

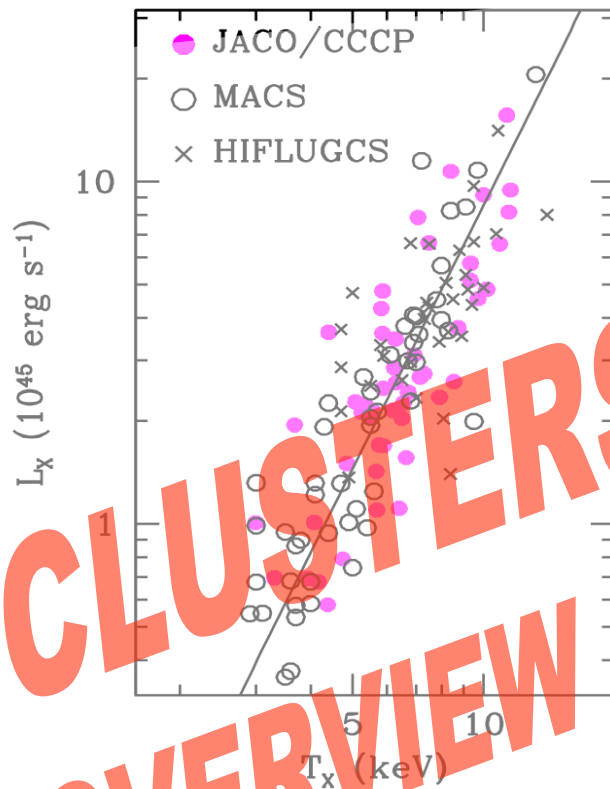
# Canadian Cluster Comparison Project

“it’s good for the masses!”

Henk Hoekstra  
(Leiden)

Arif Babul  
(Victoria)


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(SFSU)



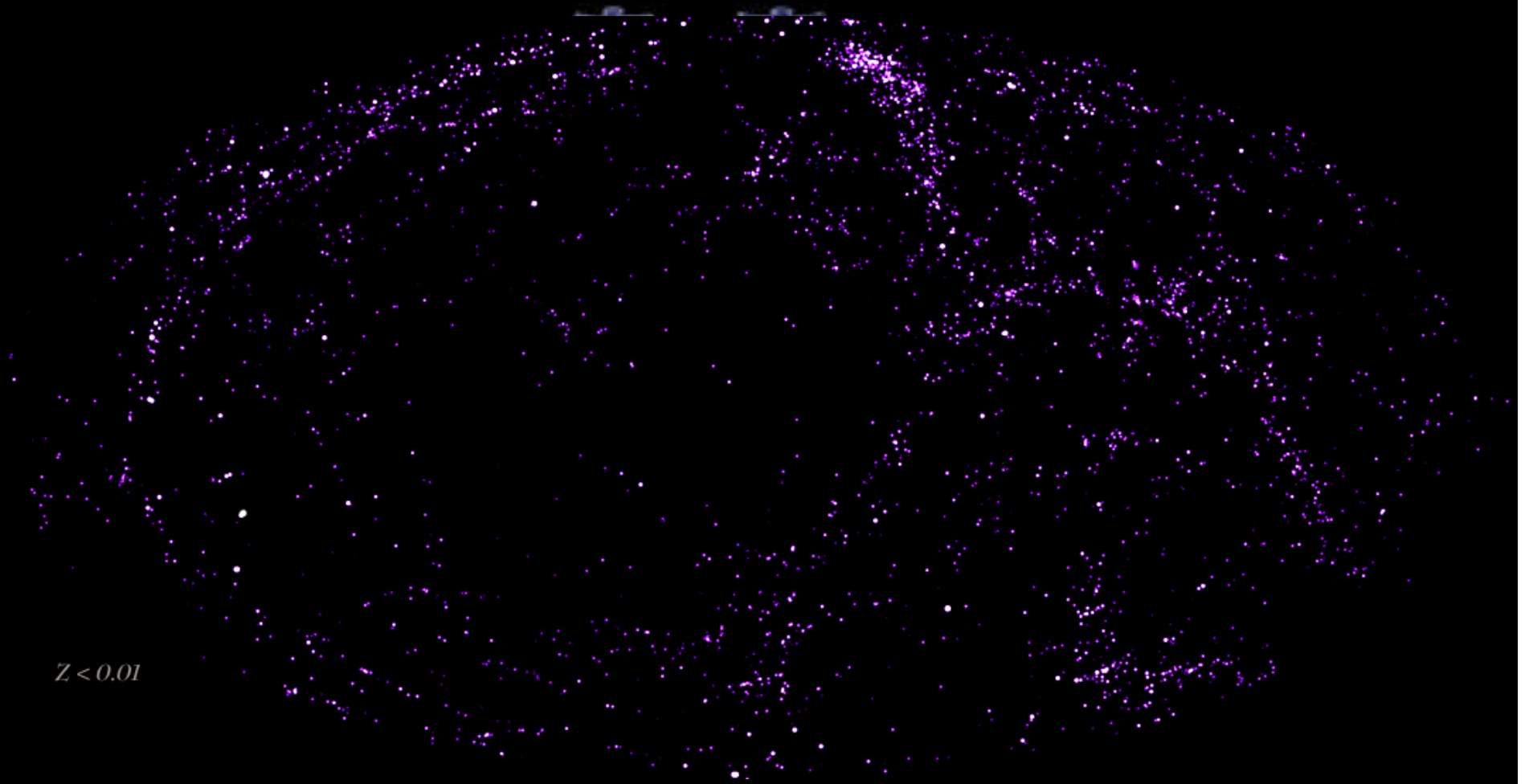
- 50 clusters with  $0.15 < z < 0.55$  ( $z \sim 0.25$ )
- CFHT accessible:  $-15^\circ < \text{dec} < 65^\circ$
- $T_x > 3 \text{ keV}$
- High quality two color optical data
- CFHT12K with B and R
- CFHT Megacam  $g'$  and  $r'$
- All except 3 have Chandra
- 3+21 have XMM
- For details see Mahdavi et al. 2013

CLUSTERS FOR COSMOLOGY:  
OVERVIEW AND PROGRESS REPORT

# THE HOLY GRAIL OF COSMOLOGY

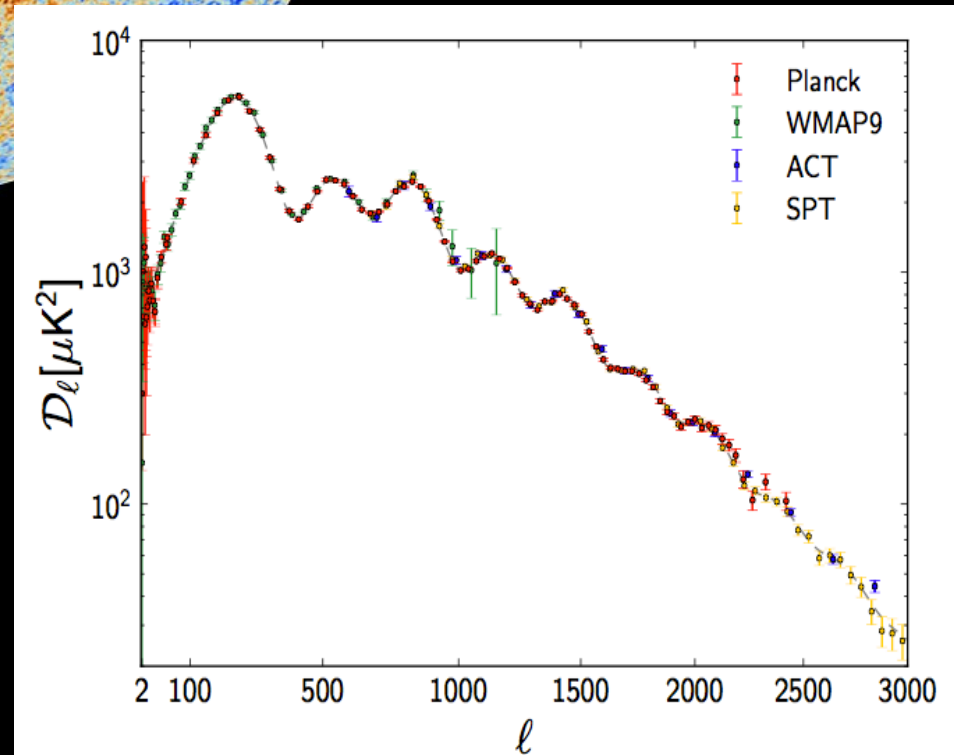
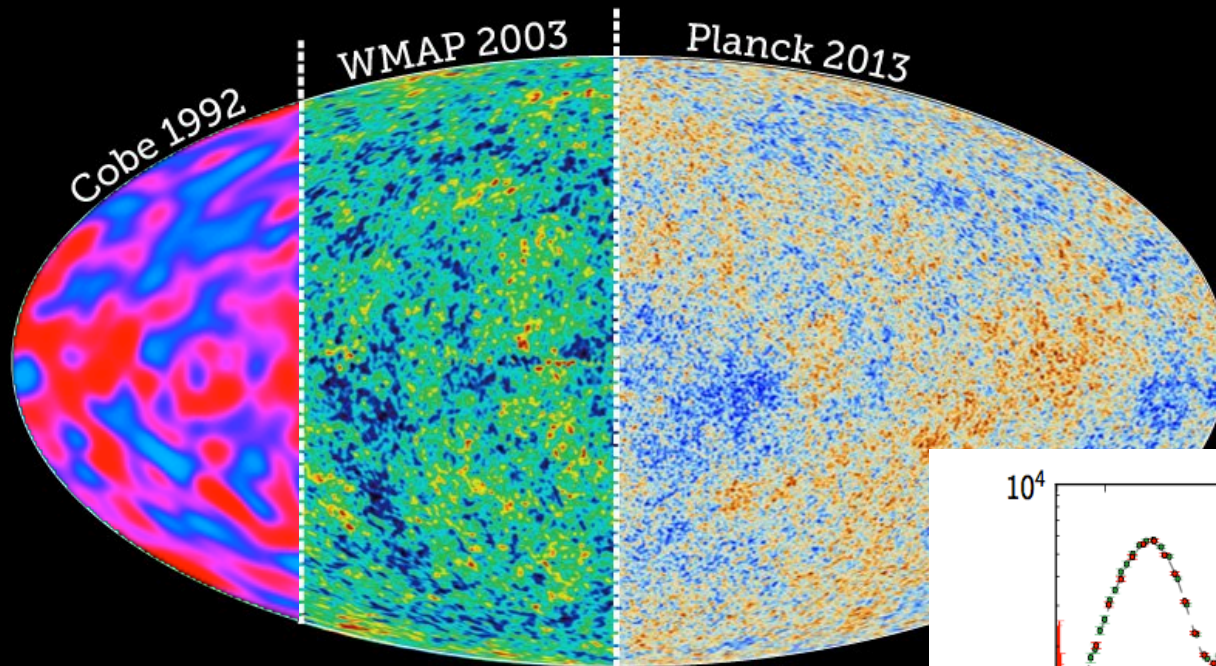
- 
- A magnifying glass is positioned in the lower-left quadrant of the slide. The lens is focused on a cluster of particles, including red spheres, purple spheres, and green rods. The background of the entire slide is a deep space scene filled with numerous galaxies of various shapes and colors, primarily in shades of blue and yellow, set against a black background with scattered stars.
- What is the make-up of the Universe?
  - What is the nature of dark matter?
  - What is the nature of dark energy?
  - What is the present-day cosmic expansion rate?
  - How is the expansion rate evolving?
  - What is the large-scale geometry of space-time?

- How was galaxy formation, and the observed large-scale structure traced by the galaxies, seeded?



