

Determination of hadronic resonance
contributions to the $B^0 \rightarrow K^{*0} \mu^+ \mu^-$
transition

Malte Hecker, on behalf of the LHCb collaboration

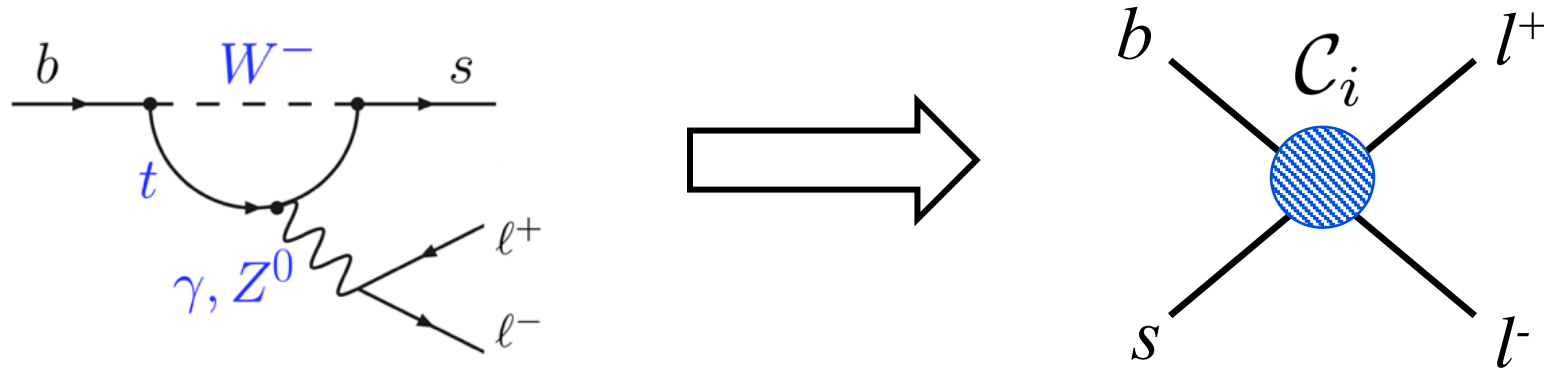
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Effective field theory

- $b \rightarrow sll$ processes can be described with effective Hamiltonian:

$$\mathcal{H}_{eff} = \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i C_i \mathcal{O}_i$$

- Particles heavier than B-meson are absorbed into Wilson Coefficients

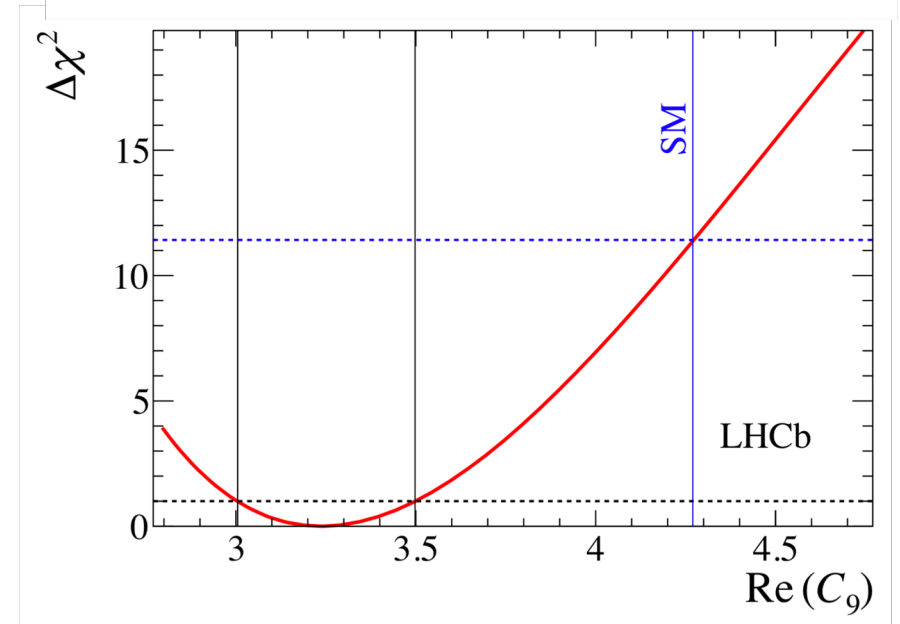
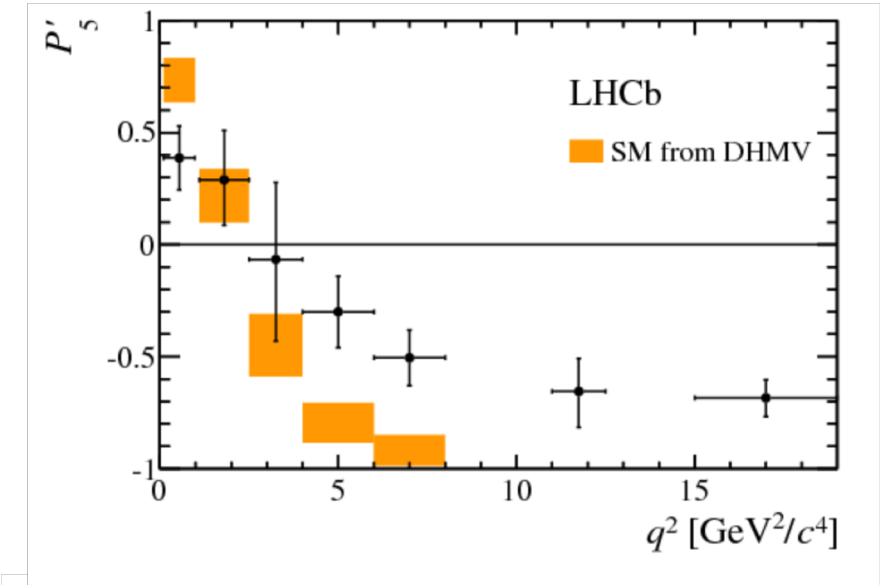


- $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ sensitive to:
 - C_7 – photon coupling
 - C_9 – vector coupling
 - C_{10} – axial vector coupling

- NP can modify the values of Wilson Coefficients: $C_i^{NP} = C_i - C_i^{SM}$

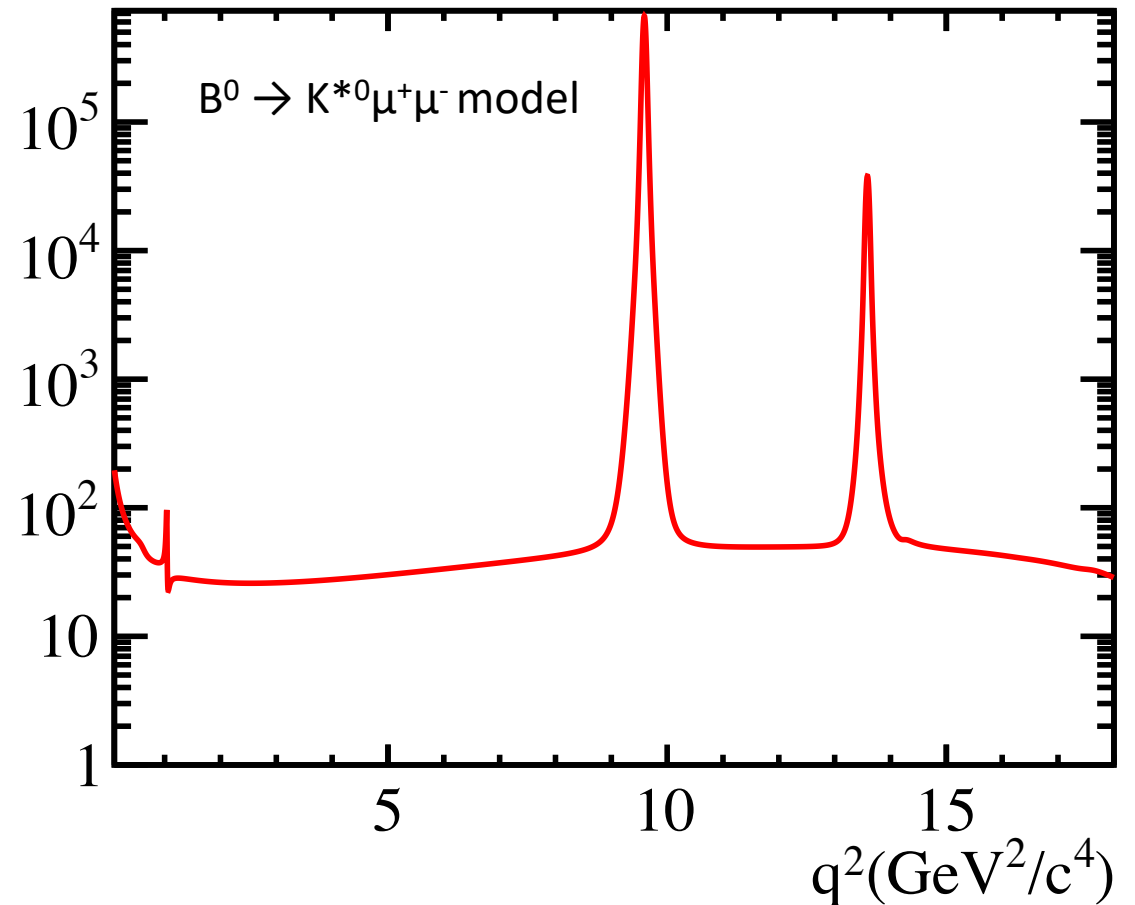
Angular analysis of the $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ decay

