

Theorist's perspective: BSM & flavour

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EPP Meeting

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Precision frontier: beyond QED

Some past indirect discoveries

parity violation

Lee, Yang 1956

Wu et al, Goldhaber et al 1957

V-A structure of weak interactions

Feynman, Gell-Mann 1957

Shudarshan, Marshak 1957

universality of weak decays

Gell-Mann, Levy 1960

CP violation

Christenson et al 1964

electroweak symmetry breaking

BEHGHK, Glashow, Salam, Weinberg
1960-67

charm to explain $K_L \rightarrow \mu\mu$ suppression

Glashow, Iliopoulos, Maiani 1970

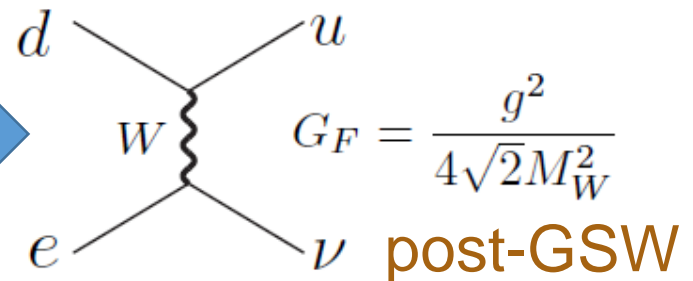
third generation to explain CPV

Kobayashi, Maskawa 1972

Neutral currents ('73), charm('74), 3rd gen. ('75), W,Z ('83),
Higgs ('12) later discovered.

$$H_W \sim G_F (\bar{p}\gamma^\mu n) (\bar{e}\gamma_\mu \nu)$$

(Fermi 1934)



The Standard Model

spin 1

electromagnetism U(1)
 weak interactions SU(2)
 strong interactions SU(3)

universal
 couplings

3 generations

spin 1/2

$\begin{pmatrix} u_L \\ d_L \end{pmatrix}$	u_R d_R	$\begin{pmatrix} c_L \\ s_L \end{pmatrix}$	c_R s_R	$\begin{pmatrix} t_L \\ b_L \end{pmatrix}$	t_R b_R	$Q = +2/3$ $Q = -1/3$
$\begin{pmatrix} \nu_{eL} \\ e_L \end{pmatrix}$	— e_R	$\begin{pmatrix} \nu_{\mu L} \\ \mu_L \end{pmatrix}$	— μ_R	$\begin{pmatrix} \nu_{\tau L} \\ \tau_L \end{pmatrix}$	— τ_R	$Q = 0$ $Q = -1$

spin 0

Higgs - sets mass scale of entire Standard Model

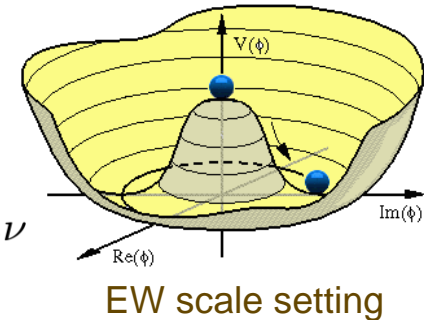
Origin of masses? Flavour mixings? What determines the weak scale?

Dynamics

At length scales above an attometre we have approximately (up to gravity)

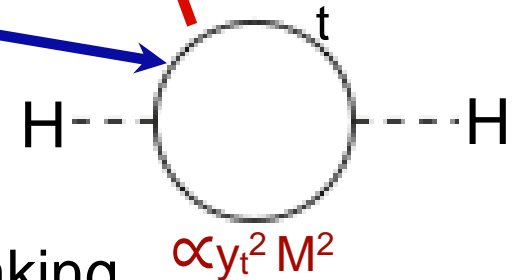
$SU(3)^5$ flavour symmetric kinetic/gauge terms

$$\mathcal{L}_{\text{SM}} = \sum_f \bar{\psi}_f \gamma^\mu D_\mu \psi_f - \frac{1}{4} \sum_i a \frac{g_i}{4} F_{\mu\nu}^i F^{i\alpha\mu\nu}$$



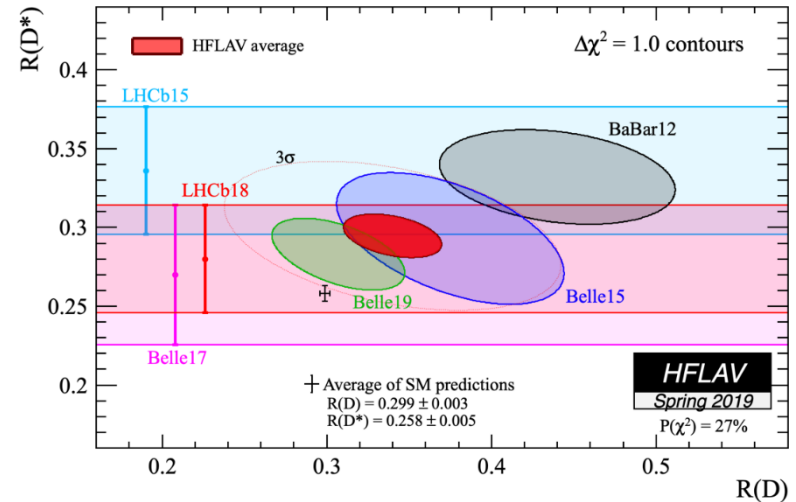
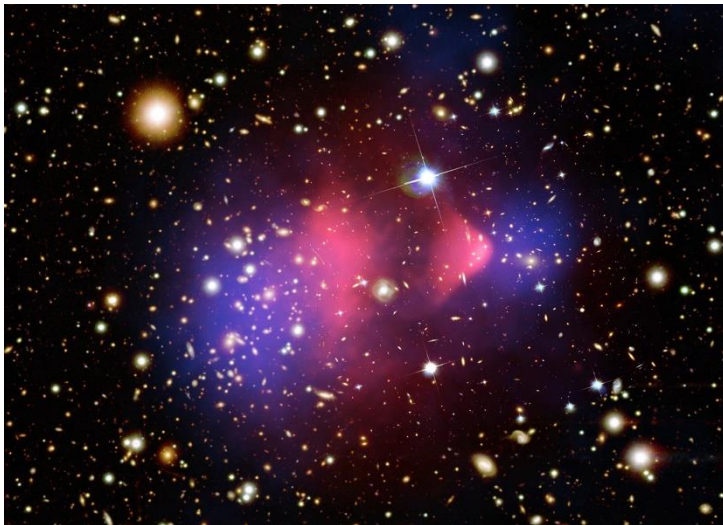
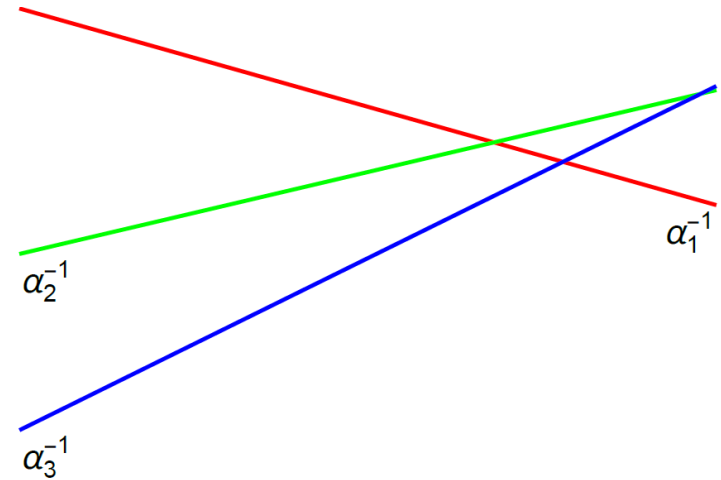
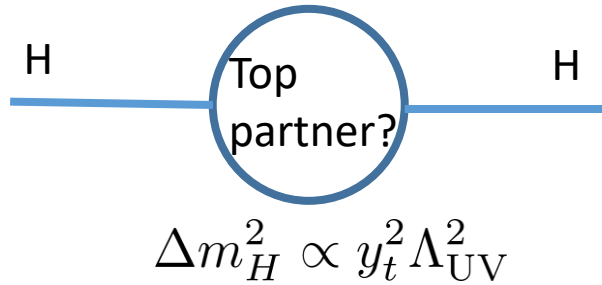
$$- \bar{u}_R Y^U \phi^{c\dagger} q_L - \bar{d}_R Y^D \phi^\dagger q_L - \bar{e}_R Y^E \phi^\dagger l_L - \mu^2 \phi^\dagger \phi - \frac{\lambda}{2} (\phi^\dagger \phi)^2$$

