

# Low Energy? Think Positive!

UV Constraints on IR Effective Field Theories

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“Positivity” Bounds

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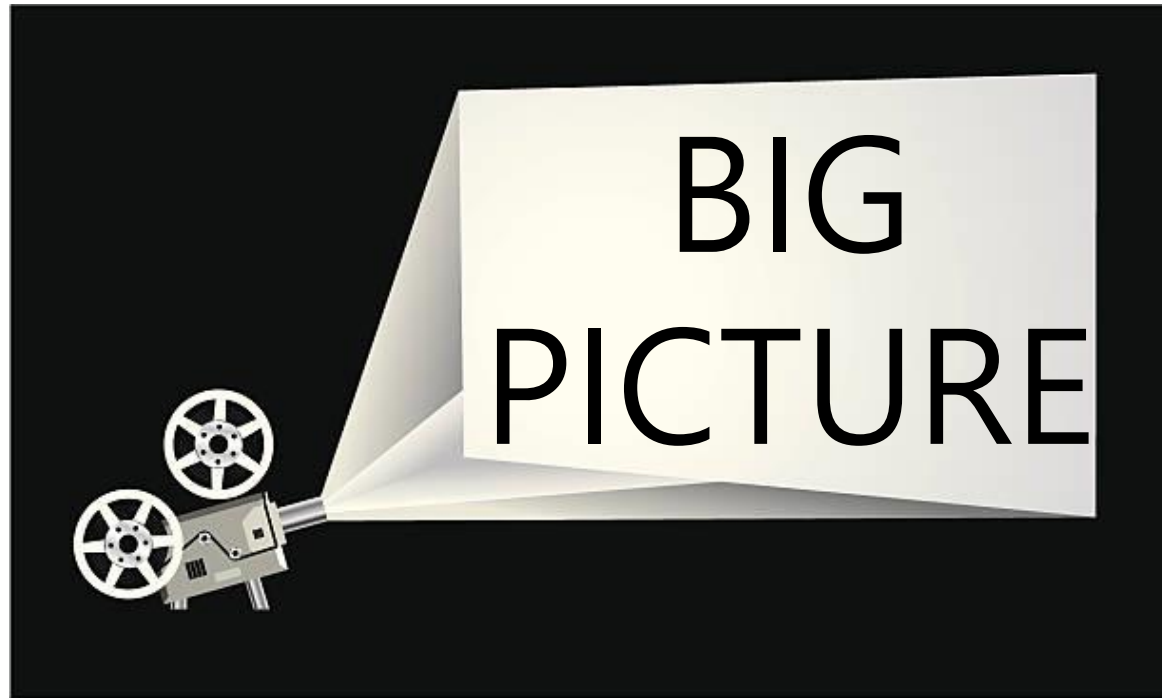
UV Constraints on IR Effective Field Theories