- Decay fully described by 3 helicity angles and squared inv. mass of muon pair (q^2)
- Angular distributions depend on Wilson coefficients
→ Can be influenced by NP
- Measurement of angular observables (e.g. P'_5) in bins of q^2 show deviation from SM at level of 3.4 standard deviations
- *“These differences could be explained by an unexpectedly large hadronic effect that changes the SM predictions.”*



Hadronic contributions

- Several decays involving *vector resonances* (e.g. $B^0 \rightarrow J/\Psi(\rightarrow \mu^+\mu^-)K^{*0}$) give same final state as $B^0 \rightarrow K^{*0}\mu^+\mu^-$
 - Interference of these $b \rightarrow sq\bar{q}(\rightarrow l^+l^-)$ processes with the $b \rightarrow sl^+l^-$ FCNC can mimic NP effect on C_9
 - Ongoing discussion whether the amount of interference under good control in the SM calculations
- Perform measurement of the interference by fitting for both penguin and resonant amplitudes



The model

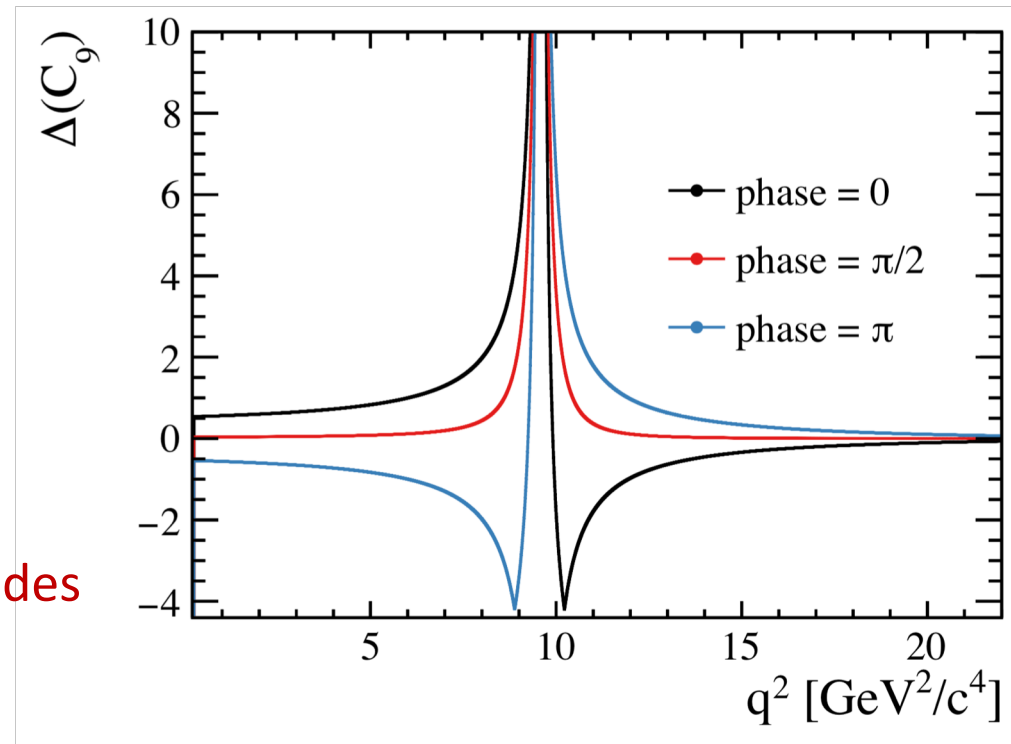
$$\frac{d^4\Gamma[B^0 \rightarrow K^{*0} \mu^+ \mu^-]}{dq^2 d\vec{\Omega}} = \frac{9}{32\pi} \sum_i \underbrace{J_i(q^2)}_{\text{angular coefficients}} \underbrace{f_i(\cos \theta_l, \cos \theta_K, \phi)}_{\text{angular terms}}$$

- $J_i(q^2)$ are bilinear combinations of decay amplitudes (depend on Wilson Coefficients and Form Factors)
- Fitting directly for amplitude parameters while including empirical model for resonance contributions:

$$C_{9,\lambda}^{\text{eff}}(q^2) = C_9 + \sum_j \underbrace{\|n_j\|}_{\text{Magnitude}} \underbrace{e^{i\delta_j}}_{\text{phase}} \underbrace{\text{BW}_j(q^2)}_{\text{BW Amplitudes}}$$