flavour-breaking fermion masses
and Higgs couplings

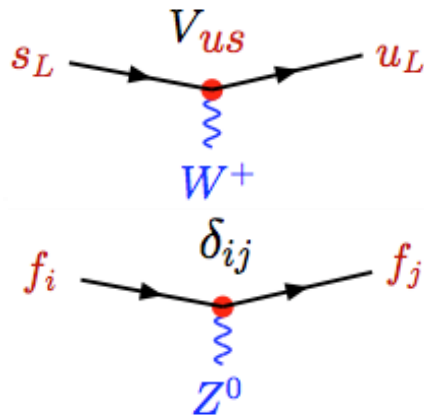


Quadratic divergence from flavour-breaking sources \rightarrow any cure likely to be flavour-breaking (happens in SUSY, composite Higgs, ...)

Beyond the SM



Flavour physics & rare decays



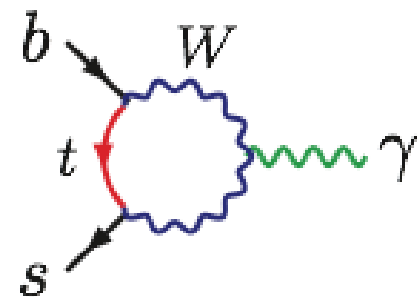
all flavour violation in charged weak current

(tree level) neutral current conserves flavor

strong & electromagnetic preserve flavour

Loop and CKM/GIM suppression of flavour-changing neutral current processes

-> enhanced BSM sensitivity



Flavour: the dogs that did not bark

From AC Doyle, "The Adventure of Silver Blaze" [with thanks to J Ellis]

Gregory (Scotland Yard detective): "Is there any other point to which you would wish to draw my attention?"

Holmes: "To the curious incident of the dog in the night-time."

Gregory: "The dog did nothing in the night-time"

Holmes: "That was the curious incident."



Quote and S Paget's illustration via Wikipedia

Absence of an effect in a BSM-sensitive observable can be as important a clue as an anomaly.

Eg Meson-antimeson mixing → constrain NP scales up to 10^5 TeV (for maximally flavor-violating BP)

Where to look

Observables with **suppressed and/or controlled SM contribution**

- flavour-changing neutral currents, eg

Meson-antimeson mixing (B_s, B_d, D, K)

$b \rightarrow s \mu^+ \mu^-$ and $b \rightarrow s \gamma$

$$\begin{array}{l} B \rightarrow K^{(*)} \mu^+ \mu^-, B \rightarrow K^{(*)} e^+ e^-, B_s \rightarrow \phi \mu^+ \mu^- \\ B \rightarrow K^{(*)} \gamma \end{array}$$

$$B \rightarrow X_s \mu^+ \mu^-, B \rightarrow X_s \gamma$$

$s \rightarrow d \nu \nu$

$$K^+ \rightarrow \pi^+ \nu \nu$$

- lepton-flavour ratios, eg

$$BR(B \rightarrow K^{(*)} \mu^+ \mu^-) / BR(B \rightarrow K^{(*)} e^+ e^-) - 1$$

$$BR(B \rightarrow D^{(*)} \tau \nu) / BR(B \rightarrow D^{(*)} l \nu) - (SM)$$

- CP violation, eg

$$K_L \rightarrow \pi \pi \quad (\epsilon_K, \epsilon'_K)$$

$$K_L \rightarrow \pi^0 \nu \nu$$

Babar, Belle
LHCb, ATLAS, CMS
Belle2

Babar, Belle, Belle2


NA62 (CERN)

Babar, Belle, LHCb
Belle2

..., NA48, KTeV

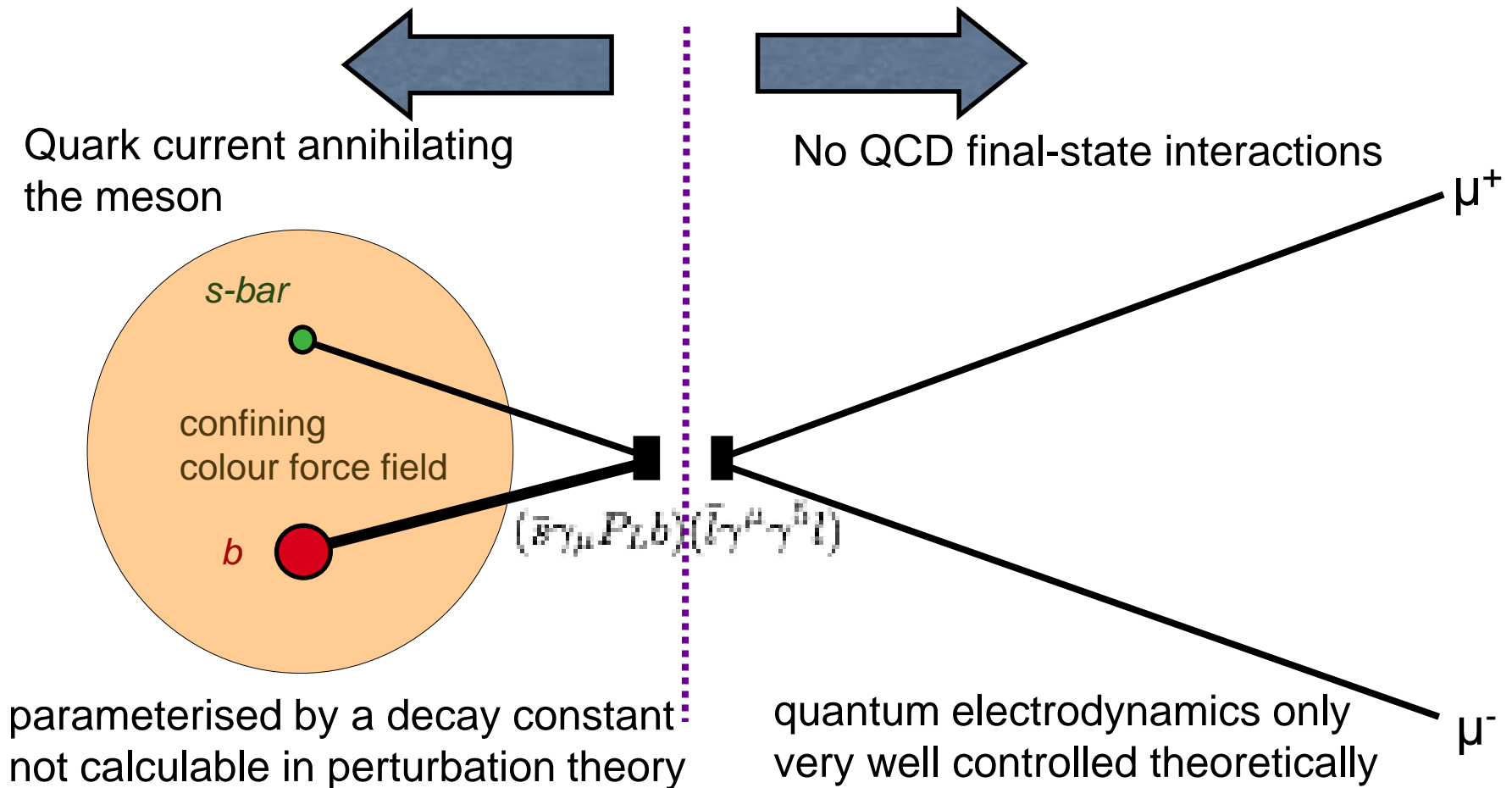
KOTO

ATLAS analyses

Analysis	Expected/plausible BSM scale	theory	current BSM significance
B(s,d) \rightarrow $\mu\mu$	(few) TeV (nat'lness)	excellent	2-3 σ
RK(*)	(few) TeV (nat'lness)	excellent	3-4 σ
B \rightarrow K* $\mu\mu$ (ee?) angular	(few) TeV (nat'lness)	good (P5') to excellent (rh current)	unclear
Tau \rightarrow 3 μ	GUT scale or below	excellent	none
B \rightarrow J/psi phi etc	(few) TeV	depends	none
B lifetimes	(few) TeV	depends	none
4 muons searches			
Bc/Bc(2S)			
Pentaquark/Zc			
CPV in b from ttbar			

