

AION/MAGIS-100



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HEP Extravaganza, 6 Dec 2023



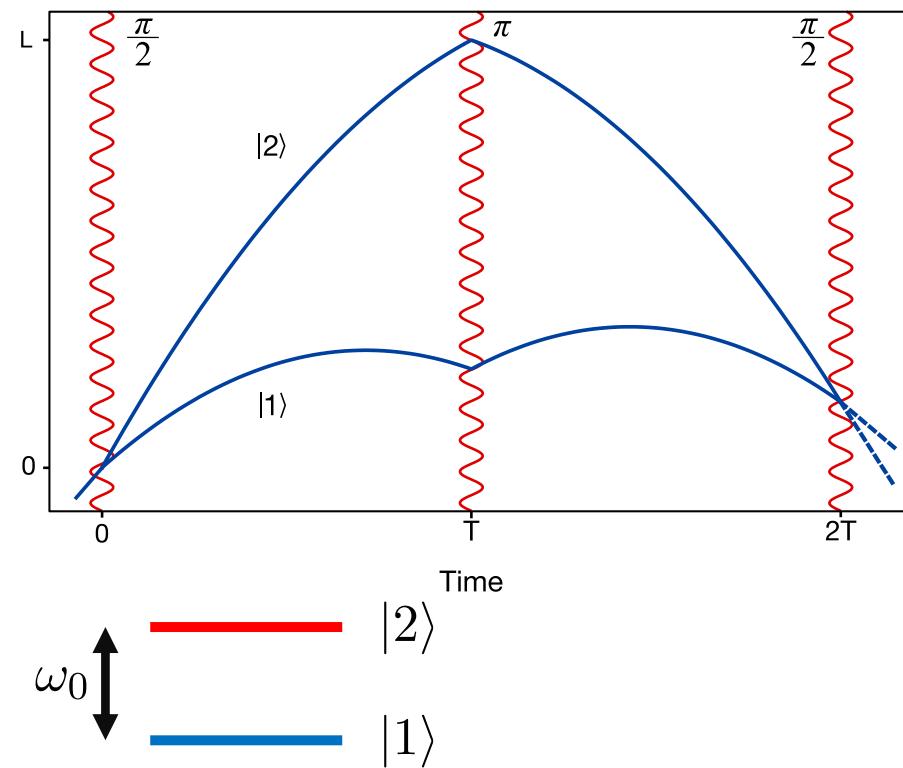
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Overview

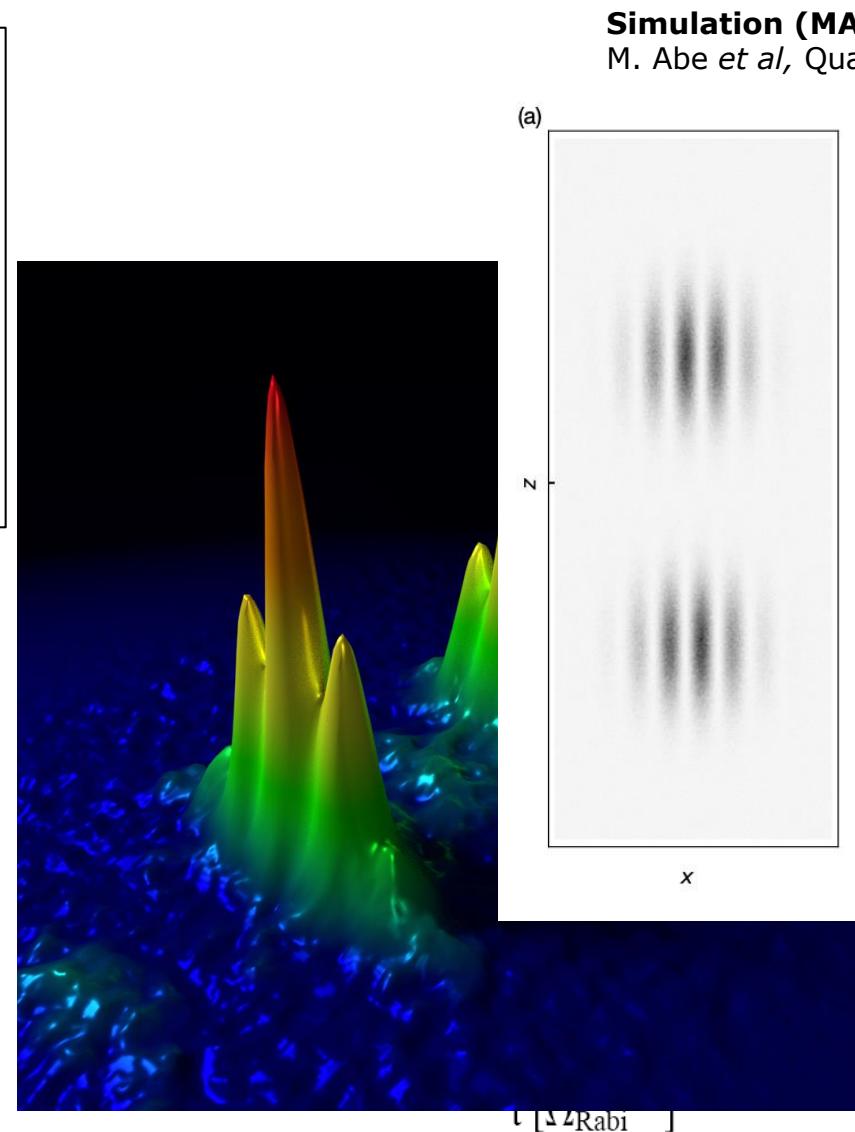
- What even is AION and MAGIS-100?
- What we have been up to
- Outlook

Speedy atom interferometry



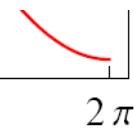
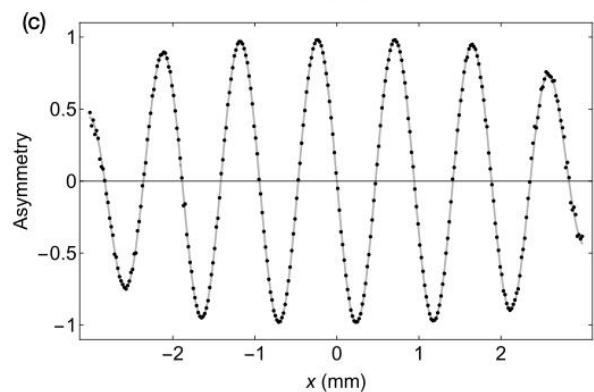
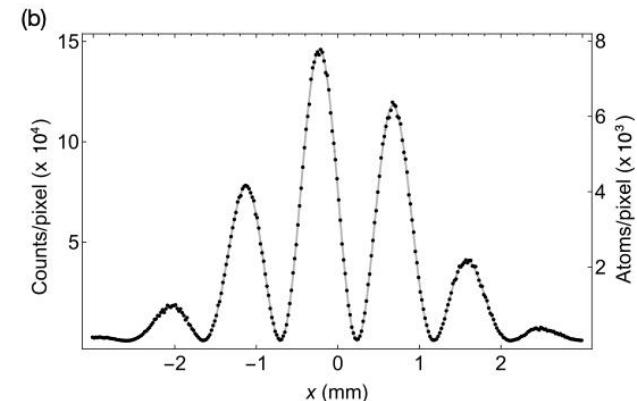
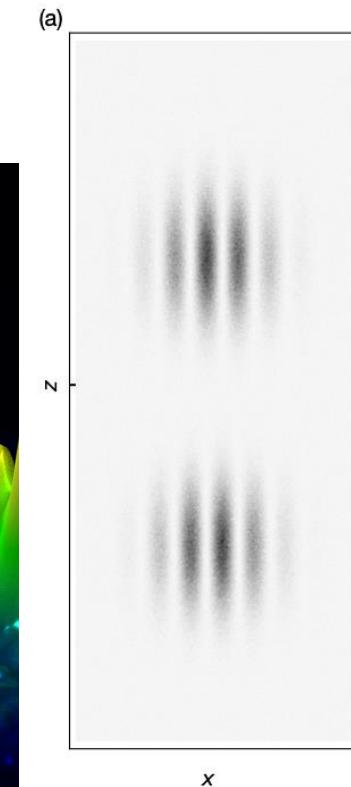
$$H_{int} = -e\mathbf{r} \cdot \mathbf{E}_0 \cos(\phi - \omega_0 t)$$

$$\Omega_{1,2} = -\frac{\langle 1|e\mathbf{r} \cdot \mathbf{E}|2\rangle}{\hbar}$$



