

Flavour Physics (of quarks)

Part 4: Flavour Changing Neutral Currents

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Warwick Week Graduate Lectures

April 2022

Lecture 1: Flavour in the SM

- ▶ Flavour in the SM
- ▶ Quark Model History
- ▶ The CKM matrix

Lecture 2: Mixing and CP violation

- ▶ Neutral Meson Mixing (no CPV)
- ▶ B -meson production and experiments
- ▶ CP violation

Lecture 3: Measuring the CKM parameters

- ▶ Measuring CKM elements and phases
- ▶ Global CKM fits
- ▶ CPT and T -reversal
- ▶ Dipole moments

Lecture 4: Flavour Changing Neutral Currents (Today)

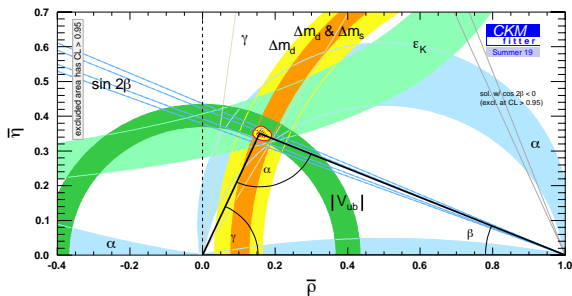
- ▶ Effective Theories
- ▶ New Physics in B mixing
- ▶ New Physics in rare $b \rightarrow s$ processes
- ▶ Lepton Flavour Violation

1. Recap

Recap

Last time we looked at

- ▶ Measurements of the CKM matrix elements
- ▶ Measurements of the CKM matrix phases
- ▶ Recall from Lecture 1 the lack of tree-level flavour-changing-neutral-currents (FCNCs) in the SM



Strong CP problem

- ▶ The complicated nature of the QCD vacuum should give rise to a term in the Lagrangian like

$$\mathcal{L}_\theta = \theta \frac{\alpha_s}{8\pi} F_\alpha^{\mu\nu} \tilde{F}_{\alpha,\mu\nu} \quad (1)$$

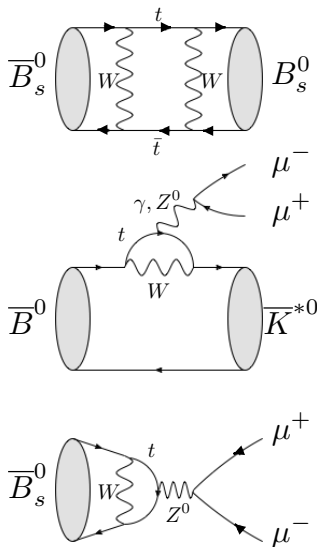
- ▶ This is both P and T -violating but C -conserving (hence CP -violating)
- ▶ This term would also contribute to the neutron dipole moment, but experimentally we know this is very small

$$d_n \sim e \cdot \theta \cdot m_q / M_N^2 \implies \theta \leq 10^{-9} \quad (2)$$

- ▶ This is incredibly small size of the θ parameter is (another) massive fine tuning problem (the so-called "strong CP problem")
- ▶ What mechanism forces θ to be so small?

- ▶ The Peccei-Quin solution to the strong CP problem is to introduce a $U(1)$ symmetry that removes the strong CP problem by dynamically making θ small
- ▶ Spontaneous breaking of this symmetry is associated with a pseudo-Nambu-Goldstone boson (in analogy with the Higgs mechanism), [the axion](#)
- ▶ The axion can be a light particle that couples very weakly to known SM particles
- ▶ There are a large number of searches for axions produced in particle colliders (direct searches)
- ▶ Can also be detected by the presence of axions converting into photons in the presence of a strong magnetic field (e.g. the CAST experiment at CERN)

- ▶ FCNC processes can probe incredibly high mass scales (well beyond those directly accessible at the LHC)
 - ▶ If there are new particles at the TeV-scale, why don't they manifest themselves in FCNC processes (the so-called "flavour problem")
- ▶ There are two types of FCNC process:
 - ▶ $\Delta F = 2$: meson anti-meson mixing
 - ▶ $\Delta F = 1$: "rare decays" e.g. $B_s^0 \rightarrow \mu^+ \mu^-$ or $B^0 \rightarrow K^{*0} \mu^+ \mu^-$
- ▶ In the SM these processes are heavily suppressed
 - ▶ They are loop processes that are CKM suppressed and (depending on the process) can also be GIM suppressed and/or helicity suppressed



3. Effective Theories

Effective Theories

- ▶ In meson/baryon decays there is a clear separation of scales which we can “decouple”
 - ▶ b quark states have $m \sim 5$ GeV while particles in loops (W^\pm, t) have $m \sim 100$ GeV

$$m_w \gg m_b > \Lambda_{\text{QCD}} \quad (3)$$

- ▶ We want to study the physics of the mixing/decay at or below a scale, Λ_{NP} , in a theory which has contributions from particles at a scale **below and above** Λ_{NP}
- ▶ We can replace the full theory with an effective theory (which is renormalisable) valid at Λ

$$\mathcal{L}(\phi_L, \phi_H) \rightarrow \mathcal{L}(\phi_L) + \mathcal{L}_{\text{eff}} = \mathcal{L}(\phi_L) + \underbrace{\sum_i C_i \mathcal{O}_i(\phi_L)}_{\text{operator product expansion}} \quad (4)$$

- ▶ In other words for interactions originating at a high scale (*i.e.* SM+NP) we get an effective matrix element

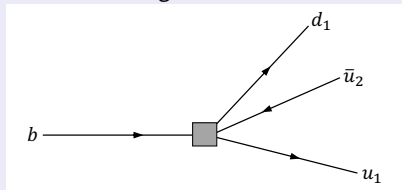
$$\langle f | H_{\text{eff}} | i \rangle = \sum_k \frac{1}{\Lambda^k} \sum_i \underbrace{C_{k,i}}_{\substack{\text{short distance} \\ \text{contribution} \\ \text{(physics} > \Lambda)}} \underbrace{\langle f | \mathcal{O}_k | i \rangle}_\Lambda \quad (5)$$

“Local operators”
long distance
contribution
(physics < Λ)

