

# Taylor-Spruit dynamo, low-field magnetars and central compact objects

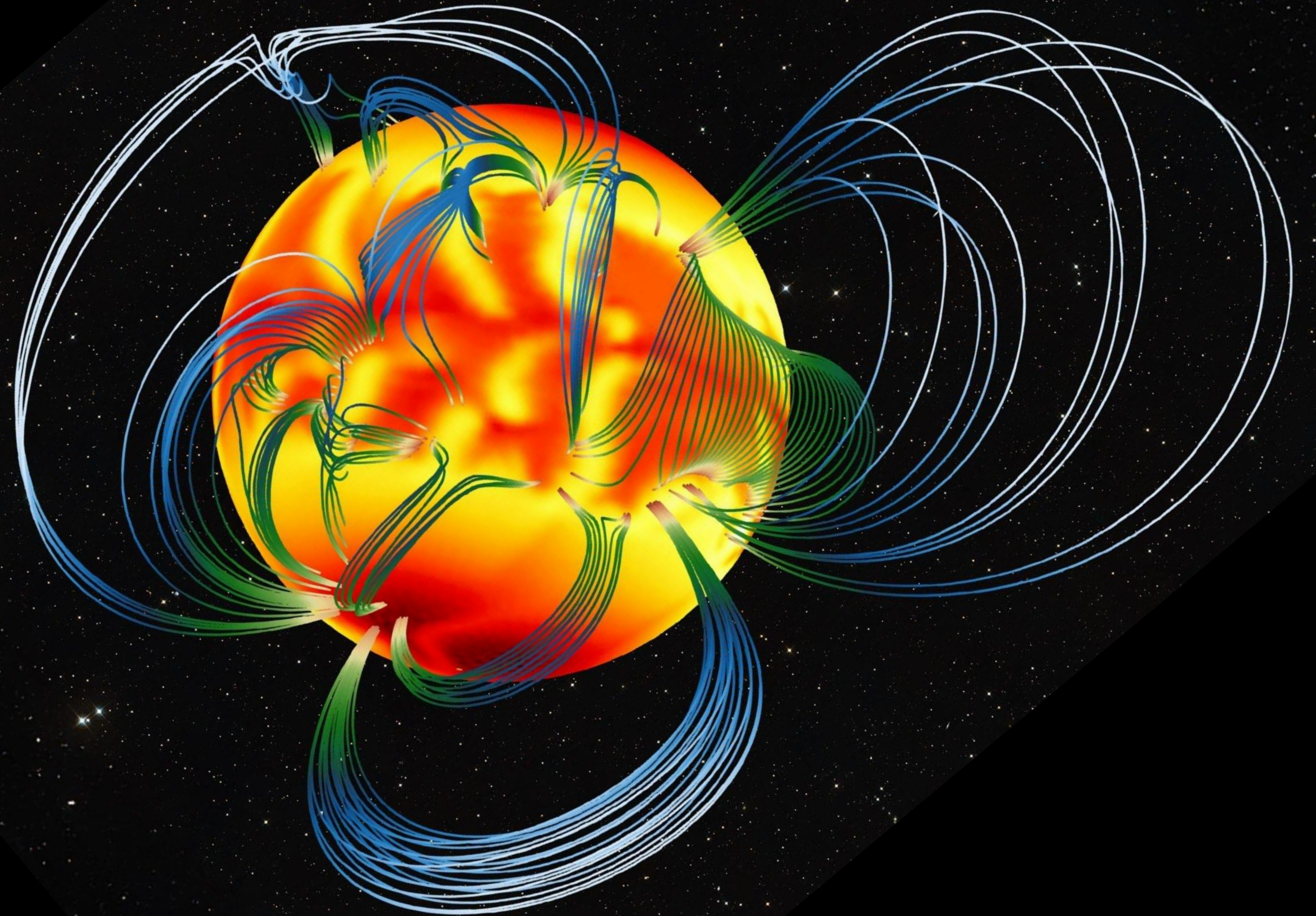
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Nicolas Moraga



THE ROYAL SOCIETY



24/06/2026

# Research group at Newcastle University, UK

## Superconductivity in neutron star cores

Main objective: to model magnetic field evolution in superconducting neutron stars cores