Magnitude and phase for each resonance relative to the penguin

BW Amplitudes

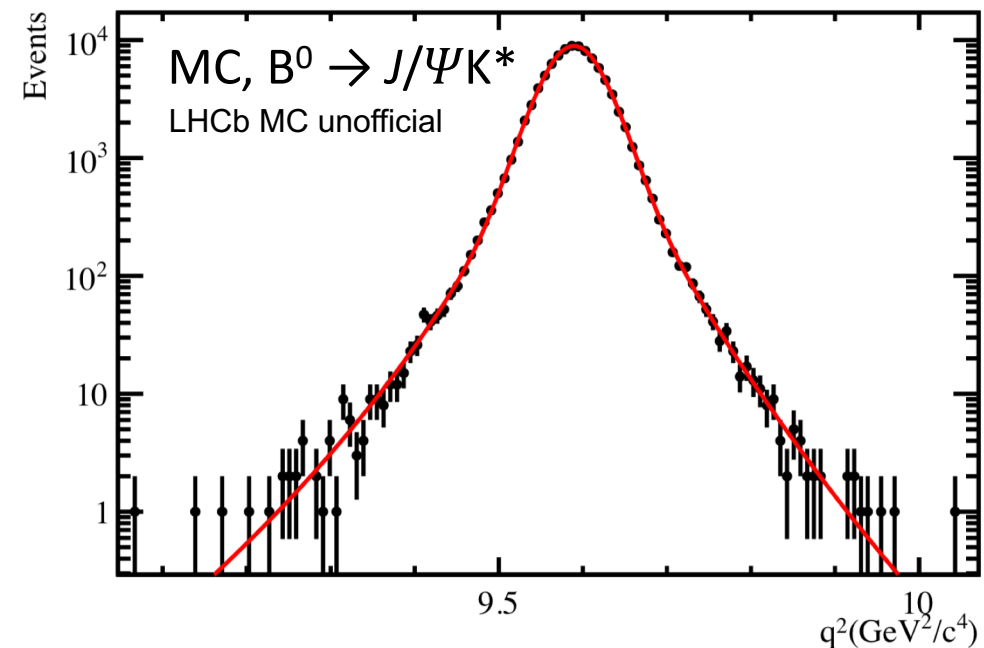
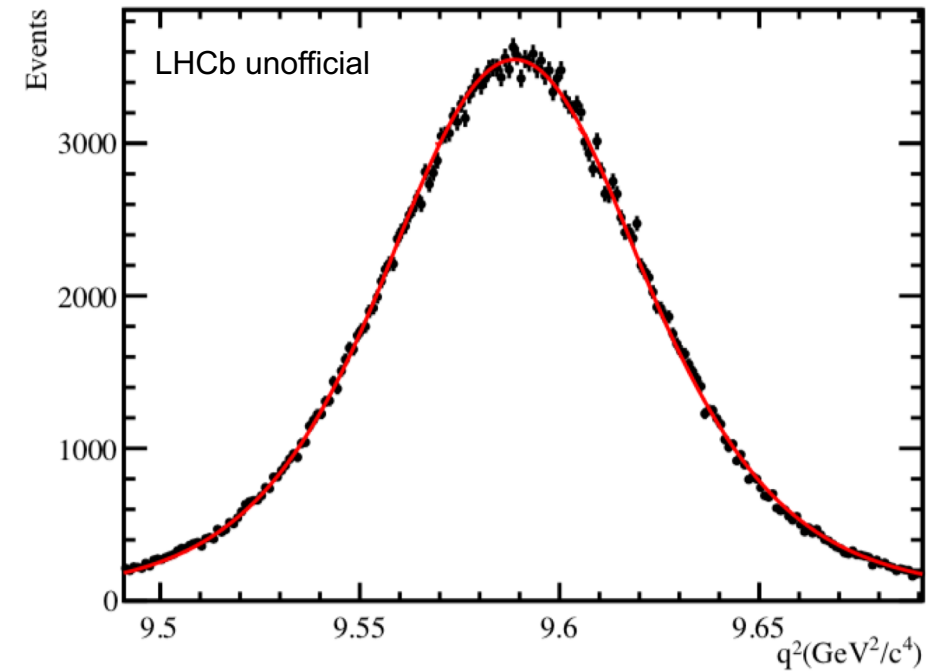


- Resonances included in our analysis: J/Ψ , $\Psi(2S)$, $\rho(770)$, $\phi(1020)$, $\Psi(3770)$, $\Psi(4040)$ and $\Psi(4160)$

Resolution in q^2

- Using kinematic fit with B^0 mass constraint to improve resolution of final state particles
- For J/Ψ , $\Psi(2S)$, $\phi(1020)$ observed peaks much wider than internal width of the resonances
- Convolve signal model with resolution model (double sided crystal ball plus Gaussian) to fit data
- Resolution parameters determined in data
- Resolution model verified in MC

Data, $B^0 \rightarrow K^* \mu^+ \mu^-$, J/Ψ core region



Background Fit Strategy

GOAL

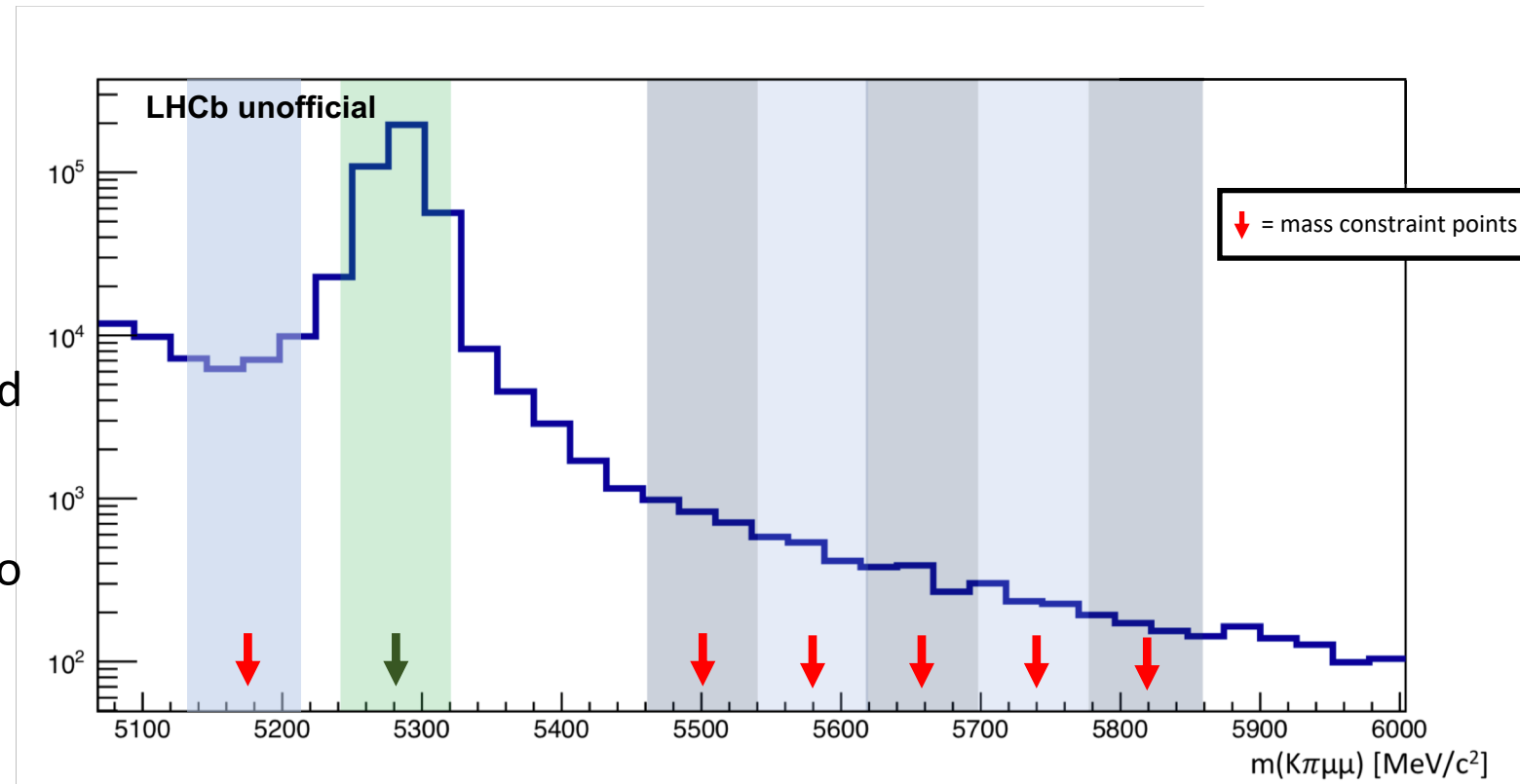
Determine a parameterization of the background in the **signal region**.

