

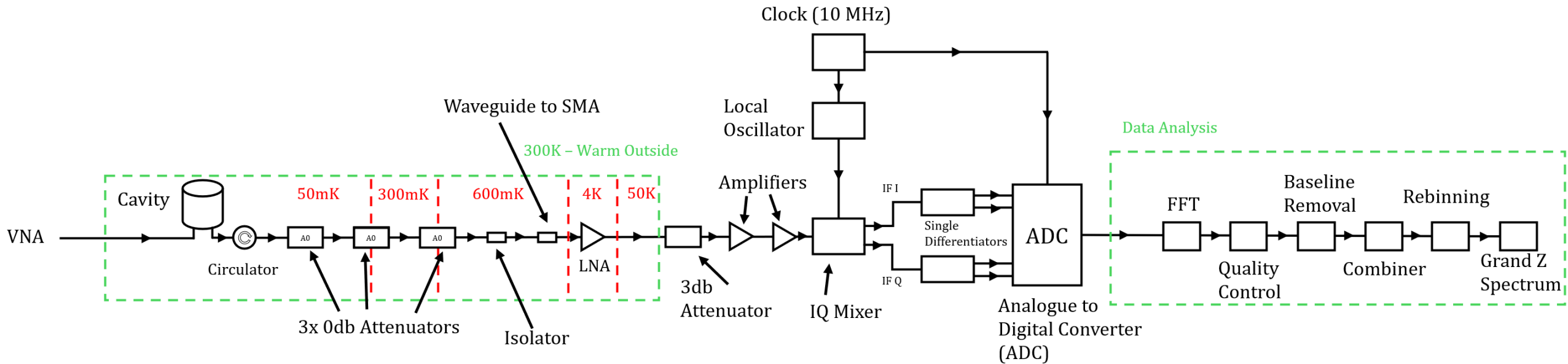
# Simulating Axioms

Blue Carn

# Context

- To make a more accurate simulation, need to start from the beginning of the pipeline
- This means working in time domain rather than frequency domain
- We can then simulate the individual components of the RF chain
- Then FFT from time domain into the frequency domain, ready to be integrated into the data analysis

# Experiment Pipeline



# Noise

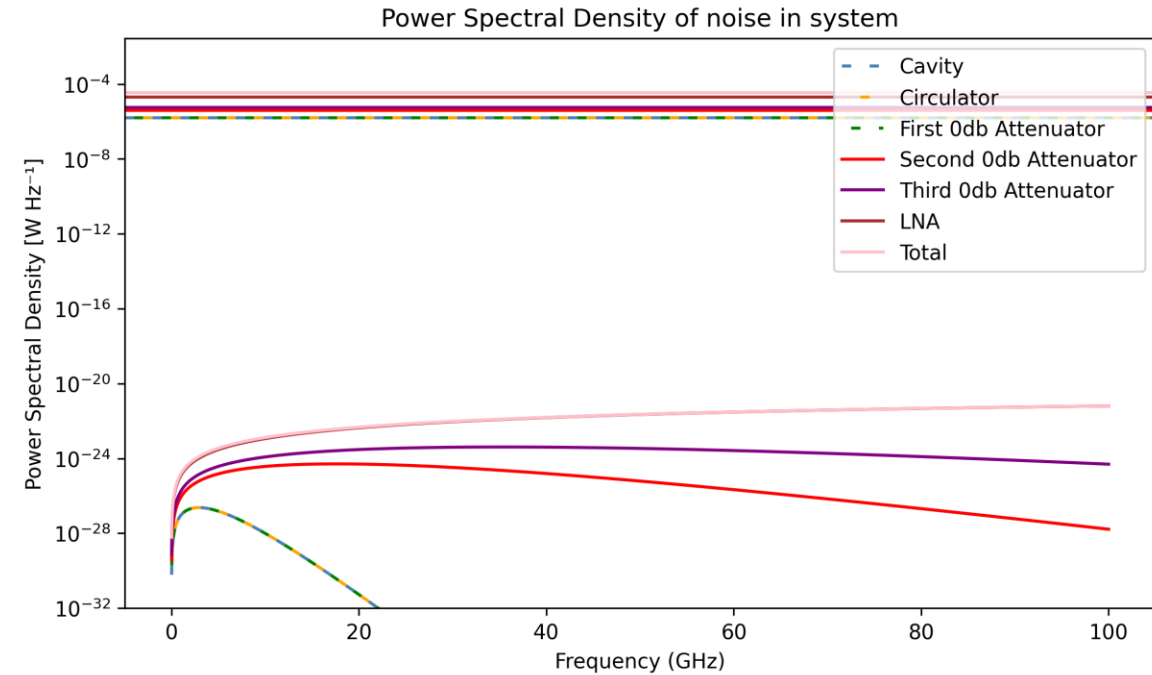
- We consider 2 types of noise
- Blackbody Radiation
  - Simulated in frequency domain

