

The nEXO 0vBB Experiment

Searching for Lepton Number Violation and Majorana Neutrinos with ¹³⁶Xe

Soud Al Kharusi, McGill University

Canadian Association of Physicists Annual Congress, June 20th 2023

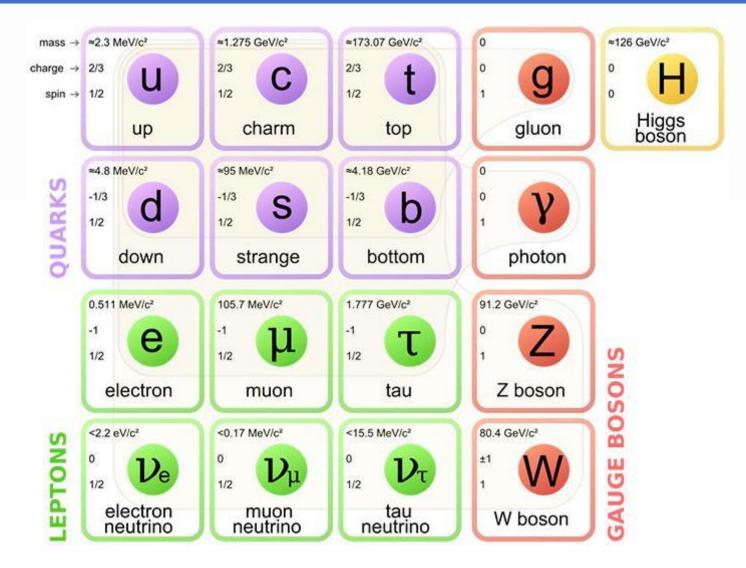
soud.alkharusi@mail.mcgill.ca

(on behalf of the nEXO Collaboration)



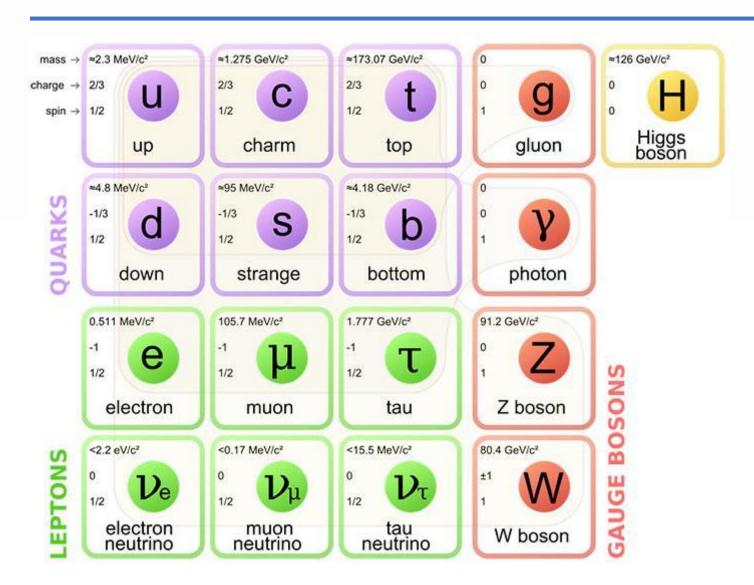
The Standard Model (SM) of Particle Physics nEX®





The Standard Model: Lagrangians

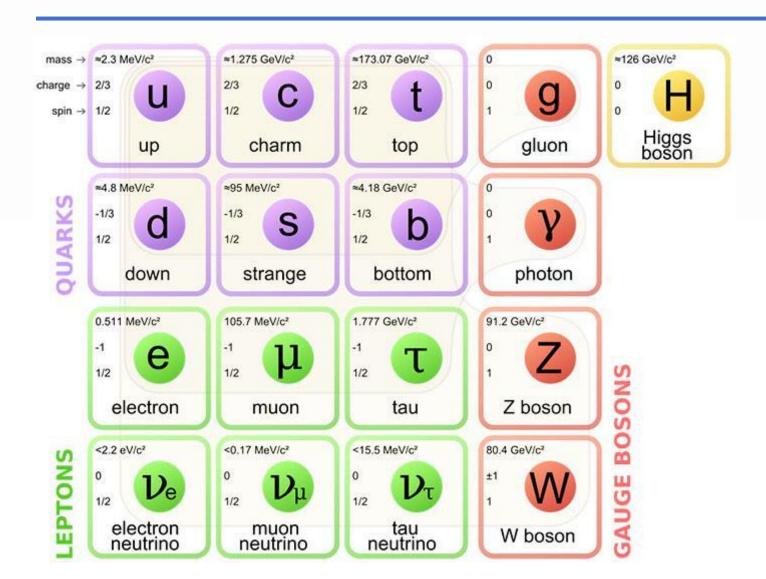




 $\mathcal{L}_{SM} = -\frac{1}{2} \partial_{\nu} g^a_{\mu} \partial_{\nu} g^a_{\mu} - g_s f^{abc} \partial_{\mu} g^a_{\nu} g^b_{\mu} g^c_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{ade} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} +$ $\frac{1}{2}ig_s^2(\bar{q}_i^{\sigma}\gamma^{\mu}q_i^{\sigma})g_u^a + \bar{G}^a\partial^2 G^a + g_sf^{abc}\partial_{\mu}\bar{G}^a\bar{G}^bg_u^c - \partial_{\nu}W_{\mu}^+\partial_{\nu}W_{\mu}^- M^2W_{\mu}^+W_{\mu}^- - \frac{1}{2}\partial_{\nu}Z_{\mu}^0\partial_{\nu}Z_{\mu}^0 - \frac{1}{2c^2}M^2Z_{\mu}^0Z_{\mu}^0 - \frac{1}{2}\partial_{\mu}A_{\nu}\partial_{\mu}A_{\nu} - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H - \frac{1}{2}\partial_{\mu}H\partial_{$ $\frac{1}{2}m_h^2H^2 - \partial_\mu\mathbb{D}^+\partial_\mu\mathbb{D}^- - M^2\mathbb{D}^+\mathbb{D}^- - \frac{1}{2}\partial_\mu\mathbb{D}^0\partial_\mu\mathbb{D}^0 - \frac{1}{2c^2}M\mathbb{D}^0\mathbb{D}^0 - \beta_h[\frac{2M^2}{c^2} + \frac{1}{2}(\frac{M^2}{c^2})]$ $\frac{2M}{g}H + \frac{1}{2}(H^2 + \mathbb{D}^0\mathbb{D}^0 + 2\mathbb{D}^+\mathbb{D}^-)] + \frac{2M^4}{g^2}\alpha_h - igc_w[\partial_\nu Z_\mu^0(W_\mu^+W_\nu^- - W_\mu^-)]$ $W_{\nu}^{+}W_{\mu}^{-}) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}W_{\mu}^{-})]$ $W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + A_{\mu}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{+}W_{\nu}^{-} +$ $\frac{1}{2}g^2W_{\mu}^+W_{\nu}^-W_{\mu}^+W_{\nu}^- + g^2c_w^2(Z_{\mu}^0W_{\mu}^+Z_{\nu}^0W_{\nu}^- - Z_{\mu}^0Z_{\mu}^0W_{\nu}^+W_{\nu}^-) +$ $g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-) + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\mu^0 (W_\mu^+ W_\mu^-)] + g^2 s_w (A_\mu Z_\mu^0 (W_\mu^+ W_\mu^-)] + g^2 s_w (A_\mu Z_\mu^0 (W_\mu^+ W_\mu^-)) + g^2 s_w (A_\mu Z_\mu^0 (W_\mu^- W_\mu^- W_\mu^-)) + g^2 s_w (A_\mu Z_\mu^0 (W_\mu^- W_\mu^- W_\mu^- W_\mu^-)) + g^2 s_w (A_\mu Z_\mu^0 (W_\mu^- W_\mu^- W_\mu^- W_\mu^- W_$ $W_{\nu}^{+}W_{\mu}^{-}$) $-2A_{\mu}Z_{\mu}^{0}W_{\nu}^{+}W_{\nu}^{-}$] $-g\alpha[H^{3}+H\mathfrak{D}^{0}\mathfrak{D}^{0}+2H\mathfrak{D}^{+}\mathfrak{D}^{-}] \frac{1}{5}g^{2}\alpha_{h}[H^{4}+(\mathbb{D}^{0})^{4}+4(\mathbb{D}^{+}\mathbb{D}^{-})^{2}+4(\mathbb{D}^{0})^{2}\mathbb{D}^{+}\mathbb{D}^{-}+4H^{2}\mathbb{D}^{+}\mathbb{D}^{-}+2(\mathbb{D}^{0})^{2}H^{2}]$ $gMW_{\mu}^{+}W_{\mu}^{-}H - \frac{1}{2}g\frac{M}{c_{+}^{2}}Z_{\mu}^{0}Z_{\mu}^{0}H - \frac{1}{2}ig[W_{\mu}^{+}(\mathfrak{D}^{0}\partial_{\mu}\mathfrak{D}^{-} - \mathfrak{D}^{-}\partial_{\mu}\mathfrak{D}^{0}) W_{\mu}^{-}(\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{+}-\mathbb{D}^{+}\partial_{\mu}\mathbb{D}^{0})]+\frac{1}{2}g[W_{\mu}^{+}(H\partial_{\mu}\mathbb{D}^{-}-\mathbb{D}^{-}\partial_{\mu}H)-W_{\mu}^{-}(H\partial_{\mu}\mathbb{D}^{+}-\mathbb{D}^{-}\partial_{\mu}H)]$ $[D^{+}\partial_{\mu}H)] + \frac{1}{2}g\frac{1}{c_{rr}}(Z_{\mu}^{0}(H\partial_{\mu}D^{0} - D^{0}\partial_{\mu}H) - ig\frac{s_{\mu}^{2}}{c_{rr}}MZ_{\mu}^{0}(W_{\mu}^{+}D^{-} - W_{\mu}^{-}D^{+}) +$ $igs_w MA_\mu (W_\mu^+ \mathbb{D}^- - W_\mu^- \mathbb{D}^+) - ig \frac{1-2c_w^2}{2c} Z_\mu^0 (\mathbb{D}^+ \partial_\mu \mathbb{D}^- - \mathbb{D}^- \partial_\mu \mathbb{D}^+) +$ $igs_w A_\mu (\hat{\mathbb{D}}^+ \partial_\mu \hat{\mathbb{D}}^- - \hat{\mathbb{D}}^- \partial_\mu \hat{\mathbb{D}}^+) - \frac{1}{4} g^2 W_\mu^+ W_\mu^- [H^2 + (\hat{\mathbb{D}}^0)^2 + 2 \hat{\mathbb{D}}^+ \hat{\mathbb{D}}^-] \frac{1}{t}g^2\frac{1}{c^2}Z_u^0Z_u^0[H^2+(\tilde{\mathbb{D}}^0)^2+2(2s_w^2-1)^2\tilde{\mathbb{D}}^+\tilde{\mathbb{D}}^-]-\frac{1}{2}g^2\frac{s_w^2}{c_w}Z_u^0\tilde{\mathbb{D}}^0(W_u^+\tilde{\mathbb{D}}^-+$ $W_{\mu}^{-} \mathbb{D}^{+}) - \frac{1}{2} i g^{2} \frac{s_{w}^{2}}{2} Z_{u}^{0} H(W_{\mu}^{+} \mathbb{D}^{-} - W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} \mathbb{D}^{+}) + \frac{1}{2} g^{2} s_{w} A_{\mu} \mathbb{D}^{0} (W_{\mu}^{+} \mathbb{D}^{-} + W_{\mu}^{-} + W_{\mu}^{-}$ $W_{\mu}^{-}\mathbb{D}^{+}) + \frac{1}{2}ig^{2}s_{w}A_{\mu}H(W_{\mu}^{+}\mathbb{D}^{-} - W_{\mu}^{-}\mathbb{D}^{+}) - g^{2}\frac{s_{w}}{c_{w}}(2c_{w}^{2} - 1)Z_{\mu}^{0}A_{\mu}\mathbb{D}^{+}\mathbb{D}^{-}$ $g^1 s_w^2 A_\mu A_\mu \bar{\omega}^+ \bar{\omega}^- - \bar{e}^\lambda (\gamma \partial + m_e^\lambda) e^\lambda - \bar{\nu}^\lambda \gamma \partial \nu^\lambda - \bar{u}_i^\lambda (\gamma \partial + m_u^\lambda) u_i^\lambda \bar{d}_i^{\lambda}(\gamma \partial + m_d^{\lambda})d_i^{\lambda} + igs_w A_{\mu}[-(\bar{e}^{\lambda}\gamma^{\mu}e^{\lambda}) + \frac{2}{3}(\bar{u}_i^{\lambda}\gamma^{\mu}u_i^{\lambda}) - \frac{1}{3}(\bar{d}_i^{\lambda}\gamma^{\mu}d_i^{\lambda})] +$ $\frac{ig}{4c_w}Z_{\mu}^0[(\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda})+(\bar{e}^{\lambda}\gamma^{\mu}(4s_w^2-1-\gamma^5)e^{\lambda})+(\bar{u}_j^{\lambda}\gamma^{\mu}(\frac{4}{3}s_w^2-1)e^{\lambda})]$ $(1-\gamma^5)u_j^{\lambda}) + (\bar{d}_j^{\lambda}\gamma^{\mu}(1-\frac{8}{3}s_w^2-\gamma^5)d_j^{\lambda})] + \frac{ig}{2\sqrt{2}}W_{\mu}^+[(\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^5)e^{\lambda}) + (\bar{d}_j^{\lambda}\gamma^{\mu}(1+\gamma^5)e^{\lambda})]$ $(\bar{u}_{j}^{\lambda}\gamma^{\mu}(1+\gamma^{5})C_{\lambda\kappa}d_{j}^{\kappa})] + \frac{ig}{2\sqrt{2}}W_{\mu}^{-}[(\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda}) + (\bar{d}_{j}^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda})]$ $\gamma^{5}(u_{i}^{\lambda})$] + $\frac{ig}{2\sqrt{2}}\frac{m_{e}^{\lambda}}{M}[-\bar{\mathbb{D}}^{+}(\bar{\nu}^{\lambda}(1-\gamma^{5})e^{\lambda}) + \bar{\mathbb{D}}^{-}(\bar{e}^{\lambda}(1+\gamma^{5})\nu^{\lambda})]$ - $\frac{g}{2}\frac{m_c^{\lambda}}{M}[H(\bar{e}^{\lambda}e^{\lambda}) + i\bar{\Theta}^0(\bar{e}^{\lambda}\gamma^5e^{\lambda})] + \frac{ig}{2M\sqrt{2}}\bar{\Theta}^+[-m_d^{\kappa}(\bar{u}_j^{\lambda}C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) +$ $m_u^{\lambda}(\bar{u}_j^{\lambda}C_{\lambda\kappa}(1+\gamma^5)d_j^{\kappa}] + \frac{ig}{2M\sqrt{2}} \tilde{\mathbb{D}}^-[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^5)u_j^{\kappa})]$ $\gamma^5 u_i^{\kappa} = \frac{g}{2} \frac{m_u^{\lambda}}{M} H(\bar{u}_i^{\lambda} u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} H(\bar{d}_i^{\lambda} d_i^{\lambda}) + \frac{ig}{2} \frac{m_u^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) + \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) + \frac{g}{2} \frac{m_$ $\frac{ig}{2}\frac{m_d^{\lambda}}{M}\tilde{\epsilon}^0(\bar{d}_i^{\lambda}\gamma^5d_i^{\lambda}) + \bar{X}^+(\partial^2 - M^2)X^+ + \bar{X}^-(\partial^2 - M^2)X^- + \bar{X}^0(\partial^2 - M^2)X^ \frac{M^2}{c^2}$ $X^0 + Y \partial^2 Y + igc_w W_u^+ (\partial_u X^0 X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^+ X^0)$ $\partial_{\mu}\bar{X}^{+}Y$) + $igc_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}X^{0} - \partial_{\mu}\bar{X}^{0}X^{+}) + igs_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}Y - igs_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}Y - igs_{w}W_{\mu}^{-}))$ $\partial_u \bar{Y} X^+$) + $igc_w Z_u^0 (\partial_u \bar{X}^+ X^+ - \partial_u \bar{X}^- X^-) + igs_w A_u (\partial_u \bar{X}^+ X^+ - \partial_u \bar{X}^- X^-)$ $\partial_{\mu}\bar{X}^{-}X^{-}$) $-\frac{1}{2}gM[\bar{X}^{+}X^{+}H + \bar{X}^{-}X^{-}H + \frac{1}{c^{2}}\bar{X}^{0}X^{0}H] +$ $\frac{1-2c_{w}^{2}}{2c_{w}}igM[\bar{X}^{+}X^{0}\mathbb{D}^{+}-\bar{X}^{-}X^{0}\mathbb{D}^{-}]+\frac{1}{2c_{w}}igM[\bar{X}^{0}X^{-}\mathbb{D}^{+}-\bar{X}^{0}X^{+}\mathbb{D}^{-}]+$ $igMs_w[X^0X^-\mathfrak{D}^+ - X^0X^+\mathfrak{D}^-] + \frac{1}{2}igM[X^+X^+\mathfrak{D}^0 - X^-X^-\mathfrak{D}^0]$