SOLUTION

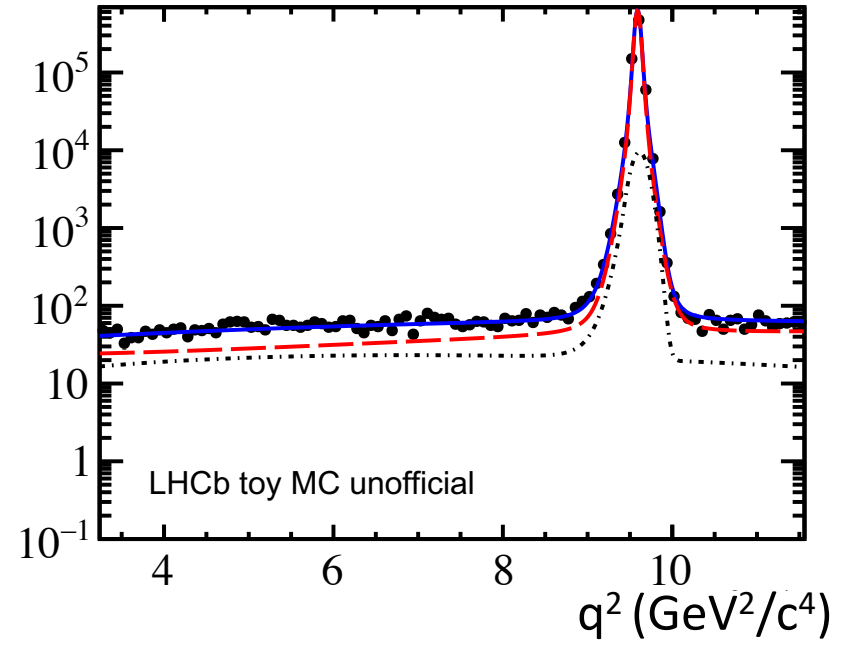
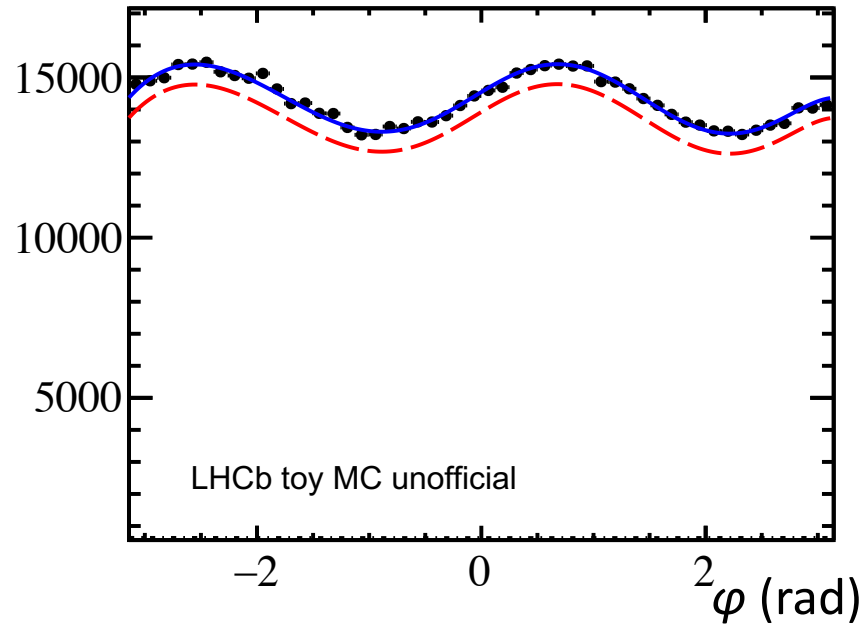
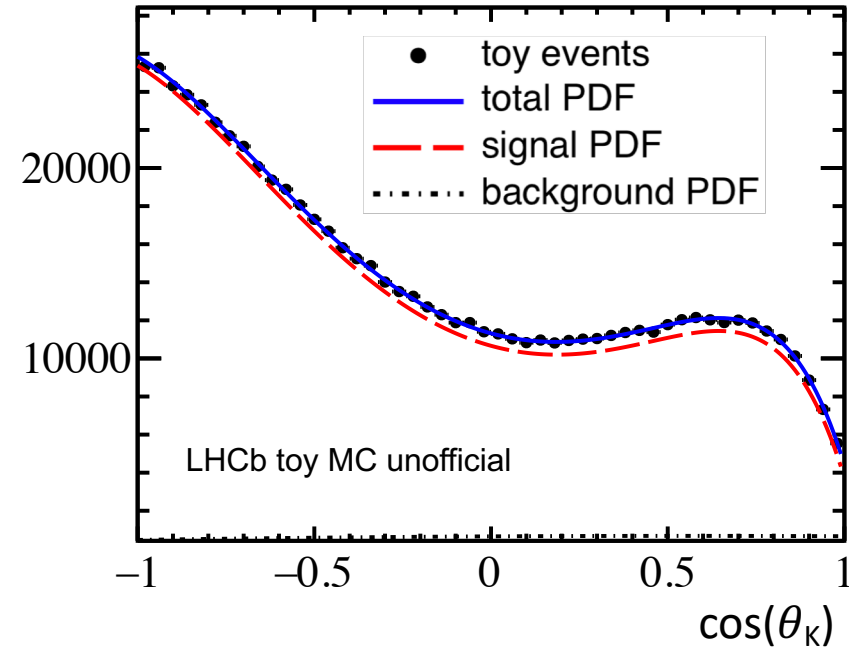
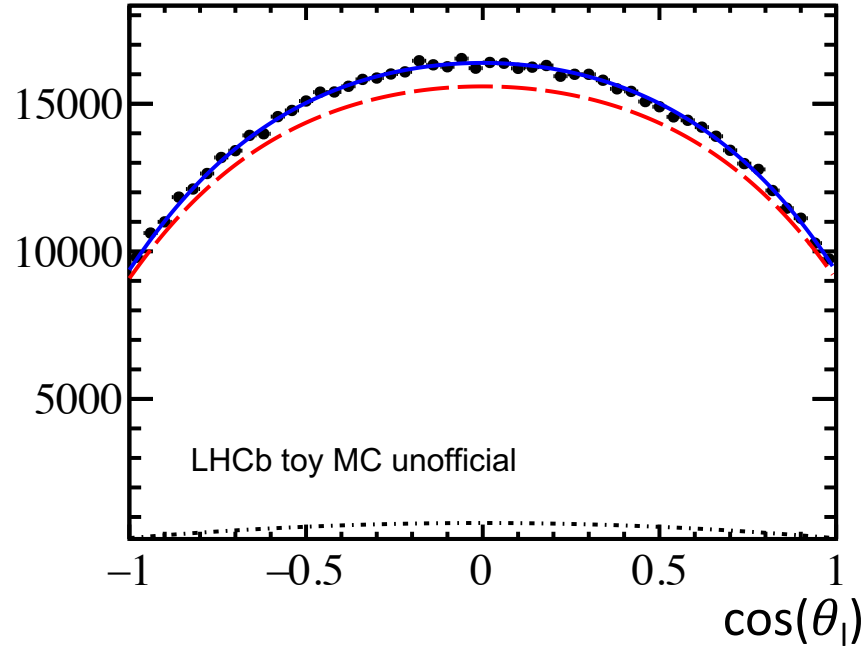
- Split up sideband into several regions
- Mass constrain events to the centre of respective region.
- Perform simultaneous fit to all sideband regions
- Interpolate background parameters into signal region – allowing for linear mass dependence of all parameters

PROBLEM

B^0 mass constraint distorts the distributions of the background and introduces a **dependence of the background shape on the width of the B^0 window**

