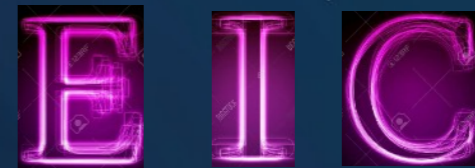


Theoretical Opportunities

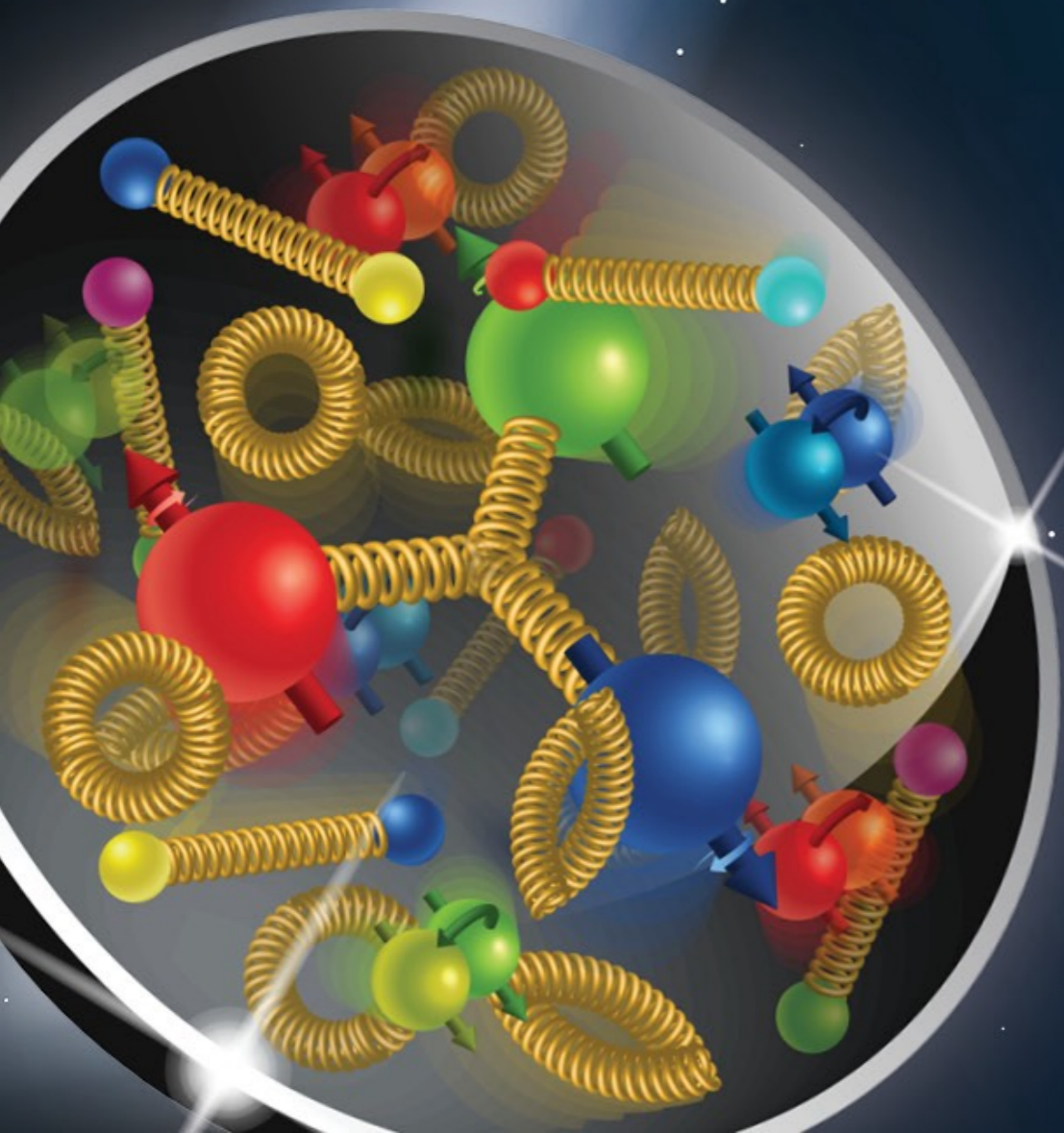
at the



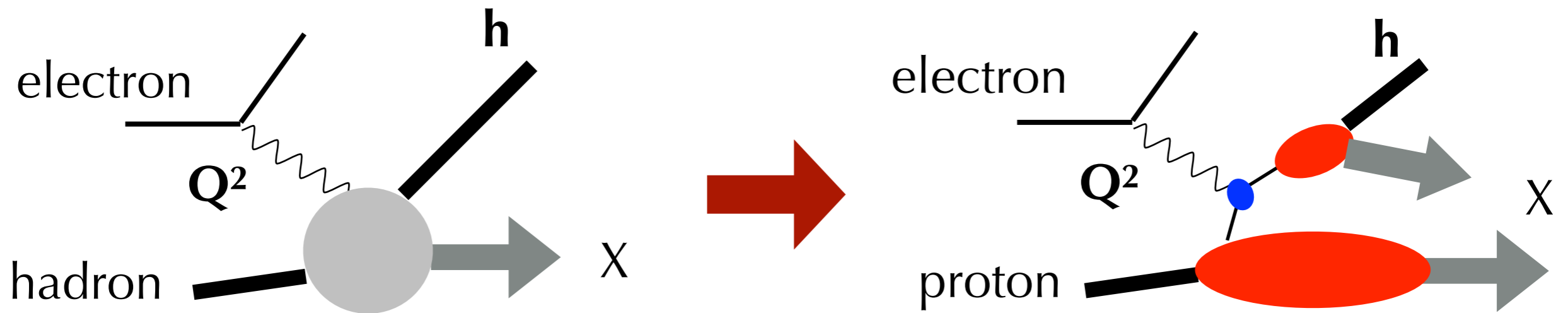
Marco Radici



Pavia

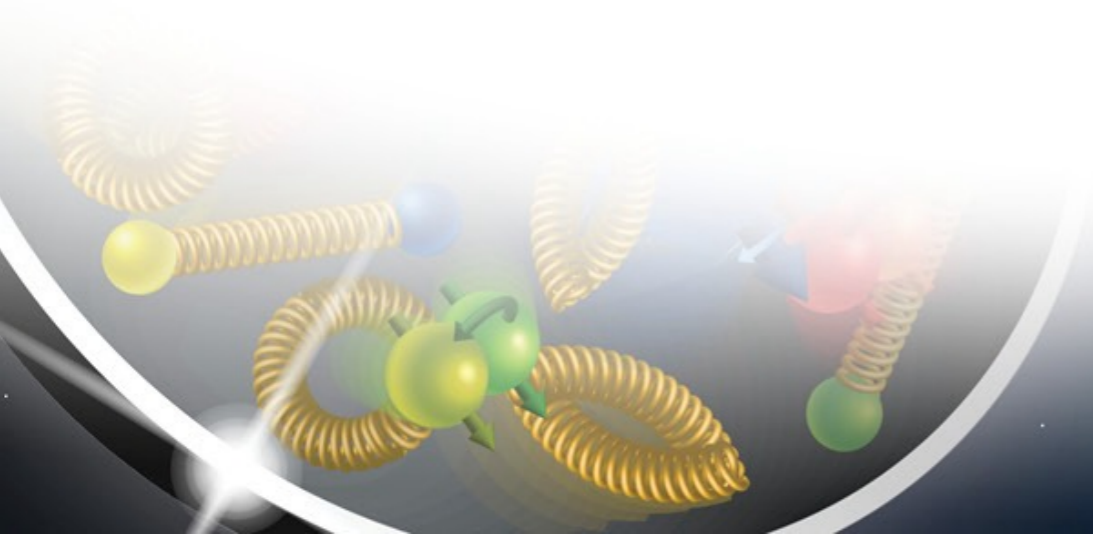


Theoretical tools : Non perturbative Maps

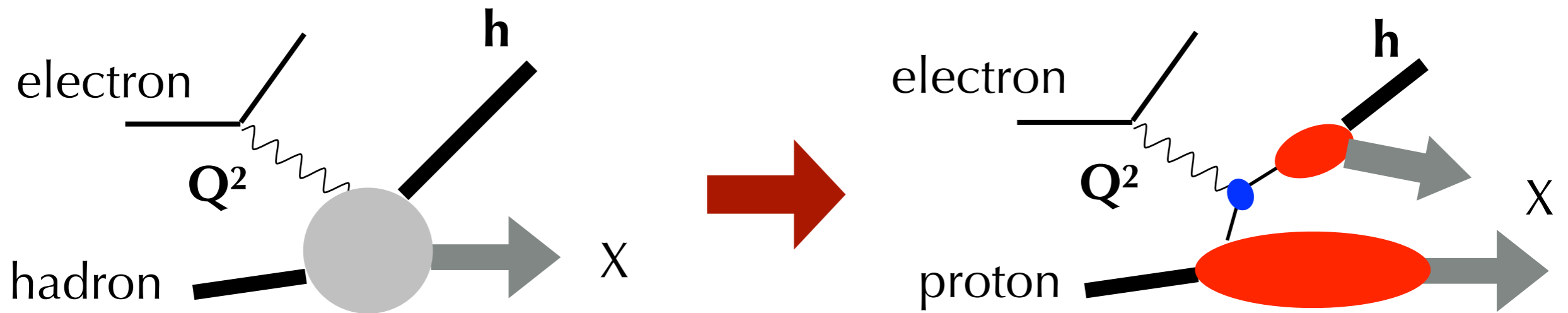


Factorization Theorem

- hard cross section, **perturbatively** calculable
- **non perturbative MAPS** of - dynamics of colored partons inside colorless hadrons
- fragmentation of colored partons in colorless hadrons



Theoretical tools : Non perturbative Maps



Factorization Theorem

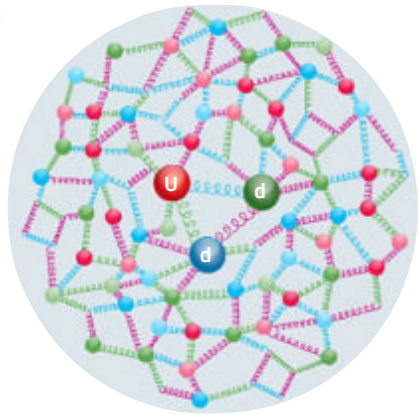
- hard cross section, **perturbatively** calculable
- **non perturbative MAPS** of - dynamics of colored partons inside colorless hadrons
- fragmentation of colored partons in colorless hadrons

**extract more
precise MAPS**



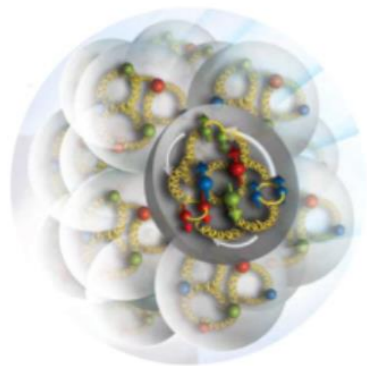
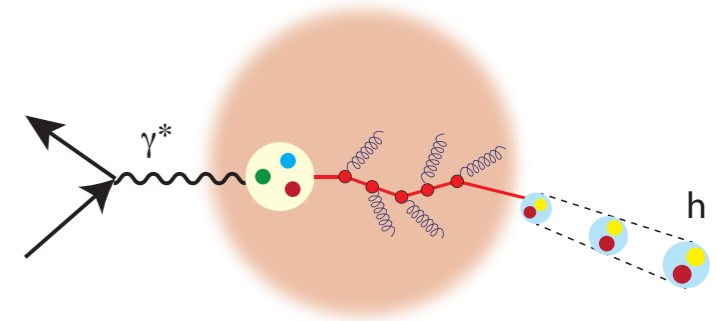
**understand how
confinement comes about**

The EIC physics case : The key questions

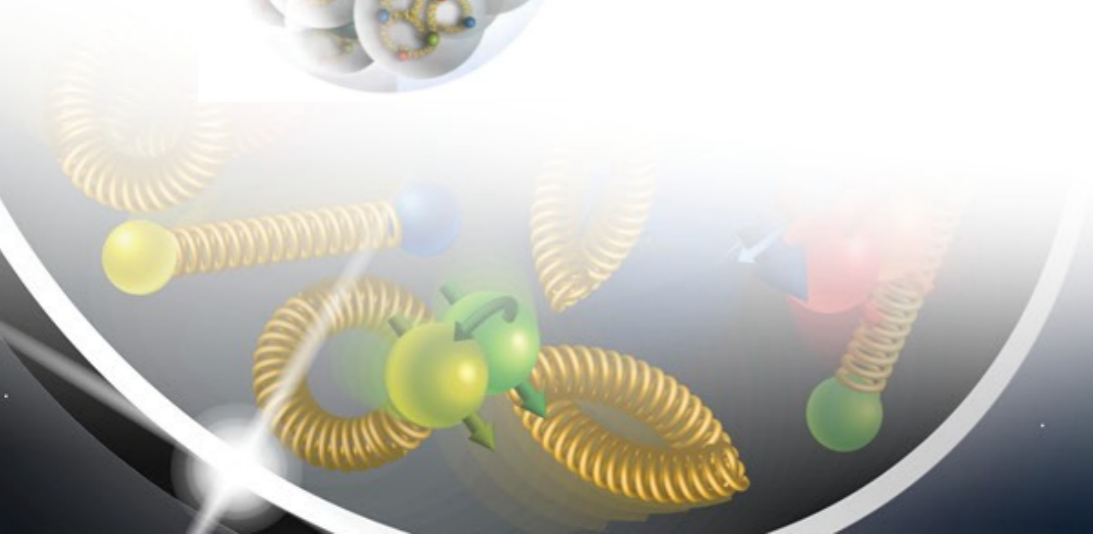


1) How are **partons** with their spins **distributed in space and momentum** inside the **Nucleon**, such that its **properties** emerge from their interactions?

2) How do **colored partons propagate** and interact with nuclear medium such that eventually **colorless hadrons emerge** ?



3) Does **gluon density saturate** at high energy, giving rise to a **universal gluonic matter** ?



The EIC physics case : Theoretical tools

1) How are **partons** with their spins **distributed in**

What do we know about these
non perturbative *MAPS* ?

And what can we learn
about them at the EIC ?

rise to a **universal gluonic matter** ?

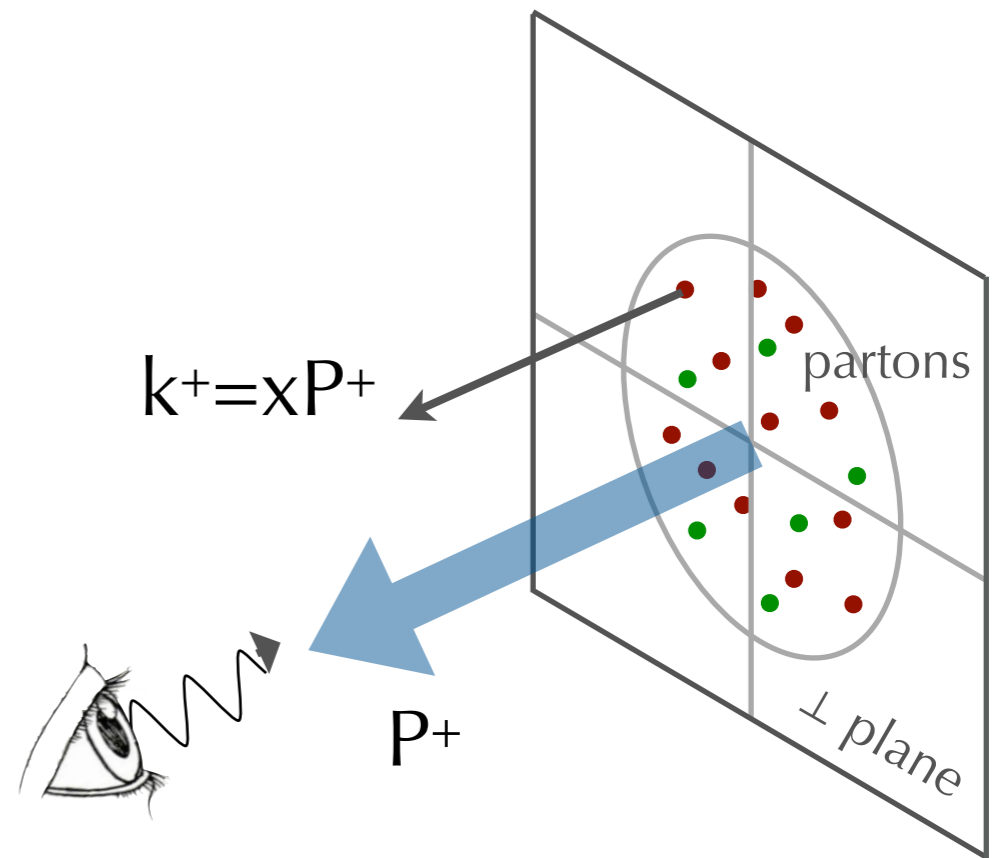
2) How
with
hadr

h

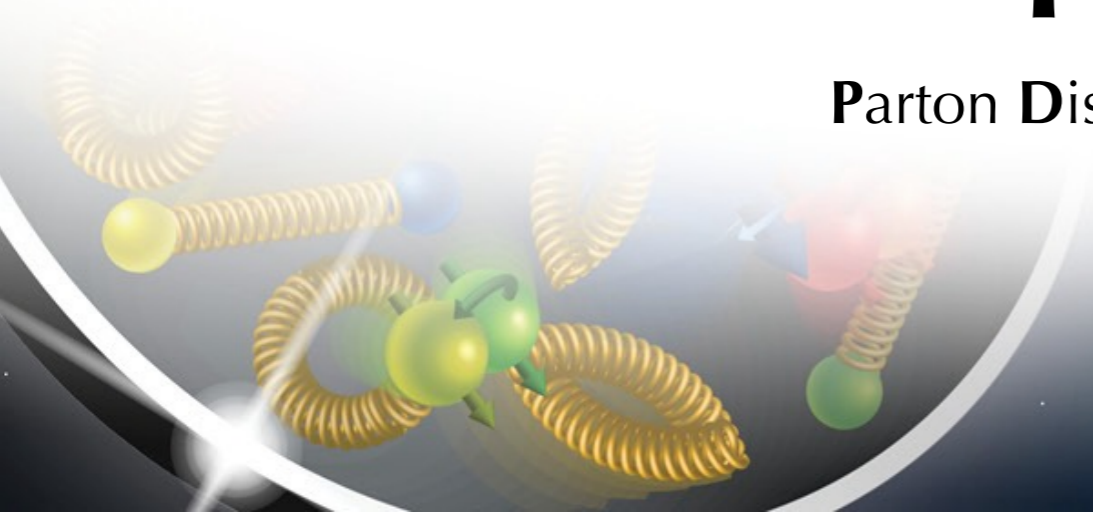
The EIC physics tools

PDF (x)

Parton Distribution Function



1-dim map



The EIC physics tools

Transverse Momentum Dependent PDF

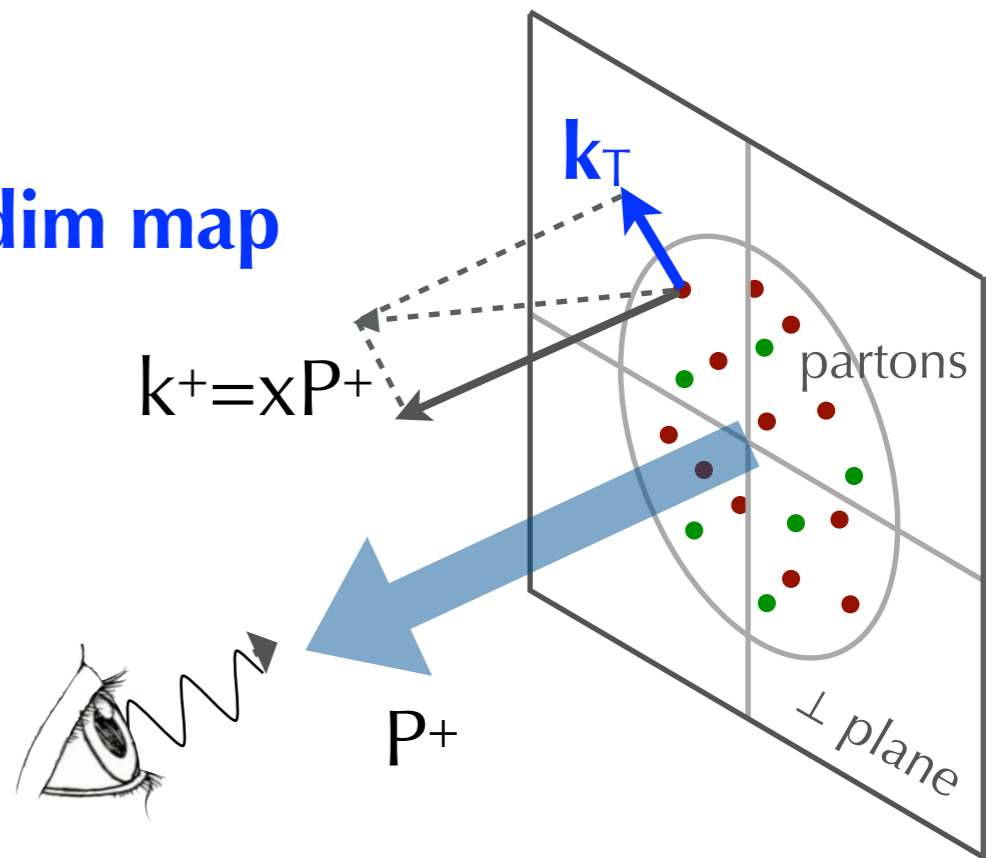
TMD
(x, \mathbf{k}_T)

$$\int d\mathbf{k}_\perp$$

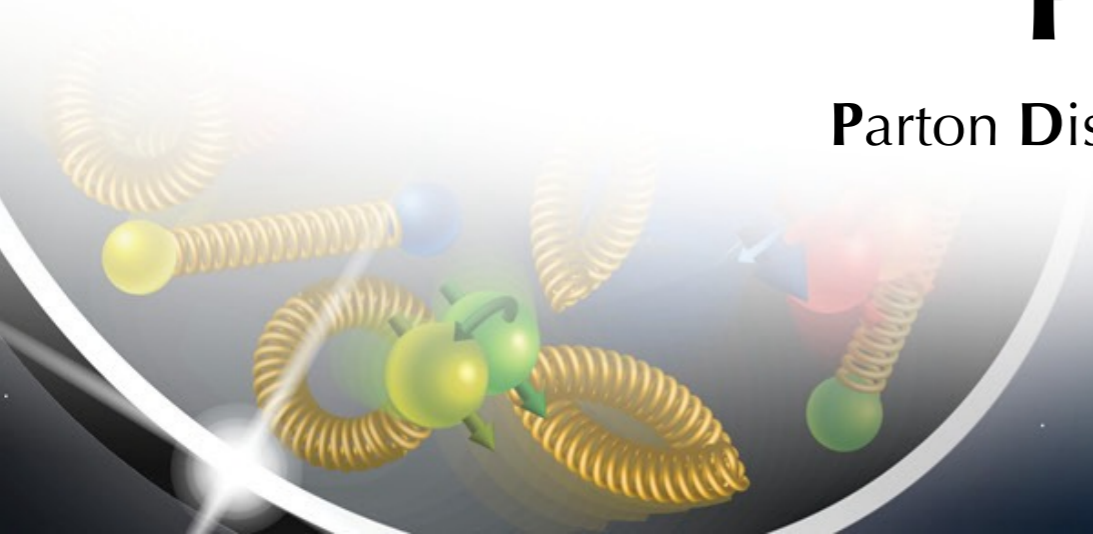
PDF(x)

Parton Distribution Function

3-dim map

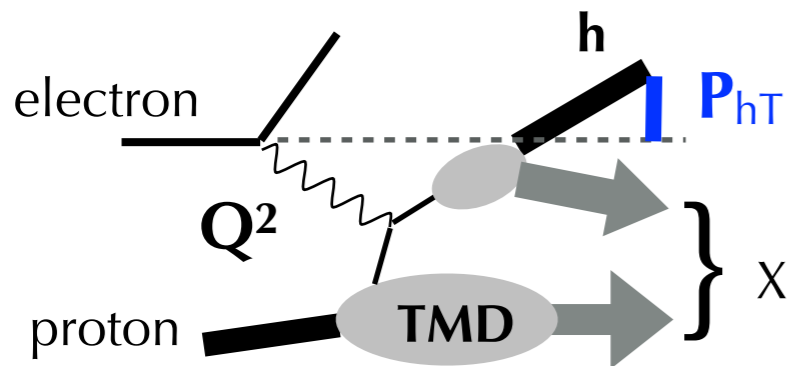


1-dim map



3D-maps in momentum space

TMD (x, \mathbf{k}_T) can be **extracted** only in semi-inclusive processes
e.g., semi-inclusive DIS (SIDIS)



soft scale $P_{hT}/z \ll Q$ to “feel” intrinsic \mathbf{k}_T
related to confined motion

z fractional energy carried by h

factorization th.'s available for various final states:
 h = light- and heavy-quark hadrons, jets, hadron-in-jet,..

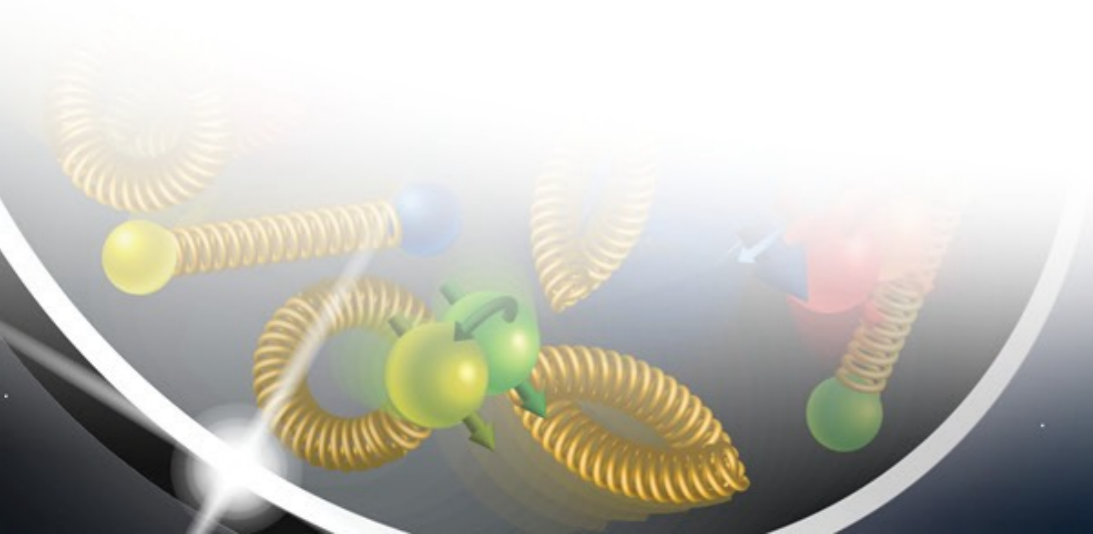
Ji, Yuan, Ma, P.R. D71 (05)

Rogers & Aybat, P.R. D83 (11)

Collins, “Foundations of Perturbative QCD” (11)

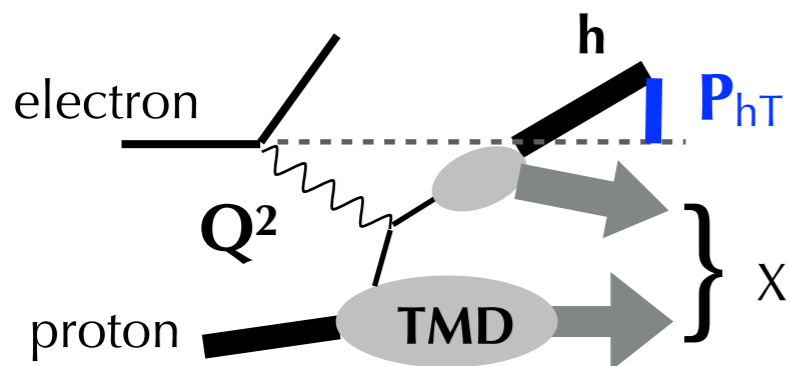
Echevarria, Idilbi, Scimemi, JHEP 1207 (12)

.....



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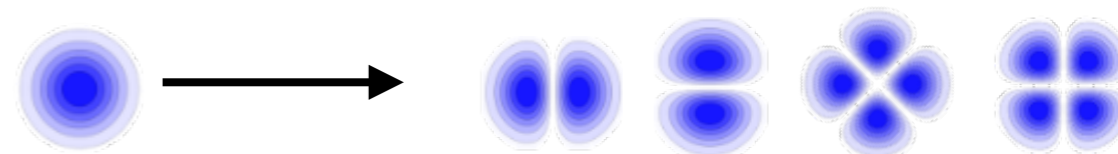
Echevarria, Idilbi, Scimemi, JHEP 1207 (12)

.....

the TMD “zoo” at leading twist

		Quark polarization		
		Unpolarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$f_1 = \odot$	\times	$h_1^\perp = \odot \uparrow - \odot \downarrow$
	L	\times	$g_1 = \odot \rightarrow - \odot \leftarrow$	$h_{1L}^\perp = \odot \nearrow - \odot \nwarrow$
	T	$f_{1T}^\perp = \odot \uparrow - \odot \downarrow$	$g_{1T} = \odot \rightarrow - \odot \leftarrow$	$h_1 = \odot \uparrow - \odot \downarrow$ $h_{1T}^\perp = \odot \nearrow - \odot \nwarrow$

