

# Measurement of antineutrino elastic scattering on free protons in the MINERvA experiment

Noë Roy, on behalf of the MINERvA collaboration

2023

June 21<sup>st</sup>

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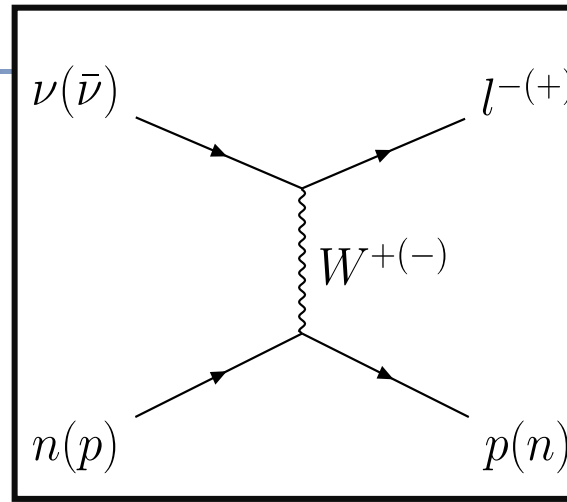


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des physiciens et physiciennes



# Why do we care?



Primary channel of interaction in high energy neutrino experiments: **neutrino scattering on nucleon**

Experiments: oscillation on various type of targets (**CH**, **Ar**, **H<sub>2</sub>O**...)

Precise models to predict the expected number of interaction in the detectors

Theoretical computations

Measurements from data

Scattering on free nucleons is be the best way to start building models for heavier nuclei

# Don't we know already that cross section?

[Phys. Rep. 3, 261–379]



## Llewellyn Smith equation :

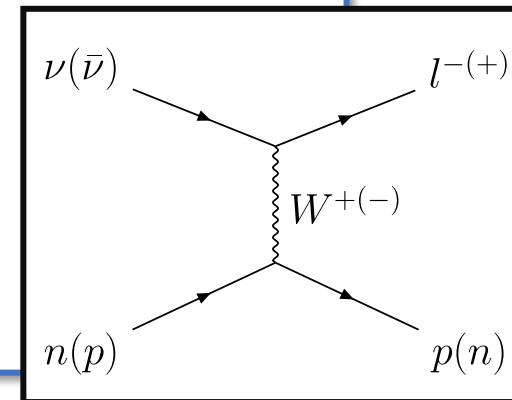
x-section wrt 4 momentum exchange between the neutrino and the nucleon

$$\frac{d\sigma}{dQ^2} \left( \begin{array}{l} \nu n \rightarrow l^- p \\ \bar{\nu} p \rightarrow l^+ n \end{array} \right) = \frac{M^2 G_F^2 \cos^2 \theta_c}{8\pi E_\nu^2} \left[ A(Q^2) \mp B(Q^2) \frac{(s-u)}{M^2} + C(Q^2) \frac{(s-u)^2}{M^4} \right]$$

$$A(Q^2) = \frac{m^2 + Q^2}{4M^2} \left[ \left( 4 + \frac{Q^2}{M^2} \right) |F_A|^2 - \left( 4 - \frac{Q^2}{M^2} \right) |F_V^1|^2 + \frac{Q^2}{M^2} \left( 1 - \frac{Q^2}{4M^2} \right) |\xi F_V^2|^2 + \frac{4Q^2}{M^2} \text{Re} F_V^{1*} \xi F_V^2 + \mathcal{O} \left( \frac{m^2}{M^2} \right) \right],$$

$$B(Q^2) = \frac{Q^2}{M^2} \text{Re} F_A^* (F_V^1 + \xi F_V^2),$$

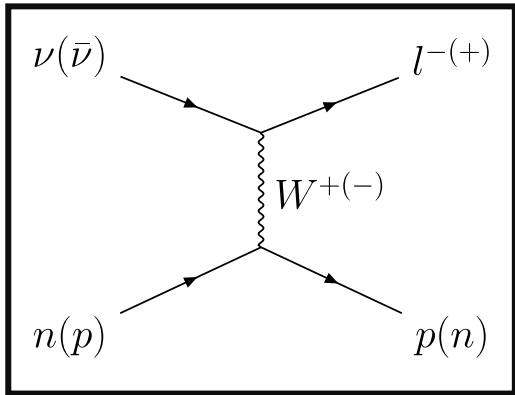
$$C(Q^2) = \frac{1}{4} \left( |F_A|^2 + |F_V^1|^2 + \frac{Q^2}{4M^2} |\xi F_V^2|^2 \right)$$



$F_V^1$ ,  $\xi F_V^2$ : Electric and magnetic form factors. Measured with **electron scattering experiment**: A lot of data and well constrained!

$F_A$ : Axial form factor, depends on the **weak interaction**. Accessible through **neutrino scattering experiments**: Much less data from scattering.

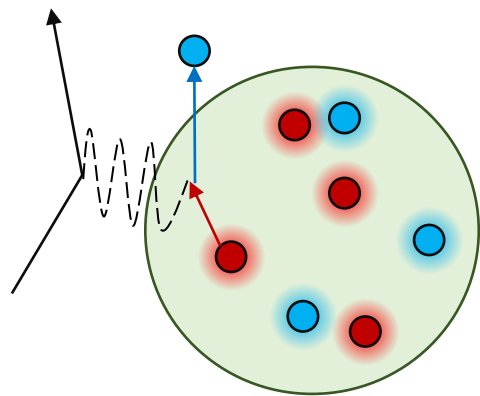
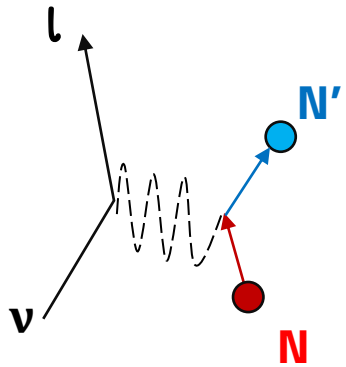
# Why “free nucleons”?



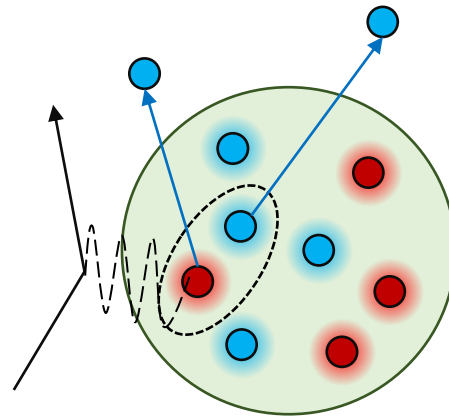
## Best case scenario:

- Neutrino scattering on a free nucleon
- Charged Current interaction with charged lepton and nucleon in final state
- Energy & Momentum conservation: Final state measurement

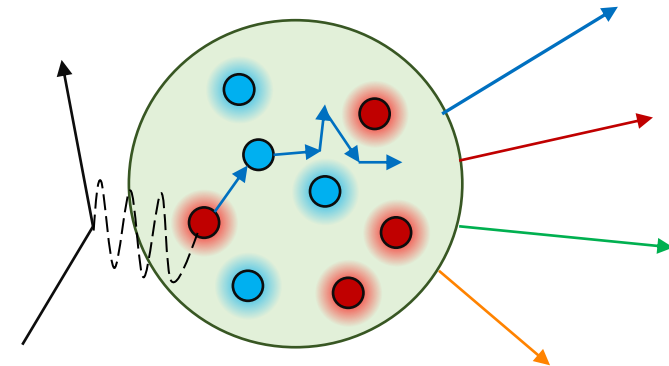
**BUT**



Fermi motion



Short range correlation



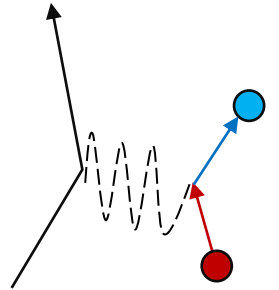
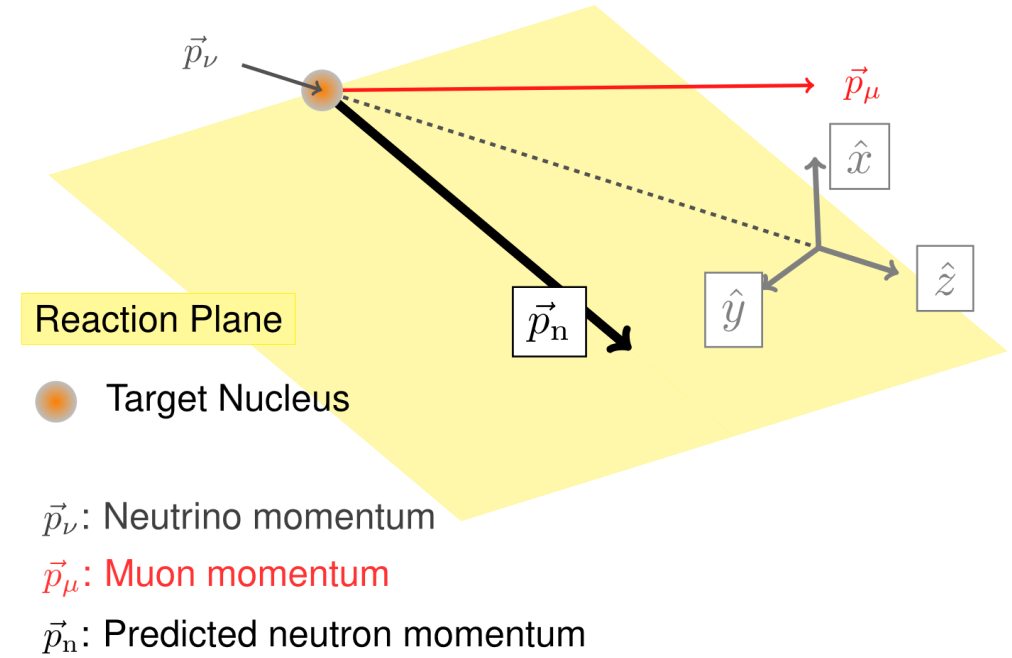
Final state interactions