Simulation (MAGIS-100)

M. Abe *et al*, Quantum Sci. Technol. **6** 044003 (2021)



Science case

Ultralight scalar dark matter → high density, wave-like characteristics



$$\mathcal{L}_\phi \supset \phi(t) \sqrt{4\pi G_N} \left[\frac{d_e}{4e^2} F_{\mu\nu} F^{\mu\nu} - d_{m_e} m_e \bar{\psi}_e \psi_e \right]$$

Photon
Couplings

Electron Mass
Couplings

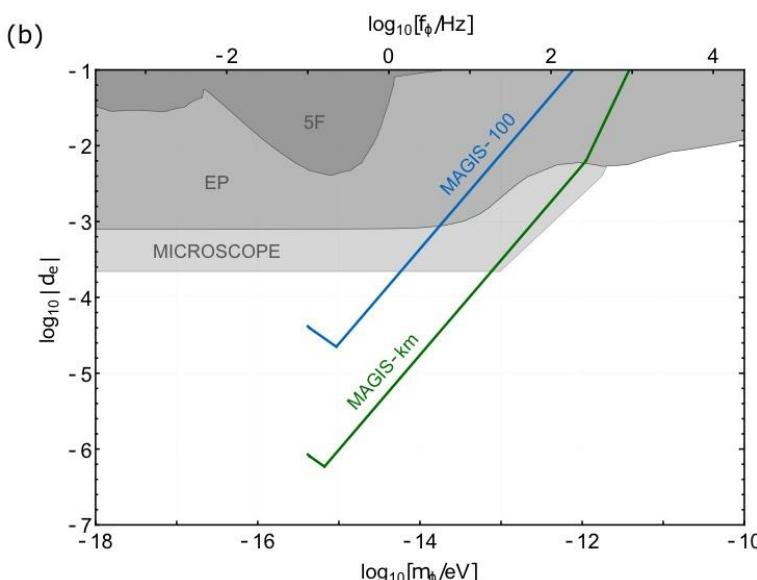
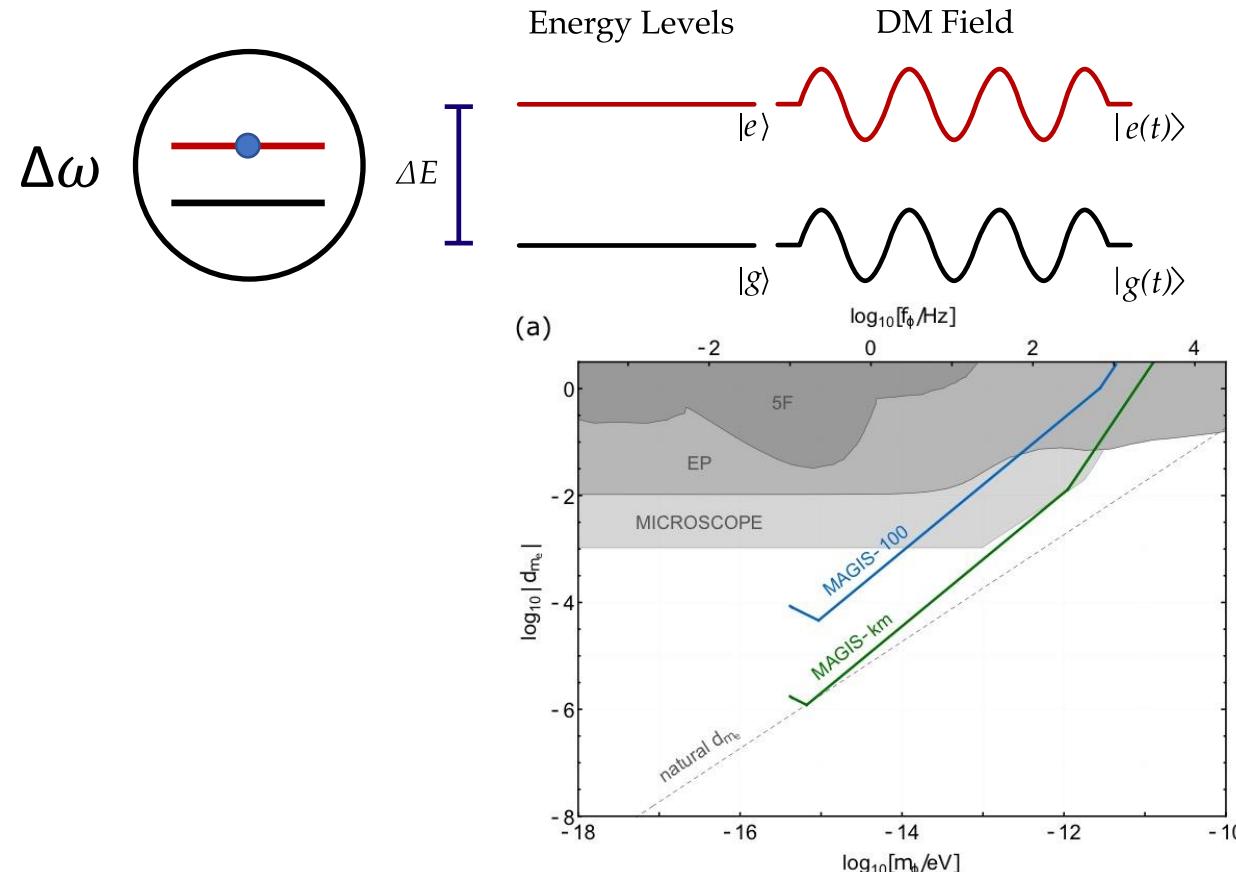
Science case

