

Theorist's perspective: BSM & flavour

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Precision frontier: beyond QED

Some past indirect discoveries

parity violation

Lee, Yang 1956
Wu et al, Goldhaber et al 1957

V-A structure of weak interactions

Feynman, Gell-Mann 1957
Shudarshan, Marshak 1957

universality of weak decays

Gell-Mann, Levy 1960

CP violation

Christenson et al 1964

electroweak symmetry breaking

BEHGHK, Glashow, Salam, Weinberg, 1960-67

charm to explain $K_L \rightarrow \mu\mu$ suppression

Glashow, Iliopoulos, Maiani 1970

third generation to explain CPV

Kobayashi, Maskawa 1972

Neutral currents ('73), charm('74), 3rd gen. ('75), W,Z ('83), Higgs ('12) later discovered.

$$H_W \sim G_F (\bar{p}\gamma^\mu n) (\bar{e}\gamma_\mu \nu) \quad (\text{Fermi 1934}) \quad \longrightarrow \quad \begin{array}{c} u \\ \diagdown \\ \text{---} W \text{---} \\ \diagup \\ e \end{array} \quad G_F = \frac{g^2}{4\sqrt{2}M_W^2} \quad \text{post-GSW}$$

The Standard Model

spin 1

electromagnetism U(1)

weak interactions SU(2)

strong interactions SU(3)

universal

couplings

3 generations

spin 1/2

$\begin{pmatrix} u_L \\ d_L \end{pmatrix}$	$\begin{pmatrix} u_R \\ d_R \end{pmatrix}$	$\begin{pmatrix} c_L \\ s_L \end{pmatrix}$	$\begin{pmatrix} c_R \\ s_R \end{pmatrix}$	$\begin{pmatrix} t_L \\ b_L \end{pmatrix}$	$\begin{pmatrix} t_R \\ b_R \end{pmatrix}$	$Q = +2/3$
$\begin{pmatrix} \nu_{eL} \\ e_L \end{pmatrix}$	$\begin{pmatrix} - \\ e_R \end{pmatrix}$	$\begin{pmatrix} \nu_{\mu L} \\ \mu_L \end{pmatrix}$	$\begin{pmatrix} - \\ \mu_R \end{pmatrix}$	$\begin{pmatrix} \nu_{\tau L} \\ \tau_L \end{pmatrix}$	$\begin{pmatrix} - \\ \tau_R \end{pmatrix}$	$Q = -1/3$
						$Q = 0$
						$Q = -1$

spin 0

Higgs - sets mass scale of entire Standard Model

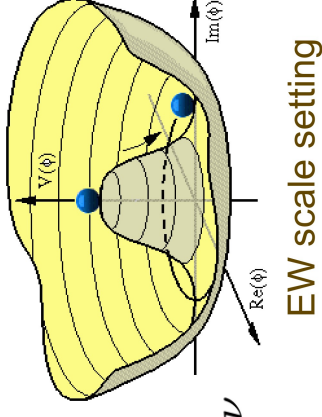
Origin of masses? Flavour mixings? What determines the weak scale?

Dynamics

At length scales above an attometre we have approximately (up to gravity)

$SU(3)^5$ flavour symmetric kinetic/gauge terms

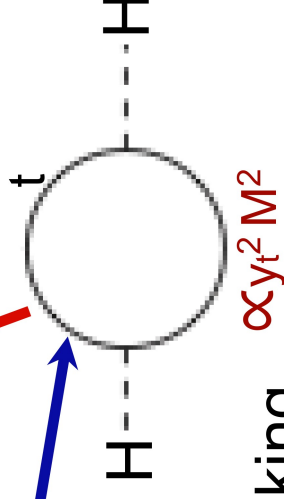
$$\mathcal{L}_{SM} = \sum_f \bar{\psi}_f \gamma^\mu D_\mu \psi_f - \frac{1}{4} \sum_i a \frac{g_i}{4} F_{\mu\nu}^{ia} F^{ia\mu\nu}$$



EW scale setting

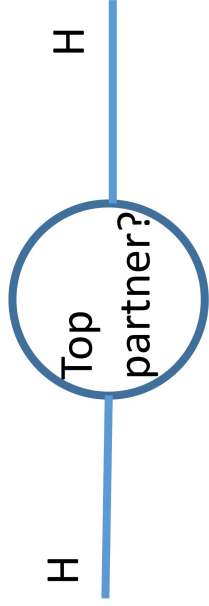
$$-\bar{u}_R Y^U \phi^{c\dagger} q_L - \bar{d}_R Y^D \phi^\dagger q_L - \bar{e}_R Y^E \phi^\dagger l_L - \mu^2 \phi^\dagger \phi - \frac{\lambda}{2} (\phi^\dagger \phi)^2$$

flavour-breaking fermion masses and Higgs couplings

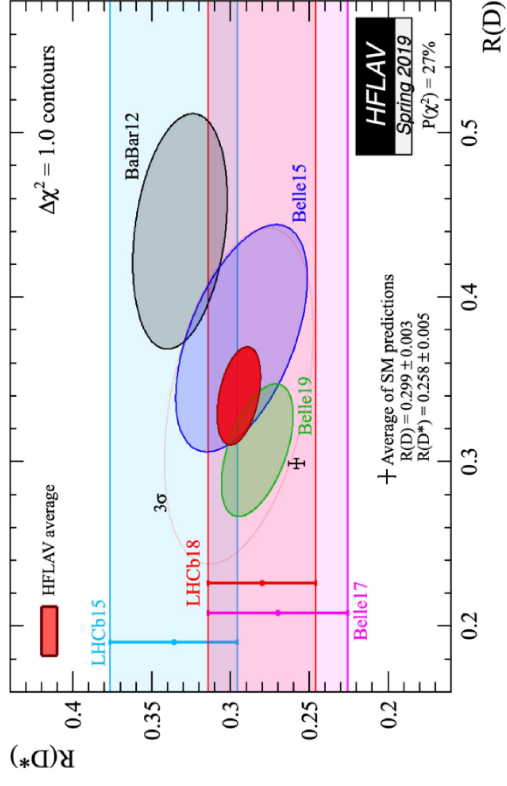
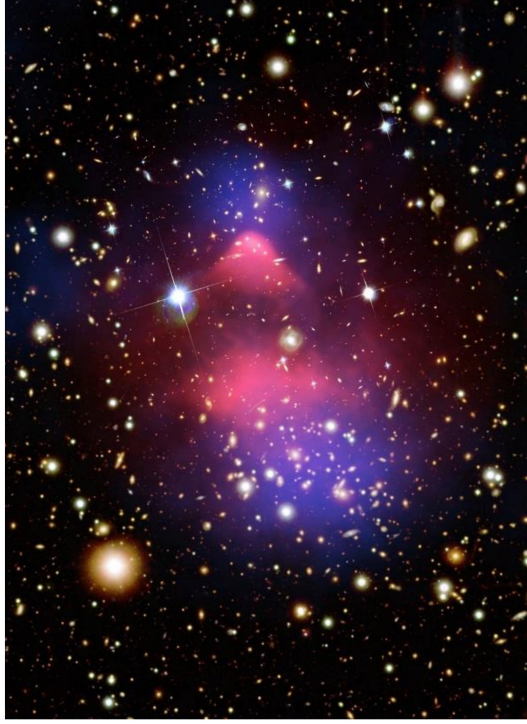
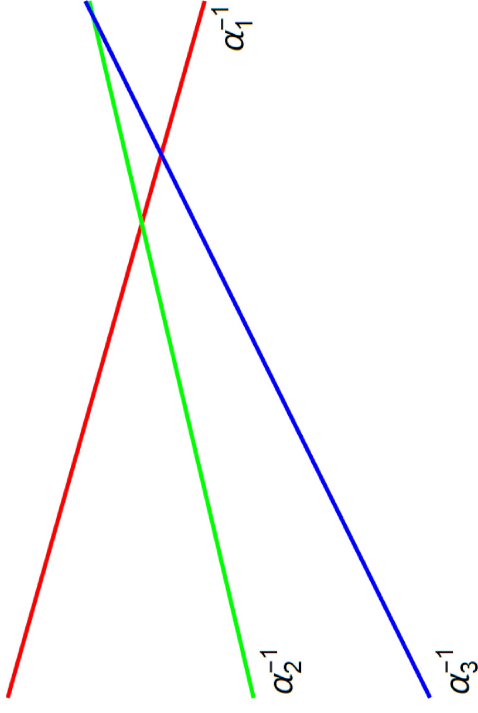


Quadratic divergence from flavour-breaking sources \rightarrow any cure likely to be flavour-breaking (happens in SUSY, composite Higgs, ...)

