Fermion masses, leptogenesis and gravitational waves in SO(10)





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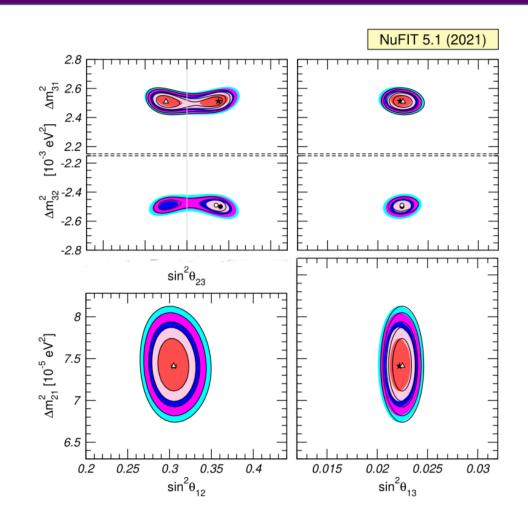
Based on the work with S. Pascoli, J. Turner, S. King, Y. Zhou and B. Fu

SUSY 2023 Southampton, 21 July 2023



The Standard Model: current issues

- Neutrino Masses and Mixing
- Baryogenesis
- The Standard Model gauge group is arbitrary
- The fermion masses and the mixing angles are free parameters
- Dark matter, ...



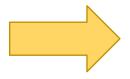


We need an extension of the Standard Model!

See talk by Yeling Zhou, Shaikh Saad etc...



Grand Unification Theory

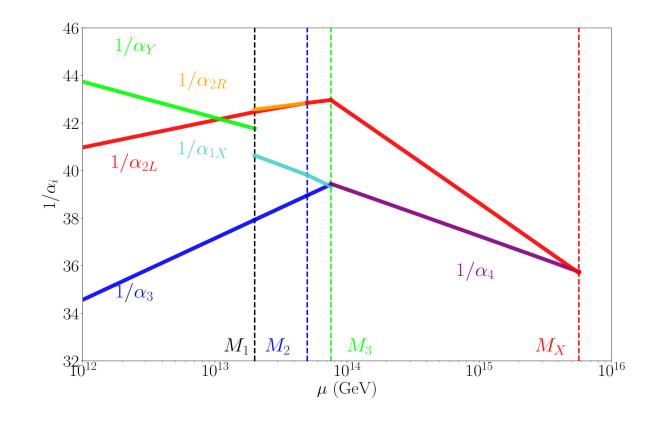


SO(10)



Gauge coupling unification

- If we study the running of the couplings of the Standard Model they almost approach the same value
- Assuming an UV complexion after a certain scale all the couplings exactly match at a certain scale
- Strong, weak and electromagnetic interactions are unified into a single fundamental force at high energies





It embeds all fermions plus an extra Standard Model singlet in one representation

$$\psi_{+} = \begin{pmatrix} u & d & \nu & e & u^c & d^c & \nu^c & e^c \end{pmatrix}_{L}$$

Reduces SM degrees of freedom and predicts fermion masses

The extra singlet can be indentified with the right-handed neutrino

Reduces SM degrees of freedom and predicts fermion masses

$$\mathcal{L} = Y_{10}\overline{\bf 16}_F {\bf 10}_H {\bf 16}_F + Y_{120}\overline{\bf 16}_F {\bf 120}_H {\bf 16}_F + Y_{\overline{126}}\overline{\bf 16}_F \overline{\bf 126}_H {\bf 16}_F$$

$$\mathcal{L}_Y = Y_u \bar{Q} \tilde{\Phi} u_R + Y_d \bar{Q} \Phi d_R + Y_e \bar{L} \Phi e_R + Y_\nu \bar{L} \tilde{\Phi} \nu_R + \text{h.c}$$



