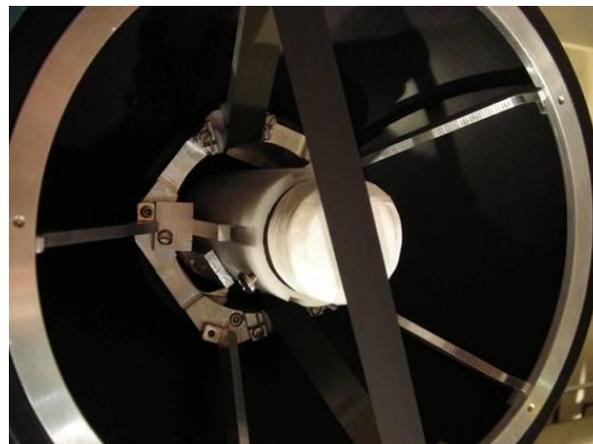
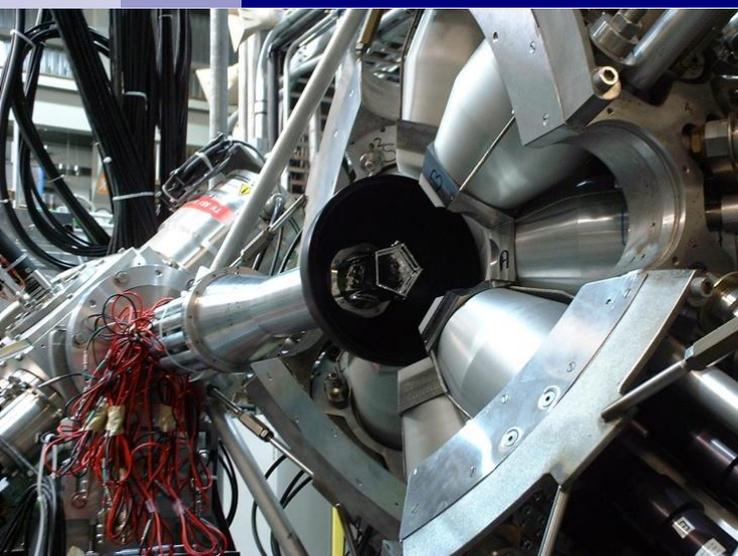


# Superaligned Fermi Beta Decay Studies at TRIUMF-ISAC

C.E. Svensson, University of Guelph

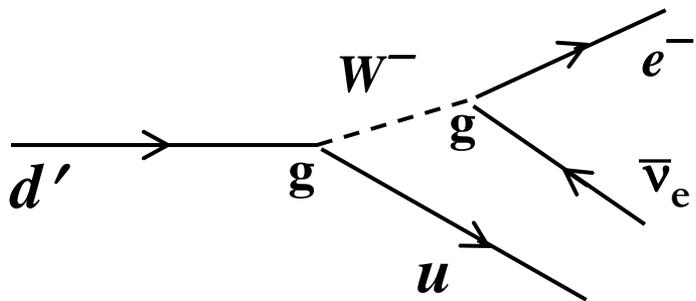


*CAP Congress,  
Sudbury, Ontario  
June 16 – 20, 2014*

# The Cabibbo-Kobayashi-Maskawa (CKM) matrix

The CKM matrix plays a central role in the Standard Model

→ and underpins all quark flavour-changing interactions:  
weak interaction eigenstates  $\neq$  quark mass eigenstates



$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

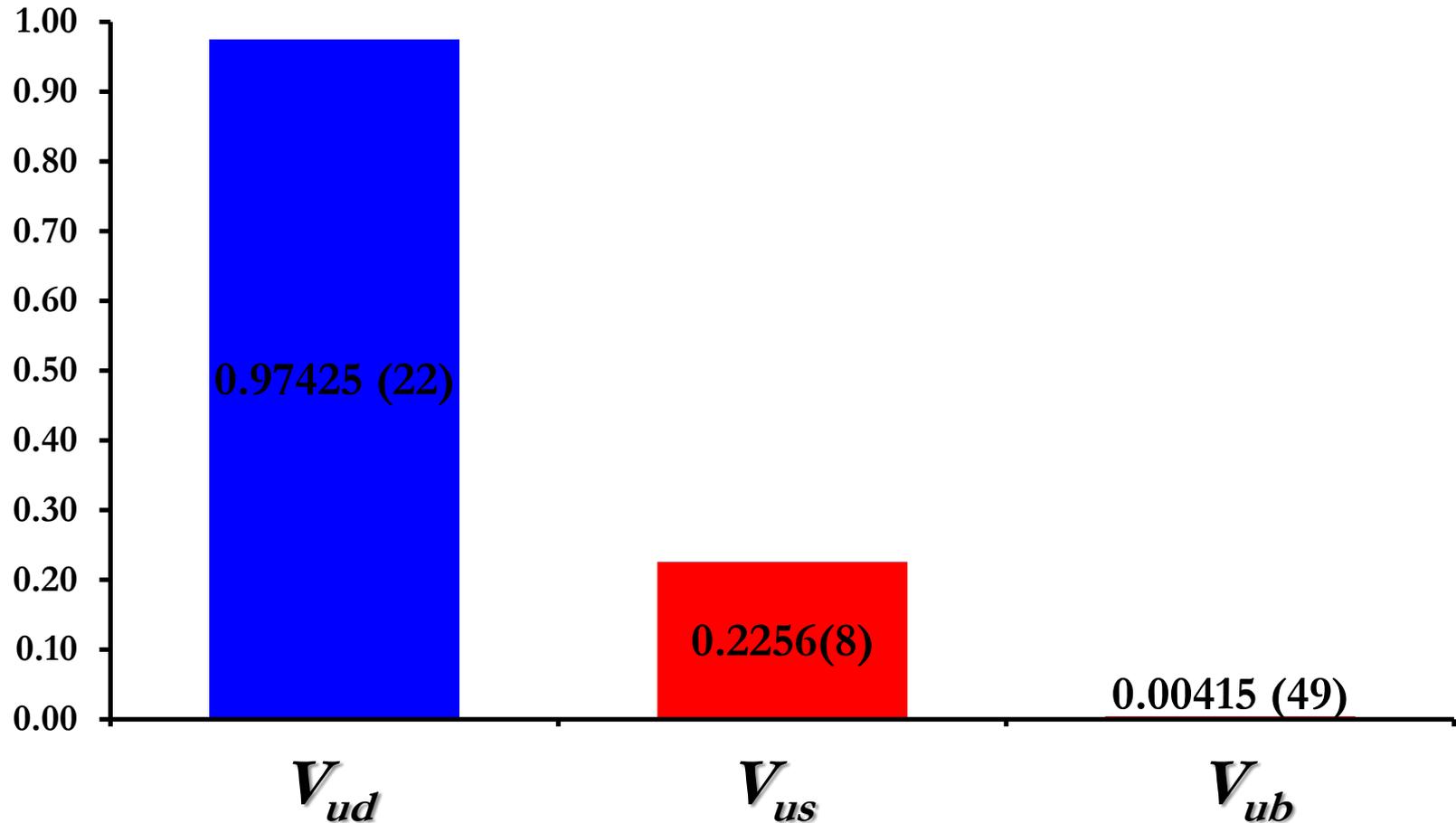
$$|d'\rangle = V_{ud}|d\rangle + V_{us}|s\rangle + V_{ub}|b\rangle$$

In the Standard Model the CKM describes a unitary transformation.

$$V_{ud}^2 + V_{us}^2 + V_{ub}^2 = 1$$

The first row of the CKM matrix provides, by far, the most demanding experimental test of this unitarity condition.

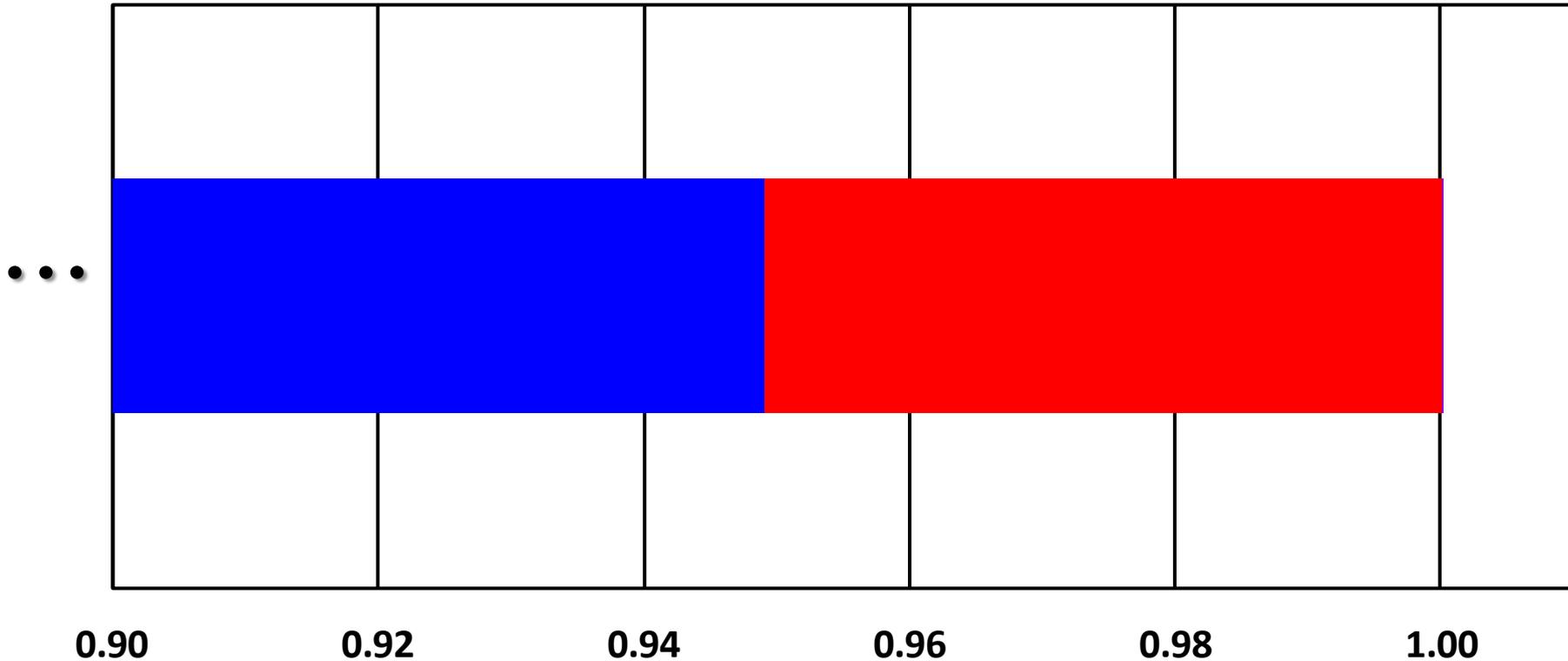
# CKM Unitarity



J.C. Hardy and I.S. Towner, Ann. Phys. (Berlin) 525, 443 (2013).

# CKM Unitarity

■  $V_{ud}$  ■  $V_{us}$  ■  $V_{ub}$



$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1.00008(43)_{V_{ud}}(36)_{V_{us}}$$

J.C. Hardy and I.S. Towner, Ann. Phys. (Berlin) 525, 443 (2013).

# New Lattice QCD Form Factor Calculations for $V_{us}$

R.J. Dowdall et al., Phys. Rev. D 88, 074504 (2013)

$K^+ \rightarrow l\nu / \pi^+ \rightarrow l\nu$  (HPQCD Collaboration)

$$|V_{us}| = 0.22564(53)$$

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1.00009(43)_{Vud}(24)_{Vus}$$

A. Bazavov et al., Phys. Rev. Lett. 112, 112001 (2014)

$K^+ \rightarrow \pi^+ l\nu$  (Fermilab Lattice and MILC Collaborations)

$$|V_{us}| = 0.22290(90)$$

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.99885(43)_{Vud}(40)_{Vus}$$

# $V_{ud}$ from Superallowed Fermi $\beta$ Decay

To first order,  $\beta$  decay ft values can be expressed as:

$$ft = \frac{K}{|M_{fi}|^2 g^2}$$

phase space (Q-value)  $\rightarrow$   $f$   
 half-life, branching ratio  $\rightarrow$   $t$   
 constants  $\rightarrow$   $K$   
 matrix element  $\rightarrow$   $|M_{fi}|^2$   
 Weak coupling strength  $\rightarrow$   $g^2$

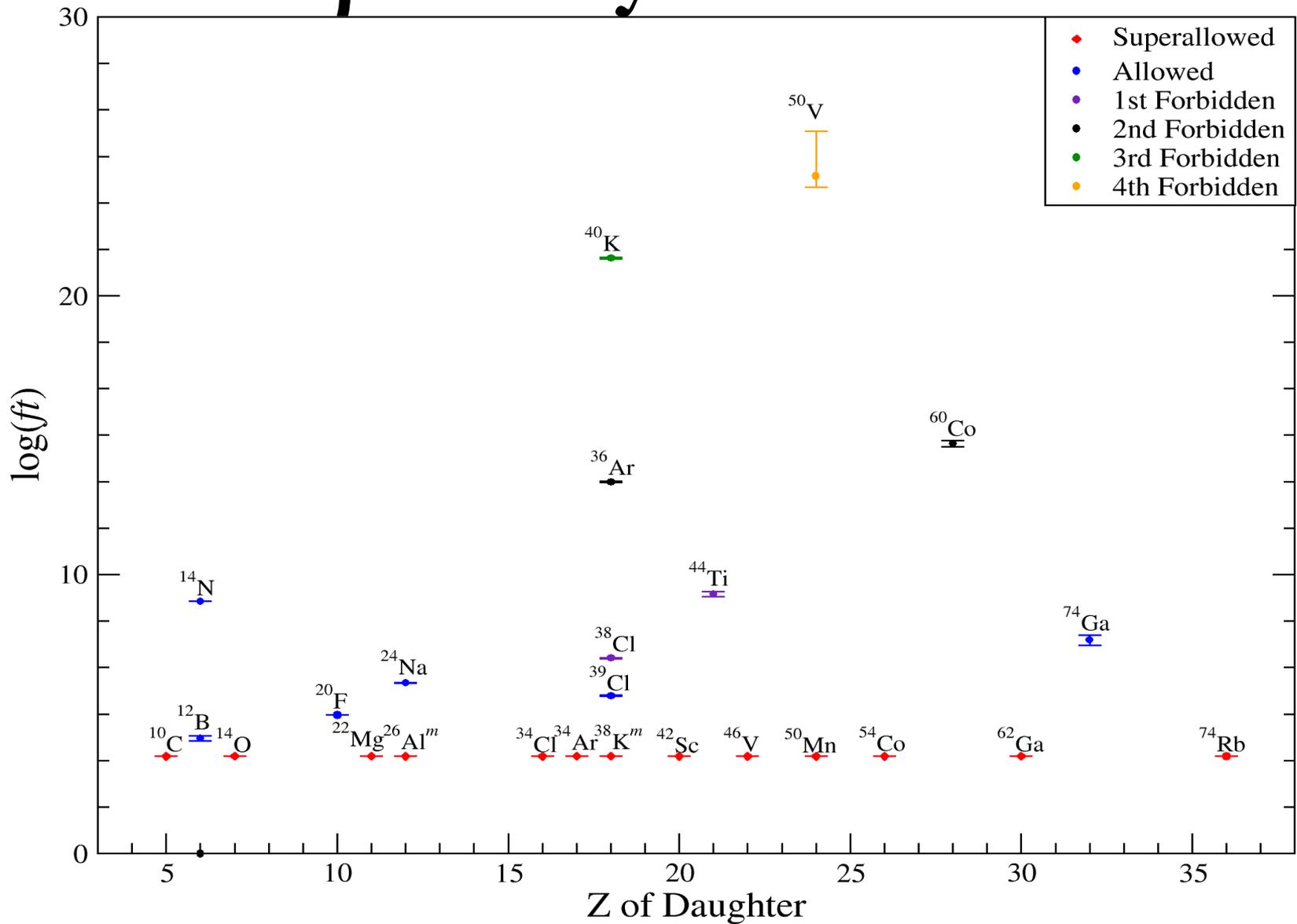
For the special case of  $0^+ \rightarrow 0^+$  (pure Fermi)  $\beta$  decays between isobaric analogue states (superallowed) the matrix element is that of an isospin ladder operator:

$$|M_{fi}|^2 = (T - T_Z)(T + T_Z + 1) = 2 \quad (\text{for } T=1)$$

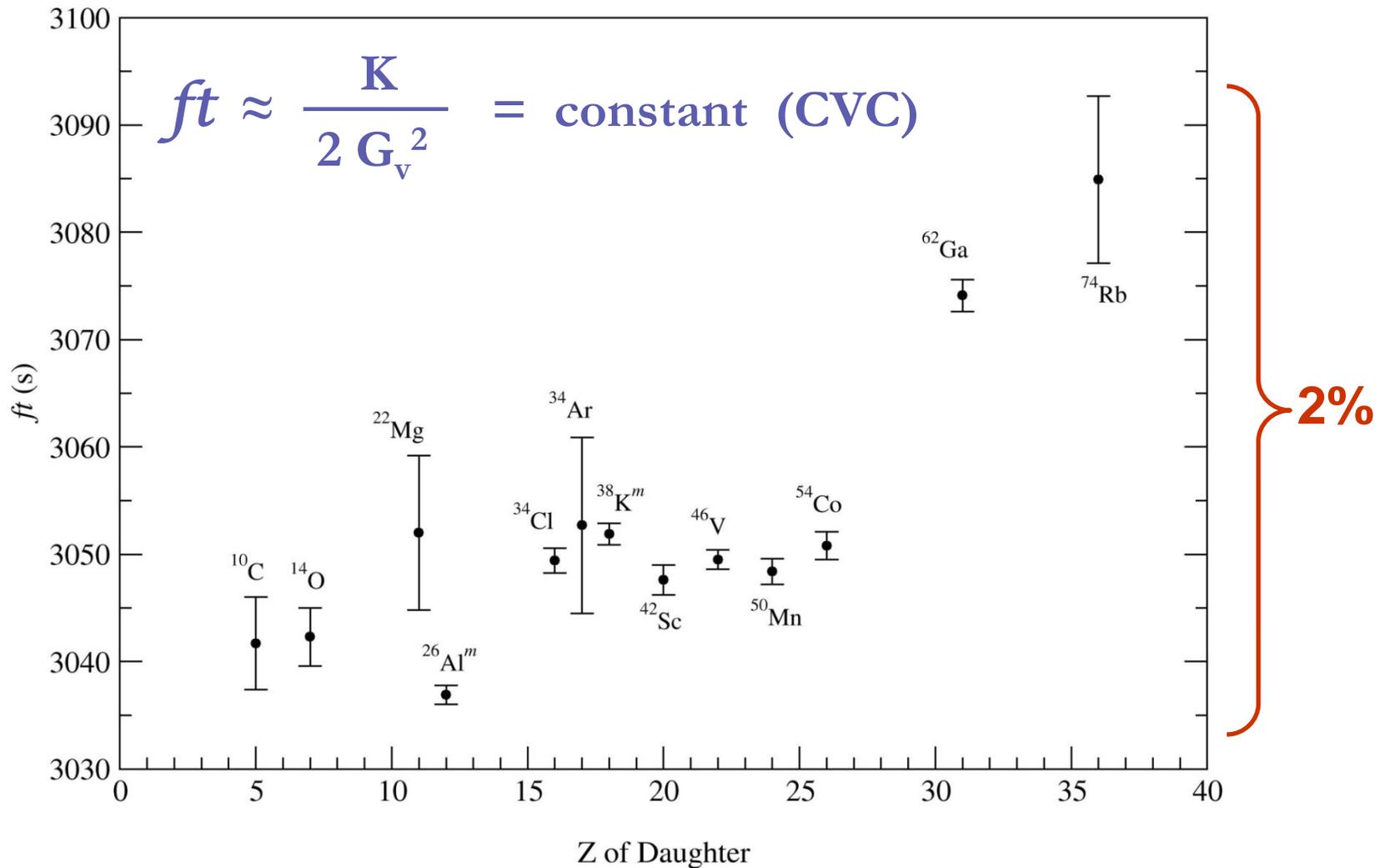
Strategy: Measure superallowed ft-values, deduce  $G_V$  and  $V_{ud}$ :

$$\begin{array}{l}
 \text{Vector coupling} \\
 \text{constant}
 \end{array}
 \rightarrow G_V^2 = \frac{K}{2 ft}
 \qquad
 |V_{ud}| = G_V / G_F \leftarrow \begin{array}{l}
 \text{Fermi coupling} \\
 \text{constant}
 \end{array}$$