Recent side project: hydrodynamic model for pulsar glitches



Dr Nicolas Moraga



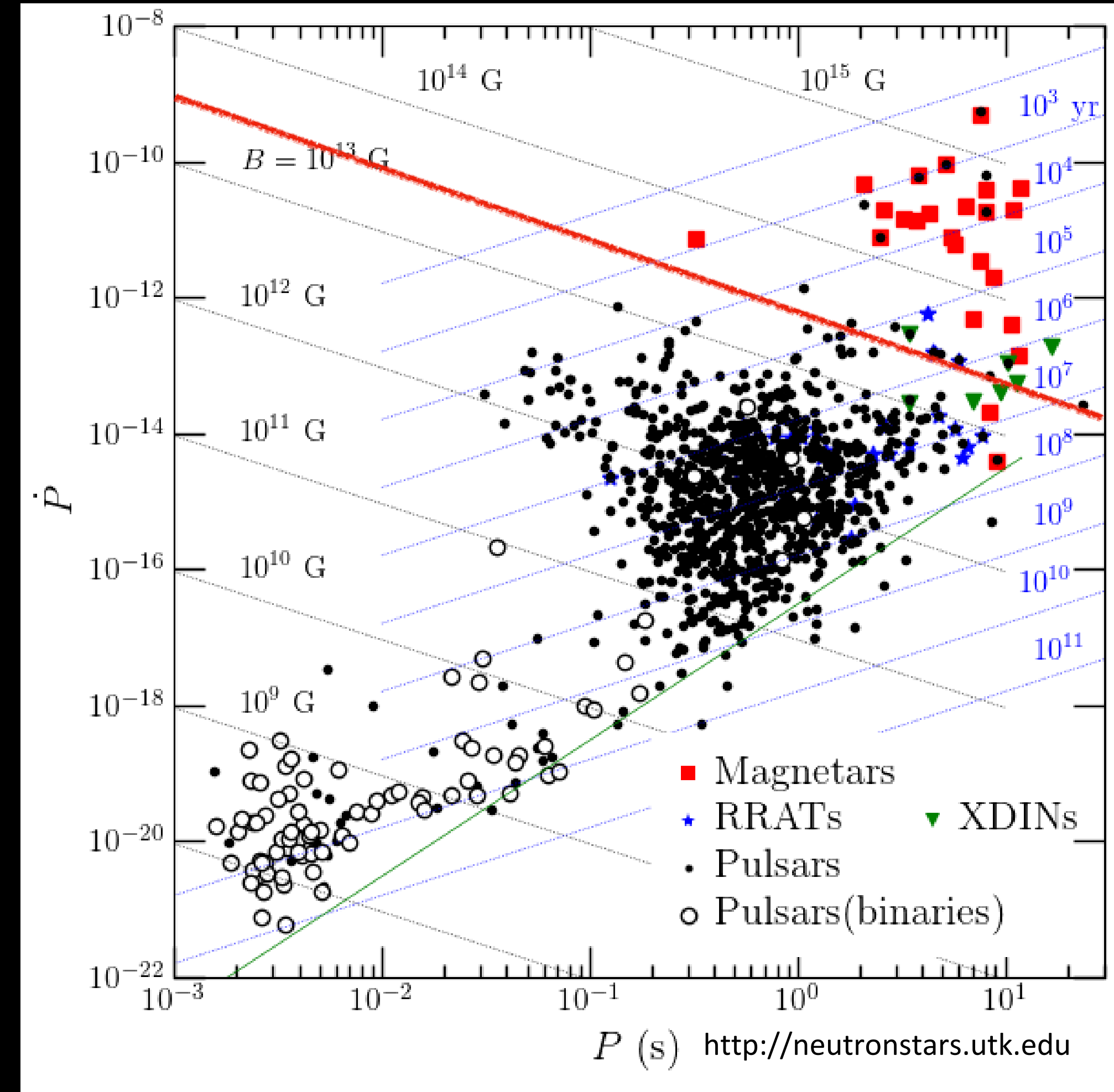
Charlie Perkins

Thursday 17:30

# Neutron stars & their magnetic fields

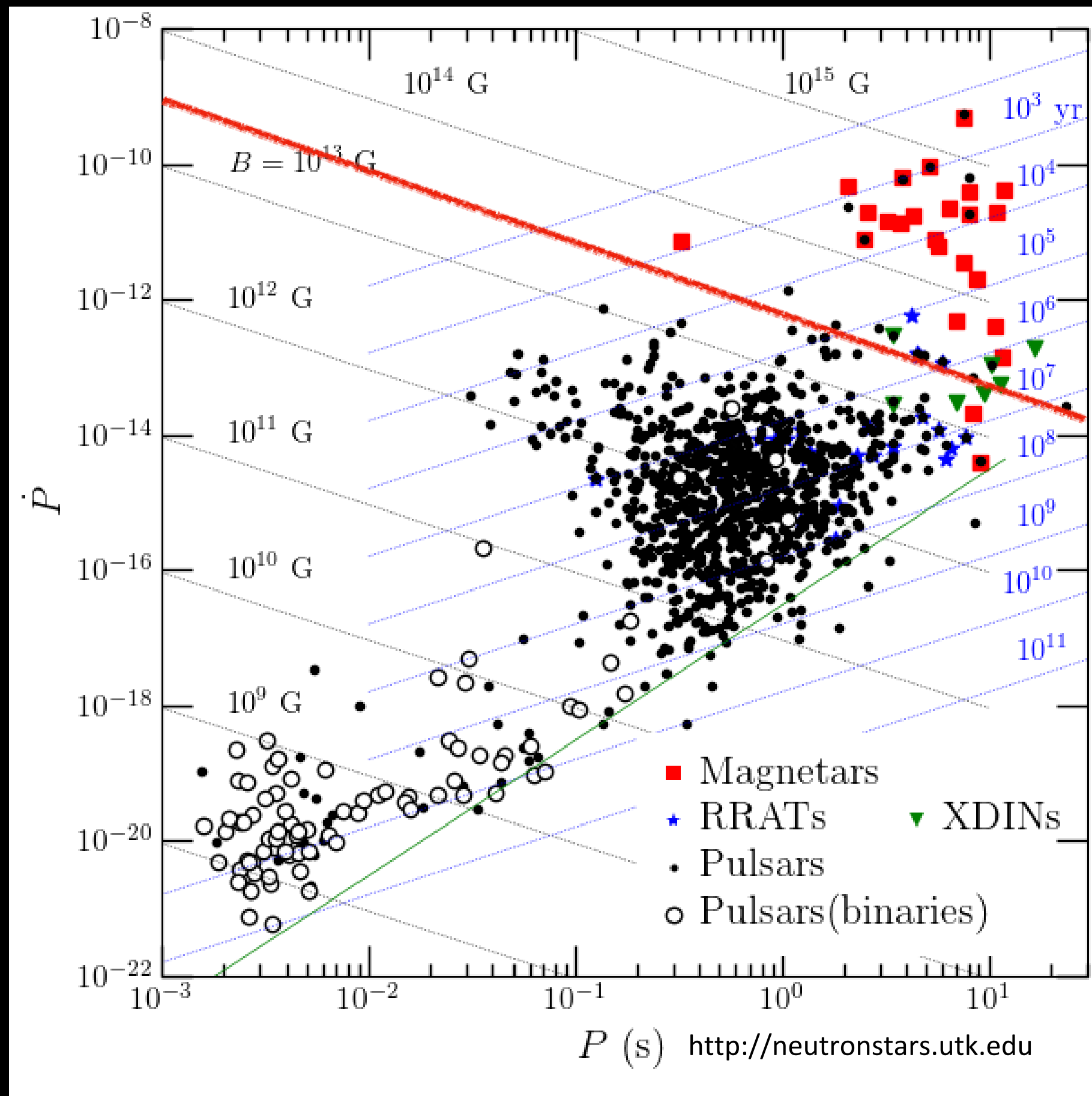
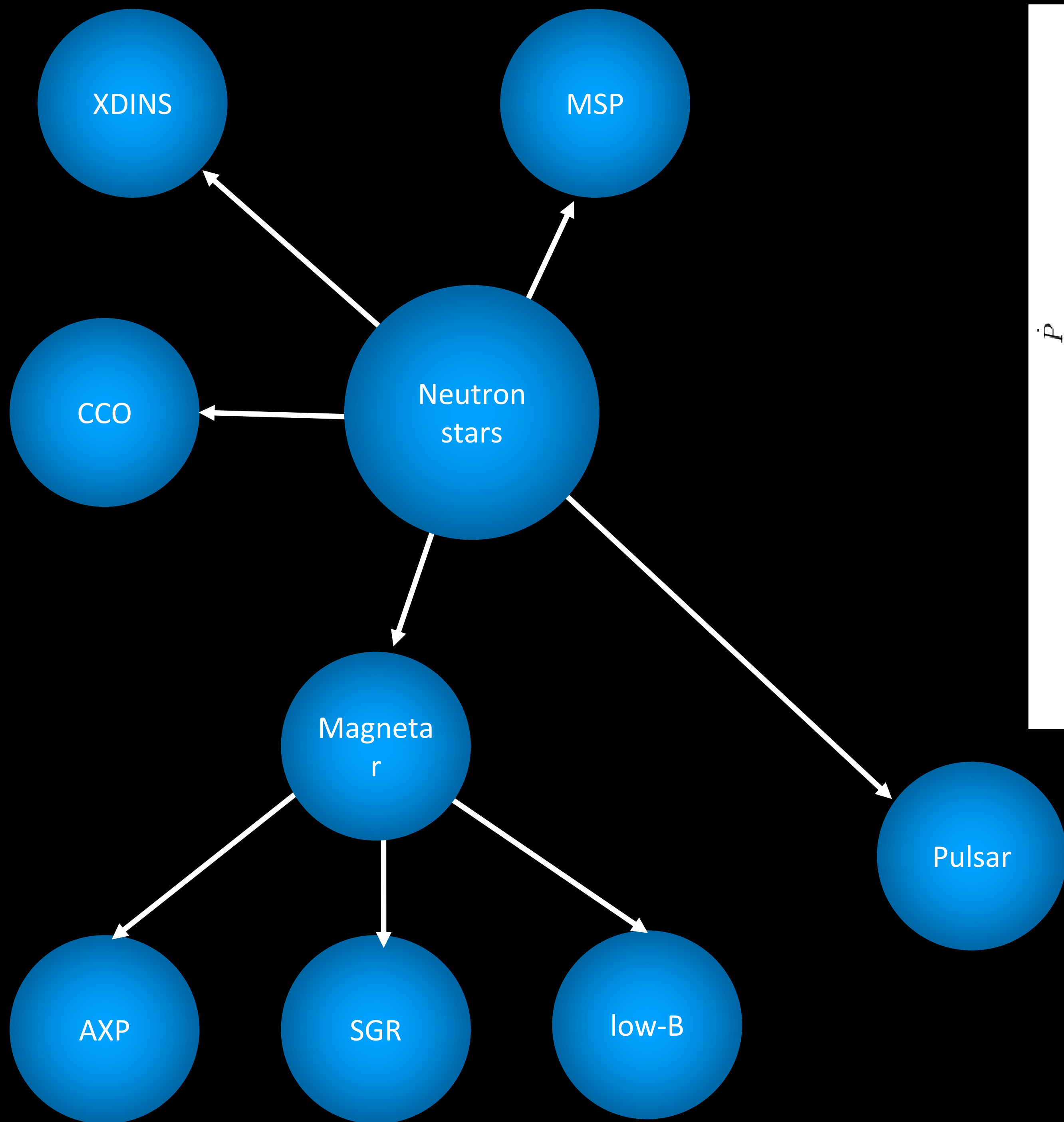
- Neutron stars (NSs) are compact ( $\sim 10$  km) remnants of the stellar evolution. A mass of NS is  $\approx 1.4M_{\odot}$ . NSs have extreme magnetic fields ( $10^8 - 10^{14}$  G).
- Main observational characteristics for neutron stars are their period and period derivatives.
- $P$  and  $\dot{P}$  indicate poloidal, dipolar magnetic field strength  $B_p$

$$B \propto \sqrt{P\dot{P}}$$



Review on magnetic field evolution: Igoshev, Popov & Hollerbach (2021)

Review on techniques: Pons, Dehman & Viganò (2026)



**NS zoo,  
Harding (2013);  
Borghese (2024)**

# Magnetars

Two classes of neutron stars: **Anomalous X-ray Pulsars** (AXP) and **Soft Gamma Repeaters** (SGR) are combined as magnetars.