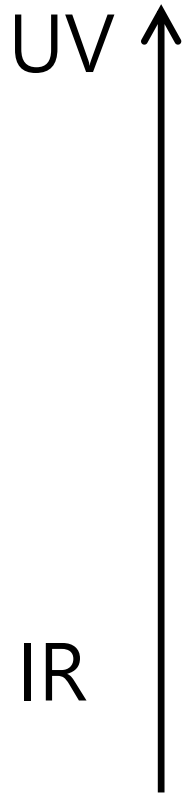
“Positivity” Bounds



Vector Boson Scattering

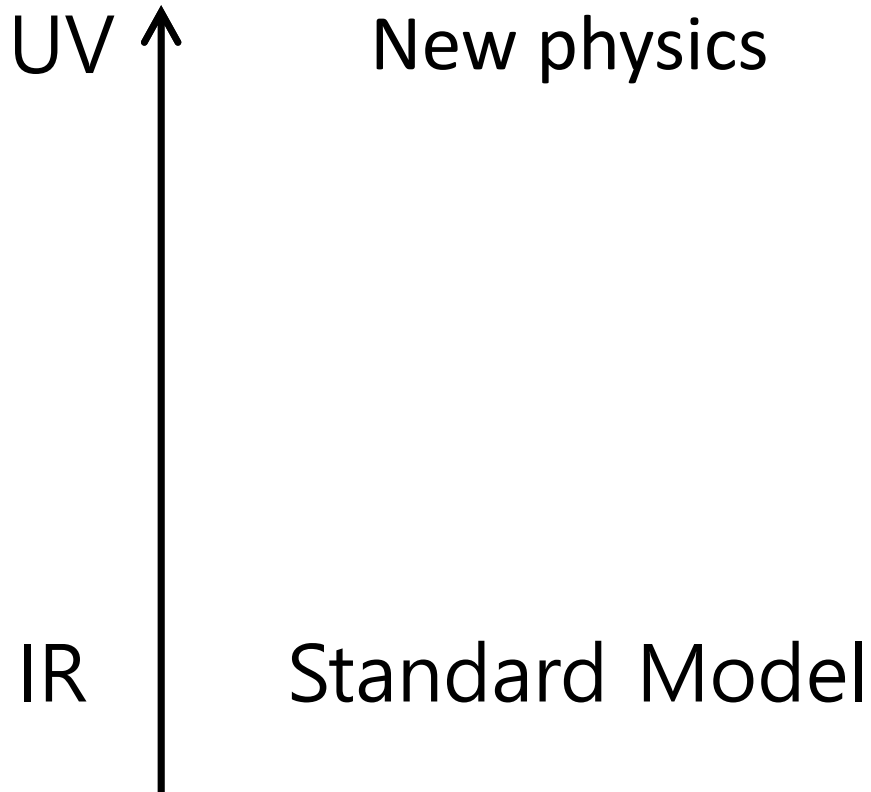
B-physics Anomalies

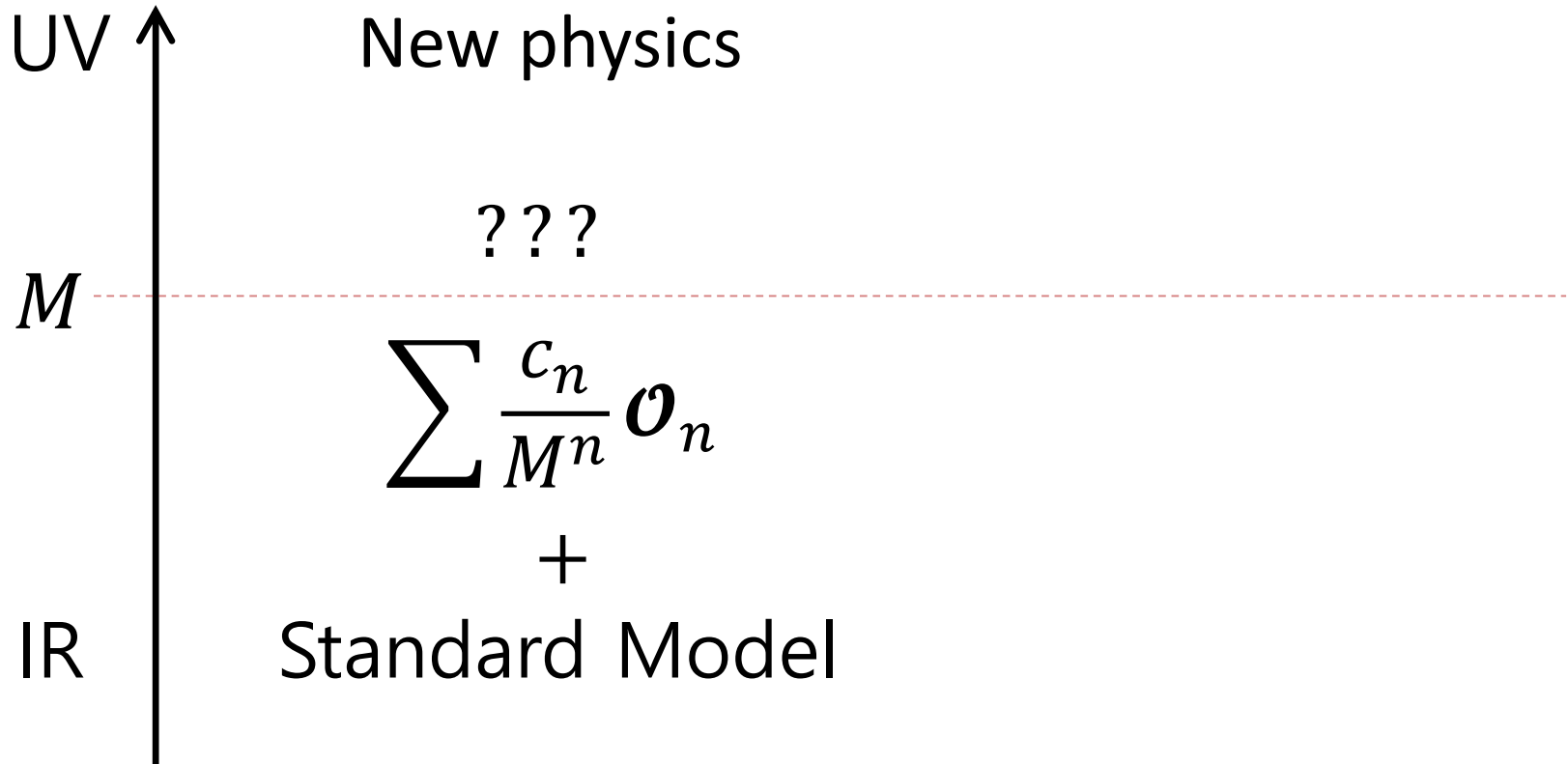




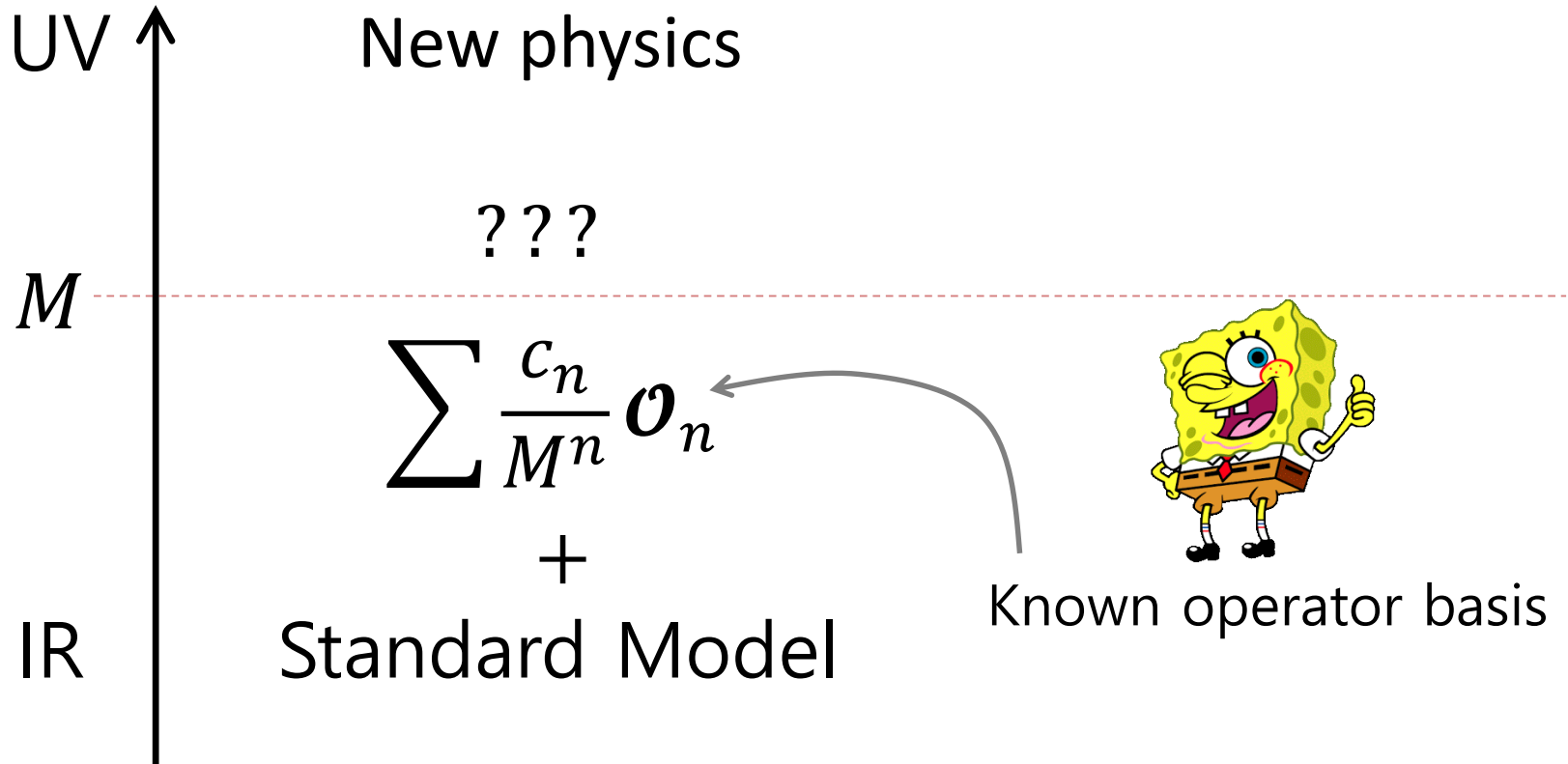


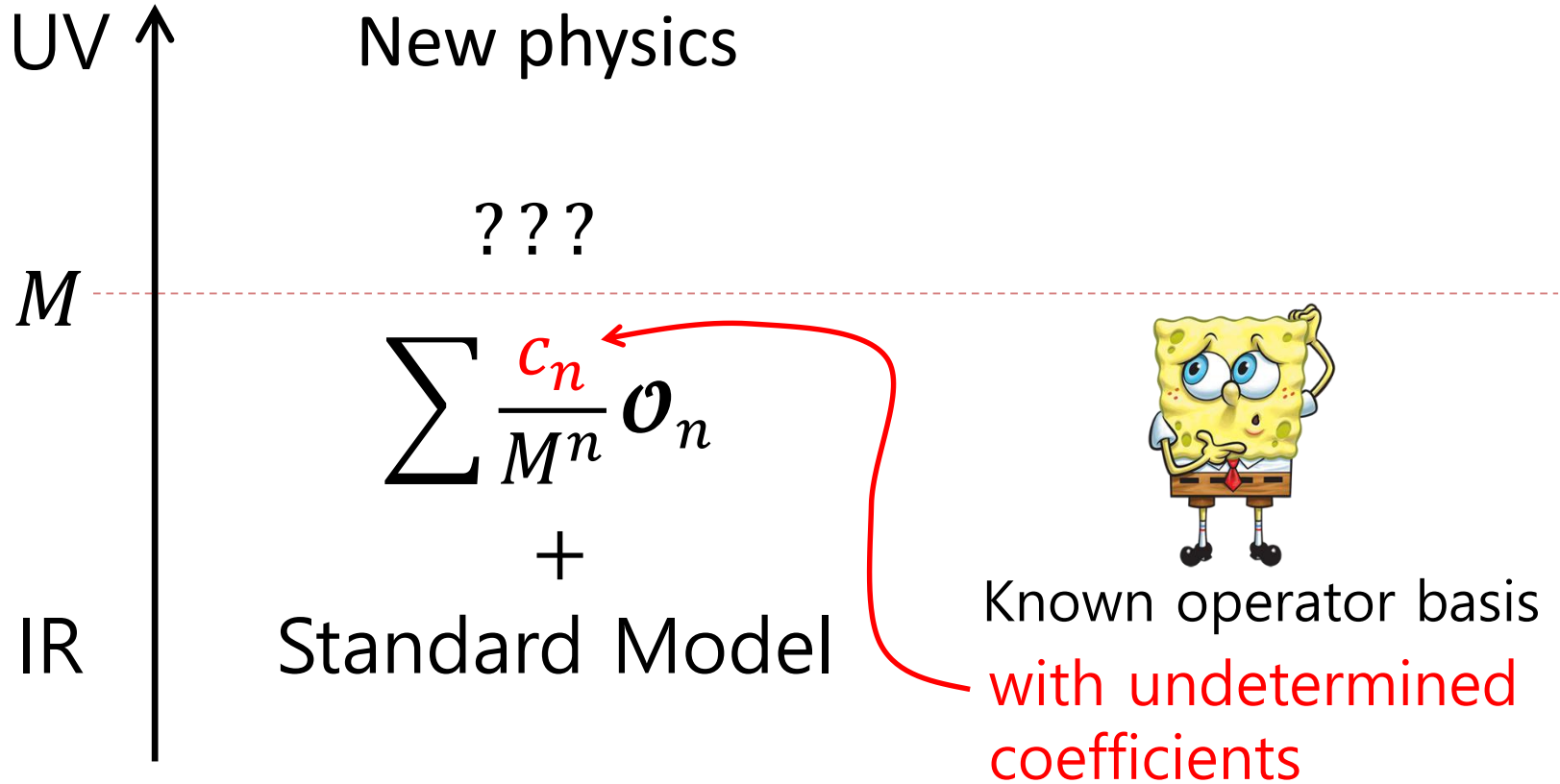
Standard Model

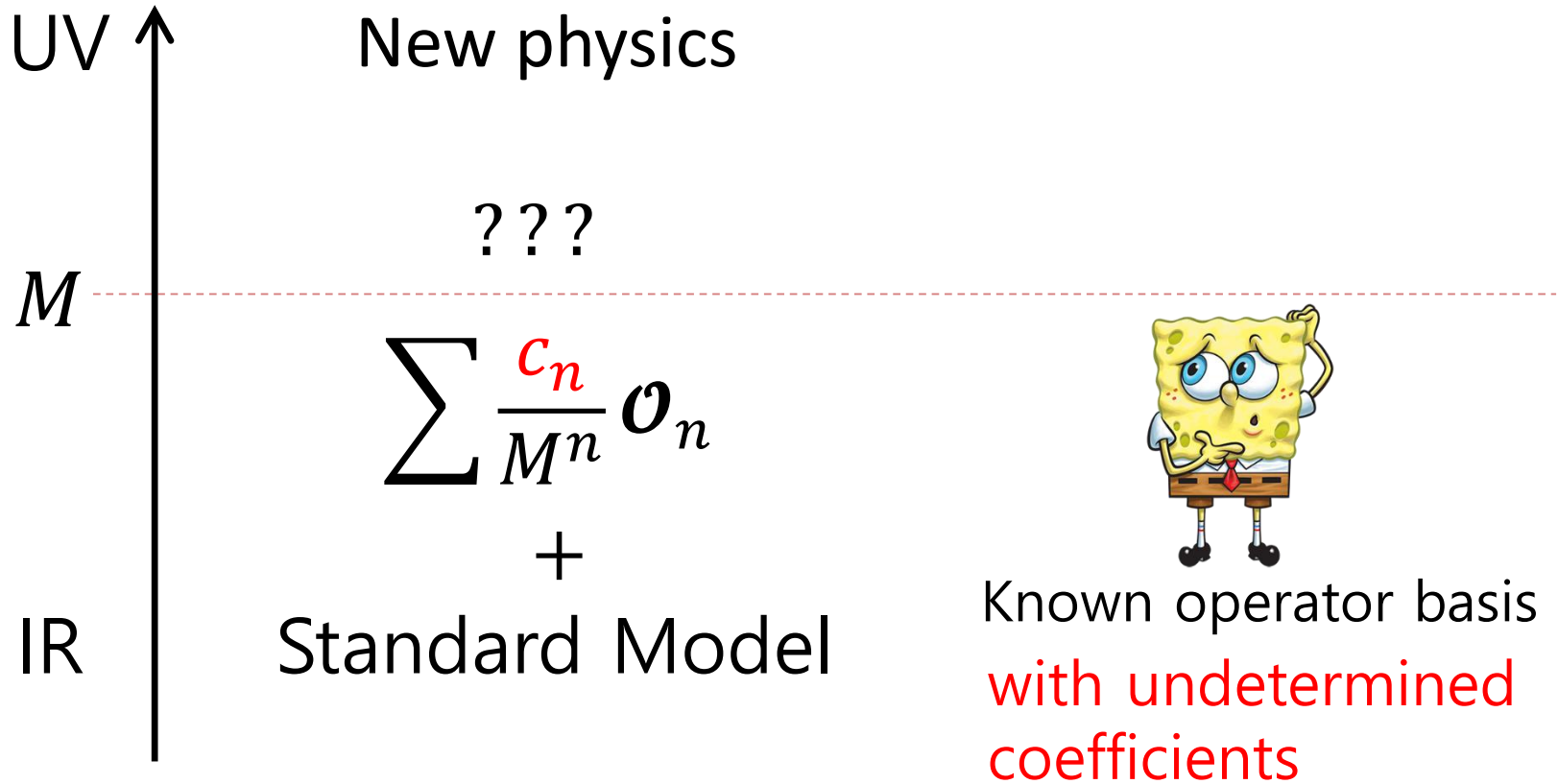




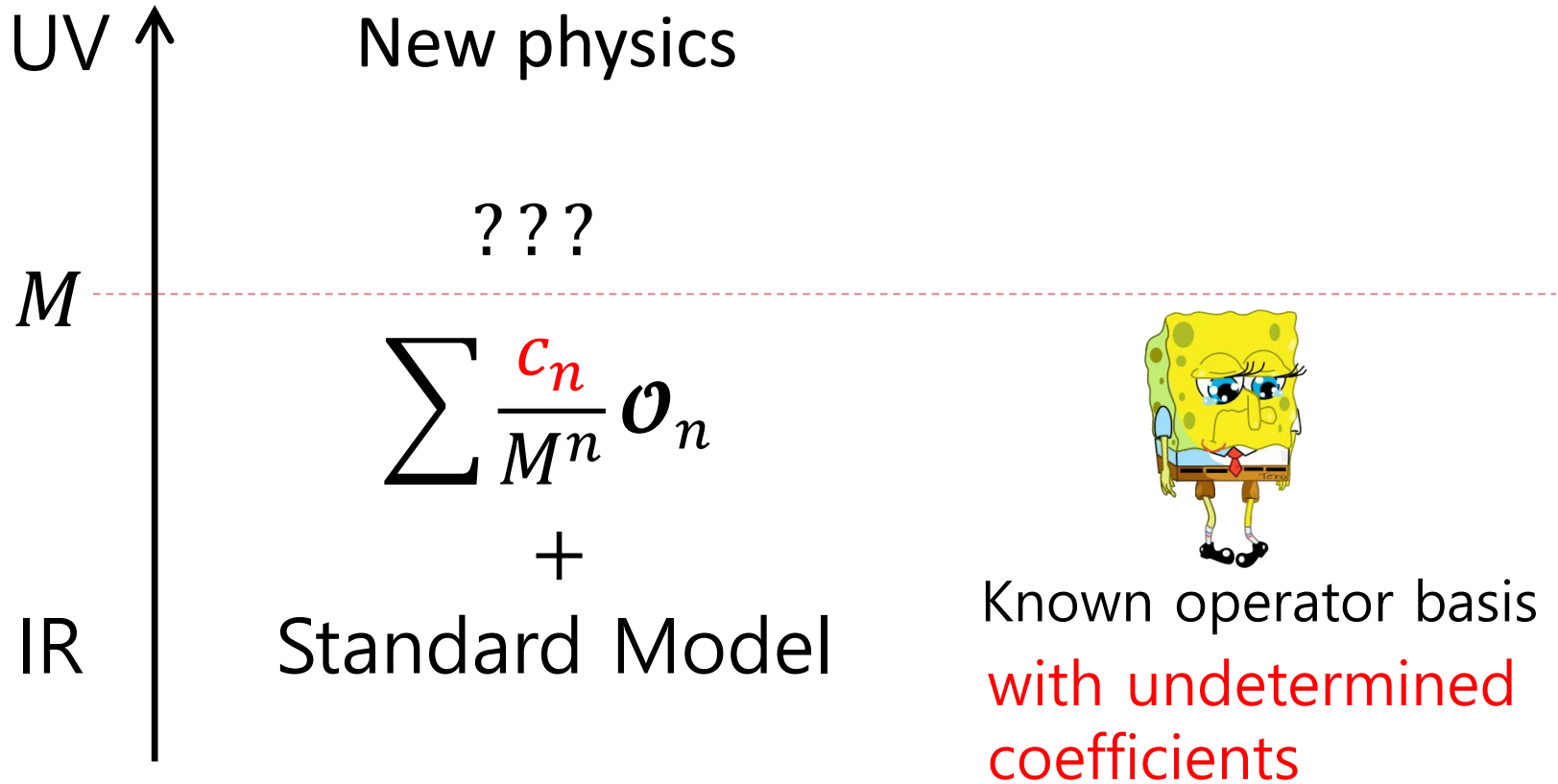




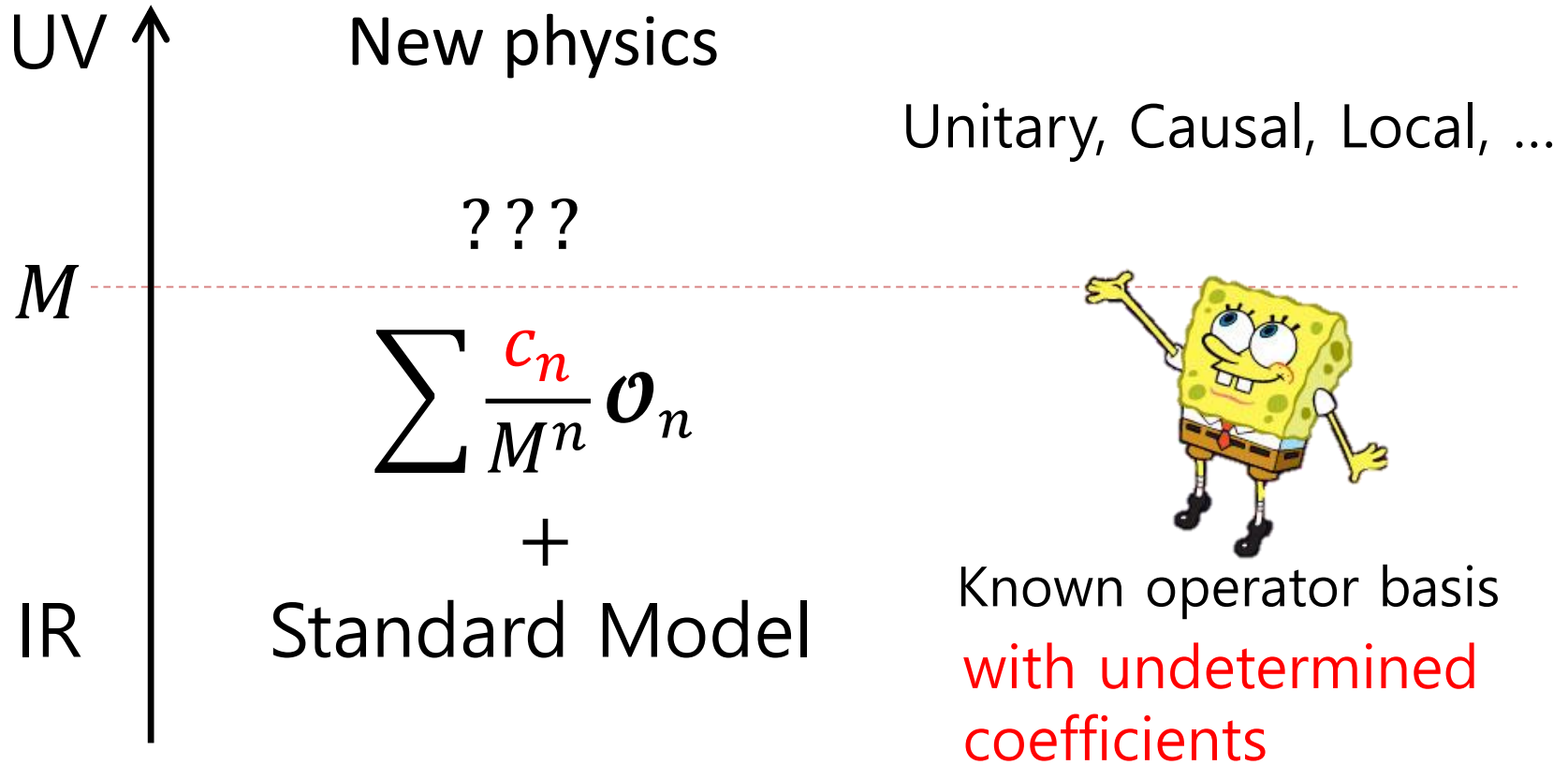




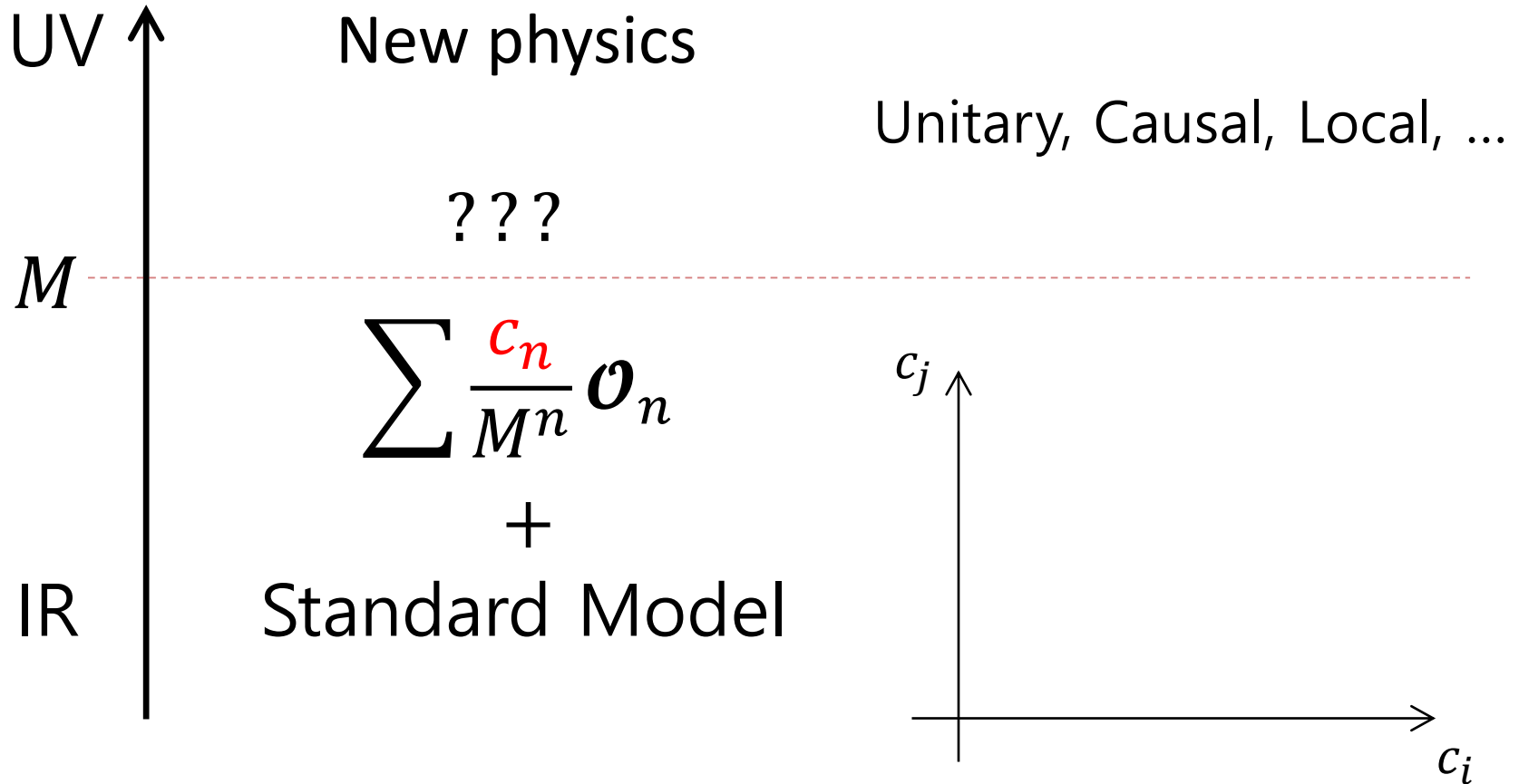
(1) Need many measurements



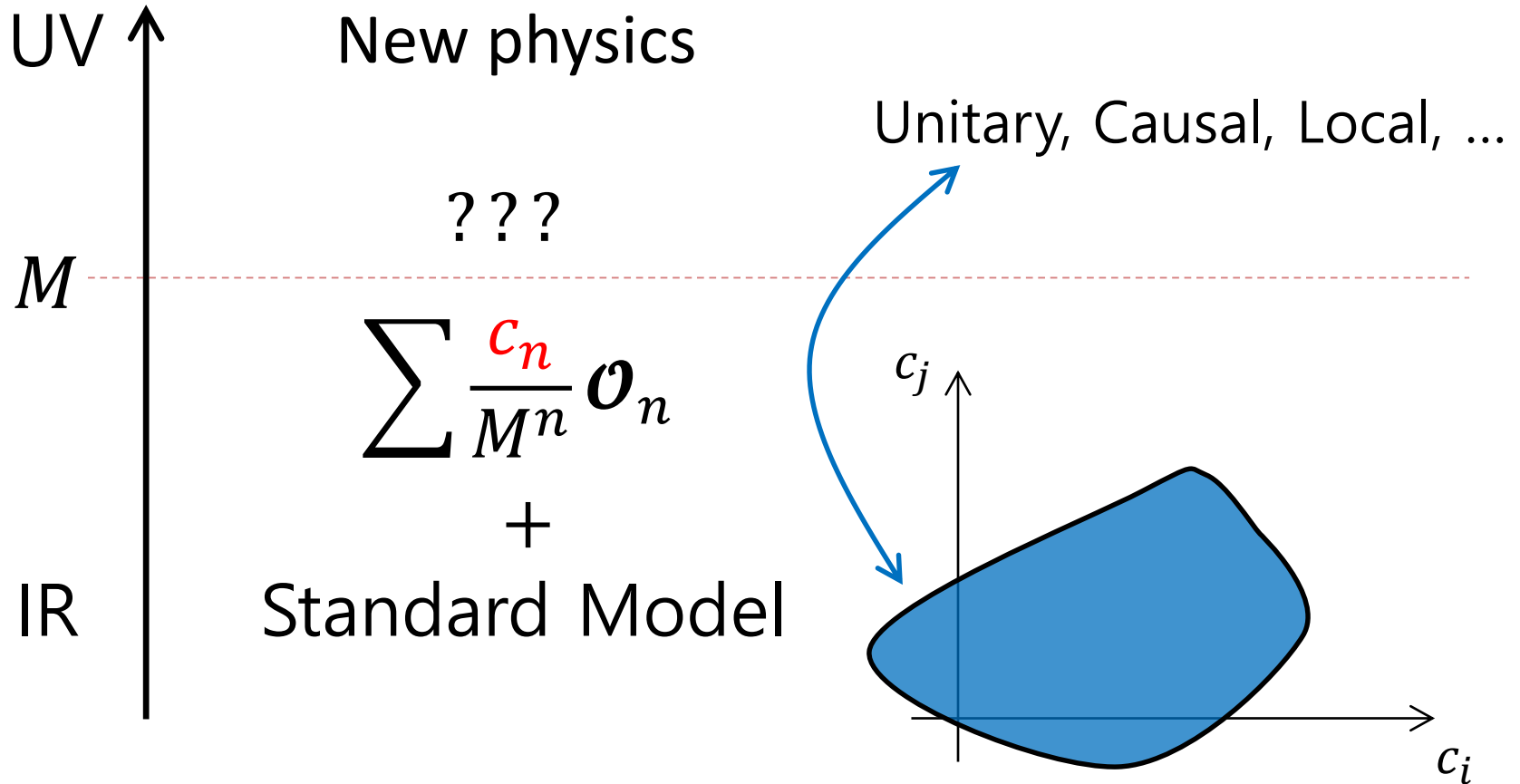
- (1) Need many measurements
- (2) No deeper understanding of UV physics



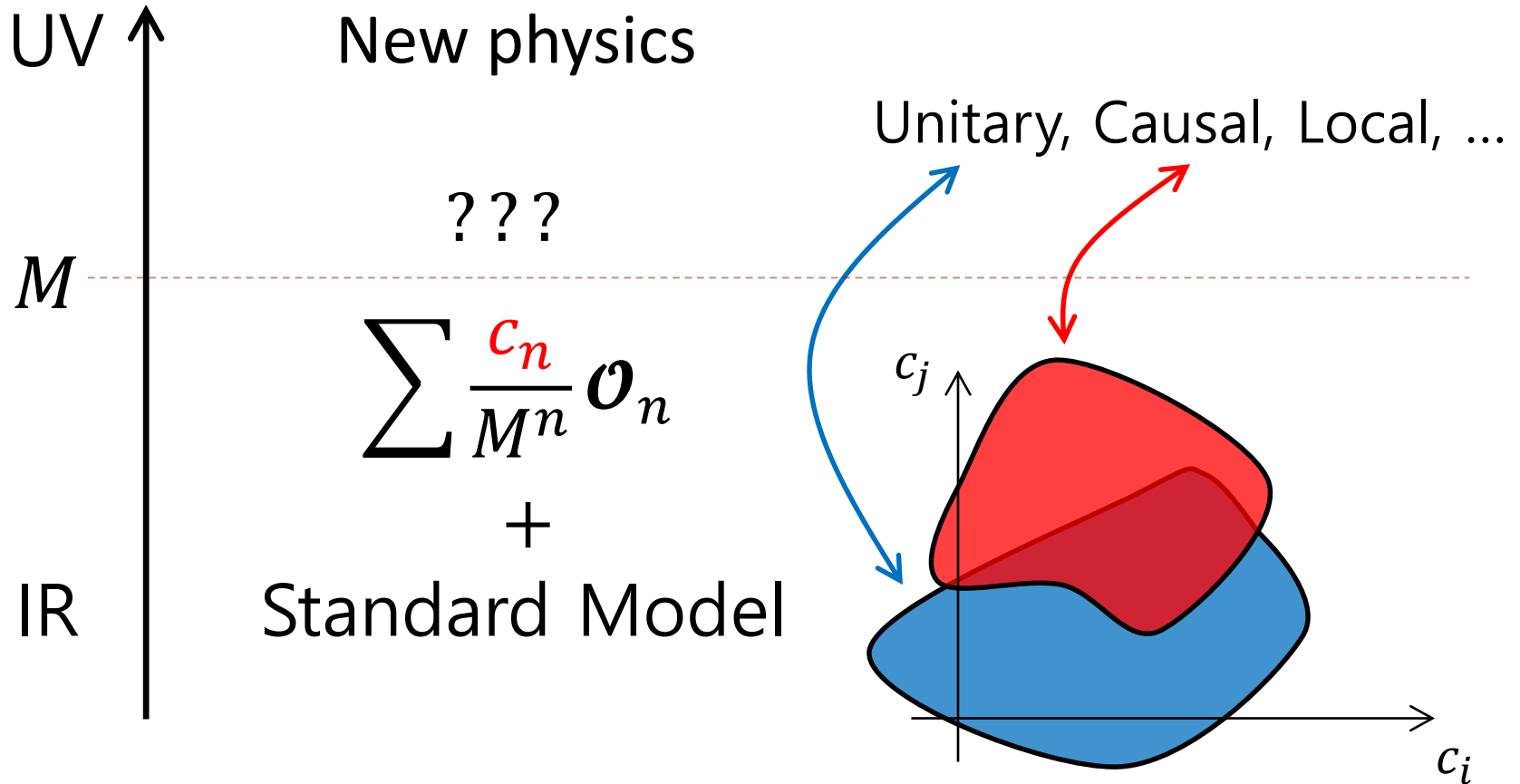
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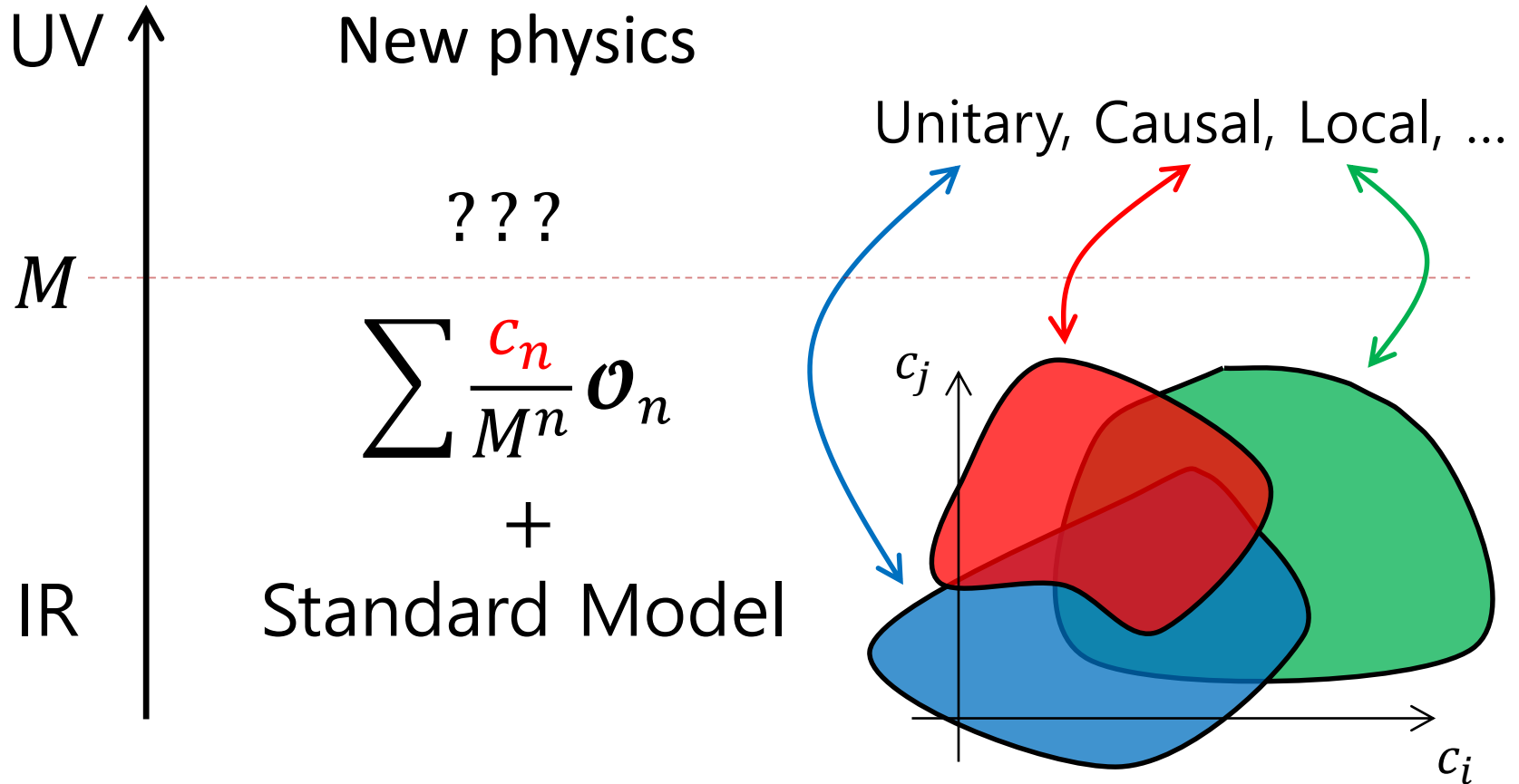


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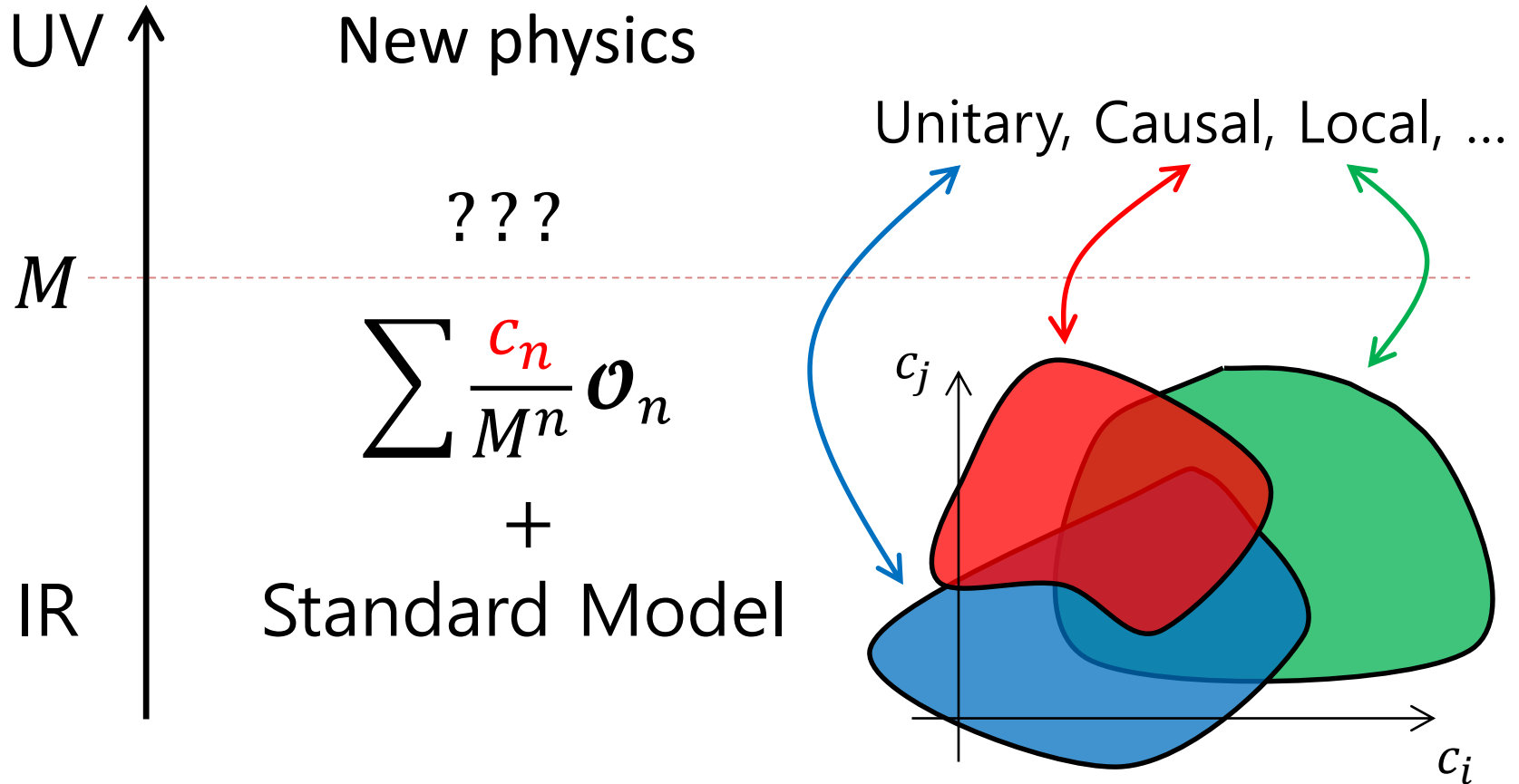


