

Novel KDK measurement of elusive  $^{40}\text{K}$  decay  
Implications for rare-event searches and geochronology

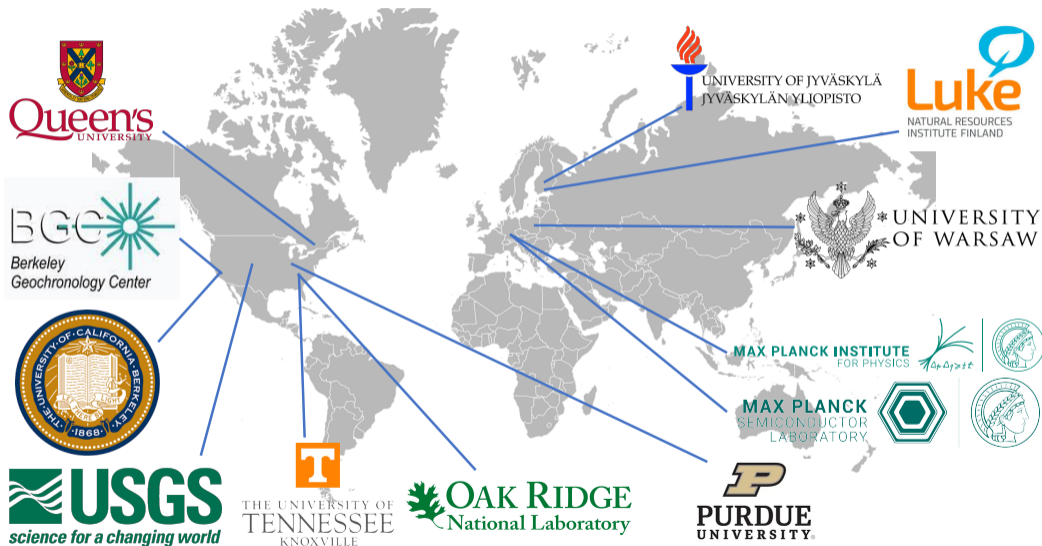
**Lilianna Hariasz**

Queen's University, Kingston, ON  
(Supervisor: **Philippe Di Stefano**)

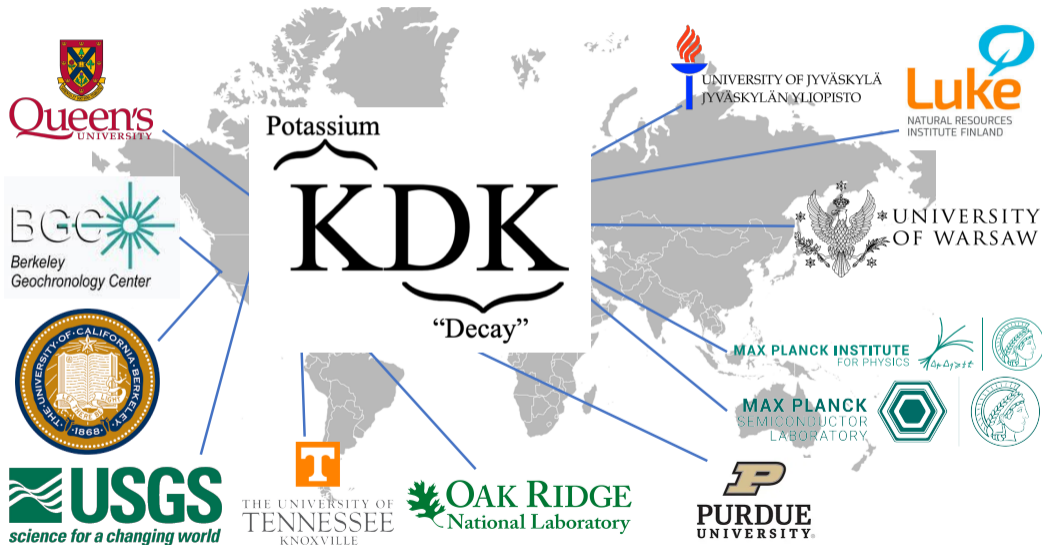
June 21, 2023

2023 CAP CONGRESS, JUNE 18-23, 2023  
*Fredericton, NB, Canada*

# The KDK collaboration

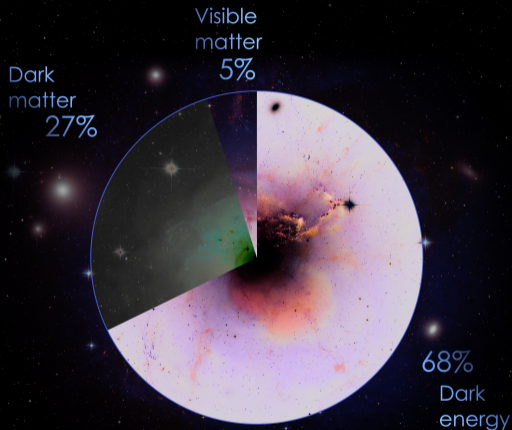


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# Dark matter

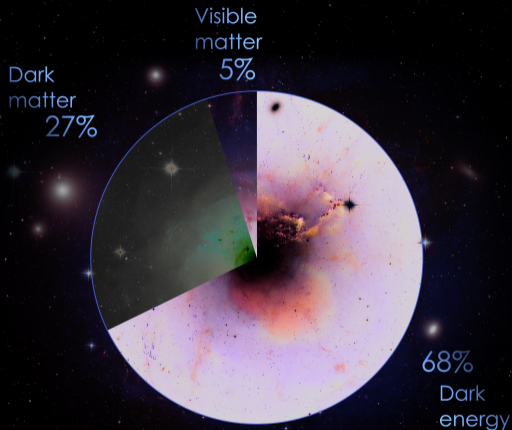
- Various searches for dark matter, particularly for **WIMPs**
- Direct-detection with NaI (DAMA/LIBRA<sup>1</sup>, SABRE<sup>2</sup>, COSINUS<sup>3</sup>,...):  $\mathcal{O}(\text{keV})$  signal
- **K in NaI;  $^{40}\text{K} \rightarrow \text{Ar}$  electron captures: irreducible 3 keV background**



