

# High Precision Half-Life Measurements for the Superalloyed Fermi $\beta^+$ Emitter $^{14}\text{O}$



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GRIFFIN

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[egfuakye-resources08](https://github.com/egfuakye-resources08)



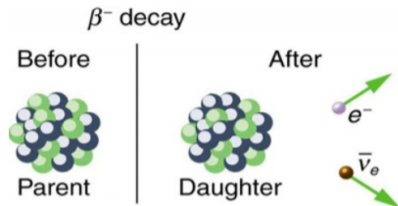
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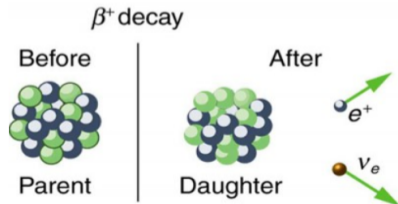
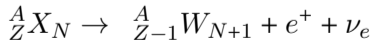
# Nuclear $\beta$ Decay

## Two Types: Beta Minus Decay, Beta Plus Decay

- **Beta Minus Decay:** Conversion of neutron into proton.



- **Beta Plus Decay:** Conversion of a proton into neutron



# Nuclear $\beta$ Decay

- Beta Decay from parent nuclei can populate several daughter states
- Momentum conservation & selection rules:

$$\vec{J}_P = \vec{J}_D + \vec{L} + \vec{S}$$

**Momentum**

$$\pi_P = \pi_D (-1)^L$$

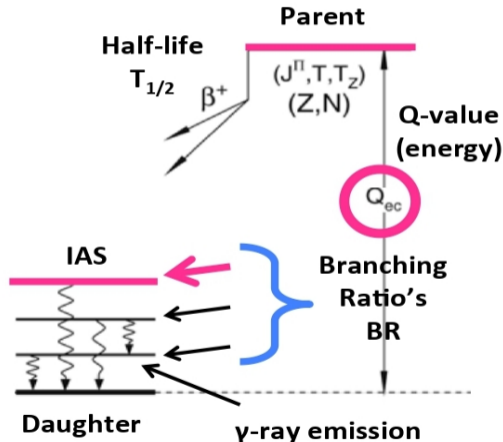
**Parity**

- Allowed decays  $L = 0$
- Forbidden decays  $L = 1, 2, 3, \dots$
- Fermi decays  $S = 0$       &      Gamow-Teller decays  $S = 1$

# Superaligned Fermi Beta Decay

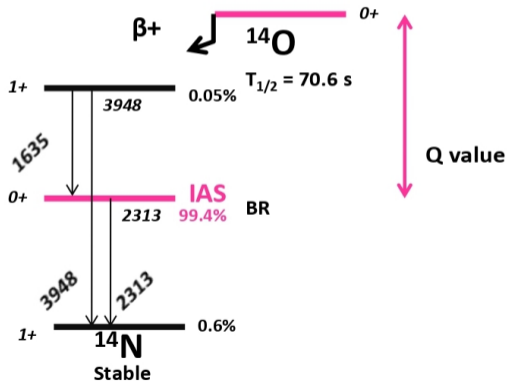
Superaligned Fermi  $\beta$  decays are beta decays between isobaric analogue states.

- $L = 0, \Delta\pi = \text{no}, S = 0$
- Allowed and pure Fermi decay (no GT)
- States have identical wave functions
- Isospin symmetry (neutrons = protons)



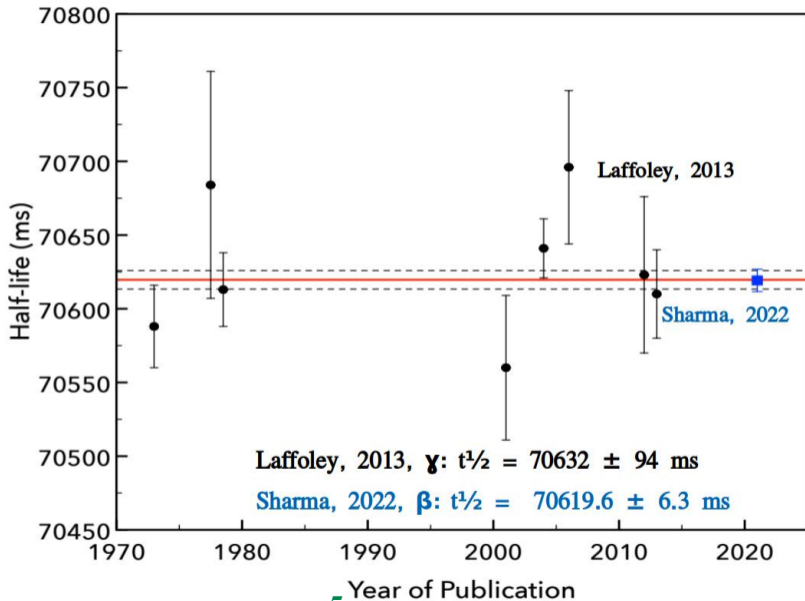
# Key Quantities to be Measured

- 1 Half life  $T_{\frac{1}{2}}$  of the parent state (**focus of this work**).
- 2 Total transition energy Q value
- 3 Branching ratio (BR) to the state of interest