$Z < 0.01$

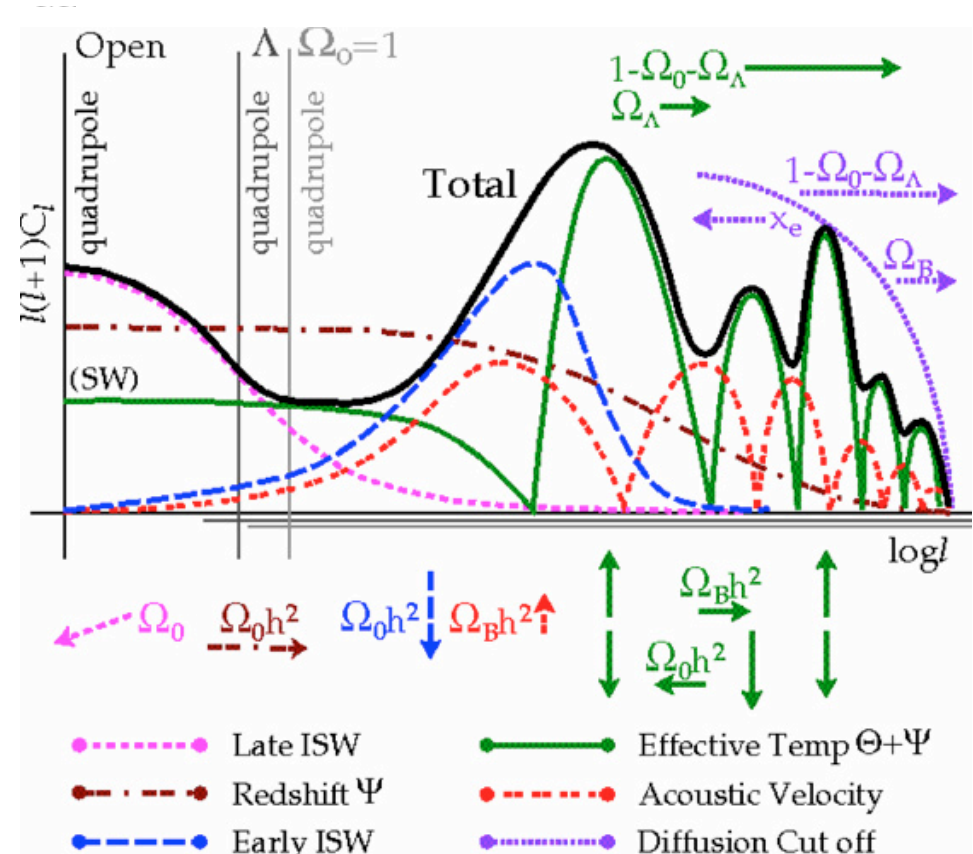
# CMB EXPERIMENTS HERALDED THE AGE OF PRECISION COSMOLOGY



Age of universe	$t_0$
Hubble constant	$H_0$
Baryon density	$\Omega_b$
Physical baryon density	$\Omega_b h^2$
Dark matter density	$\Omega_c$
Physical dark matter density	$\Omega_c h^2$
Dark energy density	$\Omega_\Lambda$
Curvature fluctuation amplitude, $k_0 = 0.002 \text{ Mpc}^{-1}$ <sup>b</sup>	$\Delta_{\mathcal{R}}^2$
Fluctuation amplitude at $8h^{-1} \text{ Mpc}$	$\sigma_8$
$l(l+1)C_{220}^{TT}/2\pi$	$C_{220}$
Scalar spectral index	$n_s$
Redshift of matter-radiation equality	$z_{eq}$
Angular diameter distance to matter-radiation eq. <sup>c</sup>	$d_A(z_{eq})$
Redshift of decoupling	$z_+$
Age at decoupling	$t_+$
Angular diameter distance to decoupling <sup>c,d</sup>	$d_A(z_+)$
Sound horizon at decoupling <sup>d</sup>	$r_s(z_+)$
Acoustic scale at decoupling <sup>d</sup>	$l_A(z_+)$
Reionization optical depth	$\tau$
Redshift of reionization	$z_{reion}$
Age at reionization	$t_{reion}$

Parameters for Extended Models'

Total density <sup>f</sup>	$\Omega_{tot}$
Equation of state <sup>g</sup>	$w_0, w_1$
Tensor to scalar ratio, $k_0 = 0.002 \text{ Mpc}^{-1}$ <sup>b,h</sup>	$r$
Running of spectral index, $k_0 = 0.002 \text{ Mpc}^{-1}$ <sup>b,i</sup>	$dn_s/d \ln k$
Neutrino density <sup>j</sup>	$\Omega_\nu h^2$
Neutrino mass <sup>j</sup>	$\sum m_\nu$
Number of light neutrino families <sup>k</sup>	$N_{eff}$



**Locations and amplitudes of the peaks in the CMB power spectrum depend on values of both astrophysical and cosmological parameters.**

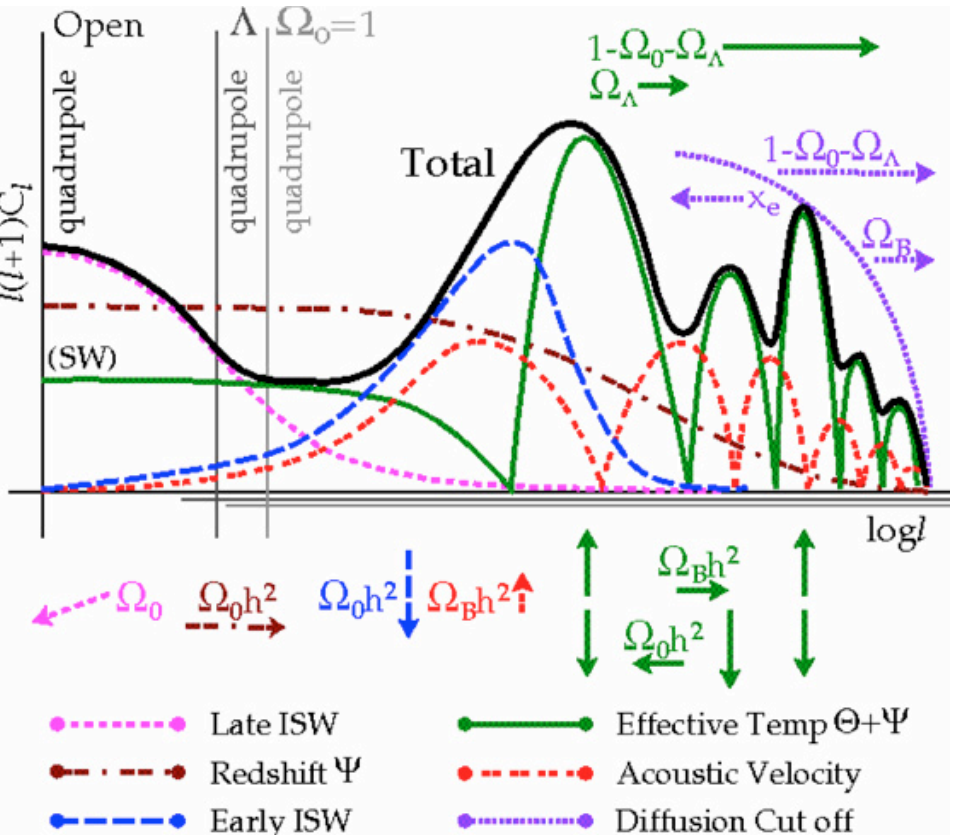
# The Minimal Model

## Just Six Numbers?

Age of universe	$t_0$
Hubble constant	$H_0$
Baryon density	$\Omega_b$
Physical baryon density	$\Omega_b h^2$
Dark matter density	$\Omega_c$
Physical dark matter density	$\Omega_c h^2$
Dark energy density	$\Omega_\Lambda$
Curvature fluctuation amplitude, $k_0 = 0.002 \text{ Mpc}^{-1} \text{ b}$	$\Delta_{\mathcal{R}}^2$
Fluctuation amplitude at $8h^{-1} \text{ Mpc}$	$\sigma_8$
$l(l+1)C_{\mathcal{R}}^{TT}/2\pi$	$C_{\mathcal{R}}^{TT}$
Scalar spectral index	$n_s$
Redshift of matter-radiation equality	$z_{\text{eq}}$
Angular diameter distance to matter-radiation eq. <sup>c</sup>	$d_A(z_{\text{eq}})$
Redshift of decoupling	$z_*$
Age at decoupling	$t_*$
Angular diameter distance to decoupling <sup>c,d</sup>	$d_A(z_*)$
Sound horizon at decoupling <sup>d</sup>	$r_s(z_*)$
Acoustic scale at decoupling <sup>d</sup>	$l_A(z_*)$
Reionization optical depth	$\tau$
Redshift of reionization	$z_{\text{reion}}$
Age at reionization	$t_{\text{reion}}$

Parameters for Extended Models<sup>e</sup>

Total density <sup>f</sup>	$\Omega_{\text{tot}}$
Equation of state <sup>g</sup>	$w_0, w_1$
Tensor to scalar ratio, $k_0 = 0.002 \text{ Mpc}^{-1} \text{ b, h}$	$r$
Running of spectral index, $k_0 = 0.002 \text{ Mpc}^{-1} \text{ b, d}$	$dn_s/d \ln k$
Neutrino density <sup>i</sup>	$\Omega_\nu h^2$
Neutrino mass <sup>j</sup>	$\sum m_\nu$
Number of light neutrino families <sup>k</sup>	$N_{\text{eff}}$



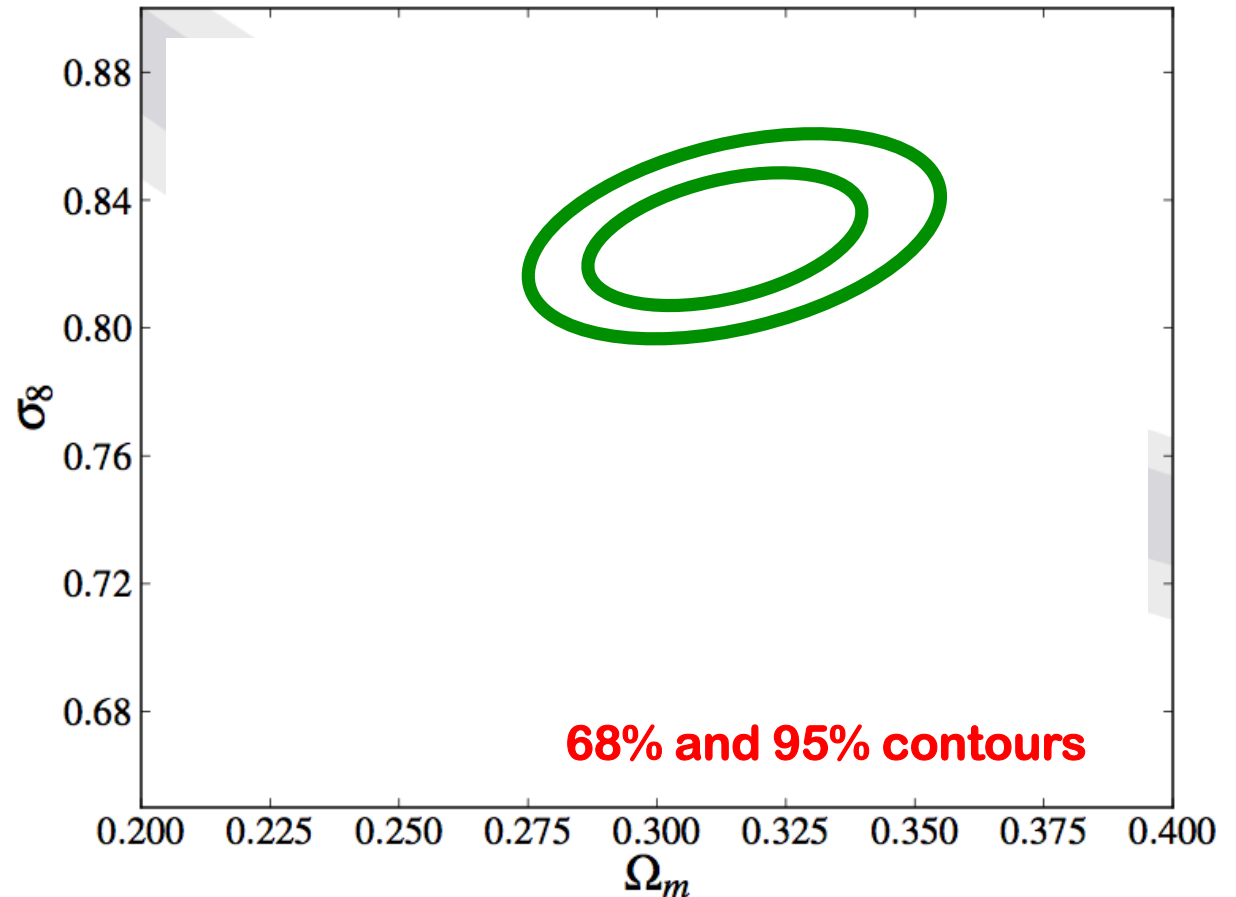
$w_0 = -1$   
 $0$   
 $0.06 \text{ eV}$   
 $3$