$$B_\nu(T) = \frac{2h\nu^3}{c^2 \left( e^{\frac{h\nu}{kT}} - 1 \right)}$$

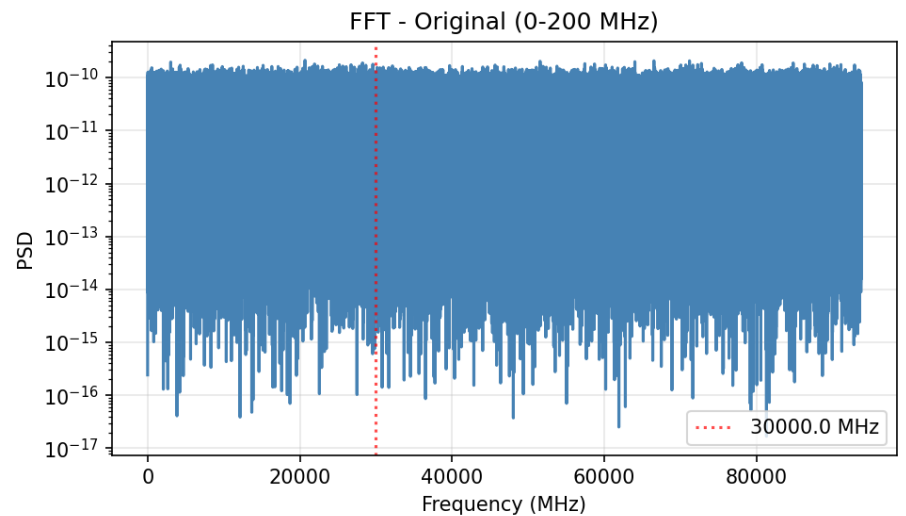
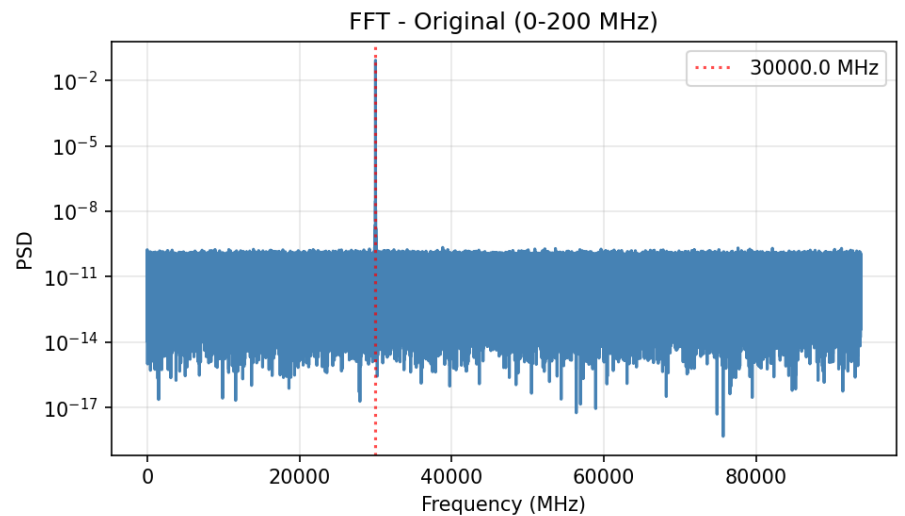
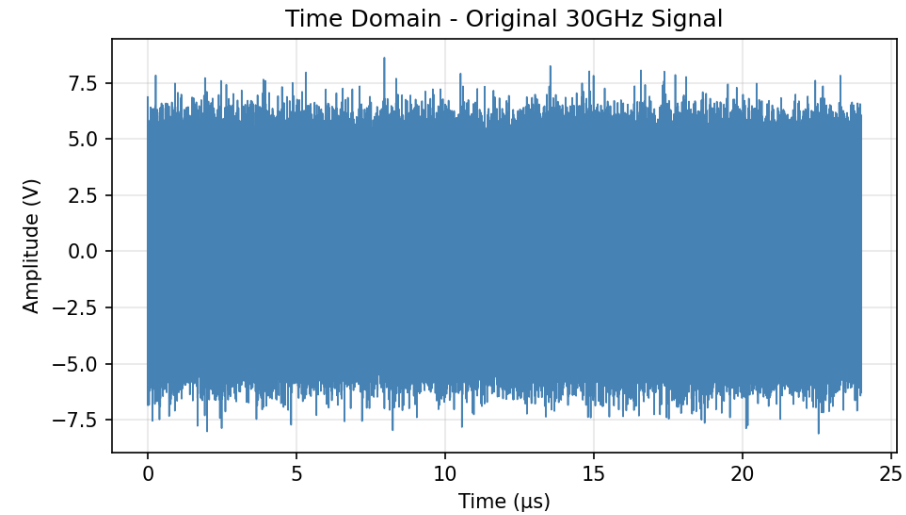
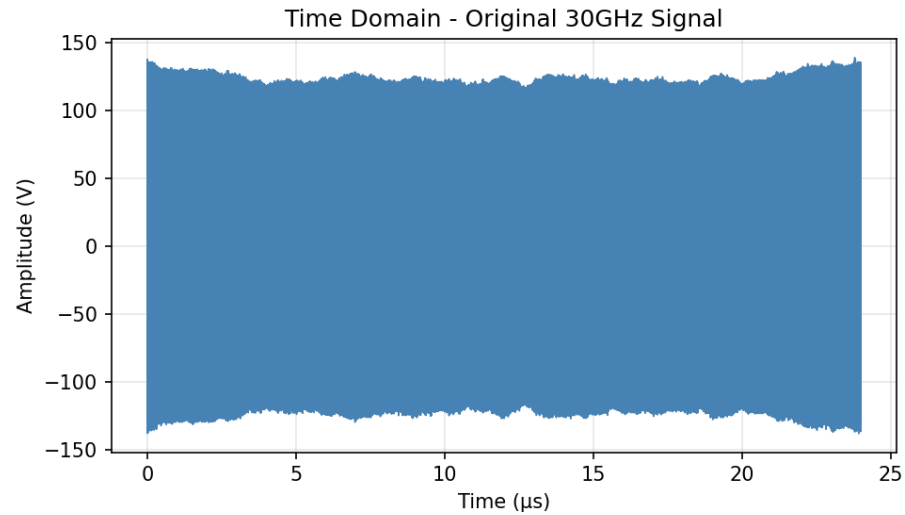
- Johnson-Nyquist Noise
  - Simulated in time domain
  - $V_{rms} = \sqrt{4kTZB}$ 
    - $Z = 50\Omega$  – impedance
    - $B$  – bandwidth of component
      - Bandwidths can be found on datasheets of components
      - Widest is LNA at 23-42 GHz, so  $B = 19\text{GHz}$  for LNA
  - Generate random number within a normal distribution with  $\sigma = V_{rms}$

# Noise

- Simulating components from within the cryostat
- Top part represents rms from Johnson-Nyquist noise
- Bottom half represents blackbody noise
- Johnson-Nyquist Noise dominates, mainly from the LNA

