


$b \rightarrow s l^+ l^-$ anomalies & ATLAS B physics

Sebastian Jäger (University of Sussex)

ATLAS B-physics meeting

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ATLAS analyses

Analysis	Expected/plausible BSM scale	theory	current BSM significance
B(s,d) \rightarrow $\mu\mu$	(few) TeV (nat'lness)	excellent	2-3 σ
RK(*)	(few) TeV (nat'lness)	excellent	3-4 σ
B \rightarrow K* $\mu\mu$ (ee?) angular	(few) TeV (nat'lness)	good (P5') to excellent (rh current)	unclear
Tau \rightarrow 3 μ	GUT scale or below	excellent	none
B \rightarrow J/psi phi etc	(few) TeV	depends	none
B lifetimes	(few) TeV	depends	none
4 muons searches			
Bc/Bc(2S)			
Pentaquark/Zc			
CPV in b from ttbar			

Outside scope of what I can discuss in this talk

Outline

In the following I will focus about two topics which I have worked on

- 1) The $b \rightarrow s$ II anomalies, with emphasis on theoretically controlled observables
- 2) A possible connection with lifetime/mixing observables

SM(EFT) theory

Rare B-decay: short-distance

BSM (and SM weak interactions) enter flavour physics through **effective contact interactions** (SMEFT/ H_{weak})

C_9 : dilepton from vector current

$$(\bar{s}\gamma_\mu P_L b)(\bar{l}\gamma^\mu l)$$

C_{10} : dilepton from axial current

$$(\bar{s}\gamma_\mu P_L b)(\bar{l}\gamma^\mu \gamma^5 l)$$

C_7 : dilepton from dipole

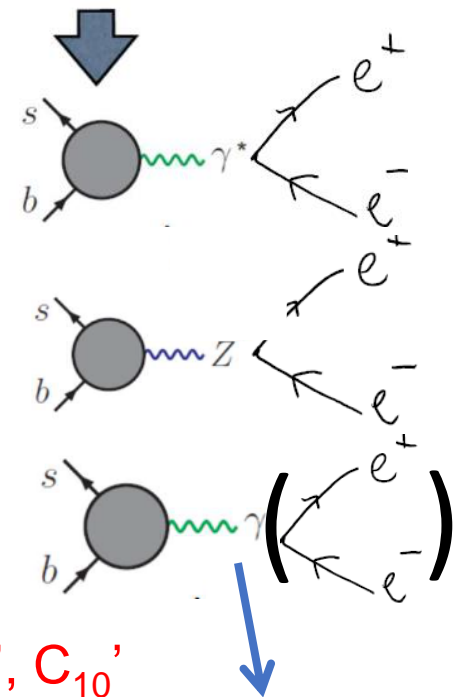
$$(\bar{s}\sigma^{\mu\nu} P_R b)F_{\mu\nu}$$

+parity conjugate “right-handed currents” - C_7' , C_9' , C_{10}'
suppressed by m_s/m_b in SM

Alternative basis with **chiral leptons** I_L, I_R

$$C_L = (C_9 - C_{10})/2 \quad C_R = (C_9 + C_{10})/2$$

in SM mainly



Can also have real photon

Importance of virtual charm

Also **purely hadronic** operators enter, in SM primarily:

$$Q_1^c = (\bar{c}_L^i \gamma_\mu b_L^j) (\bar{s}_L^j \gamma^\mu c_L^i)$$

$$Q_2^c = (\bar{c}_L^i \gamma_\mu b_L^i) (\bar{s}_L^j \gamma^\mu c_L^j)$$

RG mixes these into C_9 and C_7

+ dipole

$$C_7^{\text{eff}}(4.6\text{GeV}) = 0.02 C_1(M_W) - 0.19 C_2(M_W)$$

$$C_9(4.6\text{GeV}) = 8.48 C_1(M_W) + 1.96 C_2(M_W)$$

SM: O(50%) of total in both cases!

At $\mu=m_b$: $C_7^{\text{eff}} \sim -0.3$, $C_L \sim 4$, $C_R \approx 0$

- SM: accidentally almost left-chiral muon interactions

- Long-distance virtual charm important theory uncertainty

Rare B-decay: observables

Branching ratios

leptonic (differential in dilepton mass)

$$B_s \rightarrow \mu\mu, B_d \rightarrow \mu\mu,$$

Nonperturbative QCD fully controlled (decay constant from lattice)

semileptonic (differential in dilepton mass)

$$B \rightarrow K^{(*)}\mu\mu, B \rightarrow K^{(*)}ee, B_s \rightarrow \phi\mu\mu$$

Lepton universality ratios

$$R_{K^{(*)}}[a, b] = \frac{\int_a^b \frac{d\Gamma}{dq^2}(B \rightarrow K^{(*)}\mu^+\mu^-)dq^2}{\int_a^b \frac{d\Gamma}{dq^2}(B \rightarrow K^{(*)}e^+e^-)dq^2}$$

Form factors, 4-quark operator contributions, QED radiation cancel out to $\sim\%$ level (relative to LHCb treatment)

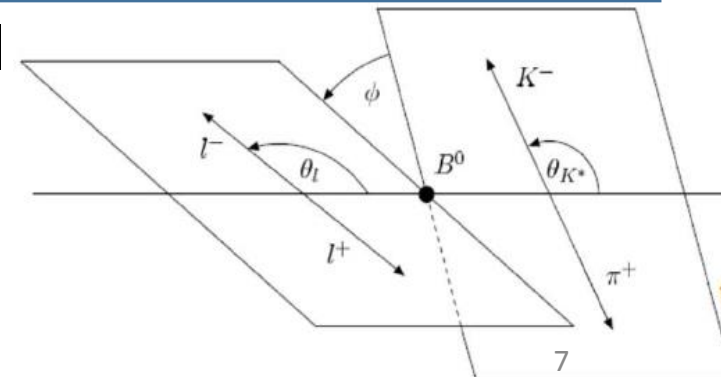
eg Bordone, Isidori, Pattori arXiv:1605.07633

differential angular distribution for $B \rightarrow VII$

3 angles, dilepton mass q^2

7 angular differential observables:

$(A_{FB}, P_5', \text{ etc})$



Lepton-flavour ratios at LHCb

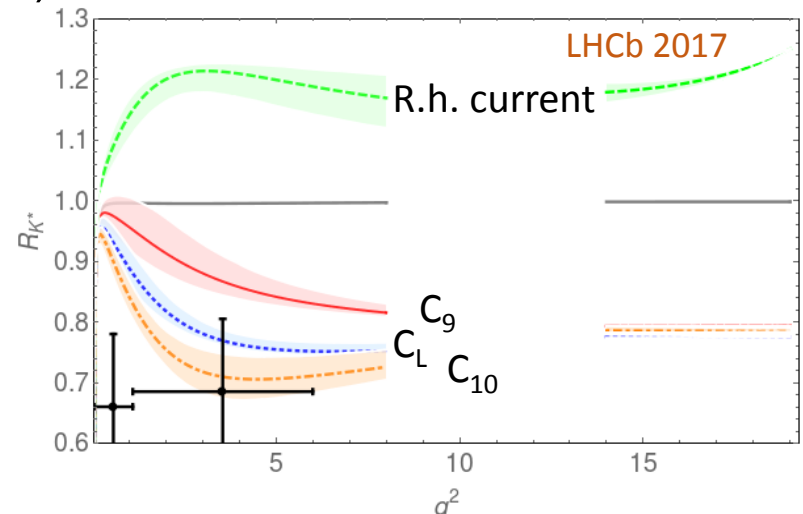
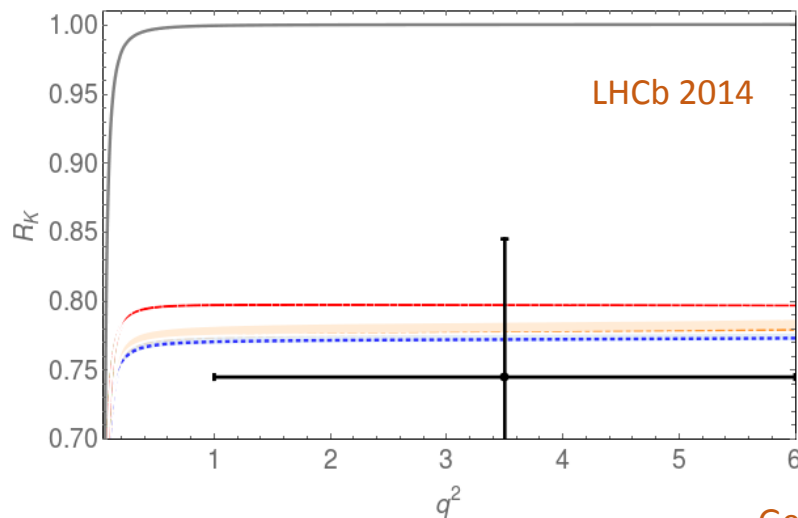
$$R_{K^{(*)}}[a, b] = \frac{\int_a^b \frac{d\Gamma}{dq^2} (B \rightarrow K^{(*)} \mu^+ \mu^-) dq^2}{\int_a^b \frac{d\Gamma}{dq^2} (B \rightarrow K^{(*)} e^+ e^-) dq^2}$$

Theory uncertainties largely cancel out, negligible relative to experiment.

leading is QED: net effect <1% after experimental corrections

Bordone, Isidori, Pattori 2016; Isidori, Nabeebaccus, Zwicky 2020

Situation in 2017 (first R_{K^*} measurement):



Geng, Grinstein, SJ, Martin Camalich, Ren, Shi arxiv:1704.05446

Sebastian Jaeger - ATLAS B meeting -

BSM fit

Observables in the fit

Basic idea: use only observables which are sensitive to $b \rightarrow s$ ll but independent of hadronic form factors, long-distance charm etc.

I.e. $R_{K^{(*)}}$ and $B_s \rightarrow \mu\mu$.

This is a well-defined set of observables, first employed in 2017, with several data updates since then. No “look-elsewhere effect” to take into account.

In the following I describe the fit in arXiv:2103.12738 (Geng, Grinstein, SJ, Li, Martin Camalich, Shi); see also work by Altmannshofer & Stangl

A note on the $B_s \rightarrow \mu\mu$ input

Together with the R_{K^*} update, LHCb presented a significant update to $BR(B_s \rightarrow \mu\mu)$