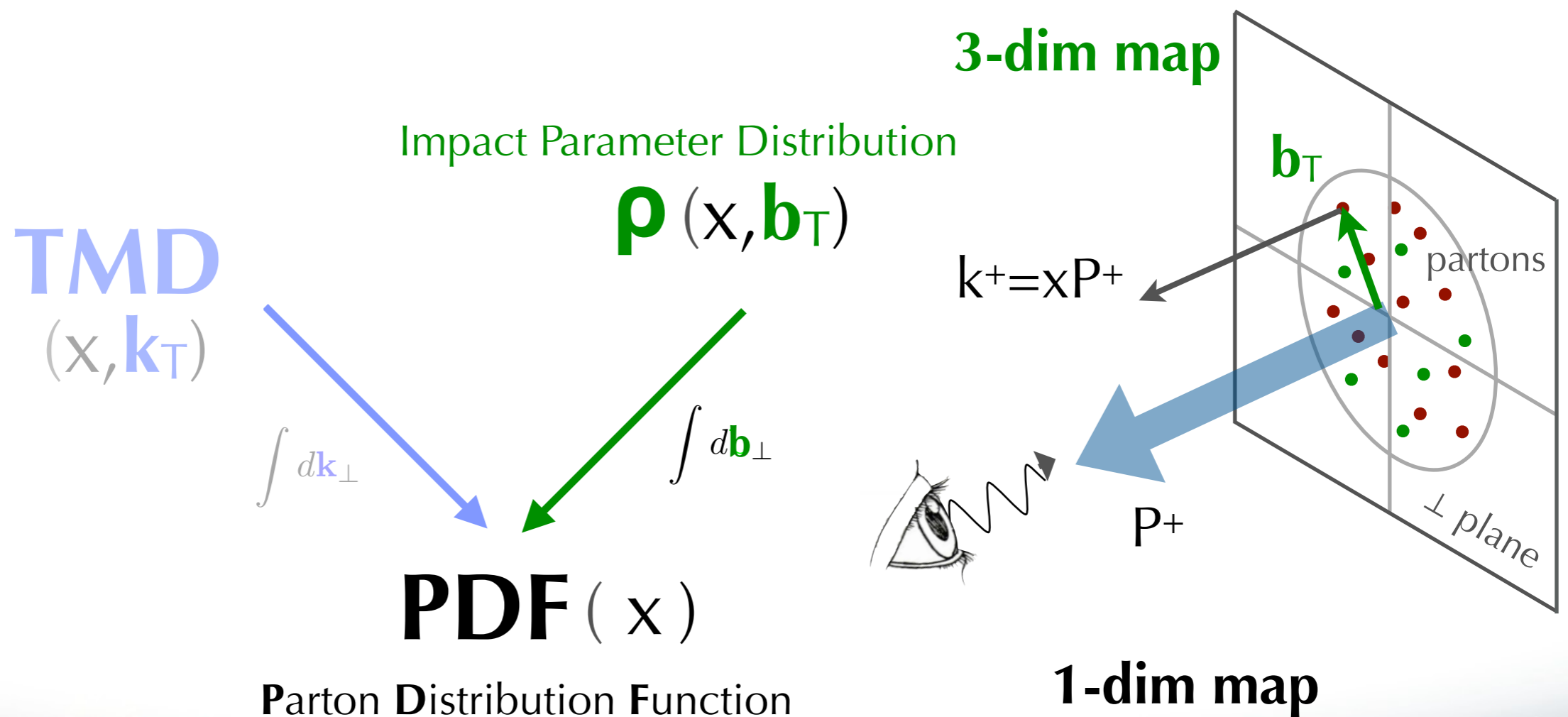
deformations induced by
spin-momentum correlations



each TMD is connected to a specific
measurable SIDIS spin asymmetry

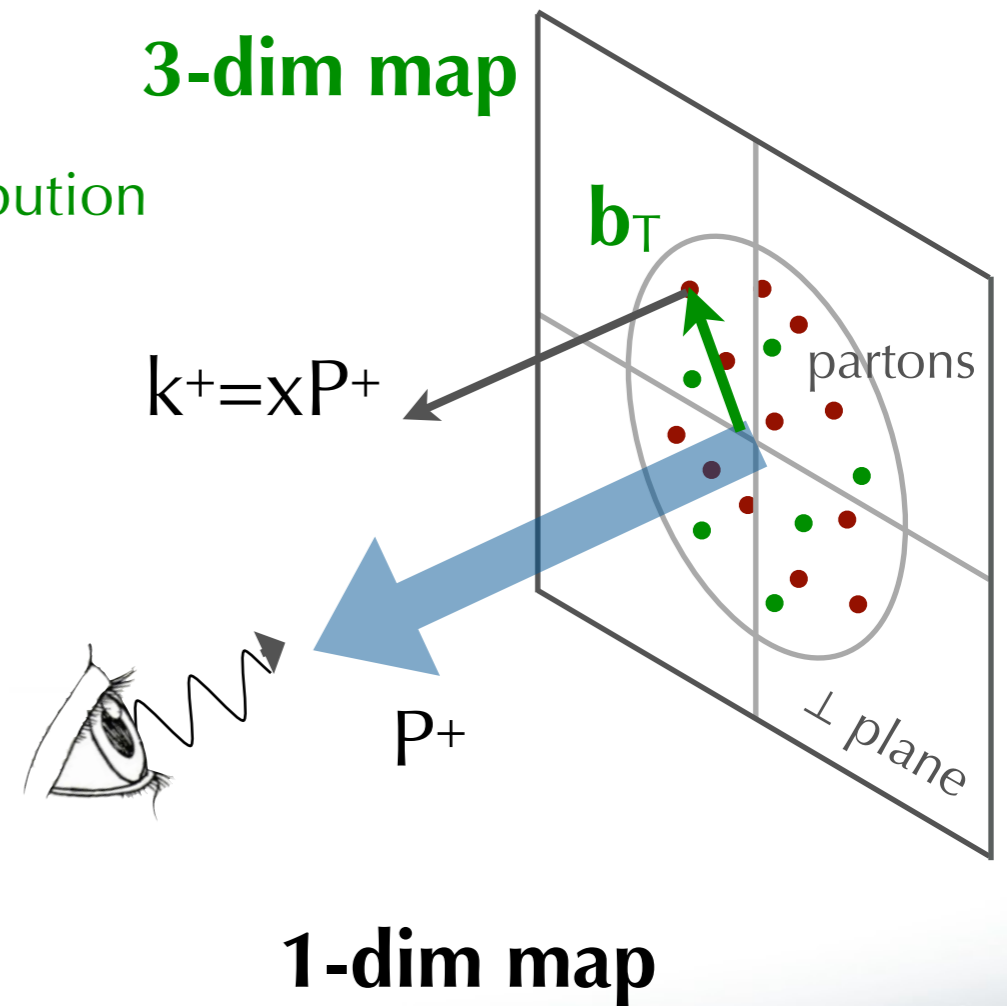
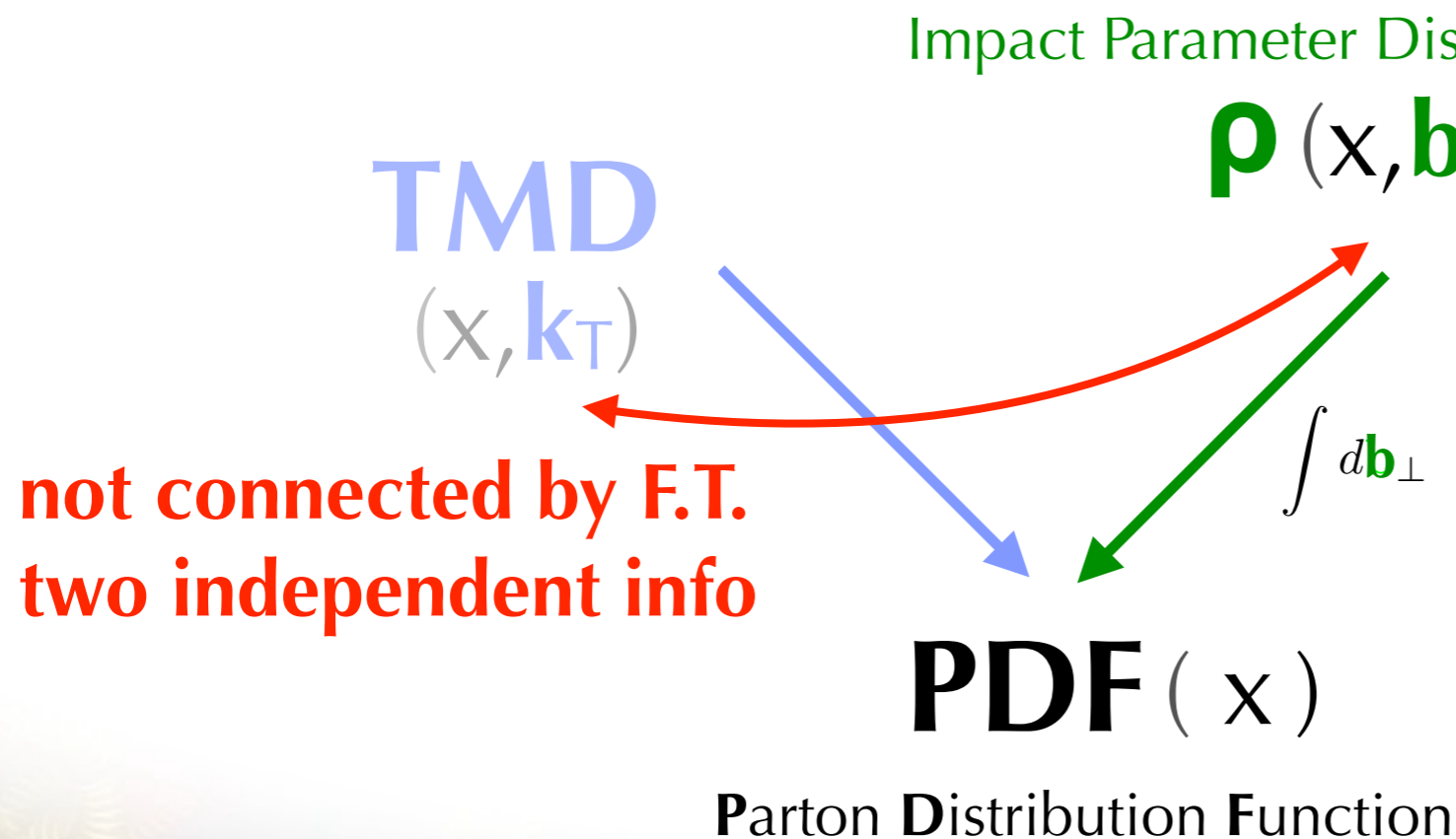
The EIC physics tools

localize partons → baseline info for MPI
(Multi-Particle Interactions)



The EIC physics tools

localize partons → baseline info for MPI
(Multi-Particle Interactions)



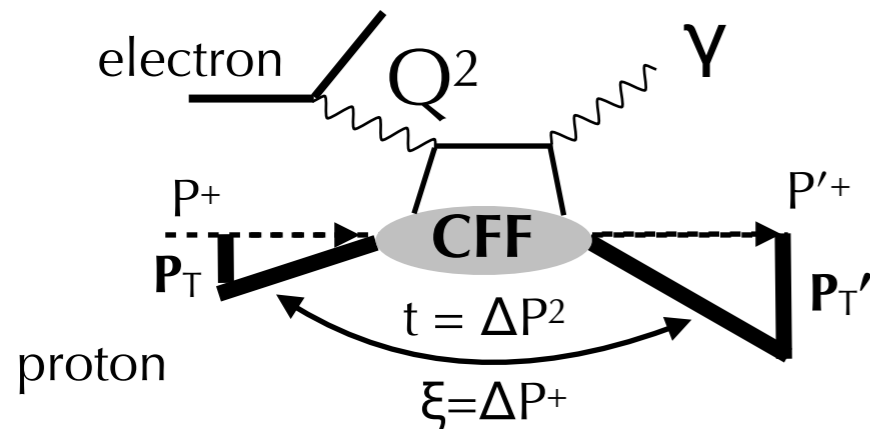
3D-maps in position space

$\rho(x, \mathbf{b}_T)$ can **not** be **directly extracted** from experimental data

$$\rho(x, \mathbf{b}_T)$$

$$\text{GPD}(x, \Delta^+=0, \Delta_T)$$

Fourier Transform



Generalized Parton Distribution $\text{GPD}(x, \xi, t)$ can be **indirectly extracted** from exclusive Deeply-Virtual Compton Scatt. **factorization th.** for $t \ll Q^2$

Compton Form Factor

$$\text{CFF}(\xi, t) = \mathcal{P} \int dx \frac{\text{GPD}(x, \xi, t)}{x - \xi} + i\pi \text{GPD}(\xi, \xi, t) + \mathcal{O}(1/Q)$$

the GPD “zoo” at leading twist

		Quark polarization		
		Unpolarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	H	\times	\mathcal{E}_T
	L	\times	\tilde{H}	$\tilde{\mathcal{E}}_T$
	T	E	\tilde{E}	H_T, \tilde{H}_T

3D-maps in position space

**Lorentz invariance →
polynomiality of GPDs**

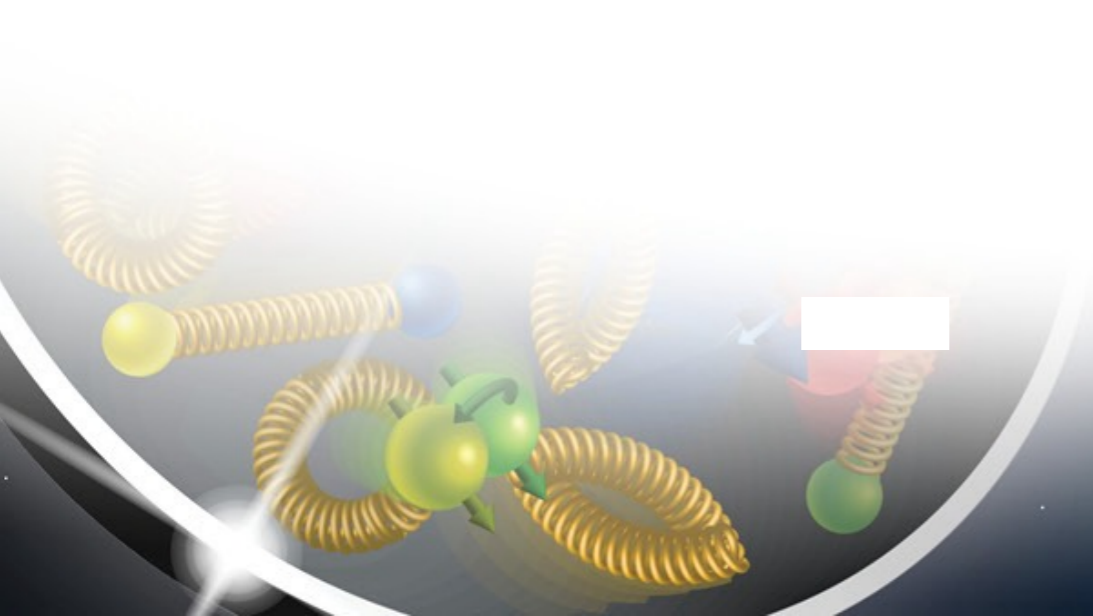
$$\sum_q \int dx x H^q(x, \xi, t) = M_2^Q(t) + \frac{4}{5} d_1^Q(t) \xi^2$$

$$\sum_q \int dx x E^q(x, \xi, t) = 2J^Q(t) - M_2^Q(t) - \frac{4}{5} d_1^Q(t) \xi^2$$

QCD Energy-Momentum Tensor (EMT)

$$T^{\mu\nu} = \bar{\psi} \gamma^\mu \frac{i \overleftrightarrow{D}^\nu}{2} \psi - F^{a\mu\lambda} F^{a\nu}{}_\lambda + \frac{1}{4} g^{\mu\nu} F^2$$

$$\langle p | T_{\mu\nu}^{Q,G} | p' \rangle = \bar{u}(p') \left[M_2^{Q,G}(t) \frac{P_\mu P_\nu}{M_N} + J^{Q,G}(t) \frac{i(P_\mu \sigma_{\nu\rho} + P_\nu \sigma_{\mu\rho}) \Delta^\rho}{2M_N} + d_1^{Q,G}(t) \frac{\Delta_\mu \Delta_\nu - g_{\mu\nu} \Delta^2}{5M_N} + \bar{c}(t) g_{\mu\nu} \right] u(p)$$



3D-maps in position space

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Charges

$M_2(0)$ = contribution of partons to mass and momentum

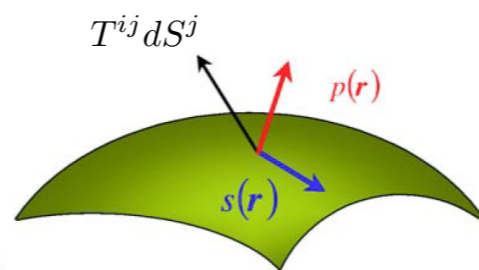
$J(0)$ = angular momentum of partons

$d_1(0)$ = "D-term" related to internal pressure

\bar{c} = "anomalous" contribution to mass (trace $T^\mu{}_\mu$)

	Energy Density	Momentum Density		
T^{00}	T^{01}	T^{02}	T^{03}	
T^{10}	T^{11}	T^{12}	T^{13}	
T^{20}	T^{21}	T^{22}	T^{23}	— shear forces
T^{30}	T^{31}	T^{32}	T^{33}	— pressure
	Energy Flux	Momentum Flux		

Mechanical properties of the Nucleon



Polyakov, P.L. *B555* (03) 57
Metz, Pasquini, Rodini, *arXiv:2006.11171*
Lorcé et al., *arXiv:2109.11785*
....

3D-maps in position space

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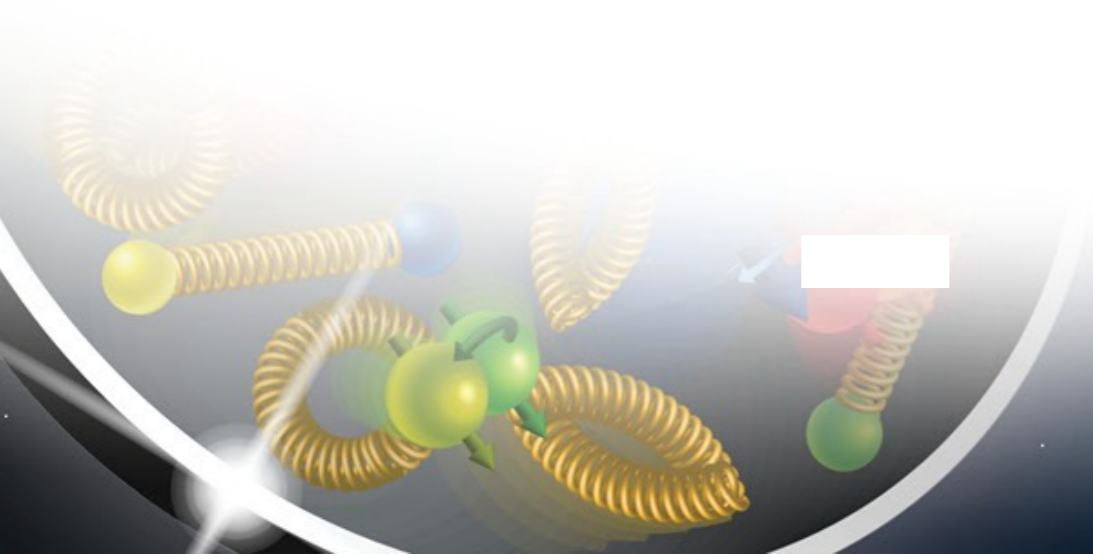
for each flavor q

$$\frac{1}{2} \int dx x \left[H(x, 0, 0) + E(x, 0, 0) \right] = J$$

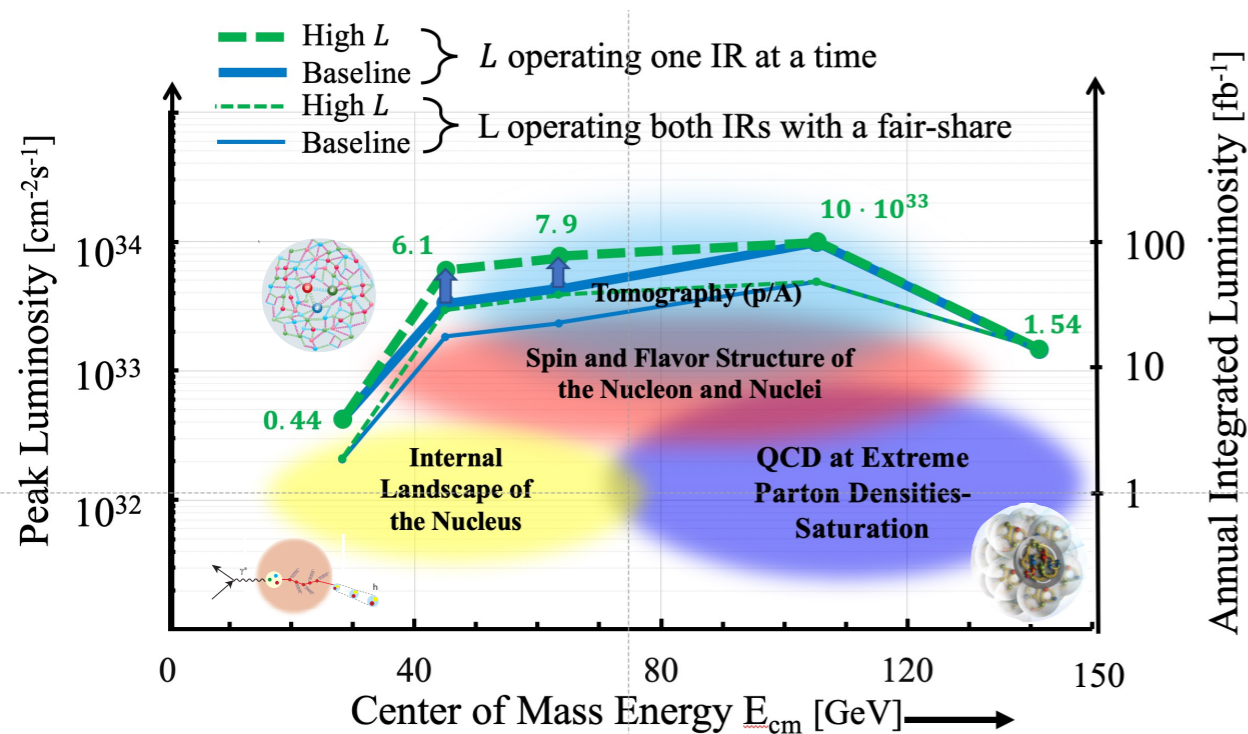
Ji sum rule

X. Ji, P.R.L. 78 (97)

**quark angular
momentum**

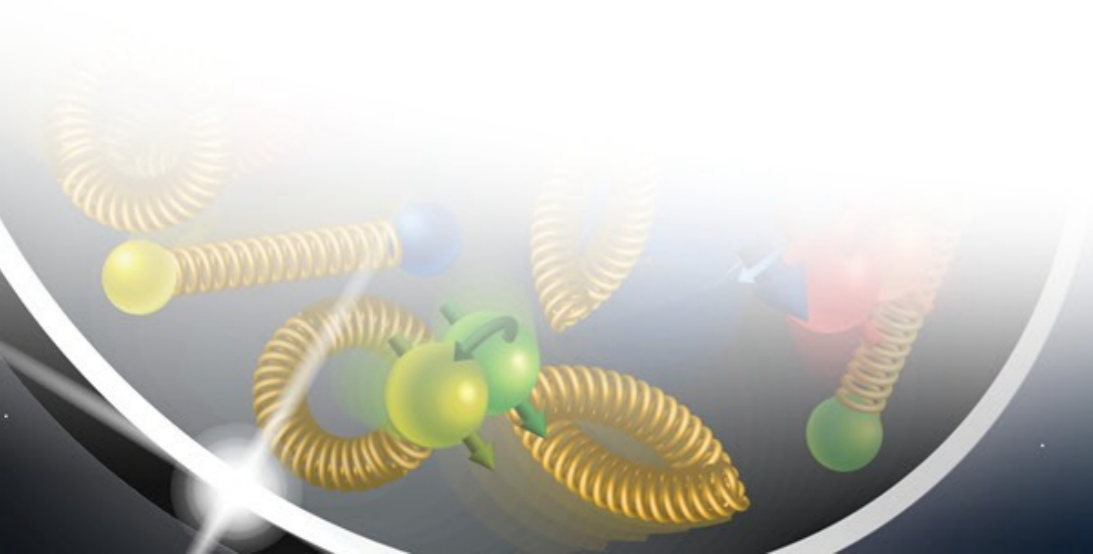


The EIC concept detector

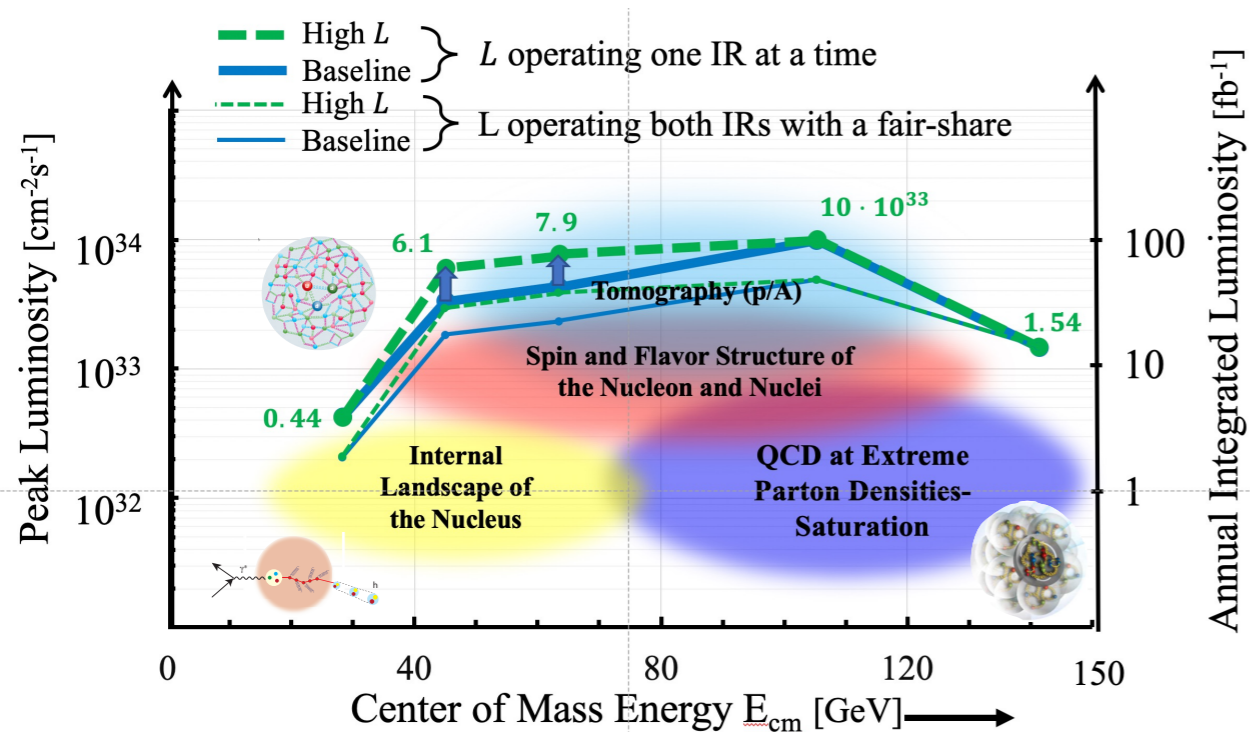


	DIS	binning
GPD	exclusive	x, Q^2, t, θ_P
TMD	semi-inclusive	$x, Q^2, z_h, P_h, \theta_h$
PDF	inclusive	x, Q^2

Detector: hermeticity, high PID over wide range, high momentum resolution, calorimeter granularity, coverage of far backward-forward region, ...



The EIC concept detector

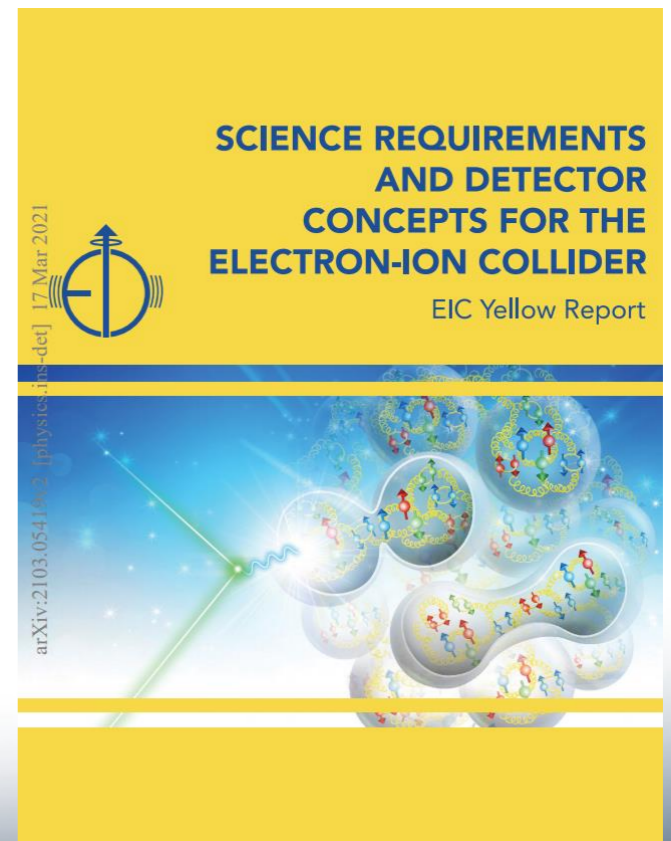


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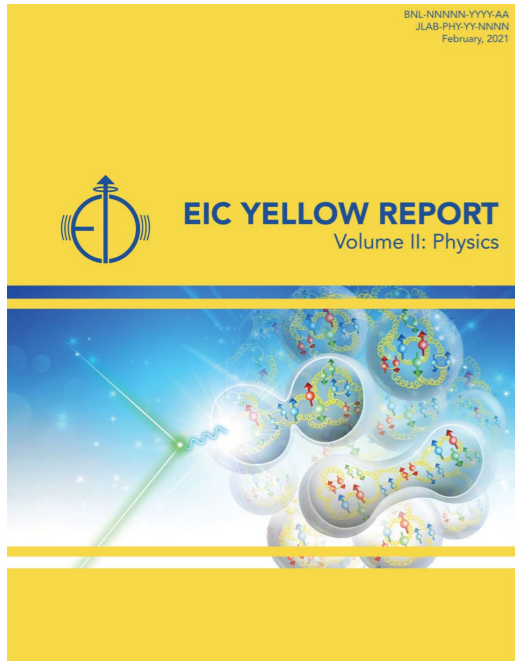
Detector: hermeticity, high PID over wide range, high momentum resolution, calorimeter granularity, coverage of far backward-forward region, ...

Enormous community effort: 902 pp, 415 authors, 151 instit.'s
Vol I (Exec. Summary) , **Vol II** (Physics) , **Vol. III** (Detector)

arXiv:2103.05419 (N.P.A in press)

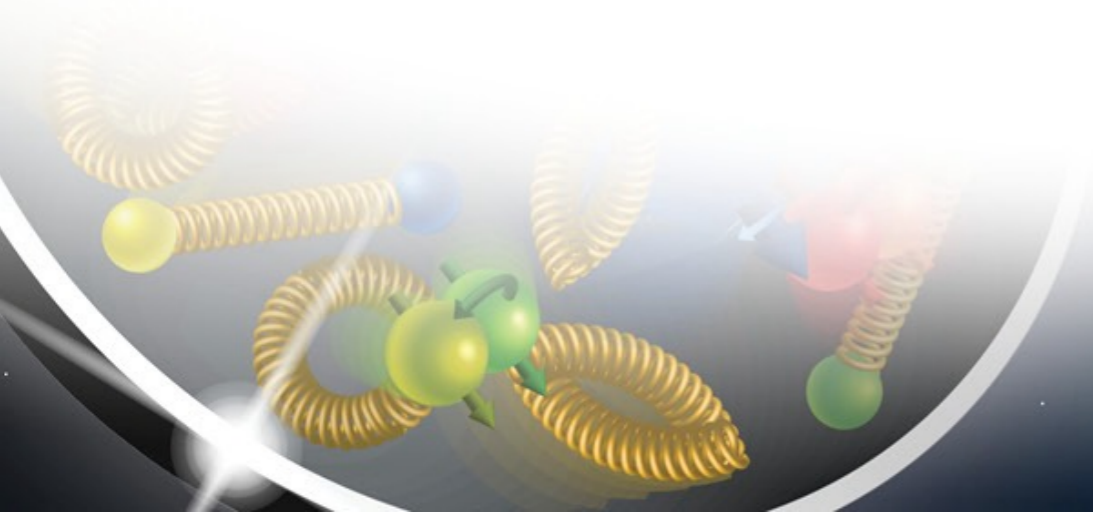


The EIC Yellow Report

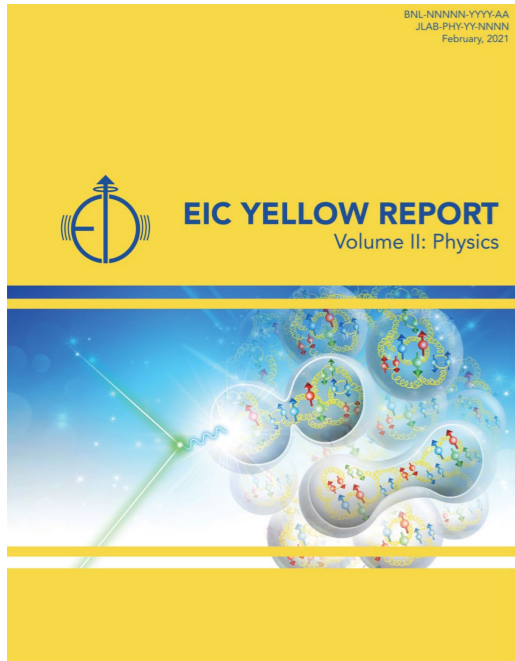


Volume II: Physics	35
5 Introduction to Volume II	37
6 The EIC Physics Case	40
7 EIC Measurements and Studies	52
7.1 Global Properties and Parton Structure of Hadrons	52
7.2 Multi-dimensional Imaging of Nucleons, Nuclei, and Mesons	105
7.3 The Nucleus: A Laboratory for QCD	146
7.4 Understanding Hadronization	186
7.5 Connections with Other Fields	214
7.6 Connected Theory Efforts	248

- ## 5 Working Groups
- Inclusive reactions
 - Semi-inclusive “
 - Exclusive “
 - Diffractive “
 - Jets & Heavy Quarks



The EIC Yellow Report



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- ## 5 Working Groups
- Inclusive reactions
 - Semi-inclusive “
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 - Jets & Heavy Quarks

7.1 Global Properties and Parton Structure of Hadrons

- 7.1.1 **Unpolarized parton structure of the proton and neutron**
- 7.1.2 **Spin structure of the proton and neutron**
- 7.1.3 Parton structure of mesons
- 7.1.4 **Origin of the mass of the nucleon and mesons**
- 7.1.5 Multi-parton correlations
- 7.1.6 Inclusive diffraction and rapidity gap physics
- 7.1.7 Global event shapes and the strong coupling constant

7.3 The Nucleus: A Laboratory for QCD

- 7.3.1 **High parton densities and saturation**
- 7.3.2 Diffraction
- 7.3.3 **Nuclear PDFs**
- 7.3.4 Particle propagation through matter and transport properties of nuclei
- 7.3.5 Collective effects
- 7.3.6 Special opportunities with jets and heavy quarks
- 7.3.7 Short-range correlations, origin of nuclear force
- 7.3.8 Structure of light nuclei
- 7.3.9 Coherent and incoherent photoproduction on heavy targets

7.5 Connections with Other Fields

- 7.5.1 Electro-weak and BSM physics
- 7.5.2 Neutrino physics
- 7.5.3 Cosmic ray/astro-particle physics
- 7.5.4 Other connections to pp, pA, AA
- 7.5.5 Connections with HEP and Snowmass Process