Outside scope of what I can discuss in this talk

A “clean” observable: Leptonic decay



Very small long-distance QED corrections Beneke, Bobeth, Szafron 2019

Rare B-decay: short-distance (theory)

BSM (and SM weak interactions) enter flavour physics through **effective contact interactions** (SMEFT/ H_{weak})

C_9 : dilepton from vector current

$$(\bar{s}\gamma_\mu P_L b)(\bar{l}\gamma^\mu l)$$

C_{10} : dilepton from axial current

$$(\bar{s}\gamma_\mu P_L b)(\bar{l}\gamma^\mu \gamma^5 l)$$

C_7 : dilepton from dipole

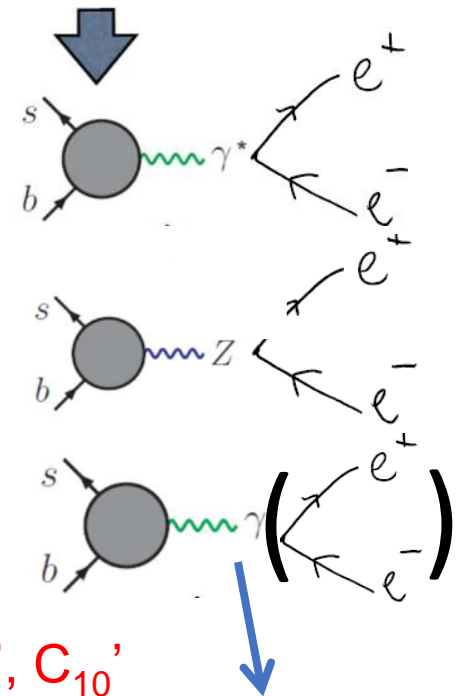
$$(\bar{s}\sigma^{\mu\nu} P_R b)F_{\mu\nu}$$

+parity conjugate “right-handed currents” - C_7' , C_9' , C_{10}'
 suppressed by m_s/m_b in SM

Alternative basis with **chiral leptons** l_L, l_R

$$C_L = (C_9 - C_{10})/2 \quad C_R = (C_9 + C_{10})/2$$

in SM mainly



Can also have real photon

Also “clean”: Lepton-flavour ratios

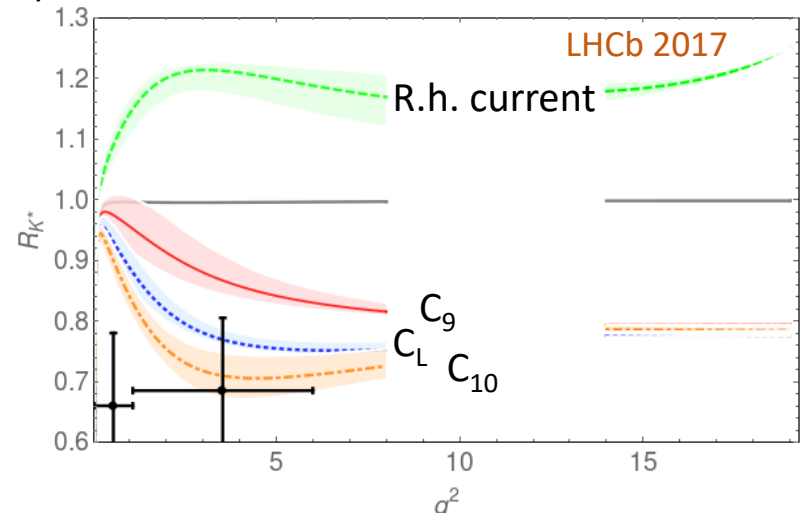
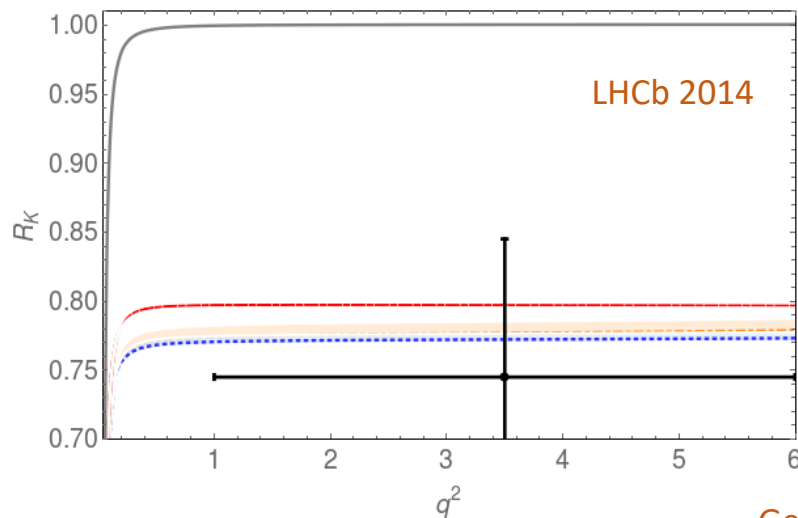
$$R_{K^{(*)}}[a, b] = \frac{\int_a^b \frac{d\Gamma}{dq^2} (B \rightarrow K^{(*)} \mu^+ \mu^-) dq^2}{\int_a^b \frac{d\Gamma}{dq^2} (B \rightarrow K^{(*)} e^+ e^-) dq^2}$$

Theory uncertainties largely cancel out, negligible relative to experiment.

leading is QED: net effect <1% after experimental corrections

Bordone, Isidori, Pattori 2016; Isidori, Nabeebaccus, Zwicky 2020

Situation in 2017 (first R_{K^*} measurement):



Geng, Grinstein, SJ, Martin Camalich, Ren, Shi arxiv:1704.05446

Rare B-decay anomalies – fit to data

Observables in the fit

Basic idea: use only observables which are sensitive to $b \rightarrow s$ ll but independent of hadronic form factors, long-distance charm etc.

I.e. $R_{K^{(*)}}$ and $B_s \rightarrow \mu\mu$.

This is a well-defined set of observables, first employed in 2017, with several data updates since then. No “look-elsewhere effect” to take into account.