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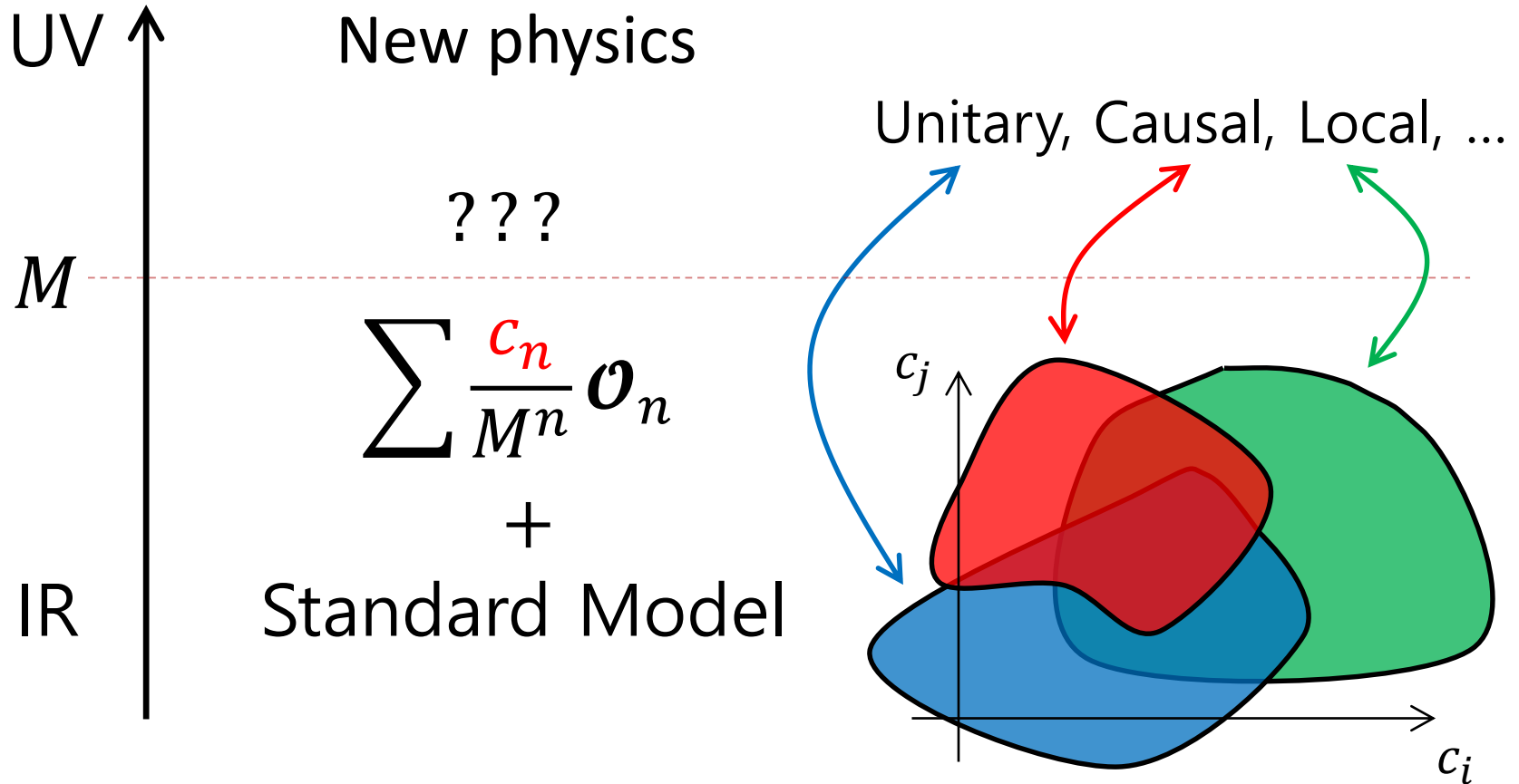




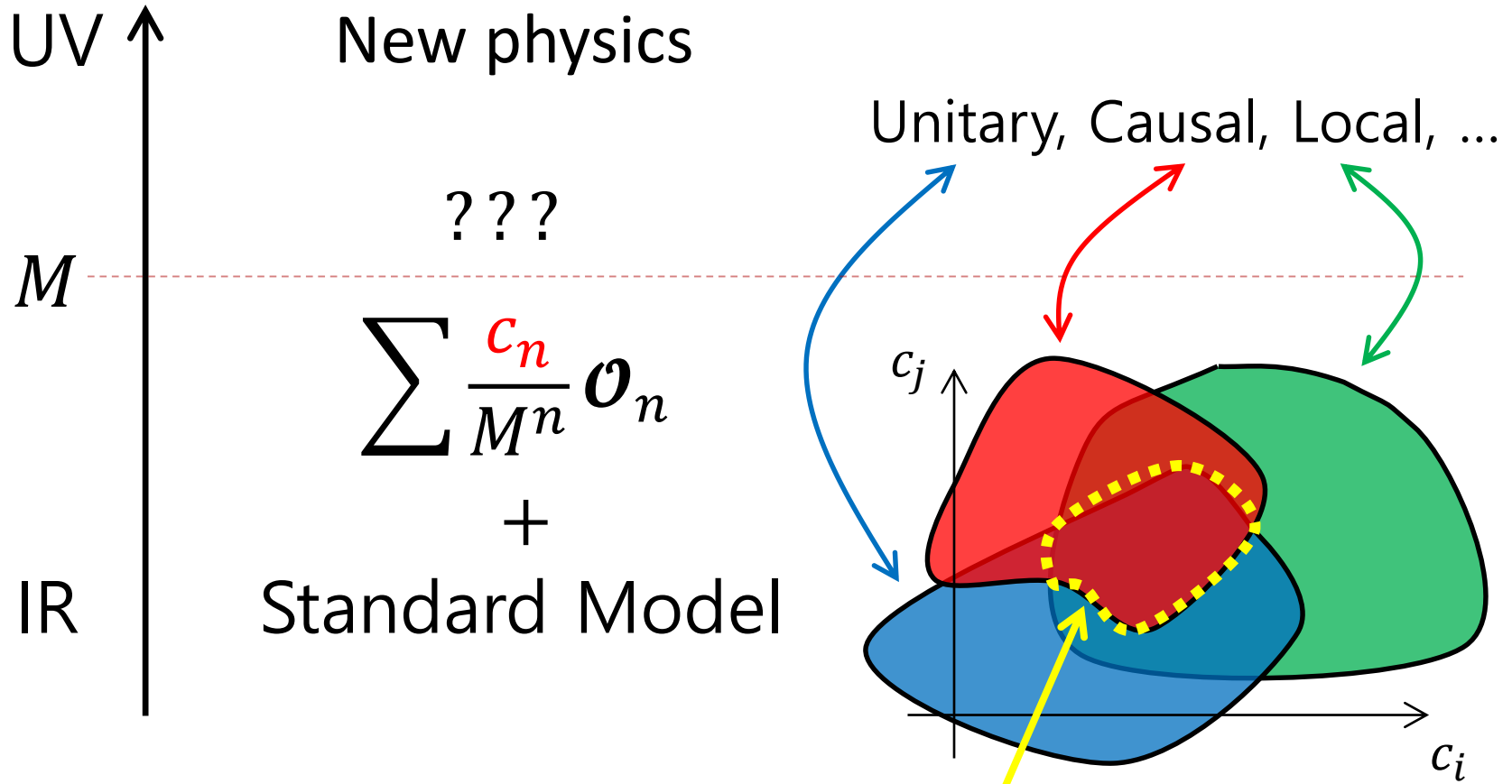
- (1) Need many measurements
- (2) No deeper understanding of UV physics



- ✓ (1) Data more constraining
- (2) No deeper understanding of UV physics



- ✓ (1) Data more constraining
- ✓ (2) Can infer UV properties from IR measurements

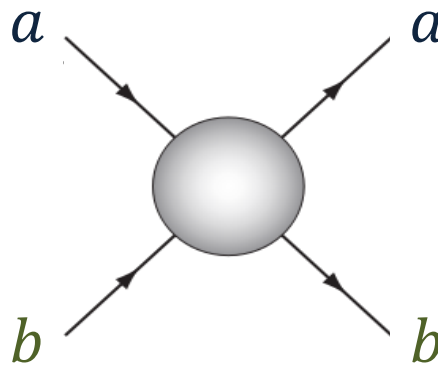


- ✓ (1) Data more constraining
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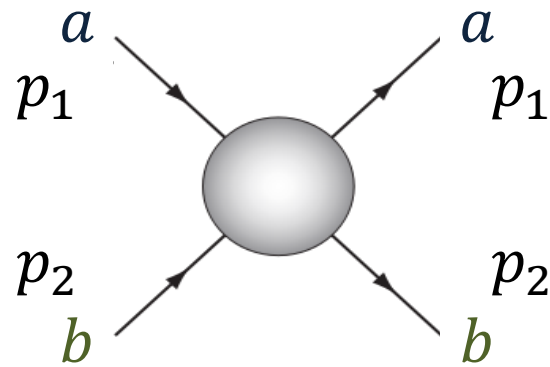
[Adams et al., 0602178]

[SM et al., in prep]



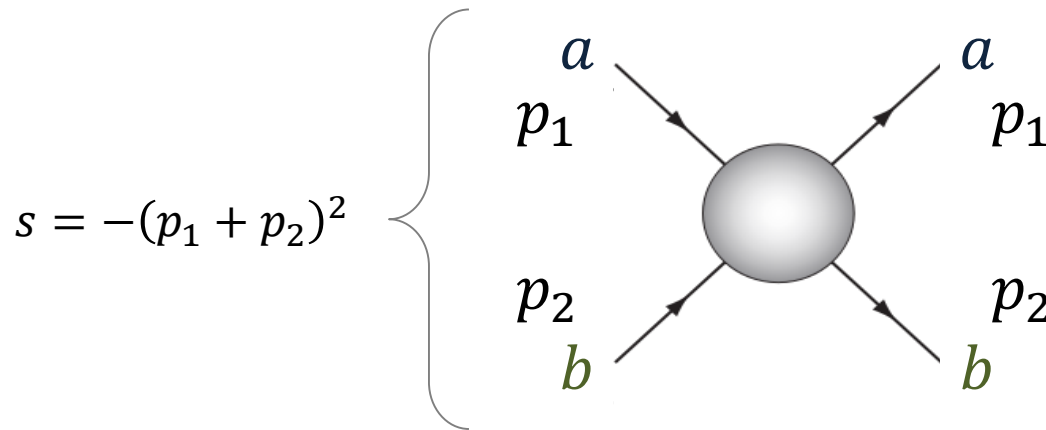
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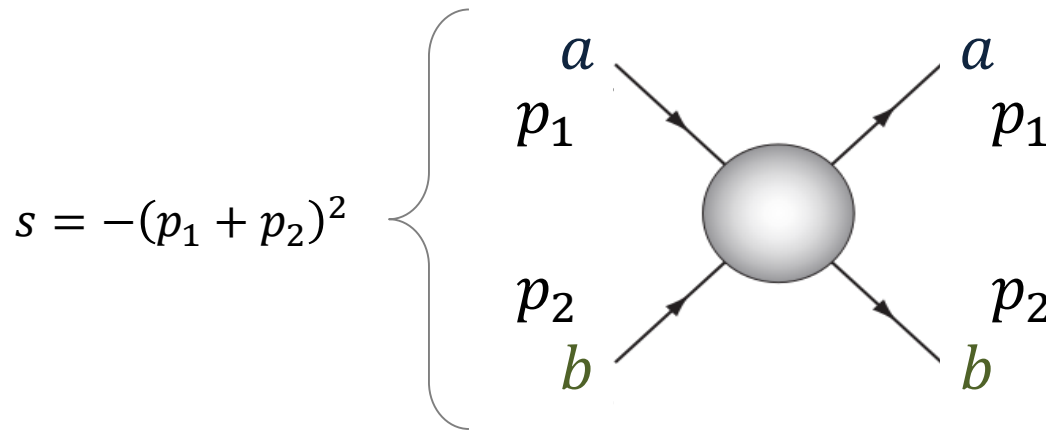


$$A_{EFT}(s) = c_0 + c_s \frac{s}{M^2} + c_{ss} \frac{s^2}{M^4} + \dots$$



[Adams et al., 0602178]

[SM et al., in prep]

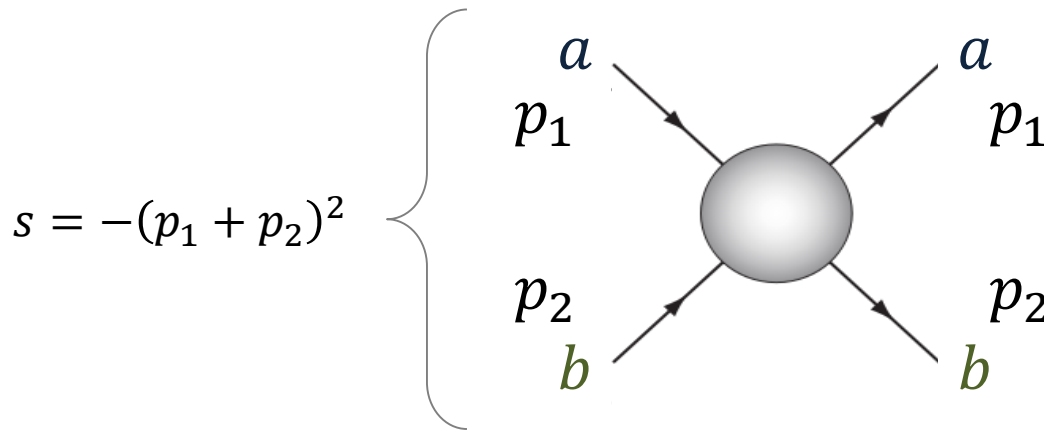


$$A_{EFT}(s) = c_0 + c_s \frac{s}{M^2} + c_{ss} \frac{s^2}{M^4} + \dots$$

If new physics is unitary and causal, then:

[Adams et al., 0602178]

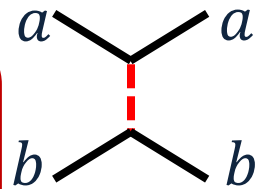
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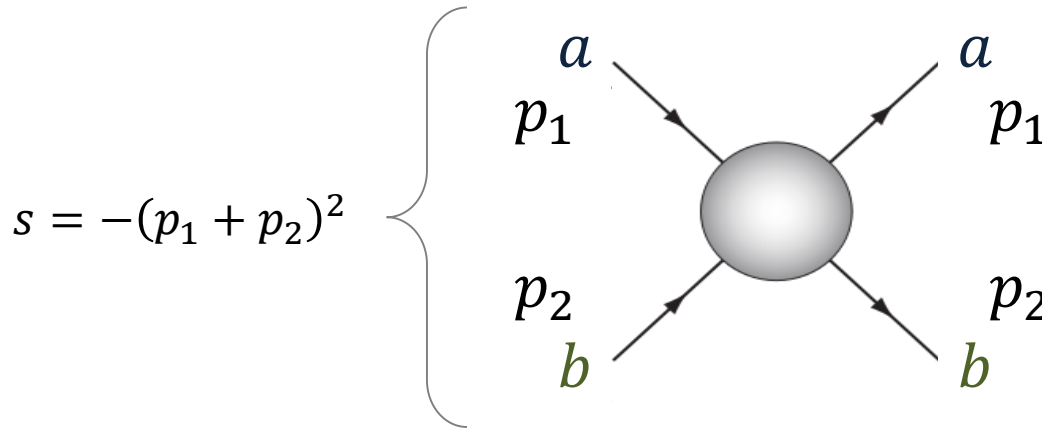
If new physics is unitary and causal, then:

$$c_s < 0 \quad \Rightarrow \quad \text{New physics in } t \text{ channel}$$



[Adams et al., 0602178]

[SM et al., in prep]

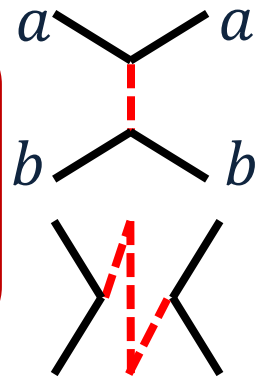


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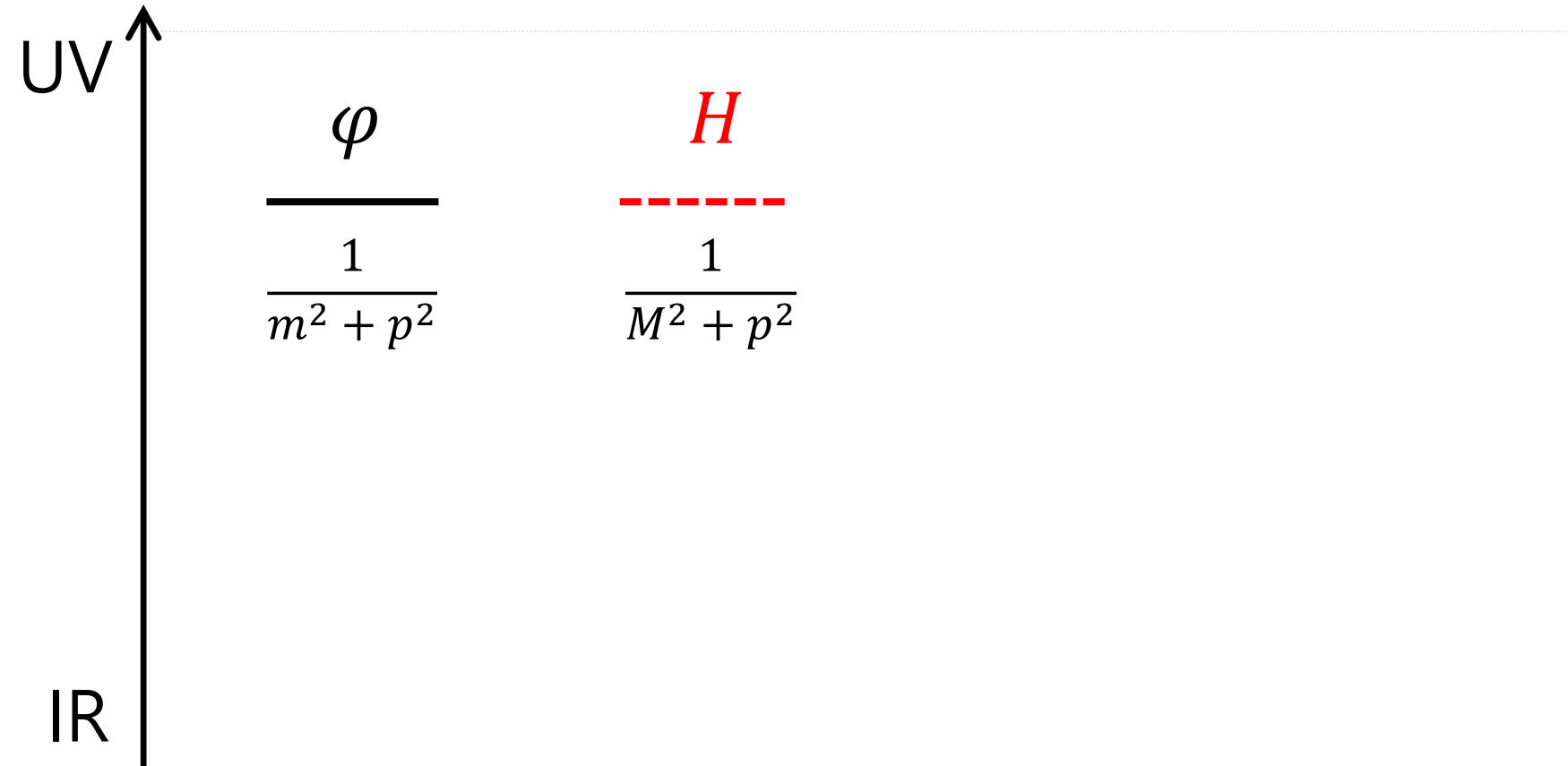
$c_s < 0 \Rightarrow$  New physics in  $t$  channel

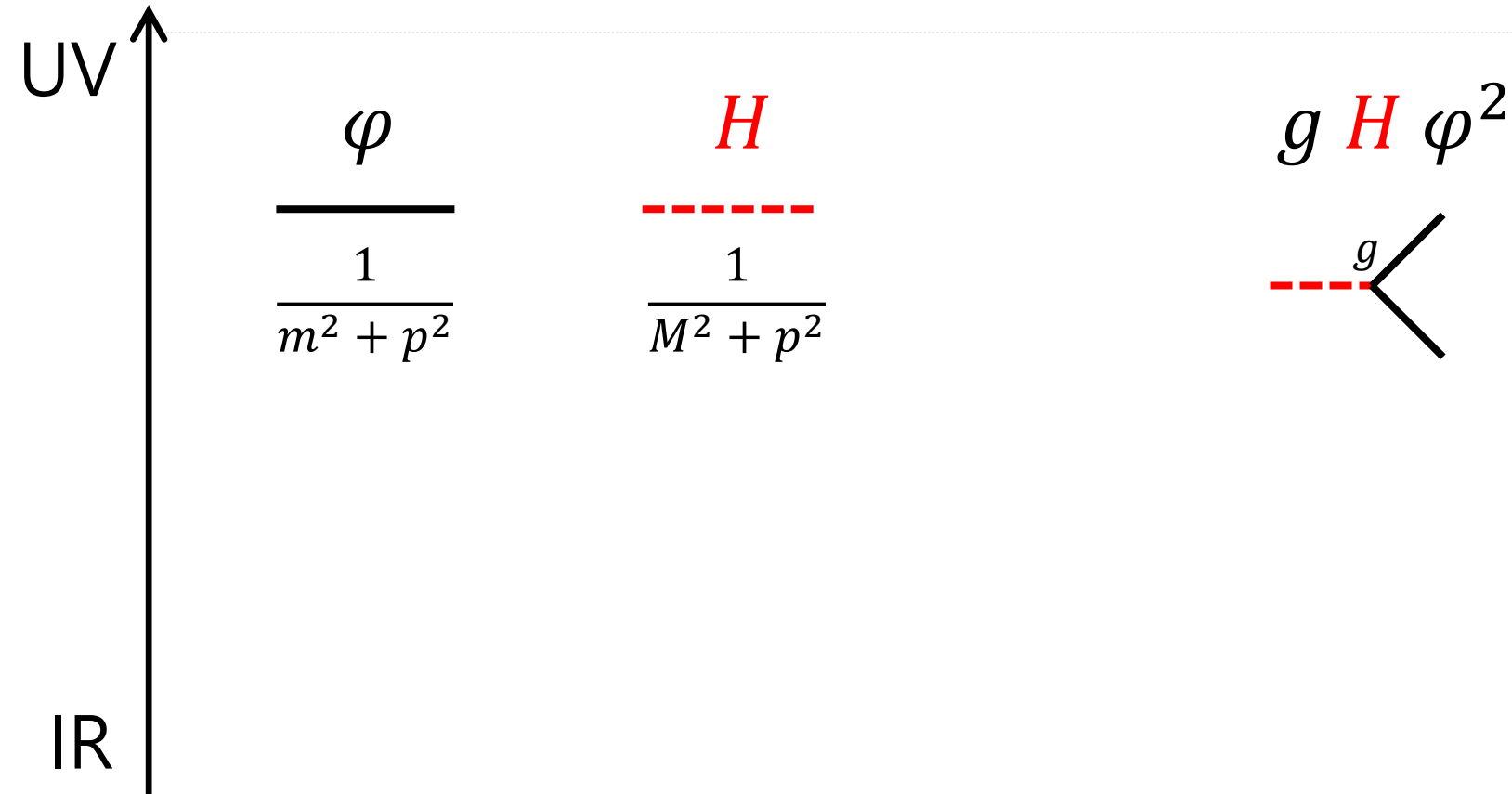
$c_{ss} < 0 \Rightarrow$  New physics is non-local



