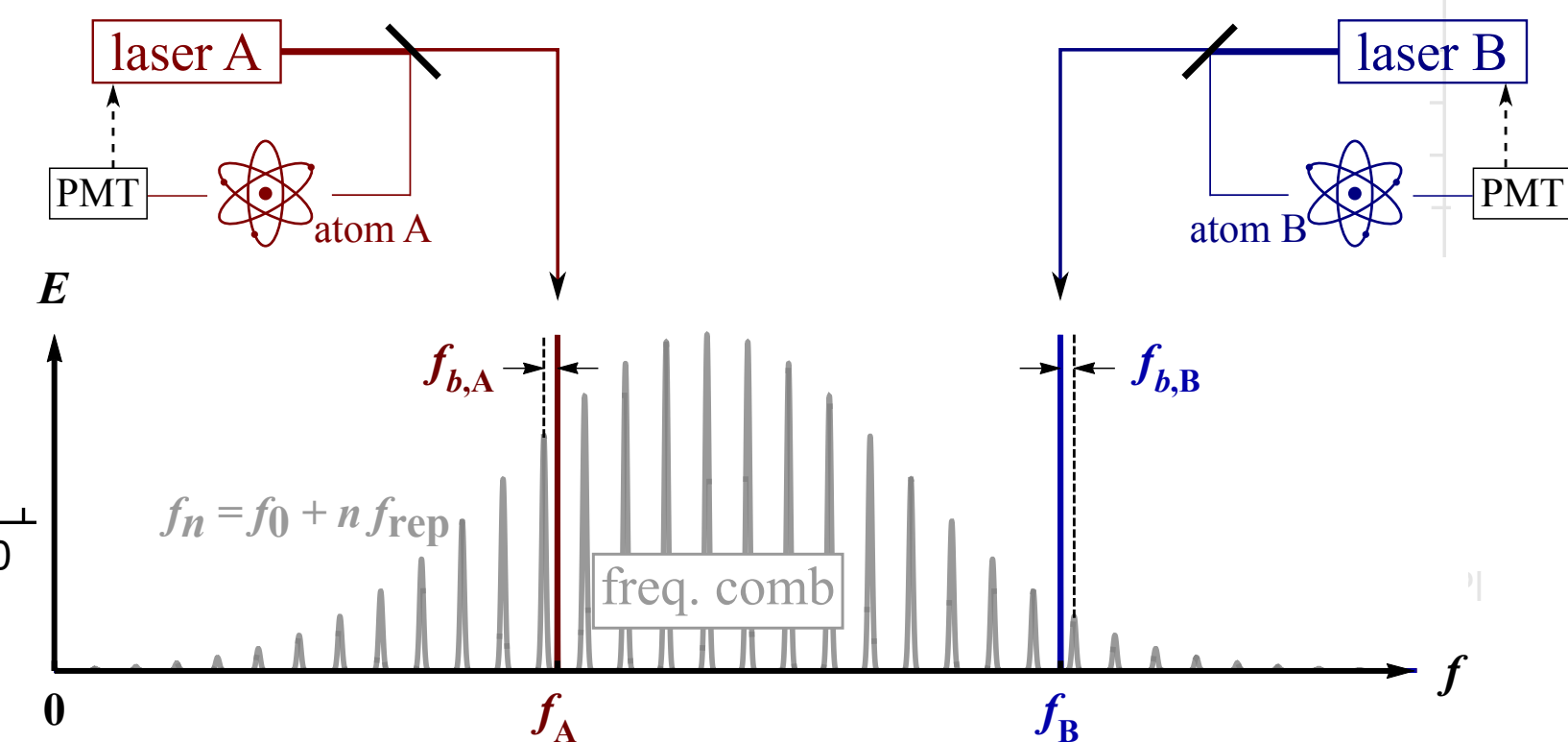
Atomic Clocks

162/1647Dy

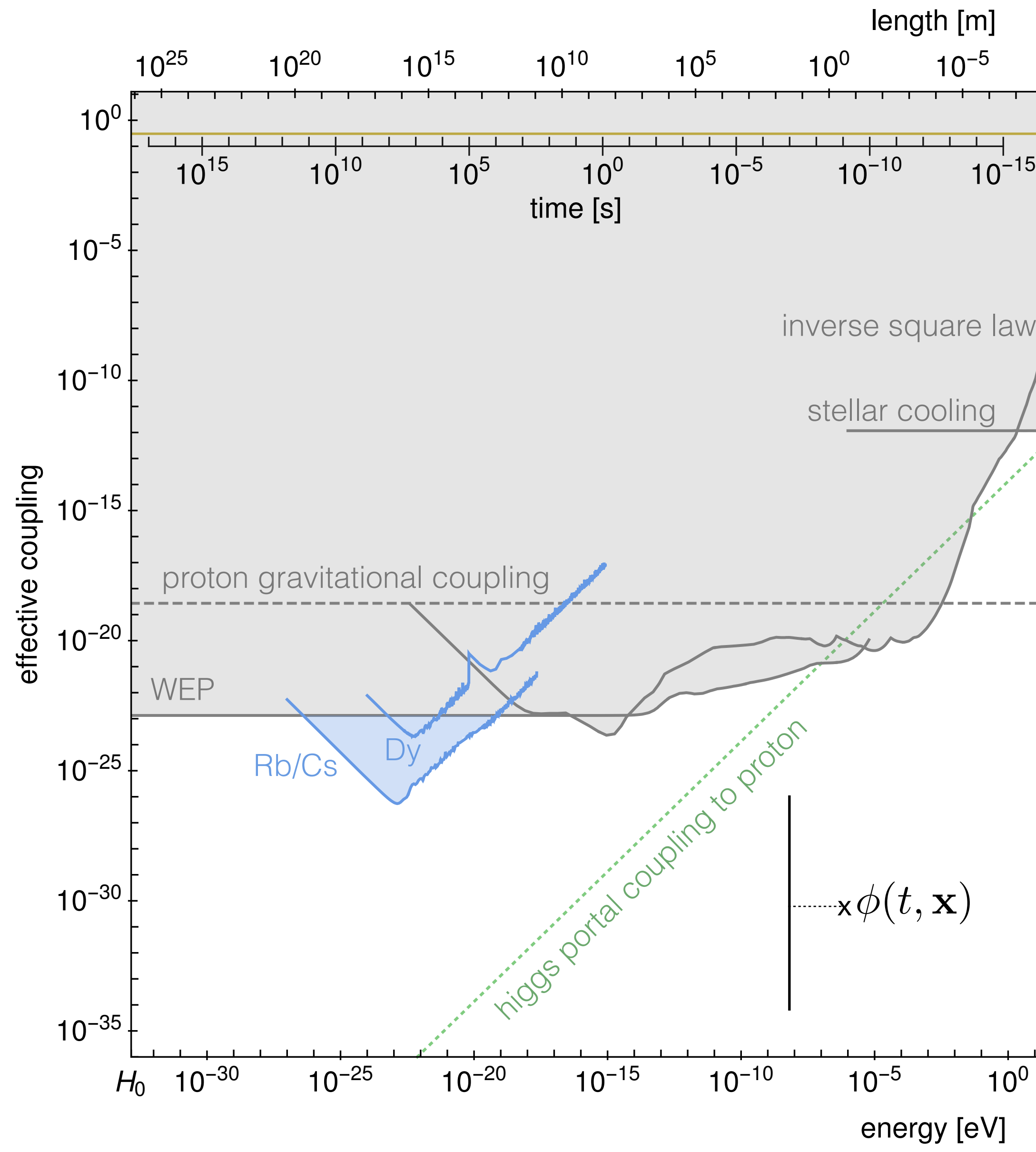
[KVT, Budker, PRL 115 1 (2015)]



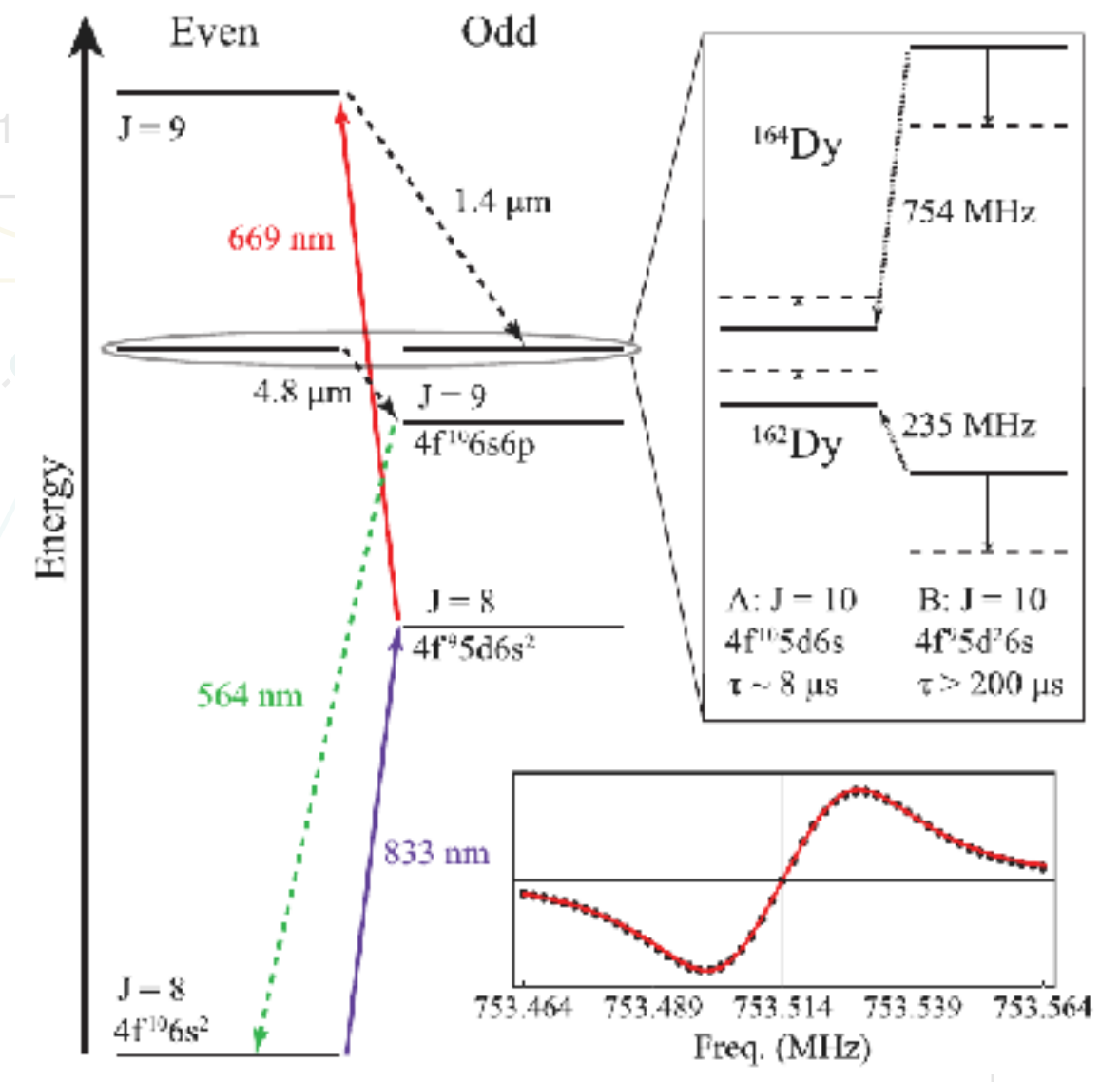
[Arvanitaki, Huang, KVT; PRD 91 1 (2015)]