# $\beta$ decay ft-values



# Superallowed $ft$ -values



# Superaligned Fermi $\beta$ Decay: Corrections

$$\mathcal{F}t = ft(1 + \delta'_R)(1 + \delta_{NS} - \delta_C) = \frac{K}{2G_V^2(1 + \Delta_R^V)} = \text{constant}$$

“Corrected” ft value  
 Experiment  
 Calculated corrections (~1%) (nucleus dependent)  
 Inner radiative correction (~2.4%) (nucleus independent)  
 CVC Hypothesis

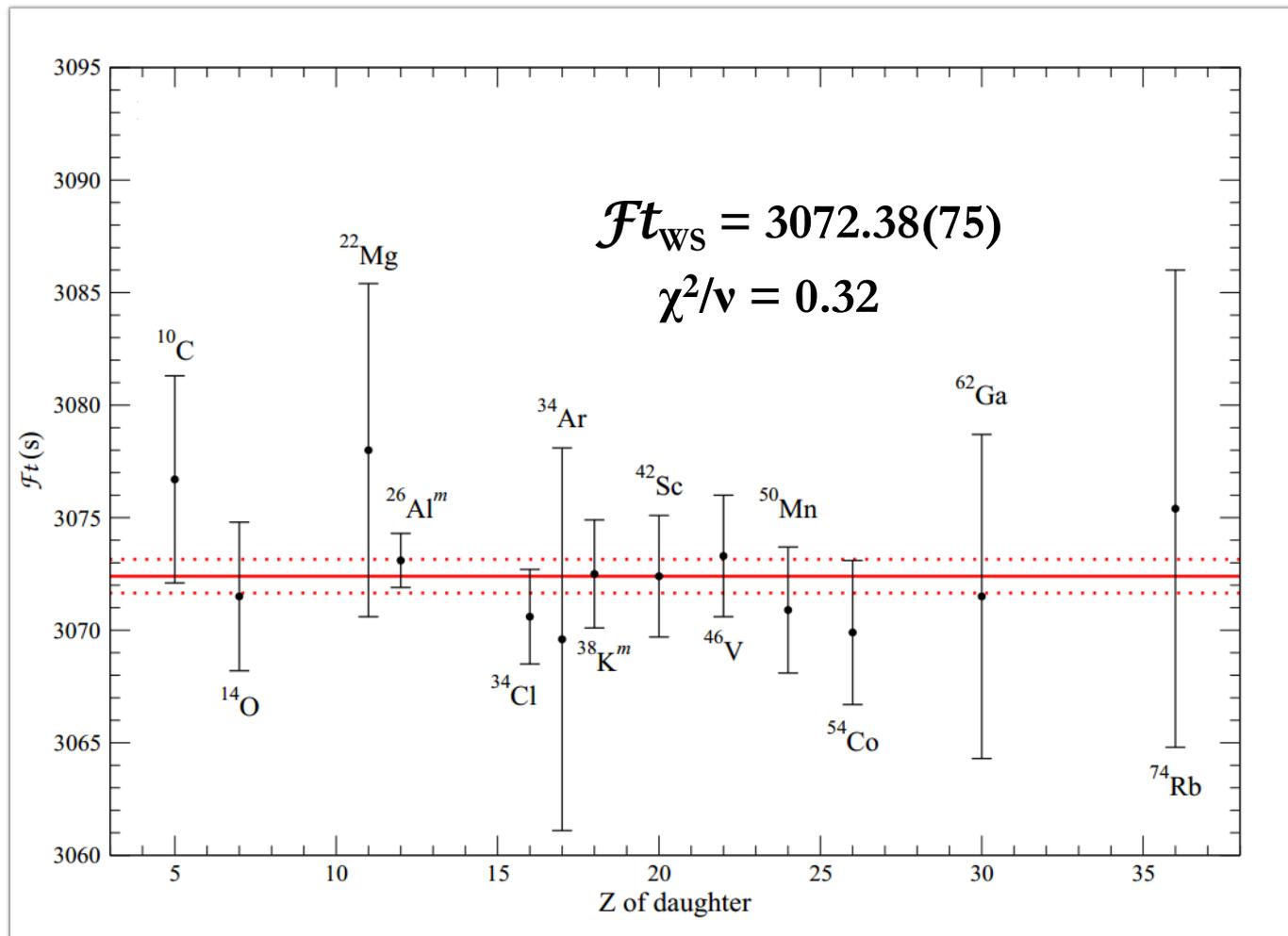
$\Delta_R^V$  = nucleus independent inner radiative correction: 2.361(38)%

$\delta'_R$  = nucleus dependent radiative correction to order  $Z^2\alpha^3$ : ~1.4%  
 - depends on electron's energy and  $Z$  of nucleus

$\delta_{NS}$  = nuclear structure dependent radiative correction: -0.3% – 0.03%

$\delta_C$  = nucleus dependent isospin-symmetry-breaking correction: 0.2% – 1.5%  
 - strong nuclear structure dependence

# Corrected Superallowed $\mathcal{F}t$ Values



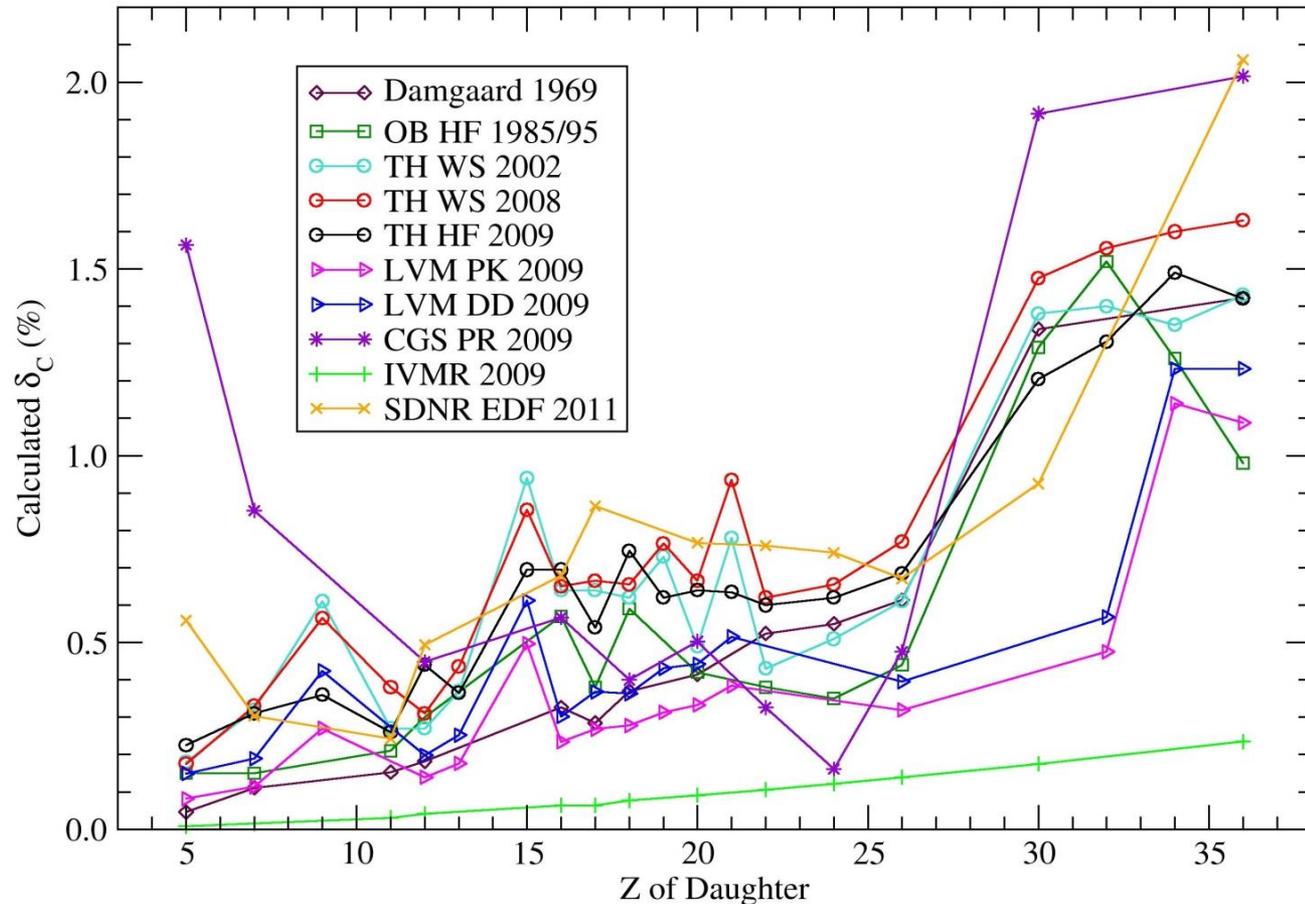
**P. Finlay, *et al.*, Phys. Rev. Lett. 106, 032501 (2011)**

**R. Dunlop, *et al.*, Phys. Rev. C 88, 045501 (2013)**

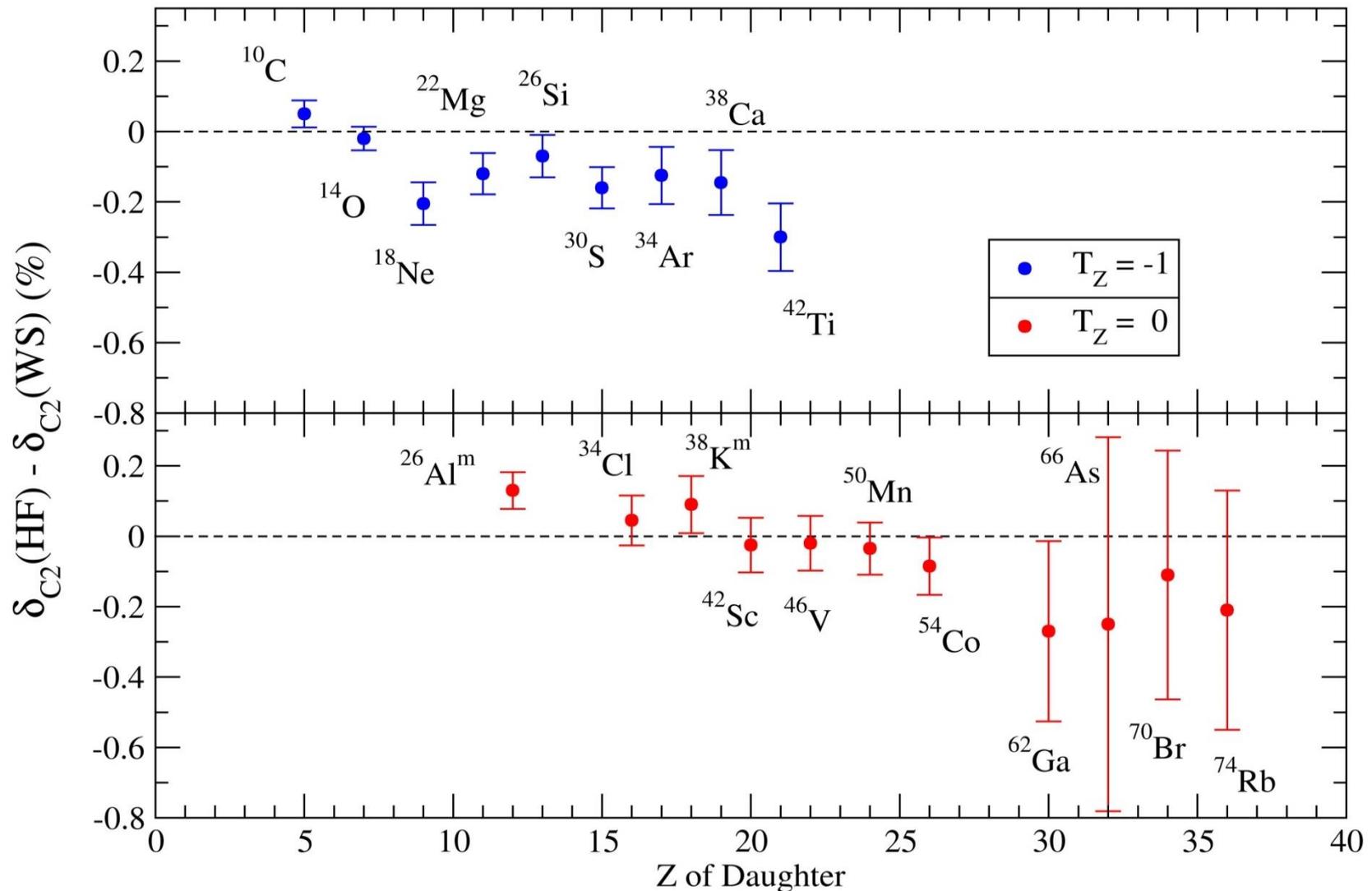
# Theoretical Treatment of $\delta_C$

Many recent approaches to ISB corrections

- Nuclear Shell Model
- Relativistic Hartree-Fock
- Random Phase Approximation
- Energy Density Functional

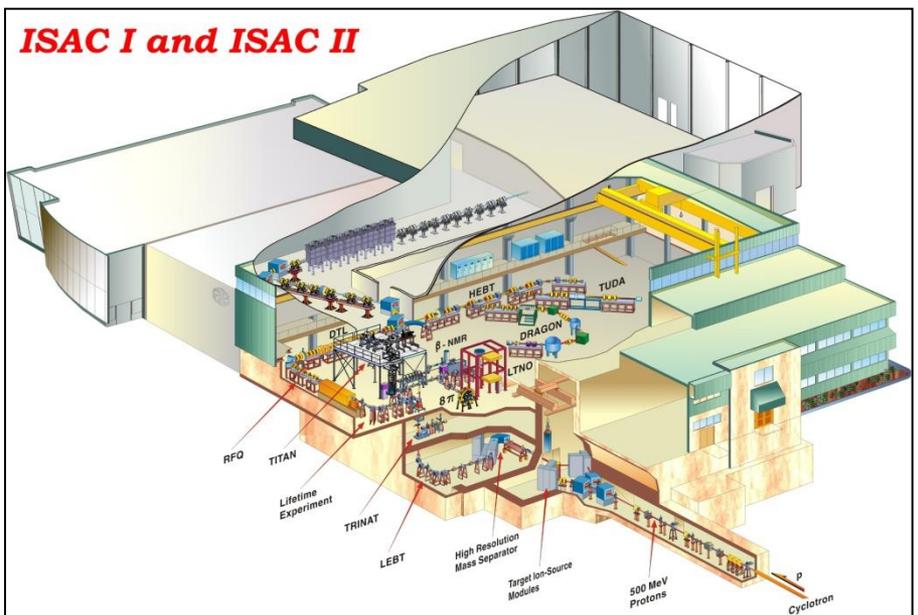
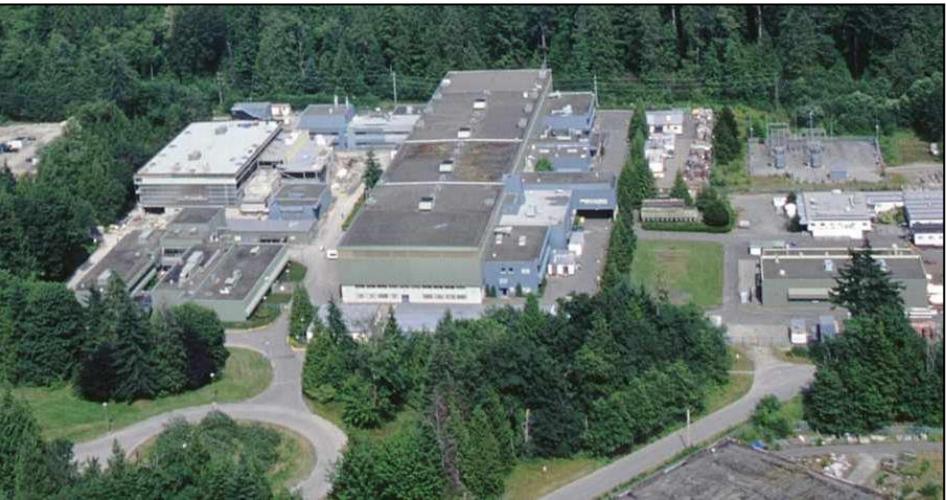


# Difference between Woods-Saxon and Hartree-Fock Radial Overlap Corrections



# TRIUMF-ISAC

Up to 100  $\mu\text{A}$ , 500 MeV proton beams from the TRIUMF main cyclotron produce high-intensity secondary beams of many of the superallowed emitters by the ISOL technique.