## New Local Physics

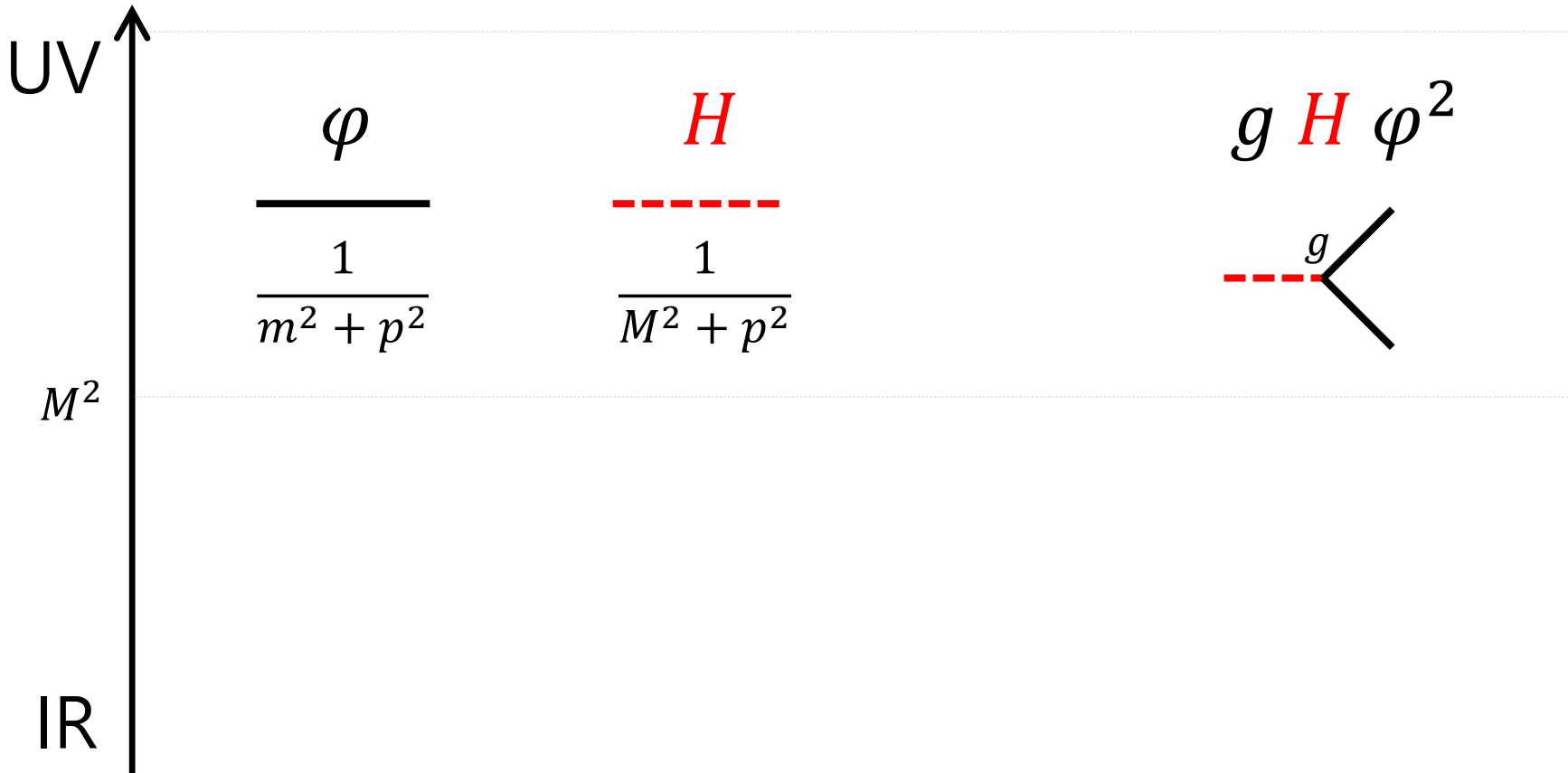
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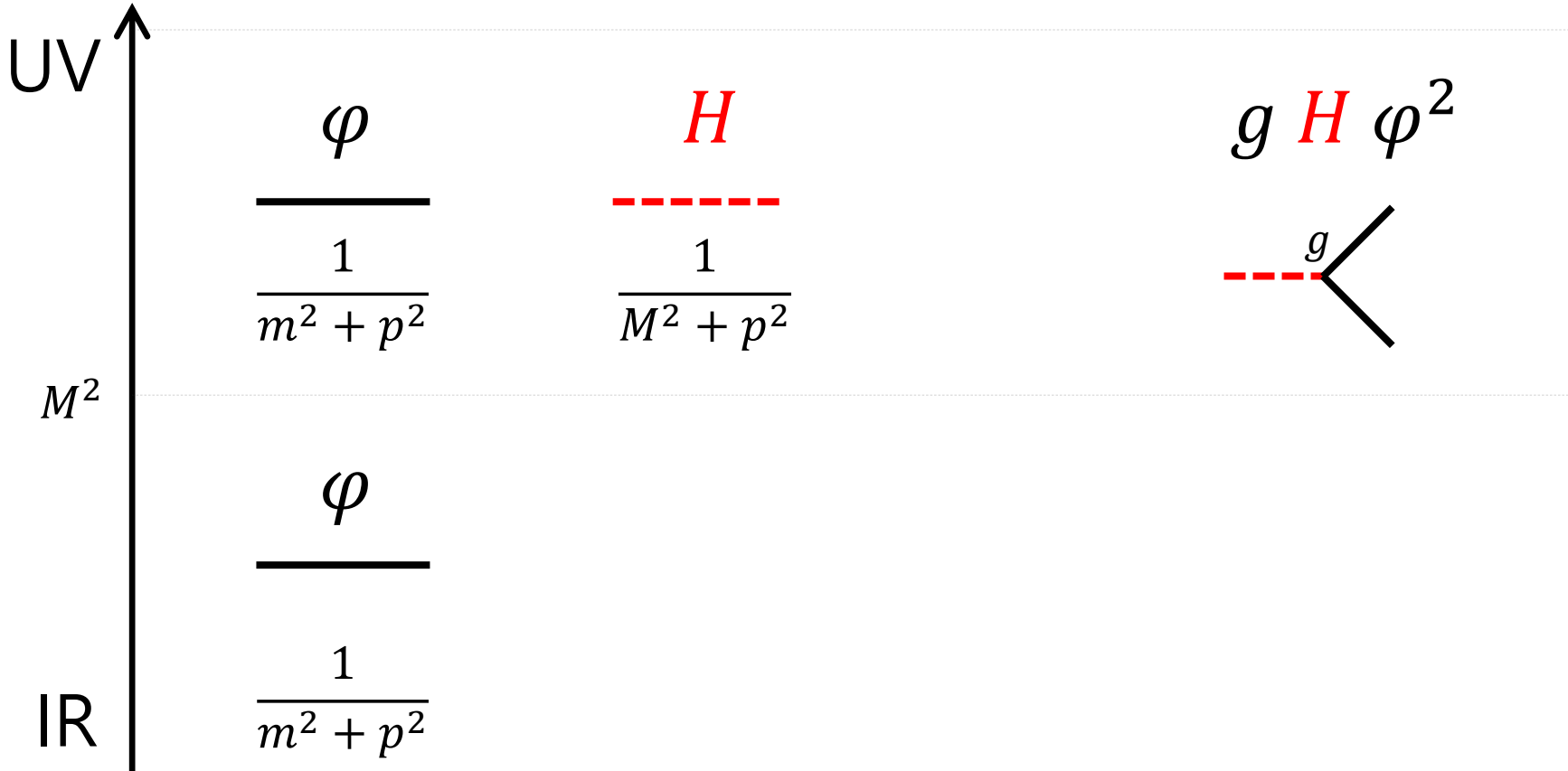
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New Local Physics

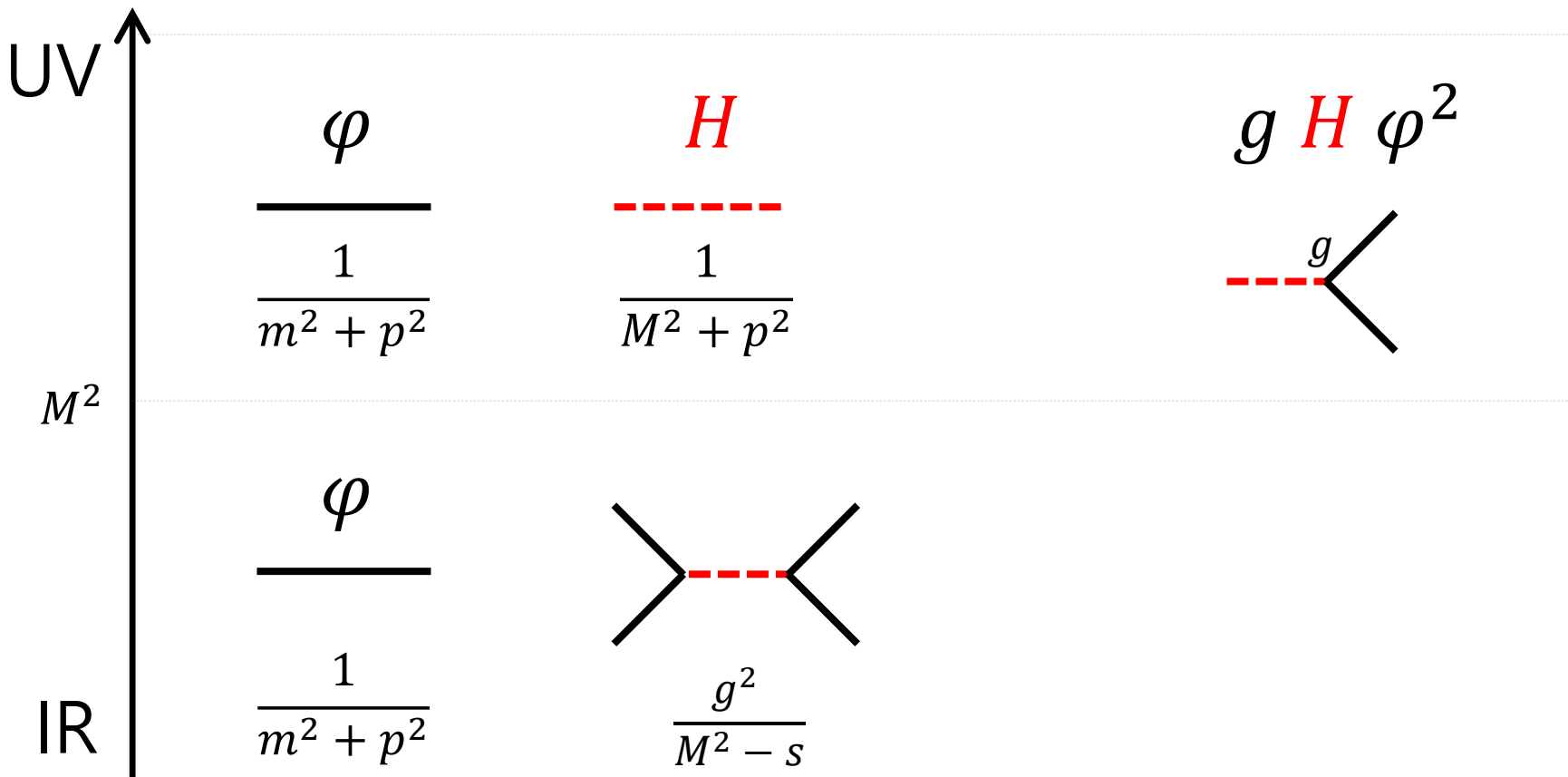
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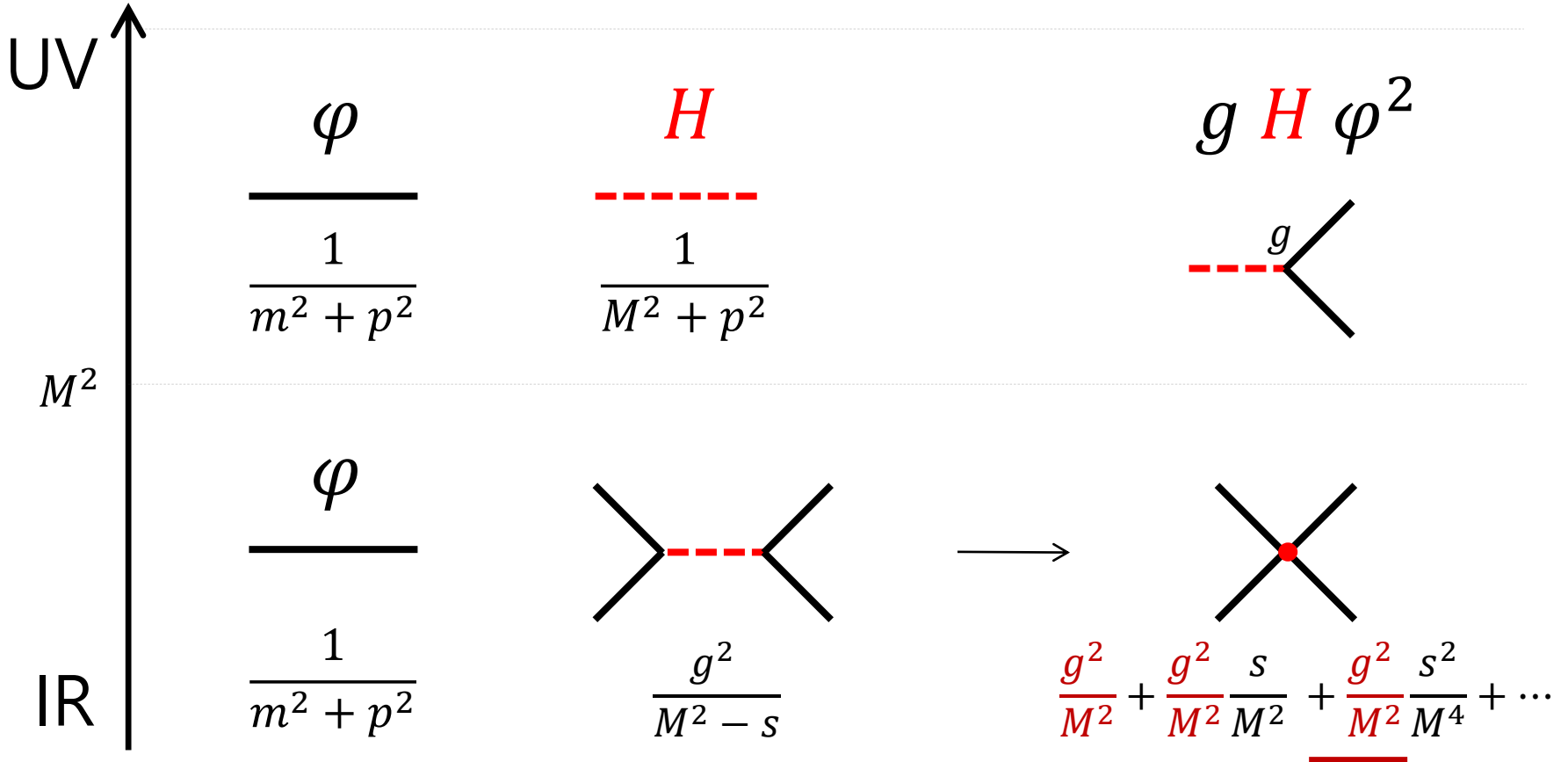
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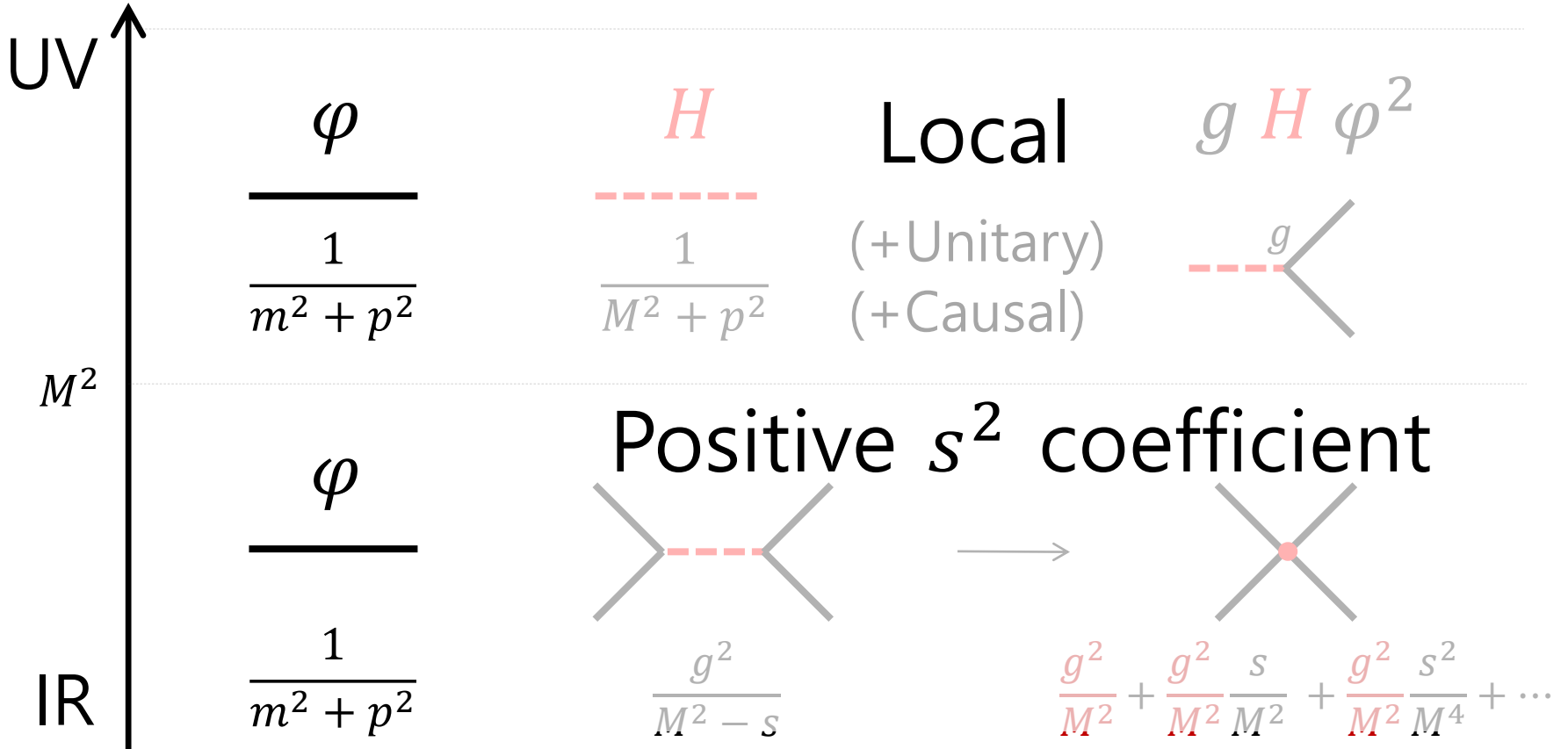
New Local Physics

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New  $t$ -channel Physics $c_s < 0 \Rightarrow$  New physics in  $t$  channel

UV  
↑  
IR



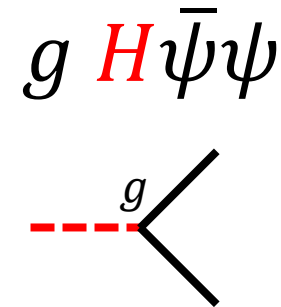
# New $t$ -channel Physics

$$c_s < 0 \Rightarrow \text{New physics in } t \text{ channel}$$



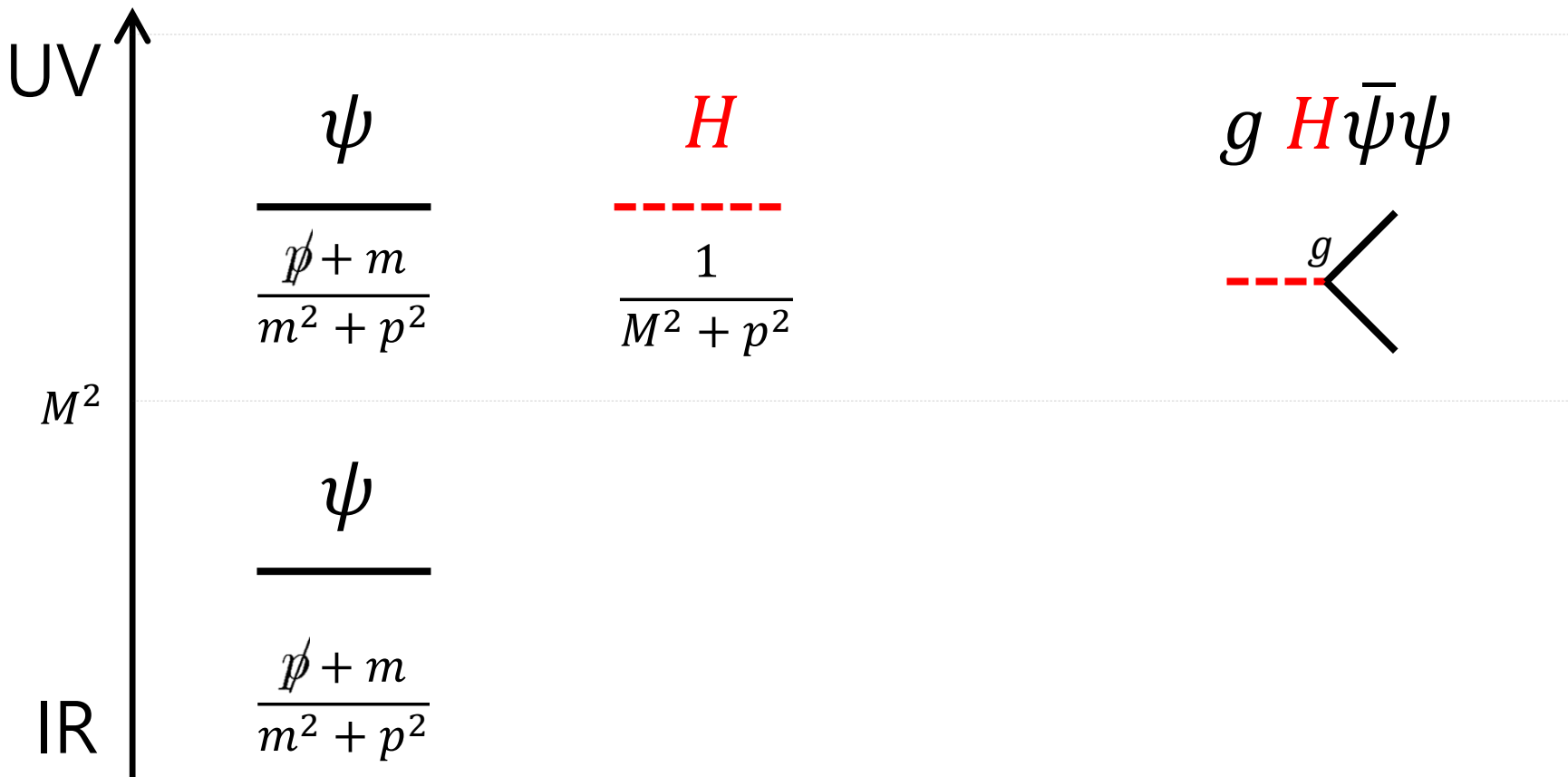
$$\frac{\psi}{\frac{\not{p} + m}{m^2 + p^2}}$$