In the following I describe the fit in arXiv:2103.12738 (Geng, Grinstein, SJ, Li, Martin Camalich, Shi); see also work by Altmannshofer & Stangl and a few others

A note on the $B_s \rightarrow \mu\mu$ input

Together with the R_{K^*} update, LHCb presented a significant update to $BR(B_s \rightarrow \mu\mu)$

ATLAS and CMS have also measured this

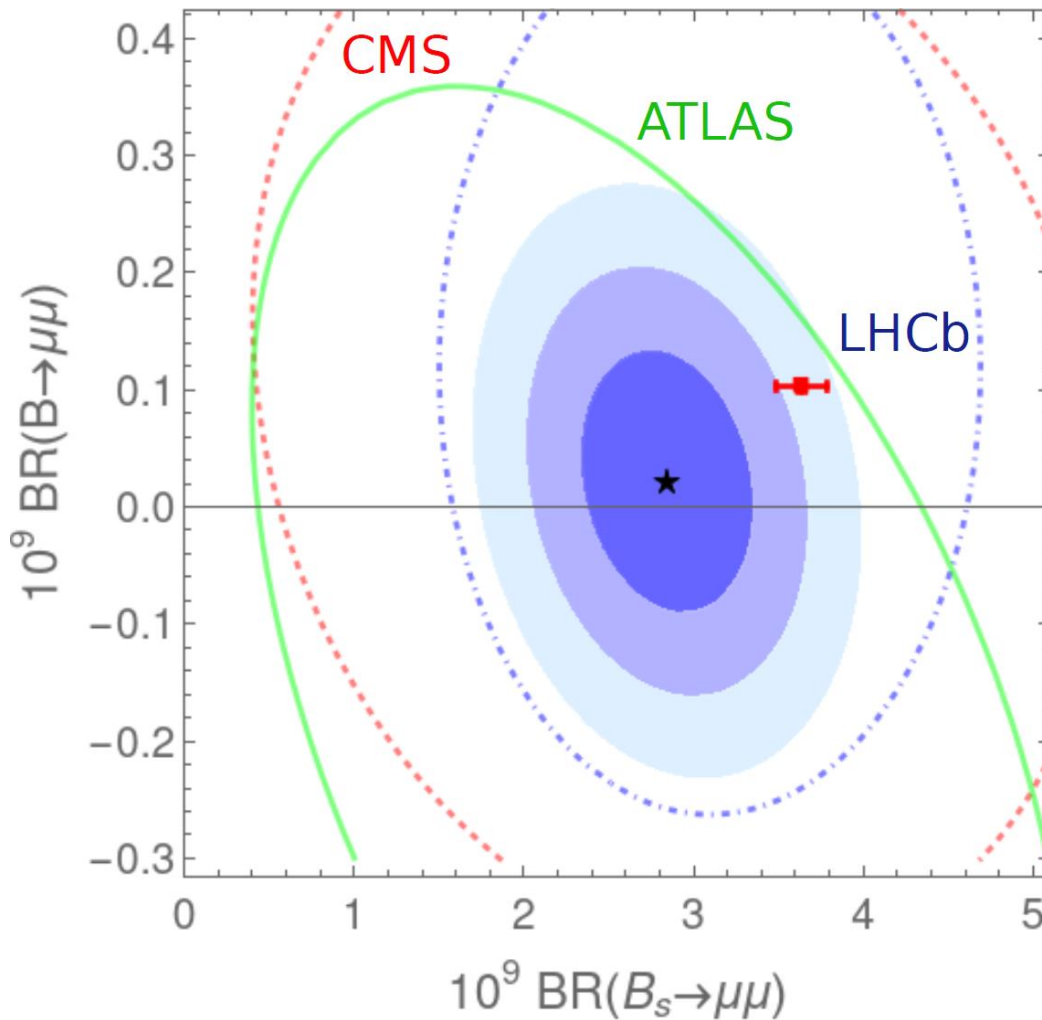
Measurements show non-negligible correlations with $BR(B_d \rightarrow \mu\mu)$ (biggest in ATLAS).

Hence to obtain a $BR(B_s \rightarrow \mu\mu)$ average first combine the 3x2 measurements.

Then profile over $BR(B_d \rightarrow \mu\mu)$.

$B_q \rightarrow \mu\mu$ world combination

Geng, Grinstein, SJ, Li, Martin Camalich, Shi arXiv:2103.12738



From this:

$$\text{BR}(B_s \rightarrow \mu\mu) = (2.8 \pm 0.3) 10^{-9}$$

$$\chi^2_{\text{min}} = 3.75 \text{ (5 d.o.f.)}$$

Input data

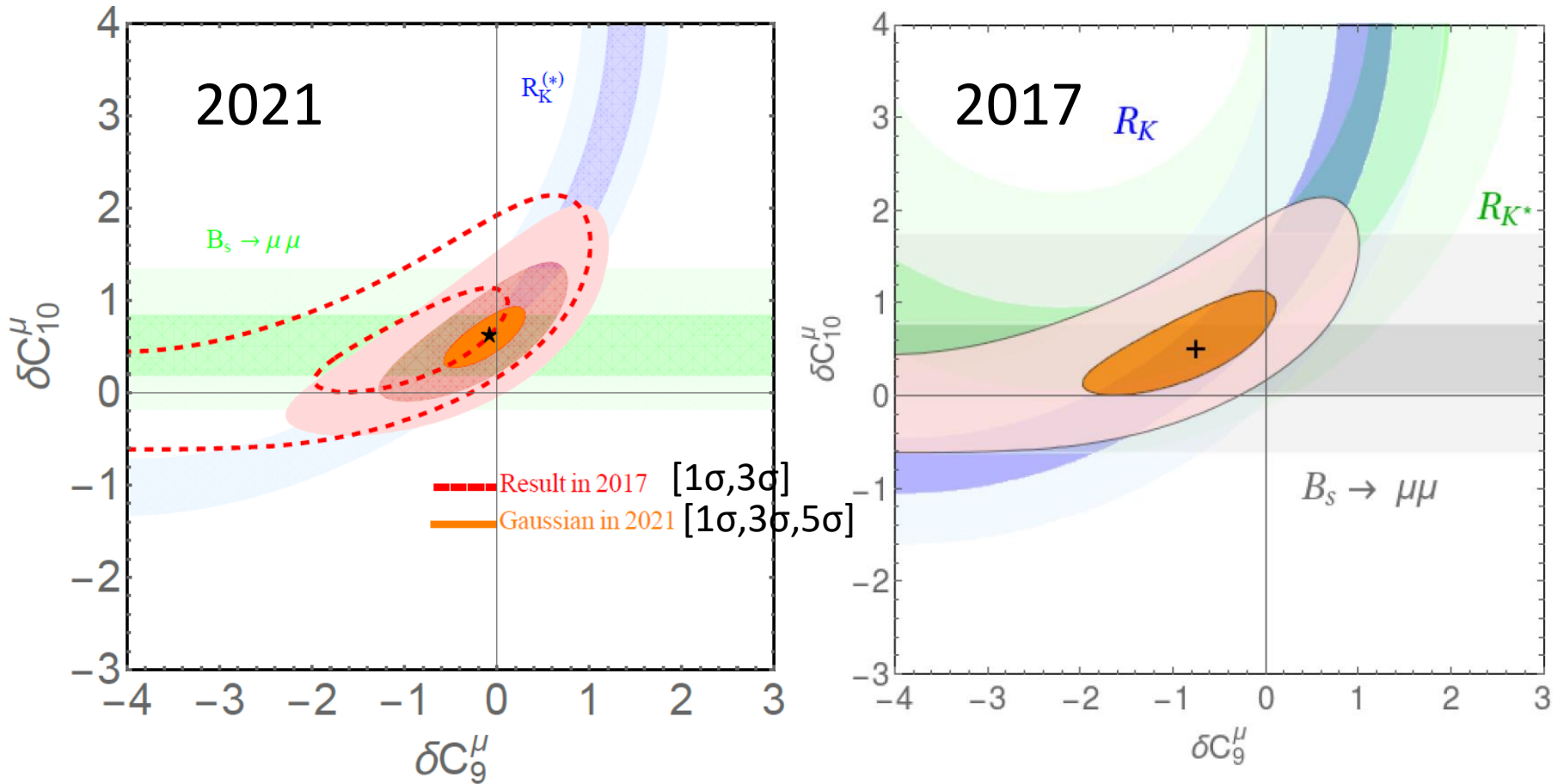
Observable	Value	Source	Reference
$BR(B_s \rightarrow \mu^+ \mu^-)$	$(2.8^{+0.8}_{-0.7}) \times 10^{-9}$	ATLAS	[11]
	$(2.9 \pm 0.7 \pm 0.2) \times 10^{-9}$	CMS	[12]
	$(3.09^{+0.46+0.15}_{-0.43-0.11}) \times 10^{-9}$	LHCb update	[10]
	$(2.842 \pm 0.333) \times 10^{-9}$	our average	this work
	$(3.63 \pm 0.13) \times 10^{-9}$	SM prediction	[13]
$R_K[1.1, 6]$	0.846 ± 0.044	LHCb	[6]
$R_K[1, 6]$	1.03 ± 0.28	Belle	[14]
$R_{K^*}[0.045, 1.1]$	0.660 ± 0.113	LHCb	[15]
$R_{K^*}[1.1, 6]$	0.685 ± 0.122	LHCb	[15]
$R_{K^*}[0.045, 1.1]$	0.52 ± 0.365	Belle	[16]
$R_{K^*}[1.1, 6]$	0.96 ± 0.463	Belle	[16]