<sup>1</sup>Bernabei et al., *Universe* 4(11), 116 (2018), <sup>2</sup>Antonello et al., *Astropart. Phys.* 106, 1-9 (2019), <sup>3</sup>Angloher et al., *Eur. Phys. J. C* 82(3), 1-11 (2022)

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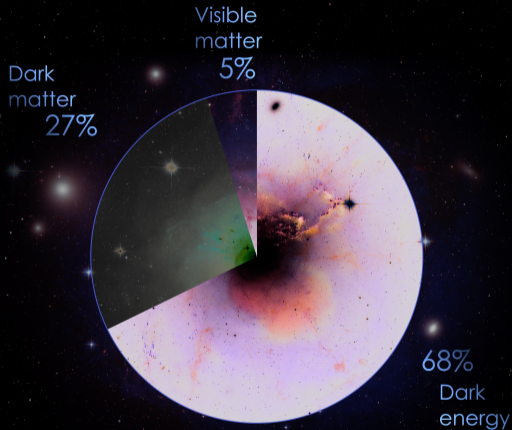
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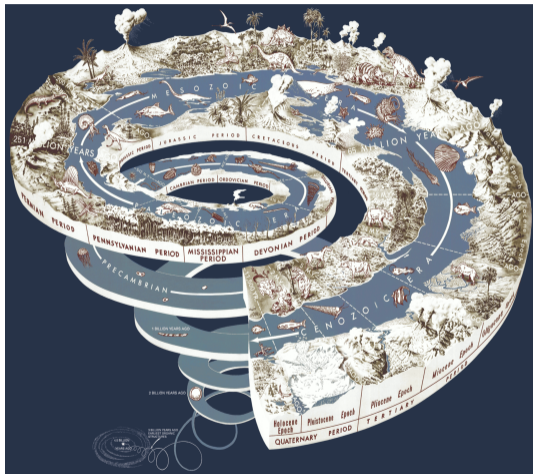
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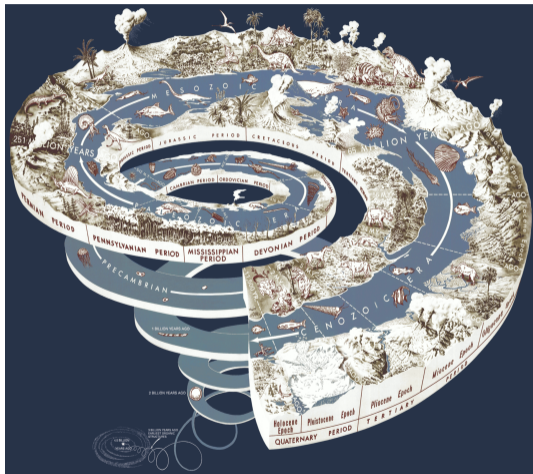
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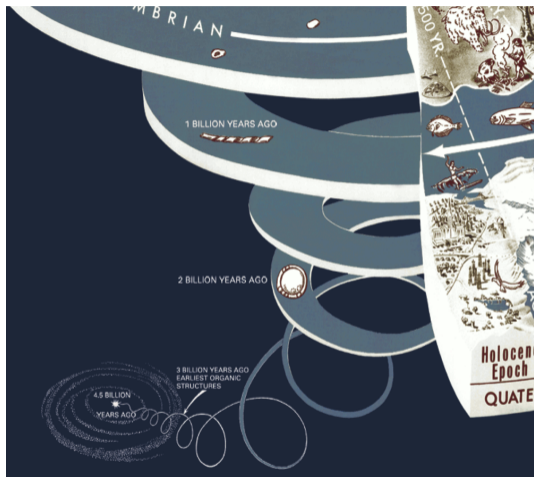


- Various dating techniques, including radioisotopic
- K/Ar and  $^{40}\text{Ar}/^{39}\text{Ar}$  techniques use knowledge of  $^{40}\text{K} \rightarrow \text{Ar}$  decays
- Long-lived  $^{40}\text{K}$  ( $t_{1/2} \sim 10^9 \text{ y}$ ) used to access timescales as old as the Earth



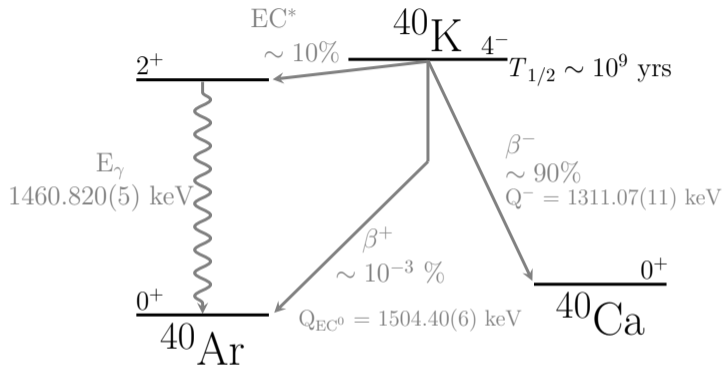
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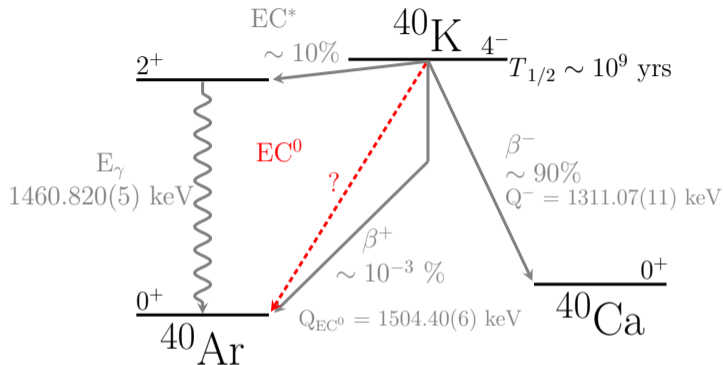
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# Nuclear Theory & $0\nu\beta\beta$