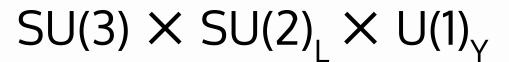
The Standard Model: Lagrangians

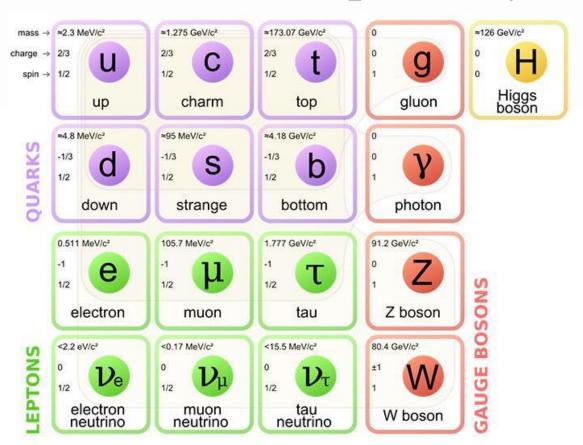




 $\mathcal{L}_{SM} = -\tfrac{1}{2} \partial_\nu g^a_\mu \partial_\nu g^a_\mu - g_s f^{abc} \partial_\mu g^a_\nu g^b_\mu g^c_\nu - \tfrac{1}{4} g^2_s f^{abc} f^{ade} g^b_\mu g^c_\nu g^d_\mu g^e_\nu +$ $\frac{1}{2}ig_s^2(\bar{q}_i^{\sigma}\gamma^{\mu}q_i^{\sigma})g_u^a + \bar{G}^a\partial^2 G^a + g_sf^{abc}\partial_{\mu}\bar{G}^a\bar{G}^bg_u^c - \partial_{\nu}W_{\mu}^+\partial_{\nu}W_{\mu}^- M^2W_{\mu}^+W_{\mu}^- - \frac{1}{2}\partial_{\nu}Z_{\mu}^0\partial_{\nu}Z_{\mu}^0 - \frac{1}{2c^2}M^2Z_{\mu}^0Z_{\mu}^0 - \frac{1}{2}\partial_{\mu}A_{\nu}\partial_{\mu}A_{\nu} - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H - \frac{1}{2}\partial_{\mu}H\partial_{$ $\frac{1}{2}m_h^2H^2 - \partial_\mu\mathbb{D}^+\partial_\mu\mathbb{D}^- - M^2\mathbb{D}^+\mathbb{D}^- - \frac{1}{2}\partial_\mu\mathbb{D}^0\partial_\mu\mathbb{D}^0 - \frac{1}{2c^2}M\mathbb{D}^0\mathbb{D}^0 - \beta_h[\frac{2M^2}{c^2} + \frac{1}{2}(\frac{M^2}{c^2})]$ $\frac{2M}{g}H + \frac{1}{2}(H^2 + \mathbb{D}^0\mathbb{D}^0 + 2\mathbb{D}^+\mathbb{D}^-)] + \frac{2M^4}{g^2}\alpha_h - igc_w[\partial_\nu Z_\mu^0(W_\mu^+W_\nu^- - W_\mu^-)]$ $W_{\nu}^{+}W_{\mu}^{-}) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}^{\prime}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}^{\prime}W_{\mu}^{-})$ $W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}W_{\mu}^{-})]$ $W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + A_{\mu}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{+}W_{\nu}^{-} +$ $\frac{1}{2}g^2W_{\mu}^+W_{\nu}^-W_{\mu}^+W_{\nu}^- + g^2c_w^2(Z_{\mu}^0W_{\mu}^+Z_{\nu}^0W_{\nu}^- - Z_{\mu}^0Z_{\mu}^0W_{\nu}^+W_{\nu}^-) +$ $g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-) + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\mu^0 (W_\mu^+ W_\mu^-)] + g^2 s_w (A_\mu Z_\mu^0 (W_\mu^+ W_\mu^-)] + g^2 s_w (A_\mu Z_\mu^0 (W_\mu^+ W_\mu^-)) + g^2 s_w (A_\mu Z_\mu^0 (W_\mu^- W_\mu^- W_\mu^-)) + g^2 s_w (A_\mu Z_\mu^0 (W_\mu^- W_\mu^- W_\mu^- W_\mu^-)) + g^2 s_w (A_\mu Z_\mu^0 (W_\mu^- W_\mu^- W_\mu^- W_\mu^- W_$ $W_{\nu}^{+}W_{\nu}^{-}) - 2A_{\mu}Z_{u}^{0}W_{\nu}^{+}W_{\nu}^{-}] - g\alpha[H^{3} + H\mathfrak{D}^{0}\mathfrak{D}^{0} + 2H\mathfrak{D}^{+}\mathfrak{D}^{-}] \frac{1}{5}g^{2}\alpha_{h}[H^{4}+(\mathbb{D}^{0})^{4}+4(\mathbb{D}^{+}\mathbb{D}^{-})^{2}+4(\mathbb{D}^{0})^{2}\mathbb{D}^{+}\mathbb{D}^{-}+4H^{2}\mathbb{D}^{+}\mathbb{D}^{-}+2(\mathbb{D}^{0})^{2}H^{2}]$ $gMW_{\mu}^{+}W_{\mu}^{-}H - \frac{1}{2}g\frac{M}{c_{+}^{2}}Z_{\mu}^{0}Z_{\mu}^{0}H - \frac{1}{2}ig[W_{\mu}^{+}(\mathfrak{D}^{0}\partial_{\mu}\mathfrak{D}^{-} - \mathfrak{D}^{-}\partial_{\mu}\mathfrak{D}^{0}) W_{\mu}^{-}(\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{+}-\mathbb{D}^{+}\partial_{\mu}\mathbb{D}^{0})]+\frac{1}{2}g[W_{\mu}^{+}(H\partial_{\mu}\mathbb{D}^{-}-\mathbb{D}^{-}\partial_{\mu}H)-W_{\mu}^{-}(H\partial_{\mu}\mathbb{D}^{+}-\mathbb{D}^{-}\partial_{\mu}H)]$ $\mathbb{D}^{+}\partial_{\mu}H)] + \frac{1}{2}g\frac{1}{c_{m}}(Z^{0}_{\mu}(H\partial_{\mu}\mathbb{D}^{0} - \mathbb{D}^{0}\partial_{\mu}H) - ig\frac{s^{2}_{m}}{c_{m}}MZ^{0}_{\mu}(W^{+}_{\mu}\mathbb{D}^{-} - W^{-}_{\mu}\mathbb{D}^{+}) +$ $igs_w M A_\mu (W_\mu^+ \bar{\mathbb{D}}^- - W_\mu^- \bar{\mathbb{D}}^+) - ig \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\bar{\mathbb{D}}^+ \partial_\mu \bar{\mathbb{D}}^- - \bar{\mathbb{D}}^- \partial_\mu \bar{\mathbb{D}}^+) +$ $a_j^{\wedge}(\gamma\partial + m_d^{\wedge})a_j^{\wedge} + igs_wA_{\mu}[-(\bar{e}^{\wedge}\gamma^{\mu}e^{\wedge}) + \frac{2}{3}(\bar{u}_j^{\wedge}\gamma^{\mu}u_j^{\wedge}) - \frac{1}{3}(\bar{u}_j^{\wedge}\gamma^{\mu}d_j^{\wedge})] +$ $\frac{ig}{4c_w}Z_{\mu}^0[(\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda})+(\bar{e}^{\lambda}\gamma^{\mu}(4s_w^2-1-\gamma^5)e^{\lambda})+(\bar{u}_j^{\lambda}\gamma^{\mu}(\frac{4}{3}s_w^2-1)e^{\lambda})]$ $(1-\gamma^5)u_j^{\lambda}) + (\bar{d}_j^{\lambda}\gamma^{\mu}(1-\frac{8}{3}s_w^2-\gamma^5)d_j^{\lambda})] + \frac{ig}{2\sqrt{2}}W_{\mu}^+[(\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^5)e^{\lambda}) + (\bar{d}_j^{\lambda}\gamma^{\mu}(1+\gamma^5)e^{\lambda})]$ $(\bar{u}_{j}^{\lambda}\gamma^{\mu}(1+\gamma^{5})C_{\lambda\kappa}d_{j}^{\kappa})] + \frac{ig}{2\sqrt{2}}W_{\mu}^{-}[(\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda}) + (\bar{d}_{j}^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda})]$ $\gamma^{5}(u_{i}^{\lambda})$] + $\frac{ig}{2\sqrt{2}}\frac{m_{e}^{\lambda}}{M}[-\bar{\mathbb{D}}^{+}(\bar{\nu}^{\lambda}(1-\gamma^{5})e^{\lambda}) + \bar{\mathbb{D}}^{-}(\bar{e}^{\lambda}(1+\gamma^{5})\nu^{\lambda})]$ - $\frac{g}{2}\frac{m_e^{\lambda}}{M}[H(\bar{e}^{\lambda}e^{\lambda}) + i\bar{\mathbb{D}}^0(\bar{e}^{\lambda}\gamma^5e^{\lambda})] + \frac{ig}{2M\sqrt{2}}\bar{\mathbb{D}}^+[-m_d^{\kappa}(\bar{u}_j^{\lambda}C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) +$ $m_u^{\lambda}(\bar{u}_j^{\lambda}C_{\lambda\kappa}(1+\gamma^5)d_j^{\kappa}] + \frac{ig}{2M\sqrt{2}} \tilde{\mathbb{D}}^-[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^5)u_j^{\kappa})]$ $\gamma^5 u_i^{\kappa} = \frac{g}{2} \frac{m_u^{\lambda}}{M} H(\bar{u}_i^{\lambda} u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} H(\bar{d}_i^{\lambda} d_i^{\lambda}) + \frac{ig}{2} \frac{m_u^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) + \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) + \frac{g}{2} \frac{m_$ $\frac{ig}{2}\frac{m_d^{\lambda}}{M}\tilde{\epsilon}^0(\bar{d}_i^{\lambda}\gamma^5d_i^{\lambda}) + \bar{X}^+(\partial^2 - M^2)X^+ + \bar{X}^-(\partial^2 - M^2)X^- + \bar{X}^0(\partial^2 - M^2)X^ \frac{M^2}{c^2}$ $X^0 + Y \partial^2 Y + igc_w W_u^+ (\partial_u X^0 X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^+ X^0)$ $\partial_{\mu}\bar{X}^{+}Y$) + $igc_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}X^{0} - \partial_{\mu}\bar{X}^{0}X^{+}) + igs_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}Y - igs_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}Y - igs_{w}W_{\mu}^{-}))$ $\partial_u \bar{Y} X^+$) + $igc_w Z_u^0 (\partial_u \bar{X}^+ X^+ - \partial_u \bar{X}^- X^-) + igs_w A_u (\partial_u \bar{X}^+ X^+ - \partial_u \bar{X}^- X^-)$ $\partial_{\mu}\bar{X}^{-}X^{-}$) $-\frac{1}{2}gM[\bar{X}^{+}X^{+}H + \bar{X}^{-}X^{-}H + \frac{1}{c^{2}}\bar{X}^{0}X^{0}H] +$ $\frac{1-2c_{w}^{2}}{2c_{w}}igM[\bar{X}^{+}X^{0}\mathbb{D}^{+}-\bar{X}^{-}X^{0}\mathbb{D}^{-}]+\frac{1}{2c_{w}}igM[\bar{X}^{0}X^{-}\mathbb{D}^{+}-\bar{X}^{0}X^{+}\mathbb{D}^{-}]+$ $igMs_w[X^0X^-\mathfrak{D}^+ - X^0X^+\mathfrak{D}^-] + \frac{1}{2}igM[X^+X^+\mathfrak{D}^0 - X^-X^-\mathfrak{D}^0]$

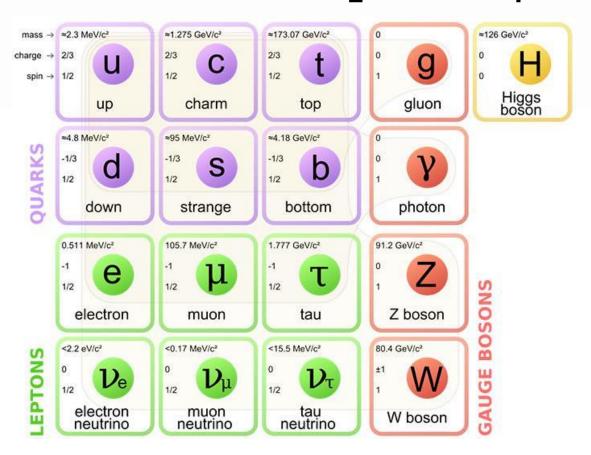
The Standard Model: Symmetries, Gauges & Groups nEX®





 $\mathcal{L}_{SM} = -\frac{1}{2} \partial_{\nu} g^a_{\mu} \partial_{\nu} g^a_{\mu} - g_s f^{abc} \partial_{\mu} g^a_{\nu} g^b_{\mu} g^c_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{ade} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} +$ $\frac{1}{2}ig_s^2(\bar{q}_i^{\sigma}\gamma^{\mu}q_i^{\sigma})g_u^a + \bar{G}^a\partial^2 G^a + g_s f^{abc}\partial_{\mu}G^aG^bg_u^c - \partial_{\nu}W_u^+\partial_{\nu}W_u^- M^2W_{\mu}^+W_{\mu}^- - \frac{1}{2}\partial_{\nu}Z_{\mu}^0\partial_{\nu}Z_{\mu}^0 - \frac{1}{2c^2}M^2Z_{\mu}^0Z_{\mu}^0 - \frac{1}{2}\partial_{\mu}A_{\nu}\partial_{\mu}A_{\nu} - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H - \frac{1}{2}\partial_{\mu}H\partial_{$ $\frac{1}{2}m_{h}^{2}H^{2} - \partial_{\mu}\mathbb{D}^{+}\partial_{\mu}\mathbb{D}^{-} - M^{2}\mathbb{D}^{+}\mathbb{D}^{-} - \frac{1}{2}\partial_{\mu}\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{0} - \frac{1}{2c^{2}}M\mathbb{D}^{0}\mathbb{D}^{0} - \beta_{h}[\frac{2M^{2}}{c^{2}} + \frac{1}{2}(\frac{2M^{2}}{c^{2}})]$ $\frac{2M}{g}H + \frac{1}{2}(H^2 + \mathbb{D}^0\mathbb{D}^0 + 2\mathbb{D}^+\mathbb{D}^-)] + \frac{2M^4}{g^2}\alpha_h - igc_w[\partial_\nu Z_\mu^0(W_\mu^+W_\nu^- - W_\mu^-)]$ $W_{\nu}^{+}W_{\mu}^{-}) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{-})$ $W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}W_{\mu}^{-})]$ $W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + A_{\mu}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{+}W_{\nu}^{-} +$ $\frac{1}{2}g^2W_{\mu}^+W_{\nu}^-W_{\mu}^+W_{\nu}^- + g^2c_w^2(Z_{\mu}^0W_{\mu}^+Z_{\nu}^0W_{\nu}^- - Z_{\mu}^0Z_{\mu}^0W_{\nu}^+W_{\nu}^-)$ $g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-) + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^- W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^- W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\mu^- W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\mu^- W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu Z_\nu^0 (W_\mu^+ W_\mu^-)]] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu Z_\nu^0 (W_\mu^+ W_\mu^-)]] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu Z_\nu^0 (W_\mu^+ W_\mu^-)]] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu Z_\nu^0 (W_\mu^+ W_\mu^-)]] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu Z_\nu^0 (W_\mu^+ W_\mu^-)]] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu Z_\nu^0 (W_\mu^+ W_\mu^-)]] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu Z_\nu^0 (W_\mu^+ W_\mu^-)]] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu Z_\mu^0 (W_\mu^+ W_\mu^-)]] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu Z_\mu^0 (W_\mu^- W_\mu^- W_\mu^-)]] + g^2 s_w (W_\mu^+ W_\mu^- W_\mu^ W_{\nu}^{+}W_{\mu}^{-}$) $-2A_{\mu}Z_{\mu}^{0}W_{\nu}^{+}W_{\nu}^{-}$] $-g\alpha[H^{3}+H\mathfrak{D}^{0}\mathfrak{D}^{0}+2H\mathfrak{D}^{+}\mathfrak{D}^{-}] \frac{1}{9}g^{2}\alpha_{h}[H^{4}+(\mathbb{D}^{0})^{4}+4(\mathbb{D}^{+}\mathbb{D}^{-})^{2}+4(\mathbb{D}^{0})^{2}\mathbb{D}^{+}\mathbb{D}^{-}+4H^{2}\mathbb{D}^{+}\mathbb{D}^{-}+2(\mathbb{D}^{0})^{2}H^{2}]$ $gMW_{\mu}^{+}W_{\mu}^{-}H - \frac{1}{2}g\frac{M}{c^{2}}Z_{\mu}^{0}Z_{\mu}^{0}H - \frac{1}{2}ig[W_{\mu}^{+}(\tilde{\mathbb{D}}^{0}\partial_{\mu}\tilde{\mathbb{D}}^{-} - \tilde{\mathbb{D}}^{-}\partial_{\mu}\tilde{\mathbb{D}}^{0}) W_{\mu}^{-}(\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{+}-\mathbb{D}^{+}\partial_{\mu}\mathbb{D}^{0})]+\frac{1}{2}g[W_{\mu}^{+}(H\partial_{\mu}\mathbb{D}^{-}-\mathbb{D}^{-}\partial_{\mu}H)-W_{\mu}^{-}(H\partial_{\mu}\mathbb{D}^{+}-\mathbb{D}^{-}\partial_{\mu}H)]$ $\mathbb{D}^{+}\partial_{\mu}H)] + \frac{1}{2}g\frac{1}{c_{w}}(Z_{\mu}^{0}(H\partial_{\mu}\mathbb{D}^{0} - \mathbb{D}^{0}\partial_{\mu}H) - ig\frac{s_{w}^{2}}{c_{w}}MZ_{\mu}^{0}(W_{\mu}^{+}\mathbb{D}^{-} - W_{\mu}^{-}\mathbb{D}^{+}) +$ $igs_w MA_\mu (W_\mu^+ \bar{\mathbb{D}}^- - W_\mu^- \bar{\mathbb{D}}^+) - ig\frac{1-2c_w^2}{2c_w} Z_\mu^0 (\bar{\mathbb{D}}^+ \partial_\mu \bar{\mathbb{D}}^- - \bar{\mathbb{D}}^- \partial_\mu \bar{\mathbb{D}}^+) +$ $a_j^{\wedge}(\gamma\partial + m_d^{\wedge})a_j^{\wedge} + igs_wA_{\mu}[-(\bar{e}^{\wedge}\gamma^{\mu}e^{\wedge}) + \frac{\pi}{3}(\bar{u}_j^{\wedge}\gamma^{\mu}u_j^{\wedge}) - \frac{\pi}{3}(\bar{u}_j^{\wedge}\gamma^{\mu}u_j^{\wedge})] +$ $\frac{ig}{4c_w}Z_{\mu}^0[(\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda})+(\bar{e}^{\lambda}\gamma^{\mu}(4s_w^2-1-\gamma^5)e^{\lambda})+(\bar{u}_j^{\lambda}\gamma^{\mu}(\frac{4}{3}s_w^2-1)e^{\lambda})$ $(1-\gamma^5)u_i^{\lambda}) + (\bar{d}_i^{\lambda}\gamma^{\mu}(1-\frac{8}{3}s_w^2-\gamma^5)d_i^{\lambda})] + \frac{ig}{2\sqrt{2}}W_{\mu}^+[(\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^5)e^{\lambda}) +$ $(\bar{u}_{j}^{\lambda}\gamma^{\mu}(1+\gamma^{5})C_{\lambda\kappa}d_{j}^{\kappa})] + \frac{ig}{2\sqrt{2}}W_{\mu}^{-}[(\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda}) + (\bar{d}_{j}^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda})]$ $[\gamma^5]u_j^{\lambda}]$ + $\frac{ig}{2\sqrt{2}}\frac{m_{\lambda}^2}{M}[-\Box^+(\bar{\nu}^{\lambda}(1-\gamma^5)e^{\lambda}) + \Box^-(\bar{e}^{\lambda}(1+\gamma^5)\nu^{\lambda})]$ - $\frac{g}{2}\frac{m_e^{\lambda}}{M}[H(\bar{e}^{\lambda}e^{\lambda}) + i\bar{\mathbb{D}}^0(\bar{e}^{\lambda}\gamma^5e^{\lambda})] + \frac{ig}{2M\sqrt{2}}\bar{\mathbb{D}}^+[-m_d^{\kappa}(\bar{u}_i^{\lambda}C_{\lambda\kappa}(1-\gamma^5)d_i^{\kappa}) +$ $m_u^{\lambda}(\bar{u}_j^{\lambda}C_{\lambda\kappa}(1+\gamma^5)d_j^{\kappa}] + \frac{ig}{2M\sqrt{2}}\tilde{\mathbb{D}}^-[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^5)u_j^{\kappa})]$ $\gamma^5 u_i^{\kappa} = \frac{g}{2} \frac{m_u^{\lambda}}{M} H(\bar{u}_i^{\lambda} u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} H(\bar{d}_i^{\lambda} d_i^{\lambda}) + \frac{ig}{2} \frac{m_u^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) + \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) + \frac{g}{2} \frac{m_$ $\frac{ig}{2}\frac{m_d^{\lambda}}{M}\tilde{\epsilon}^0(\bar{d}_i^{\lambda}\gamma^5d_i^{\lambda}) + \bar{X}^+(\partial^2 - M^2)X^+ + \bar{X}^-(\partial^2 - M^2)X^- + \bar{X}^0(\partial^2 - M^2)X^ \frac{M^2}{c^2}$ $X^0 + Y \partial^2 Y + igc_w W_u^+ (\partial_u X^0 X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^-$ $\partial_{\mu}\bar{X}^{+}Y$) + $igc_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}X^{0} - \partial_{\mu}\bar{X}^{0}X^{+}) + igs_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}Y - igs_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}Y - igs_{w}W_{\mu}^{-}))$ $\partial_u \bar{Y} X^+$) + $igc_w Z_u^0 (\partial_u \bar{X}^+ X^+ - \partial_u \bar{X}^- X^-) + igs_w A_u (\partial_u \bar{X}^+ X^+ - \partial_u \bar{X}^- X^-)$ $\partial_{\mu}\bar{X}^{-}X^{-}$) $-\frac{1}{2}gM[\bar{X}^{+}X^{+}H + \bar{X}^{-}X^{-}H + \frac{1}{c^{2}}\bar{X}^{0}X^{0}H] +$ $\frac{1-2c_{w}^{2}}{2c_{w}}igM[\bar{X}^{+}X^{0}\mathbb{D}^{+}-\bar{X}^{-}X^{0}\mathbb{D}^{-}]+\frac{1}{2c_{w}}igM[\bar{X}^{0}X^{-}\mathbb{D}^{+}-\bar{X}^{0}X^{+}\mathbb{D}^{-}]+$ $igMs_w[X^0X^-\mathfrak{D}^+ - X^0X^+\mathfrak{D}^-] + \frac{1}{2}igM[X^+X^+\mathfrak{D}^0 - X^-X^-\mathfrak{D}^0]$