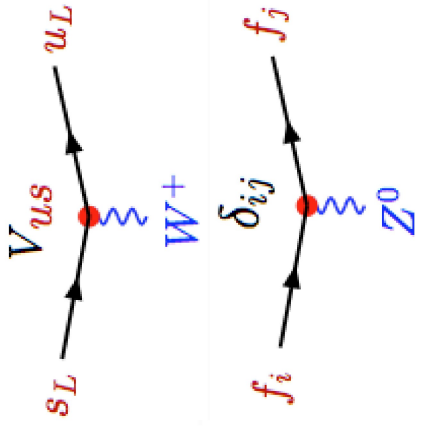
Beyond the SM



$$\Delta m_H^2 \propto y_t^2 \Lambda_{UV}^2$$



Flavour physics & rare decays



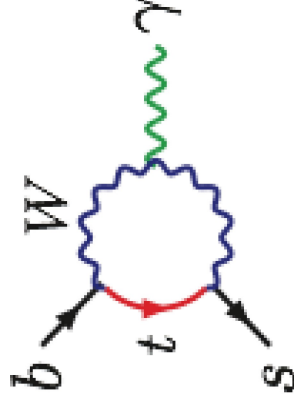
all flavour violation in charged weak current

(tree level) neutral current conserves flavor

strong & electromagnetic preserve flavour

Loop and CKM/GIM suppression of flavour-changing neutral current processes

-> **enhanced BSM sensitivity**



Flavour: the dogs that did not bark

From AC Doyle, “The Adventure of Silver Blaze” [with thanks to J Ellis]

Gregory (Scotland Yard detective): “Is there any other point to which you would wish to draw my attention?”

Holmes: “To the curious incident of the dog in the night-time.”

Gregory: “The dog did nothing in the night-time

Holmes: “That was the curious incident.”



Quote and S Paget's illustration via Wikipedia

Absence of an effect in a BSM-sensitive observable can be as important a clue as an anomaly.

Eg Meson-antimeson mixing \rightarrow constrain NP scales up to 10^5 TeV (for maximally flavor-violating BP)

Where to look

Observables with **suppressed and/or controlled SM contribution**

- flavour-changing neutral currents, eg

Meson-antimeson mixing (B_s, B_d, D, K)

$b \rightarrow s \mu^+ \mu^-$ and $b \rightarrow s \gamma$

$B \rightarrow K^{(*)} \mu^+ \mu^-$, $B \rightarrow K^{(*)} e^+ e^-$, $B_s \rightarrow \phi \mu^+ \mu^-$
 $B \rightarrow K^{(*)} \gamma$

$B \rightarrow X_s \mu^+ \mu^-$, $B \rightarrow X_s \gamma$

$s \rightarrow d \nu \nu$

$K^+ \rightarrow \pi^+ \nu \nu$

- lepton-flavour ratios, eg

$BR(B \rightarrow K^{(*)} \mu^+ \mu^-) / BR(B \rightarrow K^{(*)} e^+ e^-) - 1$

$BR(B \rightarrow D^{(*)} \tau \nu) / BR(B \rightarrow D^{(*)} l \nu) - (SM)$

- CP violation, eg

$K_L \rightarrow \pi \pi$ (ϵ_K, ϵ'_K)

$K_L \rightarrow \pi^0 \nu \nu$

Babar, Belle
 LHCb, ATLAS, CMS
 Belle2


Babar, Belle, Belle2

NA62 (CERN)

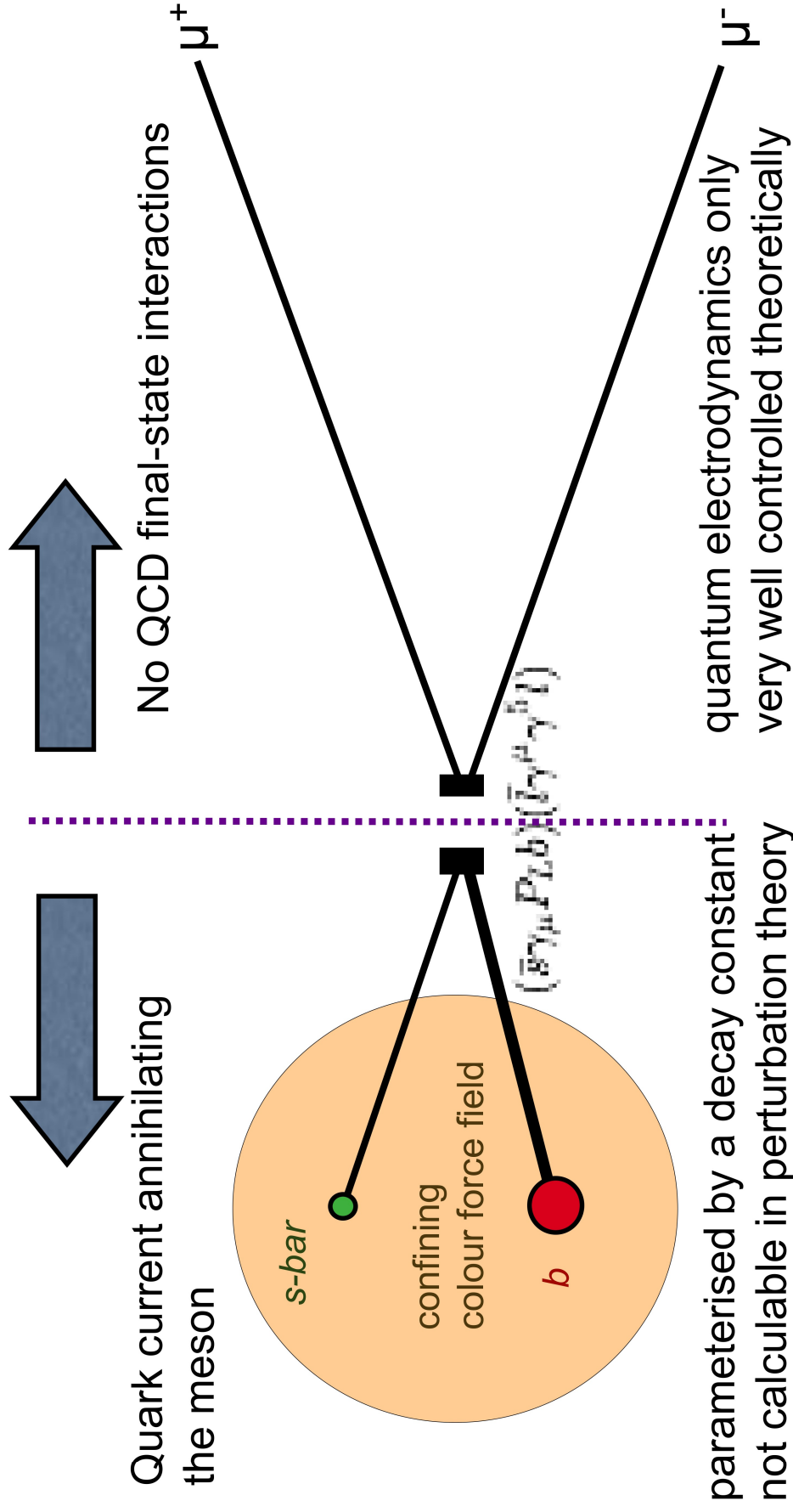
Babar, Belle, LHCb
 Belle2

..., NA48, KTeV
 KOTO

ATLAS analyses

Analysis	Expected/plausible BSM scale	theory	current BSM significance
B(s,d) \rightarrow $\mu\mu$	(few) TeV (nat'lness)	excellent	2-3 σ
RK(*)	(few) TeV (nat'lness)	excellent	3-4 σ
B \rightarrow K* $\mu\mu$ (ee?) angular	(few) TeV (nat'lness)	good (P5') to excellent (rh current)	unclear
Tau \rightarrow 3 μ	GUT scale or below	excellent	none
B \rightarrow J/ ψ ϕ etc	(few) TeV	depends	none
B lifetimes	(few) TeV	depends	none
4 muons searches			
Bc/Bc(2S)			
Pentaquark/Zc			
CPV in b from $t\bar{t}$ bar			
		Outside scope of what I can discuss in this talk	

