

QCD and the XYZs

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References

- R.T. Kleiv, TGS, Ailin Zhang, Ian Blokland
[Phys. Rev. D87 \(2013\) 125018 \[arXiv:1304.7816\]](#)
- Wei Chen, Hong-ying Jin, R.T. Kleiv, TGS, Meng Wang, Qing Xu
[Phys. Rev. D88 \(2013\) 045027 \[arXiv:1305.0244\]](#)
- Wei Chen, R.T. Kleiv, TGS, B. Bulthuis, D. Harnett, J. Ho, T. Richards, Shi-Lin Zhu
[JHEP 09 \(2013\) 019 \[arXiv:1304.4552\]](#)
- Wei Chen, TGS, Meng-Lin Du, Shi-Lin Zhu
[Eur. Phys. J C74 \(2014\) 2773 \[arXiv:1308.5060\]](#)
- Wei Chen, TGS, Shi-Lin Zhu
[Journal of APCosPA 2 \(2014\) 13 \[arXiv:1403.7457\]](#)
- Wei Chen, TGS, Hua-Xing Chen, Shi-Lin Zhu
[arXiv:1501.03863](#)
- Wei Chen, TGS, Hua-Xing Chen, Shi-Lin Zhu
[arXiv:1505.05619](#)

Outline

- Overview of XYZ states and possible interpretations
- Overview of QCD sum-rule methods
- Selected QCD sum-rule results:
 - Z_c^+ , $J^{PC} = 1^{+-}$ molecular states
 - Closed-charm tetraquark states
 - Charmonium hybrids
 - Mixed Molecular-Hybrid scenario for X(3872)
 - Diquarks and Tetraquark Scenario
- Summary

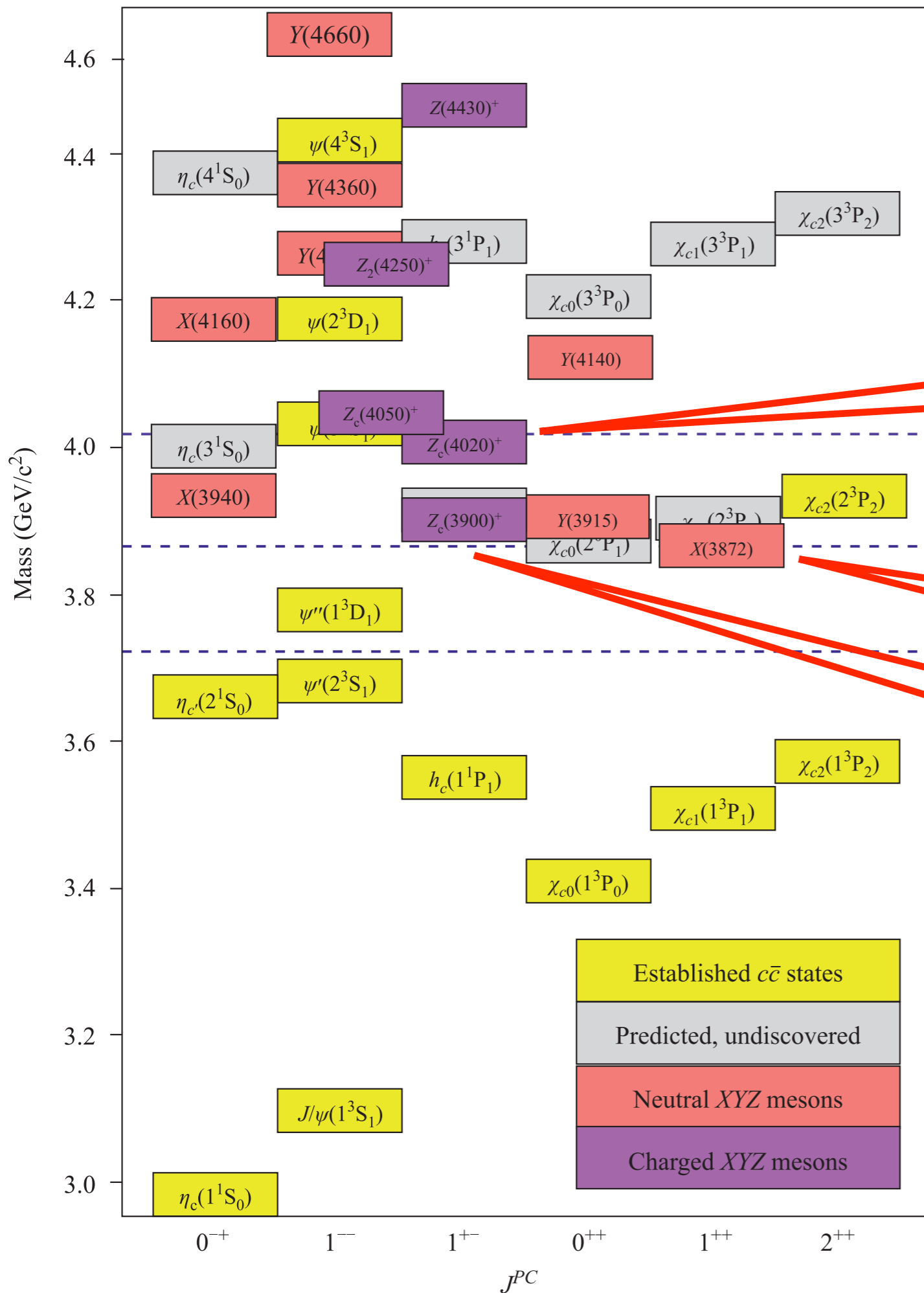
Limit discussion to charm (closed flavour) sector

What are the XYZ Mesons?

- Charmonium-like and bottomonium-like states that defy standard interpretations
- Decay into final states containing $\bar{c}c$ or $\bar{b}b$ pair
- Many such states (more than 25) discovered/confirmed since 2003 by BaBar, Belle, BES, CDF, CMS, CLEO, LHCb
- Denoted as X, Y, Z states in literature; PDG 2014 only uses X
- No sign that discovery is slowing
- Production of heavy pair from vacuum suppressed; assumed in initial state
- Charged states $Z_c^+(3900)$, $Z_1^+(4050)$, $Z_2(4250)$, $Z_c^+(4050)$, $Z_c^+(4200)$, $Z^+(4430)$
evidence for four-quark states $\bar{c}cud\bar{d}$

recent Belle results: [arXiv: 1410.7641](https://arxiv.org/abs/1410.7641), PRD90 (2014)