- These quantities are combined into the  $ft$  value of the  $\beta$  transition
- $f$  = statistical rate function, depends on Q value
- $t$  = partial half life, depends on  $T_{\frac{1}{2}}$  and the branching ratio.

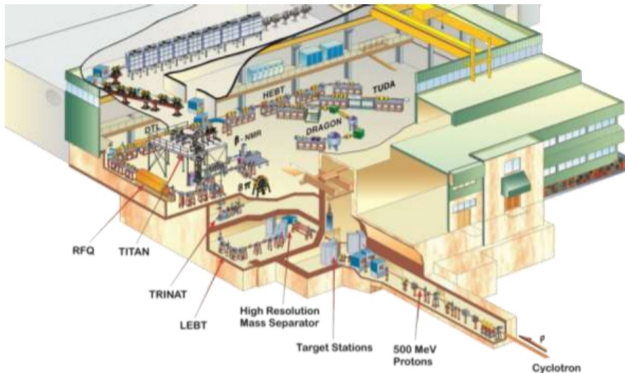
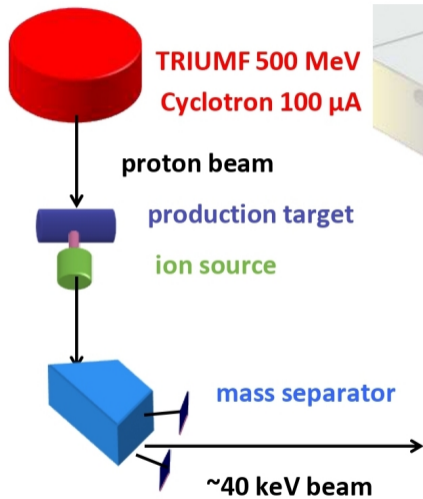
# Previous Half-Life measurements of $^{14}\text{O}$



## Our Goal:

- ① To provide half-life measurement for  $^{14}\text{O}$  from  $\gamma$ -ray counting that can be compared to the recent high precision  $\beta$  counting result (Sharma, 2022).
- ② To search for any possible systematic effects between  $\beta$  and  $\gamma$  counting techniques. (eg.  $^{34}\text{Ar}$  experiment scheduled in June, 2023 at TRIUMF, Vancouver).
- ③ To place further constraints on possible extensions of the Standard Model:  $ft$  value precision  $\leq 0.1\%$   $\rightarrow$   $\beta$  decay half-life precision  $\leq 0.05\%$ .

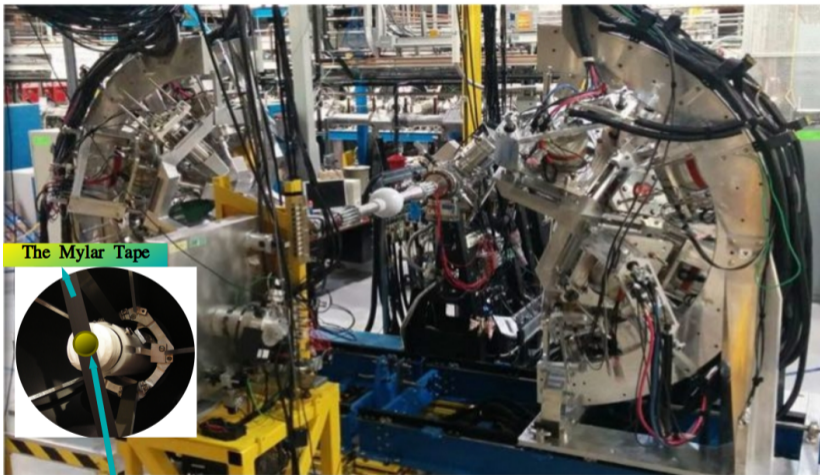
# TRIUMF ISAC (Isotope Separator and Accelerator)



experimental area  
 $^{12}\text{C}^{14}\text{O}$  beam at  $\sim 10^5$  ions/s  
 $^{26}\text{Na}$  at  $\sim 10^5$  ions/s (well-known test case)