Self-consistency of dataset: $\chi^2_{\min} = 4.61$ (8 d.o.f.) / $p = 0.80$
 (counting 6 $BR(B_q \rightarrow \mu\mu)$ measurements)

SM p-value is 5.4×10^{-5} (4.0σ) [counting $BR(B_s \rightarrow \mu\mu)$ average]
 reduces to 3.5σ when counting the 6 $BR(B_q \rightarrow \mu\mu)$ measurements
 separately

Clean fit: results: 2-parameter BSM fit

Geng, Grinstein, SJ, Li, Martin Camalich, Shi arXiv:2103.12738



Clean fits: numerical results

Geng, Grinstein, SJ, Li, Martin Camalich, Shi arXiv:2103.12738

Fit three 1-parameter scenario (vectorial, axial, left-handed coupling to muons)

TABLE II. Best fit values, χ_{\min}^2 , p -value, Pull_{SM} and confidence intervals of the Wilson coefficients in the fits of the $R_K, R_{K^*}, B_s \rightarrow \mu\mu$ data only using Gaussian form χ_{th}^2 . For the cases of single Wilson-coefficient fits, we show the 1σ and 3σ confidence intervals. In the $(\delta C_9^\mu, \delta C_{10}^\mu)$ case, the 1σ interval of each Wilson coefficient is obtained by profiling over the other one to take into account their correlation.

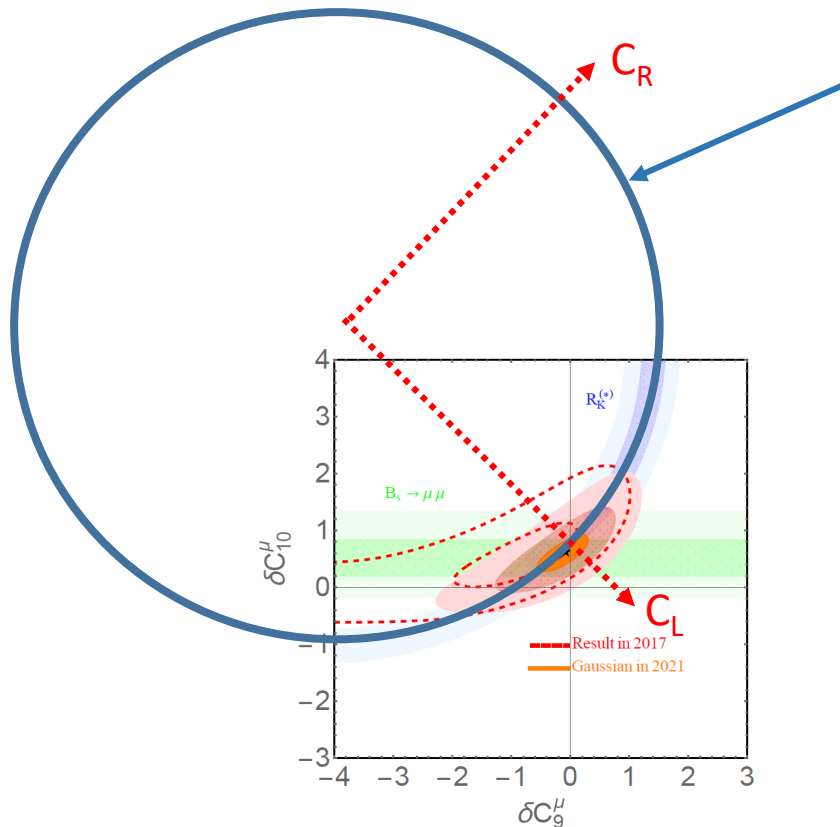
Coeff.	best fit	χ_{\min}^2	p -value	Pull_{SM}	1σ range	3σ range	ρ
δC_9^μ	-0.82	14.70 [6 dof]	0.02	4.08	[-1.06, -0.60]	[-1.60, -0.20]	-
δC_{10}^μ	0.65	6.52 [6 dof]	0.37	4.98	[0.52, 0.80]	[0.25, 1.11]	-
δC_L^μ	-0.40	7.36 [6 dof]	0.29	4.89	[-0.48, -0.31]	[-0.66, -0.15]	-
$(\delta C_9^\mu, \delta C_{10}^\mu)$	(-0.11, 0.59)	6.38 [5 dof]	0.27	4.62	$\delta C_9^\mu \in [-0.41, 0.17]$	$\delta C_{10}^\mu \in [0.38, 0.81]$	0.762
$(\delta C_L^\mu, \delta C_R^\mu)$	(-0.35, 0.25)				$\delta C_L^\mu \in [-0.45, -0.26]$	$\delta C_R^\mu \in [0.00, 0.48]$	0.406

Note that C_L is well-determined in both the left-handed and the two-parameter scenario, with consistent values. Not true for C_9 . Pure C_9 model also much worse fit ($p=1/50$).

$R_K^{(*)}$ and C_L

Assume here that the BSM effect is in the muonic mode, and no right-handed currents.

Because in the SM, $|C_R|, |C_7| \ll |C_L|$,
 $BR \approx \text{const } |C_L^{\text{SM}} + C_L^{\text{BSM}}|^2 + \dots \approx \text{const } |4 + C_L^{\text{BSM}}|^2 + \text{positive}$