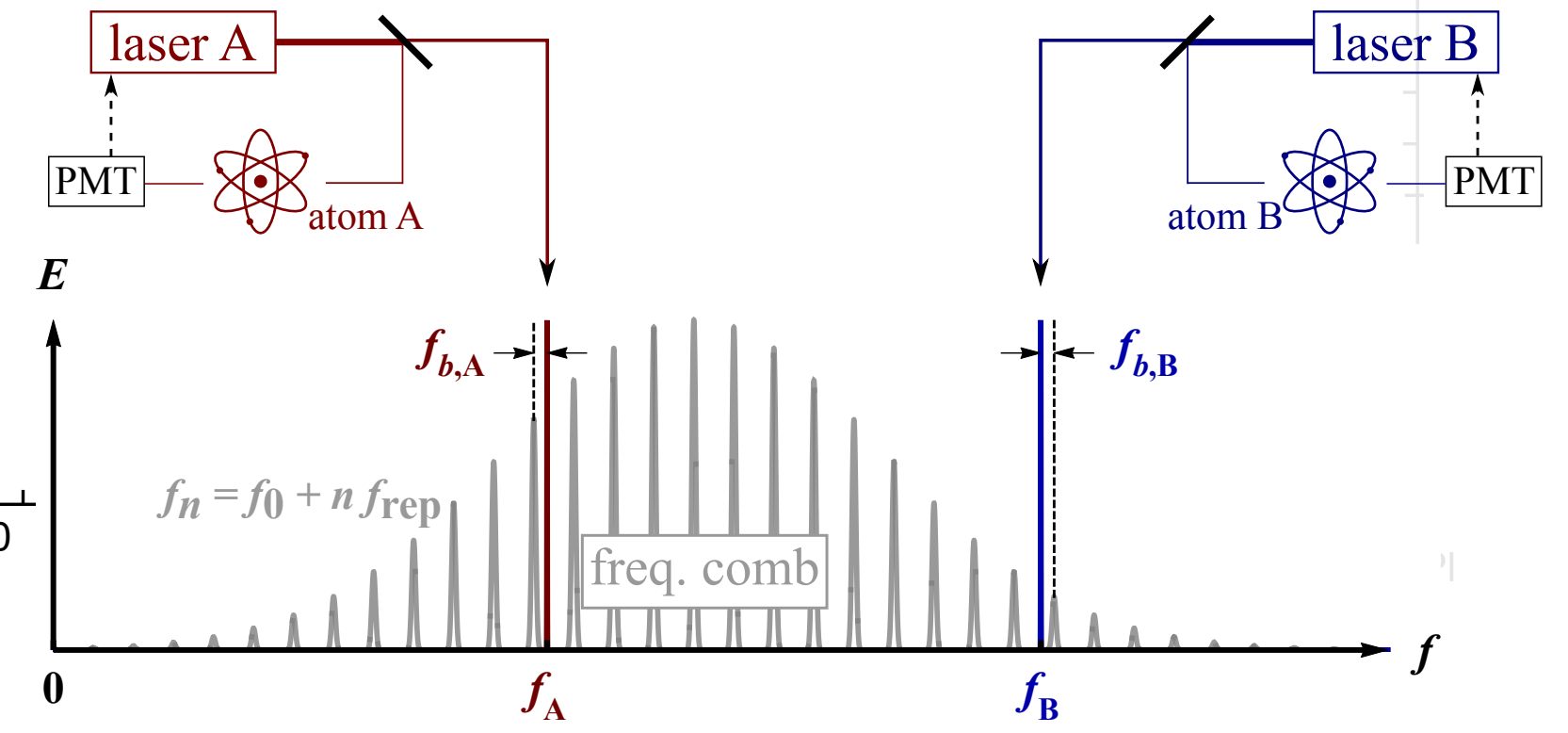
Atomic Clocks



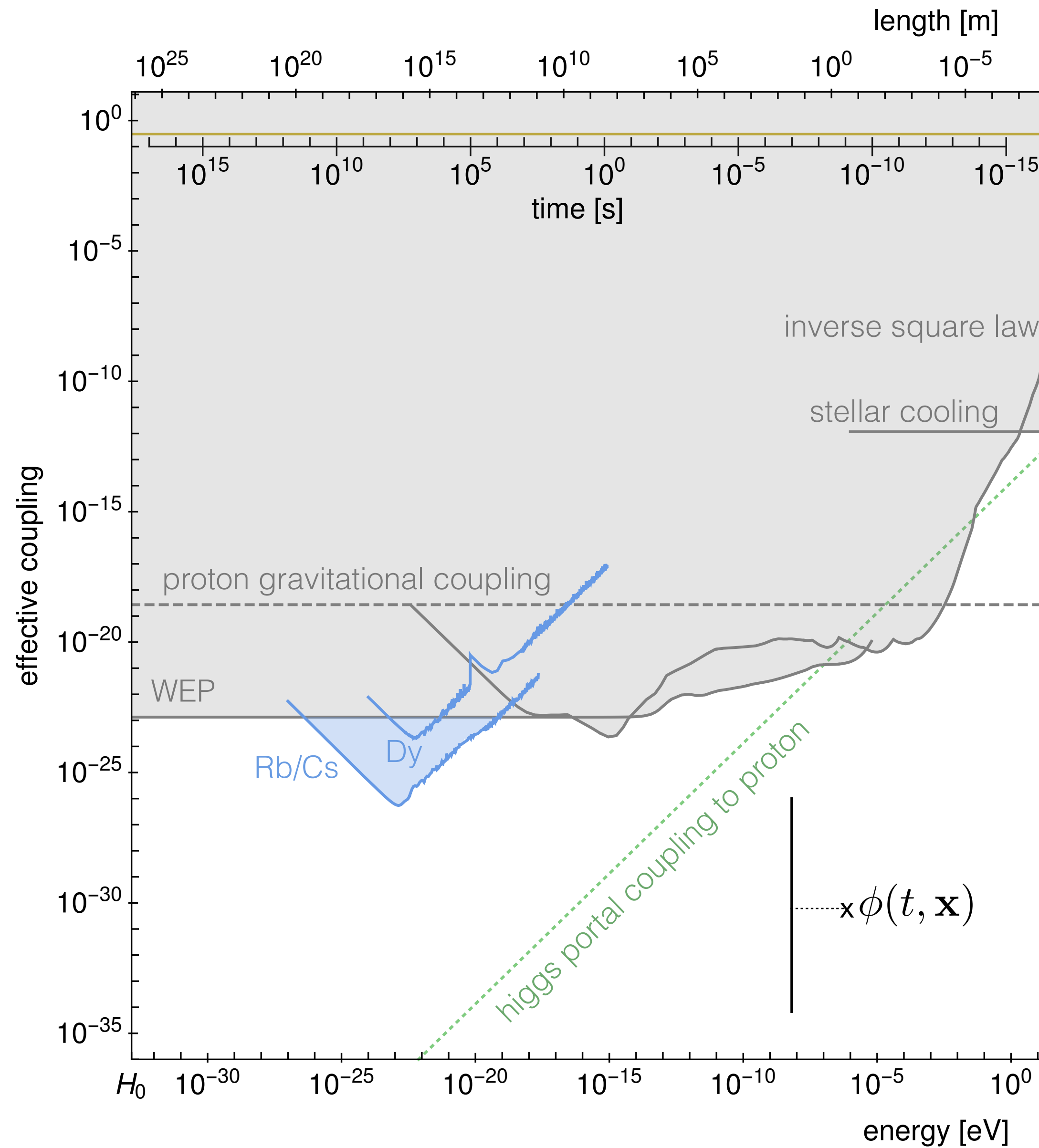
$^{162/164}\text{Dy}$
[KVT, Budker, PRL 115 1 (2015)]



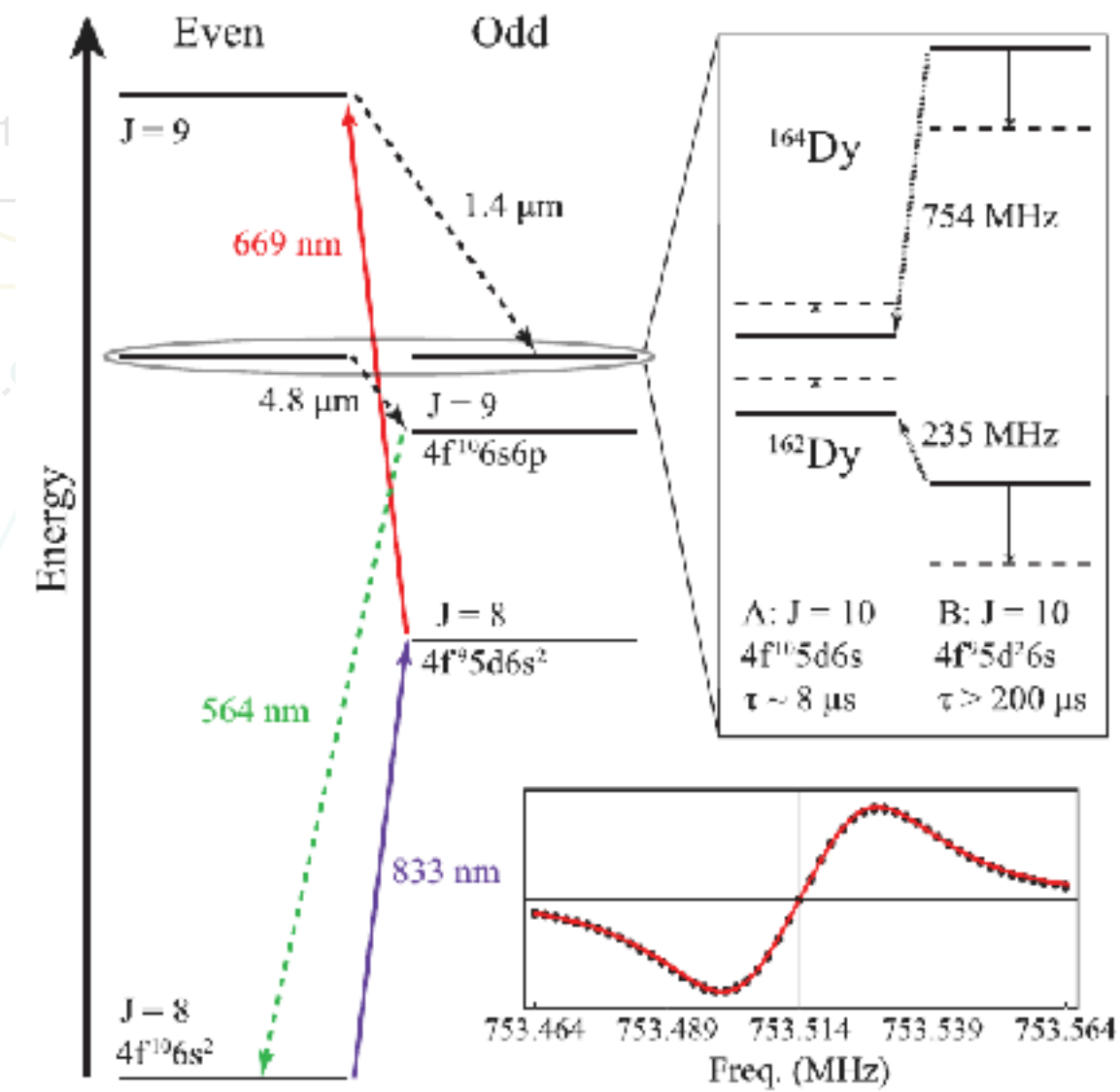
[Arvanitaki, Huang, KVT; PRD 91 1 (2015)]



Atomic Clocks

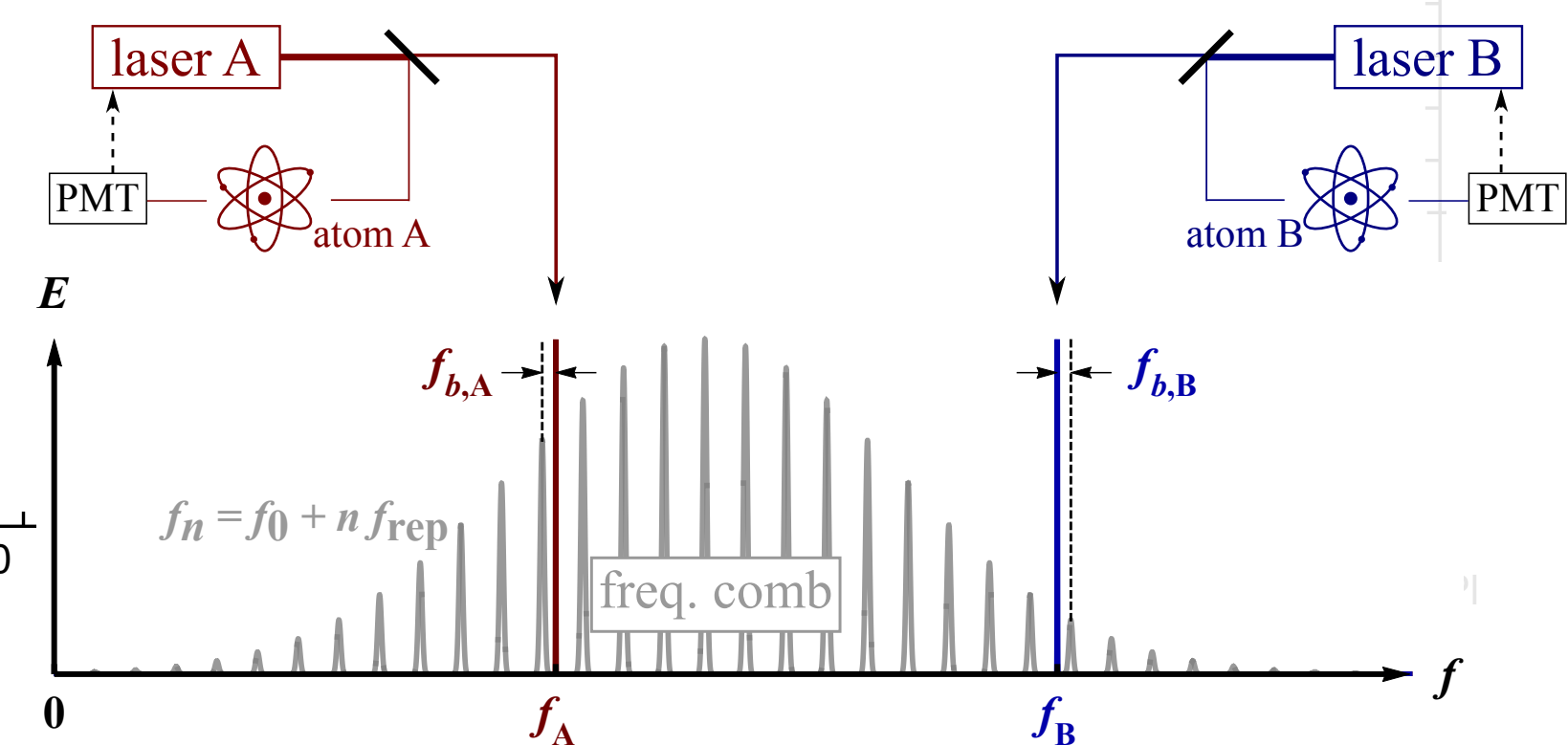


^{162/164}Dy
[KVT, Budker, PRL 115 1 (2015)]

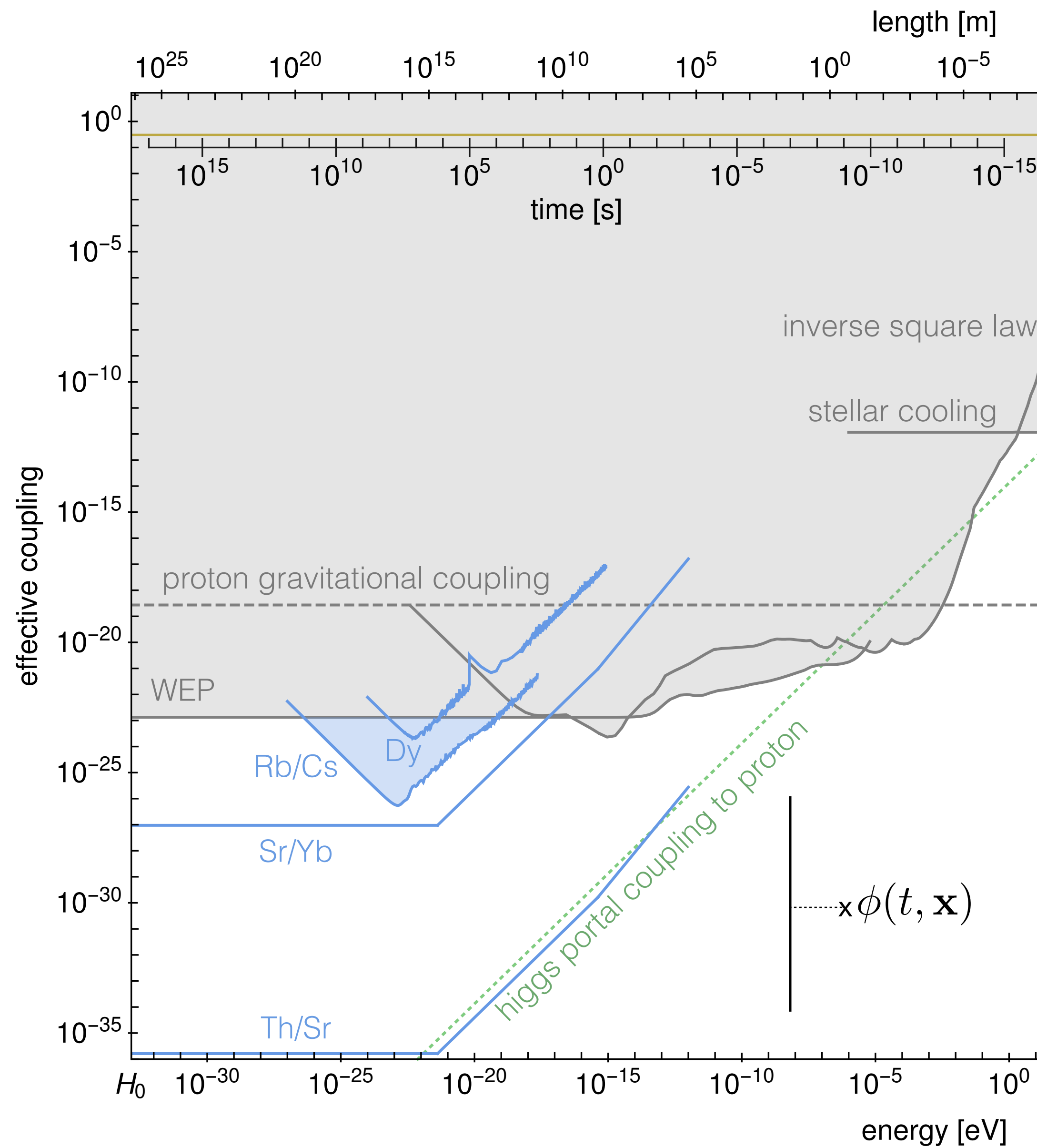


Rb/Cs
[Hees +, PRL 117 3 (2016)]