XYZ Overview



neutral partner: isotriplet

likely isosinglet

neutral partner: isotriplet

Most widths 100 MeV or less,
 Z(4200), Z(4430) widest

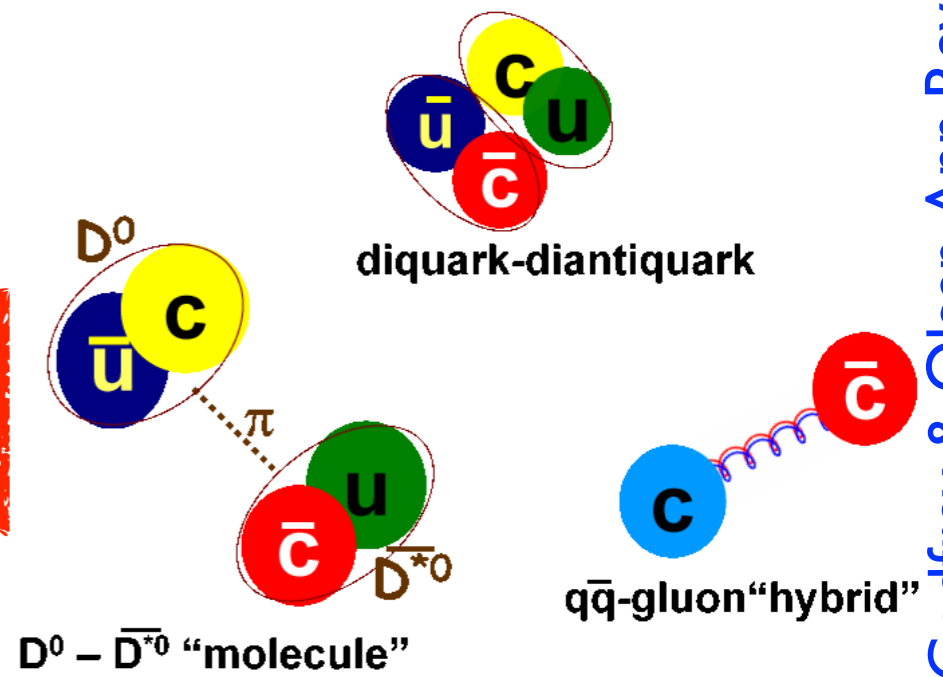
Olsen, Front. Phys. 10 (2015) 101401

Interpretations of XYZs

- **Charmonium** (needs to be ruled out first)
- **Hybrids**: mesons with gluonic excitation (colourless quark-antiquark-gluon state), can have conventional or exotic J^{PC}
- **Four-Quark** scenarios
 - **Molecules**: meson-meson bound state
 - **Tetraquarks**: diquark-antidiquark state (diquark colour triplet just like quarks)
 - **Hadrocharmonium**: tightly bound $\bar{c}c$ pair in light meson cloud
- **Mixed scenarios**: when pure interpretations fail

Also used to interpret light-quark scalar sector

Four-Quark scenarios have different internal quark configurations



QCD Sum-Rules

- Basic concept similar to lattice QCD: study **correlation functions** of (local) currents $J(x)$ with quantum numbers of state

$$\Pi(Q^2) = i \int d^4x e^{iq \cdot x} \langle 0 | T [J(x) J(0)] | 0 \rangle$$

Local operator obscures
internal structure

- Classify states $|M\rangle$ by coupling to current $\langle 0 | J | M \rangle \neq 0$
- Currents are **probes of spectrum** and might not overlap with desired state
- Apply Borel transform to correlation function's dispersion relation
- **Laplace sum-rules** relate QCD prediction to hadronic spectral function

$$\mathcal{R}_k(\tau, s_0) = \frac{1}{\pi} \int_{t_0}^{s_0} t^k \exp(-t\tau) \rho^{\text{had}}(t) dt$$

- Both lattice and QCD sum-rules predict mass from exponential decays (in distance for lattice, in Borel-transformed momentum space for sum-rules)
- Sum-rules contain power-law contributions from **QCD condensates** (non-perturbative inputs)

Z_c^+ , $J^{PC} = 1^{+-}$ Molecular States

W Chen, TGS, H-X Chen, S-L Zhu
arXiv:1505.05619

- Experimental evidence of a landscape of charged states (spin of Z_1 and Z_2 ?)

$$Z_c^+(3900), Z_1^+(4050), Z_2(4250), Z_c^+(4050), Z_c^+(4200), Z^+(4430)$$

- Can form eight independent $J^{PC} = 1^{+-}$ “molecular” currents (4 singlet-singlet and 4 octet-octet) for QCD sum-rule analysis e.g.,

$$J_{1\mu}^{(1)} = (\bar{q}_a \gamma_5 Q_a)(\bar{Q}_b \gamma_\mu q_b) + (\bar{q}_a \gamma_\mu Q_a)(\bar{Q}_b \gamma_5 q_b)$$

$D\bar{D}^*$

$$J_{1\mu}^{(8)} = (\bar{q}_a \gamma_5 \lambda_{ab}^n Q_b)(\bar{Q}_c \gamma_\mu \lambda_{cd}^n q_d) + (\bar{q}_a \gamma_\mu \lambda_{ab}^n Q_b)(\bar{Q}_c \gamma_5 \lambda_{cd}^n q_d)$$

- Can Fierz transform the eight molecular currents into tetraquark currents (4 triplet-triplet and 4 sextet-sextet)

Local operators obscure information on internal structure [Zhang, Huang, TGS PRD76 \(2007\)](#)

- Calculate QCD sum-rule for correlation function at leading loop-order, dominant non-perturbative effects from quark and mixed condensate

Z_c^+ , $J^{PC} = 1^{+-}$ QCD Sum-Rule Analysis

- QCD input parameters

$$m_c(m_c) = (1.23 \pm 0.09)\text{GeV}, \quad m_b(m_b) = (4.20 \pm 0.07)\text{GeV},$$

$$\langle \bar{q}g_s\sigma \cdot Gq \rangle = -M_0^2 \langle \bar{q}q \rangle, \quad M_0^2 = (0.8 \pm 0.2)\text{GeV}^2$$

$$\langle \bar{q}q \rangle = -(0.23 \pm 0.03)^3\text{GeV}^3, \quad \langle g_s^2 GG \rangle = (0.88 \pm 0.14)\text{GeV}^4$$

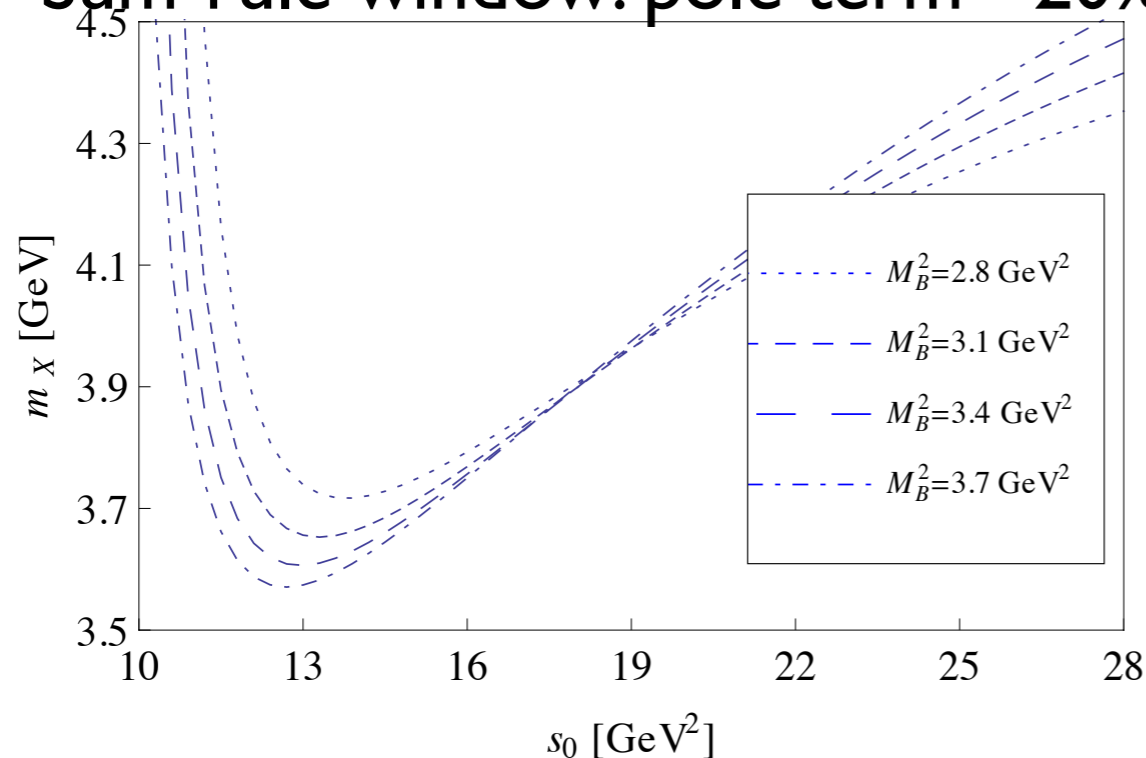
- Single narrow resonance plus QCD continuum model, predict mass M_X via