$SU(3) \times SU(2)_L \times U(1)_Y$



 $\mathcal{L}_{SM} = -\frac{1}{2} \partial_{\nu} g^a_{\mu} \partial_{\nu} g^a_{\mu} - g_s f^{abc} \partial_{\mu} g^a_{\nu} g^b_{\mu} g^c_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{ade} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} +$ $\frac{1}{2}ig_s^2(\bar{q}_i^{\sigma}\gamma^{\mu}q_i^{\sigma})g_u^a + \bar{G}^a\partial^2 G^a + g_sf^{abc}\partial_{\mu}\bar{G}^a\bar{G}^bg_u^c - \partial_{\nu}W_{\mu}^+\partial_{\nu}W_{\mu}^- M^2W_{\mu}^+W_{\mu}^- - \frac{1}{2}\partial_{\nu}Z_{\mu}^0\partial_{\nu}Z_{\mu}^0 - \frac{1}{2c^2}M^2Z_{\mu}^0Z_{\mu}^0 - \frac{1}{2}\partial_{\mu}A_{\nu}\partial_{\mu}A_{\nu} - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H - \frac{1}{2}\partial_{\mu}H\partial_{$ $\frac{1}{2}m_{h}^{2}H^{2} - \partial_{\mu}\mathbb{D}^{+}\partial_{\mu}\mathbb{D}^{-} - M^{2}\mathbb{D}^{+}\mathbb{D}^{-} - \frac{1}{2}\partial_{\mu}\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{0} - \frac{1}{2\sigma^{2}}M\mathbb{D}^{0}\mathbb{D}^{0} - \beta_{h}[\frac{2M^{2}}{\sigma^{2}} + \frac{1}{2}\partial_{\mu}\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{0}] - \frac{1}{2\sigma^{2}}M\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{0} - \beta_{h}[\frac{2M^{2}}{\sigma^{2}} + \frac{1}{2}\partial_{\mu}\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{0}] - \frac{1}{2}\partial_{\mu}\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{0} - \frac{1}{2}\partial_{\mu}\mathbb{D}^{0} - \frac{1}{2}\partial_{\mu}\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{0} - \frac{1}{2}\partial_{\mu}\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{0} - \frac{1}{2}\partial_{\mu}\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{0} - \frac{1}{2}\partial_{\mu}\mathbb{D}^{0} - \frac{1}{2}\partial_{\mu}\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{0} -$ $\frac{2M}{g}H + \frac{1}{2}(H^2 + \mathbb{D}^0\mathbb{D}^0 + 2\mathbb{D}^+\mathbb{D}^-)] + \frac{2M^4}{g^2}\alpha_h - igc_w[\partial_\nu Z_\mu^0(W_\mu^+W_\nu^- - W_\mu^-)]$ $W_{\nu}^{+}W_{\mu}^{-}) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{-})$ $W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}W_{\mu}^{-})]$ $W_{u}^{-}\partial_{\nu}W_{u}^{+}) + A_{u}(W_{\nu}^{+}\partial_{\nu}W_{u}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - \frac{1}{2}g^{2}W_{\mu}^{+}W_{\nu}^{-}W_{\nu}^{+}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\nu}^{-}W_{\nu}^{+}W_{\nu}^{-}W_{\nu$ $\frac{1}{2}g^2W_{\mu}^+W_{\nu}^-W_{\mu}^+W_{\nu}^- + g^2c_w^2(Z_{\mu}^0W_{\mu}^+Z_{\nu}^0W_{\nu}^- - Z_{\mu}^0Z_{\mu}^0W_{\nu}^+W_{\nu}^-) +$ $g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-) + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\mu^- W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\mu^- W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^-]] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu Z_\mu^0 (W_\mu^- - A_\mu^- W_\mu^- - A_\mu^0 (W_\mu^- - A_\mu^- W_\mu^- - A_\mu^- W_\mu^- - A_\mu^- W_\mu^- (W_\mu^- - A_\mu^- W_\mu^- - A_\mu^- W_\mu^- - A_\mu^- W_\mu^$ $W_{\nu}^{+}W_{\mu}^{-}$) $-2A_{\mu}Z_{\mu}^{0}W_{\nu}^{+}W_{\nu}^{-}$] $-g\alpha[H^{3}+H\mathfrak{D}^{0}\mathfrak{D}^{0}+2H\mathfrak{D}^{+}\mathfrak{D}^{-}] \frac{1}{9}g^{2}\alpha_{h}[H^{4}+(\mathbb{D}^{0})^{4}+4(\mathbb{D}^{+}\mathbb{D}^{-})^{2}+4(\mathbb{D}^{0})^{2}\mathbb{D}^{+}\mathbb{D}^{-}+4H^{2}\mathbb{D}^{+}\mathbb{D}^{-}+2(\mathbb{D}^{0})^{2}H^{2}]$ $gMW_{\mu}^{+}W_{\mu}^{-}H - \frac{1}{2}g\frac{M}{c^{2}}Z_{\mu}^{0}Z_{\mu}^{0}H - \frac{1}{2}ig[W_{\mu}^{+}(\tilde{\mathbb{D}}^{0}\partial_{\mu}\tilde{\mathbb{D}}^{-} - \tilde{\mathbb{D}}^{-}\partial_{\mu}\tilde{\mathbb{D}}^{0}) W_{\mu}^{-}(\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{+}-\mathbb{D}^{+}\partial_{\mu}\mathbb{D}^{0})]+\frac{1}{2}g[W_{\mu}^{+}(H\partial_{\mu}\mathbb{D}^{-}-\mathbb{D}^{-}\partial_{\mu}H)-W_{\mu}^{-}(H\partial_{\mu}\mathbb{D}^{+}-\mathbb{D}^{-}\partial_{\mu}H)]$ $\mathbb{D}^{+}\partial_{\mu}H)] + \frac{1}{2}g\frac{1}{c_{w}}(Z_{\mu}^{0}(H\partial_{\mu}\mathbb{D}^{0} - \mathbb{D}^{0}\partial_{\mu}H) - ig\frac{s_{w}^{2}}{c_{w}}MZ_{\mu}^{0}(W_{\mu}^{+}\mathbb{D}^{-} - W_{\mu}^{-}\mathbb{D}^{+}) +$ $igs_w MA_\mu (W_\mu^+ \bar{\mathbb{D}}^- - W_\mu^- \bar{\mathbb{D}}^+) - ig\frac{1-2c_w^2}{2c_w} Z_\mu^0 (\bar{\mathbb{D}}^+ \partial_\mu \bar{\mathbb{D}}^- - \bar{\mathbb{D}}^- \partial_\mu \bar{\mathbb{D}}^+) +$ $a_j^{\wedge}(\gamma\partial + m_d^{\wedge})a_j^{\wedge} + igs_wA_{\mu}[-(\bar{e}^{\wedge}\gamma^{\mu}e^{\wedge}) + \frac{\pi}{3}(\bar{u}_j^{\wedge}\gamma^{\mu}u_j^{\wedge}) - \frac{\pi}{3}(\bar{u}_j^{\wedge}\gamma^{\mu}u_j^{\wedge})] +$ $\frac{ig}{4c_m}Z_{\mu}^0[(\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda})+(\bar{e}^{\lambda}\gamma^{\mu}(4s_w^2-1-\gamma^5)e^{\lambda})+(\bar{u}_j^{\lambda}\gamma^{\mu}(\frac{4}{3}s_w^2-1)e^{\lambda})]$ $(1 - \gamma^5)u_j^{\lambda}) + (\bar{d}_j^{\lambda}\gamma^{\mu}(1 - \frac{8}{3}s_w^2 - \gamma^5)d_j^{\lambda})] + \frac{ig}{2\sqrt{2}}W_{\mu}^+[(\bar{\nu}^{\lambda}\gamma^{\mu}(1 + \gamma^5)e^{\lambda}) + (\bar{d}_j^{\lambda}\gamma^{\mu}(1 + \gamma^5)e^{\lambda})]$ $(\bar{u}_{j}^{\lambda}\gamma^{\mu}(1+\gamma^{5})C_{\lambda\kappa}d_{j}^{\kappa})] + \frac{ig}{2\sqrt{2}}W_{\mu}^{-}[(\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda}) + (\bar{d}_{j}^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda})]$ $[\gamma^5]u_j^{\lambda}]$ + $\frac{ig}{2\sqrt{2}}\frac{m_{\lambda}^2}{M}[-\Box^+(\bar{\nu}^{\lambda}(1-\gamma^5)e^{\lambda}) + \Box^-(\bar{e}^{\lambda}(1+\gamma^5)\nu^{\lambda})]$ - $\frac{g}{2}\frac{m_e^{\lambda}}{M}[H(\bar{e}^{\lambda}e^{\lambda}) + i\bar{\mathbb{D}}^0(\bar{e}^{\lambda}\gamma^5e^{\lambda})] + \frac{ig}{2M\sqrt{2}}\bar{\mathbb{D}}^+[-m_d^{\kappa}(\bar{u}_i^{\lambda}C_{\lambda\kappa}(1-\gamma^5)d_i^{\kappa}) +$ $m_u^{\lambda}(\bar{u}_j^{\lambda}C_{\lambda\kappa}(1+\gamma^5)d_j^{\kappa}] + \frac{ig}{2M\sqrt{2}}\tilde{\mathbb{D}}^-[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^5)u_j^{\kappa})]$ $\gamma^5 u_i^{\kappa} = \frac{g}{2} \frac{m_u^{\lambda}}{M} H(\bar{u}_i^{\lambda} u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} H(\bar{d}_i^{\lambda} d_i^{\lambda}) + \frac{ig}{2} \frac{m_u^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) + \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} \mathcal{D}^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) + \frac{g}{2} \frac{m_$ $\frac{ig}{2}\frac{m_d^{\lambda}}{M}\tilde{\epsilon}^0(\bar{d}_i^{\lambda}\gamma^5d_i^{\lambda}) + \bar{X}^+(\partial^2 - M^2)X^+ + \bar{X}^-(\partial^2 - M^2)X^- + \bar{X}^0(\partial^2 - M^2)X^ \frac{M^2}{c^2}$ $X^0 + Y \partial^2 Y + igc_w W_u^+ (\partial_u X^0 X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^+ X^0) + igs_w W_u^+ (\partial_u Y X^- - \partial_u X^-$ $\partial_{\mu}\bar{X}^{+}Y$) + $igc_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}X^{0} - \partial_{\mu}\bar{X}^{0}X^{+}) + igs_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}Y - igs_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}Y - igs_{w}W_{\mu}^{-}))$ $\partial_u \bar{Y} X^+$) + $igc_w Z_u^0 (\partial_u \bar{X}^+ X^+ - \partial_u \bar{X}^- X^-) + igs_w A_u (\partial_u \bar{X}^+ X^+ - \partial_u \bar{X}^- X^-)$ $\partial_{\mu}\bar{X}^{-}X^{-}$) $-\frac{1}{2}gM[\bar{X}^{+}X^{+}H + \bar{X}^{-}X^{-}H + \frac{1}{c^{2}}\bar{X}^{0}X^{0}H] +$ $\frac{1-2c_{w}^{2}}{2c_{w}}igM[\bar{X}^{+}X^{0}\mathbb{D}^{+}-\bar{X}^{-}X^{0}\mathbb{D}^{-}]+\frac{1}{2c_{w}}igM[\bar{X}^{0}X^{-}\mathbb{D}^{+}-\bar{X}^{0}X^{+}\mathbb{D}^{-}]+$ $igMs_w[X^0X^-\mathfrak{D}^+ - X^0X^+\mathfrak{D}^-] + \frac{1}{2}igM[X^+X^+\mathfrak{D}^0 - X^-X^-\mathfrak{D}^0]$

$$SU(3) \times SU(2)_L \times U(1)_Y$$

Only left handed fields feel the weak force;
It is parity violating

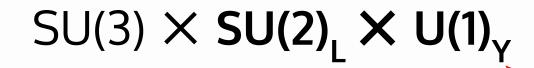
$$SU(3) \times SU(2)_L \times U(1)_Y$$

$$\Psi \rightarrow \Psi_L + \Psi_R$$

e.g. for electrons...

$$e \rightarrow e_1 + e_R$$

Forces you to write down your theory in left- and right- chiral components



Y is "weak hypercharge", a quantum number

If electroweak gauge invariance holds, \mathbf{Y} is conserved \rightarrow has to be zero for all terms of the SM Lagrangian

$$SU(3) \times SU(2)_L \times U(1)_Y$$

$$L_{SM} = ... + \sim e_L \overline{e}_R$$

Not allowed!

e, has hypercharge -1

e_R has hypercharge +2

Y is "weak hypercharge", a quantum number

If electroweak gauge invariance holds, \mathbf{Y} is conserved \rightarrow has to be zero for all terms of the SM Lagrangian

Mass in the Context of the SM



What does it mean for something to have "mass"?

• **Rest energy**! → Ignore *kinetic* terms in Lagrangian

 $\mathcal{L}_{SM} = -\frac{1}{2} \partial_{\nu} g^a_{\mu} \partial_{\nu} g^a_{\mu} - g_s f^{abc} \partial_{\mu} g^a_{\nu} g^b_{\mu} g^c_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{ade} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} +$ $\frac{1}{2}ig_s^2(\bar{q}_i^{\sigma}\gamma^{\mu}q_i^{\sigma})g_u^a + \bar{G}^a\partial^2 G^a + g_sf^{abc}\partial_{\mu}\bar{G}^a\bar{G}^bg_u^c - \partial_{\nu}W_{\mu}^+\partial_{\nu}W_{\mu}^- M^2W_{\mu}^+W_{\mu}^- - \frac{1}{2}\partial_{\nu}Z_{\mu}^0\partial_{\nu}Z_{\mu}^0 - \frac{1}{2c^2}M^2Z_{\mu}^0Z_{\mu}^0 - \frac{1}{2}\partial_{\mu}A_{\nu}\partial_{\mu}A_{\nu} - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H \frac{1}{2}m_{h}^{2}H^{2} - \partial_{\mu}\mathbb{D}^{+}\partial_{\mu}\mathbb{D}^{-} - M^{2}\mathbb{D}^{+}\mathbb{D}^{-} - \frac{1}{2}\partial_{\mu}\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{0} - \frac{1}{2c^{2}}M\mathbb{D}^{0}\mathbb{D}^{0} - \beta_{h}[\frac{2M^{2}}{c^{2}} +$ $\frac{2M}{a}H + \frac{1}{2}(H^2 + \tilde{\mathbb{D}}^0\tilde{\mathbb{D}}^0 + 2\tilde{\mathbb{D}}^+\tilde{\mathbb{D}}^-)] + \frac{2M^4}{a^2}\alpha_h - igc_w[\partial_\nu Z_\mu^0(W_\mu^+W_\nu^- - W_\mu^-)]$ $W_{\nu}^{+}W_{\mu}^{-}) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{-})$ $W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}W_{\mu}^{-})]$ $W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + A_{\mu}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{+}W_{\nu}^{-} +$ $\frac{1}{2}g^2W_{\mu}^+W_{\nu}^-W_{\mu}^+W_{\nu}^- + g^2c_w^2(Z_{\mu}^0W_{\mu}^+Z_{\nu}^0W_{\nu}^- - Z_{\mu}^0Z_{\mu}^0W_{\nu}^+W_{\nu}^-)$ $g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-) + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^- W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\mu^- W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu Z_\mu^0 (W_\mu^+ W_\mu^-)]] + g^2 s_w c_w [A_\mu Z_\mu^0 (W_\mu^+ W_\mu^- - A_\mu Z_\mu^0 (W_\mu^+ W_\mu^-)]] + g^2 s_w c_w [A_\mu Z_\mu^0 (W_\mu^+ W_\mu^- - A_\mu Z_\mu^0 (W_\mu^+ W_\mu^-)]] + g^2 s_w c_w [A_\mu Z_\mu^0 (W_\mu^+ W_\mu^- W_\mu^- - A_\mu Z_\mu^0 (W_\mu^- W_\mu^- W_\mu^-)]] + g^2 s_w c_w [A_\mu Z_\mu^0 (W_\mu^- W_\mu^- W_\mu^-$ $W_{\nu}^{+}W_{\mu}^{-}$) $-2A_{\mu}Z_{\mu}^{0}W_{\nu}^{+}W_{\nu}^{-}$] $-g\alpha[H^{3}+H\bar{D}^{0}\bar{D}^{0}+2H\bar{D}^{+}\bar{D}^{-}]$ $\frac{1}{5}g^{2}\alpha_{h}[H^{4}+(\mathbb{D}^{0})^{4}+4(\mathbb{D}^{+}\mathbb{D}^{-})^{2}+4(\mathbb{D}^{0})^{2}\mathbb{D}^{+}\mathbb{D}^{-}+4H^{2}\mathbb{D}^{+}\mathbb{D}^{-}+2(\mathbb{D}^{0})^{2}H^{2}]$ $gMW_{\mu}^{+}W_{\mu}^{-}H - \frac{1}{2}g\frac{M}{c_{+}^{2}}Z_{\mu}^{0}Z_{\mu}^{0}H - \frac{1}{2}ig[W_{\mu}^{+}(\mathfrak{D}^{0}\partial_{\mu}\mathfrak{D}^{-} - \mathfrak{D}^{-}\partial_{\mu}\mathfrak{D}^{0}) W_{u}^{-}(\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{+}-\mathbb{D}^{+}\partial_{\mu}\mathbb{D}^{0})]+\frac{1}{2}g[W_{\mu}^{+}(H\partial_{\mu}\mathbb{D}^{-}-\mathbb{D}^{-}\partial_{\mu}H)-W_{\mu}^{-}(H\partial_{\mu}\mathbb{D}^{+}-\mathbb{D}^{+}\partial_{\mu}H)]+W_{\mu}^{-}(H\partial_{\mu}H)+W_{\mu}^{-}(H\partial_{\mu$ $\mathbb{D}^{+}\partial_{\mu}H)] + \frac{1}{2}g\frac{1}{c_{m}}(Z^{0}_{\mu}(H\partial_{\mu}\mathbb{D}^{0} - \mathbb{D}^{0}\partial_{\mu}H) - ig\frac{s^{2}_{m}}{c_{m}}MZ^{0}_{\mu}(W^{+}_{\mu}\mathbb{D}^{-} - W^{-}_{\mu}\mathbb{D}^{+}) +$ $igs_w M A_\mu (W_\mu^+ \bar{\mathbb{D}}^- - W_\mu^- \bar{\mathbb{D}}^+) - ig \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\bar{\mathbb{D}}^+ \partial_\mu \bar{\mathbb{D}}^- - \bar{\mathbb{D}}^- \partial_\mu \bar{\mathbb{D}}^+) +$

$$H^2 = (\mathbb{S}^0)^2 + 2(2s_w^2 - 12\mathfrak{S}^+ \mathfrak{S}^-) = \frac{1}{2}s_w^2 \frac{2s_w^2}{2}$$

 $\frac{1}{2}ig = Z_\mu^0 H \frac{1}{2} - - - - - \frac{1}{\mu} \mathfrak{S}^+) = \frac{1}{2}g^* V_\mu$
 $f^2 = V_\mu H \frac{1}{2} - - V_\mu H_\mu + \frac{1}{2}g^* V_\mu$

 $\begin{array}{l} \frac{d_{j}(\gamma \partial + m_{d})d_{j} + igs_{w}A_{\mu}[-(e^{\lambda}\gamma^{\mu}e^{\lambda}) + \frac{1}{3}(u_{j}\gamma^{\mu}u_{j}) - \frac{1}{3}(\bar{d}_{j}\gamma^{\mu}u_{j})] +}{\frac{ig}{4c_{w}}Z_{\mu}^{0}[(\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda}) + (\bar{e}^{\lambda}\gamma^{\mu}(4s_{w}^{2}-1-\gamma^{5})e^{\lambda}) + (\bar{u}_{j}^{\lambda}\gamma^{\mu}(\frac{4}{3}s_{w}^{2}-1-\gamma^{5})u_{j}^{\lambda}) + (\bar{d}_{j}^{\lambda}\gamma^{\mu}(1-\frac{8}{3}s_{w}^{2}-\gamma^{5})d_{j}^{\lambda})] + \frac{ig}{2\sqrt{2}}W_{\mu}^{+}[(\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^{5})e^{\lambda}) + (\bar{u}_{j}^{\lambda}\gamma^{\mu}(1+\gamma^{5})C_{\lambda\kappa}d_{j}^{\kappa})] + \frac{ig}{2\sqrt{2}}W_{\mu}^{-}[(\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda}) + (\bar{d}_{j}^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^{5})u_{j}^{\lambda})] + \frac{ig}{2\sqrt{2}}\frac{M}{M}[-(\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^{5})e^{\lambda}) + \bar{e}^{-(\bar{e}^{\lambda}(1+\gamma^{5})\nu^{\lambda})] - \frac{g}{2}\frac{m_{k}^{\lambda}}{M}[H(\bar{e}^{\lambda}e^{\lambda}) + i\bar{\mathcal{D}}^{0}(\bar{e}^{\lambda}\gamma^{5}e^{\lambda})] + \frac{ig}{2\sqrt{2}}\bar{\mathcal{D}}^{-}[m_{d}^{\lambda}(\bar{d}_{j}^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^{5})u_{j}^{\kappa}) - m_{u}^{\kappa}(\bar{d}_{j}^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^{5})d_{j}^{\kappa}) + m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})u_{j}^{\lambda}) - \frac{g}{2}\frac{m_{d}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda}) - \frac{g}{2}\frac{m_{d}^{\lambda}}{M}H(\bar{d}_{j}^{\lambda}d_{j}^{\lambda}) + \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\bar{\mathcal{D}}^{0}(\bar{u}_{j}^{\lambda}\gamma^{5}u_{j}^{\lambda}) - \frac{ig}{2}\frac{m_{d}^{\lambda}}{M}\bar{\mathcal{D}}^{0}(\bar{d}_{j}^{\lambda}\gamma^{5}d_{j}^{\lambda}) + \bar{X}^{+}(\partial^{2}-M^{2})X^{+} + \bar{X}^{-}(\partial^{2}-M^{2})X^{-} + \bar{X}^{0}(\partial^{2}-\bar{u}_{j}^{\lambda}) + \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\bar{\mathcal{D}}^{0}(\bar{d}_{j}^{\lambda}\gamma^{5}d_{j}^{\lambda}) + \bar{X}^{+}(\partial^{2}-M^{2})X^{+} + \bar{X}^{-}(\partial^{2}-M^{2})X^{-} + \bar{X}^{0}(\partial^{2}-\bar{u}_{j}^{\lambda}) + \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\bar{\mathcal{D}}^{0}(\bar{d}_{j}^{\lambda}\gamma^{5}d_{j}^{\lambda}) + \bar{X}^{+}(\partial^{2}-M^{2})X^{-} + \bar{X}^{0}(\partial^{2}-\bar{u}_{j}^{\lambda}) + \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\bar{\mathcal{D}}^{0}(\bar{d}_{j}^{\lambda}\gamma^{5}d_{j}^{\lambda}) + \bar{X}^{+}(\partial^{2}-M^{2})X^{-} + \bar{X}^{0}(\partial^{2}-\bar{u}_{j}^{\lambda}) + \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\bar{\mathcal{D}}^{0}(\bar{u}_{j}^{\lambda}\gamma^{5}u_{j}^{\lambda}) - \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\bar{\mathcal{D}}^{0}(\bar{d}_{j}^{\lambda}\gamma^{5}u_{j}^{\lambda}) + \bar{X}^{-}(\partial^{2}-\bar{u}_{j}^{\lambda}) + \bar{X}^{-}(\partial^{2}-\bar{u}_{$

Mass in the Context of the SM



What does it mean for something to have "mass"?