**Anomalous X-ray pulsars** emit thermal X-ray modulating with rotational phase. No obvious sources of accretions are detected: AXPs are isolated.

**Soft Gamma Repeaters** emit large burst of X-rays and gamma rays episodically. Large emission episodes show modulation with a period of a NS.

**Low-B magnetars** have burst and outbursts but their dipolar magnetic fields are weaker than  $4 \times 10^{13}$  G

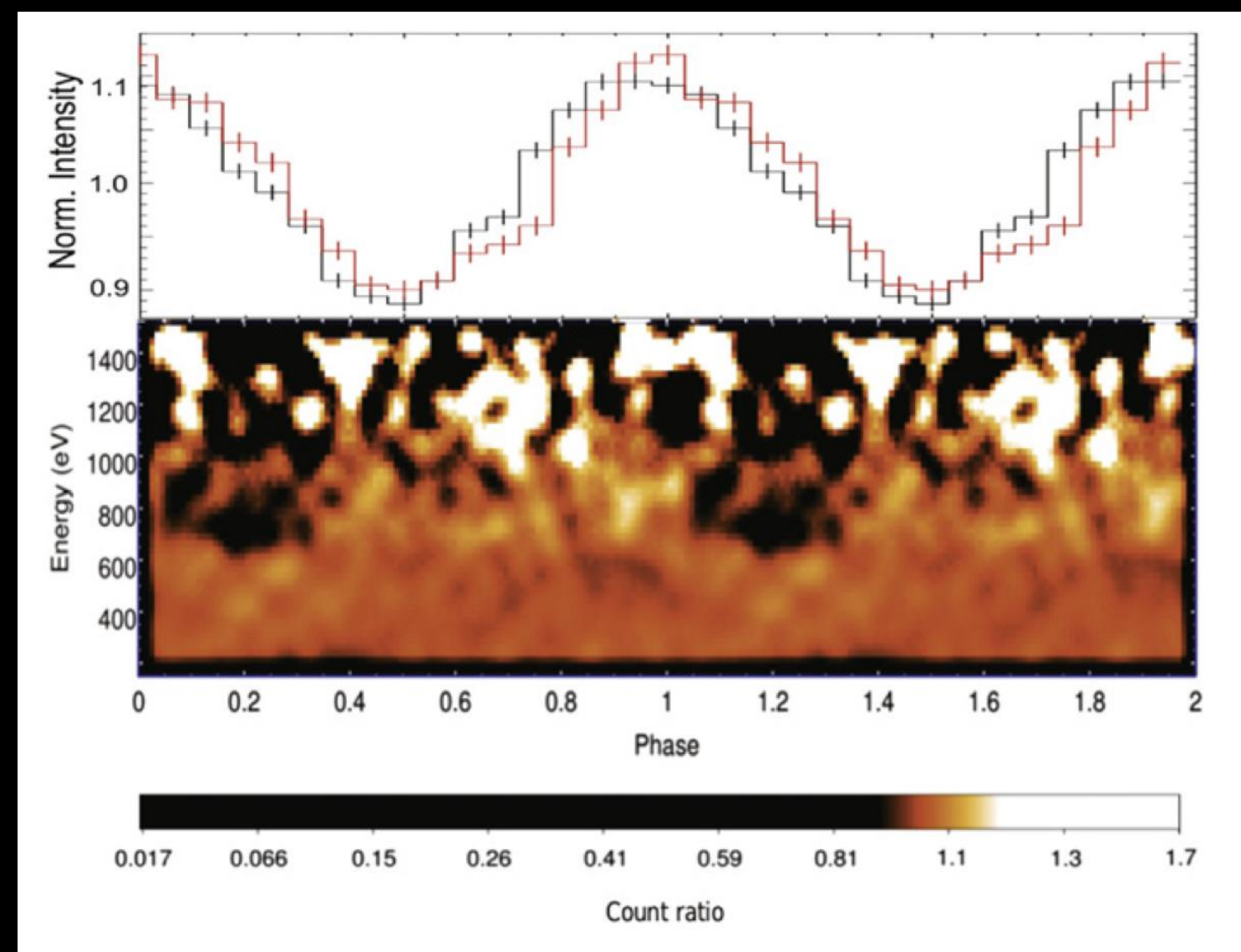
# Magnetars

Magnetars are defined now based on their transient behaviour i.e. as sources with burst and outbursts in X-ray.