$$M_X^2 = \frac{\mathcal{R}_1(\tau, s_0)}{\mathcal{R}_0(\tau, s_0)}$$

critical point of ratio

- Narrow width approximation very good since $\tau \Gamma M_X$ is small

- Sum-rule window: pole term >20%, highest dimension condensates <5%

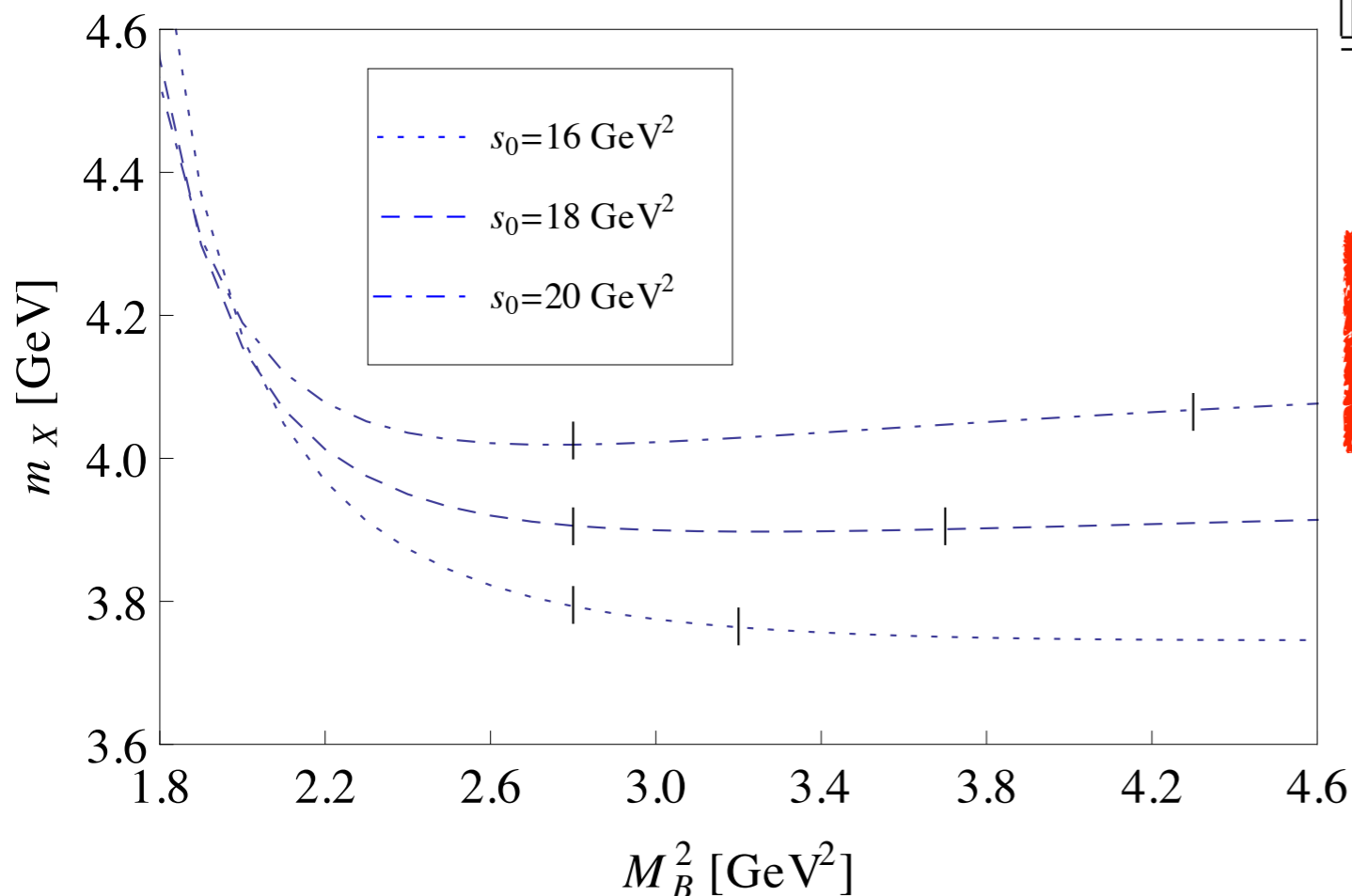


Z_c^+ , $J^{PC} = 1^{+-}$ Molecular Mass Spectrum

$Z_c(4200)$

$Z_c(3900)$, $Z_c(4020)$,
 $Z_c(4050)$

Current	s_0 (GeV^2)	M_X (GeV)
$J_{1\mu}^{(1)}, D\bar{D}^*$	21	4.22 ± 0.14
$J_{2\mu}^{(1)}, D_0^*\bar{D}_1$	—	—
$J_{3\mu}^{(1)}, D^*\bar{D}^*$	20	4.04 ± 0.12
$J_{4\mu}^{(1)}, D_1\bar{D}_1$	20	4.02 ± 0.15
$J_{1\mu}^{(8)}$	18	3.90 ± 0.12
$J_{2\mu}^{(8)}$	—	—
$J_{3\mu}^{(8)}$	18	3.85 ± 0.11
$J_{4\mu}^{(8)}$	20	4.03 ± 0.18



Landscape of charged and neutral Z_c molecular states

W Chen, TGS, H-X Chen, S-L Zhu
arXiv:1505.05619

Charmonium Hybrids

W Chen, Kleiv, TGS, Bulthuis, Harnett, Richards,
Ho, S-L Zhu, JHEP09 (2013)



- Mesons with gluonic excitation (quark-antiquark-gluon) form colourless states
- Can have conventional J^{PC} and mix with quark-antiquark mesons
- Can have non-standard J^{PC} like 1^{-+} with clear **exotic** signature
- Unique decay signatures (e.g. S-wave meson pairs suppressed) Isgur et al, PRL54 (1985)
- Y(4260) has been interpreted as hybrid candidate S-L Zhu, PLB625 (2005)
- Bag model and lattice QCD: supermultiplet structure, odd parity states lighter

Comprehensive QCD sum-rule
analysis for exotic and conventional
quantum numbers

Charmonium Hybrid QCD Sum-Rule Analysis

- Construct hybrid interpolating currents for exotic and conventional J^{PC}

$$J_\mu = g_s \bar{Q} \frac{\lambda^a}{2} \gamma^\nu G_{\mu\nu}^a Q, \quad J^{PC} = 1^{-+}, 0^{++},$$

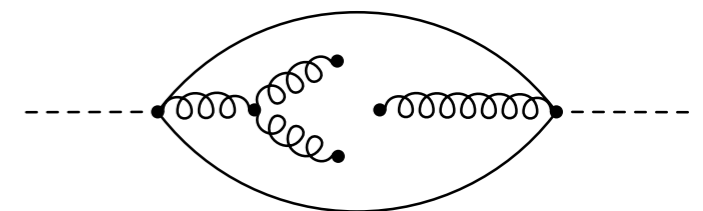
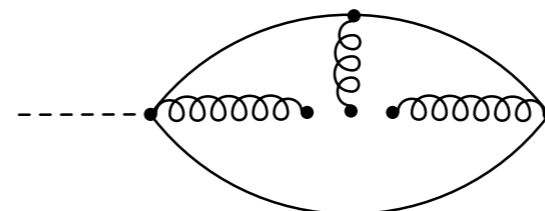
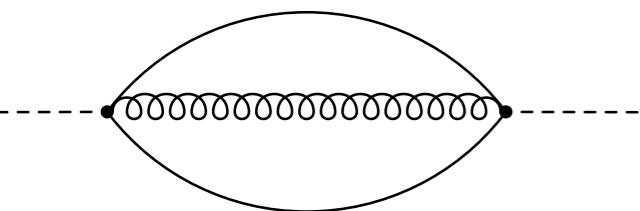
$$J_\mu = g_s \bar{Q} \frac{\lambda^a}{2} \gamma^\nu \gamma_5 G_{\mu\nu}^a Q, \quad J^{PC} = 1^{+-}, 0^{--},$$

opposite parity
 $G \rightarrow \tilde{G}$

$$J_{\mu\nu} = g_s \bar{Q} \frac{\lambda^a}{2} \sigma_{\mu\nu}^{\alpha\beta} \gamma_5 G_{\alpha\beta}^a Q, \quad J^{PC} = 2^{-+}, 1^{++}, 1^{-+}, 0^{-+}$$