A “clean” observable: Leptonic decay

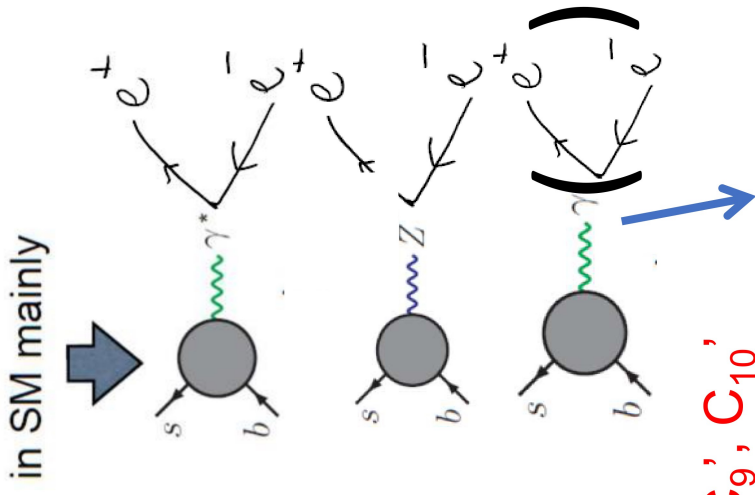


parameterised by a decay constant
not calculable in perturbation theory

Very small long-distance QED corrections [Beneke, Bobeth, Szafron 2019](#)

Rare B-decay: short-distance (theory)

BSM (and SM weak interactions) enter flavour physics through **effective contact interactions** (SMEFT/ H_{weak})



C_9 : dilepton from vector current

$$(\bar{s}\gamma_\mu P_L b)(\bar{l}\gamma^\mu l)$$

C_{10} : dilepton from axial current

$$(\bar{s}\gamma_\mu P_L b)(\bar{l}\gamma^\mu \gamma^5 l)$$

C_7 : dilepton from dipole

$$(\bar{s}\sigma^{\mu\nu} P_R b)F_{\mu\nu}$$

+parity conjugate “right-handed currents” - C_7', C_9', C_{10}' , suppressed by m_s/m_b in SM

Alternative basis with chiral leptons l_L, l_R

$$C_L = (C_9 - C_{10})/2 \quad C_R = (C_9 + C_{10})/2$$

Can also have real photon

Also “clean”: Lepton-flavour ratios

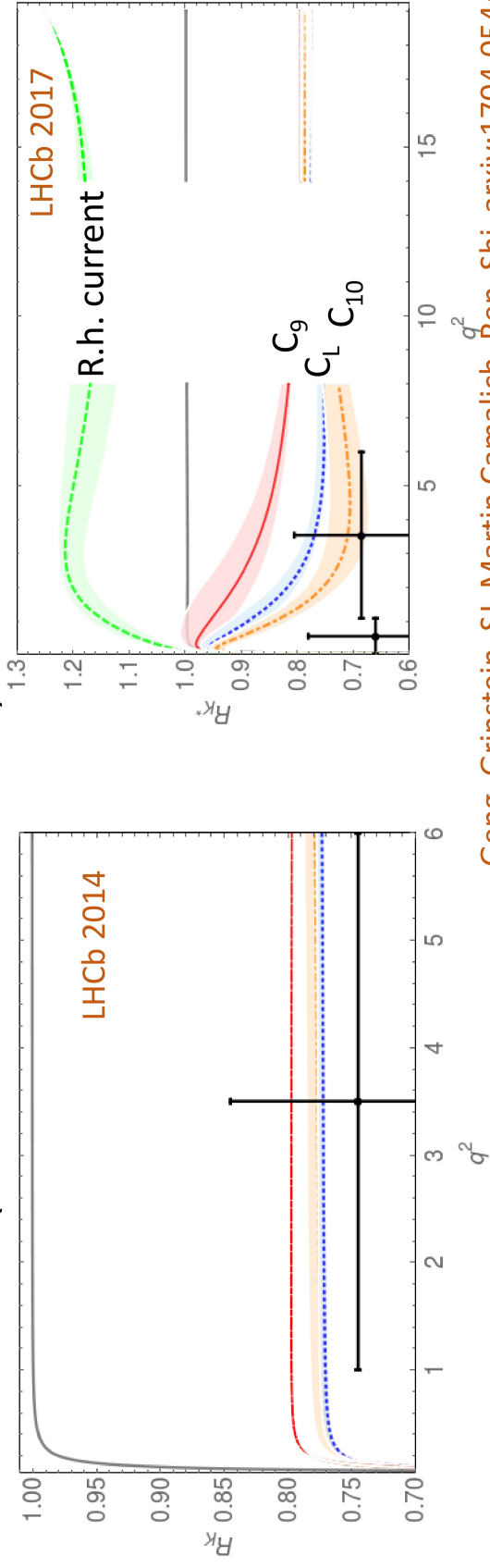
$$R_{K^{(*)}}[a, b] = \frac{\int_a^b \frac{d\Gamma}{dq^2}(B \rightarrow K^{(*)} \mu^+ \mu^-) dq^2}{\int_a^b \frac{d\Gamma}{dq^2}(B \rightarrow K^{(*)} e^+ e^-) dq^2}$$

Theory uncertainties largely cancel out, negligible relative to experiment.

leading is QED: net effect <1% after experimental corrections

[Bordone, Isidori, Pattori 2016](#); [Isidori, Nabeebaccus, Zwicky 2020](#)

Situation in 2017 (first R_{K^*} measurement):



[Geng, Grinstein, SJ, Martin Camalich, Ren, Shi arxiv:1704.05446](#)

Rare B-decay anomalies – fit to data

Observables in the fit

Basic idea: use only observables which are sensitive to $b \rightarrow s$ | | but independent of hadronic form factors, long-distance charm etc.

I.e. $R_{K^{(*)}}$ and $B_s \rightarrow \mu \mu$.

This is a well-defined set of observables, first employed in 2017, with several data updates since then. No “look-elsewhere effect” to take into account.