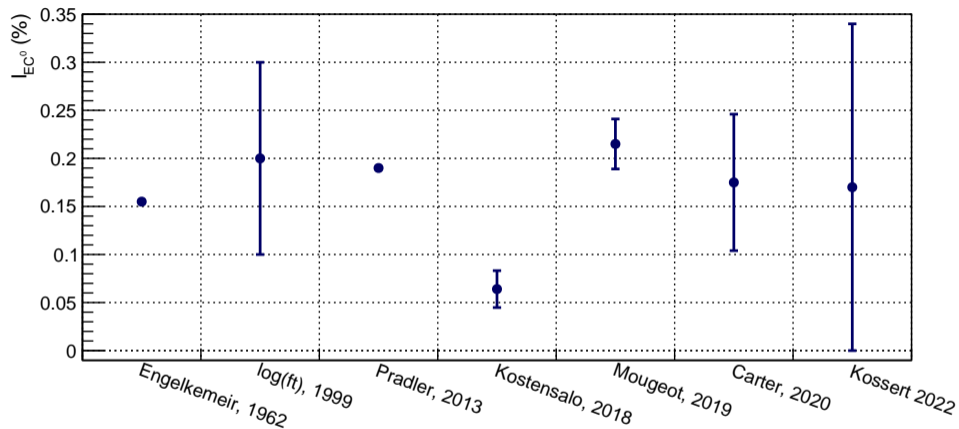
- $\text{EC}^0$ : rare *third-forbidden unique* transition
- Assumed  $I_{\text{EC}^0} \sim (0 - 0.8)\%$
- 3FU: effective weak-axial vector coupling constant  $\rightarrow 0\nu\beta\beta$  half-life ( $^{48}\text{Ca}$ )

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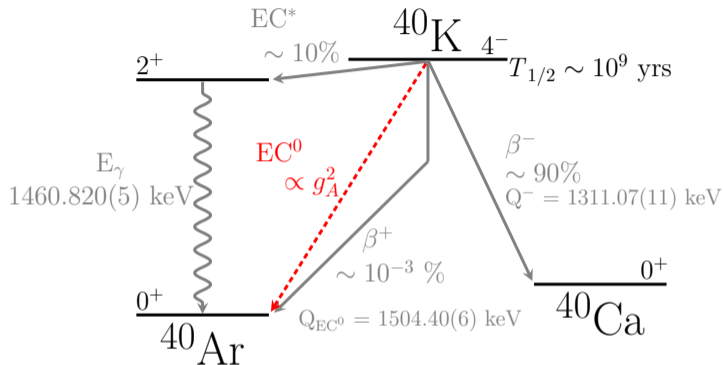
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## Direct-detection

3 keV events *with no high-energy veto available*

## Geochronology

Common exclusion<sup>[1a]</sup> of EC<sup>0</sup> branch can shift calculated ages by  
> 10,000,000 years (order of error)<sup>[1b]</sup>

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No existing 3FU electron capture measurements<sup>2</sup>: avenue to quantify uncertainties  
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KDK obtained first EC<sup>0</sup> measurement of <sup>40</sup>K

<sup>1</sup>Exclusion in <sup>a</sup>Min et al., *Geochim. Cosmochim. Acta* **64**(1), 111-121 (2001), as shown in <sup>b</sup>Carter et al., *Geochronology* **2**(2), 355-365 (2020)

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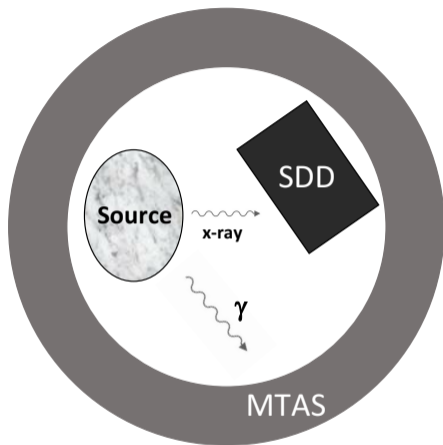
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# Coincidence technique



Coincident ( $\sim EC^*$ )

SDD signal + MTAS detection

Anti-coincident ( $\sim EC^0$ )

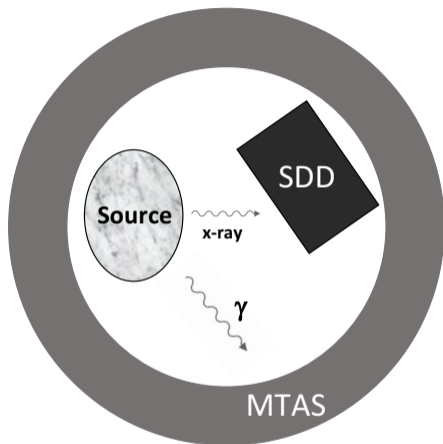
SDD signal *only*

KDK measures  $\rho = I_{EC^0}/I_{EC^*}$

Silicon Drift Detector (*MPP/HLL Munich*);  $< 1$  g

Modular Total Absorption Spectrometer (*Oak Ridge National Laboratory*); NaI(Tl),  $\sim 1,000$  kg