Reduces SM degrees of freedom and predicts fermion masses

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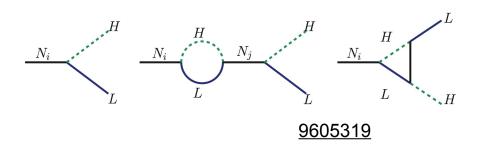
$$\mathcal{L}_Y = Y_u \bar{Q} \tilde{\Phi} u_R + Y_d \bar{Q} \Phi d_R + Y_e \bar{L} \Phi e_R + Y_\nu \bar{L} \tilde{\Phi} \nu_R + \text{h.c}$$

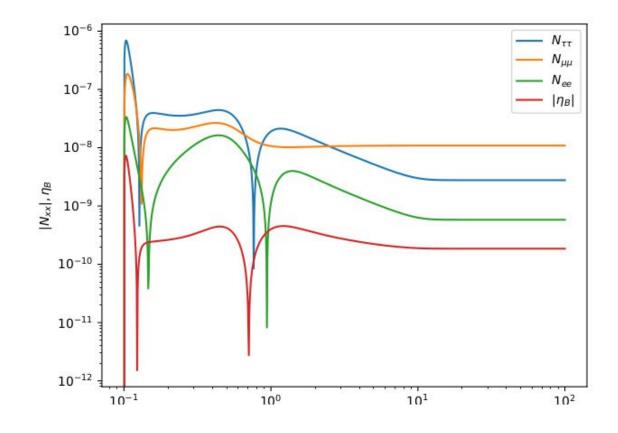
- The Yukawa couplings at low energies are now related
- The goal is to find a fixed parameterization which is dependent on the Higgs sector
- The Yukawa couplings are not anymore free parameters

$$Y_{\nu} = f(Y_u, Y_d)$$
$$Y_e = g(Y_u, Y_d)$$

The extra singlet can be identified with the right-handed neutrino

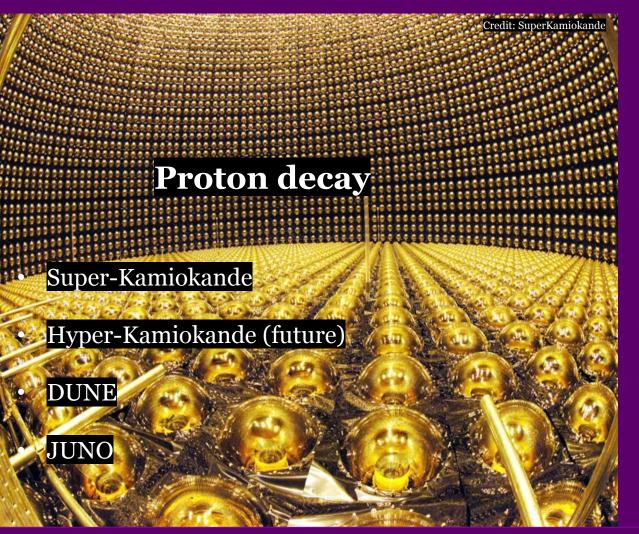
- It is possible to predict neutrino masses and mixing angles
- The presence of the right-handed neutrino allows for predicting baryogenesis via leptogenesis

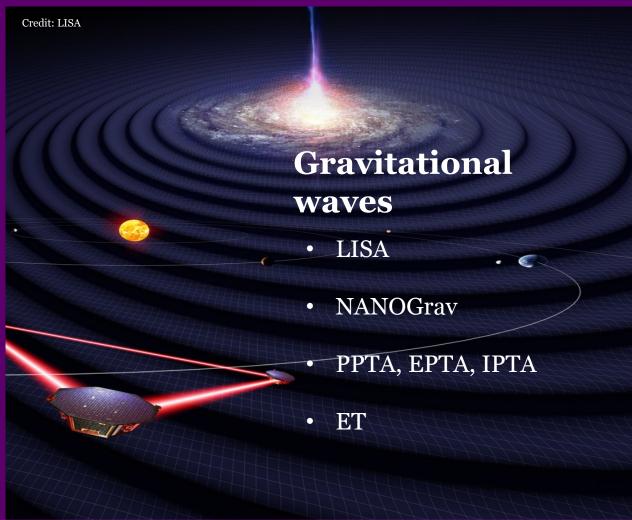






How to test SO(10)