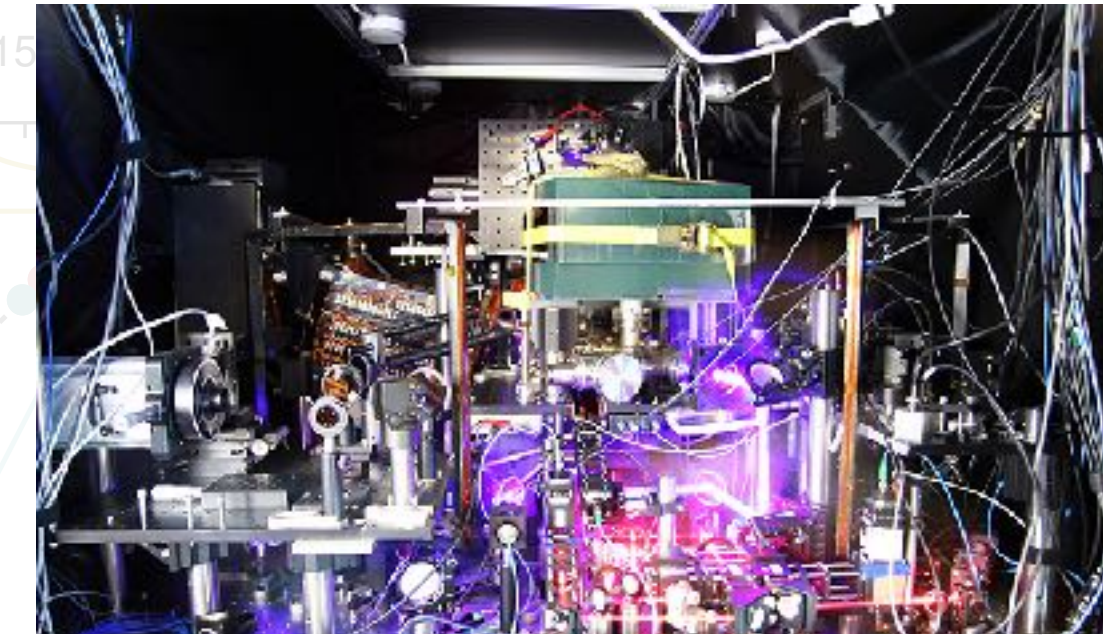
[Arvanitaki, Huang, KVT; PRD 91 1 (2015)]



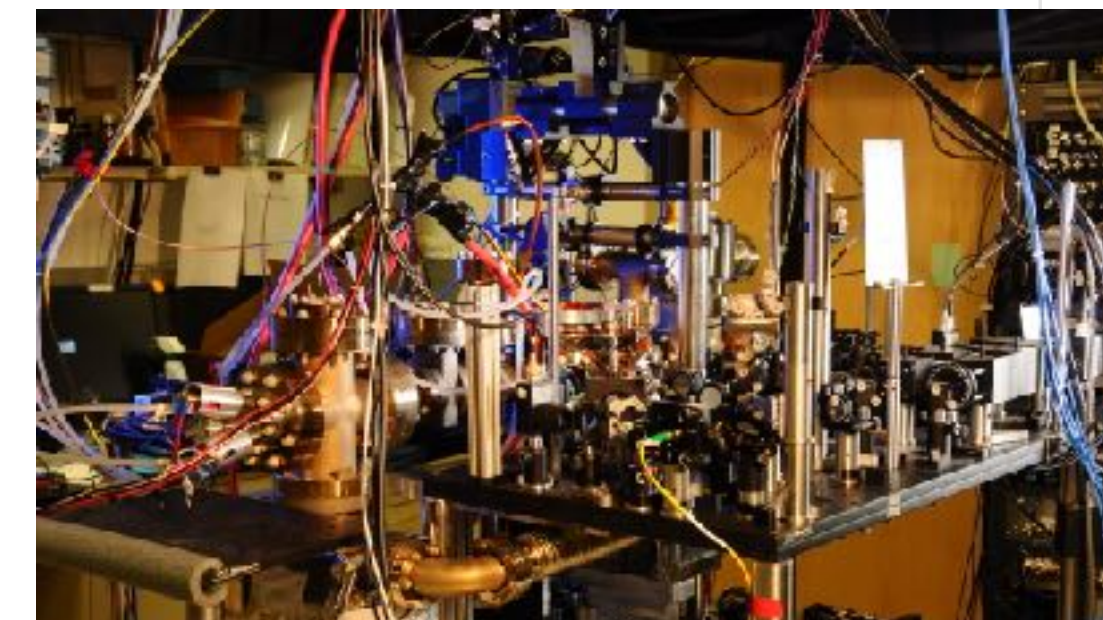
Near-Future Atomic & Nuclear Clocks



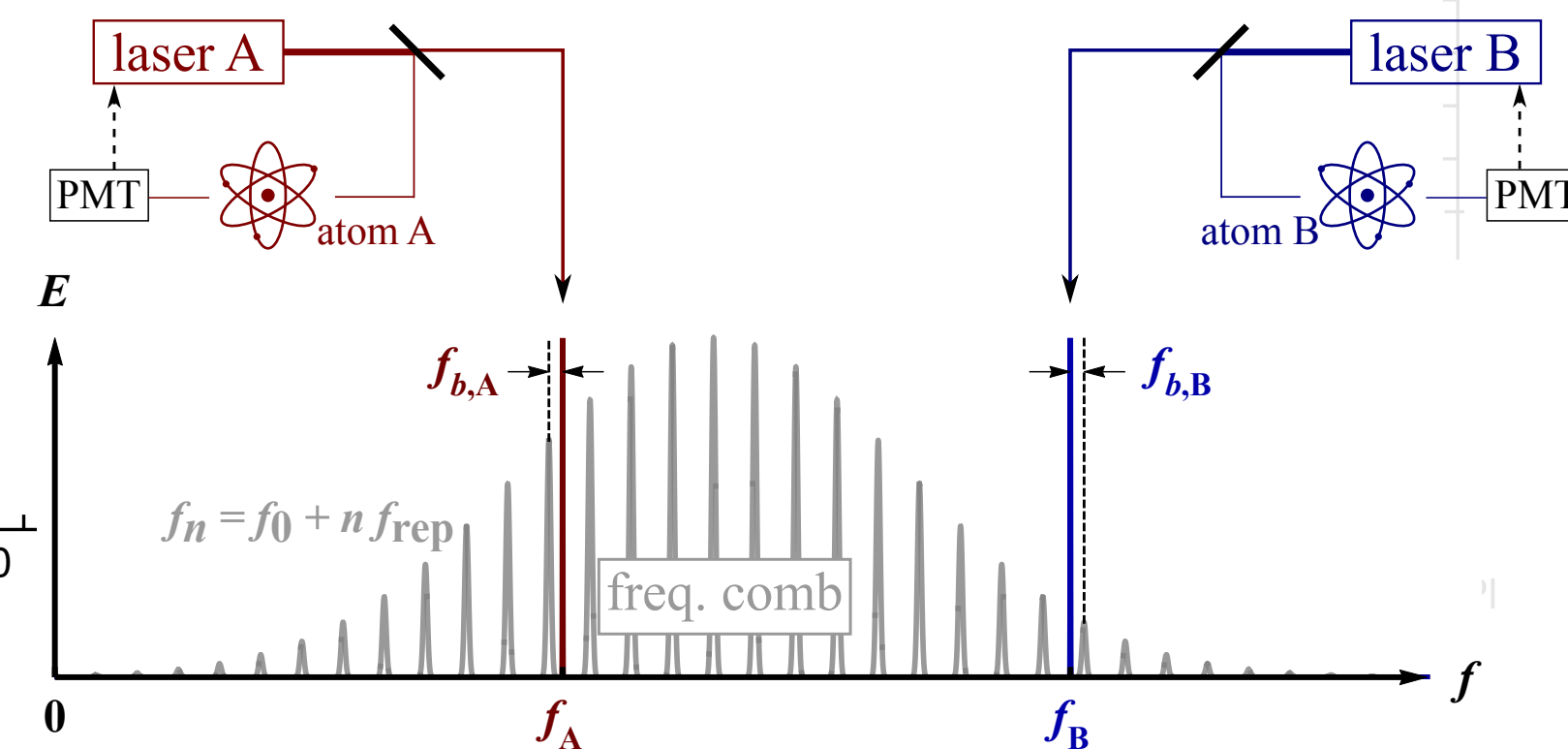
⁸⁷Sr (JILA)



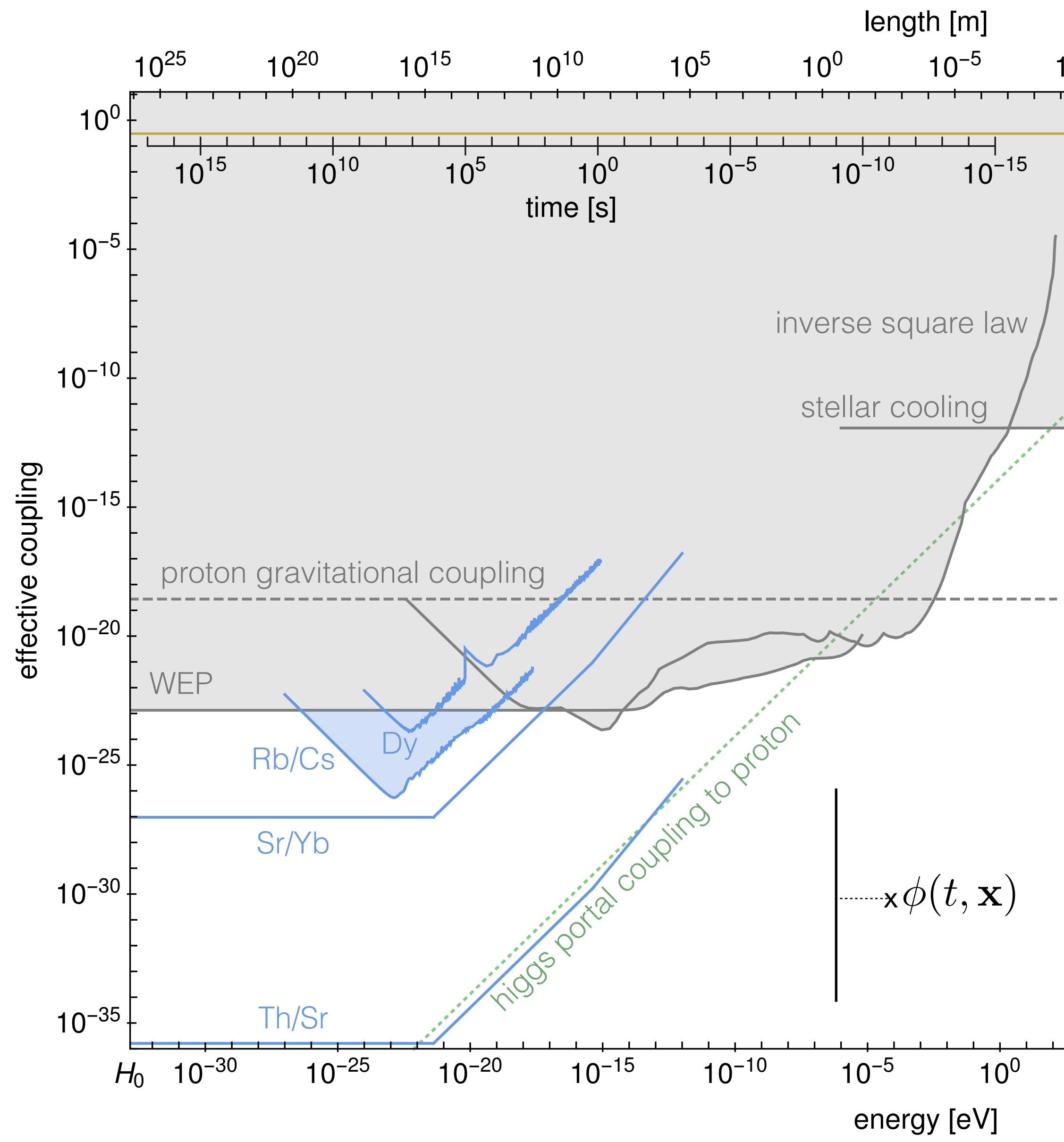
¹⁷¹Yb (NIST)



[Arvanitaki, Huang, KVT; PRD 91 1 (2015)]