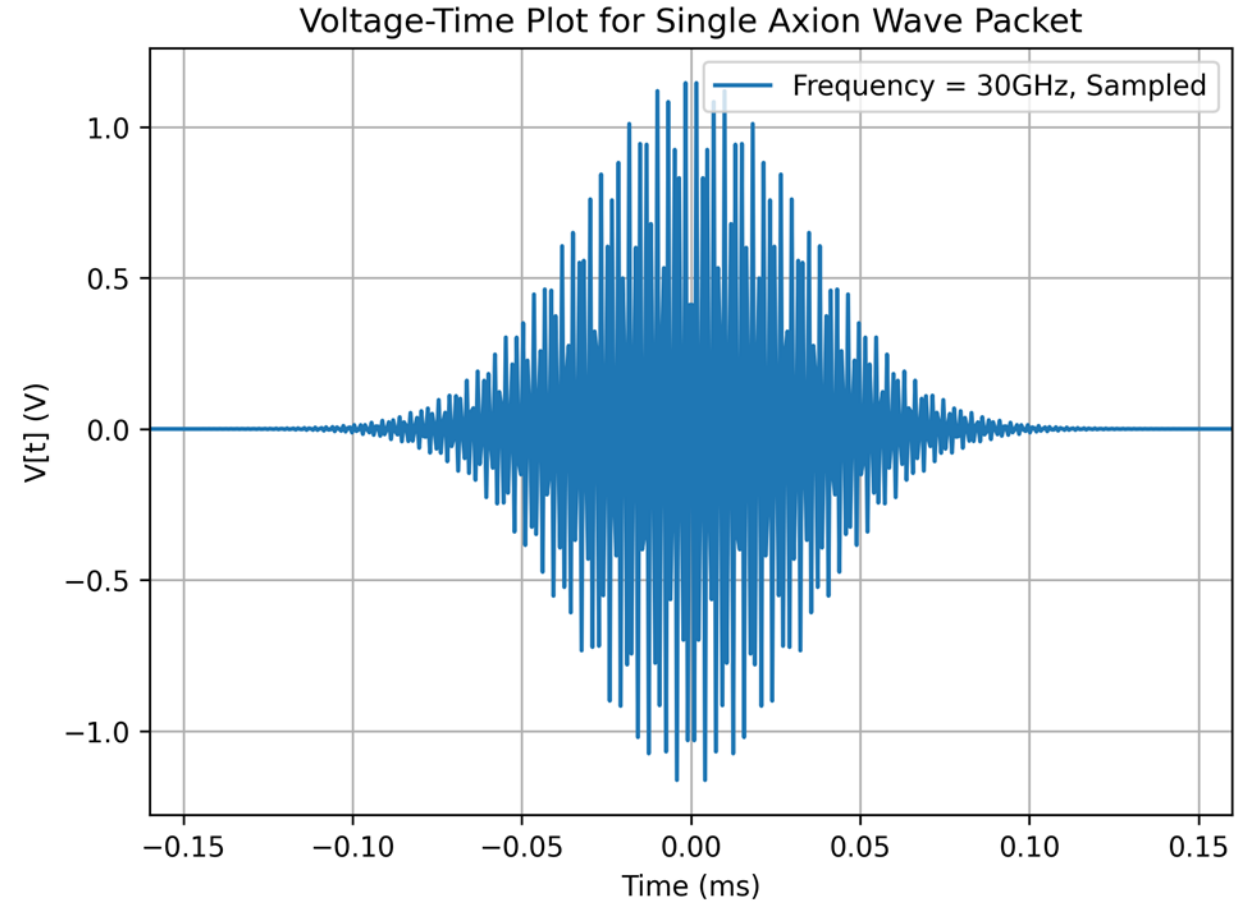


# Noise + Large Signal vs Pure Noise



# Signal - wave packets

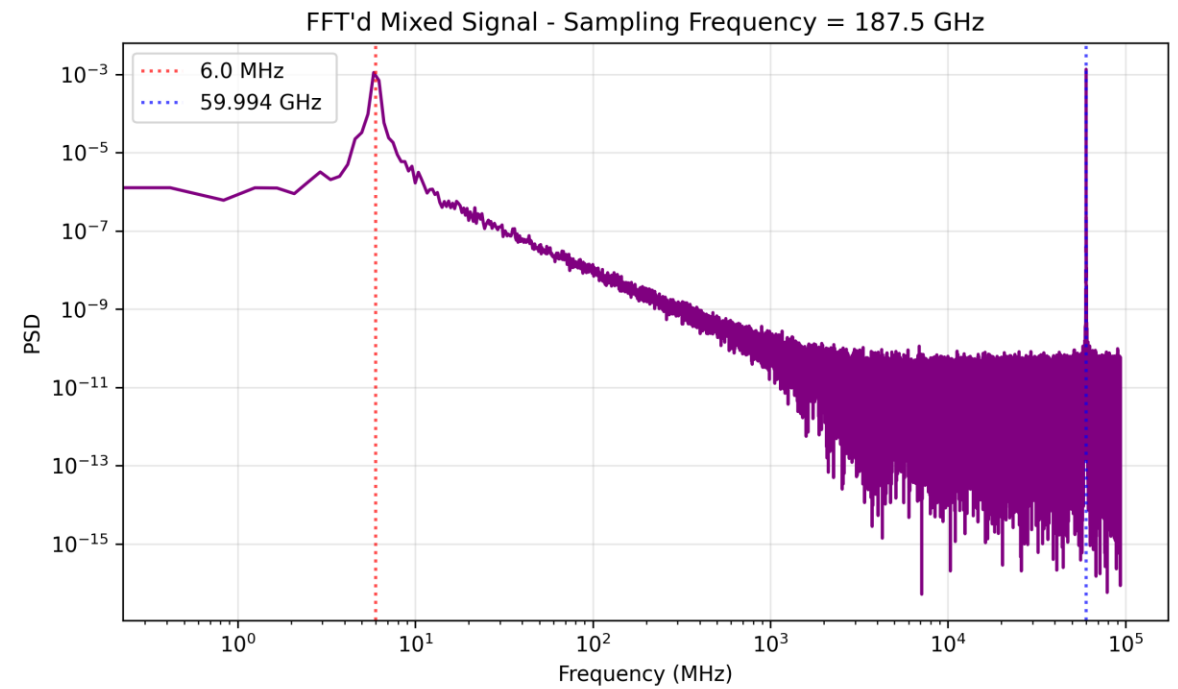
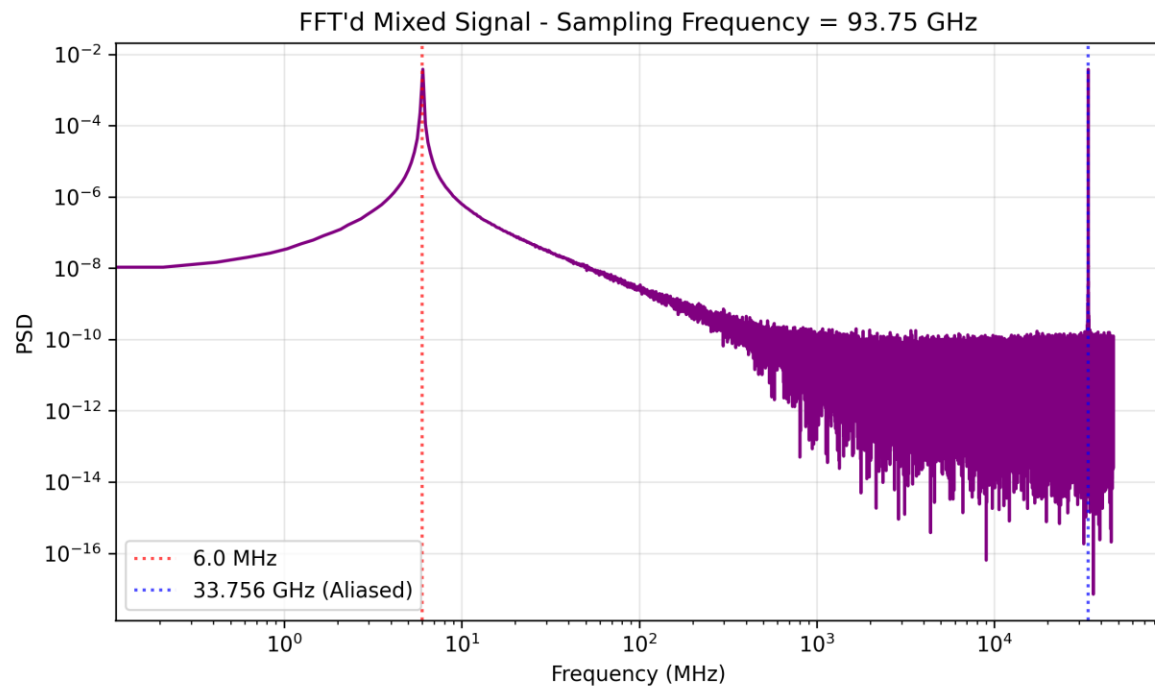
- Complex sinusoidal wave mixed with a gaussian envelope
- Occur with a random amplitude and phase at a random time
- Example of a singular wave packet (pre-sampled)



# Pre-sampling

- Due to python limitations, all functions are discretised
- For our signal of 30GHz, we can choose the rate it is “pre-sampled”
- Sampling frequency for this pre-sampling must be higher than Nyquist limit otherwise aliasing occurs
- Pre-Sampling is currently set to 6.25 samples per period, which is a sampling frequency of 187.5GHz.
  - Note this is carried over to the final wave of 6MHz, meaning that wave is sampled 31250 times per period – a lot of data for just a 6MHz wave.