7.6 Related Theory Efforts

- 7.6.1 Lattice QCD
- 7.6.2 Radiative corrections at the EIC

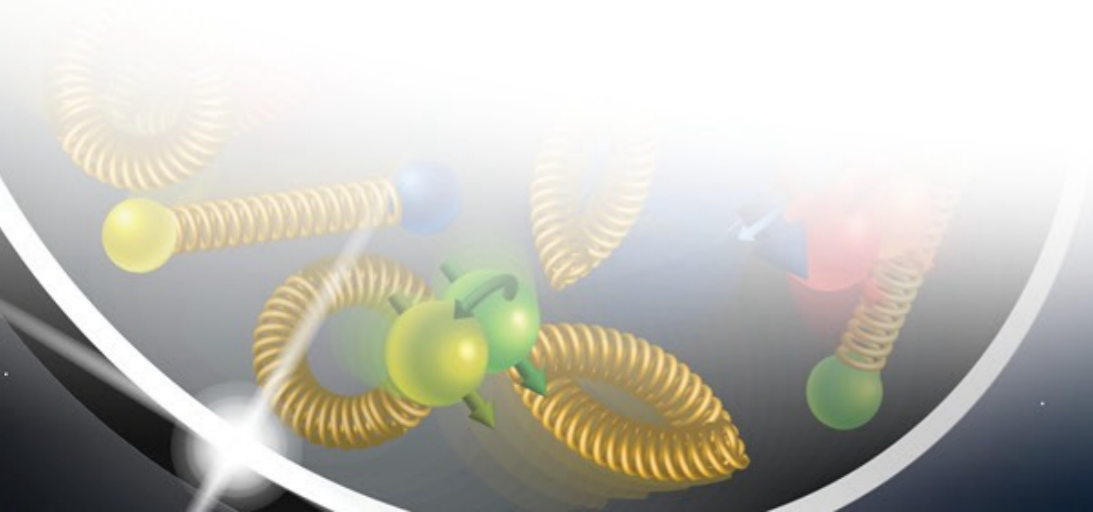
**some highlights on
projected performance
about PDFs, TMDs, GPDs**

7.4 Understanding Hadronization

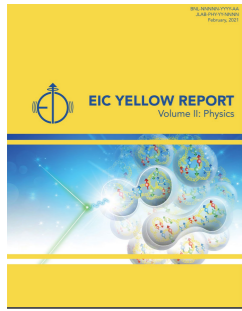
- 7.4.1 Hadronization in the vacuum
- 7.4.2 Hadronization in the nuclear environment
- 7.4.3 Particle production for identified hadron species
- 7.4.4 Production mechanism for quarkonia and exotic states
- 7.4.5 New particle production mechanisms
- 7.4.6 Spectroscopy

1-Dim Maps

collinear PDF (x)



The EIC performance : unpolarized PDFs

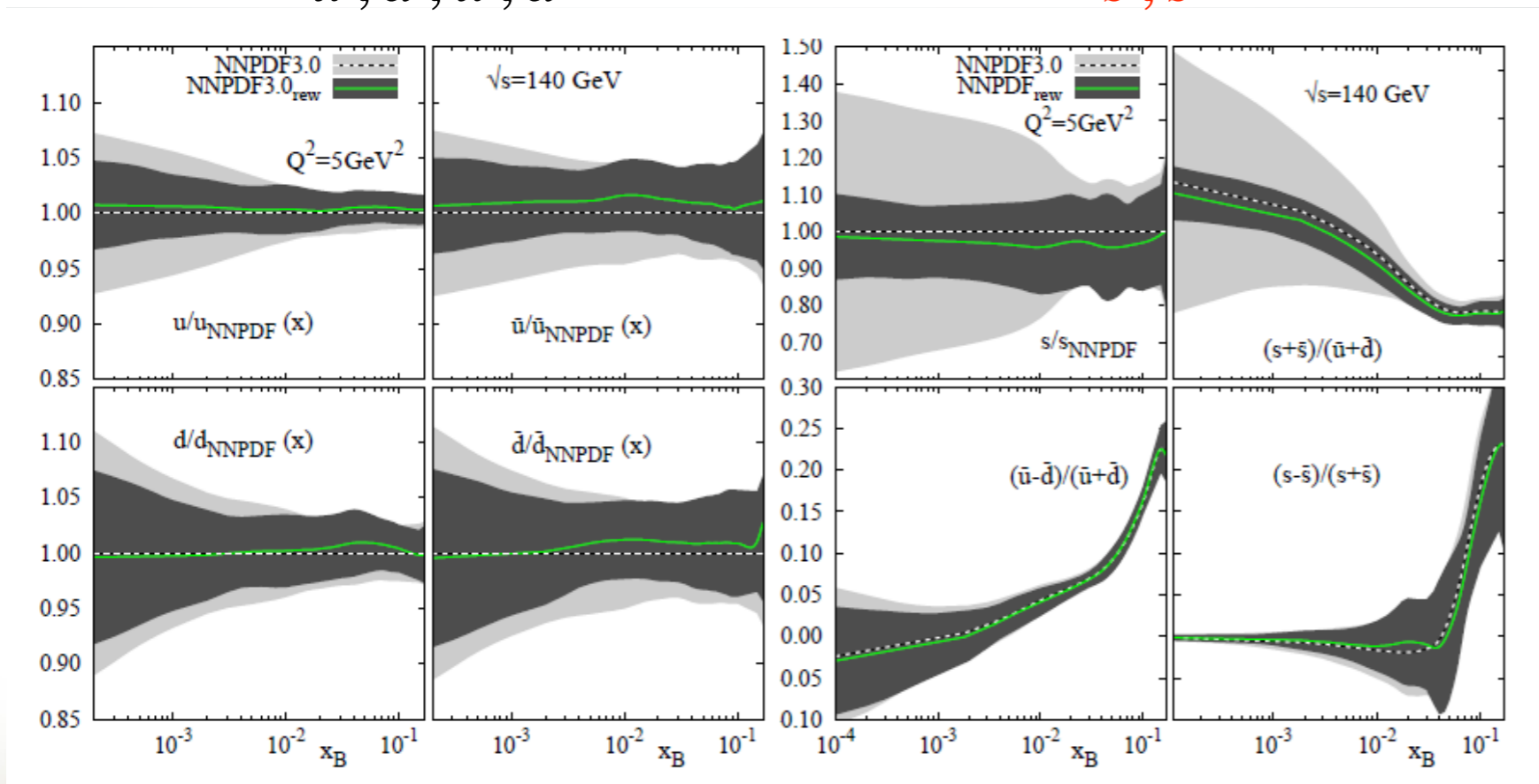


arXiv:2103.05419,
N.P.A in press

impact on unpolarized sea-quark PDFs

moderate on
 u, d, \bar{u}, \bar{d}

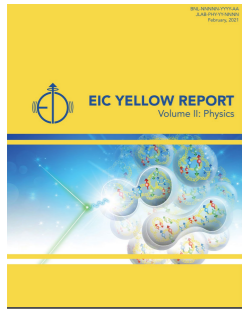
large improvement on
 s, \bar{s}



EIC at $\sqrt{s} = 140$ GeV SIDIS $e p \rightarrow e' (K^\pm, \pi^\pm) X$ $\mathcal{L} = 10 \text{ fb}^{-1}$

Aschenauer et al., P.R. D99 (19) 094004

The EIC performance : unpolarized PDFs



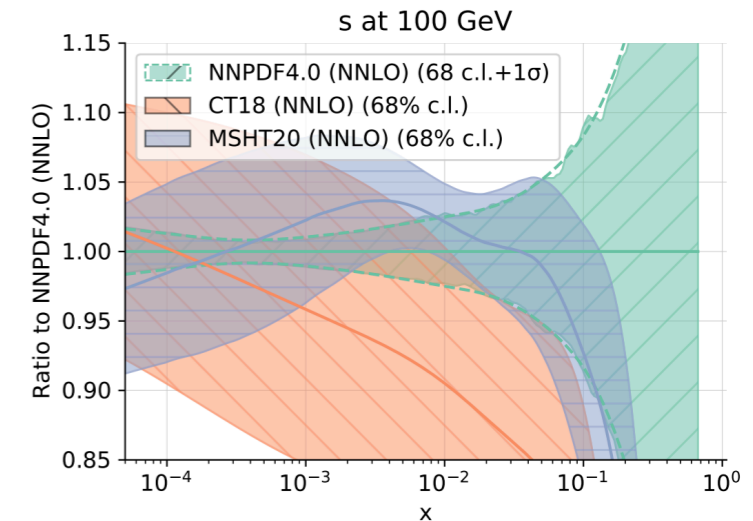
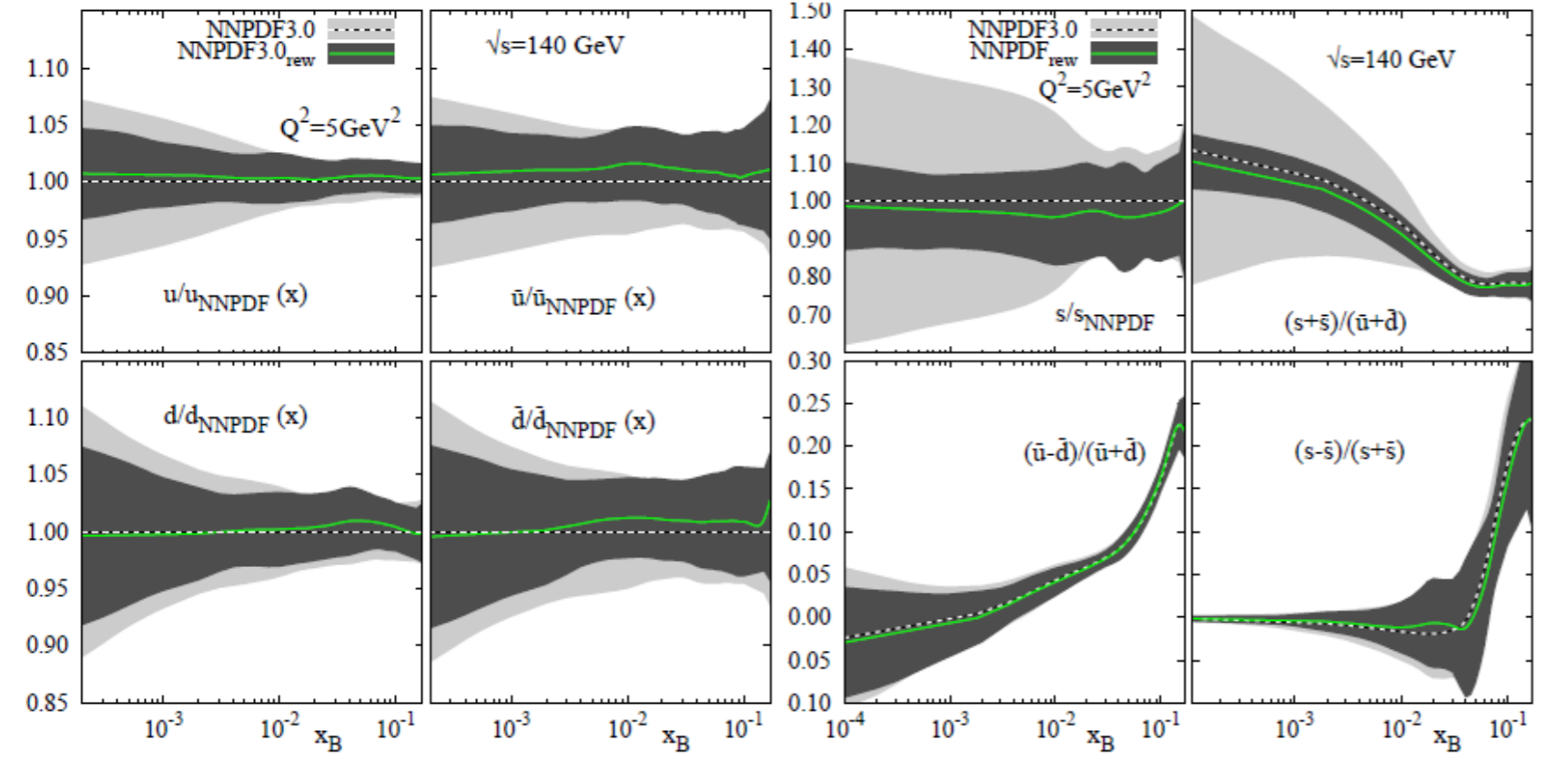
arXiv:2103.05419,
N.P.A in press

impact on unpolarized sea-quark PDFs

moderate on
 u, d, \bar{u}, \bar{d}

large improvement on
 s, \bar{s}

current large uncertainties
in strange content



Rojo @QCD-N 2021

also projected precision could help
to establish intrinsic charm content
of the proton

**important info for
BSM searches from
"BSM-independent"
source**

EIC at $\sqrt{s} = 140$ GeV SIDIS $e p \rightarrow e' (K^\pm, \pi^\pm) X$ $\mathcal{L} = 10 \text{ fb}^{-1}$

Aschenauer et al., P.R. D99 (19) 094004

The EIC performance : BSM explorations

Abdul Khalek et al., "Snowmass 2021 White Paper: EIC for High Energy Physics" arXiv:2203.13199

Parity Violating DIS

$$\vec{e} - p$$

$$A_{PV} \longrightarrow \sin^2 \theta_W$$

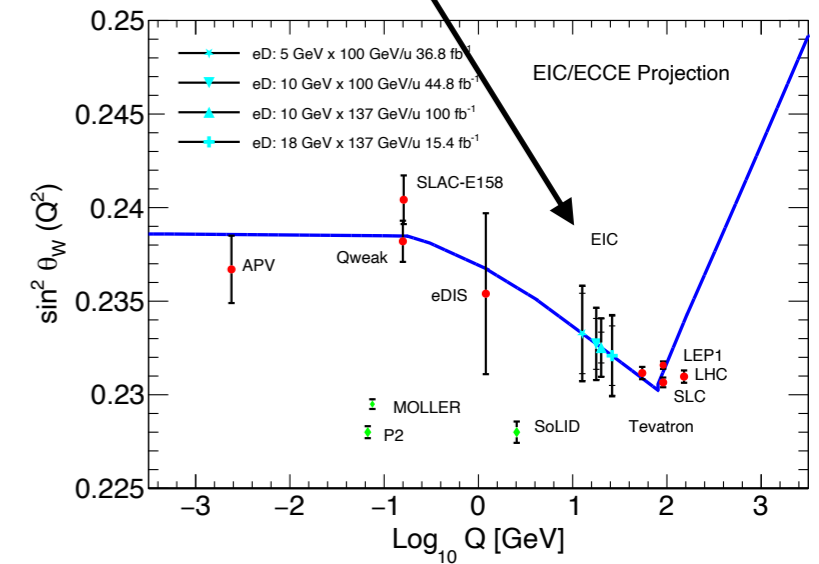
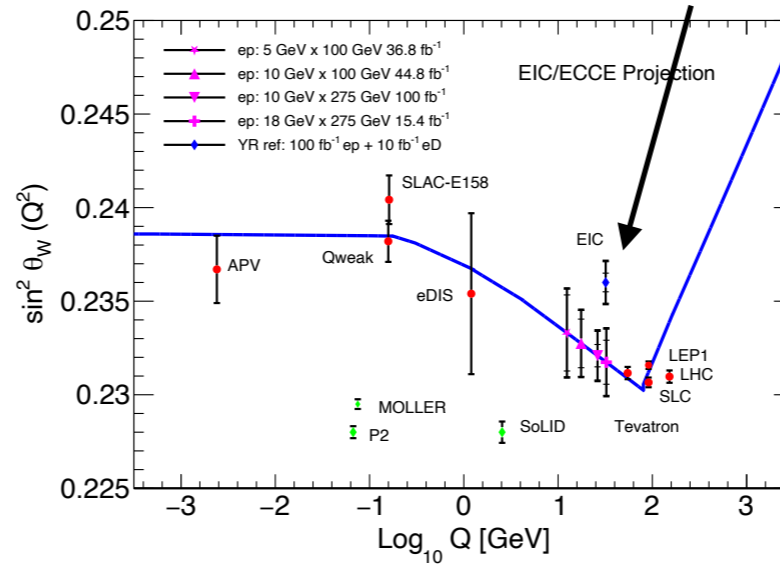
correlated PDF uncertainties

CT18NLO

MMHT2014nlo_68cl

NNPDF3.1_nlo_as_0118

bridging low- to high-energies



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Abdul Khalek et al., "Snowmass 2021 White Paper: EIC for High Energy Physics" arXiv:2203.13199

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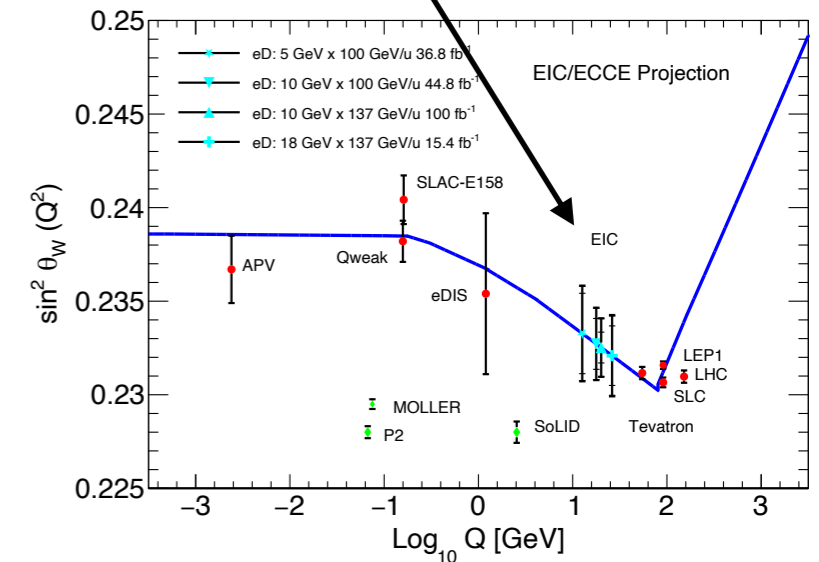
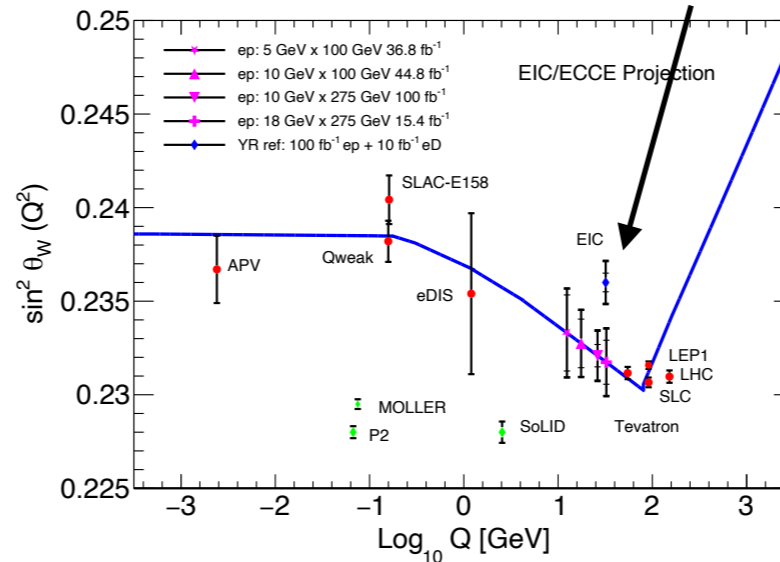
correlated PDF uncertainties

CT18NLO

MMHT2014nlo_68cl

NNPDF3.1_nlo_as_0118

bridging low- to high-energies



SMEFT

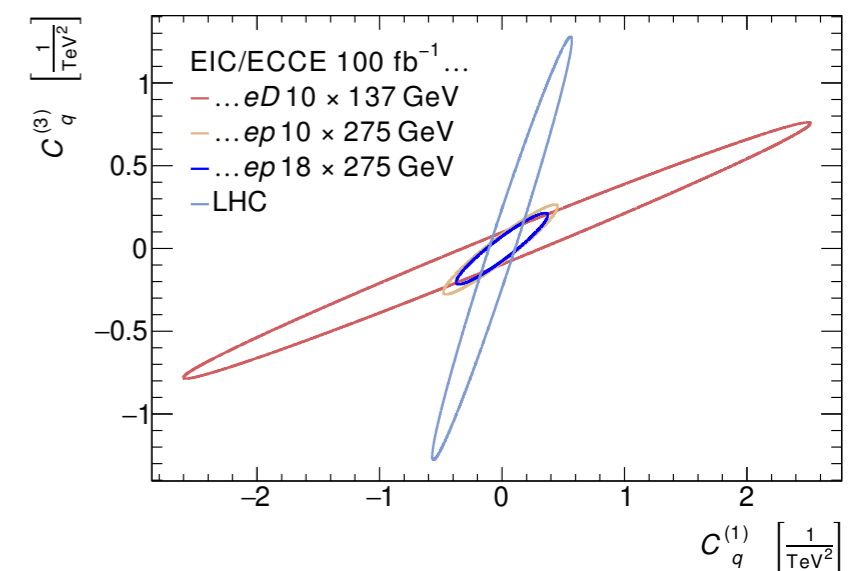
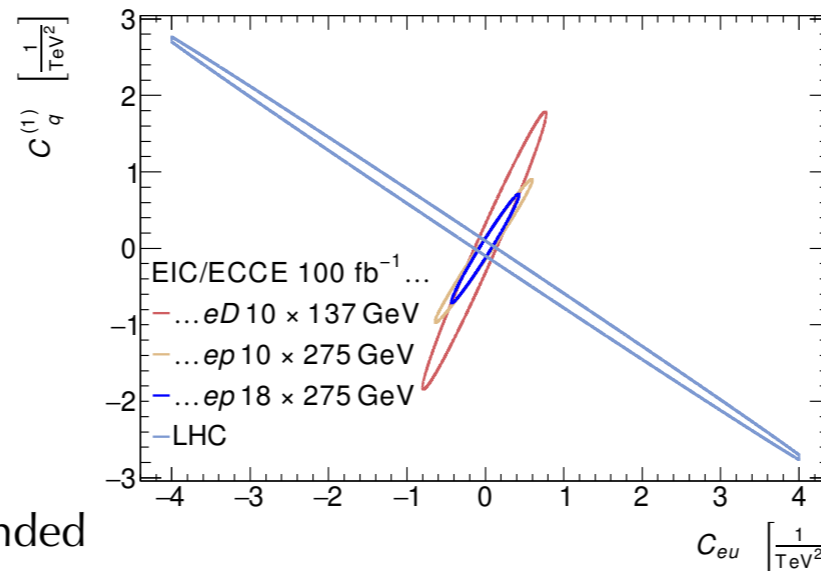
$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i C_i \mathcal{O}_i + \dots$$

$\mathcal{O}_{lq}^{(1)}$	$(\bar{l}\gamma^\mu l)(\bar{q}\gamma_\mu q)$
$\mathcal{O}_{lq}^{(3)}$	$(\bar{l}\gamma^\mu \tau^I l)(\bar{q}\gamma_\mu \tau^I q)$
\mathcal{O}_{eu}	$(\bar{e}\gamma^\mu e)(\bar{u}\gamma_\mu u)$
\mathcal{O}_{ed}	$(\bar{e}\gamma^\mu e)(\bar{d}\gamma_\mu d)$
\mathcal{O}_{lu}	$(\bar{l}\gamma^\mu l)(\bar{u}\gamma_\mu u)$
\mathcal{O}_{ld}	$(\bar{l}\gamma^\mu l)(\bar{d}\gamma_\mu d)$
\mathcal{O}_{qe}	$(\bar{q}\gamma^\mu q)(\bar{e}\gamma_\mu e)$

u, d, e right-handed

q, ℓ left-handed doublets

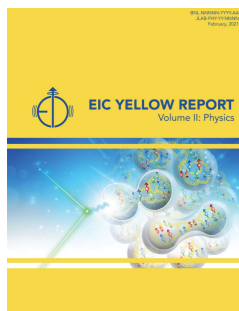
reducing degeneracy



fit of - ATLAS Drell-Yan data
- EIC PVDIS pseudodata

Aad et al., arXiv:1606.01736

The EIC performance : polarized PDFs



arXiv:2103.05419,
N.P.A in press

N spin sum rule $\frac{1}{2} = \Delta\Sigma + \Delta g + L_q + L_g$

impact on gluon & quark helicities

singlet

$$x\Delta\Sigma = x \sum_q \Delta q$$

no EIC

$x\Delta g$

EIC $\sqrt{s} = 45$ GeV

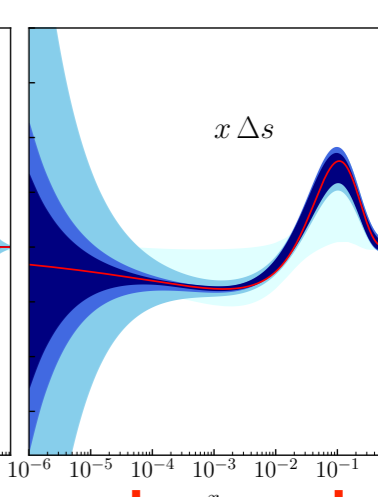
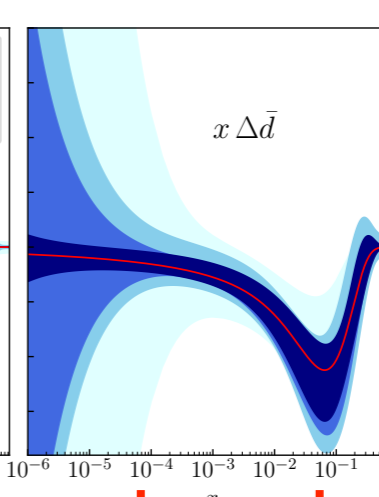
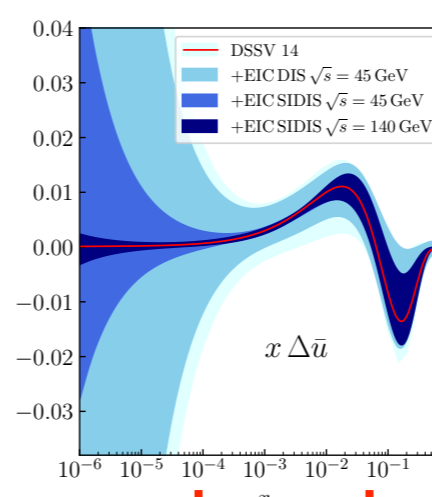
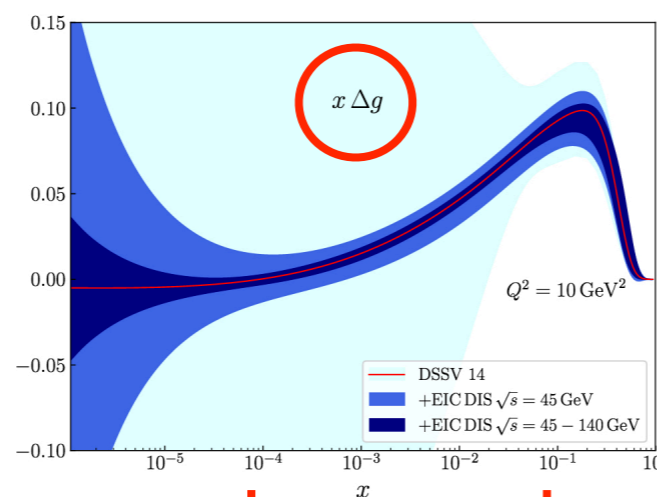
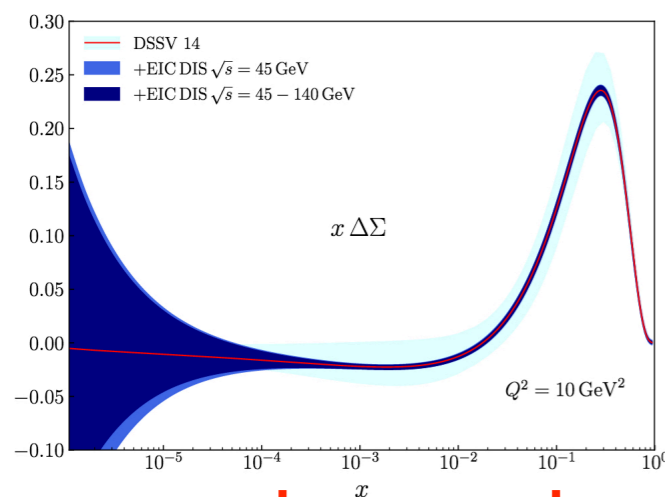
$x\Delta\bar{u}$

EIC $\sqrt{s} = 45 - 140$ GeV

$x\Delta\bar{d}$

DIS & SIDIS pseudo-data

$x\Delta s$



Borsa et al., P.R. D102 (20) 094018

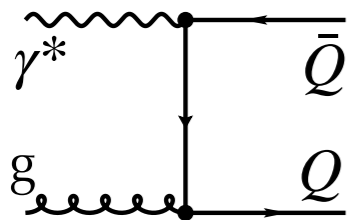
remarkable constraints in range $10^{-4} < x < 10^{-1}$, particularly for gluon helicity

still large uncertainties for $x < 10^{-4}$ beyond reach of the EIC

The EIC performance : polarized PDFs

impact on gluon helicity

Heavy-flavor production represents $\sim 15\%$ of inclusive DIS cross section at EIC kin.
Main channel **γ -g fusion sensitive to Δg at tree level**



Simulation of $\vec{e} \vec{p} \rightarrow e' + D^0 + X$ at EIC
with $Q^2=10 \text{ GeV}^2$ and $\mathcal{L}=100 \text{ fb}^{-1}$

Observable: $A_{LL}^{c\bar{c}} \propto \frac{g_1^{c\bar{c}}}{F_1^{c\bar{c}}}$

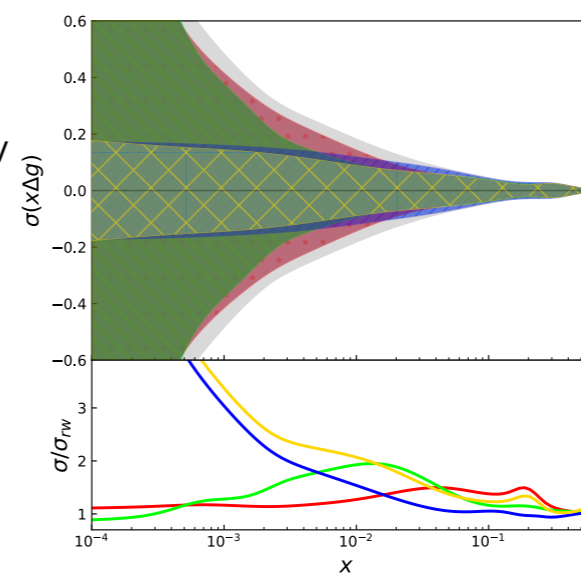
Impact on uncertainty σ of $x\Delta g(x)$

Anderle et al, arXiv:2110.04489

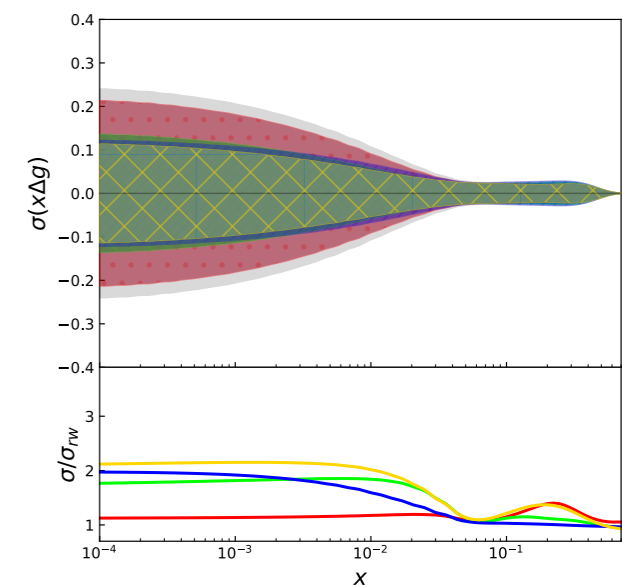
- baseline
- 5 GeV \times 41 GeV
- 5 GeV \times 100 GeV
- 18 GeV \times 275 GeV
- All config

reweighting
before
after

NNPDFpol1.1



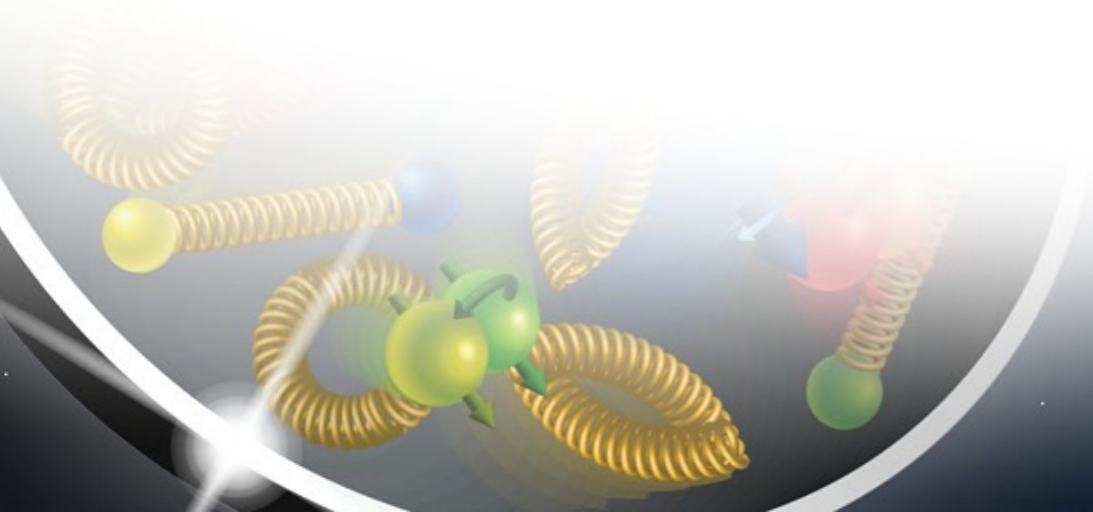
DSSV14



The EIC performance : TMDs

3-Dim Maps in momentum space

TMD (x, k_T)