Rest energy! → Ignore kinetic terms in Lagrangian

$$L_{SM} = ... + mc^2 (\overline{e}_L e_R + \overline{e}_R e_L)$$

 $\mathcal{L}_{SM} = -\frac{1}{2} \partial_{\nu} g^a_{\mu} \partial_{\nu} g^a_{\mu} - g_s f^{abc} \partial_{\mu} g^a_{\nu} g^b_{\mu} g^c_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{ade} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} +$ ${\textstyle\frac{1}{2}}ig_s^2(\bar{q}_i^\sigma\gamma^\mu q_i^\sigma)g_\mu^a + \bar{G}^a\partial^2G^a + g_sf^{abc}\partial_\mu\bar{G}^a\bar{G}^bg_\mu^c - \partial_\nu W_\mu^+\partial_\nu W_\mu^- M^{2}W_{\mu}^{+}W_{\mu}^{-} - \frac{1}{2}\partial_{\nu}Z_{\mu}^{0}\partial_{\nu}Z_{\mu}^{0} - \frac{1}{2c^{2}}M^{2}Z_{\mu}^{0}Z_{\mu}^{0} - \frac{1}{2}\partial_{\mu}A_{\nu}\partial_{\mu}A_{\nu} - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H$ $\frac{1}{2}m_h^2H^2 - \partial_{\mu}\mathbb{D}^+\partial_{\mu}\mathbb{D}^- - M^2\mathbb{D}^+\mathbb{D}^- - \frac{1}{2}\partial_{\mu}\mathbb{D}^0\partial_{\mu}\mathbb{D}^0 - \frac{1}{2c^2}M\mathbb{D}^0\mathbb{D}^0 - \beta_h[\frac{2M^2}{a^2} + \frac{1}{2}M^2]$ $\frac{2M}{g}H + \frac{1}{2}(H^2 + \mathbb{D}^0\mathbb{D}^0 + 2\mathbb{D}^+\mathbb{D}^-)] + \frac{2M^4}{g^2}\alpha_h - igc_w[\partial_\nu Z_\mu^0(W_\mu^+W_\nu^- - W_\mu^-)]$ $W_{\nu}^{+}W_{\mu}^{-}) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{-})$ $W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}W_{\mu}^{-})]$ $W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + A_{\mu}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{+}W_{\nu}^{-} +$ $\frac{1}{2}g^2W_{\mu}^+W_{\nu}^-W_{\mu}^+W_{\nu}^- + g^2c_w^2(Z_{\mu}^0W_{\mu}^+Z_{\nu}^0W_{\nu}^- - Z_{\mu}^0Z_{\mu}^0W_{\nu}^+W_{\nu}^-)$ $g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-) + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^- W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^- W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^- W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\nu^- W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - A_\mu A_\mu W_\mu^- W_\nu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^- W_\mu^-)] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^+ W_\mu^- - A_\mu A_\mu W_\mu^- W_\mu^- W_\mu^- W_\mu^-]] + g^2 s_w c_w [A_\mu Z_\nu^0 (W_\mu^- W_\mu^- W_\mu^-$ $W_{\nu}^{+}W_{\mu}^{-}$) $-2A_{\mu}Z_{\mu}^{0}W_{\nu}^{+}W_{\nu}^{-}$] $-g\alpha[H^{3}+H\mathfrak{D}^{0}\mathfrak{D}^{0}+2H\mathfrak{D}^{+}\mathfrak{D}^{-}]$ $\frac{1}{5}g^{2}\alpha_{h}[H^{4}+(\mathbb{D}^{0})^{4}+4(\mathbb{D}^{+}\mathbb{D}^{-})^{2}+4(\mathbb{D}^{0})^{2}\mathbb{D}^{+}\mathbb{D}^{-}+4H^{2}\mathbb{D}^{+}\mathbb{D}^{-}+2(\mathbb{D}^{0})^{2}H^{2}]$ $gMW_{\mu}^{+}W_{\mu}^{-}H - \frac{1}{2}g\frac{M}{c_{+}^{2}}Z_{\mu}^{0}Z_{\mu}^{0}H - \frac{1}{2}ig[W_{\mu}^{+}(\mathfrak{D}^{0}\partial_{\mu}\mathfrak{D}^{-} - \mathfrak{D}^{-}\partial_{\mu}\mathfrak{D}^{0}) W_{\mu}^{-}(\mathbb{D}^{0}\partial_{\mu}\mathbb{D}^{+}-\mathbb{D}^{+}\partial_{\mu}\mathbb{D}^{0})]+\frac{1}{2}g[W_{\mu}^{+}(H\partial_{\mu}\mathbb{D}^{-}-\mathbb{D}^{-}\partial_{\mu}H)-W_{\mu}^{-}(H\partial_{\mu}\mathbb{D}^{+}-\mathbb{D}^{-}\partial_{\mu}H)]$ $\mathbb{D}^{+}\partial_{\mu}H)] + \frac{1}{2}g\frac{1}{c_{m}}(Z^{0}_{\mu}(H\partial_{\mu}\mathbb{D}^{0} - \mathbb{D}^{0}\partial_{\mu}H) - ig\frac{s^{2}_{m}}{c_{m}}MZ^{0}_{\mu}(W^{+}_{\mu}\mathbb{D}^{-} - W^{-}_{\mu}\mathbb{D}^{+}) +$ $igs_w M A_\mu (W_\mu^+ \bar{\mathbb{D}}^- - W_\mu^- \bar{\mathbb{D}}^+) - ig \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\bar{\mathbb{D}}^+ \partial_\mu \bar{\mathbb{D}}^- - \bar{\mathbb{D}}^- \partial_\mu \bar{\mathbb{D}}^+) +$

$$\begin{array}{l} H^{2} = \frac{1}{2} \left(\frac{\mathbb{S}^{0}}{2} \right)^{2} + 2 \left(2 s_{w}^{2} - \frac{1}{2} \right)^{2} \frac{\mathbb{S}^{2}}{2} \left(\frac{\mathbb{S}^{0}}{2} \right)^{2} + 2 \left(\frac{\mathbb{S}^{0}}{2} \right)^{2} \frac{\mathbb{S}^{0}}{2} \left(\frac{\mathbb{S}^{0}}{2} \right)^{2} \frac{\mathbb{S}^{0}}{2$$

 $\begin{array}{l} d_{j}(\gamma \partial + m_{d}) d_{j} + i g s_{w} A_{\mu} [-(e^{\lambda} \gamma^{\mu} e^{\lambda}) + \frac{1}{2} (u_{j} \gamma^{\mu} u_{j}) - \frac{1}{3} (u_{j}^{\lambda} \gamma^{\mu} u_{j}^{\lambda})] + \\ \frac{i g}{4 c_{w}} Z_{0}^{\mu} [(\bar{\nu}^{\lambda} \gamma^{\mu} (1 + \gamma^{5}) \nu^{\lambda}) + (\bar{e}^{\lambda} \gamma^{\mu} (4 s_{w}^{2} - 1 - \gamma^{5}) e^{\lambda}) + (\bar{u}_{j}^{\lambda} \gamma^{\mu} (\frac{1}{3} s_{w}^{2} - 1 - \gamma^{5}) u_{j}^{\lambda}) + (\bar{d}_{j}^{\lambda} \gamma^{\mu} (1 - \frac{8}{3} s_{w}^{2} - \gamma^{5}) d_{j}^{\lambda})] + \frac{i g}{2 \sqrt{2}} W_{\mu}^{+} [(\bar{\nu}^{\lambda} \gamma^{\mu} (1 + \gamma^{5}) e^{\lambda}) + (\bar{u}_{j}^{\lambda} \gamma^{\mu} (1 + \gamma^{5}) e^{\lambda}) + (\bar{u}_{j}^{\lambda} \gamma^{\mu} (1 + \gamma^{5}) \nu_{\lambda}^{\lambda})] + \frac{i g}{2 \sqrt{2}} W_{\mu}^{-} [(\bar{e}^{\lambda} \gamma^{\mu} (1 + \gamma^{5}) \nu^{\lambda}) + (\bar{d}_{j}^{\kappa} C_{\lambda \kappa}^{\dagger} \gamma^{\mu} (1 + \gamma^{5}) u_{j}^{\lambda})] + \frac{i g}{2 \sqrt{2}} M_{\mu}^{\lambda} [H(\bar{e}^{\lambda} e^{\lambda}) + i \bar{\mathcal{O}}^{0} (\bar{e}^{\lambda} \gamma^{5} e^{\lambda})] + \frac{i g}{2 M \sqrt{2}} \bar{\mathcal{O}}^{+} [m_{d}^{\lambda} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa} (1 + \gamma^{5}) \nu^{\lambda})] - m_{u}^{\kappa} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa} (1 + \gamma^{5}) u_{j}^{\lambda}) + m_{u}^{\kappa} (\bar{u}_{j}^{\lambda} C_{\lambda \kappa} (1 + \gamma^{5}) d_{j}^{\kappa}) + \frac{i g}{2 M \sqrt{2}} \bar{\mathcal{O}}^{-} [m_{d}^{\lambda} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa} (1 + \gamma^{5}) u_{j}^{\kappa}) - m_{u}^{\kappa} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa}^{\lambda} (1 - \gamma^{5}) d_{j}^{\kappa}) + m_{u}^{\kappa} (\bar{u}_{j}^{\lambda} C_{\lambda \kappa} (1 + \gamma^{5}) u_{j}^{\kappa}) - m_{u}^{\kappa} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa}^{\lambda} (1 - \gamma^{5}) d_{j}^{\kappa}) + \frac{i g}{2 M \sqrt{2}} \bar{\mathcal{O}}^{-} [m_{d}^{\lambda} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa}^{\lambda} (1 + \gamma^{5}) u_{j}^{\kappa}) - m_{u}^{\kappa} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa}^{\lambda} (1 - \gamma^{5}) d_{j}^{\kappa}) + m_{u}^{\kappa} (\bar{u}_{j}^{\lambda} C_{\lambda \kappa} (1 + \gamma^{5}) u_{j}^{\kappa}) - m_{u}^{\kappa} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa}^{\lambda} (1 - \gamma^{5}) d_{j}^{\kappa}) + \frac{i g}{2 M \sqrt{2}} \bar{\mathcal{O}}^{-} [m_{d}^{\lambda} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa}^{\lambda} (1 + \gamma^{5}) u_{j}^{\kappa}) - m_{u}^{\kappa} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa}^{\lambda} (1 - \gamma^{5}) d_{j}^{\kappa}) + m_{u}^{\kappa} (\bar{u}_{j}^{\lambda} C_{\lambda \kappa} (1 + \gamma^{5}) u_{j}^{\kappa}) - m_{u}^{\kappa} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa}^{\lambda} (1 - \gamma^{5}) d_{j}^{\kappa}) + \frac{i g}{2 M \sqrt{2}} \bar{\mathcal{O}}^{-} m_{u}^{\kappa} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa}^{\lambda} (1 - \gamma^{5}) d_{j}^{\kappa}) + m_{u}^{\kappa} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa}^{\lambda} (1 - \gamma^{5}) d_{j}^{\kappa}) + \frac{i g}{2 M \sqrt{2}} \bar{\mathcal{O}}^{-} m_{u}^{\kappa} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa}^{\lambda} (1 + \gamma^{5}) u_{j}^{\kappa}) + m_{u}^{\kappa} (\bar{d}_{j}^{\lambda} C_{\lambda \kappa}^{\lambda} (1 - \gamma^{5}) d_{j}$

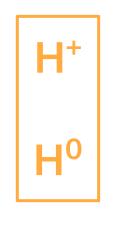
Electroweak Symmetry & The Higgs

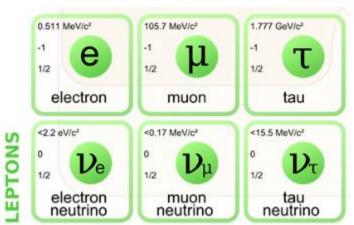


$SU(3) \times SU(2)_L \times U(1)_Y$

1. Postulate the existence of an SU(2) scalar doublet field "The Higgs field"







Electroweak Symmetry & The Higgs



$$SU(3) \times SU(2)_L \times U(1)_Y$$

1. Postulate the existence of an SU(2) scalar doublet

field "The Higgs field"

$$L_{SM} = ... + Y_c H (\overline{e}_L e_R + \overline{e}_R e_L)$$

Electro/\weak Sym/metry Brea\king (EWSB) nEX®

$$SU(3) \times SU(2)_L \times U(1)_Y$$

$$el_{ectroweak}$$
 $(low_{er}$ $el_{ectroweak}$ for_{ce} for_{ce}



$$SU(3) \times SU(2)_L \times U(1)_Y$$

2. Spontaneous Symmetry Breaking takes the Higgs doublet to a 0 and a constant vacuum expectation value, $\bf v$ (VEV)

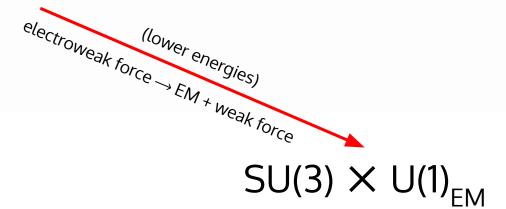
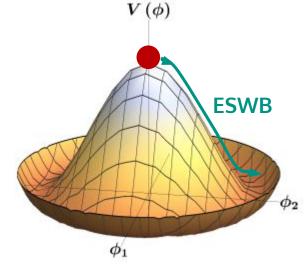


Image Credit: J.A. Gonzalez

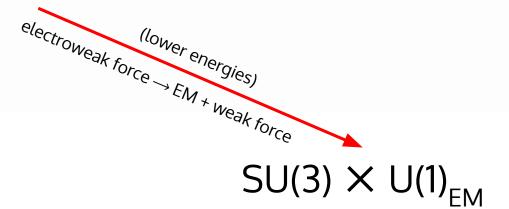


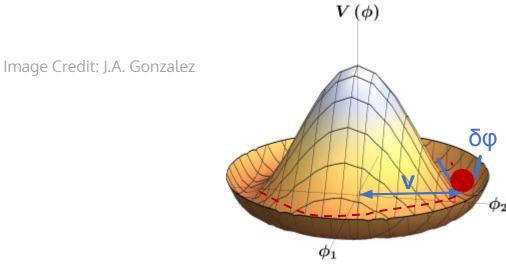
$$H \sim (\phi_1, \phi_2) \rightarrow (0, \mathbf{V} + \delta \phi)$$



$$SU(3) \times SU(2)_L \times U(1)_Y$$

2. **Spontaneous Symmetry Breaking** takes the Higgs doublet to a 0 and a constant vacuum expectation value, **v** (VEV)



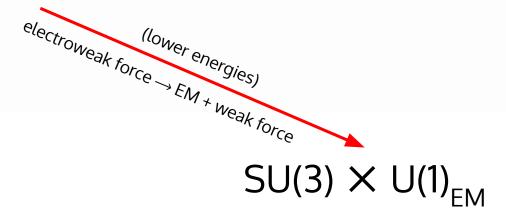


$$H \sim (\phi_1, \phi_2) \rightarrow (0, \mathbf{v} + \delta \phi)$$



$$SU(3) \times SU(2)_L \times U(1)_Y$$

$$L_{SM} = ... + Y_c H (\overline{e}_L e_R + \overline{e}_R e_L)$$

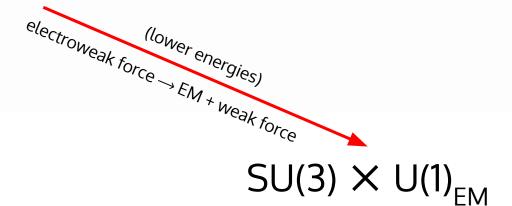




$$SU(3) \times SU(2)_{l} \times U(1)_{r}$$

$$L_{SM} = ... + Y_{c} H (\overline{e}_{L} e_{R} + \overline{e}_{R} e_{L})$$
EWSB

$$H \sim (\phi_1, \phi_2) \rightarrow (0, \mathbf{V} + \delta \phi)$$





$$SU(3) \times SU(2)_{l} \times U(1)_{r}$$

$$L_{SM} = ... + Y_c H (\overline{e}_L e_R + \overline{e}_R e_L)$$
EWSB

$$electroweak force \rightarrow EM + weak force$$

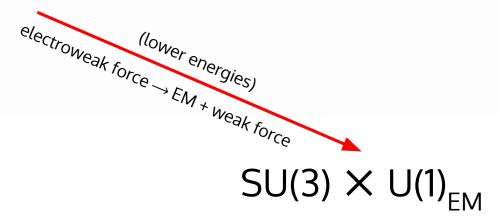
SU(3) \times U(1)_{EM}

$$H \sim (\phi_1, \phi_2) \rightarrow (0, \mathbf{v} + \delta \phi)$$

$$L_{SM} = ... + Y_{c} V (e_{L} \overline{e}_{R} + e_{R} \overline{e}_{L}) + Y_{c} \delta \phi (e_{L} \overline{e}_{R} + e_{R} \overline{e}_{L})$$



$$SU(3) \times SU(2)_{l} \times U(1)_{r}$$



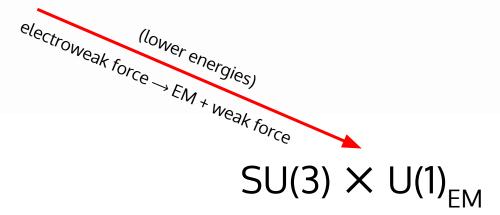
$$L_{SM} = ... + Y_{c} V (e_{L} \bar{e}_{R} + e_{R} \bar{e}_{L}) + Y_{c} \delta \phi (e_{L} \bar{e}_{R} + e_{R} \bar{e}_{L})$$

$$Coupling Constant * VEV$$

$$Coupling constant * fluctuation$$



$$SU(3) \times SU(2)_{l} \times U(1)_{r}$$



$$L_{SM} = ... + Y_{c} v (e_{L} \bar{e}_{R} + e_{R} \bar{e}_{L}) + Y_{c} h (e_{L} \bar{e}_{R} + e_{R} \bar{e}_{L})$$
this is a mass term!

this is an interaction term with the Higgs boson (h)!



$SU(3) \times SU(2)_L \times U(1)_Y$

Nobel Prize in Physics 1979



Photo from the Nobel Foundation archive. Sheldon Lee Glashow



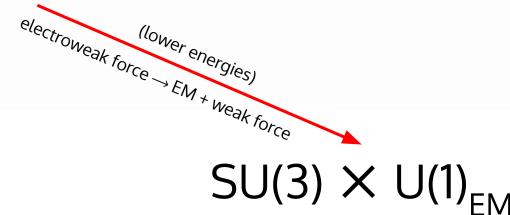
Foundation archive. Foundation archive. Abdus Salam Stev

Prize share: 1/3 Prize



Photo from the Nobel Foundation archive. Steven Weinberg Prize share: 1/3

The Nobel Prize in Physics 2013 Peter W. Higgs François Englert



Nobel Prize in Physics 1999



Martinus Veltman

Professor Emeritus at the University of
Michigan, Ann Arbor, USA, formerly at the
University of Utrecht, Utrecht, the Netherlands

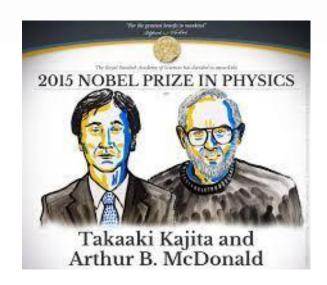


Gerardus 't Hooft
Professor at the University of Utrecht,
Utrecht, the Netherlands.