## $\gamma$ Counting — The GRIFFIN Spectrometer

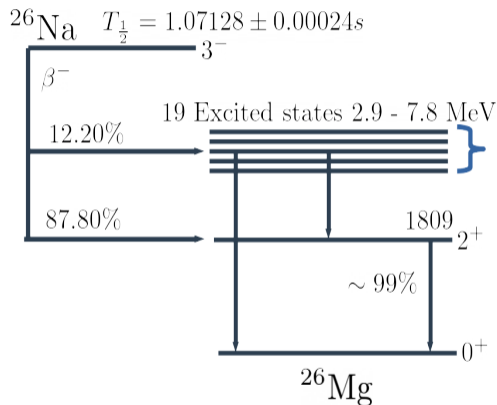


- › The radioactive beam is then implanted into the tape.
- › Spherical array of 16 Clover detectors each consists of 4 HPGe Crystals
- › ~9.1% photopeak efficiency at 1.3 MeV

# Half-Life of $^{26}\text{Na}$

- We performed half-life measurement of  $^{26}\text{Na}$  as a first experimental test of GRIFFIN for high-precision work.
- Developed pile-up fitting and correction techniques in GRIFFIN.
- $\sim 99\%$  of all  $\beta$  decays yield the 1809 keV  $\gamma$ -ray (Grinyer, 2008).

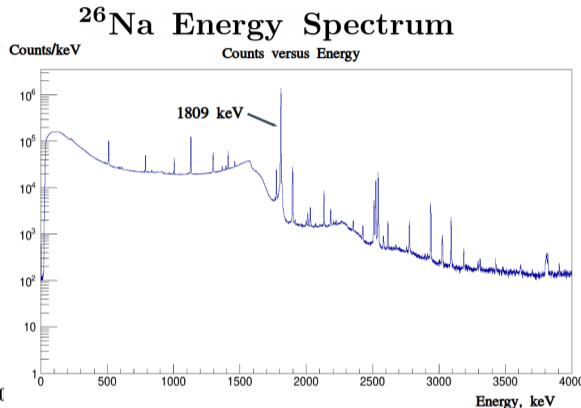
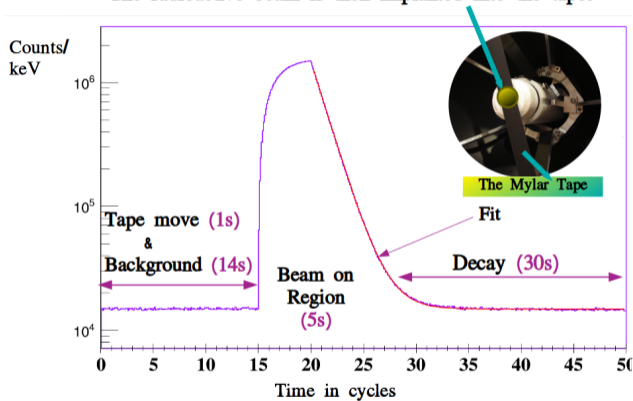
## Decay Scheme of $^{26}\text{Na}$



**Figure 1:** A simplified  $^{26}\text{Na}$   $\beta^-$  decay scheme to the stable daughter  $^{26}\text{Mg}$ .

# Half-Life of $^{26}\text{Na}$

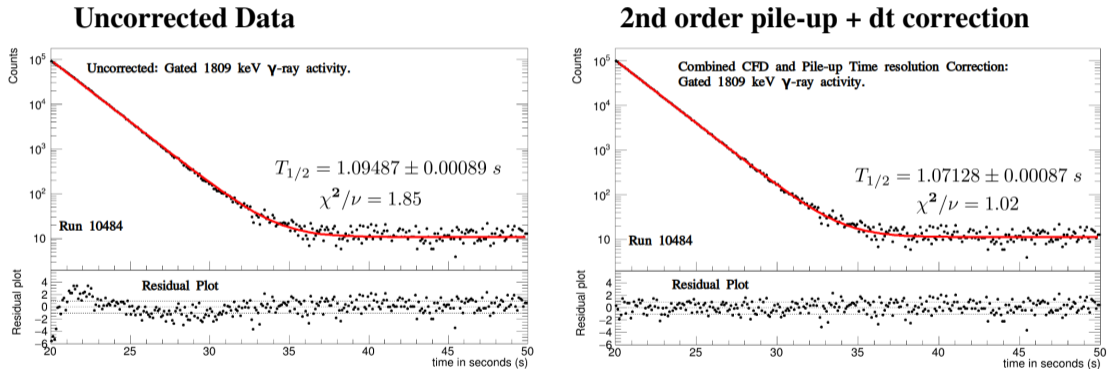
The radioactive beam is then implanted into the tape.