- Leading order correlator (QCD sum-rule) up to dim-six gluonic condensates
- Same methodology as molecular states: stability analysis of sum-rule ratio in sum-rule window of validity

$$M_X^2 = \frac{\mathcal{R}_1(\tau, s_0)}{\mathcal{R}_0(\tau, s_0)}$$



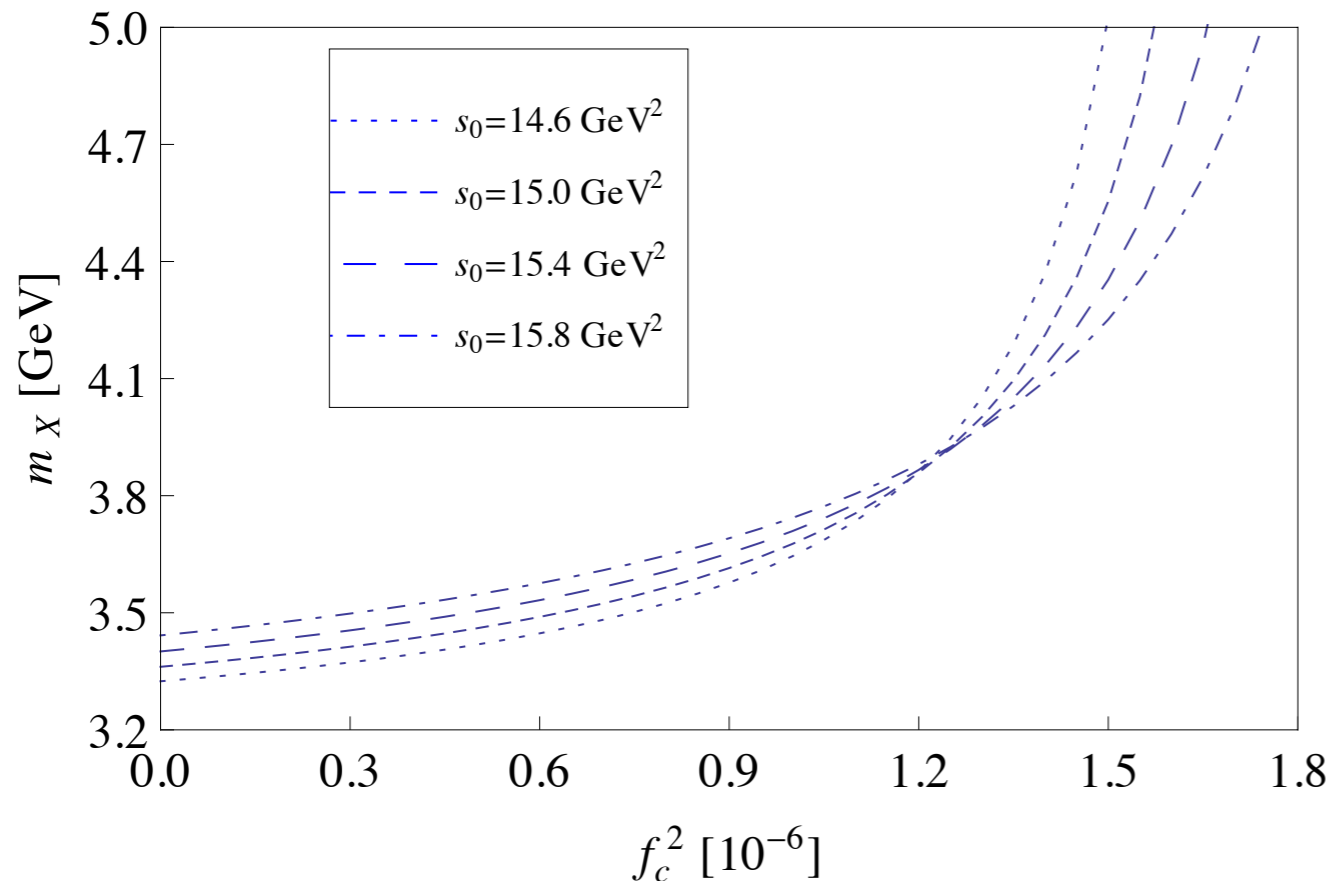
$\langle \alpha_s GG \rangle$

$\langle g_s^3 f GGG \rangle$

Charmonium Hybrid Mass Spectrum

- Supermultiplet structure based on parity
- 0^{--} anomalous: heaviest state
- For conventional J^{PC} mixing with charmonium would raise mass prediction (lower bound)
- No obvious alignment with observed XYZs

J^{PC}	$s_0(\text{GeV}^2)$	$m_X(\text{GeV})$
1^{--}	15	3.36 ± 0.15
0^{-+}	16	3.61 ± 0.21
1^{-+}	17	3.70 ± 0.21
2^{-+}	18	4.04 ± 0.23
0^{+-}	20	4.09 ± 0.23
2^{++}	23	4.45 ± 0.27
1^{+-}	24	4.53 ± 0.23
1^{++}	30	5.06 ± 0.44
0^{++}	34	5.34 ± 0.45
0^{--}	35	5.51 ± 0.50



W Chen, Kleiv, TGS, Bulthuis, Harnett, Richards, Ho, S-L Zhu, JHEP09 (2013)

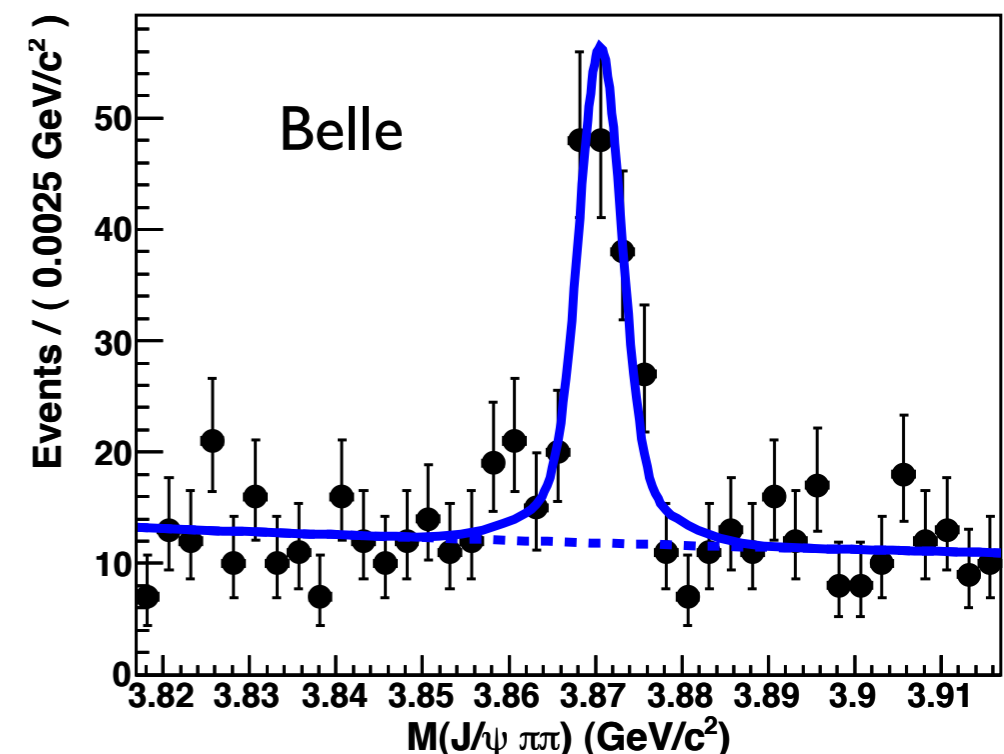
If hybrids present in XYZs might be within mixed states