# Example of Aliasing



# What is downmixing?

- Process of converting a high frequency ( $f_{RF}$ ) signal to a low frequency ( $f_{out}$ ) signal whilst preserving the data
- This is done by injecting a very similar signal with frequency:
$$f_{LO} = f_{RF} - f_{out}$$
- E.g., if we want to downmix a 30GHz signal to 6MHz,  $f_{LO} = 29.99$  GHz
- But what actually is downmixing?

# The maths of downmixing

- Let's assume our RF signal has a function:

$$x_{RF} = A \cos(2\pi * 30\text{GHz} * t)$$

- And our Local Oscillator signal has a function:

$$x_{LO} = B \cos(2\pi * 29.994\text{GHz} * t)$$

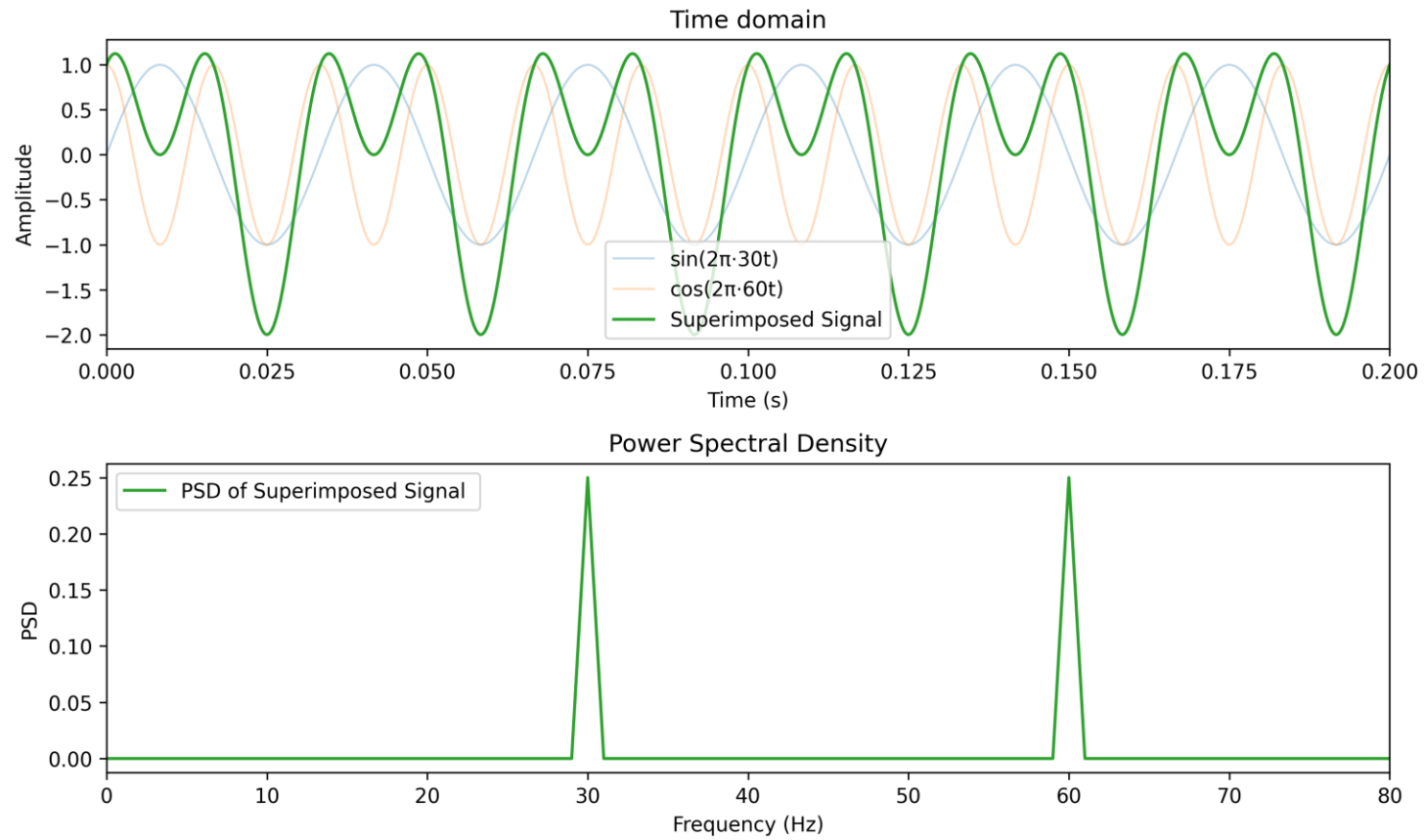
- A mixer multiplies them, and using the trigonometric identity:

$$\cos a \cos b = \frac{1}{2} [\cos(a - b) + \cos(a + b)]$$

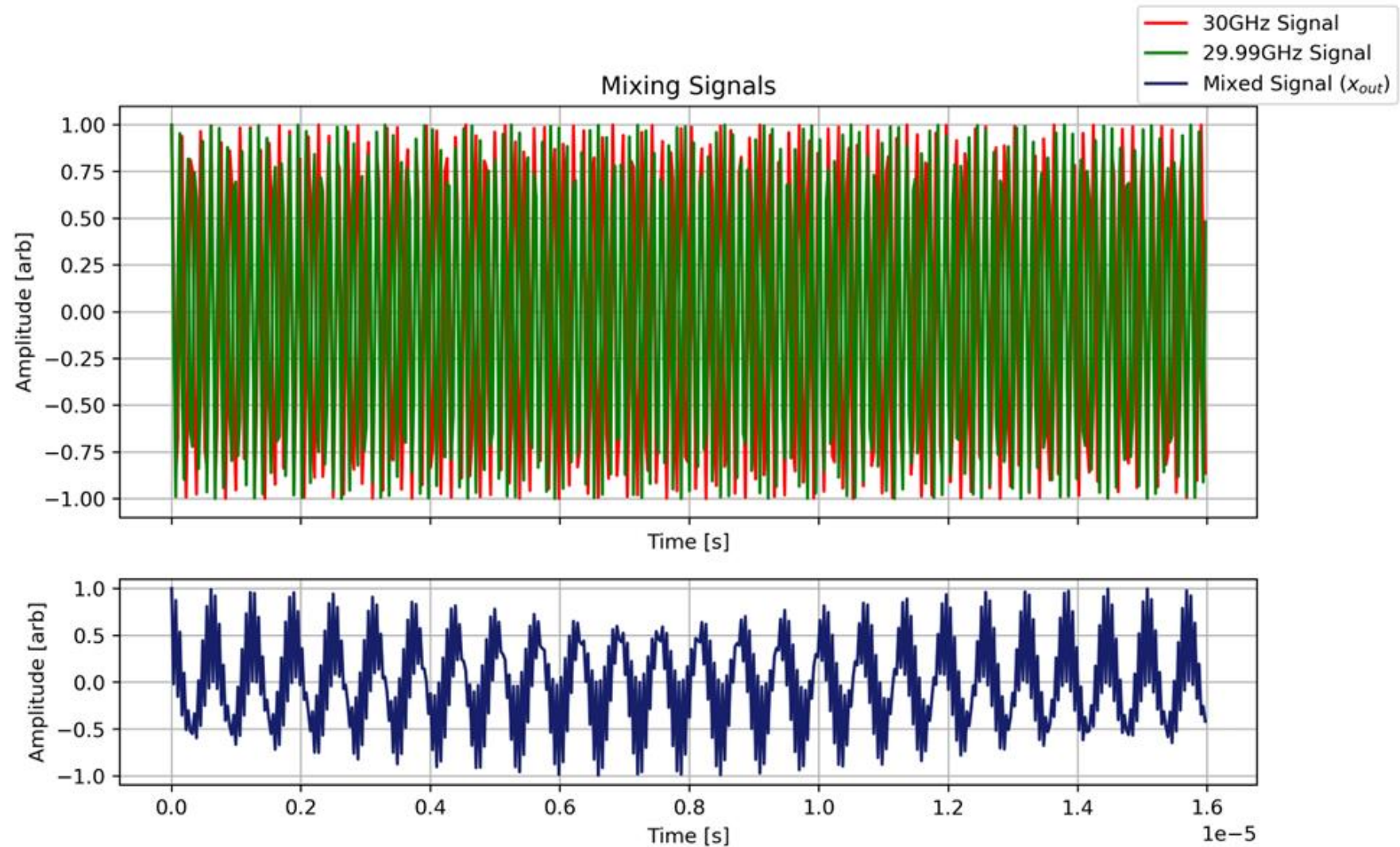
- We get:

$$x_{out} = \frac{AB}{2} [\cos(2\pi * 0.006\text{GHz} * t) + \cos(2\pi * 59.994\text{GHz} * t)]$$

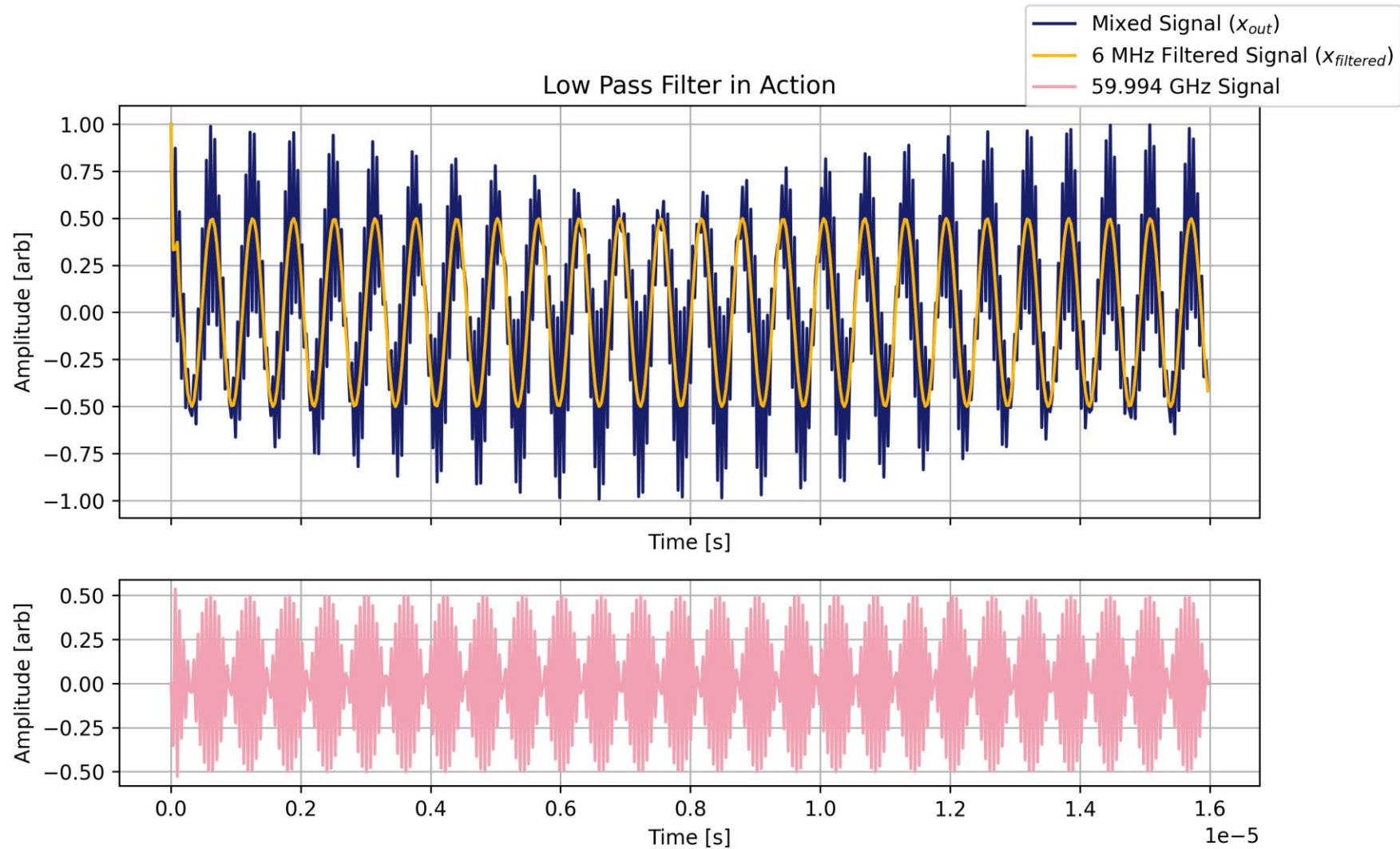
# Basic Example



# Using our simulation



# Using our simulation



# The maths of downmixing (con't)

- Dark Blue signal:

$$x_{out} = \frac{AB}{2} [\cos(2\pi * 0.006\text{GHz} * t) + \cos(2\pi * 59.994\text{GHz} * t)]$$