**Figure 2:** Left: Data collected in cycles and Right:  $\gamma$ -ray singles spectrum for  $^{26}\text{Na}$  with all the trigger events for a single run (40 mins)

# Half-Life Analysis

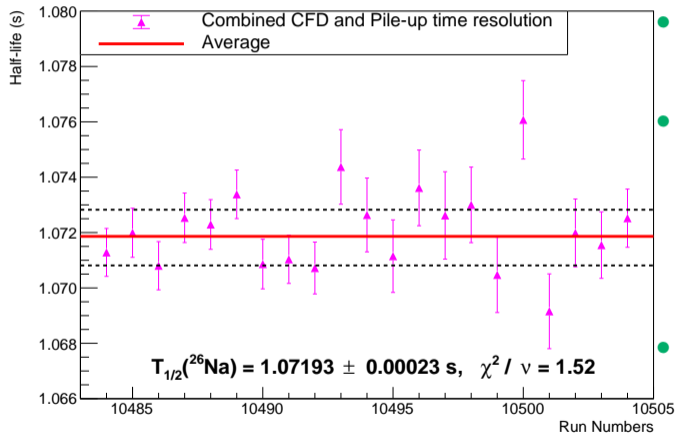
$^{26}\text{Na}$  Gated 1809keV Activity with total decay time of 30s.



**Figure 3:** Non-corrected decay curve (left) and Combined CFD and Pile-up time resolution correction decay curve(right) obtained from a single run following a gate on the 1809-keV transition in  $^{26}\text{Mg}$ .

# Half-Life Analysis: Previous works on $^{26}\text{Na}$

Deduced half-life of  $^{26}\text{Na}$  versus all the run numbers.



- Current Result ( $\gamma$ -counting):  
 $T_{1/2}(^{26}\text{Na}) = 1.07193 \pm 0.00023 \text{ s}$
- Previous Result:  
Grinyer et al. (2005, 2007)  
 $T_{1/2}(^{26}\text{Na}, \beta) = 1.07128 \pm 0.00025 \text{ s}$   
 $T_{1/2}(^{26}\text{Na}, \gamma) = 1.07167 \pm 0.00055 \text{ s}$
- Good agreement with previous high-precision measurements.

# 1D $\gamma$ -ray singles spectrum for $^{14}\text{O}$

Counts/keV

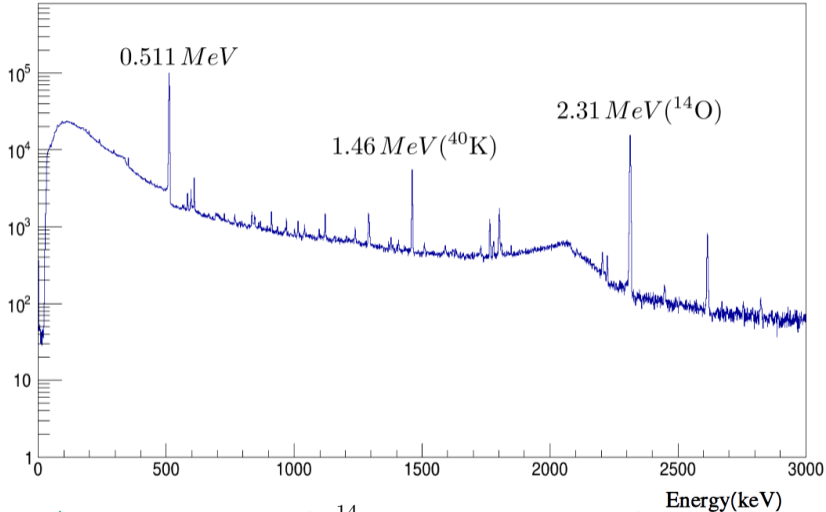


Figure 4:  $\gamma$ -ray singles spectrum for  $^{14}\text{O}$  with all the trigger events for a single run (22 mins).