ATLAS and CMS have also measured this

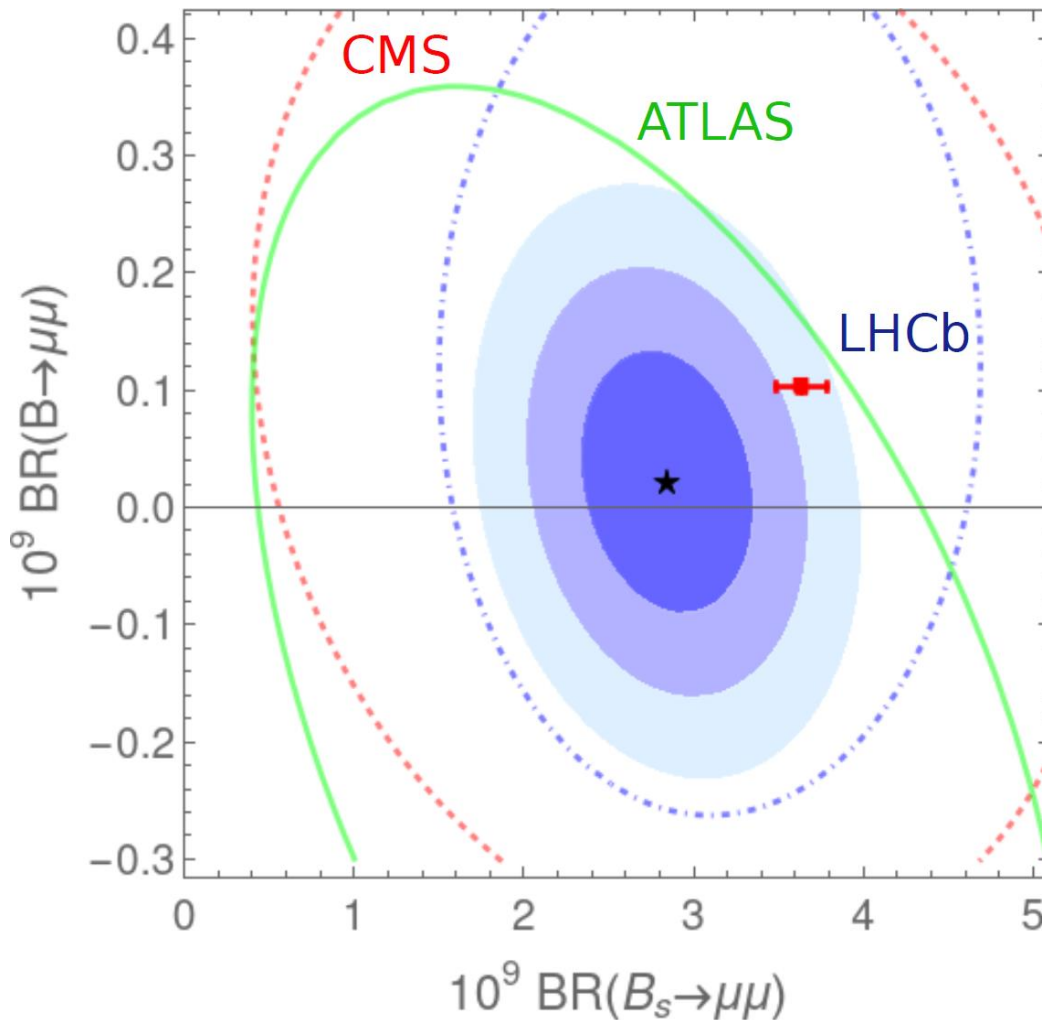
Measurements show non-negligible correlations with $BR(B_d \rightarrow \mu\mu)$ (biggest in ATLAS).

Hence to obtain a $BR(B_s \rightarrow \mu\mu)$ average first combine the 3x2 measurements.

Then profile over $BR(B_d \rightarrow \mu\mu)$.

$B_q \rightarrow \mu\mu$ world combination

Geng, Grinstein, SJ, Li, Martin Camalich, Shi arXiv:2103.12738



From this:

$$\text{BR}(B_s \rightarrow \mu\mu) = (2.8 \pm 0.3) 10^{-9}$$

$$\chi^2_{\text{min}} = 3.75 \text{ (5 d.o.f.)}$$

Input data

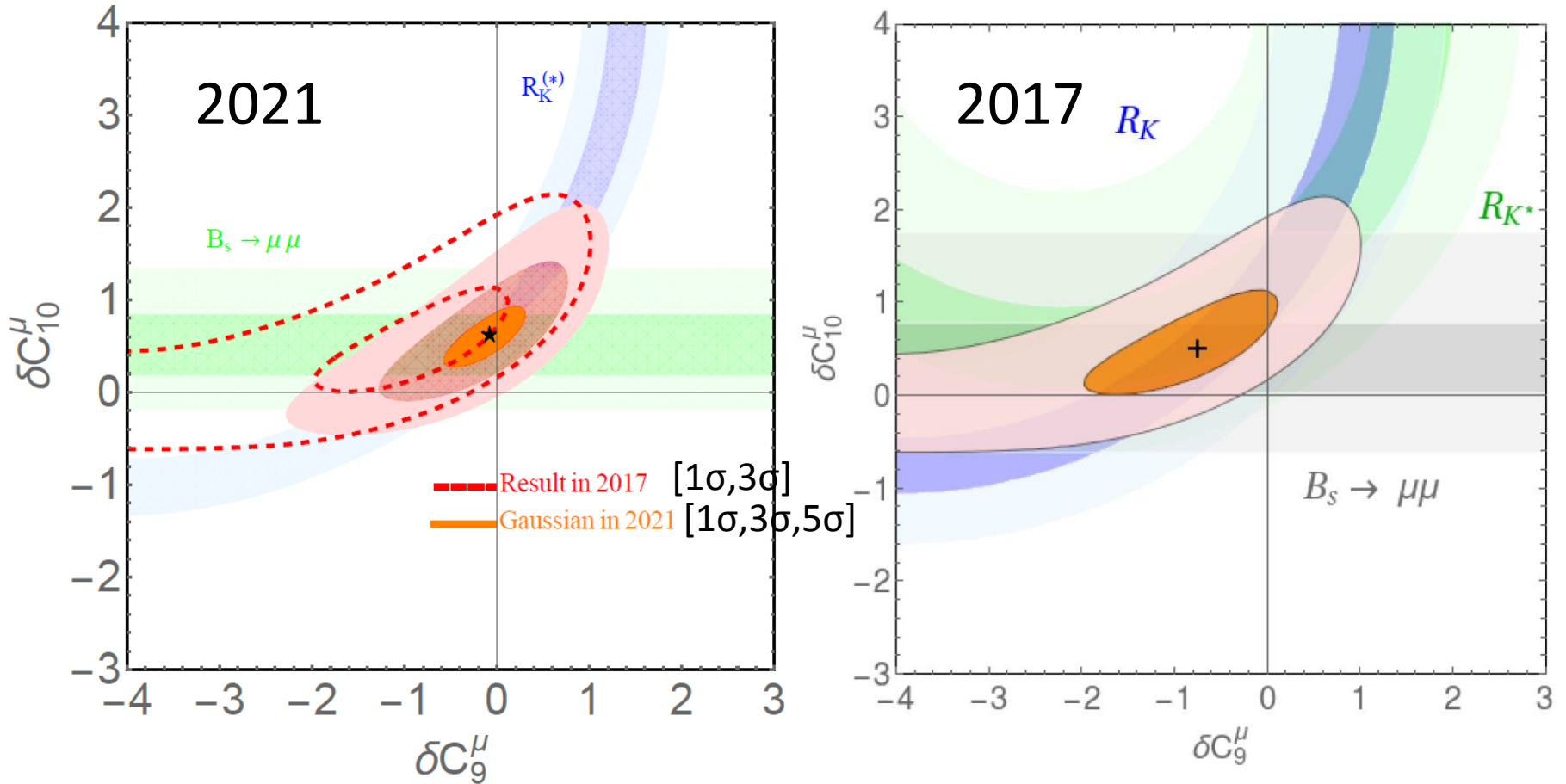
Observable	Value	Source	Reference
$BR(B_s \rightarrow \mu^+ \mu^-)$	$(2.8^{+0.8}_{-0.7}) \times 10^{-9}$	ATLAS	[11]
	$(2.9 \pm 0.7 \pm 0.2) \times 10^{-9}$	CMS	[12]
	$(3.09^{+0.46+0.15}_{-0.43-0.11}) \times 10^{-9}$	LHCb update	[10]
	$(2.842 \pm 0.333) \times 10^{-9}$	our average	this work
	$(3.63 \pm 0.13) \times 10^{-9}$	SM prediction	[13]
$R_K[1.1, 6]$	0.846 ± 0.044	LHCb	[6]
$R_K[1, 6]$	1.03 ± 0.28	Belle	[14]
$R_{K^*}[0.045, 1.1]$	0.660 ± 0.113	LHCb	[15]
$R_{K^*}[1.1, 6]$	0.685 ± 0.122	LHCb	[15]
$R_{K^*}[0.045, 1.1]$	0.52 ± 0.365	Belle	[16]
$R_{K^*}[1.1, 6]$	0.96 ± 0.463	Belle	[16]

Self-consistency of dataset: $\chi^2_{\min} = 4.61$ (8 d.o.f.) / $p = 0.80$
 (counting 6 $BR(B_q \rightarrow \mu\mu)$ measurements)

SM p-value is 5.4×10^{-5} (4.0σ) [counting $BR(B_s \rightarrow \mu\mu)$ average]
 reduces to 3.5σ when counting the 6 $BR(B_q \rightarrow \mu\mu)$ measurements
 separately

Clean fit: results: 2-parameter BSM fit

Geng, Grinstein, SJ, Li, Martin Camalich, Shi arXiv:2103.12738



Clean fits: numerical results

Geng, Grinstein, SJ, Li, Martin Camalich, Shi arXiv:2103.12738

Fit three 1-parameter scenario (vectorial, axial, left-handed coupling to muons)

TABLE II. Best fit values, χ_{\min}^2 , p -value, Pull_{SM} and confidence intervals of the Wilson coefficients in the fits of the $R_K, R_{K^*}, B_s \rightarrow \mu\mu$ data only using Gaussian form χ_{th}^2 . For the cases of single Wilson-coefficient fits, we show the 1σ and 3σ confidence intervals. In the $(\delta C_9^\mu, \delta C_{10}^\mu)$ case, the 1σ interval of each Wilson coefficient is obtained by profiling over the other one to take into account their correlation.

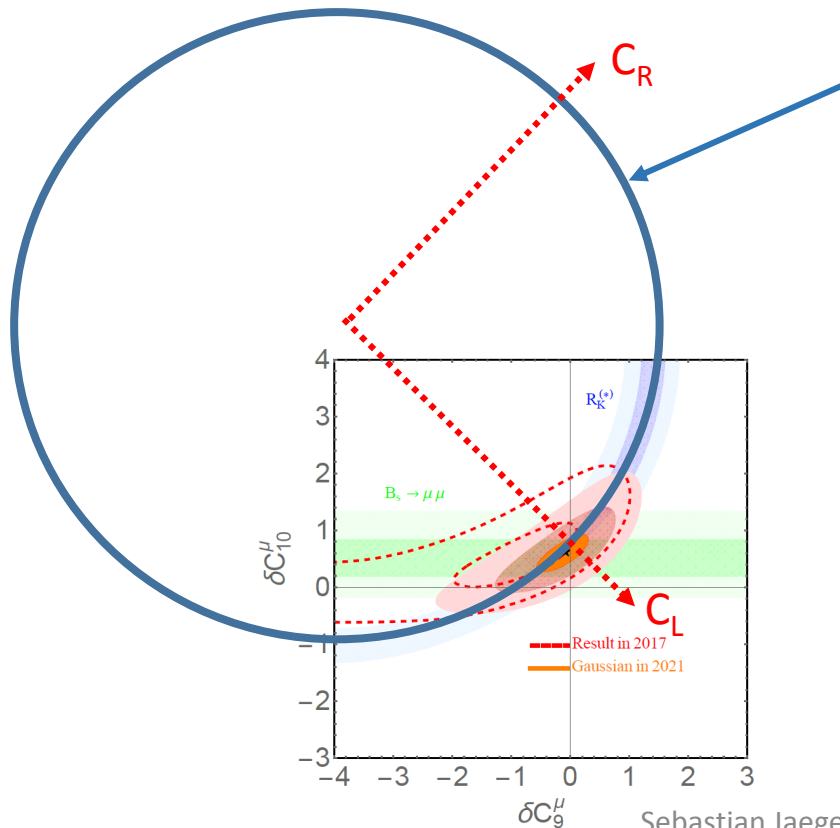
Coeff.	best fit	χ_{\min}^2	p -value	Pull_{SM}	1σ range	3σ range	ρ
δC_9^μ	-0.82	14.70 [6 dof]	0.02	4.08	[-1.06, -0.60]	[-1.60, -0.20]	-
δC_{10}^μ	0.65	6.52 [6 dof]	0.37	4.98	[0.52, 0.80]	[0.25, 1.11]	-
δC_L^μ	-0.40	7.36 [6 dof]	0.29	4.89	[-0.48, -0.31]	[-0.66, -0.15]	-
$(\delta C_9^\mu, \delta C_{10}^\mu)$	(-0.11, 0.59)	6.38 [5 dof]	0.27	4.62	$\delta C_9^\mu \in [-0.41, 0.17]$	$\delta C_{10}^\mu \in [0.38, 0.81]$	0.762
$(\delta C_L^\mu, \delta C_R^\mu)$	(-0.35, 0.25)				$\delta C_L^\mu \in [-0.45, -0.26]$	$\delta C_R^\mu \in [0.00, 0.48]$	0.406

Note that C_L is well-determined in both the left-handed and the two-parameter scenario, with consistent values. Not true for C_9 . Pure C_9 model also much worse fit ($p=1/50$).