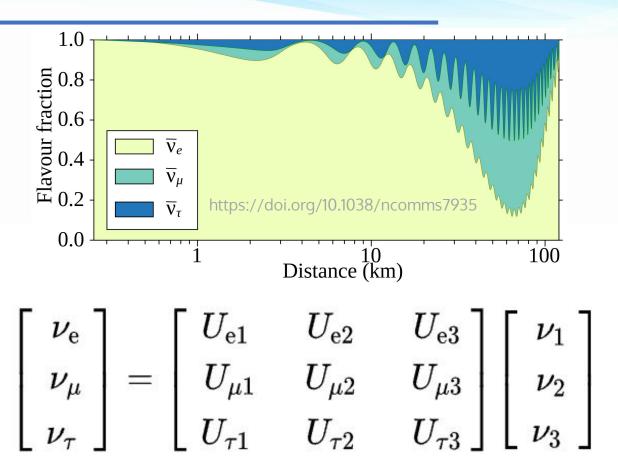
Neutrinos must have mass because they ~OSCILLATE~!



 Neutrino mass & flavour eigenstates are not the same, but related by a matrix



Solar neutrino problem: SOLVED

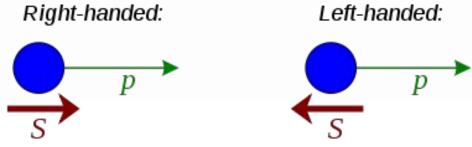


The Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix relates flavour and mass eigenstates of neutrinos

Where do neutrino masses come from?



• **Experimentally**: all neutrinos we've ever seen have left-handed helicity, and all anti-neutrinos are right-handed

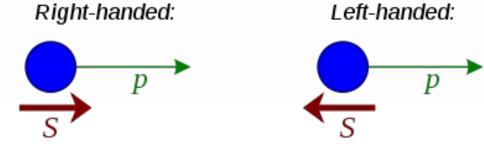


Where do neutrino masses come from?



• **Experimentally**: all neutrinos we've ever seen have left-handed helicity, and all anti-neutrinos are right-handed

Given the fact that **neutrinos are massive**, they **do not travel at** *c*



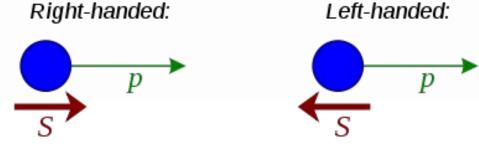
You can Lorentz boost into a frame where you will have the opposite helicity

Where do neutrino masses come from?



• **Experimentally**: all neutrinos we've ever seen have left-handed helicity, and all anti-neutrinos are right-handed

Given the fact that **neutrinos are massive**, they **do not travel at** *c*



You can Lorentz boost into a frame where you will have the opposite helicity

Neutrinos are neutral particles, so are neutrinos their own antiparticle (Majorana fermions)?

(neutrinos are almost always ultra relativistic, E >> m ... the limit where helicity \longleftrightarrow chirality)

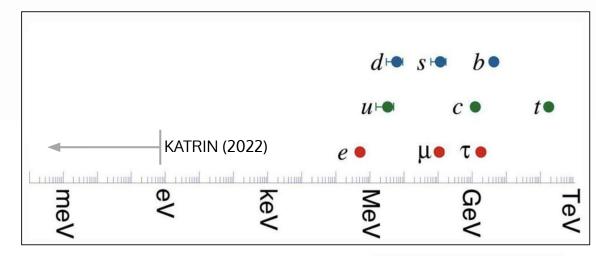
The Neutrino Mass Problem



Are neutrinos Dirac or Majorana fermions?

If Dirac: why is the coupling of neutrinos to the Higgs >10⁶ times smaller than that of the next lightest fermion?

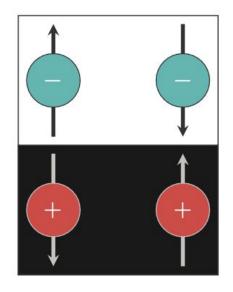
If Majorana: could this explain the smallness of neutrino masses?

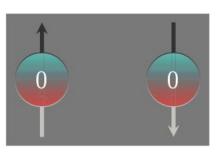


Standard Model Fermion masses / HITOSHI MURAYAMA (adapted)



- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator:
- Seesaw mechanisms:
- Matter vs Antimatter?





Credit: The State of the Art of Neutrino Physics



- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator: there is one unique way you can construct a next-leading-order operator in the SM using only SM particles.
- Seesaw mechanisms:
- Matter vs Antimatter?



- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator: there is one unique way you can construct a next-leading-order operator in the SM using only SM particles.
 - Naturally produces Majorana neutrinos & violates Lepton number conservation
- Seesaw mechanisms:
- Matter vs Antimatter?



- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator: there is one unique way you can construct a next-leading-order operator in the SM using only SM particles.
- Seesaw mechanisms:
- Matter vs Antimatter?

$$L_{real} \sim L_{SM} + L_{Weinberg}$$

$$L_{Weinberg} = Y_c / \Lambda \ \overline{L}_L \overline{\Phi} \Phi^{\dagger} L_L$$

 Λ : energy scale of new physics

Y_c: coupling constant

Φ: Higgs field



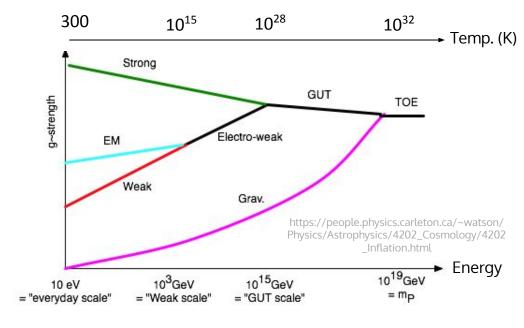
- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator: there is one unique way you can construct a next-leading-order operator in the SM using only SM particles.
- Seesaw mechanisms:
- Matter vs Antimatter?

$$L_{real} \sim L_{SM} + L_{Weinberg}$$

$$L_{Weinberg} = Y_c / \Lambda L_{\Phi} \Phi^{\dagger} L_{L}$$

 Λ : energy scale of new physics

Y_c: coupling constant Φ: Higgs field





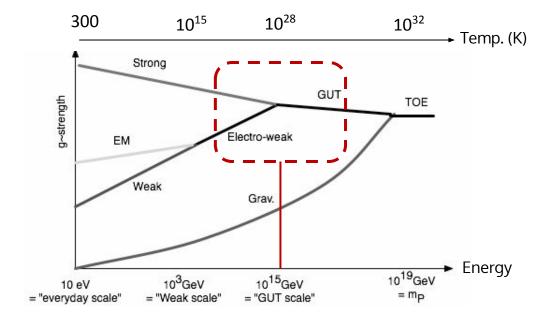
- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator: there is one unique way you can construct a next-leading-order operator in the SM using only SM particles.
- Seesaw mechanisms:
- Matter vs Antimatter?

$$L_{real} \sim L_{SM} + L_{Weinberg}$$

$$L_{Weinberg} = Y_c / \Lambda L_{\Phi} \Phi^{\dagger} L_{L}$$

 Λ : energy scale of new physics

Y_c: coupling constant Φ: Higgs field





- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator
- Seesaw mechanisms: having masses of neutrinos be contain both Dirac and Majorana terms give you a natural "seesaw" → allowing neutrino masses to be small
- Matter vs Antimatter?



m_D is the Dirac mass ~ VEV

- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator
- Seesaw mechanisms: having masses of neutrinos be contain both Dirac and Majorana terms give you a natural "seesaw" \rightarrow allowing neutrino masses to be small
- Matter vs Antimatter?

diagonalize the mass matrix to find mass eigenvalues $m_1=rac{m_D^2}{m_R-m_L}$ $m_1=m_R-m_L$ $m_2=m_R-m_L$

Do Majorana neutrinos help us?



- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator
- Seesaw mechanisms: having masses of neutrinos be both Dirac and Majorana neutrinos give you a natural "seesaw" forcing neutrino masses to be small
- Matter vs Antimatter?

 $m_1 = 0$ due to $SU(2)_1 \times U(1)_2$ gauge invariance

$$\mathscr{L}_m = rac{1}{2}((ar{
u}_L)^car{
u}_R)inom{
u_L}{m_D \quad m_R}inom{
u_L}{(
u_R)^c} + h.c.. \qquad \qquad m_1 = rac{m_D^2}{m_R - n_L} \ m_2 = m_R - n_L.$$

Do Majorana neutrinos help us?



- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator
- Seesaw mechanisms: having masses of neutrinos be both Dirac and Majorana neutrinos give you a natural "seesaw" forcing neutrino masses to be small

m₁ can be made *really* small if m_D << m_R

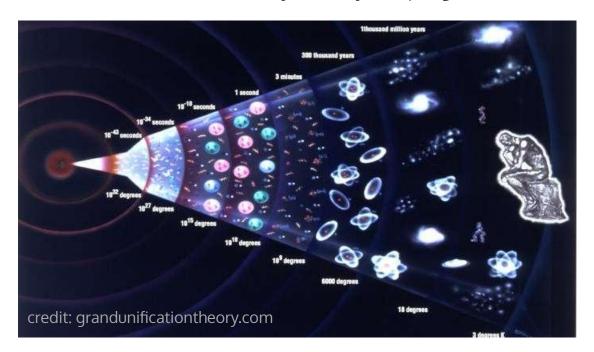
Matter vs Antimatter?

 $\mathscr{L}_m = rac{1}{2} ((ar{
u}_L)^c ar{
u}_R) egin{pmatrix} n_L & m_D \ m_D & m_R \end{pmatrix} egin{pmatrix}
u_L \ (
u_R)^c \end{pmatrix} + h. c. . & m_1 = rac{m_D^2}{m_R - n_L} \ m_2 = m_R - n_L. \end{cases}$

Do Majorana neutrinos help us?



- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator
- Seesaw mechanisms
- Matter vs Antimatter? Maybe m_R associated with Λ and are *really* heavy?
 - Possible explanation for the matter / antimatter asymmetry!! (leptogenesis)



But how can we test these ideas?



- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator
- Seesaw mechanisms
- Matter vs Antimatter?

NB: if neutrinos have masses ~meV, then Λ will be ~10¹² TeV

LHC \sqrt{s} energy is ~13 TeV: we should not expect to see this new physics at colliders in our lifetime!

But how can we test these ideas?



- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator
- Seesaw mechanisms
- Matter vs Antimatter?

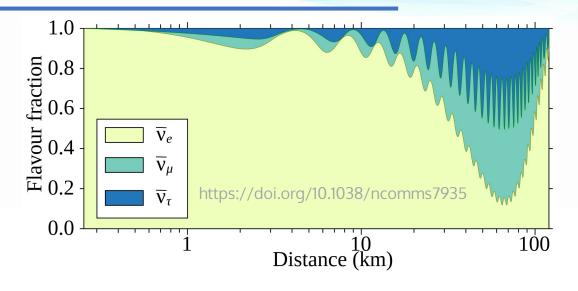
NB: if neutrinos have masses ~meV, then Λ will be ~10¹² TeV

LHC \sqrt{s} energy is ~13 TeV: we should not expect to see this new physics at colliders in our lifetime!

... so what do we do?

What can neutrino ~OSCILLATIONS~ tell us?





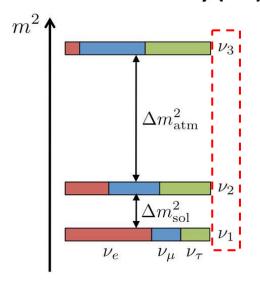
$$\left[egin{array}{c}
u_{
m e} \\
u_{\mu} \\
u_{ au} \end{array}
ight] = \left[egin{array}{ccc} U_{
m e1} & U_{
m e2} & U_{
m e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{ au 1} & U_{ au 2} & U_{ au 3} \end{array}
ight] \left[egin{array}{c}
u_1 \\
u_2 \\
u_3 \end{array}
ight]$$

The PMNS matrix relates flavour and mass eigenstates of neutrinos

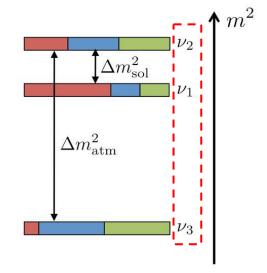
What can neutrino ~OSCILLATIONS~ tell us?

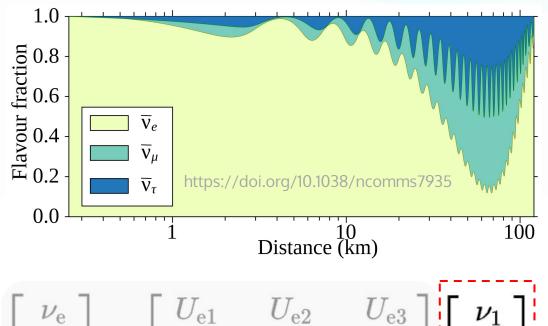


normal hierarchy (NH)



inverted hierarchy (IH)





$$\left[egin{array}{c}
u_{
m e} \\

u_{\mu} \\

u_{ au}
\end{array}
ight] = \left[egin{array}{ccc} U_{
m e1} & U_{
m e2} & U_{
m e3} \\
U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\
U_{ au 1} & U_{ au 2} & U_{ au 3}
\end{array}
ight] \left[egin{array}{c}
u_1 \\

u_2 \\

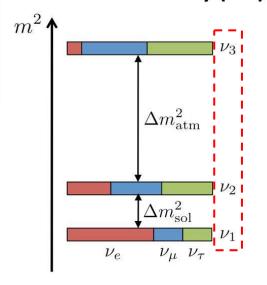
u_3
\end{array}
ight]$$

The PMNS matrix relates flavour and mass eigenstates of neutrinos

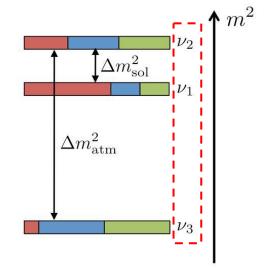
What can neutrino ~OSCILLATIONS~ tell us?

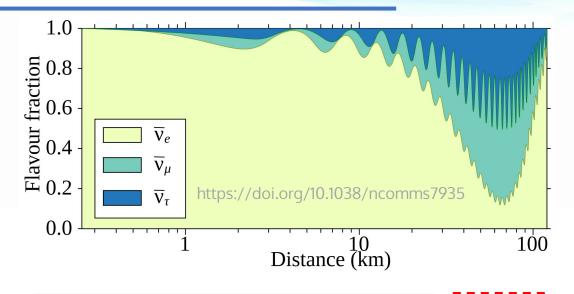


normal hierarchy (NH)



inverted hierarchy (IH)



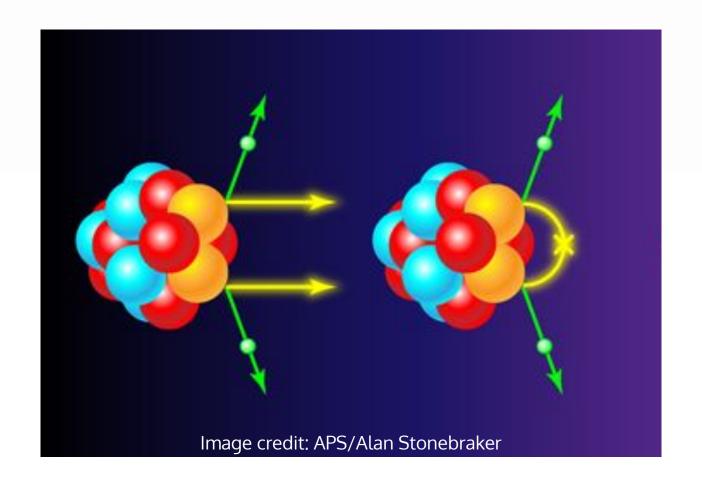


$$\left[egin{array}{c}
u_{
m e} \
u_{
m \mu} \
u_{
m r} \end{array}
ight] = \left[egin{array}{ccc} U_{
m e1} & U_{
m e2} & U_{
m e3} \ U_{
m \mu1} & U_{
m \mu2} & U_{
m \mu3} \ U_{
m \tau1} & U_{
m \tau2} & U_{
m \tau3} \end{array}
ight] \left[egin{array}{c}
u_1 \
u_2 \
u_3 \end{array}
ight]$$

The PMNS matrix relates flavour and mass eigenstates of neutrinos

... but no information on Majorana vs Dirac :(

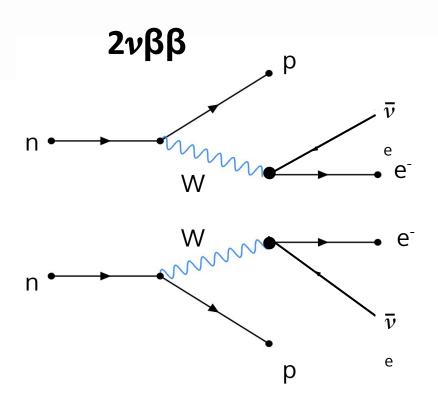


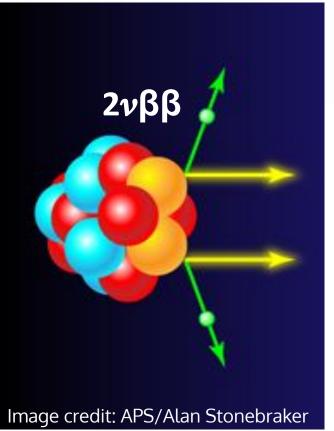


What is $2\nu\beta\beta$?



 Simultaneous conversion of two nucleons into two charged leptons and two antineutrinos

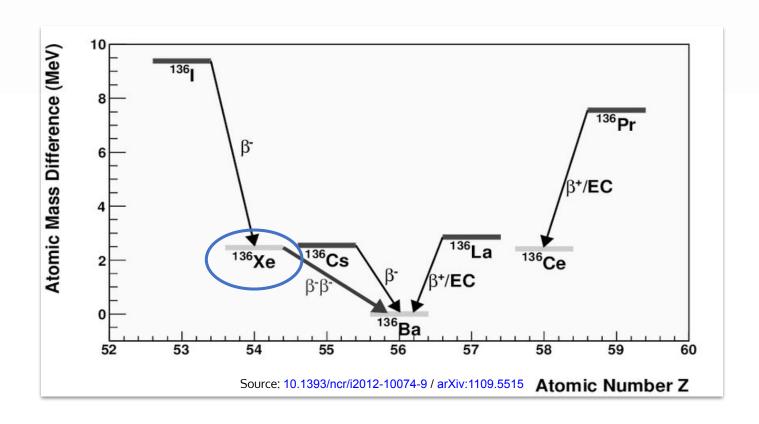




ββ-decays are rare

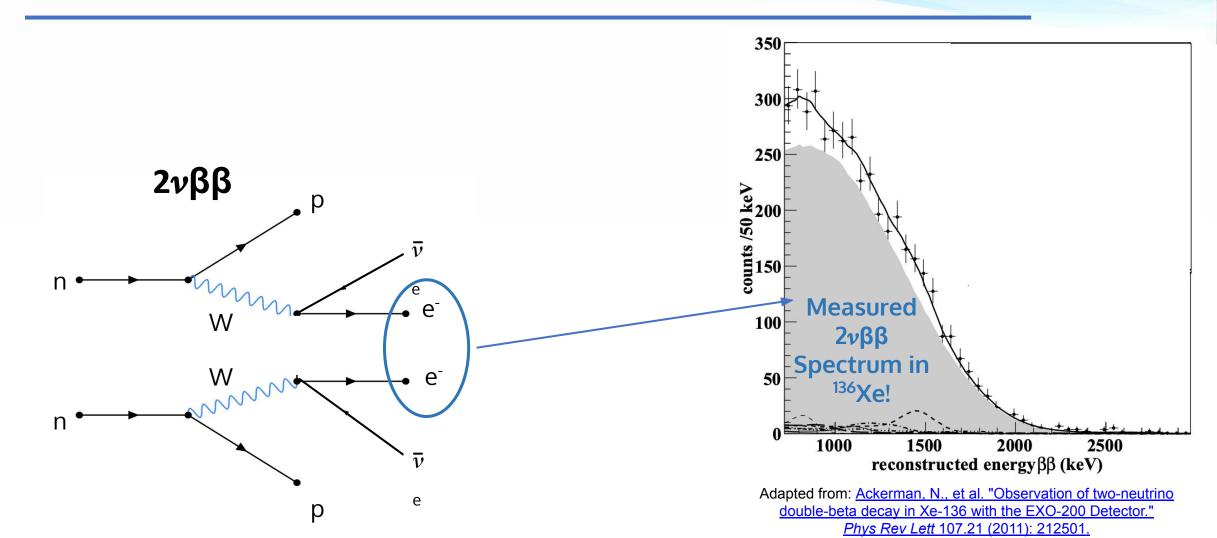


• Second-order weak interaction process



0νββ vs 2νββ

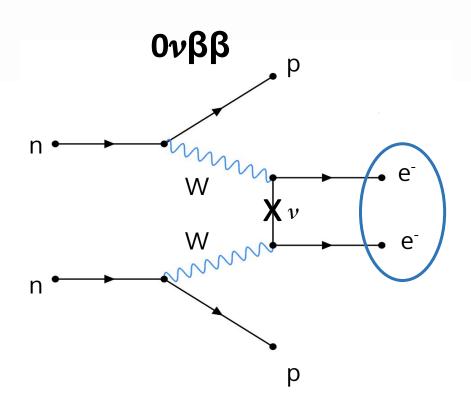


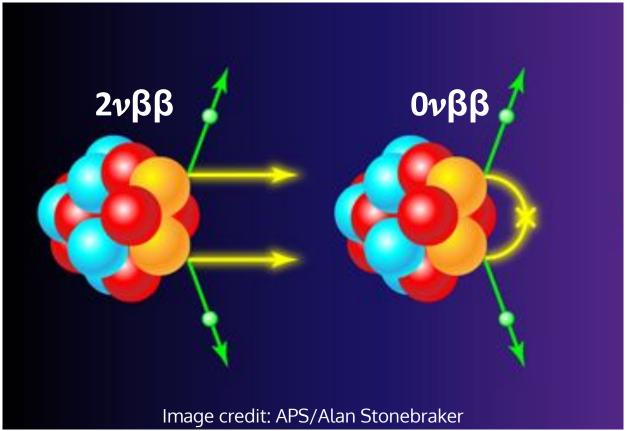


What is $0\nu\beta\beta$?