# EVEN THEN, THE PARAMETERS ARE DEGENERATE

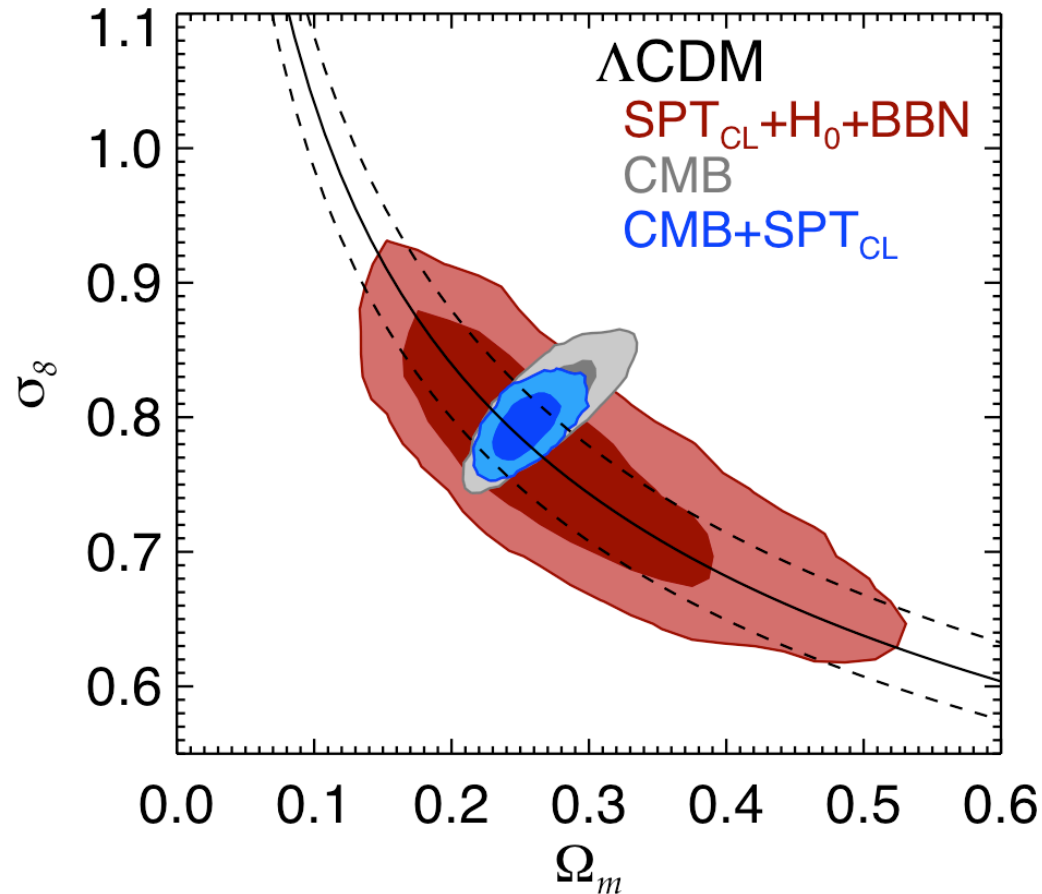
## FOCUS ON THE $\Omega_m - \sigma_8$ PLANE

$$\Omega_m = 0.315 \pm 0.017$$
$$H_0 = 67.3 \pm 1.2$$
$$\sigma_8 = 0.829 \pm 0.012$$

68% confidence Interval



# USE OF COMPLEMENTARY PROBES CAN GREATLY REDUCE UNCERTAINTIES



**CMB MEASURES PARAMETERS AT HI-Z  
CLUSTERS/LSS MEASURE PARAMETERS AT LOW-Z**

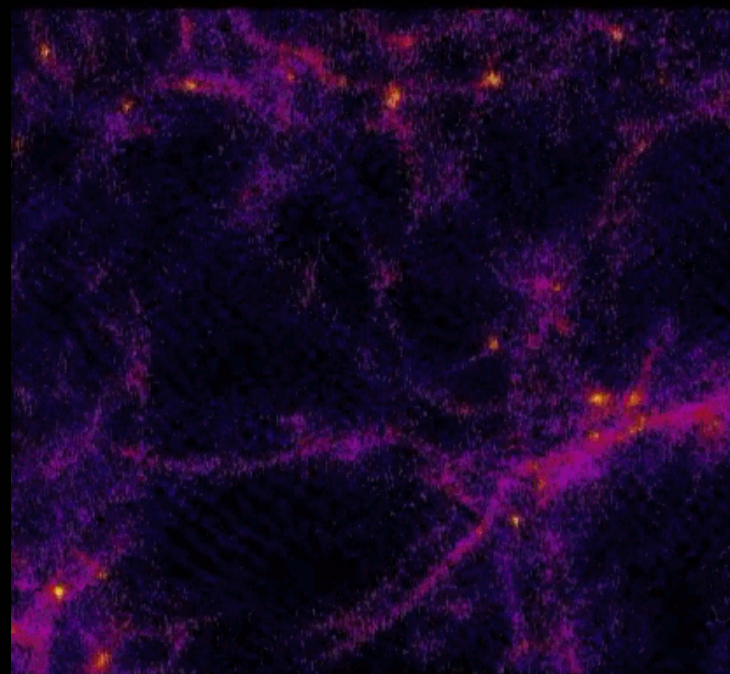
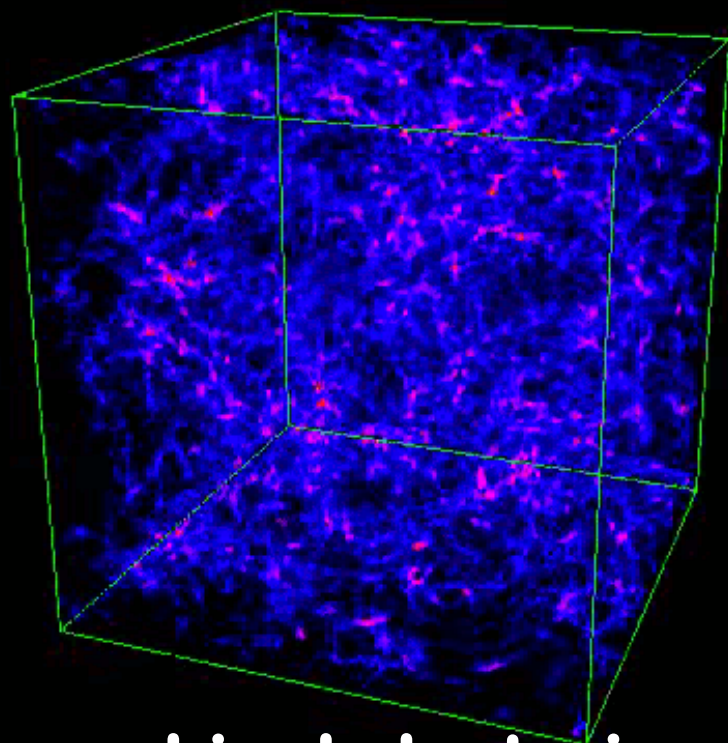