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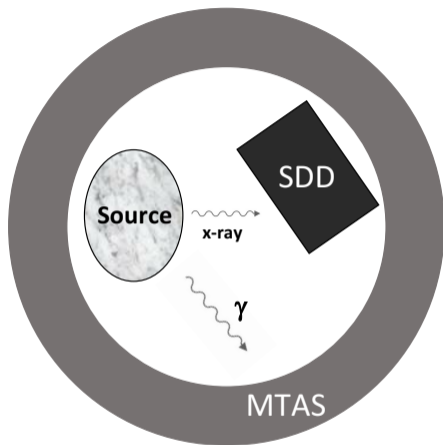
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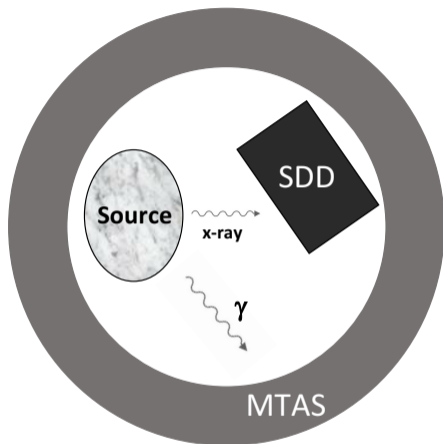
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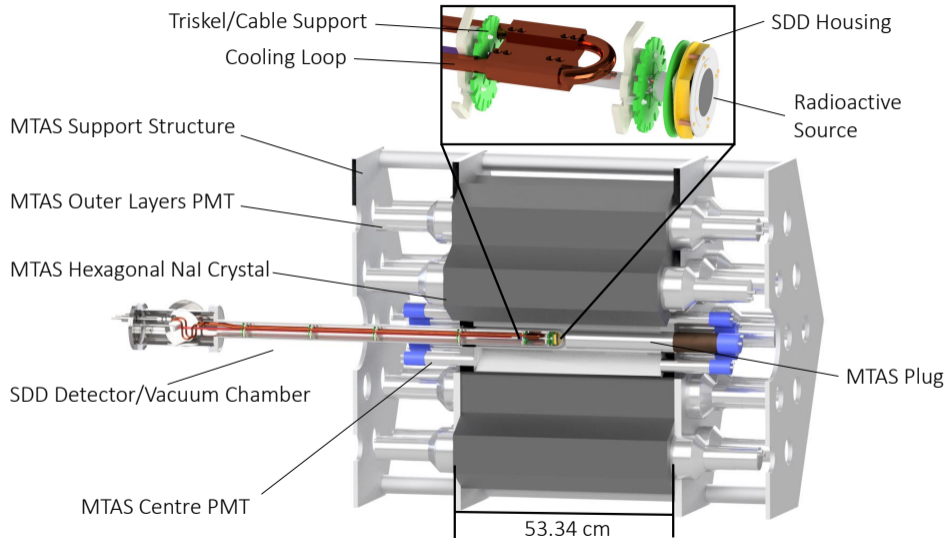
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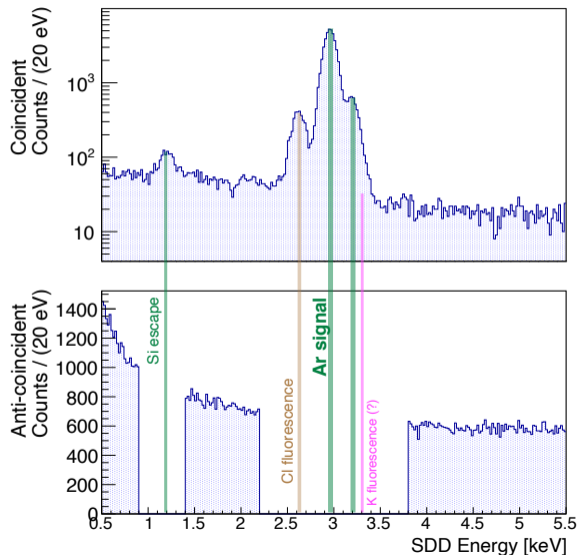
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# Schematic



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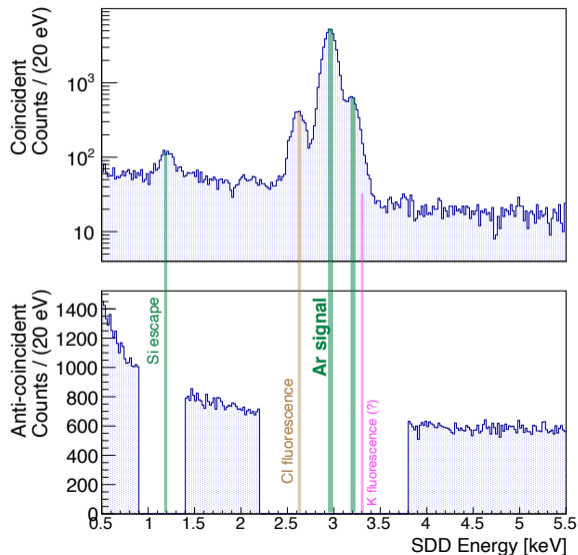


Blinded analysis:

- Likelihood method, statistical procedure
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Testing methods:  
open analysis of  $^{65}\text{Zn}$  data

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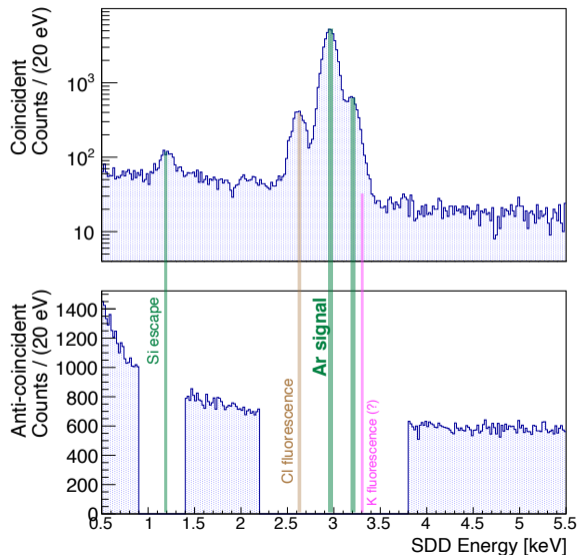
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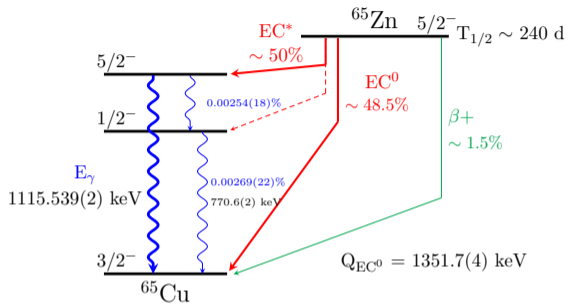