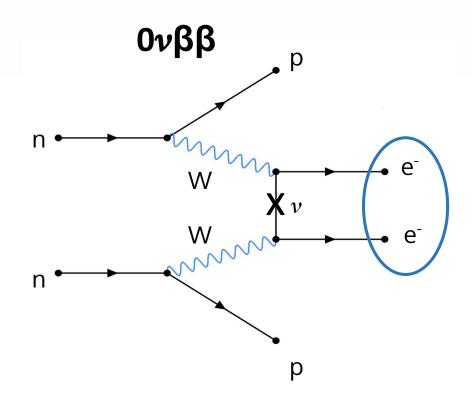
 Simultaneous conversion of two nucleons into two charged leptons and two antineutrinos

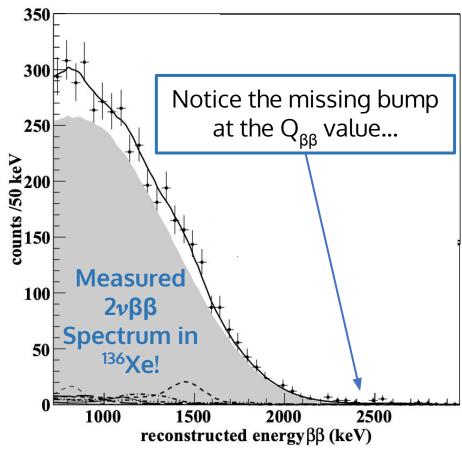




0νββ vs 2νββ





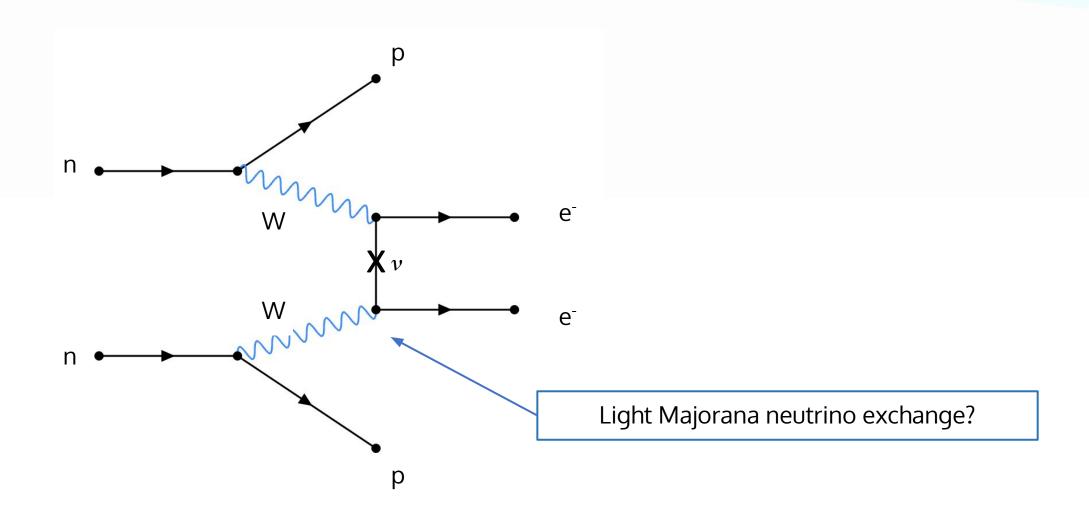


Adapted from: Ackerman, N., et al. "Observation of two-neutrino double-beta decay in Xe-136 with the EXO-200 Detector."

Phys Rev Lett 107.21 (2011): 212501.

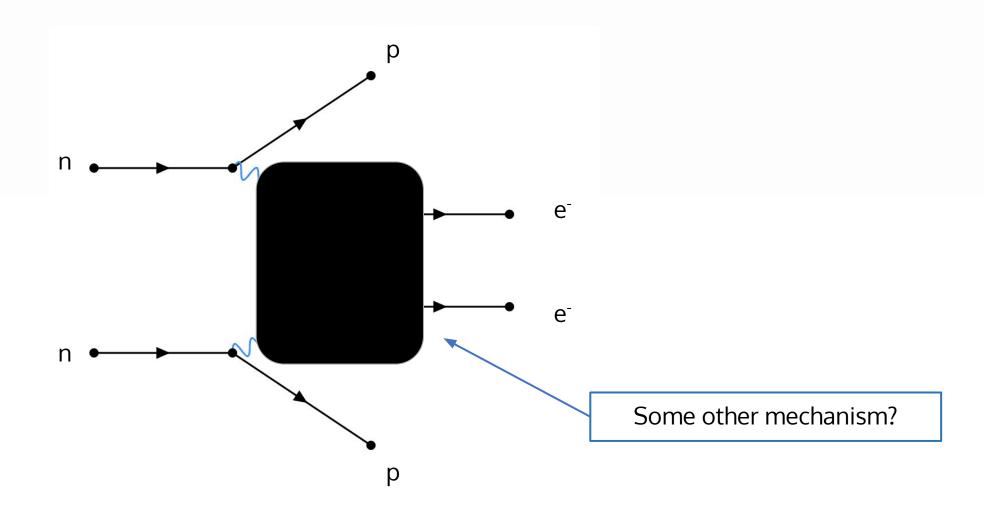
How would 0νββ even work?





How would 0νββ even work?

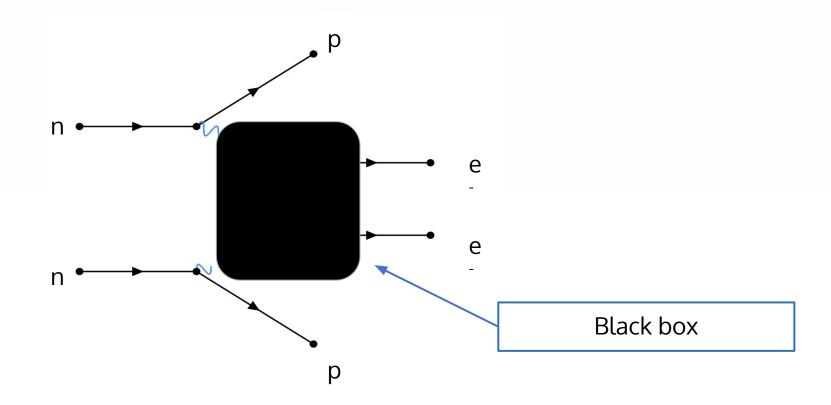




The Black Box Theorem

Searching for 0νββ: The Black Box





Regardless of what mechanism $0\nu\beta\beta$ proceeds by, it always implies new physics

(Schechter, and Valle. Phys. Rev. D 25.11 (1982): 2951. "black box theorem")

Searching for 0νββ: The Real Motivation



Particle physics community searching for physics beyond the standard model



Searching for $0\nu\beta\beta$: The Real Motivation



Particle physics community searching for physics beyond the standard model



Searching for 0νββ: The Real Motivation



Particle physics community searching for physics beyond the standard model



Searching for 0νββ: The Real Motivation



Particle physics community searching for physics beyond the standard model

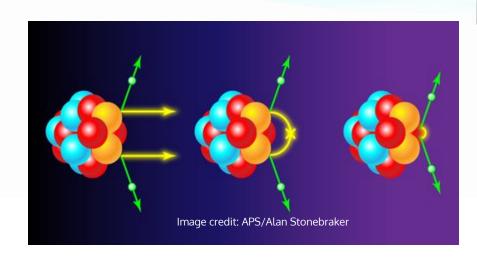


Regardless of what mechanism 0νββ proceeds by, it always implies new physics (Schechter, and Valle. Phys. Rev. D 25.11 (1982): 2951. "black box theorem")

Why Search for 0νββ?



- The discovery of neutrino mass from oscillation experiments provides **new pathways to mass generation** in the SM
 - Dirac vs Majorana masses
 - feeble couplings to Higgs field vs seesaw mechanisms
- Implications for matter-antimatter asymmetry problem
- Neutrinoless double beta decay (0νββ) exploits the nucleus as a virtual environment to probe high energy physics processes

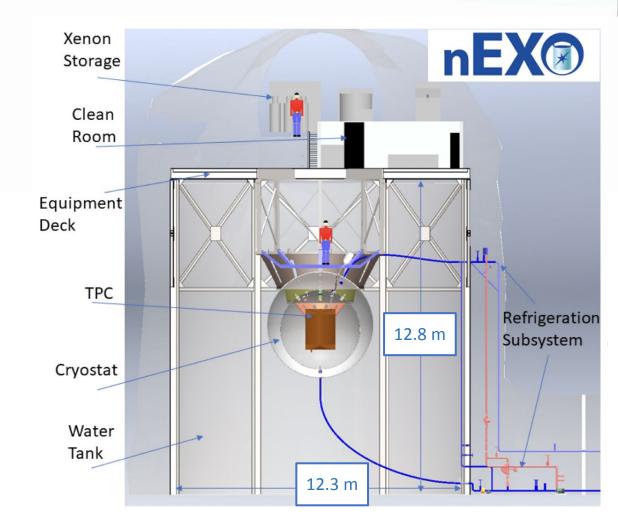


Searches for neutrinoless double beta decay ($0\nu\beta\beta$) are searches for Lepton Number Violation & Physics Beyond the Standard Model

What is nEXO?

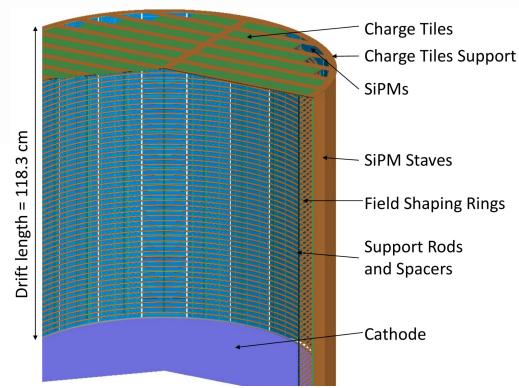


- 5-tonne single-phase liquid xenon Time Projection Chamber (LXe TPC)
- LXe is enriched to 90% in the target isotope, ¹³⁶Xe
- Extensive radio-assay program
 - ultra low backgrounds validated by EXO-200 data





- Homogeneous, dense, liquid detector medium with high-Z nucleus
 - online purification
 - \circ self-shielding of γ radiation
 - scalability
- Multiparameter Analysis
- Possibility to tag daughter nucleus
- Possibility for control run in case of discovery

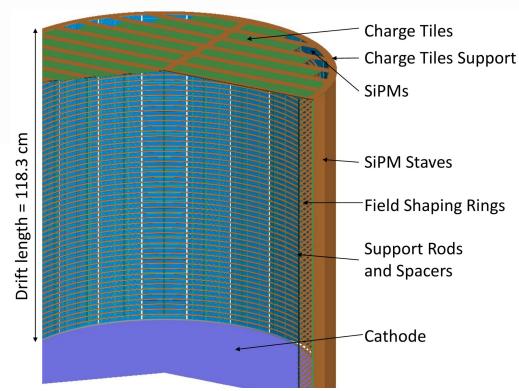




- Homogeneous, dense, liquid detector medium with high-Z nucleus
 - o online purification
 - \circ self-shielding of γ radiation
 - scalability

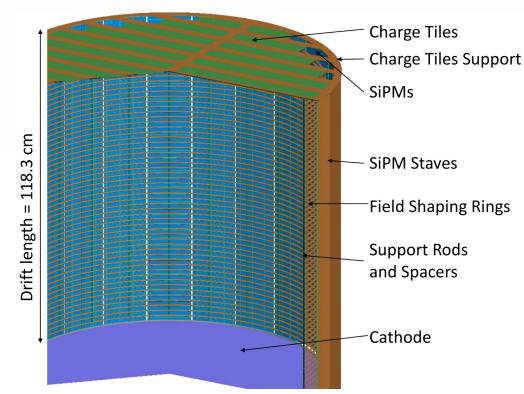
Multiparameter Analysis

- Less sensitive to background fluctuations
- Robust against unknown backgrounds
- Possibility to tag daughter nucleus
- Possibility for control run in case of discovery



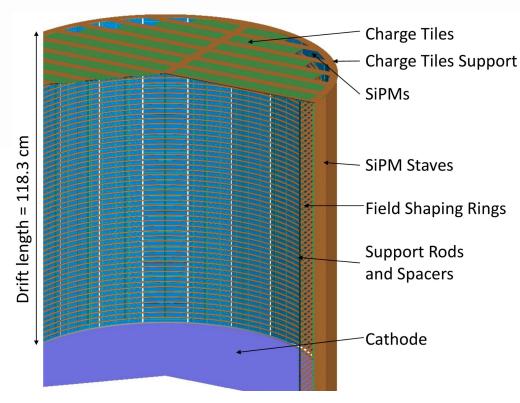


- Homogeneous, dense, liquid detector medium with high-Z nucleus
 - online purification
 - \circ self-shielding of γ radiation
 - scalability
- Multiparameter Analysis
 - Less sensitive to background fluctuations
 - Robust against unknown backgrounds
- Possibility to tag daughter nucleus; "Ba-tagging" upgrade
 - o Nature 569, no. 7755 (2019): 203-207
- Possibility for control run in case of discovery





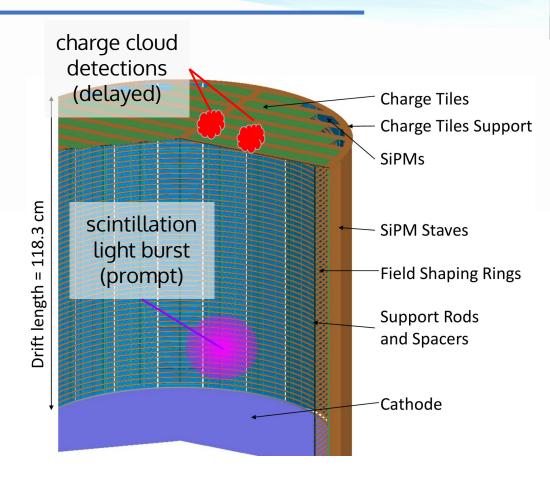
- Homogeneous, dense, liquid detector medium with high-Z nucleus
 - online purification
 - \circ self-shielding of γ radiation
 - scalability
- Multiparameter Analysis
 - Less sensitive to background fluctuations
 - Robust against unknown backgrounds
- Possibility to tag daughter nucleus; "Ba-tagging" upgrade
 - Nature 569, no. 7755 (2019): 203-207
- Possibility for control run in case of discovery
 - use unenriched xenon & repeat the experiment!
 - ... and the ability to go to a GXe TPC and study $0\nu\beta\beta$ mechanism if discovered.



How does nEXO's TPC work?



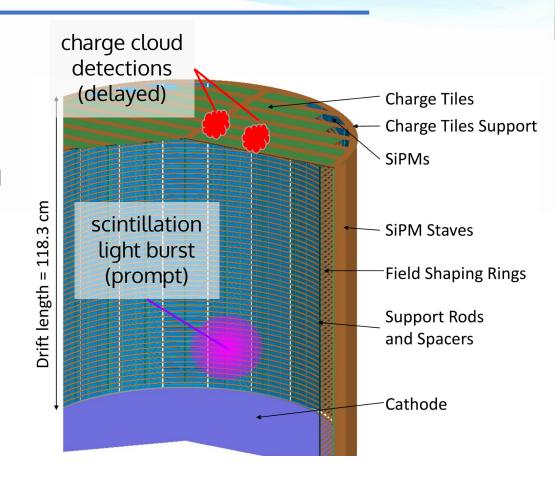
- Energy deposits in the LXe liberate electrons, ionize the surrounding liquid
 - excited dimers Xe₂ release ~175 nm scintillation light
 - o ionization clouds drift to segmented anode in applied E-field
- Combination of light + charge readout gives us...



How does nEXO's TPC work?



- Energy deposits in the LXe liberate electrons, ionize the surrounding liquid
 - excited dimers of Xe₂ release ~175 nm scintillation light
 - o ionization clouds drift to segmented anode in applied E-field
- Combination of light + charge readout gives us:
 - Improved energy resolution
 - Improved spatial positioning (event localization)
 - \circ Discriminator between α , β and γ events



An Active R&D Program

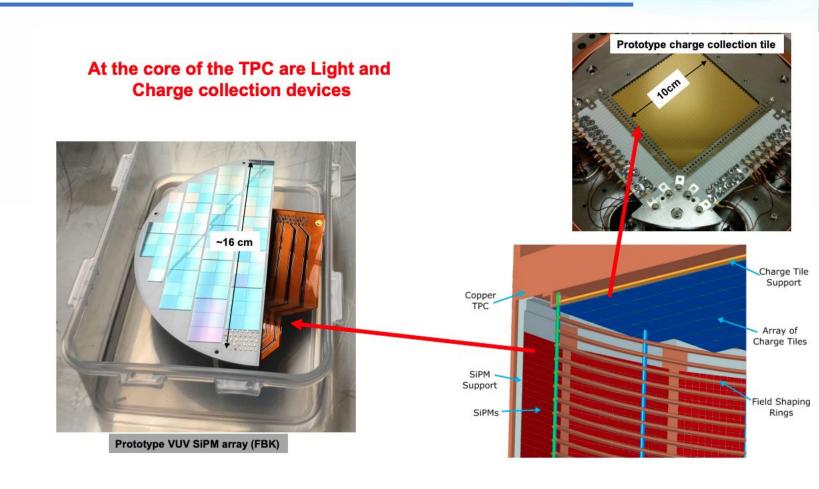
Hardware?