In the following I describe the fit in arXiv:2103.12738 (Geng, Grinstein, SJ, Li, Martin Camalich, Shi); see also work by Altmannshofer & Stangl and a few others

A note on the $B_s \rightarrow \mu\mu$ input

Together with the R_{K^*} update, LHCb presented a significant update to $BR(B_s \rightarrow \mu\mu)$

ATLAS and CMS have also measured this

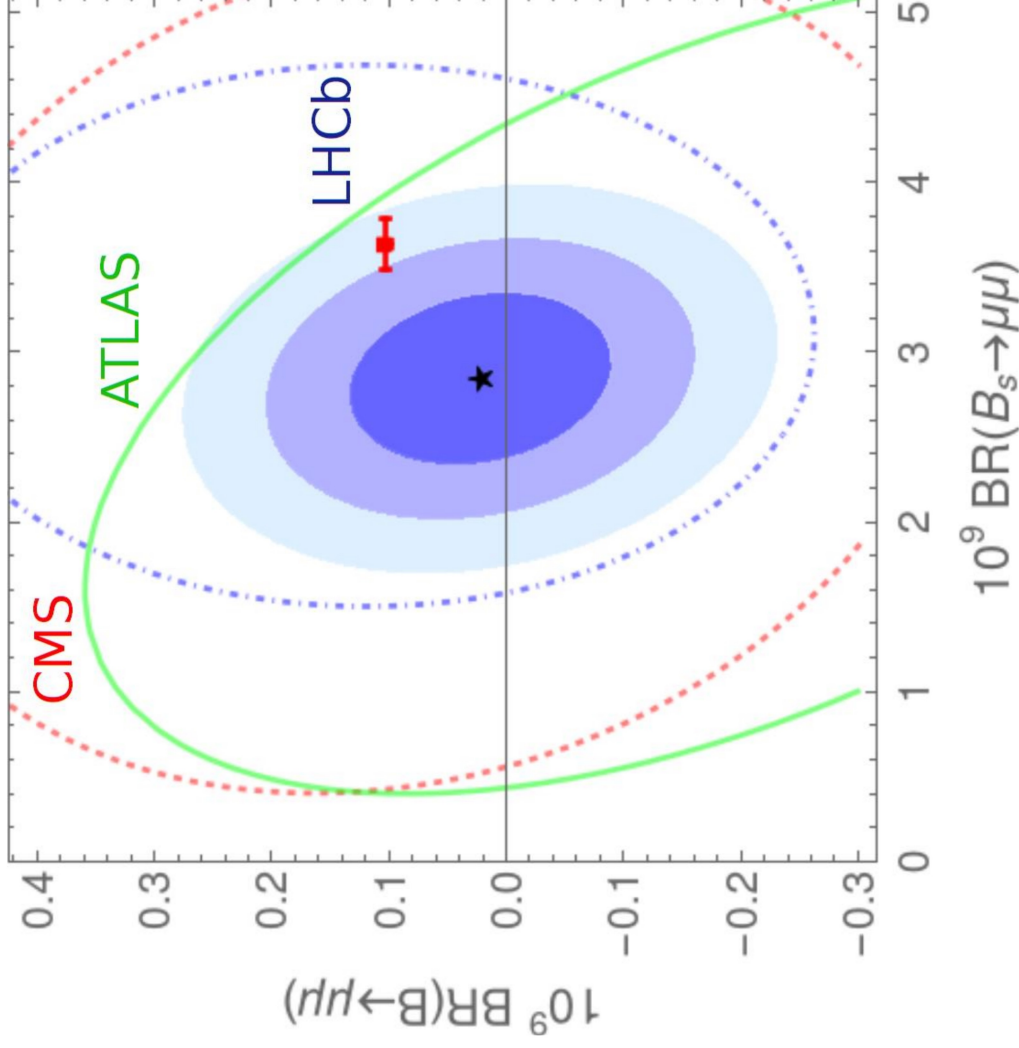
Measurements show non-negligible correlations with $BR(B_d \rightarrow \mu\mu)$ (biggest in ATLAS).

Hence to obtain a $BR(B_s \rightarrow \mu\mu)$ average first combine the 3x2 measurements.

Then profile over $BR(B_d \rightarrow \mu\mu)$.

$B_q \rightarrow \mu\mu$ world combination

Geng, Grinstein, SJ, Li, Martin Camalich, Shi arXiv:2103.12738



From this:

$$\text{BR}(B_s \rightarrow \mu\mu) = (2.8 \pm 0.3) 10^{-9}$$

$$\chi^2_{\text{min}} = 3.75 \text{ (5 d.o.f.)}$$

Input data

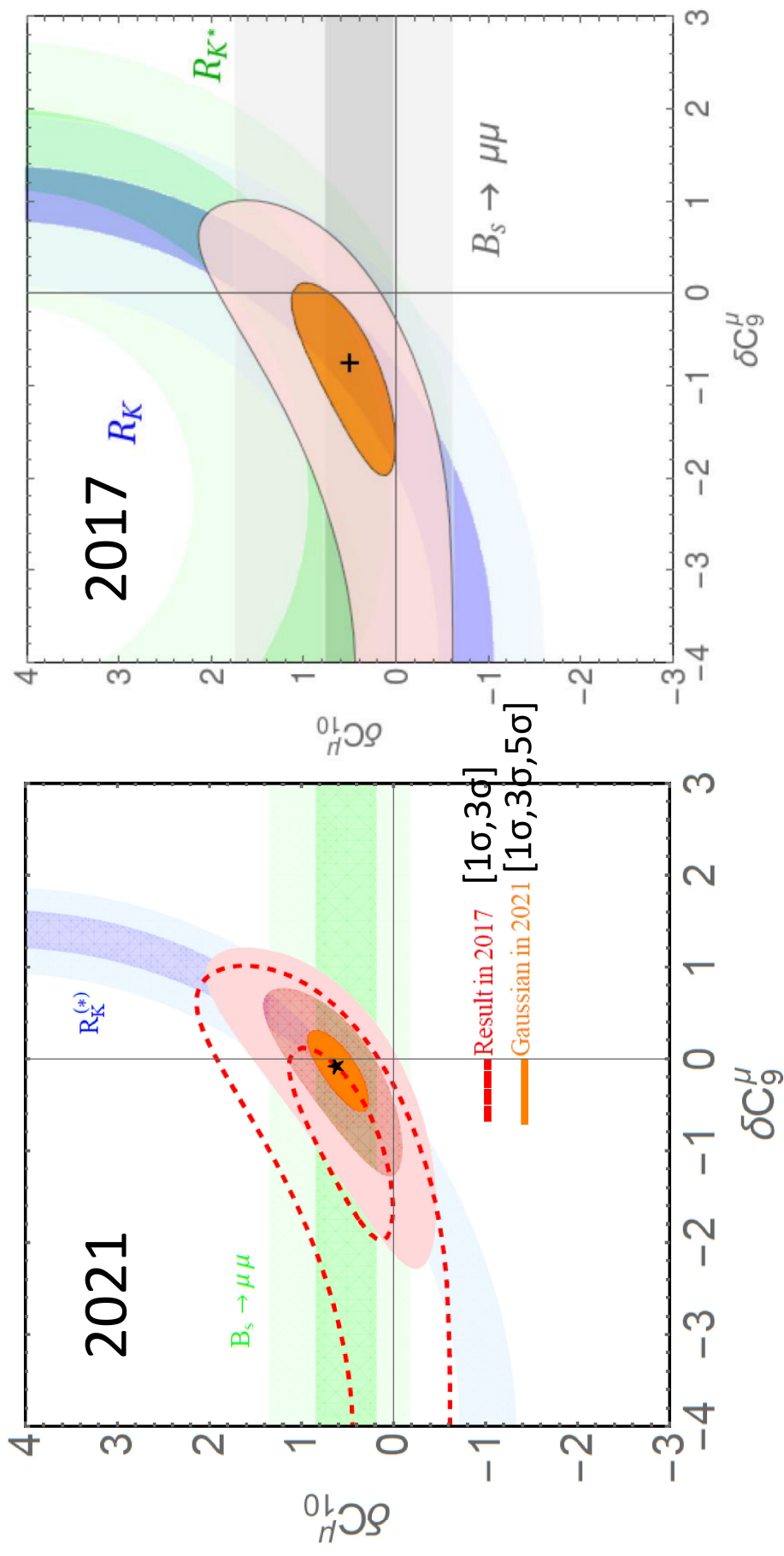
Observable	Value	Source	Reference
	$(2.8_{-0.7}^{+0.8}) \times 10^{-9}$	ATLAS	[11]
	$(2.9 \pm 0.7 \pm 0.2) \times 10^{-9}$	CMS	[12]
$BR(B_s \rightarrow \mu^+ \mu^-)$	$(3.09_{-0.43-0.11}^{+0.46+0.15}) \times 10^{-9}$	LHCb update	[10]
	$(2.842 \pm 0.333) \times 10^{-9}$	our average	this work
	$(3.63 \pm 0.13) \times 10^{-9}$	SM prediction	[13]
$R_K[1.1, 6]$	0.846 ± 0.044	LHCb	[6]
$R_K[1, 6]$	1.03 ± 0.28	Belle	[14]
$R_{K^*}[0.045, 1.1]$	0.660 ± 0.113	LHCb	[15]
$R_{K^*}[1.1, 6]$	0.685 ± 0.122	LHCb	[15]
$R_{K^*}[0.045, 1.1]$	0.52 ± 0.365	Belle	[16]
$R_{K^*}[1.1, 6]$	0.96 ± 0.463	Belle	[16]