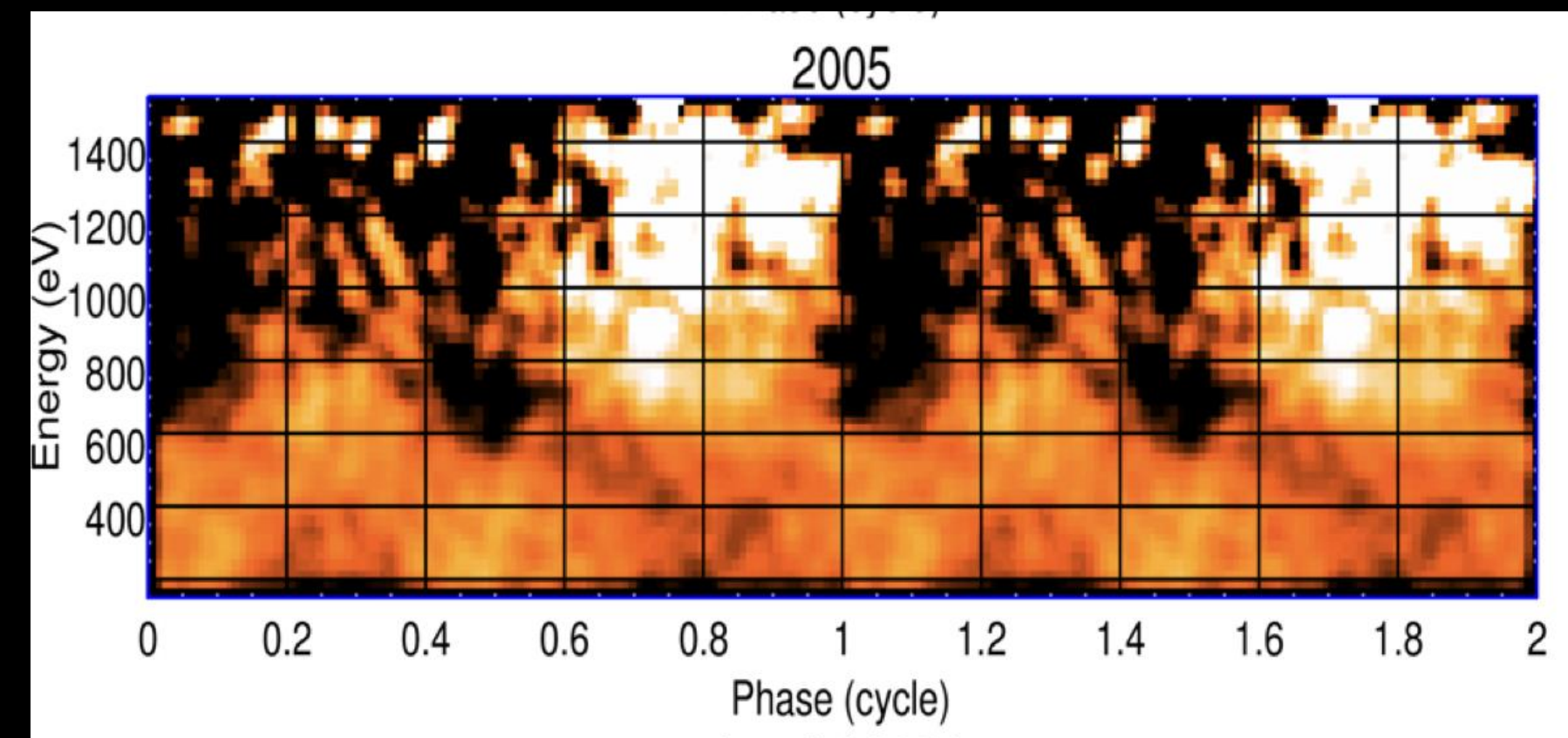
# XDINS and their tangled magnetic fields

X-ray spectra is well described with thermal blackbody but in some cases absorption features are present.

Some of these objects have phase dependant absorption features which could be produced by proton cyclotron resonant scattering in a localised loop near NS surface with magnetic field  $\sim 5$  times stronger than dipolar estimate. Similar is found for low-B magnetars



RX J0720.4-3125; Borghese+ (2015)