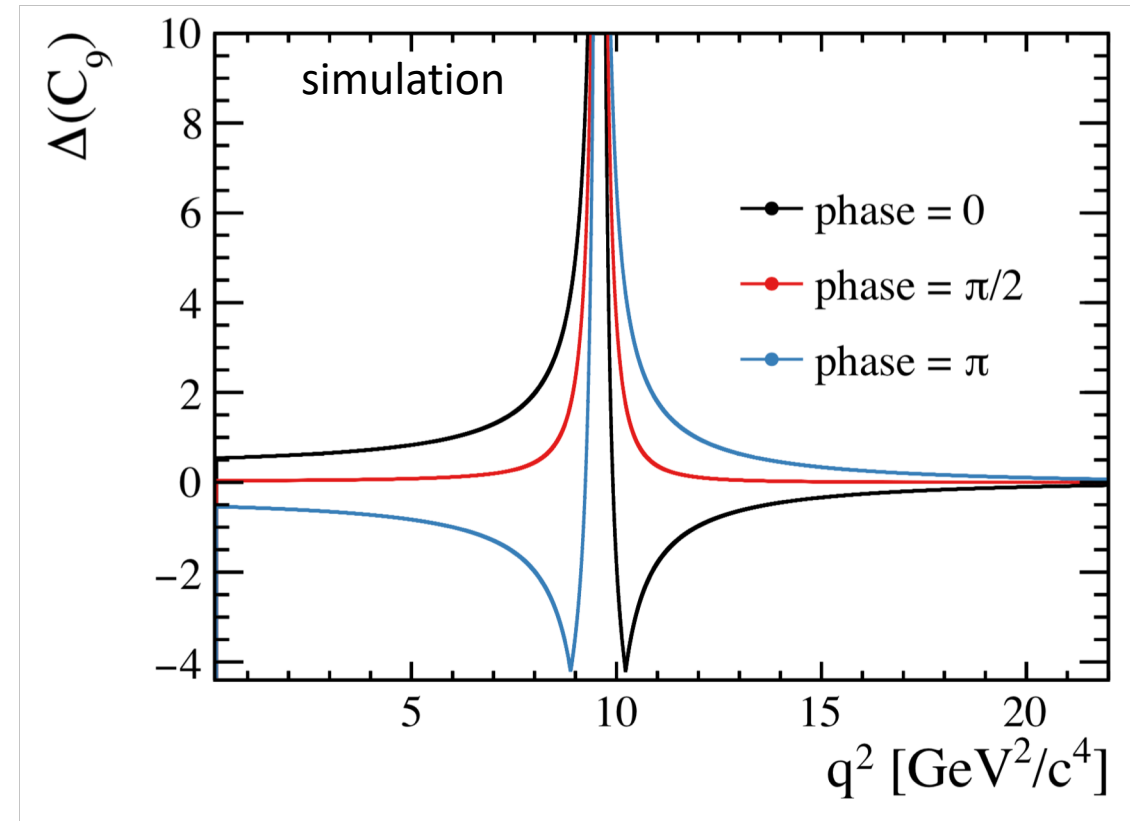


Projections of Toy Fits - Signal + Background: J/ψ region



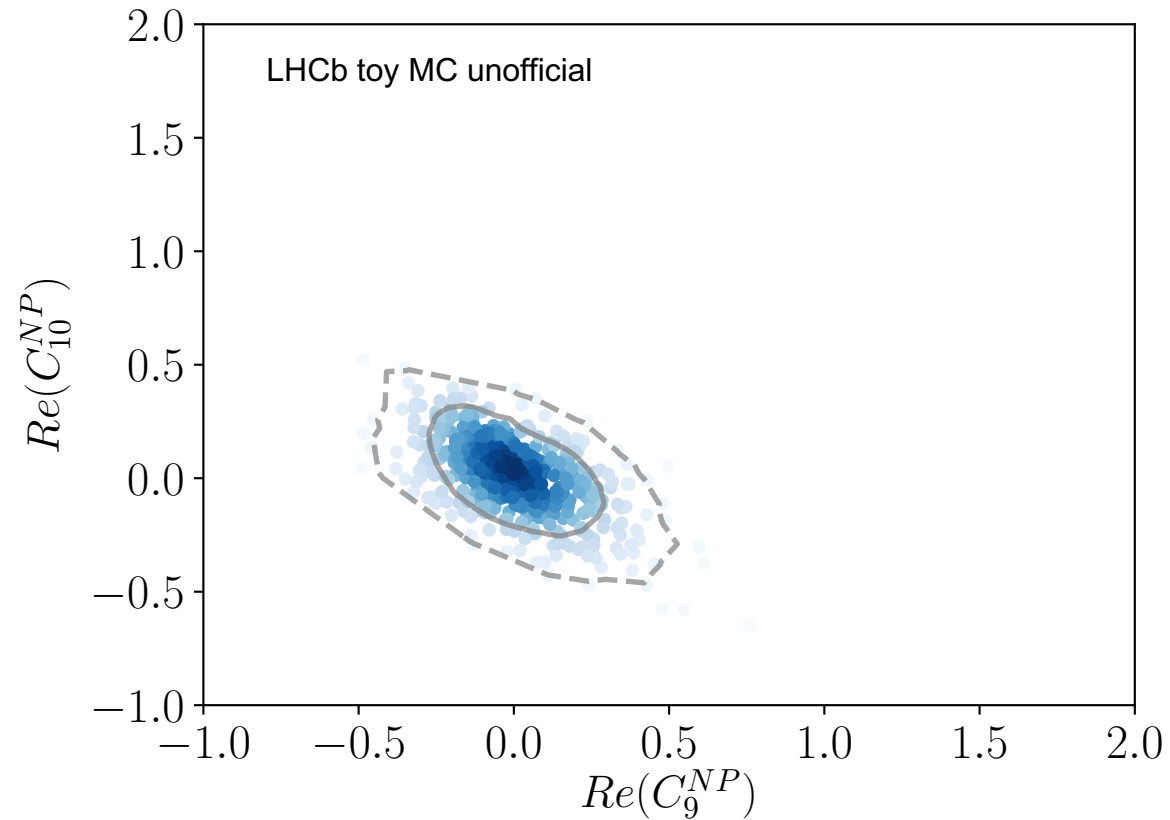
Sensitivity to phases and Wilson Coefficients

Require ~ 0.1 rad precision on the phases to ascertain role from non-local effects



Expected Sensitivity

- Not yet including background effects
- Form Factors floated within existing constraints
- Statistical precision with run1+run2:
 - $\sim 5\%$ for Wilson Coefficients
 - ~ 0.01 rad for the phases