The Enigmatic X(3872)

- Discovery by Belle, confirmed by CDF, D0, BaBar [Belle PRL91 \(2003\)](#)
- PDG mass 3871.69 ± 0.17 MeV and width $\Gamma < 1.2$ MeV
- LHCb settles quantum numbers: $J^{PC} = 1^{++}$ [LHCb PRL110 \(2013\)](#)
- Large isospin violation: $X \rightarrow \rho J/\psi$ and $X \rightarrow \omega J/\psi$ comparable (Belle/BaBar)
- Isospin not well understood: likely an isosinglet
- **Molecular** interpretation explains isospin violation but hard to describe radiative decays $X \rightarrow \gamma J/\psi$ [Swanson PLB588 \(2004\)](#)

Mixed scenario likely needed
for X(3872)

Godfrey hep-ph/0605152
Coito et al EPJC71 (2011)



Mixed Hybrid/Molecular Currents

- Mixed I^{++} hybrid/molecular currents for QCD sum-rule analysis

$$J_{\mu}^h = \frac{1}{2} g \bar{c} \gamma^{\nu} \lambda^a \tilde{G}_{\mu\nu}^a c, \quad \tilde{G}_{\mu\nu}^a = \frac{1}{2} \epsilon_{\mu\nu\alpha\beta} G_a^{\alpha\beta}, \quad J_{\nu}^m = \frac{1}{\sqrt{2}} (\bar{q}_a \gamma_5 c_a \bar{c}_b \gamma_{\nu} q_b - \bar{q}_a \gamma_{\nu} c_a \bar{c}_b \gamma_5 q_b)$$

$$J_{\nu}^{\xi} = \sqrt{1 - \xi^2} J_{\nu}^m + \xi \sigma J_{\nu}^h$$

- Parameter $0 < \xi < 1$ **interpolates** between molecular and hybrid limits; σ is mass scale (set $\sigma = 1$ GeV with no loss of generality)

Harnett, Kleiv, TGS, H-Y Jin, JPG39 (2012)

Lee et al arXiv:0803.1168

- Mixed current correlation function contains known hybrid-hybrid and molecular-molecular results; off-diagonal (hm) correlator must be calculated

$$\Pi_{\mu\nu}^{\xi}(q) = i \int d^4x e^{iq \cdot x} \langle 0 | T [J_{\mu}^{\xi}(x) J_{\nu}^{\xi}(0)] | 0 \rangle$$

$$\Pi_{\mu\nu}^{hm}(q) = i \int d^4x e^{iq \cdot x} \langle 0 | T [J_{\mu}^h(x) J_{\nu}^m(0)] | 0 \rangle$$

I^{++} transverse part

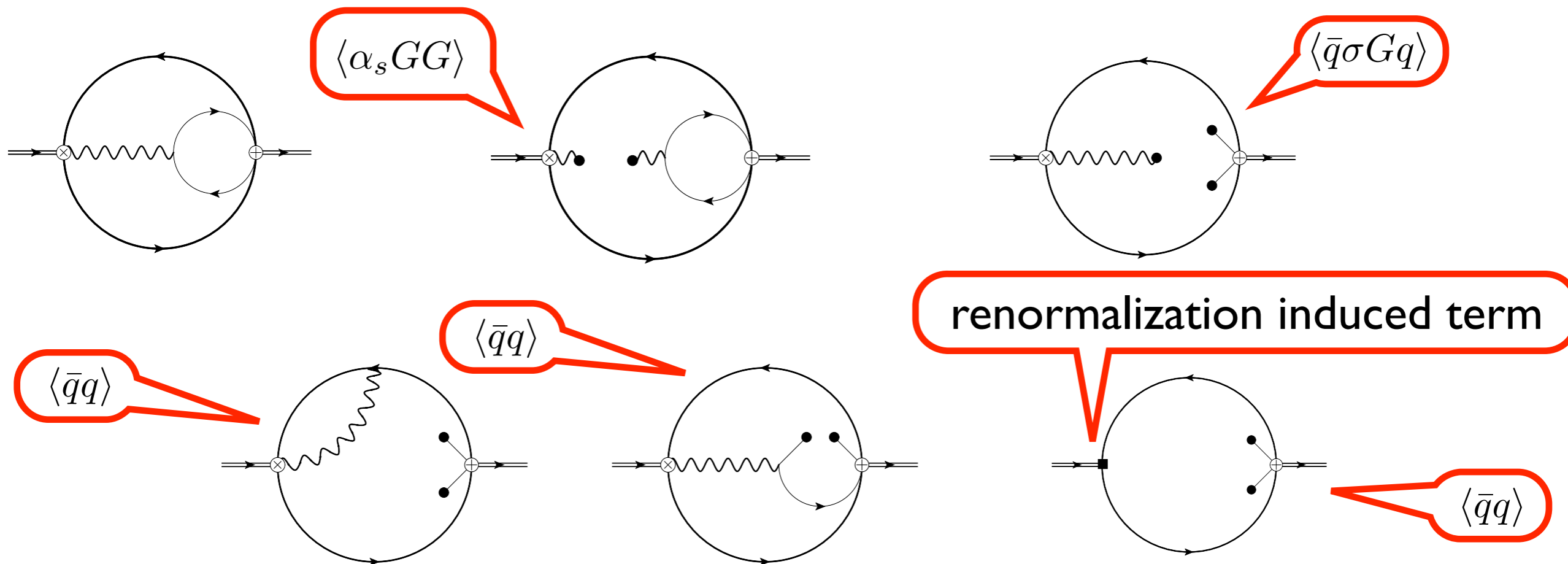
Molecule/Hybrid QCD Sum-Rule Analysis

- Mixed correlator subtle: need to renormalize hybrid (composite) operator

$$[J_\mu^h]_R = Z_1 [J_\mu^h]_B + Z_2 m^2 [\mathcal{O}_\mu]_B + \dots, \quad Z_1 = 1 + \frac{\alpha}{\pi} \frac{Z_{h1}}{\epsilon}, \quad Z_2 = -\frac{10}{243} \frac{\alpha}{\pi} \frac{1}{\epsilon}$$

$$\mathcal{O}_\mu = \bar{c} \Gamma_\mu c, \quad \Gamma_\mu = \epsilon_{\mu\nu\alpha\beta} (\gamma^\nu \sigma^{\alpha\beta} + \gamma^\alpha \sigma^{\beta\nu} - \gamma^\beta \sigma^{\alpha\nu})$$