# Outgoing neutron in antineutrino scattering



## On antineutrino a scattering on H:

- Simple process
- Position neutron direction known from muon measurement



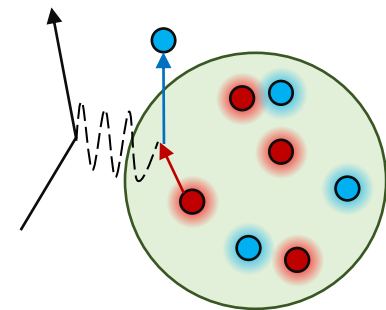
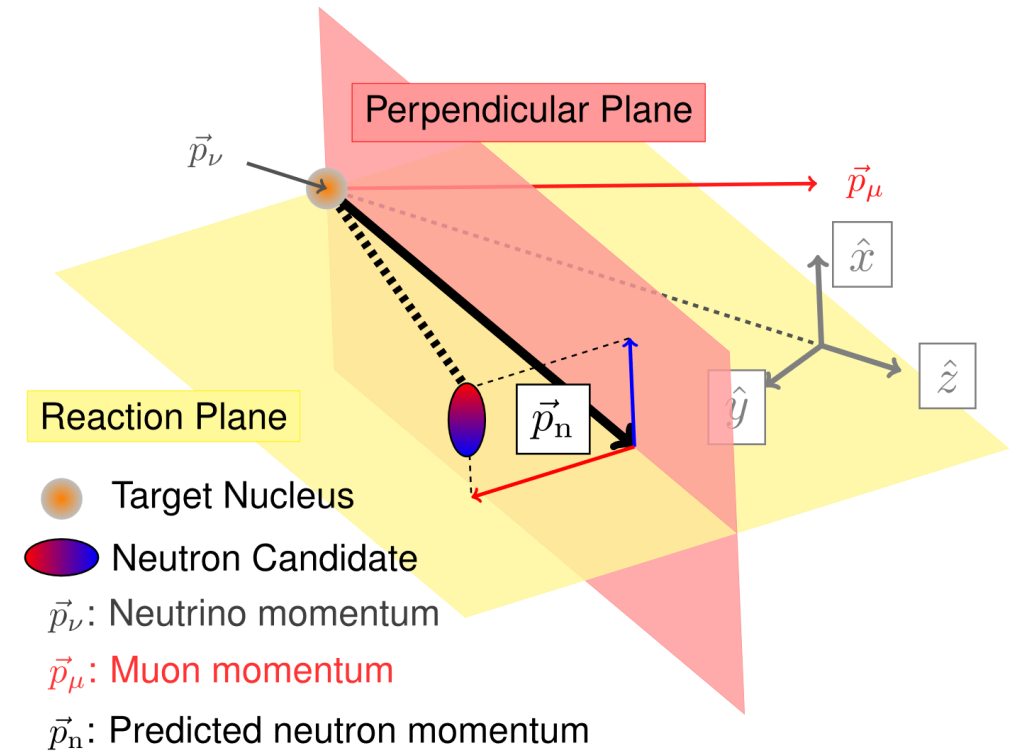
# Outgoing neutron in antineutrino scattering

## On antineutrino a scattering on H:

- Simple process
- Position neutron direction known from muon measurement

## On a scattering on $Z > 1$ :

- Initial nucleon momentum
- Final state interaction
- Position of neutron direction deviates from prediction!



# Outgoing neutron in antineutrino scattering

## On antineutrino a scattering on H:

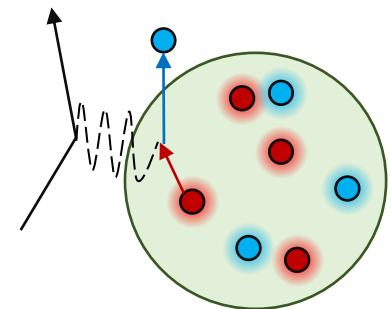
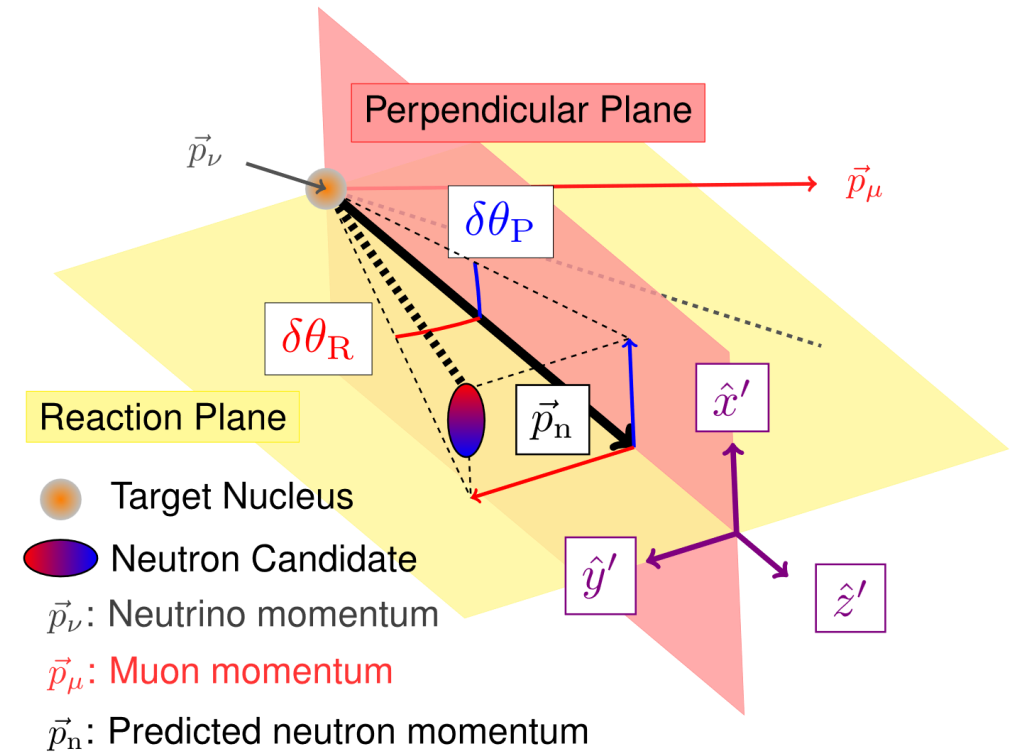
- Simple process
- Position neutron direction known from muon measurement

## On a scattering on $Z > 1$ :

- Initial nucleon momentum
- Final state interaction
- Position of neutron direction deviates from prediction!

## Use deviation to separate both interactions:

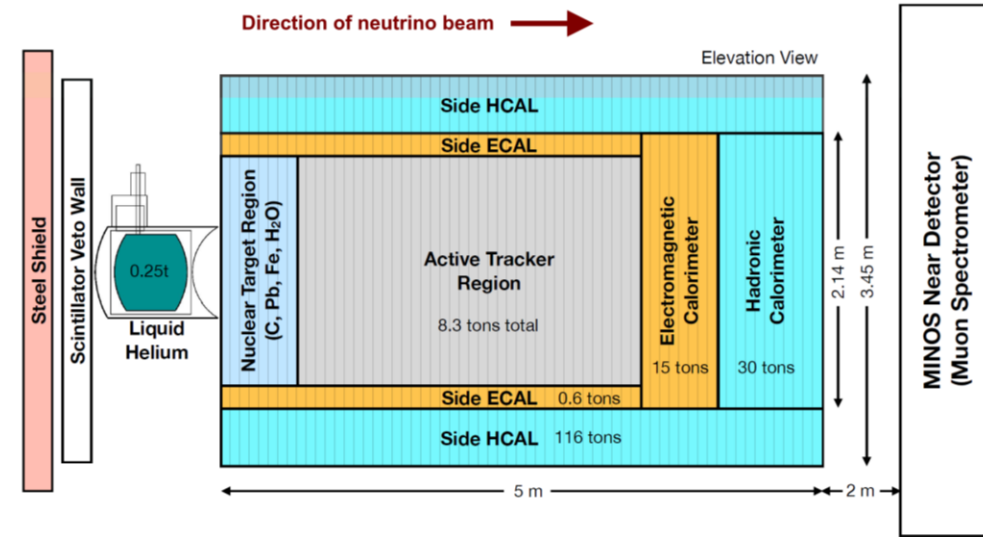
- Define  $\delta\theta_R$  and  $\delta\theta_P$  as the deviation between the predicted position and the measured position



# Detecting a neutron with the MINERvA detector



- $\mu^{+}$  leaves a track in the detector and is used to identify the vertex position
- n interacts knocking off a proton to leave an "isolated energy deposit".