Basic principles and backgrounds validated and measured by EXO-200

nEXO upgrades from EXO-200 include

- use of SiPMs
- custom made charge tiles
- electroformed copper for TPC
- water-Cherenkov muon veto



Many Canadian Contributions



- **SiPM use in liquid xenon** environments (LOLX experiment)
 - see talk by <u>S. Bron</u> & poster by <u>L. Rudolph</u>
- Characterization & stability of SiPMs
 - see talk by <u>L. Darroch</u>
- water-Cherenkov Outer Detector & radiation shield
 - see talk by <u>S. Majidi</u>
- R&D toward potential Ba-tagging upgrade
 - o see talks by <u>H. Rasiwala, D. Ray</u>, <u>R. Collister</u>
- Many Equity Diversity & Inclusion activities
 - see talk from <u>E. Caden</u>



Multiparameter Analysis

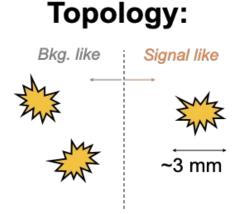
nEXO is not a counting experiment



Three high-level variables:

- ~1% Energy resolution at Q_{ββ}
- Standoff distance to detector components (precise event localization, depth in xenon)
- **Topology** score (DNN): single- and multi-site discrimination (β -like vs γ -like event separation)

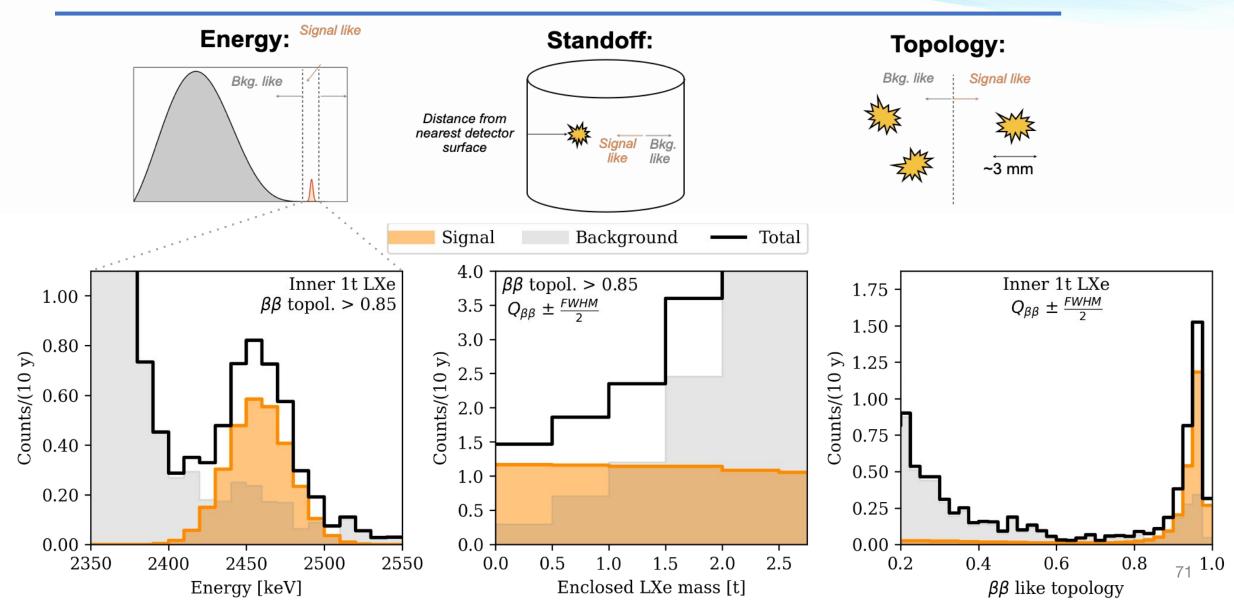
Energy: Signal like Distance from nearest detector surface Signal Bkg. like like like



Multiparameter Analysis



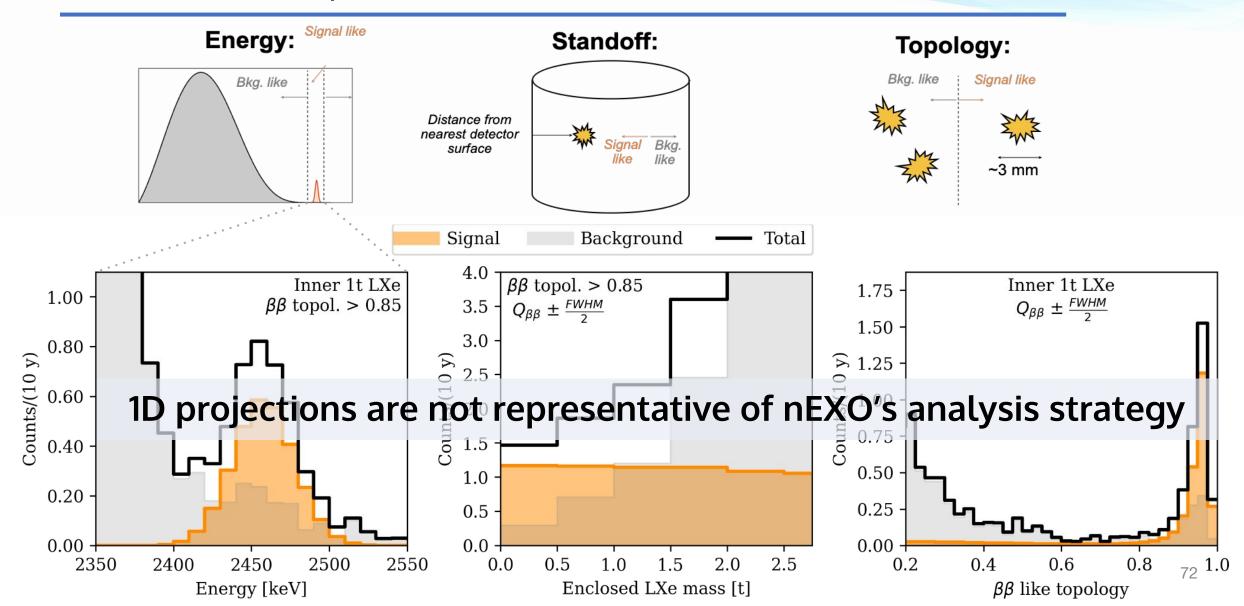
A 3D Parameter Space



Multiparameter Analysis



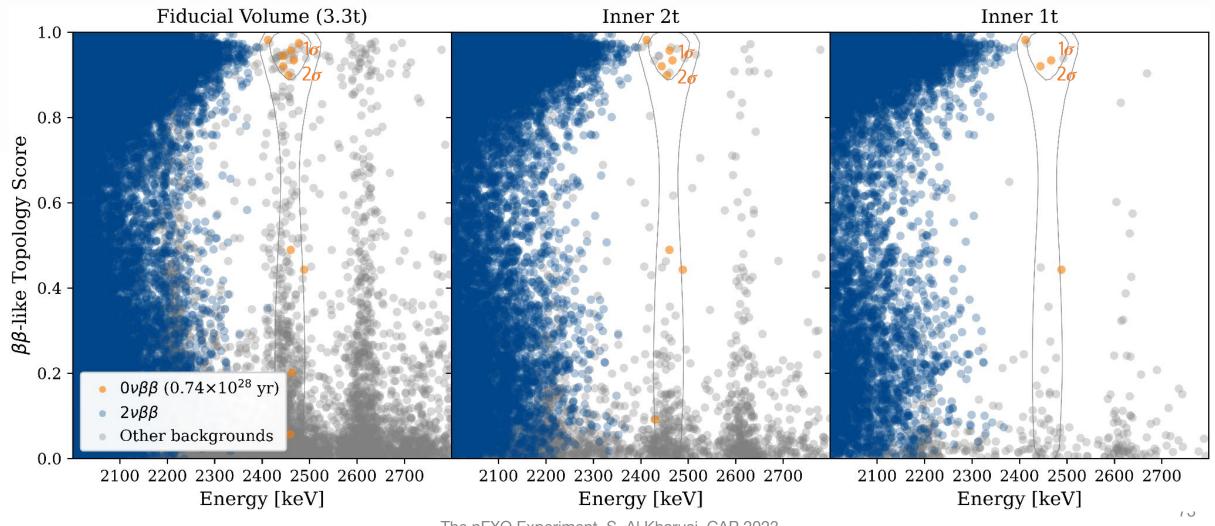
A 3D Parameter Space





What will nEXO data look like?

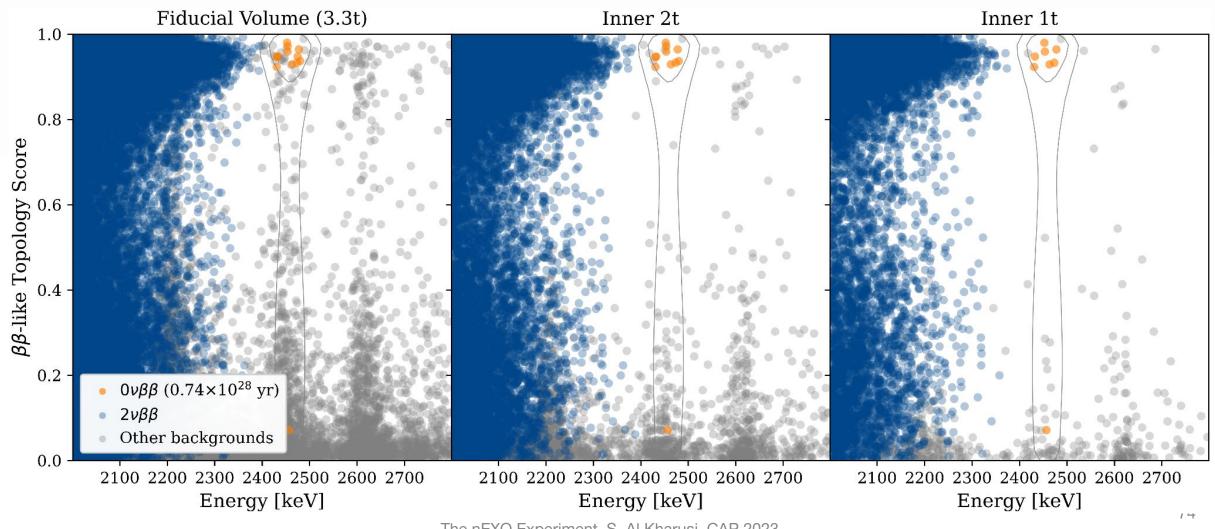
Below: realizations of nEXO 10 yr dataset at 7.4x10²⁷ yr half life(3 σ discovery potential)





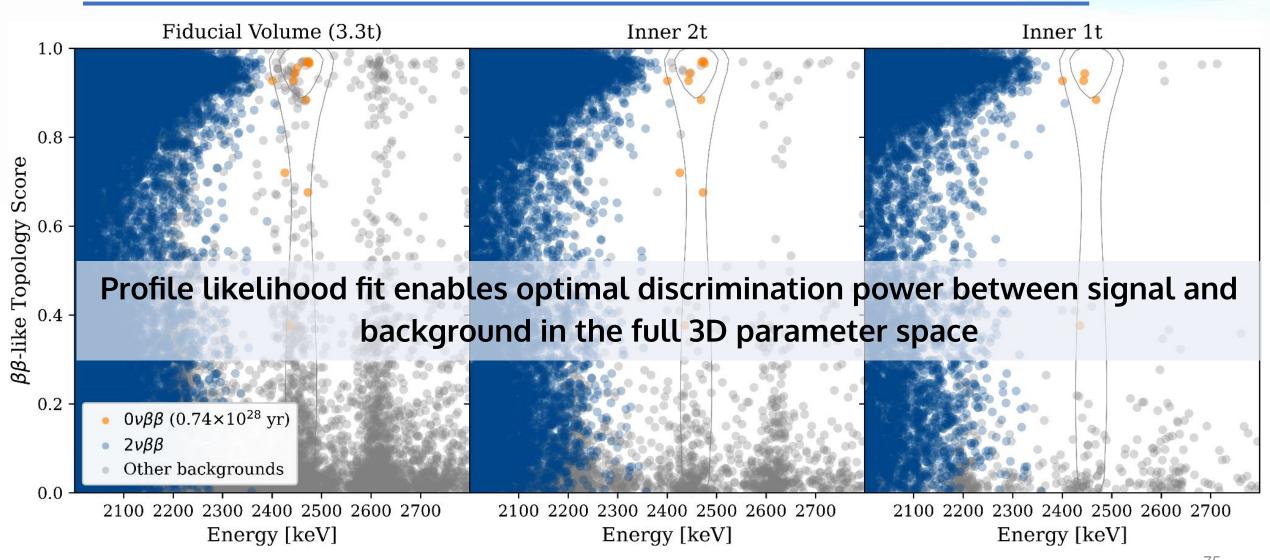
What will nEXO data look like?

Below: realizations of nEXO 10 yr dataset at 7.4x10²⁷ yr half life(3 σ discovery potential)





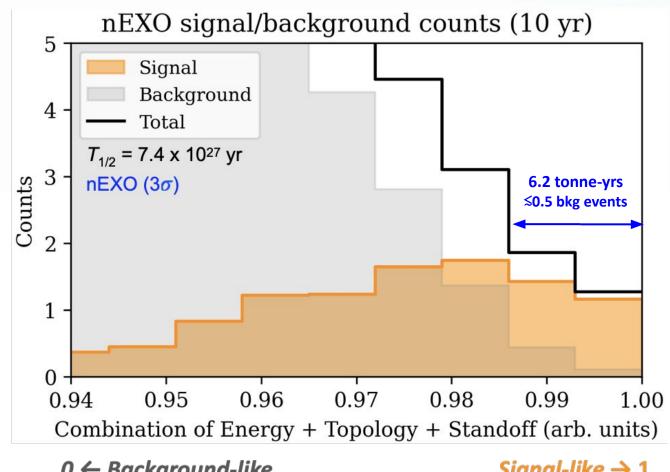
3D profile likelihood fit: ultimate test of $0\nu\beta\beta$ hypothesis



3D→ 1D visualization



Arranging the 3D bins into 1D, ordered by signal-to-background ratio, helps visualize the signal and background separation in nEXO

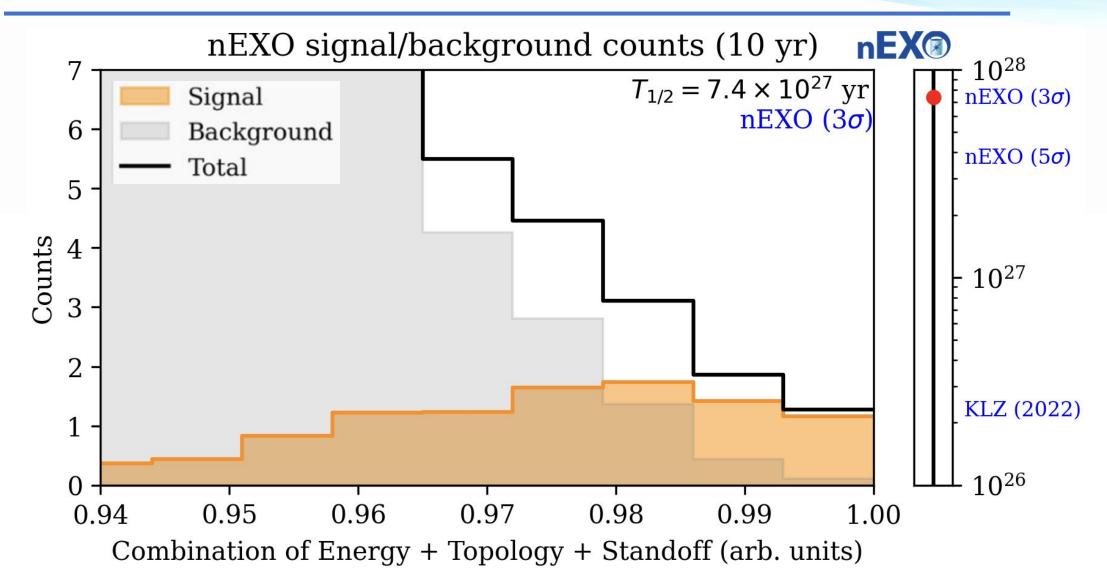


0 ← Background-like

Signal-like \rightarrow 1

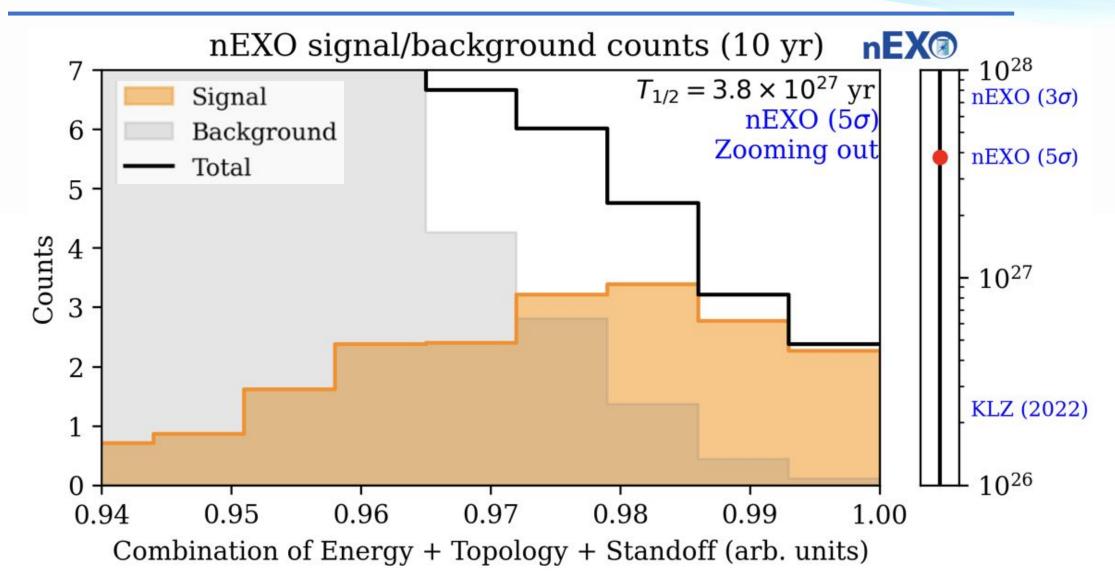


3D→ 1D visualization



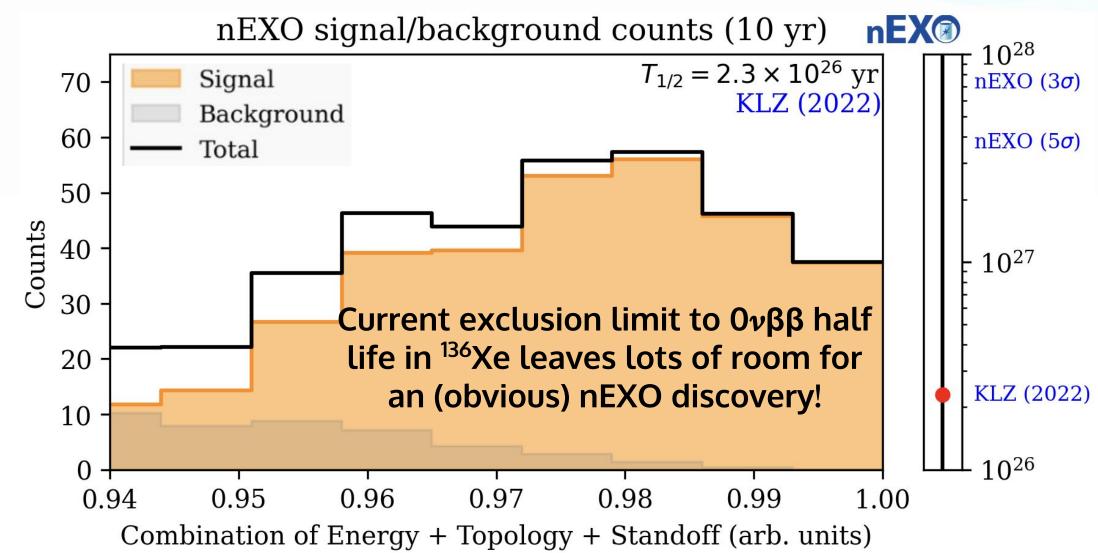


3D→ 1D visualization



nEX®

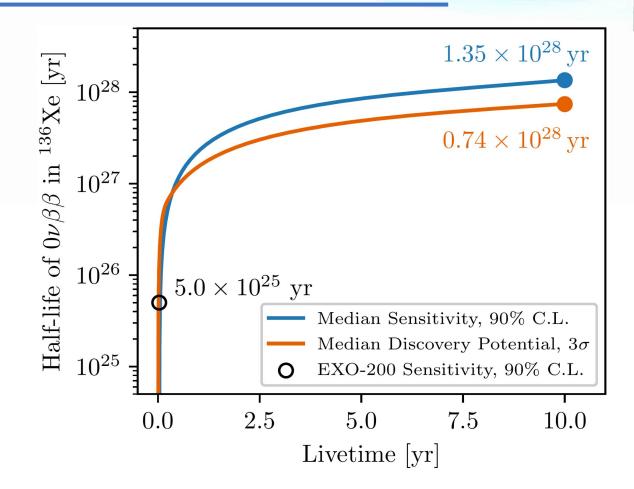
3D→ 1D visualization





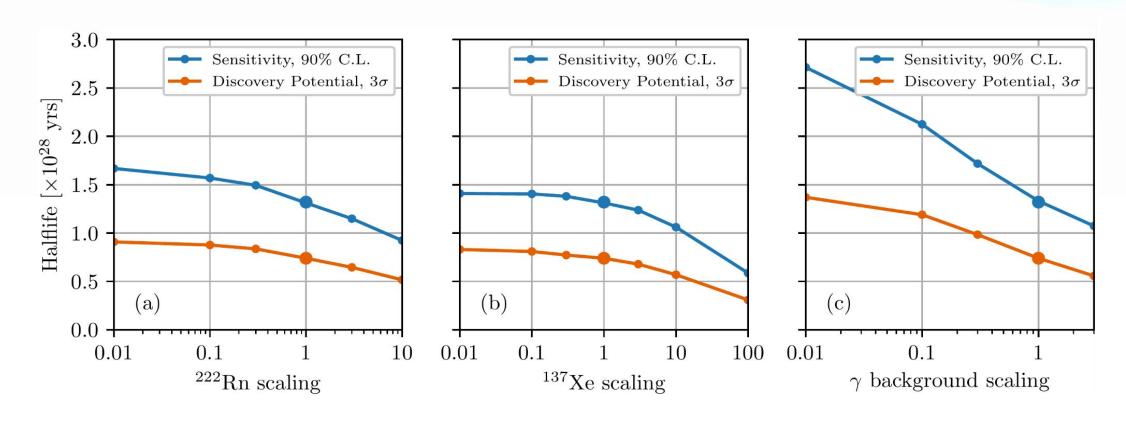


- In 6.5 years of data, nEXO will reach a exclusion sensitivity to 0νββ half life in xenon >10²⁸ years (90% C.L.)
 - Age of the universe $x10^{18}$!