- Leading order, condensates up to dimension five

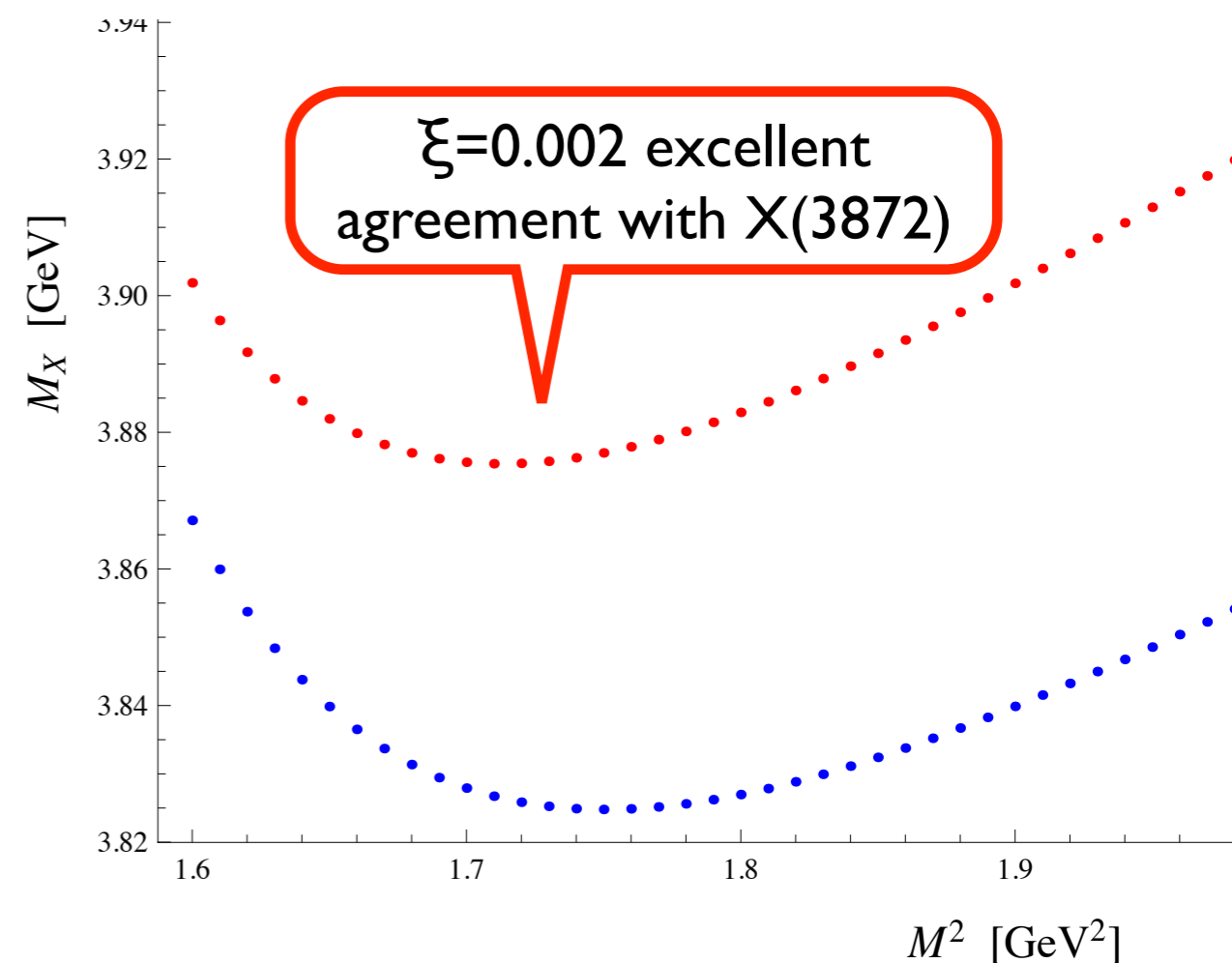
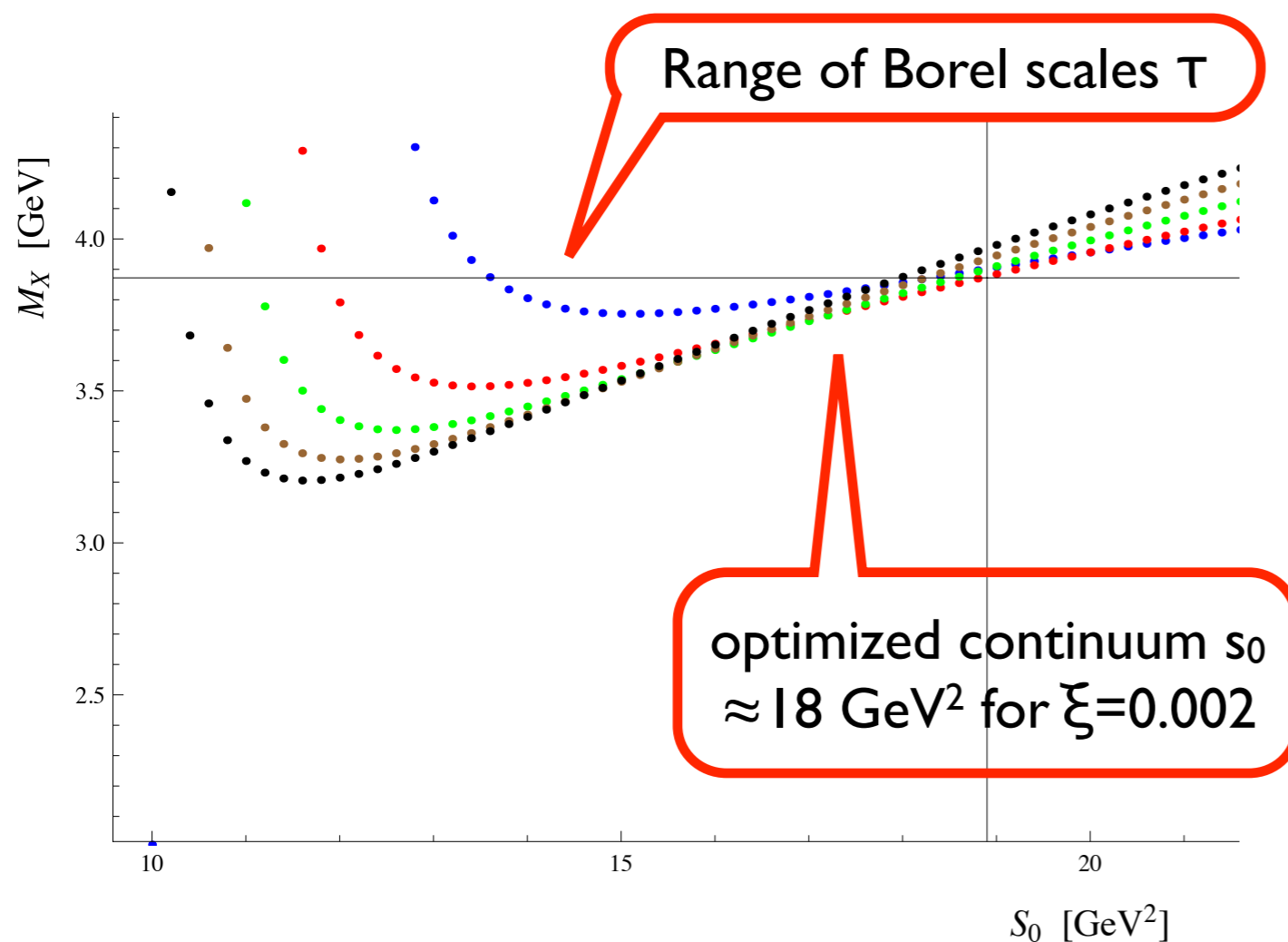


W Chen, H-Y Jin, Kleiv, TGS, M Wang, Q Xu, PRD88 (2013)

X(3872): Mixed Hybrid/Molecule

W Chen, H-Y Jin, Kleiv, TGS,
M Wang, Q Xu, PRD88 (2013)

- Scan QCD sum rule for M_X over mixing parameter ξ (must optimize s_0)
- M_X increases as ξ increases from zero (pure molecule) until max at $\xi \approx 0.002$
- Viable scenario of X(3872) coupling to **mixtures of hybrid/molecular** currents
- **Significant mixing** (compare $\xi \approx 0.002$ to ratios of pure correlation functions)