Self-consistency of dataset: $\chi^2_{\min} = 4.61$ (8 d.o.f.) / $p = 0.80$
 (counting 6 $BR(B_q \rightarrow \mu\mu)$ measurements)

SM p-value is 5.4×10^{-5} (4.0σ) [counting $BR(B_s \rightarrow \mu\mu)$ average]
 reduces to 3.5σ when counting the 6 $BR(B_q \rightarrow \mu\mu)$ measurements
 separately

Clean fit: results: 2-parameter BSM fit

Geng, Grinstein, SJ, Li, Martin Camalich, Shi [arXiv:2103.12738](https://arxiv.org/abs/2103.12738)



Clean fits: numerical results

Geng, Grinstein, SJ, Li, Martin Camalich, Shi arXiv:2103.12738

Fit three 1-parameter scenario (vectorial, axial, left-handed coupling to muons)

TABLE II. Best fit values, χ^2_{\min} , p -value, Pull_{SM} and confidence intervals of the Wilson coefficients in the fits of the R_K , R_{K^*} , $B_s \rightarrow \mu\mu$ data only using Gaussian form χ^2_{th} . For the cases of single Wilson-coefficient fits, we show the 1σ and 3σ confidence intervals. In the $(\delta C_9^\mu, \delta C_{10}^\mu)$ case, the 1σ interval of each Wilson coefficient is obtained by profiling over the other one to take into account their correlation.

Coeff.	best fit	χ^2_{\min}	p -value	Pull_{SM}	1σ range	3σ range	ρ
δC_9^μ	-0.82	14.70 [6 dof]	0.02	4.08	[-1.06, -0.60]	[-1.60, -0.20]	-
δC_{10}^μ	0.65	6.52 [6 dof]	0.37	4.98	[0.52, 0.80]	[0.25, 1.11]	-
δC_L^μ	-0.40	7.36 [6 dof]	0.29	4.89	[-0.48, -0.31]	[-0.66, -0.15]	-
$(\delta C_9^\mu, \delta C_{10}^\mu)$	$(-0.11, 0.59)$	6.38 [5 dof]	0.27	4.62	$\delta C_9^\mu \in [-0.41, 0.17]$	$\delta C_{10}^\mu \in [0.38, 0.81]$	0.762
$(\delta C_L^\mu, \delta C_R^\mu)$	$(-0.35, 0.25)$				$\delta C_L^\mu \in [-0.45, -0.26]$	$\delta C_R^\mu \in [0.00, 0.48]$	0.406

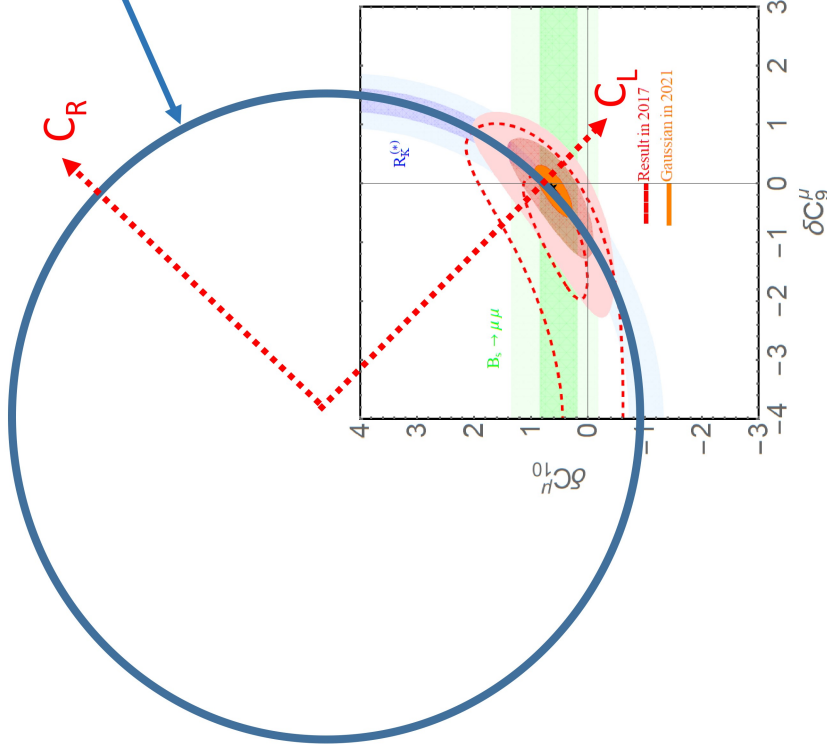
Note that C_L is well-determined in both the left-handed and the two-parameter scenario, with consistent values. Not true for C_9 . Pure C_9 model also much worse fit ($p=1/50$).

$R_K^{(*)}$ and C_L

Assume here that the BSM effect is in the muonic mode, and no right-handed currents.

Because in the SM, $|C_R|, |C_7| \ll |C_L|$,
 $BR \approx \text{const } |C_L^{\text{SM}} + C_L^{\text{BSM}}|^2 + \dots \approx \text{const } |4 + C_L^{\text{BSM}}|^2$ + positive