- ▶ The so-called “**Wilson coefficients**” are independent of Λ

Non-leptonic b decay

e.g. $b \rightarrow u\bar{c}s$



$$H_{\text{eff}}(b \rightarrow u_1 \bar{u}_2 d_1) =$$

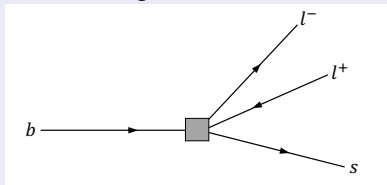
$$\frac{G_F}{\sqrt{2}} V_{u_1 b} V_{u_2 d_1}^* [\mathcal{C}_1 \mathcal{O}_1^{u_1 \bar{u}_2 d_1} + \mathcal{C}_2 \mathcal{O}_2^{u_1 \bar{u}_2 d_1}]$$

$$\mathcal{O}_1^{u_1 \bar{u}_2 d_1} = (\bar{u}_1^\alpha \gamma_\mu (1 - \gamma_5) b^\beta) (\bar{d}_1^\beta \gamma^\mu (1 - \gamma_5) u_2^\alpha)$$

$$\mathcal{O}_2^{u_1 \bar{u}_2 d_1} = (\bar{u}_1^\alpha \gamma_\mu (1 - \gamma_5) b^\alpha) (\bar{d}_1^\beta \gamma^\mu (1 - \gamma_5) u_2^\beta)$$

EW penguin

e.g. $b \rightarrow s \ell^+ \ell^-$



$$H_{\text{eff}}(b \rightarrow s \ell^+ \ell^-) =$$

$$\frac{2G_F}{\sqrt{2}} V_{ts} V_{tb}^* \sum_{i=9,10} \mathcal{C}_i \mathcal{O}_i$$

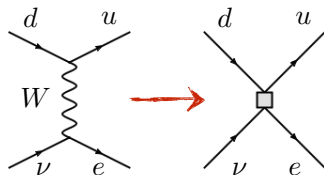
$$\mathcal{O}_9 = (\bar{s}_L \gamma_\mu b_L) (\bar{\ell} \gamma^\mu \ell)$$

$$\mathcal{O}_{10} = (\bar{s}_L \gamma_\mu b_L) (\bar{\ell} \gamma^\mu \gamma_5 \ell)$$

$$\mathcal{C} = \mathcal{C}_{\text{SM}} + \mathcal{C}_{\text{NP}} \quad \text{and is complex}$$

Fermi's theory

- ▶ In the Fermi model of the weak interaction, the full electroweak Lagrangian (which was unknown at the time) is replaced by a low-energy theory (QED) plus a single operator with an effective coupling constant

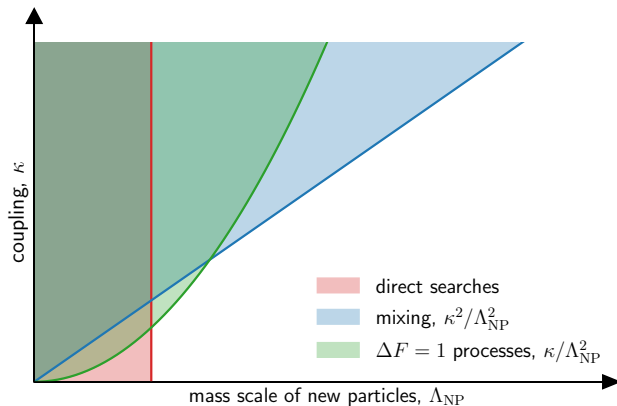


- ▶ At low energies the full theory can be replaced by a 4-fermion operator and a single coupling constant, G_F , as

$$\lim_{q^2 \rightarrow 0} \left(\frac{g^2}{m_W^2 - q^2} \right) = \frac{g^2}{m_W^2} \quad (6)$$

- ▶ The Lagrangian simplifies to

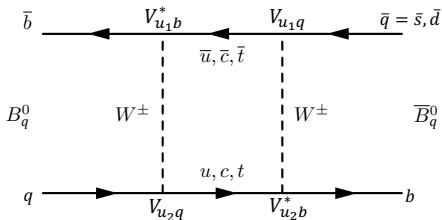
$$\mathcal{L}_{EW} \rightarrow \mathcal{L}_{QED} + \frac{G_F}{\sqrt{2}} (\bar{u}d)(e\bar{\nu}) \quad (7)$$



- ▶ In reality the direct searches do have *some* dependence on κ as you need a coupling to SM particles in order to produce the new particles in pp collisions

4. $\Delta F = 2$ processes (NP in B mixing)

- ▶ Take neutral B mixing diagram as an example



- ▶ Have an amplitude (summed over up-type quarks in the loop, u_1, u_2)

$$\mathcal{A}(B_q^0 \rightarrow \bar{B}_q^0) = \sum_{u_1, u_2} (V_{u_1 b}^* V_{u_1 q})(V_{u_2 b}^* V_{u_2 q}) A_{u_1 u_2} \quad \text{where} \quad A_{u_1 u_2} \propto m_{u_1} m_{u_2} / m_W^2 \quad (8)$$

- ▶ Inserting the known CKM constraint $V_{ub}^* V_{ud} + V_{cb}^* V_{cd} + V_{tb}^* V_{td} = 0$ gives

$$\mathcal{A}(B_q^0 \rightarrow \bar{B}_q^0) = \sum_{u_1} (V_{u_1 b}^* V_{u_1 d} [V_{tb}^* V_{td} (A_{tu_1} - A_{uu_1}) + V_{cb}^* V_{cd} (A_{cu_1} - A_{uu_1})]) \quad (9)$$

so for the B system the top totally dominates as $A_{tu_1} \gg A_{cu_1} \gg A_{uu_1}$

- ▶ Introducing new physics at some higher scale, Λ_{NP} , with coupling, κ_{NP}

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{\kappa_{\text{NP}}^2}{\Lambda_{\text{NP}}^{d-4}} \mathcal{O}_i^{(d)} \quad (10)$$

- ▶ With the **SM contribution** from the box diagram

$$(V_{tb}^* V_{td})^2 \frac{g^4 m_t^2}{16\pi^2 m_W^4}$$

- ▶ and a **NP contribution** (at dimension 6)

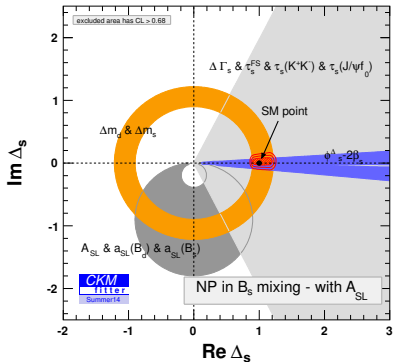
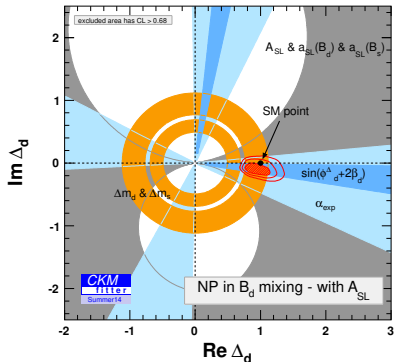
$$\frac{\kappa_{\text{NP}}^2}{\Lambda_{\text{NP}}^2}$$