# WHY ARE CLUSTERS USEFUL COSMO PROBES?

Evolution of Structure in a Low Omega Universe

200 Mpc across

Time = 0.95 Gyr



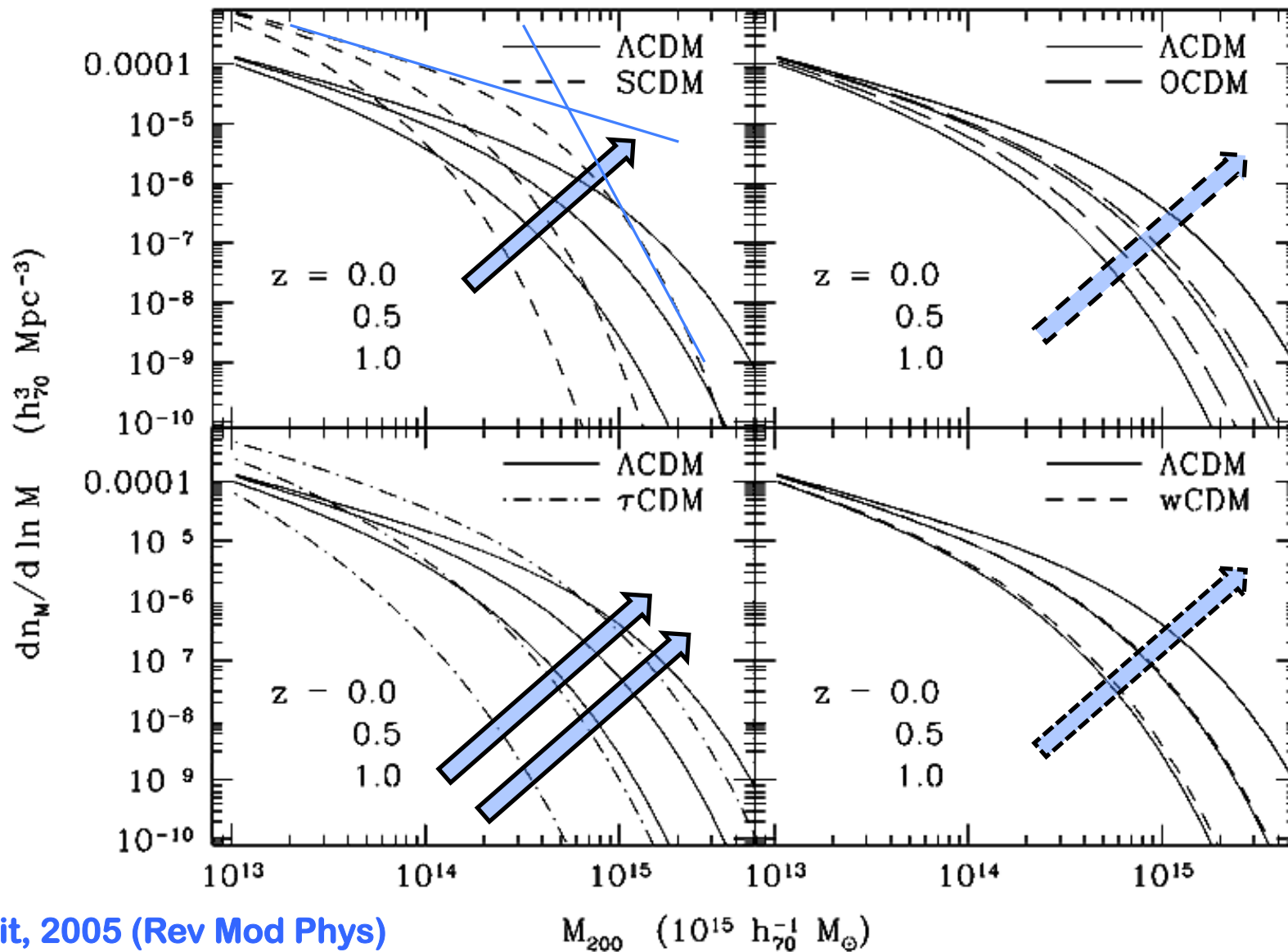
**Hierarchical clustering:**

**Massive structures are built up thru mergers of smaller structures**

**Cluster formation is ongoing.**

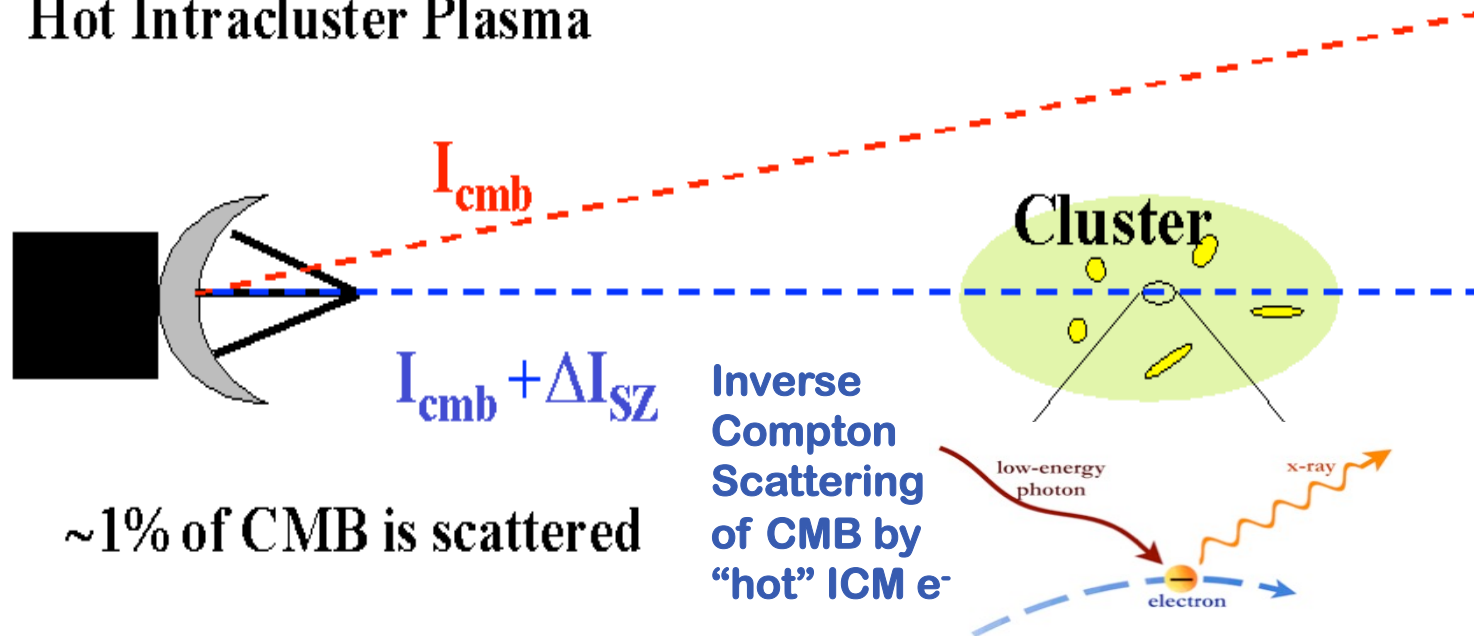
**Rate of assembly depends of cosmology.**

# CLUSTER MASS FUNCTION AND ITS GROWTH IS A PROBE OF RECENT COSMOLOGICAL EVOL.



# CURRENT MICROWAVE EXPERIMENTS THAT STUDY THE CMB CAN ALSO DETECT CLUSTERS VIA SZ EFFECT

Inverse scattering of CMB Photons by Hot Intracluster Plasma



Two Components of the Electron Velocities

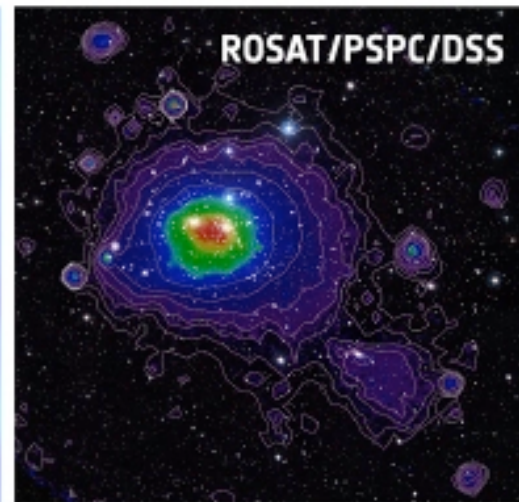
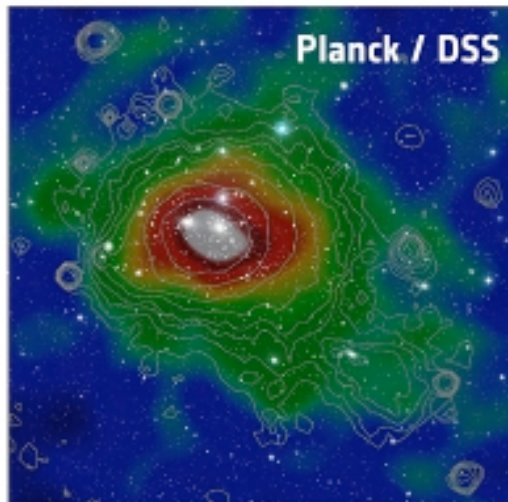
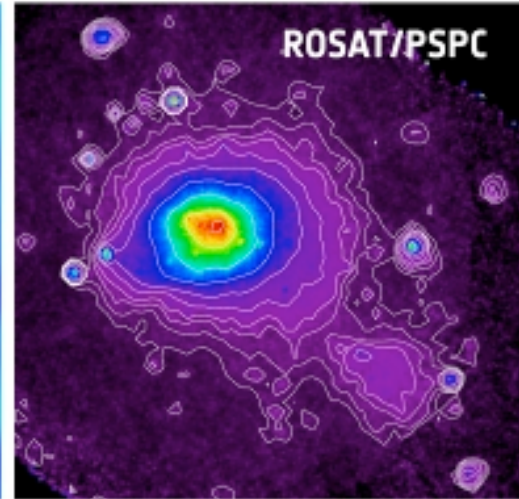
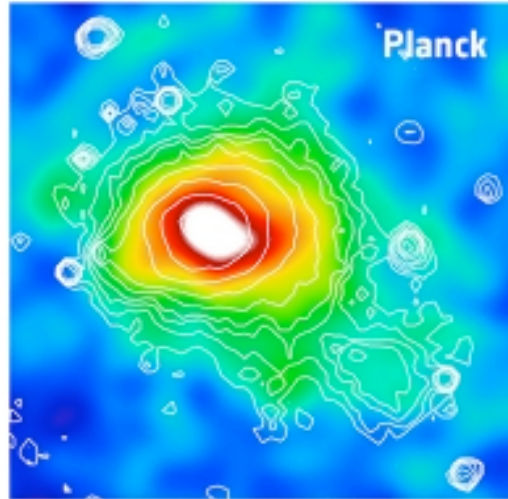
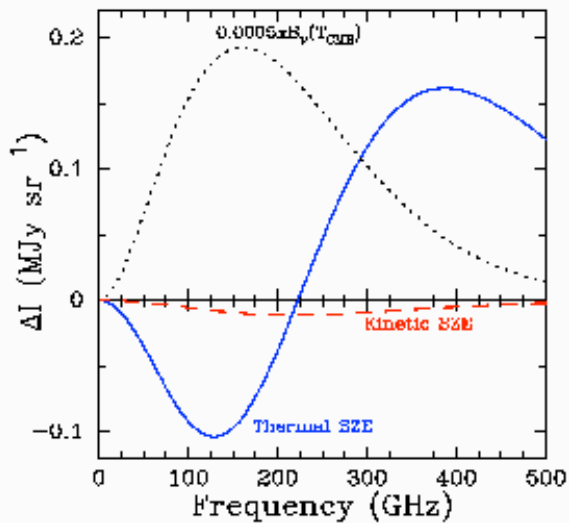
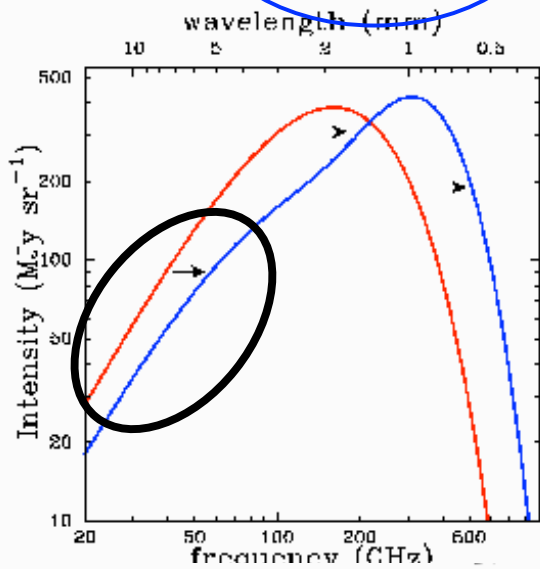
- Thermal ( $T_e \sim 100,000,000$  K)
- Bulk Motion (Doppler Shift)

Produce Two Components of the SZ effect

$z \sim 1100$   $t \sim 300,000$  years

# DETECTING CLUSTERS VIA SZ EFFECT

$$\frac{\Delta T}{T_{\text{CMB}}} = g(\lambda) \int dl n_e(l) \frac{k_B T_e(l)}{m_e c^2} \sigma_T = y \quad (\text{compton } y \text{ parameter})$$



