

# Probing Physics with White Dwarfs and Neutron Stars

Jeremy Heyl

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Others: Ramandeep Gill, Jason Kalirai, Paola Marigo, Harvey Richer, Pier-Emmanuel Tremblay



# Outline

## White Dwarfs

Magnetic White Dwarfs

Cooling White Dwarfs

## Neutron Stars

Magnetic Neutron Stars

Cooling Neutron Stars

Superconducting Neutron Stars

# Stars

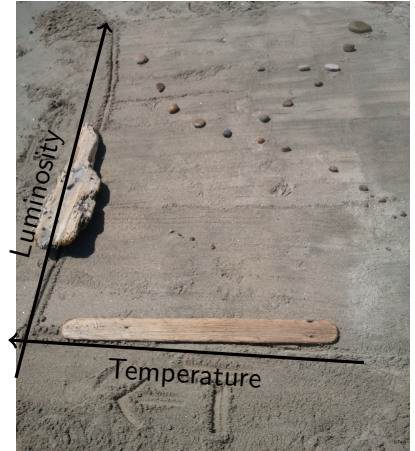
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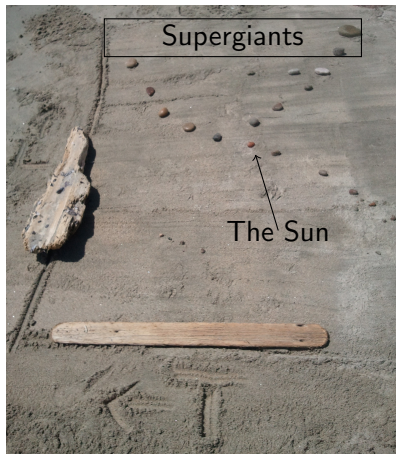
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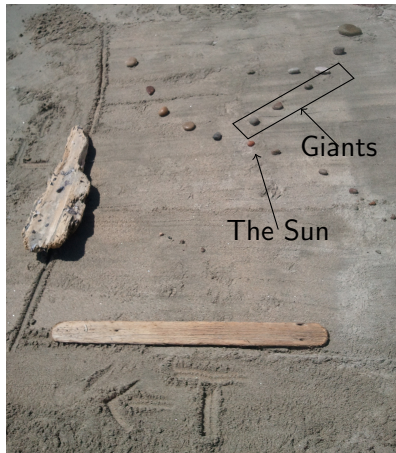
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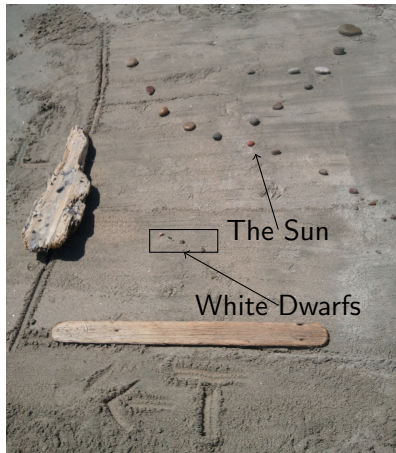
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- ▶ The Sun consumes hydrogen in its core – main sequence.
- ▶ Supergiants become neutron stars.
- ▶ Giants consume hydrogen in a shell and helium in the core,
- ▶ And become white dwarfs.





# How big are compact objects?

## White Dwarfs

Gravity yields:  $P_0 \sim \frac{GM^2}{R^4}$

Relativistic degenerate electrons

$$P_0 \sim \frac{m_e c^2}{\lambda_e^3}, M = \frac{m_p}{\lambda_e^3} R^3$$

Solving yields

$$R = \lambda_e \frac{m_p}{m_p}, M = \frac{m_p^3}{m_p^2}$$

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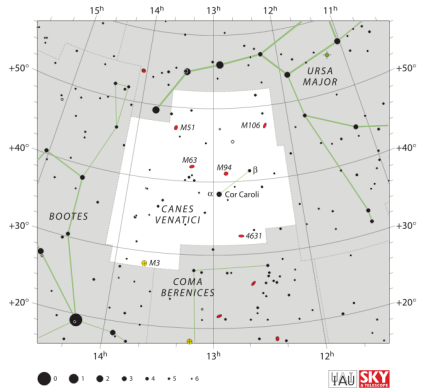
$$R = \lambda_n \frac{m_p}{m_n}, M = \frac{m_p^3}{m_n^2}$$

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# How strong can white-dwarf fields be?