The EIC performance : unpolarized TMDs

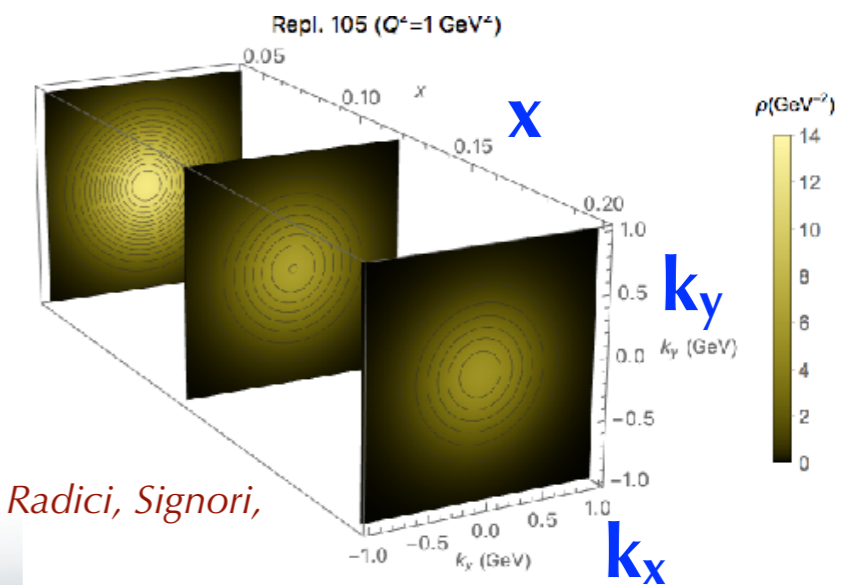
the unpolarized quark TMD $f_{1q}(x, \mathbf{k}_T)$

the best known TMD (most recent fits)

	Framework	HERMES	COMPASS	DY	Z production	N of points	χ^2/N_{points}
PV 2017 arXiv:1703.10157	NLL	✓	✓	✓	✓	8059	1.5
SV 2017 arXiv:1706.01473	NNLL'	✗	✗	✓	✓	309	1.23
BSV 2019 arXiv:1902.08474	NNLL'	✗	✗	✓	✓	457	1.17
SV 2019 arXiv:1912.06532	N ³ LL	✓	✓	✓	✓	1039	1.06
PV 2019 arXiv:1912.07550	N ³ LL	✗	✗	✓	✓	353	1.07
MAP 2022 in preparation	N ³ LL	✓	✓	✓	✓	2031	1.06

tomography in momentum space

PV 2017
Bacchetta, Delcarro, Pisano, Radici, Signori,
JHEP **06** (17) 081



The EIC performance : unpolarized TMDs

the unpolarized quark TMD $f_{1q}(x, k_T)$

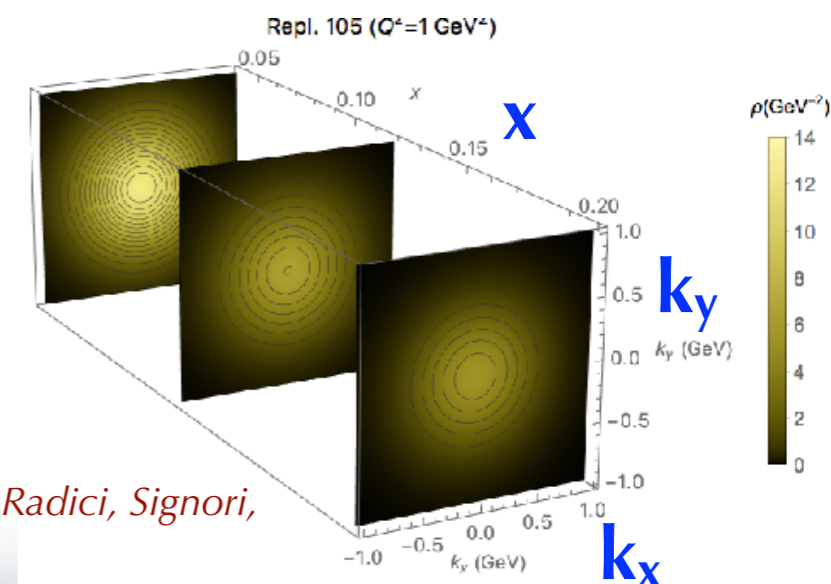
Lessons to be learnt :

- non-perturbative k_T dependence is not a simple Gaussian
- average $\langle k_T^2 \rangle$ strongly depends on x , and might depend on flavor (in particular for fragmentation)
- Gaussian non perturbative evolution seems preferred
- modern fits can reach $N^3LL+NNLO$ perturbative accuracy with reduced $\chi^2 \sim 1$ on thousands data points

the best known TMD (most recent fits)

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tomography in momentum space



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JHEP **06** (17) 081

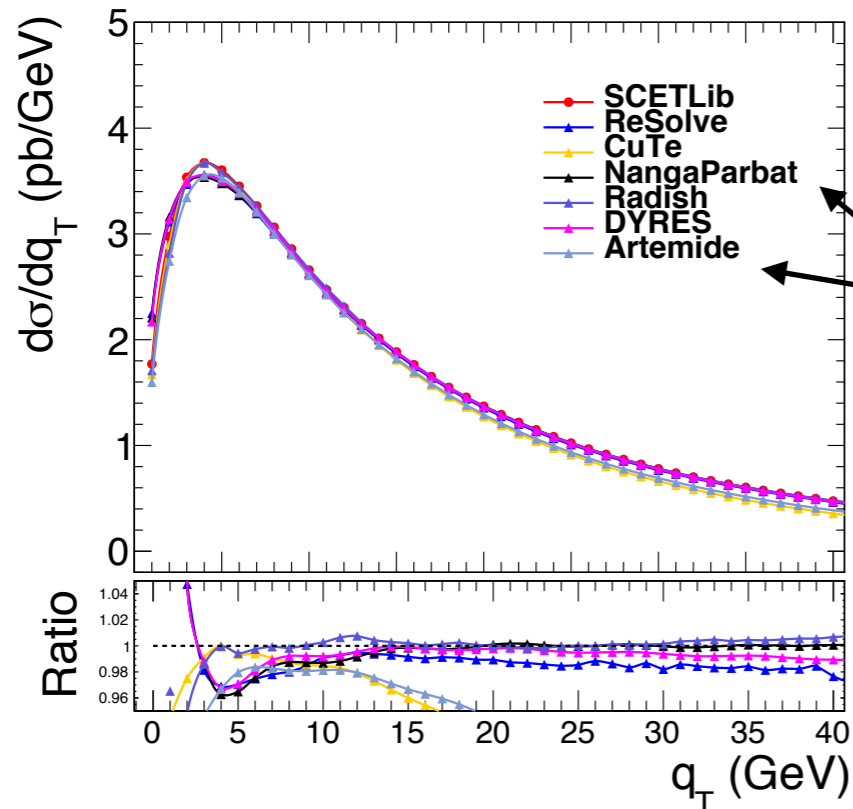
The EIC performance : unpolarized TMDs

the unpolarized quark TMD $f_{1q}(x, k_T)$

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same accuracy as PDF
benchmarking codes @LHC

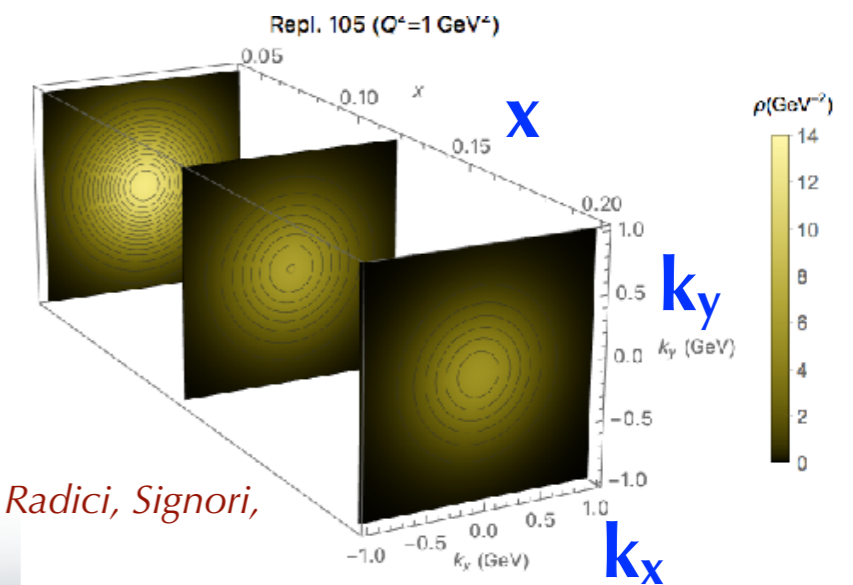


Z production at $\eta=0$ (ATLAS kin)

G. Bozzi, I. Scimemi (eds.) et al.,
Yellow Report of CERN EW WG, in preparation

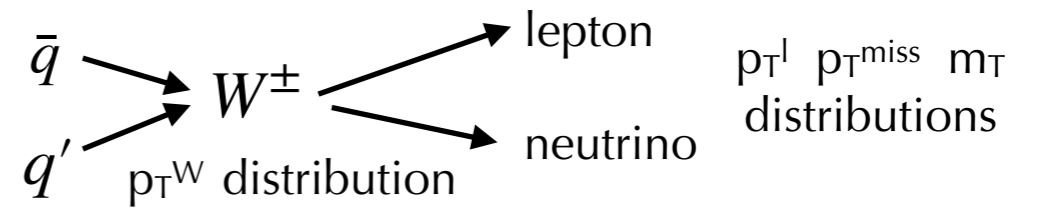
tomography in
momentum space

PV 2017
Bacchetta, Delcarro, Pisano, Radici, Signori,
JHEP **06** (17) 081

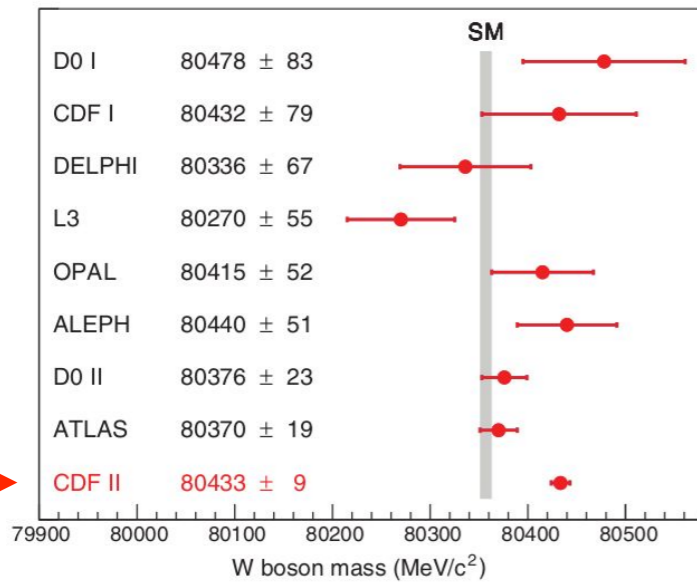


Impact on M_W extraction

QCD radiation
intrinsic quark k_T

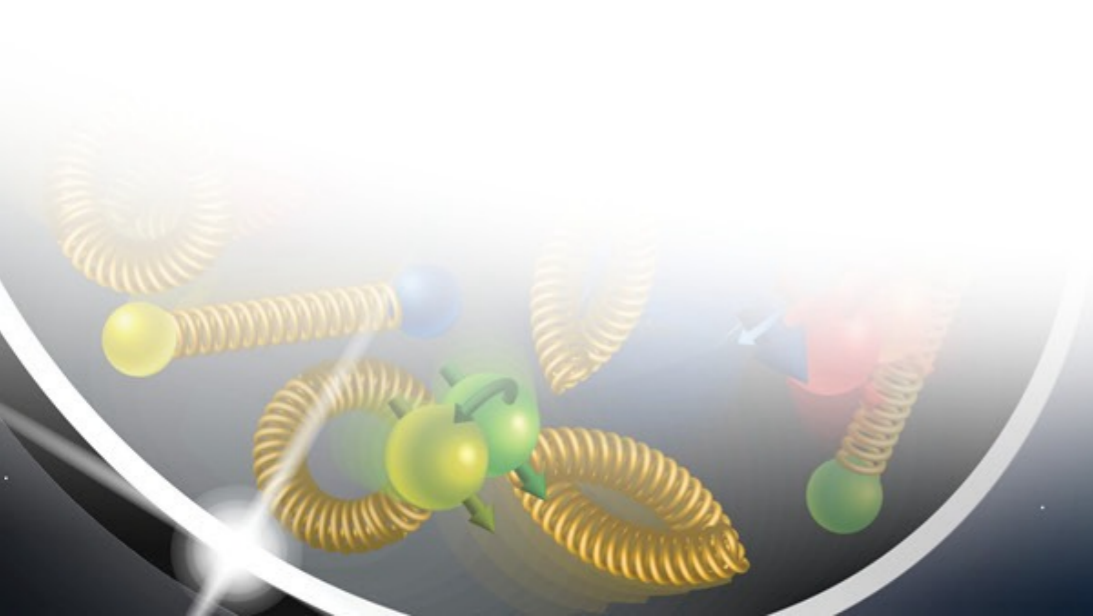


surprising CDF result



~ 7σ ! →

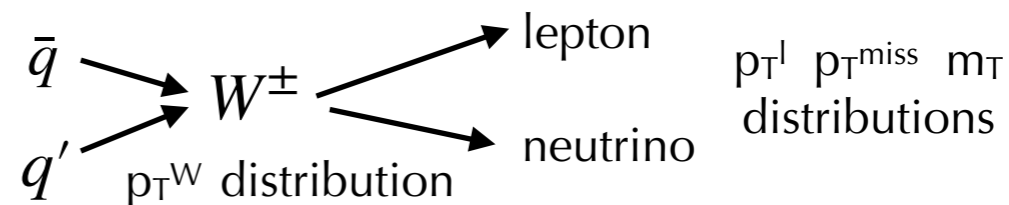
SM expectation: $M_W = 80357 \pm 6$ MeV



Impact on M_W extraction

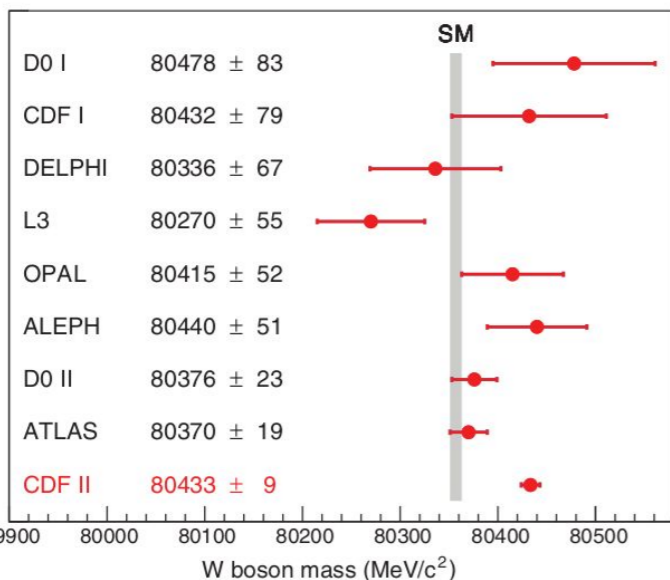
QCD radiation

intrinsic quark k_T



surprising CDF result

but all analyses assume a flavor-independent Gaussian



~ 7σ ! →

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Physics Letters B 788 (2019) 542–545

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Effect of flavor-dependent partonic transverse momentum on the determination of the W boson mass in hadronic collisions

Alessandro Bacchetta^{a,b,*}, Giuseppe Bozzi^{a,b}, Marco Radici^b, Mathias Ritzmann^c, Andrea Signori^d

^a Dipartimento di Fisica, Università di Pavia, via Bassi 6, I-27100 Pavia, Italy
^b INFN, Sezione di Pavia, via Bassi 6, I-27100 Pavia, Italy
^c Nikhef, Science Park 105, NL-1098 XG Amsterdam, the Netherlands
^d Theory Center, Thomas Jefferson National Accelerator Facility, 12000 Jefferson Avenue, Newport News, VA 23606, USA

template fit

50 **pseudo-data sets** of “Z-equivalent”
flavor-dep. k_T -distrib.
 at $M_W=80.385$ GeV

30 **templates** of **flavor-indep.** k_T -distrib.

set 1

...

set 50

template 1: $M_W=80.370$ $\chi^2_{\text{set-i}}(1)$

⋮

best $\chi^2_{\text{set-i}}(\dots)$

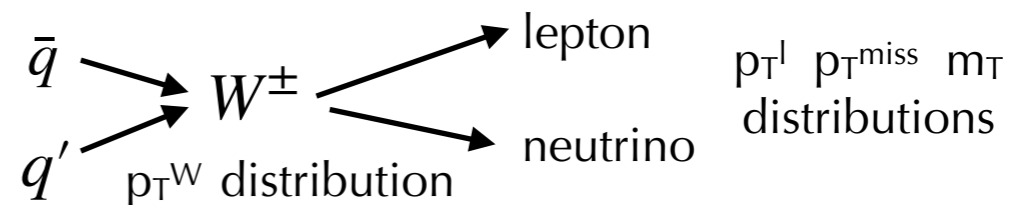
template 30: $M_W=80.400$ $\chi^2_{\text{set-i}}(30)$

Signori et al., JHEP11 (13) 194

Impact on M_W extraction

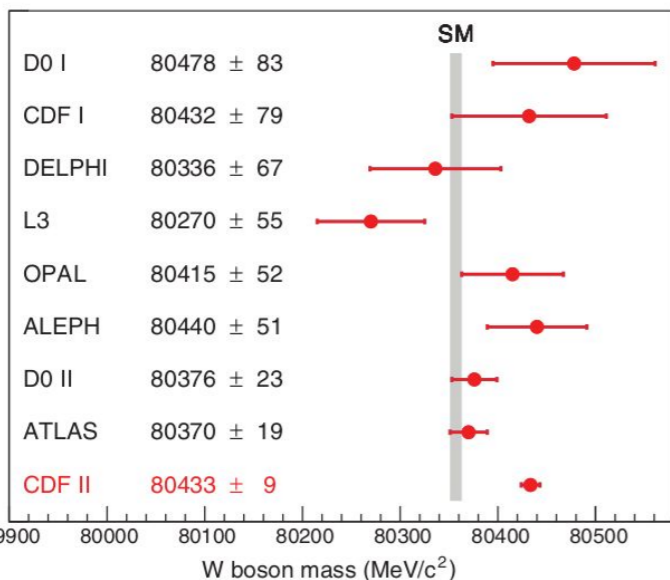
QCD radiation

intrinsic quark k_T



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but all analyses assume a flavor-independent Gaussian



$\sim 7\sigma!$

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^d Theory Center, Thomas Jefferson National Accelerator Facility, 12000 Jefferson Avenue, Newport News, VA 23606, USA

SM expectation: $M_W = 80357 \pm 6$ MeV

additional uncertainty

$$-6 \leq \Delta M_{W^+} \leq 9$$

$$-4 \leq \Delta M_{W^-} \leq 3$$

in opposite directions!

± 2.5 MeV stat. uncertainty

template fit

50 **pseudo-data sets** of “Z-equivalent”
flavor-dep. k_T -distrib.
 at $M_W = 80.385$ GeV

30 **templates** of **flavor-indep.** k_T -distrib.

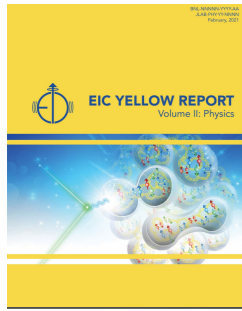
template 1: $M_W = 80.370$ $\chi^2_{\text{set-i}}(1)$

⋮
 best $\chi^2_{\text{set-i}}(\dots)$

template 30: $M_W = 80.400$ $\chi^2_{\text{set-i}}(30)$

set 1 ... set 50
Signori et al., JHEP11 (13) 194

The EIC performance : unpolarized TMDs



arXiv:2103.05419,
N.P.A in press

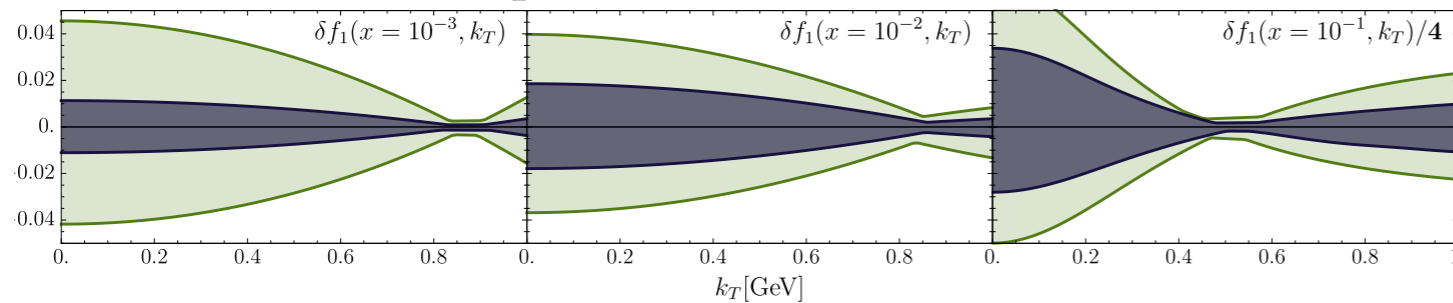
EIC impact

$Q = 2 \text{ GeV}$

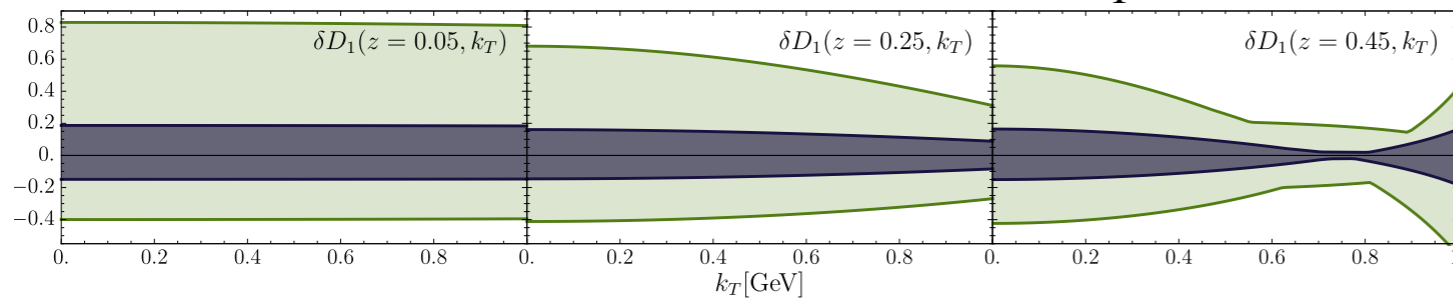
SIDIS $e p \rightarrow e' \pi^\pm X$

$\mathcal{L} = 10 \text{ fb}^{-1}$

unpolarized TMDPDF $f_1^u(x, k_T; Q)$



unpolarized TMDFF $D_1^{u \rightarrow \pi^+}(z, P_T; Q)$



SV 2019



+ EIC

$e^- \rightarrow \leftarrow p$

5×41

5×100

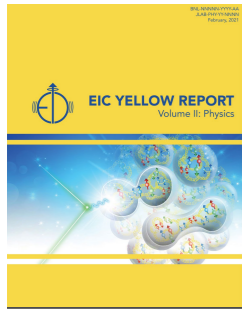
10×100

18×100

18×275

GeV

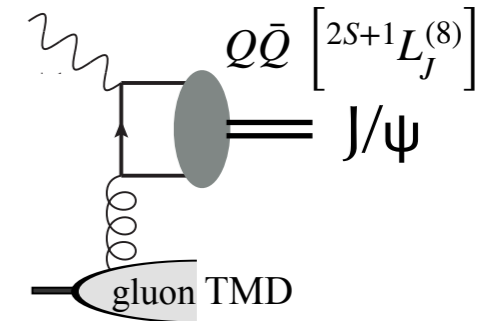
The EIC performance : unpolarized TMDs



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N.P.A in press

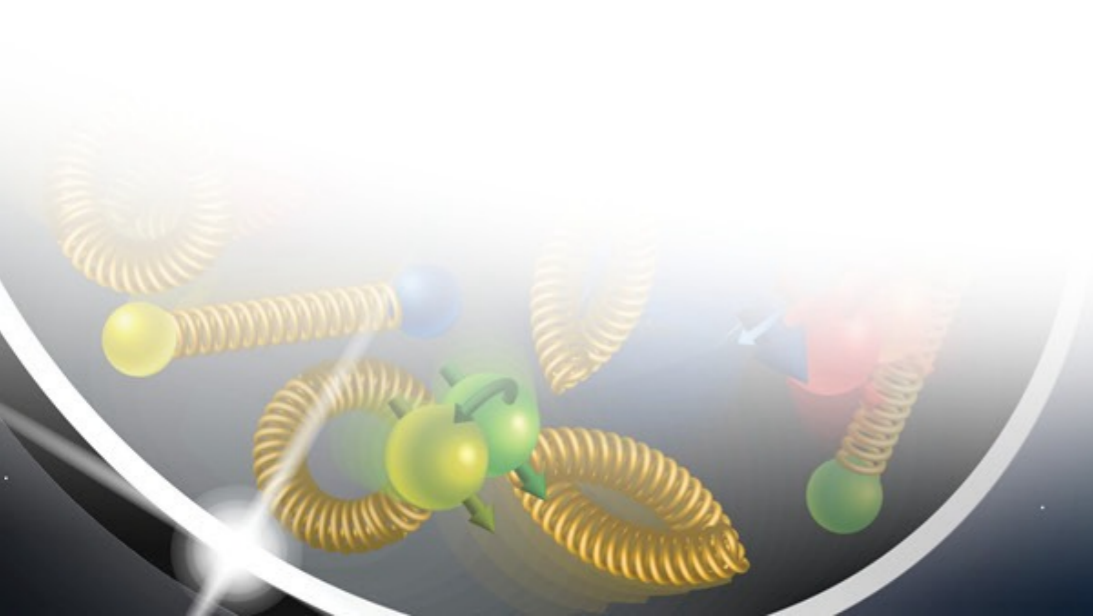
EIC : explore the unknown gluon TMD

- gluons carry “two color charges” → difficult to neutralize
- useful channels: heavy-quarkonium → production of J/ψ , ...
back-to-back di-jet production

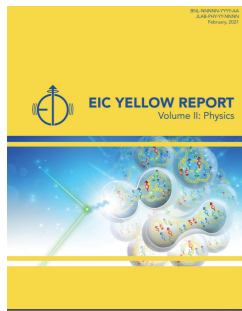


Bacchetta et al., arXiv:1809.02056

D'Alesio et al., arXiv:1908.00446



The EIC performance : unpolarized TMDs

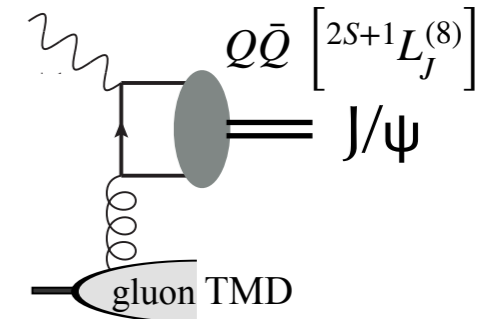


arXiv:2103.05419,
N.P.A in press

EIC : explore the unknown gluon TMD

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- useful channels: heavy-quarkonium → production of J/ψ , ...
back-to-back di-jet production



Bacchetta et al., arXiv:1809.02056
D'Alesio et al., arXiv:1908.00446

- unknown “Shape function” $Q\bar{Q} \rightarrow J/\psi$

Boer et al., arXiv:2004.06740
Boer et al., arXiv:2102.00003
D'Alesio et al., arXiv:2110.07529
Fleming et al., arXiv:1910.03586
Echevarria, arXiv:1907.06494
....

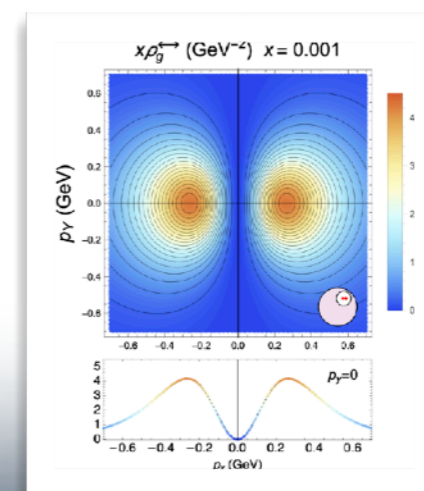
depend on angular momentum and color structure of $Q\bar{Q}$
must be extracted from experiment ← opportunity at the EIC

- also model calculation

Bacchetta et al., arXiv:2005.02288

gluon density in unpol. proton

$$\rho_g^{\leftrightarrow} = \frac{1}{2} \left[f_1^g + \frac{k_x^2 - k_y^2}{2M^2} h_1^{\perp g} \right]$$

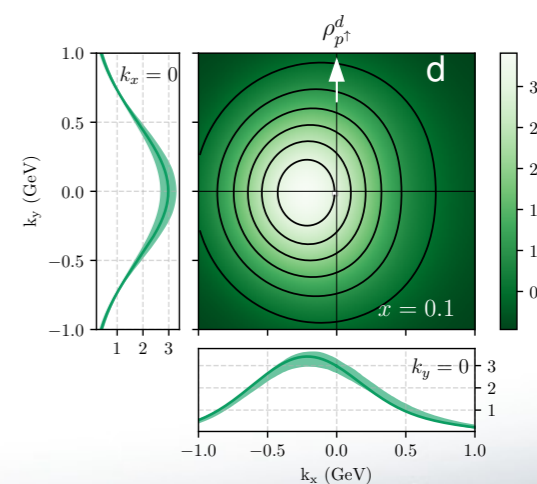
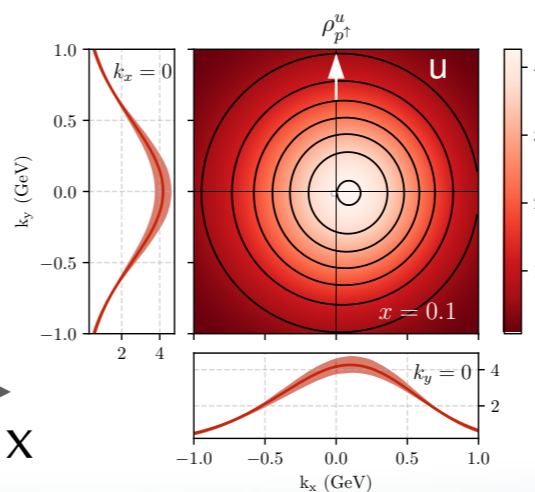
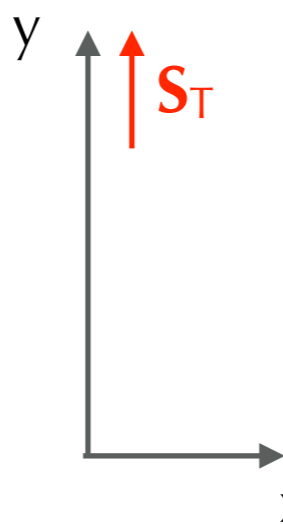
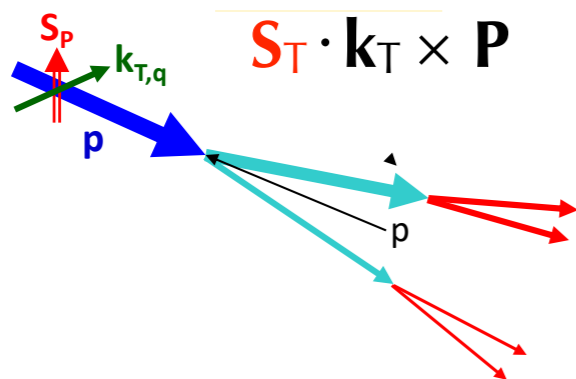


The EIC performance : polarized TMDs

the Sivers TMD $f_{1T\perp q}(\mathbf{x}, \mathbf{k}_T)$

how the momentum distribution of unpolarized quarks is distorted by the transverse polarization of the nucleon
 → access to quark orbital angular momentum

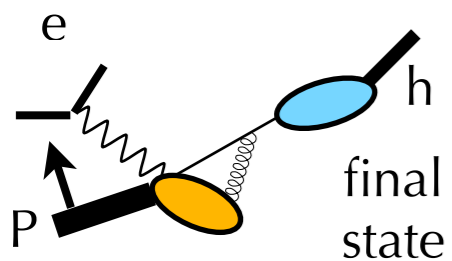
		Quark polarization		
		Unpolarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$f_1 = \odot$	✗	$h_1^\perp = \uparrow \ominus - \downarrow \ominus$
	L	✗	$g_1 = \odot \rightarrow - \ominus \rightarrow$	$h_{1L}^\perp = \uparrow \rightarrow - \downarrow \rightarrow$
	T	$f_{1T}^\perp = \uparrow \odot - \downarrow \ominus$	$g_{1T} = \odot \rightarrow - \ominus \rightarrow$	$h_1 = \uparrow \uparrow - \downarrow \uparrow$ $h_{1T}^\perp = \uparrow \rightarrow - \downarrow \rightarrow$



Bacchetta et al., P.L. **B827** (22) 136961, arXiv:2004.14278

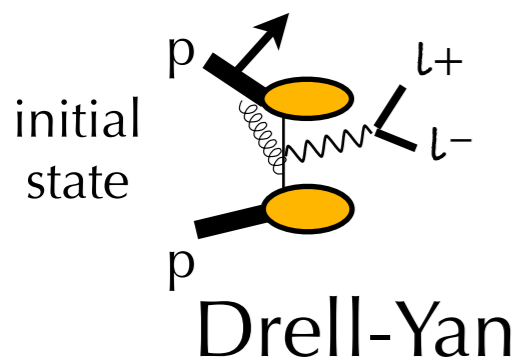
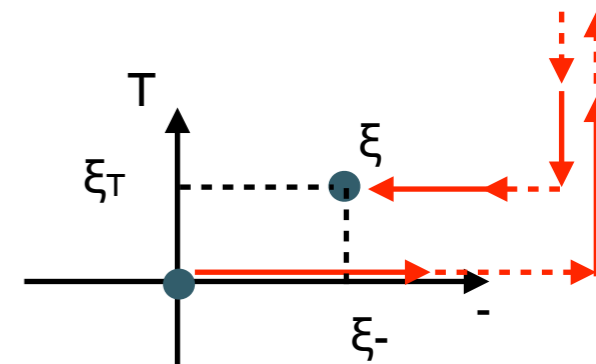
The EIC performance : polarized TMDs

the quark Sivers TMD is not universal !