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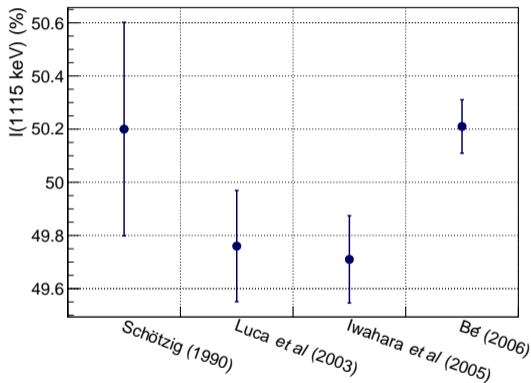
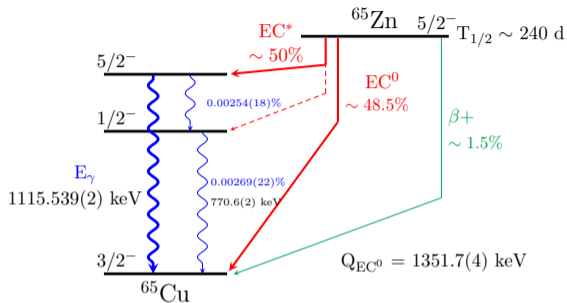
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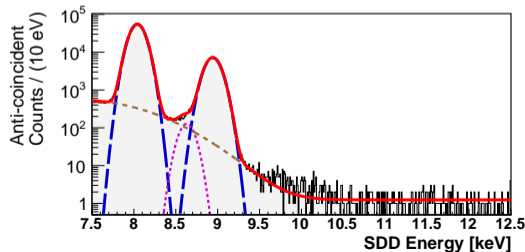
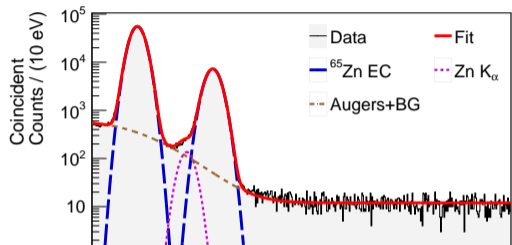
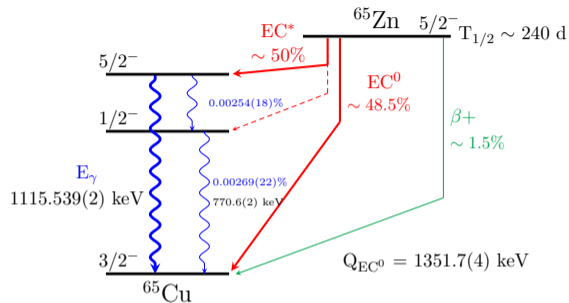
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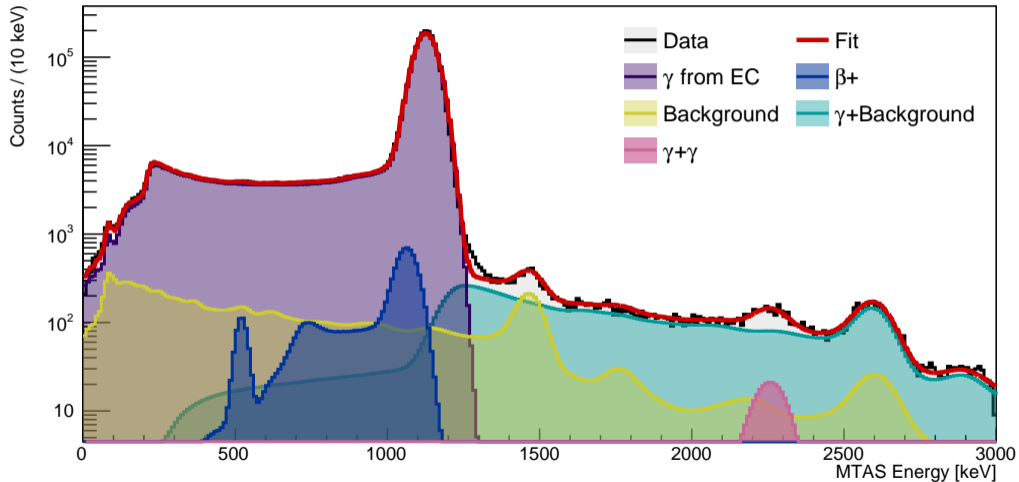
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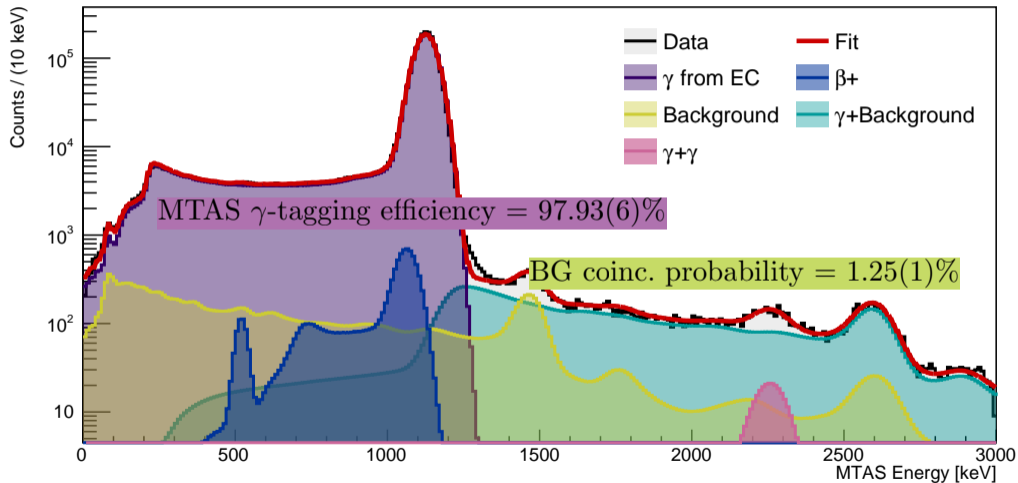