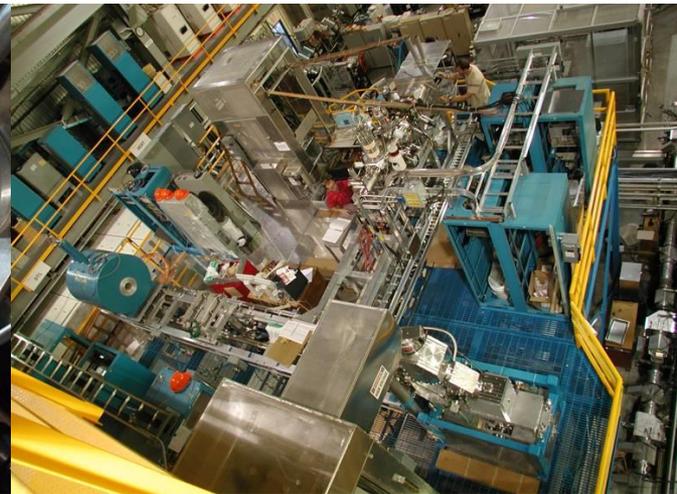
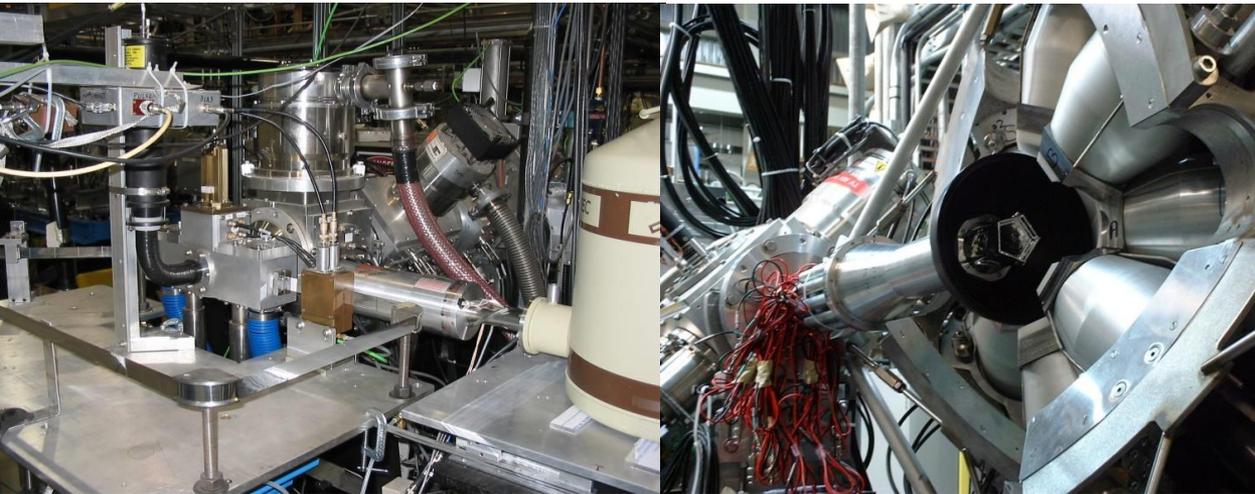


# Superaligned Fermi $\beta$ Decay Studies at ISAC

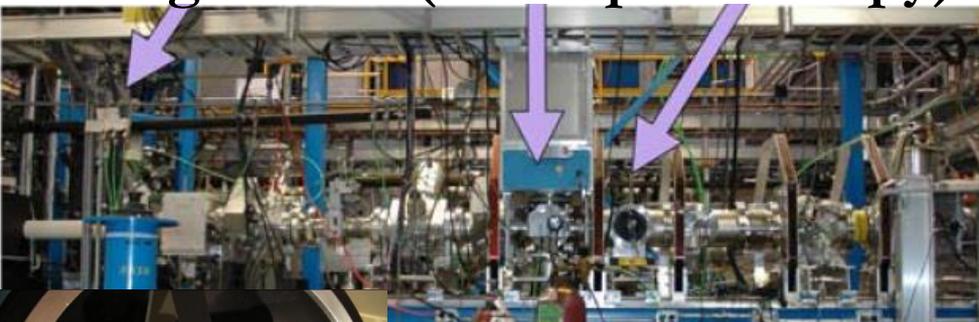
Halflives (GPS)

Branching ratios ( $8\pi$ )

Masses (TITAN)

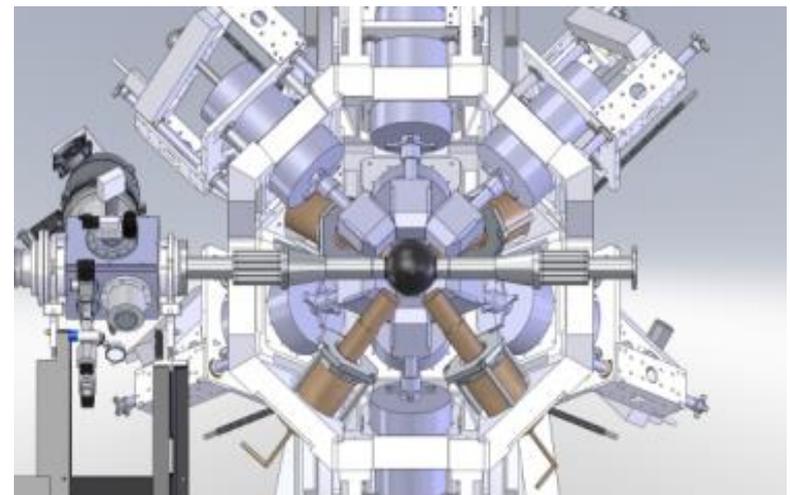


Charge Radii (laser spectroscopy)



Halflives (ZDS)

Near Future (GRIFFIN)



$T_{1/2}$ , G.C. Ball *et al*, PRL 86 1454 (2001)

BR, A. Piechaczek *et al*, PRC 67, 051305 (2003)

BR, R. Dunlop *et al*, PRC 88, 045501 (2013)

Q: S. Ettenauer *et al.*, PRL 107, 272501 (2011)

CR: E. Mané *et al*, PRL 107, 212502 (2011)

$^{74}\text{Rb}$

# Superaligned $\beta$ Decay Studies at ISAC

$T_{1/2}$ , G.F. Grinyer, PRC 77, 201501 (2008)

BR, B.H. Hyland, PRL 97, 102501 (2006)

BR, P. Finlay PRC 78, 044321 (2008)

$^{62}\text{Ga}$

$^{66}\text{As}$

$^{70}\text{Br}$

$T_{1/2}$  and BR

$^{54}\text{Co}$

$^{50}\text{Mn}$

$^{46}\text{V}$

$^{38m}\text{K}$

$T_{1/2}$  and BR

$^{34}\text{Ar}$

$N=Z$  line

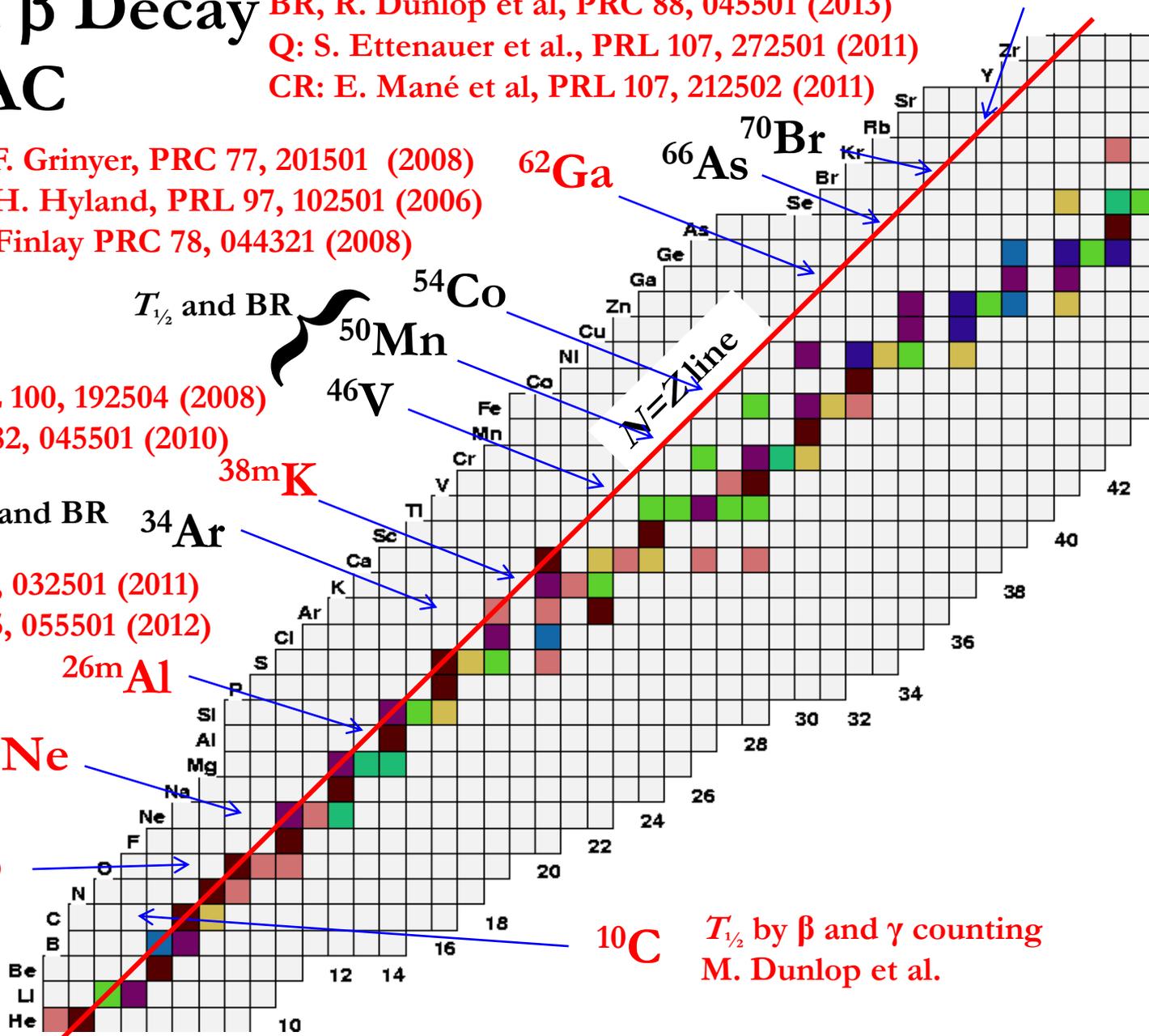
$^{26m}\text{Al}$

$^{18}\text{Ne}$

$^{14}\text{O}$

$^{10}\text{C}$

$T_{1/2}$  by  $\beta$  and  $\gamma$  counting  
M. Dunlop *et al.*



BR, K.G. Leach *et al.*, PRL 100, 192504 (2008)

$T_{1/2}$ , G.C. Ball *et al*, PRC 82, 045501 (2010)

$T_{1/2}$  P. Finlay *et al*, PRL 106, 032501 (2011)

BR, P. Finlay *et al*, PRC 85, 055501 (2012)

$T_{1/2}$ , G.F. Grinyer *et al*,

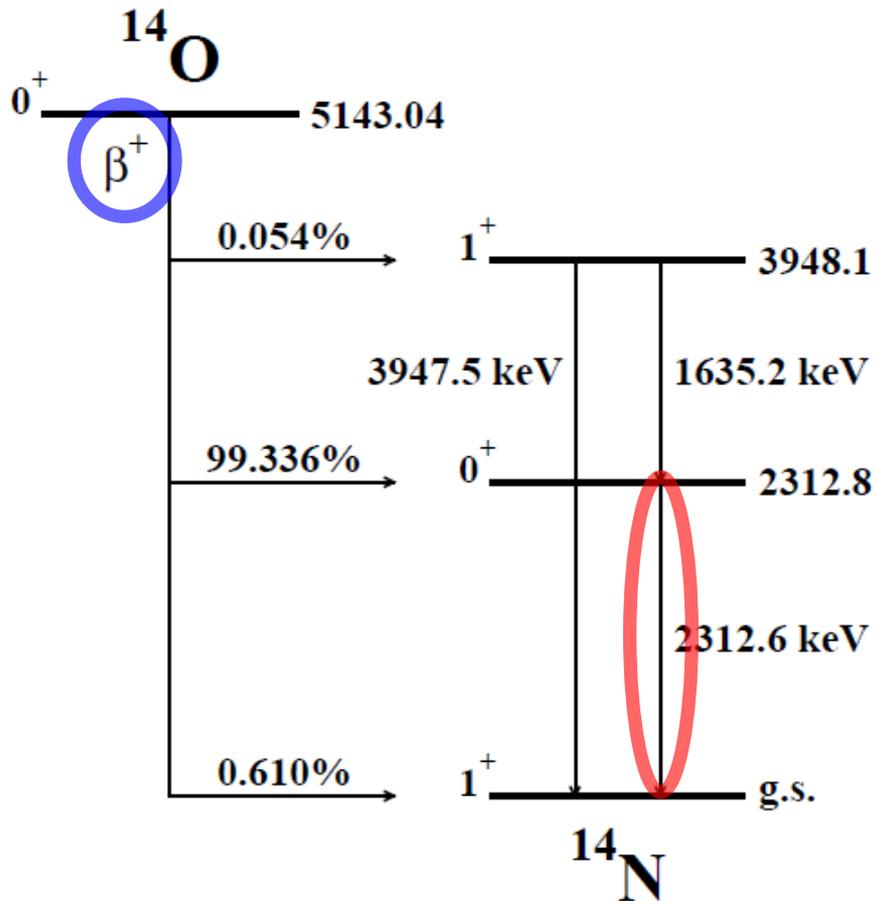
PRC 76, 025503 (2007)

PRC 87, 045502 (2013)

$T_{1/2}$ , A.T. Laffoley *et al*,

PRC 88, 015501 (2013)

# $^{14}\text{O}$ Half-Life Measurement



Simultaneous independent direct  $\beta$  and  $\gamma$ -ray counting experiments using the  $8\pi$  spectrometer and the Zero-Degree Scintillator.

## $\gamma$ Counting:

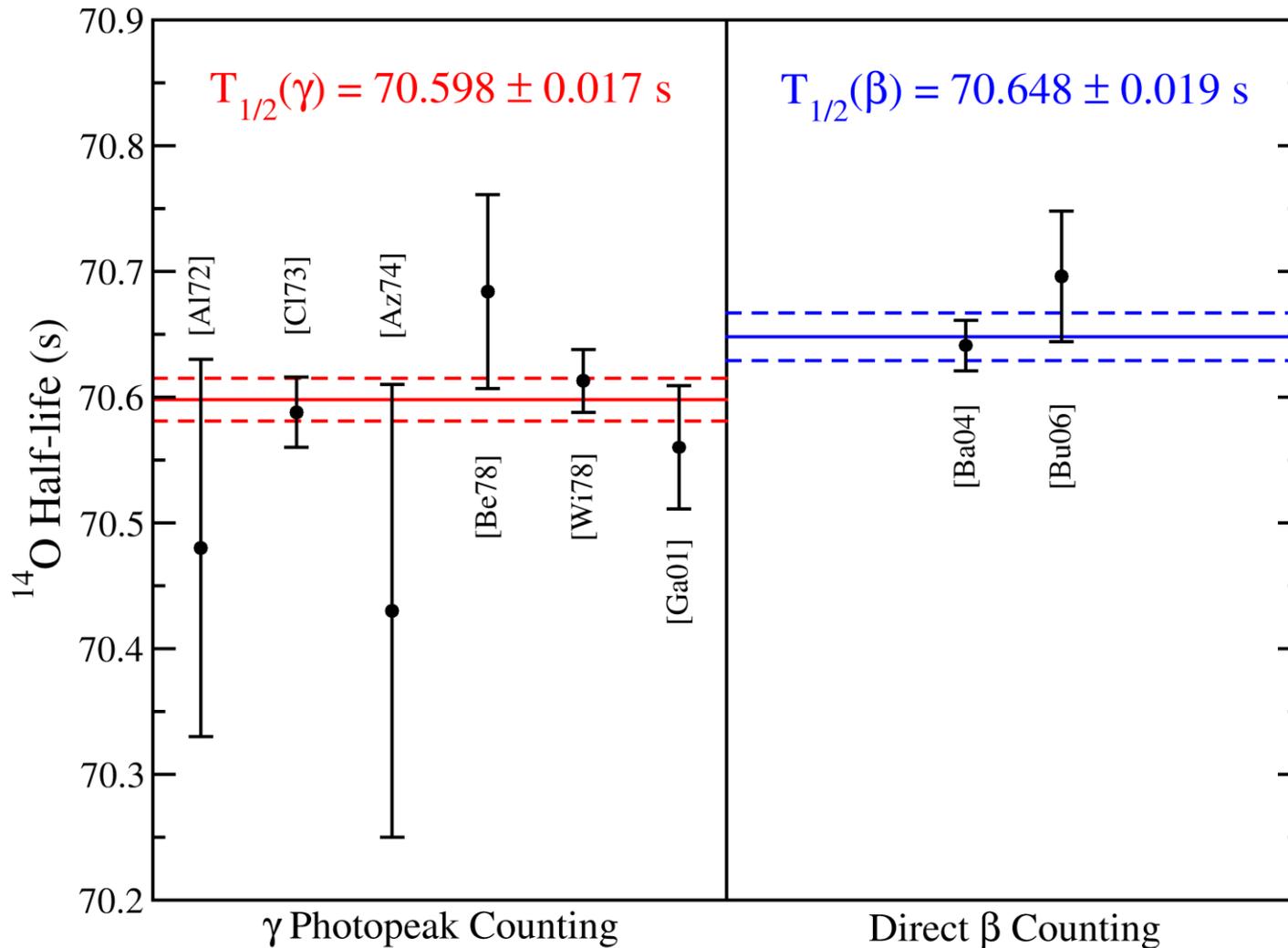
- Decay Selective
- Slow & Inefficient

## $\beta$ Counting:

- Fast & Efficient
- Not Decay Selective

Previous measurements reveal a systematic discrepancy between detection method

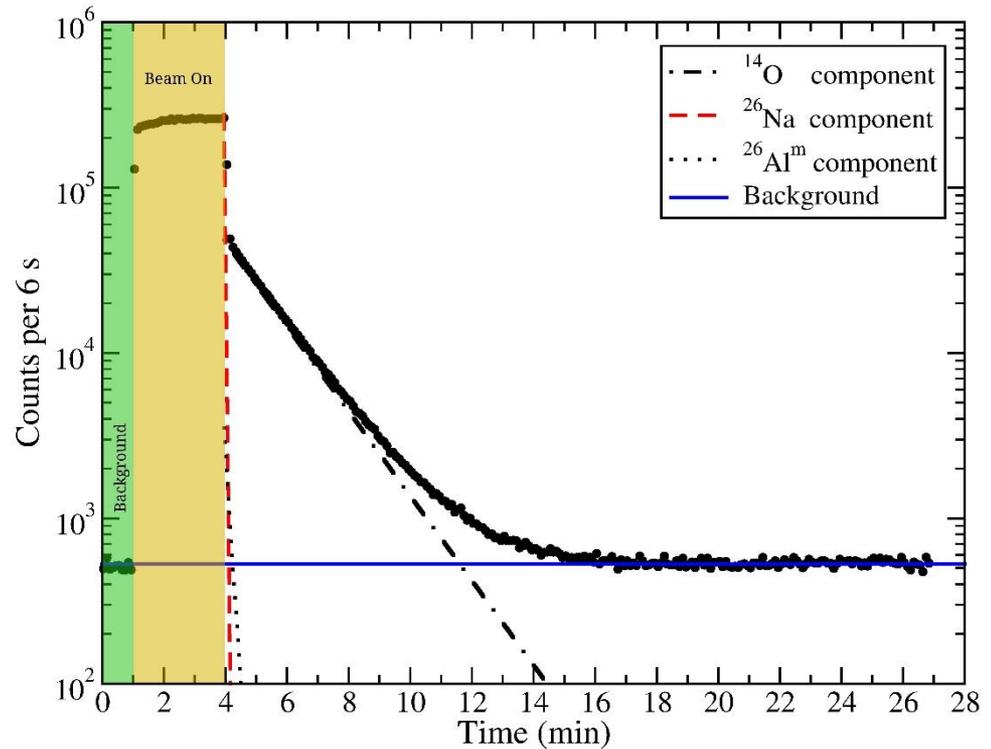
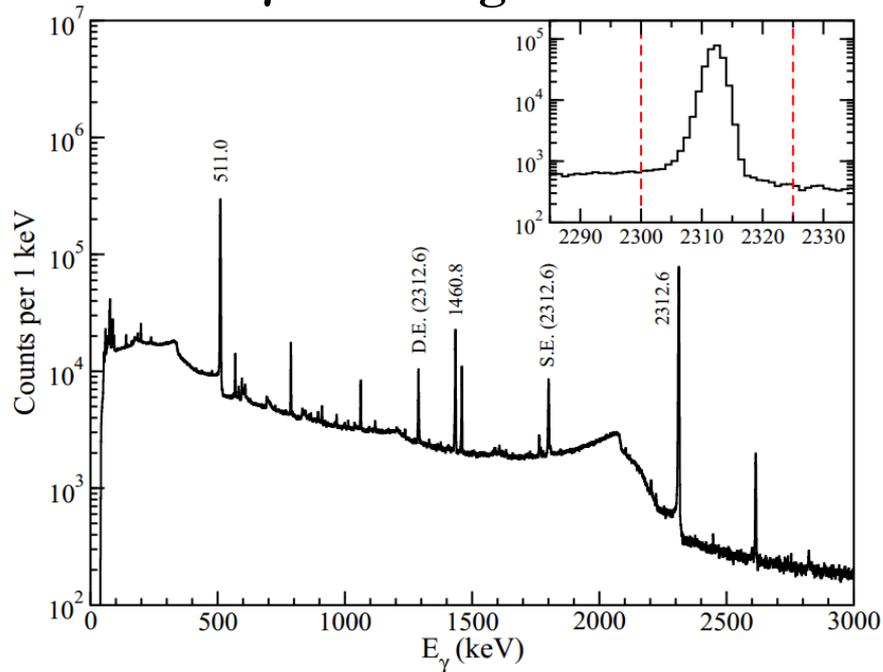
# $^{14}\text{O}$ Half-Life vs Detection Method