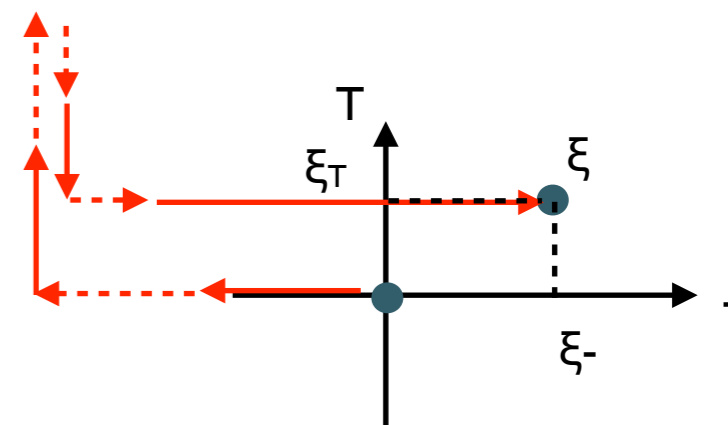
SIDIS

in SIDIS, gauge link structure is "future pointing" → describes residual color final-state interactions



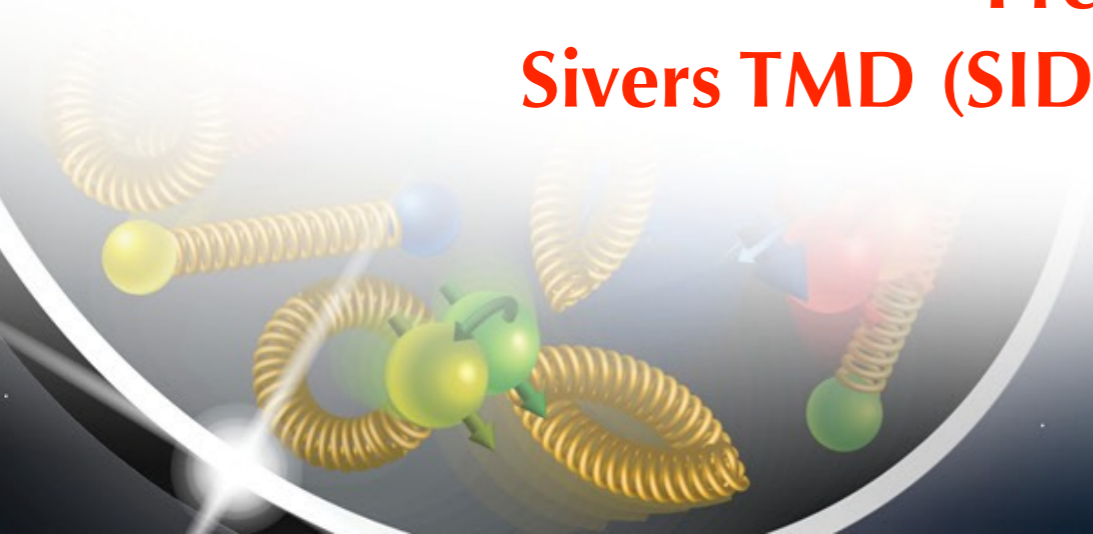
Drell-Yan

in Drell-Yan, gauge link structure is "past pointing" → describes color initial-state interactions



Prediction of QCD:

Sivers TMD (SIDIS) = - Sivers TMD (Drell-Yan)



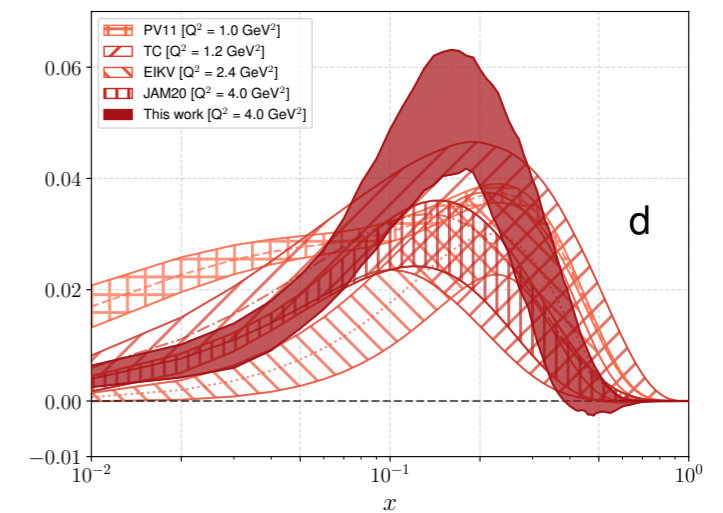
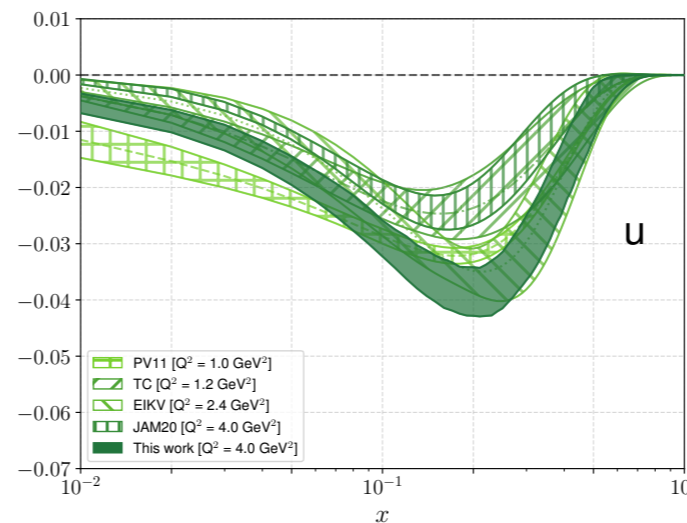
The EIC performance : polarized TMDs

most recent extractions of quark Sivers

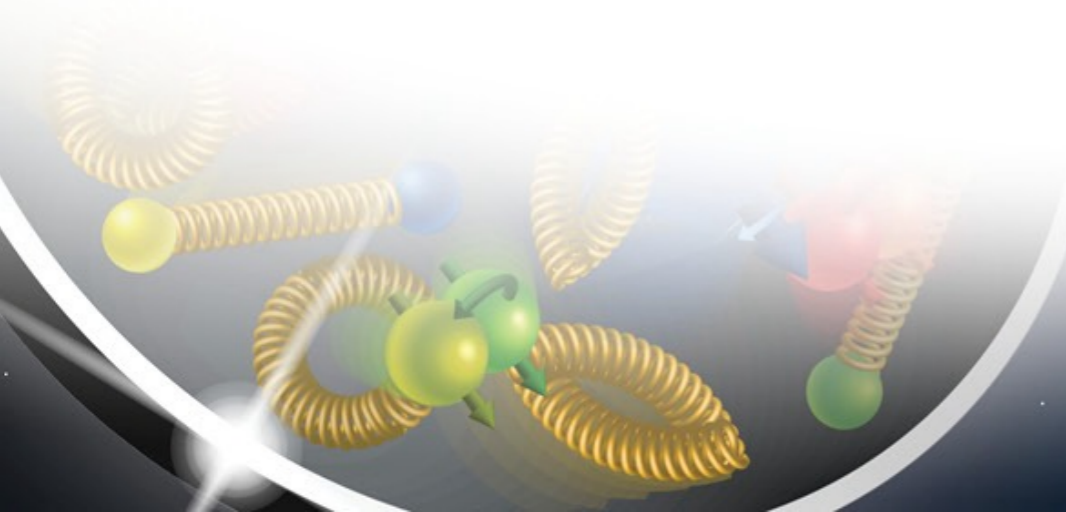
	Framework	SIDIS	DY	W/Z production	e+e-	N of points
JAM 2020 arXiv:2002.08384	extended parton model	✓	✓	✓	✓	517
Pavia 2020 arXiv:2004.14278	LO+NLL	✓	✓	✓	✗	150
EKT 2020 arXiv:2009.10710	NLO+N ² LL	✓	✓	✓	✗	243
BPV 2020 arXiv:2012.05135 arXiv:2103.03270	ζ prescription	✓	✓	✓	✗	76

all parametrizations are in fair agreement for valence flavors

sea-quarks $\sim O(10^{-3})$ smaller

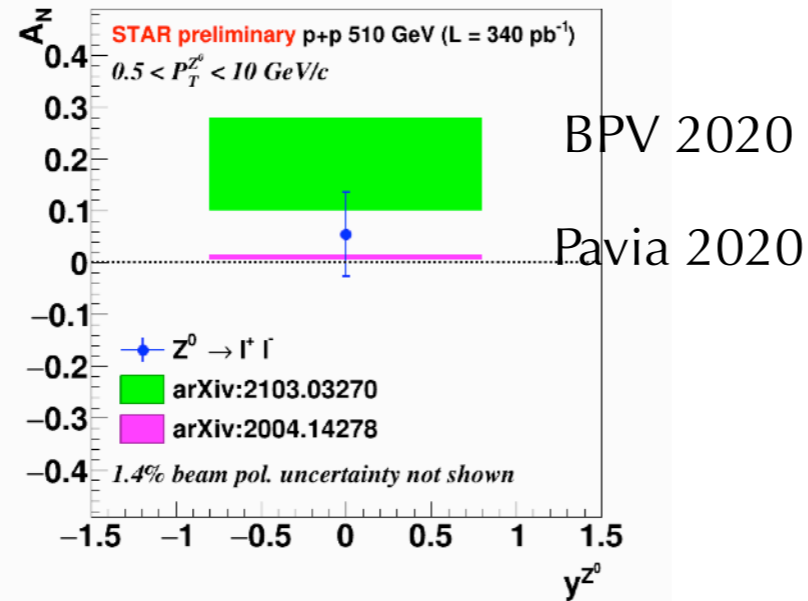
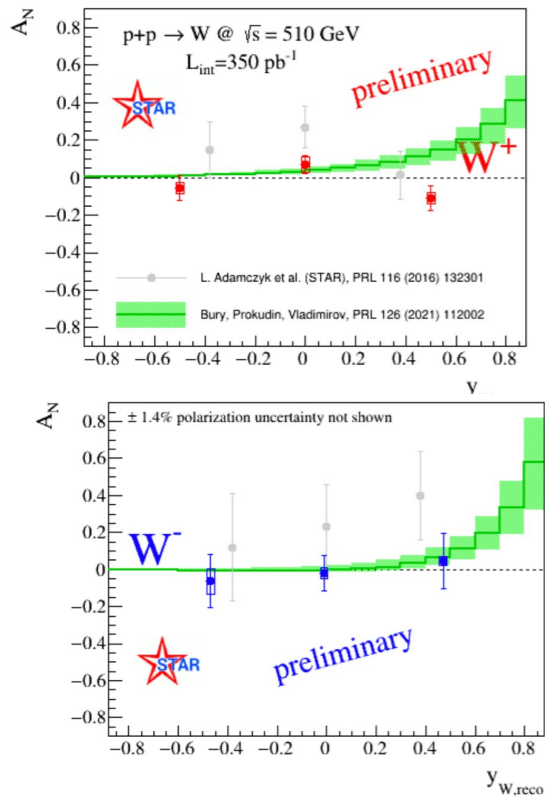


Bacchetta et al., arXiv:2004.14278

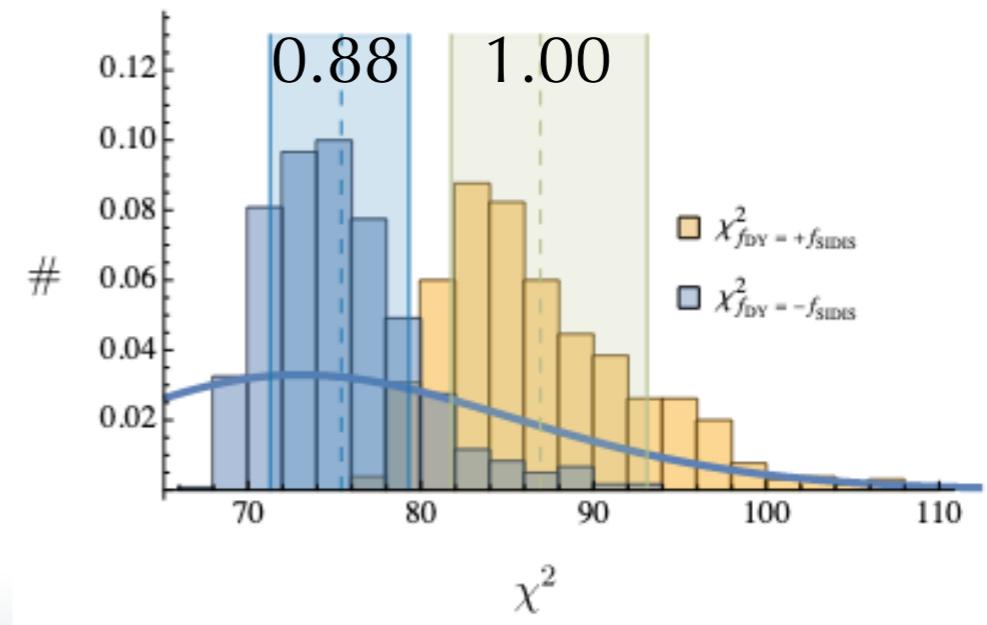


The EIC performance : polarized TMDs

predictions on recent STAR Drell-Yan data

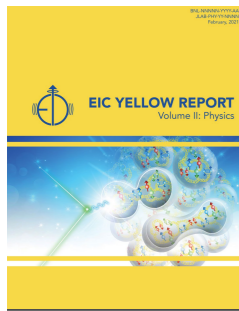


still not enough to confirm sign change:



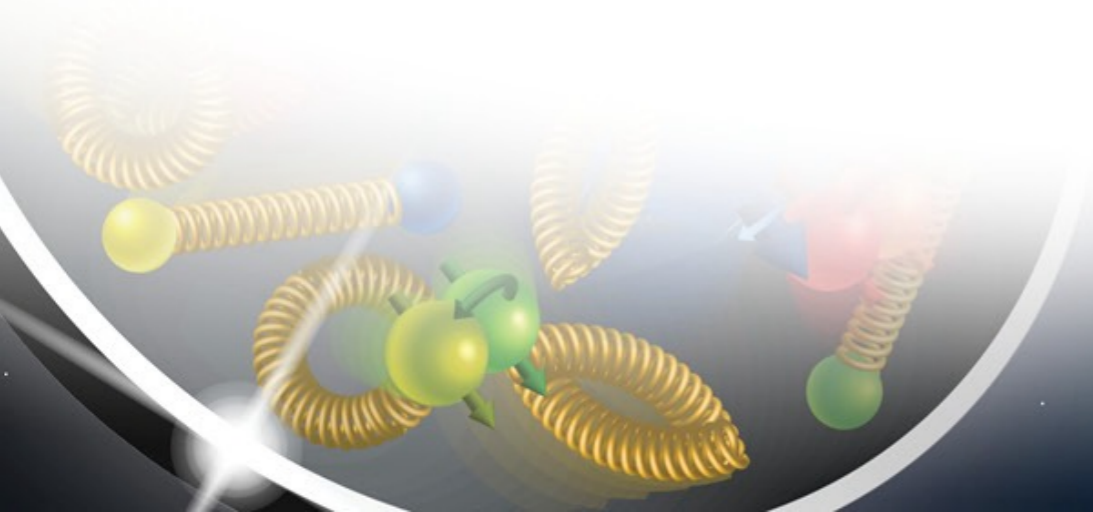
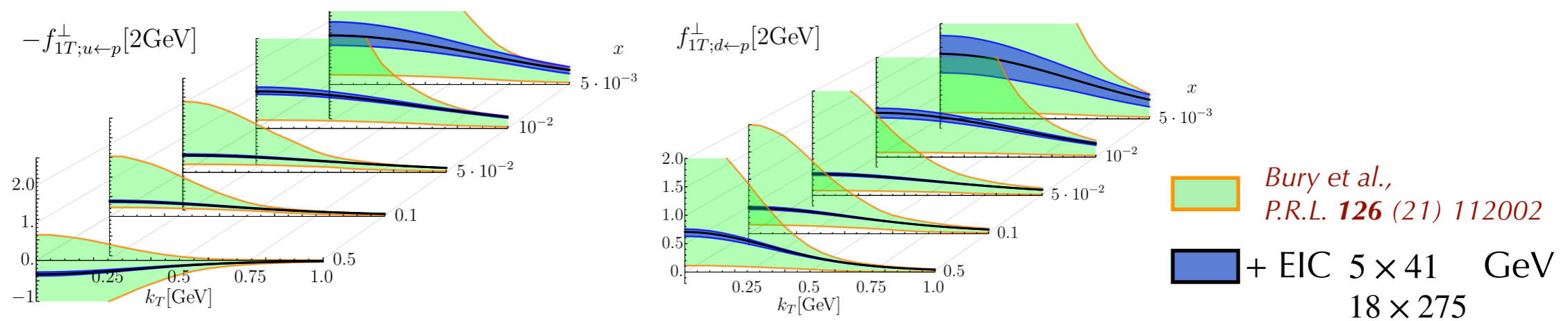
Bury et al., arXiv:2103.03270

The EIC performance : polarized TMDs

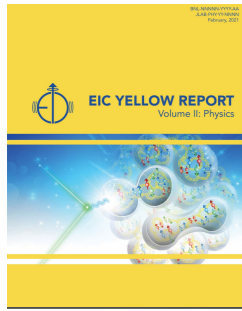


arXiv:2103.05419,
N.P.A in press

EIC impact

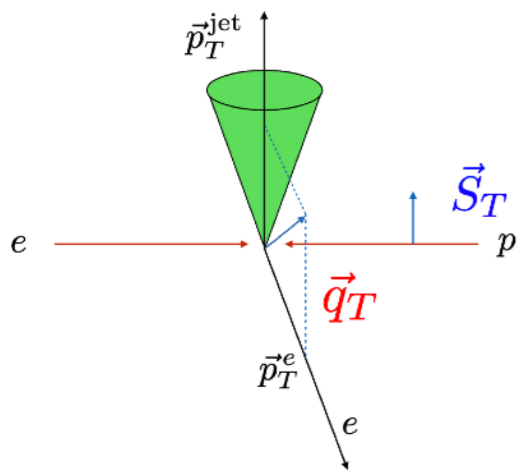
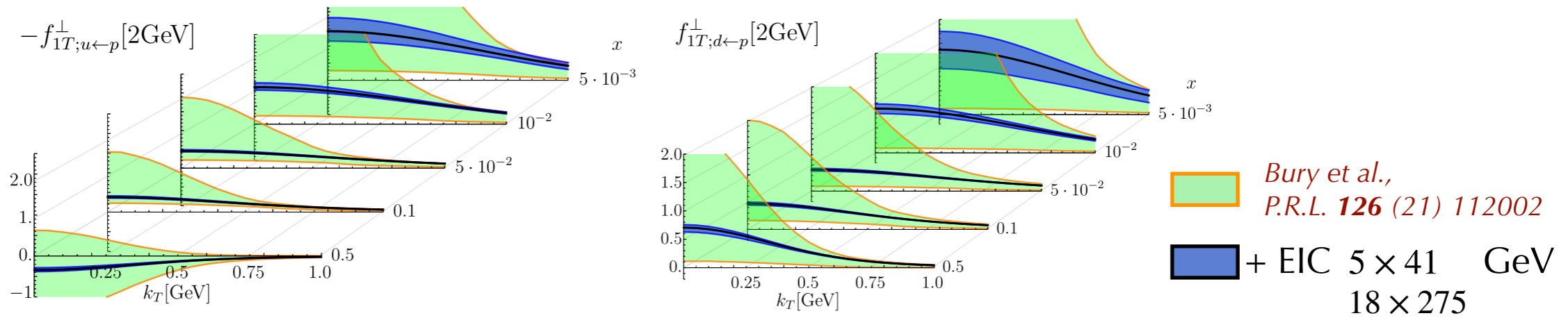


The EIC performance : polarized TMDs



arXiv:2103.05419,
N.P.A in press

EIC impact



opportunities with jets and Heavy Flavors

electron-jet azimuthal correlations

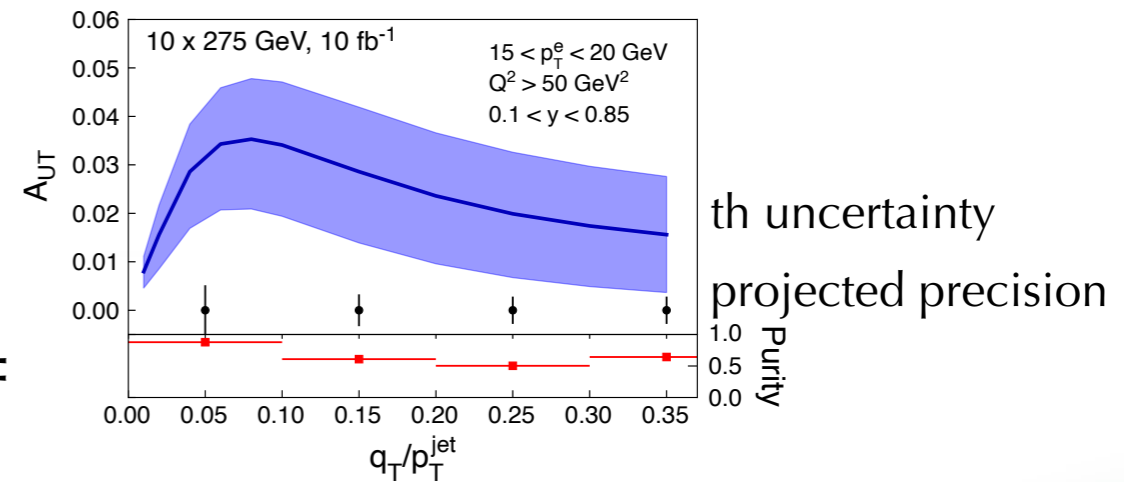
$$|\vec{q}_T| = |\vec{p}_T^e + \vec{p}_T^{\text{jet}}| \ll |\vec{p}_T^{\text{jet}}|$$



$$A_{UT} \sim d\sigma(S_T) - d\sigma(-S_T)$$

Sivers effect free from TMD FF

Arratia et al., arXiv:2007.07281



also access to gluon Sivers TMD from $D^0\bar{D}^0$, charm di-jets and J/ψ production

Zheng et al., arXiv:1805.05290

Rajesh et al., arXiv:2108.04866

The EIC performance : polarized TMDs

transversity $h_1^q(x, k_T)$

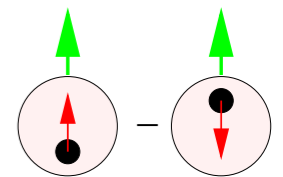
- net density of \perp -pol. quark in \perp -pol. proton
- prototype of chiral-odd parton densities

		Quark polarization		
		Unpolarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$f_1 = \odot$	\times	$h_1^\perp = \uparrow - \downarrow$
	L	\times	$g_1 = \rightarrow - \leftarrow$	$h_{1L}^\perp = \rightarrow - \leftarrow$
	T	$f_{1T}^\perp = \uparrow - \downarrow$	$g_{1T} = \rightarrow - \leftarrow$	$h_1 = \uparrow - \downarrow$ $h_{1T}^\perp = \rightarrow - \leftarrow$

survives k_T integration



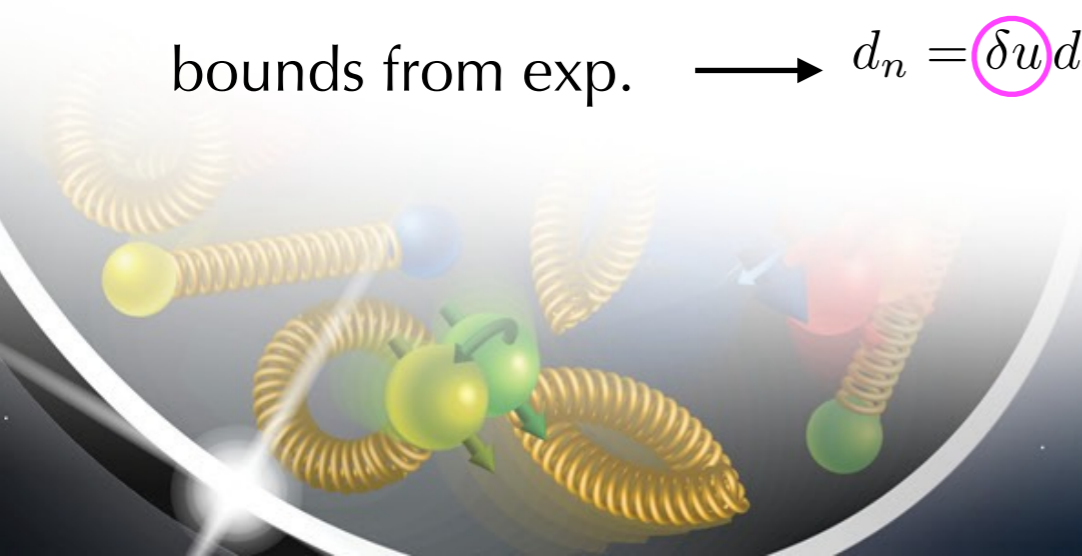
collinear PDF $h_1^q(x)$



- no chiral-odd structures in SM Lagrangian; potential doorway to BSM physics

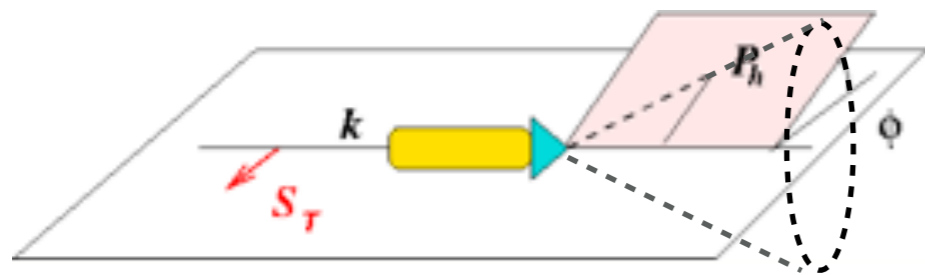
Example: SMEFT studies of strong CP violation via neutron EDM d_n

bounds from exp. $\longrightarrow d_n = \delta u d_u + \delta d d_d + \delta s d_s$ tensor charge $\delta^q(Q^2) = \int_0^1 dx h_1^{q-\bar{q}}(x, Q^2)$



The EIC performance : polarized TMDs

transversity is chiral-odd \rightarrow needs a chiral-odd partner in the cross section
two different fragmentation mechanisms:



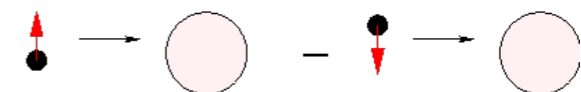
Collins effect

$$\mathbf{S}_T \cdot \mathbf{k} \times \mathbf{P}_{hT}$$

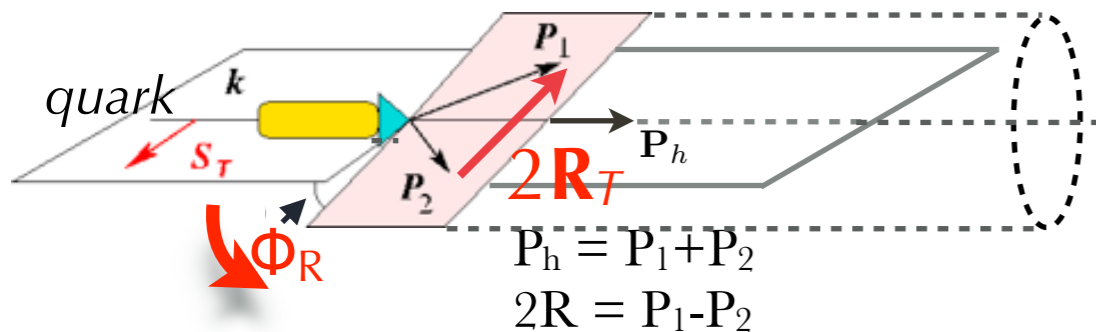
Collins, N.P. B396 (93) 161

requires knowledge of chiral-odd

Collins TMD FF H_1^\perp



probes transversity as TMD PDF



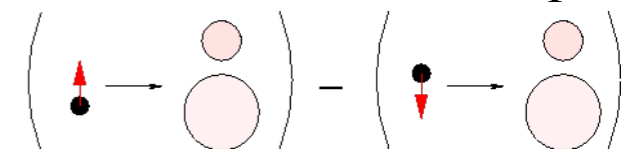
di-hadron mechanism

$$\mathbf{S}_T \cdot \mathbf{P}_2 \times \mathbf{P}_1 = \mathbf{S}_T \cdot \mathbf{P}_h \times \mathbf{R}_T$$

Collins et al., N.P. B420 (94)

requires knowledge of

chiral-odd DiFF H_1^{\leftarrow}



probes transversity as PDF

if $R_T^2 \propto M_{h_1 h_2}^2 \ll Q^2$ define di-hadron fragmentation function (DiFF)

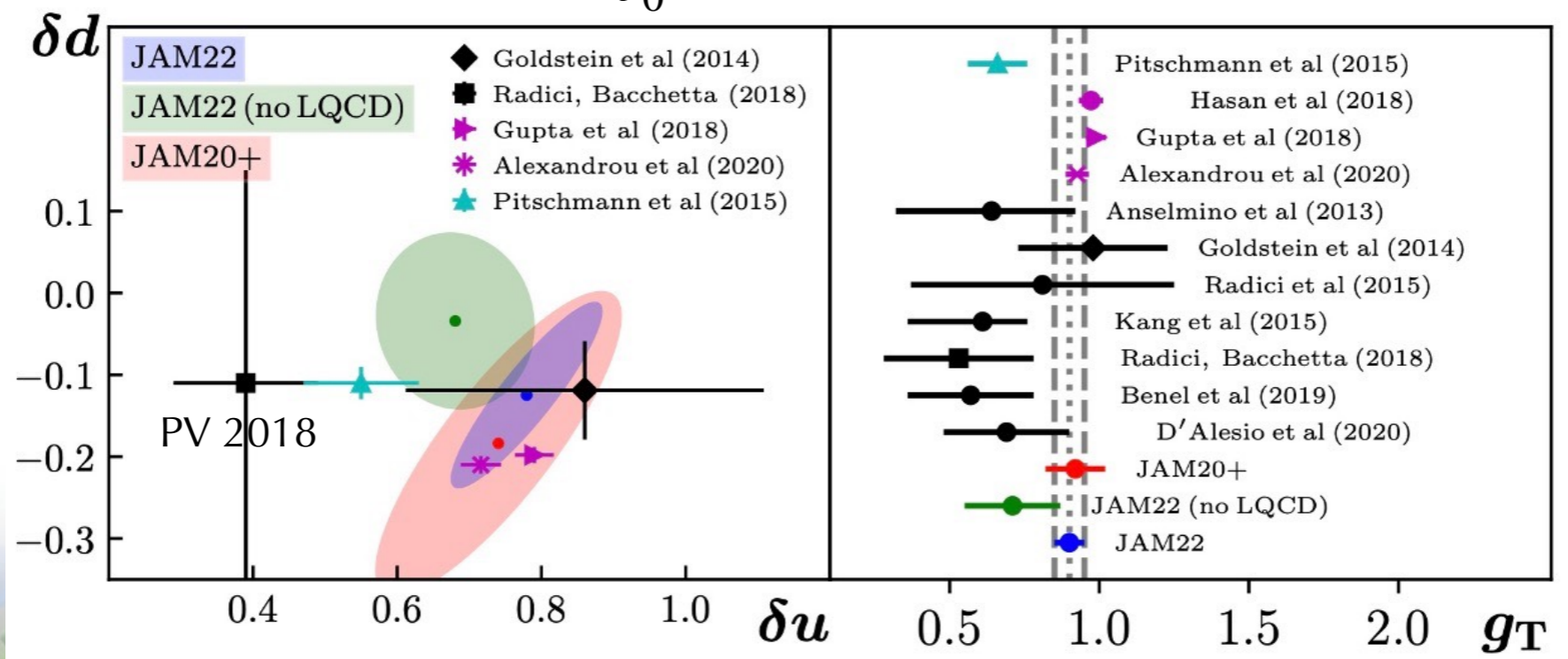
The EIC performance : polarized TMDs

most recent extractions

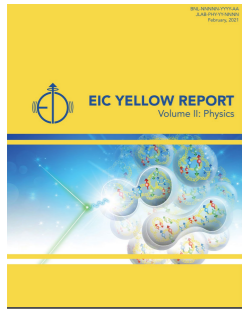
	Mechanism	Framework	SIDIS	e+e-	p-p collisions	N pts
PV 2018 arXiv:1802.05212	collinear DiFF	LO	✓	✓	✓	78
JAM 2020 arXiv:2002.08384	Collins effect	generalized parton model	✓	✓	✓	517
MEX 2019 arXiv:1912.03289	collinear DiFF	LO	✓	✓	✗	68
CA 2020 arXiv:2001.01573	Collins effect	generalized parton model	✓	✓	✗	76
JAM 2022 arXiv:2205.00999	Collins effect	generalized parton model	✓	✓	✓	634

tensor charge $\delta^q(Q^2) = \int_0^1 dx h_1^{q-\bar{q}}(x, Q^2)$ $g_T = \delta u - \delta d$