$$\frac{H}{\frac{1}{M^2 + p^2}}$$



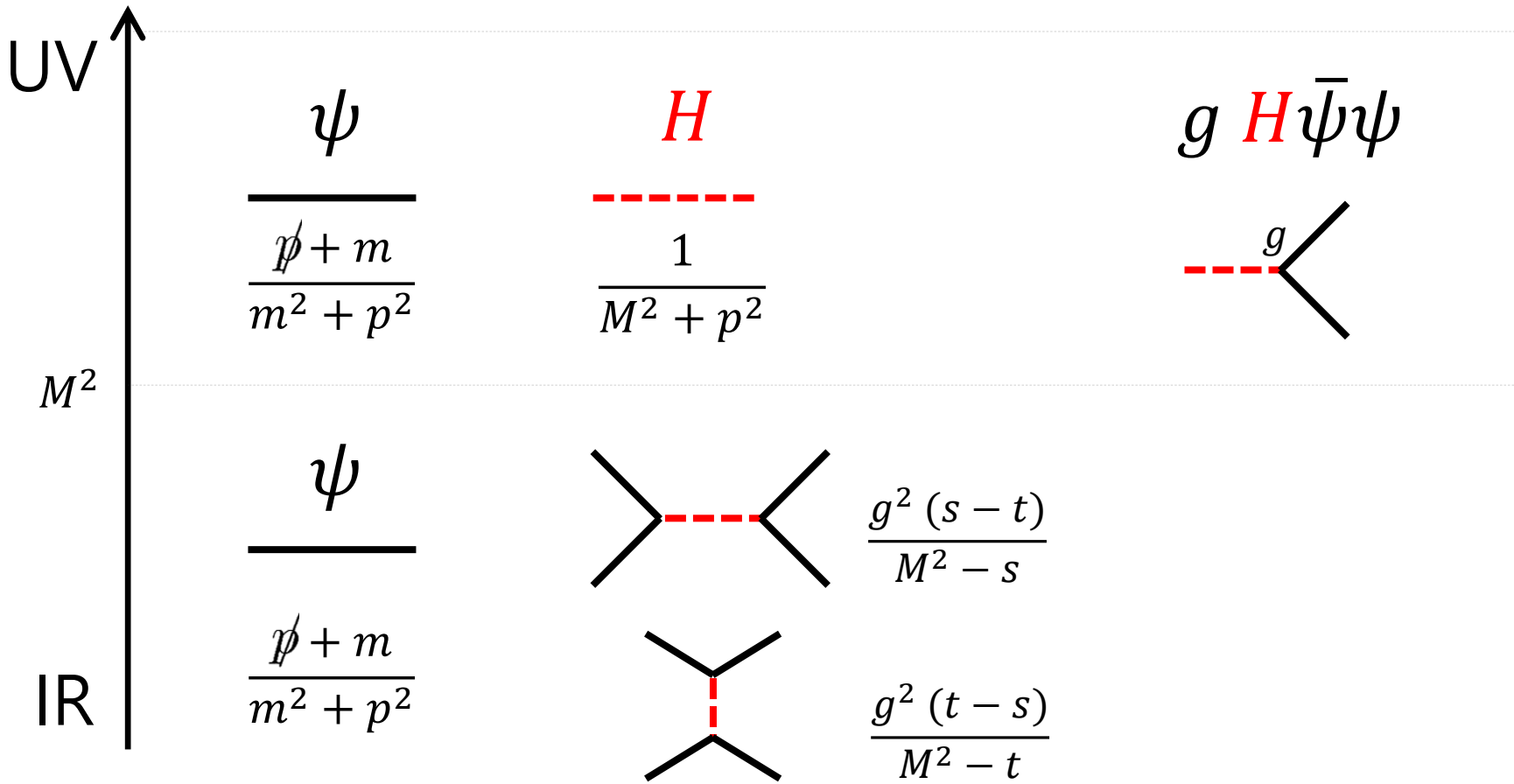
New  $t$ -channel Physics

$c_s < 0 \Rightarrow$  New physics in  $t$  channel



# New $t$ -channel Physics

$c_s < 0 \Rightarrow$  New physics in  $t$  channel



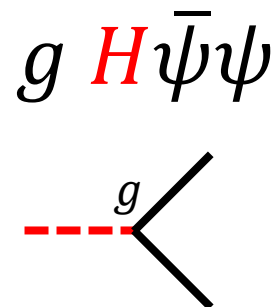
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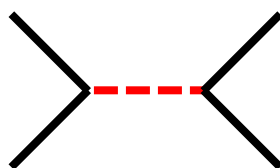
UV  
  
  
  
  
  
  
  
  
  
  
IR

$$\frac{\psi}{\frac{\not{p} + m}{m^2 + p^2}}$$

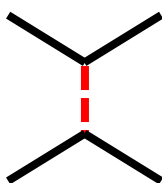
$$\frac{H}{\frac{1}{M^2 + p^2}}$$



$$\frac{\psi}{\frac{\not{p} + m}{m^2 + p^2}}$$



$$\frac{g^2 (s - t)}{M^2 - s} \rightarrow +g^2 \frac{s}{M^2} + \dots$$

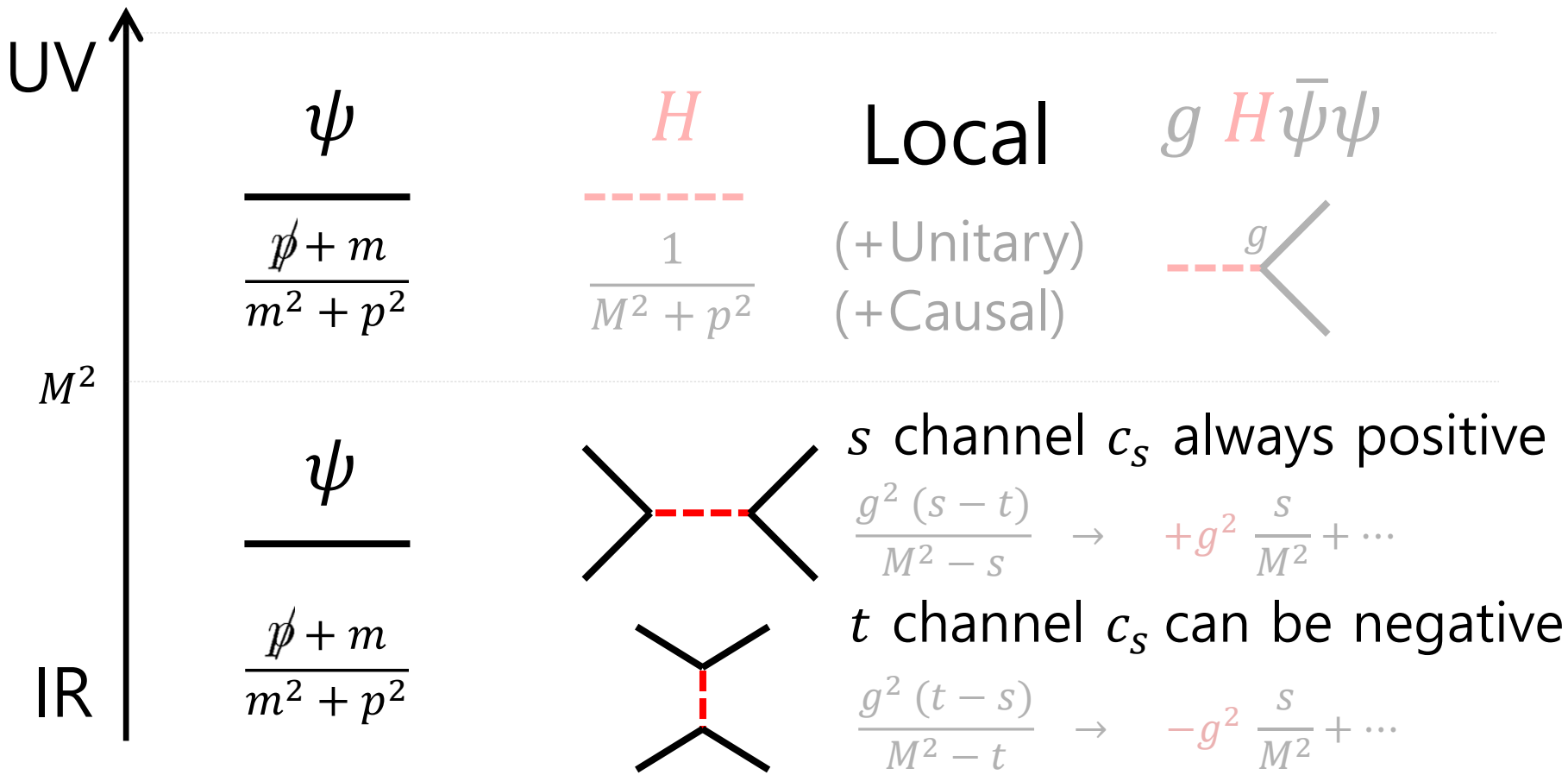


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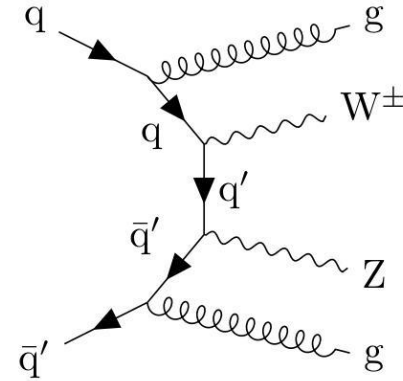
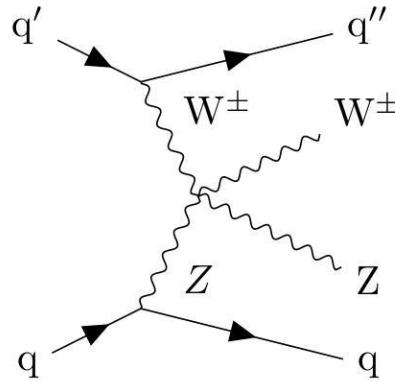
## CMS Collaboration, 1901.04060

Measurement of electroweak WZ boson production and search for new physics in WZ + two jets events in pp collisions at  $\sqrt{s} = 13$  TeV

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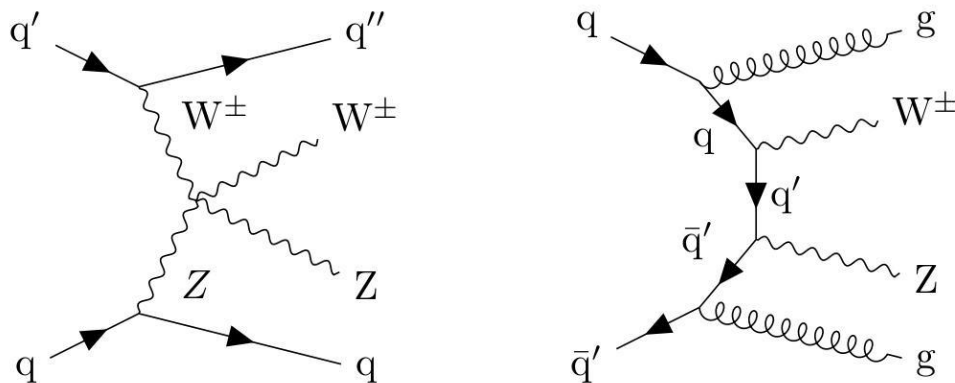
SM:



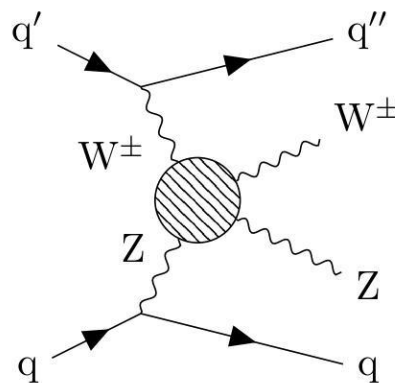
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SM:



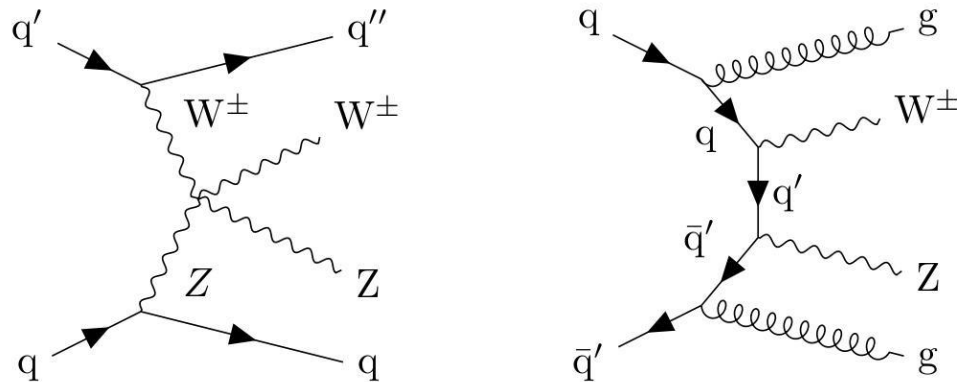
BSM:



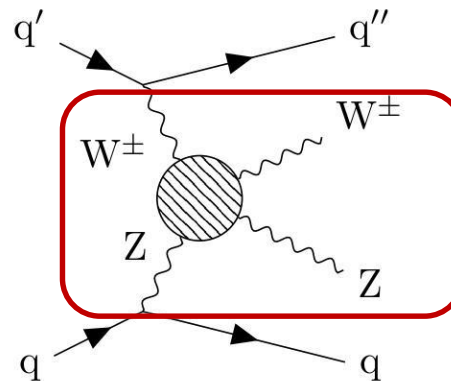
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SM:



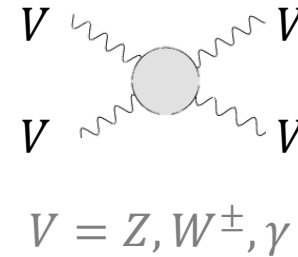
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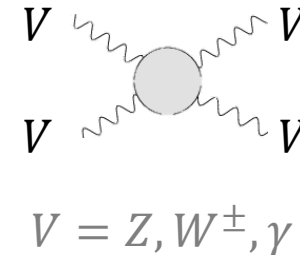
$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{f_i}{\Lambda^4} \mathcal{O}_i$$



CMS Collaboration, 1901.04060

Measurement of electroweak WZ boson production and search for new physics in WZ + two jets events in pp collisions at  $\sqrt{s} = 13$  TeV

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{f_i}{\Lambda^4} \mathcal{O}_i$$



$$f_{S,0} \quad \mathcal{O}_{S,0} = [(D_\mu \Phi)^\dagger D_\nu \Phi] \times [(D^\mu \Phi)^\dagger D^\nu \Phi]$$

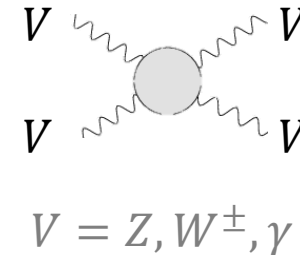
$$f_{S,1} \quad \mathcal{O}_{S,1} = [(D_\mu \Phi)^\dagger D^\mu \Phi] \times [(D_\nu \Phi)^\dagger D^\nu \Phi]$$



CMS Collaboration, 1901.04060

Measurement of electroweak WZ boson production and search for new physics in WZ + two jets events in pp collisions at  $\sqrt{s} = 13$  TeV

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{f_i}{\Lambda^4} O_i$$



$$f_{S,0} \quad O_{S,0} = [(D_\mu \Phi)^\dagger D_\nu \Phi] \times [(D^\mu \Phi)^\dagger D^\nu \Phi]$$

$$f_{S,1} \quad O_{S,1} = [(D_\mu \Phi)^\dagger D^\mu \Phi] \times [(D_\nu \Phi)^\dagger D^\nu \Phi]$$

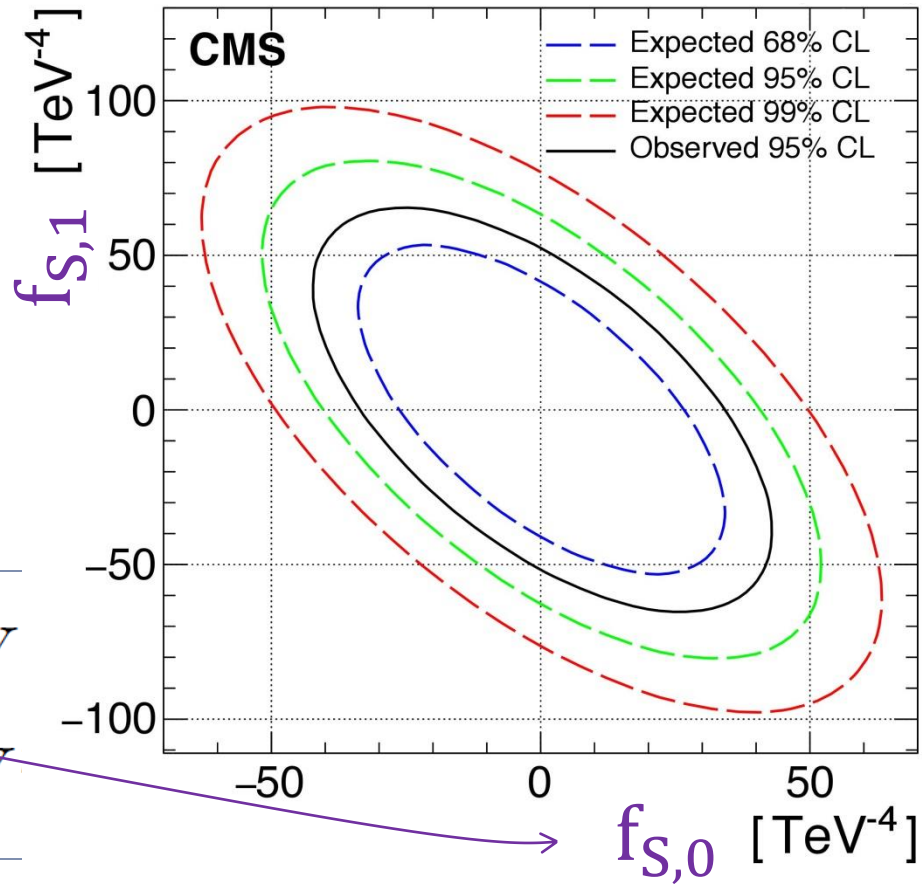
$$f_{M,0} \quad O_{M,0} = \text{Tr} \left[ \hat{W}_{\mu\nu} \hat{W}^{\mu\nu} \right] \times [(D_\beta \Phi)^\dagger D^\beta \Phi]$$

$$f_{M,1} \quad O_{M,1} = \text{Tr} \left[ \hat{W}_{\mu\nu} \hat{W}^{\nu\beta} \right] \times [(D_\beta \Phi)^\dagger D^\mu \Phi]$$



CMS Collaboration, 1901.04060

Measurement of electroweak WZ boson production and search for new physics in WZ + two jets events in pp collisions at  $\sqrt{s} = 13$  TeV



$f_{S,0}$   
 $f_{S,1}$

$$O_{S,0} = [(D_\mu \Phi)^\dagger D_\nu \Phi]$$

$$O_{S,1} = [(D_\mu \Phi)^\dagger D_\nu \Phi]$$

$f_{M,0}$   
 $f_{M,1}$

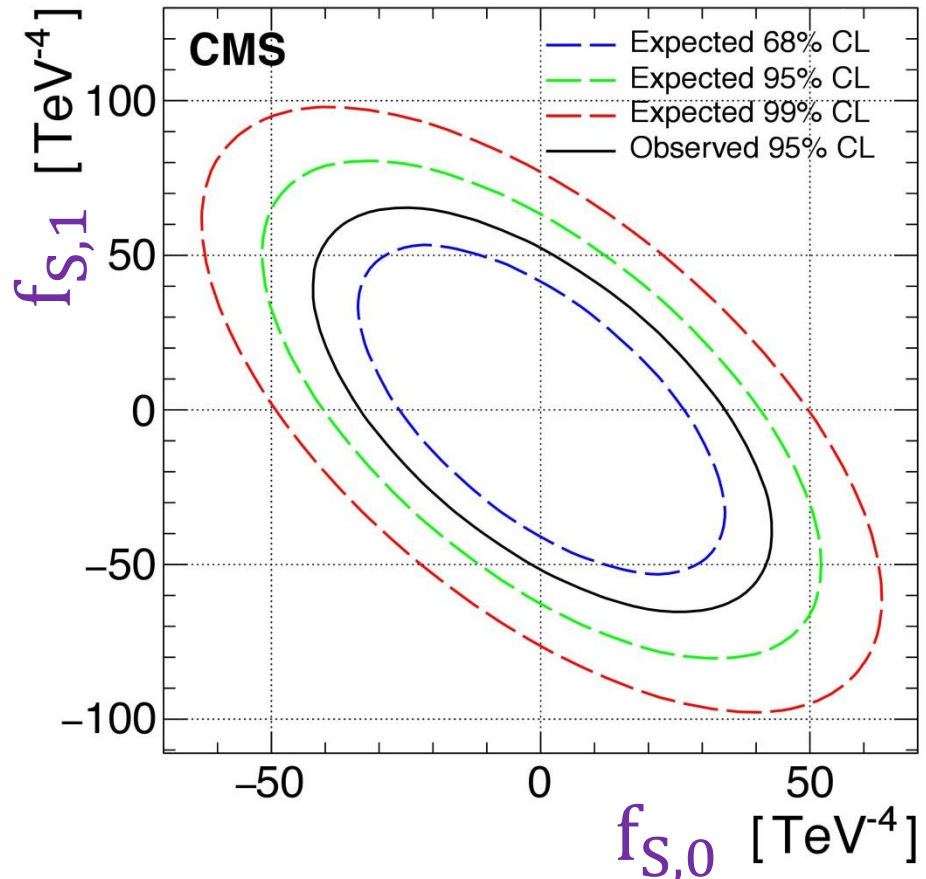
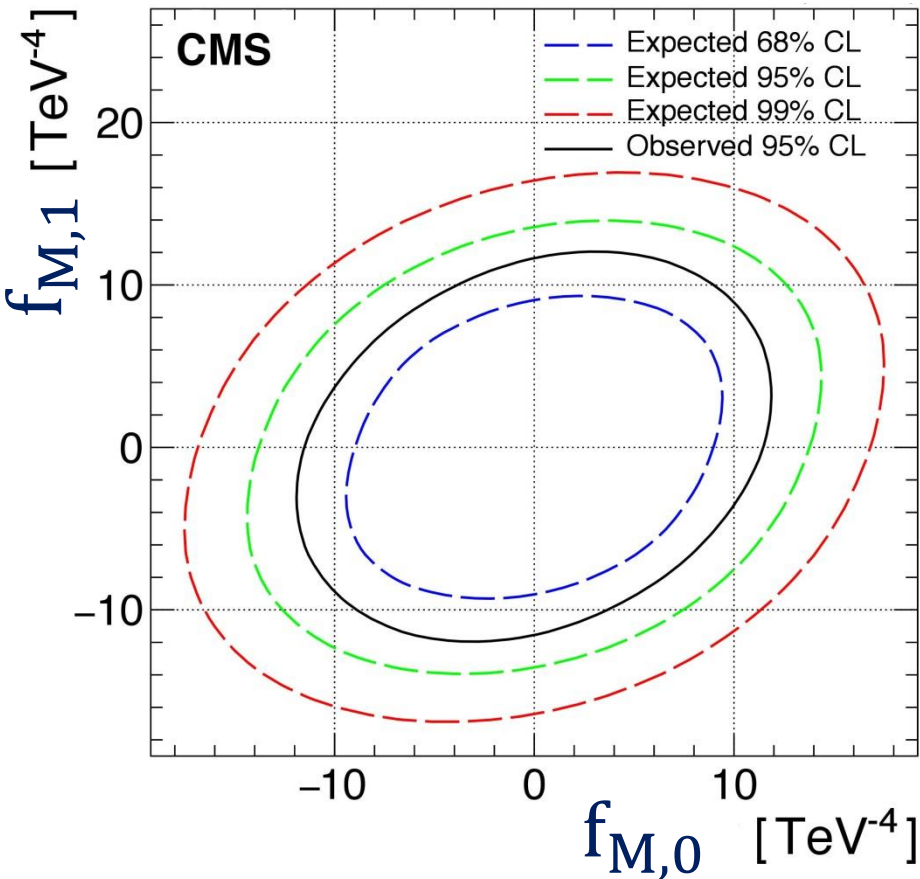
$$O_{M,0} = \text{Tr} [\hat{W}_{\mu\nu} \hat{W}^{\mu\nu}]$$