- We then apply a low pass filter to cut off the summed frequency, leaving us with:

$$x_{filtered} = \frac{AB}{2} \cos(2\pi * 0.006\text{GHz} * t)$$

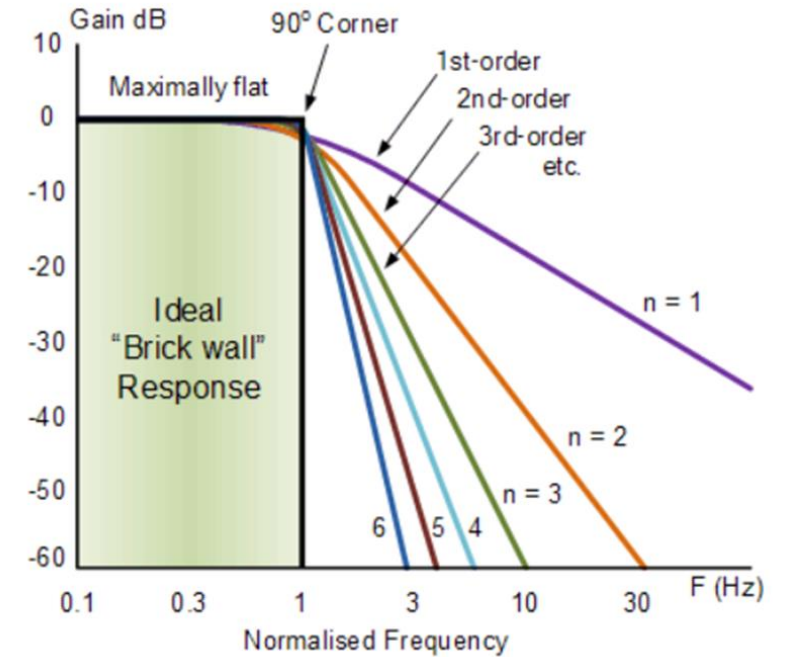
# Why do we downmix?

- To directly sample GHz signals
  - Incredibly high sampling rate is needed
  - Enormous data storage
  - Excessive computational power
- Hardware Limitations
  - At higher frequencies, hardware becomes expensive and difficult to build
  - At lower frequencies, hardware is cheap and high quality

# Filters

- Reduce signal after a given frequency
- Butterworth filter is the most common type
- For a “perfect” filter,  $n$  tend to infinity