$R_K^{(*)}$ and C_L

Assume here that the BSM effect is in the muonic mode, and no right-handed currents.

Because in the SM, $|C_R|, |C_7| \ll |C_L|$,
 $BR \approx \text{const } |C_L^{\text{SM}} + C_L^{\text{BSM}}|^2 + \dots \approx \text{const } |4 + C_L^{\text{BSM}}|^2 + \text{positive}$



$BR(B \rightarrow K^{(*)} \mu \mu) =$
SM value

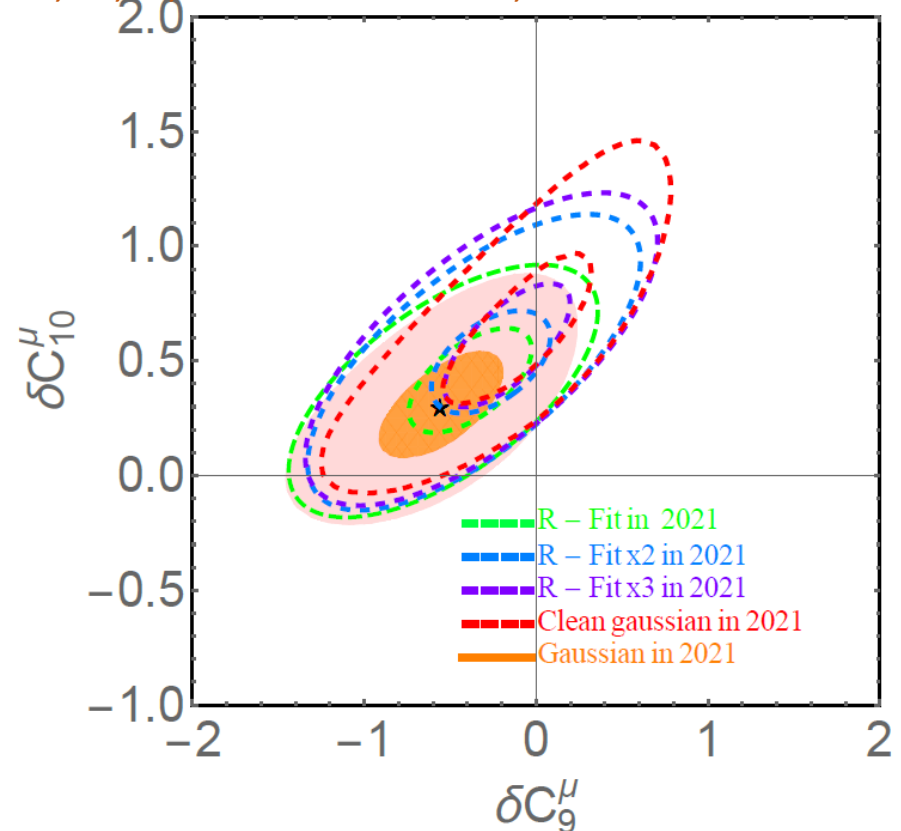
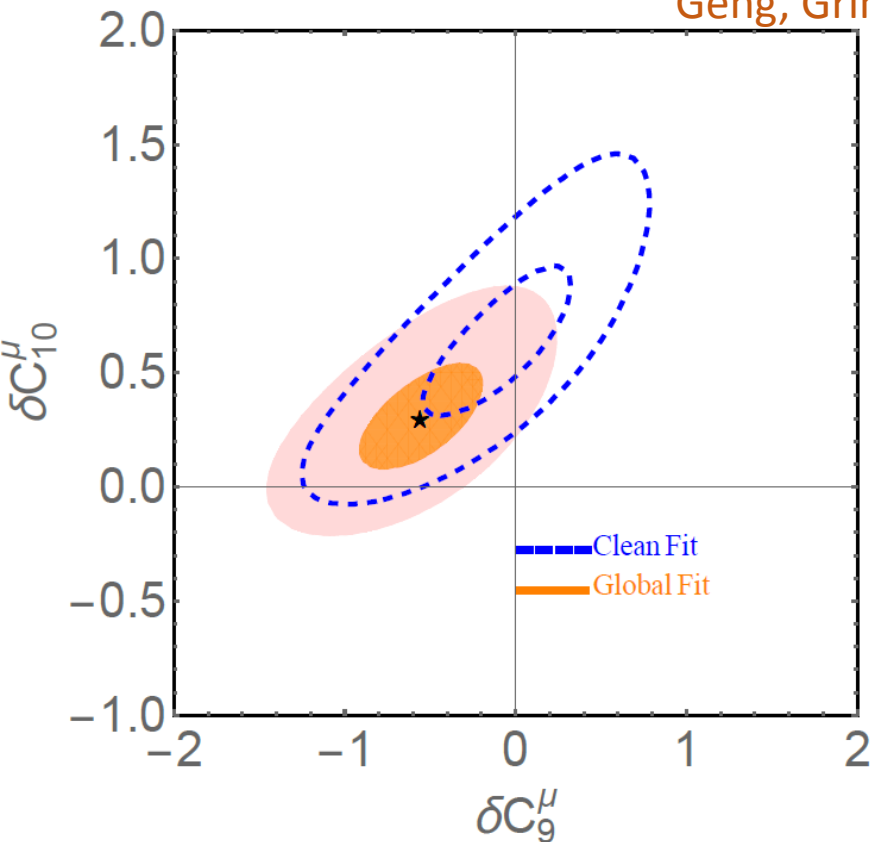
Only C_L^{BSM} can interfere destructively: $R_K^{(*)}$ point to purely left-handed coupling

$$(\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

with $\sim -(10-15)\%$ of SM value

Adding $B \rightarrow K^* \mu \mu$ angular data

Geng, Grinstein, SJ, Li, Martin Camalich, Shi arXiv:2103.12738



Left plot: extra data pulls fit approx. along the C_R direction.
 $C_L=0$ remains excluded at high confidence.
 $p(\text{SM})$ up at 0.02

Right plot: effect of increasing hadronic uncertainties

Minimal contact interaction

In summary, the B-decay anomalies suggest at a minimum the interaction

$$\frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

numerically $\Lambda \sim 40$ TeV

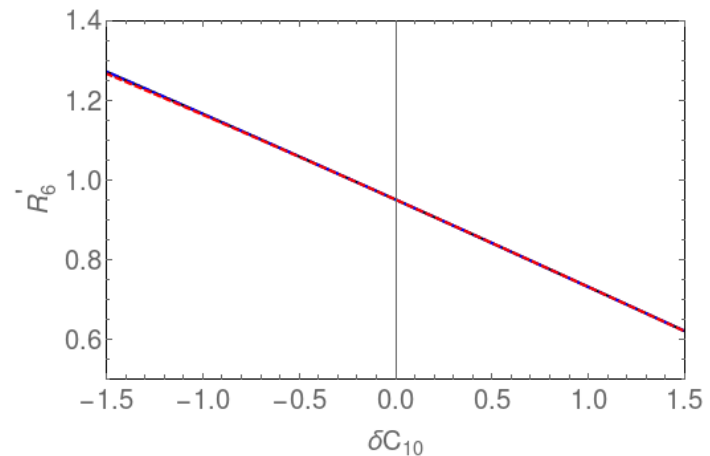
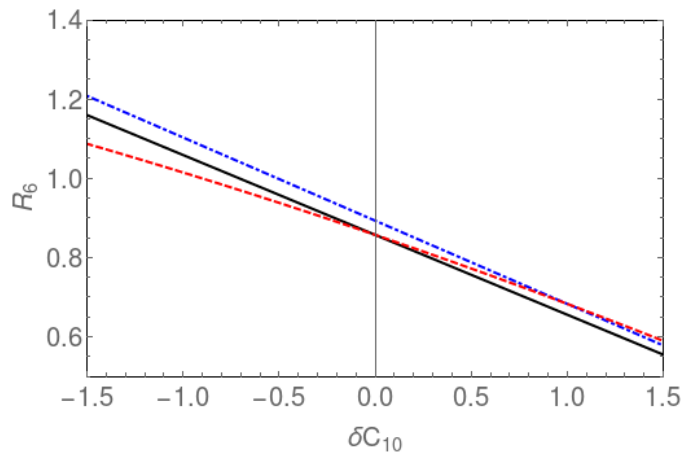
Small enough to be a loop effect even BSM (as it is in SM!)

Determining CR (break C9/C10 degeneracy)

Geng, Grinstein, SJ, Martin Camalich, Ren, Shi arxiv:1704.05446

Propose to measure observable

$$R_6[a, b] = \frac{\int_a^b \Sigma_6^\mu dq^2}{\int_a^b \Sigma_6^e dq^2} \approx \frac{C_{10}^\mu}{C_{10}^e} \times \frac{\int_a^b |\vec{k}| q^2 \beta_\mu^2 \operatorname{Re}[H_{V-}^{(\mu)}(q^2)] V_-(q^2)}{\int_a^b |\vec{k}| q^2 \operatorname{Re}[H_{V-}^{(e)}(q^2)] V_-(q^2)} \quad \text{and/or} \quad R'_6 = \langle P_2^{(\mu)} \rangle / \langle P_2^{(e)} \rangle$$



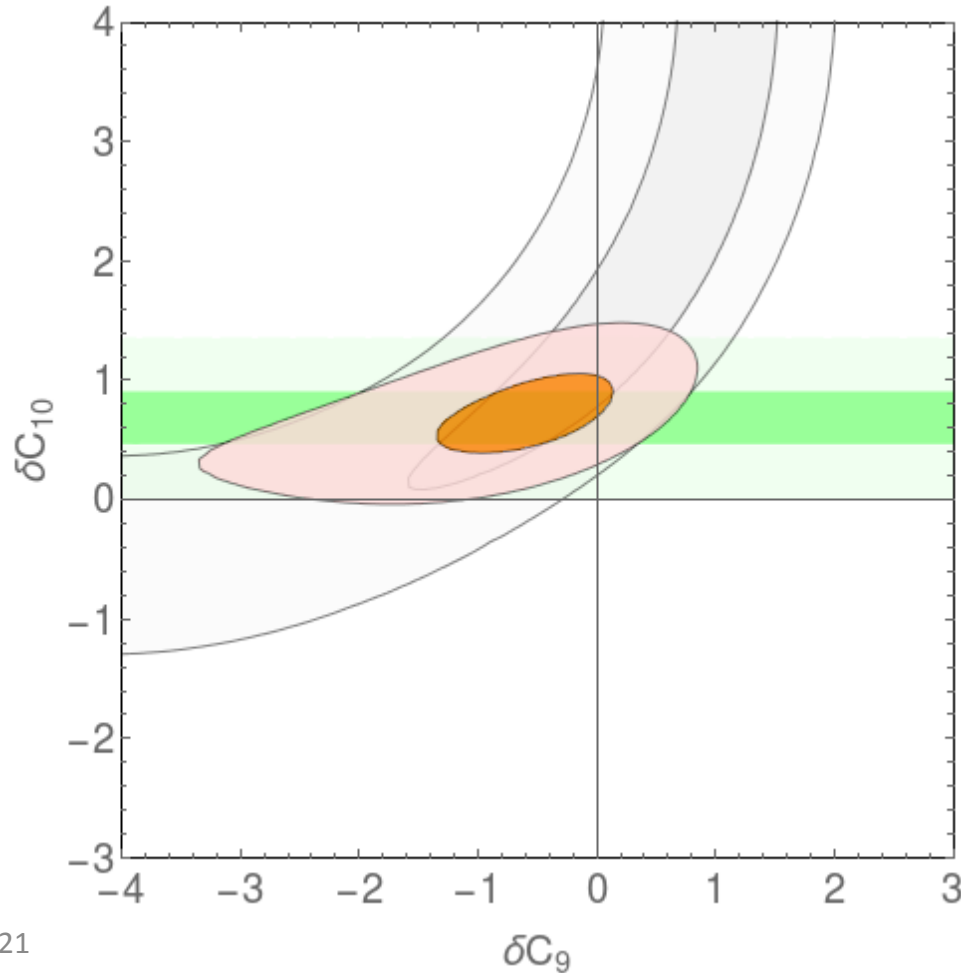
Remains very clean in presence of new physics.