Near-Future Atomic & Nuclear Clocks



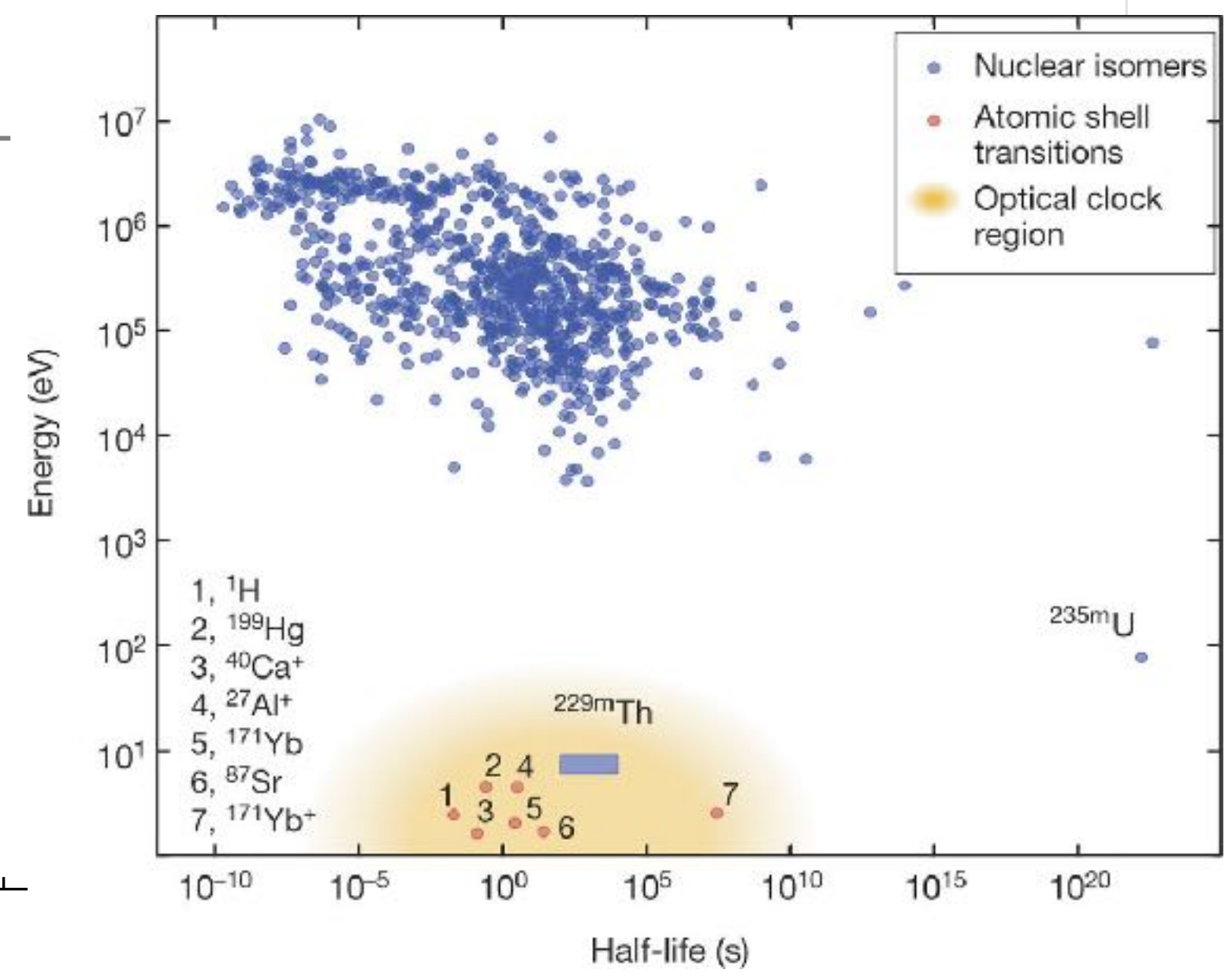
²²⁹Th nuclear clock

$$\omega_0 = 8.28 \pm 0.17 \text{ eV}$$

$$\frac{1}{\omega_0 \tau} \approx 10^{-20}$$

[Seiferle +, Nature (2019)]

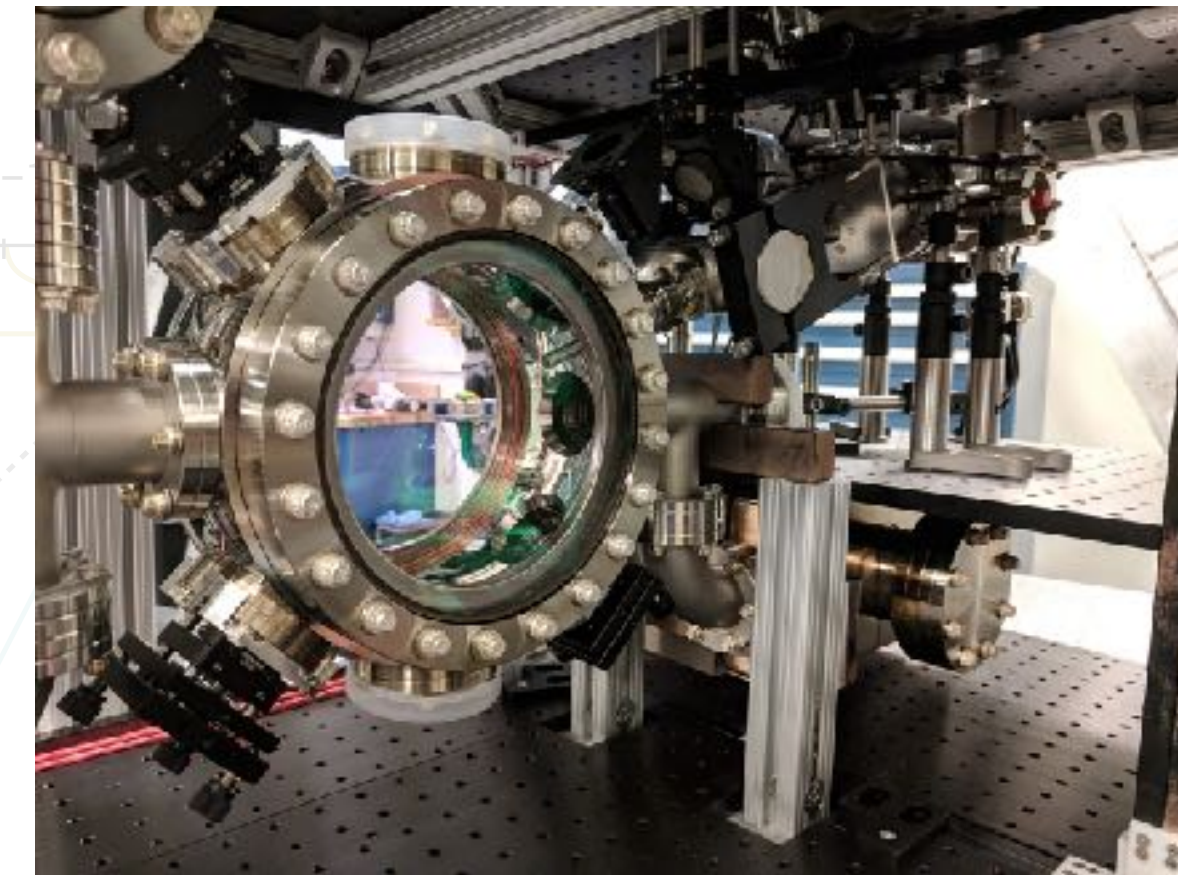
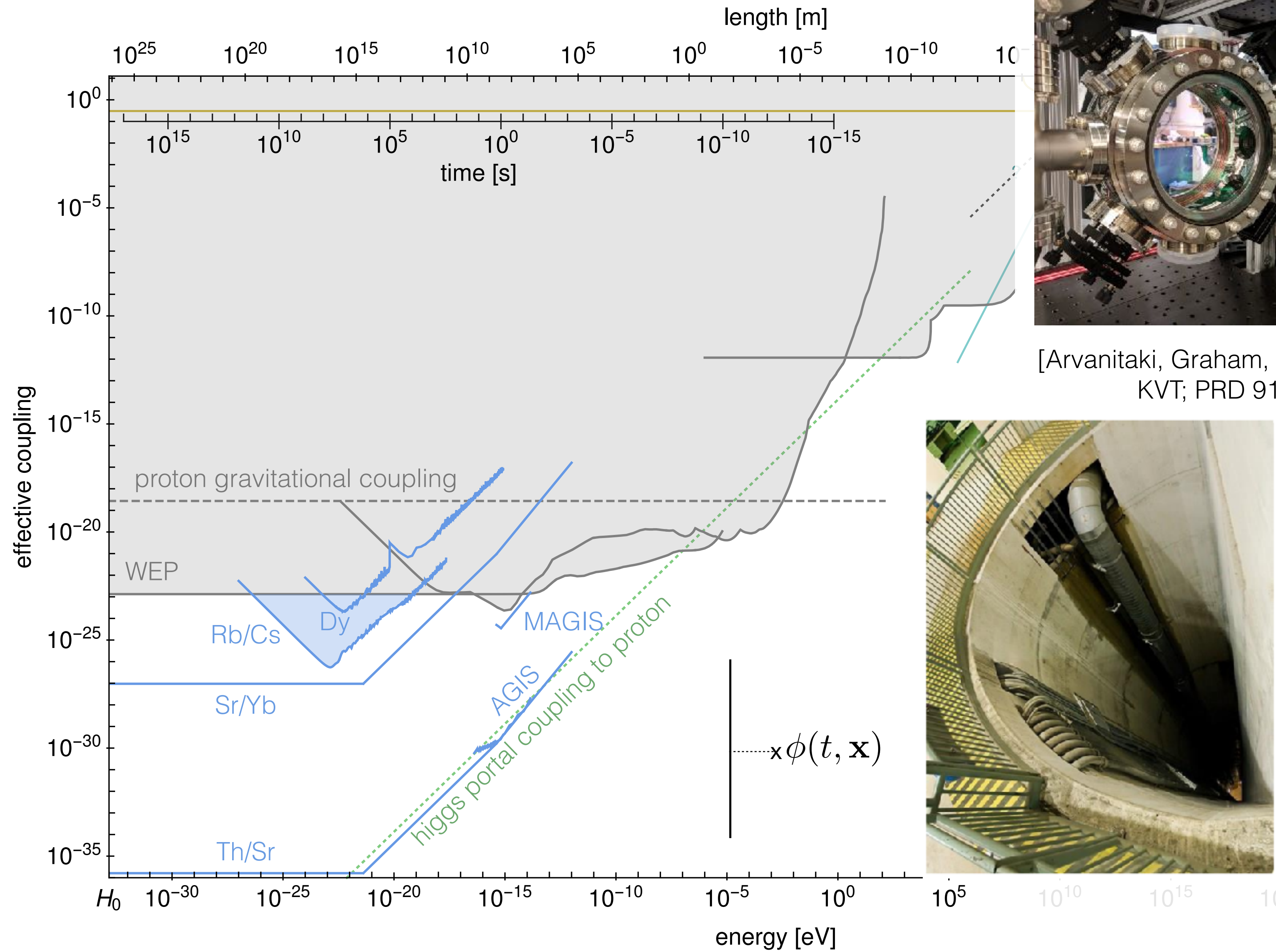
- Direct excitation imminent
- UV lasers in development
- Reduction of systematics
- Accidental cancellation



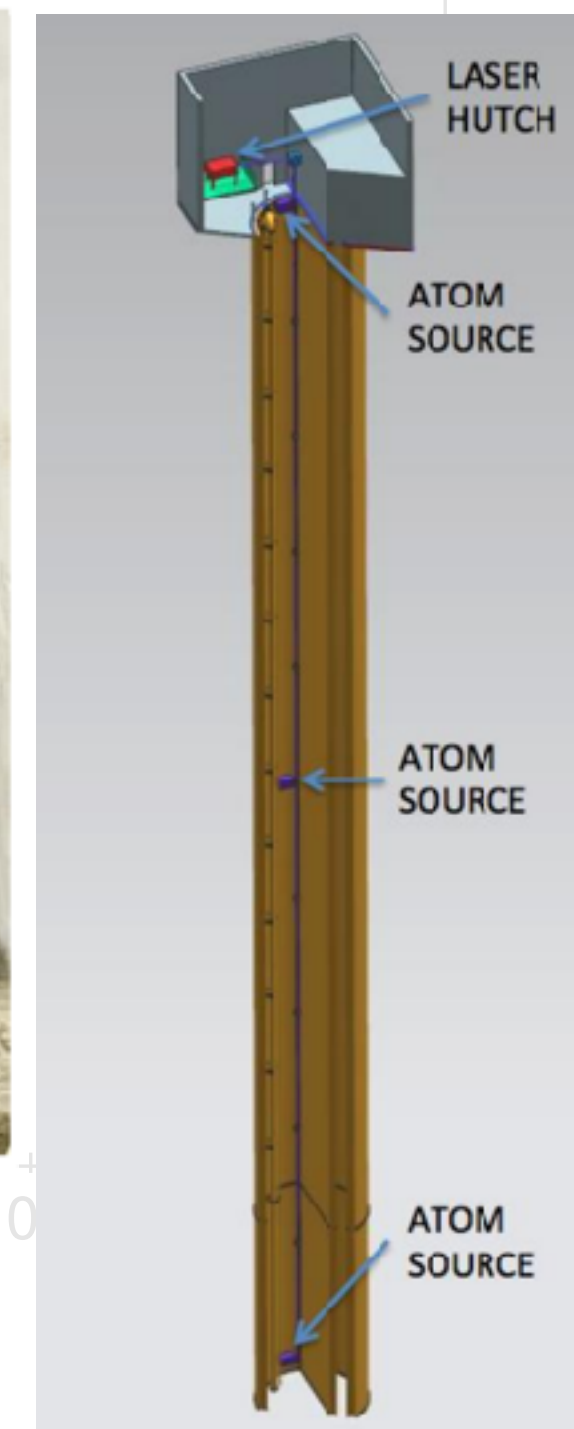
[von der Wense +, Nature (2016)]

Atom Interferometry

MAGIS-100

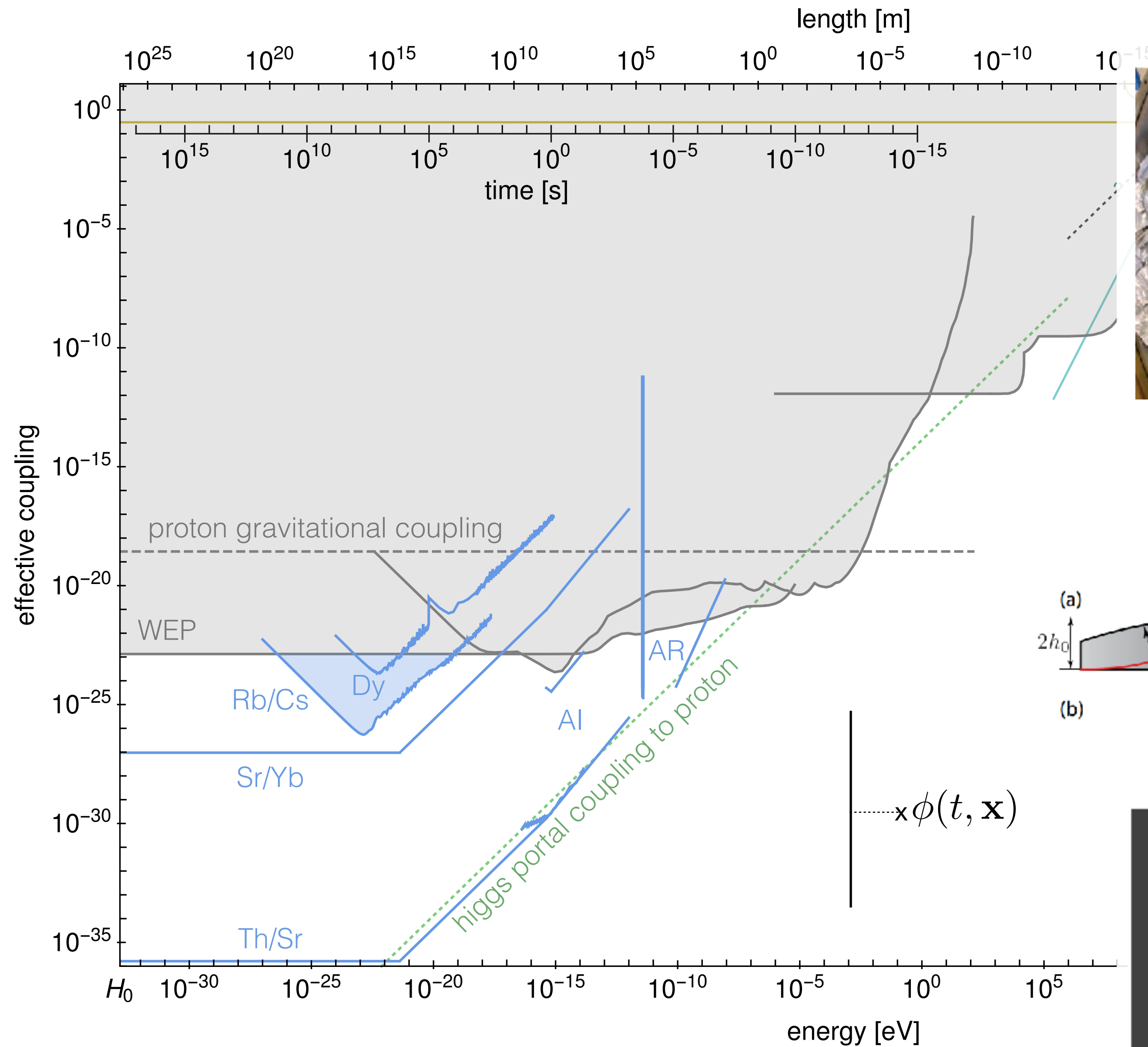


[Arvanitaki, Graham, Hogan, Rajendran, KVT; PRD 91 1 (2015)]