Inverse Compton Scattering of CMB by "hot" ICM e<sup>-</sup>

# FOCUS ON THE $\Omega_m - \sigma_8$ PLANE

Ade et al. 2013: Planck Collaboration XX/XXI

## PRIMARY CMB RESULTS

$$\Omega_m = 0.315 \pm 0.017$$

$$H_0 = 67.3 \pm 1.2$$

$$\sigma_8 = 0.829 \pm 0.012$$

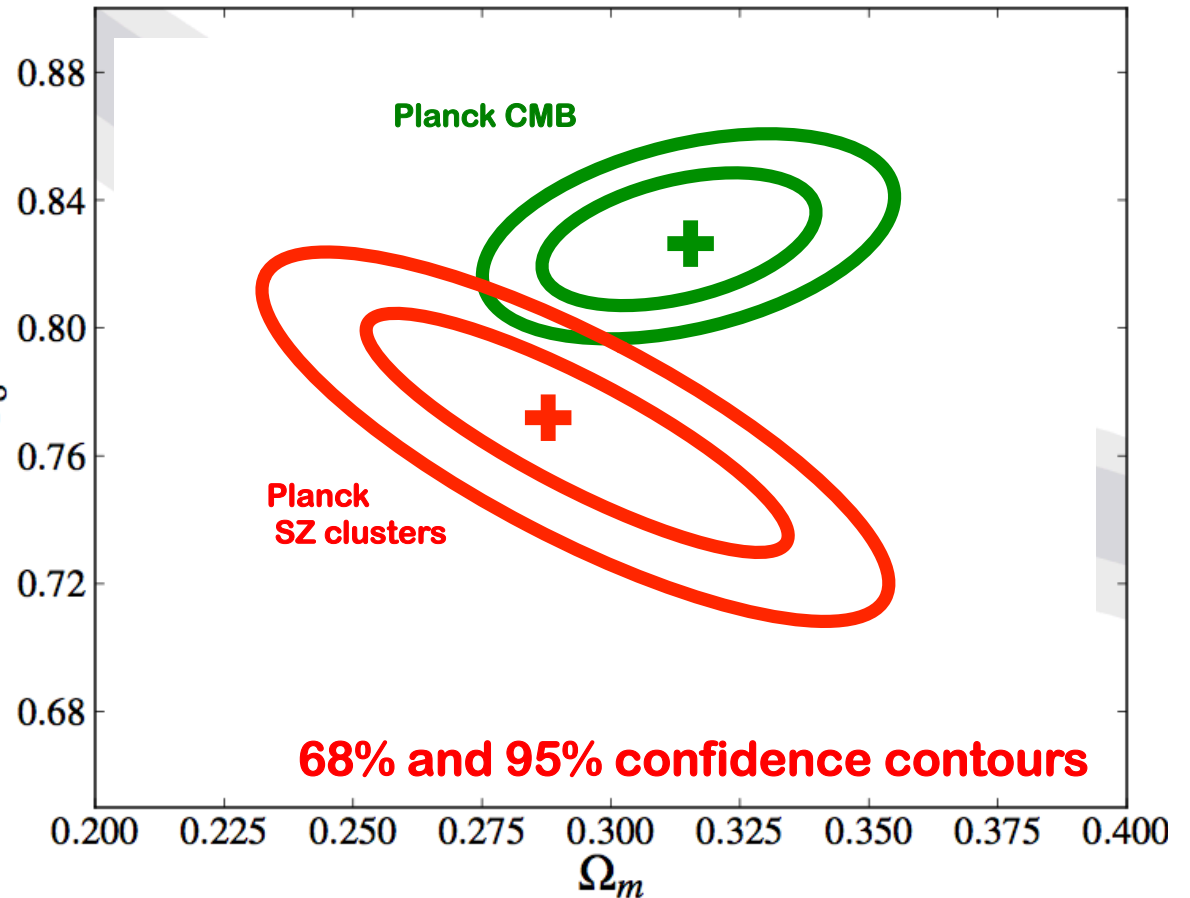
## LOCAL ESTIMATE OF $H_0$

$$H_0 = 73.8 \pm 2.4$$

## From clusters:

$$\Omega_m = 0.29 \pm 0.02$$

$$\sigma_8 = 0.77 \pm 0.012$$



Planck CMB is measuring cosmology at  $t \sim 370,000$  yrs.

Planck Clusters gives cosmology at more recent epoch.

# SO WHAT'S GOING ON?

## ◆ Systematics in the Planck CMB data

Spergel et al. (2014) and others have looked at this.  
Moves CMB results towards Clusters but not enough.

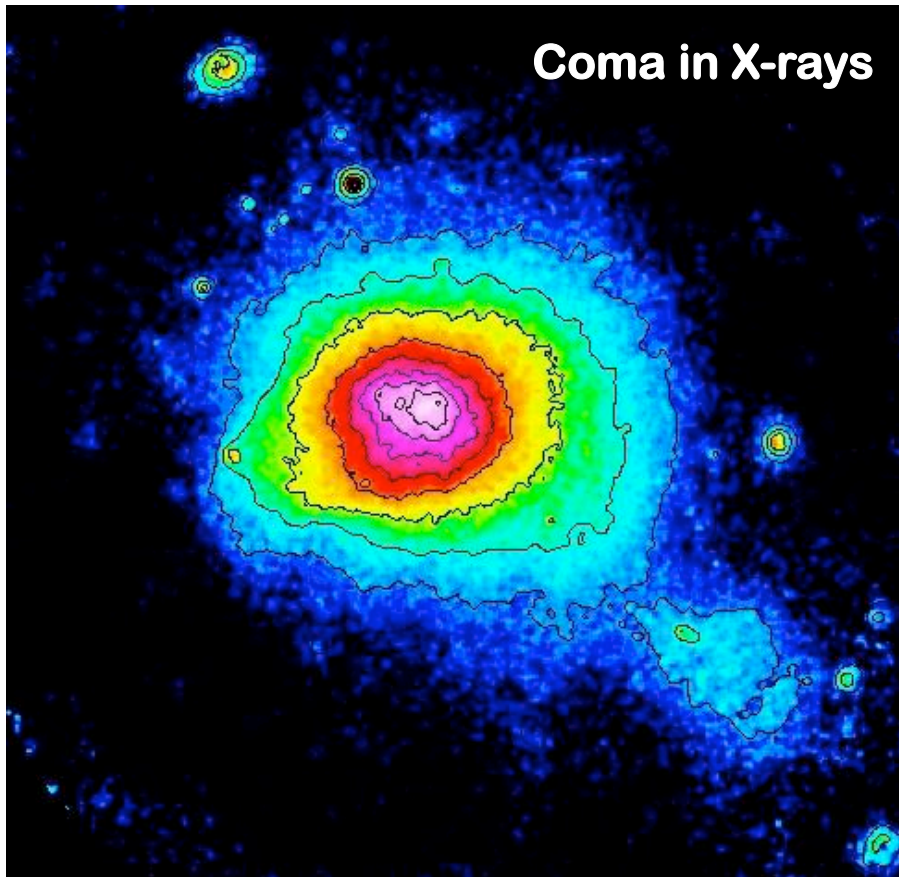
## ◆ Systematics in the Planck SZ Cluster analysis

Focus of CCCP analysis (Remainder of this talk).

## ◆ Failure of the vanilla (six-parameter) model → new physics

Exploits the fact that CMB and Cluster measurements are at different epoch. (Premature in light of above but interesting proposals are circulating.)

# PLANCK SZ CLUSTER ANALYSIS: PREMISED ON MEASURING CLUSTER MASS FUNCTION



CLUSTERS ARE LARGELY DARK mass cannot be easily measured

PLANCK MEASURE  $Y_{sz}$

FOR SUBSET OF CLUSTERS WITH X-RAY DATA, USE X-RAY DATA TO ESTIMATE MASS:  $M_x$

$M_x$  IS A BIASED ESTIMATOR OF TRUE MASS  $M$ :  $M_x = \xi M$

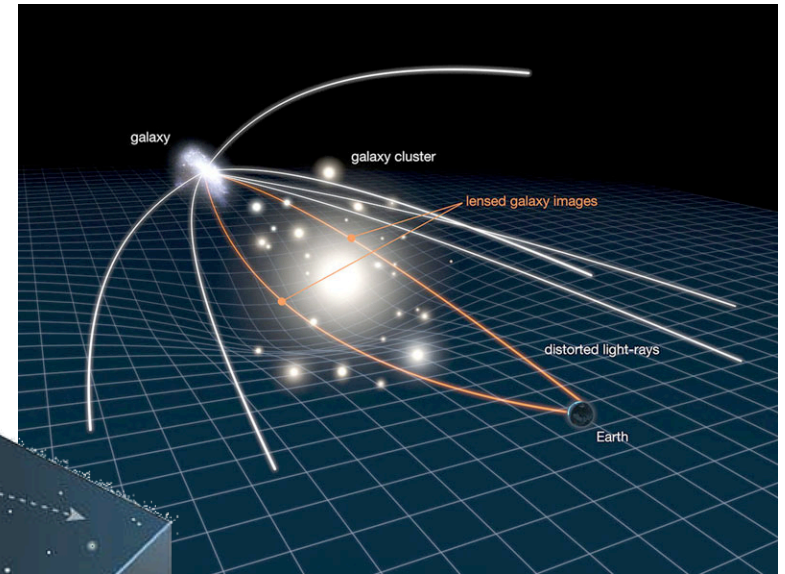
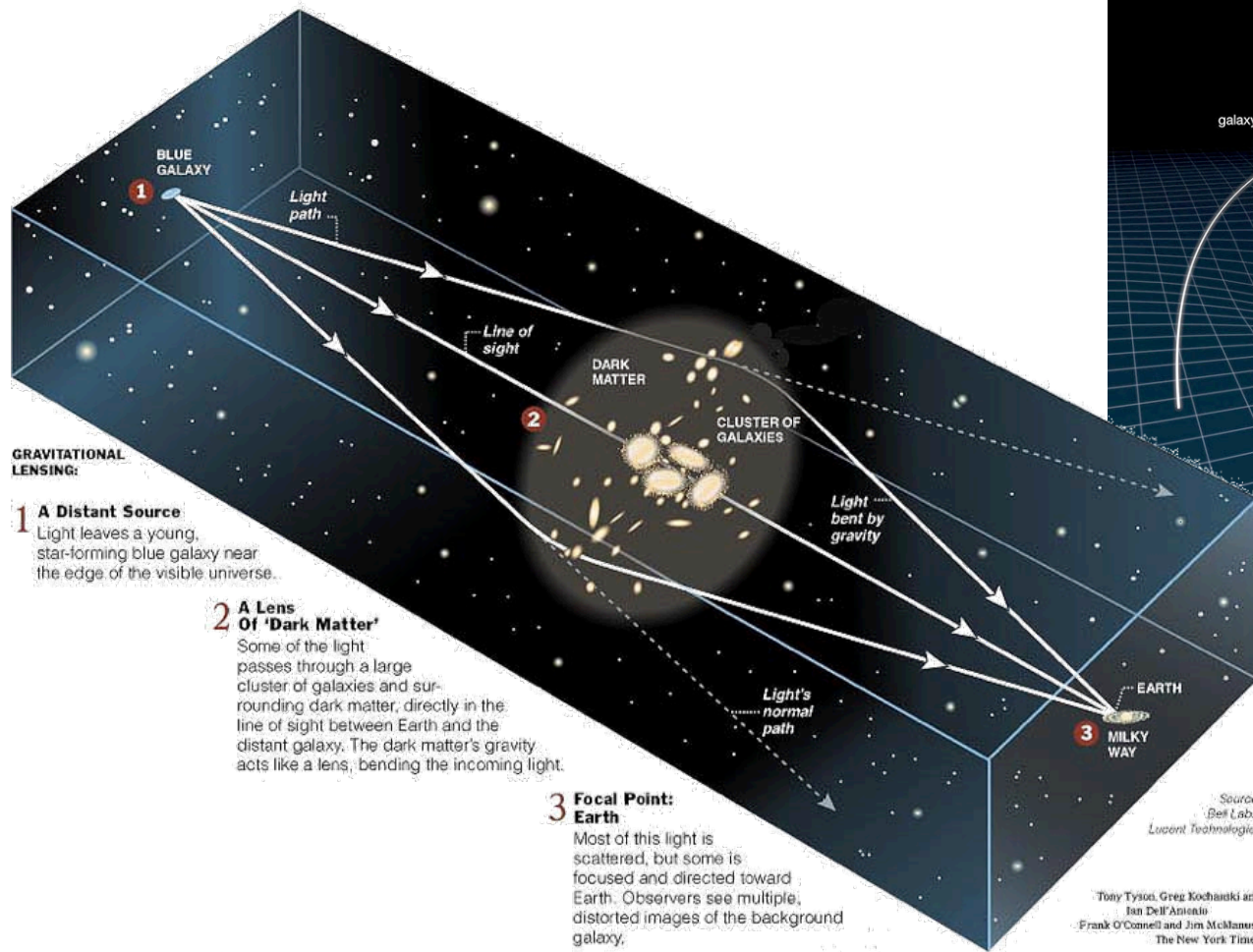
PLANCK:  $\xi = [ 0.7, 1.0 ]$   
 $\langle \xi \rangle = 0.8$