$$O_{M,1} = \text{Tr} [\hat{W}_{\mu\nu} \hat{W}^{\mu\nu}]$$

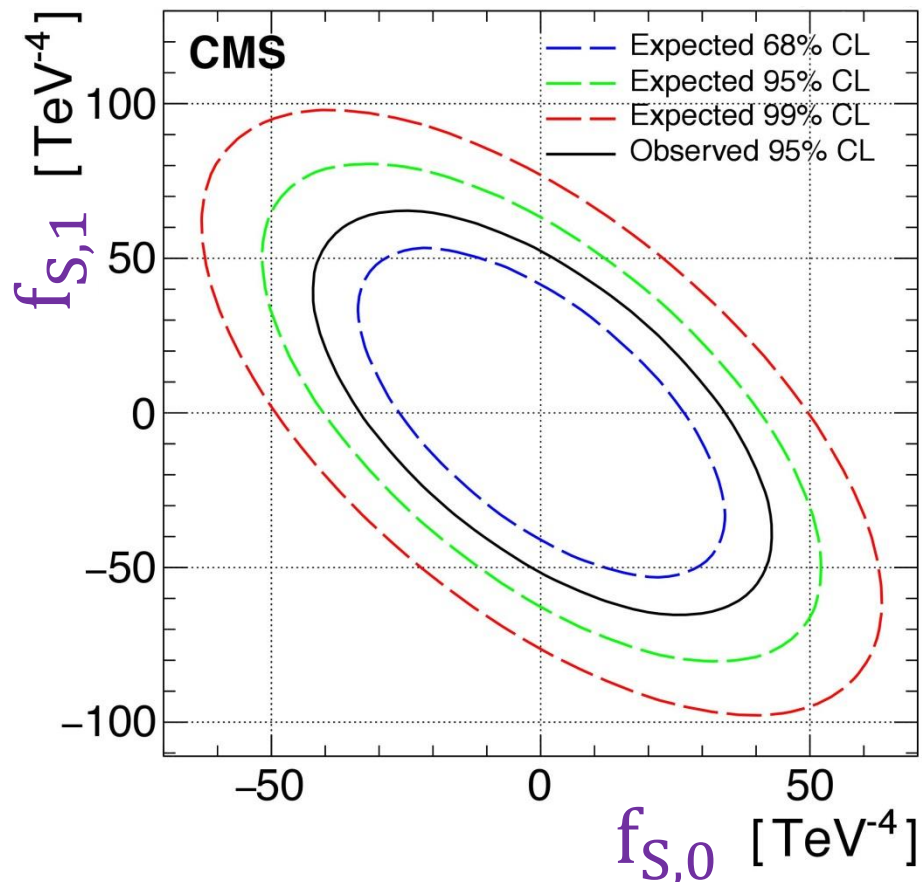
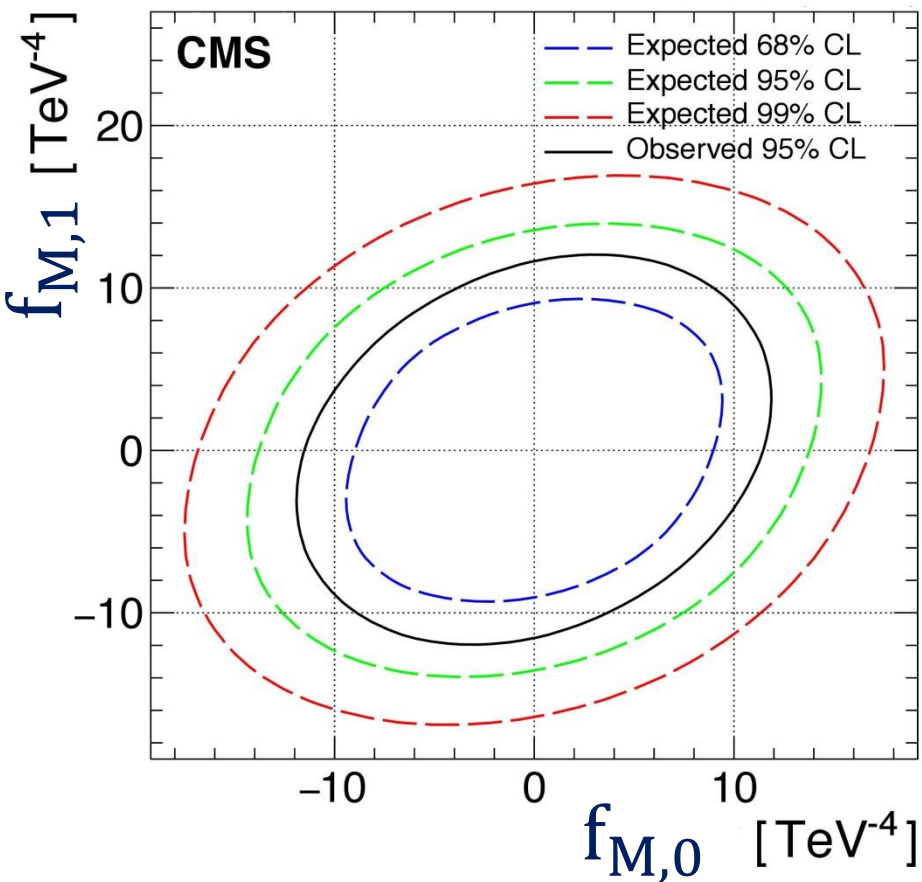


CMS Collaboration, 1901.04060

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New physics **non-local** if:



[Zhang, Zhou, 1808.00010]

[Bi et al, 1902.08977]

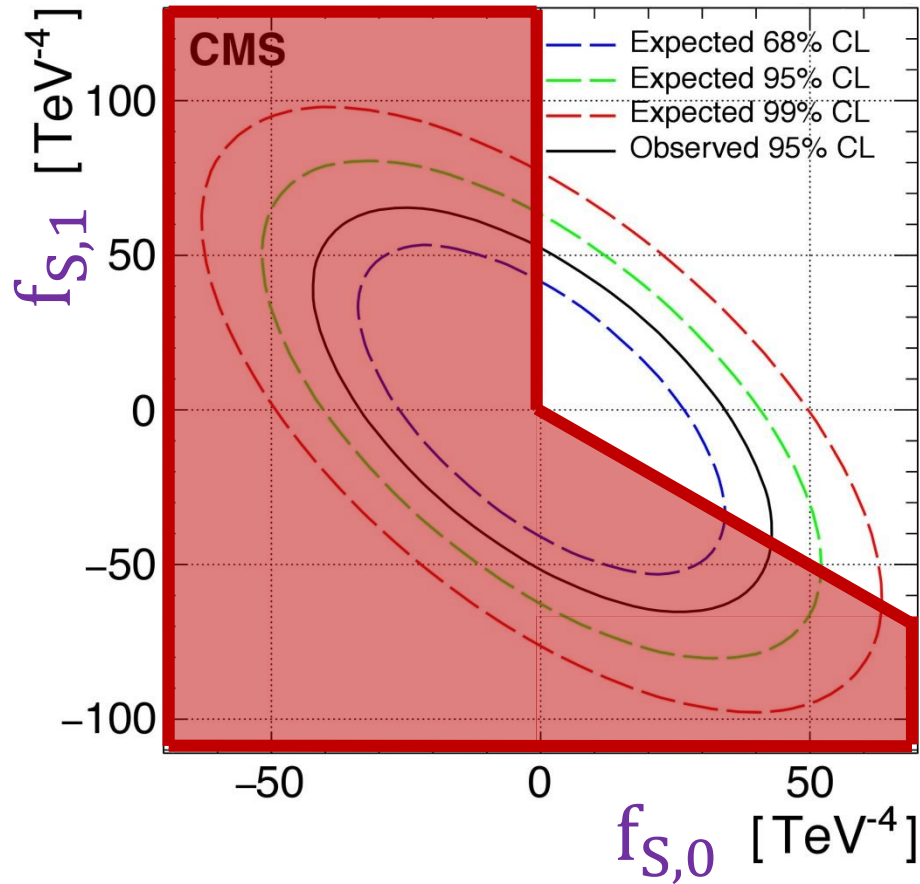
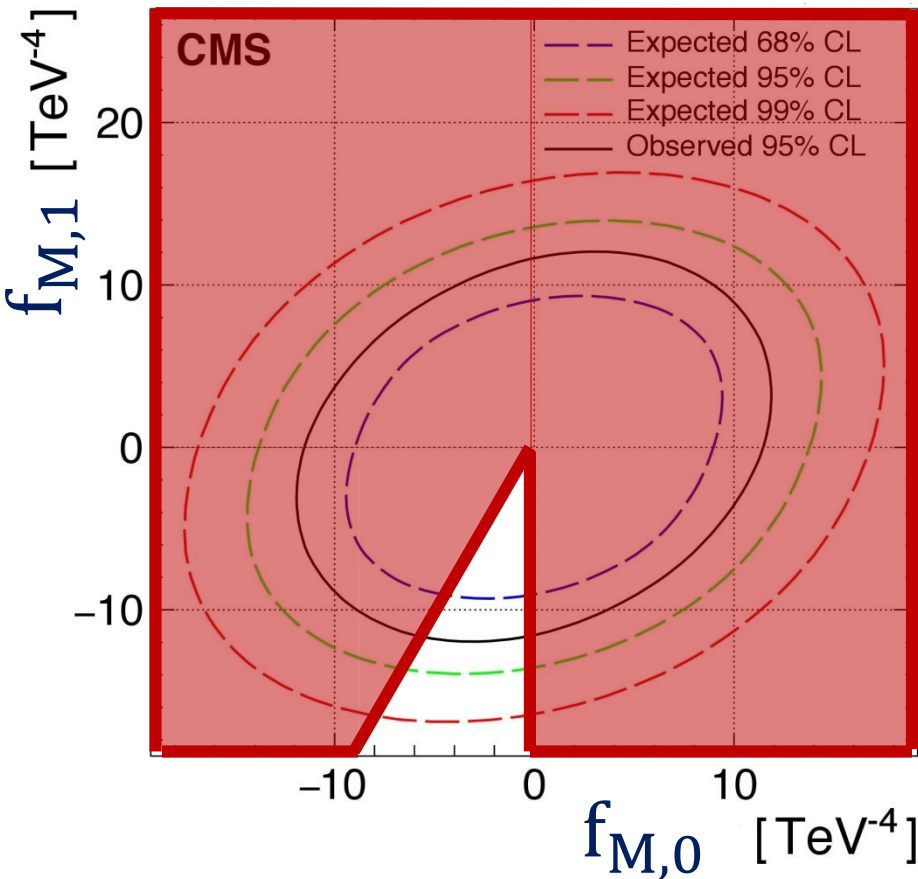
New physics **non-local** if:

$$-f_{M,0} < 0$$

$$2f_{M,0} - f_{M,1} < 0$$

$$f_{S,0} < 0$$

$$f_{S,0} + f_{S,1} < 0$$





# *Physics*



Buttazzo et al, 1706.07808

*B*-physics anomalies: a guide to combined explanations

Buttazzo et al, 1706.07808

*B*-physics anomalies: a guide to combined explanations

$$\begin{aligned}
\mathcal{L}_{\text{EFT}} = & \mathcal{L}_{\text{SM}} \\
& - \frac{1}{v^2} \lambda_{ij}^q \lambda_{\alpha\beta}^\ell \left[ C_T (\bar{Q}_L^i \gamma_\mu \sigma^a Q_L^j) (\bar{L}_L^\alpha \gamma^\mu \sigma^a L_L^\beta) \right. \\
& \left. + C_S (\bar{Q}_L^i \gamma_\mu Q_L^j) (\bar{L}_L^\alpha \gamma^\mu L_L^\beta) \right]
\end{aligned}$$



Buttazzo et al, 1706.07808

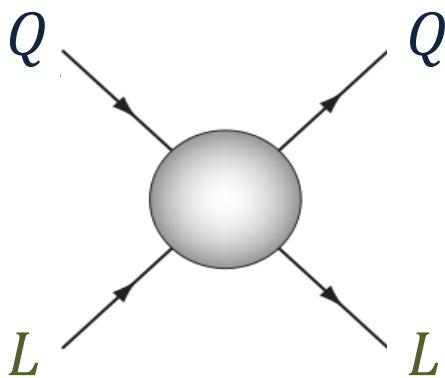
*B*-physics anomalies: a guide to combined explanations

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} - \frac{1}{v^2} \lambda_{ij}^q \lambda_{\alpha\beta}^\ell \left[ \underline{C_T} (\bar{Q}_L^i \gamma_\mu \sigma^a Q_L^j) (\bar{L}_L^\alpha \gamma^\mu \sigma^a L_L^\beta) + \underline{C_S} (\bar{Q}_L^i \gamma_\mu Q_L^j) (\bar{L}_L^\alpha \gamma^\mu L_L^\beta) \right]$$

Buttazzo et al, 1706.07808

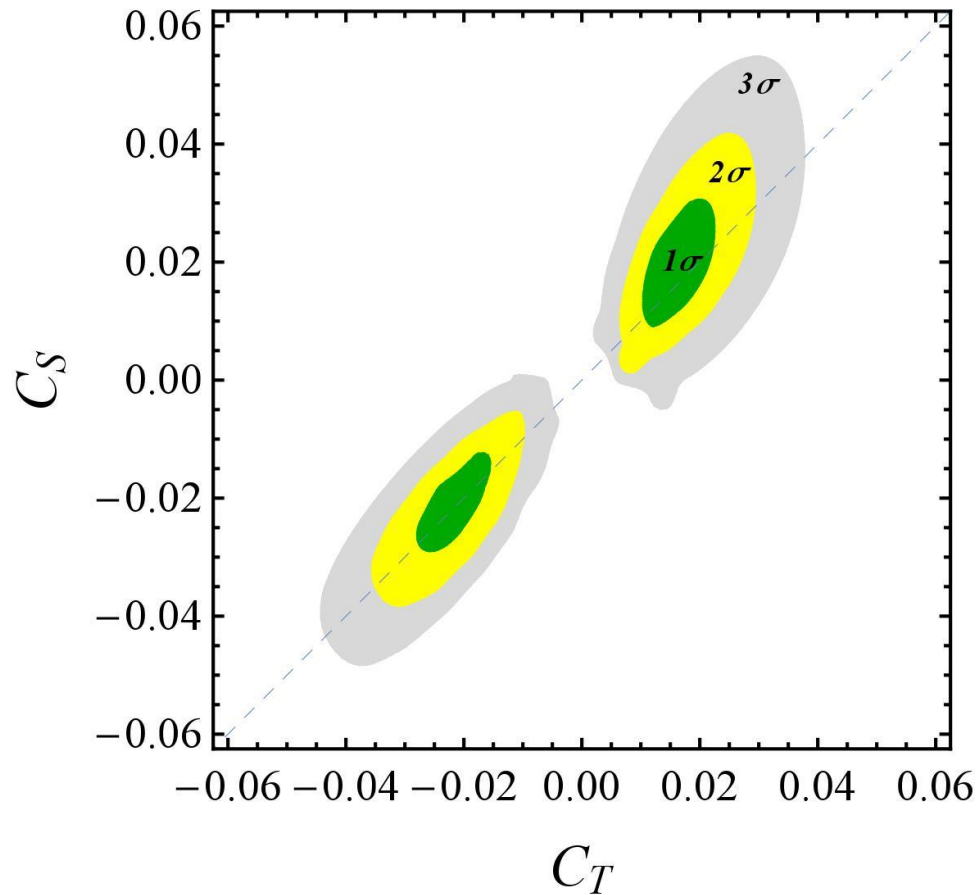
*B*-physics anomalies: a guide to combined explanations

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} - \frac{1}{v^2} \lambda_{ij}^q \lambda_{\alpha\beta}^\ell \left[ \underline{C_T} (\bar{Q}_L^i \gamma_\mu \sigma^a Q_L^j) (\bar{L}_L^\alpha \gamma^\mu \sigma^a L_L^\beta) + \underline{C_S} (\bar{Q}_L^i \gamma_\mu Q_L^j) (\bar{L}_L^\alpha \gamma^\mu L_L^\beta) \right]$$



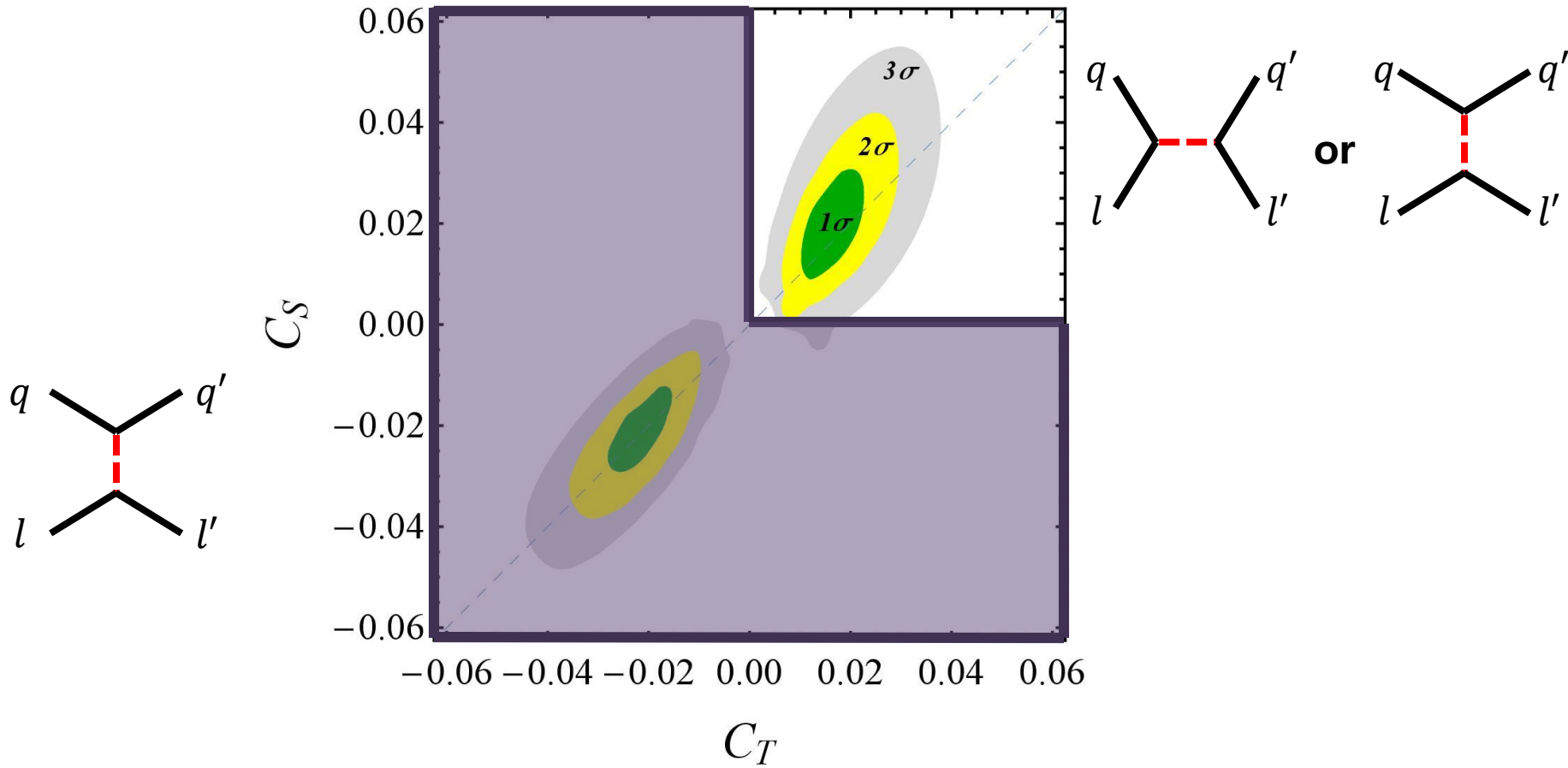
$$A_{\text{EFT}}(s) \sim \mathbf{C_S} s$$