Q=2 GeV



The EIC performance : polarized TMDs



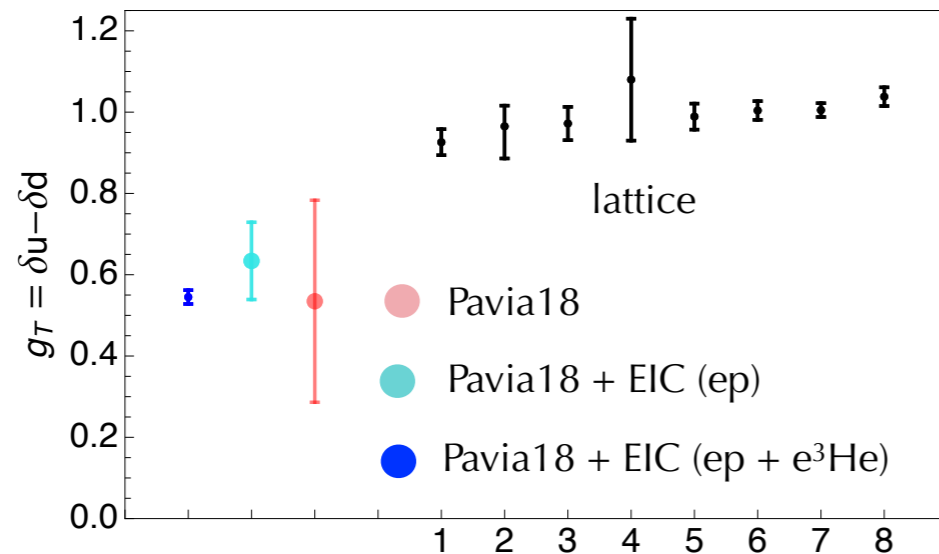
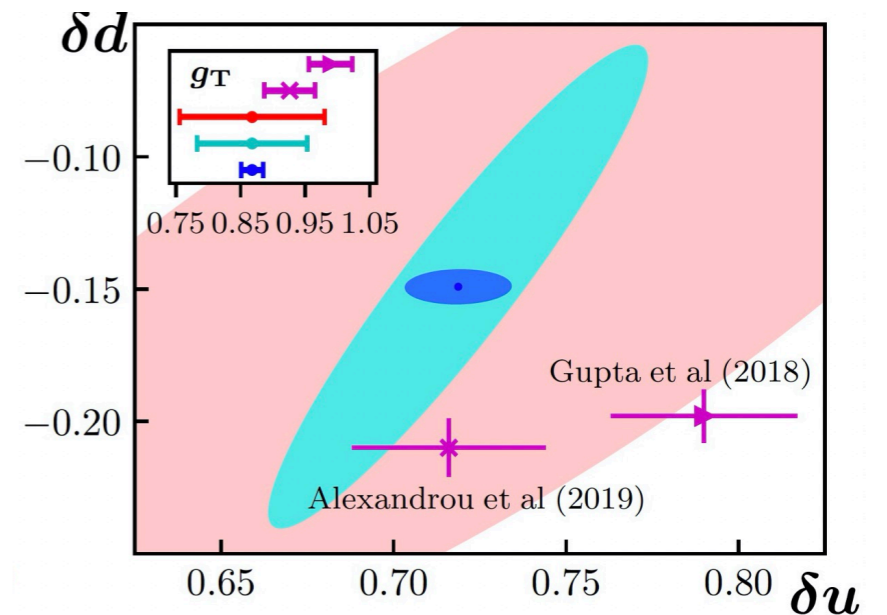
arXiv:2103.05419,
N.P.A in press

EIC impact

Collins effect

$\mathcal{L}=10 \text{ fb}^{-1}$, 8223 data pts.
proton [GeV]: 5x41, 5x100, 10x100, 18x275
 ^3He [GeV]: 5x41, 5x100, 18x100

■ JAM20
■ JAM20 + EIC(ep)
■ JAM20 + EIC(ep+e ^3He)

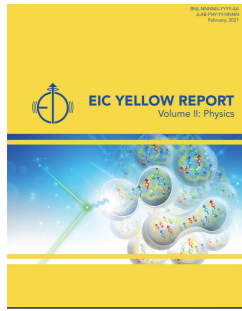


di-hadron mechanism

$\mathcal{L}=10 \text{ fb}^{-1}$, 3852 data pts, proton & ^3He [GeV]: 10x100

- 1) **ETMC '19** *Alexandrou et al., arXiv:1909.00485*
- 2) **Mainz '19** *Harris et al., P.R. D100 (19) 034513*
- 3) **LHPC '19** *Hasan et al., P.R. D99 (19) 114505*
- 4) **JLQCD '18** *Yamanaka et al., P.R. D98 (18) 054516*
- 5) **PNDME '18** *Gupta et al., P.R. D98 (18) 034503*
- 6) **ETMC '17** *Alexandrou et al., P.R. D95 (17) 114514; (E) P.R. D96 (17) 099906*
- 7) **RQCD '14** *Bali et al., P.R. D91 (15) 054501*
- 8) **LHPC '12** *Green et al., P.R. D86 (12) 114509*

The EIC performance : polarized TMDs



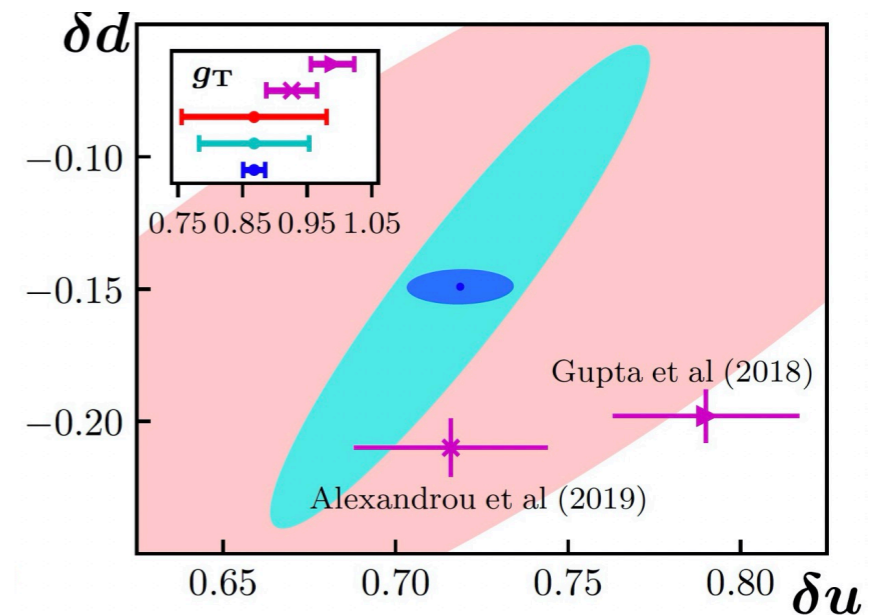
arXiv:2103.05419,
N.P.A in press

EIC impact

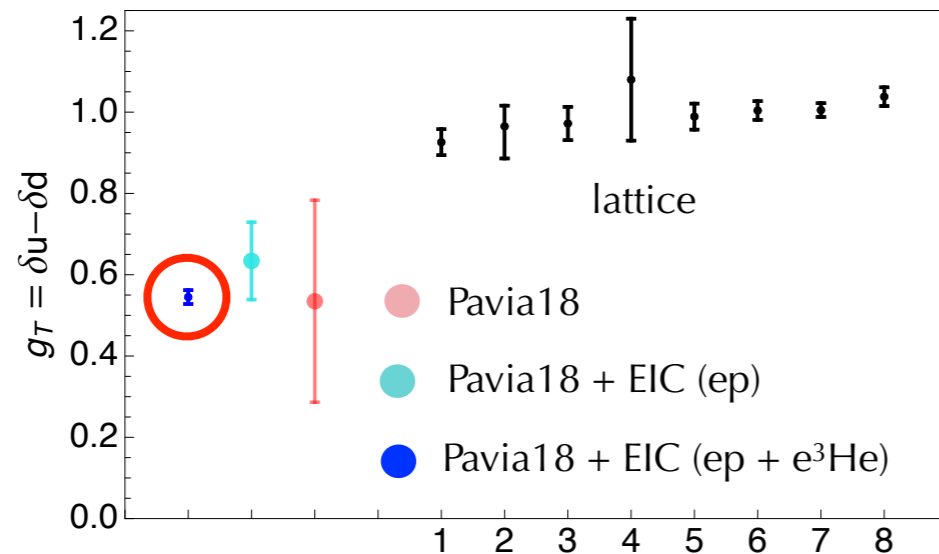
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■ JAM20
■ JAM20 + EIC(ep)
■ JAM20 + EIC(ep+e³He)



comparable/higher precision than lattice



di-hadron mechanism

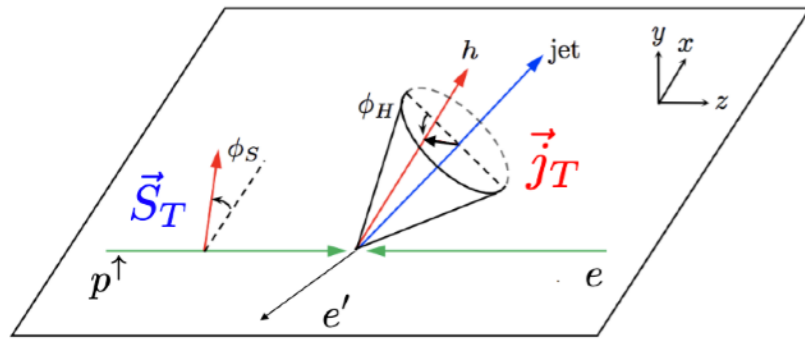
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- 8) **LHPC '12** *Green et al., P.R. D86 (12) 114509*

The EIC performance : polarized TMDs

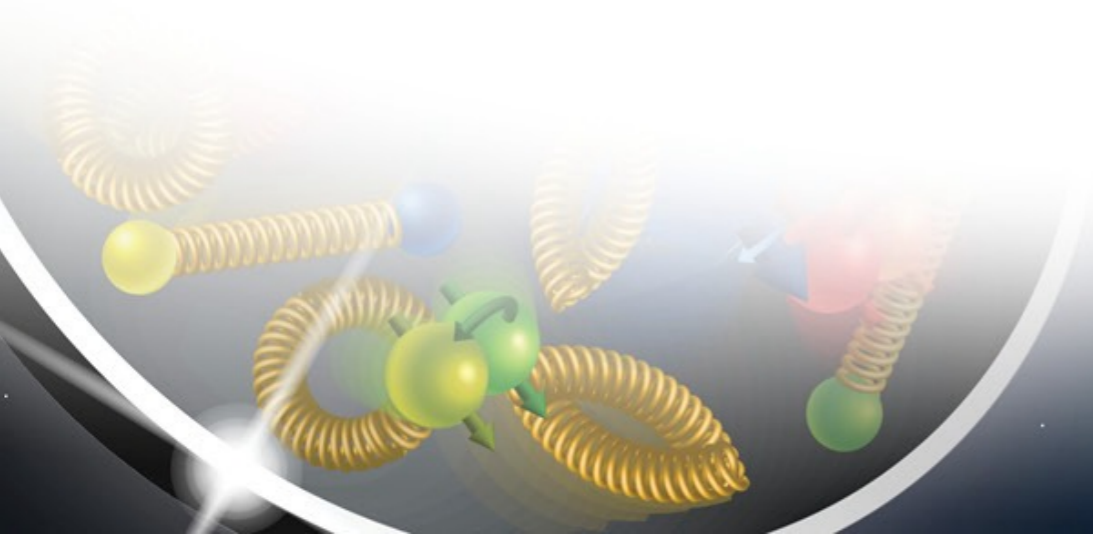
a new opportunity: jet substructure

$$e + p \rightarrow e' + \text{jet} (h) + X$$



if $j_T^2 \ll (P_T^{jet})^2$ hybrid factorisation scheme: requires knowledge of Collins TMD FF H_1^\perp
- TMD framework for fragmentation
- collinear framework for collision **but probes transversity as PDF**

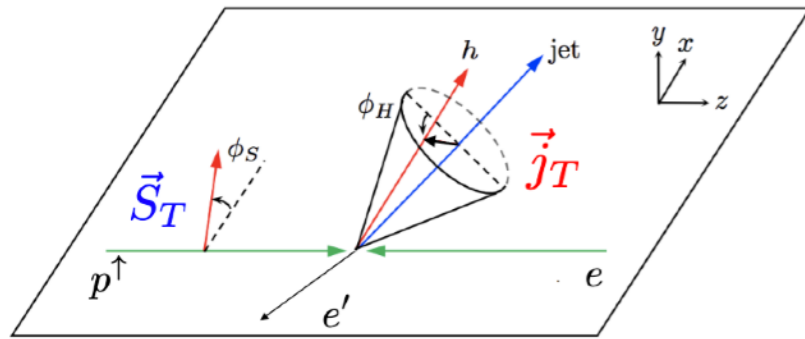
hadron-in-jet Collins effect



The EIC performance : polarized TMDs

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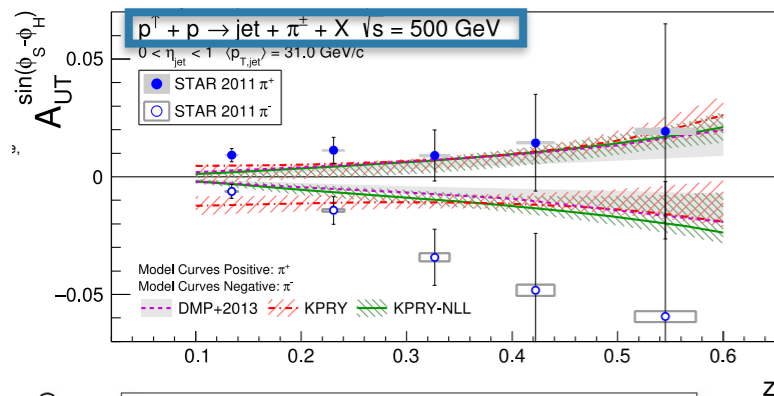
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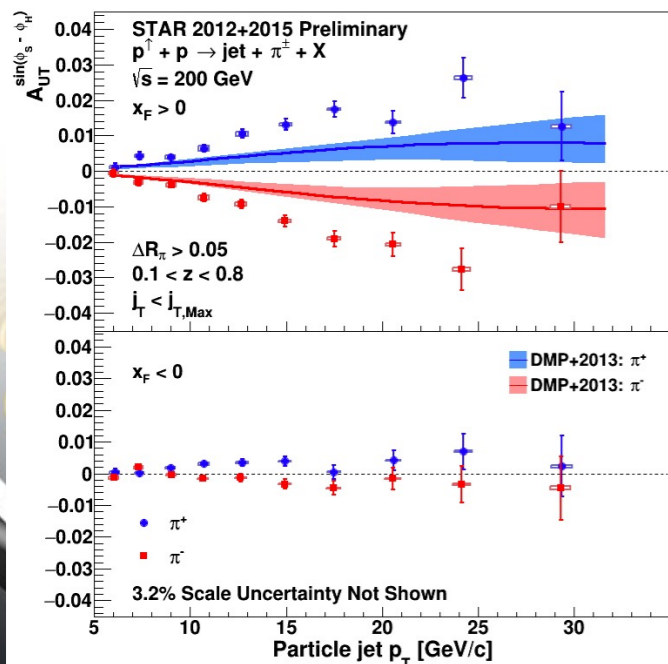
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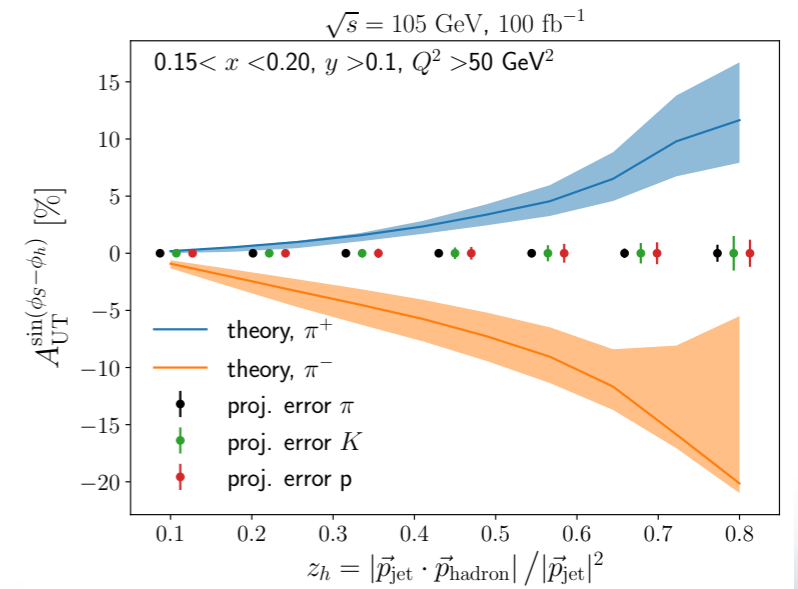
measured in
p-p collision
at STAR

KPRY
*Kang et al.,
P.L. B774 (17) 635*

DMP
*D'Alesio et al.,
P.L. B773 (17) 300*



predicted
at the EIC

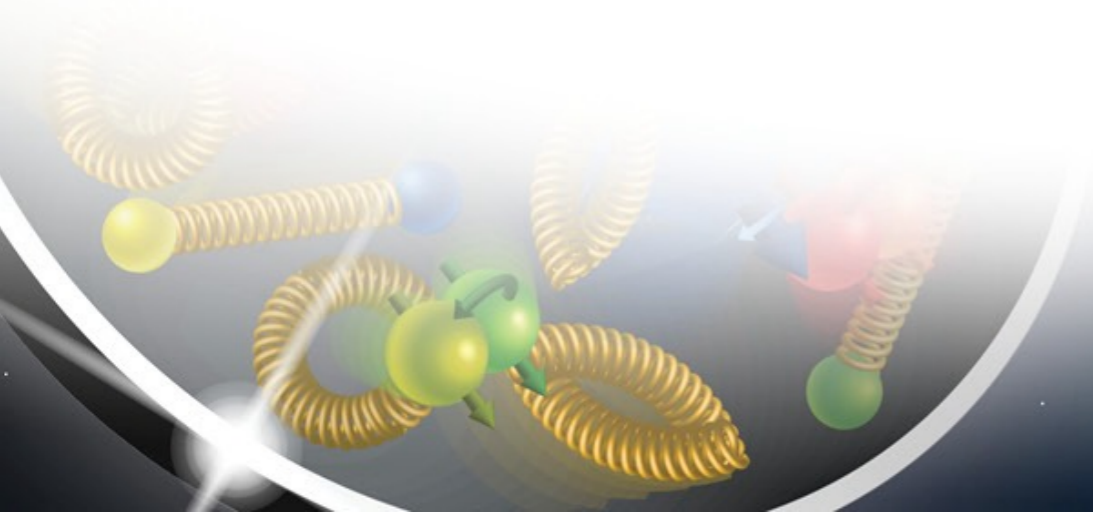


Arratia et al., arXiv:2007.07281

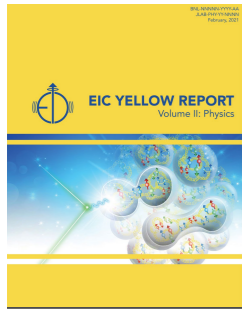
The EIC performance : nuclear PDF

1-Dim Maps in nuclei

nuclear PDF (x)



The EIC performance : nuclear PDF



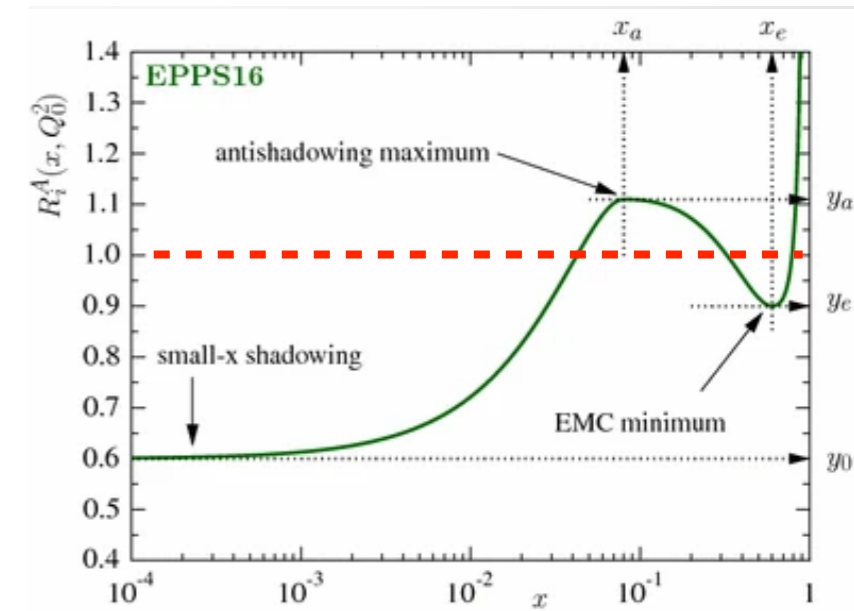
arXiv:2103.05419,
N.P.A in press

the nuclear modification factor R_A

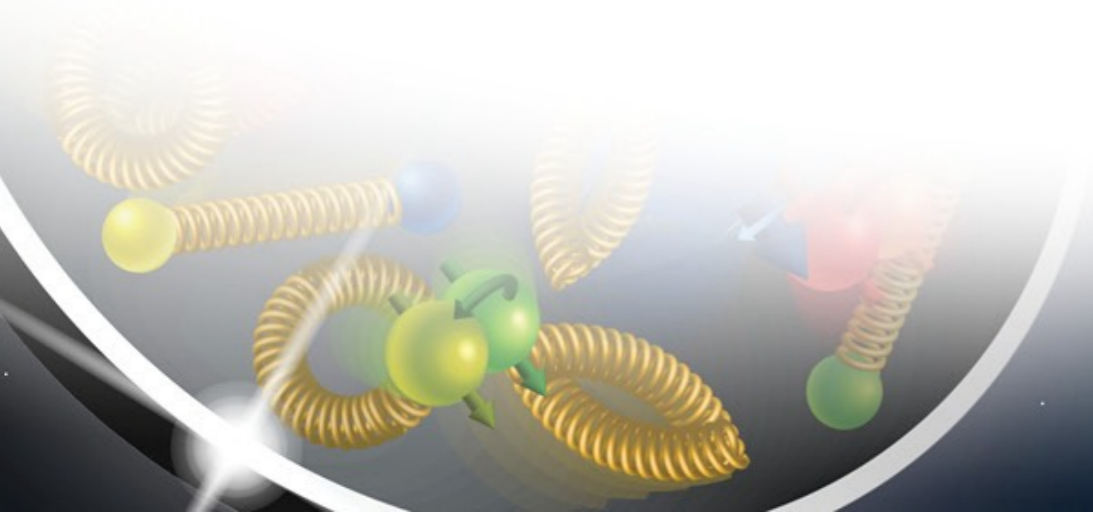
nuclear PDFs are different from free proton PDFs :

$$f_{p/A}^i(x; Q^2) = R_A^i(x; Q^2) f_p^i(x; Q^2)$$

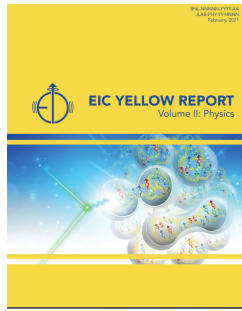
- provides **input on initial state** for heavy-ion collisions
- **complementary** to LHC and RHIC **p-A collisions**



Eskola et al., E.P.J. C77 (16) 163



The EIC performance : nuclear PDF



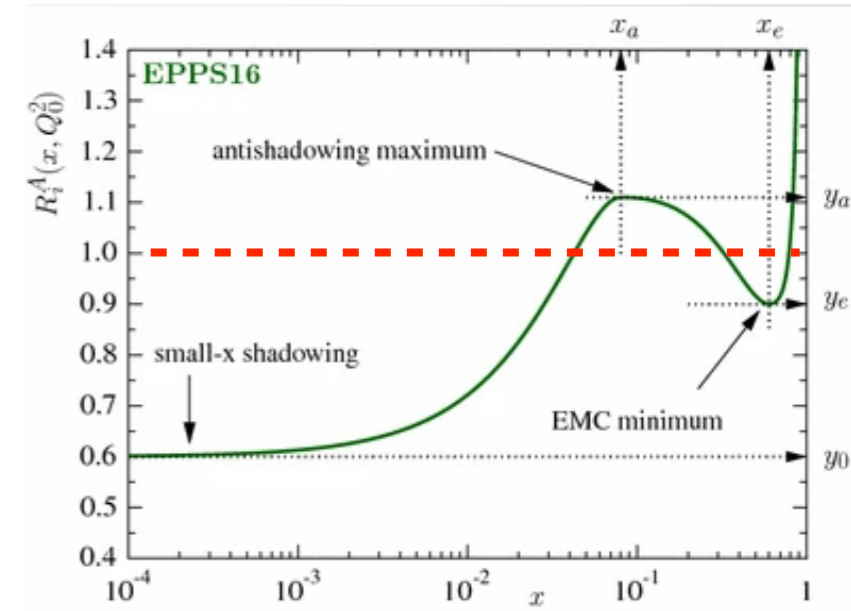
arXiv:2103.05419,
N.P.A in press

the nuclear modification factor R_A

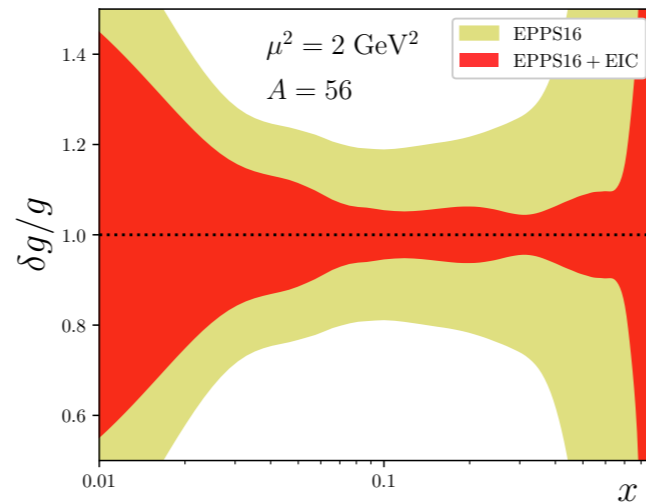
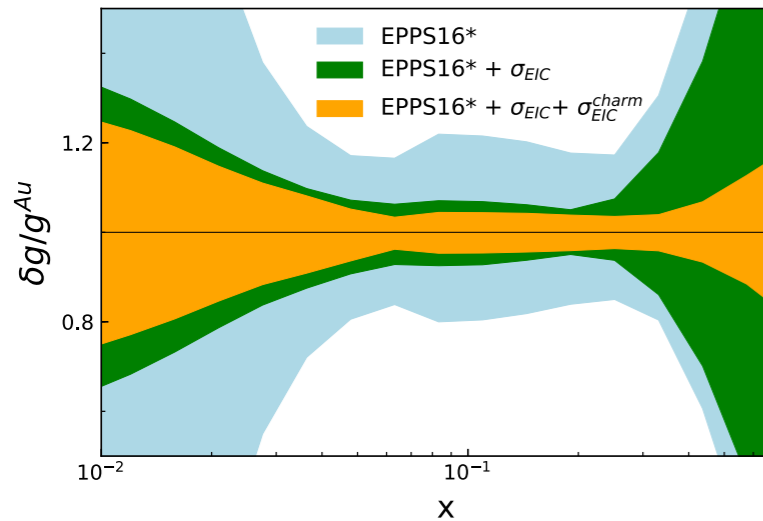
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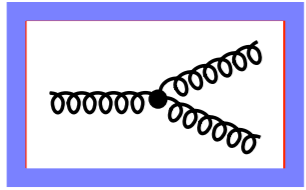
Eskola et al., E.P.J. C77 (16) 163



EPPS16nlo

**importance of F_2^{charm}
for high x gluons**

The EIC performance : saturation

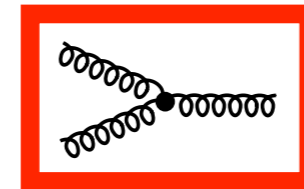
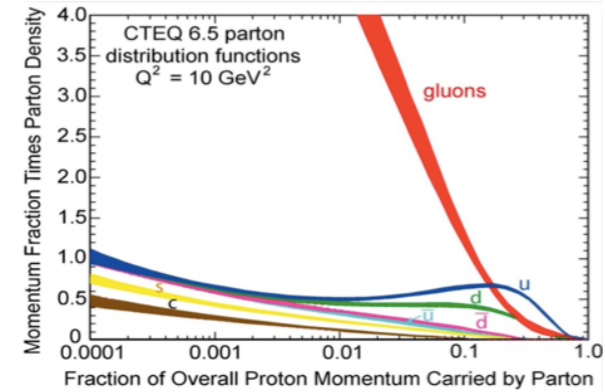


gluon self-interaction
→ proliferation of # gluons

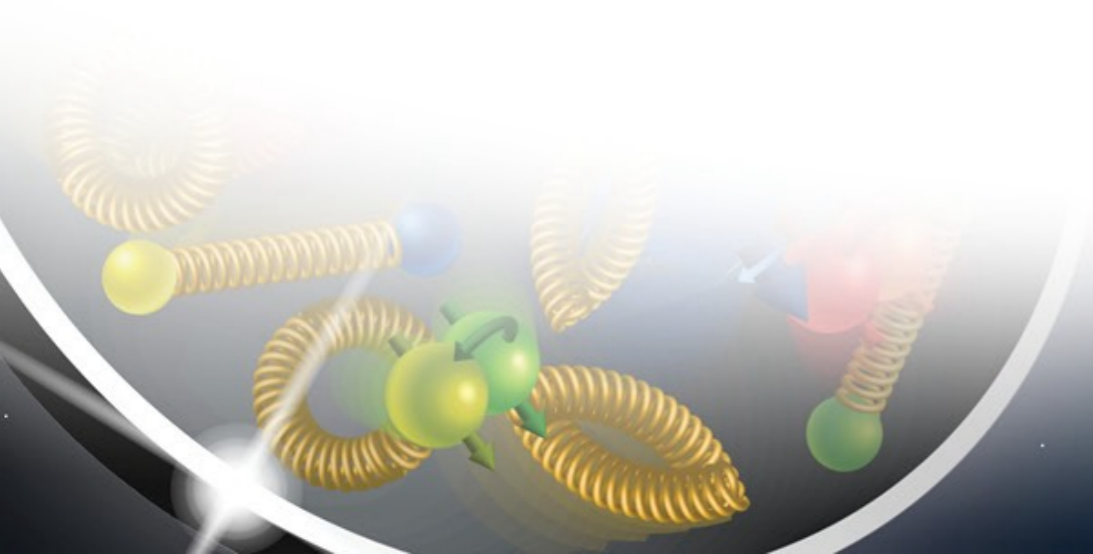
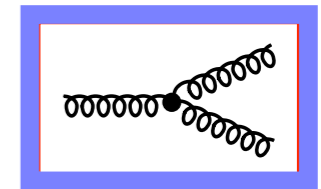
dramatic rise of gluon density @ low x

unitarity → gluons must recombine to
balance splitting (**saturation**)