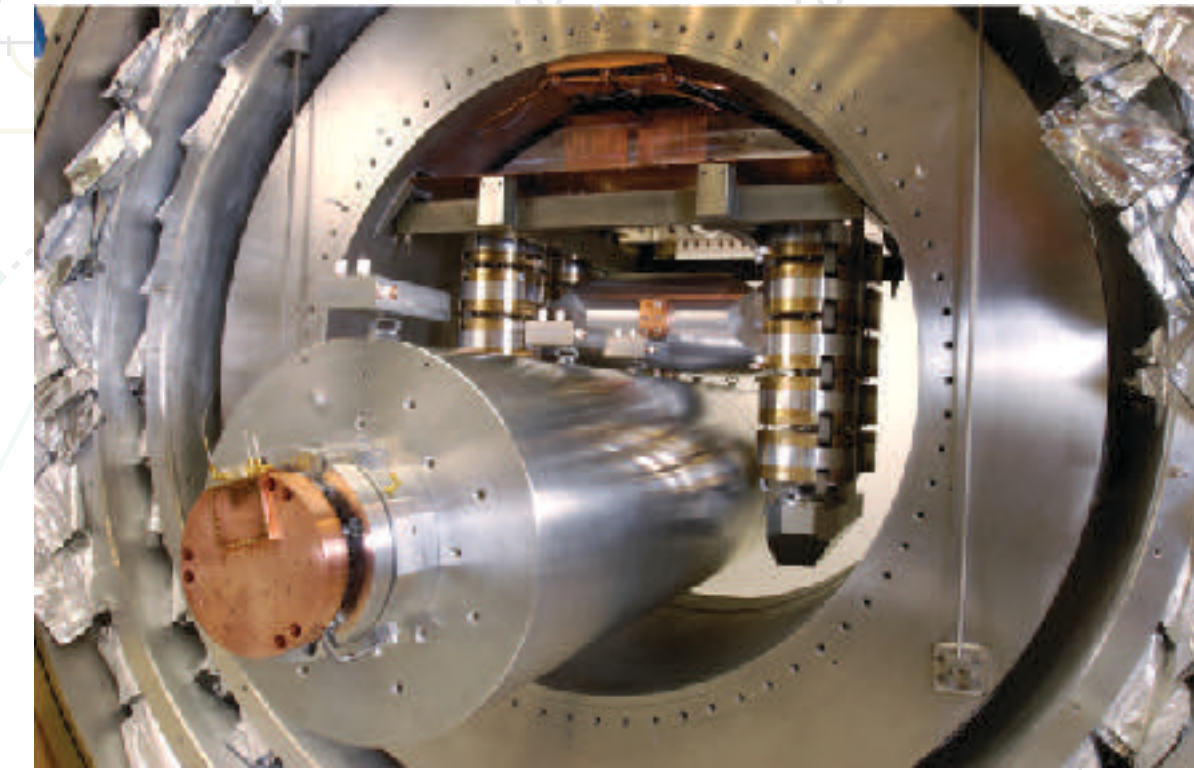


Acoustic Resonators

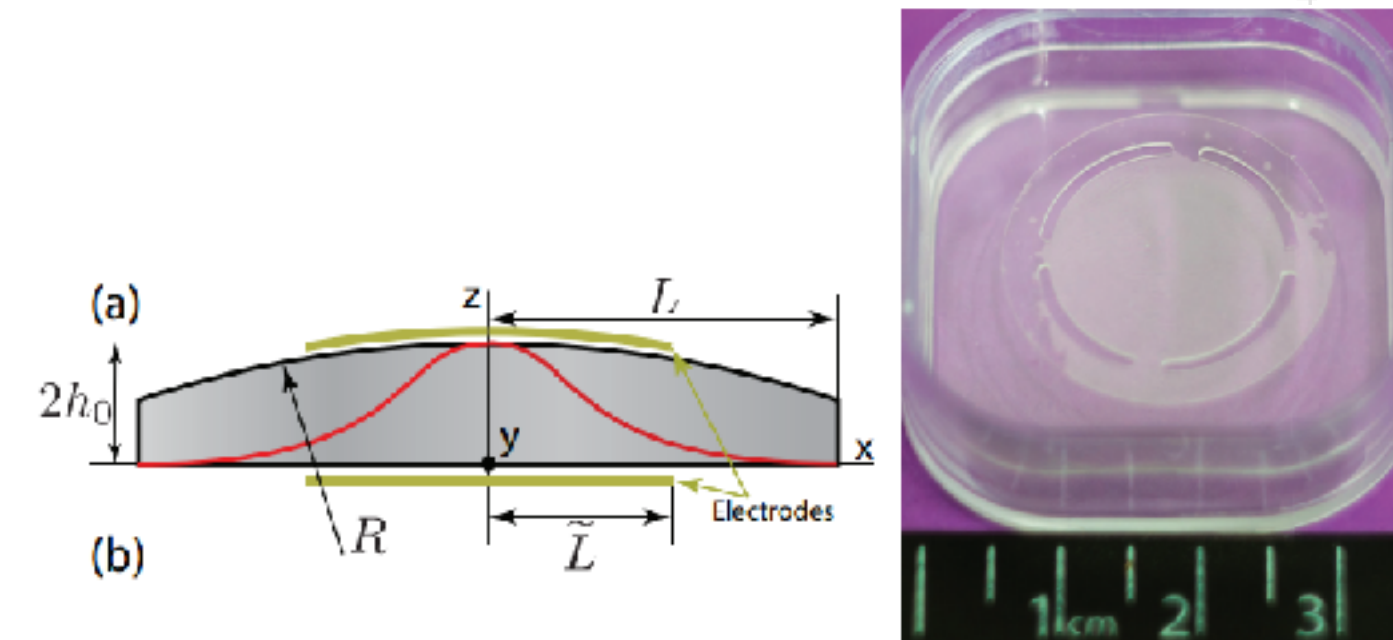
[Arvanitaki, Dimopoulos, KVT;
PRL 116 3 (2016)]



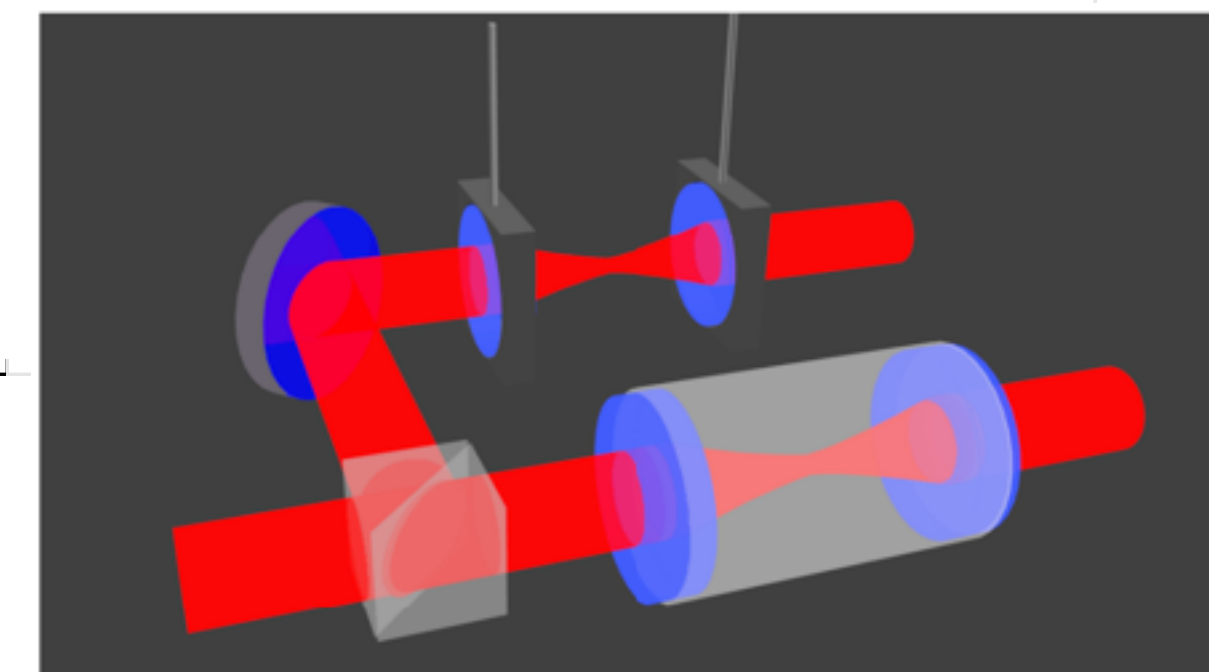
[Branca +; PRL 117 2 (2017)]



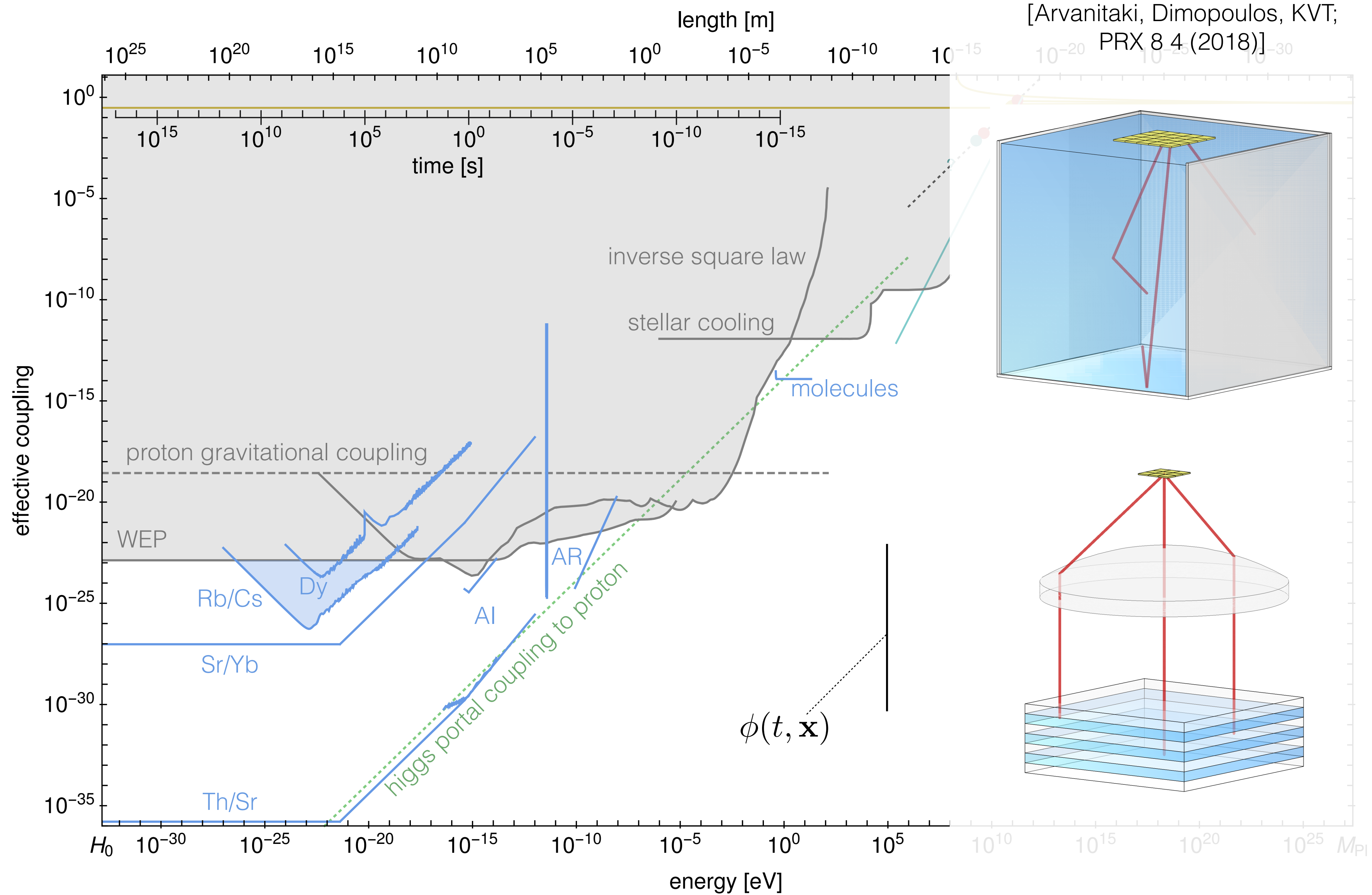
[Goryachev +; PRD 90 10 (2014)]



[Geraci +; PRL 123 3 (2019)]