Ideal Frequency Response for a Butterworth

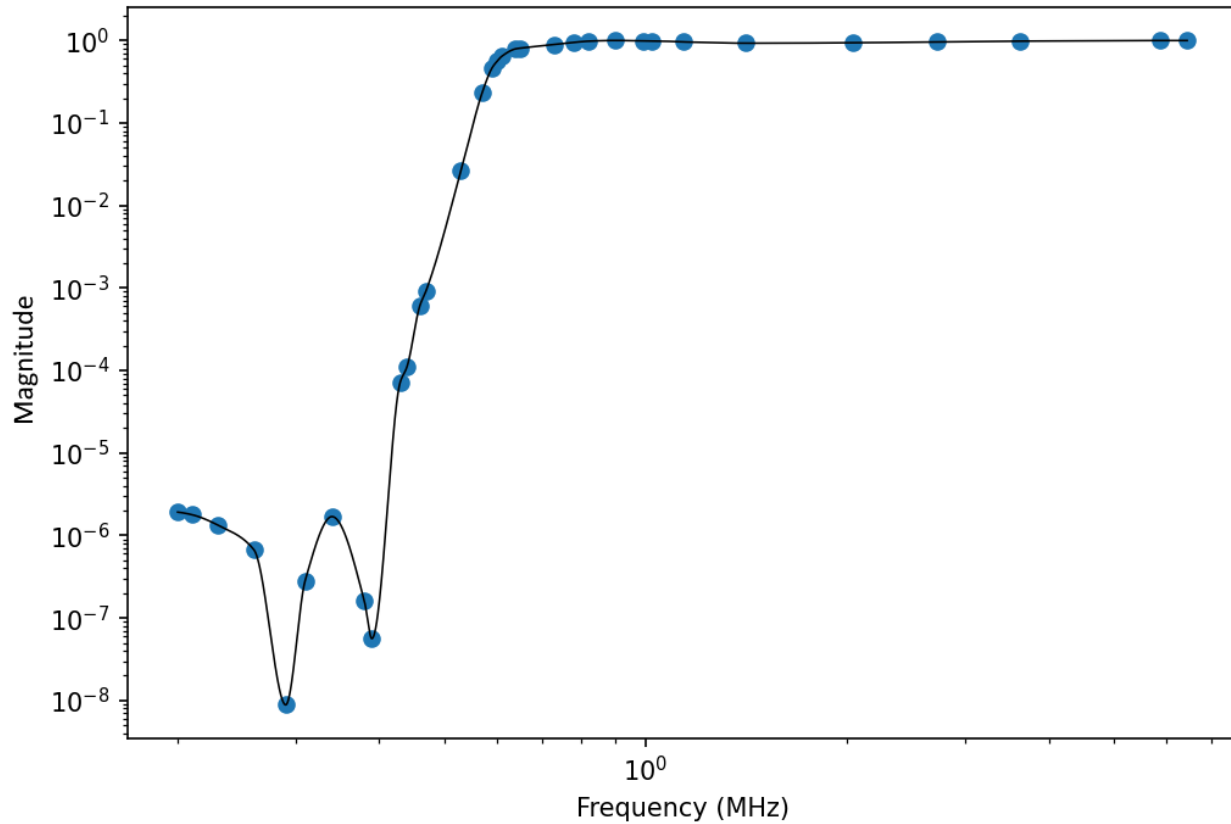


# Types of filter

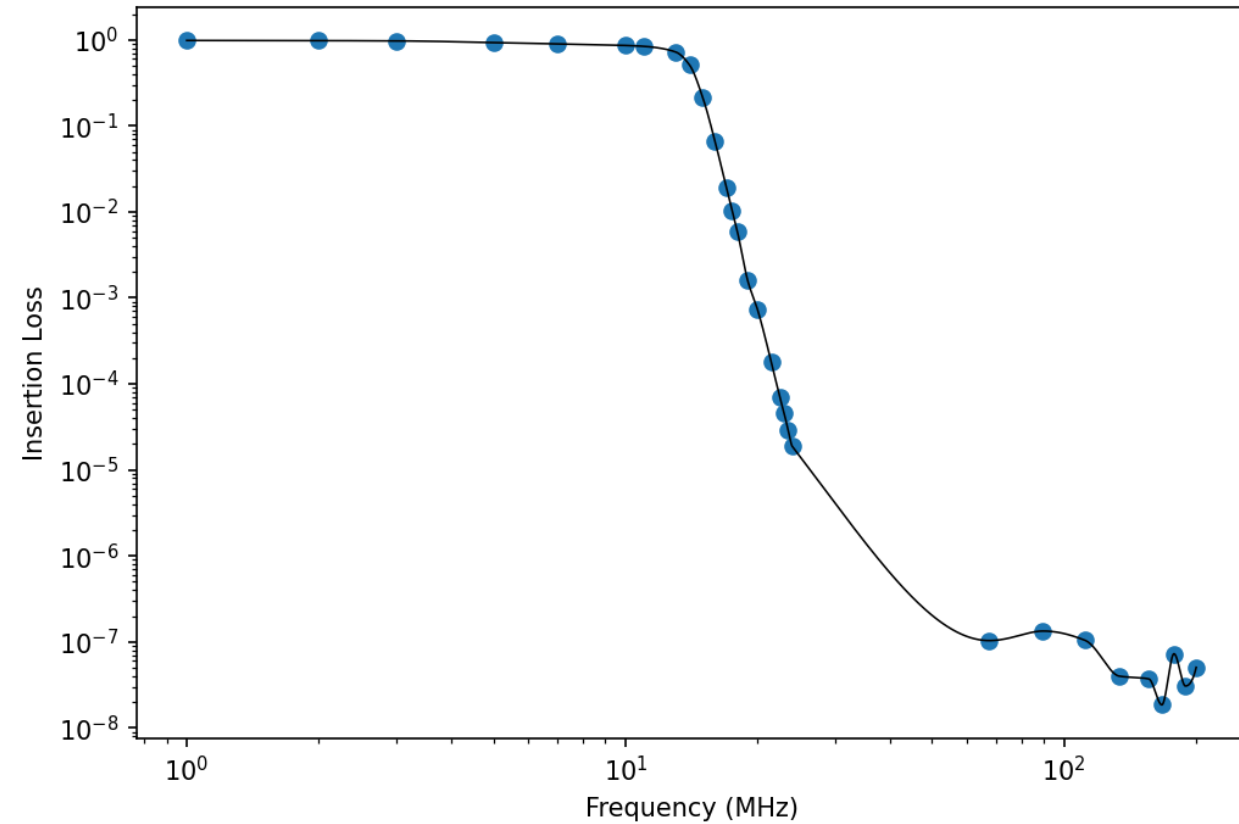
- Low pass filter
  - Cuts off unwanted high frequencies from mixing (that 59.994GHz component)
- Low pass filter
  - Cuts off unwanted low frequencies from the mains and radio sources

# Our filters (from datasheet)

High Pass Filter



Low Pass Filter



# Signal Scaling

Power Scaling of the signal in accordance to the formula:

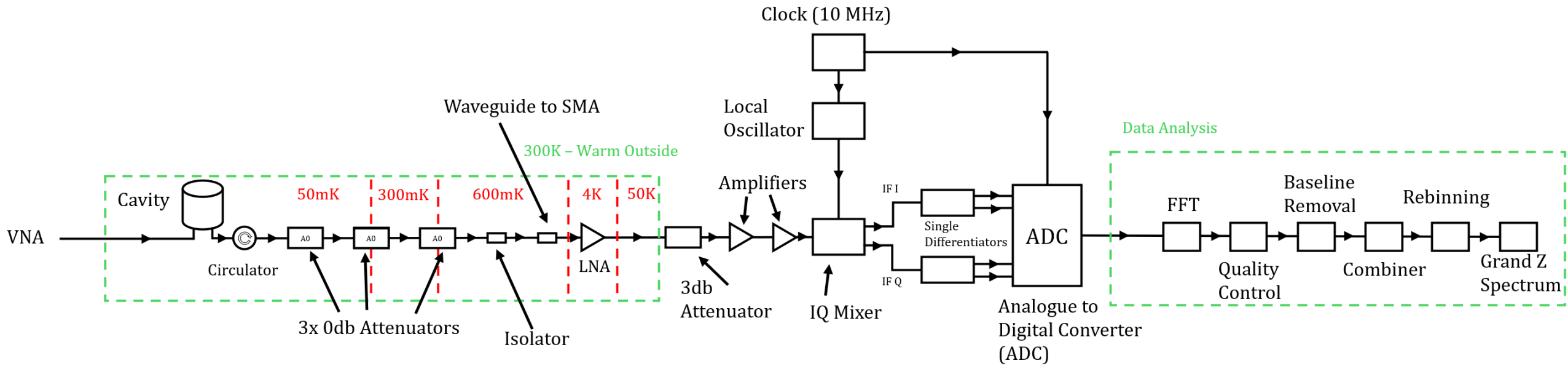
$$P_{\text{sig}} = 1.79 \times 10^{-21} \left( \frac{V}{200} \right) \left( \frac{B}{7.6} \right)^2 C \left( \frac{g_y}{0.97} \right)^2 \left( \frac{\rho_a}{0.45} \right) \left( \frac{\nu_a}{750 \times 10^6} \right) \left( \frac{Q}{70000} \right)$$

- Parameters on the left
- Scaling from Amplifiers = 98dB

Parameter	Symbol	Value
Cavity volume	$V$	0.005383 L
Magnetic field	$B$	3 T
Form factor	$C$	0.69
Axion coupling (CAST benchmark)	$g_{a\gamma\gamma}^{\text{CAST}}$	$4 \times 10^{-10}$
Axion coupling (KSVZ benchmark)	$g_{a\gamma\gamma}^{\text{KSVZ}}$	$4.9 \times 10^{-14}$
Local axion density	$\rho_a$	$0.45 \text{ GeV cm}^{-3}$
Axion frequency	$\nu_a$	30 GHz
Quality factor	$Q$	2000
Impedance	$Z$	$50 \Omega$
Integration time	$t_{\text{int}}$	1.6 ms
Sampling frequency	$f_s$	62.5 MHz
Nyquist frequency	$f_{\text{Nyq}}$	31.25 MHz
Intermediate frequency after mixing	$f_{\text{IF}}$	6 MHz
Total amplifier gain	$G_{\text{tot}}$	98 dB