Time varying atom transition frequency

$$\Delta\phi \sim \omega_A(2L/c)$$

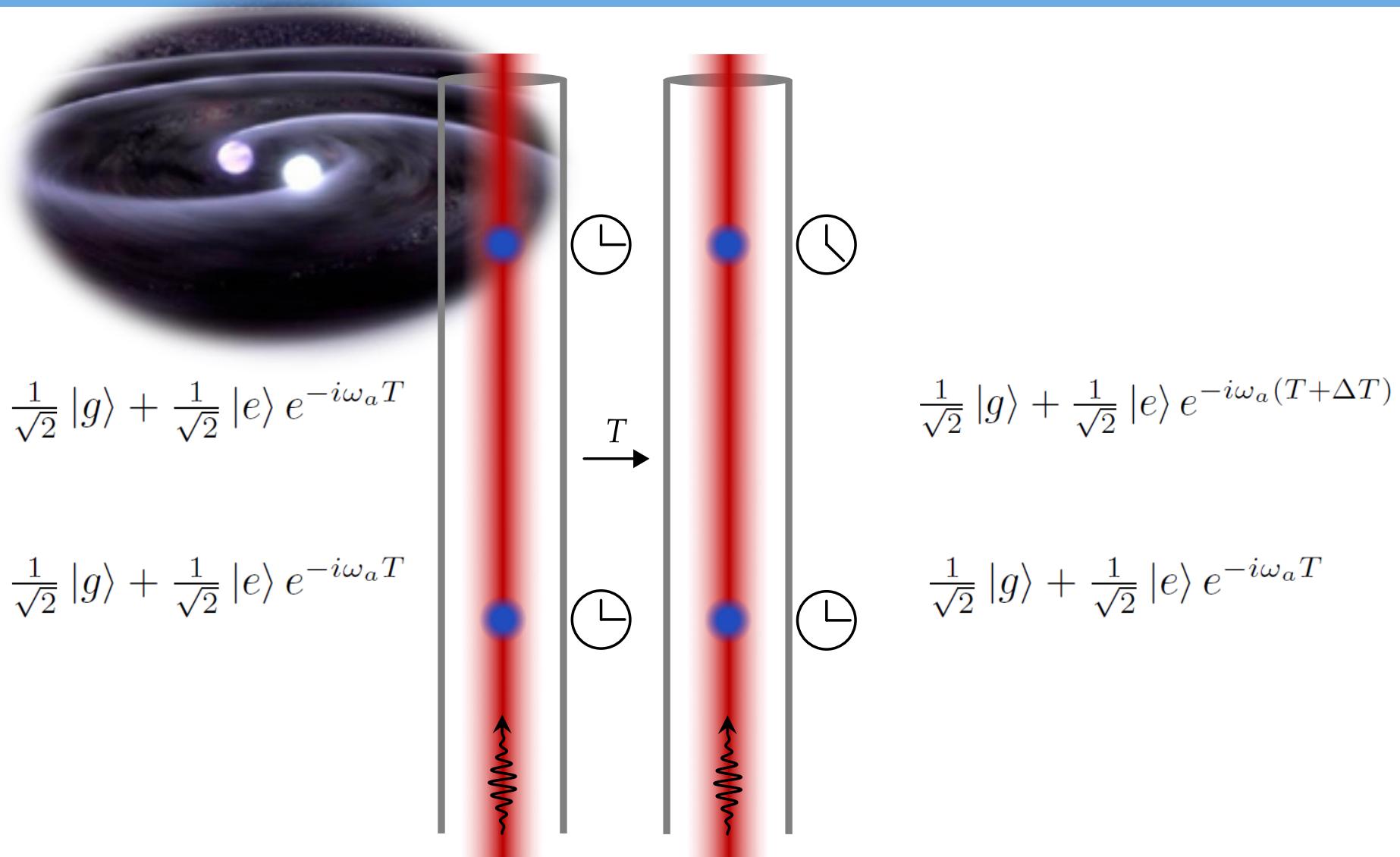
Dark Matter $\delta\omega_A$

Gravitational Waves $\delta L = hL$



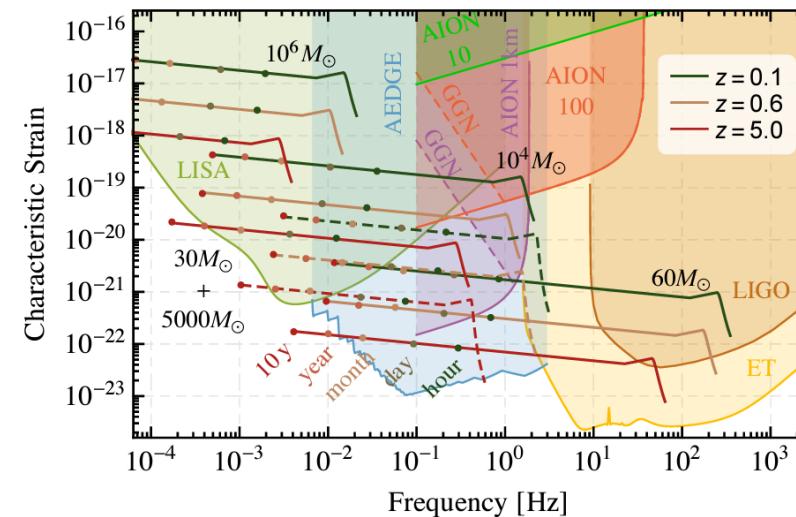
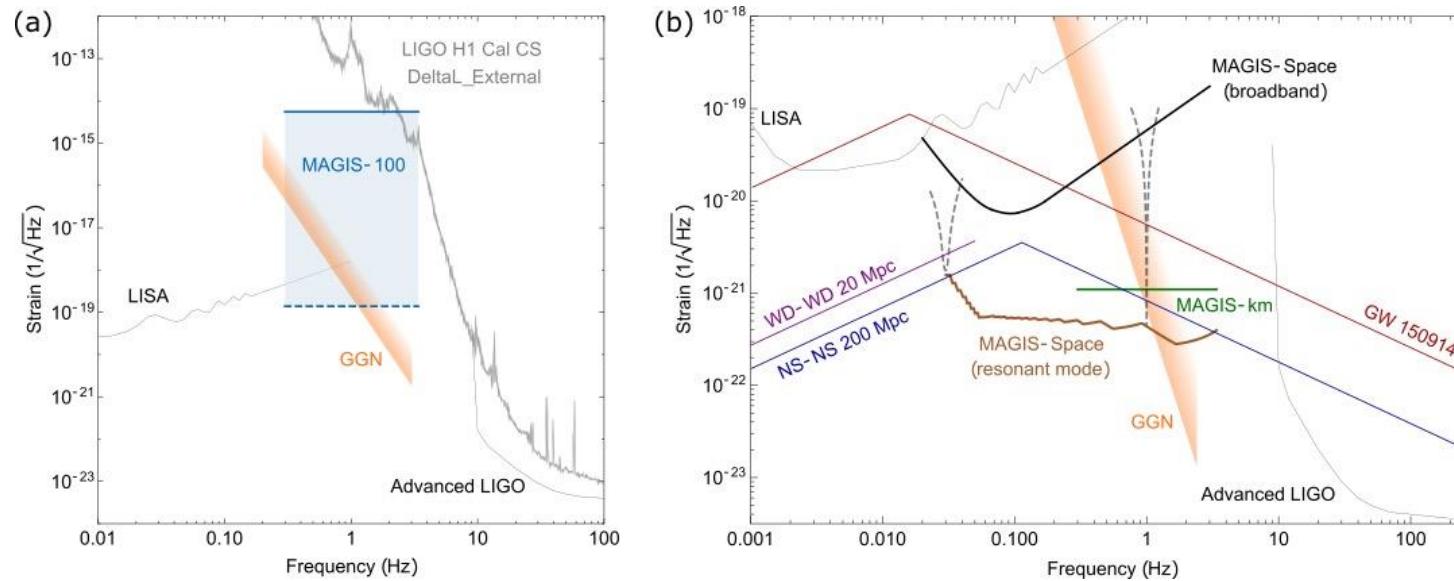
M. Abe *et al.*, *Quantum Sci. Technol.*, **6**, 4, 2021.