Let's calculate the expected magnetic field of a white dwarf.

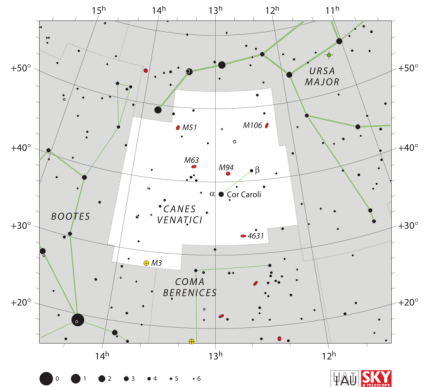
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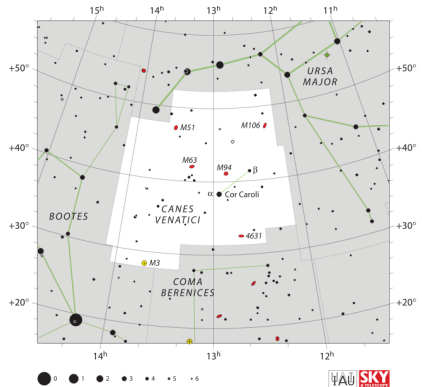
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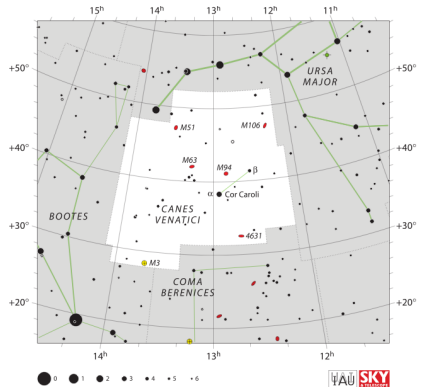
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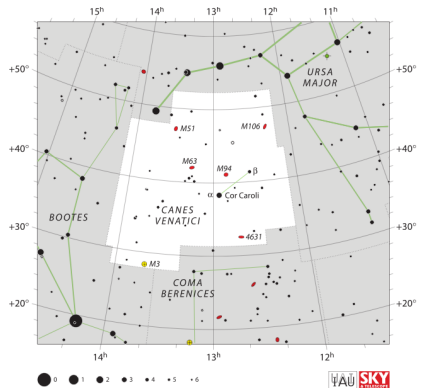
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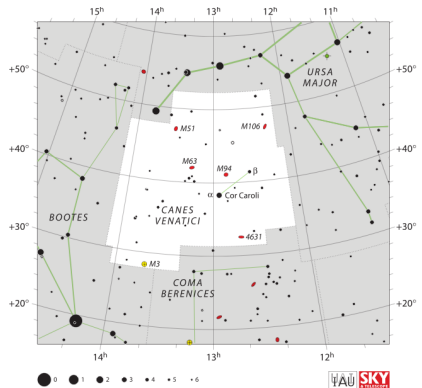
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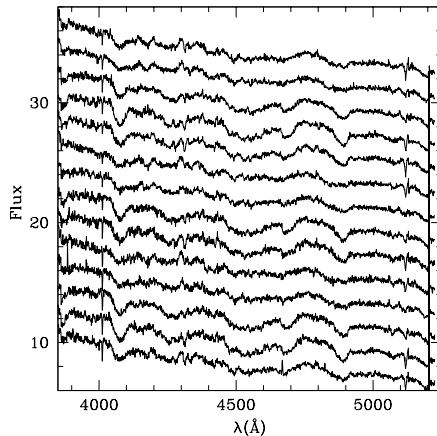
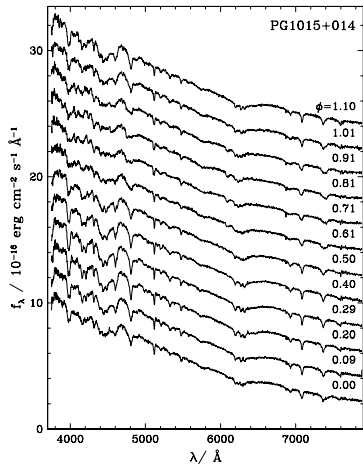
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- ▶ Magnetic Ap stars have 1 kG fields and are bigger than the Sun.
- ▶  $B \sim 100\text{MG} = 10^4\text{T}$ .





