

# Search for Supersymmetry in the three lepton + ETmiss final state

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# Supersymmetry

Supersymmetry (SUSY) is an extension of the Standard Model (SM) of particle physics

→ All SM particles get a "super-partner" which differs by 1/2 unit of spin

SM particles			SUSY particles			
Particle	Name	Spin		Sparticle	Name	Spin
$q$	quarks	1/2		$\tilde{q}$	squarks	0
$l$	leptons	1/2	$Q, Q^\dagger$	$\tilde{l}$	sleptons	0
$W^\pm, W^0$	W-bosons	1	$\iff$	$\tilde{W}^\pm, \tilde{W}^0$	winos	1/2
$B$	B-boson	1		$\tilde{B}$	bino	1/2
$G$	gluons	1		$\tilde{G}$	gluinos	1/2
$H_{1,2}$	Higgses	0		$\tilde{H}_{1,2}$	Higgsinos	1/2

} "Gauginos"

→ Gauginos and higgsinos mix to form physical mass eigenstates:

- Two charged states called charginos:  $\tilde{\chi}_i^\pm$   $i=1,2$
- Four neutral states called neutralinos:  $\tilde{\chi}_j^0$   $j=1,2,3,4$

→ R-parity ( $P_R$ ) conserving models

SUSY particles:  $P_R = -1$   
 SM particles:  $P_R = +1$

- SUSY particles are pair produced
- Lightest Supersymmetric particle (LSP) is absolutely stable

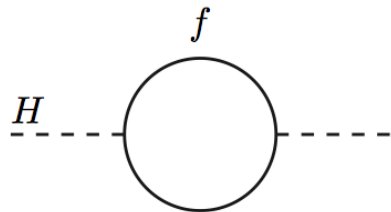
# Why search for Supersymmetry?

Standard model cannot explain the presence of a “dark matter” in the Universe

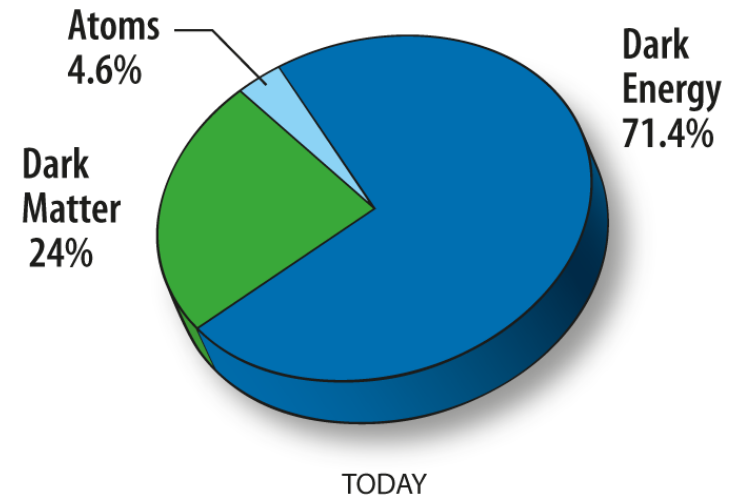
- SUSY can provide a dark matter candidate!

Hierarchy problem of the Standard Model

- Higgs boson receives massive quantum corrections to its mass
- SUSY provides cancellations to these large corrections



$$\Delta m_H^2 = -\frac{|\lambda_f|^2}{8\pi^2} \Lambda_{UV}^2 + \dots$$



Standard model put to rigorous tests in the absence of a signal

- SUSY searches typically probe the tails of distributions where the most rare Standard model events occur
- “Yesterday discovery is today's background”

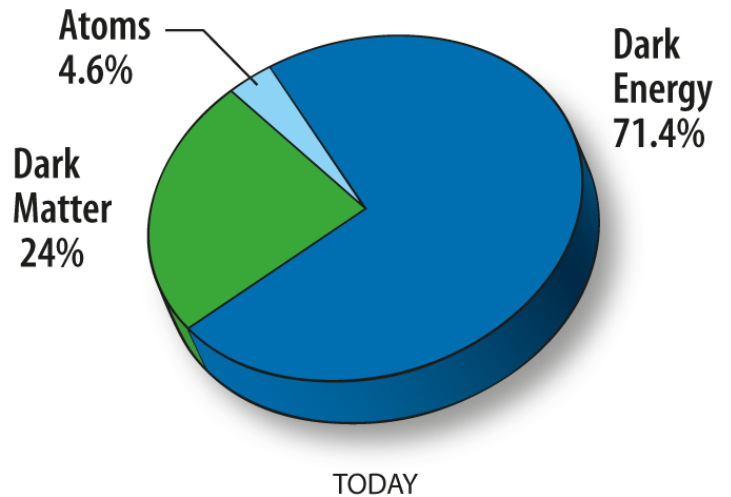
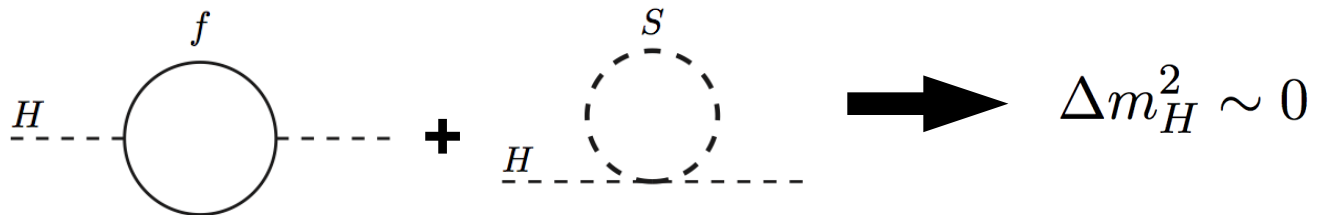
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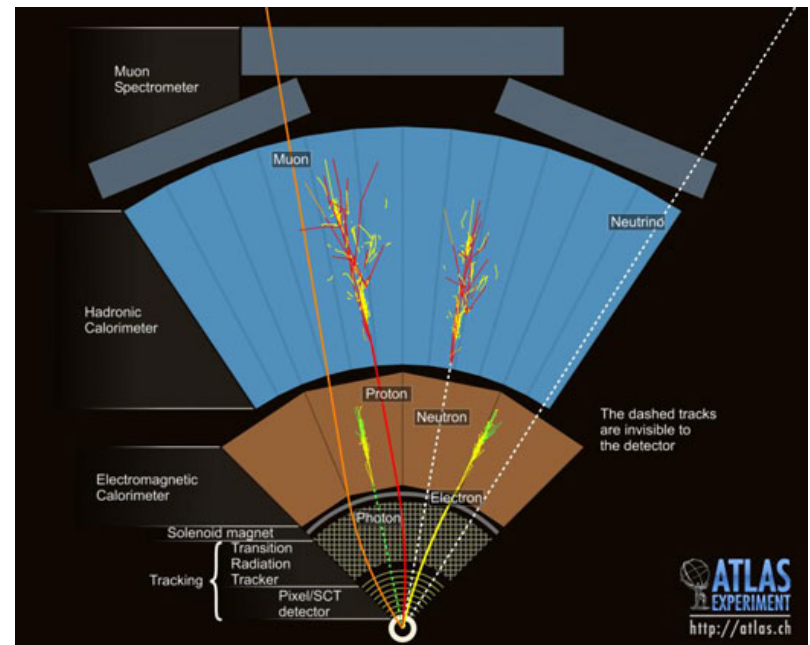
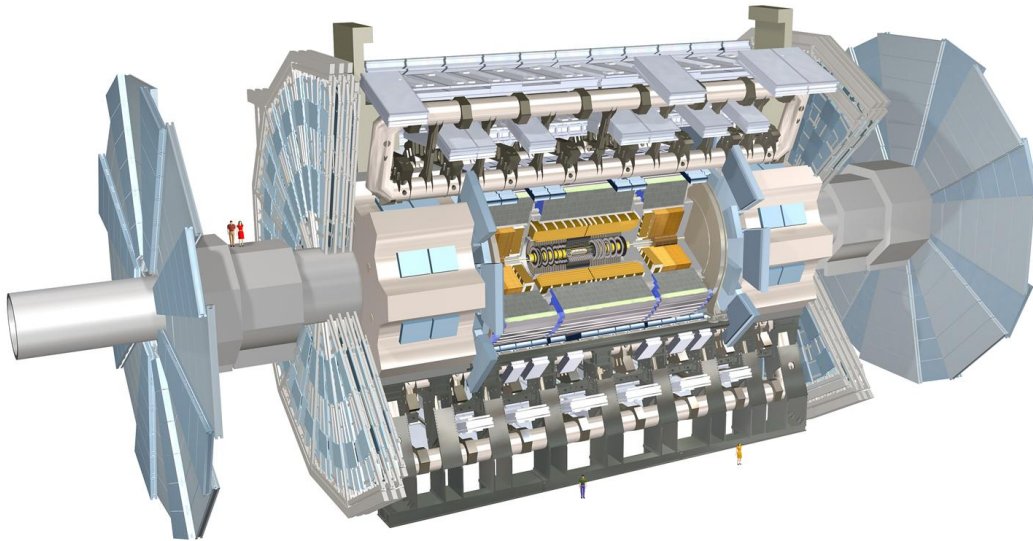
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- “Yesterday discovery is today's background”