USE RESULTING  $Y_{sz} - M$  TO DERIVE MASSES OF ALL OTHER CLUSTERS (MASS-OBSERVABLE)

HSE: 
$$\frac{dP}{dr} = -\frac{GM(r)\rho(r)}{r^2}$$

IF USE  $\langle \xi \rangle = 0.6$  INSTEAD OF 0.8, THE TENSION IS RESOLVED

# WE CAN EMPIRICALLY ESTABLISH $Y_{sz} - M$ FOR CLUSTERS IN THE NEARBY UNIVERSE – USING WEAK GRAV LENSING!



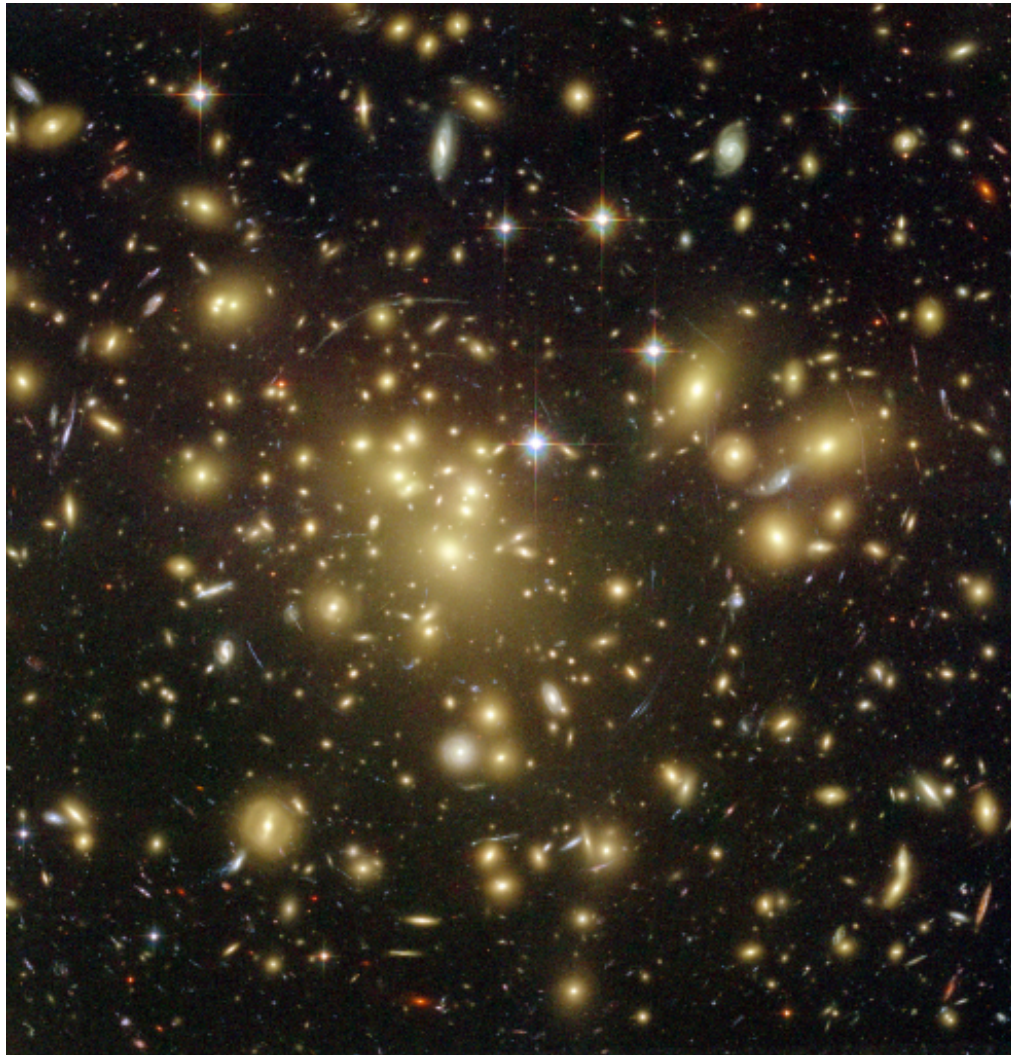
Source:  
Bell Labs,  
Lucent Technologies

Tony Tyson, Greg Kochanski and  
Pat Del'Amico  
Frank O'Connell and Jim McManus  
The New York Times



**Canadian Cluster Comparison Project**  
**it's good for the masses!**

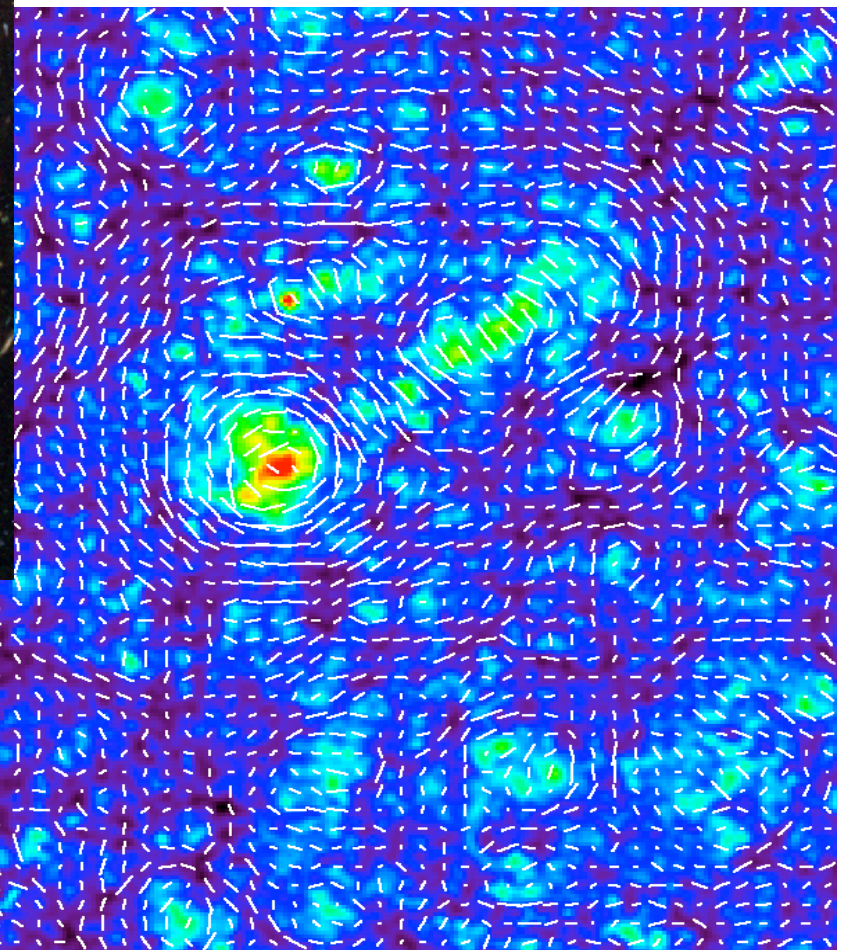




$$\gamma_1 = \frac{1}{2}(\partial_1^2 - \partial_2^2)\psi$$

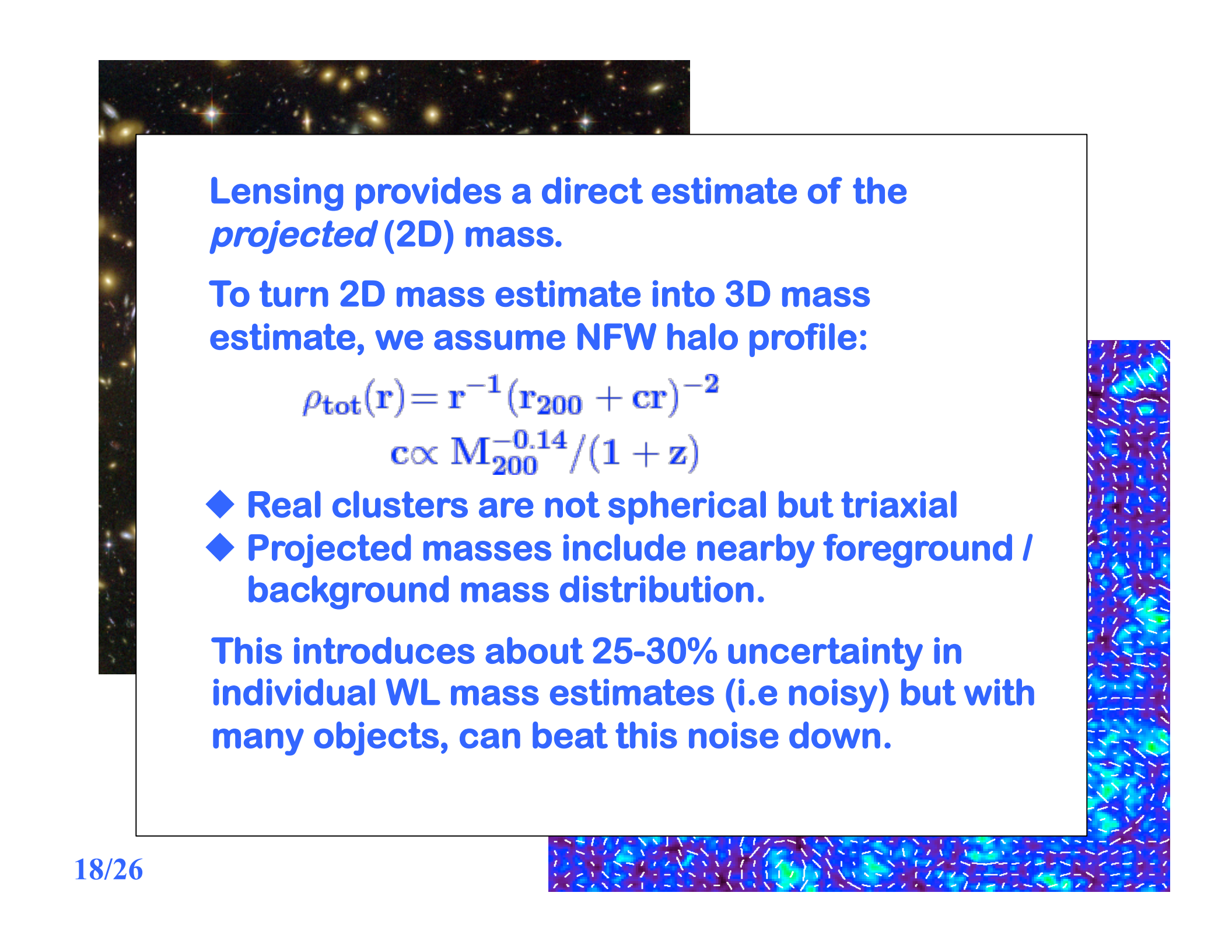
$$\gamma_2 = \partial_1\partial_2\psi,$$

$$\kappa = \frac{1}{2}(\partial_1^2 + \partial_2^2)\psi,$$



$$\kappa(\theta) = \frac{\Sigma(\theta)}{\Sigma_{\text{crit}}},$$

$$\Sigma_{\text{crit}} = \frac{c^2}{4\pi G} \frac{D_{\text{OS}}}{D_{\text{OL}}D_{\text{LS}}},$$



Lensing provides a direct estimate of the *projected* (2D) mass.