New physics in B mixing

- ▶ Quantify the NP contribution to B mixing with a multiplicative factor such that

$$M_{12} = M_{12,SM} \cdot \Delta_q \quad (11)$$

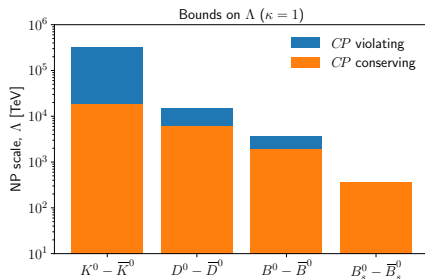
- ▶ Constraints provided by CKM fitter show that the result is consistent with the SM (i.e. $\text{Re}(\Delta) = 1$ and $\text{Im}(\Delta) = 0$)



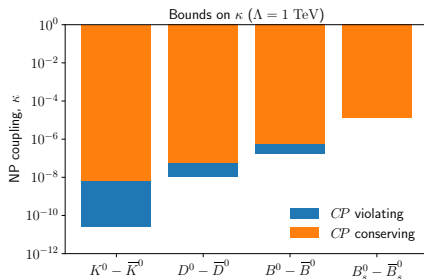
New physics constraints from neutral mixing

- ▶ So far everything shows consistency with the SM
- ▶ We can use this to set limits on the size of the NP scale (Λ) or coupling to SM (κ)

Plots produced using [\[arXiv:1002.0900\]](#)



Scale of NP if $\kappa = 1$



Size of κ if $\Lambda = 1$ TeV

Small couplings?

- ▶ New flavour violating sources (if there are any) must be highly tuned
 - ▶ Either come with a very small coupling constant
 - ▶ Or must have a very large mass
- ▶ For an $\mathcal{O}(1)$ effect:

- ▶ generic tree-level

$$\kappa_{\text{NP}} \sim 1 \quad \longrightarrow \quad \Lambda_{\text{NP}} \gtrsim 10^4 \text{ TeV}$$

- ▶ generic loop-order

$$\kappa_{\text{NP}} \sim \frac{1}{(4\pi)^2} \quad \longrightarrow \quad \Lambda_{\text{NP}} \gtrsim 10^3 \text{ TeV}$$

- ▶ tree-level with “alignment”

$$\kappa_{\text{NP}} \sim (y_t V_{ti}^* V_{tj})^2 \quad \longrightarrow \quad \Lambda_{\text{NP}} \gtrsim 5 \text{ TeV}$$

- ▶ loop-order with “alignment”

$$\kappa_{\text{NP}} \sim \frac{(y_t V_{ti}^* V_{tj})^2}{(4\pi)^2} \quad \longrightarrow \quad \Lambda_{\text{NP}} \gtrsim 0.5 \text{ TeV}$$

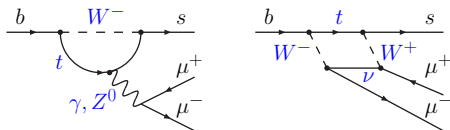
Minimal Flavour Violation

- ▶ One way of achieving small couplings is to build models that have a flavour structure which is “aligned” with the CKM matrix
 - ▶ Require that the Yukawa couplings are also the unique source of flavour breaking beyond the SM
- ▶ This is referred to as **minimal flavour violation** (MFV)
- ▶ The couplings to new particles are naturally suppressed by the Hierarchy of CKM elements
- ▶ Clearly this massively degrades the sensitivity to finding it

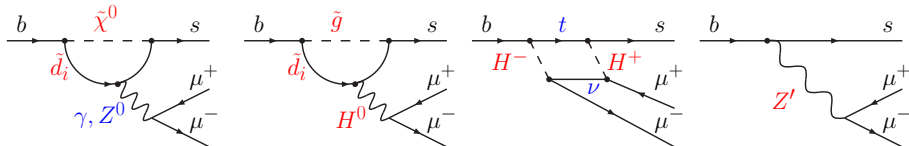
5. $\Delta F = 1$ processes (Rare B decays)

$\Delta F = 1$ FCNC decays

- ▶ FCNC transitions only occur at loop order (and beyond) in the SM
- ▶ The SM diagrams involve the charged current interaction (W^\pm)



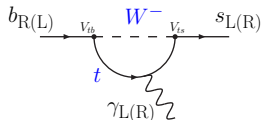
- ▶ New particles can also contribute (at either tree or loop level depending on the NP characteristics)



- ▶ The effect of the NP amplitudes can be to enhance (or suppress) decays, introduce new sources of CP violation or modify angular distributions of final-state particles (as their spin structure and coupling will be different to the SM)

Properties of $\Delta F = 1$ processes

- ▶ There are a large number of other observables that can be considered
- ▶ In the SM, photons from $b \rightarrow s\gamma$ decays are predominantly left-handed ($C_7/C_7' \sim m_b/m_s$) due to the charged current interaction



- ▶ The flavour structure of the SM implies that the rate of $b \rightarrow d$ processes is suppressed by $|V_{td}/V_{ts}|^2$ relative to $b \rightarrow s$ processes
- ▶ In the SM

$$\Gamma(B \rightarrow M\mu^+\mu^-) \approx \Gamma(B \rightarrow Me^+e^-)$$

due to the universal couplings of the gauge bosons (except the Higgs) to the different lepton flavours (known as **lepton universality**). The only differences in the rate come down to phase-space considerations

- ▶ Direct lepton flavour violation is unobservable **in the SM** at any conceivable experiment due to the small size of the neutrino mass

The effective theory for rare $b \rightarrow s$ decays

- ▶ Can write an effective theory Hamiltonian as

$$H_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{\alpha_e}{4\pi} \sum_i C_i(\mu) \mathcal{O}_i(\mu) \quad (12)$$

Weak decay, $(1/m_W)^2$

CKM suppression

Loop suppression, $(1/4\pi)^2$

Wilson coefficient (integrating out scales above μ)

Local operator with different Lorentz structure (vector, axial vector etc.)