# ATLAS Detector

ATLAS is a general purpose physics detector at the LHC

- Electrons and muons reconstructed using information from tracking, calorimeter, and muon systems
- Hadronically decaying taus identified using multi-variate techniques
- b-hadrons give displaced tracks and identified using neutral network algorithms
- Particles which don't interact with the detector contribute to missing transverse momentum

$$E_T^{miss} = - \sum_i^{N_{obj}} \vec{p}_T^i$$

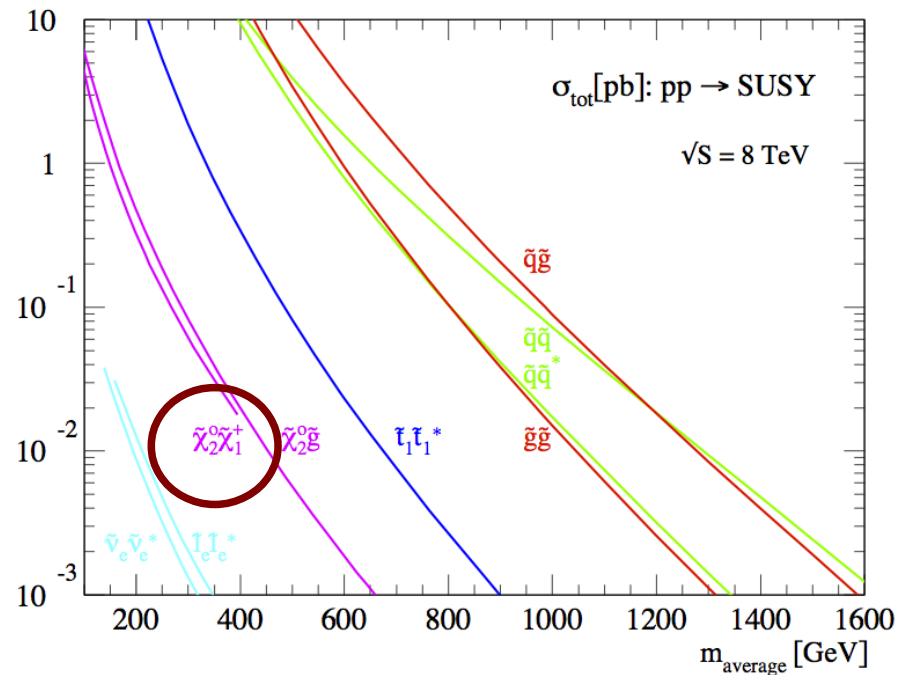
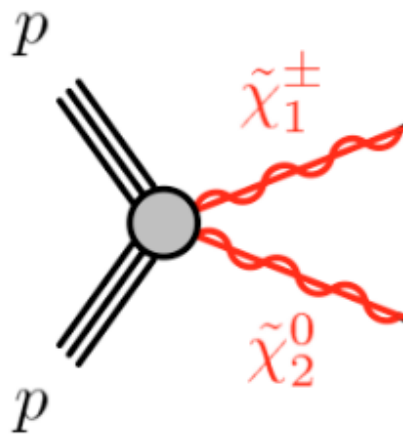


# Electroweak SUSY production

Electroweak (EWK) production of charginos and neutralinos attractive signature

- Naturalness requires light higgsinos  $\Rightarrow$  could be accessible at the LHC
- EWK production is dominant if squarks and gluinos are heavy
- Large lepton multiplicity  $\Rightarrow$  clean final state at the LHC
- Full 2012 data set used, corresponding to  $20.3 \text{ fb}^{-1} \Rightarrow$  sensitive to rare processes

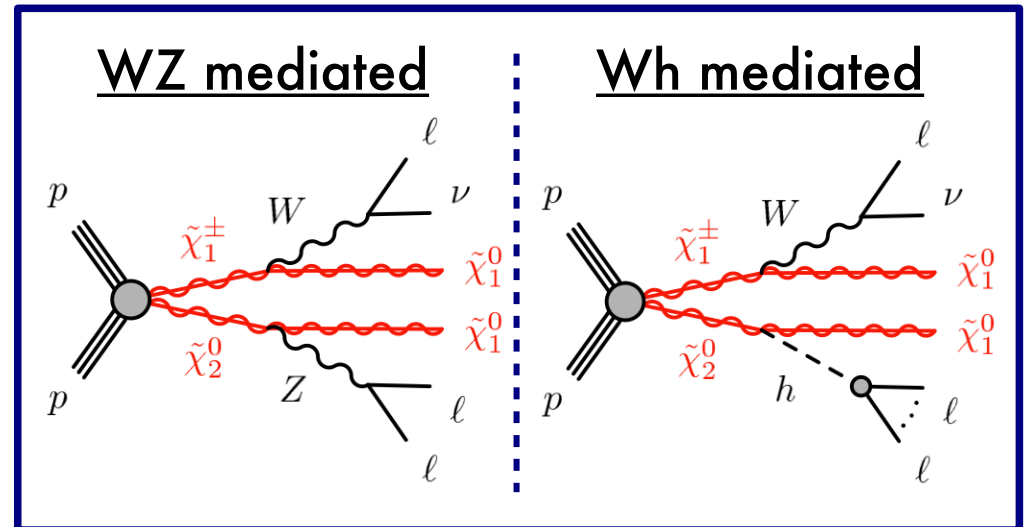
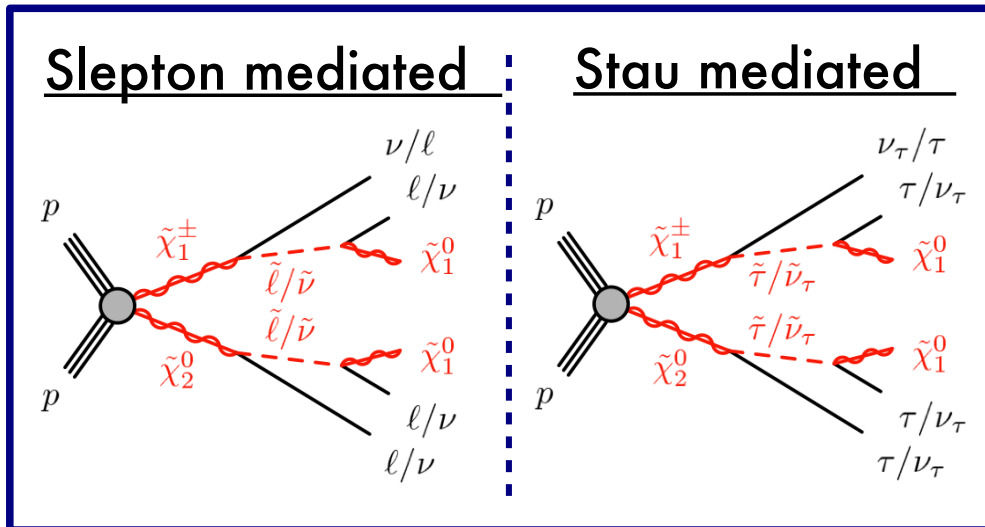
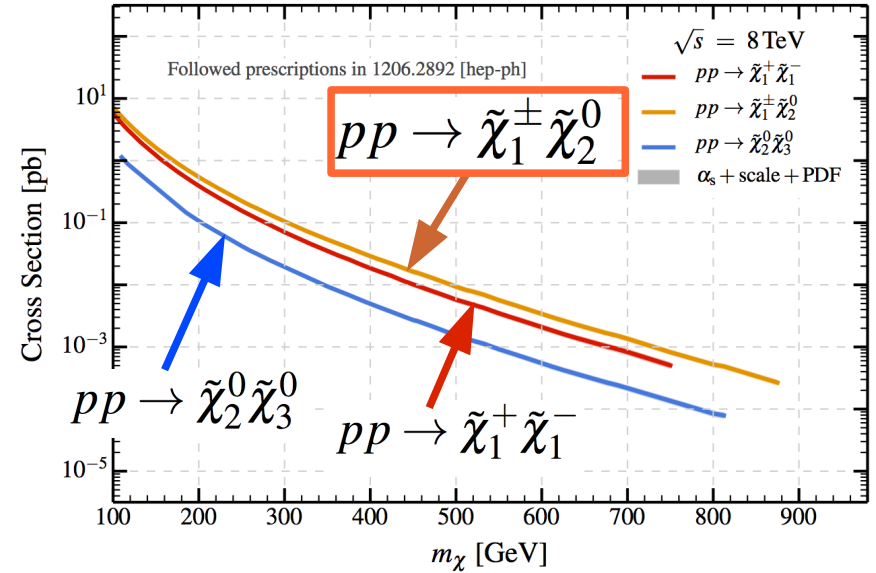
Direct production of lowest accessible neutralino and chargino mass eigenstates