Probes a LUV C10 precisely, irrespective of values of C9e, C9mu

Prospective fit with LUV obs. only

Geng, Grinstein, SJ, Martin Camalich, Ren, Shi [arxiv:1704.05446](https://arxiv.org/abs/1704.05446)

Consider a hypothetical experimental result $R6' = 0.80(5)$ [other data from 2017 – not updated!]



Charming new B-physics

Charm and new physics

Postulated to explain non-observation of $K_L \rightarrow \mu^+ \mu^-$ (GIM)

Discovery **key to establishing SM**

In B physics, charm appears in leading decays through a partonic $b \rightarrow c\bar{c}s$ transition. Large CKM factor.

Usually one assumes BSM corrections to be negligible.

Is this assumption well grounded in data (or theory)?

Observables

rare semileptonic (P5' etc)

radiative ($B \rightarrow X_s \gamma$)

width/lifetime differences

$$\Delta\Gamma_s \quad \tau_{B_s} / \tau_{B_d}$$

} All calculable
in heavy-quark
expansion
(1/m_b)

exclusive charmful: BR, A_{CP} , S_{CP}
precisely measured

- not calculable (HQE is $1/(m_c \alpha_s)$)

will show a data-driven method

Rare & radiative decays

Standard Model: tree-level W exchange

$$Q_1^c = (\bar{c}_L^i \gamma_\mu b_L^j)(\bar{s}_L^j \gamma^\mu c_L^i)$$

$$Q_2^c = (\bar{c}_L^i \gamma_\mu b_L^i)(\bar{s}_L^j \gamma^\mu c_L^j)$$

RG evolution:

$$Q_9 \propto (\bar{s} \gamma_\mu P_L b)(\bar{l} \gamma^\mu l)$$

$$Q_7 \propto (\bar{s} \sigma_{\mu\nu} P_R b) F^{\mu\nu}$$

$$C_7^{\text{eff}}(4.6\text{GeV}) = 0.02 C_1(M_W) - 0.19 C_2(M_W)$$

$$C_9(4.6\text{GeV}) = 8.48 C_1(M_W) + 1.96 C_2(M_W)$$

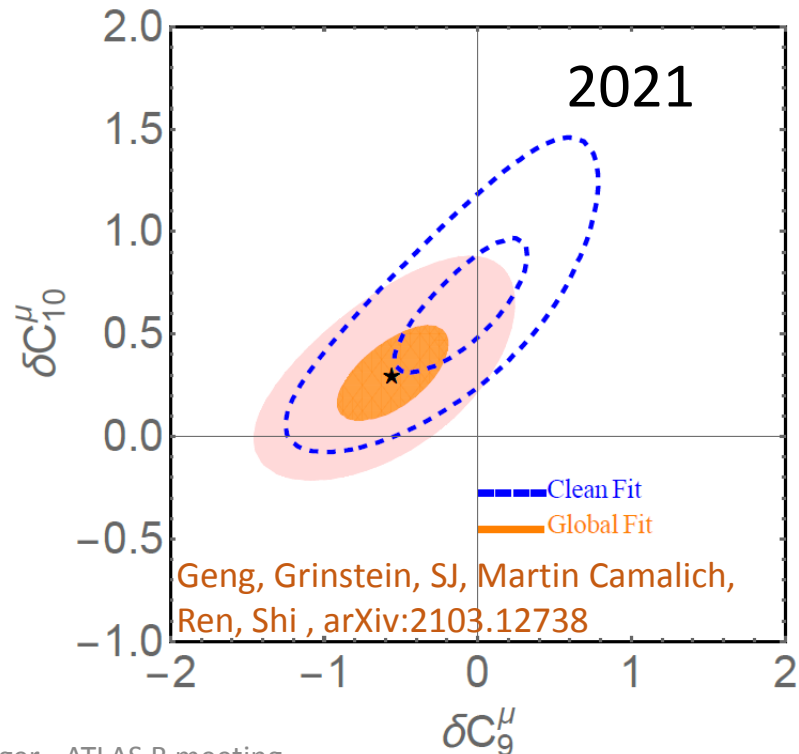
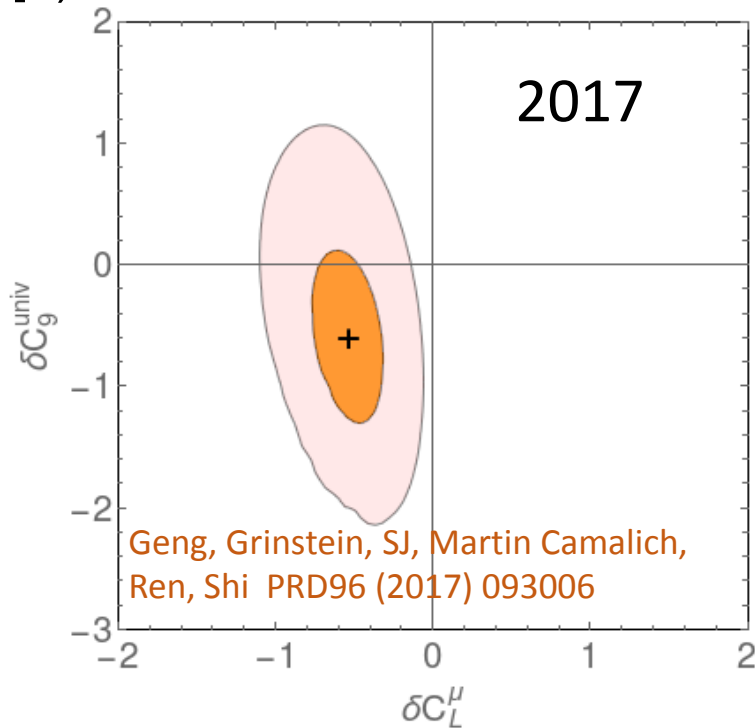
In SM: O(50%) in both cases comes from virtual charm

Rare & radiative decays: experiment

Rare B-decay data shows tensions with SM

- 1) Lepton-universality breaking - needs lepton-flavour specific effect
- 2) $B_s \rightarrow \mu\mu$
- 3) angular distribution (P_5') - could be lepton-universal C_9 -type effect

[2] could be either, but not via C_9]



A UV model may well give both.

Charming BSM scenario

SJ, Kirk, Lenz, Leslie arxiv:1701.09183

As long as NP mass scale M is \gg mb, most general BSM in $b \rightarrow c\bar{c}s$ **model-independently** captured by an effective Hamiltonian with 20 operators/Wilson coefficients (including SM)

$$Q_1^c = (\bar{c}_L^i \gamma_\mu b_L^j)(\bar{s}_L^j \gamma^\mu c_L^i),$$

$$Q_2^c = (\bar{c}_L^i \gamma_\mu b_L^i)(\bar{s}_L^j \gamma^\mu c_L^j),$$

$$Q_3^c = (\bar{c}_R^i b_L^j)(\bar{s}_L^j c_R^i),$$

$$Q_4^c = (\bar{c}_R^i b_L^i)(\bar{s}_L^j c_R^j),$$

$$Q_5^c = (\bar{c}_R^i \gamma_\mu b_R^j)(\bar{s}_L^j \gamma^\mu c_L^i),$$

$$Q_6^c = (\bar{c}_R^i \gamma_\mu b_R^i)(\bar{s}_L^j \gamma^\mu c_L^j),$$

$$Q_7^c = (\bar{c}_L^i b_R^j)(\bar{s}_L^j c_R^i),$$

$$Q_8^c = (\bar{c}_L^i b_R^i)(\bar{s}_L^j c_R^j),$$

$$Q_9^c = (\bar{c}_L^i \sigma_{\mu\nu} b_R^j)(\bar{s}_L^j \sigma^{\mu\nu} c_R^i),$$

$$Q_{10}^c = (\bar{c}_L^i \sigma_{\mu\nu} b_R^i)(\bar{s}_L^j \sigma^{\mu\nu} c_R^j),$$

+ parity conjugates

RG evolution - numerical

SJ, Kirk, Lenz, Leslie, arxiv:1701.09183 and arXiv:1910.12924,

Some elements first arise at two loops – still give important constraints.

$$\begin{pmatrix} C_1^c(\mu_b) \\ C_2^c(\mu_b) \\ C_3^c(\mu_b) \\ C_4^c(\mu_b) \\ C_5^c(\mu_b) \\ C_6^c(\mu_b) \\ C_7^c(\mu_b) \\ C_8^c(\mu_b) \\ C_9^c(\mu_b) \\ C_{10}^c(\mu_b) \\ C_{7\gamma}^{\text{eff}}(\mu_b) \\ C_{9V}(\mu_b) \end{pmatrix} = \begin{pmatrix} 1.1 & -0.27 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -0.27 & 1.1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0.92 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0.33 & 1.9 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1.9 & 0.33 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0.92 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1.0 & 0.05 & 2.70 & 1.70 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0.37 & 2.0 & 2.30 & -0.55 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0.07 & 0.07 & 1.80 & 0.04 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0.01 & -0.02 & -0.29 & 0.82 \\ 0.02 & -0.19 & -0.015 & -0.13 & 0.56 & 0.17 & -1.0 & -0.47 & 4.00 & 0.70 \\ 8.50 & 2.10 & -4.30 & -2.00 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} C_1^c(M_W) \\ C_2^c(M_W) \\ C_3^c(M_W) \\ C_4^c(M_W) \\ C_5^c(M_W) \\ C_6^c(M_W) \\ C_7^c(M_W) \\ C_8^c(M_W) \\ C_9^c(M_W) \\ C_{10}^c(M_W) \end{pmatrix}$$

Enormous RG effects - can accommodate P_5'

SJ, Kirk, Lenz, Leslie arxiv:1701.09183

RH(primed) 4-quark ops constrained by both C_7' and C_9'

Observables/constraints

Lifetime ratio $\frac{\tau(B_s)}{\tau(B_d)} = 0.9994 \pm 0.0025$

Width difference $\Delta\Gamma_s^{\text{exp}} = 0.088 \pm 0.006 \text{ ps}^{-1}$

Inclusive radiative decay $\mathcal{B}(\bar{B} \rightarrow X_s \gamma)^{\text{exp}} = (3.32 \pm 0.15) \times 10^{-4}$

‘Pseudo-observables:’ fitted Wilson coefficients from (mainly) exclusive radiative and semileptonic decay