Buttazzo et al, 1706.07808

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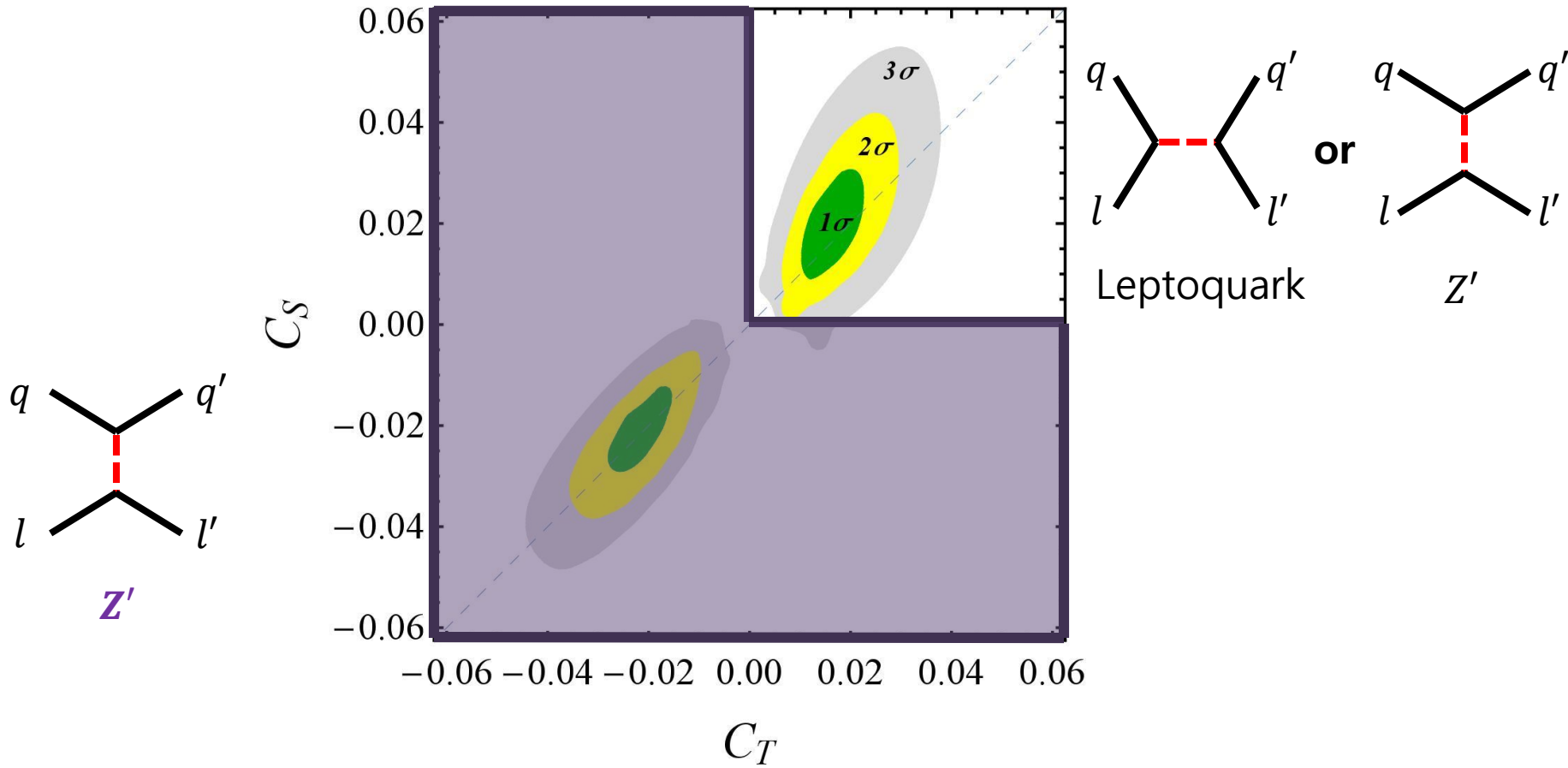
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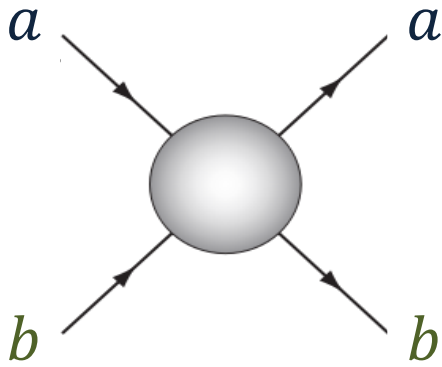


Buttazzo et al, 1706.07808

*B*-physics anomalies: a guide to combined explanations





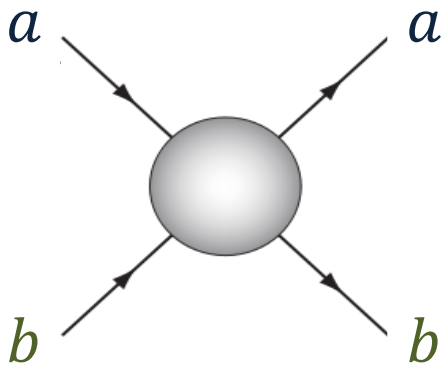


$$A_{EFT}(s) = c_0 + c_s \frac{s}{M^2} + c_{ss} \frac{s^2}{M^4} + \dots$$

$c_s < 0 \Rightarrow$  New physics in  $t$  channel

$c_{ss} < 0 \Rightarrow$  New physics is non-local

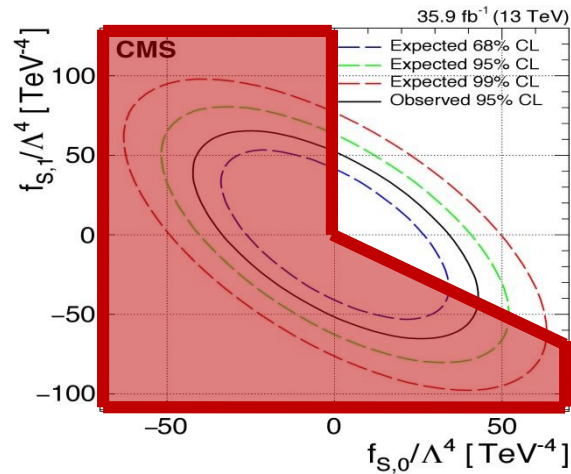
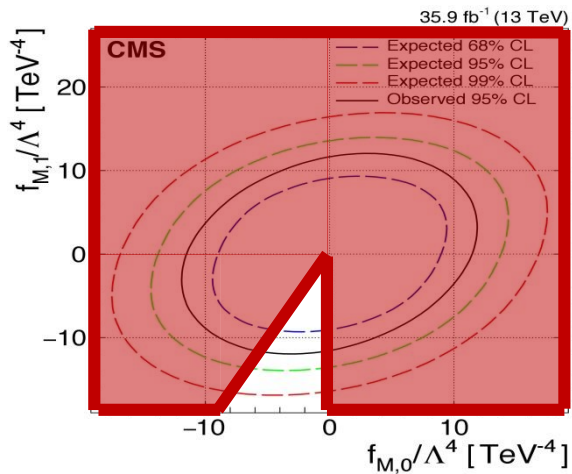




$$A_{EFT}(s) = c_0 + c_s \frac{s}{M^2} + c_{ss} \frac{s^2}{M^4} + \dots$$

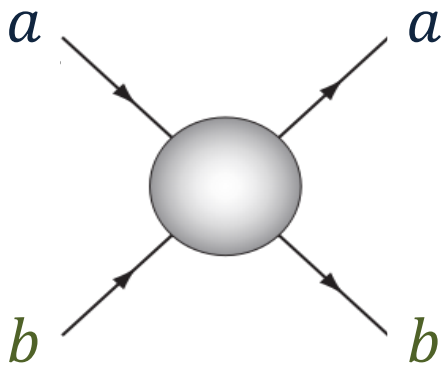
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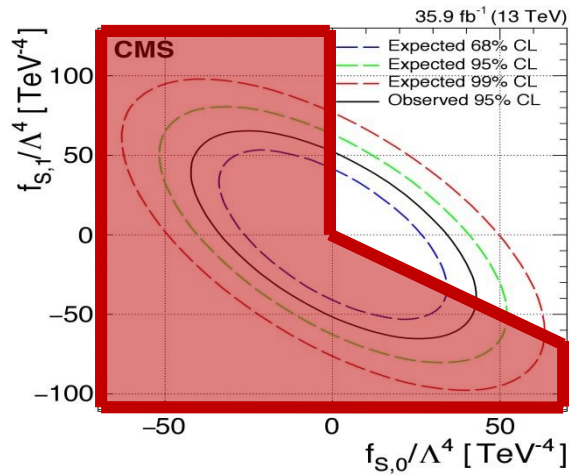
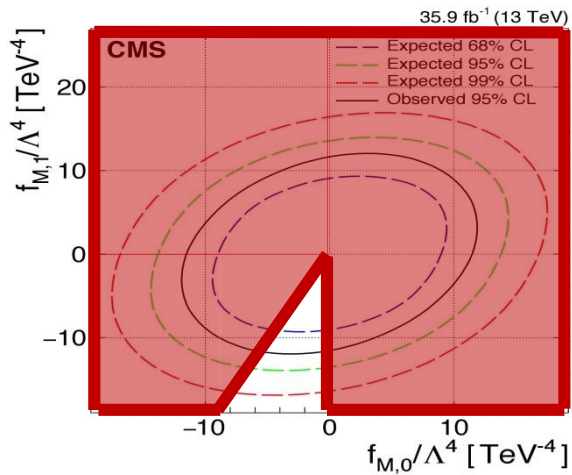
## Vector Boson Scattering



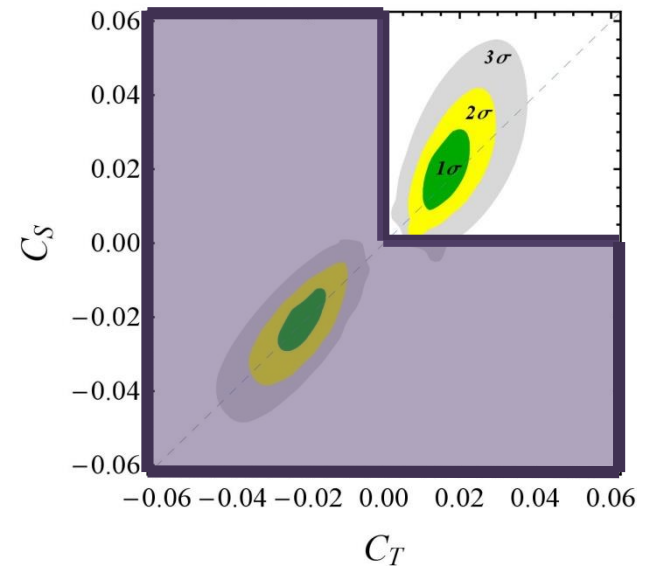


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Vector Boson Scattering



B-physics

# Backup Slides



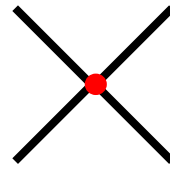
Buttazzo et al, 1706.07808

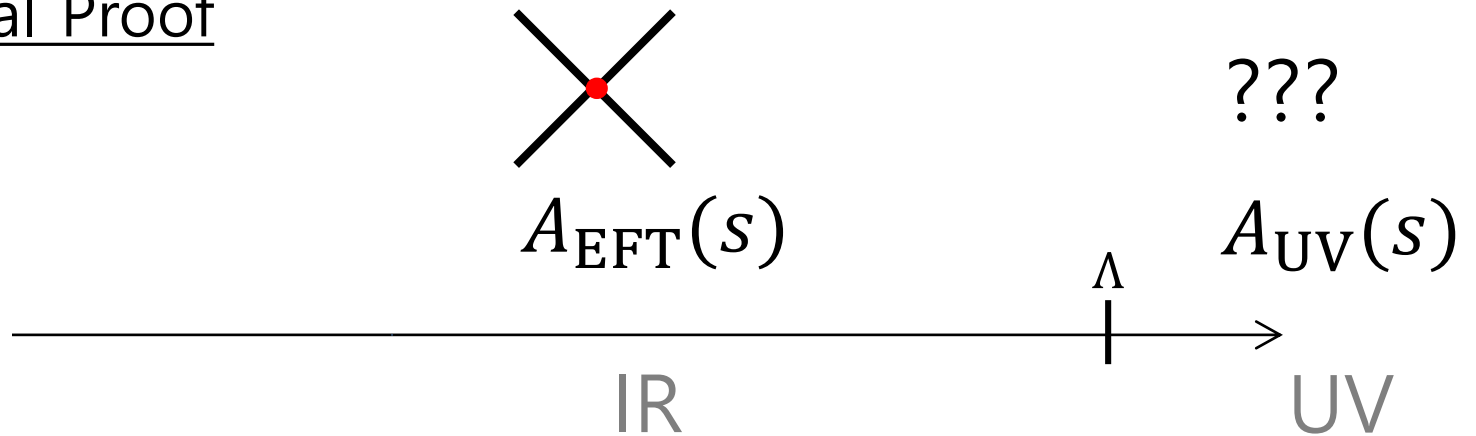
B-physics anomalies: a guide to combined explanations

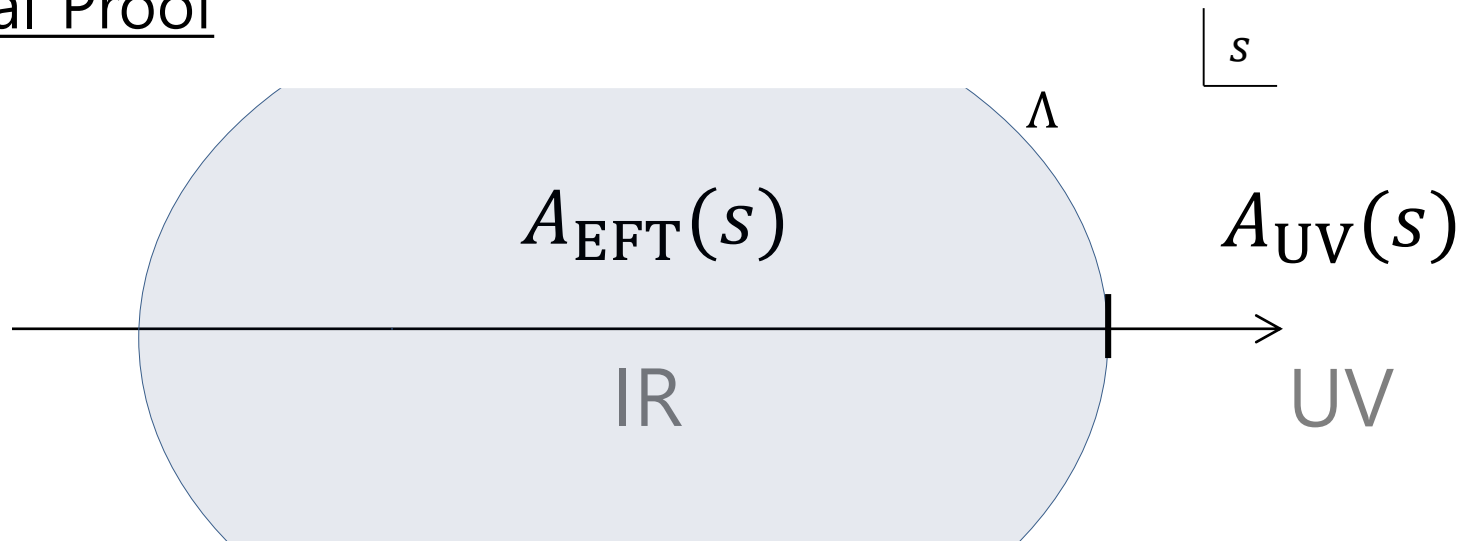
Observable	Experimental bound	Linearised expression
$R_{D^{(*)}}^{\tau\ell}$	$1.237 \pm 0.053$	$1 + 2C_T(1 - \lambda_{sb}^q V_{tb}^*/V_{ts}^*)(1 - \lambda_{\mu\mu}^\ell/2)$
$\Delta C_9^\mu = -\Delta C_{10}^\mu$	$-0.61 \pm 0.12$ [36]	$-\frac{\pi}{\alpha_{\text{em}} V_{tb} V_{ts}^*} \lambda_{\mu\mu}^\ell \lambda_{sb}^q (C_T + C_S)$
$R_{b \rightarrow c}^{\mu e} - 1$	$0.00 \pm 0.02$	$2C_T(1 - \lambda_{sb}^q V_{tb}^*/V_{ts}^*) \lambda_{\mu\mu}^\ell$
$B_{K^{(*)}\nu\bar{\nu}}$	$0.0 \pm 2.6$	$1 + \frac{2}{3} \frac{\pi}{\alpha_{\text{em}} V_{tb} V_{ts}^* C_\nu^{\text{SM}}} (C_T - C_S) \lambda_{sb}^q (1 + \lambda_{\mu\mu}^\ell)$
$\delta g_{\tau L}^Z$	$-0.0002 \pm 0.0006$	$0.033C_T - 0.043C_S$
$\delta g_{\nu\tau}^Z$	$-0.0040 \pm 0.0021$	$-0.033C_T - 0.043C_S$
$ g_\tau^W/g_\ell^W $	$1.00097 \pm 0.00098$	$1 - 0.084C_T$
$\mathcal{B}(\tau \rightarrow 3\mu)$	$(0.0 \pm 0.6) \times 10^{-8}$	$2.5 \times 10^{-4} (C_S - C_T)^2 (\lambda_{\tau\mu}^\ell)^2$

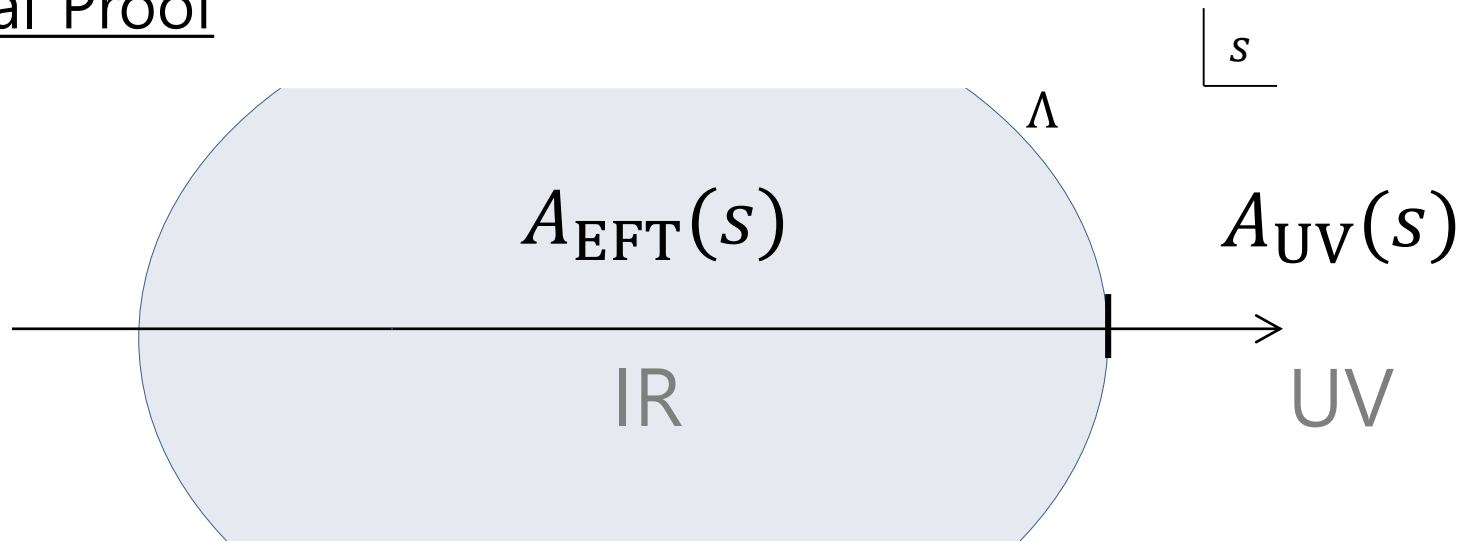
## General Proof



General Proof $A_{\text{EFT}}(s)$ 

General Proof

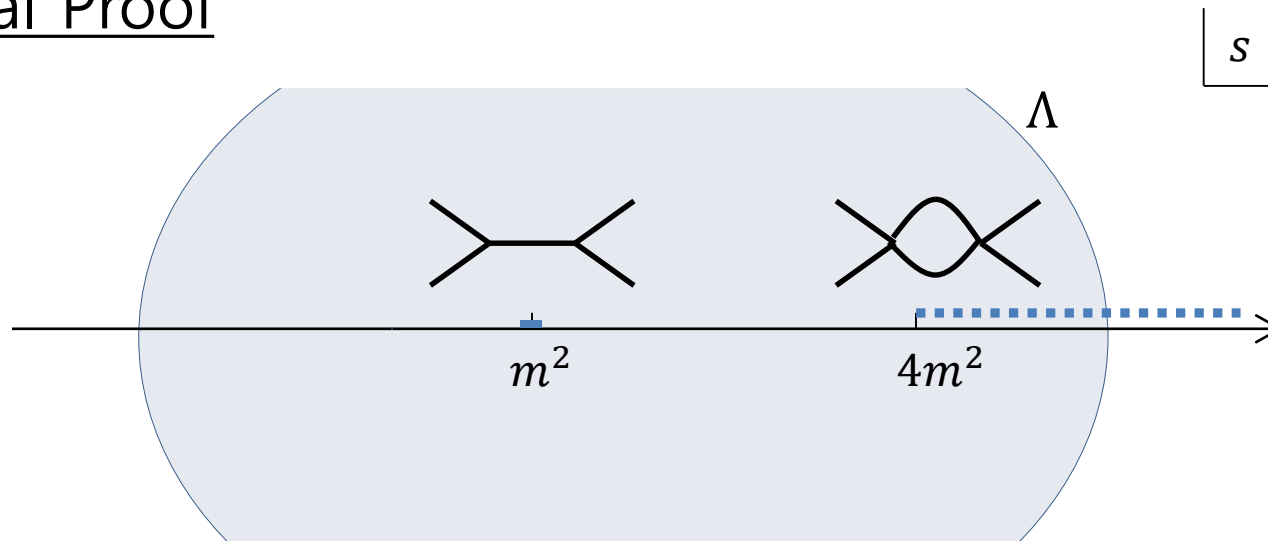
General Proof

General Proof

## Causality

$\Rightarrow A(s)$  is analytic (up to known poles & branch cuts)

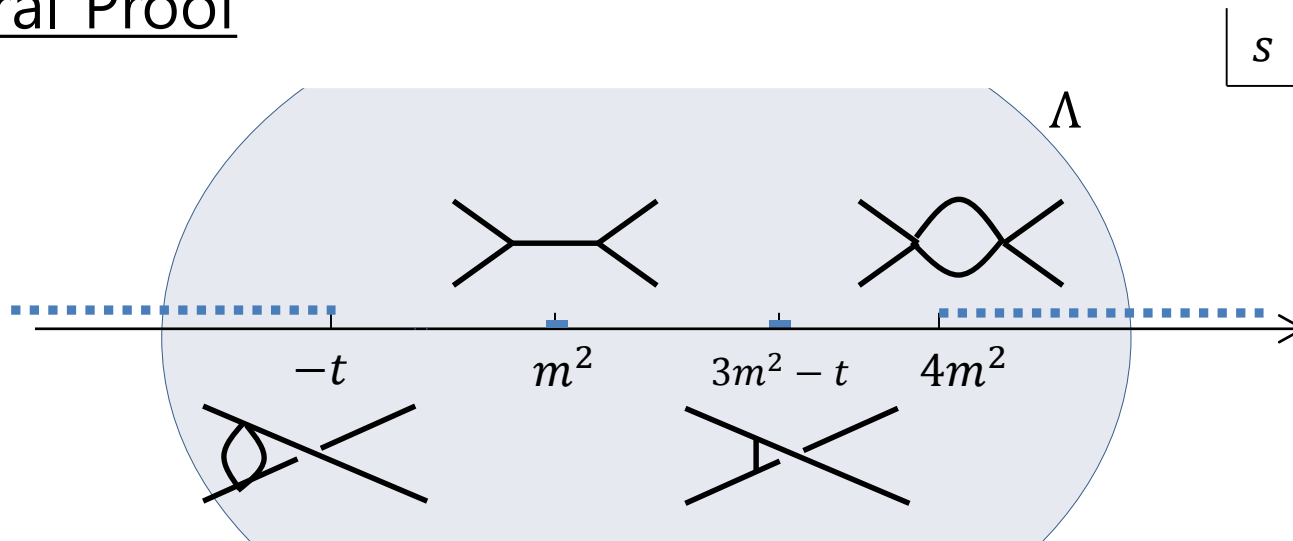


General Proof

## Causality

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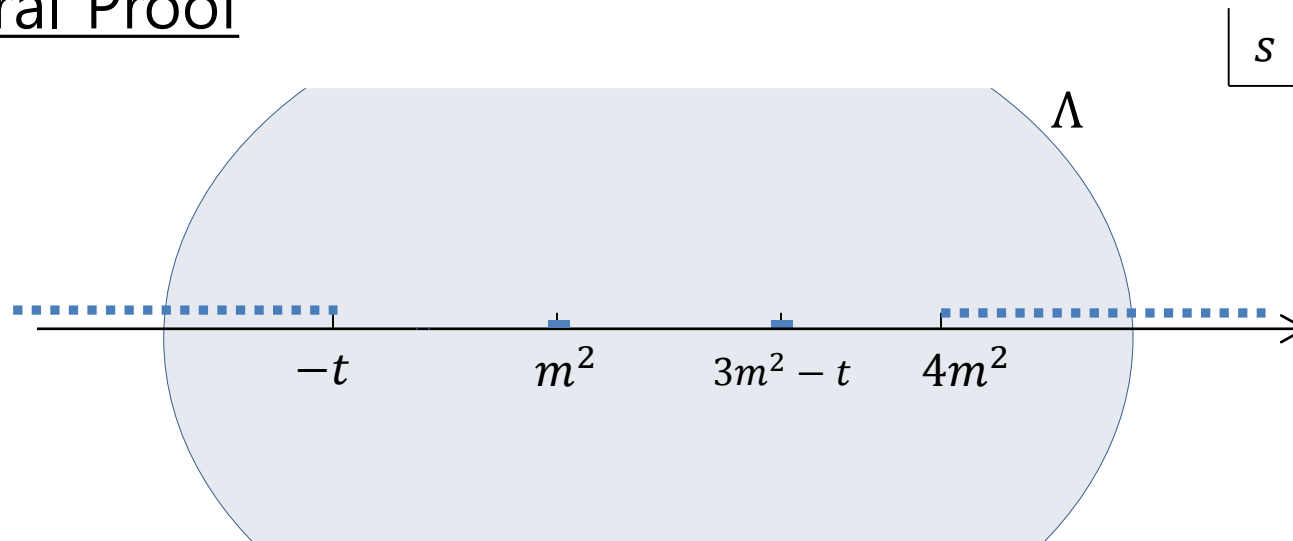
# General Proof