$BR(B \rightarrow K^{(*)} \mu \mu) =$
 SM value



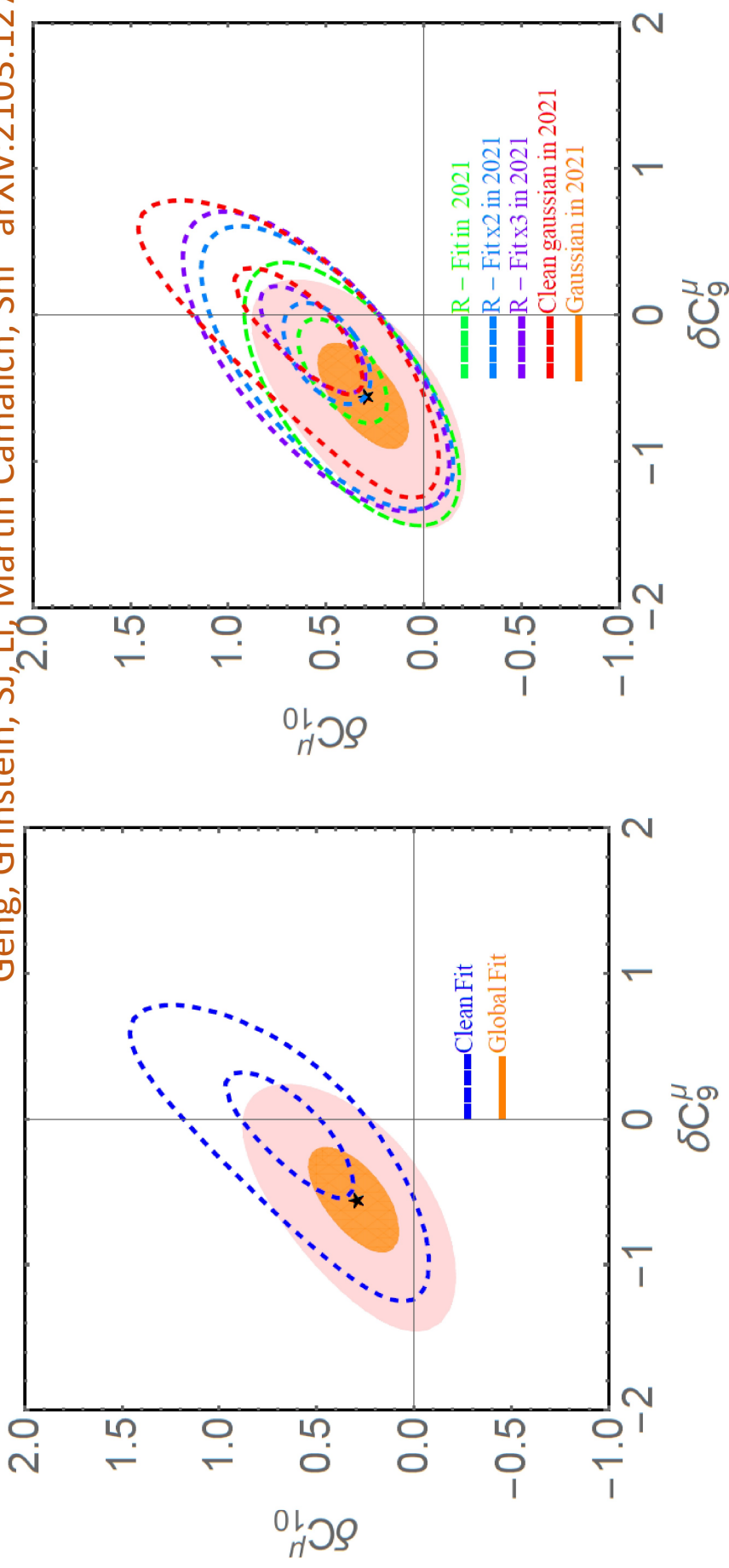
Only C_L^{BSM} can interfere
 destructively: $R_K^{(*)}$ point to
 purely left-handed coupling

$$(\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma^\mu \mu_L)$$

with $\sim -(10-15)\%$ of SM value

Adding $B \rightarrow K^* \mu \mu$ angular data

Geng, Grinstein, SJ, Li, Martin Camalich, Shi arXiv:2103.12738



Left plot: extra data pulls fit approx. along the C_R direction. $C_L=0$ remains excluded at high confidence.

$p(\text{SM})$ up at 0.02

Right plot: effect of increasing hadronic uncertainties

Minimal contact interaction

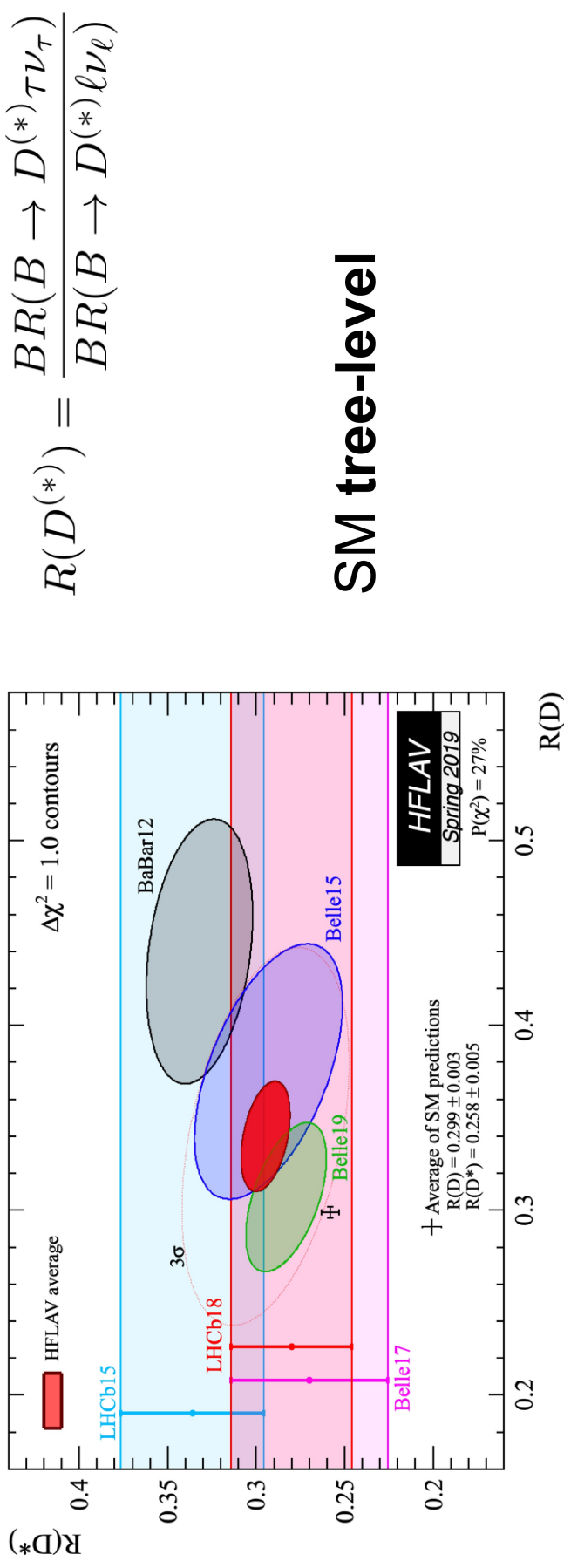
In summary, the B-decay anomalies suggest at a minimum the interaction

$$\frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

numerically $\Lambda \sim 40 \text{ TeV}$

Small enough to be a loop effect even BSM (as it is in SM!)

Non-rare semileptonic decays



$$R(D^{(*)}) = \frac{BR(B \rightarrow D^{(*)}) \tau \nu_\tau}{BR(B \rightarrow D^{(*)}) \ell \nu_\ell}$$

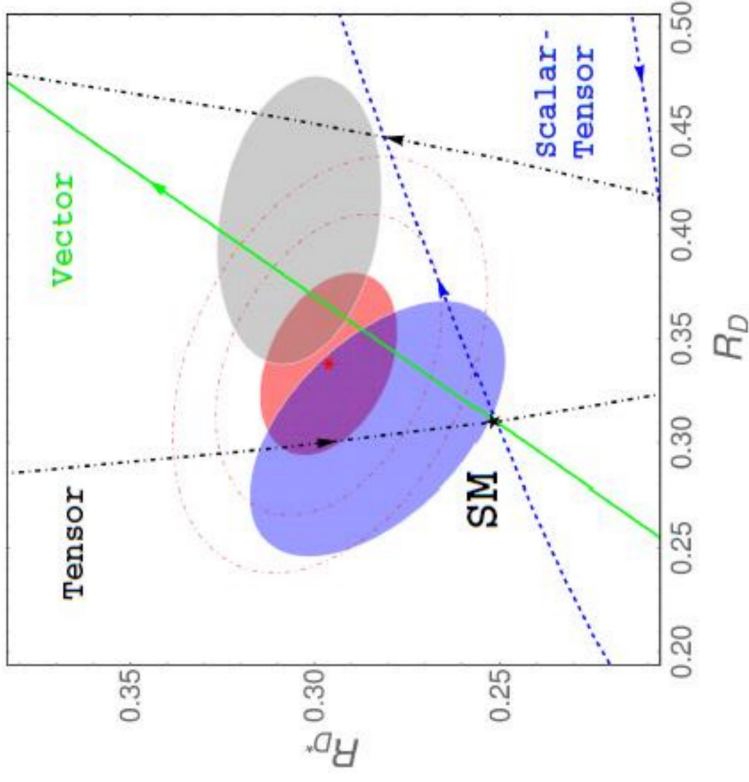
SM tree-level

large effect; theory error still (almost) negligible

Possible BSM

ϵ_R^I flavour-universal by $SU(2) \times U(1)$
 invariance (no dim-6 SMEFT operator)

$$\mathcal{L}_{\text{eff}}^{\text{LE}} \supset -\frac{4G_F V_{cb}}{\sqrt{2}} [(1 + \epsilon_L^I)(\bar{\tau}\gamma_\mu P_L \nu_\tau)(\bar{c}\gamma^\mu P_L b) + \epsilon_R^I(\bar{\tau}\gamma_\mu P_L \nu_\tau)(\bar{c}\gamma^\mu P_L b) + \epsilon_S^I(\bar{\tau} P_{LV_\tau})(\bar{c} P_L b) + \epsilon_T^I(\bar{\tau} P_{LV_\tau})(\bar{c} P_R b) + \epsilon_T^I(\bar{\tau}\sigma_{\mu\nu} P_{LV_\tau})(\bar{c}\sigma^{\mu\nu} P_L b)] + \text{H.c.},$$