# Electroweak SUSY sector

Direct production of  $\tilde{\chi}_1^\pm$  and  $\tilde{\chi}_2^0$  has the largest production cross section

- Decay can proceed through sleptons and/or bosons
- W,Z and h assumed to have Standard Model branching ratios



# Beyond the Standard Model search strategy

1) Identify regions of the phase space which are statistically sensitive to the observation of SUSY

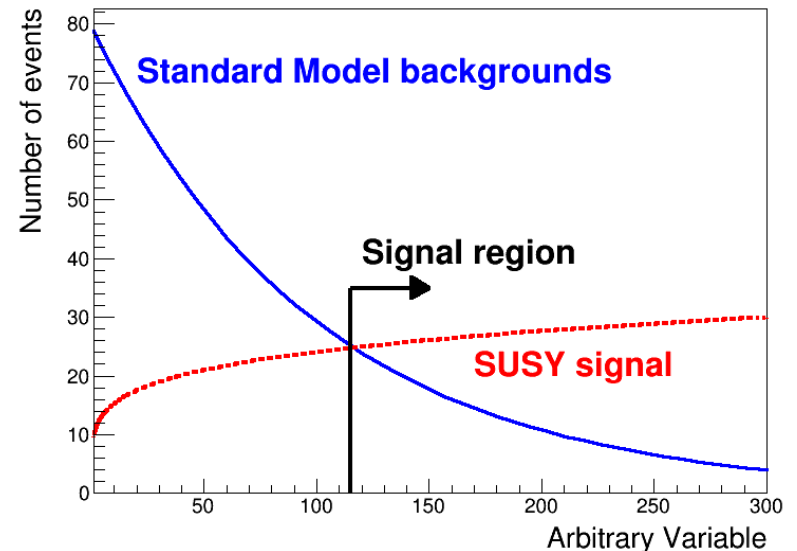
- These regions are called 'signal regions'
- They remain blind for the duration of the analysis

2) Estimate and validate Standard Model backgrounds

- Monte Carlo simulations and/or data driven techniques are typically used

3) Unblind signal regions

- In the absence of an excess, set limits in particular SUSY models



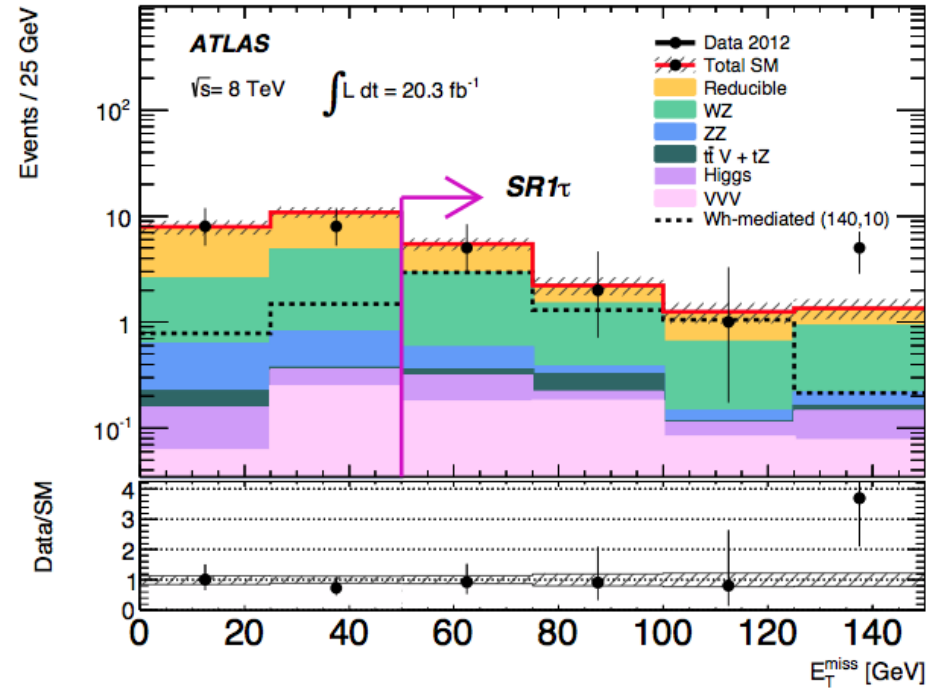


# Signal region selection

Signal regions are classified depending on the tau multiplicity

→ Electron and muon only signal regions binned in:

- Missing energy
- Invariant mass of di-leptons
- Transverse mass of the lepton and missing energy



All signal regions veto b-quarks  $\Rightarrow$  common in dominant background processes

Total of 24 almost statistically independent signal regions

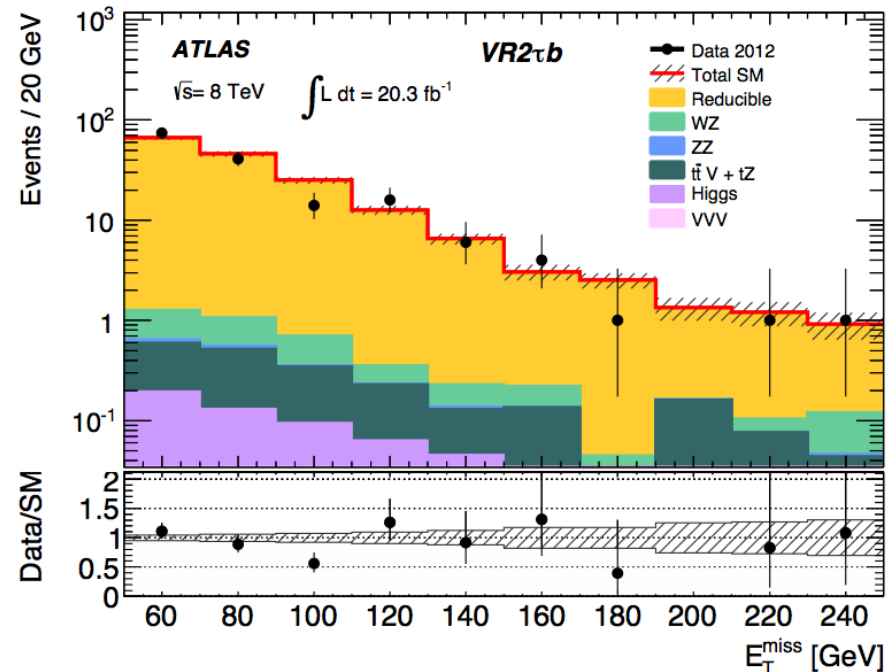
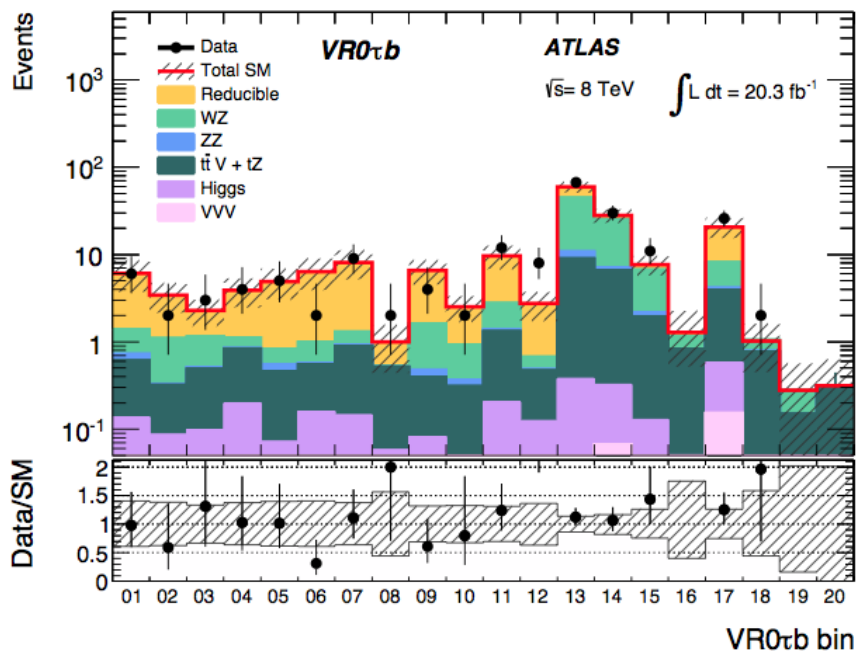
$$m_T = \sqrt{2p_T^\ell E_T^{\text{miss}} (1 - \cos(\Delta\phi(\ell, E_T^{\text{miss}}))}$$