## Event selection:

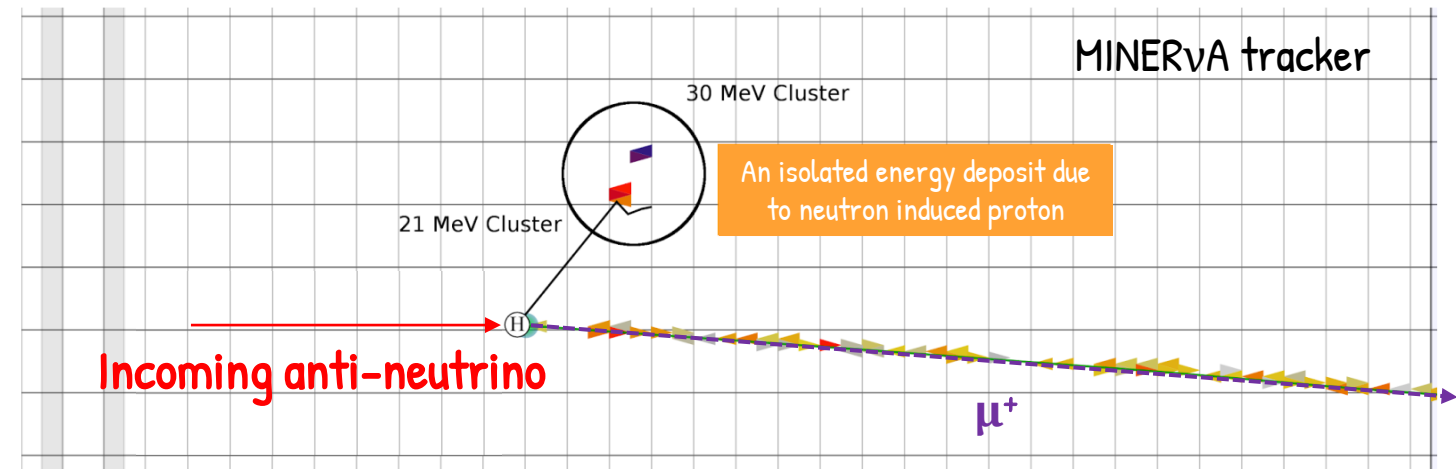
- No Hadronic tracks (charged mesons or pions)

## Neutron candidate:

- 10 cm away from the muon axis

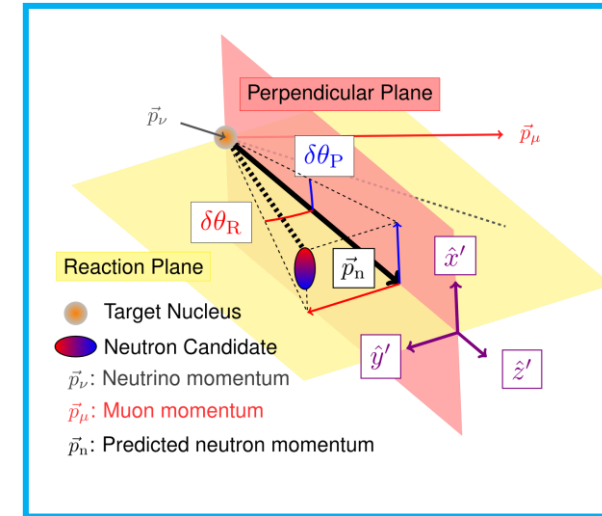
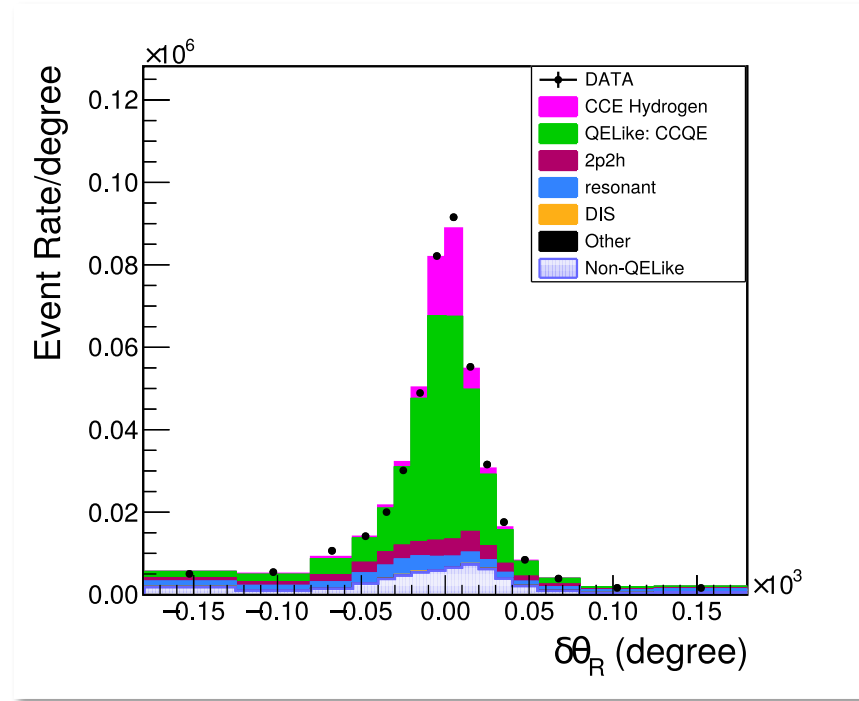
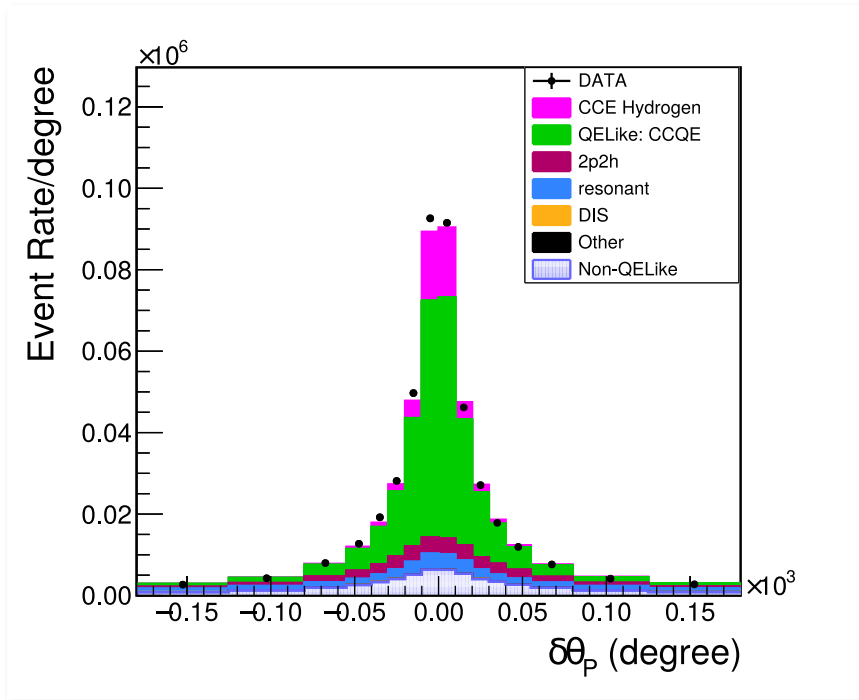
## Muon candidate:

- Muon energy [1.5; 20] GeV
- $\theta_{\mu} < 20^{\circ}$  wrt the neutrino beam





# Deviation angles measurement



Data and Monte-Carlo distribution of the deviation angles

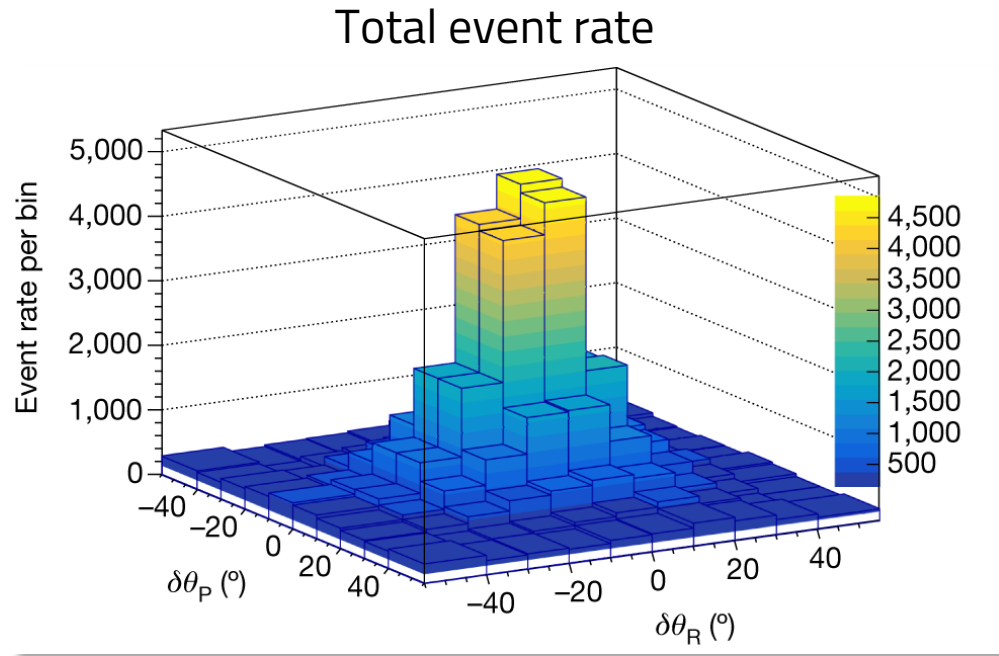
**Elastic scattering on H** centered on 0 with little deviation