- ▶ Then introduce new particles that give rise to corrections

$$\Delta H_{\text{eff}} = \frac{\kappa_{\text{NP}}}{\Lambda_{\text{NP}}^2} \mathcal{O}_{\text{NP}} \quad (13)$$

NP scale

local operator

- ▶ The constant κ can share some, all or none of the suppression of the SM process

Leptonic decay operators

- ▶ Have already seen some of the non-leptonic operators (and the $b \rightarrow sl^+l^-$ operators \mathcal{O}_9 and \mathcal{O}_{10})

$$\mathcal{O}_7 = \frac{m_b}{e} \bar{s} \sigma^{\mu\nu} P_R b F_{\mu\nu}$$

EW penguin

$$\mathcal{O}_8 = g_s \frac{m_b}{e^2} \bar{s} \sigma^{\mu\nu} P_R T^\alpha b G_{\mu\nu}^\alpha$$

gluonic penguin

$$\mathcal{O}_9 = \bar{s} \gamma_\mu P_L b \bar{\ell} \gamma^\mu \ell$$

vector current

$$\mathcal{O}_{10} = \bar{s} \gamma_\mu P_L b \bar{\ell} \gamma^\mu \gamma_5 \ell$$

axial-vector current

$$\mathcal{O}'_7 = \frac{m_b}{e} \bar{s} \sigma^{\mu\nu} P_L b F_{\mu\nu}$$

$$\mathcal{O}'_8 = g_s \frac{m_b}{e^2} \bar{s} \sigma^{\mu\nu} P_L T^\alpha b G_{\mu\nu}^\alpha$$

$$\mathcal{O}'_9 = \bar{s} \gamma_\mu P_R b \bar{\ell} \gamma^\mu \ell$$

$$\mathcal{O}'_{10} = \bar{s} \gamma_\mu P_R b \bar{\ell} \gamma^\mu \gamma_5 \ell$$

right handed currents
(suppressed in the SM)

- ▶ Scalar and pseudo-scalar operators (e.g. from Higgs penguins)

$$\begin{aligned}\mathcal{O}_S &= \bar{s}P_R b \bar{\ell} \ell, & \mathcal{O}'_S &= \bar{s}P_L b \bar{\ell} \ell \\ \mathcal{O}_P &= \bar{s}P_R b \bar{\ell} \gamma_5 \ell, & \mathcal{O}'_P &= \bar{s}P_L b \bar{\ell} \gamma_5 \ell\end{aligned}$$

- ▶ Tensor operators

$$\mathcal{O}_T = \bar{s} \sigma_{\mu\nu} b \bar{\ell} \sigma^{\mu\nu} \ell, \quad \mathcal{O}'_T = \bar{s} \sigma_{\mu\nu} b \bar{\ell} \sigma^{\mu\nu} \ell$$

- ▶ All of these are vanishingly small in the SM
- ▶ **In principle one could also introduce LFV versions of every operator**

- ▶ In the effective theory we then have

$$\mathcal{A}(B \rightarrow f) = V_{tb}^* V_{tq} \sum_i C_i(M_W) U(\mu, m_W) \langle f | \mathcal{O}_i(\mu) | B \rangle_{\text{had. mat. elem.}} \quad (14)$$

- ▶ For **inclusive processes** the sum over exclusive states is related to the quark level decays

$$\mathcal{B}(B \rightarrow X_s \gamma) = \mathcal{B}(b \rightarrow s \gamma) + \mathcal{O}(\Lambda_{\text{QCD}}^2 / m_B^2) \quad (15)$$

- ▶ For **exclusive processes** we need to compute form-factors / decay constants
- ▶ In leptonic decays the matrix element can be factorised into a leptonic current and a B meson decay constant, f_{B_q}

$$\langle \ell^+ \ell^- | j_\ell j_q | B_q \rangle = \langle \ell^+ \ell^- | j_\ell | 0 \rangle \langle 0 | j_q | B_q \rangle \approx \langle \ell^+ \ell^- | j_\ell | 0 \rangle \cdot f_{B_q} \quad (16)$$

- ▶ In semi-leptonic decays the matrix element can be factorised into a leptonic current times a form-factor

$$\langle \ell^+ \ell^- M | j_\ell j_q | B_q \rangle = \langle \ell^+ \ell^- | j_\ell | 0 \rangle \langle M | j_q | B_q \rangle \approx \langle \ell^+ \ell^- | j_\ell | 0 \rangle \cdot F(q^2) + \mathcal{O}(\Lambda_{\text{QCD}} / m_B) \quad (17)$$

although, due to hadronic contributions, this factorisation is not exact

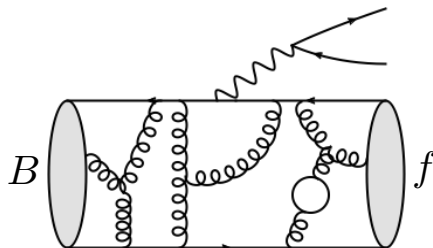
Form-factors

- ▶ Alas, we never have free quarks so we need to compute hadronic matrix elements (form-factors and decay constants) which relate us back to a real life mesonic or baryonic decay system
- ▶ This is the **non-perturbative** regime of QCD *i.e.* very difficult (and very nasty) to estimate
- ▶ Fortunately there have been considerable recent developments (last 10-20 years) which do provide us the tools to make some calculations in different kinematic regimes

What we can do



Real life



- ▶ Lattice QCD
 - ▶ Non-perturbative approach to QCD using a discretised system of points in space and time
 - ▶ As the lattice becomes infinitely large and the spacing infinitely small the continuum of QCD is reached
- ▶ Light-Cone-Sum-Rules (LCSR)
 - ▶ Exploit parton-hadron duality to compute form-factors and decay constants
- ▶ Operator product expansions (OPE)
 - ▶ Match physics at relevant scales
- ▶ Heavy quark expansion
 - ▶ Exploit the heaviness of the b quark, $m_b \gg \Lambda_{\text{QCD}}$
- ▶ QCD factorisation
 - ▶ Light quark has large energy in the meson decay frame
 - ▶ *e.g.* in $B \rightarrow \pi$ decays, quarks in the π have high energy in the B rest frame
- ▶ Soft Collinear Effective Theory
 - ▶ Model the system as highly energetic quarks interacting with soft collinear gluons
- ▶ Chiral perturbation theory

6. FCNC Experimental Results

FCNC Experimental Results

- ▶ Will mainly focus on recent measurements of B decay processes, predominantly involving $b \rightarrow s$ transitions
- ▶ These are some of the less well tested (only recently had sufficient samples of B decays for many of these measurements)
- ▶ FCNC decays of charm and strange can also be studied however the GIM mechanism is much more effective (*i.e.* there is a larger natural cancellation) for them
 - ▶ For the charm mesons the masses and mass differences are small (*i.e.* $m_c - m_s$)
 - ▶ For strange the top contribution is considerably suppressed relative to the B decays because $V_{ts} \ll V_{tb}$
- ▶ These are some of the arguments that make B physics so compelling (at least to some)