Internal Structure of Multiquark XYZs

- Molecular and diquark scenarios of XYZs cluster quarks differently

- Diquarks are in colour triplet; experience colour force like quarks

- Two mixed neutral states $[cq]_{\bar{3}}[\bar{c}\bar{q}]_3$ (q=u,d)

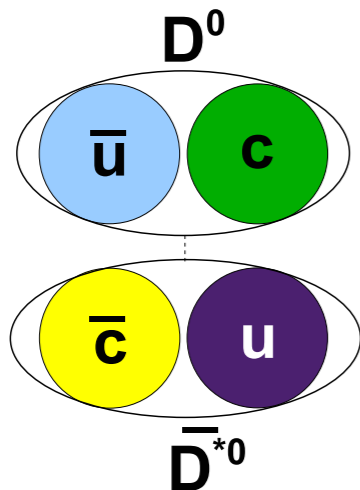
Maiani et al PRD71 (2005)

- Phenomenological input of constituent diquark mass $M_{[cq]} = 1933 \text{ MeV}$

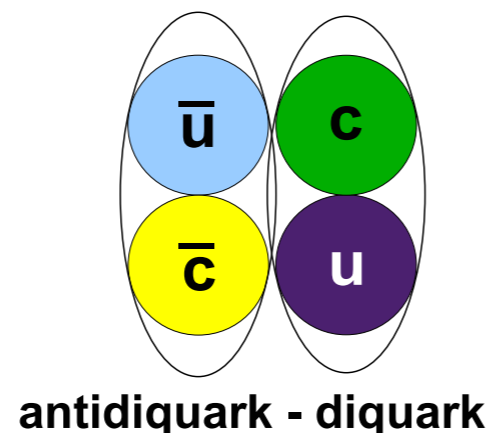
- Decay by “single switch” process $[cq]_{\bar{3}}[\bar{c}\bar{q}]_3 \rightarrow [\bar{c}c]_0[\bar{q}q]_0$

J/ψ

tuned to X(3872) !!



$D^0-\bar{D}^{*0}$ “molecule”



antidiquark - diquark

Can QCD say anything about internal structure? Diquark mass prediction provides indirect probe

Nielsen et al PhysRep497 (2010)

Heavy-Light Diquarks

Kleiv, TGS, Zhang, Blokland, PRD87 (2013)

- Gauge dependent diquark currents for QCD sum-rule analysis

$$J_\alpha = \epsilon_{\alpha\beta\gamma} Q_\beta^T C O q_\gamma; \quad O = \gamma_5, I, \gamma_\mu, \gamma_\mu \gamma_5 \quad (J^P = 0^+, 0^-, 1^+, 1^-)$$

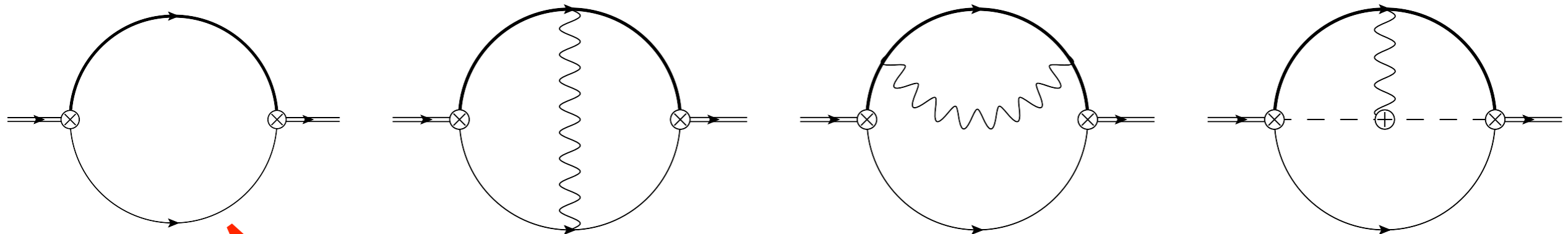
- Schwinger string extracts gauge invariant information from correlator

Dosch, Jamin, Stech,
ZPC42 (1989)

$$\Pi(Q^2) = i \int d^4x e^{iq \cdot x} \langle 0 | T [J_\alpha(x) S_{\alpha\omega}[x, 0] J_\omega^\dagger(0)] | 0 \rangle$$

$$S_{\alpha\omega}[x, 0] = P \exp \left[ig \frac{\lambda_{\alpha\omega}^a}{2} \int_0^x dz^\mu A_\mu^a(z) \right]$$

- Calculate correlator: next-to-leading perturbation theory



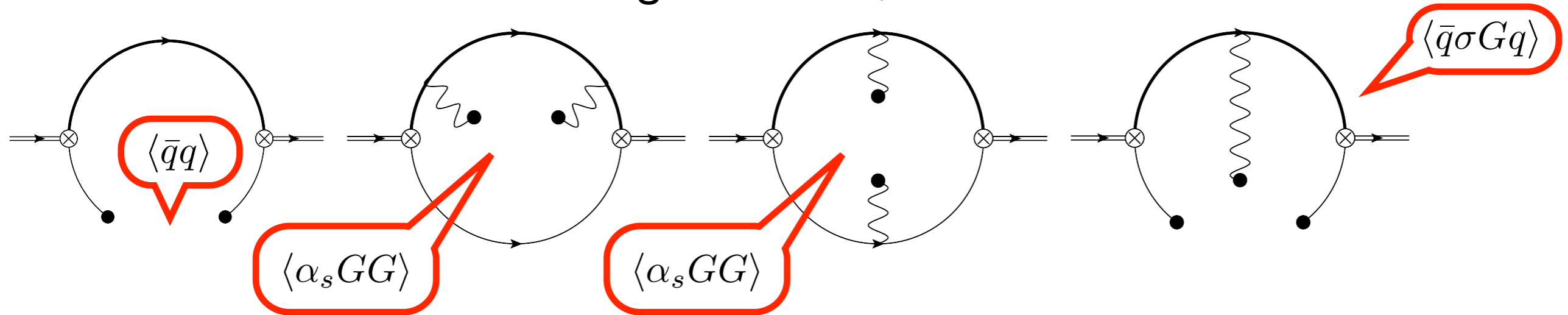
Include diquark renormalization
Kleiv, TGS, JPG38 (2011)