Science case



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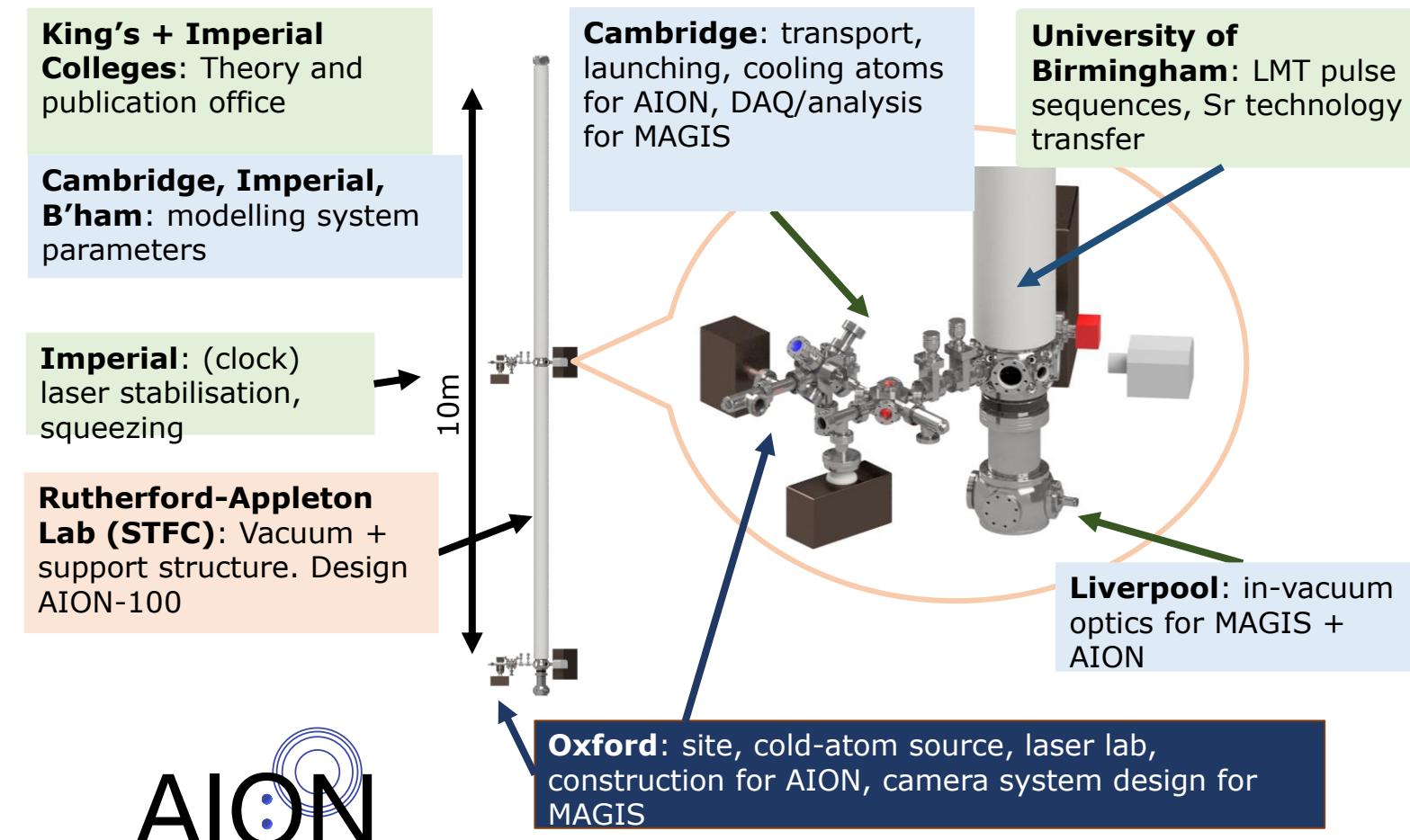
Science case



J. Cosmol. Astropart. Phys. 5, 011 (2020)

Atom Interferometer Observatory and Network

- UK consortium of 7 institutions
- Develop ultracold strontium laboratories in parallel
- Staged project for increased baseline atom interferometers 10m -> 100m -> 1km
- Investigate technology development and network with MAGIS-100 for large scale science goals



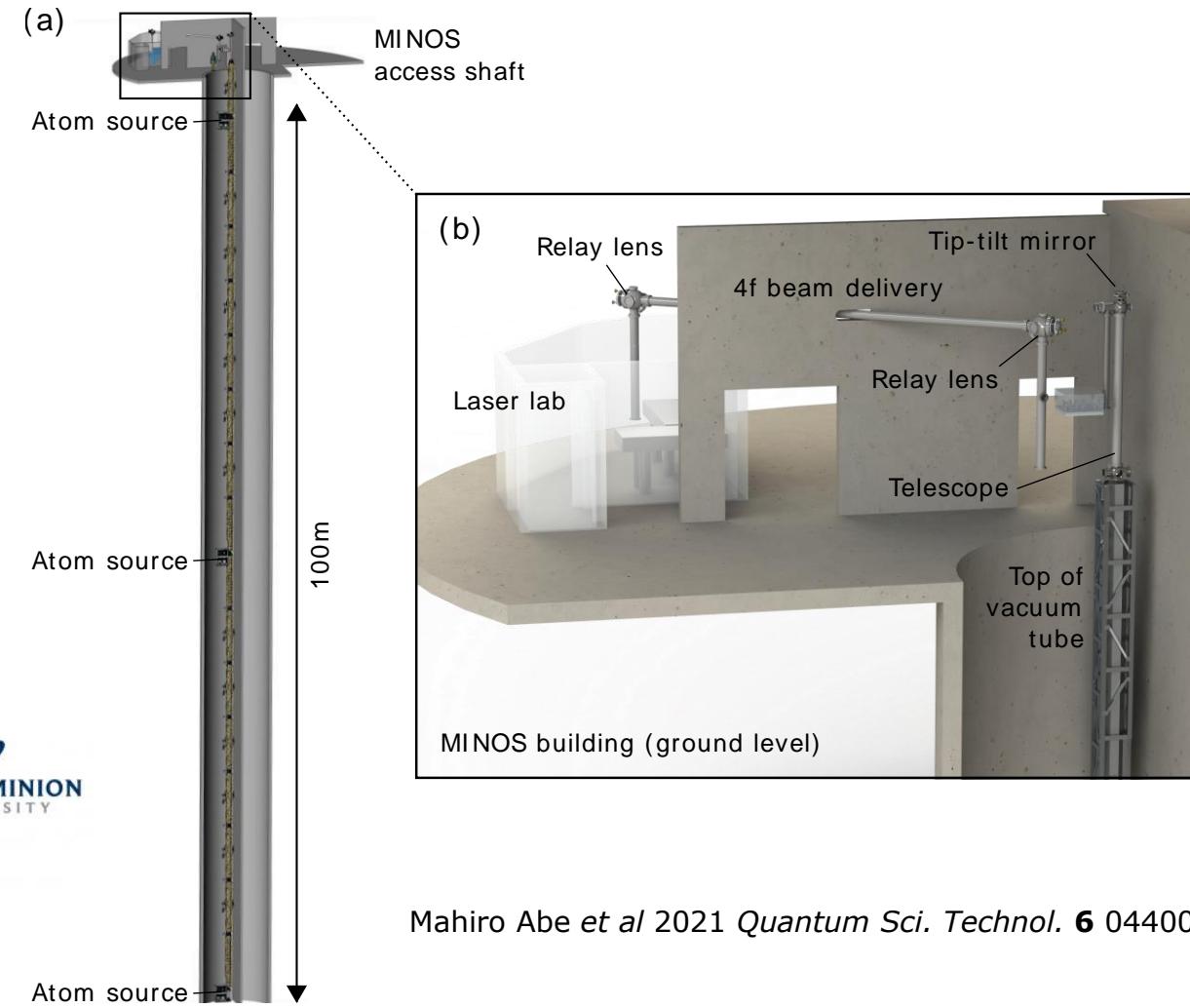
L. Badurina *et al* JCAP05(2020)011

MAGIS-100

Matter-wave Atomic Gradiometer Interferometric Sensor



- Long-baseline atom interferometer being built at Fermilab US
- 3 strontium atom sources along vertical baseline
- Test bed experiment for simultaneous atom interferometer control
- Prototype 10m device at Stanford



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Mahiro Abe *et al* 2021 *Quantum Sci. Technol.* **6** 044003



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Cambridge activities

- Data acquisition, monitoring, and control
 - Hardware and software for control systems
 - Environmental monitoring
 - Computing infrastructure
- Simulations and data analysis
 - Matter-wave simulations, systematics
 - Offline coordination for MAGIS-100
- AION and MAGIS-100 timing and data synchronization