$BR(B \rightarrow K^{(*)} \mu \mu) =$
SM value

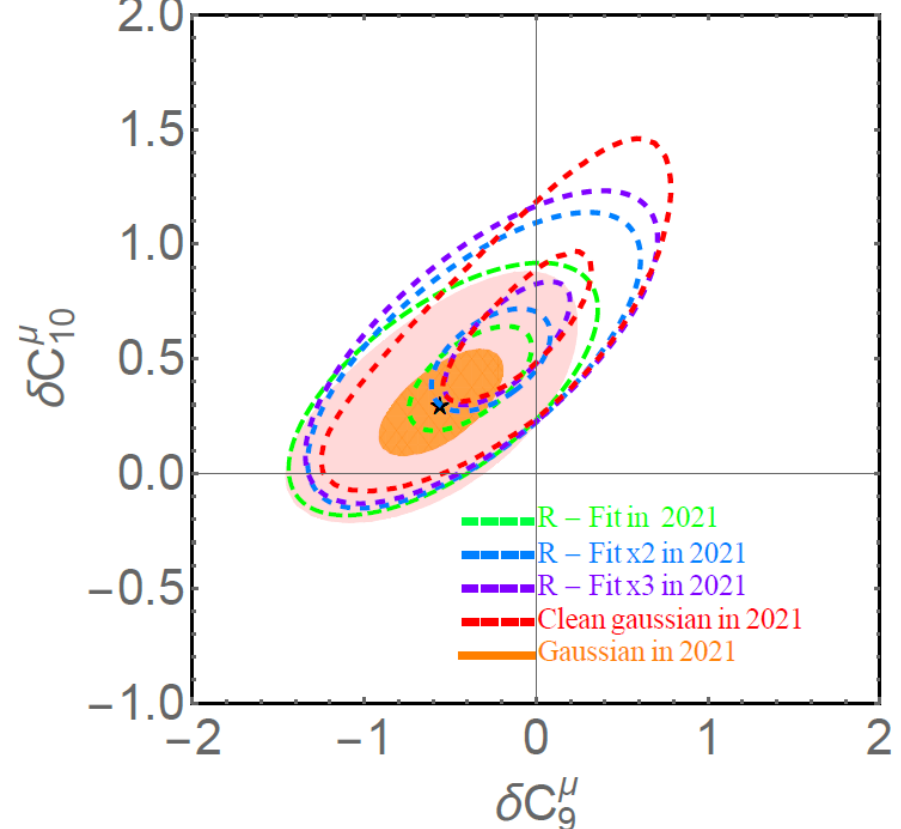
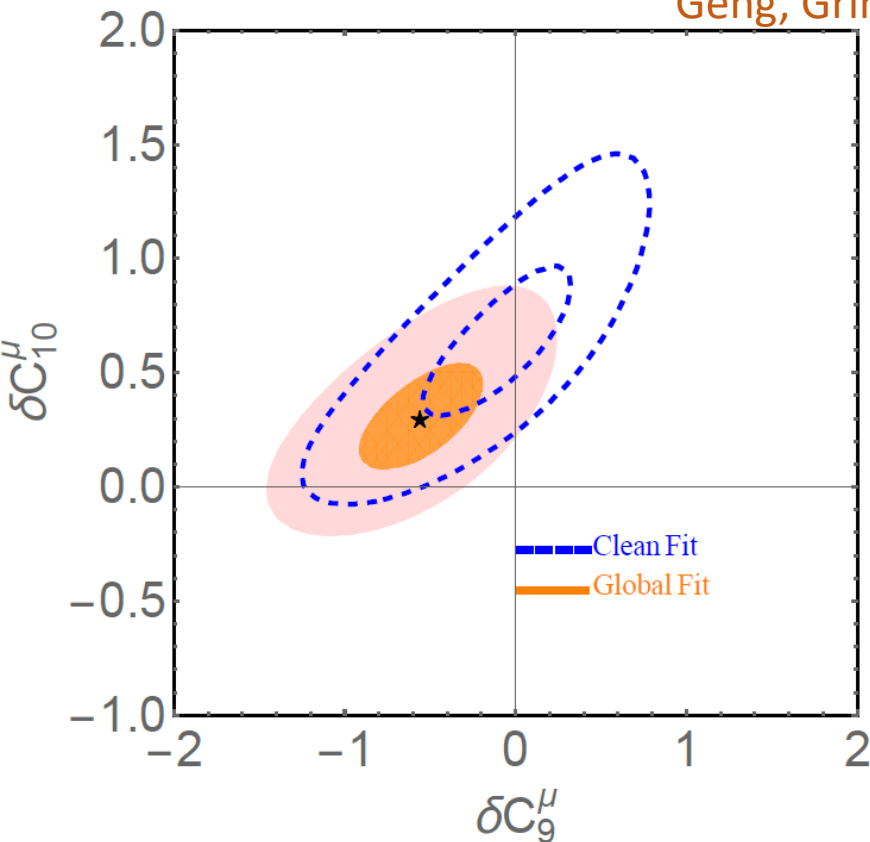
Only C_L^{BSM} can interfere destructively: $R_K^{(*)}$ point to purely left-handed coupling

$$(\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

with $\sim -(10-15)\%$ of SM value

Adding $B \rightarrow K^* \mu \mu$ angular data

Geng, Grinstein, SJ, Li, Martin Camalich, Shi arXiv:2103.12738



Left plot: extra data pulls fit approx. along the C_R direction.
 $C_L=0$ remains excluded at high confidence.
 $p(\text{SM})$ up at 0.02

Right plot: effect of increasing hadronic uncertainties

Minimal contact interaction

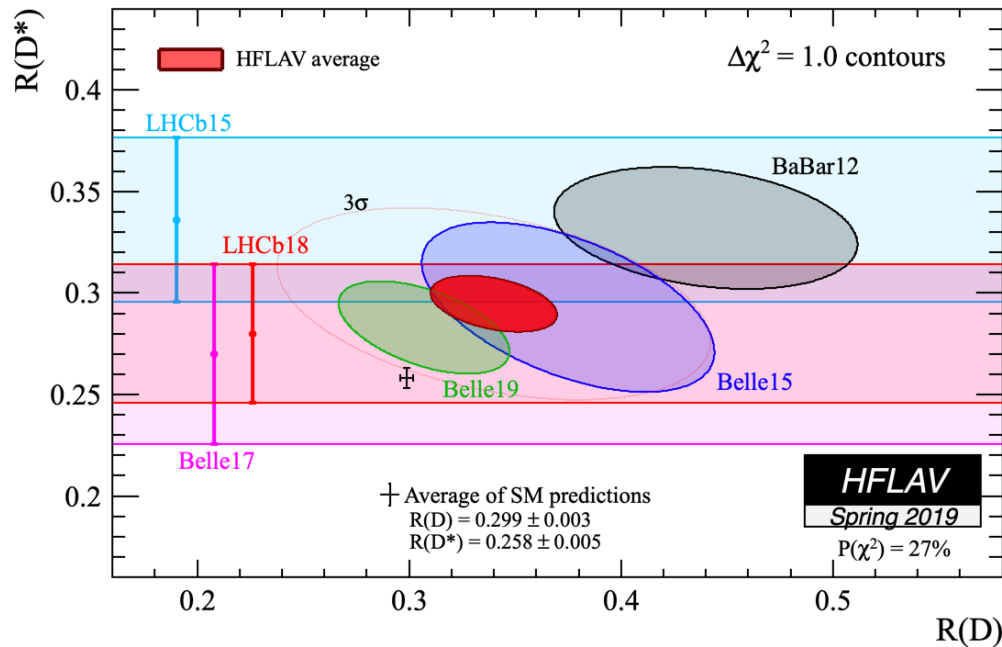
In summary, the B-decay anomalies suggest at a minimum the interaction

$$\frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

numerically $\Lambda \sim 40 \text{ TeV}$

Small enough to be a loop effect even BSM (as it is in SM!)

Non-rare semileptonic decays



$$R(D^{(*)}) = \frac{BR(B \rightarrow D^{(*)} \tau \nu_\tau)}{BR(B \rightarrow D^{(*)} \ell \nu_\ell)}$$

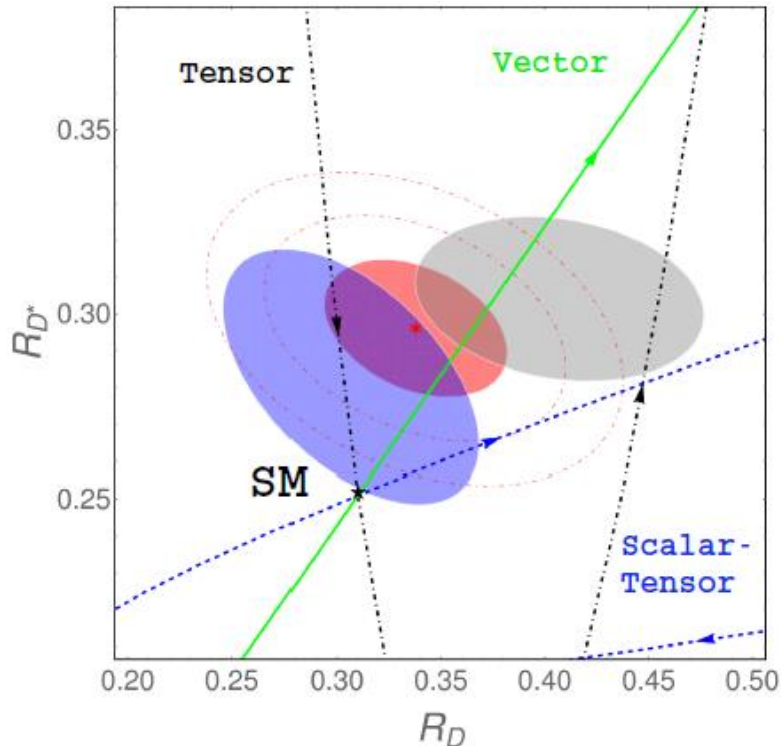
SM tree-level

large effect; theory error still (almost) negligible

Possible BSM

ϵ_R^l flavour-universal by SU(2) x U(1) invariance (no dim-6 SMEFT operator)

$$\mathcal{L}_{\text{eff}}^{\text{LE}} \supset -\frac{4G_F V_{cb}}{\sqrt{2}} [(1 + \epsilon_L^\tau)(\bar{\tau}\gamma_\mu P_L \nu_\tau)(\bar{c}\gamma^\mu P_L b) + \epsilon_R^\tau(\bar{\tau}\gamma_\mu P_L \nu_\tau)(\bar{c}\gamma^\mu P_L b) + \epsilon_{S_L}^\tau(\bar{\tau} P_L \nu_\tau)(\bar{c} P_L b) + \epsilon_{S_R}^\tau(\bar{\tau} P_L \nu_\tau)(\bar{c} P_R b) + \epsilon_T^\tau(\bar{\tau}\sigma_{\mu\nu} P_L \nu_\tau)(\bar{c}\sigma^{\mu\nu} P_L b)] + \text{H.c.},$$