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# Experiment Pipeline

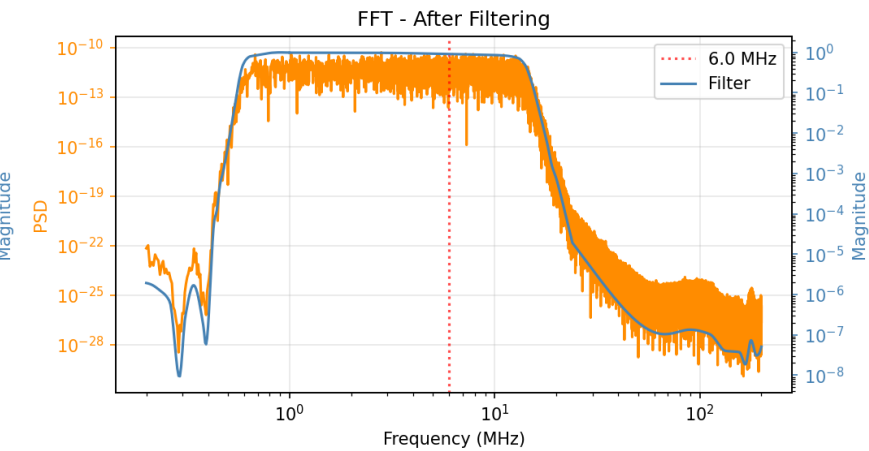
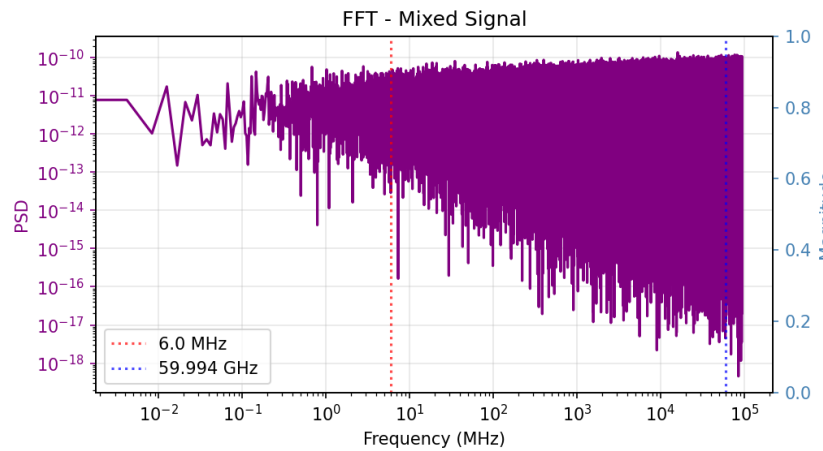
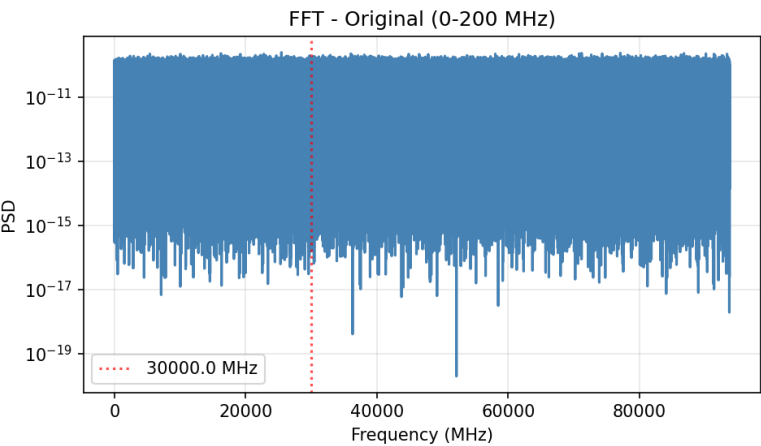
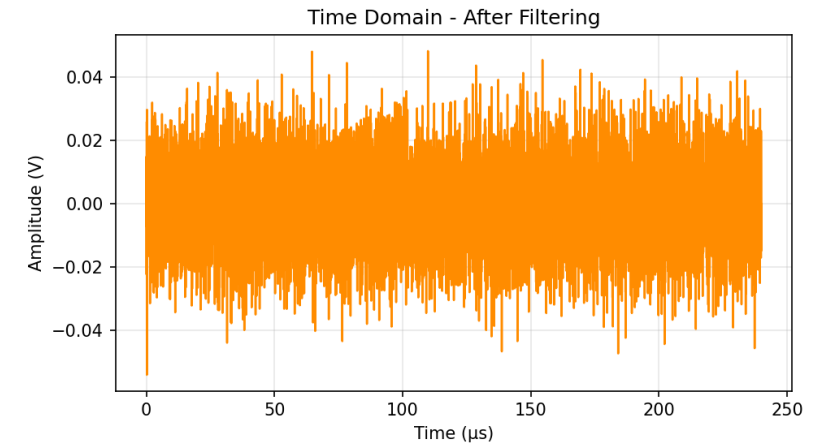
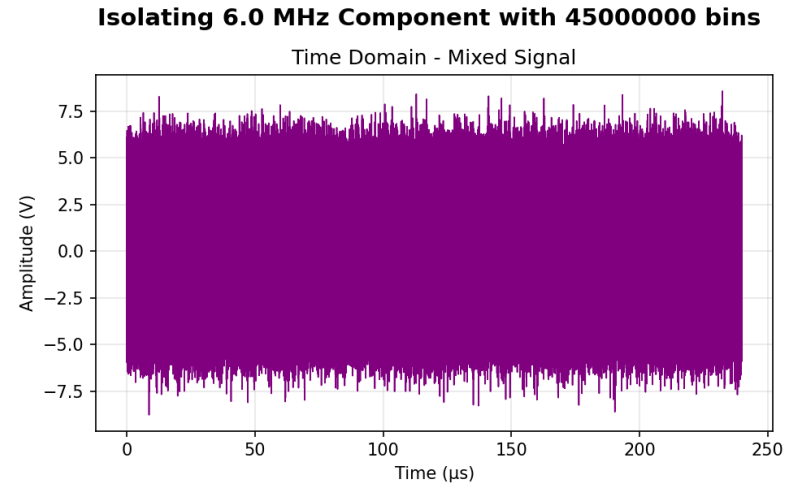
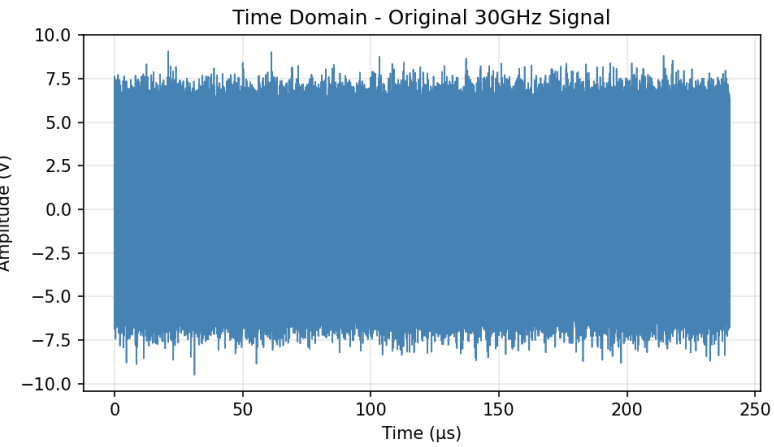


# Voltage Graphs

Raw Signal  
(Wave packets + Noise)

Raw Signal Mixed with  
Local Oscillator

Mixed Signal passed through  
Filters



# Next Steps

- I need to pass my MPhys interview
- Need to integrate this simulation with the rest of the data analysis
- Need to optimise the code
  - For the full 1.6ms integration time we currently are aiming for, this generates many GBs of data, which takes a long time to generate and manipulate