# White Dwarf Spectra

PG1015+014 : Left (Euchner et al. 2006), Right (Keck;Heyl)



# Axions and White Dwarfs

White dwarfs have exquisite polarimetric observations, finding no linear polarization to the few percent level.

Their fields are weaker  $10^{8-9}$  G, but the stars are bigger, and we know the field geometry.

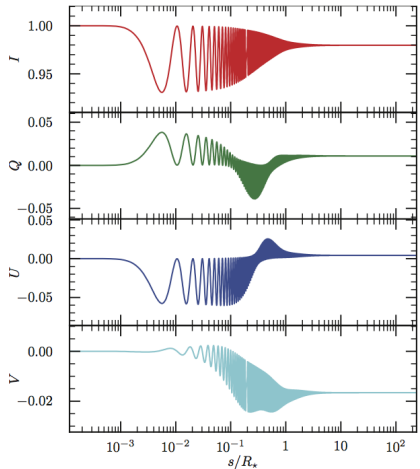
Gill, Heyl 11

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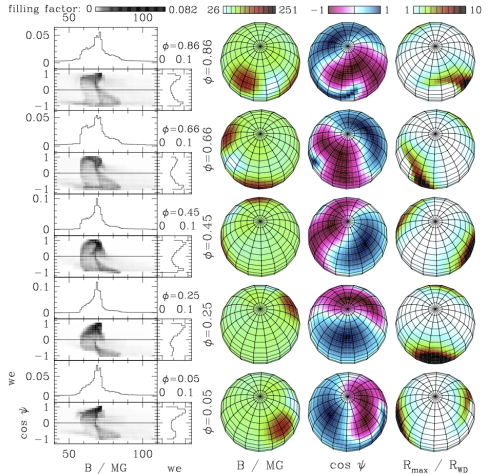


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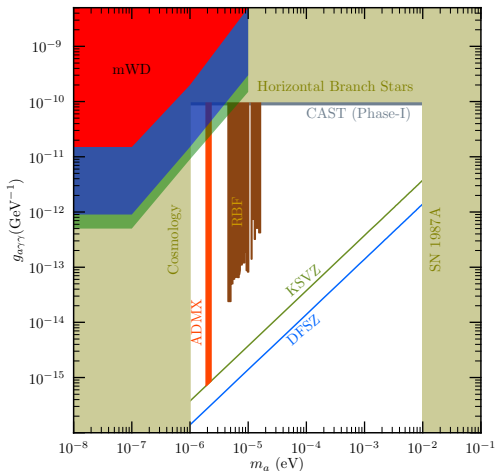
Euchner et al 06

# Axions and White Dwarfs

Let's look at more strongly magnetized white dwarfs:  
PG 1031+234 and  
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The observed minimum polarization of a few percent excludes some of the currently allowed region for axion-like particles.