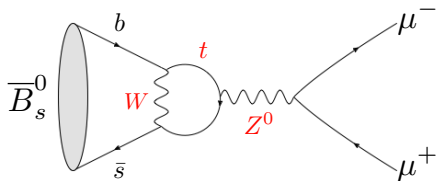
The $B_{(s)}^0 \rightarrow \mu^+ \mu^-$ decay

- ▶ $B_s^0 \rightarrow \mu^+ \mu^-$ is the golden channel for study of FCNC decays
- ▶ It is highly suppressed in the SM
 1. Loop suppressed
 2. CKM suppressed
 3. Helicity suppressed (pseudo-scalar B to two spin- $\frac{1}{2}$ muons)

SM process

with neutral current (axial-vector)

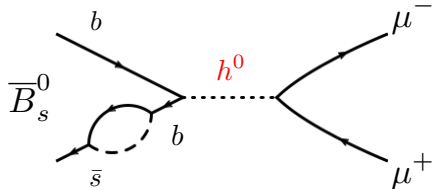
There is also a contribution from W^\pm box diagrams



Possible NP process

with scalar operators

No helicity suppression e.g. SUSY at high $\tan(\beta)$



$B_s^0 \rightarrow \mu^+ \mu^-$ in the SM

- ▶ Nice and clean because only one operator contributes in the SM

$$\mathcal{O}_{10} = (\bar{s}\gamma_\mu b)(\bar{\mu}\gamma^\mu\gamma_5\mu) \quad (18)$$

- ▶ The branching fraction in the SM is

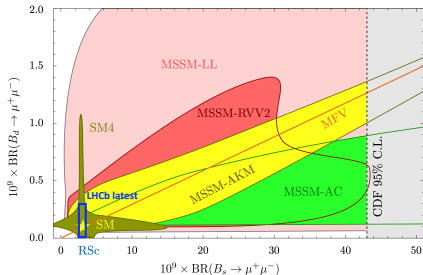
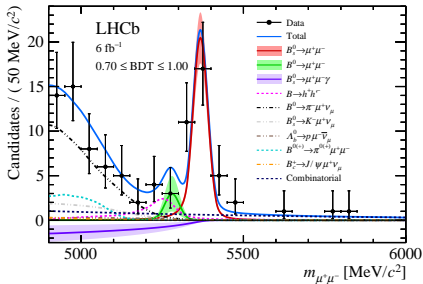
$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = \underbrace{|V_{tb}^* V_{ts}|^2}_{\text{CKM factors}} \frac{G_F^2 \alpha_e^2}{16\pi^3 \Gamma_H} M_B M_\mu^2 \underbrace{f_B^2}_{\text{Decay constant } \langle 0 | \bar{s}\gamma^\mu\gamma_5 b | B \rangle = i f_B p^\mu} \sqrt{1 - \frac{4M_\mu^2}{M_B^2}} |\mathcal{C}_{10}(m_b)|^2 \underbrace{\left(\frac{M_\mu^2}{M_B^2}\right)}_{\text{helicity suppression}}$$

- ▶ Beyond the SM

$$\frac{\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)_{\text{NP}}}{\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)_{\text{SM}}} = \frac{1}{|\mathcal{C}_{\text{SM}}|^2} \left[\left(1 - 4 \frac{m_\mu^2}{m_B^2}\right) \left| \frac{m_B}{2m_\mu} (\mathcal{C}_S - \mathcal{C}'_S) \right|^2 + \left| \frac{m_B}{2m_\mu} (\mathcal{C}_P - \mathcal{C}'_P) + (\mathcal{C}_{10} - \mathcal{C}'_{10}) \right|^2 \right]$$

$B_s^0 \rightarrow \mu^+ \mu^-$ experimental results

- ▶ Observation is the end of a long road of searches
- ▶ $B_s^0 \rightarrow \mu^+ \mu^-$ ($B^0 \rightarrow \mu^+ \mu^-$) now observed at $> 7\sigma$ ($\sim 3\sigma$). Both are consistent with the SM predictions
- ▶ No sign of NP here (unfortunately) but this does set some very strong constraints on many models



Photon polarisation

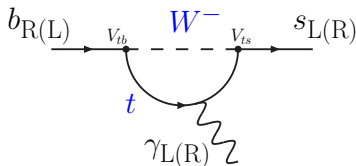
- ▶ In radiative B decays allows both

$$b_L \rightarrow s_R \gamma_R \quad (19)$$

$$b_R \rightarrow s_L \gamma_L \quad (20)$$

- ▶ However the charged current interaction **only** couples to left-handed quarks
- ▶ Need a helicity flip (boost into suitable frame) to either the b or s quark
- ▶ The right-handed contribution is therefore suppressed by

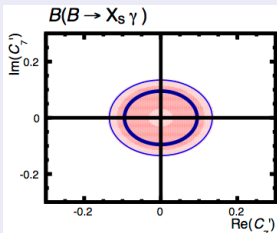
$$\frac{\mathcal{A}(b_L \rightarrow s_R \gamma_R)}{\mathcal{A}(b_R \rightarrow s_L \gamma_L)} \sim \frac{m_s}{m_b}$$



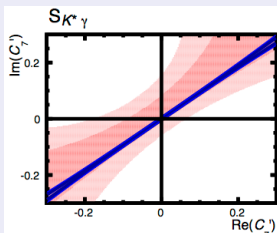
Radiative decays

- ▶ Constraints on right-handed currents in $b \rightarrow s\gamma$ decays
- ▶ Results are consistent with the LH polarisation expected in the SM

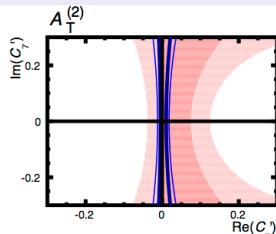
Inclusive branching fraction



Time-dependent CP violation in $B \rightarrow [K_S^0 \pi^0] \gamma$



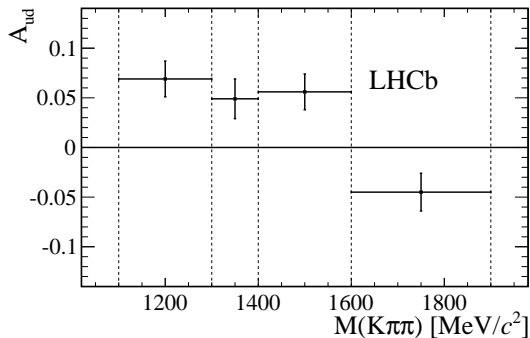
Angular distribution of $B \rightarrow K^* e^+ e^-$



Is the photon polarised?