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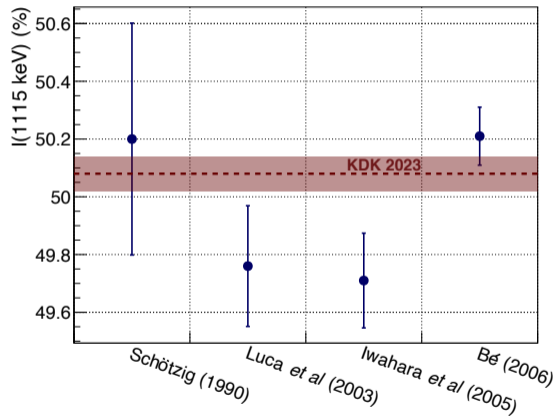
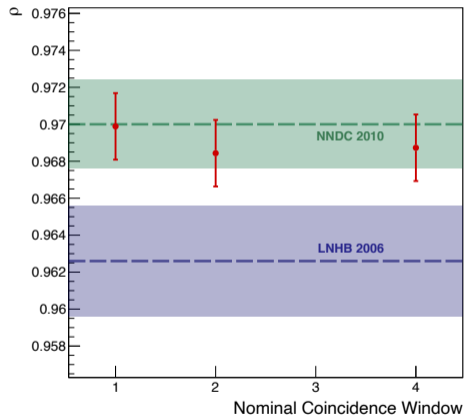


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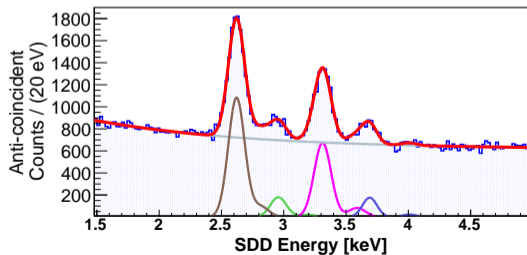
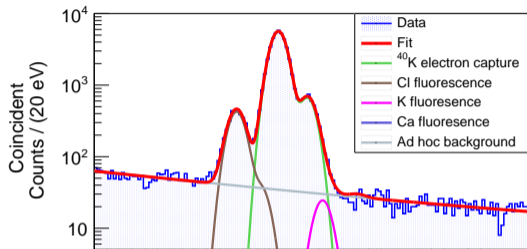


Values at 2  $\mu\text{s}$  SDD+MTAS coincidence window

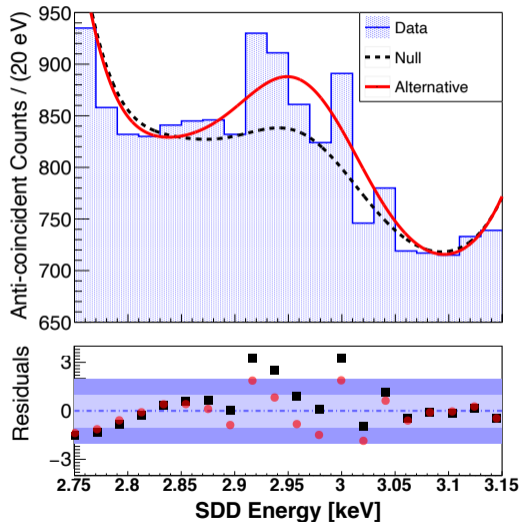
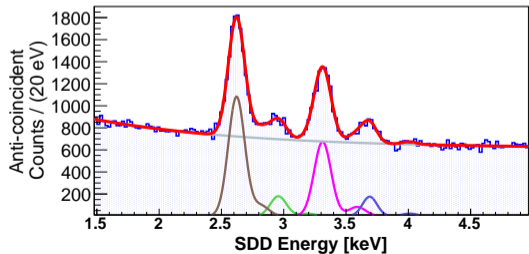
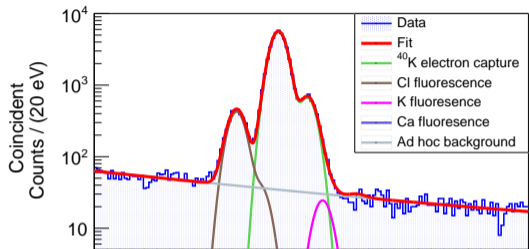
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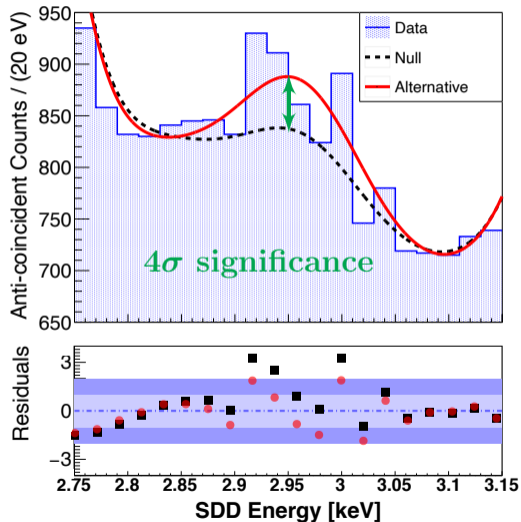
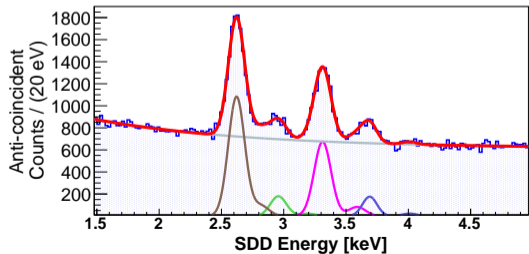
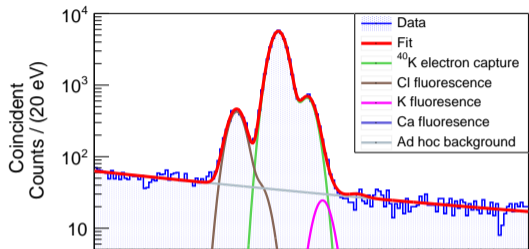