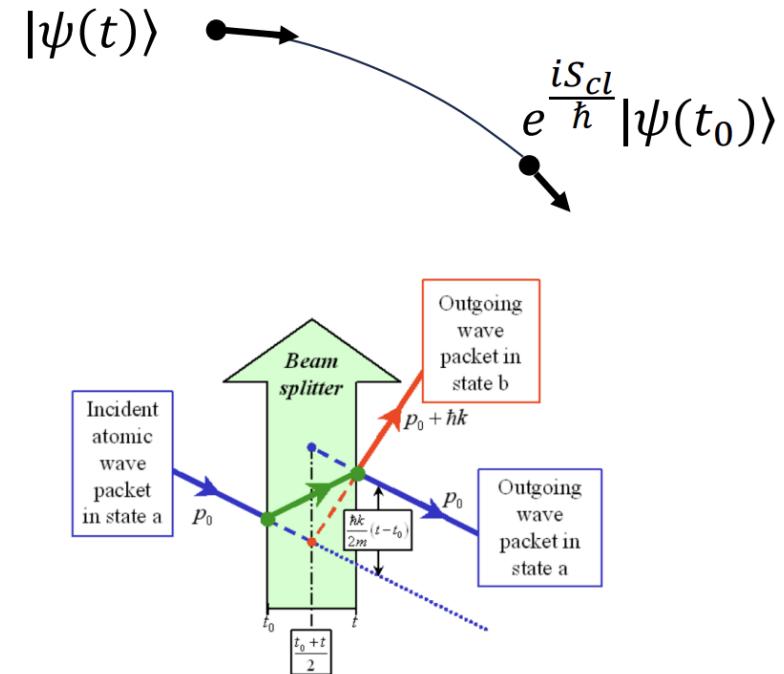
Matter-wave simulations

Recap: 3-pulse sequence on on thermal cloud

Simulation of a thermal/diffuse cloud using an ensemble of Gaussian wavepackets (10^5 atoms, 15nK, 1cm)

Allows the use of

- the semi-classical approach^[2] for free propagation
- the *ttt*-scheme^[3] for atom-laser interactions



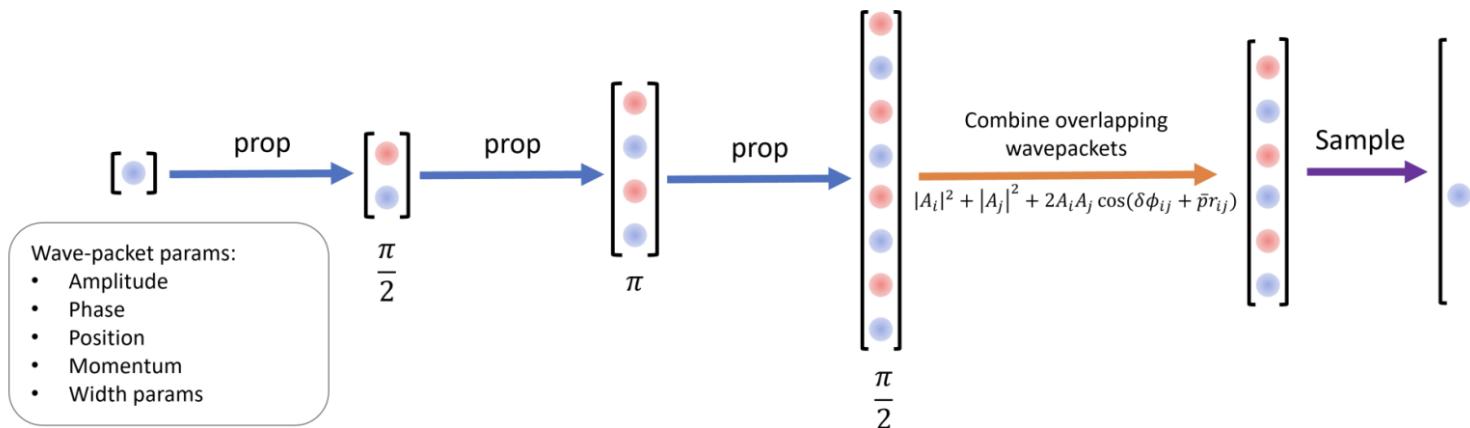
Noam Mouelle's work

Matter-wave simulations

Recap: 3-pulse sequence on on thermal cloud

Code specs:

- Python
- Wavepacket params stored in $N_{atoms} \times N_{paths} \times N_{dim}$ Numpy arrays, allowing the use of vectorization

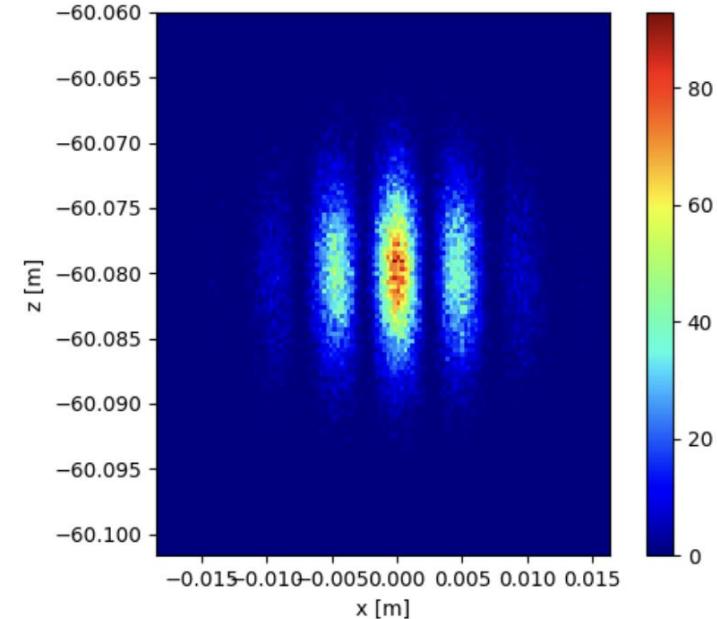
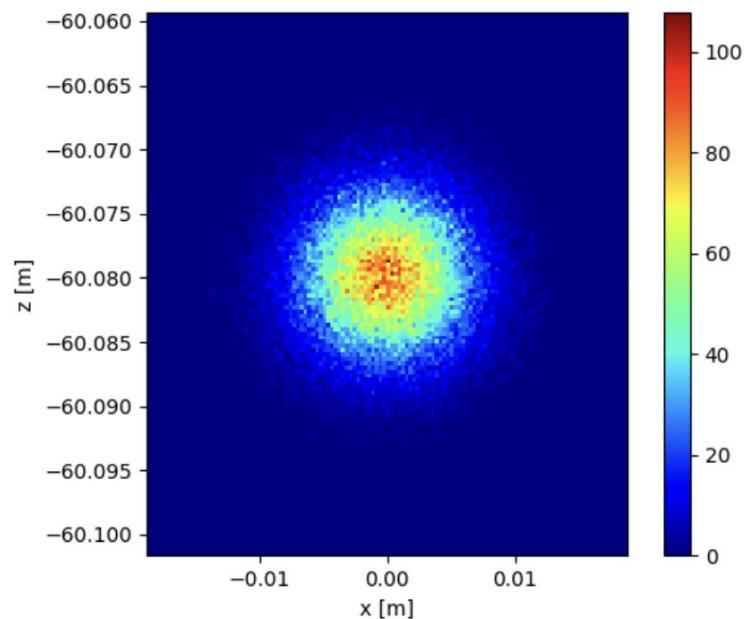