**Quasi elastic scattering (QE-Like) on Carbon:** Centered on 0 with some smearing

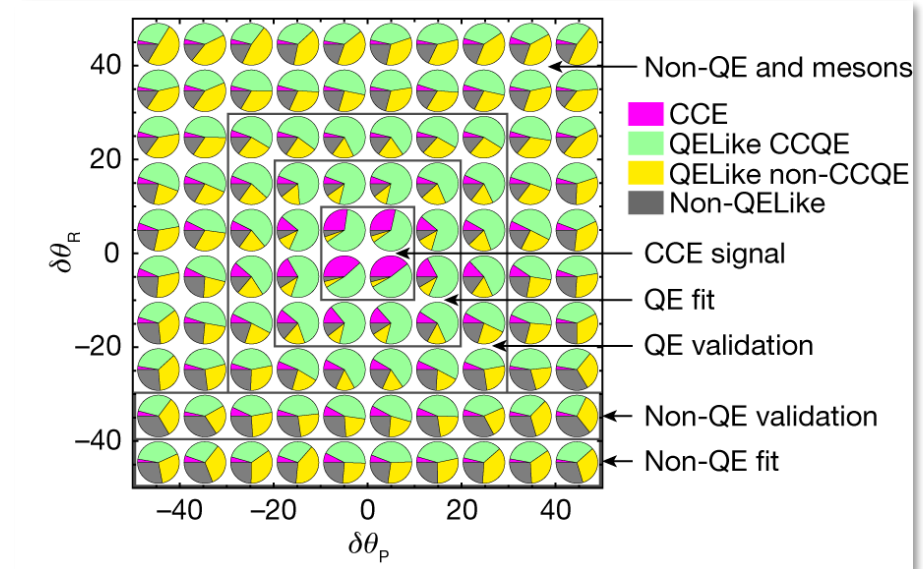
**Other type of background** (not simple scattering)

**Clear difference between H and C scattering but signal/background ratio is not good, need to get smarter !**

# Let's look in 2 dimensions!



## Monte-Carlo Fractions

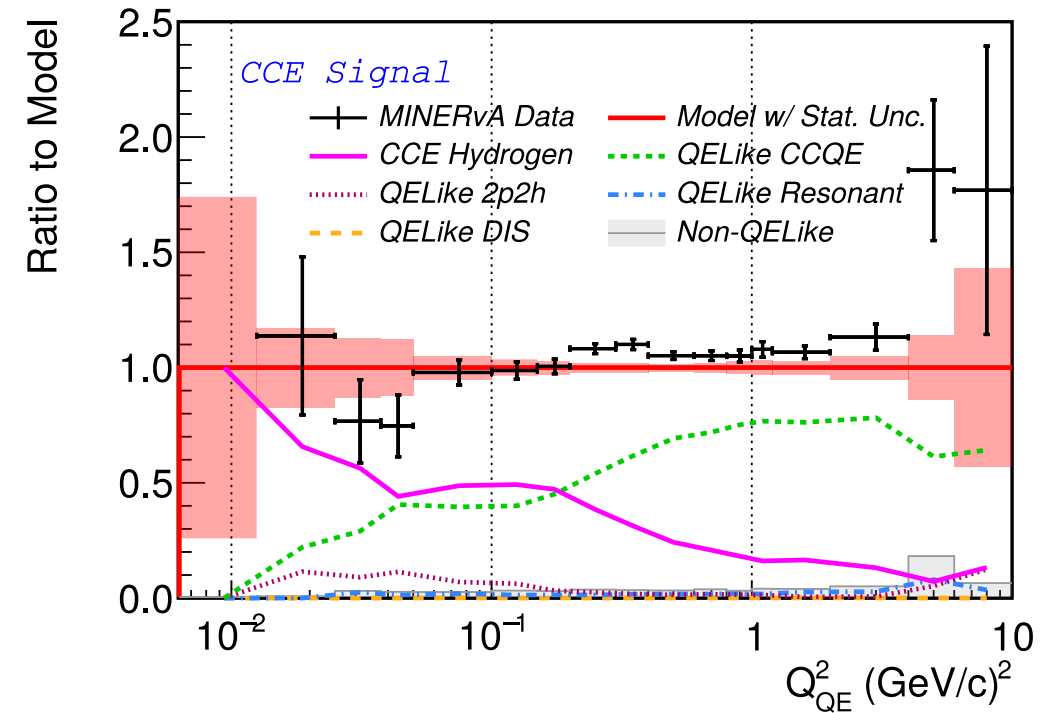
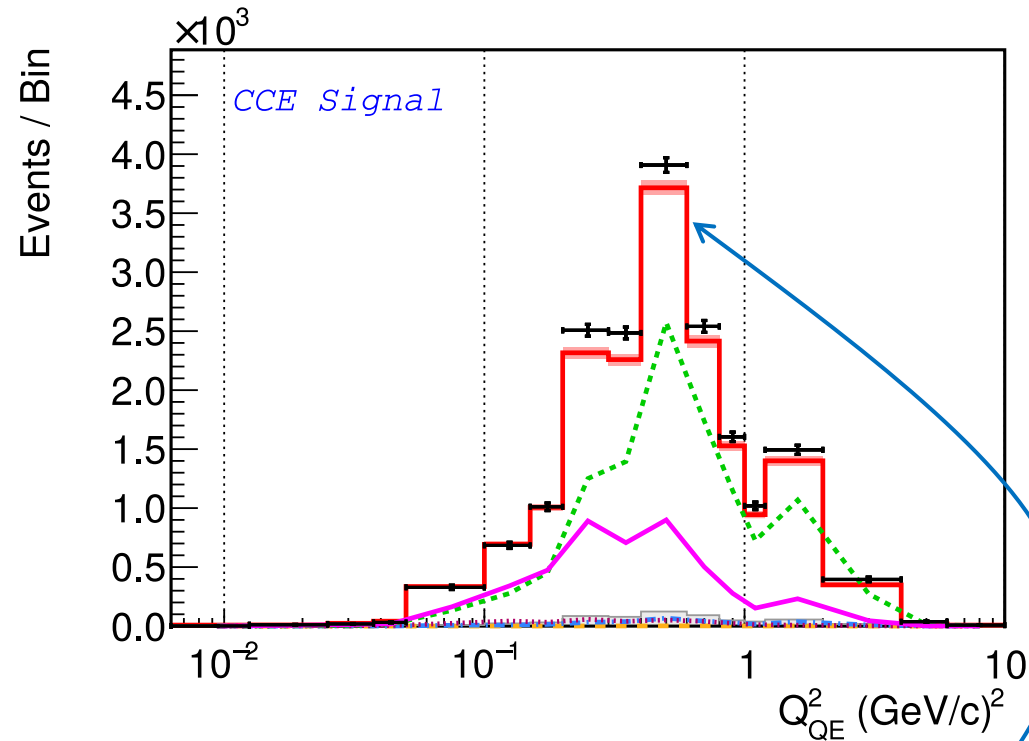


The  $(\delta\theta_P, \delta\theta_R)$  2D space can be used to improve the signal – background ratio!

**Center region used for signal selection**

**Outer regions used for background constraints and fit validation**

# Extracting a cross section

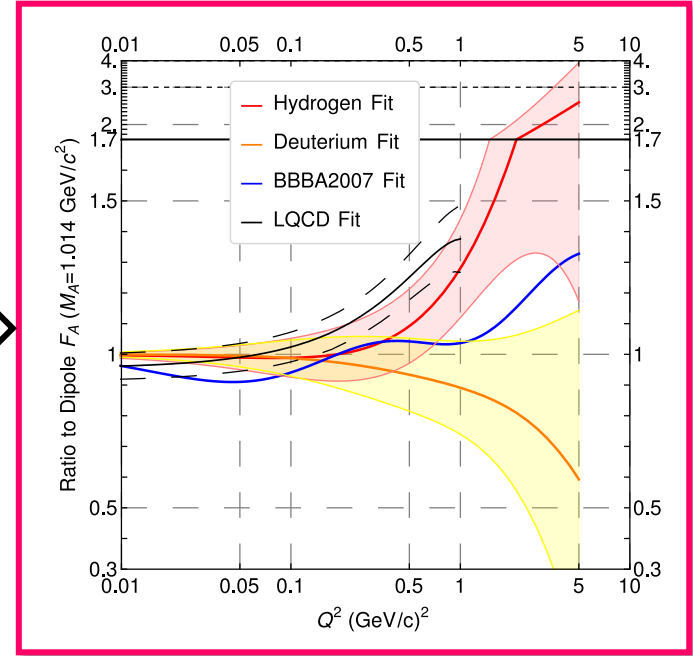
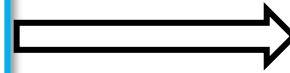
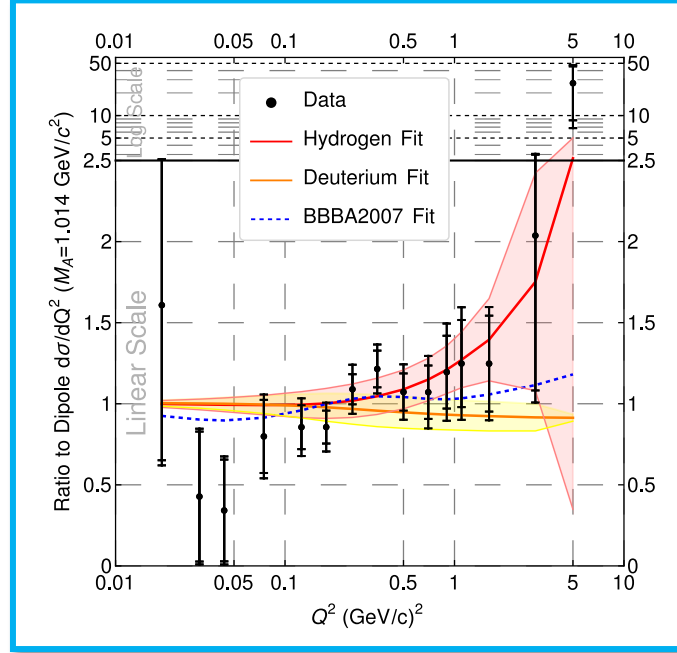
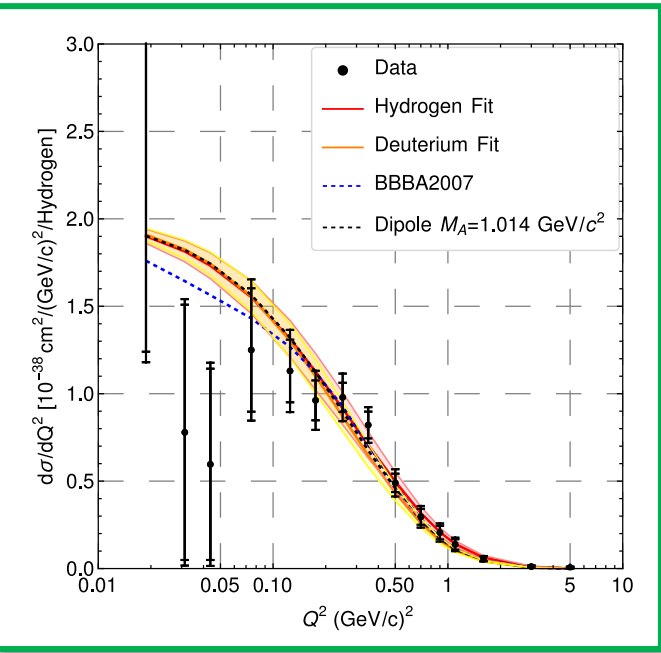