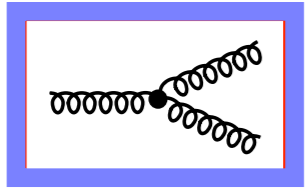
effect not clearly seen at HERA



=

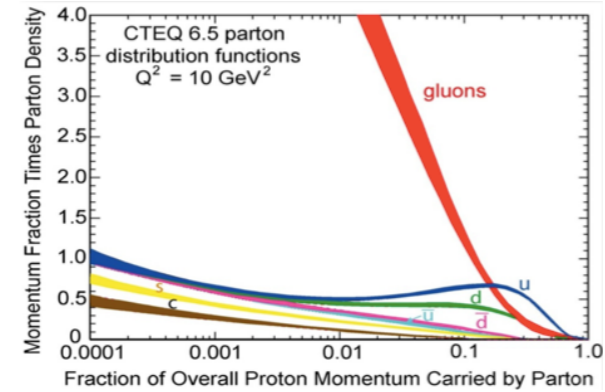


The EIC performance : saturation



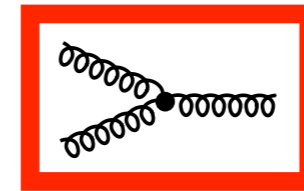
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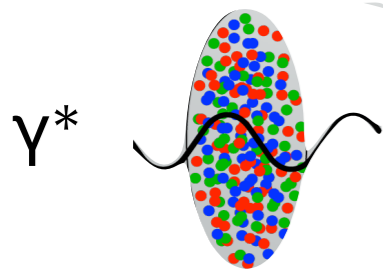
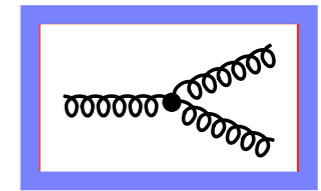


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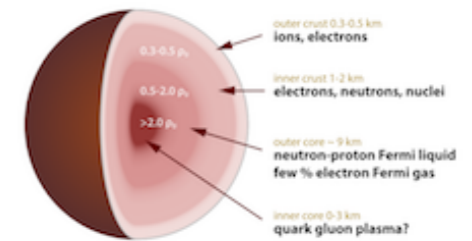


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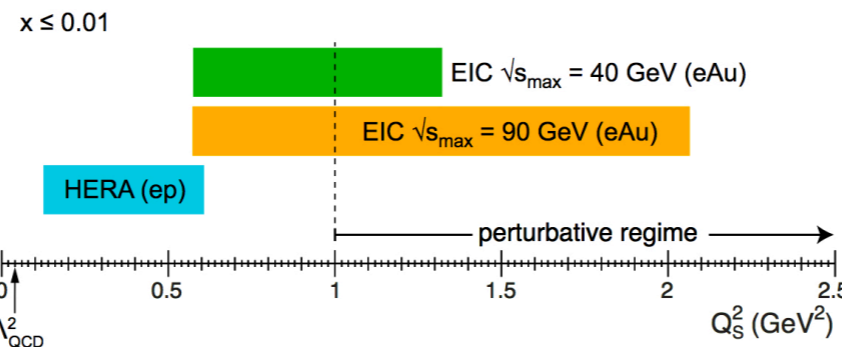
- EIC: reach same saturation scale Q_s at larger x → smaller \sqrt{s}
- nucleus acts as Q_s amplifier

$$[Q_s(x, A)]^2 \sim \left(\frac{A}{x}\right)^{\frac{1}{3}}$$



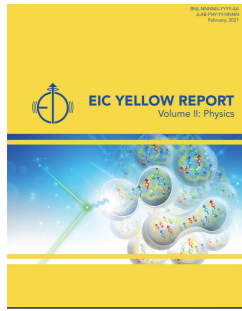
the Color Glass Condensate model

Iancu et al., P.L. B510 (01) 133



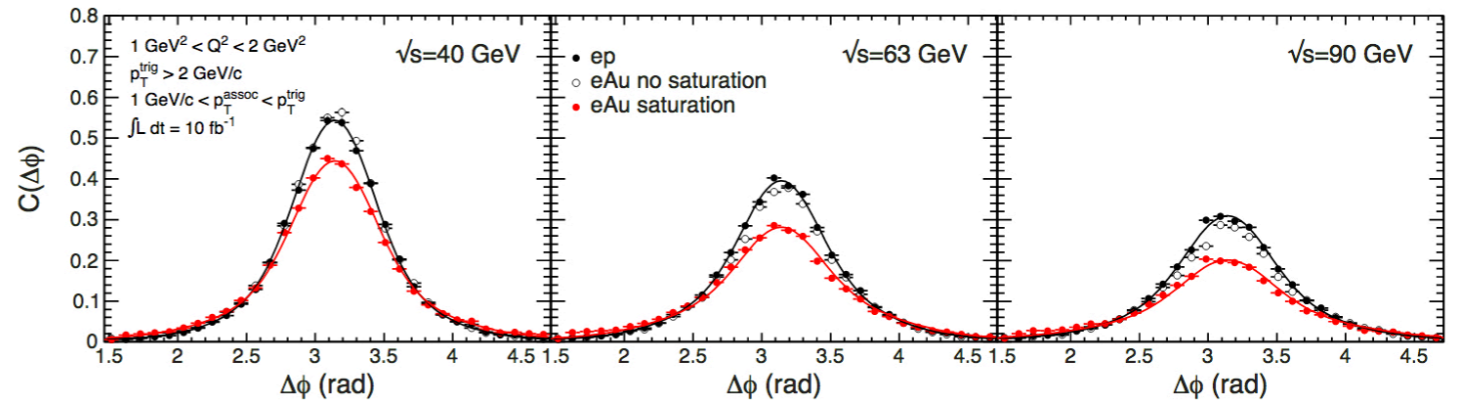
implications for astrophysics of neutron stars

The EIC performance : saturation



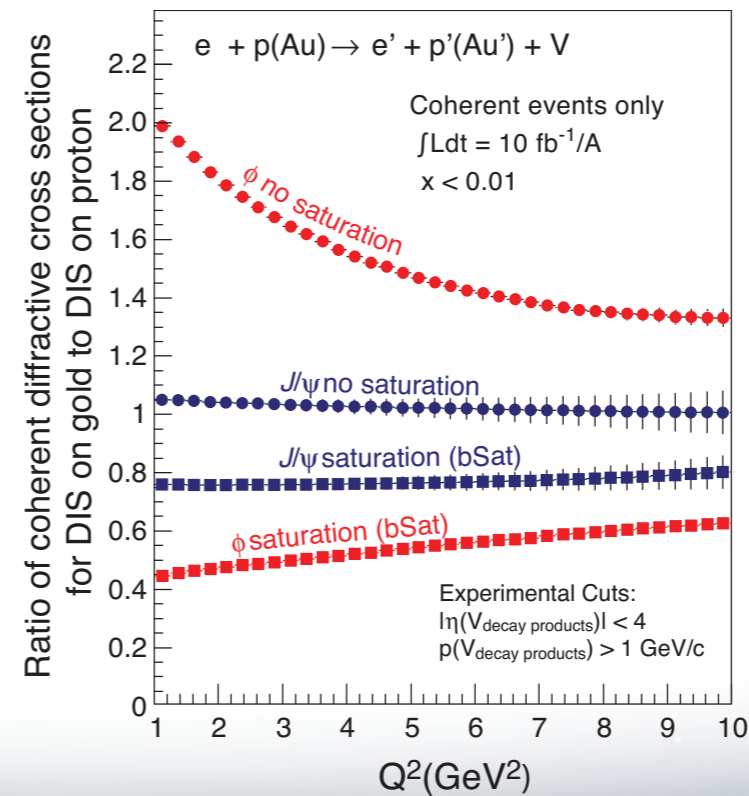
arXiv:2103.05419,
N.P.A in press

1- key observable:
di-hadron correlations in **e-A** vs. e-p



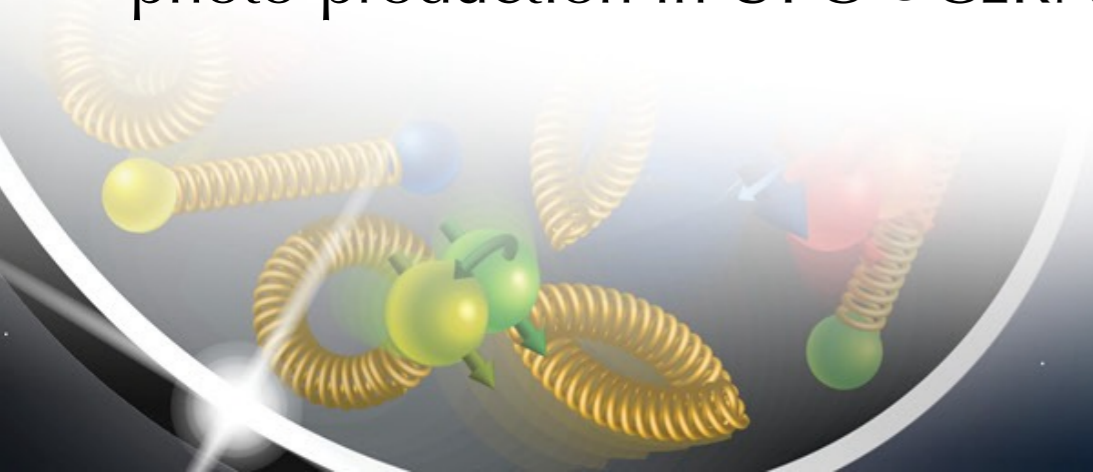
Aschenauer et al., Rept.Prog.Phys. 82 (19) 024301

2- key observable:
diffractive scatt. $\sigma_{\text{diff}} \sim [\text{gluon}(x, Q^2)]^2$



Abdul Khalek et al.,
“Snowmass 2021 White Paper:
EIC for High Energy Physics”
arXiv:2203.13199

complementary to vector-meson
photo-production in UPC @CERN



The EIC Users Group map

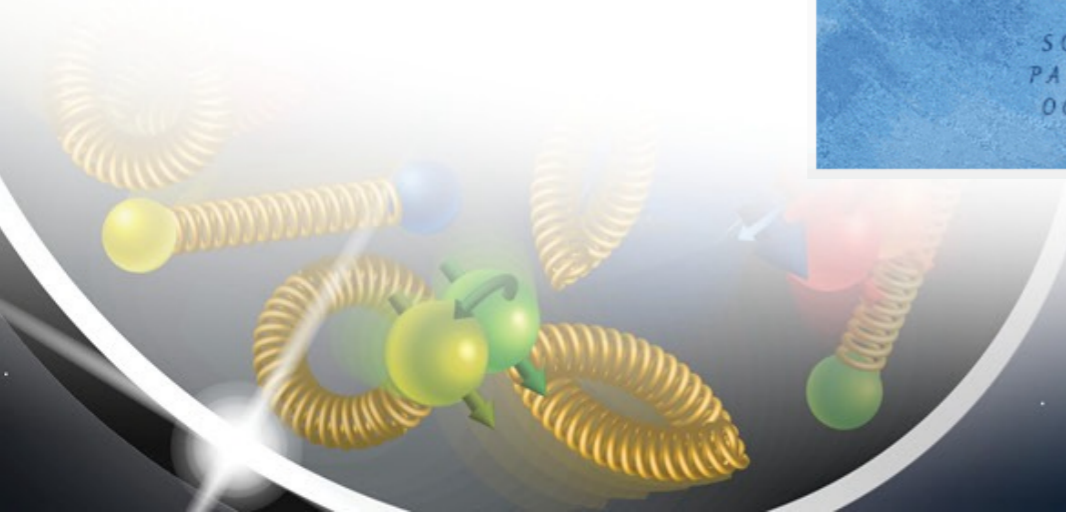
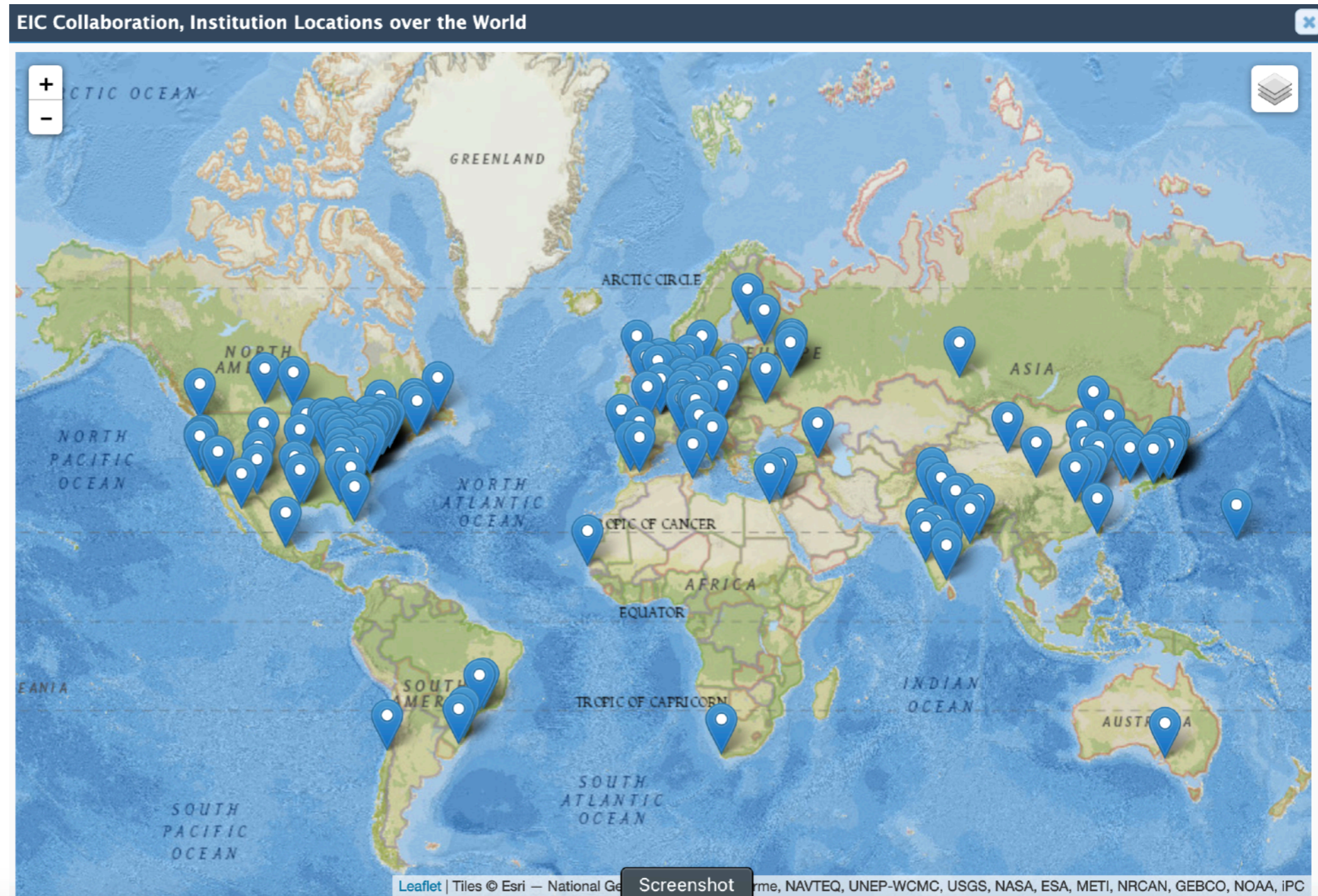
www.eicug.org

at Jun. 6th 2022

36 countries

266 Institutions

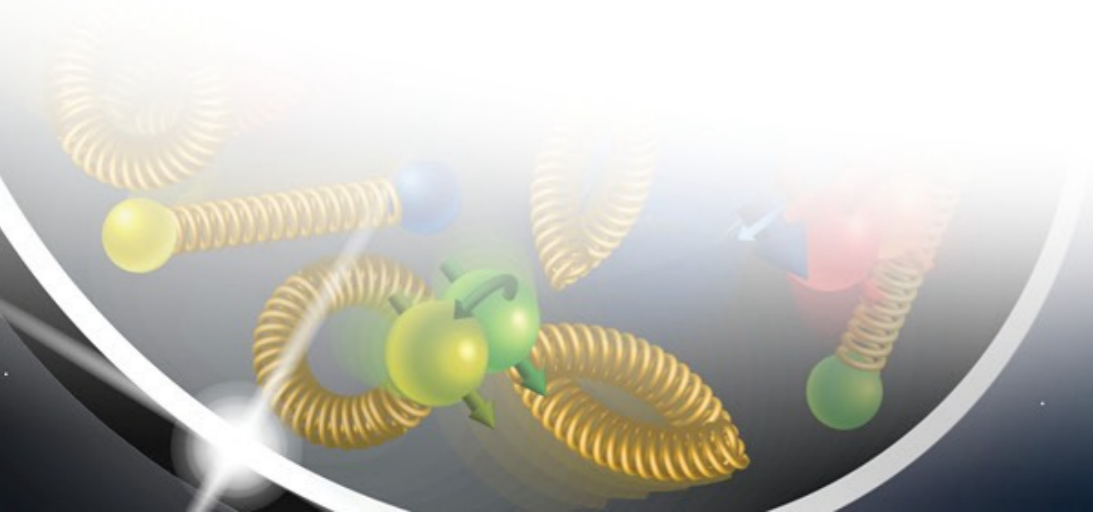
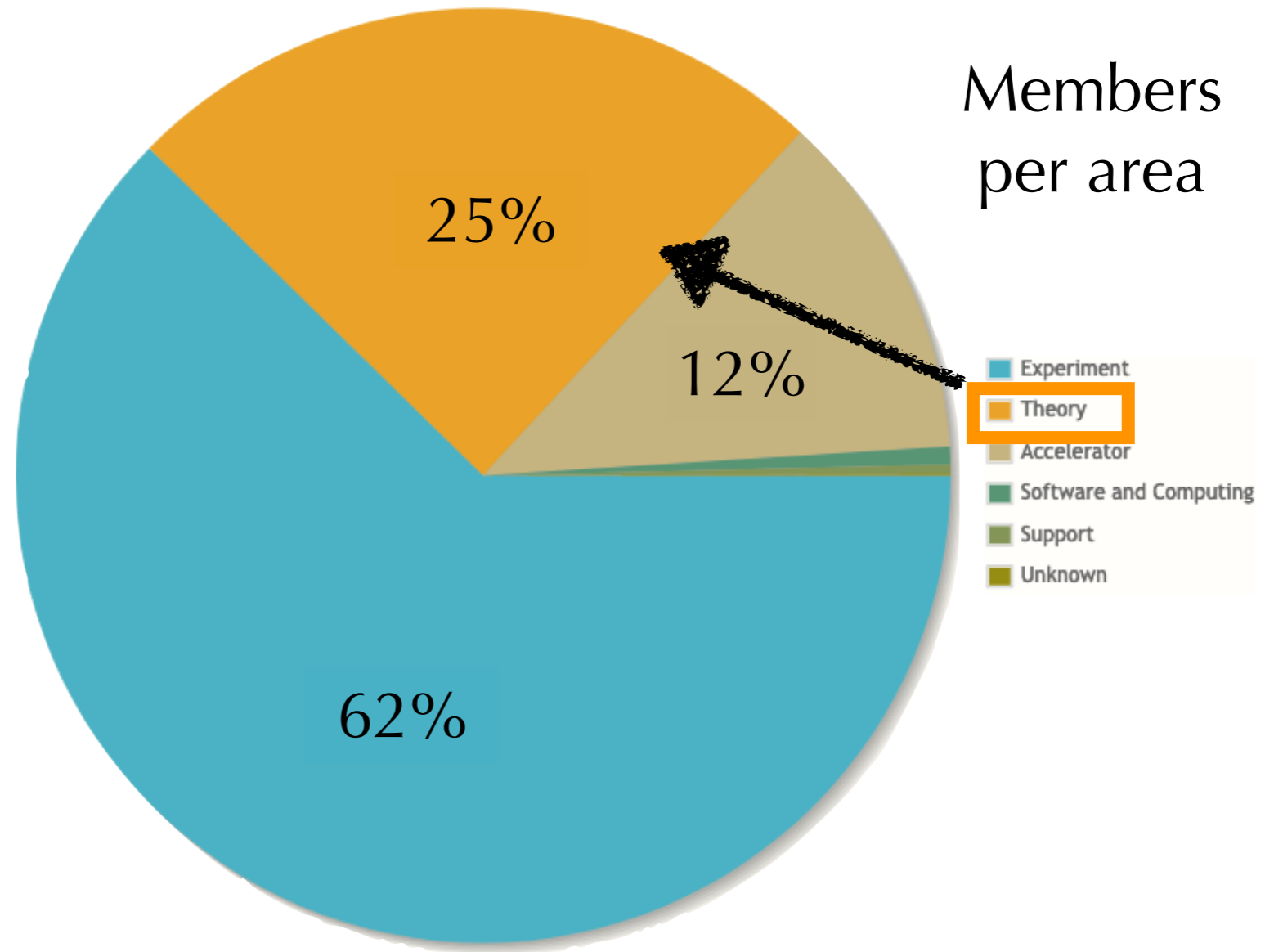
1330 members



The EIC Users Group composition

at Jun. 6th 2022

strong community
of theorists

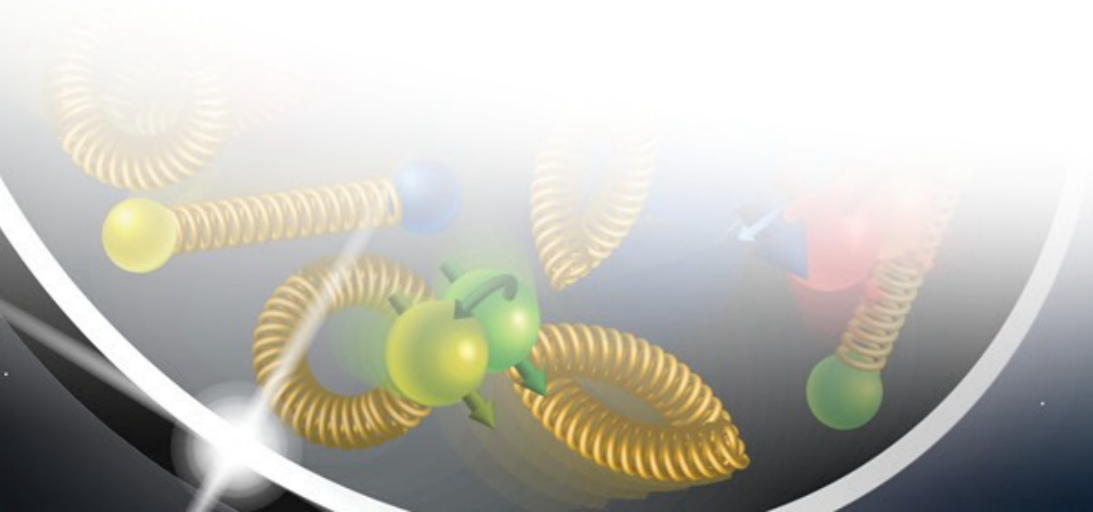
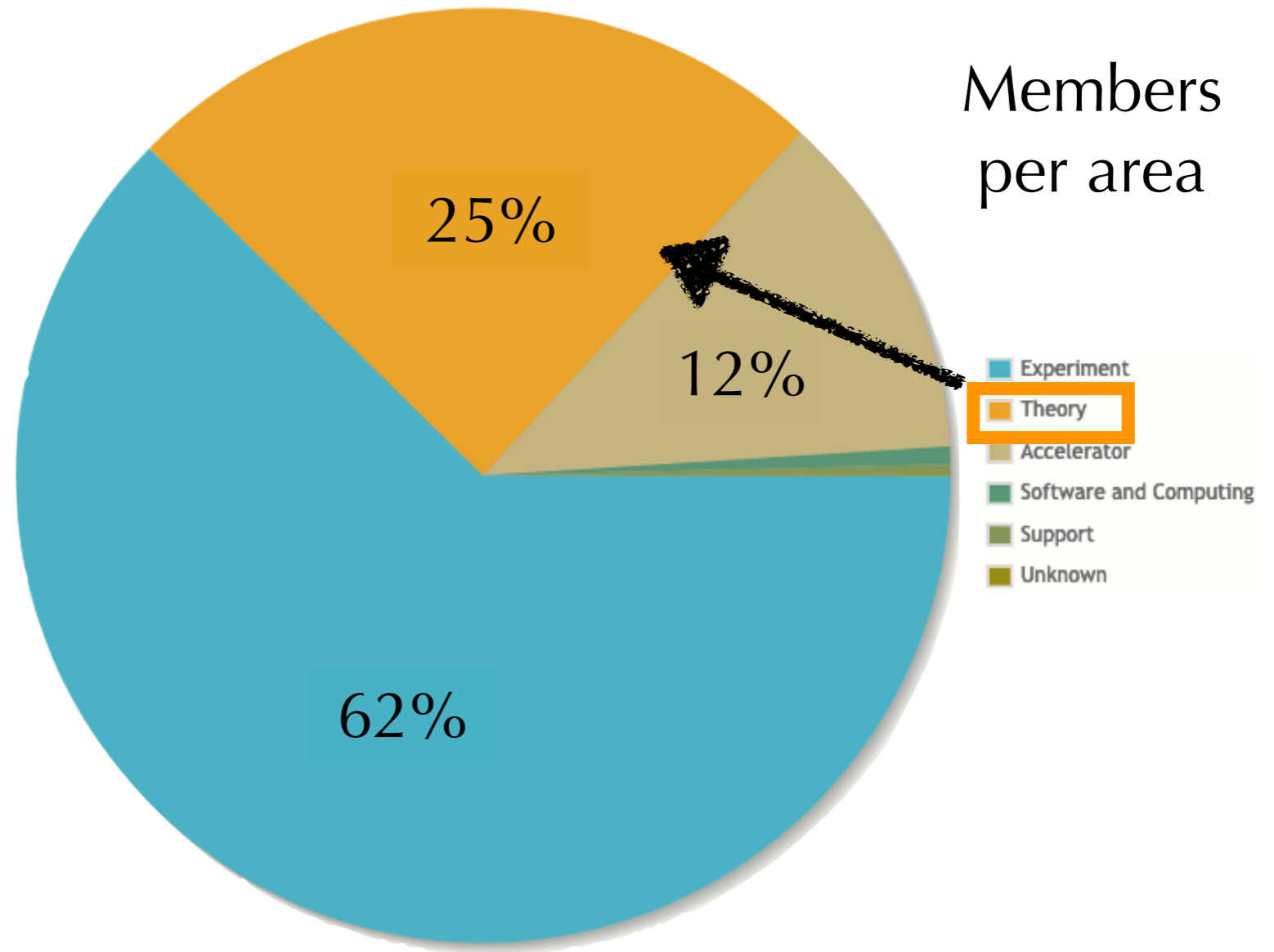


The EIC Users Group composition

at Jun. 6th 2022

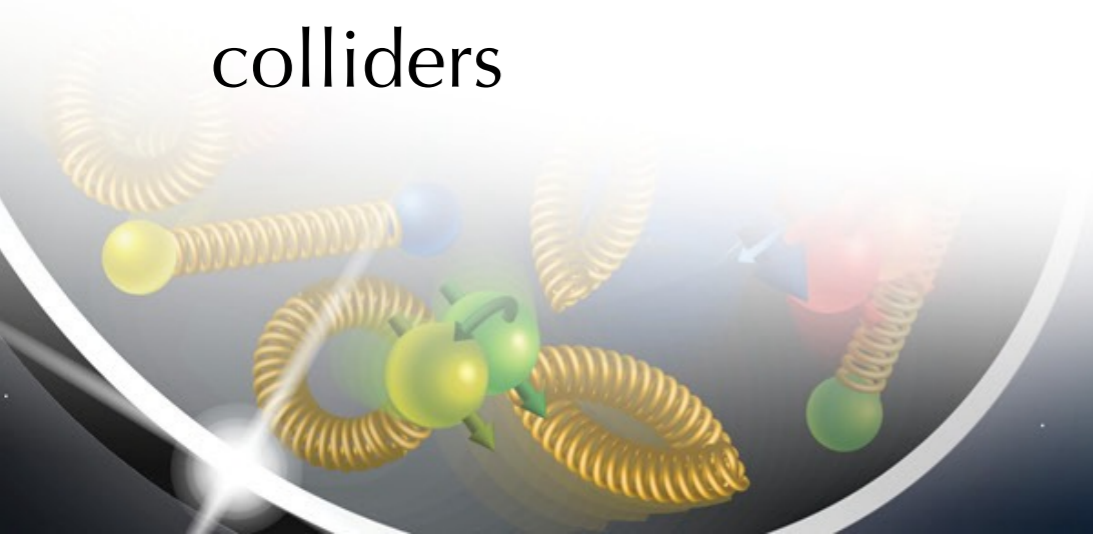
strong community
of theorists

**young students
and/or postdocs
welcome to join!**



Recap

- the EIC addresses fundamental (open) questions about visible matter:
 - spin and flavor partonic structure of nucleons and nuclei
 - 3D-imaging (tomography) in momentum and position space
 - matter at extreme parton densities \rightarrow onset of saturation
- As high-luminosity, high-polarization collider with wide range in energy and ion species, the EIC is unique in the panorama of next two decades
- The EIC offers unprecedented opportunities to advance our knowledge of the confined partonic structure of hadrons, with scientific outcomes that are complementary to the LHC and other colliders



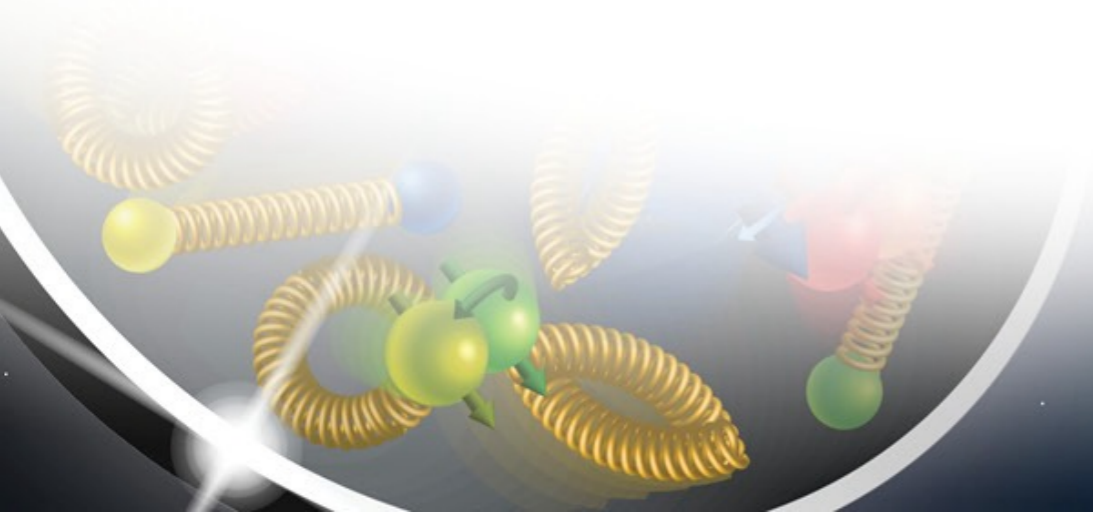


THANK YOU
for your
ATTENTION!