Noam Mouelle's work

Matter-wave simulations

Recap: 3-pulse sequence on on thermal cloud

Binned distributions



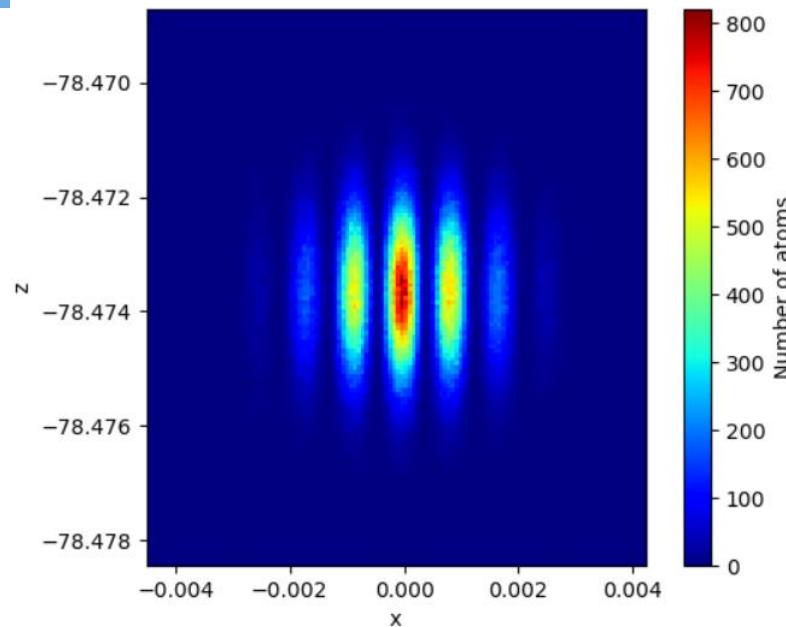
Noam Mouelle's work

Matter-wave simulations

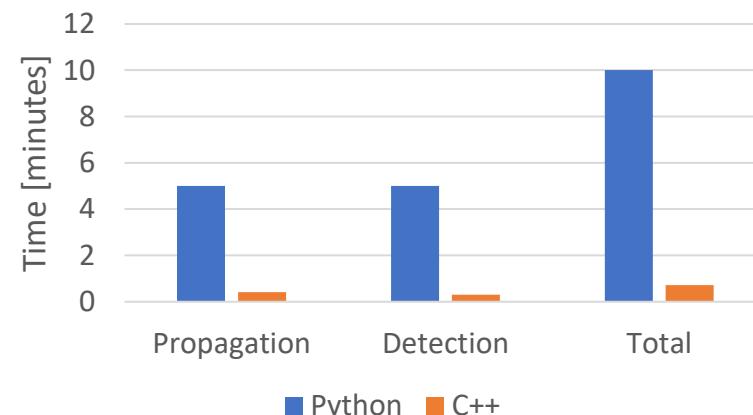
- Developing a MC simulation of atom cloud propagation:
 - Laser wavefront aberration
 - Non-uniform phase-shifts (gravity gradients etc.)
- Recently moved from Python prototype to C++
- Hope to focus on inference of phase shift from images

Noam Mouelle's work

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Simulation time, 1 million atoms, 3 pulse sequence



Bayesian inference for atom interferometry



Bayesian Inference (Python)

$$p(\boldsymbol{\theta} | d, M) = \frac{p(d|\boldsymbol{\theta}, M) p(\boldsymbol{\theta} | M)}{p(d|M)} = \frac{L(\boldsymbol{\theta}) \uparrow (\boldsymbol{\theta})}{Z}$$

$\boldsymbol{\theta}$: parameter

$p(\boldsymbol{\theta} | d, M)$: posterior

Simulation

d : data

$L(\boldsymbol{\theta})$: likelihood

Waveform/DM
Field, etc.

M : model

$\uparrow (\boldsymbol{\theta})$: prior

Bilby: arXiv:1811.02042



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14

Bayesian inference for atom interferometry



MAGIS-100



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Post-Newtonian Gravitational Waves (Inspiral)

$$\tilde{h}(f) = \frac{5}{96} \left[\frac{A_+^2 F_+^2 + A_\times^2 F_\times^2}{D_L} \right] f^{-2/3} M_z^{5/6} f^{-7/6} e^{-(f)}$$

$$(f) = 2\hat{f} t_c - \varphi_c - \frac{\hat{f}}{4} + \frac{3}{128} (\hat{f} M_z f)^{-5/3} - \varphi_P - \varphi_D - \dots$$

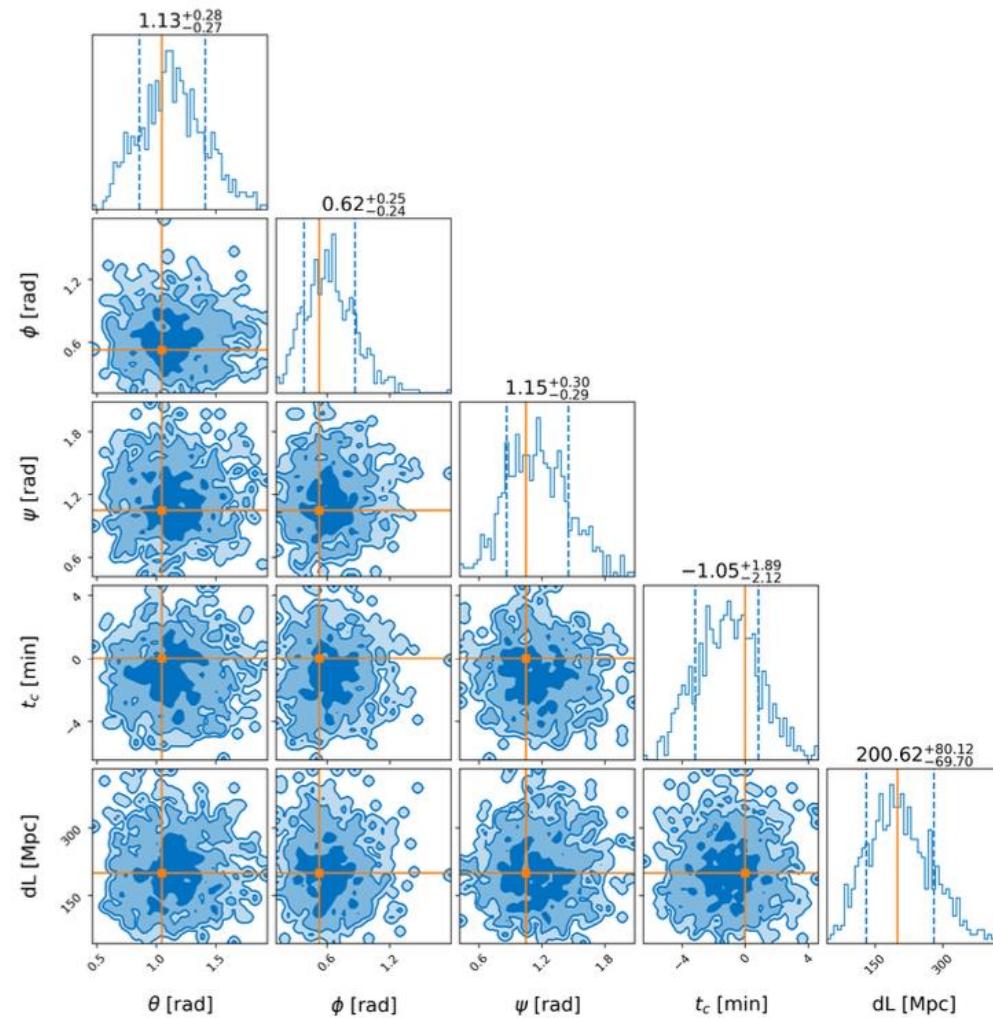
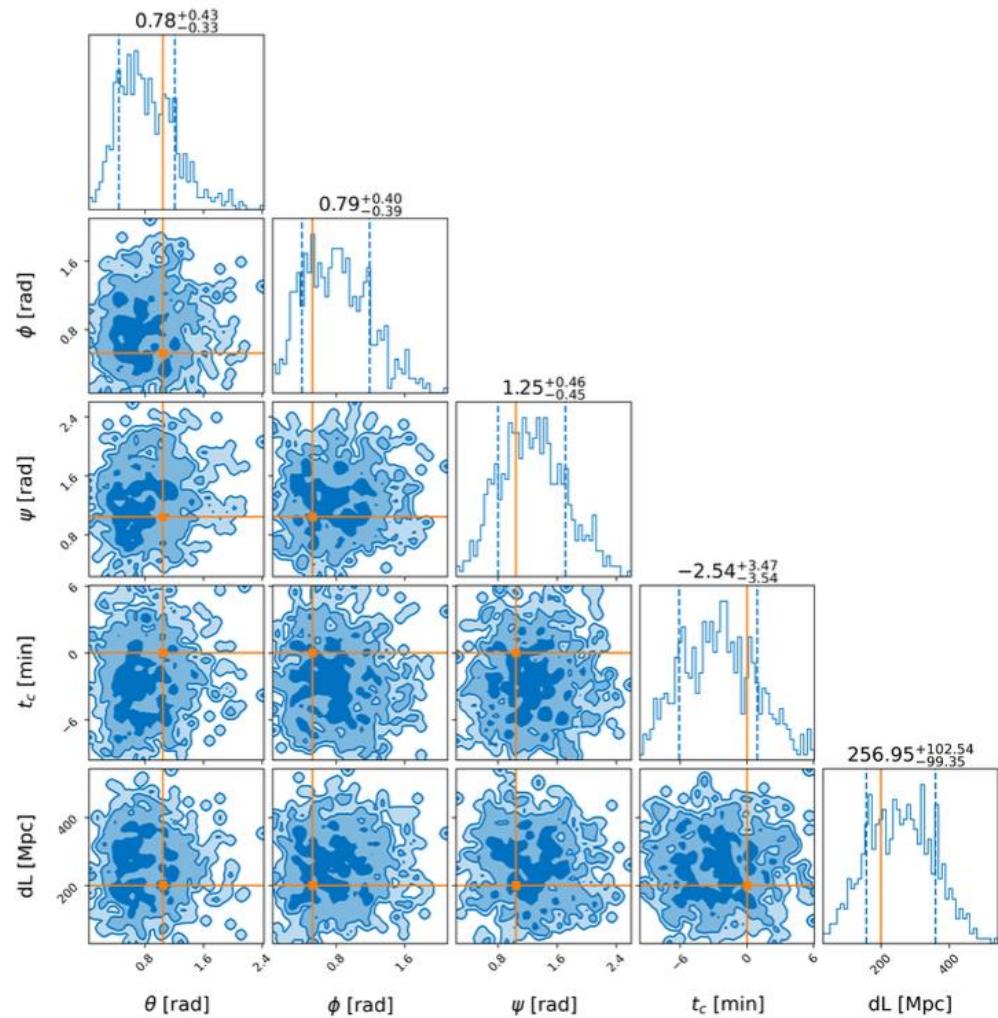
$$\Rightarrow = \{m_\mu, m_{\text{chirp}}, \sqrt{f}, \varphi, \hat{f}, dL\}$$