# $^{14}\text{O}$ Half-Life Measurement at ISAC

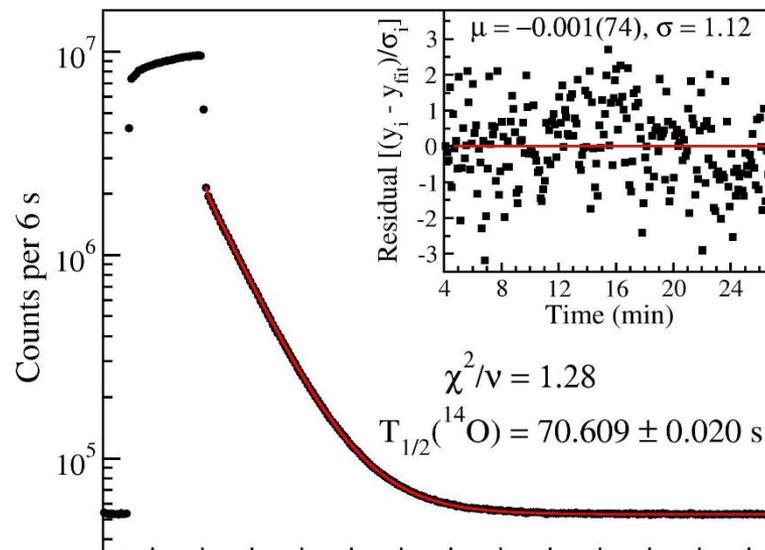
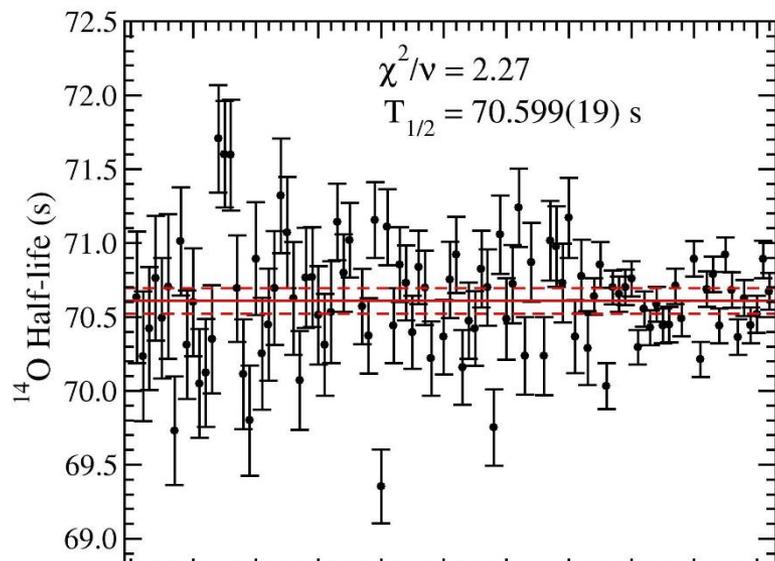
Beam {  $^{12}\text{C}-^{14}\text{O}$ :  $T_{1/2} = 70.620$  s  
 $^{26}\text{Al}^m$ :  $T_{1/2} = 6.3465$  s  
 $^{26}\text{Na}$ :  $T_{1/2} = 1.072$  s

## $\gamma$ Counting

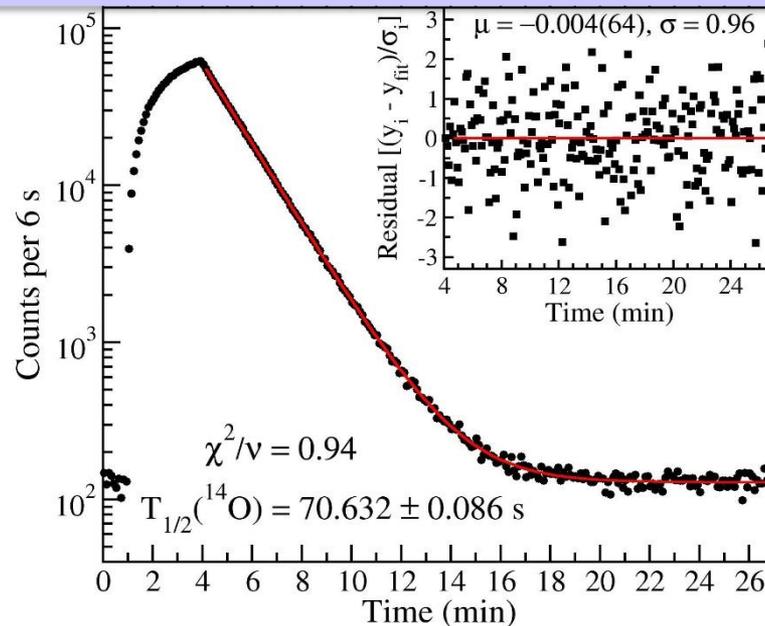
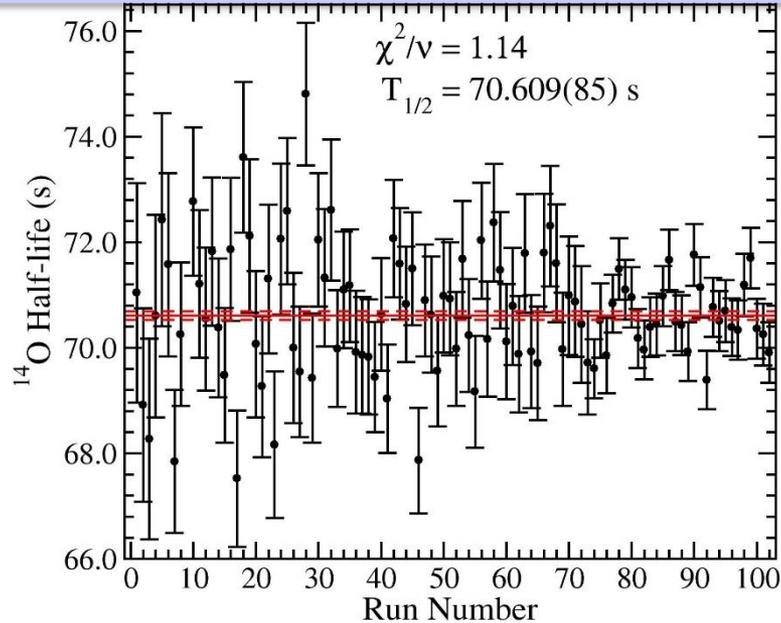


## $\beta$ Counting

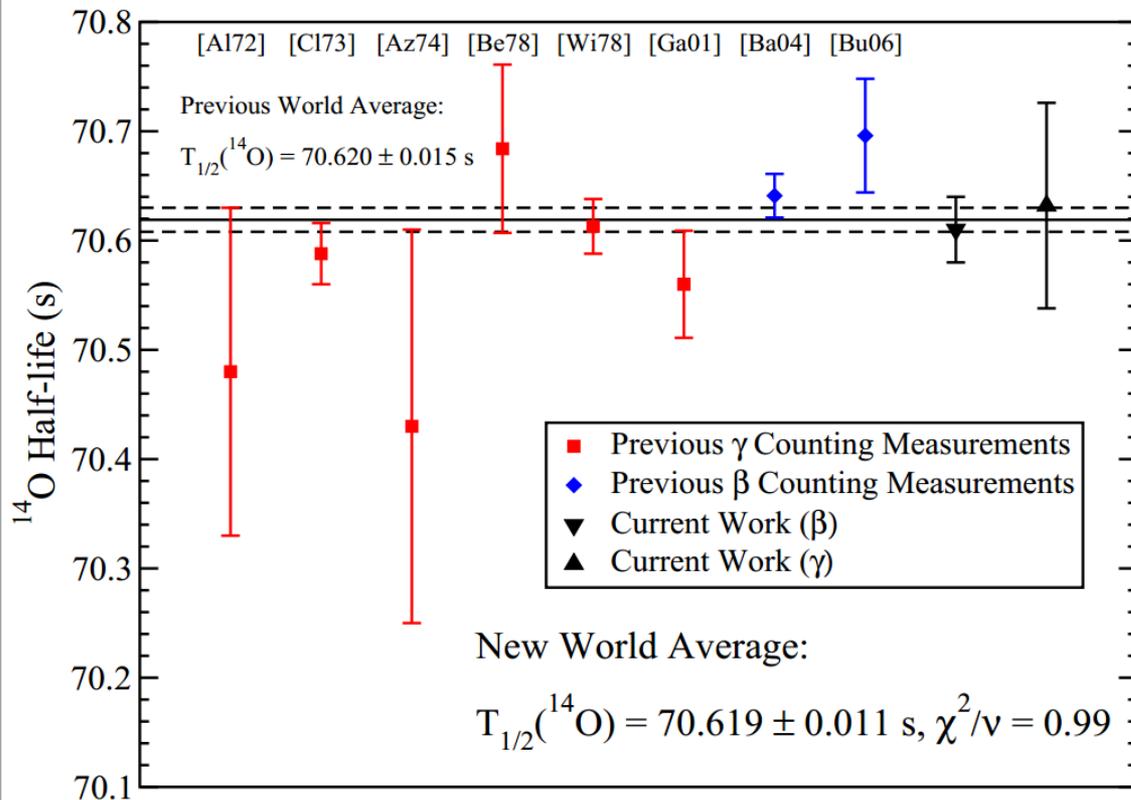
$\beta$



$\gamma$



# $^{14}\text{O}$ Half-Life



- ◆ Initial experiment shows consistency between  $\beta$  and  $\gamma$  half-life measurements for  $^{14}\text{O}$ .
- ◆ A follow-up experiment is scheduled for July, 2014 to push to 0.01% precision.
- ◆ *ft* measurements for light superallowed Fermi  $\beta$  emitters are required to constrain scalar currents in the weak interaction.

A.T. Laffoley *et al.*, Phys. Rev. C **88**, 015501 (2013)

# $^{18}\text{Ne}$ Superallowed Decay

$T = 1$   $^{18}\text{Ne}$   
 $T_{1/2} = 1.6654(11)$  s  
 $Q = 4443.6$  keV

$0^+$

$\beta^+$

$1^+$  1701 0.19%

$\beta^+$

$0^-$  1081 0.0002%

$T = 1$

$0^+$  1042 7.70%

$\beta^+$

$T = 0$   $^{18}\text{F}$   $1^+$  0 92.11%

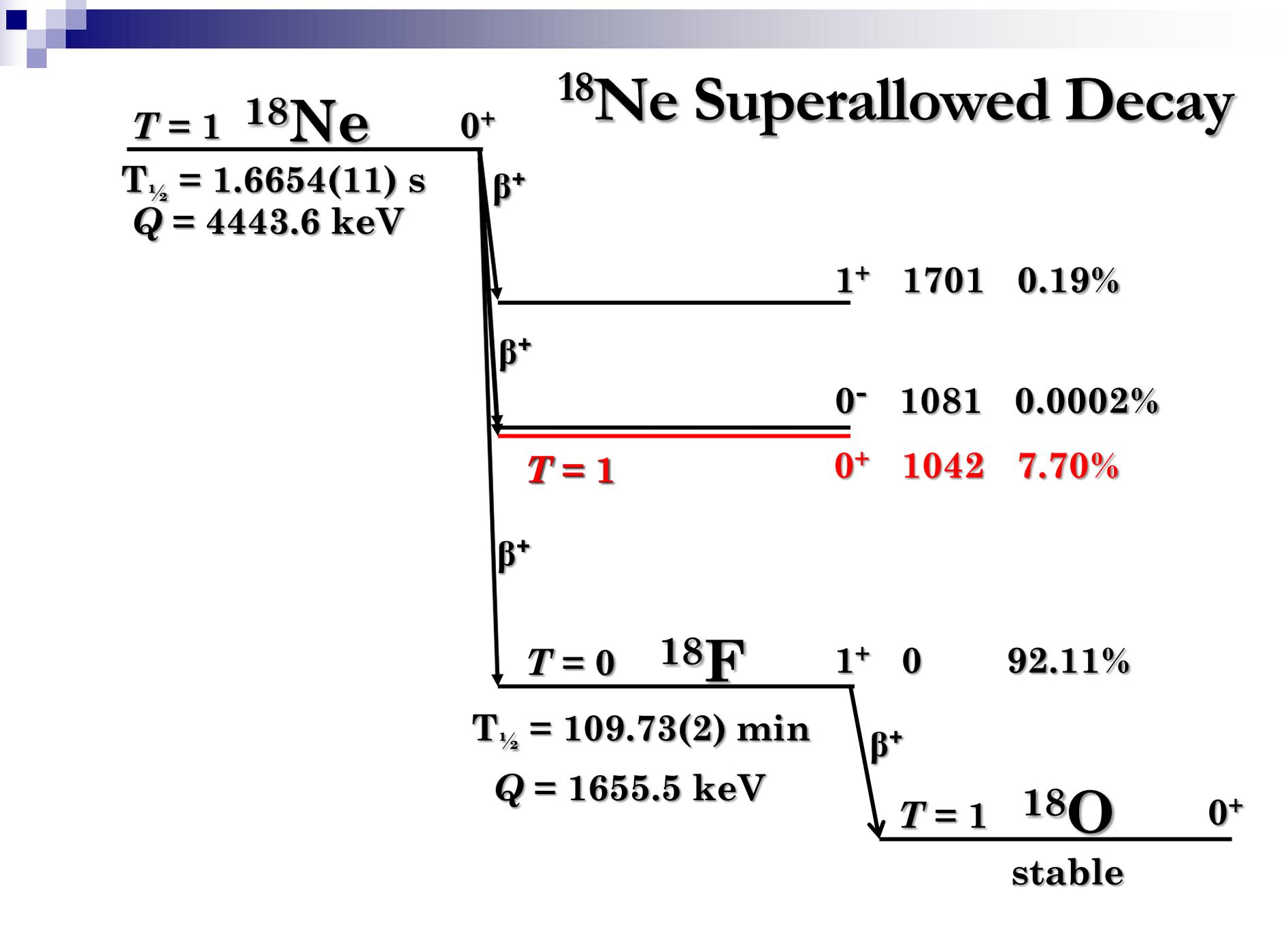
$T_{1/2} = 109.73(2)$  min

$Q = 1655.5$  keV

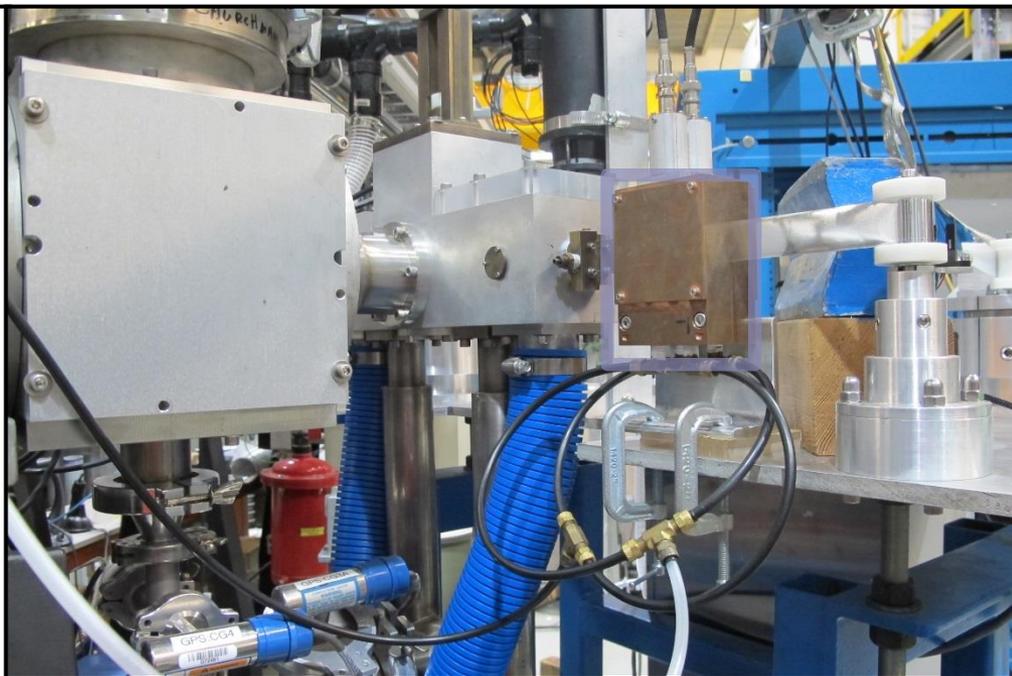
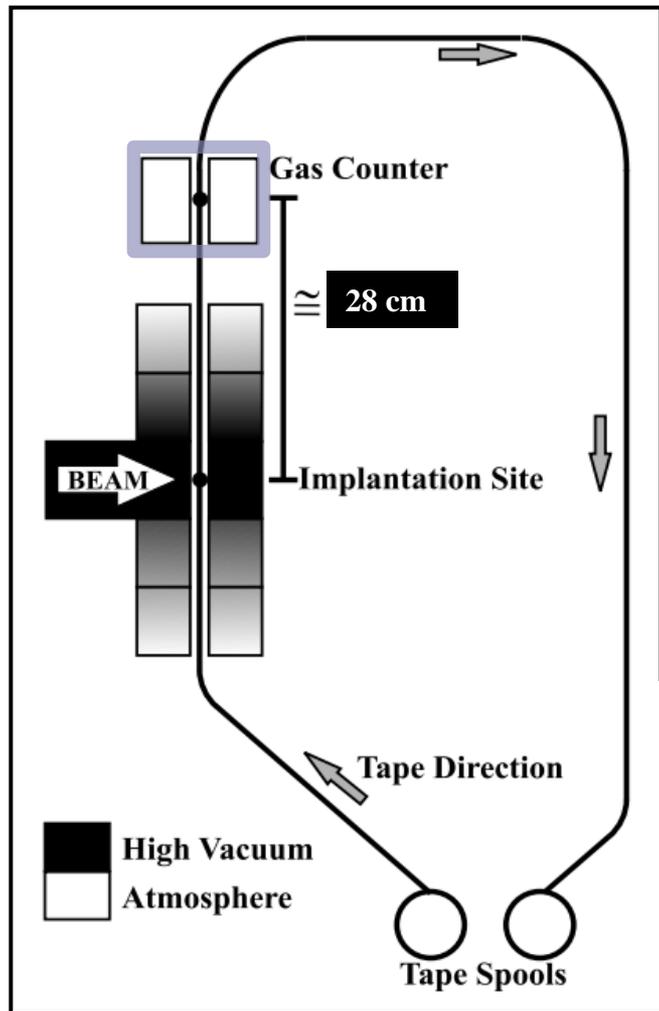
$\beta^+$