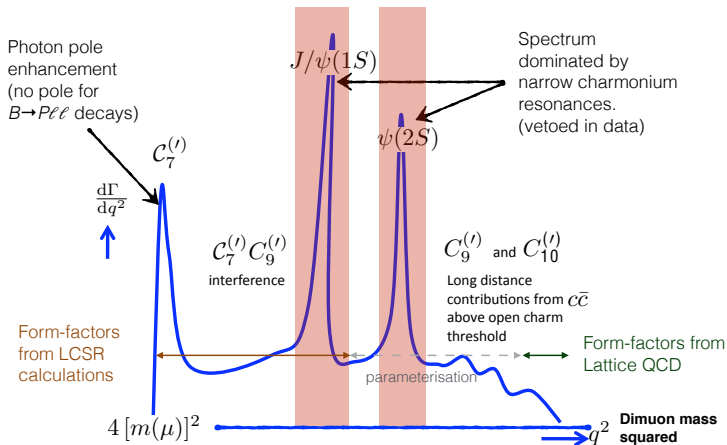
- ▶ Yes, in $B^+ \rightarrow K^+ \pi^- \pi^+ \gamma$ decays the photon has a preferred direction with respect to the $K^+ \pi^- \pi^+$ decay plane
- ▶ This can only happen if the photon is polarised

[arXiv:1402.6852]



$$b \rightarrow sl^+l^-$$

- ▶ A very important class of decays for FCNC limits are $b \rightarrow sl^+l^-$ transitions
- ▶ Understanding distributions with respect to the invariant mass of the di-lepton spectrum (q^2) is vital

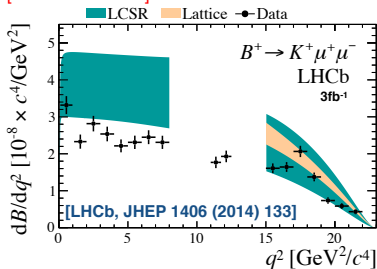


slide from Tom Blake

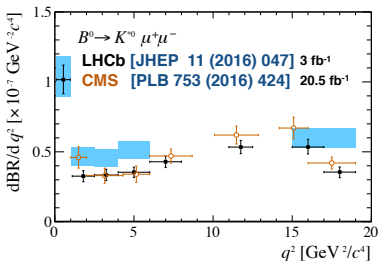
Branching fractions in $b \rightarrow s \mu^+ \mu^-$

- ▶ The LHCb (and CMS) Run 1 datasets already have precise measurements of differential branching fractions with at least comparable precision to the SM theory expectations

[arXiv:1403.8044]



[arXiv:1606.04731], [arXiv:1507.08126]



- ▶ SM predictions have large theory uncertainties from the hadronic form-factors (of which there are 3 for $B^\pm \rightarrow K^\pm$ and 7 for $B \rightarrow K^*$)
- ▶ Details of theory predictions in [arXiv:1111.2558], [arXiv:1306.0434] and [arXiv:1411.3161]

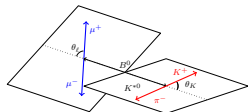
The $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ angular basis

- ▶ We have a four-body final state (as $K^{*0} \rightarrow K^+ \pi^-$)

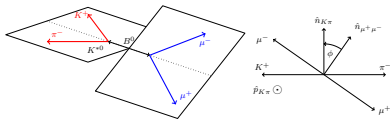
- ▶ The angular distribution provides many observables that are sensitive to new physics
- ▶ The branching fraction might not be affected (or affected at a very small level) however angular distributions can be affected by different spin structure of NP particles
- ▶ For example, at low q^2 , the angle between the two decay planes, ϕ , is sensitive to the photon polarisation

- ▶ The four-body system is described by three decay angles (defined in the helicity basis) and the dimuon invariant mass squared, q^2

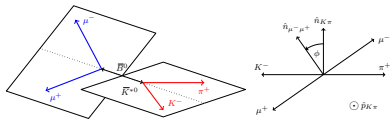
- ▶ ϕ angle between the two decay planes in the B rest-frame
- ▶ θ_ℓ, θ_K angle between the B momentum in the B frame and the $K\pi$ or $\ell^+ \ell^-$ momentum in their decay frame



(a) θ_K and θ_ℓ definitions for the B^0 decay



(b) ϕ definition for the B^0 decay



(c) ϕ definition for the \bar{B}^0 decay

The $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ angular distribution

- ▶ A rather complex angular distribution with many observables (which depend on form-factors for the $B \rightarrow K^*$ transition plus the Wilson coefficients)
- ▶ The CP -averaged angular decay rate (where $\Omega = (\theta_K, \theta_\ell, \phi)$) is

$$\begin{aligned} \frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^3(\Gamma + \bar{\Gamma})}{d\vec{\Omega}} \Big|_P &= \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\ &+ \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \\ &- F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\theta \\ &+ S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi \\ &+ \frac{4}{3} A_{FB} \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi \\ &\left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right] \end{aligned}$$

F_L

fractional longitudinal polarisation of the K^{*0}

A_{FB}

forward-backward asymmetry of the dilepton system

S_5

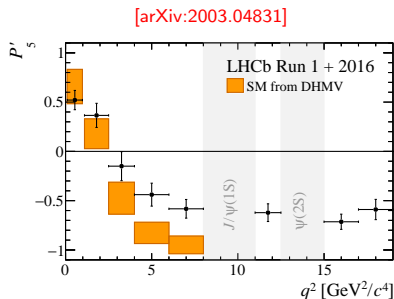
particularly sensitive to C_9

Form-factor “free” observables

- ▶ Several experiments have produced such an angular analysis (LHCb is the most sensitive)
- ▶ In QCD factorisation / SCET there are only two form factors
 - ▶ One is associated with A_0 and the other with A_{\parallel} and A_{\perp}
- ▶ Can then construct ratios of observables which are independent of the form-factors (at least to leading order) e.g.

$$P'_5 = S_5 / \sqrt{F_L(1 - F_L)}$$

- ▶ Historically there has been quite a bit of tension between predictions and measurement of P'_5 . In the latest LHCb measurement ([arXiv:]) this specific tension is a bit reduced but there remains an overall considerable tension with the SM (arising from discrepancies in P'_5 and A_{FB} and F_L)