Schwinger string

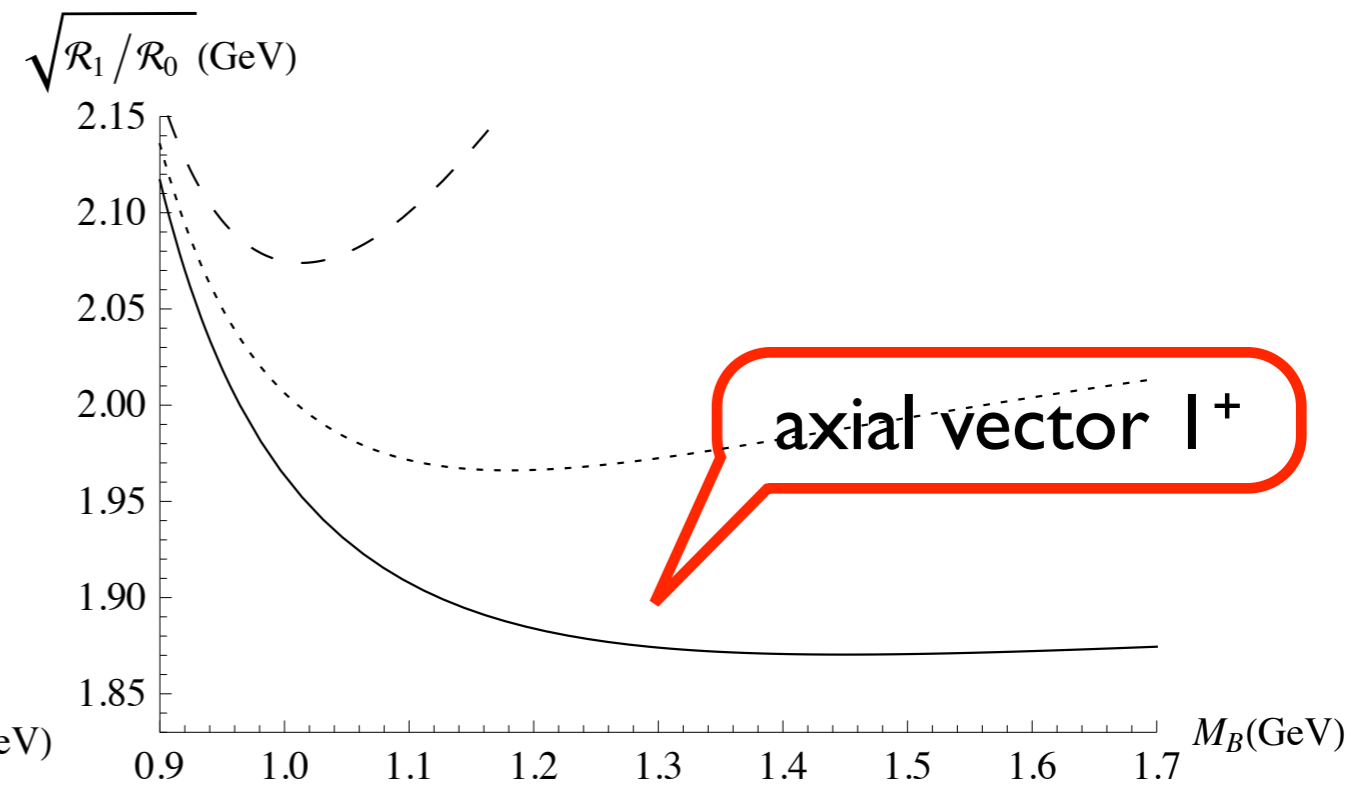
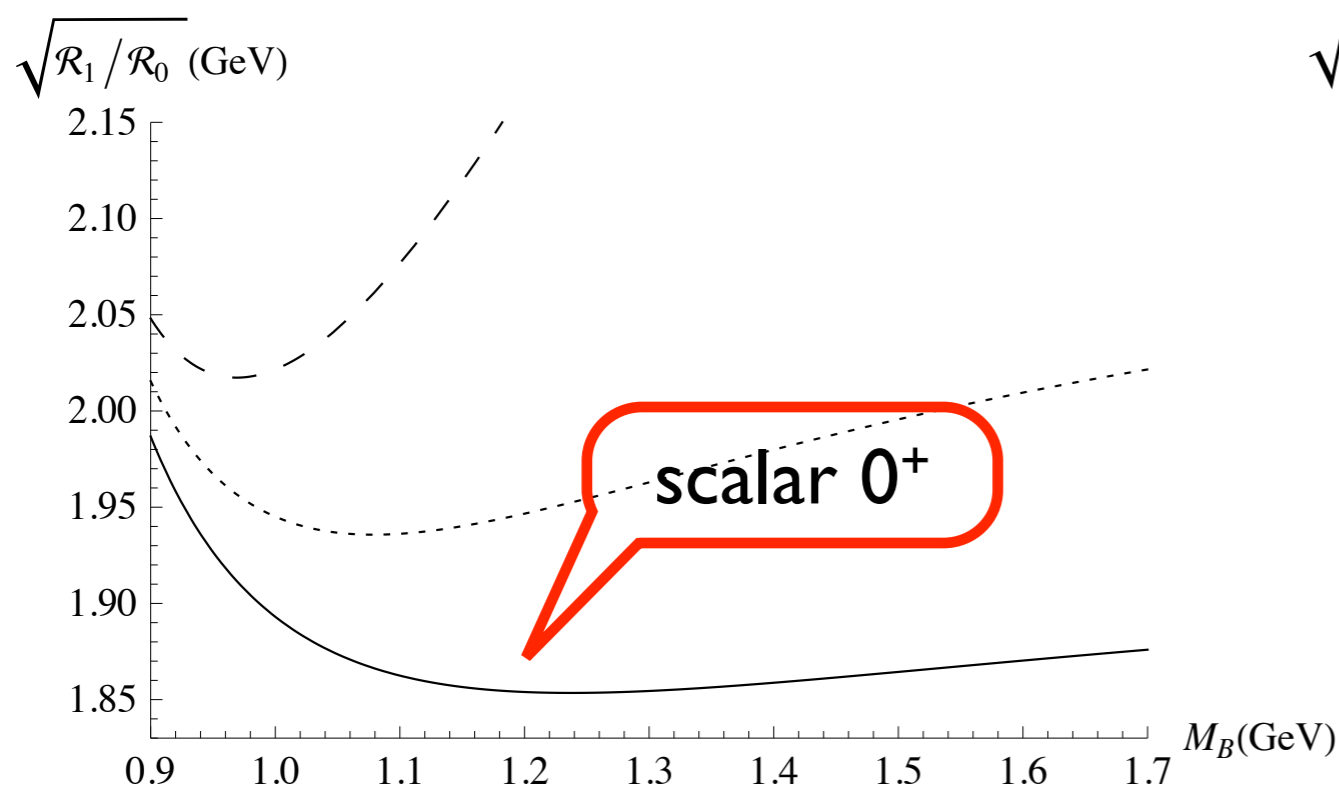
Heavy-Light Diquark Correlator

Kleiv, TGS, Zhang, Blokland,
PRD87 (2013)

- Calculate correlator: leading-order in QCD condensates to dimension five



- Standard sum-rule analysis: only stable results for positive parity diquarks
Jaffe: no negative parity “worse” diquarks



Charm-Light Diquark Mass

Kleiv, TGS, Zhang, Blokland,
PRD87 (2013)

- [cq] positive parity diquark QCD sum-rule mass predictions nearly degenerate

$$M_s = 1.86 \pm 0.05 \text{ GeV}, \quad M_a = 1.87 \pm 0.1 \text{ GeV}$$

- Excellent agreement with tetraquark model tuned to X(3872)

$$M_{[cq]} = 1933 \text{ MeV} \quad \text{Maiani et al PRD71 (2005)}$$

Indirect QCD evidence supporting
tetraquark model for XYZs

Additional results

Discussion

- Rich landscape of XYZ mesons observed that cannot be explained as charmonium states
- Many charged states now observed: multi-quark scenarios seem inevitable and provide unifying theme with light scalars
- Neutral partners for some charged states, completing isospin multiplets
- Open question: internal quark structure of multi-quark states (e.g. tetraquark versus molecular); difficult to answer with analyses based on local operators
- No evidence of pure charmonium hybrids amongst known XYZs; QCD evidence of viable mixed hybrid/multi-quark states to resolve stubborn puzzles
- QCD can provide indirect evidence for multi-quark models (e.g., agreement between diquark mass predictions in QCD and tetraquark models)

Key challenge for QCD

compelling unifying theoretical framework for the XYZs

Thank you!



People. Discovery. Innovation.



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University of Saskatchewan

Additional QCD Sum-Rule Results

- Bottomonium hybrids W Chen, Kleiv, TGS, Bulthuis, Harnett, Richards, Ho, S-L Zhu, JHEP09 (2013)
- Bottom/Charm hybrids W Chen, TGS, S-L Zhu, JPG 41 (2014)
- Open-flavour (bottom/charm) tetraquarks W Chen, TGS, S-L Zhu, PRD 89 (2014)
- $Z_c(4200)$ decay widths $Z_c^+(4200) \rightarrow J/\psi\pi^+, \eta_c\rho^+, D^+\bar{D}^{*0}$
W Chen, TGS, H-X Chen, S-L Zhu, arXiv:1501.03863

Summary