Backup Slides

Impact parameter distributions

$$\rho(x, b_T)$$

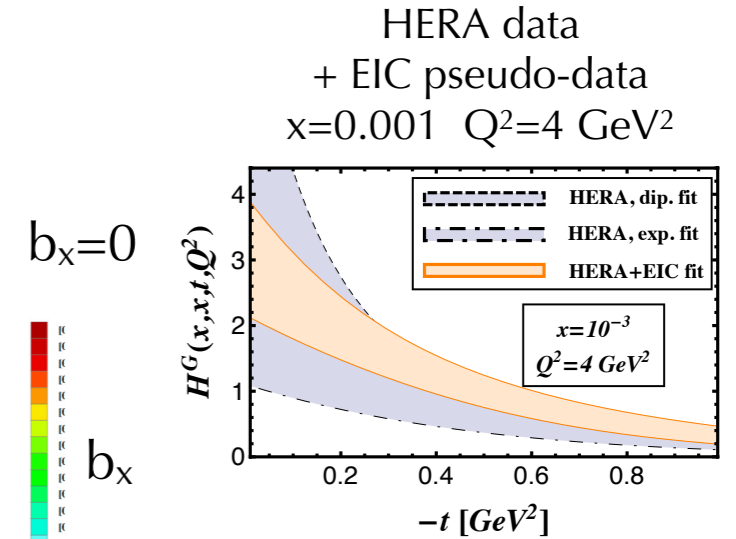
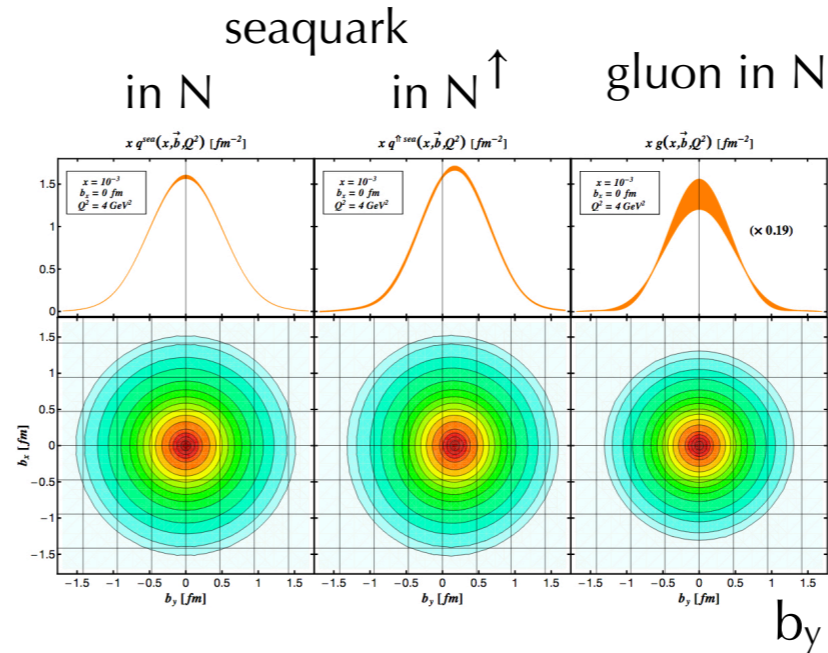


The EIC performance : GPDs

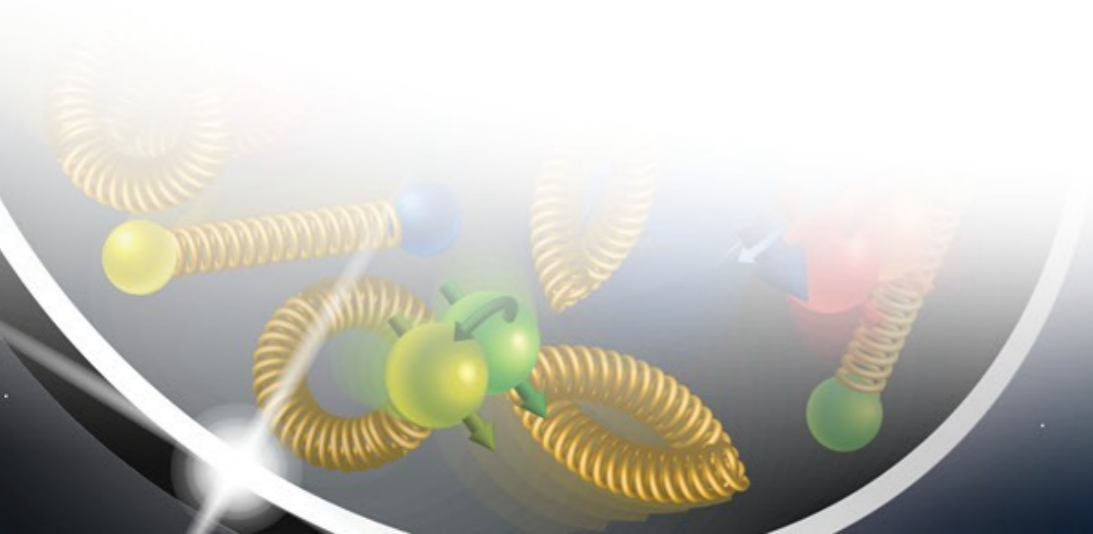
impact parameter distribution $\rho(x, \mathbf{b}_T)$

Phenomenology

- local fits of GPD
(of DVCS in given kinematic bins)



Aschenauer et al., JHEP09 (13) 093

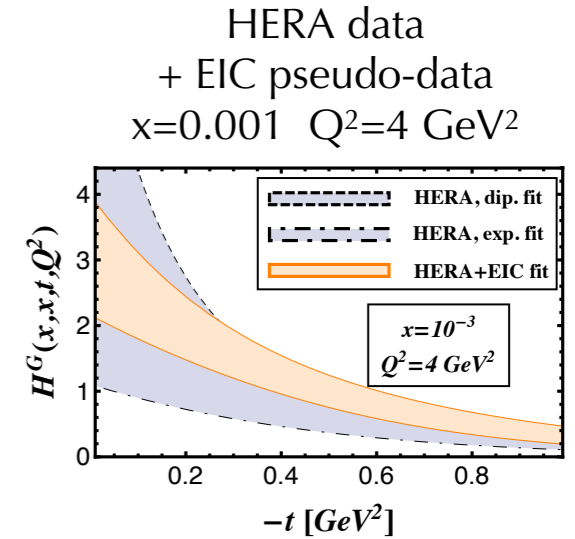
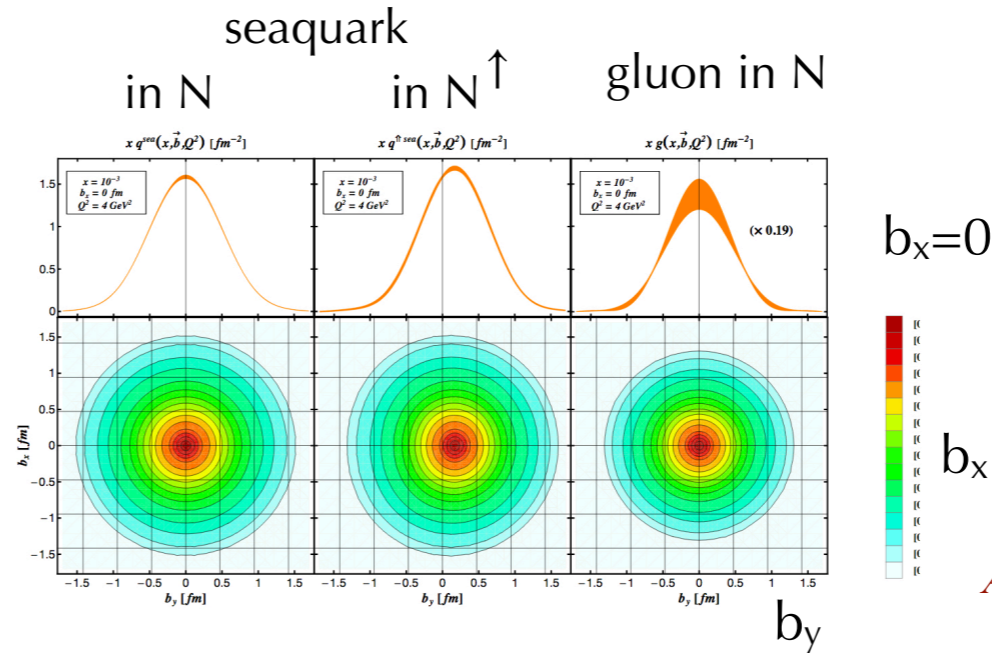


The EIC performance : GPDs

impact parameter distribution $\rho(x, \mathbf{b}_T)$

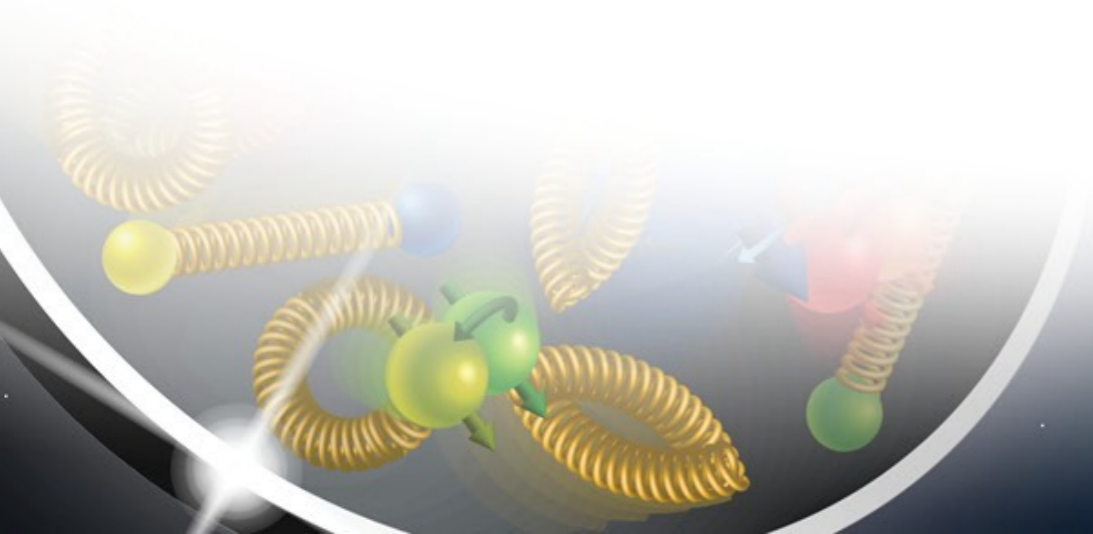
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Aschenauer et al., JHEP09 (13) 093

- models: GK *Goloskokov & Kroll, EPJ C42 (05) 281* VGG *Vanderhaeghen et al., PRL 80 (98) 5064* reggeized diquark *Goldstein et al., PR D84 (11) 034007*

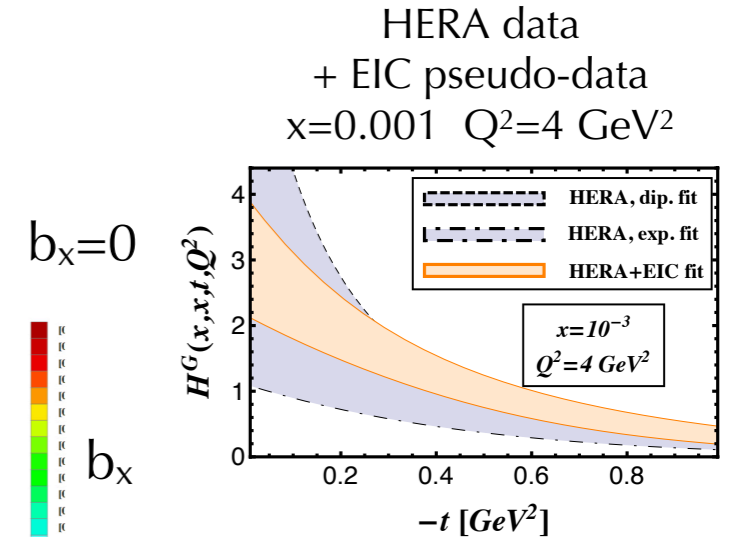
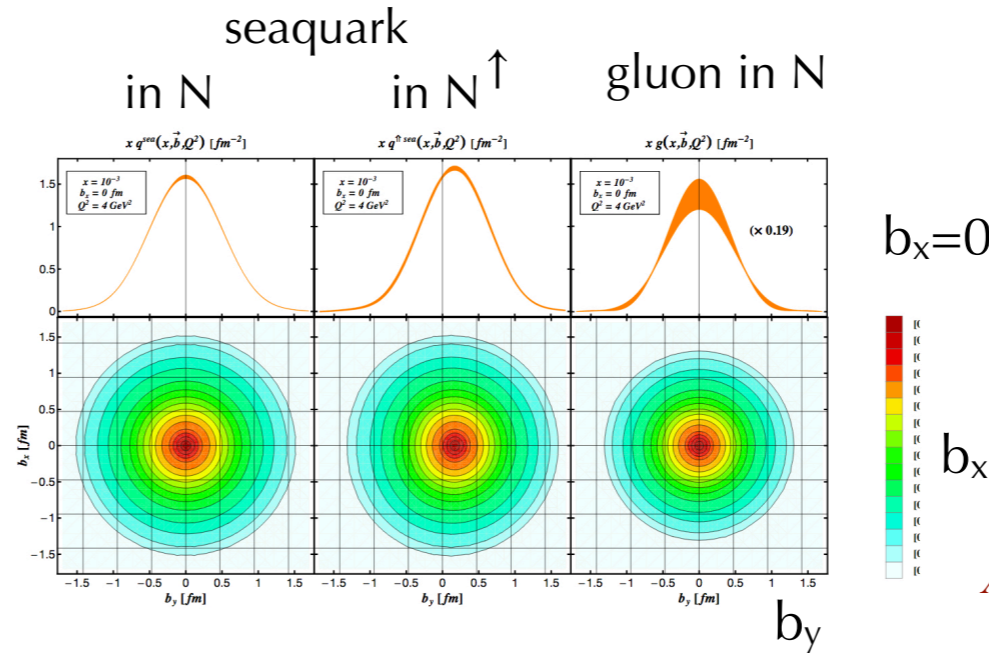


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Aschenauer et al., JHEP09 (13) 093

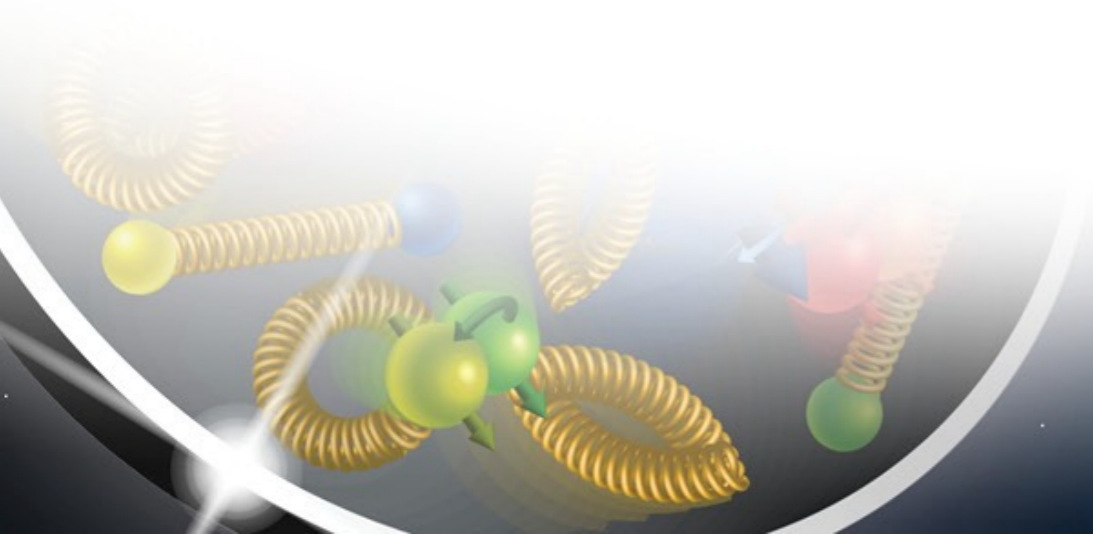
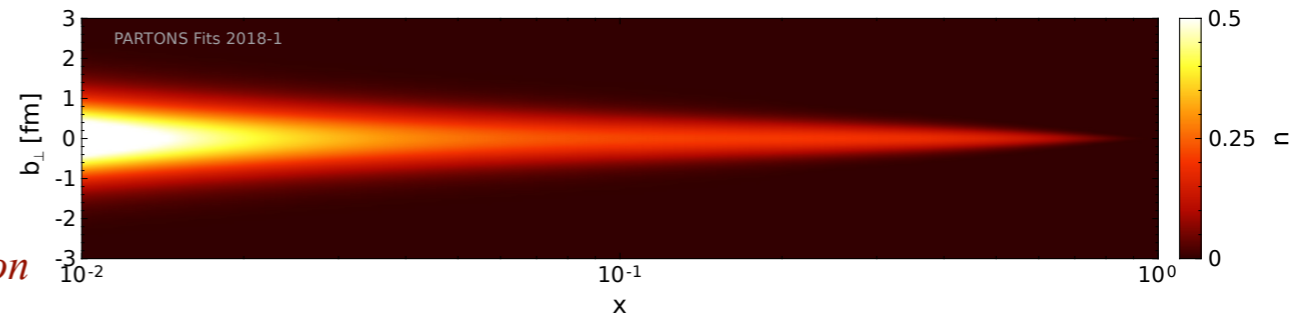
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- global fits of CFF
(of DVCS)

Kumericki et al., NPB794 (08) 244

Moutarde et al., EPJ C78 (18) 890

PARTON Collaboration

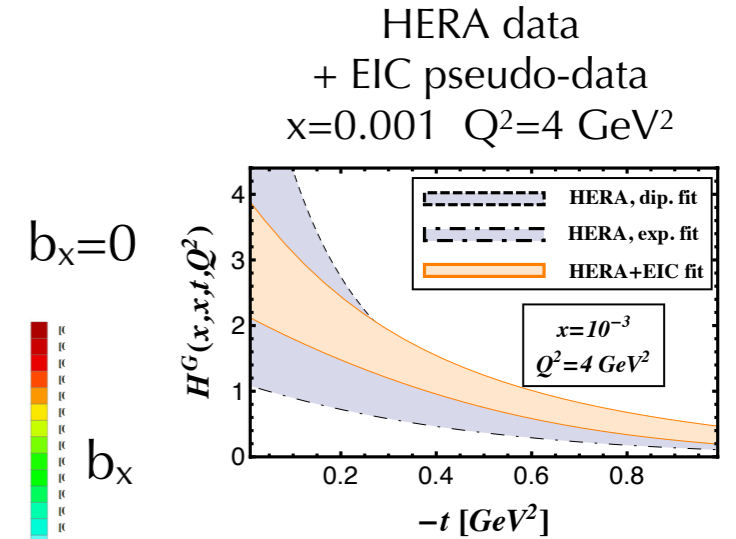
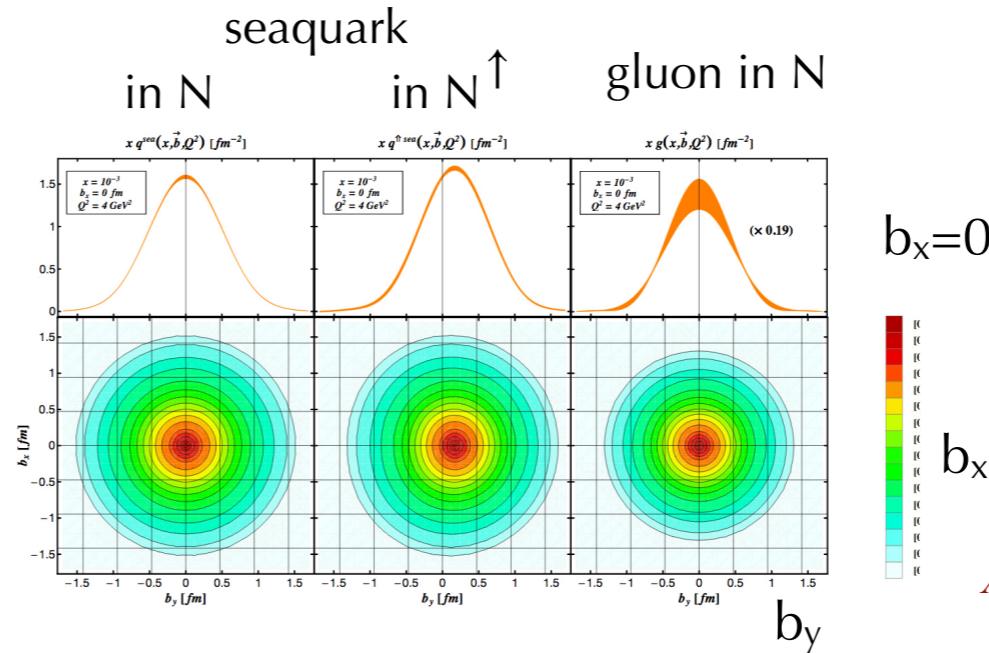


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Aschenauer et al., JHEP09 (13) 093

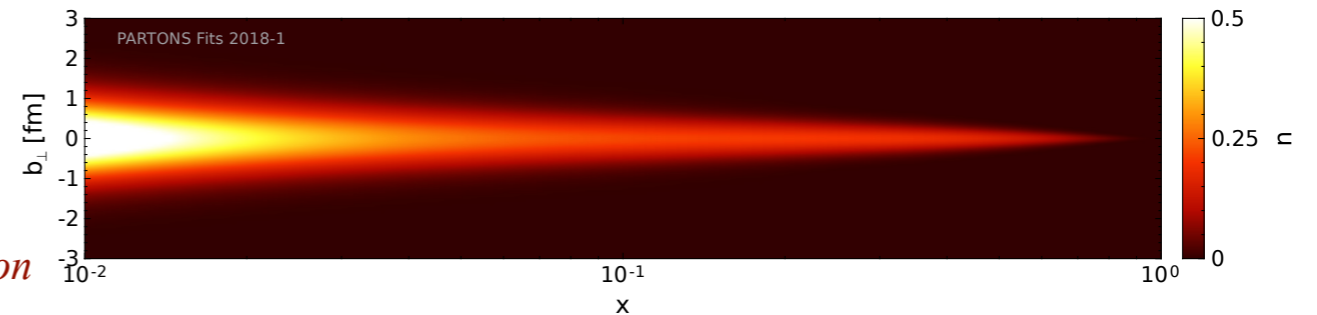
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Kumericki et al., NPB794 (08) 244

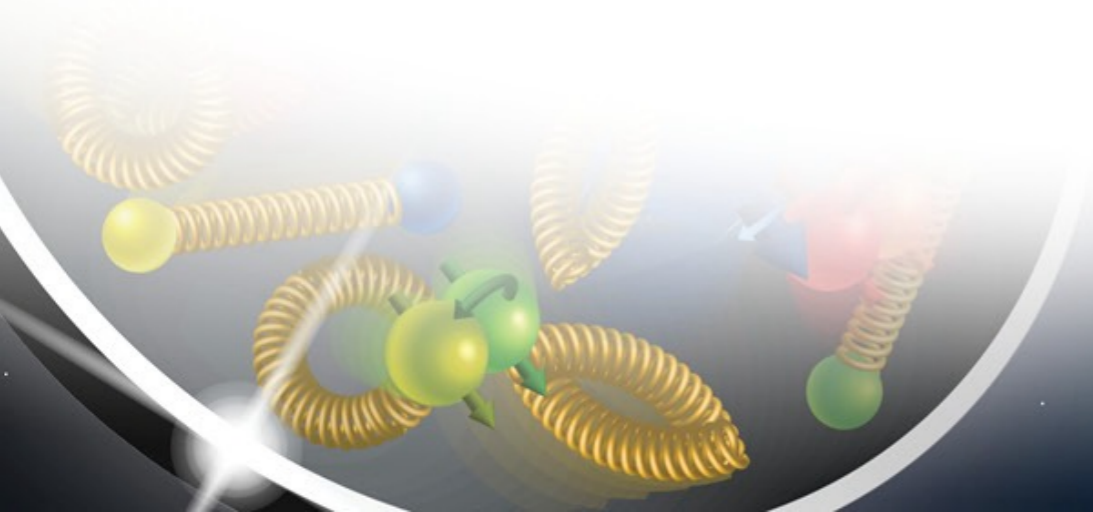
Moutarde et al., EPJ C78 (18) 890

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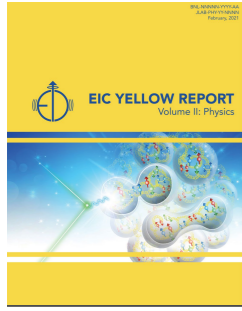


future developments: neural network techniques for GPDs
combine DVCS, DVMP, TCS to solve ambiguity
in extraction of GPD from CFF

Decomposition of Nucleon mass



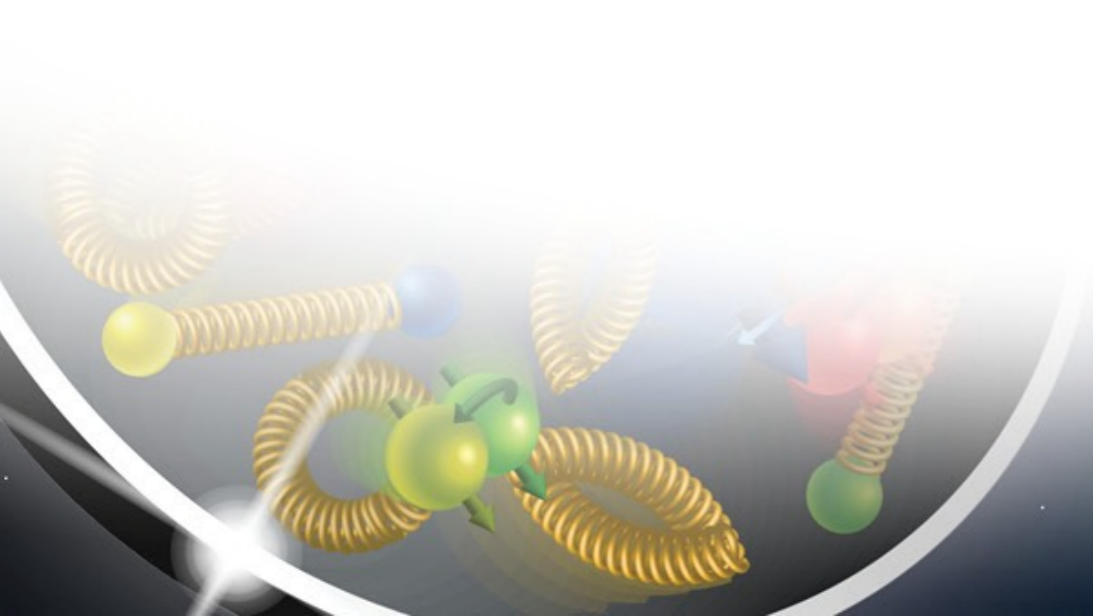
The EIC performance : origin of N mass



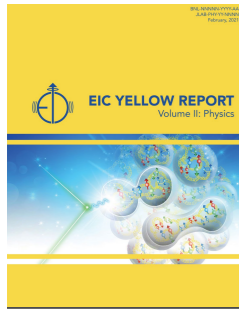
arXiv:2103.05419,
N.P.A in press

Nucleon mass decomposition with QCD EMT $T^{\mu\nu}$

$$\langle p | T_{\mu\nu}^{Q,G} | p' \rangle = \bar{u}(p') \left[M_2^{Q,G}(t) \frac{P_\mu P_\nu}{M_N} + J^{Q,G}(t) \frac{i(P_\mu \sigma_{\nu\rho} + P_\nu \sigma_{\mu\rho}) \Delta^\rho}{2M_N} + d_1^{Q,G}(t) \frac{\Delta_\mu \Delta_\nu - g_{\mu\nu} \Delta^2}{5M_N} + \bar{c}(t) g_{\mu\nu} \right] u(p)$$



The EIC performance : origin of Nucleon mass



arXiv:2103.05419,
N.P.A in press

Nucleon mass decomposition with QCD EMT $T^{\mu\nu}$

$$\langle p | T_{\mu\nu}^{Q,G} | p' \rangle = \bar{u}(p') \left[M_2^{Q,G}(t) \frac{P_\mu P_\nu}{M_N} + J^{Q,G}(t) \frac{i(P_\mu \sigma_{\nu\rho} + P_\nu \sigma_{\mu\rho}) \Delta^\rho}{2M_N} + d_1^{Q,G}(t) \frac{\Delta_\mu \Delta_\nu - g_{\mu\nu} \Delta^2}{5M_N} + \bar{c}(t) g_{\mu\nu} \right] u(p)$$

forward matrix elements
($\Delta=p-p'=0 \rightarrow t=\Delta^2=0$)

$$M_N = E_Q + E_G$$

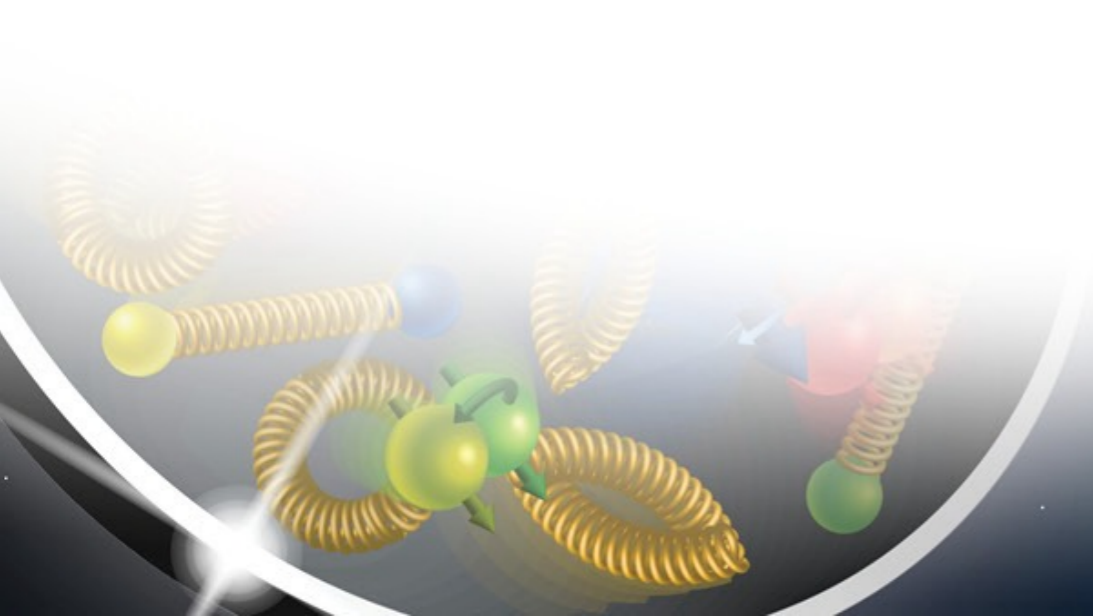
relativistic motion
of quarks and gluons
(~70% ?)

$$+ \bar{c}_q(0) \left(= \langle \bar{\psi} m \psi \rangle \right)$$

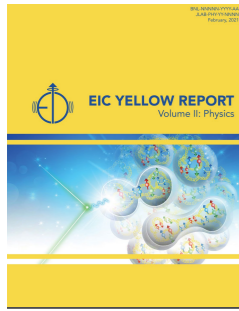
quark condensate
 σ -term from πN scatt.
(~9%?)

$$+ \bar{c}_g(0) \left(= \left\langle \frac{\beta(g)}{2g} F^2 + \gamma_m \bar{\psi} m \psi \right\rangle \right)$$

trace anomaly
?



The EIC performance : origin of Nucleon mass



arXiv:2103.05419,
N.P.A in press

Nucleon mass decomposition with QCD EMT $T^{\mu\nu}$

$$\langle p | T_{\mu\nu}^{Q,G} | p' \rangle = \bar{u}(p') \left[M_2^{Q,G}(t) \frac{P_\mu P_\nu}{M_N} + J^{Q,G}(t) \frac{i(P_\mu \sigma_{\nu\rho} + P_\nu \sigma_{\mu\rho}) \Delta^\rho}{2M_N} + d_1^{Q,G}(t) \frac{\Delta_\mu \Delta_\nu - g_{\mu\nu} \Delta^2}{5M_N} + \bar{c}(t) g_{\mu\nu} \right] u(p)$$

forward matrix elements
($\Delta=p-p'=0 \rightarrow t=\Delta^2=0$)

$$M_N = E_Q + E_G + \bar{c}_q(0) \left(= \langle \bar{\psi} m \psi \rangle \right) + \bar{c}_g(0) \left(= \left\langle \frac{\beta(g)}{2g} F^2 + \gamma_m \bar{\psi} m \psi \right\rangle \right)$$

relativistic motion
of quarks and gluons
(~70% ?)

quark condensate
 σ -term from πN scatt.
(~9%?)

trace anomaly
?

$\langle F^2 \rangle$ from threshold γ - / e-production of J/ψ and Y

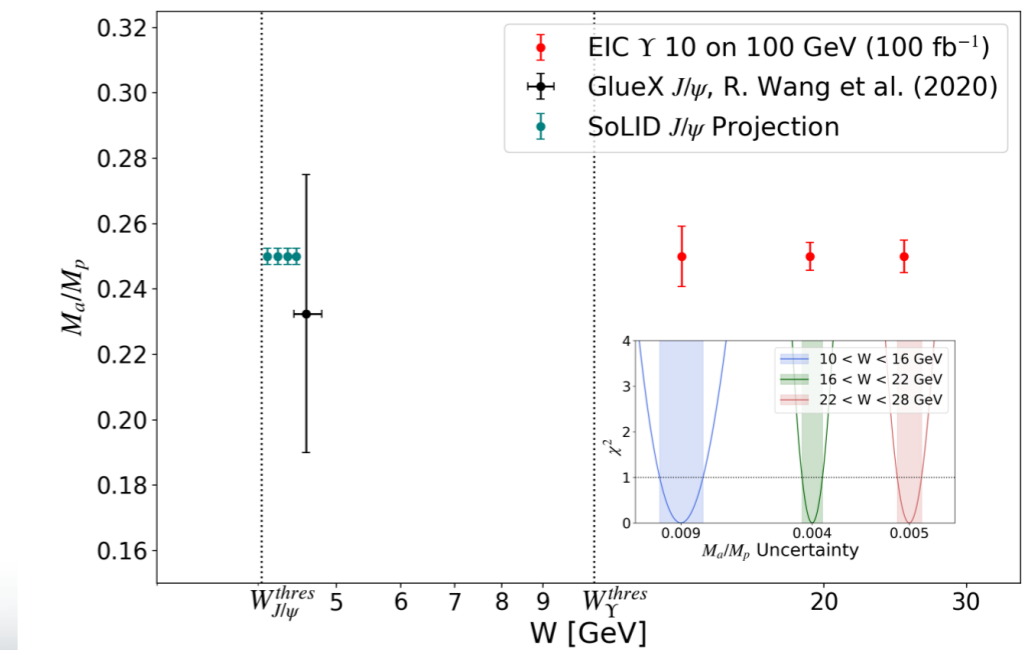
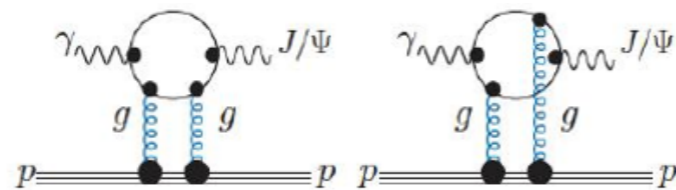


Figure 7.26: Projection of the trace anomaly contribution to the proton mass (M_a/M_p) with Y photoproduction on the proton at the EIC in 10×100 GeV electron/proton beam-energy