nEXO Sensitivity Robustness



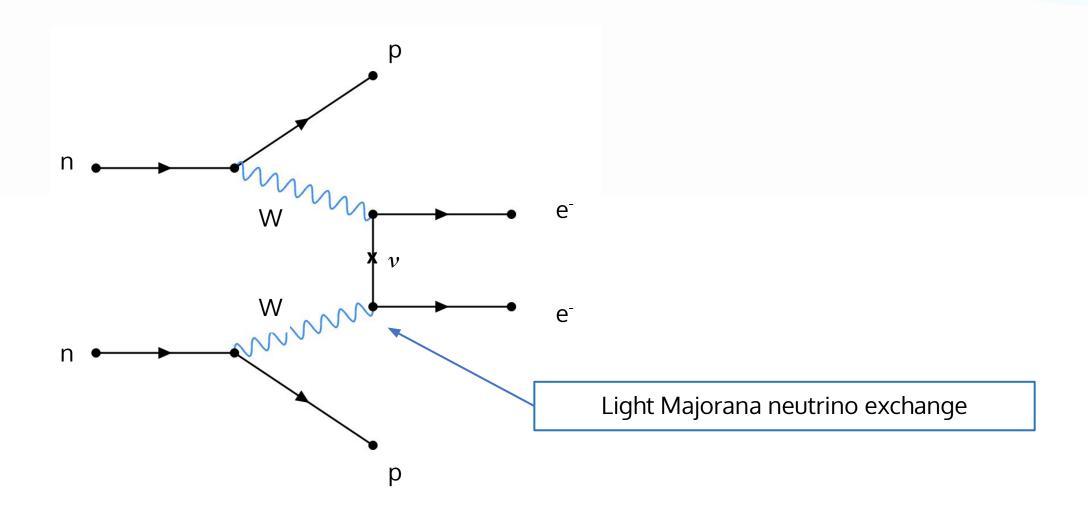


Confidence in the sensitivity estimate arises from a detailed conservative model with measured input parameters

G Adhikari et al. (nEXO Collaboration), 2022 J. Phys. G: Nucl. Part. Phys. 49 015104

A Neutrino Mass Measurement?





nEX®

Neutrino Mass Measurement

- Half lives of $0\nu\beta\beta$ correspond to an effective Majorana mass of the electron neutrino $< m_{\beta\beta} > 1$
 - combination of 3 neutrino mass states
 - Assumes dominant process for 0νββ is light-Majorana neutrino exchange
- $\langle m_{\beta\beta} \rangle$ is isotope-independent

$$|m_{\beta\beta}\rangle = \left|\sum_{i=1}^{3} U_{ei}^{2} m_{i}\right|$$

$$\left[egin{array}{c}
u_{
m e} \\

u_{\mu} \\

u_{ au}
\end{array}
ight] = \left[egin{array}{ccc} U_{
m e1} & U_{
m e2} & U_{
m e3} \\
U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\
U_{ au 1} & U_{ au 2} & U_{ au 3}
\end{array}
ight] \left[egin{array}{c}
u_1 \\

u_2 \\

u_3
\end{array}
ight]$$

The PMNS matrix relates flavour and mass eigenstates of neutrinos

nEX®

Neutrino Mass Measurement

- Half lives of $0\nu\beta\beta$ correspond to an effective Majorana mass of the electron neutrino $< m_{\beta\beta} > 1$
 - combination of 3 neutrino mass states
 - \circ Assumes dominant process for $0\nu\beta\beta$ is light-Majorana neutrino exchange
- <m_{ββ}> is isotope-independent

$$\langle m_{\beta\beta}\rangle = \left|\sum_{i=1}^{3} U_{ei}^{2} m_{i}\right|$$

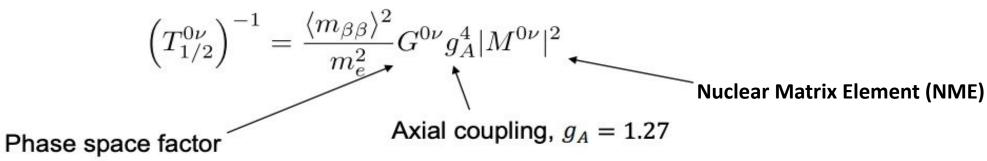
$$\left[egin{array}{c}
u_{
m e} \\
u_{\mu} \\
u_{ au}
\end{array}
ight] = \left[egin{array}{ccc} U_{
m e1} & U_{
m e2} & U_{
m e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{ au 1} & U_{ au 2} & U_{ au 3} \end{array}
ight] \left[egin{array}{c}
u_1 \\
u_2 \\
u_3 \end{array}
ight]$$

The PMNS matrix relates flavour and mass eigenstates of neutrinos

nEX®

Neutrino Mass Measurement

- Half lives of $0\nu\beta\beta$ correspond to an effective Majorana mass of the electron neutrino $< m_{\beta\beta} >$
- $\langle m_{\beta\beta} \rangle$ is isotope-independent
 - BUT: depends on your choice nuclear matrix element (NME) when converting from a half life measurement to
 neutrino mass, NME is least constrained theoretical parameter below



J. Kotila and F. Iachello, Phys Rev C 85, 034316 (2012)

nEX®

Neutrino Mass Measurement

- Half lives of $0\nu\beta\beta$ correspond to an effective Majorana mass of the electron neutrino $< m_{\beta\beta} > 1$
- $\langle m_{\beta\beta} \rangle$ is isotope-independent
 - Depends on your choice nuclear matrix element (NME) when converting from a half life measurement to neutrino
 mass, NME is least constrained theoretical parameter below
 - \circ Complex nuclear physics could change <m_{gg}> estimates \rightarrow we need to search for $0\nu\beta\beta$ in multiple isotopes

$$\left(T_{1/2}^{0\nu}\right)^{-1} = \frac{\langle m_{\beta\beta}\rangle^2}{m_e^2} G^{0\nu} g_A^4 |M^{0\nu}|^2$$
Nuclear Matrix Element (NME)

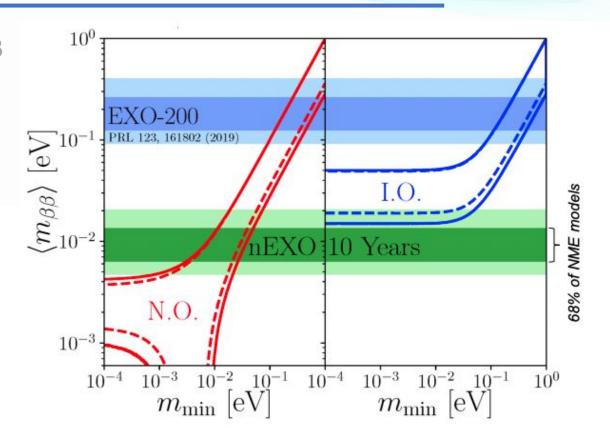
Phase space factor

J. Kotila and F. Iachello, Phys Rev C 85, 034316 (2012)

Neutrino Mass Measurement



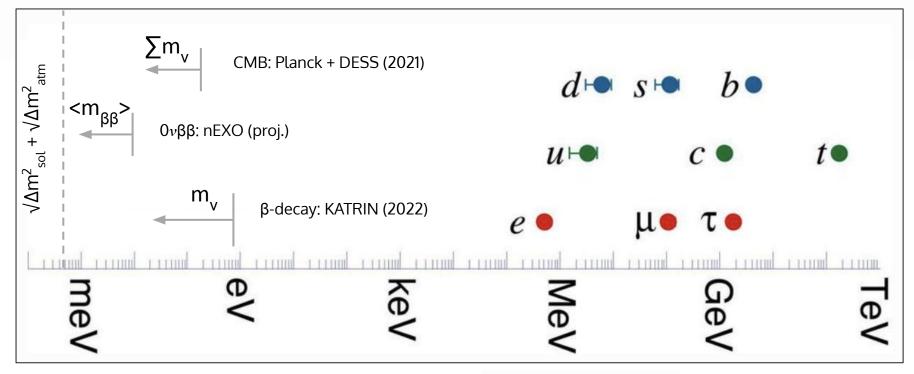
- In 6.5 years, nEXO will reach a sensitivity to 0νββ
 half life in xenon >10²⁸ years
 - Age of the universe $\times 10^{18}$!
- Effective Majorana mass of the neutrino ≤8 meV;
 excludes inverted mass ordering parameter space



nEXO sensitivity to neutrino mass <m_{ββ}> a neutrino mass measurement in an exciting time!



- In 6.5 years, nEXO will reach a sensitivity to 0νββ half life in xenon >10²⁸ years
- Effective Majorana mass of the neutrino ≤8 meV



Standard Model Fermion masses / HITOSHI MURAYAMA (adapted)

Summary



nEXO is **searching for Lepton Number Violation via 0νββ in ¹³⁶Xe**

A multiparameter likelihood fit maximizes the physics reach of nEXO and significantly reduces the probability of false-positives

Several upgrades to nEXO are possible in case of a $0\nu\beta\beta$ discovery (depleted xenon control run, ¹³⁶Ba tagging)

Obvious pathway to exploring $0\nu\beta\beta$ mechanisms post-discovery (GXe TPCs)

Xenon nEX® Storage Clean Room Equipment Deck TPC Refrigeration 12.8 m Subsystem Cryostat Water Tank 12.3 m

We live in a very exciting time for fundamental/neutrino physics!

Thank you!



Ask me about nEXO Diversity Equity & Inclusion Activities:

- Mentorship program
- Climate surveys
- Outreach

Follow us!
one-XOexperiment











soud.alkharusi@mail.mcgill.ca

Thank you!



nEXO Publications:

2022:

- Performance of novel VUV-sensitive Silicon Photo-Multipliers for nEXO
- Development of a 127Xe calibration source for nEXO

2021:

- nEXO: neutrinoless double beta decay search beyond 1028 year half-life sensitivity
- Reflectivity of VUV-sensitive silicon photomultipliers in liquid Xenon
- Event reconstruction in a liquid xenon Time Projection Chamber with an optically-open field cage

2020:

- Reflectance of Silicon Photomultipliers at Vacuum Ultraviolet Wavelengths
- Measurements of electron transport in liquid and gas Xenon using a laser-driven photocathode

2019:

- Characterization of the Hamamatsu VUV4 MPPCs for nEXO
- Simulation of charge readout with segmented tiles in nEXO

2018

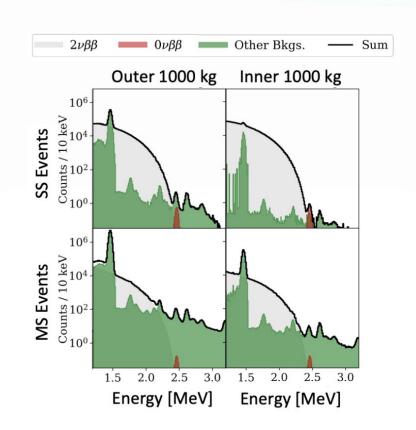
nEXO pre-conceptual design report



Unknown external background?



If an unknown decay were strong enough to produce as many SS events in the inner 3000 kg as a 3σ discovery at a half-life of 5.7×10^{27} yr, this decay would produce 271 counts in the MS outer volume, enough to rule out the expected background model at p < 0.00001.

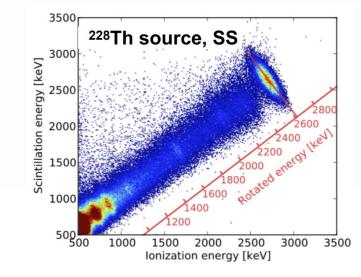


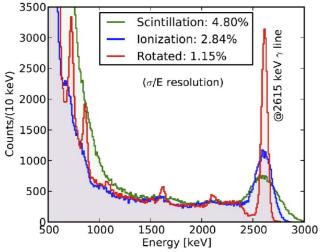
Phys. Rev.C 97, 065503 (2018)

Rotated energy scale



- LXe rotated energy (exploiting anticorrelation in charge and light) allows for optimization of energy resolution
 - Conti, E., et al. "Correlated fluctuations between luminescence and ionization in liquid xenon." Phys. Rev. B 68.5 (2003): 054201.
- 2022: LZ <u>achieved <0.7% energy resolution</u> in LXe!



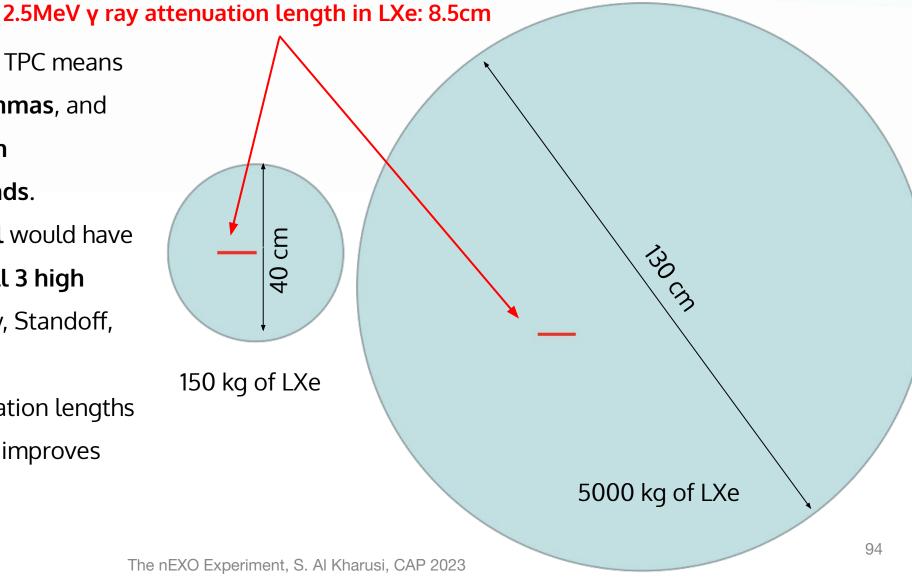


LXe TPC Scalability (1/2)



LXe is self shielding: larger TPC means better attenuation of gammas, and even **better constraints on** fluctuations to backgrounds.

- Any potential 0νββ signal would have to not be anomalous in all 3 high level distributions: Energy, Standoff, and Topology.
 - Due to gamma attenuation lengths << detector scale, this improves with larger masses



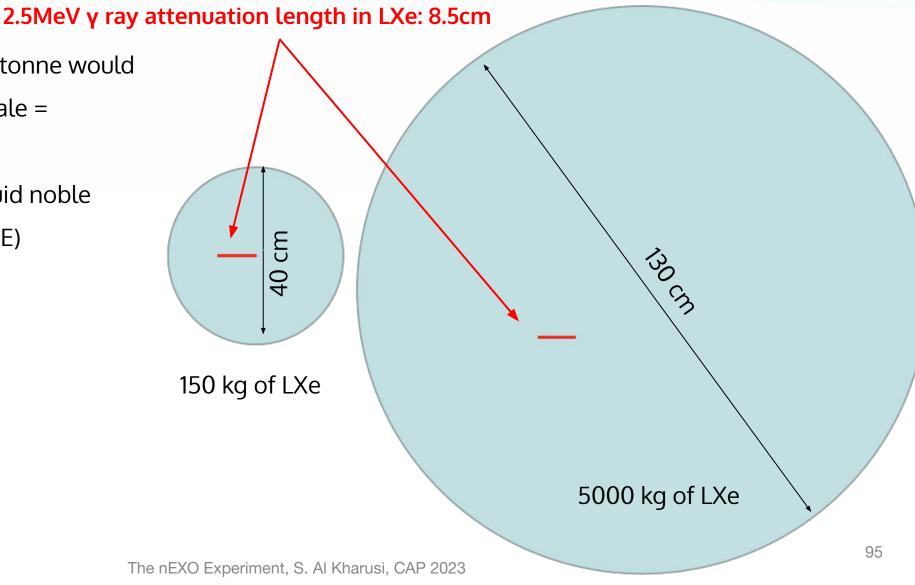
LXe TPC Scalability (2/2)



Going from 5 tonne to 100 tonne would require LXe TPCs of size scale =

1.3*(100/5)^(1/3) ~ 3.5 m We know how to make liquid noble

TPCs even larger (see DUNE)



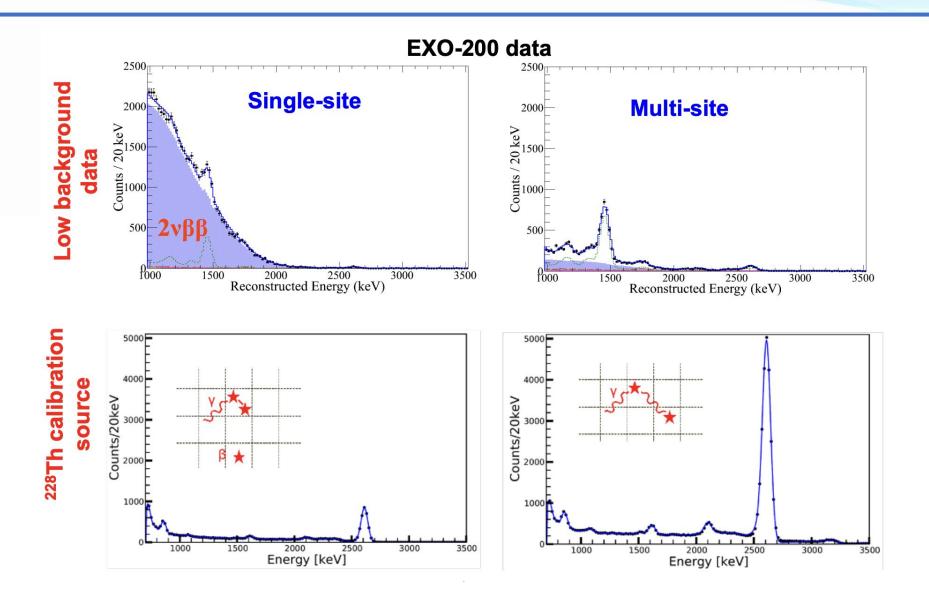
Beyond 0νββ discovery?



- If 0νββ is discovered in any isotope, we would want to explore what mechanism is producing the decay
 - \circ We would do this by measuring the **energy and angular distributions** of the two emitted electrons in 0vββ events
 - Straightforward in an enriched gaseous xenon TPC
 - Design constraints set by half life measurements in an LXe TPC (e.g. nEXO)
- $0\nu\beta\beta$ decay mechanisms change the value of $< m_{\beta\beta} >$, and probe couplings to BSM physics
- Discovering $0\nu\beta\beta$ and exploring it in multiple isotopes is key
 - Nuclear physics is hard, and extracting BSM physics couplings without multiple isotopes confirming $0\nu\beta\beta$, half lives, mechanisms etc... will be difficult



EXO-200 Validation



Do Majorana neutrinos help us?



- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator
- Seesaw mechanisms
- Matter vs Antimatter? Maybe m_Rassociated with ∧ and are really heavy?
 - Possible explanation for the matter / antimatter asymmetry!! (leptogenesis)

Sakharov conditions

- 1. CP Violation
- 2. Non-equilibrium state
- 3. Baryon number violation

Do Majorana neutrinos help us?



- Lose two degrees of freedom in the SM for Majorana neutrinos
- Weinberg operator
- Seesaw mechanisms
- Matter vs Antimatter? Maybe m_Rassociated with ∧ and are really heavy?
 - Possible explanation for the matter / antimatter asymmetry!! (leptogenesis)

Sakharov conditions (in the context of leptogenesis)

- I. CP Violation \rightarrow m_R is Majorana; no lepton number.
- 2. Non-equilibrium state \rightarrow Universe is expandING
- 3. Baryon number violation \rightarrow sphaleron processes