$T = 1$   $^{18}\text{O}$   $0^+$

stable

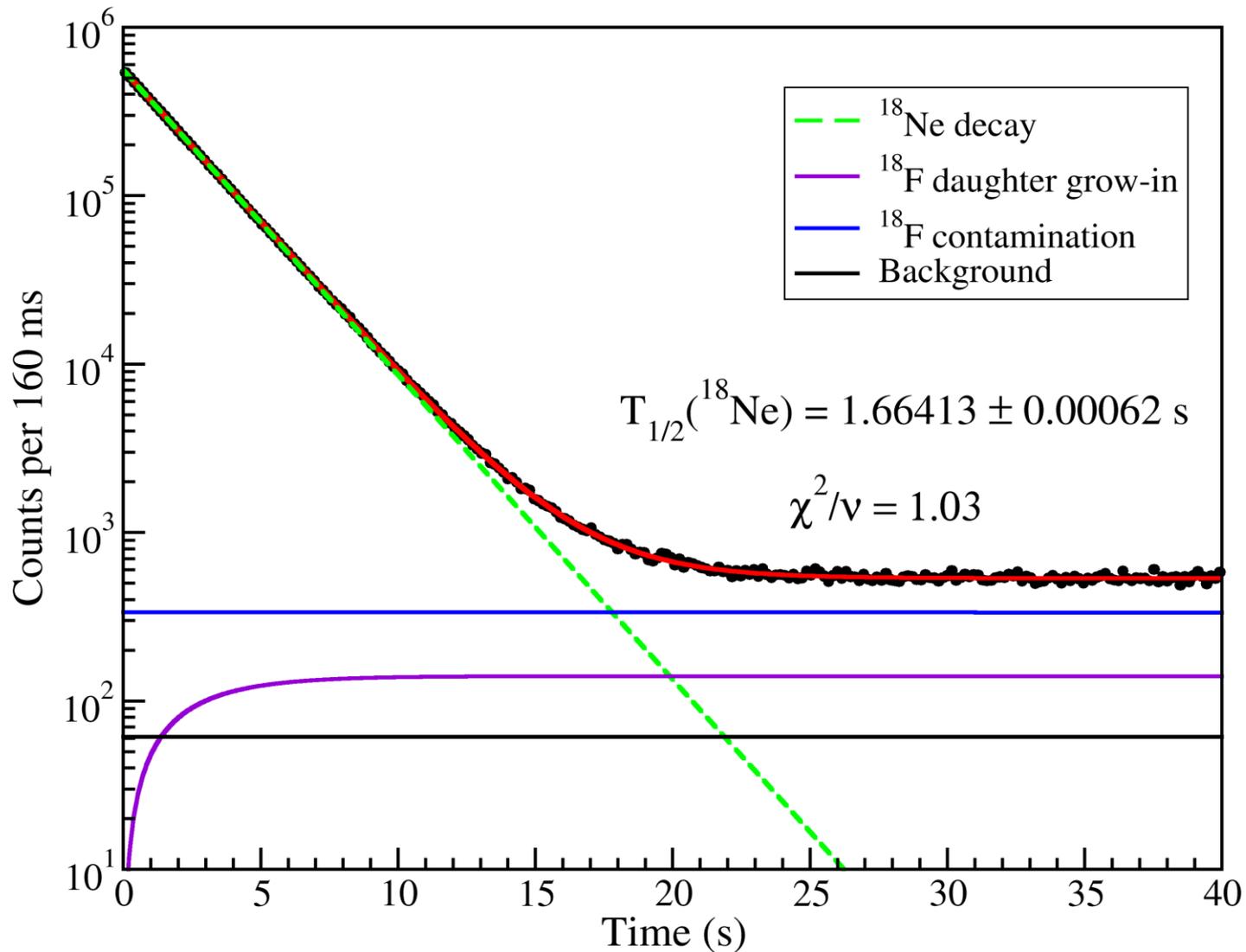


# 4 $\pi$ Gas Counter and Thick Tape Transport

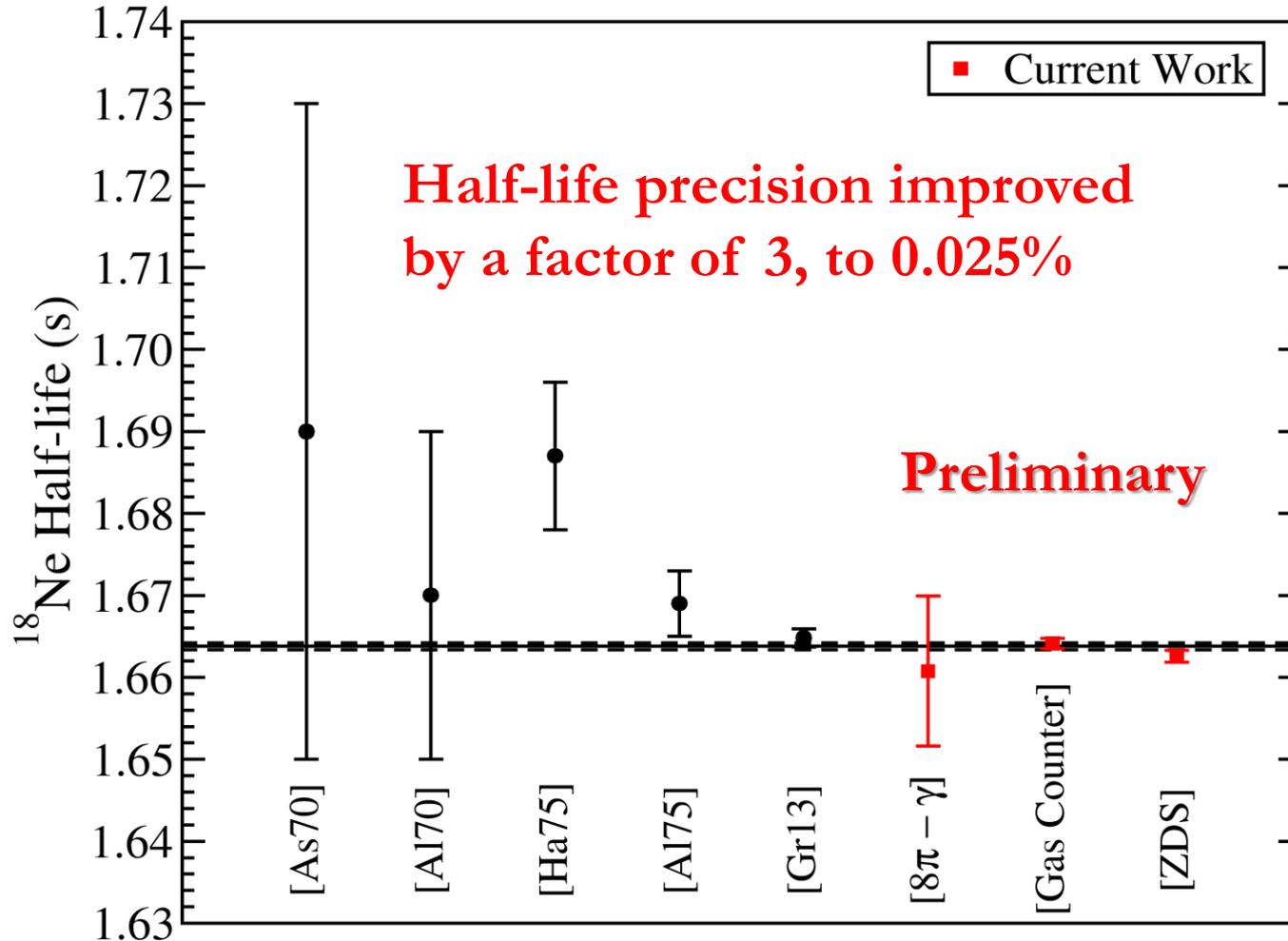


- ◆ 4 $\pi$  continuous-flow gas-proportional counter and tape transport system
- ◆ Methane (CH<sub>4</sub>) gas
- ◆ ~ 100% efficient  $\beta$  counter
- ◆ Very low background rates

# $^{18}\text{Ne}$ Sample Data – Gas Counter



# Status of $^{18}\text{Ne}$ Half-life



# $^{74}\text{Rb}$ Superalloyed Decay ( $T_{1/2} \sim 65$ ms)

**Half-life:** Measured with the GPS  $4\pi$  gas proportional counter at ISAC.

$$T_{1/2} = 64.761(31) \text{ ms}$$

*G.C. Ball et al., Phys. Rev. Lett. 86, 1454 (2001).*

**Mass:** First demonstration of a high charge state mass measurement for a short-lived isotope with the TITAN Penning trap.

*S. Ettenauer et al., Phys. Rev. Lett. 107, 272501 (2011).*

**Charge Radius:** Measured via collinear laser spectroscopy:

$$\langle r_{\text{ch}}^2 \rangle^{1/2} = 4.19(1) \text{ fm}$$

Reduces uncertainty in theoretical  $\delta_{\text{C}2}$  by  $\sim 20\%$

*E. Mané et al., Phys. Rev. Lett. 107, 212502 (2011).*

**Branching Ratio:** Measured with the  $8\pi$  Spectrometer to  $\pm 0.03\%$

$$\text{BR} = 99.545 (31) \%$$

*R. Dunlop et al., Phys. Rev. C 88, 045501 (2013).*

# Superaligned $\beta$ Branching Ratios for $A \geq 62$ and the Pandemonium Effect

VOLUME 88, NUMBER 25

PHYSICAL REVIEW LETTERS

24 JUNE 2002

## Superaligned Beta Decay of Nuclei with $A \geq 62$ : The Limiting Effect of Weak Gamow-Teller Branches

J. C. Hardy and I. S. Towner\*

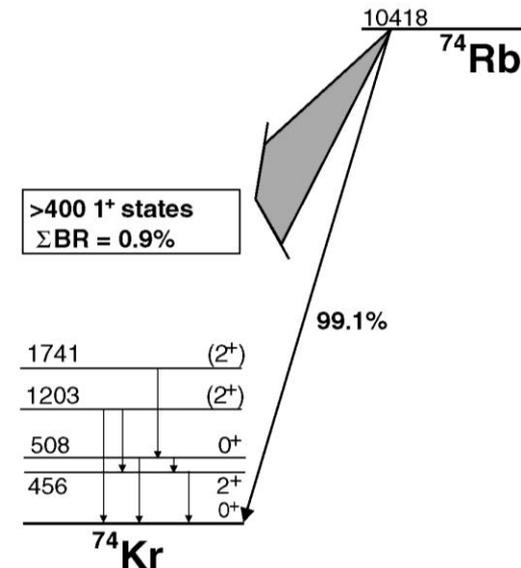
*Cyclotron Institute, Texas A & M University, College Station, Texas 77843*

(Received 16 January 2002; published 6 June 2002)

The most precise value of  $V_{ud}$ , which is obtained from superallowed nuclear  $\beta$  decay, leads to a violation of Cabibbo-Kobayashi-Maskawa unitarity by  $2.2\sigma$ . Experiments are underway on two continents to test and improve this result through decay studies of odd-odd  $N = Z$  nuclei with  $A \geq 62$ . We show, in a series of illustrative shell-model calculations, that numerous weak Gamow-Teller branches are expected to compete with the superallowed branch in each of these nuclei. Though the total Gamow-Teller strength is significant, many of the individual branches will be unobservably weak. Thus, new techniques must be developed if reliable  $f_t$  values are to be obtained with 0.1% precision for the superallowed branches.

DOI: 10.1103/PhysRevLett.88.252501

PACS numbers: 23.40.Hc, 21.60.Cs, 27.50.+e



For large Q-value  $\beta$  decays, there are generally many weak  $\beta$  branches to the large number of daughter states within the Q-value window.

In the subsequent  $\gamma$  decay, many individual  $\gamma$ -rays may be too weak to identify.

The sum of these unobserved  $\gamma$  intensities will, however, generally be sufficient to prevent precision determination of  $\beta$  decay branching ratios through  $\gamma$ -ray spectroscopy.

# $8\pi$ Spectrometer – Decay Spectroscopy at ISAC-I

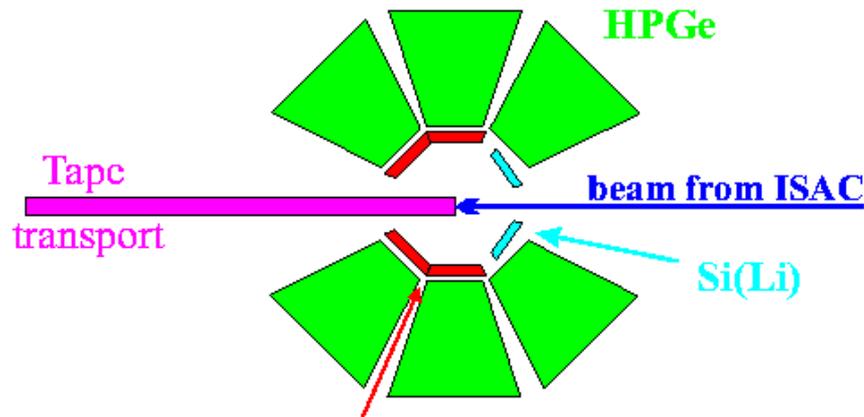
## $8\pi$ Spectrometer at ISAC

20 Compton-Suppressed HPGe detectors  
and 10 BaF2 detectors for  $\gamma$ -ray detection

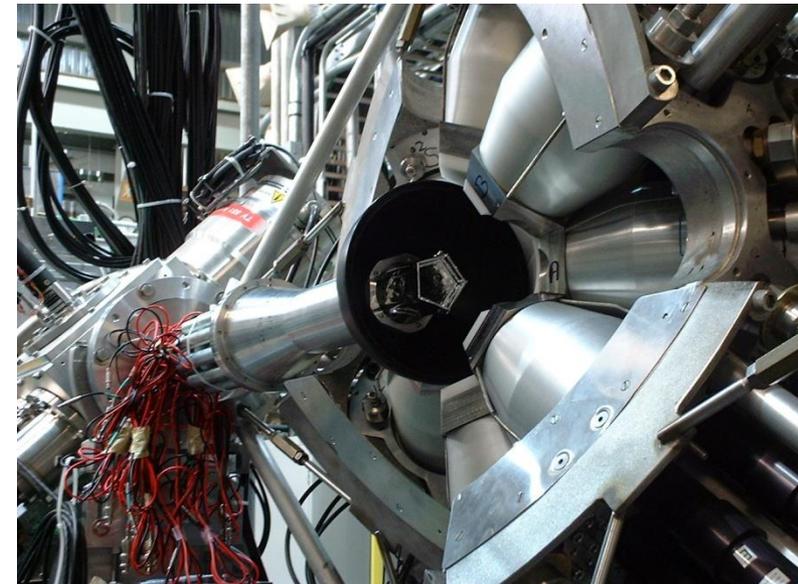
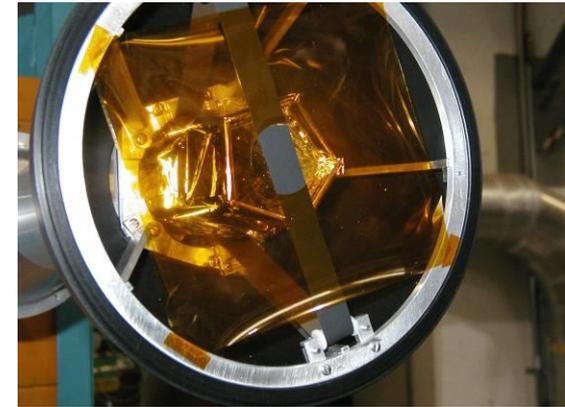
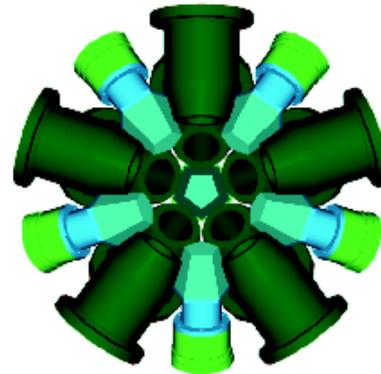
20 plastic scintillators for  $\beta$  detection

5 Si(Li) detectors for conversion electron spectroscopy

Fast, in-vacuum tape transport system

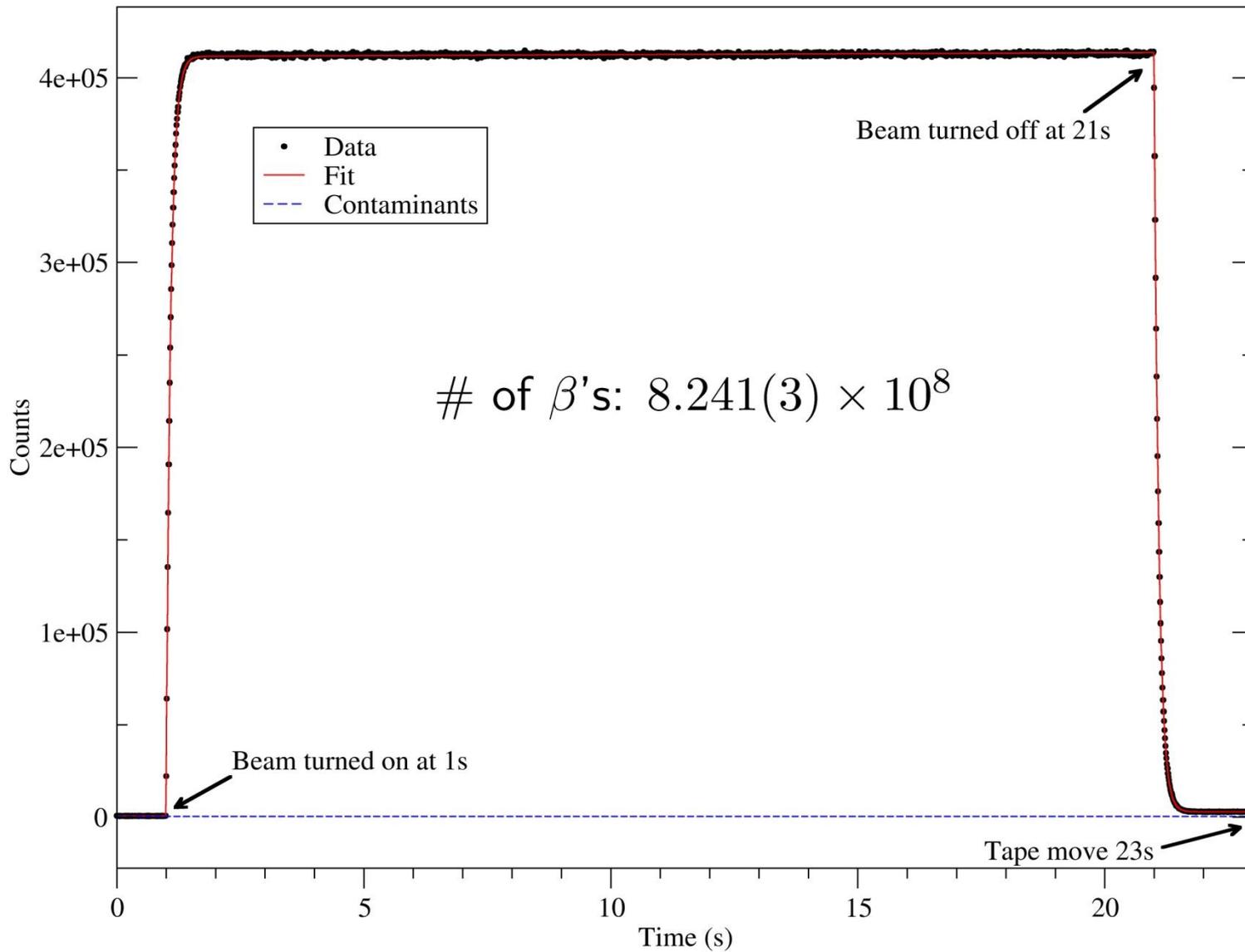


**2 $\pi$  (or 4 $\pi$ ) array of positron counters**

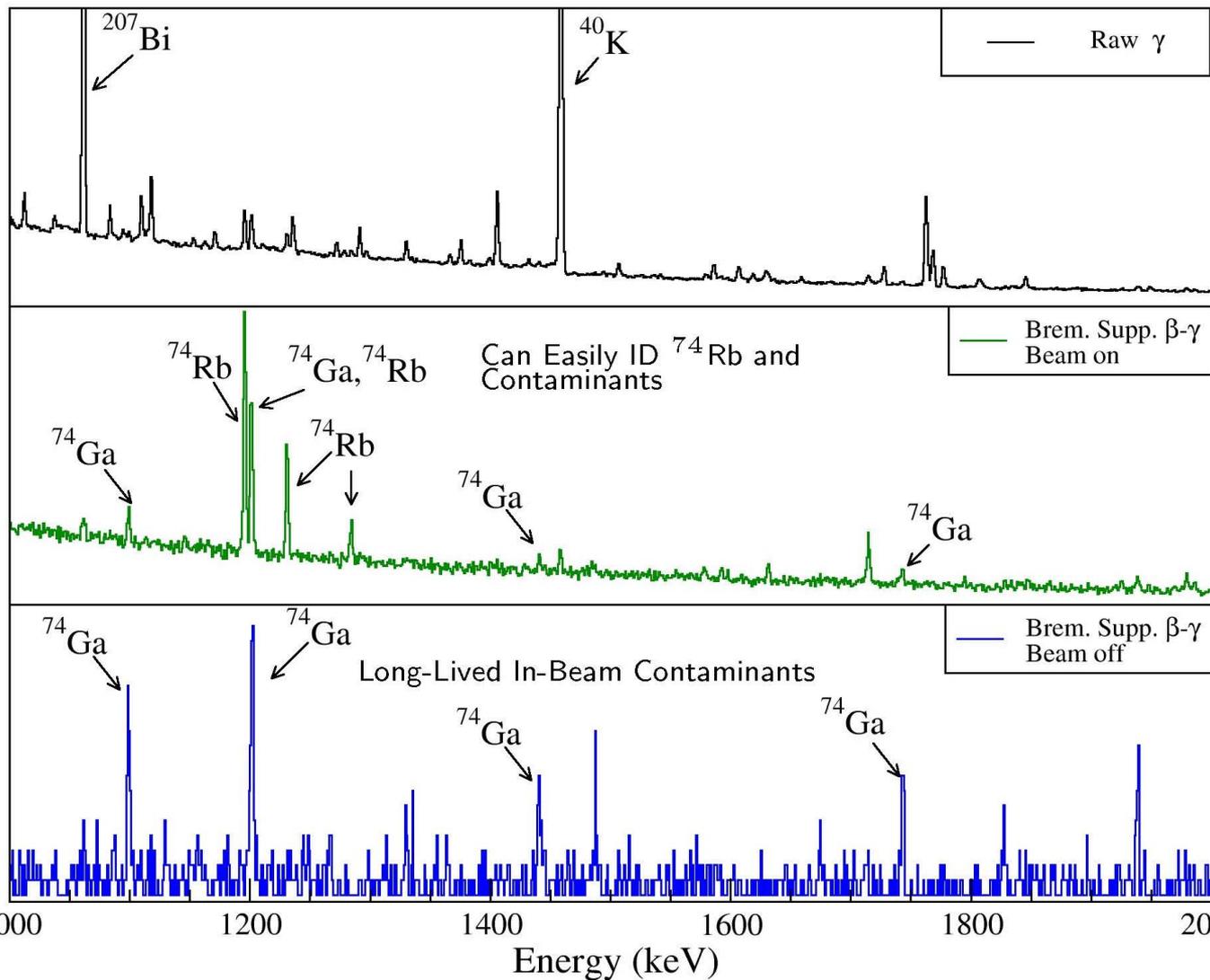


Simultaneous collection of  $\gamma$ -singles,  $\gamma\gamma$  coincidences,  $\beta$  tagging, conversion electrons, and lifetime measurements