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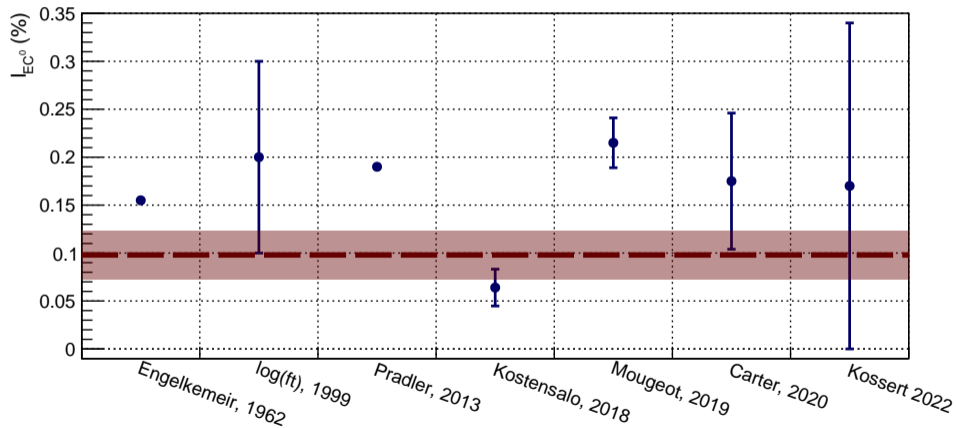








$$\rho = I_{\text{EC}^0}/I_{\text{EC}^*} = \left( 0.95^{\text{stat}} \pm 0.22^{\text{syst}} \pm 0.10 \right) \times 10^{-2} \rightarrow \boxed{I_{\text{EC}^0} = (0.098 \pm 0.025)\%}$$



# Implications of $^{40}\text{K}$ result

## DM direct-detection

- Quantified 3 keV background in NaI
- DAMA/LIBRA: tends to loosen constraints on result interpretation

## Geochronology

- $I_{\text{EC}^0}$  omission  $\rightarrow$  K/Ar ages overestimated
- Indirect effect on  $^{40}\text{Ar}/^{39}\text{Ar}$

## Nuclear theory

- First 3FU EC measurement
- Significant  $g_A$  quenching from  $g_A^{\text{bare}}$ ,
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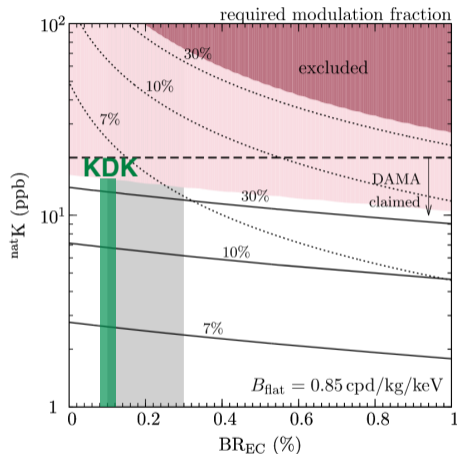
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From Pradler *et al* (2013) [arXiv:1210.5501](https://arxiv.org/abs/1210.5501)

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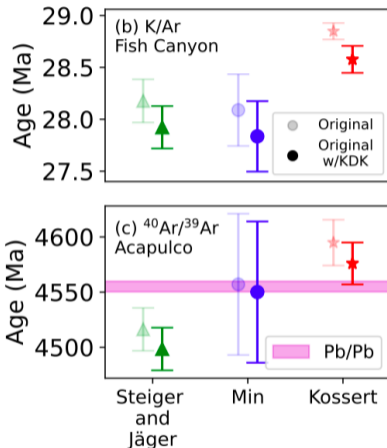
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From Stukel *et al* (KDK) [arXiv:2211.10319](https://arxiv.org/abs/2211.10319)

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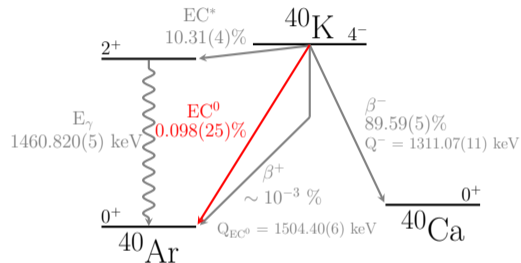
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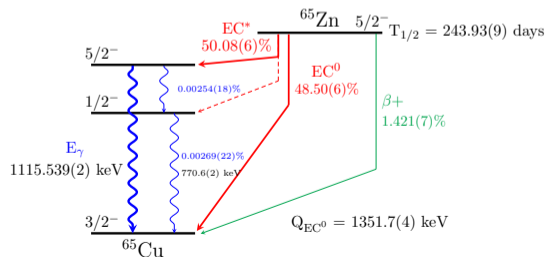
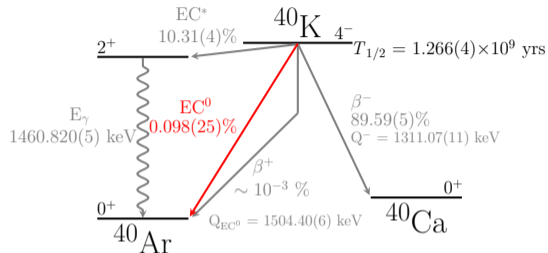
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Editors' Suggestion

## Rare $^{40}\text{K}$ Decay with Implications for Fundamental Physics and Geochronology

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(KDK Collaboration)

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## Evidence for ground-state electron capture of $^{40}\text{K}$

[Jointly accepted by PRC; Hariasz *et al* [arXiv:2211.10343](https://arxiv.org/abs/2211.10343)]

## Precision measurement of $^{65}\text{Zn}$ electron-capture decays with the KDK coincidence setup

[Hariasz *et al*, *Nucl. Data Sheets* 189-224 (2023)]

KDK+: upcoming measurement of  $^{40}\text{K}$   $\beta^+$  branch



# Thank you

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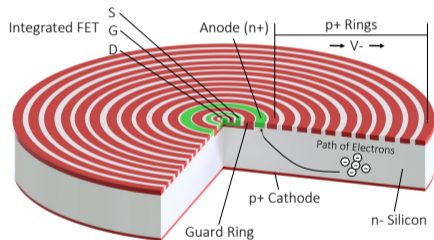
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# SDD Details