$$d_j = h_j + n_j$$

Gaussian noise given by PSD: $\sigma_j^2 / \frac{1}{2\Delta f} P_n(f)$

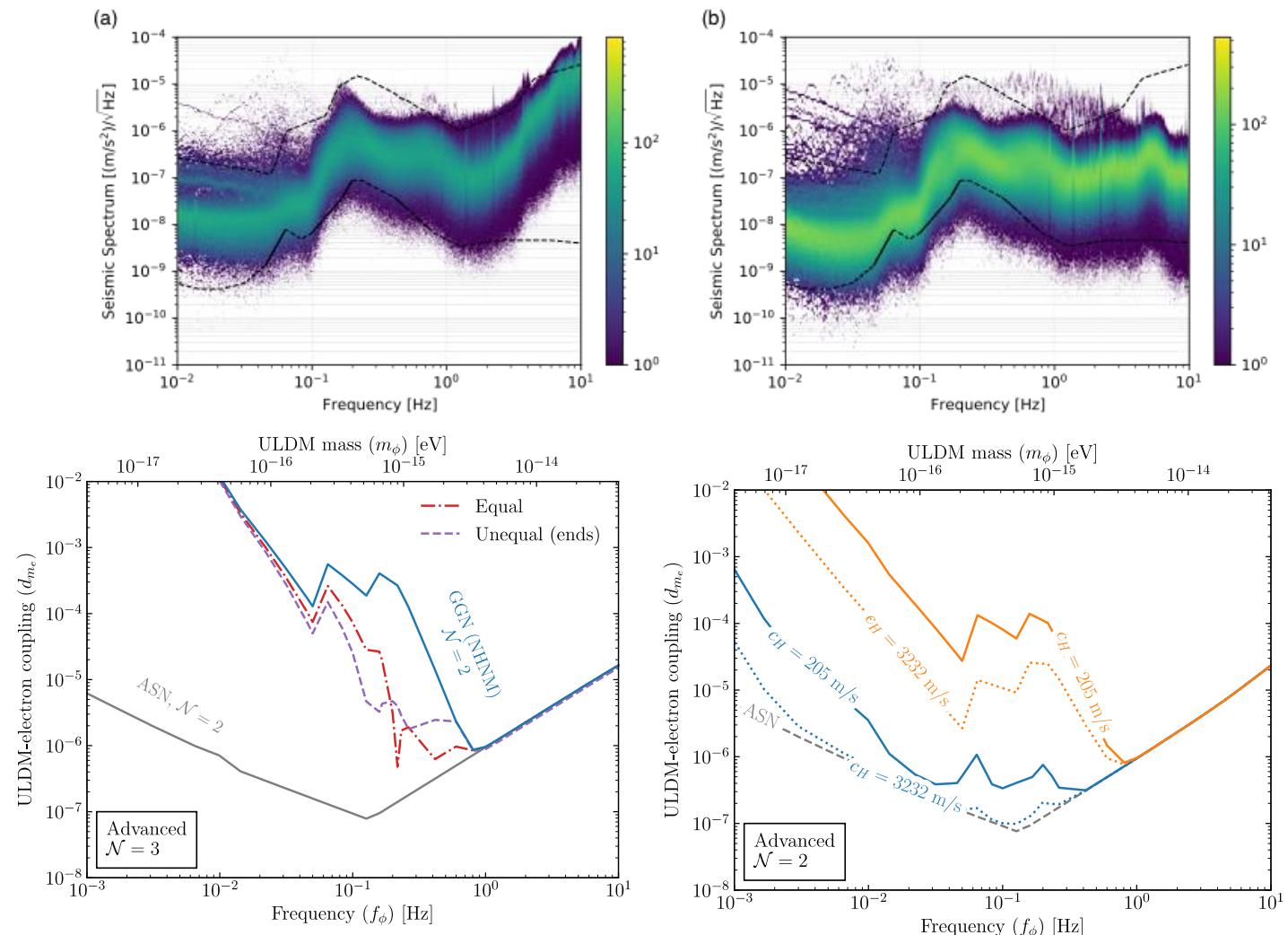
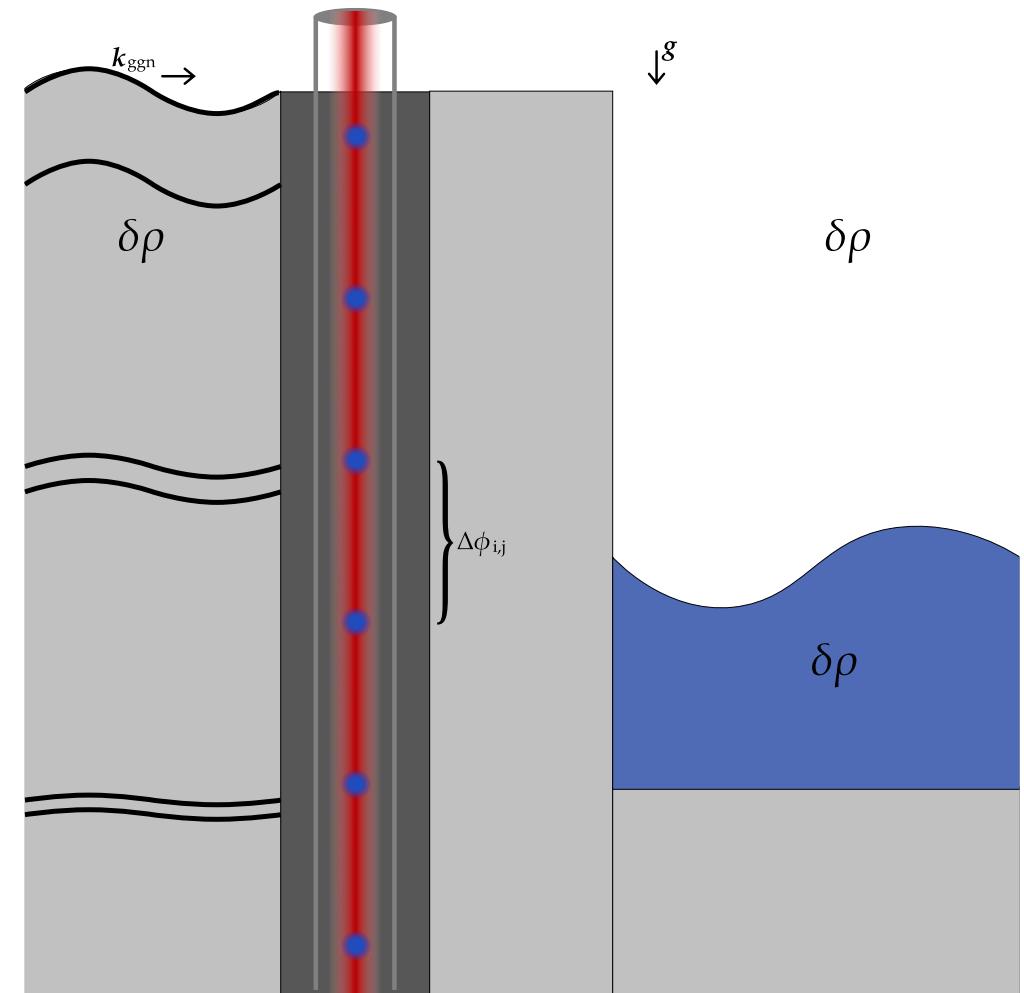
Yu Zhi's work