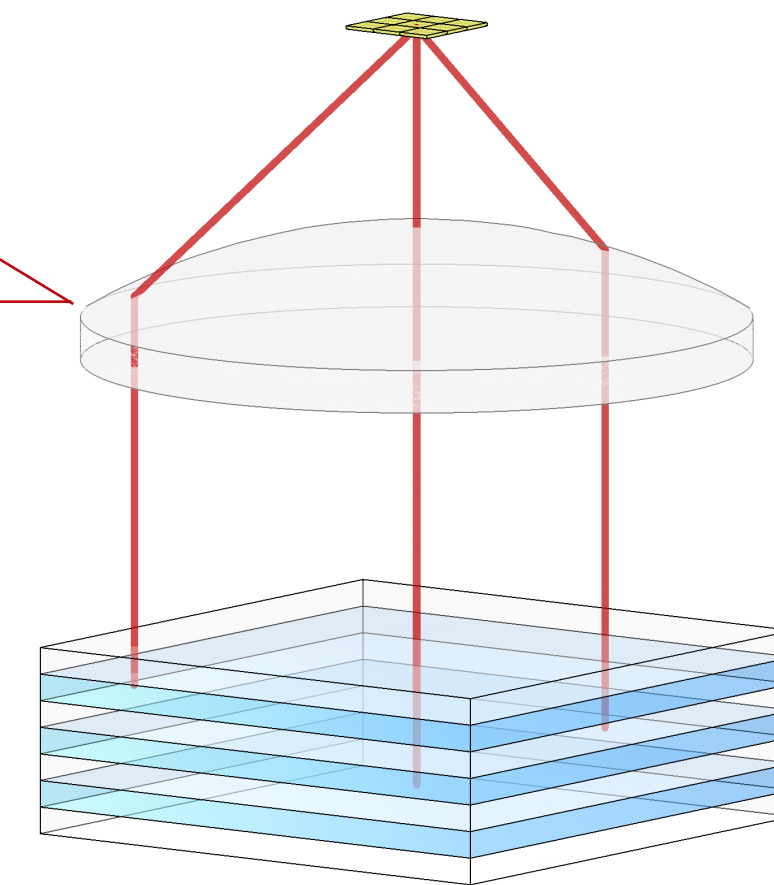
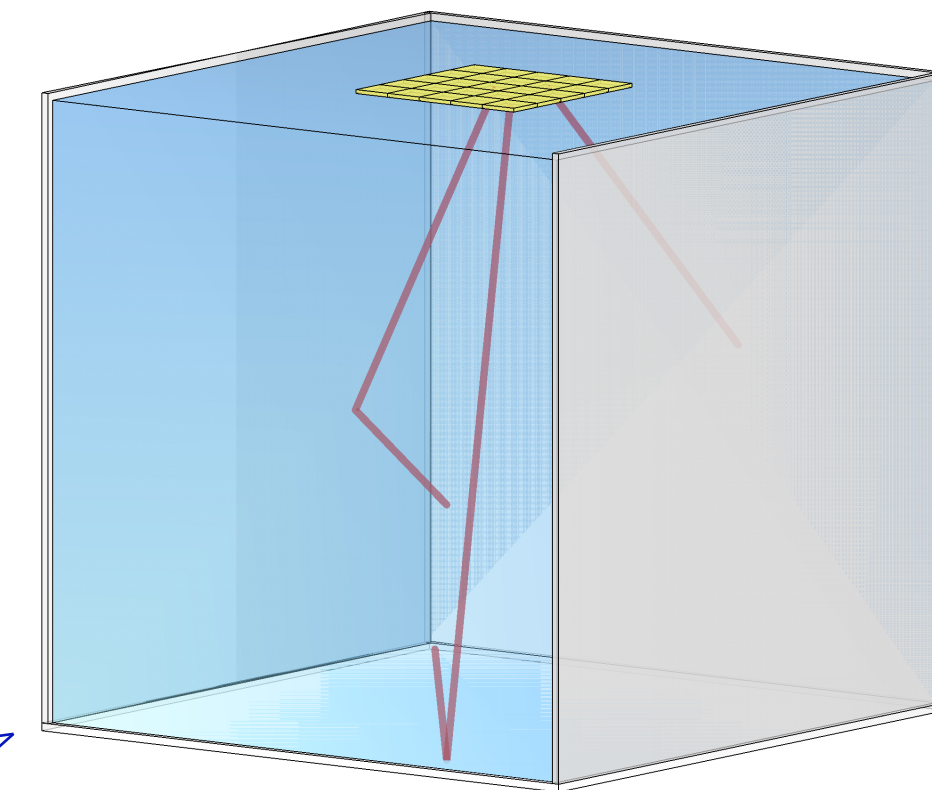
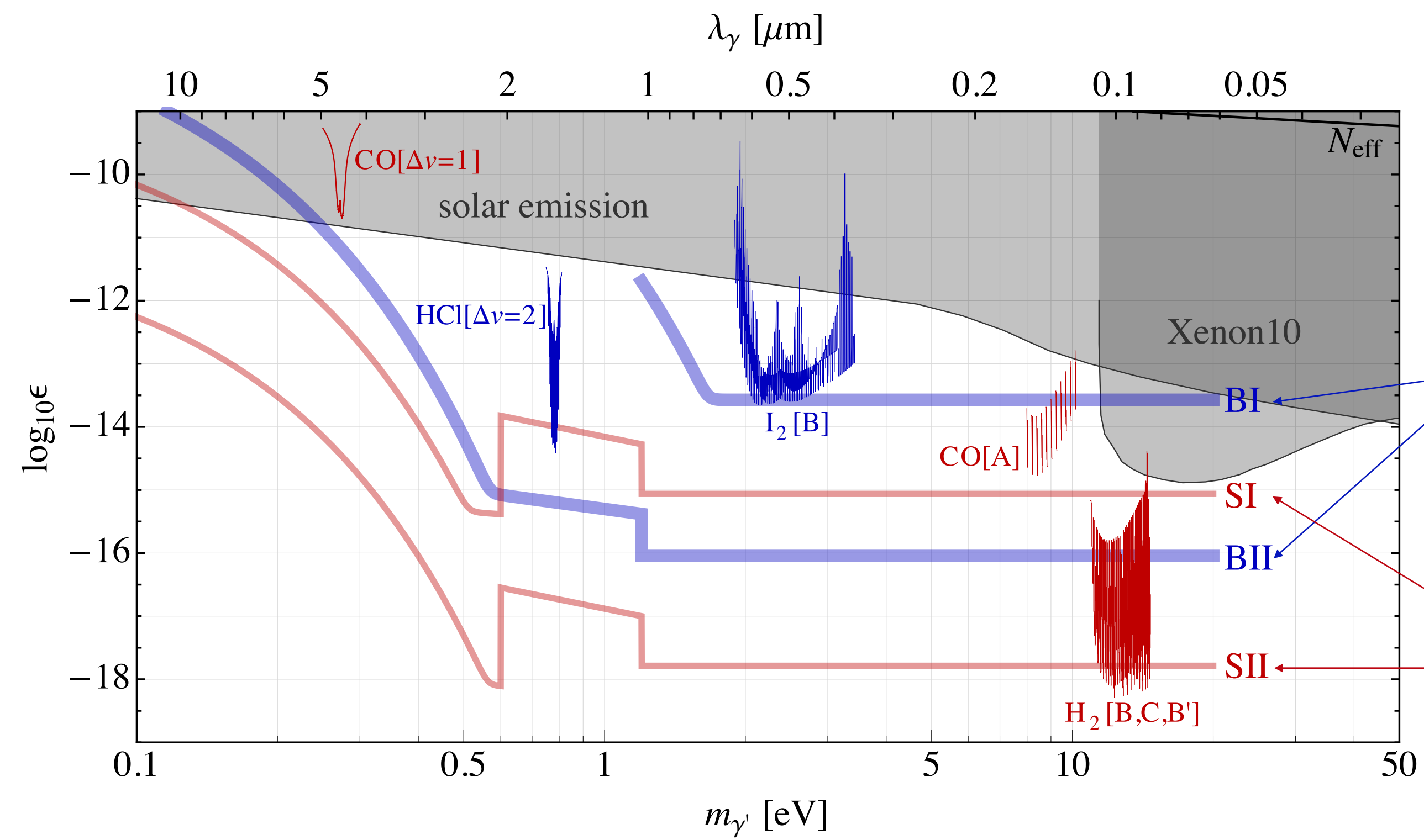


Resonant Absorption onto Molecules

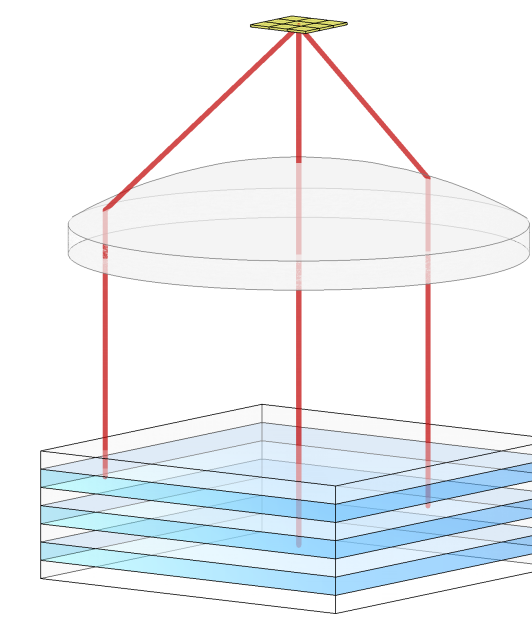
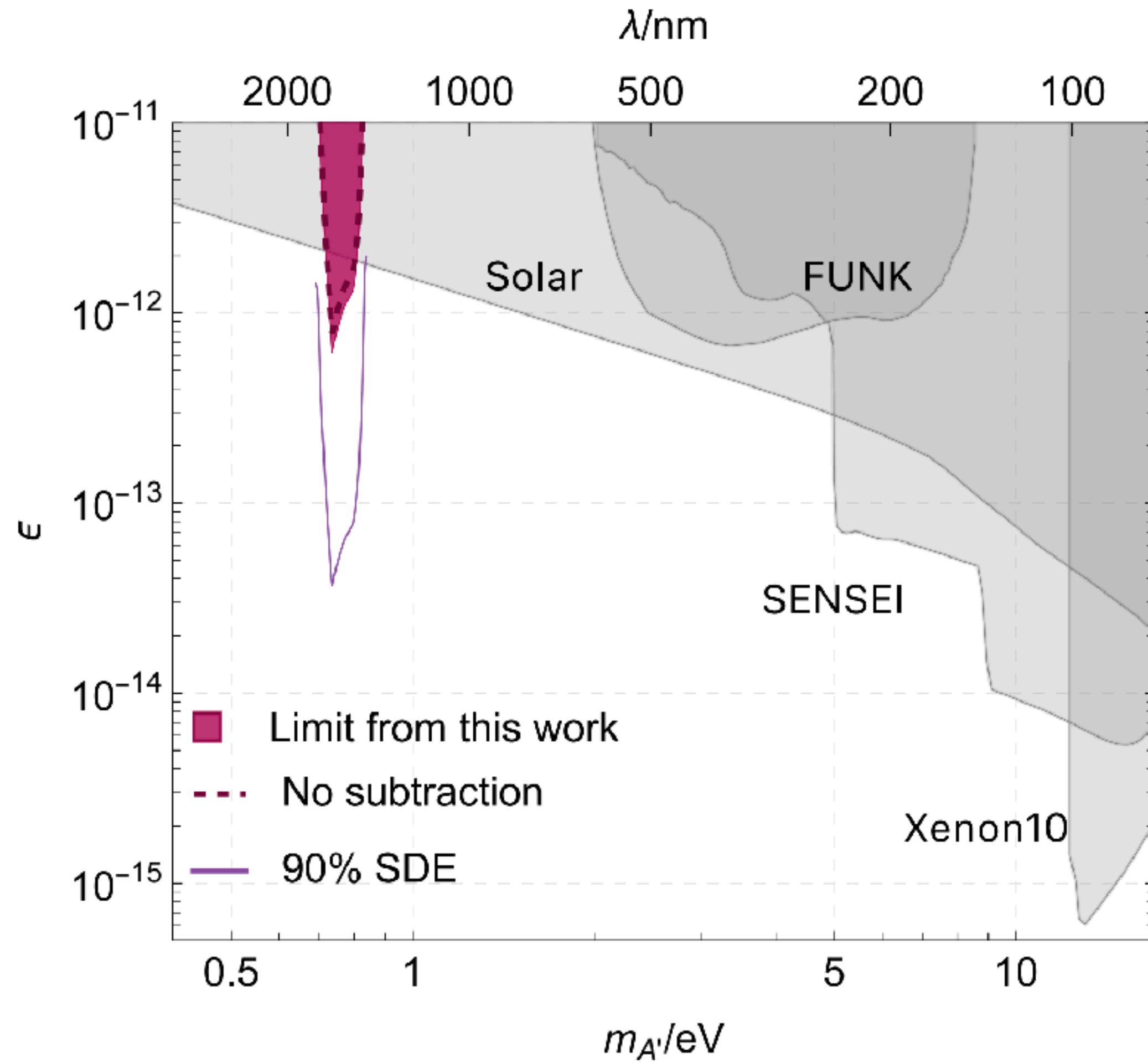


Molecular Absorption of Dark Photons

[Arvanitaki, Dimopoulos, KVT;
PRX 8 4 (2018)]