# Validation regions

Validation regions used to verify background modelling and variable shapes

- Kinematically close to the signal regions
- Target dominant backgrounds
- Small signal contamination

Good agreement observed in all validation regions

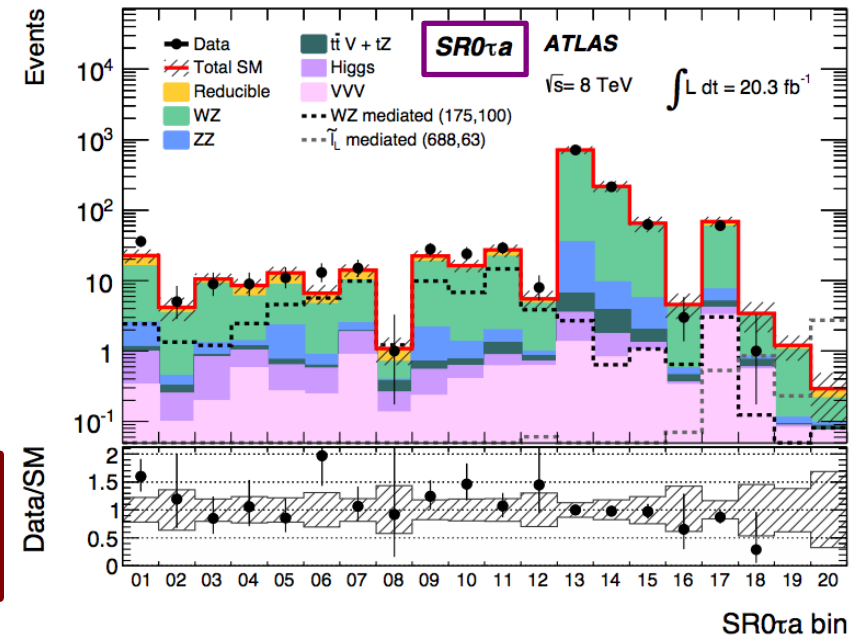


# Unblinded signal regions

Good agreement seen in all validation regions, proceed to unblind signal regions

→ Observations are consistent with Standard Model expectations

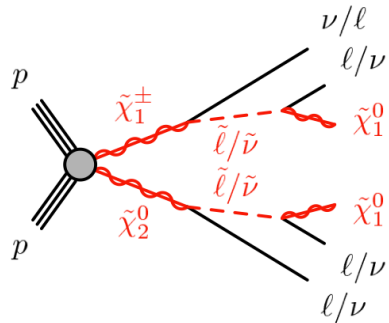
Sample	SR0 $\tau$ b	SR1 $\tau$	SR2 $\tau$ a	SR2 $\tau$ b
<i>WZ</i>	$0.68 \pm 0.20$	$4.6 \pm 0.6$	$1.51^{+0.35}_{-0.33}$	$2.09^{+0.30}_{-0.31}$
<i>ZZ</i>	$0.028 \pm 0.009$	$0.36 \pm 0.08$	$0.049^{+0.016}_{-0.014}$	$0.135 \pm 0.025$
<i>t<math>\bar{t}</math>V + tZ</i>	$0.17^{+0.32}_{-0.17}$	$0.16^{+0.18}_{-0.16}$	$0.21^{+0.27}_{-0.21}$	$0.023^{+0.015}_{-0.018}$
<i>VVV</i>	$1.0 \pm 1.0$	$0.5 \pm 0.5$	$0.09 \pm 0.09$	$0.031 \pm 0.033$
Higgs	$0.49 \pm 0.17$	$0.28 \pm 0.12$	$0.021 \pm 0.010$	$0.08 \pm 0.04$
Reducible	$1.5 \pm 0.4$	$4.3 \pm 0.8$	$5.1 \pm 0.7$	$4.9 \pm 0.7$
Total SM	$3.8 \pm 1.2$	$10.3 \pm 1.2$	$6.9 \pm 0.8$	$7.2^{+0.7}_{-0.8}$
Data	3	13	6	5



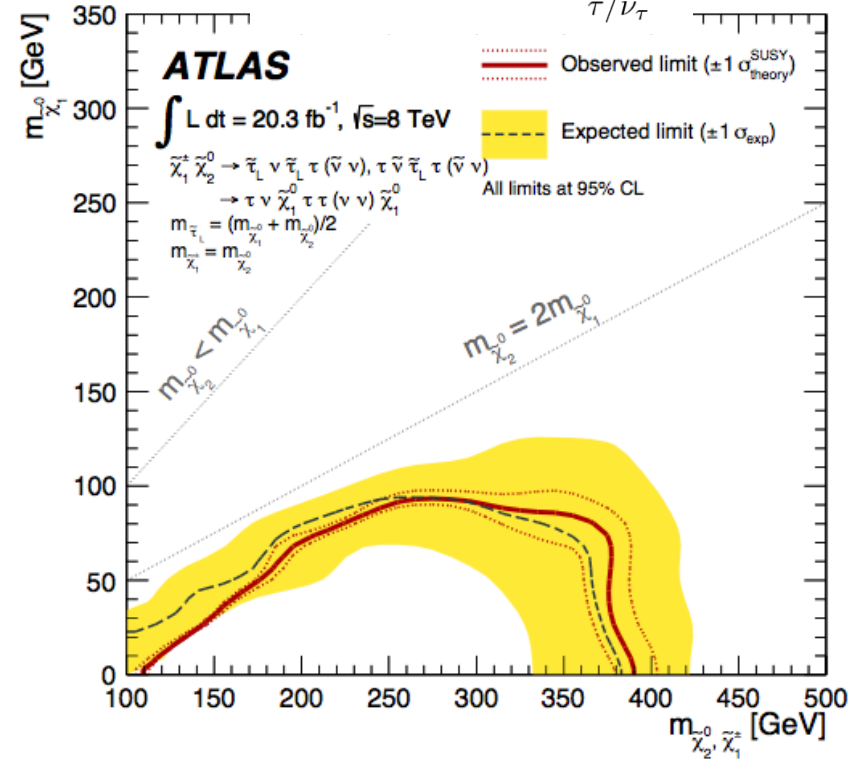
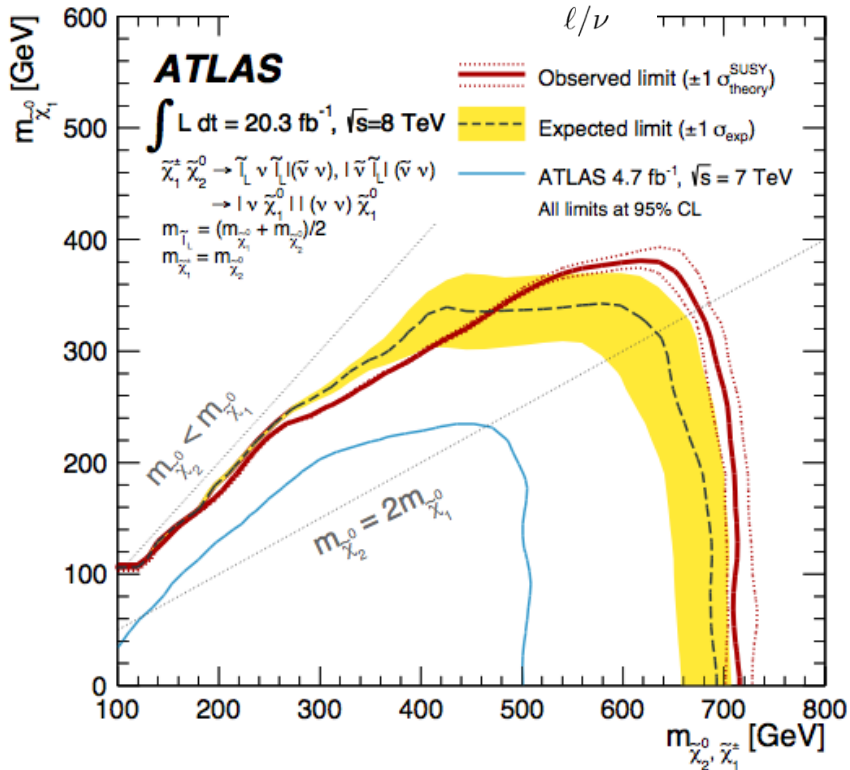
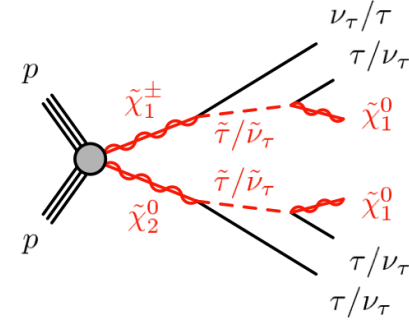
# Interpretation in SUSY simplified models