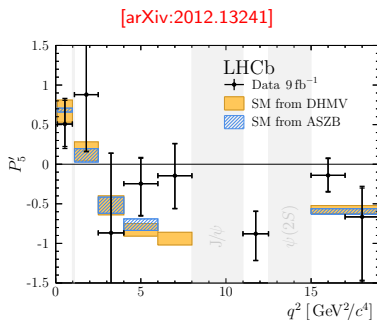


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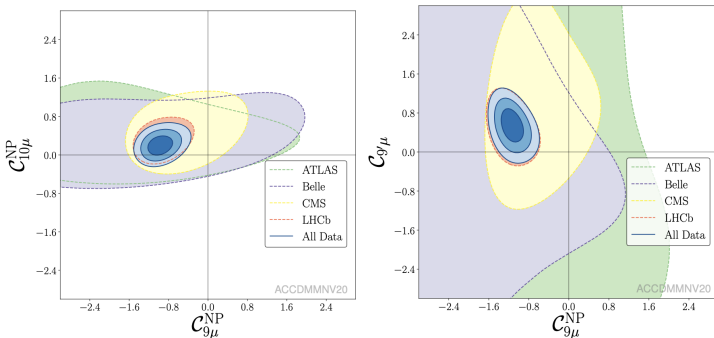
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- ▶ Also see it in the charged mode,
 $B^+ \rightarrow K^{*+} \mu^+ \mu^-$



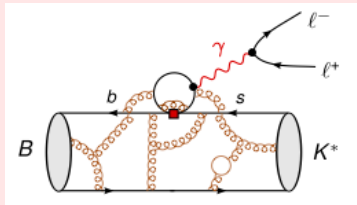
- ▶ These measurements then lead to some very nice interpretations in terms of the Wilson coefficients with global fits to $b \rightarrow s$ data
- ▶ Note a general pattern of consistency between experiments/measurements **and data** seems to favour a modified vector coupling ($C_9^{NP} \neq 0$) at $\sim 4 - 5\sigma$ (if you entirely trust the theory assumptions)

[arXiv:1903.09578] (updated 2020)



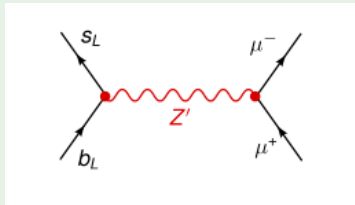
Interpretation of global fits

Pessimist's view point



- ▶ A vector-like contribution could point to a problem with our understanding of QCD
- ▶ e.g. are we correctly estimating the contribution from charm loops that produce dimuon pairs via a virtual photon?

Optimist's view point



- ▶ Vector-like contribution could come from a new tree-level contribution (e.g. Z' with $m \sim O(1)$ TeV)
- ▶ A Z' should also give effects elsewhere (e.g. particularly in mixing, which it doesn't) so a challenge for model builders who need to suppress this

Which one are you?

Further work is needed from both experiment and theory to establish what is going on here

- ▶ In the SM ratios like

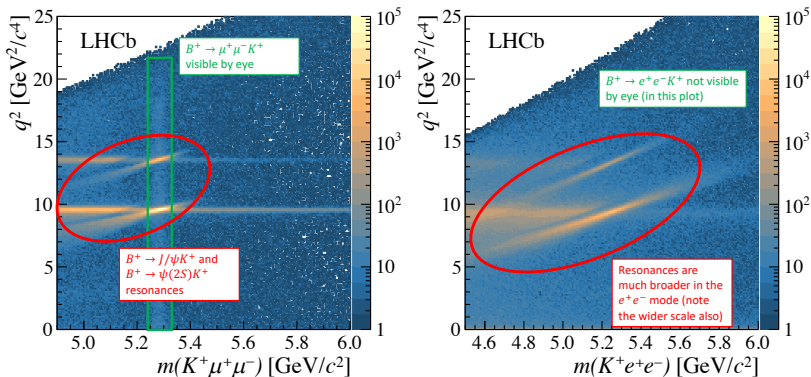
$$R_K = \frac{\int d\Gamma(B^+ \rightarrow K^+ \mu^+ \mu^-)/dq^2 \cdot dq^2}{\int d\Gamma(B^+ \rightarrow K^+ e^+ e^-)/dq^2 \cdot dq^2} \quad (21)$$

should only differ from unity by phase space

- ▶ The dominant SM processes couple equally to the different lepton flavour (apart from the Higgs)
- ▶ Incredibly theoretically clean since hadronic uncertainties cancel in the ratio (they have the same hadronic matrix element). The only consideration is from small electroweak corrections as q^2 approaches 0
- ▶ Experimentally these are much more challenging, primarily due to differences in muon/electron reconstruction
 - ▶ In particular Bremsstrahlung radiation from the electrons
 - ▶ LHCb does not have a high resolution ECAL
 - ▶ Electron efficiency is much poorer than muon efficiency at LHCb (trigger and reconstruction)

$B^+ \rightarrow K^+ l^+ l^-$ candidates

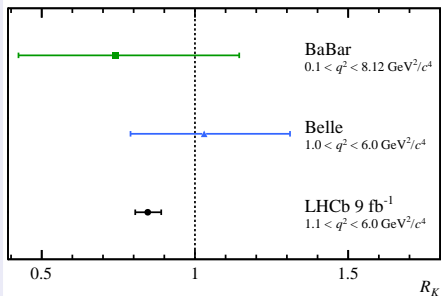
- ▶ Have to correct electrons for energy loss due to Bremsstrahlung (look for ECAL clusters (*i.e.* photons) associated with the electron track)
- ▶ This is successful to some extent but even after Bremsstrahlung recovery there are significant differences in mass resolution between the dielectron and dimuon final states



Lepton universality results

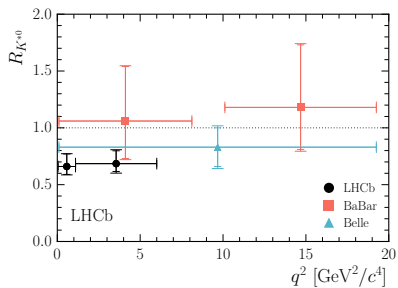
R_K from $B^\pm \rightarrow K^\pm \ell^+ \ell^-$

[arXiv:2103.11769]



$R_{K^{*0}}$ from $B^0 \rightarrow K^{*0} \ell^+ \ell^-$

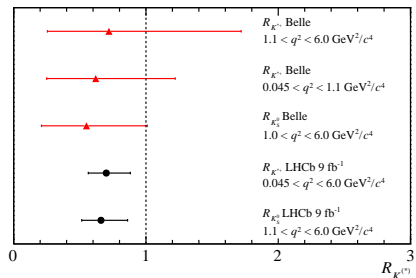
[arXiv:1705.05802]



Lepton universality results

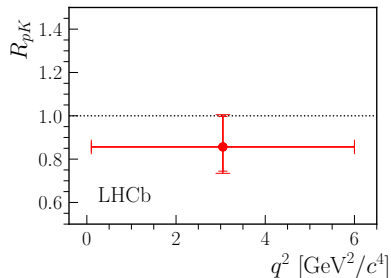
$R_{K_S^0}$ and $R_{K^{*+}}$

[arXiv:2110.09501]