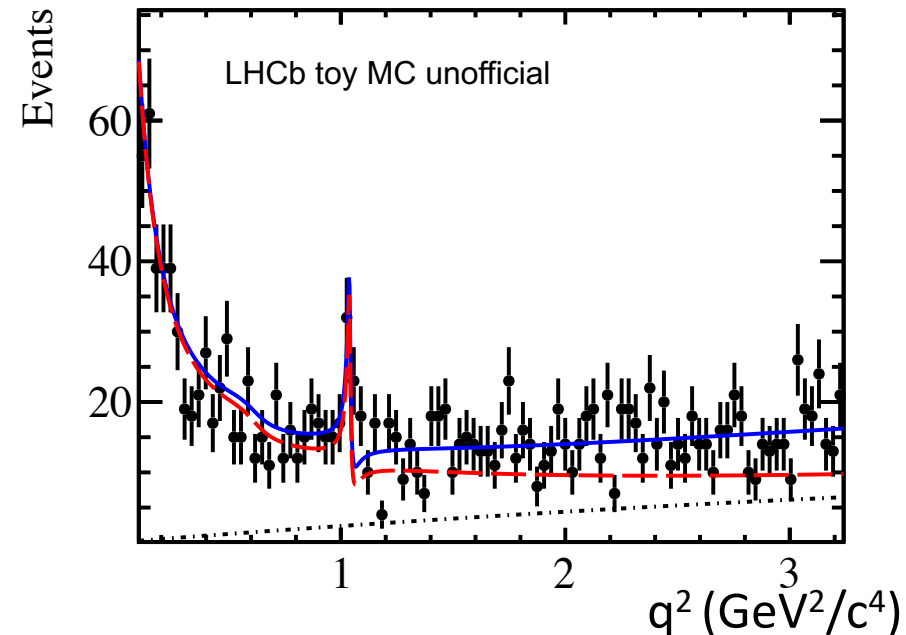
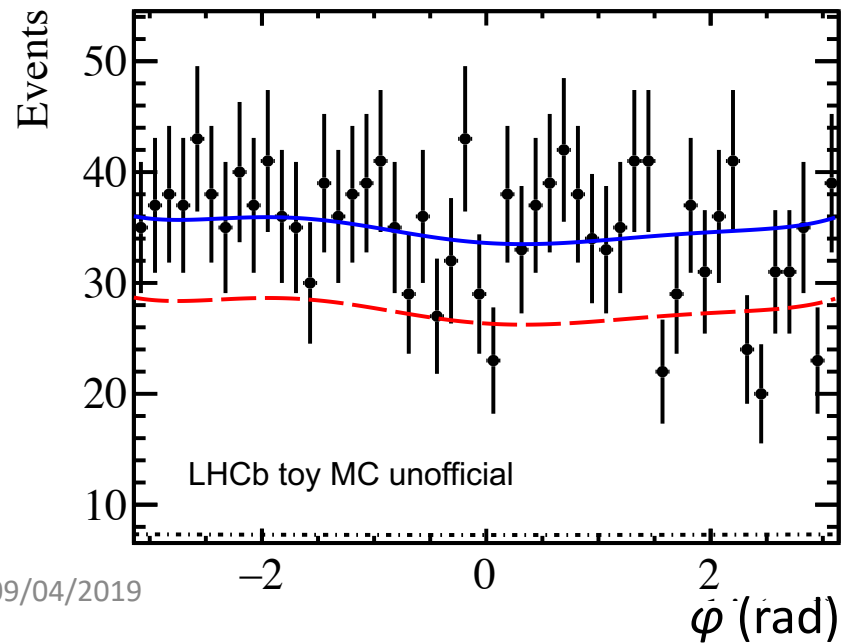
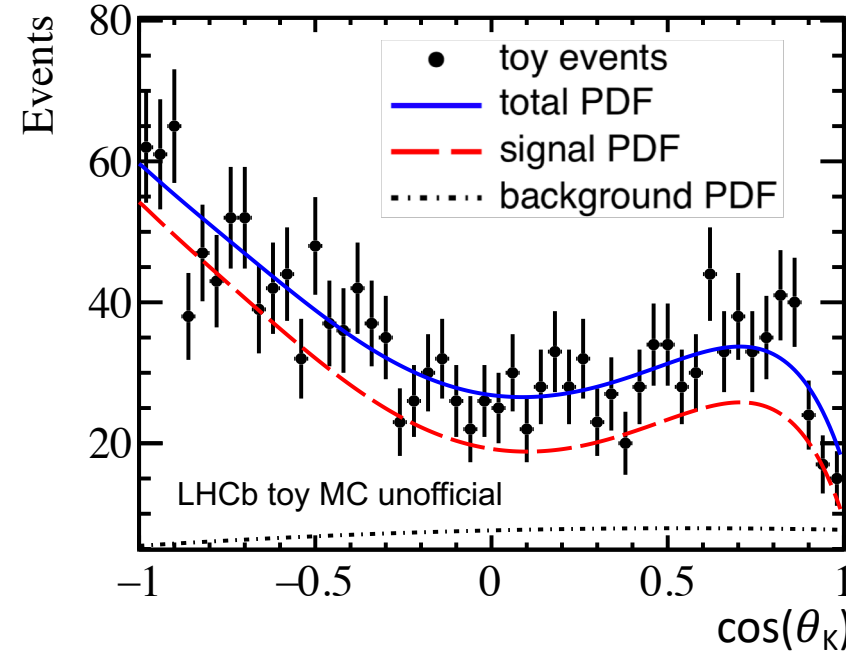
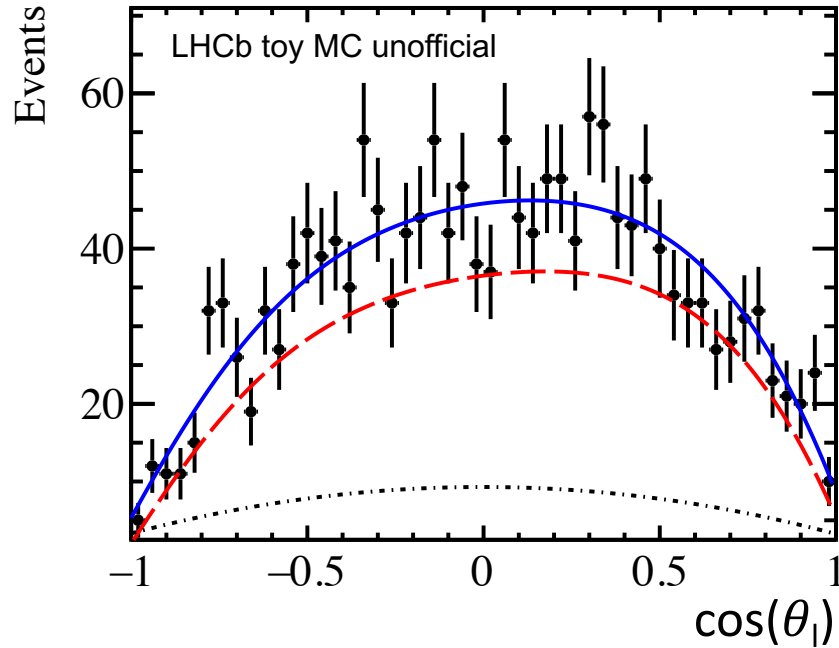
- High sensitivity to Wilson Coefficients due to use of full q^2 spectrum and unbinned fit
- Sensitivity to phases far better than required to ascertain role of non-local effects