# Counting $^{74}\text{Rb}$ $\beta$ Decays with SCEPTAR



# Identifying $\gamma$ -rays from $^{74}\text{Rb}$ Decay



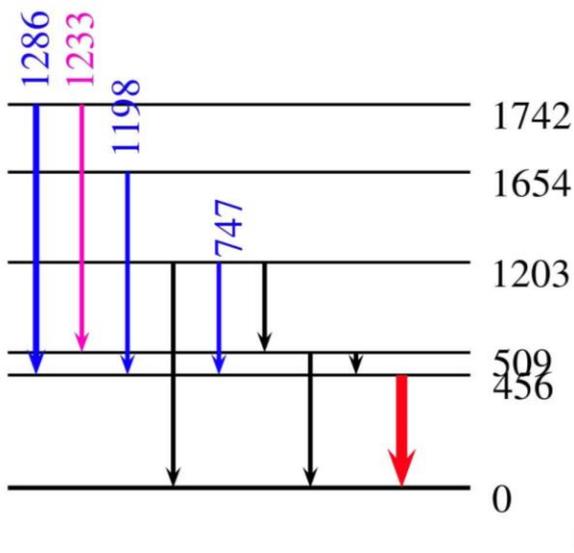
Raw  $\gamma$ -spectrum contains lines from room background and in-beam contaminants

$\beta$ - $\gamma$  coincidence, Bremsstrahlung suppression reduce background

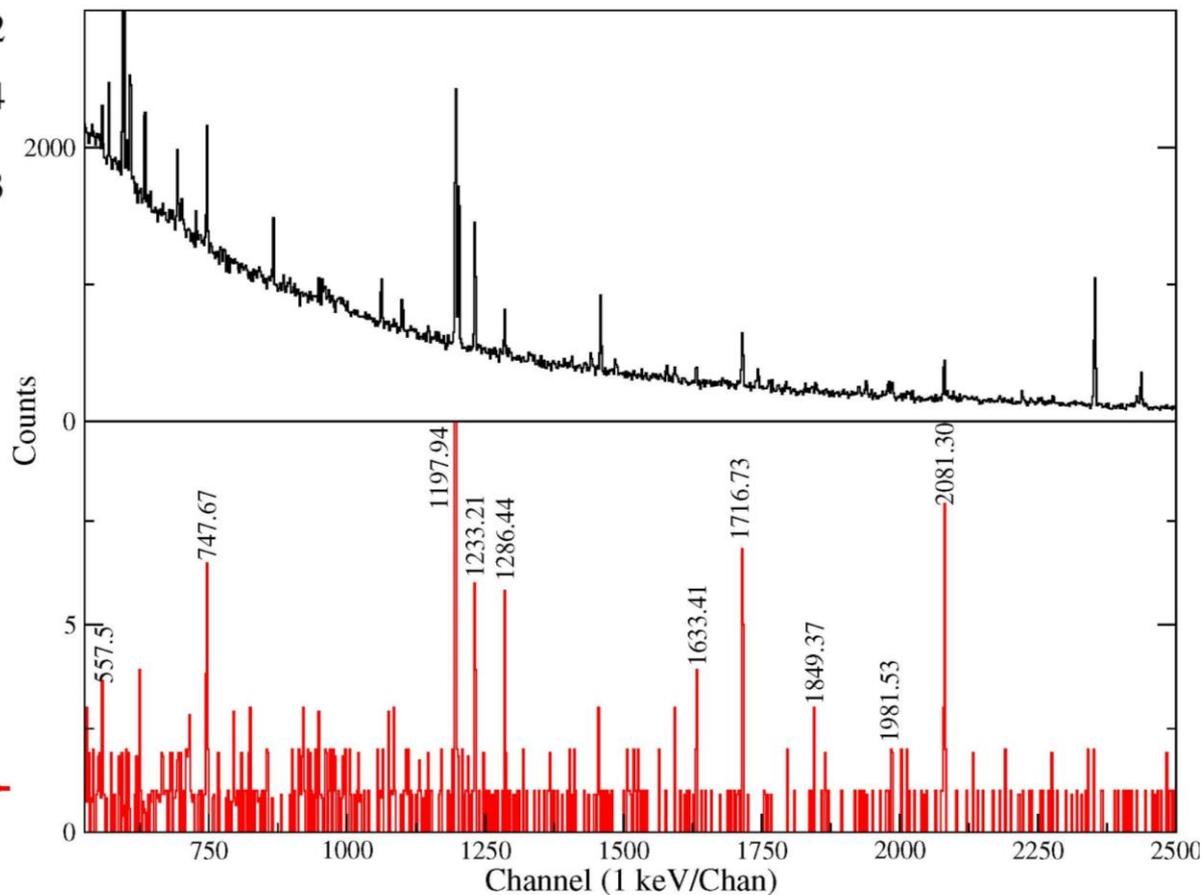
Spectrum during beam-off allows one to identify long-lived contaminants

# $\gamma$ - $\gamma$ Coincidences following ppm $\beta$ -decay branches of $^{74}\text{Rb}$

All  $\beta - \gamma$  Coincidences 

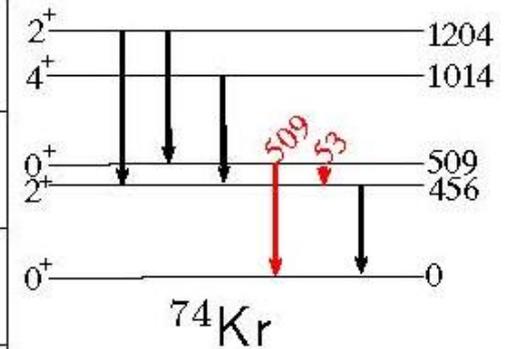
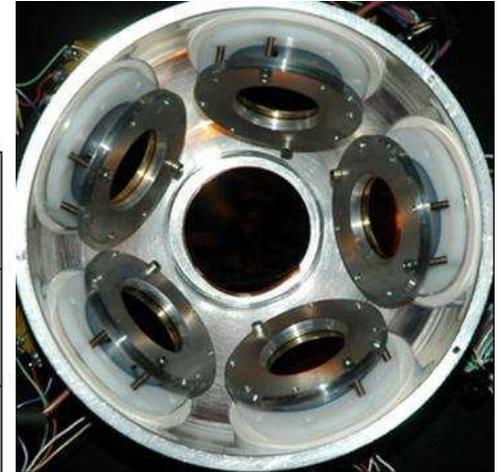
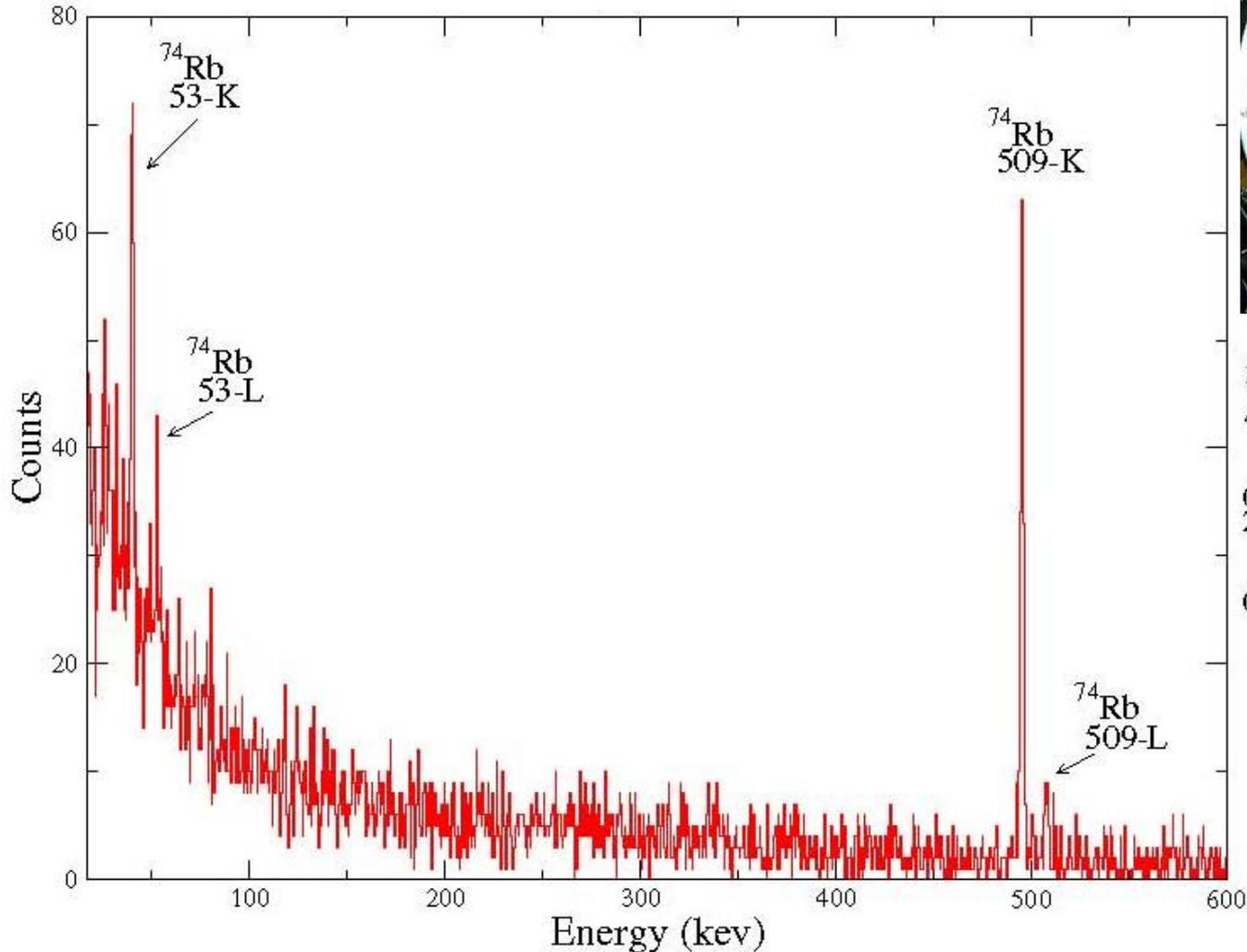


Gated on 456 keV  $\gamma$ -ray 

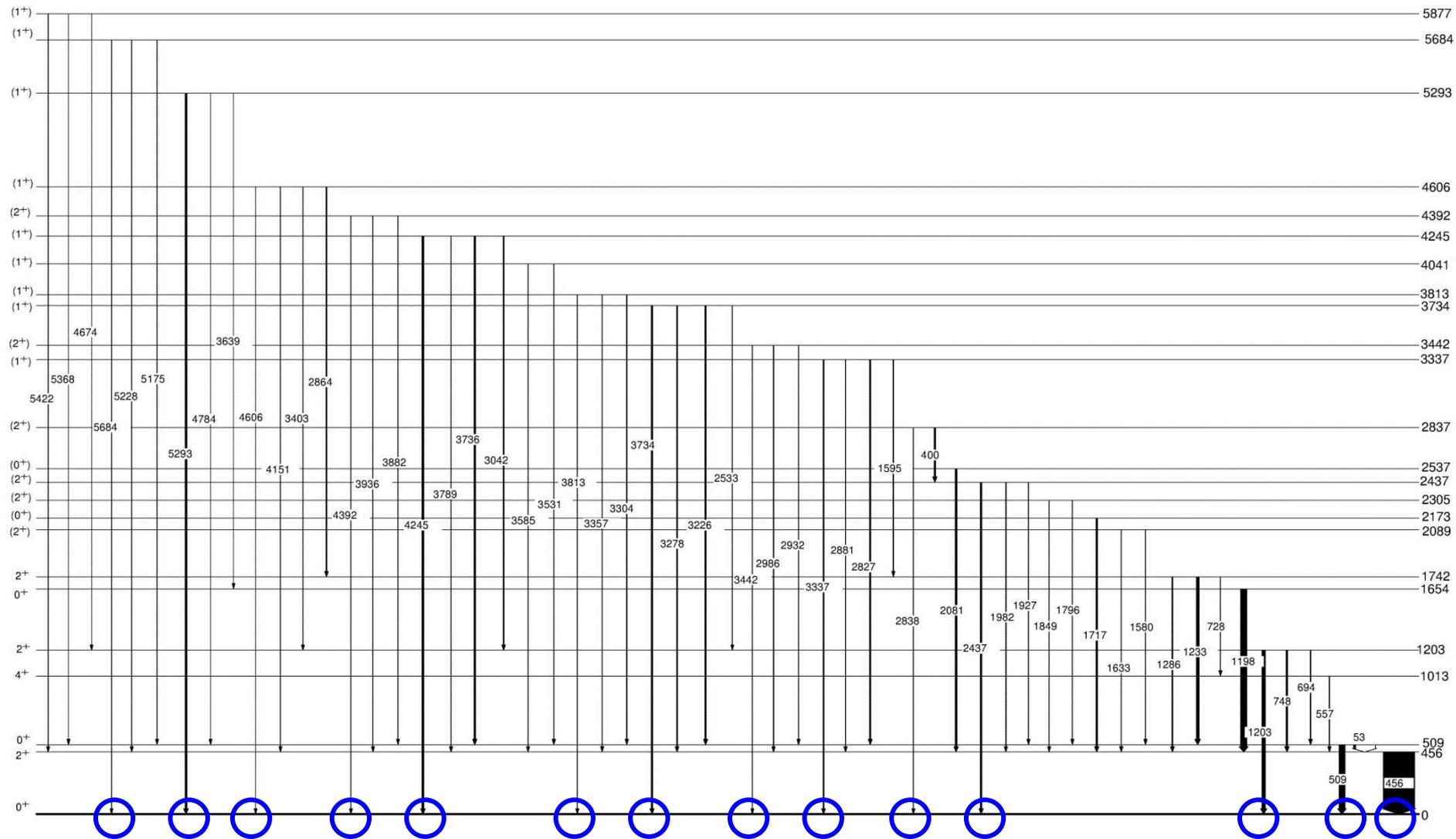


# Internal Conversion Decay of the $0^+_2$ State of $^{74}\text{Kr}$

## $\beta - \gamma - \text{electron}$ Coincidence Spectrum



# 57 $\gamma$ -ray transitions identified following $^{74}\text{Rb}$ decay



Ground-state  $\gamma$ -feeding of  $I_{gs} = 3950(70)$  ppm identified.

# Controlling Pandemonium via $2^+$ “Collector” States

$$I'_{gs} = 3950(70) \text{ ppm}$$

Direct  $\beta$  feeding of  $2^+$  states is negligible

$$I'_{2+} = 1225(57) \text{ ppm}$$

$$B_{gs} = I'_{gs} / (I'_{gs} + I'_{2+})$$

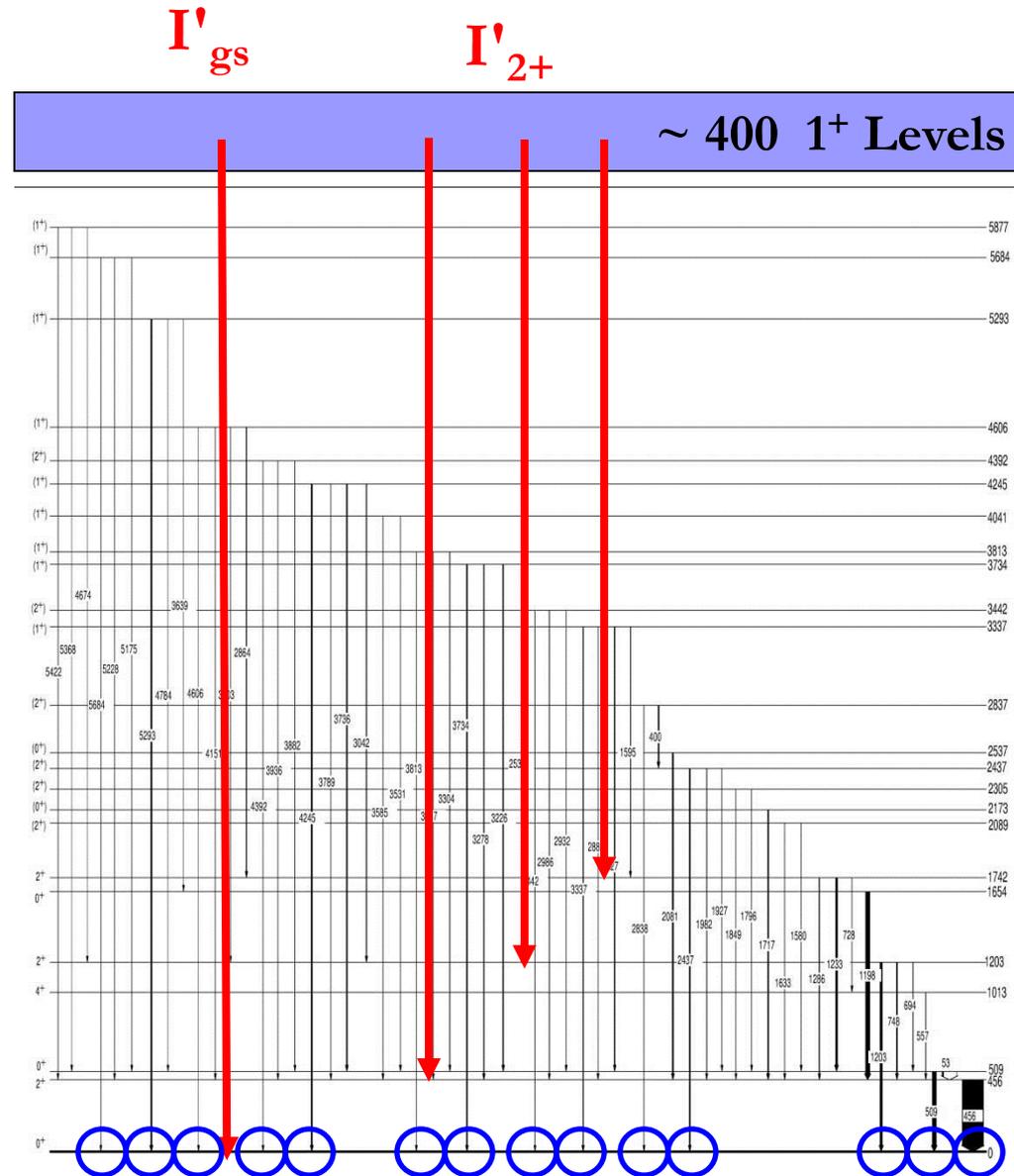
Expt + Shell Model:

$$B_{gs} = 0.33(11)$$

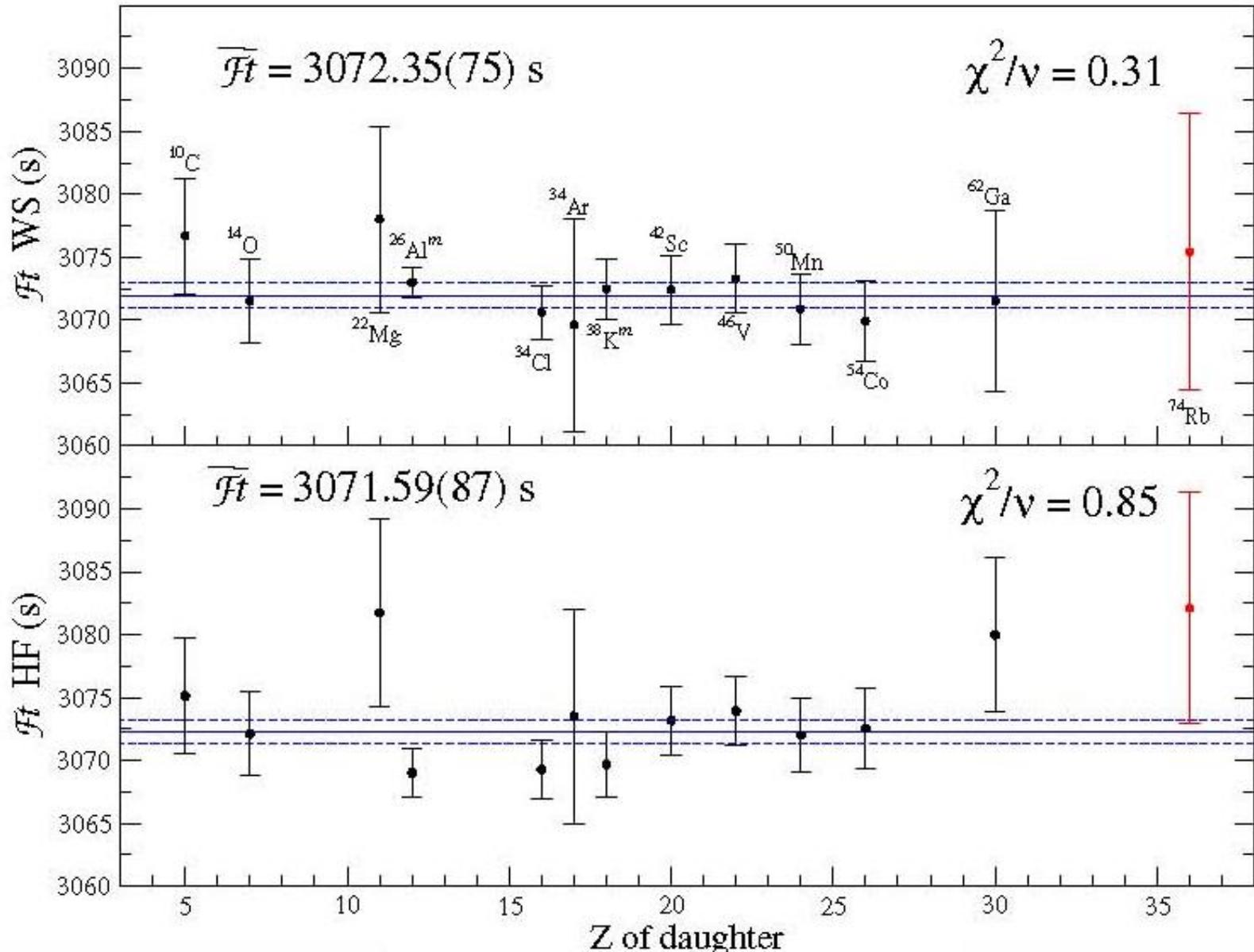
$$I'_{gs} = 600(300) \text{ ppm}$$

Superaligned Branching Ratio:  
 $99.545 \pm 0.031 \%$

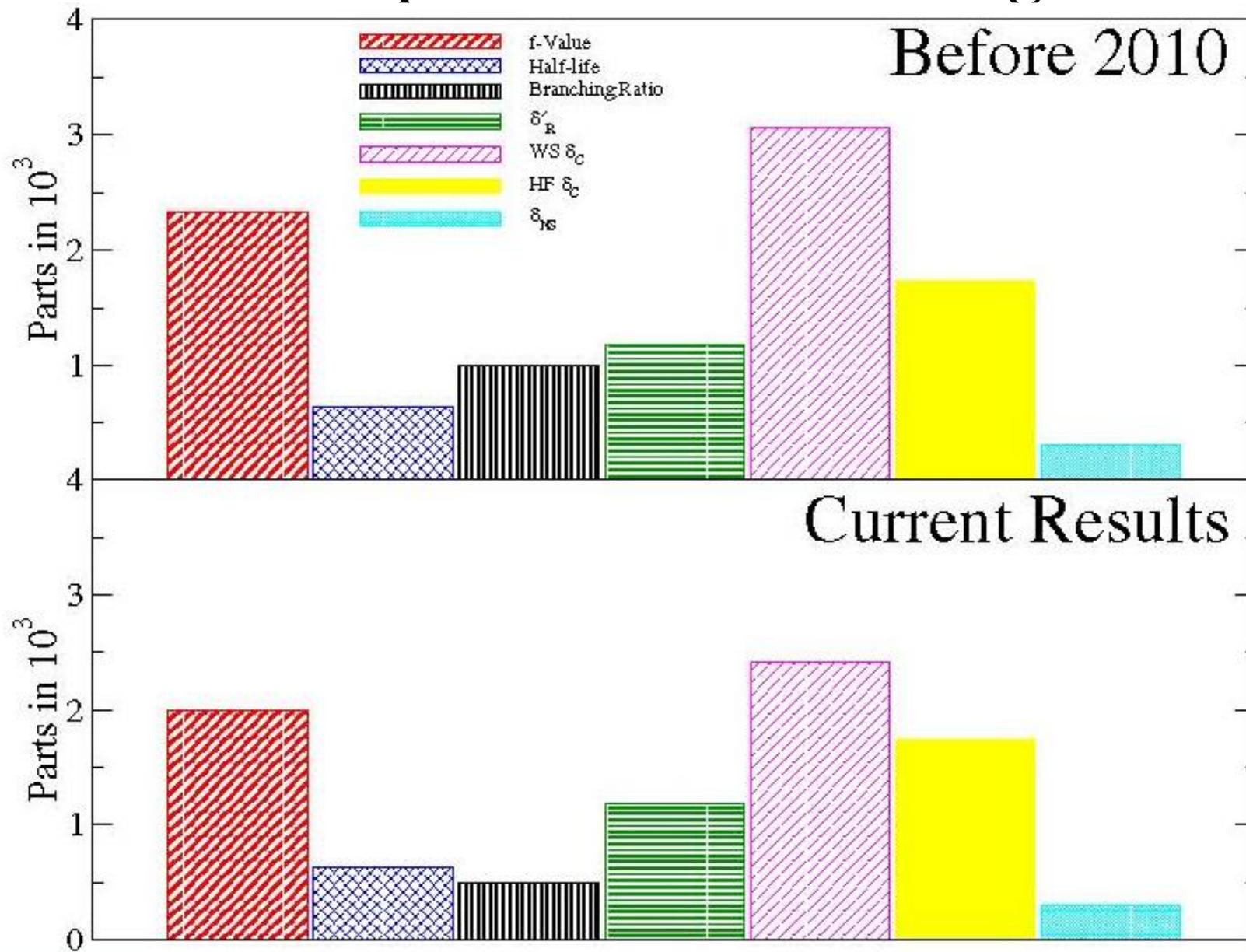
R. Dunlop PRC 88, 045501 (2013)

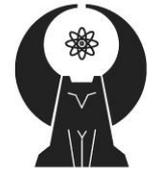


# $^{74}\text{Rb}$ Superaligned Decay



# $^{74}\text{Rb}$ Superaligned Error Budget





GRIFFIN

The Future ...

*Gamma*

*Ray*

*Infrastructure*

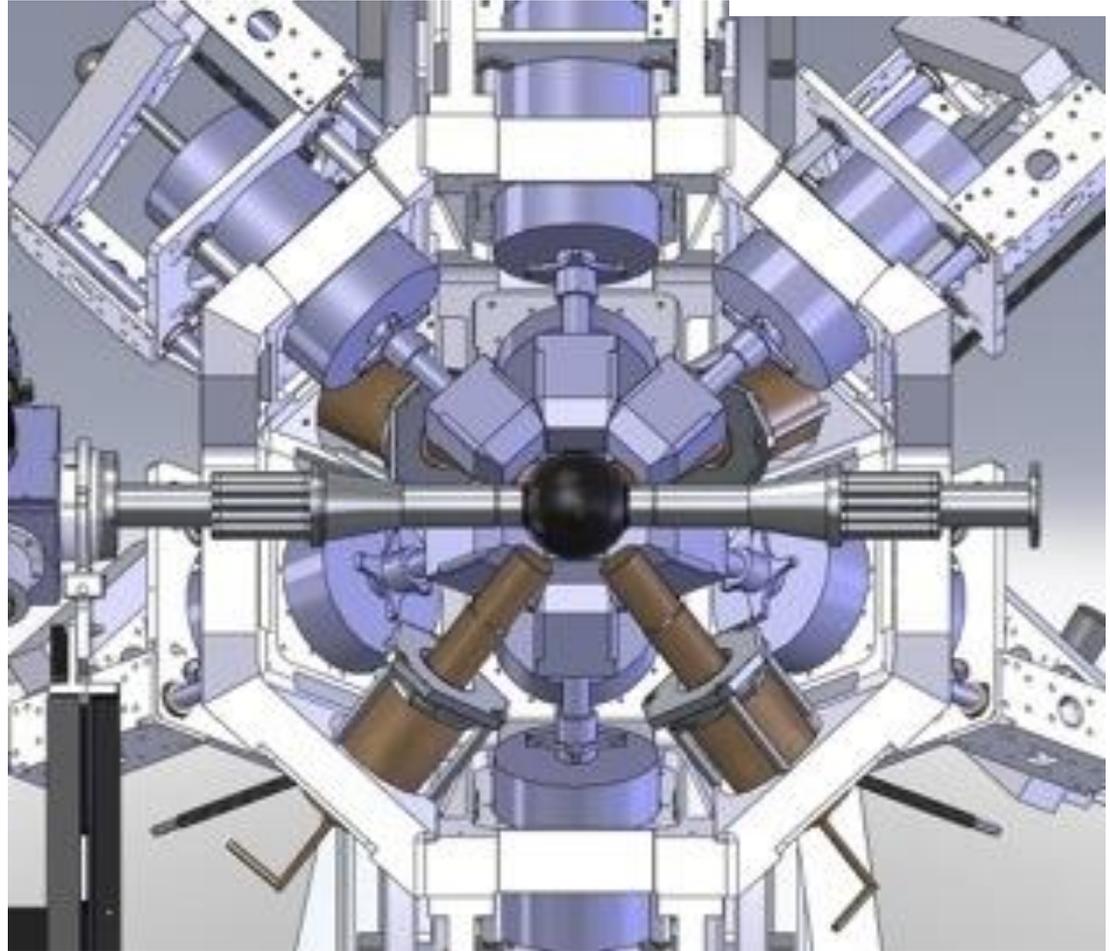
*For*

*Fundamental*

*Investigations*

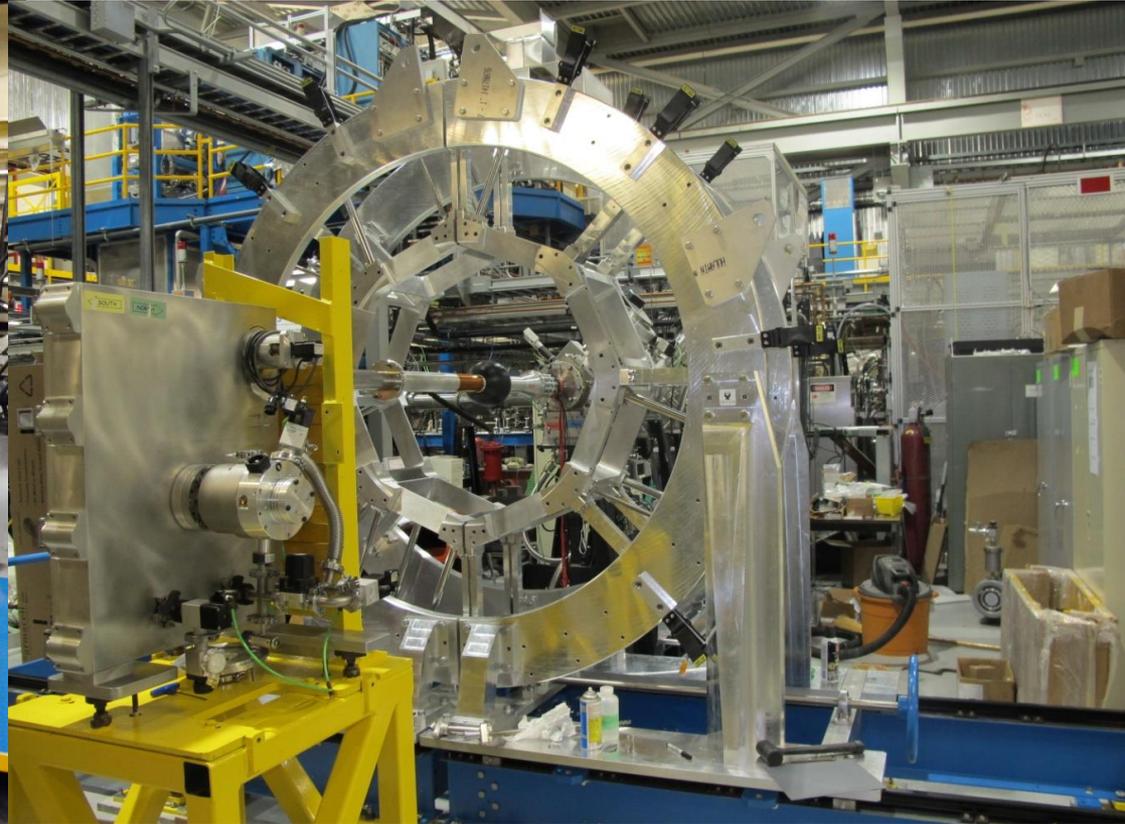
*of*

*Nuclei*



**A new high-efficiency decay spectroscopy facility for ISAC-I**

# GRIFFIN @ ISAC-I



June 14, 2014

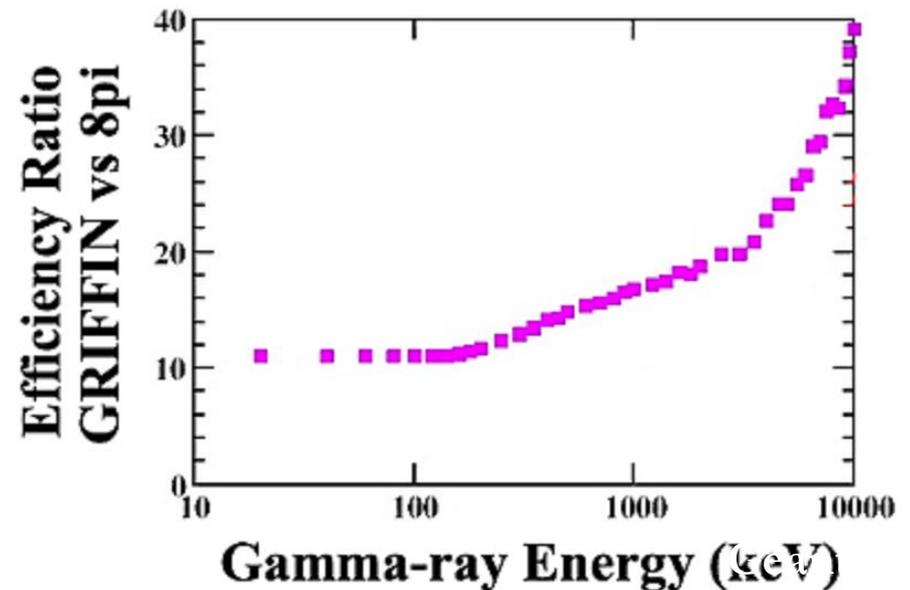
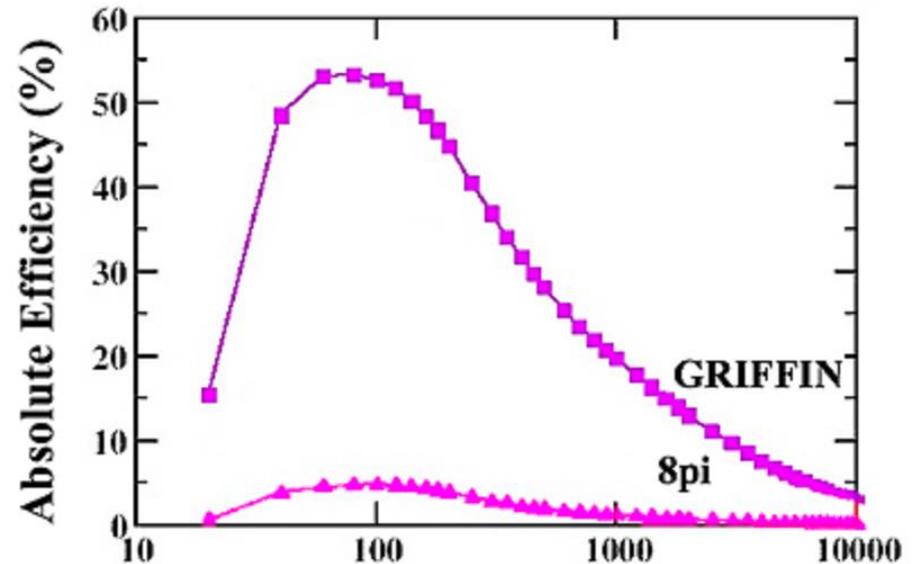
# GRIFFIN