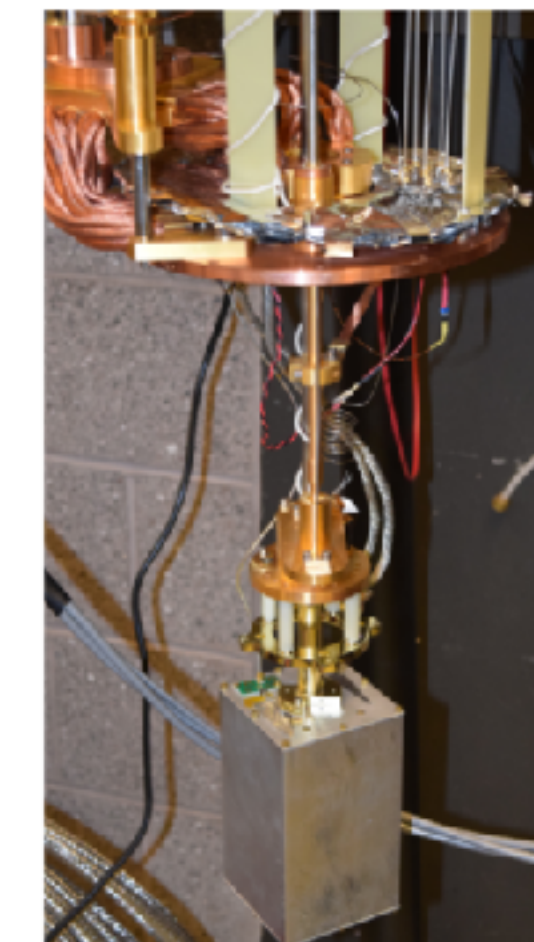
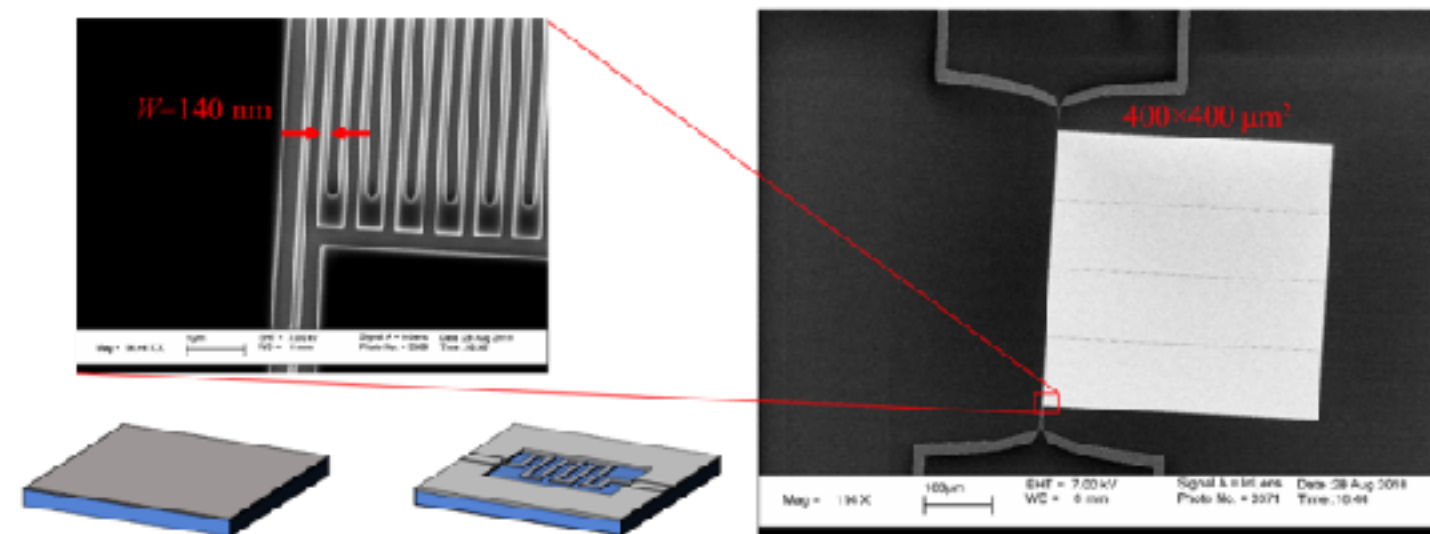
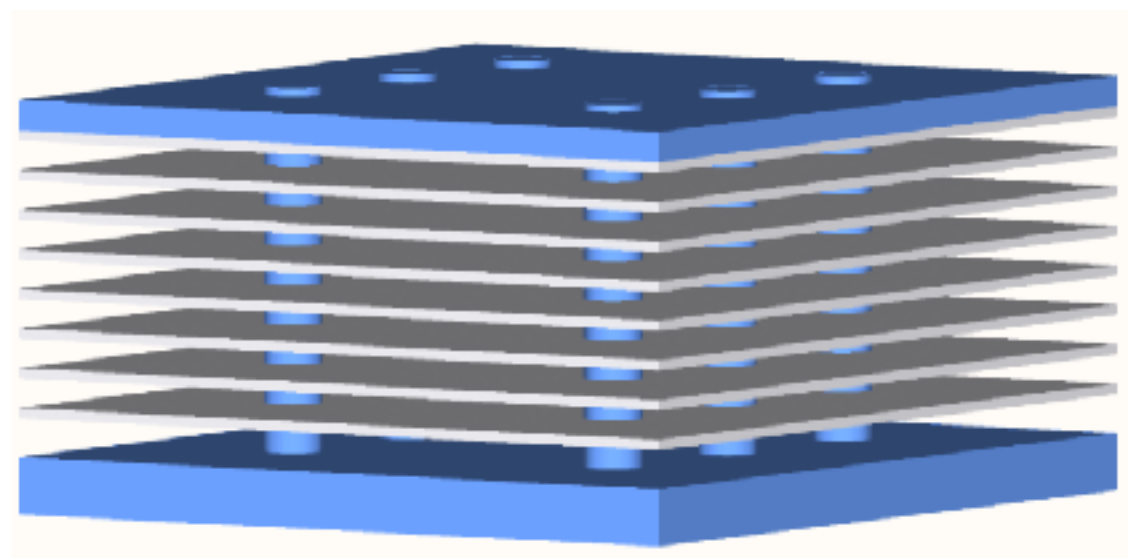


Absorption of Dark Photons

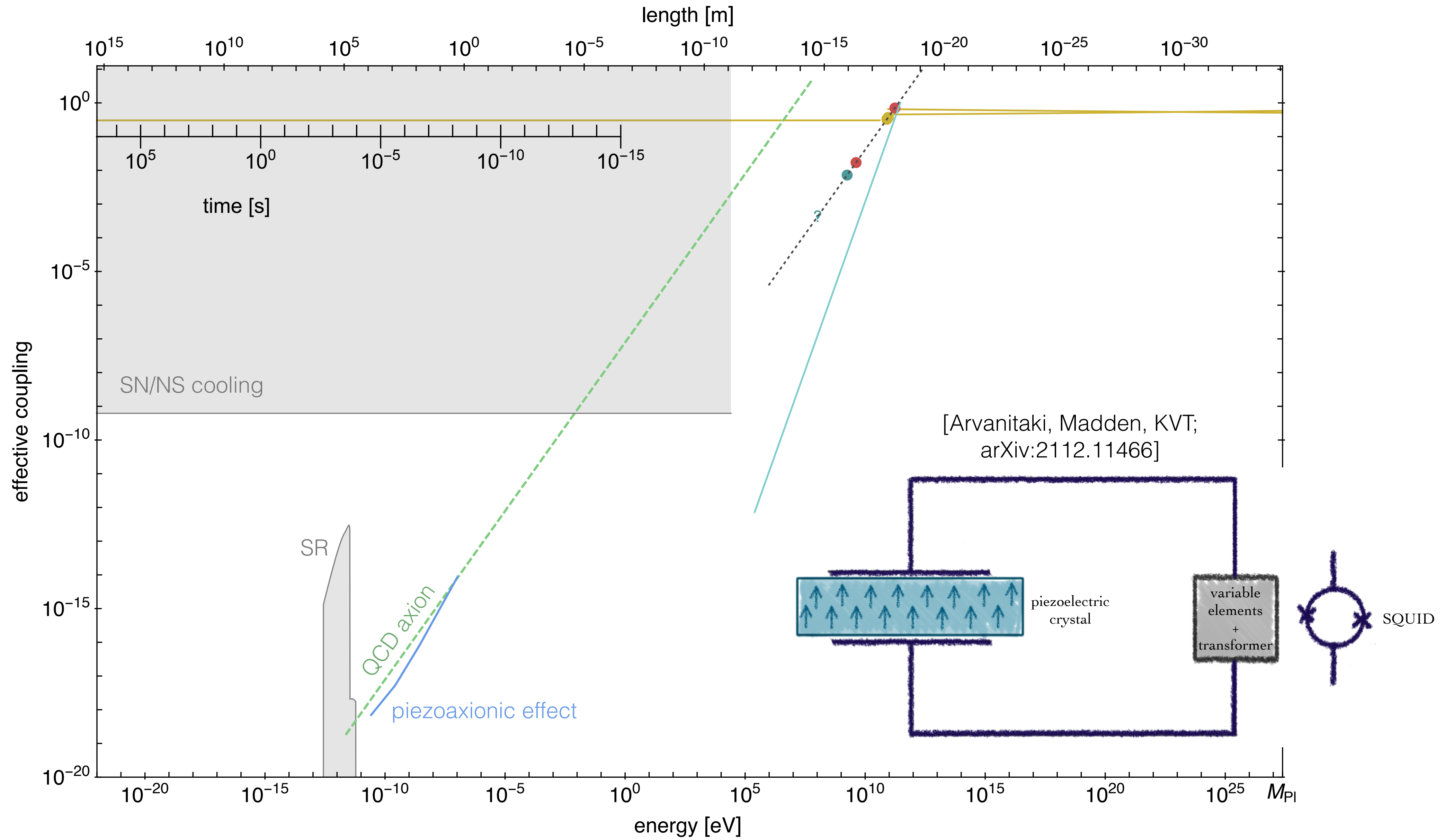


[Baryakhtar, Huang, Lasenby;
PRD 98 3 (2018)]

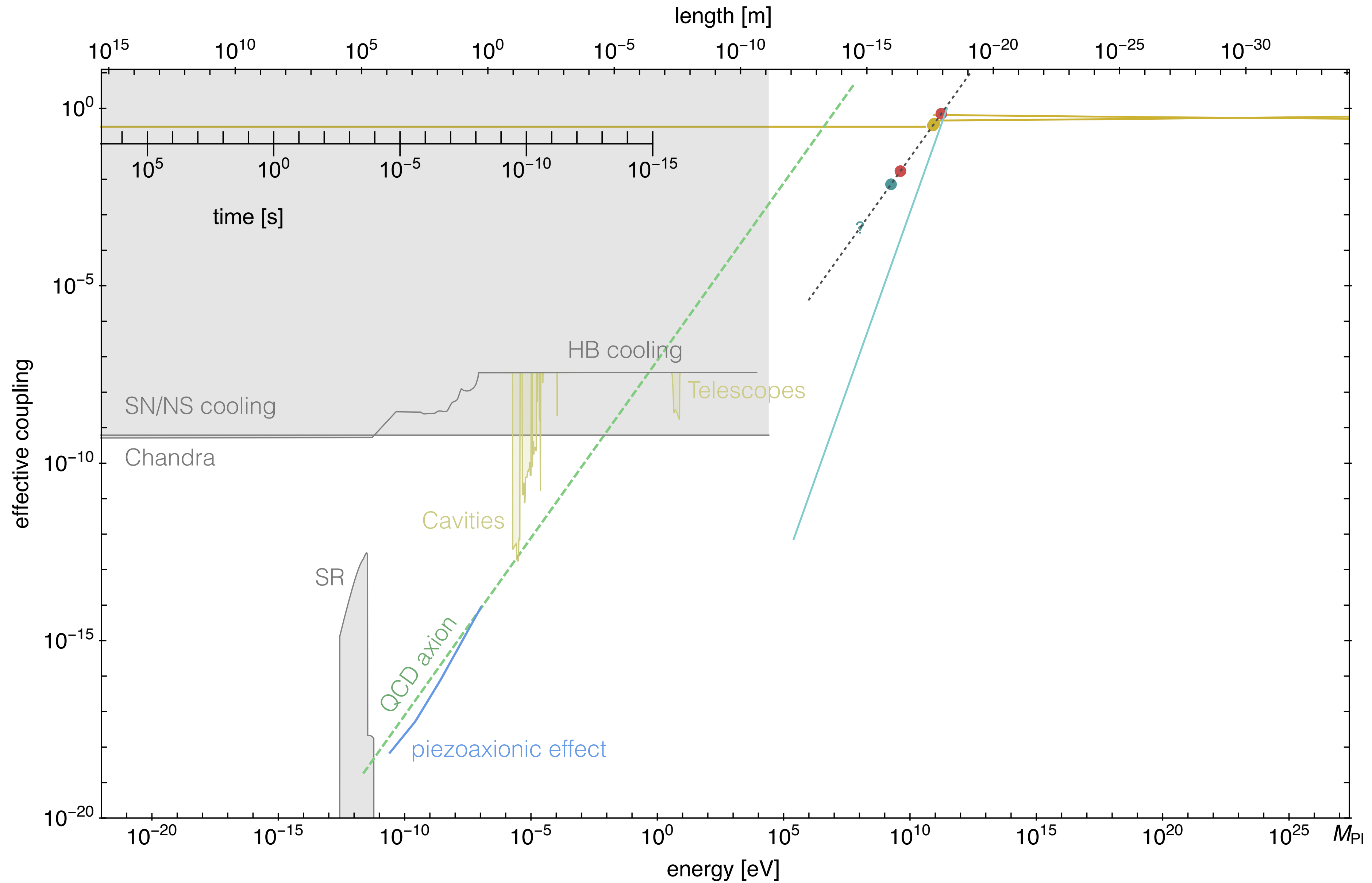
[Chiles, Charaev,
Lasenby, Baryakhtar, Huang, ...,
KVT, ..., Nam, Berggren;
arXiv:2110.01582]