$$\left( \frac{d\sigma}{dQ^2} \right)_i = \frac{\sum_j U_{ji} (N_j^{\text{data}} - N_j^{\text{bkg-pred}})}{\Phi N_H \epsilon_i (\Delta Q^2)_i}$$

## We have everything!

- Unfolding matrix from Data – MC studies
- Efficiency from Data – MC studies
- Flux from models and neutrino-electron scattering measurements
- Number of Hydrogen targets from the detector qualification
- **Measured signal** from data – predicted background

# Cross section and Axial form factor



## Comparison of **our result (Hydrogen fit)** with various models:

**Deuterium Fit<sup>1</sup>**: Deuterium scattering data in Bubble chamber

**BBBA2007<sup>2</sup>**: Deuterium and pion production electroproduction data

Dipole model:  $F_A(Q^2) = F_A(0) \left(1 + \frac{Q^2}{M_A^2}\right)^{-2}$  used in neutrino generators

Our measurement favors higher cross sections for higher  $Q^2$

## From x-section fit of $F_A$ :

**Tension with Deuterium fit**

Deuterium fit had to be tweaked at higher  $Q^2$  due to the lack of statistics

**Agreement with Lattice QCD fit<sup>3</sup> up to 1 GeV**

YORK [1] Phys. Rev. D 93, 113015

[2] Eur. Phys. J. C 53 (2008)

[3] Eur. Phys. J. A 55, 196

# Conclusion



We have performed a **statistically significant** measurement of antineutrino elastic scattering on free proton.

This is the **first  $F_A$  measurement for the last 30 years!** -> [More details in the Nature article<sup>1</sup>](#)

Extracted “proton weak radius”:  $\sqrt{\langle r_A^2 \rangle} = 0.73(17)\text{fm}$

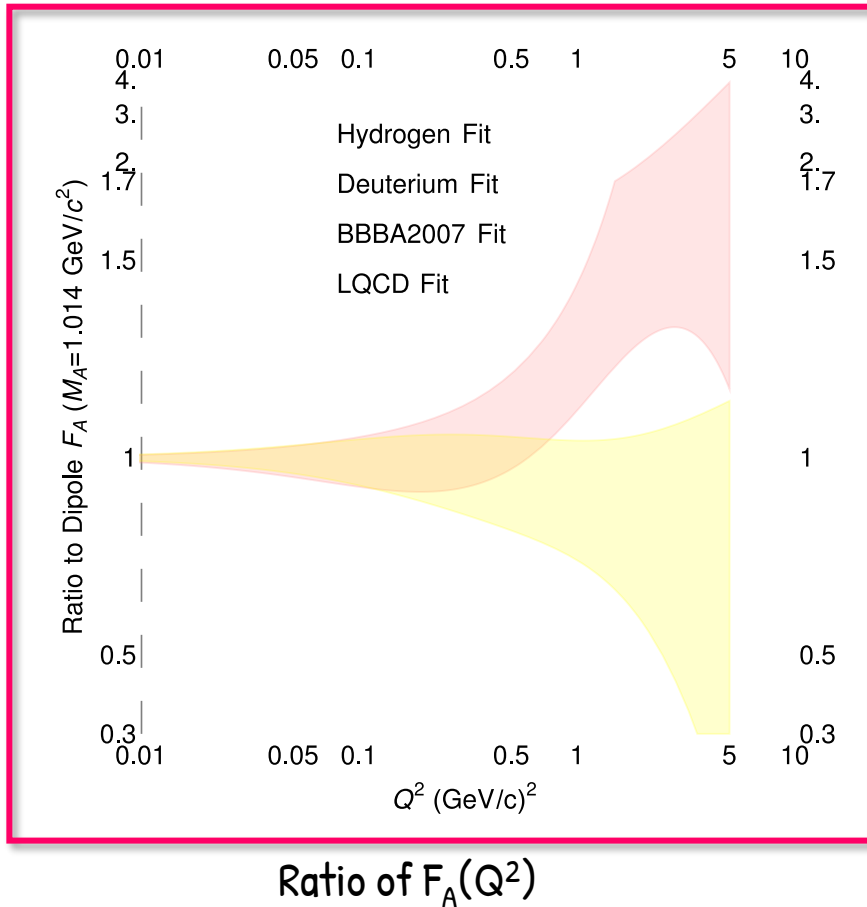
- Developed algorithm that tag neutron candidates and differentiate scattering on H/C in a CH target
- Extracted a  $\bar{\nu}_\mu$ -H CCE cross section in the MINERvA tracker
- Fitted the cross section to export the Axial form factor and compared it with different models
- This measurement will help in better understanding axial vector nucleon structure
- See [Maria's](#) talk next session for more cross-section measurement in MINERvA

YORK **1) Unless indicated otherwise, all the plots were extracted from here**



Backup

# Cross section measurement



Measurement of  $F_A$  for different experiments.

- Lattice QCD fit consistent with our Fitted value up to 1 GeV
- Tension between our fit and deuterium fit.
  - Deuterium fit had to be tweaked at higher  $Q^2$  due to the lack of statistics.
- Measurement of proton radius with the limit at 0 of  $F_A(Q^2)$

$$-\left. \frac{1}{F_A(0)} \frac{dF_A}{dQ^2} \right|_{Q^2=0} = -\frac{1}{6} \langle r_A^2 \rangle$$

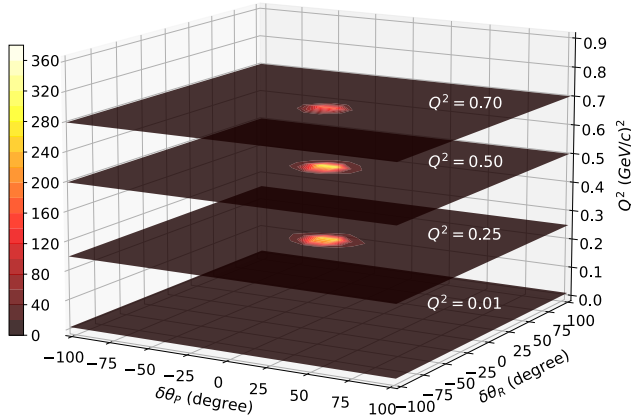
$$-\sqrt{\langle r_A^2 \rangle} = 0.73(17)\text{fm}$$

**We measured the « proton radius » by throwing anti-neutrino at H atoms without nuclear correction or other theoretical assumption!**