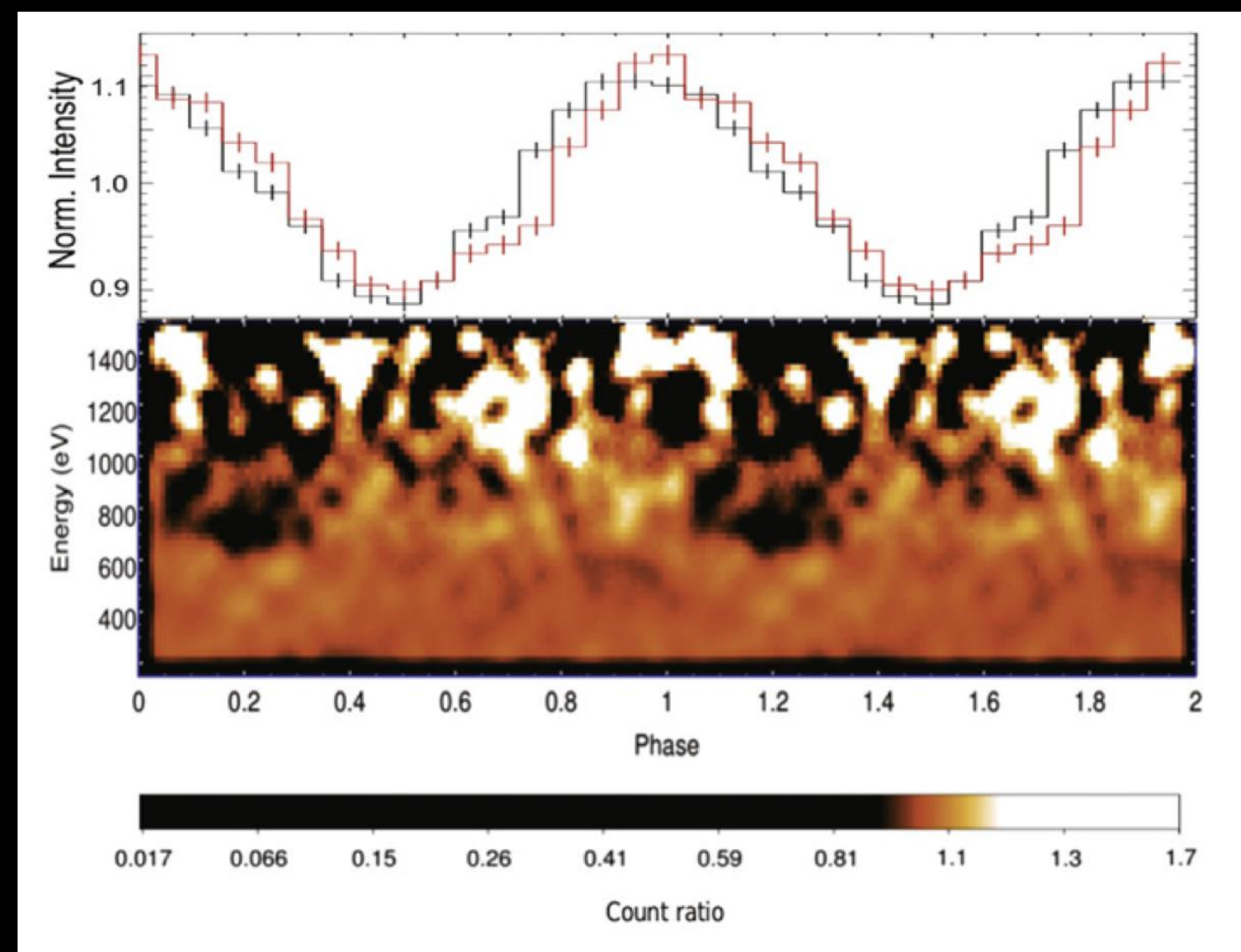


RX J1308.6+21275; Borghese+ (2017)

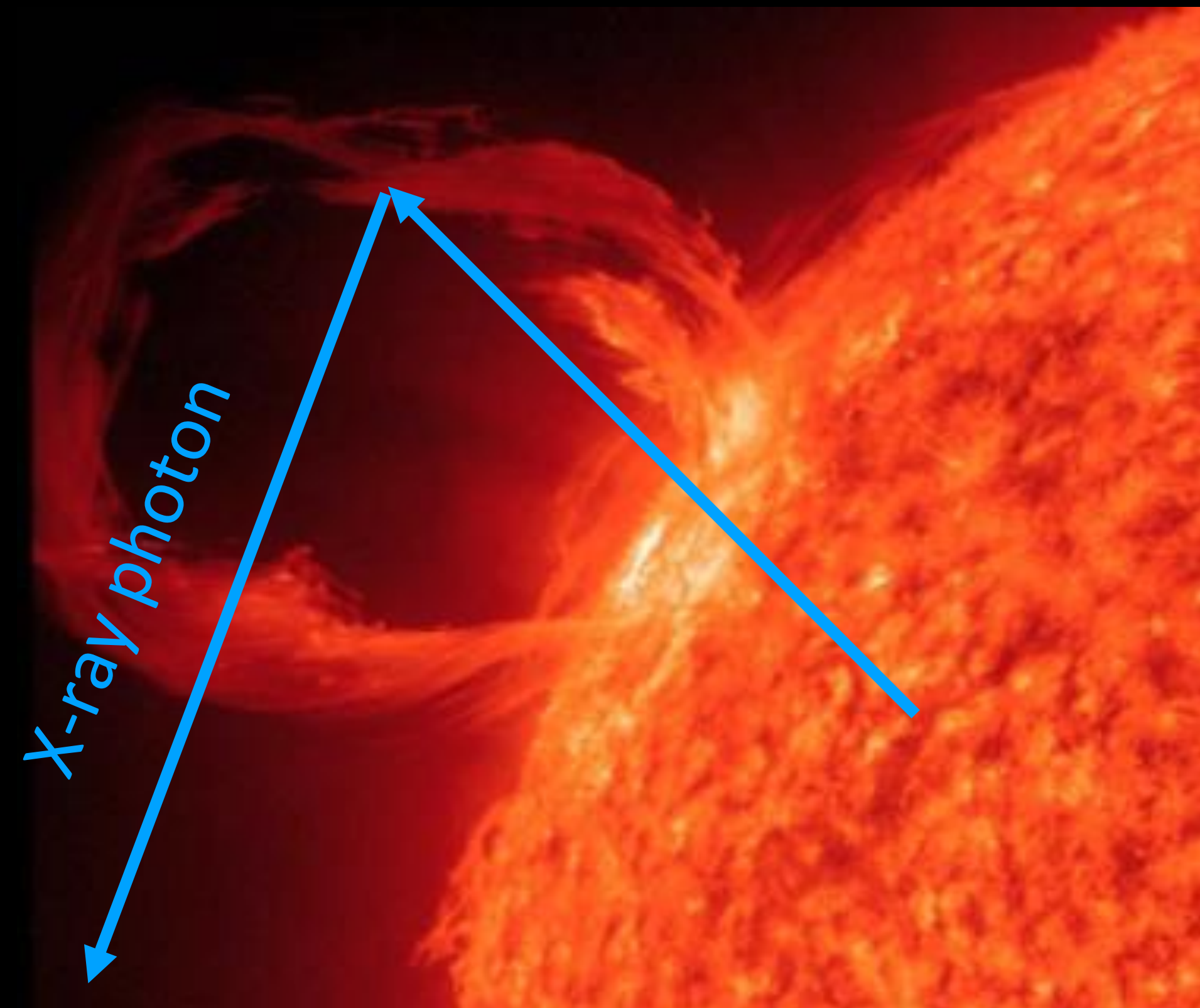
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RX J0720.4-3125; Borghese+ (2015)



# Central compact objects (CCOs)

A handful of young isolated NSs discovered in close vicinity to geometric centra of supernova remnants. (de Luca 2017)

CCOs emit only thermal X-ray radiation. No radio emission was discovered.

Periods and period derivatives are measured in three cases. Periods are typical for normal radio pulsars. Period derivatives are very small  $\sim 10^{-17}$  s/s.