Limits set at 95% CL for chargino and neutralino production

## Decay via sleptons



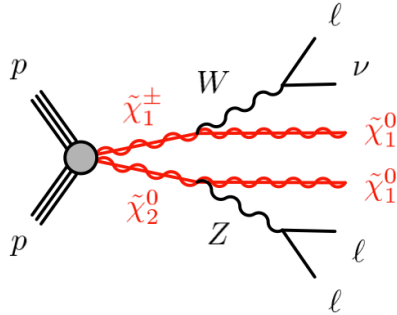
## Decay via staus



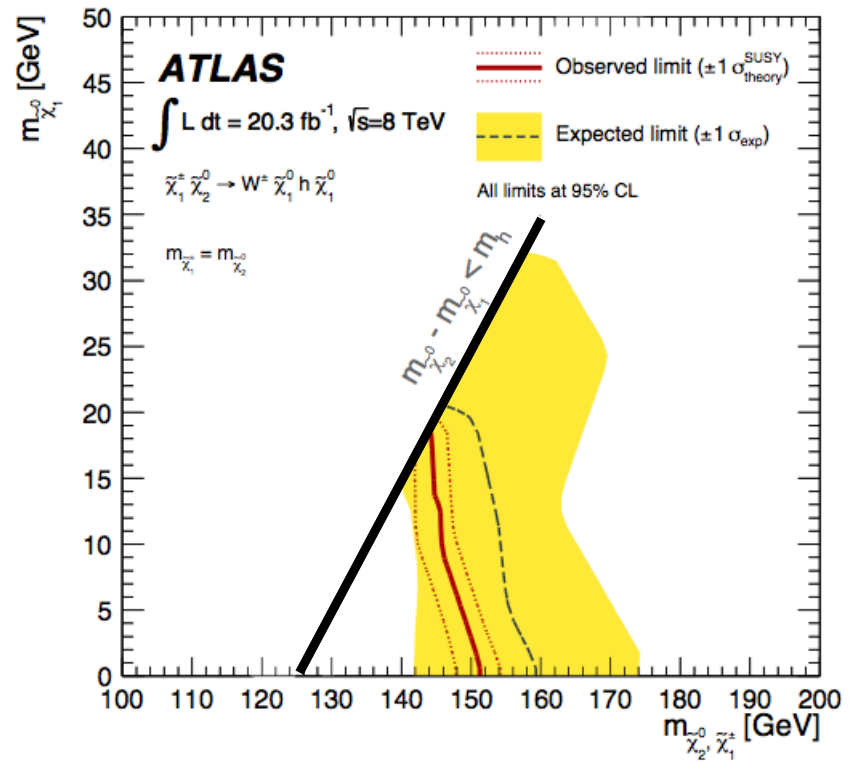
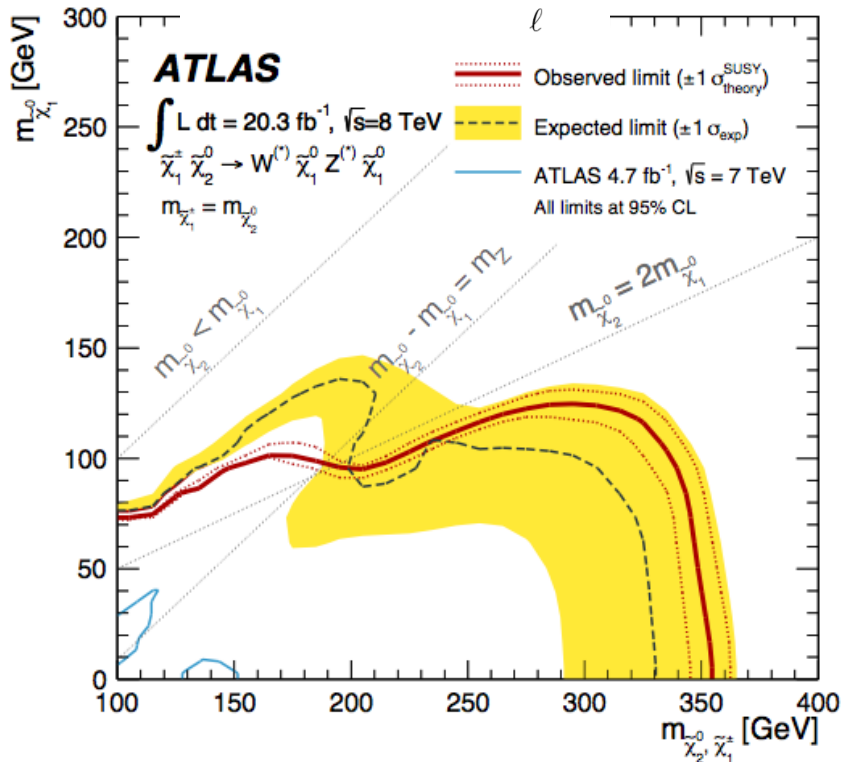
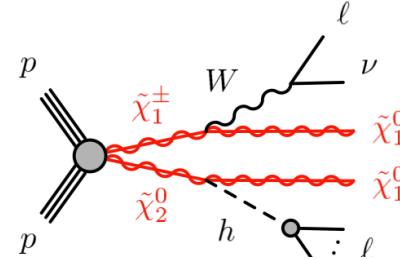
# Interpretation in SUSY simplified models