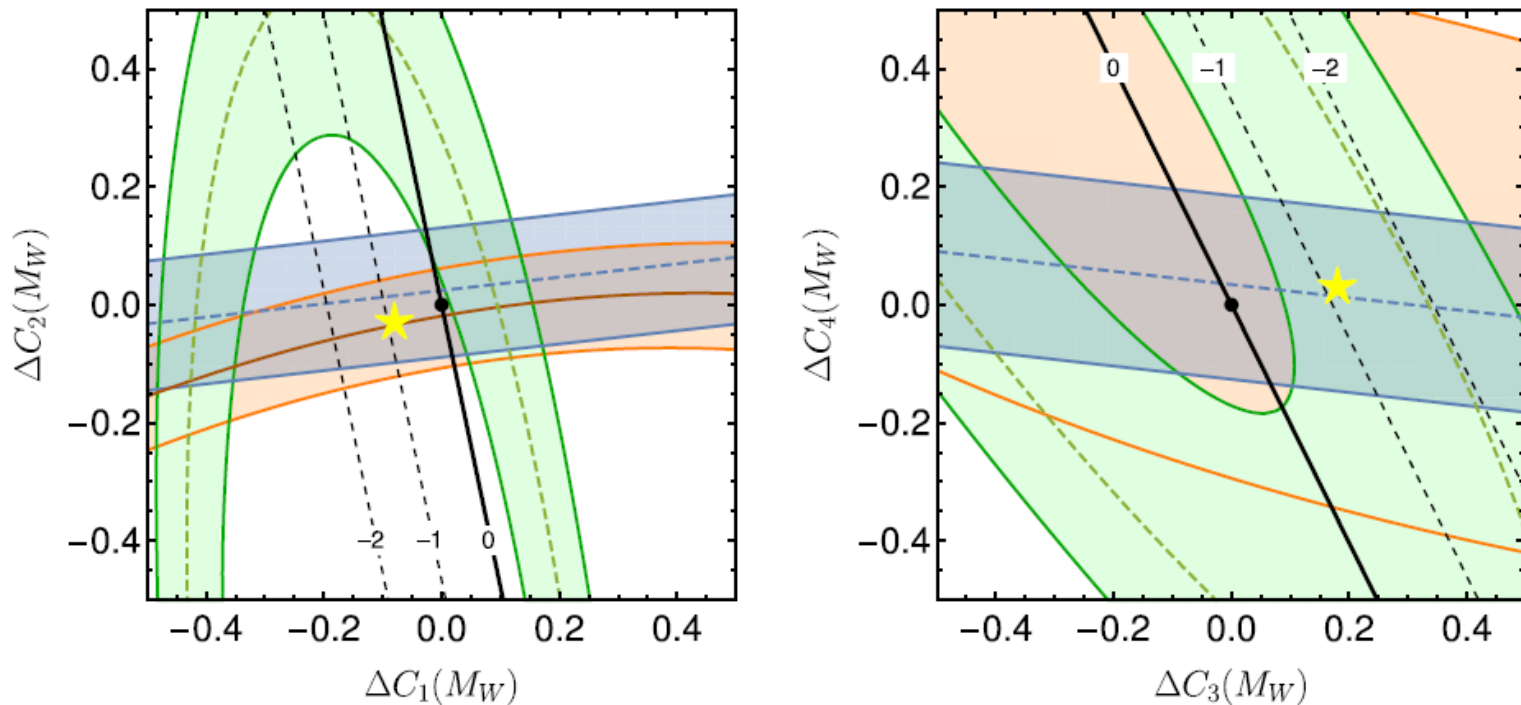
$$C'_{7\gamma} = 0.018 \pm 0.037 \quad \text{Aebischer et al arXiv:1903.10434}$$

$$C'_{9V} = 0.09 \pm 0.15 \quad \text{Paul \& Straub arXiv:1608.02556}$$

Global analysis

SJ, Kirk, Lenz, Leslie, arXiv:1910.12924

‘LH currents’ – strong mixing into C_9



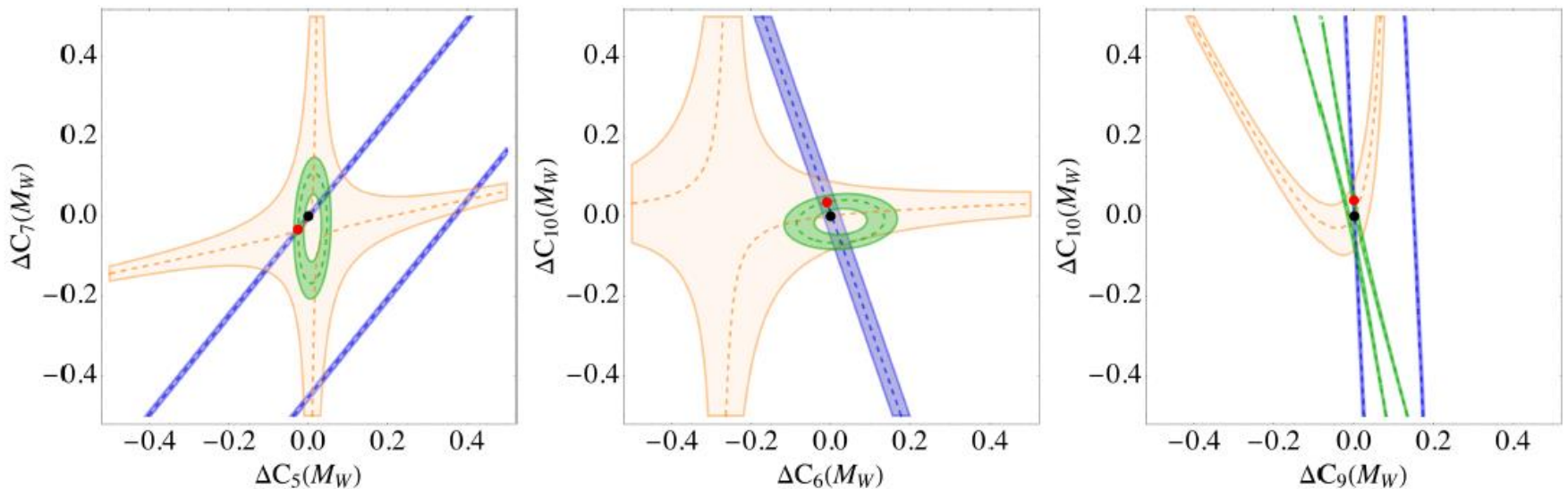
Blue – radiative decay, green – lifetime ratio, brown – width difference

Dashed/solid black: $C_9(\text{BSM})$

Global analysis

SJ, Kirk, Lenz, Leslie, arXiv:1910.12924

‘LH currents’ – strong mixing into dipole

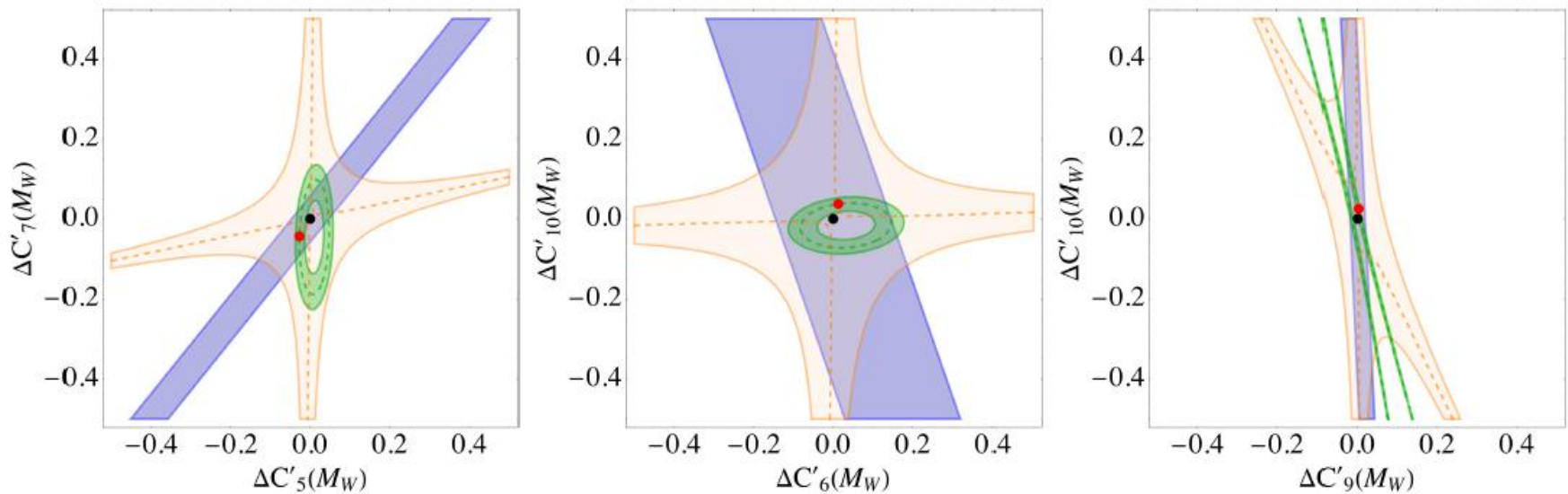


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Global analysis

SJ, Kirk, Lenz, Leslie, arXiv:1910.12924

‘RH currents’ – strong mixing into dipole



Blue – radiative decay, green – lifetime ratio, brown – lifetime difference

Lower bounds on NP scale

SJ, Kirk, Lenz, Leslie, arXiv:1910.12924

Delta C < 0

Delta C > 0

Coeff.	$\Delta\chi^2 \leq 1$	Λ_- (TeV)	Λ_+ (TeV)
ΔC_5	[-0.01, 0.01]	9.7	10.5
ΔC_6	[-0.02, 0.02]	5.6	5.8
ΔC_7	[-0.01, 0.01]	8.8	9.7
ΔC_8	[-0.02, 0.02]	6.2	6.9
ΔC_9	[-0.001, 0.005]	22.3	12.6
ΔC_{10}	[0.01, 0.05]	-	3.8
$\Delta C'_1$	[-0.01, 0.02]	11.9	5.5
$\Delta C'_2$	[-0.04, 0.09]	4.5	2.8
$\Delta C'_3$	[-0.04, 0.02]	4.5	7.0
$\Delta C'_4$	[-0.07, 0.03]	3.2	5.1
$\Delta C'_5$	[-0.02, 0.03]	5.9	4.8
$\Delta C'_6$	[-0.07, 0.10]	3.3	2.8
$\Delta C'_7$	[-0.03, 0.02]	5.2	6.6
$\Delta C'_8$	[-0.05, 0.04]	3.7	4.3
$\Delta C'_9$	[0.002, 0.010]	-	8.6
$\Delta C'_{10}$	[-0.08, -0.06], [0.02, 0.05]	7.1	3.5

$B \rightarrow J/\psi K_S$ & CP violation

If new physics in $b \rightarrow c\bar{c}s$ is CP-violating, it will impact on the precisely measured exclusive $B \rightarrow J/\psi K_S$ decays.

Three precisely observables:

$$S_{J/\psi K_S} = 0.699 \pm 0.017$$

$$C_{J/\psi K_S} = -0.005 \pm 0.015$$

$$\mathcal{B}(B_d \rightarrow J/\psi K_S) = (8.73 \pm 0.32) \times 10^{-4}$$

Note: The impact on the semileptonic asymmetry turns out to be comparably small (will show).

Exclusive B-decay

Exclusive charmful hadronic B-decays suffer from large hadronic uncertainties

e.g data suggests corrections to (calculable) naïve factorisation $O(100\%)$

Weak sensitivity to BSM contributions, especially if CP-conserving

$B \rightarrow J/\psi K_S$: theory

Problem: hadronic matrix elements $\langle J/\psi K_S | Q_i | B \rangle$

Heavy-quark expansion uncontrolled

expansion parameter is $\Lambda_{\text{QCD}}/(\alpha_s m_c)$

$$\text{But } \langle J/\psi K_S | Q_1 | B \rangle = \frac{M_B p_c}{2} f_{J/\psi} F^{B \rightarrow K} \left(1 + \frac{1}{N_c^2} \right)$$

factorizes naively, up to colour-suppressed corrections.