16 large-volume clover-type  
HPGe  $\gamma$ -ray detector

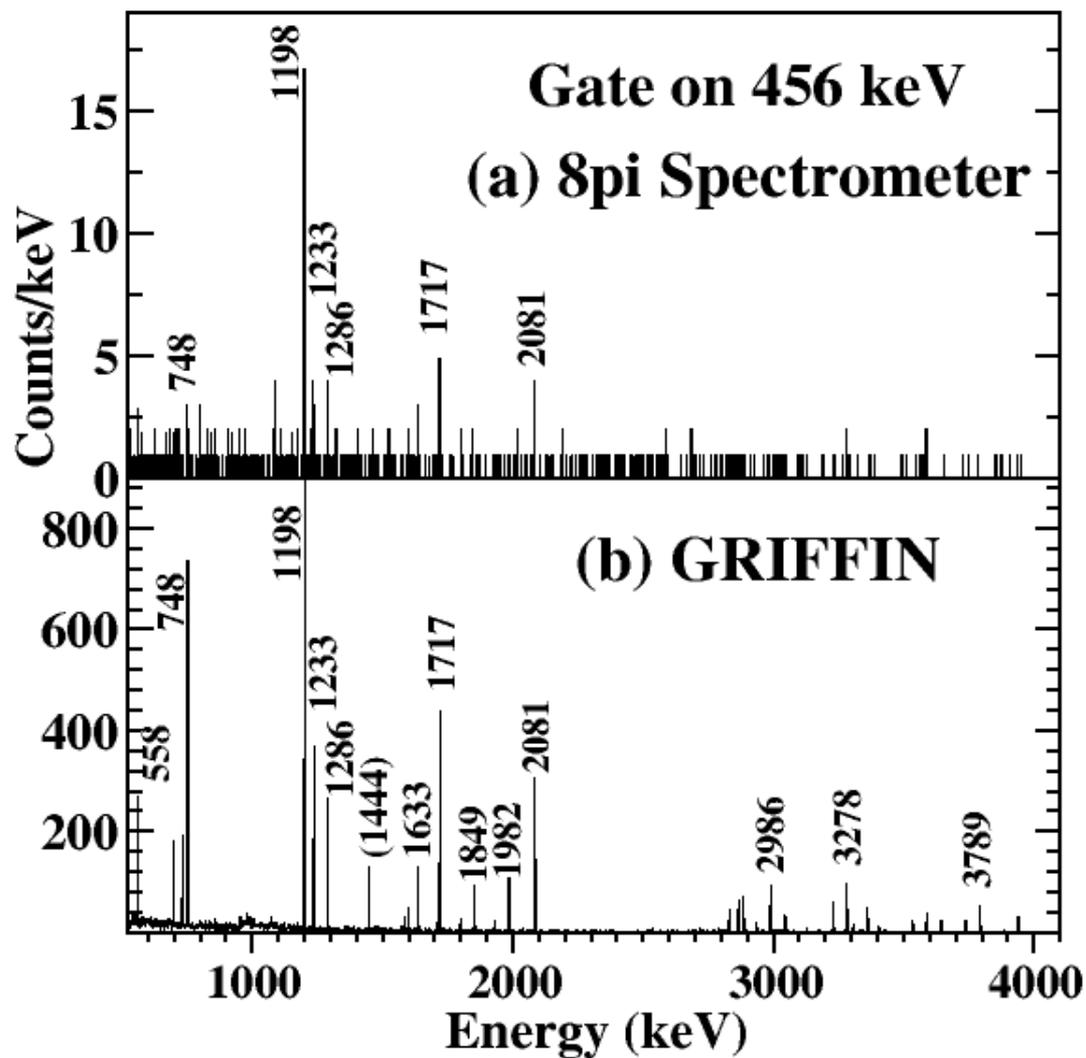
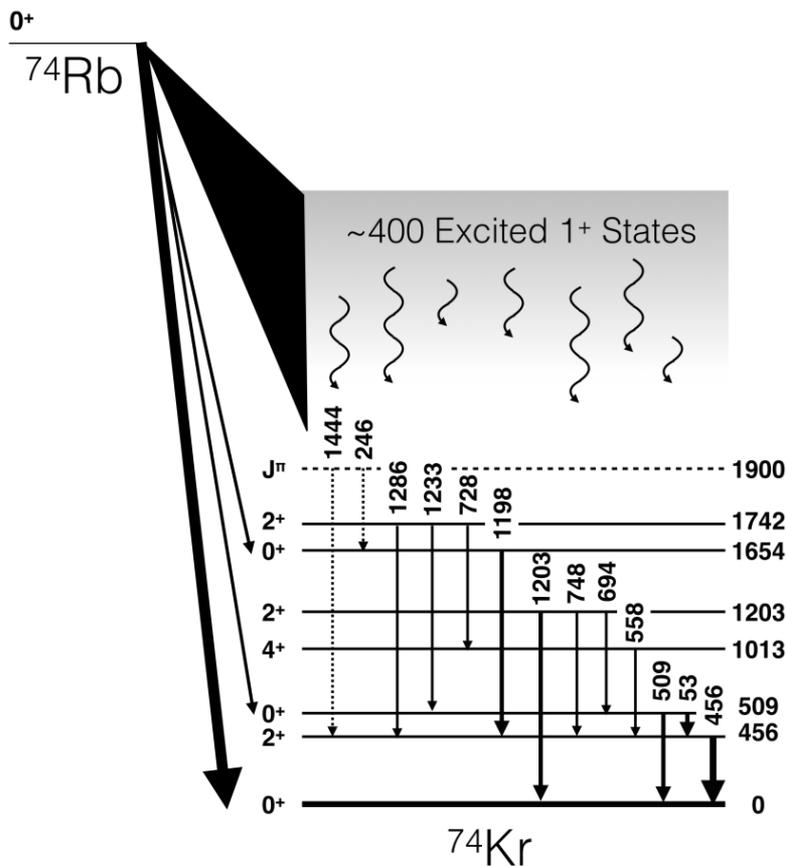
17 times the efficiency of the  
 $8\pi$  at  $E_\gamma = 1$  MeV

Efficiency improvement  
increases with  $\gamma$ -ray energy

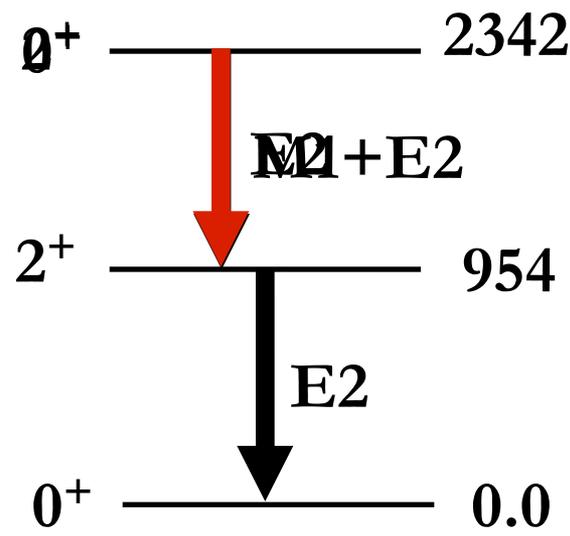
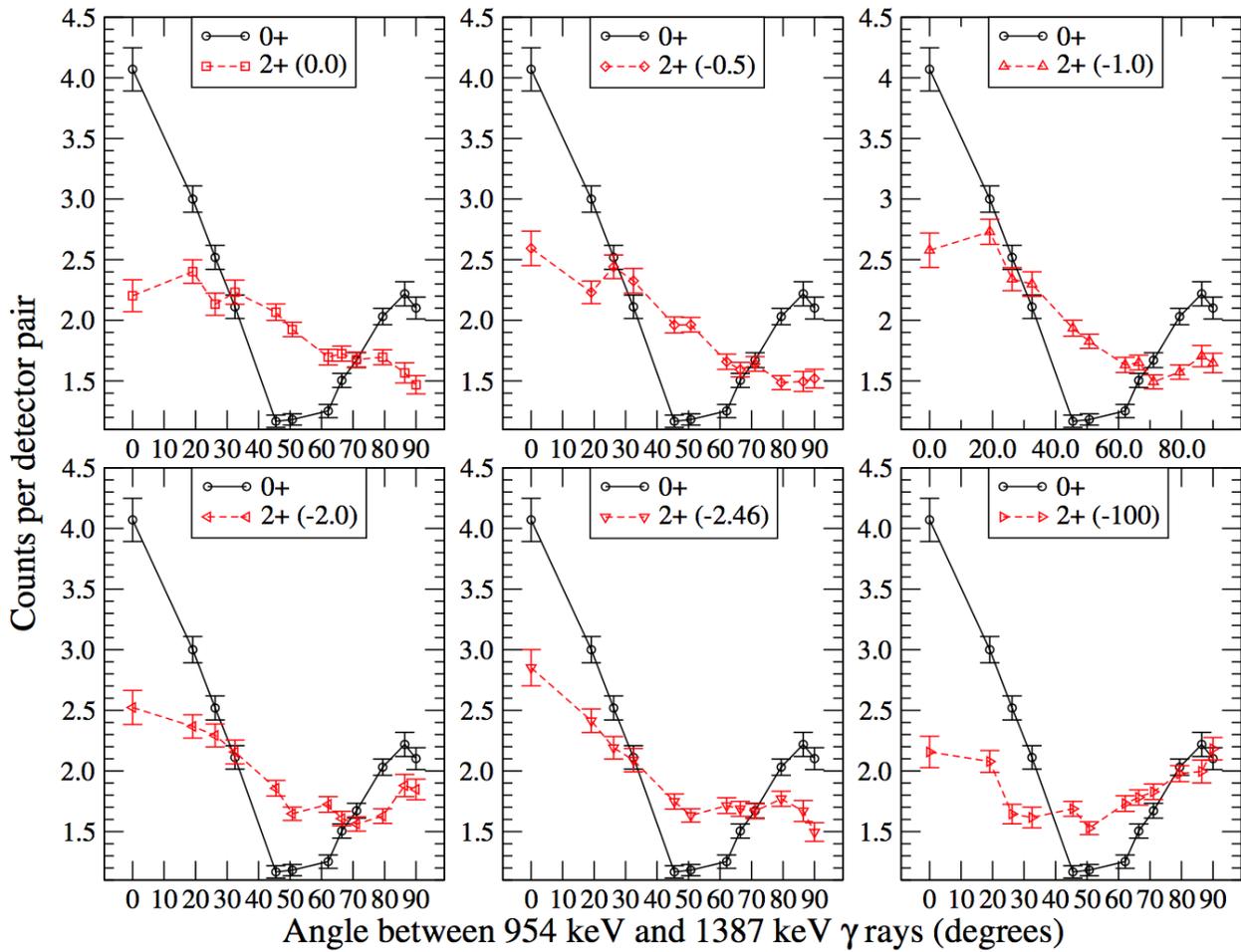
$\sim 300\times$  the  $\gamma$ - $\gamma$  efficiency  
of the  $8\pi$



# $^{74}\text{Rb}$ Superallowed Decay with GRIFFIN

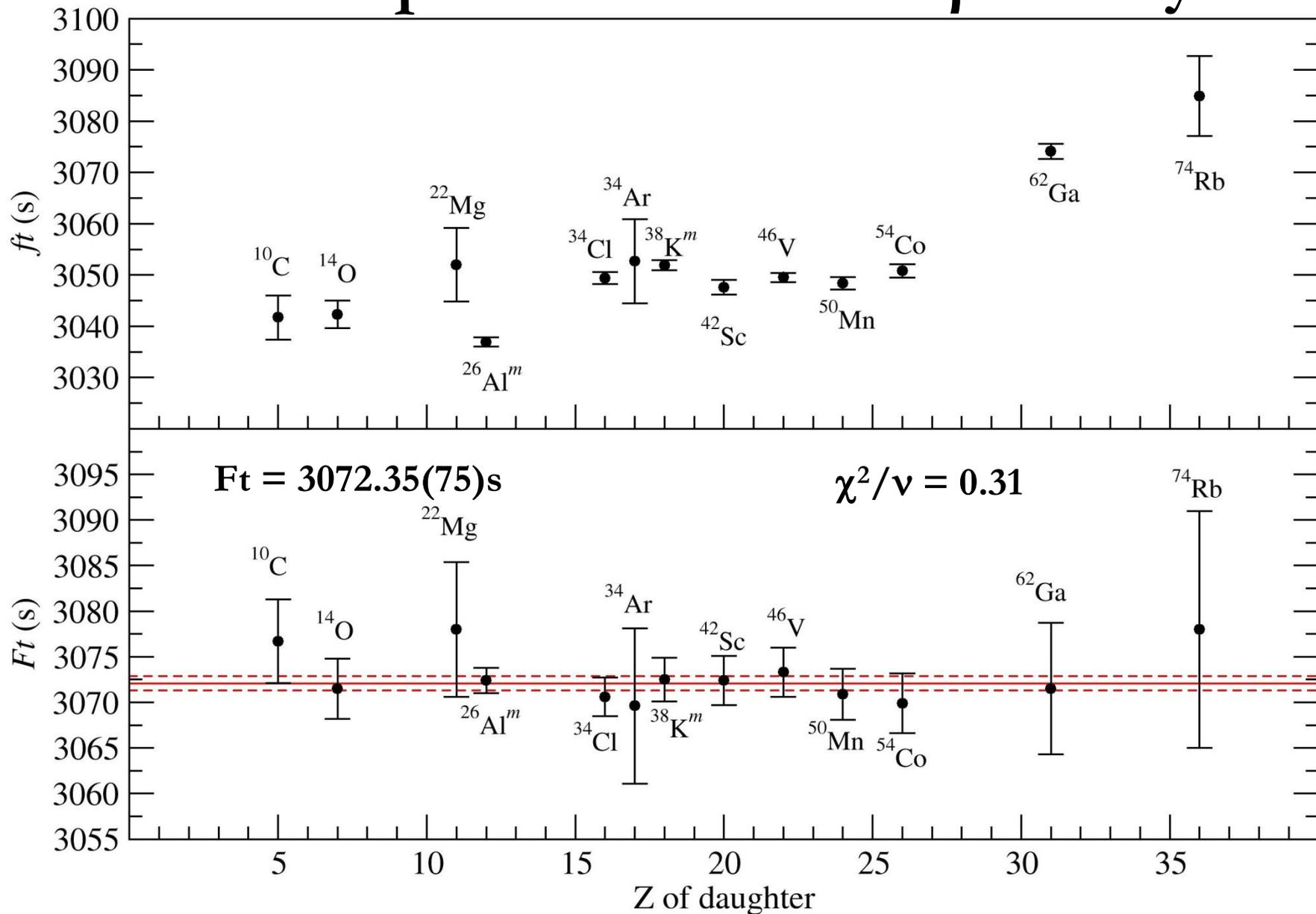


# Angular Correlation Measurements with GRIFIN (S1518: $^{62}\text{Ga}$ superallowed decay)



Using GRIFIN  
we can determine  
the spin-parity of  
the 2342 keV state

# World Superallowed Fermi $\beta$ Decay Data



# World Superallowed Fermi $\beta$ Decay Data

CVC hypothesis confirmed to  $\pm 0.013\%$

Set limits on maximally parity violating weak scalar currents:

$$C_S/C_V = 0.0011 \pm 0.0013$$

$V_{ud}$  determined from the superallowed data is, by far, the most precisely determined element of the CKM quark-mixing matrix:

$$|V_{ud}| = 0.97425 \pm 0.00022$$

and together with  $V_{us}$  (and  $V_{ub}$ ) provides the most demanding experimental test of the unitarity of the CKM matrix:

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1.00008 \pm 0.00056$$

Model-dependence of the strongly nuclear structure dependent isospin symmetry breaking corrections in superallowed Fermi  $\beta$  decays remains a key focus of research for both the theoretical and experimental communities.

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$T_{1/2}$ , G.C. Ball *et al*, PRL 86 1454 (2001)

BR, A. Piechaczek *et al*, PRC 67, 051305 (2003)

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Q: S. Ettenauer *et al.*, PRL 107, 272501 (2011)

CR: E. Mané *et al*, PRL 107, 212502 (2011)

$^{74}\text{Rb}$

# Superaligned $\beta$ Decay Studies at ISAC

$T_{1/2}$ , G.F. Grinyer, PRC 77, 201501 (2008)

BR, B.H. Hyland, PRL 97, 102501 (2006)

BR, P. Finlay PRC 78, 044321 (2008)

$^{62}\text{Ga}$

$^{66}\text{As}$

$^{70}\text{Br}$

$T_{1/2}$  and BR

$^{54}\text{Co}$

$^{50}\text{Mn}$

$^{46}\text{V}$

$^{38m}\text{K}$

$T_{1/2}$  and BR

$^{34}\text{Ar}$

$N=Z$  line

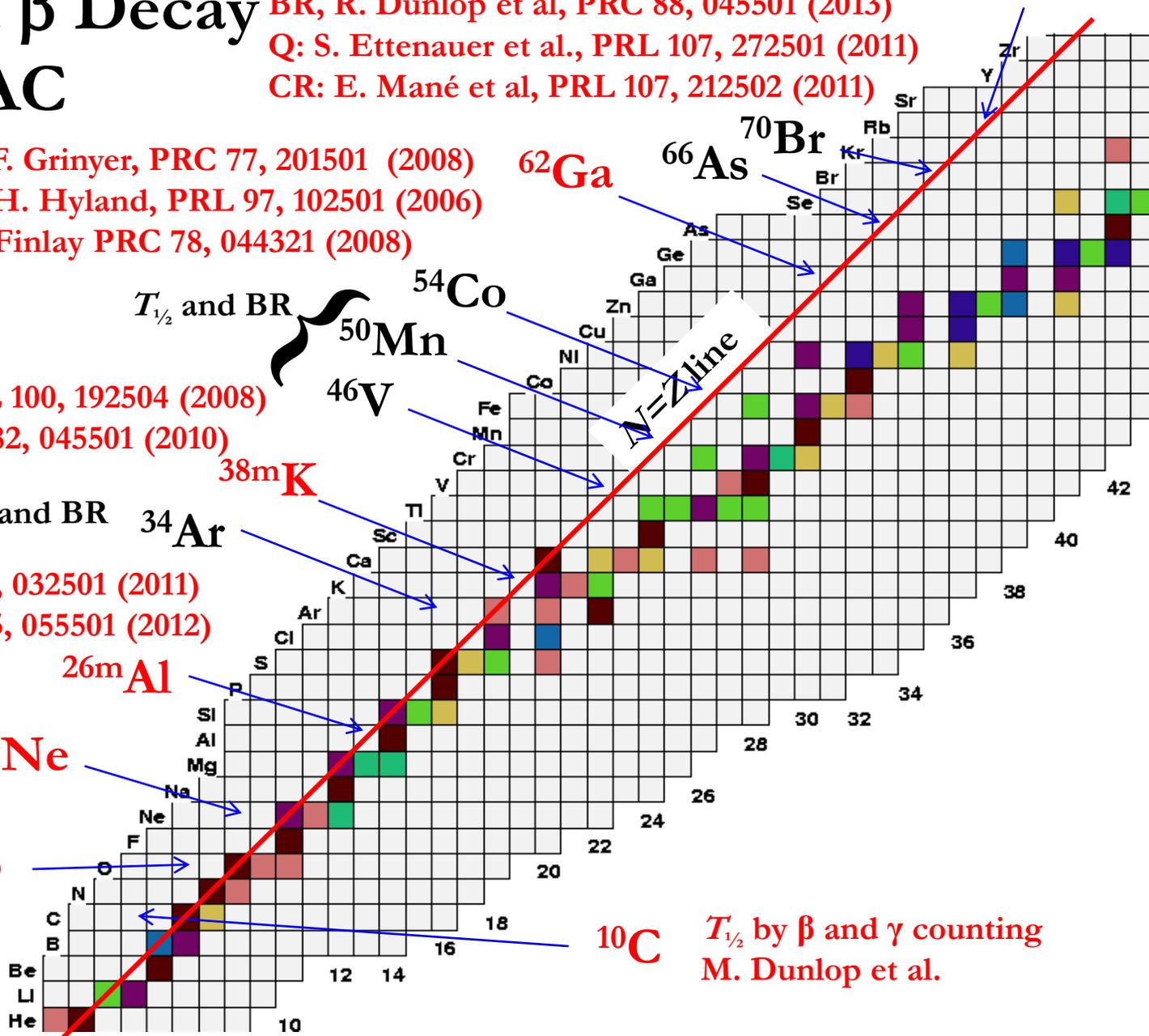
$^{26m}\text{Al}$

$^{18}\text{Ne}$

$^{14}\text{O}$

$^{10}\text{C}$

$T_{1/2}$  by  $\beta$  and  $\gamma$  counting  
M. Dunlop *et al.*



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$T_{1/2}$  P. Finlay *et al*, PRL 106, 032501 (2011)

BR, P. Finlay *et al*, PRC 85, 055501 (2012)

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PRC 76, 025503 (2007)

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$T_{1/2}$ , A.T. Laffoley *et al*,

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