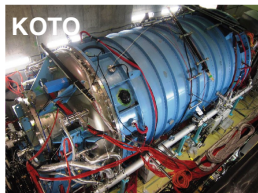
R_{pK} from $\Lambda_b^0 \rightarrow pK^- \ell^+ \ell^-$

[arXiv:1912.08139]



Rare kaon decays

- ▶ Two new rare kaon decay experiments
 - ▶ KOTO at J-PARC, searching for $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$
 - ▶ NA62 at CERN, searching for $K^+ \rightarrow \pi^+ \nu \bar{\nu}$
- ▶ The advantage (theoretically) of final states with neutrinos is that there is no contribution from quark loops involving light quarks (which can annihilate to produce charged leptons e.g. charm loops)
- ▶ The challenge experimentally is these are incredibly rare (and contain just one charged track in the final state)

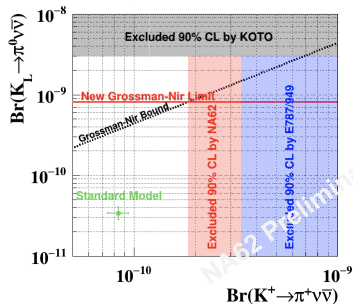
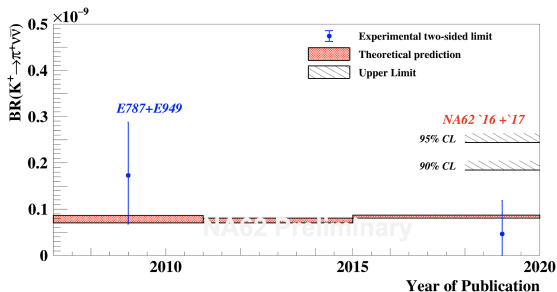


- ▶ Aim to collect a dataset of $\sim 100 K^+ \rightarrow \pi^+ \nu \bar{\nu}$ decays
- ▶ Currently have ~ 3 events in analysed data (2016+2017) giving

$$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (4.7^{+7.2}_{-4.7}) \times 10^{-11}$$

i.e. consistent with zero

- ▶ Also search for lepton number violating $K^\pm \rightarrow \pi^\mp \ell^\pm \ell^\pm$ decays



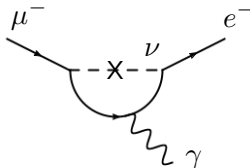
7. Lepton Flavour Violation

Lepton Flavour Violation

- ▶ Essentially forbidden in the SM by the smallness of the neutrino mass

$$\mathcal{B}(\mu \rightarrow e\gamma) \propto \frac{m_\nu^4}{m_W^4} \sim 10^{-54} \quad (22)$$

- ▶ Very powerful null test of the SM
- ▶ **Any** visible signal is a clear sign of New Physics

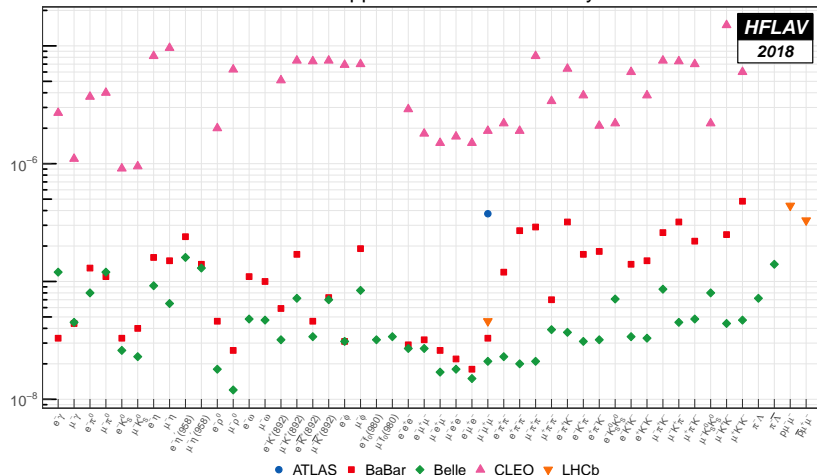


- ▶ Different signatures include
 1. $\mu \rightarrow e\gamma$ at rest (MEG at PSI, Mu2E at PSI)
 2. $\mu \rightarrow 3e$ (Mu3e at PSI)
 3. μ conversion in field of Au nucleus (SINDRUM II at PSI)

Lepton Flavour Violation in τ s

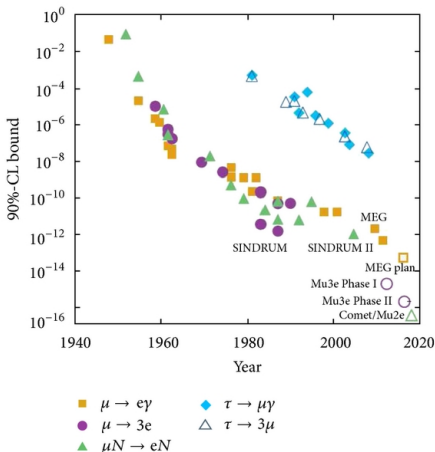
- ▶ A large number of experimental signatures
- ▶ Global summary (averages) provided by HFLAV

90% CL upper limits on τ LFV decays



Charged LFV future

- ▶ Data taking has begun at MEG-II (aiming for $O(10^{-14})$)
- ▶ New $\mu \rightarrow 3e$ experiment (Mu3e) at PSI
- ▶ Two new conversion experiments (Mu2e) at PSI and (COMET) at J-PARC
- ▶ Expect improvements for LFV τ decays from Belle 2



8. Recap

New Physics?

- ▶ We have seen in these lectures the incredible success of the CKM matrix as a predictive tool for properties of flavour decays
- ▶ Our various measurements which constrain the CKM picture are all consistent with the SM predictions
- ▶ However, there are some very tantalising hints that could suggest New Physics
 - ▶ Tension in V_{ub} (and to a lesser extent V_{cb})
 - ▶ Enhancement / tension in $B \rightarrow D^{(*)} \tau \nu_\tau$
 - ▶ Anomalies in $B \rightarrow K^{(*)} \ell^+ \ell^-$ decays
 - ▶ Muon $g-2$
- ▶ These should all be resolved in the next 5-10 years
- ▶ **It's an exciting time to be a flavour physicist!**

} all at $\gtrsim 3\sigma$

In this lecture we have covered

- ▶ Effective theories
- ▶ Flavour Changing Neutral Current processes
- ▶ Experimental constraints on new particles in $\Delta F = 1$ and $\Delta F = 2$ FCNCs
- ▶ Minimal Flavour Violation
- ▶ Lepton Flavour Violation
- ▶ Future Flavour Violation Experiments

End of Lecture 4

GAME OVER

Thanks for playing (listening)!