Bayesian inference for atom interferometry

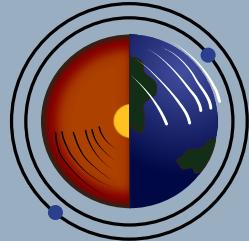


Yu Zhi's work

Environmental noise impacts



Workshops



**Atom Interferometric Sensing
of Earth's Spheres**
27-28 March 2023
Queens' College Cambridge, UK

UNIVERSITY OF CAMBRIDGE MAGIS-100 AION UKRI Natural Environment Research Council

- 27 in-person, 10 remote
- International members of earth science (seismologists, atmospheric, geophysics)
- International members of atom interferometry (AION, MAGIS-100, Hannover)
- UKRI funding representatives from NERC and STFC
- Commercial representative from Güralp
- Tutorials from both sides
- Small group discussions



Summary and outlook

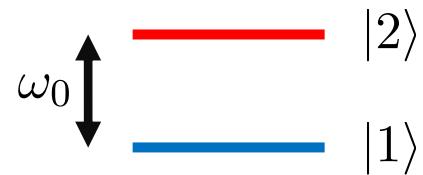
- A lot of work in support of AION and MAGIS-100
- Looking forward to hardware and software contributions
- Simulation work making excellent progress
- Closer integration with Cambridge AMO group

Backups



Atom optics

- Two-level system in electromagnetic field



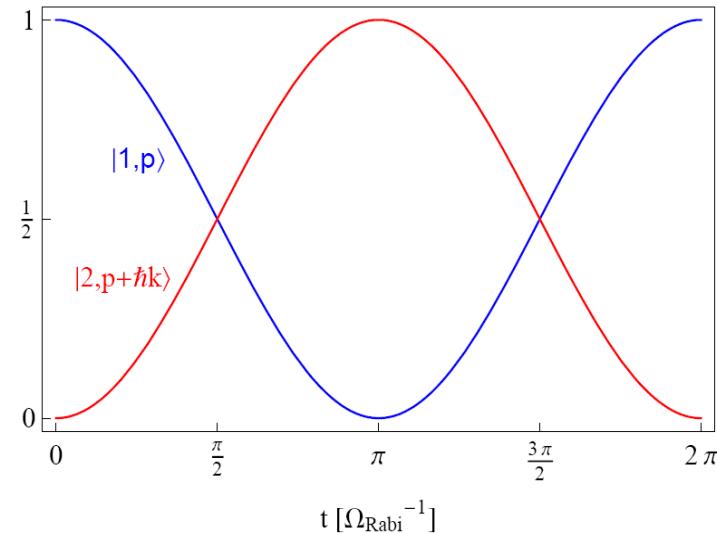
$$|\psi(t)\rangle = c_1(t)|1\rangle + c_2(t)|2\rangle$$

$$c_1(t) = c_1(0) \cos(\Omega t/2) - ie^{-i\phi} c_2(0) \sin(\Omega t/2)$$

$$c_2(t) = -ie^{-i\phi} c_1(0) \sin(\Omega t/2) + c_2(0) \cos(\Omega t/2)$$

$$\|c_1(t)^2\| = \cos^2(\Omega t/2)$$

$$\|c_2(t)^2\| = \sin^2(\Omega t/2)$$



- Beamsplitters, $\pi/2$ -pulse

$$|1\rangle \rightarrow \frac{1}{\sqrt{2}}(|1\rangle - ie^{i\phi}|2\rangle)$$

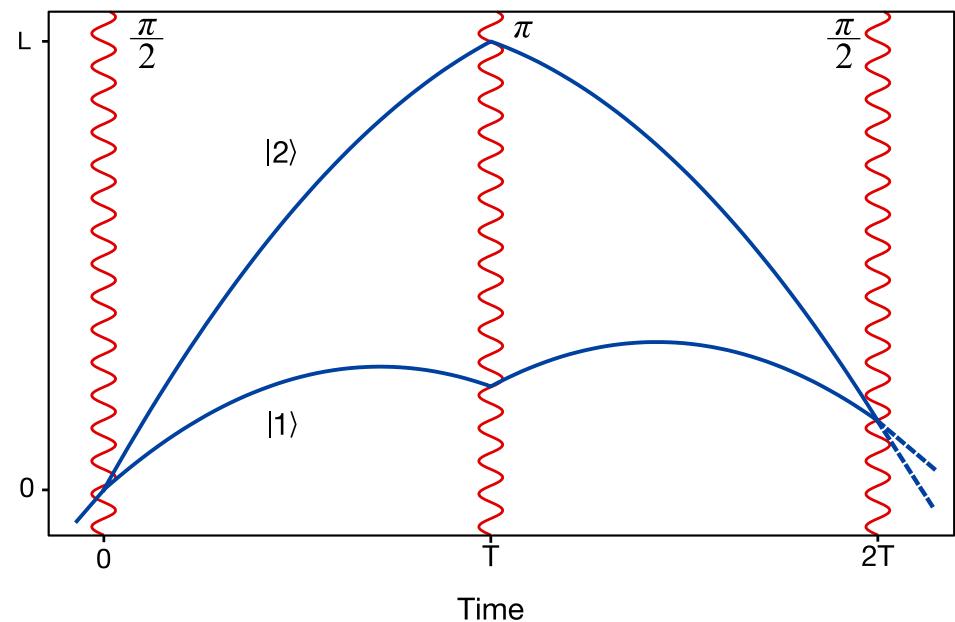
- Mirrors, π -pulse

$$|1\rangle \rightarrow -ie^{i\phi}|2\rangle$$



Atom interferometry

Phase Shift



$$\Delta\phi = \Delta\phi_{\text{laser}} + \Delta\phi_{\text{propagation}} + \Delta\phi_{\text{separation}}$$

$$\Delta\phi_{\text{laser}} = \sum_j^{\text{upper}} \pm\phi_L(t_j, \mathbf{x}_u(t_j)) - \sum_j^{\text{lower}} \pm\phi_L(t_j, \mathbf{x}_l(t_j))$$

$$\Delta\phi_{\text{propagation}} = \sum_{\text{upper}} \left(\int_{t_i}^{t_f} (L_c - E_i) dt \right) - \sum_{\text{lower}} \left(\int_{t_i}^{t_f} (L_c - E_i) dt \right)$$

$$\Delta\phi_{\text{separation}} = \langle \mathbf{p} \rangle \cdot \Delta \mathbf{x}$$

Leading order phase shift

$$\Delta\phi = kgT^2$$