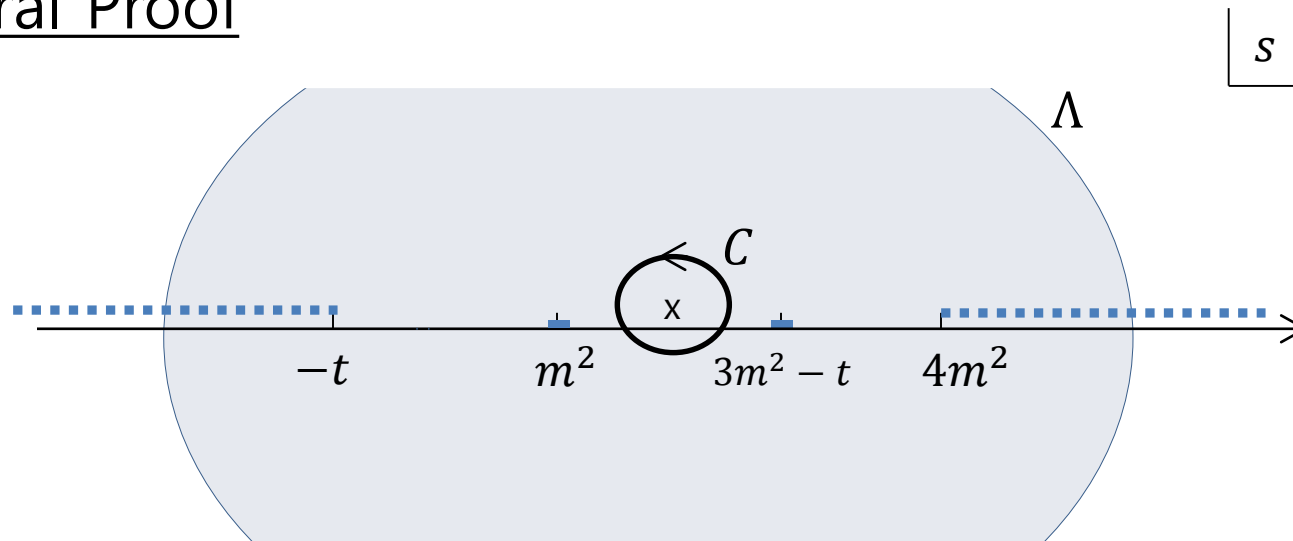
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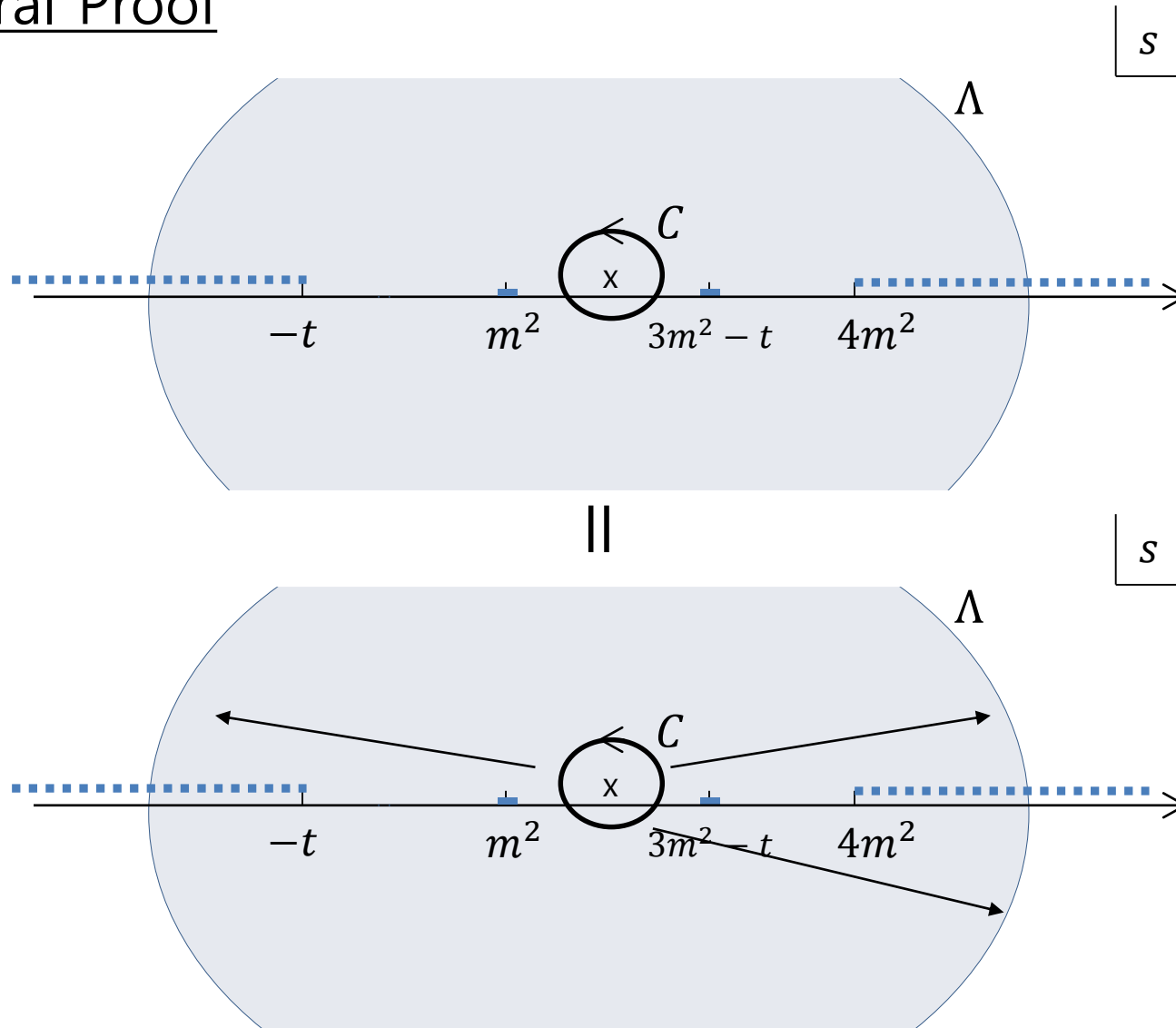
## General Proof



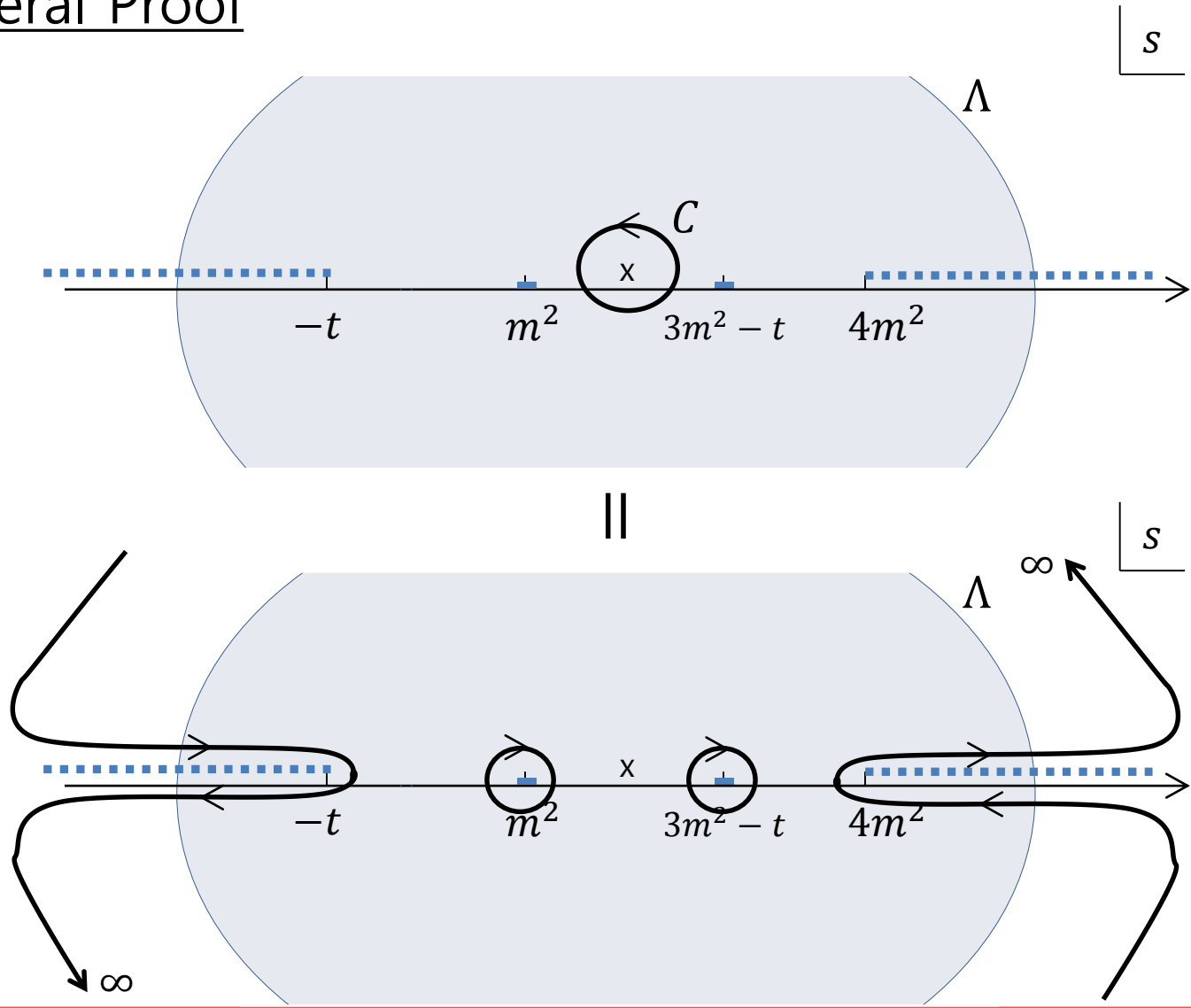
## General Proof



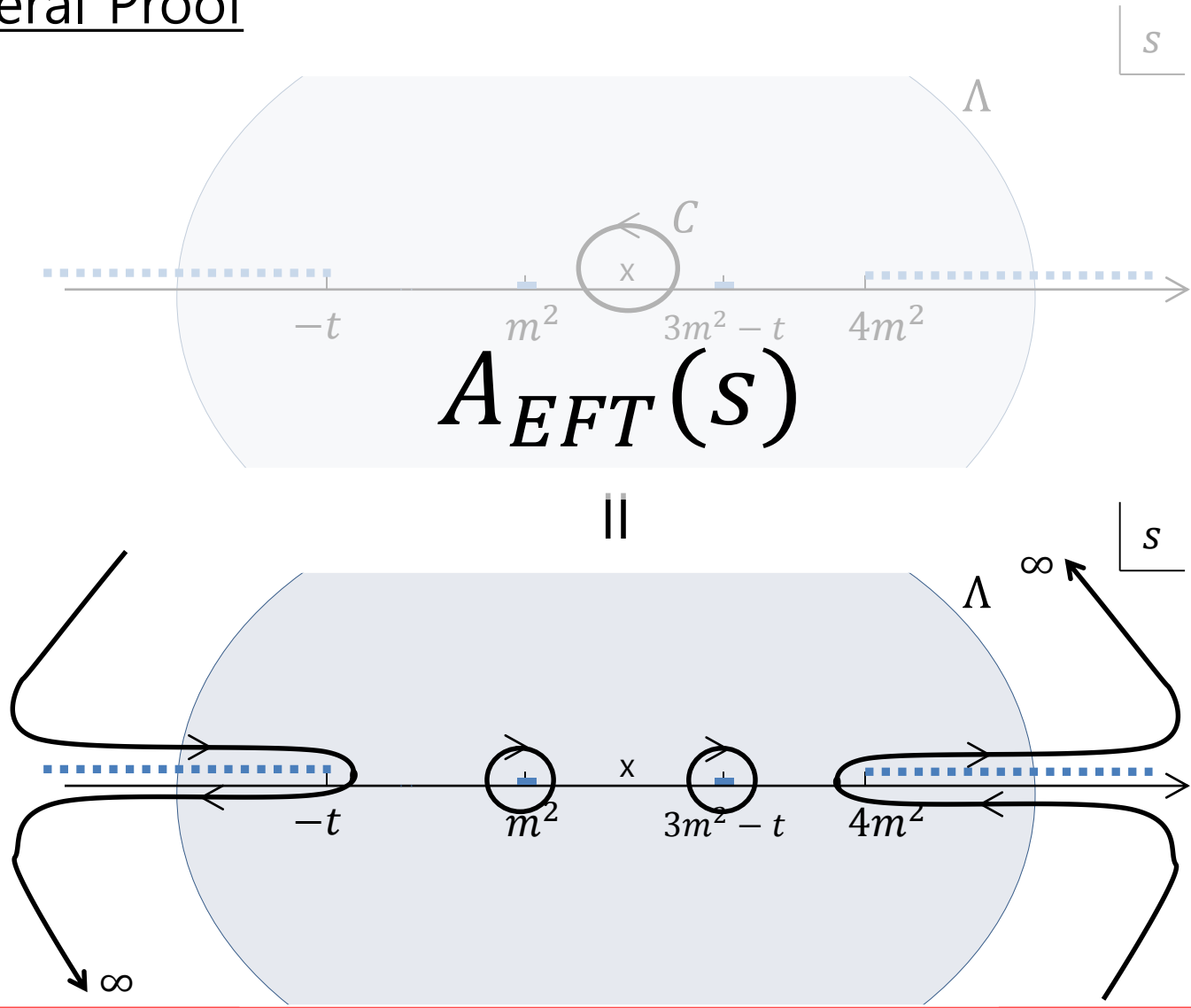
# General Proof



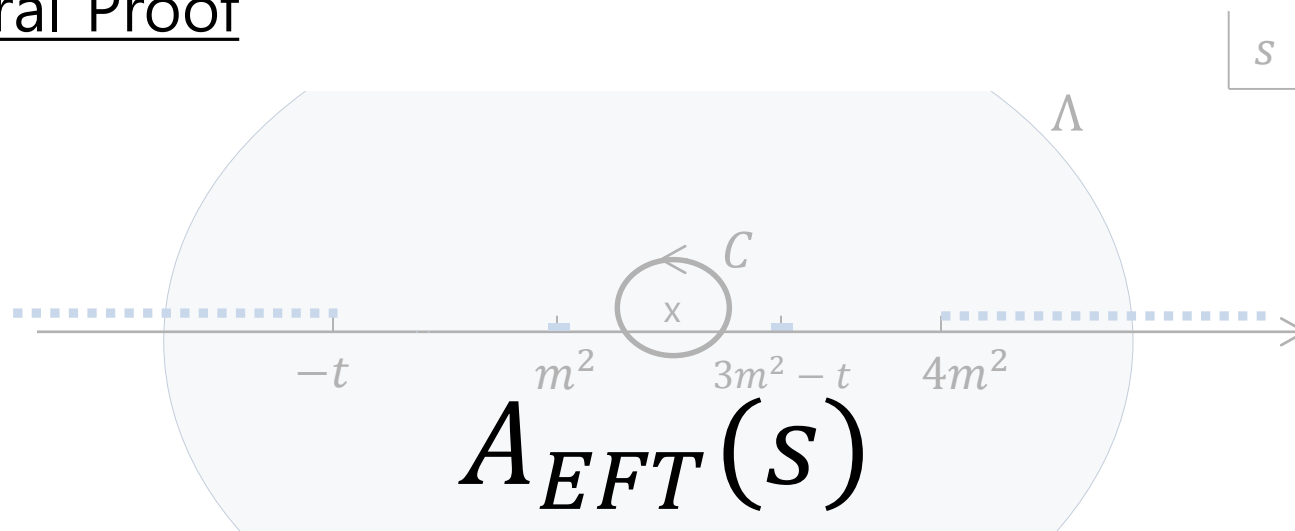
# General Proof



# General Proof

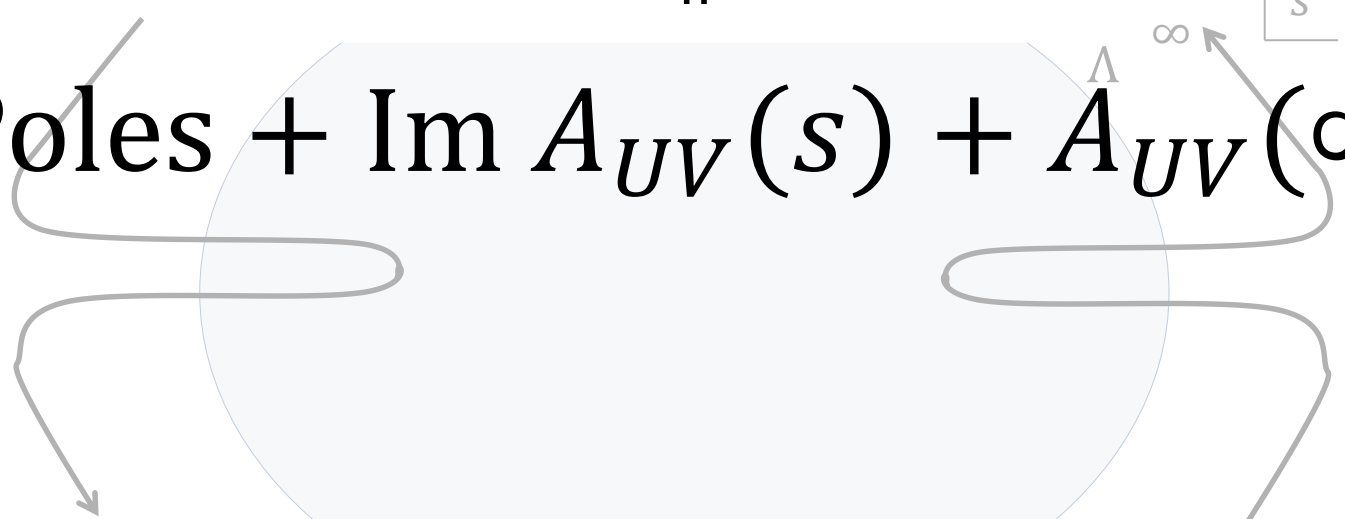


General Proof



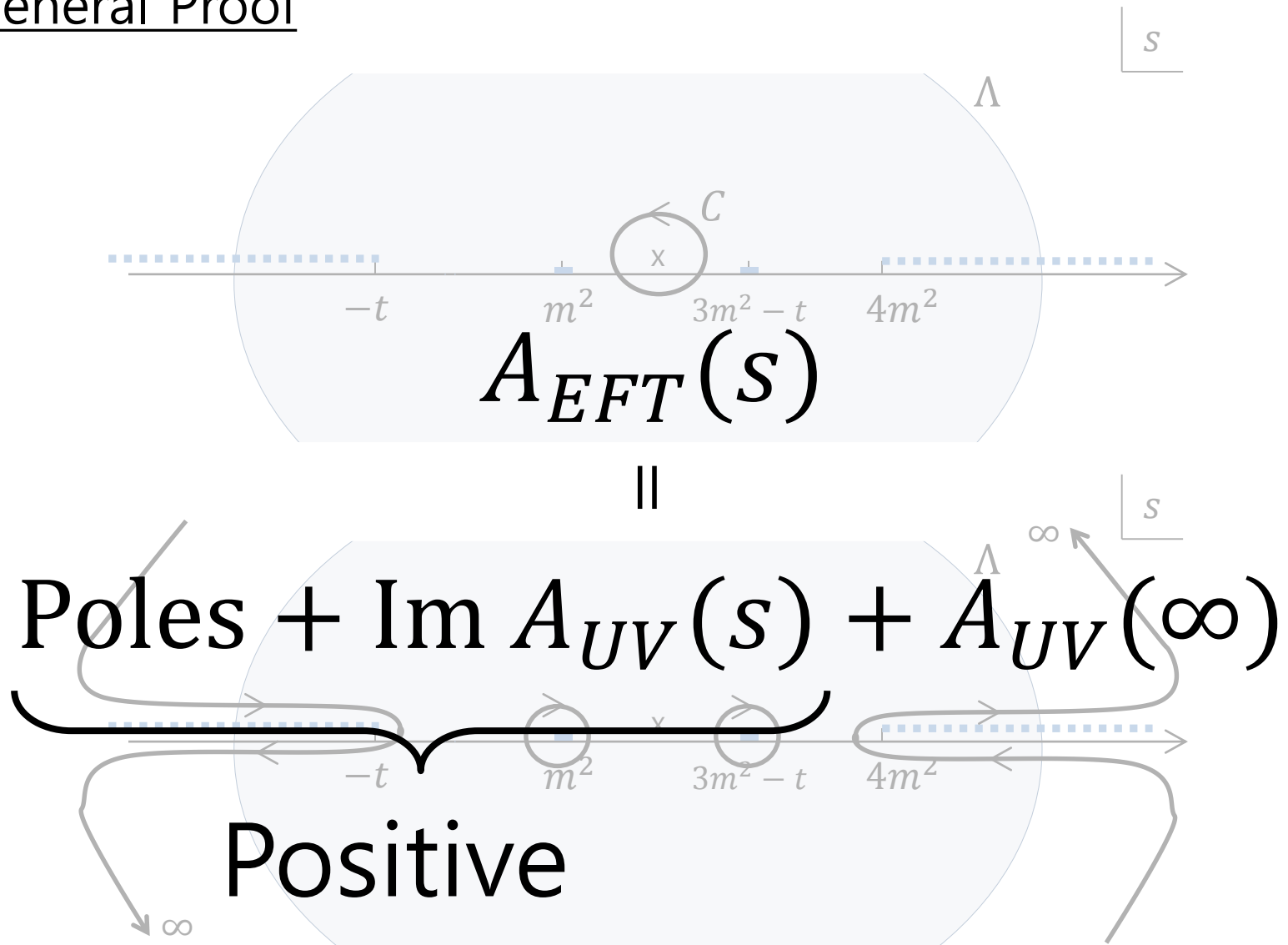
||

Poles +  $\text{Im } A_{UV}(s) + \hat{A}_{UV}(\infty)$





General Proof



General Proof