Fu, King, LM, Pascoli, Turner, Zhou 2209.00021

Type IIIc breaking chain

$$SO(10)$$

$$\mathbf{54} \quad \text{broken at } M_X$$
 $G_3^c \equiv SU(4) \times SU(2)_L \times SU(2)_R \times Z_2^C$

$$\mathbf{210} \quad \text{broken at } M_3$$
 $G_2^c \equiv SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_X \times Z_2^C$

$$\mathbf{45} \quad \text{broken at } M_2$$
 $G_1 \equiv SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_X$

$$\boxed{\mathbf{126}} \quad \text{broken at } M_1$$
 $G_{\text{SM}} \equiv SU(3)_c \times SU(2)_L \times U(1)_Y$



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String tension

$$G\mu \simeq \frac{1}{2\left(\alpha_{2R}\left(M_{1}\right) + \alpha_{1X}\left(M_{1}\right)\right)} \frac{M_{1}^{2}}{M_{\rm pl}^{2}}$$

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Proton lifetime

$$\tau \simeq 6.9 \times 10^{35} \times \left(\frac{M_U}{10^{16} \text{GeV}}\right)^4 \text{yr}$$

The two scales are linked by

gauge unification constraint

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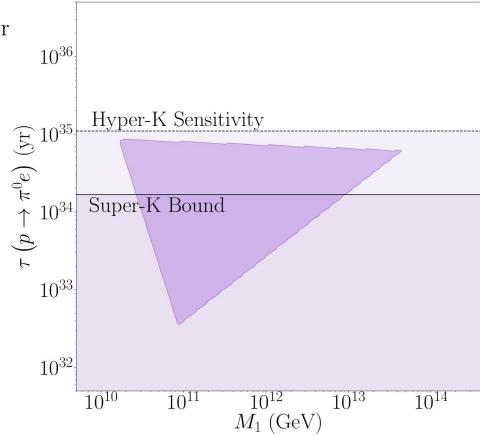
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Set RHN neutrino mass up to Yukawa couplings





$$Y_{10}, Y_{120}, Y_{\overline{126}} \\ \downarrow \\ Y_e, Y_{\nu_R}, Y_{\nu}, Y_u, Y_d \rightarrow \text{Fermion masses} \\ \downarrow \\ Y_u = h + r_2 f + i \, r_3 h' \,, \qquad Y_d = r_1 (h + f + i \, h') \,, \qquad Y_{\nu} = h - 3 r_2 f + i \, c_{\nu} h' \,, \\ \downarrow \\ \text{Boltzmann} \\ \text{equations} \qquad Y_e = r_1 (h - 3 f + i \, c_e h') \,, \qquad M_{\nu_R} = f \, \frac{\sqrt{3} \, r_1}{V_{16}} v_S \,, \\ \end{pmatrix}$$



$$Y_{10}, Y_{120}, Y_{\overline{126}}$$

$$\downarrow$$

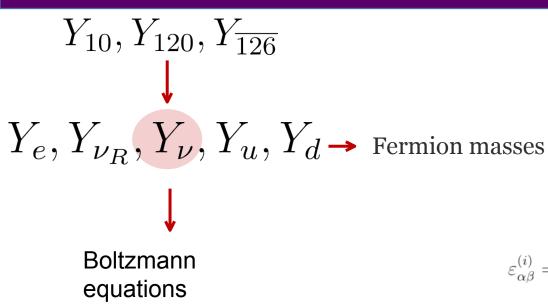
$$Y_{e}, Y_{\nu_{R}}, Y_{\nu}, Y_{u}, Y_{d} \rightarrow \text{Fermion masses}$$