If new physics only affects C_1 or C_2 , the incalculable hadronic dynamics is largely contained in a single

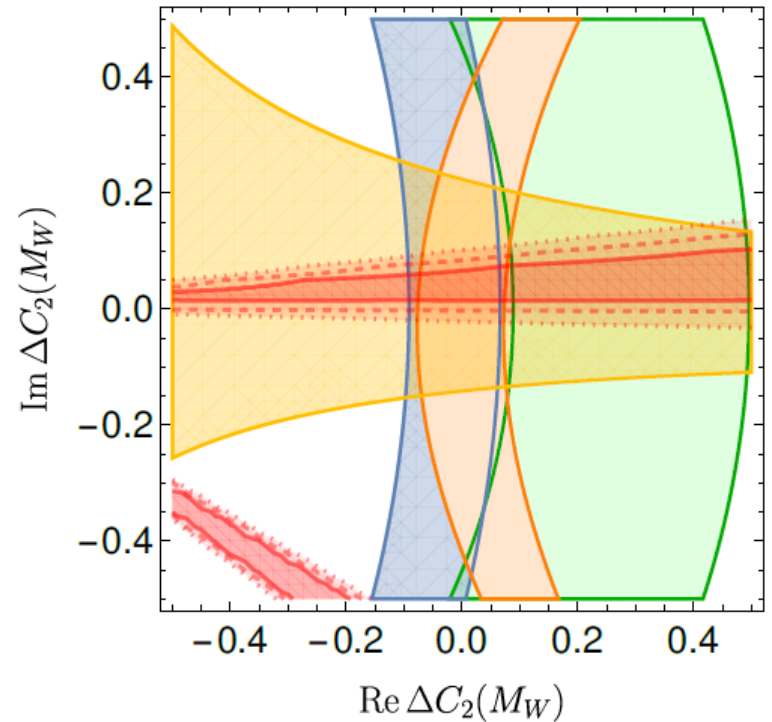
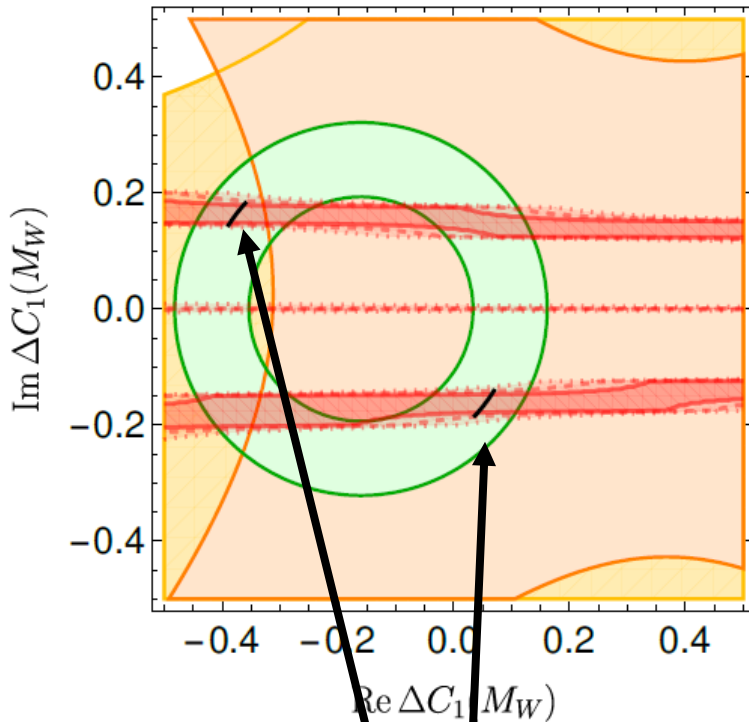
complex ratio $r_{21} = \langle Q_2 \rangle / \langle Q_1 \rangle$

$$\text{e.g. } \lambda_{J/\psi K_S} = \frac{q}{p} \frac{\bar{A}}{A} \propto \frac{C_1^* + r_{21} C_2^*}{C_1 + r_{21} C_2}$$

4 unknowns (Re C, Im C, Re r_{21} , Im r_{21}) : fit to data !

Global analysis: CP-violating case

SJ, Kirk, Lenz, Leslie, arXiv:1910.12924

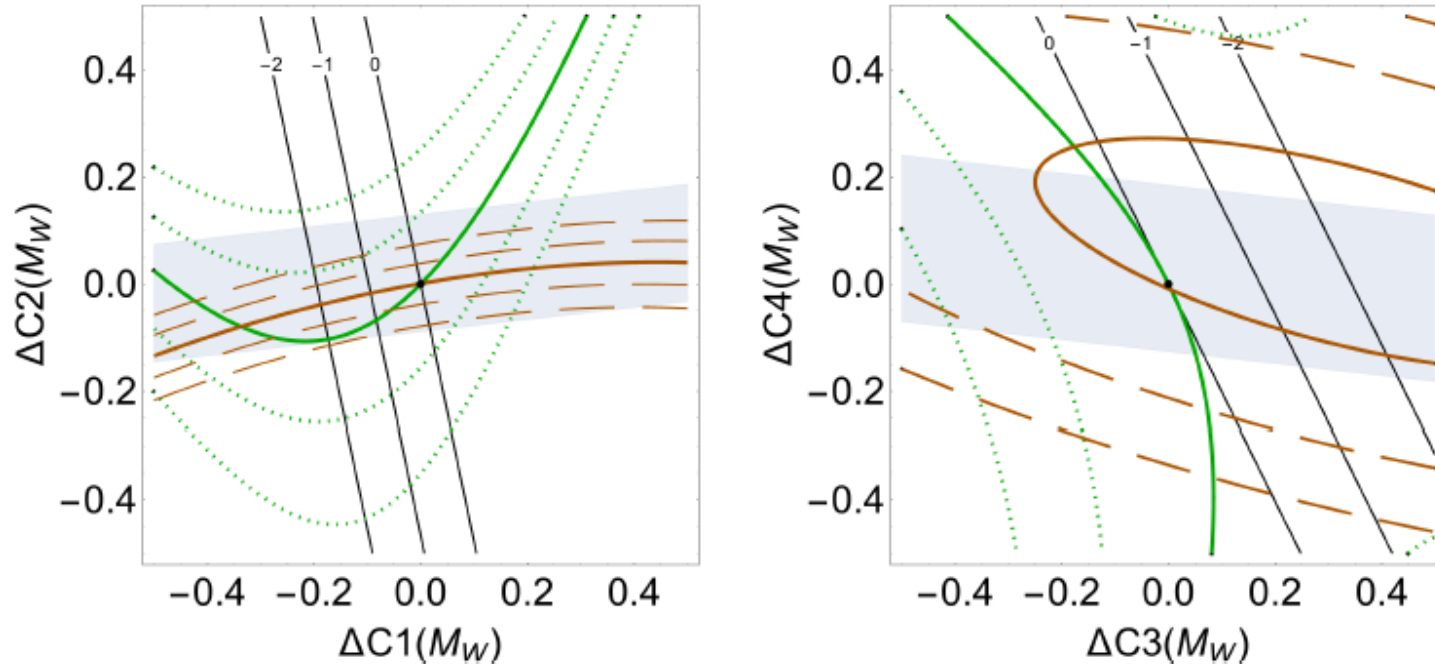


- $\tau(B_s)/\tau(B_d)$
- $\mathcal{B}(B_s \rightarrow X_s \gamma)$
- $\Delta\Gamma_s$
- a_{sl}^s
- $B_d \rightarrow J/\psi K_S$

Fitted r_{21} agrees with naïve (!) factorisation

Future prospects for mixing

SJ, Kirk, Lenz, Leslie arxiv:1701.09183



Brown – width difference, green -- lifetime ratio
solid – SM central value
spacing of contours – projected half-width of a 1- σ band
Grey – current $BR(B \rightarrow X_s \gamma)$

Assumptions: 5% combined (th/exp) error on width difference
0.001 combined error on lifetime ratio

Conclusions

The LHCb updates on R_{K^*} and on $BR(B_s \rightarrow \mu\mu)$ have increased the tension with the SM to 4.0σ . ATLAS contribution is and will be important.

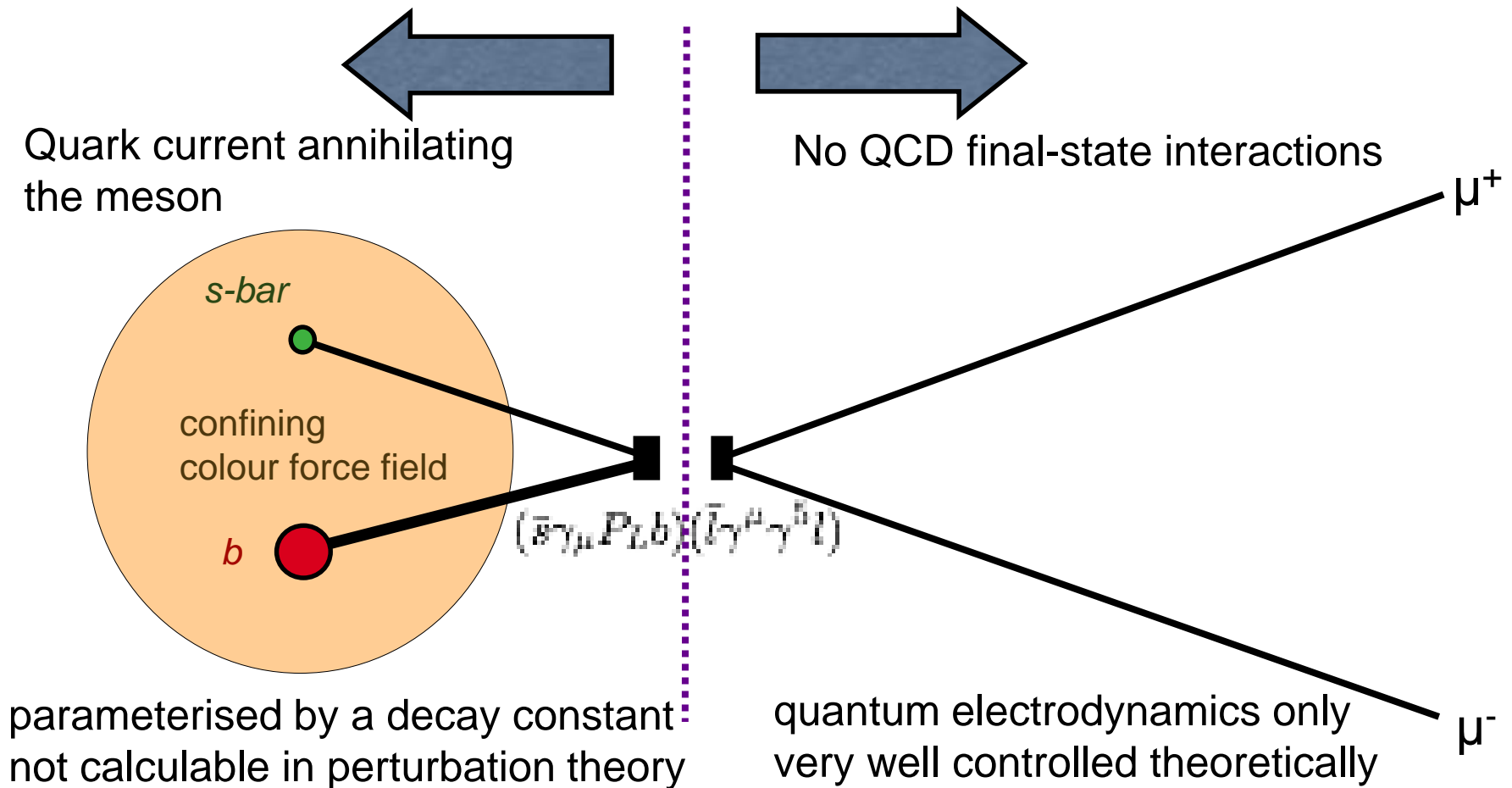
The leptonic decay itself is more than 2σ off and plays an important role in pinning down a region in the 2-parameter BSM fit [always assuming left-handed quark interactions]

In my opinion, this is unlikely to be a statistical fluctuation and very unlikely to be a theoretical issue.