# $(\delta\theta_P, \delta\theta_R)$ distributions - sidebands

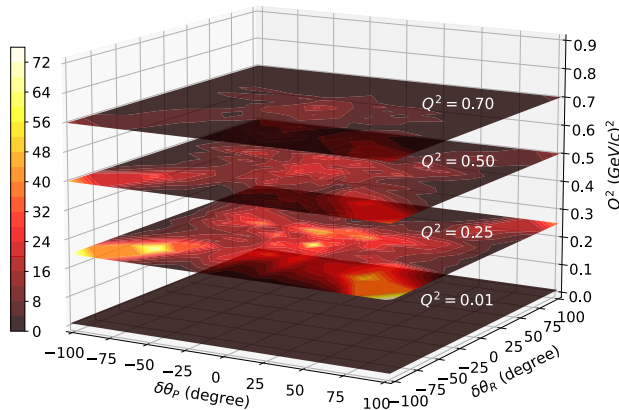


CCE Event Rate



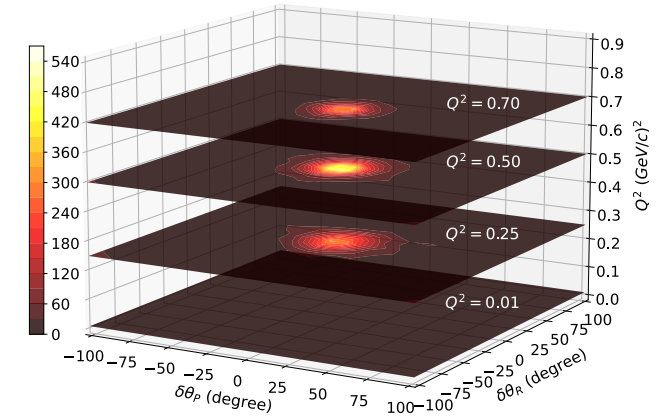
**SIGNAL: Elastic on H**

QELike 2p2h Event Rate



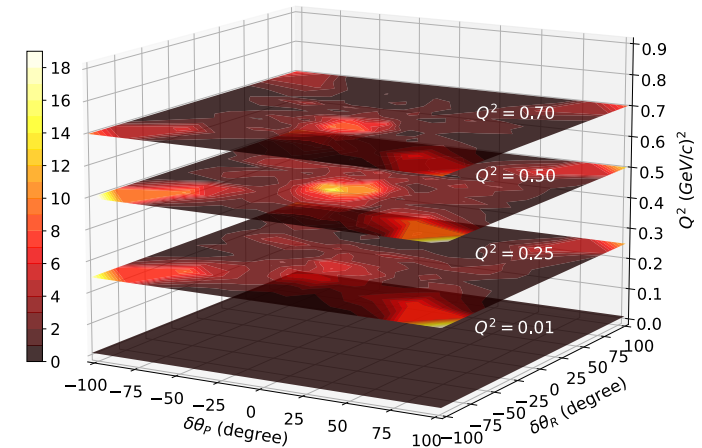
**Background: QELike 2p2h**

CCQE Event Rate

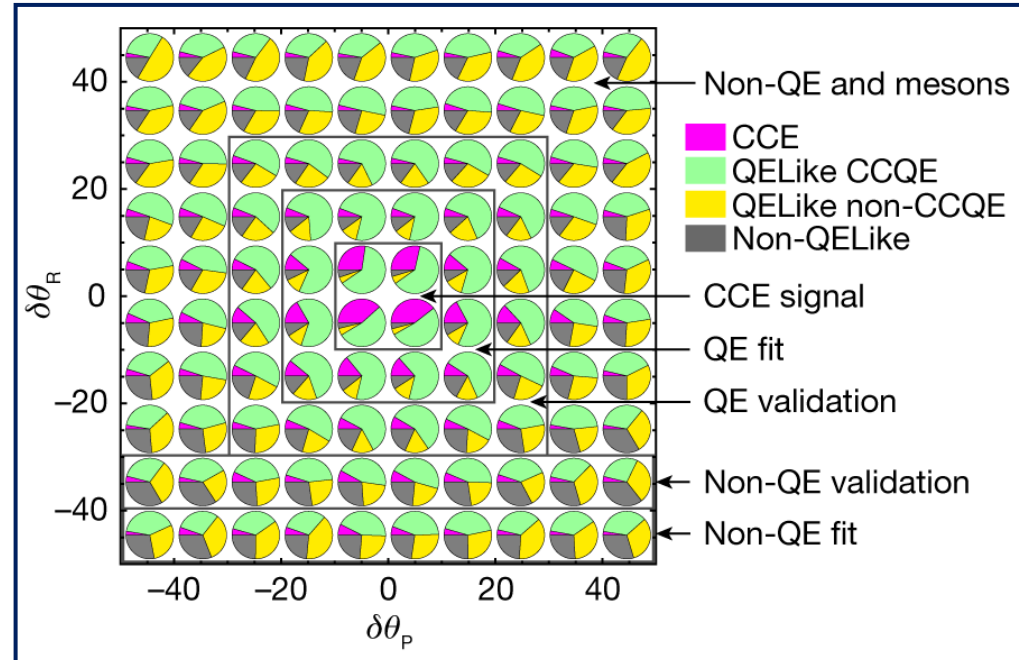


**Background: QELike CCQE (on C)**

QELike Resonant Event Rate



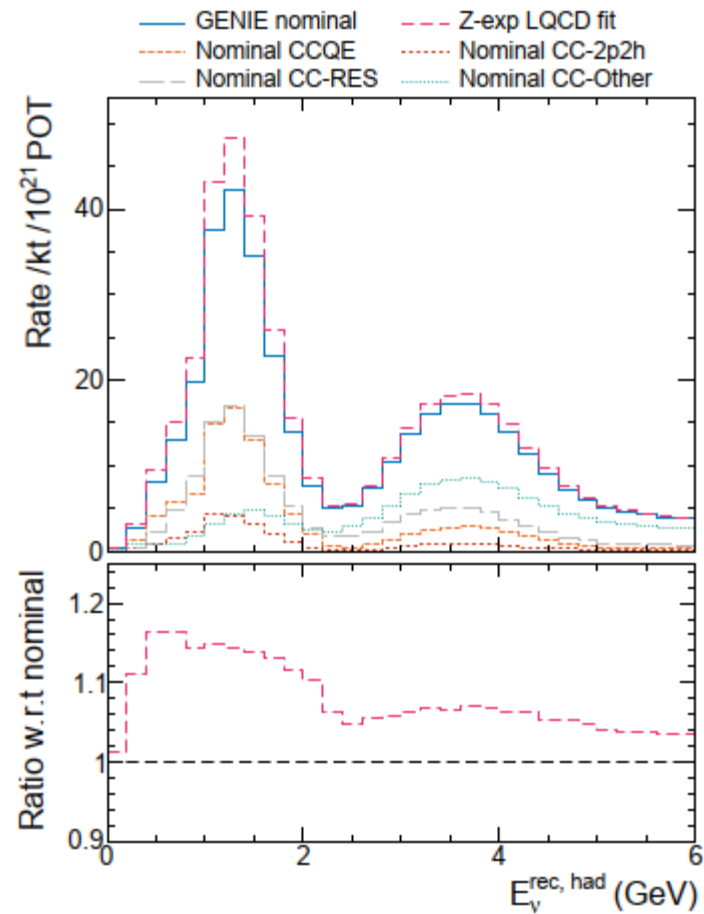
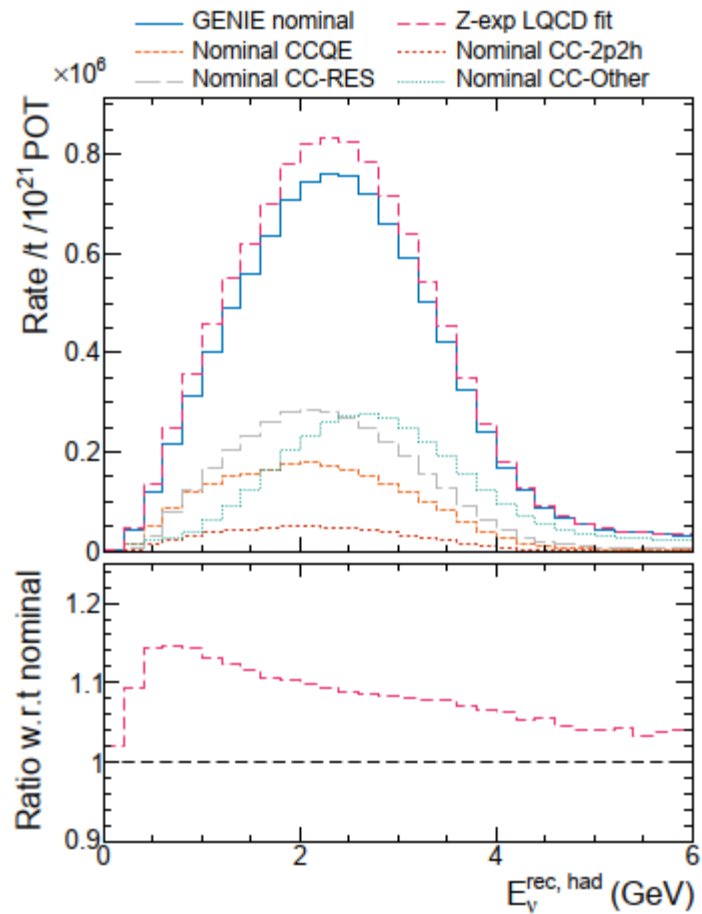
**Background: QELike Resonant**



**Regions of the 2D angular distribution used to fit the backgrounds proportion in the signal region.**

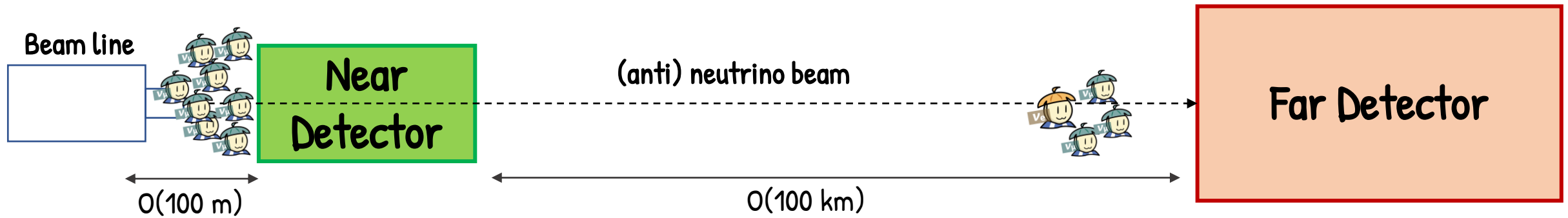


# Effect on DUNE data (?)



[Meyer et. al](#)

# Oscillation studies in long baseline neutrino experiments



$$N_{\mu}(E_{\nu}) = P(\nu_{\mu} \rightarrow \nu_{\mu}) \Phi_{\nu}(E_{\nu}) \sigma(E_{\nu}) \epsilon(E_{\nu})$$

$P(\nu_{\mu} \rightarrow \nu_{\mu})$ : Oscillation probability carried by the PMNS matrix