Best fit value moved **substantially** closer to SM with Belle 2019 update

Different BSM operators imply different correlations between shifts to R_D , R_{D^*}

BSM implications of B-anomalies (qualitative)

Scale of new physics

Di Luzio, Nardecchia 2017

B-decay anomalies point to (at least) the interactions

$$\frac{1}{\Lambda^2} (\bar{c}_L \gamma^\mu b_L) (\bar{\nu}_\tau \gamma_\mu \tau_L) \qquad \frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

numerically $\Lambda \sim 4 \text{ TeV}$ and $\Lambda \sim 40 \text{ TeV}$.

For a tree-level mediator,

$$\Lambda^{-2} = (g_{\text{NP}} M_{\text{NP}})^{-2} \quad \rightarrow \quad M_{\text{NP}} = g_{\text{NP}} \Lambda \leq 4\pi \Lambda \sim (30, 300 \text{ TeV})$$

Stronger constraint from partial-wave unitarity: maximal NP scale of **below 10 (100) TeV**.

If the NP is less than maximally flavour-violating, or the NP is weakly coupled, the scale will be 1-2 orders of magnitudes lower.

While the bounds are (so far) high, the fact that there are any at all should be encouraging, further refinements may be possible.

Tree-level mediators: leptoquarks

Scalar or vector leptoquarks can generate interactions

Eg Gripaos, Nardecchia, Renner, ...
(Hiller, Nisandzic 2017)

$$\frac{1}{\Lambda^2} (\bar{c}_L \gamma^\mu b_L) (\bar{\nu}_\tau \gamma_\mu \tau_L)$$

$$\frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

$(3, 1, -1/3)$ or $(3, 3, 2/3)$

$(3, 3, -1/3)$

$(3, 1, 2/3)$ or $(3, 3, 2/3)$

$(3, 1, 2/3)$ or $(3, 3, 2/3)$

(more possibilities at loop level Eg Bauer, Neubert; Becirevic et al)

Tree-level mediators: W' , Z'

$$\frac{1}{\Lambda^2} (\bar{c}_L \gamma^\mu b_L) (\bar{\nu}_\tau \gamma_\mu \tau_L)$$

$$\frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

$(0, 3, 0)$

$(0, 3, 0)$ or $(0, 1, 0)$

- appear as resonances in composite models (KK excitations in RS, vectors coupling to symmetry currents in 4D composite models)

- Z' exchange contributes to B_s mixing at tree-level. **Leptoquarks do not!**

Isidori et al, Quiros et al, Ligeti et al, Becirevic et al, Crivellin et al,

...

Summary & outlook

Flavour provides a plethora of observables sensitive to new physics

Stringent constraints on new physics, not only from meson-antimeson mixing

Significant progress in lattice calculations for flavour phenomenology, (much) more to come

B-anomalies – independent verification by upcoming Belle2 experiment. Near-discovery level significance already with theoretically clean measurements

BACKUP

A Z' model for $R_{K^{(*)}}$

Accommodating *all* $b \rightarrow s$ II anomalies *requires* a muon-specific C_L – type interaction

$$\frac{1}{\Lambda^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

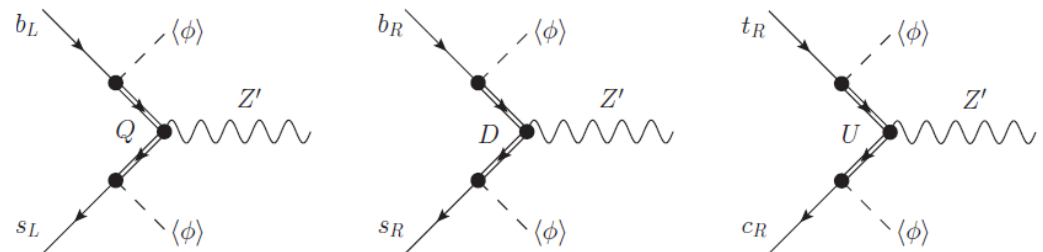
with $\Lambda \sim 30$ TeV

However, C_R is weakly constrained and can also be present.

Anomaly-free Z' model with gauged $L_\mu - L_\tau$, nonminimal (dim-6) coupling to quarks, can eg come from heavy vectorlike quarks:

Altmannshofer et al 2014

Also Crivellin et al, ...



The small coupling to quarks suppresses contributions to B_s mixing

Importance of virtual charm

Also **purely hadronic** operators enter, in SM primarily:

$$Q_1^c = (\bar{c}_L^i \gamma_\mu b_L^j) (\bar{s}_L^j \gamma^\mu c_L^i)$$

$$Q_2^c = (\bar{c}_L^i \gamma_\mu b_L^i) (\bar{s}_L^j \gamma^\mu c_L^j)$$

RG mixes these into C_9 and C_7

+ dipole

$$C_7^{\text{eff}}(4.6\text{GeV}) = 0.02 C_1(M_W) - 0.19 C_2(M_W)$$

$$C_9(4.6\text{GeV}) = 8.48 C_1(M_W) + 1.96 C_2(M_W)$$

SM: O(50%) of total in both cases!