BSM involving charm quarks may contribute to $P5'$ anomaly (not R_{K^*}) and provide connection with theoretically controlled hadronic observables (lifetime differences/ratios, CPV in $B \rightarrow J/\psi K$ etc).

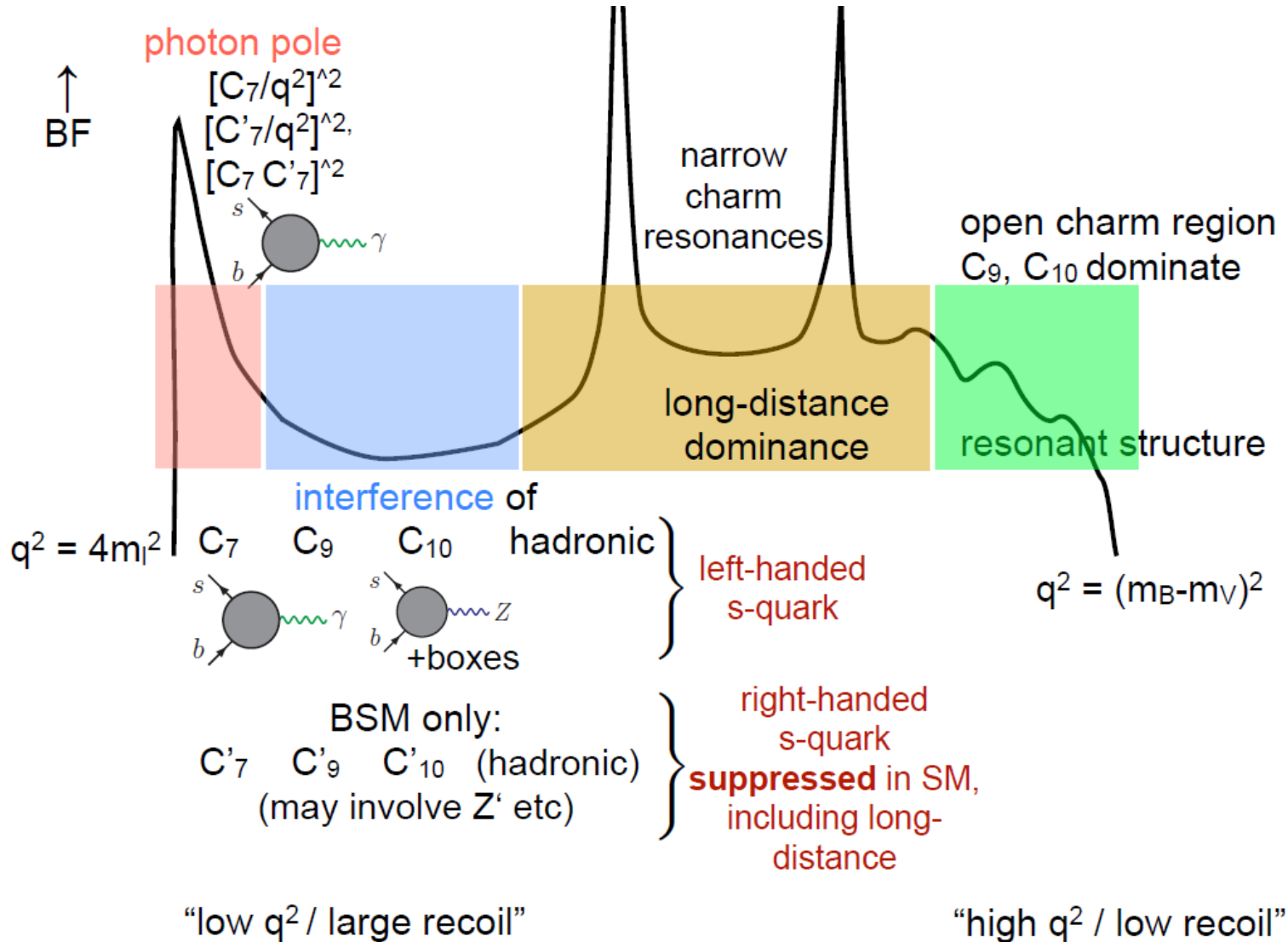
BACKUP

Leptonic decay



Very small long-distance QED corrections Beneke, Bobeth, Szafron 2019

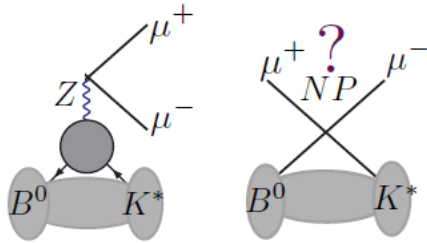
B->V | I: rate (schematic)



Decay amplitude structure

Two mechanisms to produce dilepton in & beyond SM

- via axial lepton current (in SM: Z, boxes) **C10**



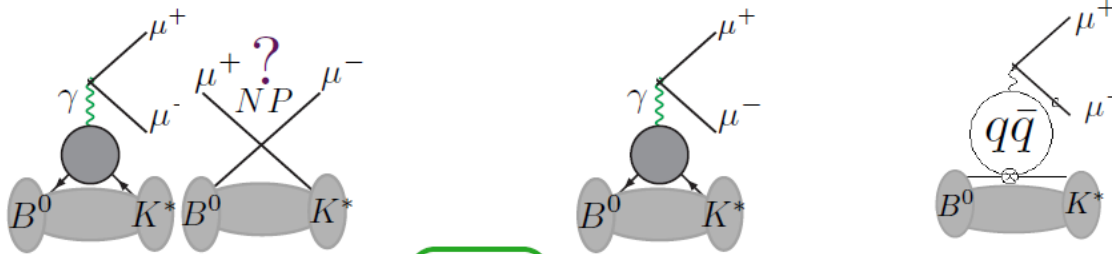
K^* helicity

$$H_A(\lambda) \propto \tilde{V}_\lambda(q^2) C_{10} - V_{-\lambda}(q^2) C'_{10}$$

one form factor (nonperturbative) per helicity
amplitudes factorize naively

[nb - one more amplitude if not neglecting lepton mass]

- via vector lepton current (in SM: (mainly) photon) **C7, C9, hadronic hamiltonian**



$$H_V(\lambda) \propto \tilde{V}_\lambda(q^2) C_9 - V_{-\lambda}(q^2) C'_9 + \frac{2m_b m_B}{q^2} \left(\tilde{T}_\lambda(q^2) C_7 - \tilde{T}_{-\lambda}(q^2) C'_7 \right) - \frac{16\pi^2 m_B^2}{q^2} h_\lambda(q^2)$$

photon pole at $q^2=0$

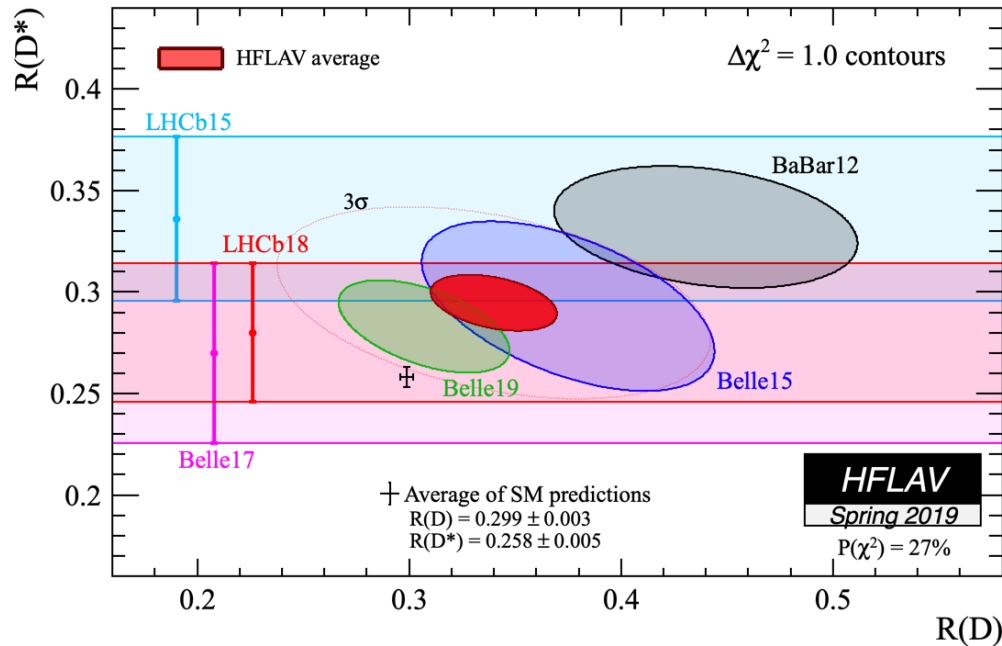
two form factors interfere for each helicity

nonlocal “quark loops”
do **not** factorize naively

Natural, systematic discussion in terms of helicity amplitudes **SJ, Martin Camalich 2012, 2014**

Photon pole absent for helicity-0 (form factor rescaling)

Non-rare semileptonic decays



$$R(D^{(*)}) = \frac{BR(B \rightarrow D^{(*)}\tau\nu_\tau)}{BR(B \rightarrow D^{(*)}\ell\nu_\ell)}$$

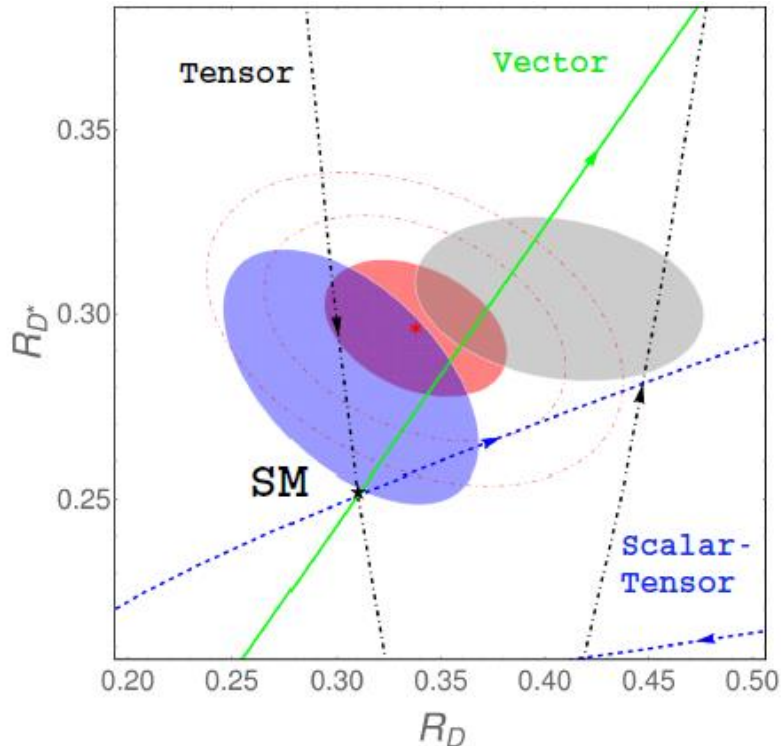
SM tree-level

large effect; theory error still (almost) negligible

Possible BSM

ϵ_R^l flavour-universal by SU(2) x U(1) invariance (no dim-6 SMEFT operator)

$$\mathcal{L}_{\text{eff}}^{\text{LE}} \supset -\frac{4G_F V_{cb}}{\sqrt{2}} [(1 + \epsilon_L^\tau)(\bar{\tau}\gamma_\mu P_L \nu_\tau)(\bar{c}\gamma^\mu P_L b) + \epsilon_R^\tau(\bar{\tau}\gamma_\mu P_L \nu_\tau)(\bar{c}\gamma^\mu P_L b) + \epsilon_{S_L}^\tau(\bar{\tau} P_L \nu_\tau)(\bar{c} P_L b) + \epsilon_{S_R}^\tau(\bar{\tau} P_L \nu_\tau)(\bar{c} P_R b) + \epsilon_T^\tau(\bar{\tau}\sigma_{\mu\nu} P_L \nu_\tau)(\bar{c}\sigma^{\mu\nu} P_L b)] + \text{H.c.},$$



Best fit value moved **substantially** closer to SM with Belle 2019 update

Different BSM operators imply different correlations between shifts to R_D , R_{D^*}

Scale of new physics & no-lose theorem

Di Luzio, Nardecchia 2017

The B-decay anomalies point to (at least) the interactions

$$\frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L) \qquad \frac{1}{\Lambda^2} (\bar{c}_L \gamma^\mu b_L) (\bar{\nu}_\tau \gamma_\mu \tau_L)$$

numerically $\Lambda \sim 30$ TeV and $\Lambda \sim 3$ TeV, respectively

(The latter operator is suggested by the $R_{D^{(*)}}$ anomalies, which I did not discuss.)