$$\downarrow$$

$$Y_{v} = -\frac{3r_{2}+1}{r_{2}-1}Y_{u} + \frac{4r_{2}}{r_{1}(r_{2}-1)}\operatorname{Re} Y_{d} + i\frac{c_{\nu}}{r_{1}}\operatorname{Im} Y_{d},$$

$$Y_{e} = -\frac{4r_{1}}{r_{2}-1}Y_{u} + \frac{r_{2}+3}{r_{2}-1}\operatorname{Re} Y_{d} + ic_{e}\operatorname{Im} Y_{d}.$$





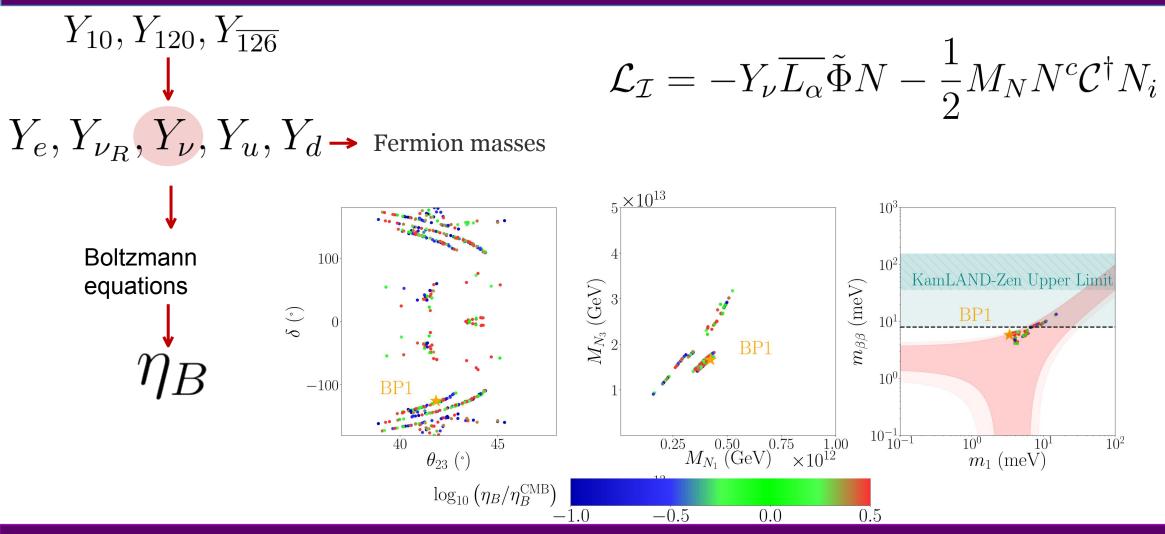
$$\mathcal{L}_{\mathcal{I}} = -Y_{\nu} \overline{L_{\alpha}} \tilde{\Phi} N - \frac{1}{2} M_N N^c \mathcal{C}^{\dagger} N_i$$

We solved **Density Matrix Equations** using ULYSSES

$$\varepsilon_{\alpha\beta}^{(i)} = \frac{3}{32\pi \left(\tilde{Y}_{\nu}^{\dagger}\tilde{Y}_{\nu}\right)_{ii}} \sum_{j\neq i} \left\{ i \left[\tilde{Y}_{\nu\alpha i} \tilde{Y}_{\nu\beta j}^{\star} \left(\tilde{Y}_{\nu}^{\dagger} \tilde{Y}_{\nu}\right)_{ji} - \tilde{Y}_{\nu\beta i}^{\star} \tilde{Y}_{\nu\alpha j} \left(\tilde{Y}_{\nu}^{\dagger} \tilde{Y}_{\nu}\right)_{ij} \right] \frac{\xi \left(x_{j}/x_{i}\right)}{\sqrt{x_{j}/x_{i}}} + i \frac{2}{3 \left(x_{j}/x_{i} - 1\right)} \left[\tilde{Y}_{\nu\alpha i} \tilde{Y}_{\nu\beta j}^{\star} \left(\tilde{Y}_{\nu}^{\dagger} \tilde{Y}_{\nu}\right)_{ij} - \tilde{Y}_{\nu\beta i}^{\star} \tilde{Y}_{\nu\alpha j} \left(\tilde{Y}_{\nu}^{\dagger} \tilde{Y}_{\nu}\right)_{ji} \right] \right\},$$