At $\mu=m_b$: $C_7^{\text{eff}} \sim -0.3$, $C_L \sim 4$, $C_R \approx 0$

- SM: accidentally almost left-chiral muon interactions

- Long-distance virtual charm important theory uncertainty

C_9 from BSM $(\bar{s}b)(\bar{\tau}\tau)$ operators

Bobeth, Haisch arXiv:1109.1826

Crivellin et al arXiv:1807.02068

Similarly strong RG mixing into C_9 as in charming BSM case

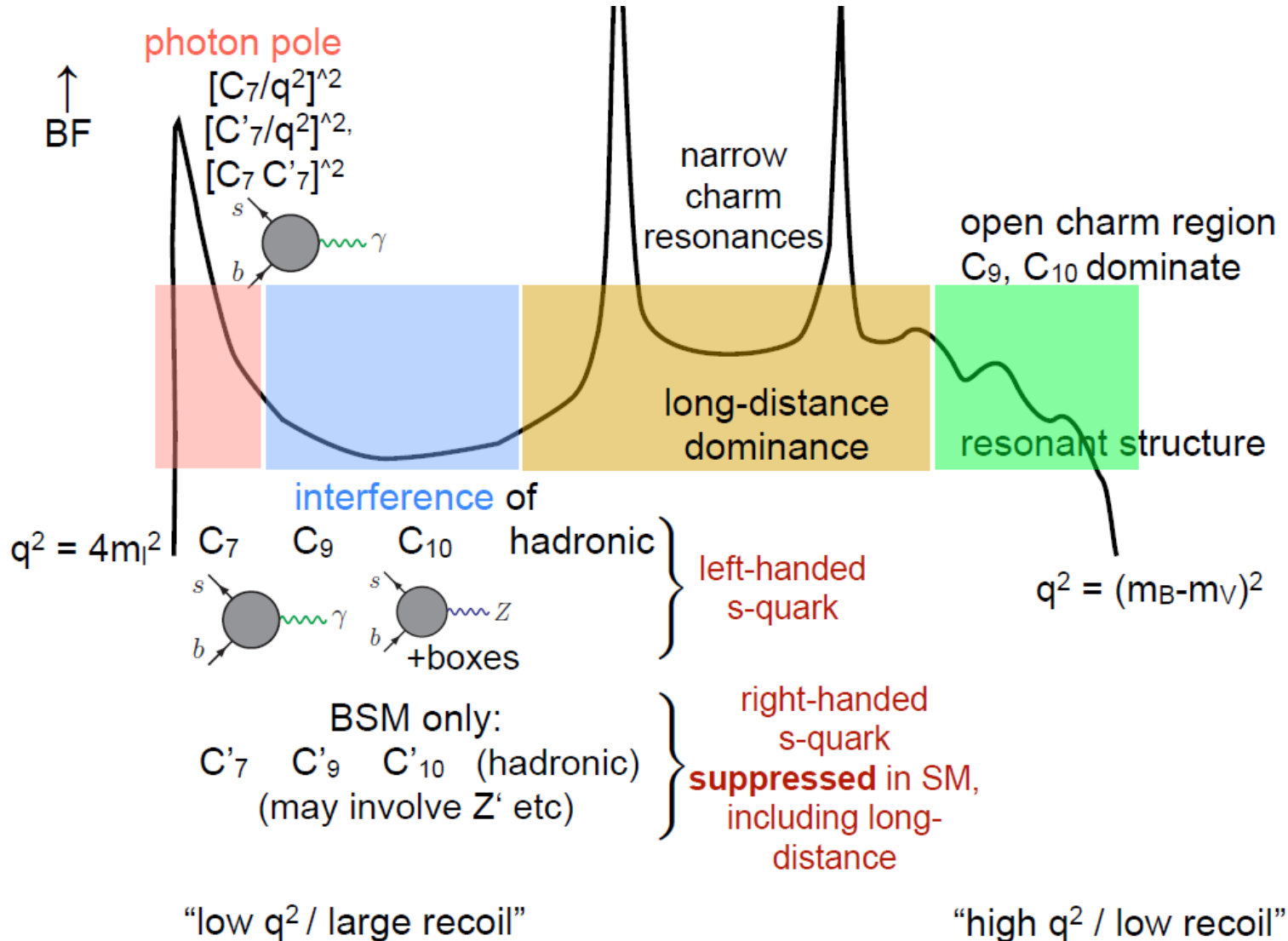
- This operator is automatically present for “left-handed” $R_{D^{(*)}}$ explanations via $(\bar{c}_L \gamma^\mu b_L) (\bar{\nu}_\tau \gamma_\mu \tau_L)$

This is a consequence of $SU(2)_W$ symmetry and the experimental bound on $B \rightarrow K^* \nu \bar{\nu}$ [Buras et al arXiv:1409.4557](#)

- Radiatively generated C_9 is again $O(1)$ and negative (and lepton-universal)

τ

B->V | I: rate (schematic)



Rare decay null tests of the SM

2 clean null tests of SM from (mainly) $B \rightarrow K^* \gamma$ and $B \rightarrow K^* \mu \mu$

$$P_1 \equiv \frac{I_9 + \bar{I}_9}{2(I_{2s} + \bar{I}_{2s})} = \frac{-2 \operatorname{Re}(H_V^+ H_V^{-*} + H_A^+ H_A^{-*})}{|H_V^+|^2 + |H_V^-|^2 + |H_A^+|^2 + |H_A^-|^2}$$

$$P_8^{CP} \equiv -\frac{I_9 - \bar{I}_9}{4(I_{2s} + \bar{I}_{2s})} = -\frac{\operatorname{Im}(H_V^+ H_V^{-*} + H_A^+ H_A^{-*})}{|H_V^+|^2 + |H_V^-|^2 + |H_A^+|^2 + |H_A^-|^2}$$

≈ 0

≈ 0

(Melikhov 1998)
 Krueger, Matias 2002
 Lunghi, Matias 2006
 Becirevic, Schneider 2011
 Becirevic, Kou, et al 2012
 SJ, Martin Camalich 2012

Very suppressed in the absence of right-handed currents. No effect seen in data.

‘Pseudo-observables:’ Wilson coefficients from global fit

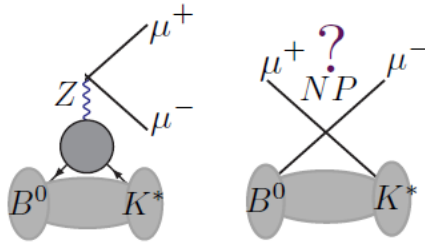
$$C'_{7\gamma} = 0.018 \pm 0.037 \quad \text{Aebischer et al arXiv:1903.10434}$$

$$C'_{9V} = 0.09 \pm 0.15 \quad \text{Paul \& Straub arXiv:1608.02556}$$

Decay amplitude structure

Two mechanisms to produce dilepton in & beyond SM

- via axial lepton current (in SM: Z, boxes) **C10**



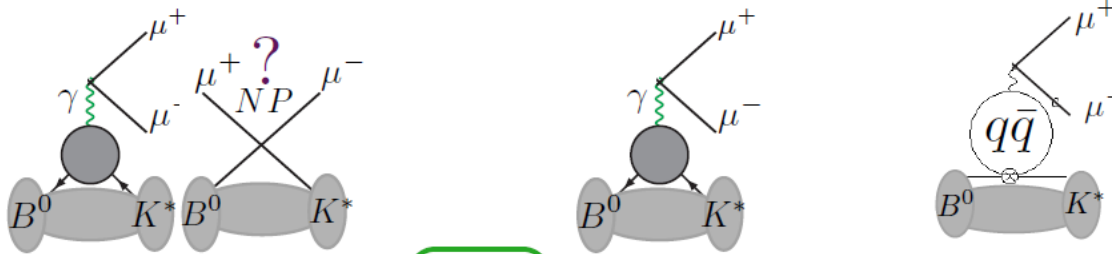
K^* helicity

$$H_A(\lambda) \propto \tilde{V}_\lambda(q^2) C_{10} - V_{-\lambda}(q^2) C'_{10}$$

one form factor (nonperturbative) per helicity
amplitudes factorize naively

[nb - one more amplitude if not neglecting lepton mass]

- via vector lepton current (in SM: (mainly) photon) **C7, C9, hadronic hamiltonian**



$$H_V(\lambda) \propto \tilde{V}_\lambda(q^2) C_9 - V_{-\lambda}(q^2) C'_9 + \frac{2m_b m_B}{q^2} (\tilde{T}_\lambda(q^2) C_7 - \tilde{T}_{-\lambda}(q^2) C'_7) - \frac{16\pi^2 m_B^2}{q^2} h_\lambda(q^2)$$

photon pole at $q^2=0$

two form factors interfere for each helicity

nonlocal “quark loops”
do **not** factorize naively

Natural, systematic discussion in terms of helicity amplitudes **SJ, Martin Camalich 2012, 2014**

Photon pole absent for helicity-0 (form factor rescaling)

Rare B-decay: observables

Branching ratios

leptonic (differential in dilepton mass)

$$B_s \rightarrow \mu\mu, B_d \rightarrow \mu\mu,$$

Nonperturbative QCD fully controlled (decay constant from lattice)

semileptonic (differential in dilepton mass)

$$B \rightarrow K^{(*)}\mu\mu, B \rightarrow K^{(*)}ee, B_s \rightarrow \phi\mu\mu$$

Lepton universality ratios

$$R_{K^{(*)}}[a, b] = \frac{\int_a^b \frac{d\Gamma}{dq^2}(B \rightarrow K^{(*)}\mu^+\mu^-)dq^2}{\int_a^b \frac{d\Gamma}{dq^2}(B \rightarrow K^{(*)}e^+e^-)dq^2}$$

Form factors, 4-quark operator contributions, QED radiation cancel out to $\sim\%$ level (relative to LHCb treatment)

eg Bordone, Isidori, Pattori arXiv:1605.07633

differential angular distribution for $B \rightarrow VII$

3 angles, dilepton mass q^2

7 angular differential observables:

$(A_{FB}, P_5', \text{ etc})$