$\Phi_{\nu}(E_{\nu})$ : neutrino Flux, constrained by the near detector studies

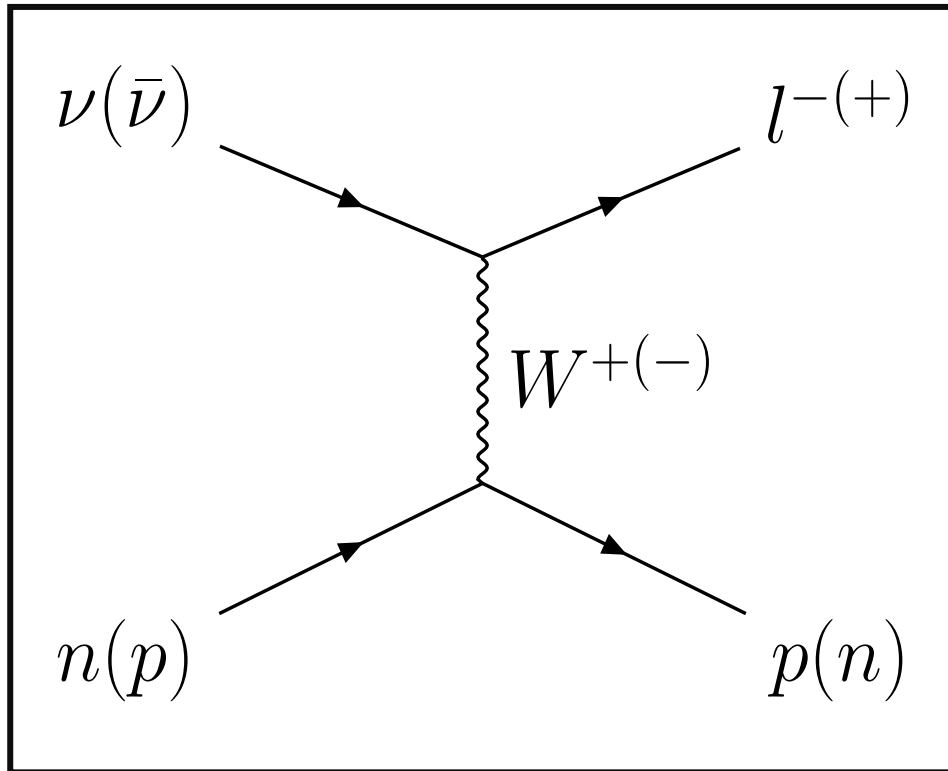
$\sigma(E_{\nu})$ : Neutrino cross section, constrained by near detector studies and neutrino interaction models

$\epsilon(E_{\nu})$ : Detector efficiency, from Data-Monte Carlo studies

# How to understand the neutrino cross sections



Main channel of interaction for (anti) neutrinos: (Quasi) elastic scattering



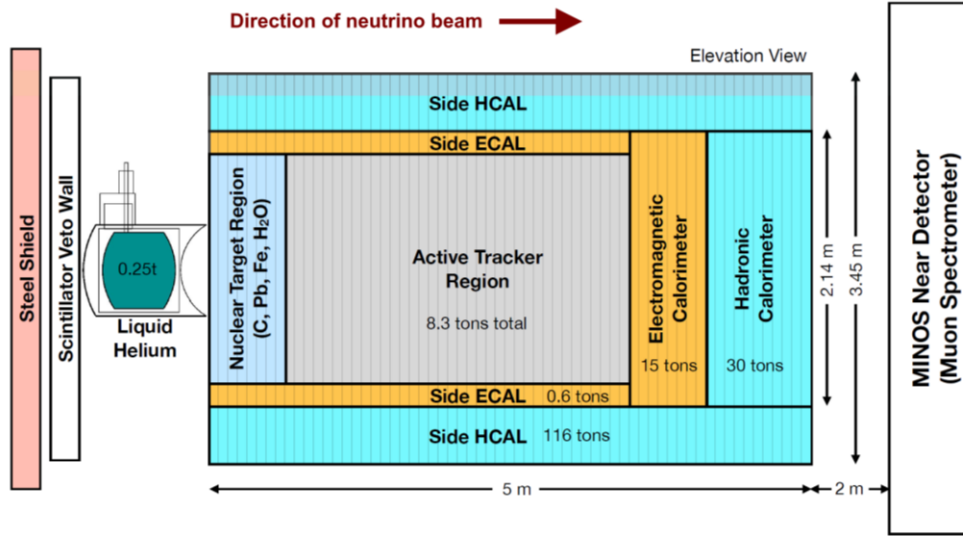
Signal of interest:

Charged lepton emitted in time & space coincidence with a hadron in the detector.

Different type of detector (**plastic scintillators**, **water Cerenkov**, **time projection chambers**...)

**But always the same dominant interaction of interest!**

# The MINERvA experiment

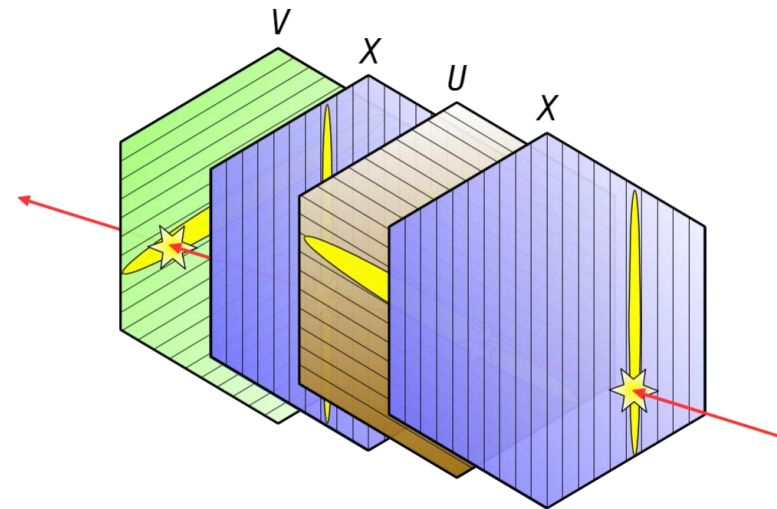
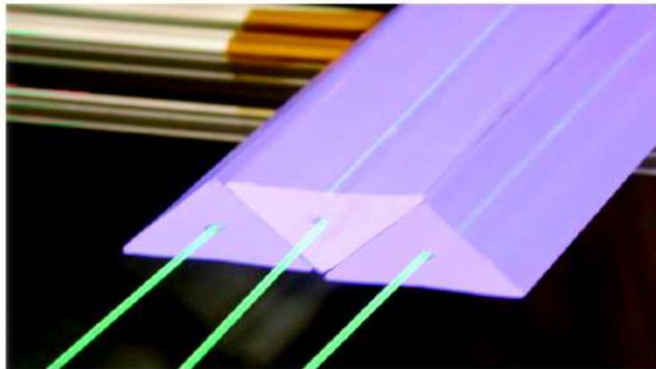


High resolution scintillator detector located at Fermilab in the NuMI beamline

Beamline produces muon (anti) neutrinos that interact in the detector

Detector tracker is composed of hexagonal planes, each constructed from triangular hydrocarbon (CH) strips

The planes are oriented on 3 different directions to be able to get a 3D reconstruction of particles



# Free nucleon cross-section: Llewellyn Smith equations

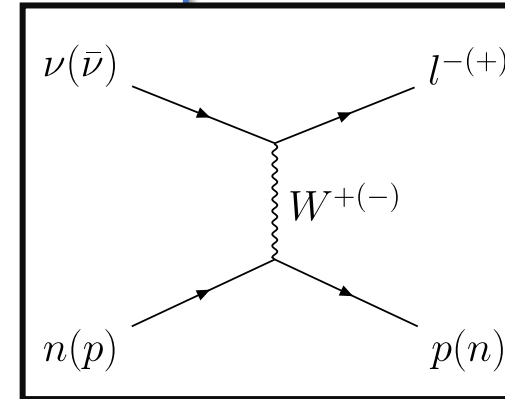


$$\frac{d\sigma}{dQ^2} \begin{pmatrix} \nu n \rightarrow l^- p \\ \bar{\nu} p \rightarrow l^+ n \end{pmatrix} = \frac{M^2 G_F^2 \cos^2 \theta_c}{8\pi E_\nu^2} \left[ A(Q^2) \mp B(Q^2) \frac{(s-u)}{M^2} + C(Q^2) \frac{(s-u)^2}{M^4} \right]$$

$$A(Q^2) = \frac{m^2 + Q^2}{4M^2} \left[ \left( 4 + \frac{Q^2}{M^2} \right) |F_A|^2 - \left( 4 - \frac{Q^2}{M^2} \right) |F_V^1|^2 + \frac{Q^2}{M^2} \left( 1 - \frac{Q^2}{4M^2} \right) |\xi F_V^2|^2 + \frac{4Q^2}{M^2} \text{Re} F_V^{1*} \xi F_V^2 + \mathcal{O} \left( \frac{m^2}{M^2} \right) \right],$$

$$B(Q^2) = \frac{Q^2}{M^2} \text{Re} F_A^* (F_V^1 + \xi F_V^2),$$

$$C(Q^2) = \frac{1}{4} \left( |F_A|^2 + |F_V^1|^2 + \frac{Q^2}{4M^2} |\xi F_V^2|^2 \right)$$



# How to measure the cross section ?



$$\left(\frac{d\sigma}{dQ^2}\right)_i = \frac{\sum_j U_{ji} (N_j^{\text{data}} - N_j^{\text{bkg-pred}})}{\Phi N_H \epsilon_i (\Delta Q^2)_i}$$

$Q^2$ : 4-momentum transfer squared

$\left(\frac{d\sigma}{dQ^2}\right)_i$ : Differential cross section in the  $i^{\text{th}}$   $Q^2$  bin