$$K_i \equiv \frac{\tilde{\Gamma}i}{H\left(T = MN_i\right)}, \quad \tilde{\Gamma}i = \frac{MN_i\left(\tilde{Y}\nu^{\dagger}\tilde{Y}\nu^{\dagger}\right)_{ii}}{8\pi}$$



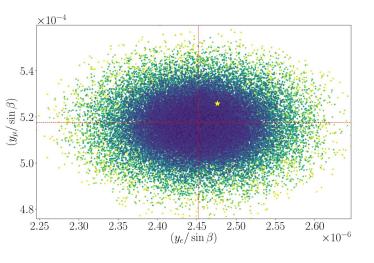


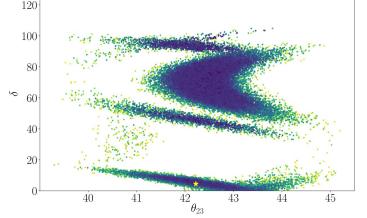


GUTFIT

$$\mathcal{P}_m \in \{a_1, a_2, r_1, r_2, c_e, c_\nu, m_0, \eta_q\}$$

$$\mathcal{O}_n \in \{m_e, m_\mu, m_\tau, \theta_{12}, \theta_{13}, \theta_{23}, \Delta m_{21}^2, \Delta m_{31}^2\}$$





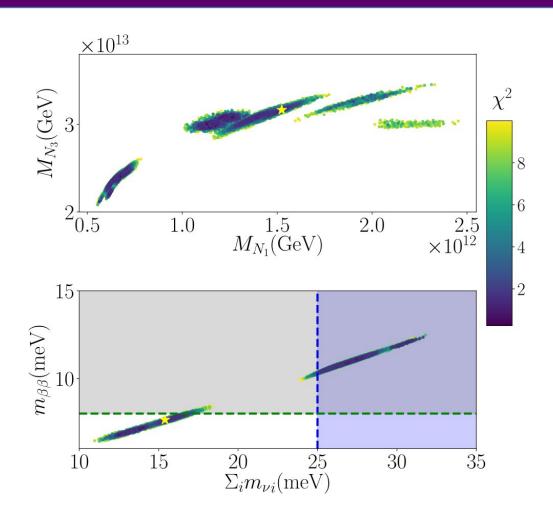
- We considered a different models
- GUTFIT used for scanning the parameter space in the next works
- Scan the parameter space using the MultiNest algorithm (nested sampling)
- It minimize the chi squared.

$$\chi^2 = \sum_n \left[\frac{\mathcal{O}_n(\mathcal{P}_m) - \mathcal{O}_n^{\mathrm{bf}}}{\sigma_{\mathcal{O}_n}} \right]^2$$

Preliminary 23xx.xxxx



Neutrinoless double beta decay and cosmology tests



- SUSY SO(10) model
- Partially testable by neutrinoless double beta decay and cosmological surveys
- It achieve leptogenesis, predict fermion masses and mixing angles

Preliminary 23xx.xxxx



Conclusions



Successful gauge coupling unification



Prediction of fermion masses and mixing angles



Testable with next-gen GW and proton decay experiments



Predict both neutrinoless double beta decay and neutrino masses in reach of the next-generation experimens



Thank you