Best fit value moved
substantially closer to SM
 with Belle 2019 update

Different BSM operators
 imply different correlations
 between shifts to R_D , R_D^*

BSM implications of B-anomalies (qualitative)

Scale of new physics

Di Luzio, Nardecchia 2017

B-decay anomalies point to (at least) the interactions

$$\frac{1}{\Lambda^2} (\bar{c}_L \gamma^\mu b_L) (\bar{\nu}_\tau \gamma_\mu \tau_L) \quad \frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

numerically $\Lambda \sim 4$ TeV and $\Lambda \sim 40$ TeV.

For a tree-level mediator,

$$\Lambda^{-2} = (g_{\text{NP}} M_{\text{NP}})^{-2} \quad \rightarrow \quad M_{\text{NP}} = g_{\text{NP}} \Lambda \lesssim 4\pi \Lambda \sim (30, 300 \text{ TeV})$$

Stronger constraint from partial-wave unitarity: maximal NP scale of **below 10 (100) TeV**.

If the NP is less than maximally flavour-violating, or the NP is weakly coupled, the scale will be 1-2 orders of magnitudes lower.

While the bounds are (so far) high, the fact that there are any at all should be encouraging, further refinements may be possible.

Tree-level mediators: leptoquarks

Scalar or vector leptoquarks can generate interactions

Eg Gripaos, Nardecchia, Renner, ...
(Hiller, Nisandzic 2017)

$$\frac{1}{\Lambda^2} (\bar{c}_L \gamma^\mu b_L) (\bar{\nu}_\tau \gamma_\mu \tau_L)$$

$$\frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

$(3, 1, -1/3)$ or $(3, 3, 2/3)$

$(3, 3, -1/3)$

$(3, 1, 2/3)$

or $(3, 3, 2/3)$

$(3, 1, 2/3)$ or $(3, 3, 2/3)$

(more possibilities at loop level Eg Bauer, Neubert; Becirevic et al)

Tree-level mediators: W' , Z'

$$\frac{1}{\Lambda^2} (\bar{c}_L \gamma^\mu b_L) (\bar{\nu}_\tau \gamma_\mu \tau_L) \quad \frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

$$(0, 3, 0)$$

$$(0, 3, 0) \quad \text{or} \quad (0, 1, 0)$$

- appear as resonances in composite models (KK excitations in RS, vectors coupling to symmetry currents in 4D composite models)

- Z' exchange contributes to B_s mixing at tree-level. **Leptoquarks do not!**

Isidori et al, Quiros et al, Ligeti et al, Becirevic et al, Crivellin et al, ...

Summary & outlook

Flavour provides a plethora of observables sensitive to new physics

Stringent constraints on new physics, not only from meson-antimeson mixing

Significant progress in lattice calculations for flavour phenomenology, (much) more to come

B-anomalies – independent verification by upcoming Belle2 experiment. Near-discovery level significance already with theoretically clean measurements

BACKUP

A Z' model for $R_{K^{(*)}}$

Accommodating *all* $b \rightarrow s$ anomalies requires a muon-specific C_L – type interaction

$$\frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

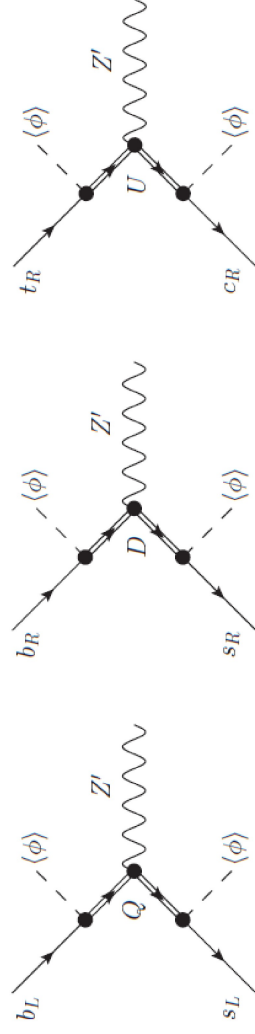
with $\Lambda \sim 30$ TeV

However, C_R is weakly constrained and can also be present.

Anomaly-free Z' model with gauged $L_\mu - L_\tau$, nonminimal (dim-6) coupling to quarks, can eg come from heavy vectorlike quarks:

Altmannshofer et al 2014

Also Crivellin et al, ...



The small coupling to quarks suppresses contributions to Bs mixing

Importance of virtual charm

Also purely hadronic operators enter, in SM primarily:

$$Q_1^c = (\bar{c}_L^i \gamma_\mu b_L^j) (\bar{s}_L^j \gamma^\mu c_L^i)$$

$$Q_2^c = (\bar{c}_L^i \gamma_\mu b_L^i) (\bar{s}_L^j \gamma^\mu c_L^j)$$

RG mixes these into C_9 and C_7

+ dipole

$$C_7^{\text{eff}}(4.6\text{GeV}) = 0.02 C_1(M_W) - 0.19 C_2(M_W)$$

$$C_9(4.6\text{GeV}) = 8.48 C_1(M_W) + 1.96 C_2(M_W)$$

SM: 0(50%) of total in both cases!

At $\mu=m_b$: $C_7^{\text{eff}} \sim -0.3$, $C_L \sim 4$, $C_R \approx 0$

- SM: accidentally almost left-chiral muon interactions

- Long-distance virtual charm important theory uncertainty

C_9 from BSM $(\bar{s}b)(\bar{\tau}\tau)$ operators

Bobeth, Haisch arXiv:1109.1826

Crivellin et al arXiv:1807.02068

Similarly strong RG mixing into C_9 as in charming BSM case

- **This operator is automatically present for “left-handed” $R_{D^{(*)}}$ explanations via $(\bar{c}_L \gamma^\mu b_L)(\bar{\nu}_\tau \gamma_\mu \tau_L)$**