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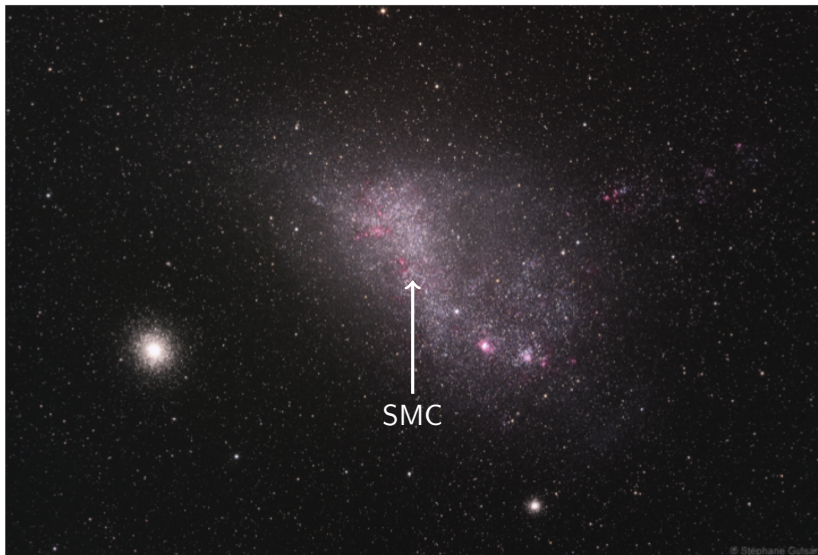


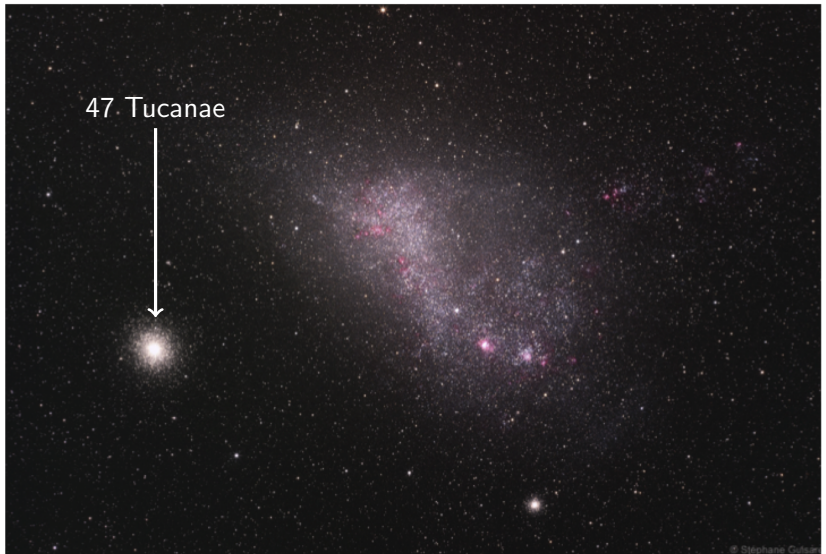
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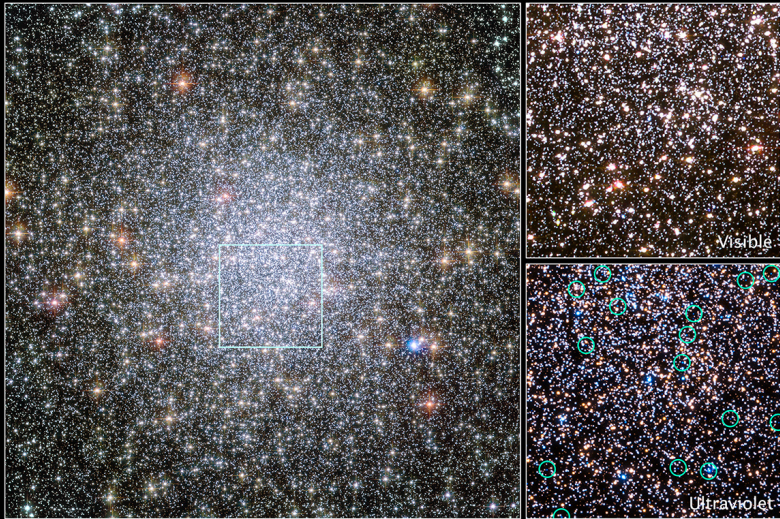