# Energy gate on the 2.3 MeV photopeak in $^{14}\text{N}$

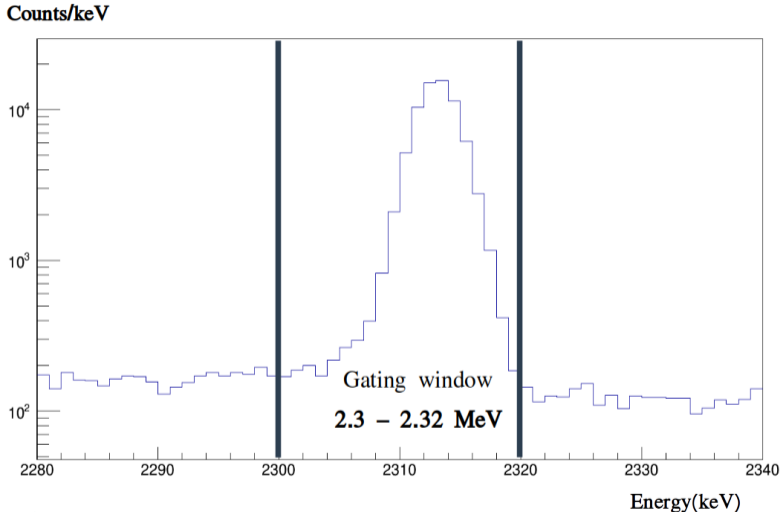


Figure 5: Typical zoomed in region (2280 - 2340 keV) from the  $\gamma$ -ray singles spectrum of  $^{14}\text{O}$ .

# Looking at the Pile Up and Single Events Spectra

Not Pile-up Events (blue) & Pile up Events(Red).

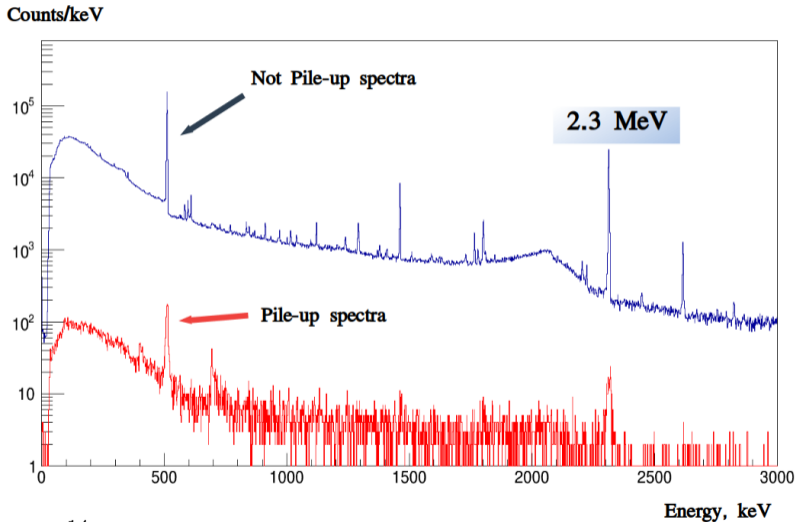


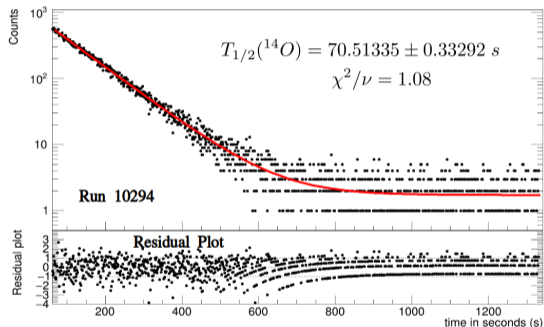
Figure 6:  $^{14}\text{O}$  Energy spectra to distinguish between not pile-up and pile-up events.



# Half-Life Analysis: $^{14}\text{O}$ Gated 2.3MeV Activity

Preliminary Results:  $^{14}\text{O}$  Gated 2.3MeV Activity with total decay time of 1280s.

## Uncorrected Data



## 1st order pile-up + dt correction

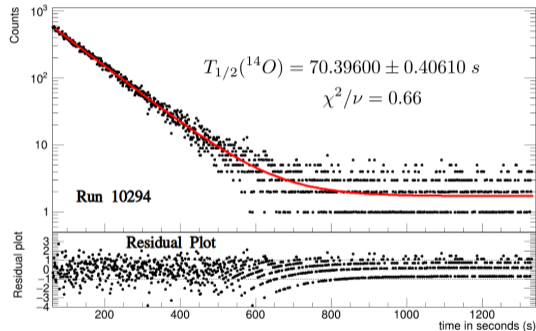


Figure 7: Non-corrected decay curve (left) and 1st order pile-up and dead-time (dt) correction decay curve(right) obtained from a single run following a gate on the 2.3-MeV transition in  $^{14}\text{N}$ .