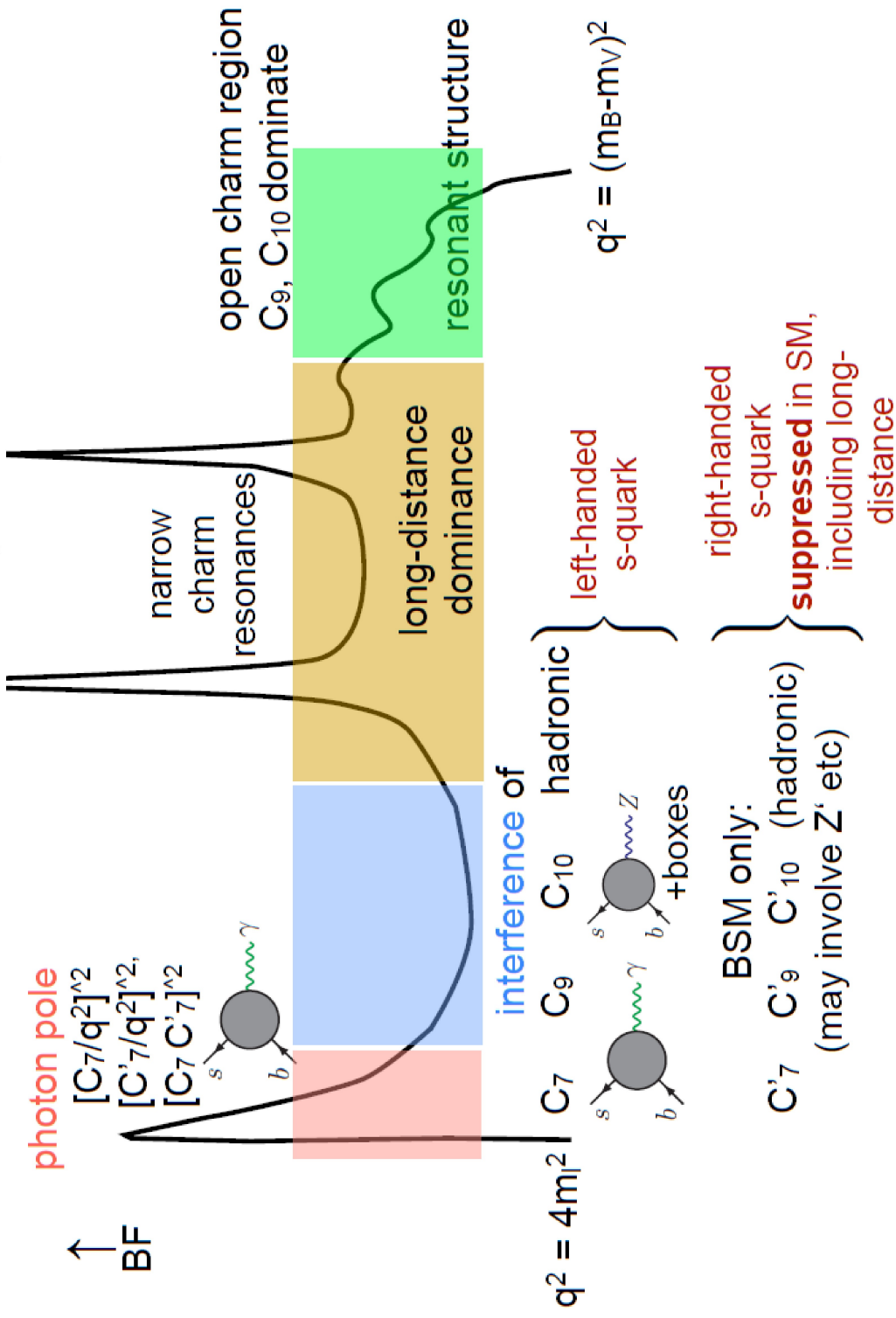
This is a consequence of $SU(2)_W$ symmetry and the experimental bound on $B \rightarrow K^* \nu \bar{\nu}$

Buras et al arXiv:1409.4557

- Radiatively generated C_9 is again $O(1)$ and negative (and lepton-universal)

τ

B → V l l: rate (schematic)



“low q^2 / large recoil”

“high q^2 / low recoil”

Rare decay null tests of the SM

2 clean null tests of SM from (mainly) $B \rightarrow K^* \gamma$ and $B \rightarrow K^* \mu \mu$

$$P_1 \equiv \frac{I_3 + \bar{I}_3}{2(I_{2s} + \bar{I}_{2s})} = \frac{-2 \operatorname{Re}(H_V^+ H_V^- + H_A^+ H_A^-)}{|H_V^+|^2 + |H_V^-|^2 + |H_A^+|^2 + |H_A^-|^2}$$

$$P_2^{CP} \equiv -\frac{I_9 - \bar{I}_9}{4(I_{2s} + \bar{I}_{2s})} = -\frac{\operatorname{Im}(H_V^+ H_V^- + H_A^+ H_A^-)}{|H_V^+|^2 + |H_V^-|^2 + |H_A^+|^2 + |H_A^-|^2}$$

$$\approx 0$$

$$\approx 0$$

(Melikhov 1998)
 Krueger, Matias 2002
 Lunghi, Matias 2006
 Becirevic, Schneider 2011
 Becirevic, Kou, et al 2012
 SJ, Martin Camalich 2012

Vey suppressed in the absence of right-handed currents. No effect seen in data.

‘Pseudo-observables.’ Wilson coefficients from global fit

$$C'_{7\gamma} = 0.018 \pm 0.037$$

Aebischer et al arXiv:1903.10434

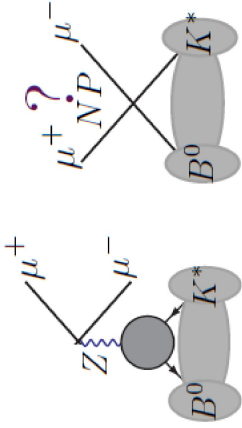
$$C'_{9V} = 0.09 \pm 0.15$$

Paul & Straub arXiv:1608.02556

Decay amplitude structure

Two mechanisms to produce dilepton in & beyond SM

- via axial lepton current (in SM: Z, boxes) **C10**



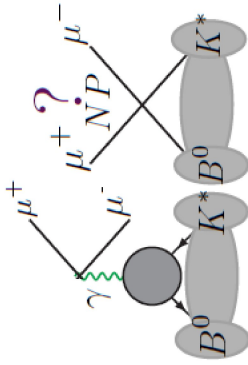
K^* helicity

$$H_A(\lambda) \propto \tilde{V}_\lambda(q^2) C_{10} - V_{-\lambda}(q^2) C'_{10}$$

one form factor (nonperturbative) per helicity amplitudes factorize naively

[nb - one more amplitude if not neglecting lepton mass]

- via vector lepton current (in SM: (mainly) photon) **C7, C9, hadronic hamiltonian**



$$H_V(\lambda) \propto \tilde{V}_\lambda(q^2) C_9 - V_{-\lambda}(q^2) C'_9 + \frac{2 m_b m_B}{q^2} (\tilde{T}_\lambda(q^2) C_7 - \tilde{T}'_{-\lambda}(q^2) C'_7) - \frac{16 \pi^2 m_B^2}{q^2} h_\lambda(q^2)$$

photon pole at $q^2=0$

two form factors interfere for each helicity

nonlocal "quark loops" do **not** factorize naively

Natural, systematic discussion in terms of helicity amplitudes SJ, Martin Camalich 2012, 2014

Photon pole absent for helicity-0 (form factor rescaling)

Rare B-decay: observables

Branching ratios

leptonic (differential in dilepton mass)

$$B_s \rightarrow \mu\mu, B_d \rightarrow \mu\mu,$$

Nonperturbative QCD
fully controlled (decay
constant from lattice)

semileptonic (differential in dilepton mass)

$$B \rightarrow K^{(*)}\mu\mu, B \rightarrow K^{(*)}ee, B_s \rightarrow \phi\mu\mu$$

Lepton universality ratios

$$R_{K^{(*)}}[a, b] = \frac{\int_a^b \frac{d\Gamma}{dq^2}(B \rightarrow K^{(*)}\mu^+\mu^-) dq^2}{\int_a^b \frac{d\Gamma}{dq^2}(B \rightarrow K^{(*)}e^+e^-) dq^2}$$

Form factors, 4-quark operator
contributions, QED radiation
cancel out to $\sim\%$ level (relative
to LHCb treatment)

eg Bordone, Isidori, Pattori arXiv:1605.07633

differential angular distribution for $B \rightarrow Vll$

3 angles, dilepton mass q^2

7 angular differential observables:

$(A_{FB}^l, P_5^l, \text{etc})$