Conclusion

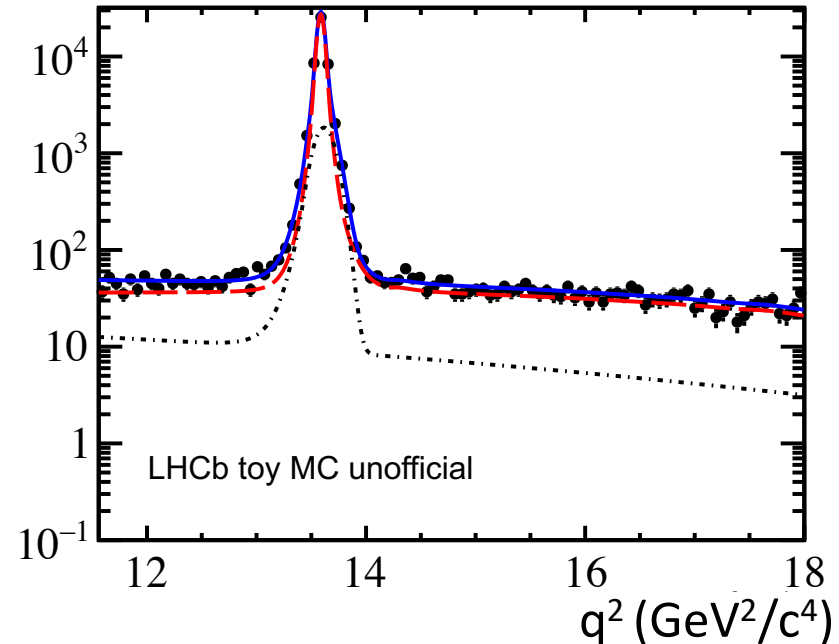
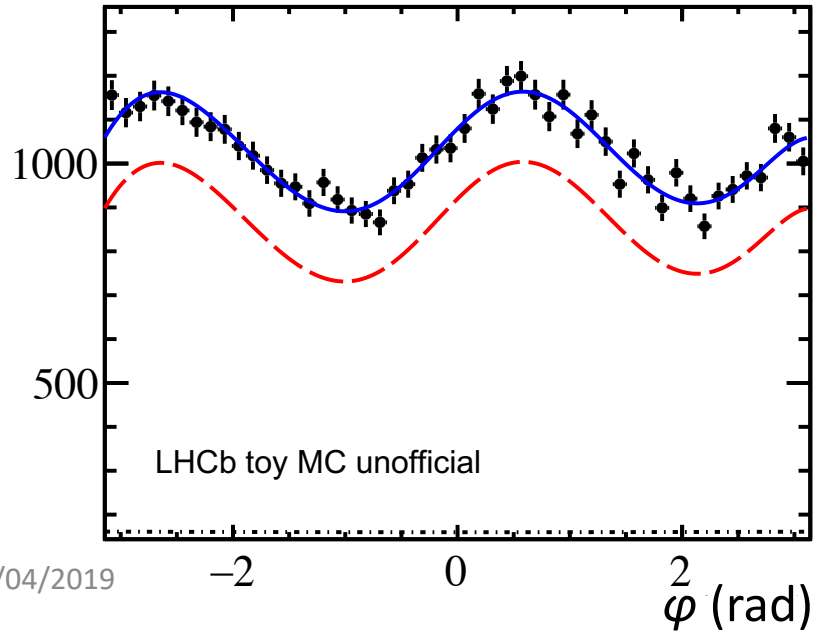
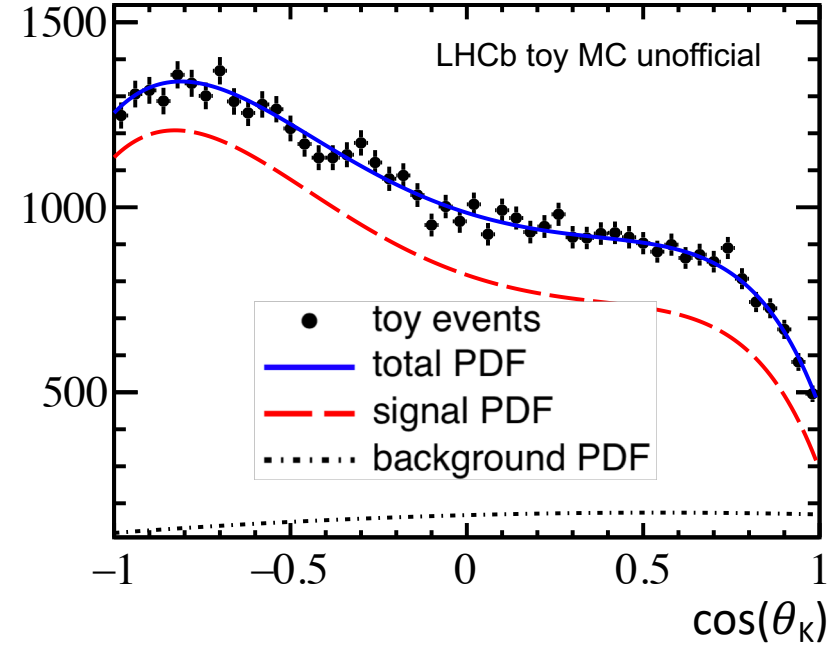
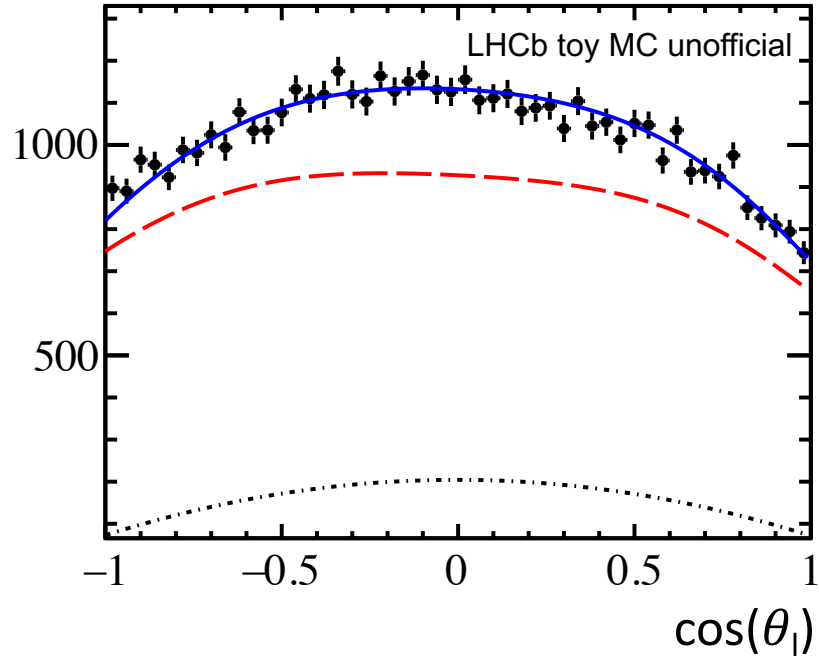
- Crucial to understand hadronic effects in $B^0 \rightarrow K^{*0}\mu^+\mu^-$ to interpret the observed discrepancies with the Standard Model
- Empirical model to determine Wilson Coefficients and the level of hadronic interference in unbinned fit to full q^2 spectrum of $B^0 \rightarrow K^{*0}\mu^+\mu^-$
- Kinematic fit with B^0 mass constraint to improve the crucial q^2 resolution. This has implications for background fit
- Very promising sensitivity to C_9 , C_{10} and the phases

Backup

Projections of Toy Fits - Signal + Background: φ region



Projections of Toy Fits - Signal + Background: $\Psi(2S)$ region

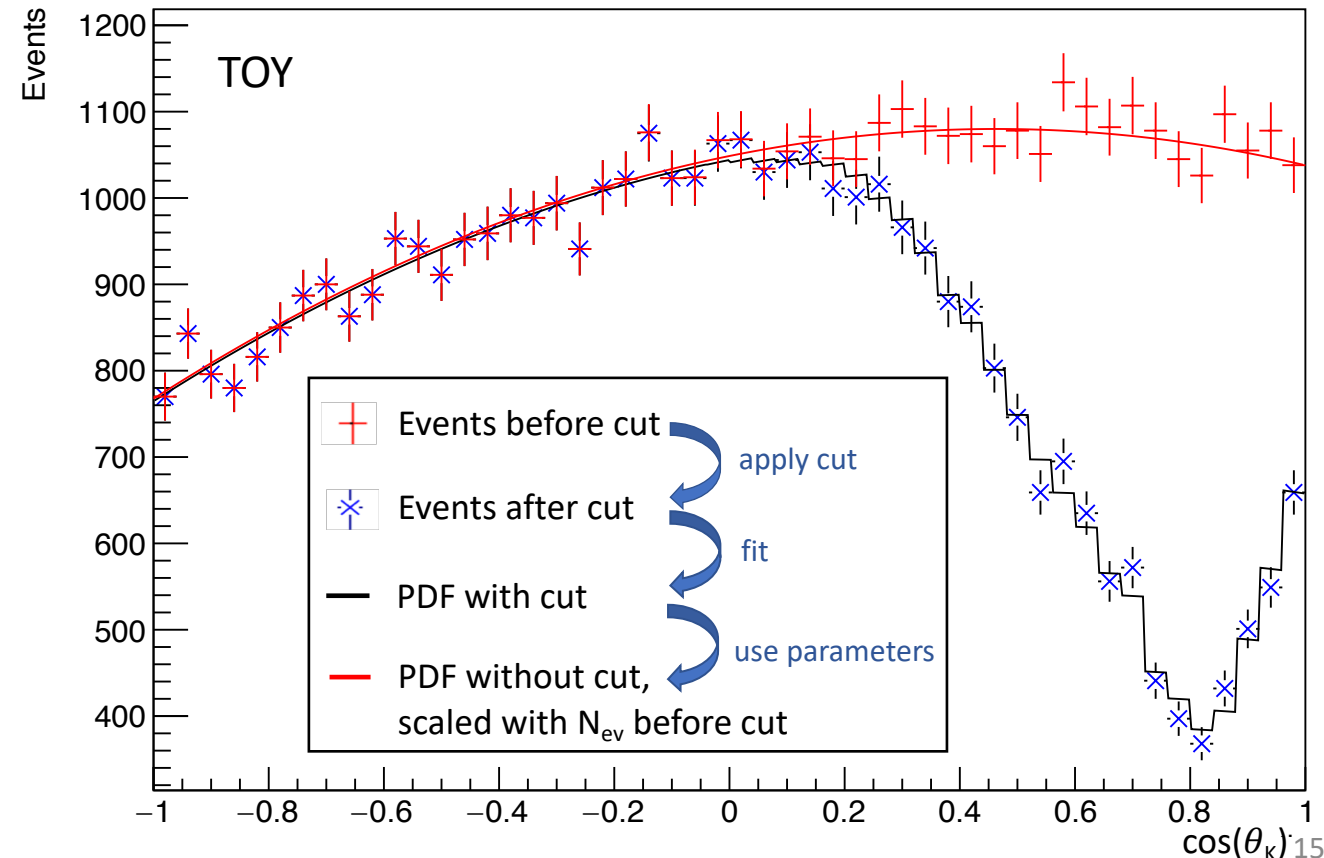


The effect of the $K\mu\mu$ veto

- To reject background events from $B^+ \rightarrow K^+\mu\mu$ (plus random π^-) in our $K^+\pi^-\mu\mu$ -sample we use a veto:

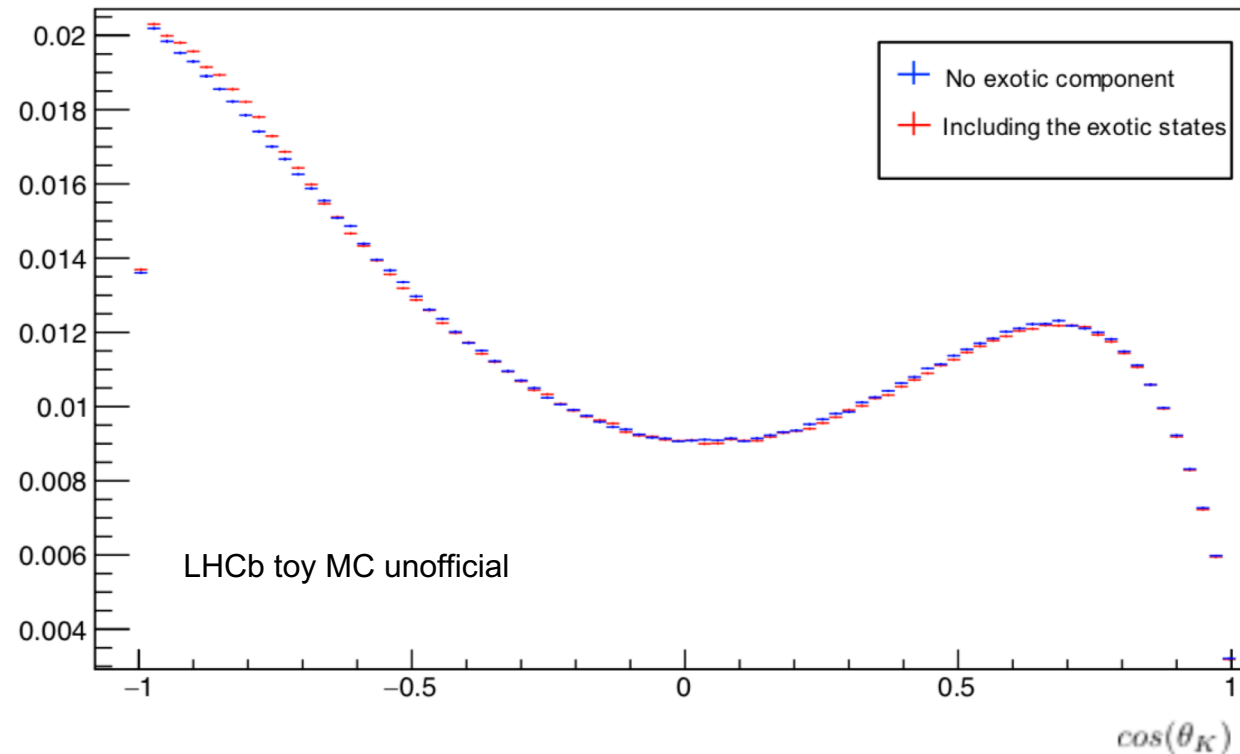
Remove all events with: **$(5220 < m(K\mu\mu) < 5340) \text{ MeV}/c^2$** and $m(K\pi\mu\mu) > 5380 \text{ MeV}/c^2$

- This causes a gap in the $\cos(\theta_K)$, q^2 , and $m(K\pi\mu\mu)$ phase space which can cause biases in the sideband fit
- By adjusting the normalisation of the PDF we can recover the correct background parameters



Z(4430) and Z(4200)

- Charmonium-like states with a quark content of $|c\bar{c}ud\rangle$
- Decaying to $\Psi(2S)\pi$ or $J/\Psi\pi$



The model (Blake et al., Eur.Phys.J. C78 (2018) no.6 453)

The differential decay rate of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ transitions depends on 6 complex amplitudes $A_{\parallel}^{L,R}$, $A_{\perp}^{L,R}$, $A_0^{L,R}$

$$\begin{aligned}
 \mathcal{A}_0^{L,R}(q^2) &= -8N \frac{m_B m_{K^*}}{\sqrt{q^2}} \left\{ (C_9 \mp C_{10}) A_{12}(q^2) + \frac{m_b}{m_B + m_{K^*}} C_7 T_{23}(q^2) + \mathcal{G}_0(q^2) \right\} \\
 \mathcal{A}_{\parallel}^{L,R}(q^2) &= -N \sqrt{2} (m_B^2 - m_{K^*}^2) \left\{ (C_9 \mp C_{10}) \frac{A_1(q^2)}{m_B - m_{K^*}} + \frac{2m_b}{q^2} C_7 T_2(q^2) + \mathcal{G}_{\parallel}(q^2) \right\} \\
 \mathcal{A}_{\perp}^{L,R}(q^2) &= N \sqrt{2} \lambda \left\{ (C_9 \mp C_{10}) \frac{V(q^2)}{m_B + m_{K^*}} + \frac{2m_b}{q^2} C_7 T_1(q^2) + \mathcal{G}_{\perp}(q^2) \right\},
 \end{aligned}$$

Wilson Coefficients

Form Factors

Non-local hadronic contributions

Form Factors modelled with parameters obtained from combination of Light Cone Sum Rules and Lattice QCD

Straub et al, JHEP08 (2016) 098

$$F^i(q^2) = \frac{1}{1 - q^2/m_{R_i}^2} \sum_{k=0}^2 \alpha_k^i [z(q^2) - z(0)]^k$$

Modelling non-local hadronic contributions

$$\mathcal{G}_0 = \frac{m_b}{m_B + m_{K^*}} T_{23}(q^2) \zeta^0 e^{i\omega^0} + A_{12}(q^2) \sum_j \eta_j^0 e^{i\theta_j^0} A_j^{\text{res}}(q^2)$$

$$\mathcal{G}_{\parallel} = \frac{2m_b}{q^2} T_2(q^2) \zeta^{\parallel} e^{i\omega^{\parallel}} + \frac{A_1(q^2)}{m_B - m_{K^*}} \sum_j \eta_j^{\parallel} e^{i\theta_j^{\parallel}} A_j^{\text{res}}(q^2)$$

$$\mathcal{G}_{\perp} = \frac{2m_b}{q^2} T_1(q^2) \zeta^{\perp} e^{i\omega^{\perp}} + \frac{V(q^2)}{m_B + m_{K^*}} \sum_j \eta_j^{\perp} e^{i\theta_j^{\perp}} A_j^{\text{res}}(q^2)$$

Magnitude and phase of non-local contribution to dipole form factor

Sum over all resonances

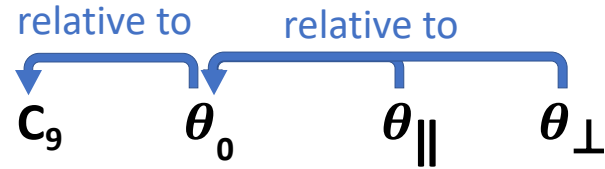
Magnitude and phase for each resonance

BW Amplitudes

- Resonances included in our analysis: J/Ψ , $\Psi(2S)$, $\rho(770)$, $\phi(1020)$, $\Psi(3770)$, $\Psi(4040)$ and $\Psi(4160)$
- BF of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ is implicitly included in the model through the magnitudes of the resonances which are measured relative to the penguin

Comparison to other models

Three phases for every resonance:



- Amplitude analyses of $B \rightarrow VK^*$ (for J/Ψ , $\Psi(2S)$, $\phi(1020)$, $\rho(770)$) decays from LHCb, Belle and BaBar constrain sizes of the magnitudes $\eta_{0,\parallel,\perp}$ and the relative phases $\theta_{\parallel,\perp}$
- The phase θ_0 (relative to the penguin) of each resonance is completely unknown**
- Fixing the relative phases and varying the unknown phases θ_0 , can predict angular observables and compare to data and other models
- In the fit to data also include contribution from S-wave amplitudes for both short-distance and non-local components