© Stéphane Gilman



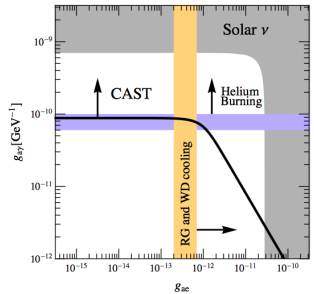
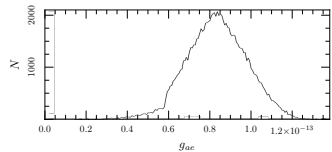
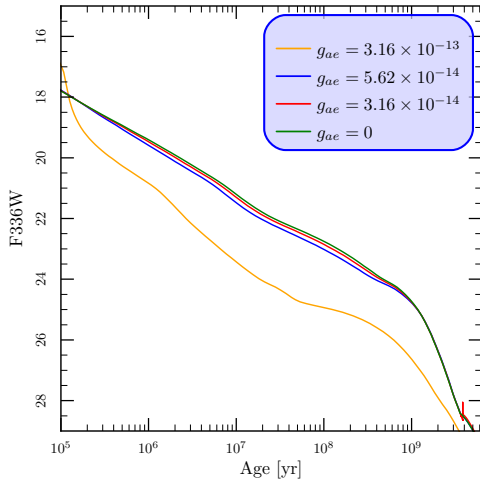




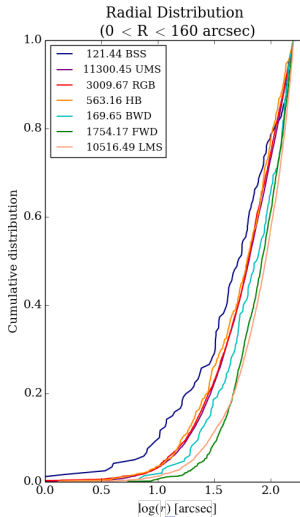
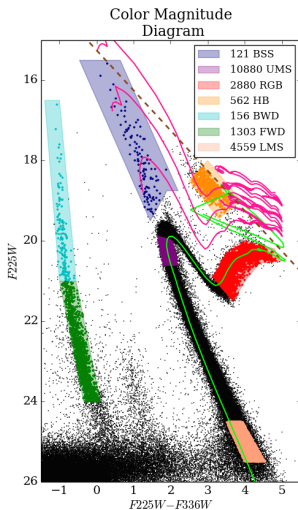


**Globular Cluster 47 Tucanae**  
*Hubble Space Telescope* ■ ACS/WFC ■ WFC3/UVIS

# Cooling White Dwarfs

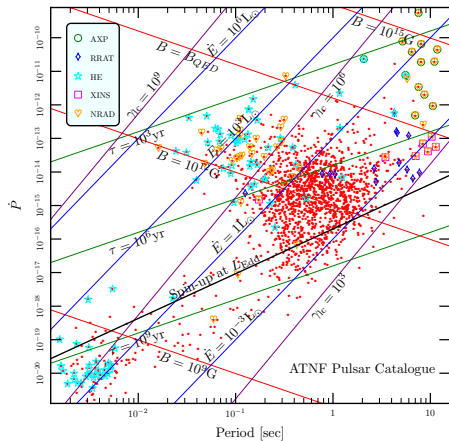


# Relaxation



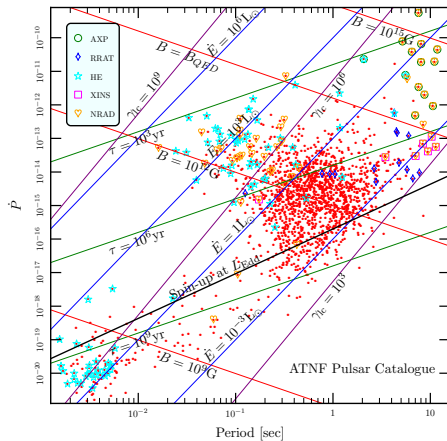
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- ▶ The first neutron stars to be identified were radio pulsars.