# Half-Life Analysis: $^{14}\text{O}$ Gated 2.3MeV Activity

Preliminary Results: Half-life of  $^{14}\text{O}$  versus run numbers.

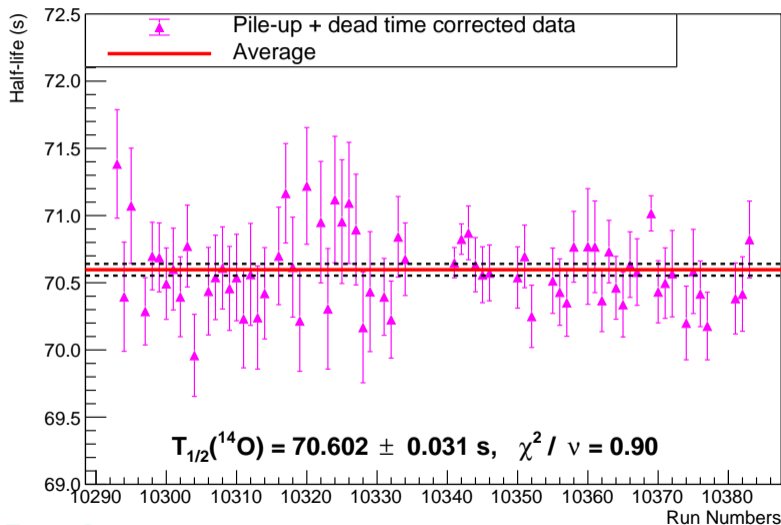


Figure 8: Pile-up and dead time correction of the deduced Half life's versus run numbers.

## Summary and Future Work

- ① We performed a half-life measurement of  $^{26}\text{Na}$  as a first experimental test of GRIFFIN for high-precision work.
- ② The Half life for the 2.3MeV activity from  $^{14}\text{O}$  has been determined and was found to be  $T_{\frac{1}{2}}(\text{avg}) = 70.602 \pm 0.031$  s.
- ③ Sharma et al. (2022) measured the high-precision half-life of  $^{14}\text{O}$  via  $\beta$ -counting. The half-life of  $^{14}\text{O}$  was determined to be  $T_{\frac{1}{2}} = 70.6196 \pm 0.0063$  s.
- ④ At this time, the analysis is in its preliminary stages and further extensive work is required in the upcoming weeks.
- ⑤ Future Work: Studies of  $^{34}\text{Ar}$  as a superallowed Fermi  $\beta$  decay experiment scheduled in June, 2023 at TRIUMF, Vancouver.

# Collaborators & References

## COLLABORATORS

Thank you very much for your support !

S. Sharma<sup>1</sup>, G.F. Grinyer<sup>1a</sup>, G.C. Ball<sup>2</sup>, J.R. Leslie<sup>3</sup>, C.E. Svensson<sup>4</sup>, F.A. Ali<sup>4b</sup>, C. Andreoiu<sup>5</sup>, N. Bernier<sup>2,6c</sup>, S.S. Bhattacharjee<sup>2</sup>, V. Bildstein<sup>4</sup>, C. Burbadge<sup>4</sup>, R. Caballero-Folch<sup>2</sup>, R. Coleman<sup>4</sup>, A. Diaz Varela<sup>4</sup>, M.R. Dunlop<sup>4</sup>, R. Dunlop<sup>4</sup>, A.B. Garnsworthy<sup>2</sup>, E. Gyabeng Fuakye<sup>1</sup>, G.M. Huber<sup>1</sup>, B. Jigmeddorj<sup>4</sup>, K. Kapoor<sup>1</sup>, A.T. Laffoley<sup>4</sup>, K.G. Leach<sup>7</sup>, J. Long<sup>8</sup>, A.D. MacLean<sup>4</sup>, C.R. Natzke<sup>2,7</sup>, B. Olaizola<sup>2d</sup>, A.J. Radich<sup>4</sup>, N. Saei<sup>1</sup>, J.T. Smallcombe<sup>2e</sup>, A. Talebitaher<sup>1</sup>, K. Whitmore<sup>5</sup>, and T. Zidar<sup>4</sup>

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<sup>8</sup> Department of Physics, University of Notre Dame, Notre Dame, IN 46556, USA