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## Decay via WZ

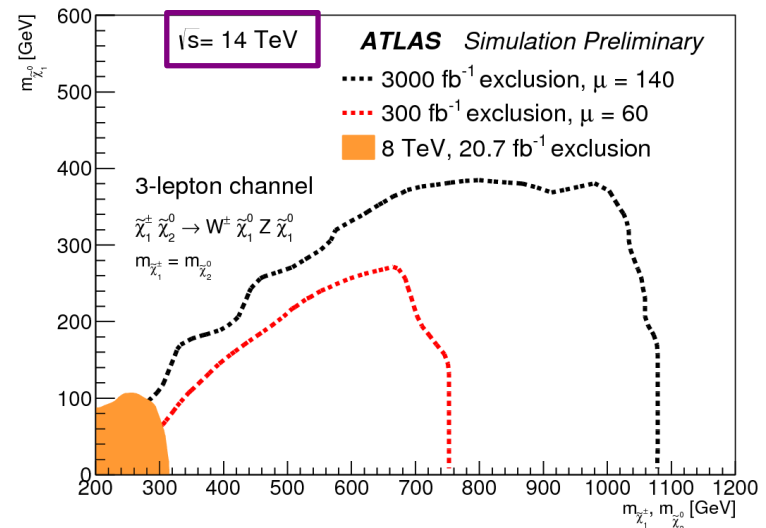


## Decay via Wh



# Conclusions

- Presented the results for a SUSY search in the three lepton final state
  - Based on 20.3 fb<sup>-1</sup> of data collected by the ATLAS detector in 2012
  - Target the direct production of  $\tilde{\chi}_1^\pm$  and  $\tilde{\chi}_2^0$  in R-parity conserving models
  - Explored intermediate decays through sleptons, staus, WZ and Wh
- Observations were consistent with Standard model expectations
- Limits were set in the context of simplified SUSY models
- ATLAS will begin data taking in 2015
  - Centre of mass energy increased to ~14 TeV
  - Stay tuned!



# Additional Slides

# Monte Carlo Generator

Process	Generator + fragmentation/hadronisation	Cross-section	Tune	PDF set
<b>Dibosons</b> $WW, WZ, ZZ$	POWHEG-r2129 [34, 35] + PYTHIA-8.165 [38]	NLO QCD with MCFM-6.2 [39, 40]	AU2 [36]	CT10 [37]
* $WZ, ZZ$	aMC@NLO-2.0.0.beta3 [41] + HERWIG-6.520 [42] (or + PYTHIA-6.426)	NLO QCD with MCFM-6.2	AU2	CT10
$ZZ$ via gluon fusion (not incl. in POWHEG)	gg2VV [43] + HERWIG-6.520	NLO	AUET2B [44]	CT10
$W\gamma, Z\gamma$	SHERPA-1.4.1 [45]	NLO	(internal)	CT10
<b>Tribosons</b> $WWW, ZWW$	MADGRAPH-5.0 [46] + PYTHIA-6.426	NLO [47]	AUET2B	CTEQ6L1 [48]
<b>Higgs</b> via gluon fusion	POWHEG-r2092 + PYTHIA-8.165	NNLL QCD, NLO EW [49]	AU2	CT10
via vector-boson-fusion	POWHEG-r2092 + PYTHIA-8.165	NNLO QCD, NLO EW [49]	AU2	CT10
associated $W/Z$ production	PYTHIA-8.165	NNLO QCD, NLO EW [49]	AU2	CTEQ6L1
associated $t\bar{t}$ -production	PYTHIA-8.165	NNLO QCD [49]	AU2	CTEQ6L1
<b>Top+Boson</b> $t\bar{t}W, t\bar{t}Z$	ALPGEN-2.14 [50] + HERWIG-6.520	NLO [51, 52]	AUET2B	CTEQ6L1
* $t\bar{t}W, t\bar{t}Z$	MADGRAPH-5.0 + PYTHIA-6.426	NLO	AUET2B	CTEQ6L1
$t\bar{t}WW$	MADGRAPH-5.0 + PYTHIA-6.426	NLO [52]	AUET2B	CTEQ6L1
$tZ$	MADGRAPH-5.0 + PYTHIA-6.426	NLO [53]	AUET2B	CTEQ6L1
<b><math>t\bar{t}</math></b>	POWHEG-r2129 + PYTHIA-6.426	NNLO+NNLL [54–59]	PERUGIA2011C	CT10
<b>Single top</b> $t$ -channel	ACERMC-38 [60] + PYTHIA-6.426	NNLO+NNLL [61]	AUET2B	CTEQ6L1
$s$ -channel, $Wt$	MC@NLO-4.06 [62, 63] + HERWIG-6.520	NNLO+NNLL [64, 65]	AUET2B	CT10
<b><math>W</math>+jets, <math>Z</math>+jets</b>	ALPGEN-2.14 + PYTHIA-6.426 (or + HERWIG-6.520)	DYNNLO-1.1 [66] with MSTW2008 NNLO [67]	PERUGIA2011C	CTEQ6L1



# Electroweak SUSY sector

Simplified supersymmetric models used for optimization and interpretation

- Masses and decay modes of the relevant particles are the only free parameters
- Wino like  $\tilde{\chi}_1^\pm$  and  $\tilde{\chi}_2^0$  and mass degenerate, bino like  $\tilde{\chi}_1^0$

Results also interpreted in the context of the phenomenological MSSM

Slepton mediated	Stau mediated	WZ mediated	Wh mediated
$\text{BR}(\tilde{\chi}_2^0, \tilde{\chi}_1^\pm \rightarrow \tilde{\ell}_L) = 50\%$ $\text{BR}(\tilde{\chi}_2^0, \tilde{\chi}_1^\pm \rightarrow \tilde{\nu}_\ell) = 50\%$	$\text{BR}(\tilde{\chi}_2^0, \tilde{\chi}_1^\pm \rightarrow \tilde{\tau}) = 50\%$ $\text{BR}(\tilde{\chi}_2^0, \tilde{\chi}_1^\pm \rightarrow \tilde{\nu}_\tau) = 50\%$	$\text{BR}(\tilde{\chi}_1^\pm \rightarrow W + \tilde{\chi}_1^0) = 100\%$ $\text{BR}(\tilde{\chi}_2^0 \rightarrow Z + \tilde{\chi}_1^0) = 100\%$	$\text{BR}(\tilde{\chi}_1^\pm \rightarrow W + \tilde{\chi}_1^0) = 100\%$ $\text{BR}(\tilde{\chi}_2^0 \rightarrow h + \tilde{\chi}_1^0) = 100\%$
$m_{\tilde{\ell}_L, \tilde{\nu}_\ell} = \frac{m_{\tilde{\chi}_2^0} + m_{\tilde{\chi}_1^0}}{2}$	$m_{\tilde{\tau}, \tilde{\nu}_\tau} = \frac{m_{\tilde{\chi}_2^0} + m_{\tilde{\chi}_1^0}}{2}$	<p>W and Z and have SM masses and BRs</p>	<p>W and h and have SM masses and BRs</p>

# Signal region selection

Select events with exactly three leptons (electrons, muons or hadronically decaying taus)

- Dominant backgrounds: WZ, ttbar, W and Z +jets
- Backgrounds are suppressed with cuts on various kinematic variables
- SR0 $\tau\alpha$ : 20 statistically independent signal regions with cuts on mSFOS, mT and E<sub>T</sub><sup>miss</sup>
- All signal regions statistically independent with the exception of SR2 $\tau\alpha$  and SR2 $\tau\beta$

Signal region	SR0 $\tau\alpha$	SR0 $\tau\beta$	SR1 $\tau$	SR2 $\tau\alpha$	SR2 $\tau\beta$
Flavour/sign	$l^+l^-l, l^+l^-l'$	$l^\pm l^\pm l'^\mp$	$\tau^\pm l^\mp l'^\mp, \tau^\pm l^\mp l'^\mp$	$\tau\tau l$	$\tau^+\tau^-l$
<i>b</i> -tagged jet	veto	veto	veto	veto	veto
$E_T^{\text{miss}}$	binned	> 50	> 50	> 50	> 60
Other	$m_{\text{SFOS}}$ binned $m_T$ binned	$p_T^{3\text{rd } l} > 20$ $\Delta\phi_{\ell\ell'}^{\text{min}} \leq 1.0$	$p_T^{2\text{nd } l} > 30$ $\sum p_T^\ell > 70$ $m_{\ell\tau} < 120$ $m_{ee}$ Z veto	$m_{T2}^{\text{max}} > 100$	$\sum p_T^\tau > 110$ $70 < m_{\tau\tau} < 120$
Target model	$\tilde{\ell}, WZ$ -mediated	<i>Wh</i> -mediated	<i>Wh</i> -mediated	$\tilde{\tau}_L$ -mediated	<i>Wh</i> -mediated

$$m_T = \sqrt{2p_T^\ell E_T^{\text{miss}} (1 - \cos(\Delta\phi(\ell, E_T^{\text{miss}}))}$$