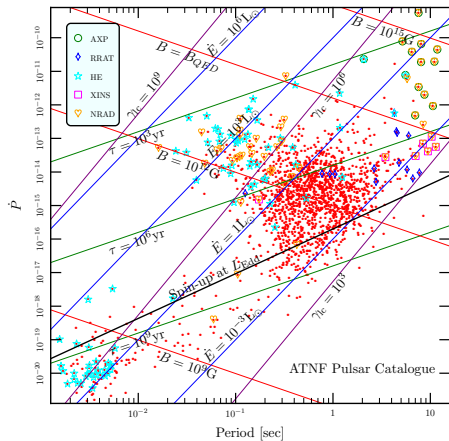
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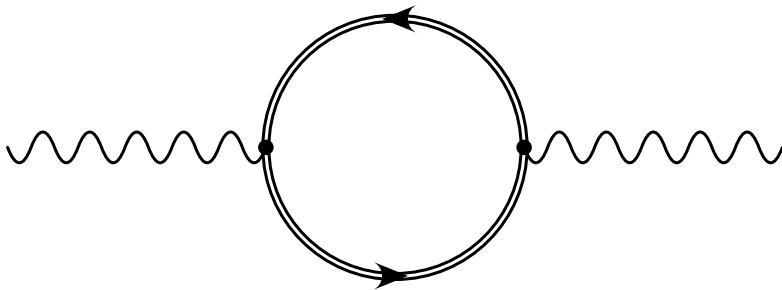
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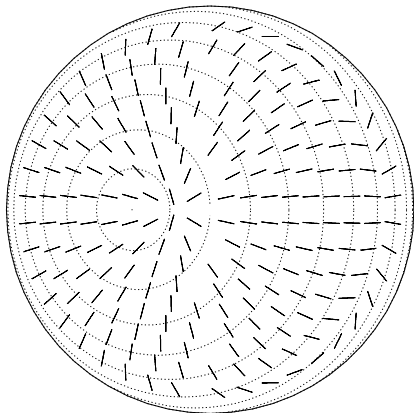


# Magnetic Fields



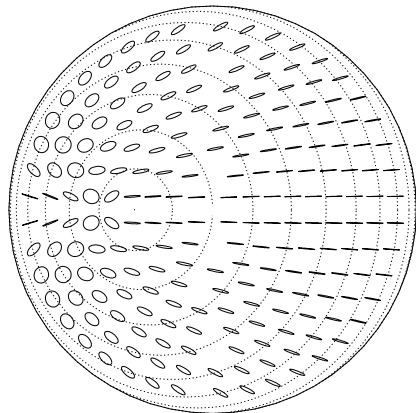
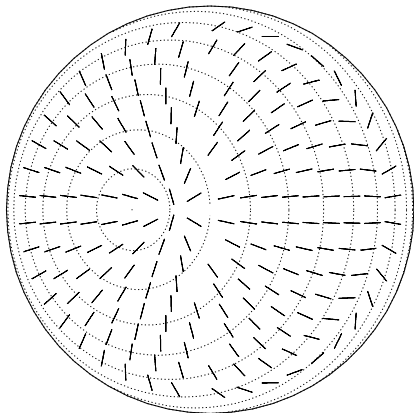
$$S = S_0 + \frac{1}{2} f^{\mu\nu} f^{\alpha\beta} \frac{\delta^2 S}{\delta f^{\mu\nu} \delta f^{\alpha\beta}}$$

# Why does this matter?



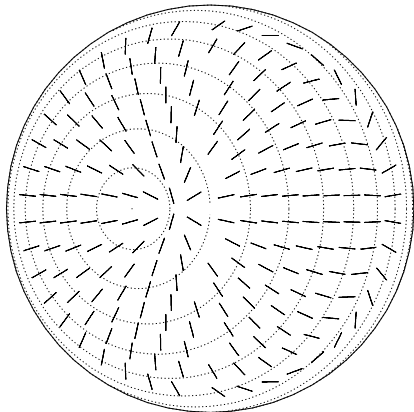
Heyl, Shaviv 02

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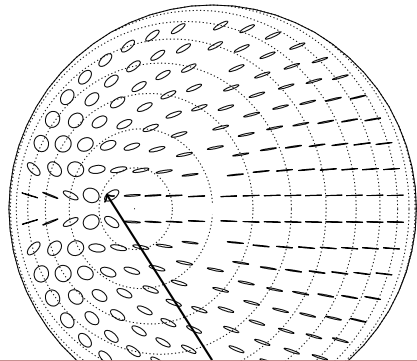