To turn 2D mass estimate into 3D mass estimate, we assume NFW halo profile:

$$\rho_{\text{tot}}(\mathbf{r}) = r^{-1} (r_{200} + cr)^{-2}$$
$$c \propto M_{200}^{-0.14} / (1 + z)$$

- ◆ Real clusters are not spherical but triaxial
- ◆ Projected masses include nearby foreground / background mass distribution.

This introduces about 25-30% uncertainty in individual WL mass estimates (i.e noisy) but with many objects, can beat this noise down.

# THEORETICALLY SIMPLE, IN PRACTISE...

## SOURCES OF NOISE:

Random intrinsic shape of galaxies.



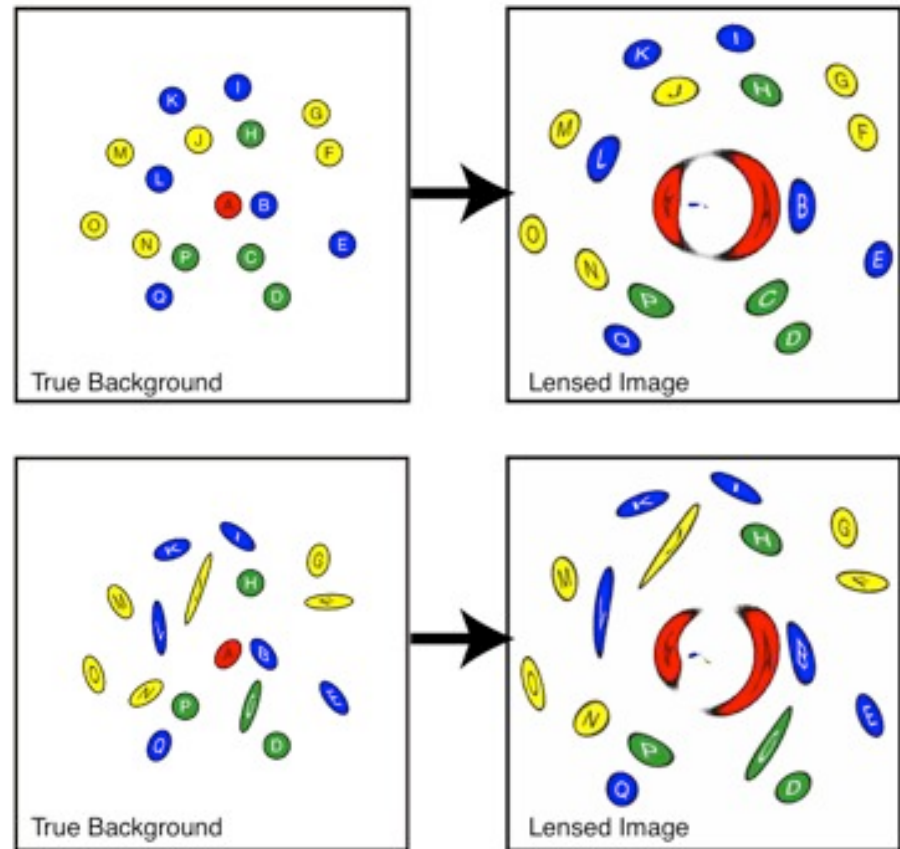
Atmospheric seeing and telescope point spread function

Background noise in the CCD image

Foreground and cluster galaxies

Faint unresolved galaxies

Distance between lens and background galaxies



# UNDERSTANDING SYSTEMATIC OFFSETS:

We have undertaken a thorough analysis of the entire pipeline to understand and quantify different sources of systematic biases:

$$\gamma_i^{\text{obs}} = (1 + \mu) \gamma_i^{\text{true}} + \mathbf{c}$$

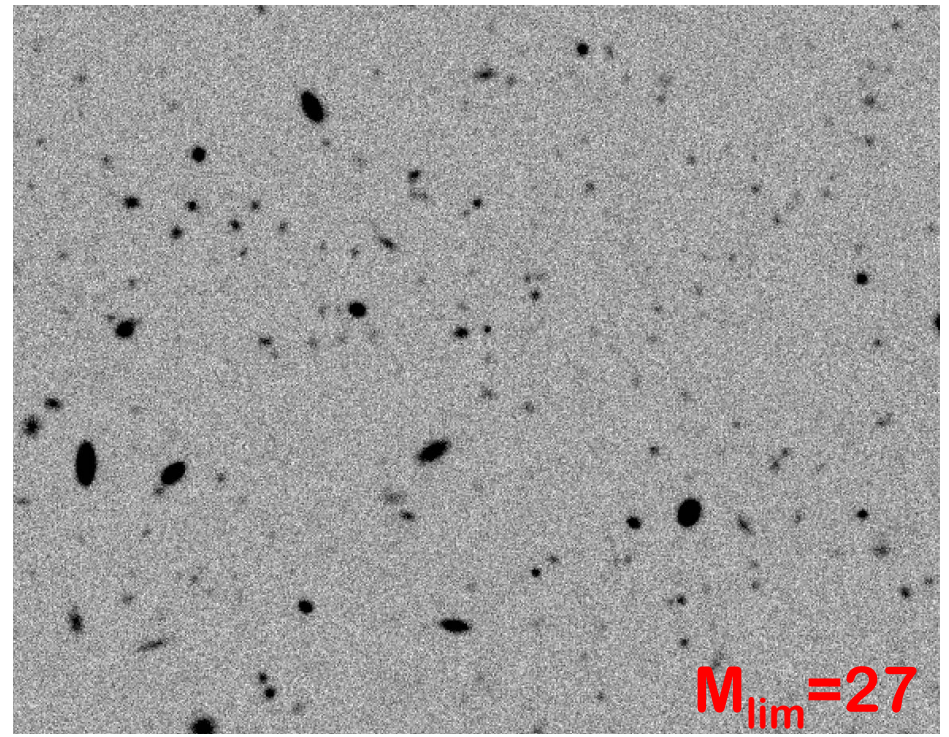
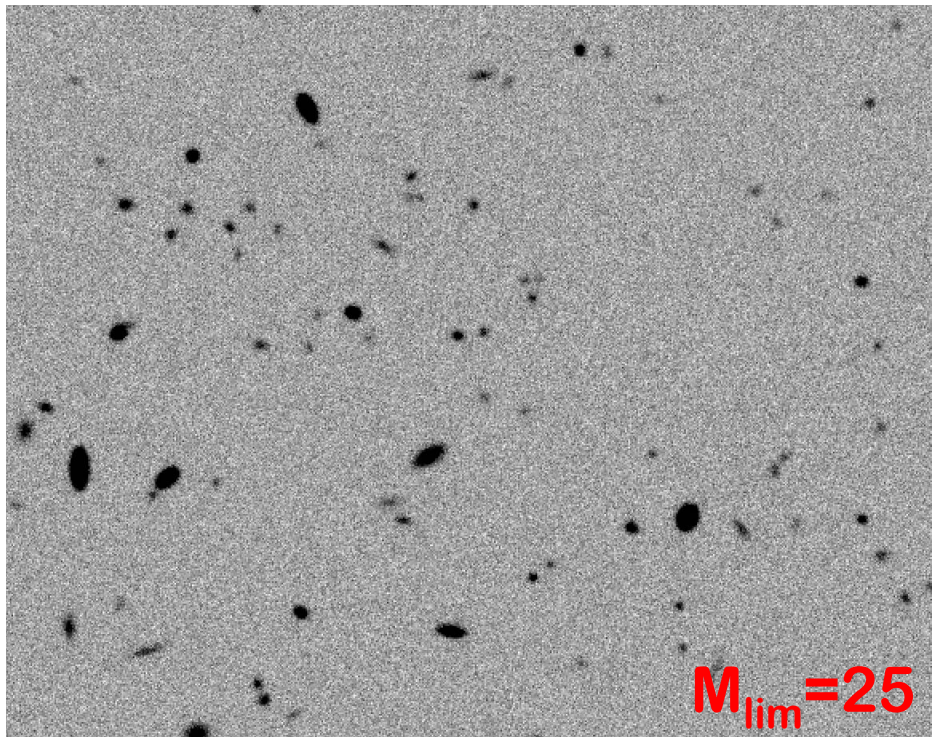
For cluster work:  
not important due  
to azimuthal avrg

- ❖ **Start with an input mock galaxy distribution**
  - correct number counts and redshift distribution
  - appropriate ellipticity distribution (mag dependent)
- ❖ **Apply a known shear due to intervening lens → “truth”**
- ❖ **Create a lensed image; add “appropriate” noise level**
- ❖ **Impose correct PSF – size (seeing) and distortions**
- ❖ **Analyze mock images via identical pipeline/approach**
- ❖ **Compare results to true input to determine multiplicative and additive biases.**

**MOCK IMAGES MUST MATCH OBSERVATIONS IN ALL ASPECTS!**

# FAINT UNRESOLVED GALAXIES

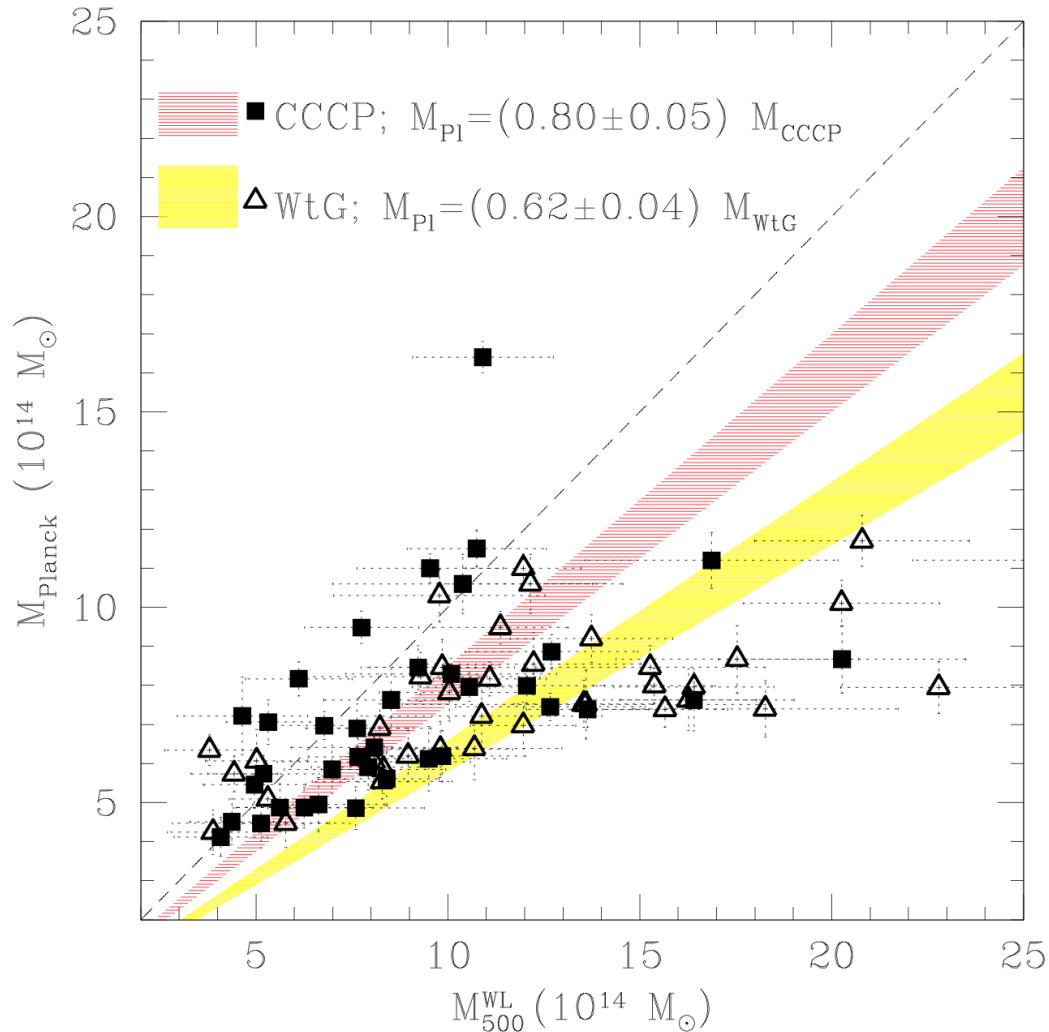
MOCK IMAGE MUST INCLUDE THE POPULATION OF GALAXIES – EVEN IF UNRESOLVED – AT LEAST 1.5 MAGNITUDES FAINTER THAN THE LIMITING MAGNITUDE OF SOURCES USED IN THE LENSING ANALYSIS.