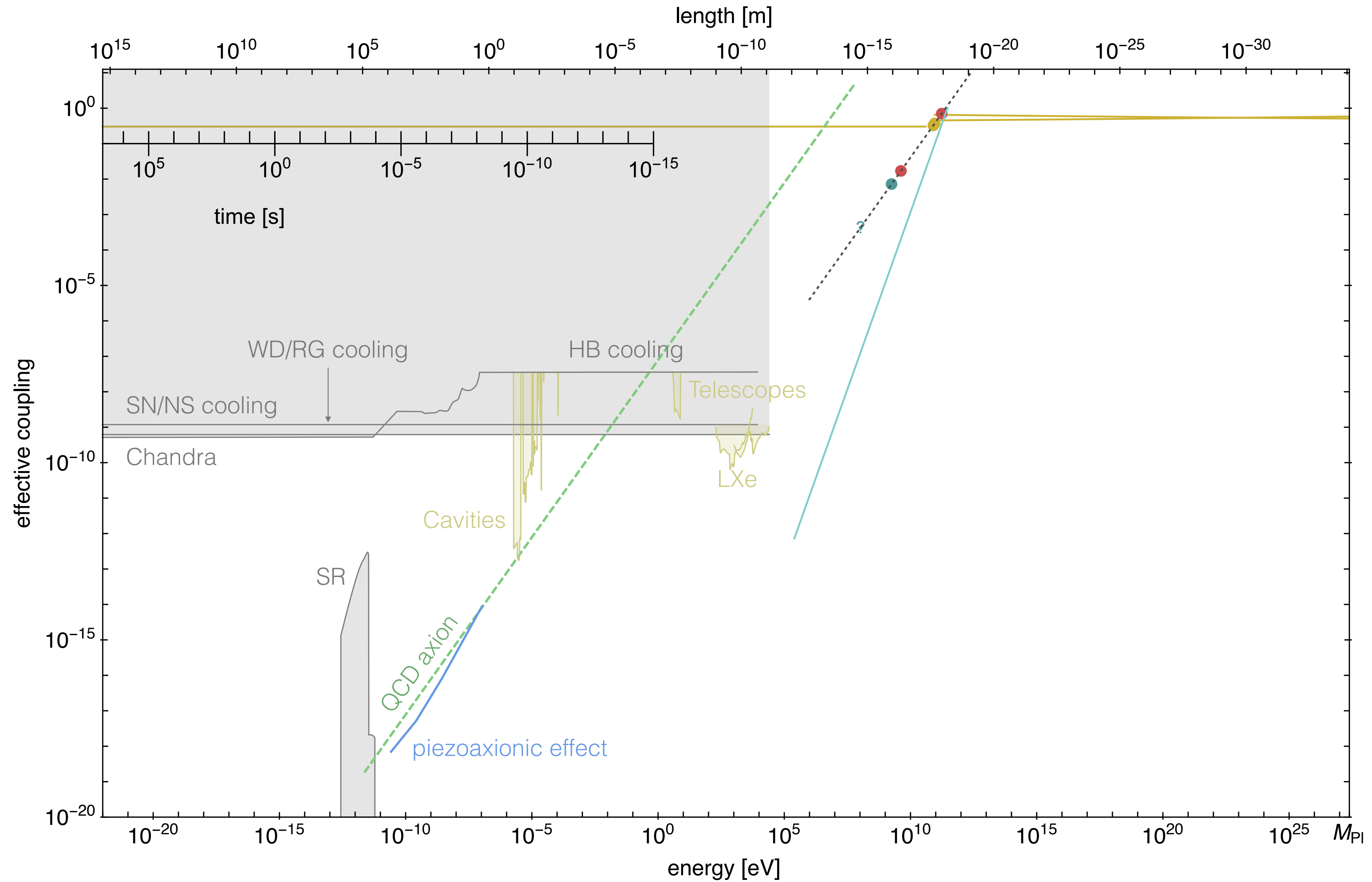
Axion Nuclear Coupling



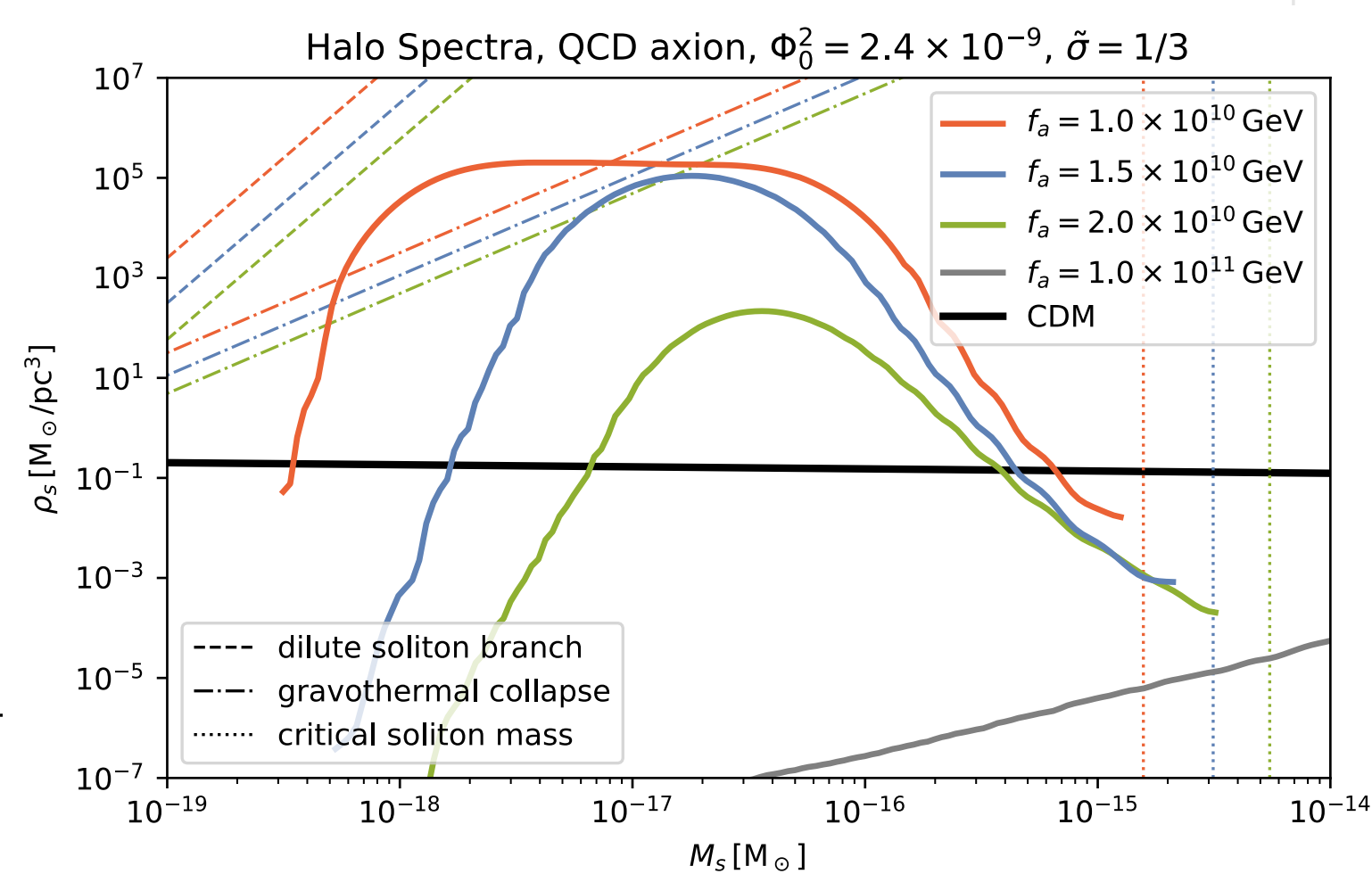
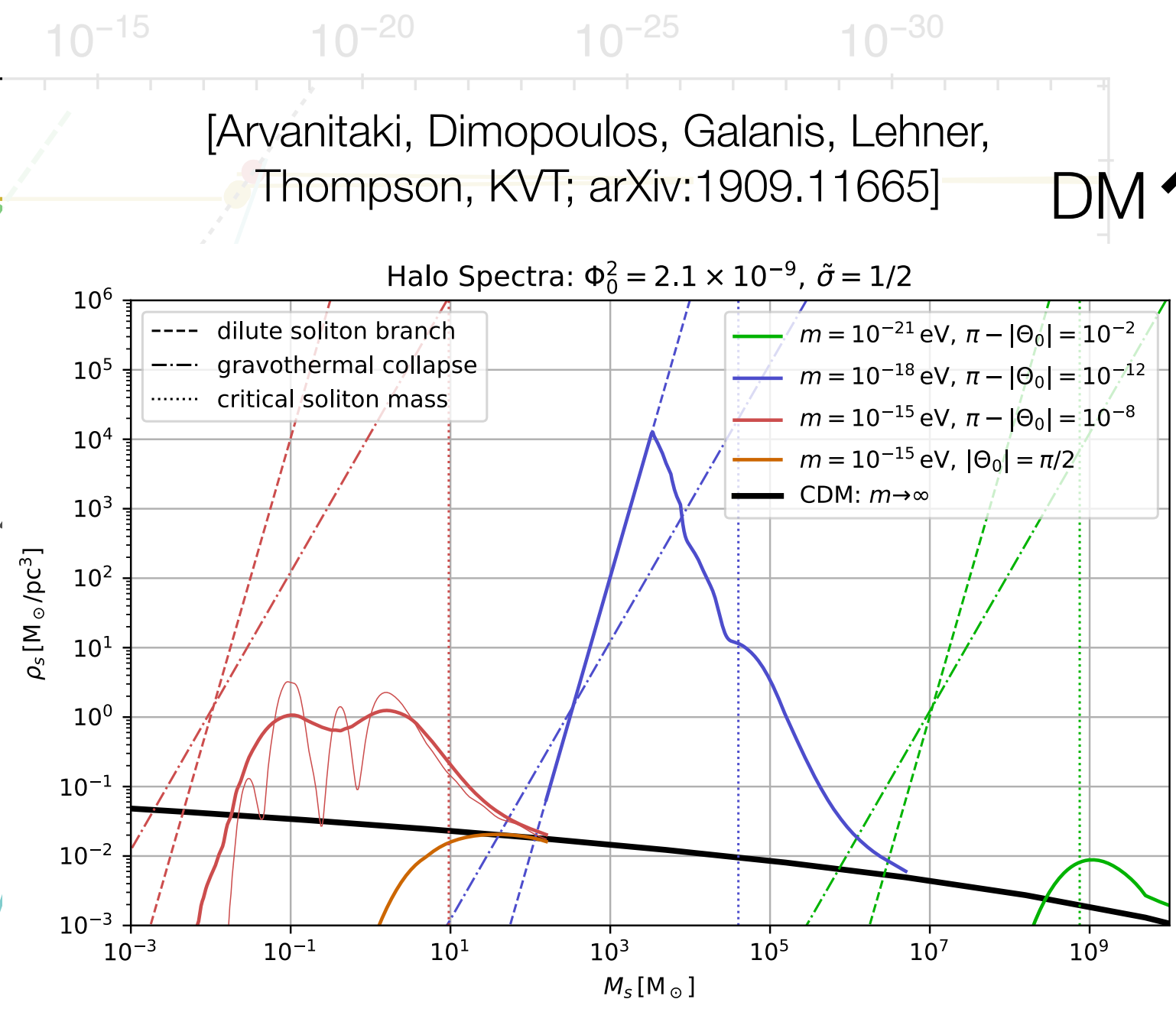
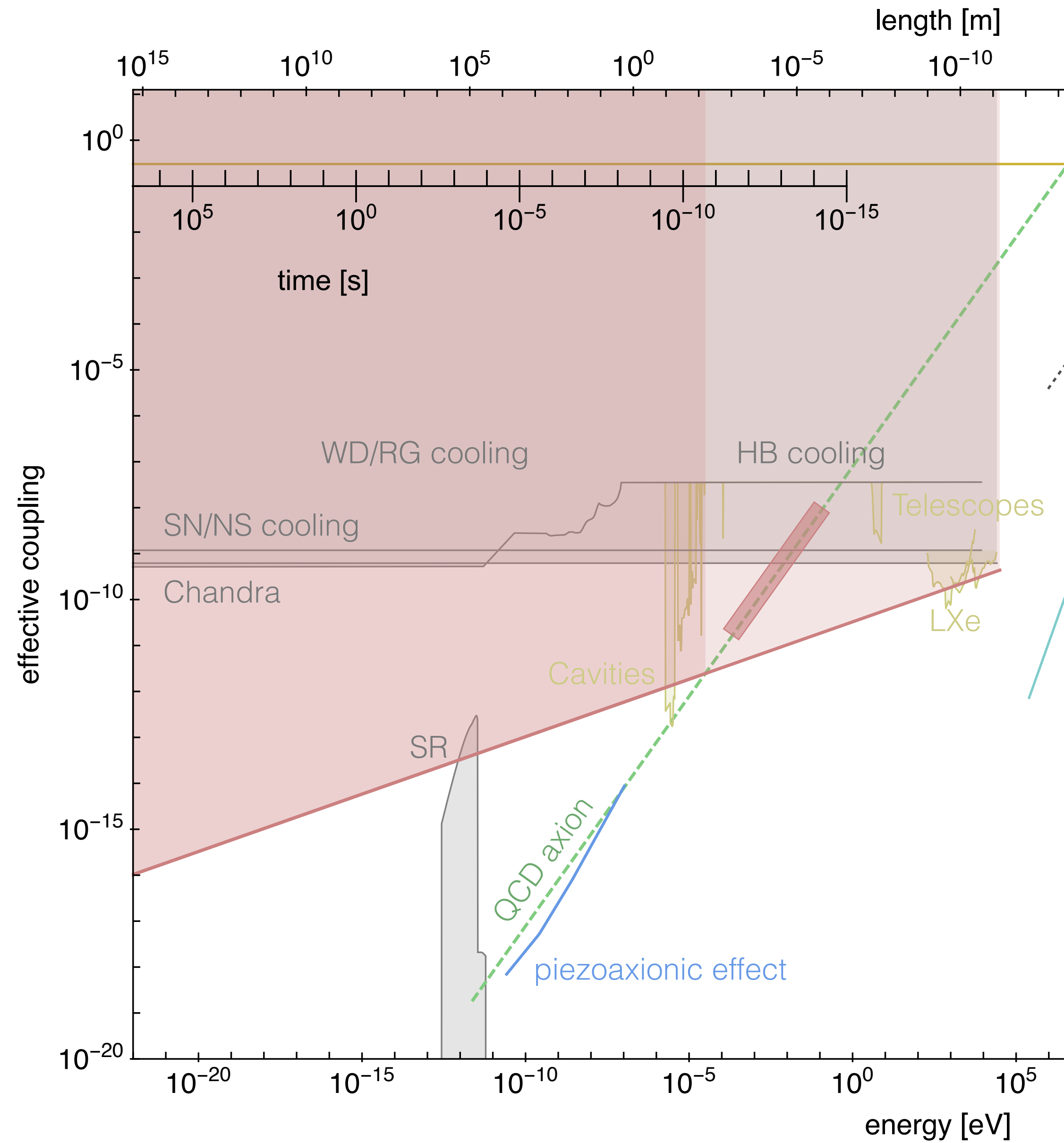
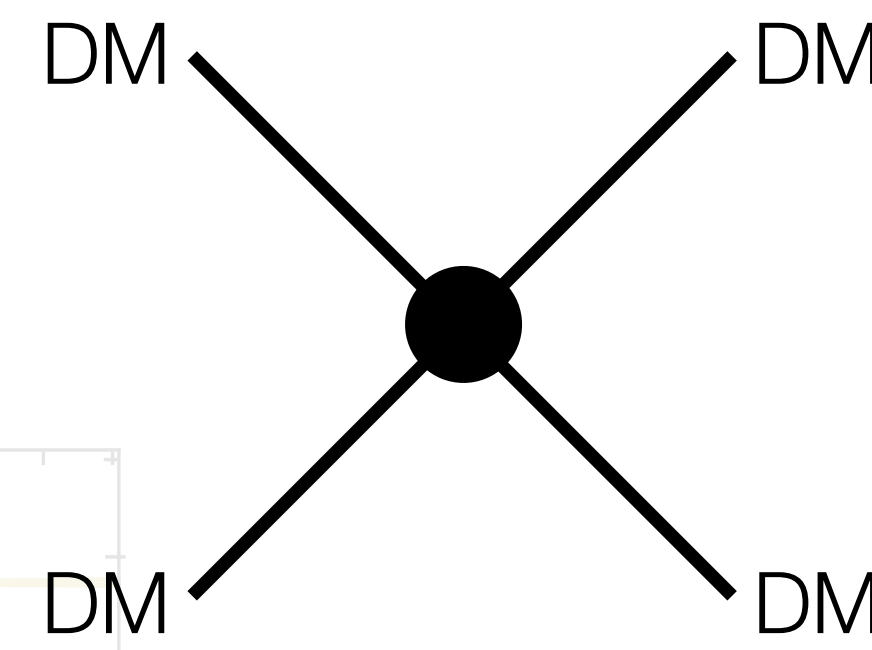
Axion Photon Coupling



Axion Electron Coupling



Compact Axion DM Structures



The Outline

How does dark matter fit into theoretical particle physics?

The evidence for dark matter!

A motivation “metric” for dark matter theories

General principles of precision-frontier dark matter detection

Future Outlook

Technological Improvements

Hard Engineering

Innovative Background Mitigation

Innovative Detection Concepts

Indirect Gravitational Probes



“Measure what is measurable, and make measurable what is not so.” — Galileo