$\Delta Q^2$ : Width of the  $i^{\text{th}}$  bin

$U_{ij}$ : Unfolding matrix that carries the detector smearing

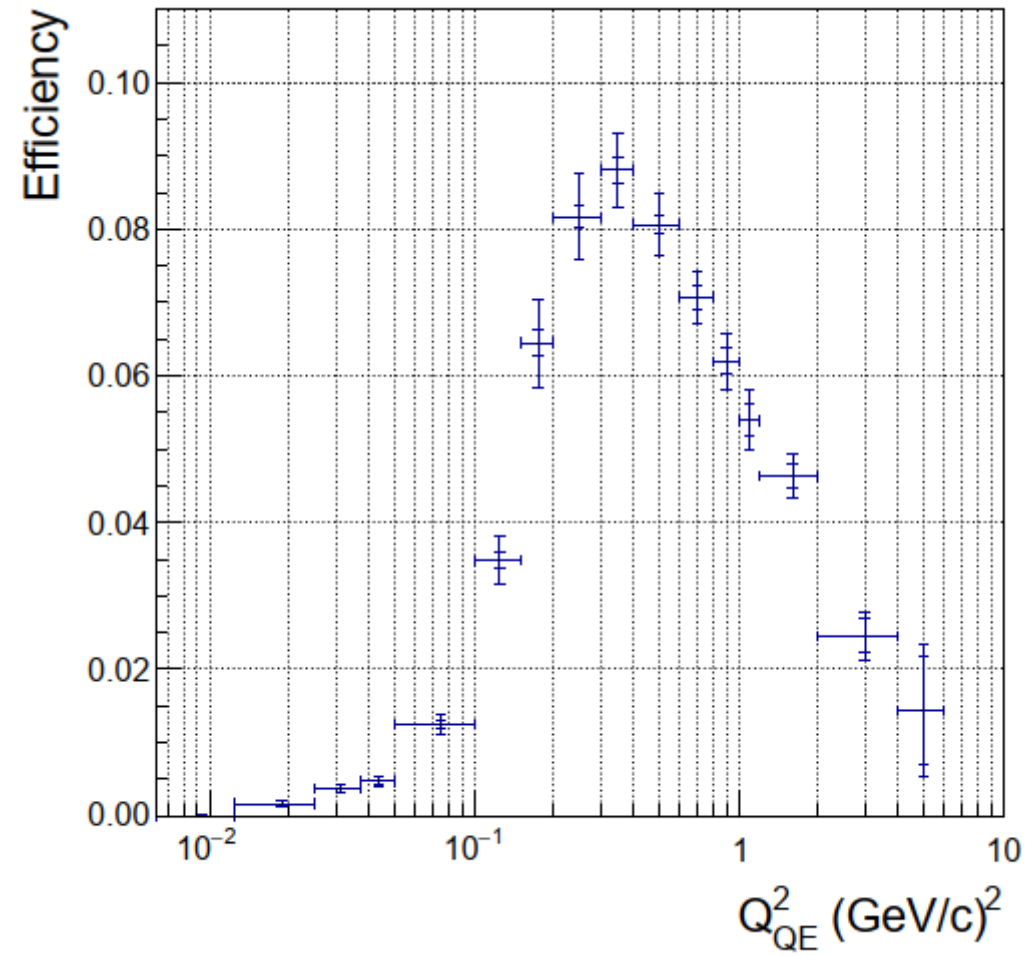
$N_j^{\text{data}}$ : What we measure

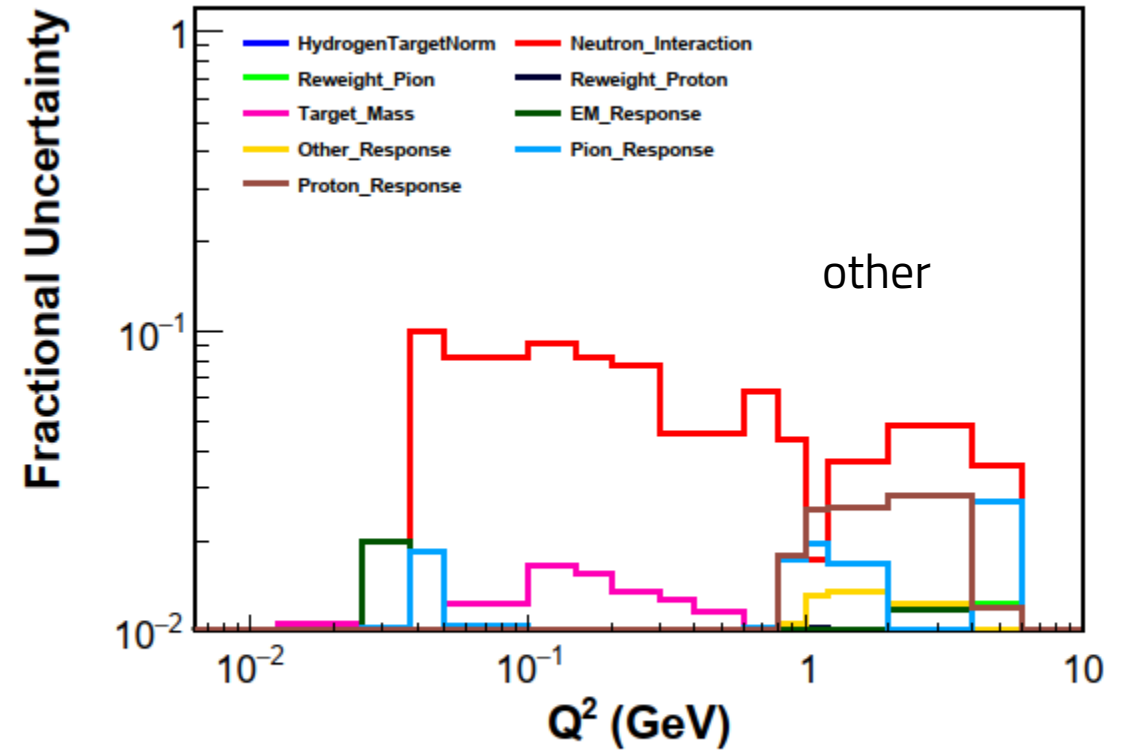
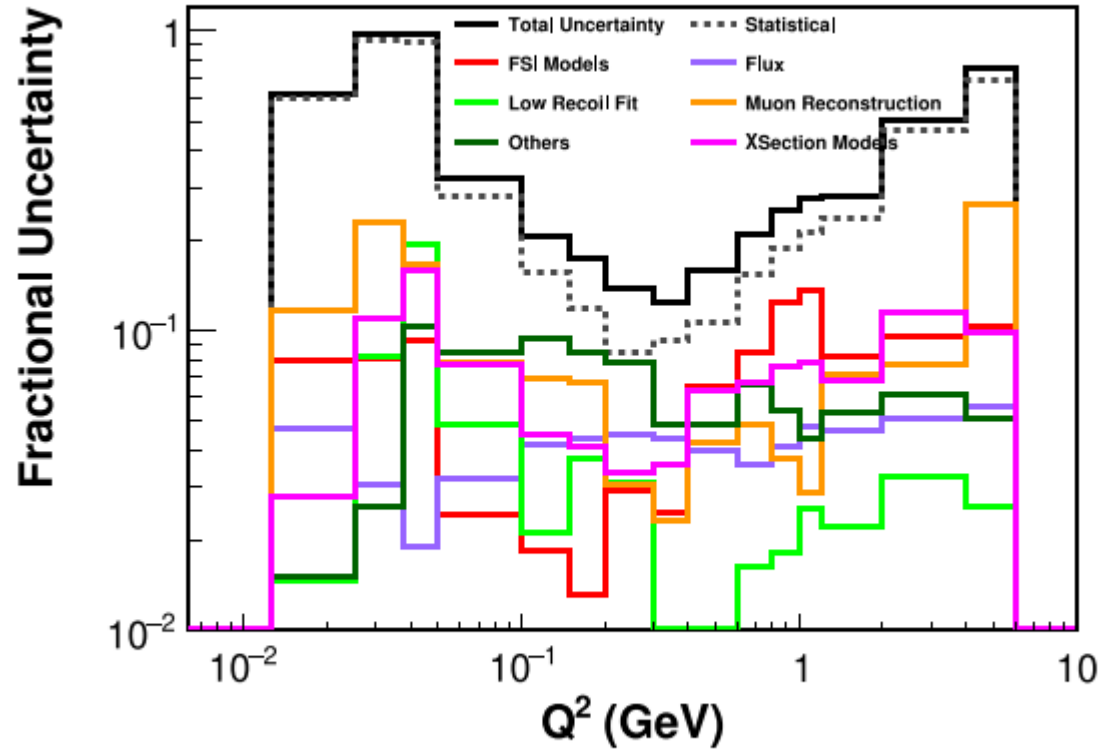
$N_j^{\text{bkg-pred}}$ : Background prediction from models

$\Phi$ : Flux knowledge

$N_H$ : Number of hydrogen targets

$\epsilon_i$ : signal efficiency







## z-expansion formalism and constraints on $a_k$

$$F_A(Q^2) = \sum_{k=0}^{k_{\max}} a_k z^k$$

$$z = \frac{\sqrt{t_{\text{cut}} + Q^2} - \sqrt{t_{\text{cut}} - t_0}}{\sqrt{t_{\text{cut}} + Q^2} + \sqrt{t_{\text{cut}} - t_0}}$$

$$\sum_{k=n}^{\infty} k(k-1) \dots (k-n+1) a_k = 0, \quad n \in (0, 1, 2, 3)$$

$$\chi^2 = \Delta X \cdot \text{cov}^{-1} \cdot \Delta X + \lambda \left[ \sum_{k=1}^5 \left( \frac{a_k}{5a_0} \right)^2 + \sum_{k=5}^{k_{\max}} \left( \frac{ka_k}{25a_0} \right)^2 \right]$$

Central value fit:  $k_{\max} = 8, \lambda = 0.13$