# Validation regions

Validation regions (VR) used to verify background modelling and variable shapes

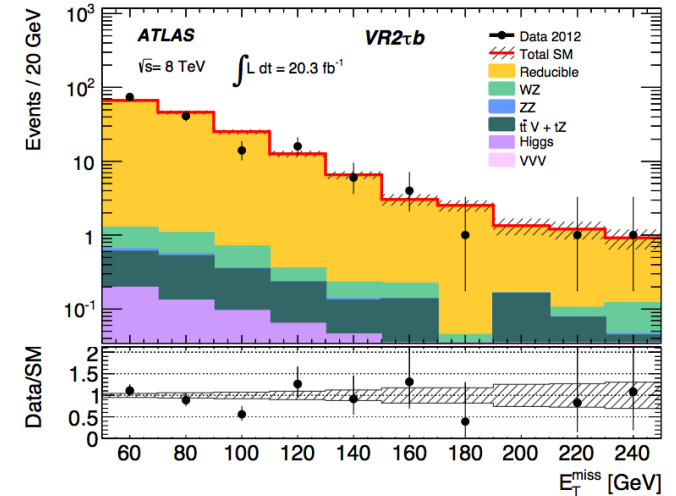
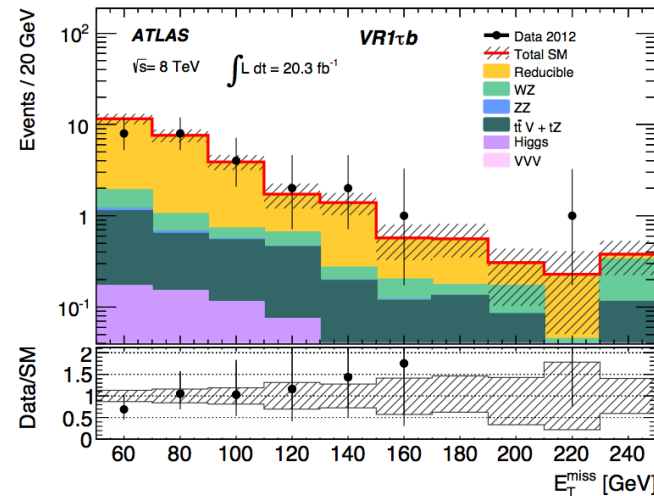
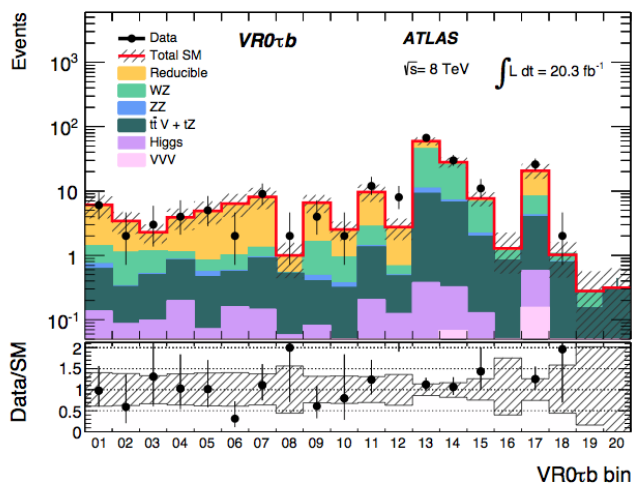
- Defined to be close kinematically close to the signal regions with small expected signal contamination
- Target dominant backgrounds:  $t\bar{t}$ , WZ, W+jets and Z+jets
- Good agreement observed in all regions

Region name	N( $\ell$ )	N( $\tau$ )	Flavour/sign	Z boson	$E_T^{\text{miss}}$	N(b-tagged jets)	Target process	
VR0 $\tau$ noZa	3	0	$\ell^+\ell^-\ell, \ell^+\ell^-\ell'$	$m_{\text{SFOS}} \& m_{3\ell}$ veto	35–50	–	$WZ^*, Z^*Z^*, Z^*+\text{jets}$	} $0\tau$ VRs
VR0 $\tau$ Za	3	0	$\ell^+\ell^-\ell, \ell^+\ell^-\ell'$	request	35–50	–	WZ, Z+jets	
VR0 $\tau$ noZb	3	0	$\ell^+\ell^-\ell, \ell^+\ell^-\ell'$	$m_{\text{SFOS}} \& m_{3\ell}$ veto	> 50	1	$t\bar{t}$	
VR0 $\tau$ Zb	3	0	$\ell^+\ell^-\ell, \ell^+\ell^-\ell'$	request	> 50	1	WZ	} $1\tau$ VRs
VR0 $\tau$ b	3	0	$\ell^+\ell^-\ell, \ell^+\ell^-\ell'$	binned	binned	1	WZ, $t\bar{t}$	
VR1 $\tau$ a	2	1	$\tau^\pm\ell^\mp\ell^\mp, \tau^\pm\ell^\mp\ell'^\mp$	–	35–50	–	WZ, Z+jets	} $1\tau$ VRs
VR1 $\tau$ b	2	1	$\tau^\pm\ell^\mp\ell^\mp, \tau^\pm\ell^\mp\ell'^\mp$	–	> 50	1	$t\bar{t}$	
VR2 $\tau$ a	1	2	$\tau\tau\ell$	–	35–50	–	W+jets, Z+jets	} $2\tau$ VRs
VR2 $\tau$ b	1	2	$\tau\tau\ell$	–	> 50	1	$t\bar{t}$	

$0\tau$  VRs

$1\tau$  VRs

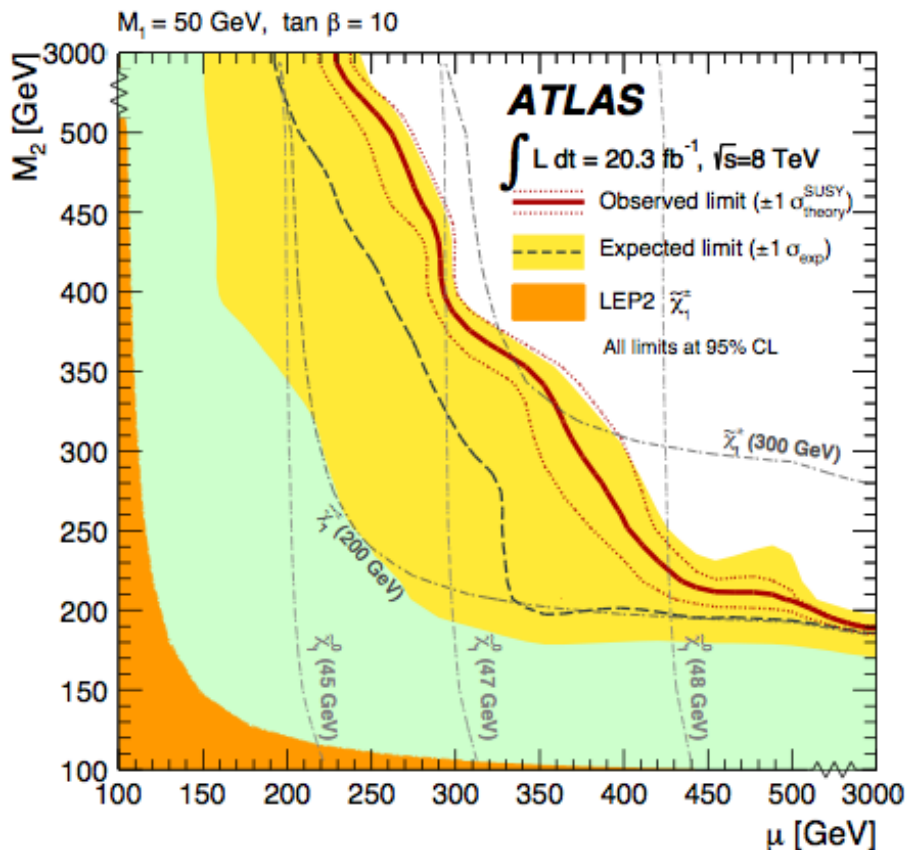
$2\tau$  VRs



# Phenomenological MSSM

Results interpreted in the context of the pMSSM

- Sleptons, heavy higgs, squarks and gluinos are "decoupled"
- $M_1$  fixed to 50 GeV to get the correct dark matter relic density – Z funnel
- Includes all chargino and neutralino production modes (higher mass eigenstates)
- Decays through WZ drive the limit in the bulk