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Heyl, Shaviv 02



*Quasi-Tangential Region* Wang, Lai 09

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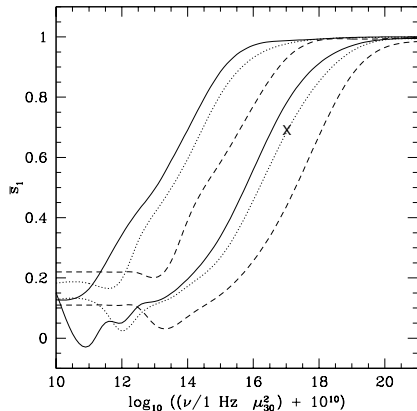
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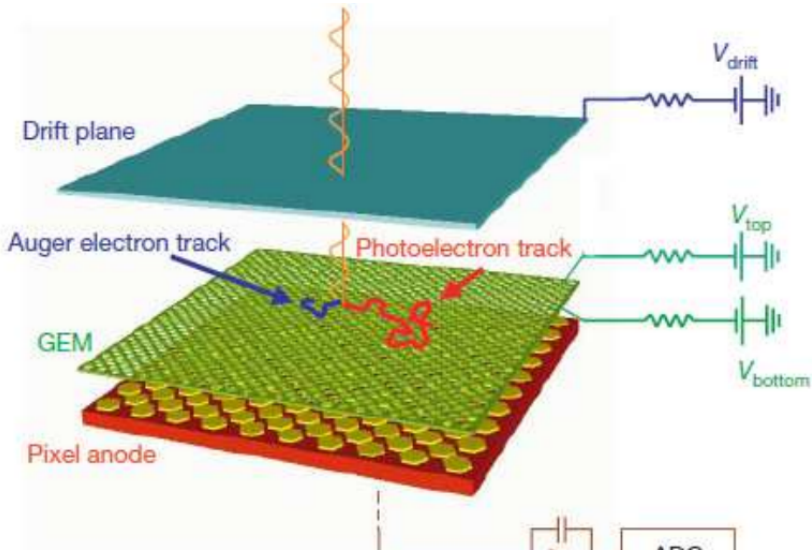
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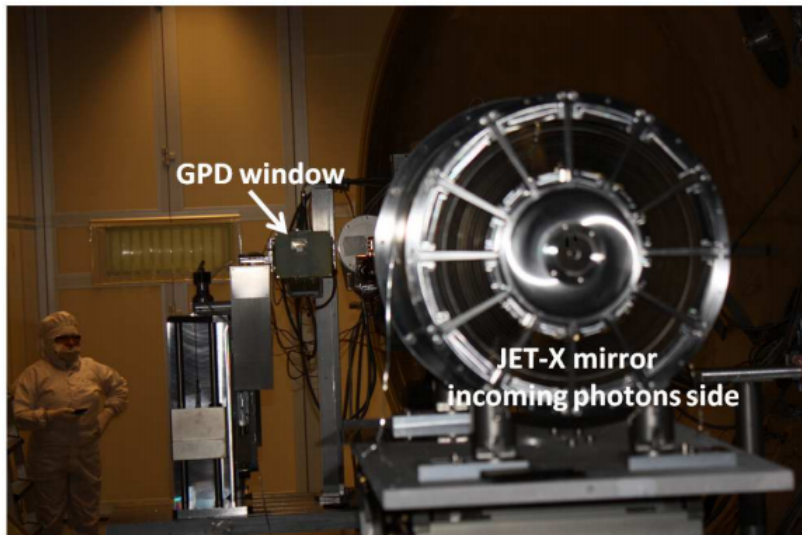