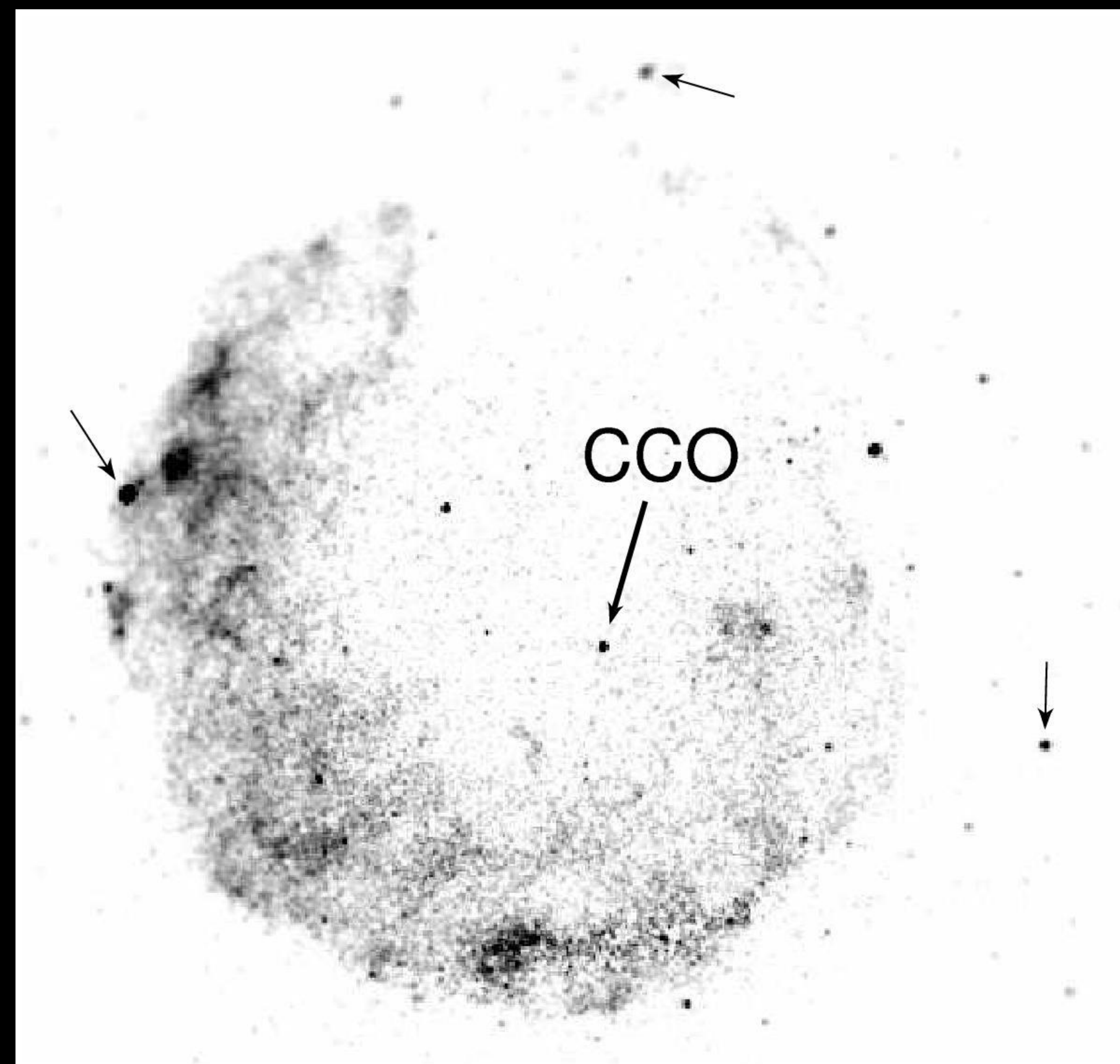
# Central compact objects (CCOs)

PF ~ 9-11% in two cases, 64% in one case

Thermal emission of CCOs is stronger than expected based on isolated NS cooling:

$$L_{\text{bol}}/E > 10$$

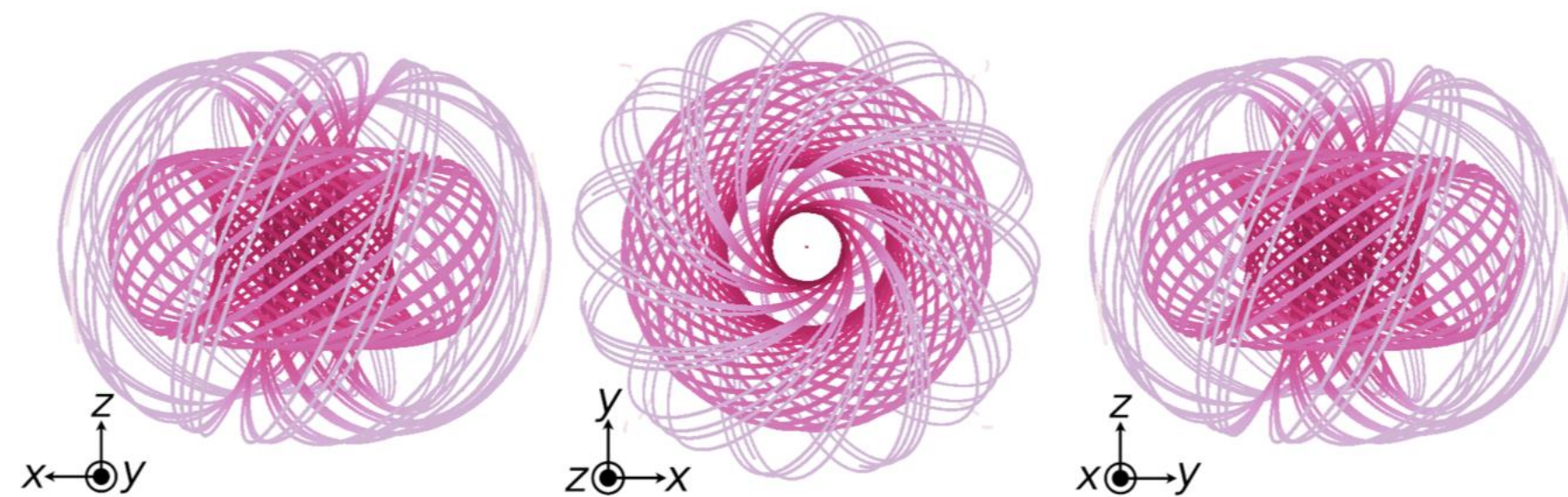
CCO have hidden magnetic fields Hidden = multipolar or toroidal magnetic fields which cannot be measured though spin-down.