- Recall in the case of the Fermi theory, $G_F \sim g^2/M_W^2$

- Redoing the calculation here, $M_{NP} = g_{NP} \Lambda \leq 4\pi \Lambda$.
For the **rare decay** anomalies, at most 300-400 TeV.

Partial-wave unitarity: maximal NP scale **below 100 TeV**.

If the NP is less than maximally flavour-violating, or the NP is weakly coupled, the scale will be 1-2 orders of magnitudes lower.

While the bounds are (so far) high, the fact that there are any at all should be encouraging, further refinements may be possible.

$SU(2)_W$ & model-independent constraints

Two purely left-handed $SU(2)$ invariants once doublet structure of fermions considered (for each choice of generation indices)

$$O_S = (\bar{L}\gamma_\mu \bar{L})(\bar{Q}\gamma^\mu Q) \quad O_T = (\bar{L}\gamma_\mu \sigma^I \bar{L})(\bar{Q}\gamma^\mu \sigma^I Q)$$

Both operators contribute to further processes that are experimentally constrained, in particular:

$$B \rightarrow K^* \nu\nu \quad \rightarrow \quad C_{T,3323} \approx C_{S,3323}$$

at one loop:

$$Z \rightarrow \pi\pi, Z \rightarrow \nu\nu$$

$$\tau \rightarrow Z^* \mu, W^* \nu \quad (\rightarrow 3 \text{ leptons})$$

Problematic for very low Λ

Tree-level mediators: leptoquarks

Scalar or vector leptoquarks can generate interactions

Eg Gripaos, Nardecchia, Renner, ...
(Hiller, Nisandzic 2017)

$$\frac{1}{\Lambda^2} (\bar{c}_L \gamma^\mu b_L) (\bar{\nu}_\tau \gamma_\mu \tau_L)$$

$$\frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

$(3, 1, -1/3)$ or $(3, 3, 2/3)$

$(3, 3, -1/3)$

$(3, 1, 2/3)$ or $(3, 3, 2/3)$

$(3, 1, 2/3)$ or $(3, 3, 2/3)$

(more possibilities at loop level Eg Bauer, Neubert; Becirevic et al)

Tree-level mediators: W' , Z'

$$\frac{1}{\Lambda^2} (\bar{c}_L \gamma^\mu b_L) (\bar{\nu}_\tau \gamma_\mu \tau_L)$$

$$\frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

$(0, 3, 0)$

$(0, 3, 0)$ or $(0, 1, 0)$

- appear as resonances in composite models (KK excitations in RS)
- Z' exchange contributes to B_s mixing at tree-level (unlike leptoquarks)

Isidori et al, Quiros et al, Ligeti et al, Becirevic et al, Crivellin et al,

...

A Z' model for $R_{K^{(*)}}$

Accommodating *all* $b \rightarrow s$ II anomalies *requires* a muon-specific C_L – type interaction

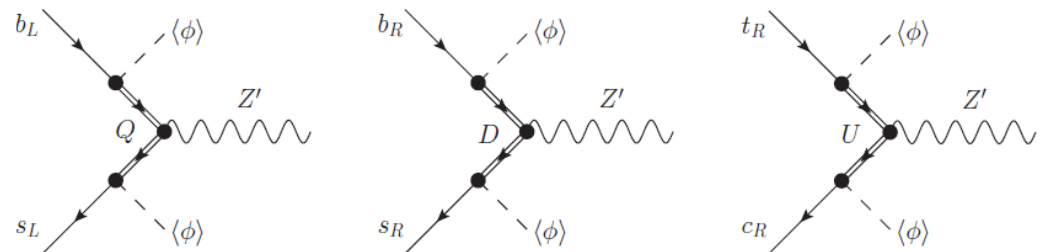
$$\frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

with $\Lambda \sim 30$ TeV

However, C_R is weakly constrained and can also be present.

Anomaly-free Z' model with gauged $L_\mu - L_\tau$, nonminimal (dim-6) coupling to quarks, can eg come from heavy vectorlike quarks:

Altmannshofer et al 2014



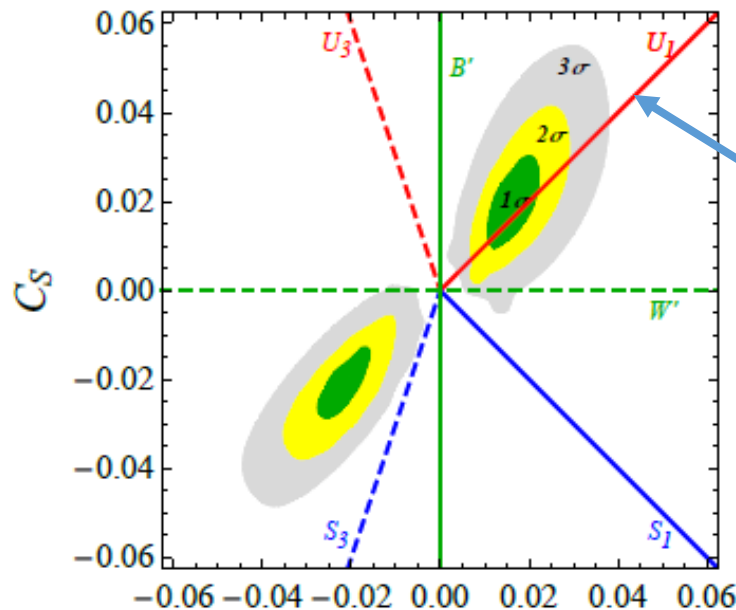
The small coupling to quarks suppresses contributions to B_s mixing

Also Crivellin et al, ...

Global fit & single mediators

- Global fit to anomalies, previously mentioned constraints, and the coefficients of the two purely left-handed operators
- Compare to pattern predicted by a single mediator

(Axis scales depend on flavour structure of mediator couplings, fitted simultaneously.)



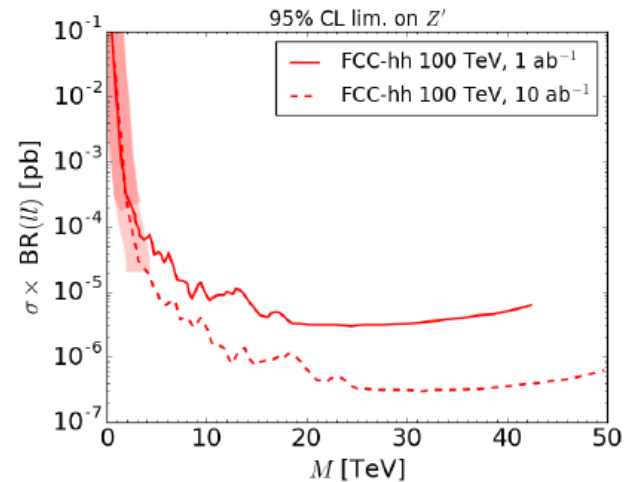
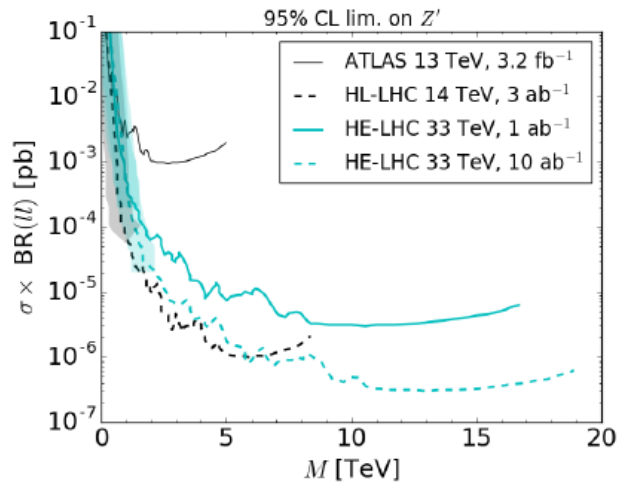
(3, 1, 2/3)
vector
leptoquark

C_T
Buttazzo, Greljo, Isidori, Marzoca arXiv:1706.07808

Future collider direct searches

Allanach, Gripaos, You arXiv:1710.06363

- Consider simplified Z' and LQ models of $R_{K(*)}$



FCC-hh 100 TeV 1 ab⁻¹ covers all of viable Z' parameter space, 33 TeV LHC “most”,

Leptoquark coverage slightly less perfect

C_9 from BSM $(\bar{s}b)(\bar{c}c)$ operators

SJ, Kirk, Lenz, Leslie arxiv:1701.09183

SJ, Kirk, Lenz, Leslie w.i.p.

&

Evolution from M_W to 4.6 GeV: $[Q_{3,4} \sim (\bar{s}_L \gamma^\mu b_L)(\bar{c}_R \gamma_\mu c_R)]$

$$\Delta C_7^{\text{eff}} = 0.02\Delta C_1 - 0.19\Delta C_2 - 0.01\Delta C_3 - 0.13\Delta C_4$$

$$\Delta C_9^{\text{eff}} = 8.48\Delta C_1 + 1.96\Delta C_2 - 4.24\Delta C_3 - 1.91\Delta C_4$$

- Setting ΔC_2 to 1 and rest to zero, reproduce the (large) SM charm contribution to $C_9(4.6 \text{ GeV})$.

But C_1 and C_3 are even more effective in generating C_9 !

- C_2 and C_4 feed strongly into C_7^{eff} , hence $B \rightarrow X_s \gamma$

But C_1 and C_3 are practically irrelevant for radiative decay!

Interesting interconnections between rare decays and B-lifetime (difference) observables

C_9 from BSM $(\bar{s}b)(\bar{\tau}\tau)$ operators

Bobeth, Haisch arXiv:1109.1826

Crivellin et al arXiv:1807.02068

Similarly strong RG mixing into C_9 as in charming BSM case

- This operator is automatically present for “left-handed” $R_{D^{(*)}}$ explanations via $(\bar{c}_L \gamma^\mu b_L) (\bar{\nu}_\tau \gamma_\mu \tau_L)$

This is a consequence of $SU(2)_W$ symmetry and the experimental bound on $B \rightarrow K^* \nu \bar{\nu}$ [Buras et al arXiv:1409.4557](#)

- Radiatively generated C_9 is again $O(1)$ and negative (and lepton-universal)

τ