# XIPE



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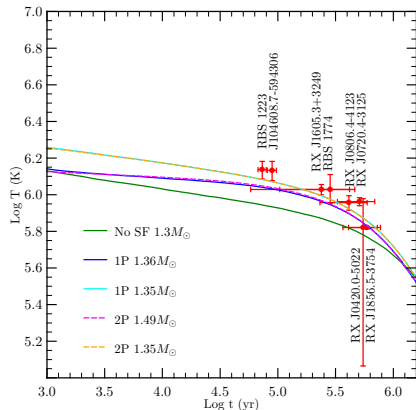
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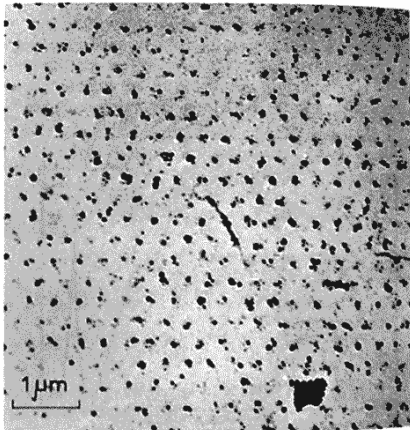
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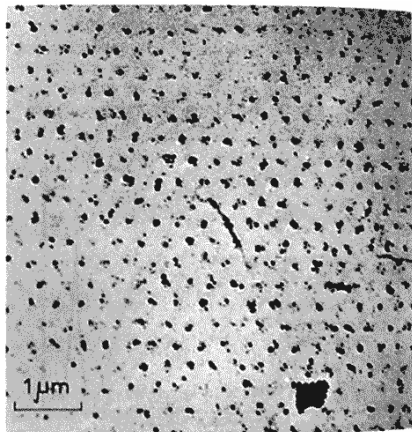
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Essmann & Träuble 1967

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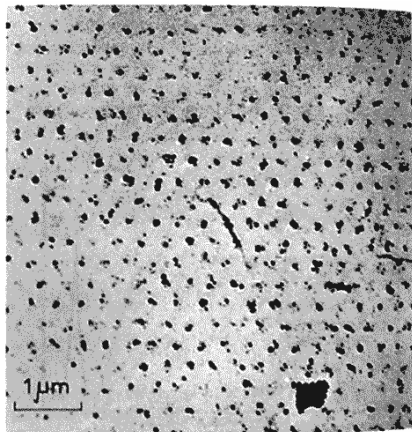
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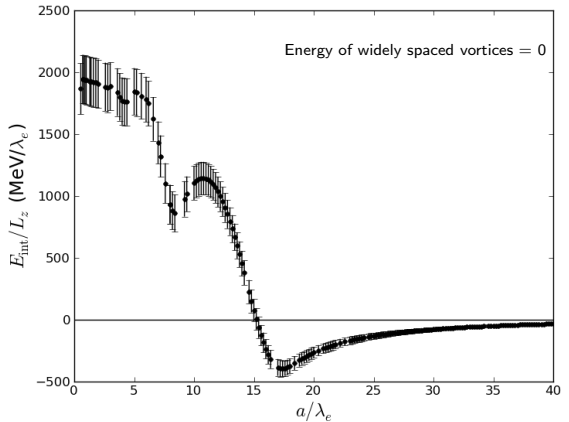
$$a \sim \sqrt{\frac{4h}{\pi e B}} = 7B_{12}\text{pm} = 19\lambda_e$$

and

$$\lambda_L = \sqrt{\frac{mc^2}{8\pi q^2 n_0}} = 7\rho_{15}\text{fm}$$

# Casimir Force

Discovery of an attractive Casimir interaction



# Circle Packing



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- ▶ For stronger fields, the tubes will be evenly and closely packed (like the conventional model).
- ▶ These bounds are qualitative as we need to model the superconductor more accurately.