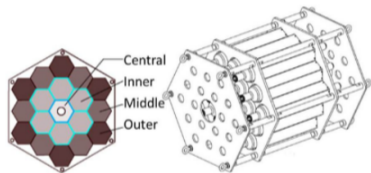


- Increasingly-biased  $p^+$  rings
- Planar cathode
- Central  $n^+$  anode is at potential minimum
- Gate of field-effect transistor (FET) connected to anode

## MTAS Insert

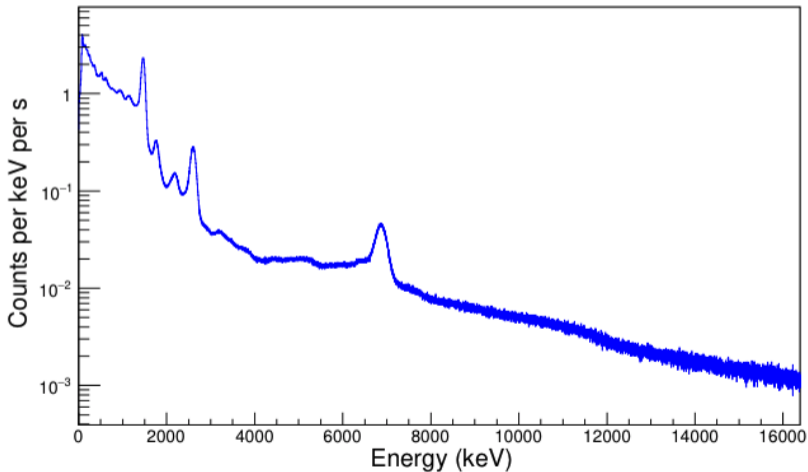
- Contains SDD + source
- 2mm width except for endcap
- Endcap is 30cm long, 0.63mm thick to reduce scattering

# MTAS Details



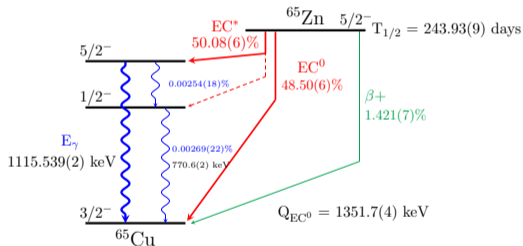
- 19 NaI(Tl) hexagonal volumes
- $\sim 53 \text{ cm} \times 18 \text{ cm}$
- Inner, Middle Outer: one PMT at each end
- Center: 6 PMTs on each end, hole through center for source
- total mass  $\sim 1 \text{ ton}$
- $\sim 4\pi \text{ sr}$  coverage
- surrounded by lead shielding

Peaks:  $^{40}\text{K}$  (1460 keV),  $^{214}\text{Bi}$  (1760 keV),  $^{208}\text{Tl}$  (2614 keV),  $^{127}\text{I}$  &  $^{23}\text{Na}$  neutron captures (6800 keV).



# $^{65}\text{Zn}$ - 3rd Electron Capture Branch

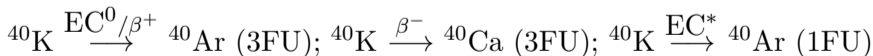
- Electron capture branch to the 770 keV level
- Intensity per 100 for 770 keV = 0.00269(22)
- Intensity per 100 for 330 keV = 0.00254(18)
- This means decay directly to 770 keV occurs 0.00015(28) % of the time
- The systematic effect of the intermediate  $^{65}\text{Cu}$  energy level on  $\rho$  is smaller than the statistical error



# Uniqueness, Forbiddenness - I/II

From [this link](#)

Type of Transition	Selection Rules	$L_{e\nu}$	$\Delta\pi?$	$ft$
superallowed	$\Delta I = 0, \pm 1^*$	0	no	$1 \times 10^3 - 1 \times 10^4$
allowed	$\Delta I = 0, \pm 1$	0	no	$2 \times 10^3 - 10^6$
1 <sup>st</sup> forbidden	$\Delta I = 0, \pm 1$	1	yes	$10^6 - 10^8$
unique**1 <sup>st</sup> forbidden	$\Delta I = \pm 2$	1	yes	$10^8 - 10^9$
2 <sup>nd</sup> forbidden	$\Delta I = \pm 1^{***}, \pm 2$	2	no	$2 \times 10^{10} - 2 \times 10^{13}$
unique 2 <sup>nd</sup> forbidden	$\Delta I = \pm 3$	2	no	$10^{12}$
3 <sup>rd</sup> forbidden	$\Delta I = \pm 2^{***}, \pm 3$	3	yes	$10^{18}$
unique 3 <sup>rd</sup> forbidden	$\Delta I = \pm 4$	3	yes	$4 \times 10^{15}$
4 <sup>th</sup> forbidden	$\Delta I = \pm 3^{***}, \pm 4$	4	no	$10^{23}$
unique 4 <sup>th</sup> forbidden	$\Delta I = \pm 5$	4	no	$10^{19}$



${}^{65}\text{Zn}$  all allowed.

# Uniqueness, Forbiddenness - II/II

From [this link](#)

Nomenclature	Meaning
$\vec{L}, L$	Total orbital angular momentum of the $e\nu$ pair
$\vec{S}, S$	Total spin angular momentum of the $e\nu$ pair
Fermi (F) transition	$e\nu$ intrinsic spins anti-align, $S = 0$
Gamow-Teller (GT) transition	$e\nu$ intrinsic spins align, $S = 1$
Superallowed	The nucleon that changed form, did not change shell-model orbital.
Allowed	$L = 0$ transition. $M_{if}^0 \neq 0$ . See (15.27).
$n^{\text{th}}$ forbidden	The $e\nu$ pair carry off $n$ units of orbital angular momentum
Unique	$\vec{L}$ and $\vec{S}$ are aligned.

“Unique transitions are Gamow-Teller transitions where L and S are aligned.”