- 1 Grinyer, G. (2008). High-precision half-life measurements for superallowed Fermi  $\beta$  decays (Doctoral dissertation).
- 2 Sharma, S., Grinyer, G. F., Ball, G. C., Leslie, J. R., Svensson, C. E., Ali, F. A., ... & Zidar, T. (2022). High-precision half-life determination of  $^{14}\text{O}$  via direct  $\beta$  counting. *The European Physical Journal A*, 58(5), 83.
- 3 Laffoley, A. T., Svensson, C. E., Andreoiu, C., Austin, R. A. E., Ball, G. C., Blank, B., ...& Unsworth, C. (2013). High-precision half-life measurements for the superallowed Fermi  $\beta^+$  emitter  $^{14}\text{O}$ . *Physical Review C*, 88(1), 015501.
- 4 Grinyer, G. F., Svensson, C. E., Andreoiu, C., Andreyev, A. N., Austin, R. A. E., Ball, G. C., ... & Zganjar, E. F. (2007). Pile-up corrections for high-precision superallowed  $\beta$  decay half-life measurements via  $\gamma$ -ray photopeak counting. .



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GRIFFIN

A.B. Garnsworthy et al.,

# Regina GRIFFIN Group

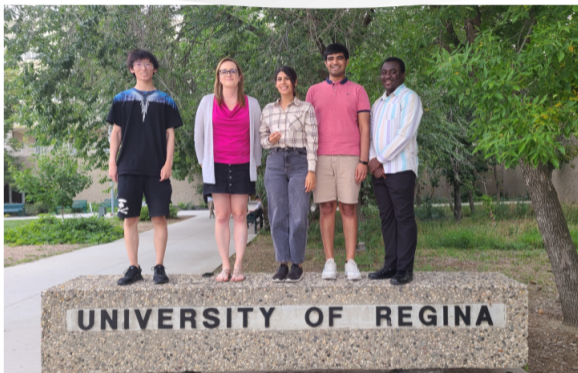


PHOTO CREDIT: SHAFAKAT ARIFEEEN

L to R: J. Liu, Dr. Grinyer, N. Saei, D. Shah, E. Gyabeng Fuakye (me!)



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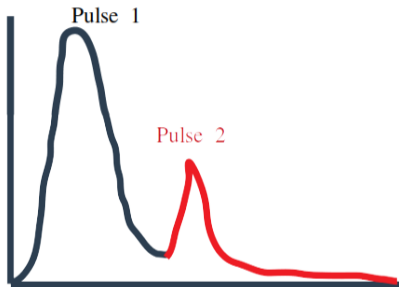
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**Any Questions ?**

# Backup Slides

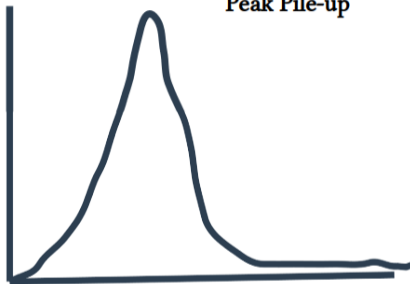
# Detector Pulse pile-up

## Tail Pile-up



First order pulse pile-up where **pulse 2** is riding on the tail of pulse 1.

## Peak Pile-up



If the pulses **are very close in time**, the system will simply record the two pulses as a single event with a **combined pulse amplitude**.

- The number of pile-up events depend strongly on the count rate of the system.

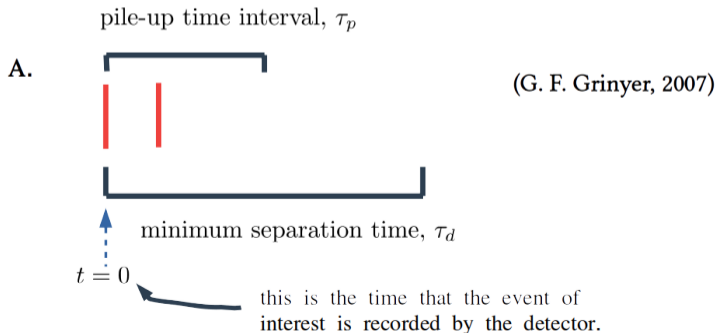


# Detector Pulse pile-up

## Common types of Pile-up

### Post-piled-up

- Post pile-up is defined as the probability that the pile-up is caused by events arriving after the events of interest has been recorded.

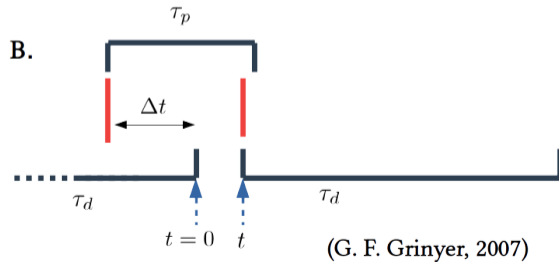


# Detector Pulse pile-up

## Common Types of Pile-up

### II. Pre-piled-up

- The possibility that the event of interest is piled-up by an event that came before, in a process defined as “pre-pile-up”



# 1st Order Pile-up Corrections

## Step-by-Step Correction

### 1. Deadfraction Correction

$$N_i' = \frac{N_i}{1 - D_i}$$

$D_i =$  Dead fraction

Deadtime is the total period of time during which hit detection cannot be processed even if they are present.