## Parameters of the model

- $M_1$ : mass parameter of bino field
- $M_2$ : mass parameter of the wino fields
- $\mu$ : mass parameter of the higgsino fields
- $\tan \beta \equiv \langle H_2 \rangle / \langle H_1 \rangle$

Parameters above determine the properties of the neutralinos and charginos

- Production cross section
- Branching fractions
- Masses

# Background modelling

Standard model backgrounds classified into two categories:

→ **Irreducible backgrounds**: 3 real, prompt leptons

- Diboson production: WZ and ZZ
- Triboson production: VVV
- Top + vector boson: ttV and tZ
- Higgs production

} Estimated using Monte Carlo predictions

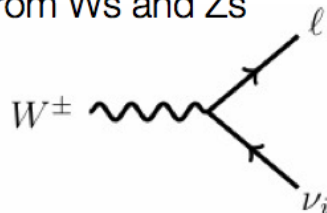
→ **Reducible backgrounds**: One or two 'fake' leptons

- Top quark: single and pair production
- Diboson production: WW
- Single boson production: W or Z

} Estimated using a data drive technique

## Real leptons

prompt leptons coming from Ws and Zs

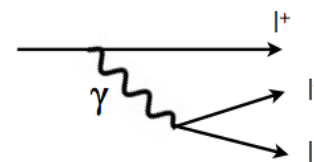


## Fake leptons

HF/LF fakes from jets



Conversion leptons from photon radiation



# Data driven estimate: Matrix Method

- Matrix method
  - Relates tight (T) and loose (L) leptons to real (R) and fake (F) objects
  - Leading lepton real ~99% of the time, reduces matrix to 4x4

$$\begin{pmatrix} N_{TT} \\ N_{TL'} \\ N_{LT} \\ N_{LL'} \end{pmatrix} = \begin{pmatrix} \epsilon_1 \epsilon_2 & \epsilon_1 f_2 & f_1 \epsilon_2 & f_1 f_2 \\ \epsilon_1 (1 - \epsilon_2) & \epsilon_1 (1 - f_2) & f_1 (1 - \epsilon_2) & f_1 (1 - f_2) \\ (1 - \epsilon_1) \epsilon_2 & (1 - \epsilon_1) f_2 & (1 - f_1) \epsilon_2 & (1 - f_1) f_2 \\ (1 - \epsilon_1)(1 - \epsilon_2) & (1 - \epsilon_1)(1 - f_2) & (1 - f_1)(1 - \epsilon_2) & (1 - f_1)(1 - f_2) \end{pmatrix} \cdot \begin{pmatrix} N_{RR} \\ N_{RF} \\ N_{FR} \\ N_{FF} \end{pmatrix}$$

- Coefficients are real lepton efficiency ( $\epsilon$ ) and fake rate ( $f$ )
- Invert matrix and solve for number of fake leptons passing tight requirements

$$N_{Fake \rightarrow TT} = \epsilon_1 f_2 \times N_{RF} + f_1 \epsilon_2 \times N_{FR} + f_1 f_2 \times N_{FF}$$

- Semi-data driven (see next slide)

# Matrix Method: Fake rates

- Fake rates depend on
  - Fake type (HF, LF, Conversions)
  - Process it originates from (ttbar, V+jets, etc)
- Determine a weighted average fake rate to be used in region XR

$$f_{XR}^{\ell} = \sum_{i,j} (SF^i \times R_{XR}^{i,j} \times F_{ij}) \quad \longrightarrow \quad \begin{array}{l} i = \text{fake type} \\ j = \text{process} \end{array}$$

- $F_{ij} \Rightarrow$  fake efficiency for fake type  $i$  from process  $j$  in region XR
  - $R_{ij} \Rightarrow$  fraction of fake type  $i$  and process  $j$  in region XR
  - $SF^i \Rightarrow$  scale factor for fake type  $i$
- Scale factors measured in dedicated CR's
    - Assumed to be region independent

# Object selection

## Electrons

- Baseline
  - IsEMmedium++
  - $p_T > 10 \text{ GeV}$  &  $|\eta| < 2.47$
  - Author 1 or 3
  - Good OQ
  - Overlap removal
- Signal
  - IsEMtight++
  - Isolation cuts
  - D0 significance and z0 cuts

## Muons

- Baseline
  - STACO loose
  - $p_T > 10 \text{ GeV}$  &  $|\eta| < 2.40$
  - ID hit requirements
  - Overlap removal
- Signal
  - Isolation cuts
  - D0 significance and z0 cuts

## MET

- Egamma10noTau\_Default

## Taus

- Baseline
  - $p_T > 20 \text{ GeV}$  &  $|\eta| < 2.50$
  - $nTrack == 1 \ || \ 3$
  - $|charge| == 1$
- Signal
  - EleBDTLoose==0
  - MuonVeto==0
  - JetBDTSigMedium==1

## Overlap removal

- Discard lowest ET ele if  $\Delta R(ele,ele) < 0.05$
- Discard jet if  $\Delta R(jet,ele) < 0.2$
- **Discard tau if  $\Delta R(tau,ele) < 0.2$**
- **Discard tau if  $\Delta R(tau,mu) < 0.2$**
- Discard ele if  $\Delta R(jet,ele) < 0.4$
- Discard mu if  $\Delta R(jet,mu) < 0.4$
- Discard ele & mu if  $\Delta R(mu,ele) < 0.01$
- Discard both muons if  $\Delta R(mu,mu) < 0.05$
- Discard both leptons if  $\Delta m(SFOS) < 12 \text{ GeV}$
- **Discard jet if  $\Delta R(jet,signal \ tau) < 0.2$**

## Triggers

- Lowest unprescaled single isolated and double lepton triggers



# Trigger selection

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Single and di-lepton triggers used

- Lepton is required to have fired the trigger and meet  $p_T$  requirements
- Logical OR taken for all trigger bits

Trigger	$p_T$ threshold [GeV]
Single Isolated $e$	25
Single Isolated $\mu$	25
Double $e$	14,14 25,10
Double $\mu$	14,14 18,10
Combined $e\mu$	14( $e$ ),10( $\mu$ ) 18( $\mu$ ),10( $e$ )

# Systematic uncertainties

## Systematic uncertainties for signal regions

	SR0 $\tau_a$	SR0 $\tau_b$	SR1 $\tau$	SR2 $\tau_a$	SR2 $\tau_b$
Cross-section	4–25%	37%	9%	3.1%	3.0%
Generator	3.2–35%	11%	3.1%	6%	< 1%
Statistics on irreducible background	0.8–26%	8%	5%	5%	3.1%
Statistics on reducible background	0.4–29%	14%	8%	13%	12%
Electron misidentification probability	0.3–10%	1.3%	< 1%	–	–
Muon misidentification probability	0.1–24%	2.2%	< 1%	–	–
$\tau$ misidentification probability	–	–	8%	4%	5%

# Binning of $SR0\tau a$

Binned in  $m_{SFOS}$ ,  $m_T$  and  $m_{ET}$

$SR0\tau a$ bin	$m_{SFOS}$	$m_T$	$E_T^{\text{miss}}$	$3\ell Z$ veto
1	12–40	0–80	50–90	no
2	12–40	0–80	> 90	no
3	12–40	> 80	50–75	no
4	12–40	> 80	> 75	no
5	40–60	0–80	50–75	yes
6	40–60	0–80	> 75	no
7	40–60	> 80	50–135	no
8	40–60	> 80	> 135	no
9	60–81.2	0–80	50–75	yes
10	60–81.2	> 80	50–75	no
11	60–81.2	0–110	> 75	no
12	60–81.2	> 110	> 75	no
13	81.2–101.2	0–110	50–90	yes
14	81.2–101.2	0–110	> 90	no
15	81.2–101.2	> 110	50–135	no
16	81.2–101.2	> 110	> 135	no
17	> 101.2	0–180	50–210	no
18	> 101.2	> 180	50–210	no
19	> 101.2	0–120	> 210	no
20	> 101.2	> 120	> 210	no