FAINT UNRESOLVED GALAXIES IMPACT SHAPES OF BRIGHTER SOURCE GALAXIES VIA BLENDING AND BY INTRODUCING CORRELATED NOISE IN THE IMAGES.

# AND, COMBINING EVERYTHING TOGETHER...

## WE COMPARE TO PLANCK MASSES

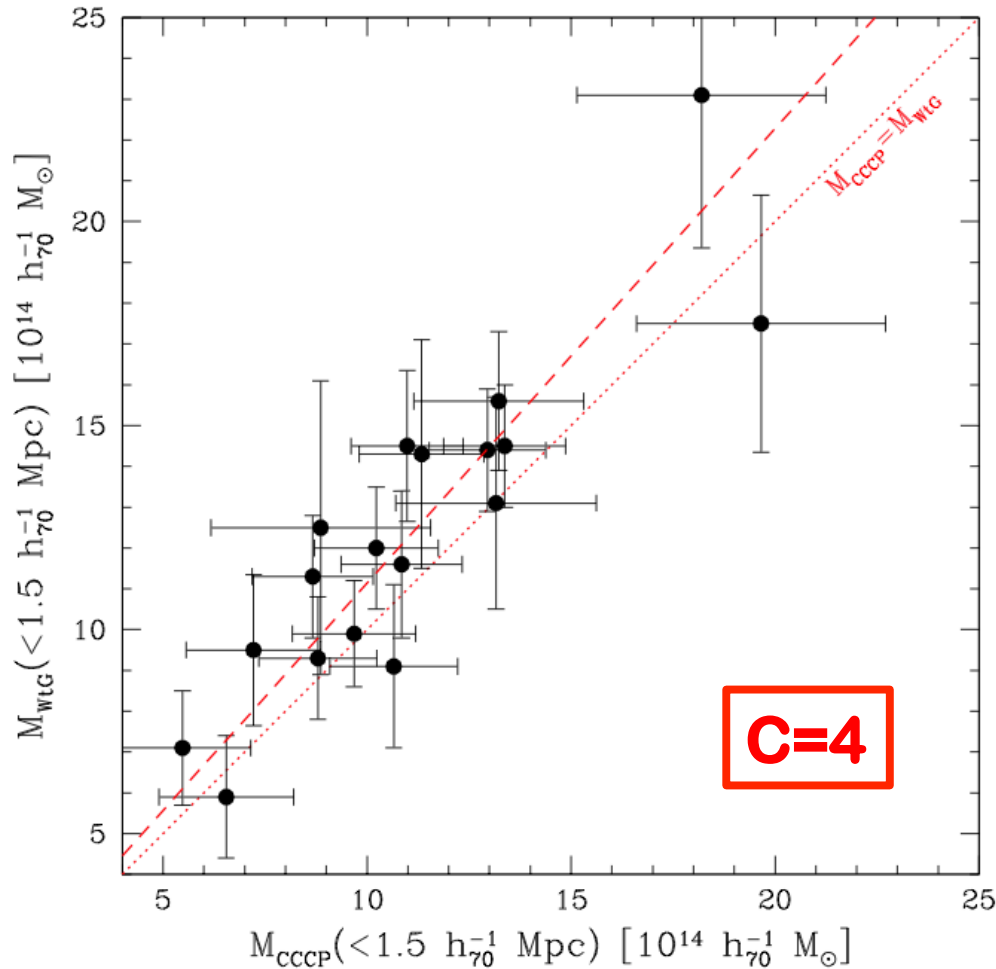


$$\frac{M_{500}^{\text{Planck,Hydro}}}{M_{500}^{\text{WL}}} = \xi = 0.8$$

**THE VALUE OF  $\xi$  WITH CCCP MASSES IS SAME AS THAT ASSUMED IN PLANCK COSMOLOGY ANALYSIS.**

**TENSION BETWEEN PLANCK CLUSTER ANALYSIS AND PLANCK CMB ANALYSIS REMAINS.**

# SO WHAT THEN, NEW PHYSICS?



**EXCITING BUT...**

**ANOTHER GROUP (WtG)  
HAS MEASURED WL MASSES  
AND FIND  $\xi = 0.6$ .**

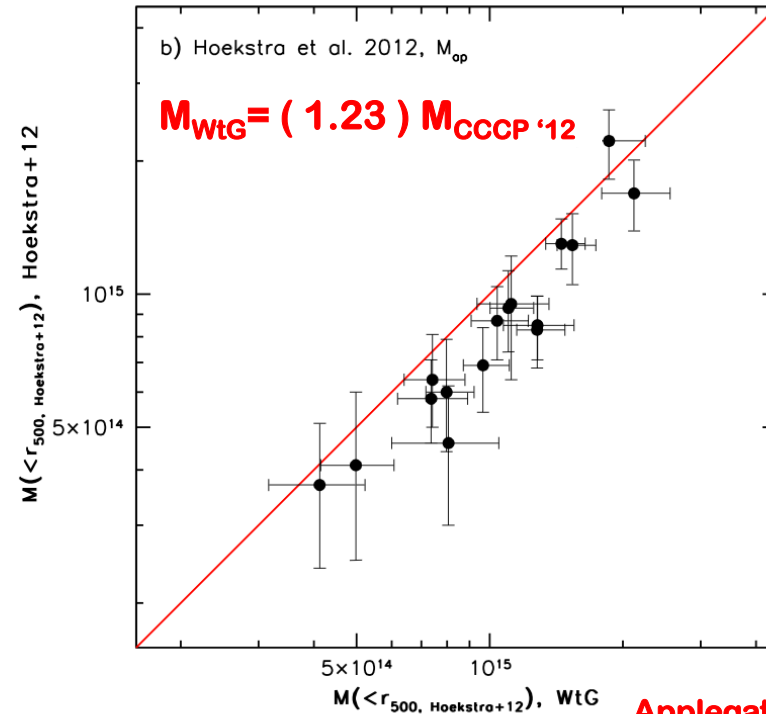
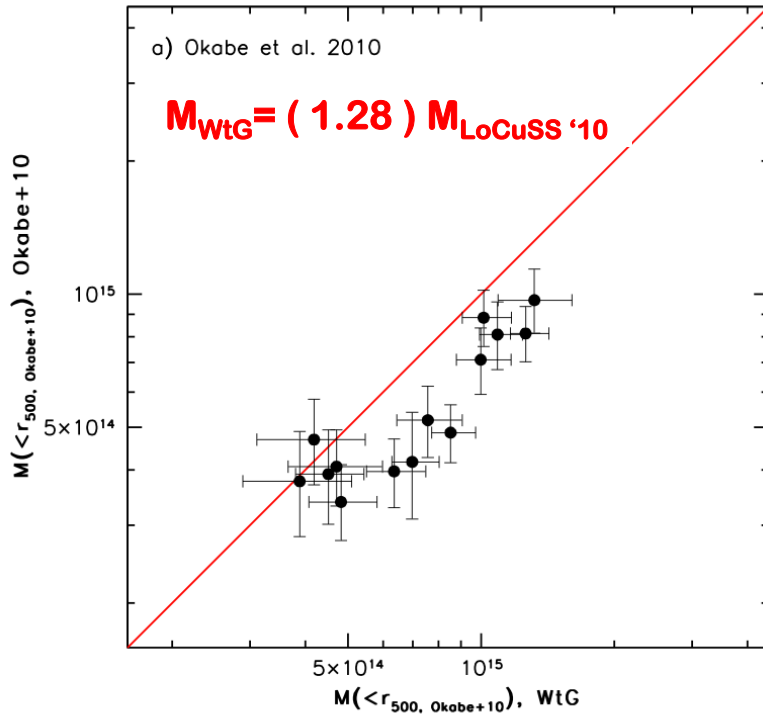
**THIS WOULD RESOLVE THE  
TENSION BWT TWO PLANCK  
COSMOLOGY RESULTS**

**BUT...**

$$M_{\text{WtG}} = (1.11 \pm 0.04) M_{\text{CCCP}} '14$$

← **11% !!!**

AND....



Applegate et al 2014

For the same set of clusters, masses are systematically off by  $\sim 25\%$ ,  $\rightarrow$  bigger than statistical uncertainties

OBSTACLE TO “PRECISION COSMOLOGY WITH CLUSTERS”

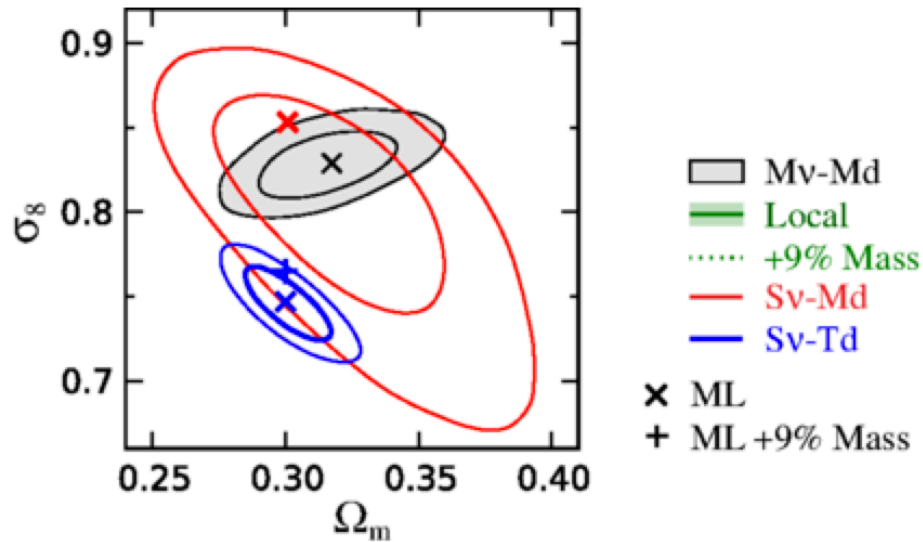


## SUMMARY

- ◆ **Planck CMB and Planck Cluster determinations of  $\Omega_m$  and  $\sigma_8$  are in tension.**
- ◆ **We use weak lensing mass determinations of 50 clusters to test the key assumption underpinning the Planck Clusters analysis.**
- ◆ **We have carried out an extensive analysis of systematic biases of our WL measurement and analysis pipeline.**
- ◆ **At the end of it all, our results support the Planck assumption.**
- ◆ **But another group (WtG) finds that Planck assumption is off by 15% but WtG masses are 10–20% larger than other determinations.**

**OBSTACLE TO “PRECISION COSMOLOGY WITH CLUSTERS”**

# BUT WHAT NEW PHYSICS? food for thought



**TENSION BTW HI-Z &  
LO-Z PARAMETERS  
CAN BE RESOLVED:**

**ONE EXTRA STERILE  $\nu$**

$$\Delta N_{\text{eff}} = 1$$

$$M_s \sim 0.4\text{-}0.8 \text{ eV}$$