### 2. 1<sup>st</sup> Order Pile-up Correction

$$N_i'' = \frac{N_i'}{1 - P_i}$$

$P_i = \frac{\text{Pile-up Events}}{\text{All Events}}$

$$N_i'' = \frac{N_i}{(1 - D_i) \times (1 - P_i)}$$

★ RATE DEPENDENT CORRECTIONS

# Higher Order Pile-up Corrections

## Bin-by-bin pile-up correction

### 1. Deadfraction Correction

$D_i =$  Dead fraction

$$N'_i = \frac{N_i}{1 - D_i}$$

Deadtime is the total period of time during which hit detection cannot be processed even if they are present.

### 2. Higher Order Pile-up Corrections

RATE DEPENDENT  
CORRECTIONS

$$N''_i = \frac{N_i}{(1 - D_i) \times (1 - P_{\text{fit-total}})}$$



# Higher Order Pile-up Corrections

## Analytical Expressions by (G. F. Grinyer, 2007)

$$P = 1 - e^{-(2-a_4)x} [e^{a_4x} + (1 - a_4)x] \quad 1$$

$$P = 1 - e^{-2x}(1 + \alpha x) \quad 2$$

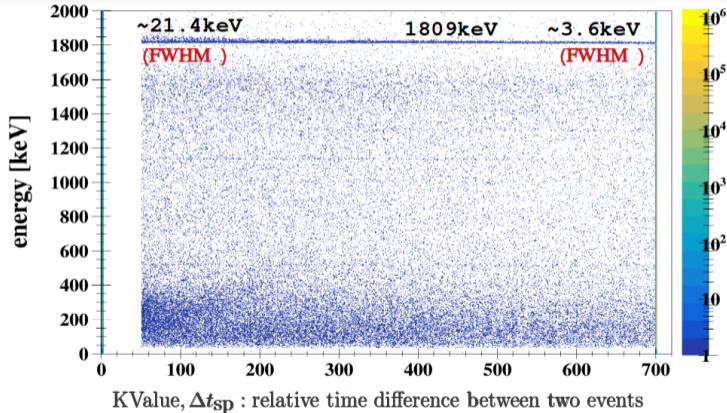
$$P = \epsilon_p [1 - e^{-2x}(1 + x)] \quad 3$$

The probability of pile up with a **non zero time resolution, CFD** and **detection efficiency** in 1, 2 and 3 respectively.

$$P_{\text{fit-total}} = a_6 \left( 1 - e^{-(2-a_4)x} [e^{a_4x} + a_5(1 - a_4)x] \right) \quad 4$$

# Dead-time and Detector Pulse Pile-up Corrections

Signal pile-up occurs when more than one energy deposition from different physics events is present in a detector element during the processing time of the initial interaction.



One can clearly see the dependence of the energy resolution on the k-value. The energy resolution worsens with decreasing integration length as expected and vice versa.

# 1st Order Pile-up Corrections

## 1. Deadfraction Correction

$$N'_i = \frac{N_i}{1 - D_i}$$

$D_i$  = Dead fraction

0.53%

## 2. 1<sup>st</sup> Order Pile-up Correction

$$N''_i = \frac{N'_i}{1 - P_i}$$

$P_i$  =  $\frac{\text{Pile-up Events}}{\text{All Events}}$

0.78%

$$N''_i = \frac{N_i}{(1 - D_i) \times (1 - P_i)}$$

★ RATE DEPENDENT CORRECTIONS

### Rate-Dependent Refinements

#### ➤ Trigger-Energy Threshold

- Corrects for **pile-up** caused by sub threshold energy events.

#### ➤ Pile-up Time Resolution

- Corrects for **pile-up** events not resolved (in time) by the **pile-up circuitry**.



## Selection Criteria Utilized

1

Decay data for the Na-26 experiment were collected in cycles(1, 14, 5, 30 s)★

- The first selection criterion: **REJECT** those cycles that had very few, or even zero, total counts recorded during the decay measurement.

2

Apply an energy gate on the 1809-keV transition in  $^{26}\text{Mg}$

3

Remove Pile Up Events using a gate on the K-Values



The precise values of the tape move, background, beam-on time and decay measurement were varied on a **run-by-run** basis.