Klochkov, Suleimanov, Sasaki & Santangelo (2016)

# Hidden magnetic field scenario

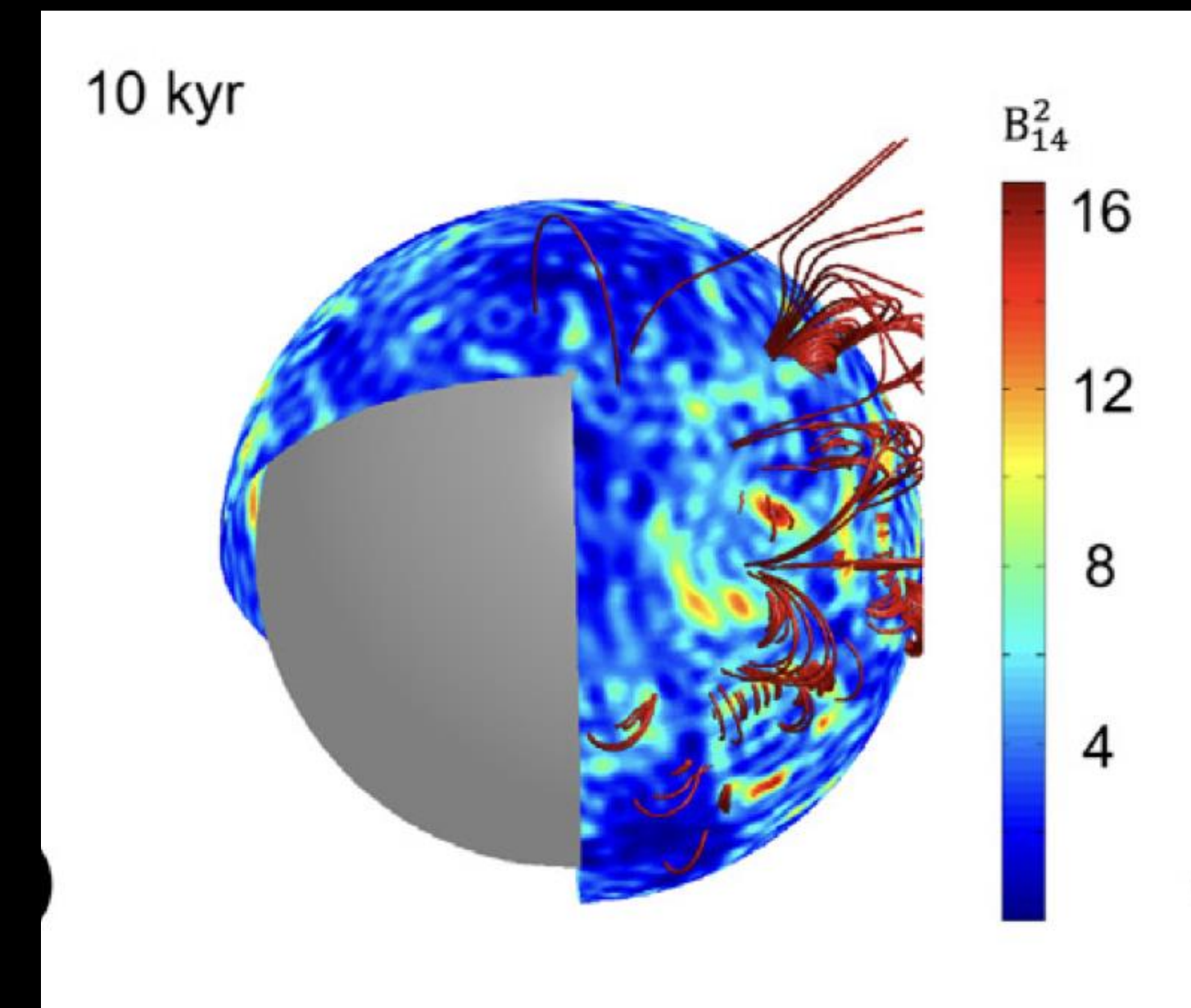
Strong subsurface magnetic fields buried during the SN explosion (Muslimov & Page 1995, Viganò & Pons 2012). Alternatively, small scale magnetic fields (Igoshev, Gourgouliatos & Hollerbach 2021; Gourgouliatos, Hollerbach, Igoshev 2020).



**Figure 1.** Magnetic field line visualization of the Prendergast magnetic field as given by equations 7-9. The color of the field lines indicates the strength of the magnitude of the field, with darker color indicating a stronger magnitude. The field consists of a combination of twisting toroidal and poloidal components with its axis of symmetry aligned with the z-axis. To aid in visualization we select 2 helical structures, but the field is continuous and has many nesting structures.

Kaufman et al. (2022)

Prendergast

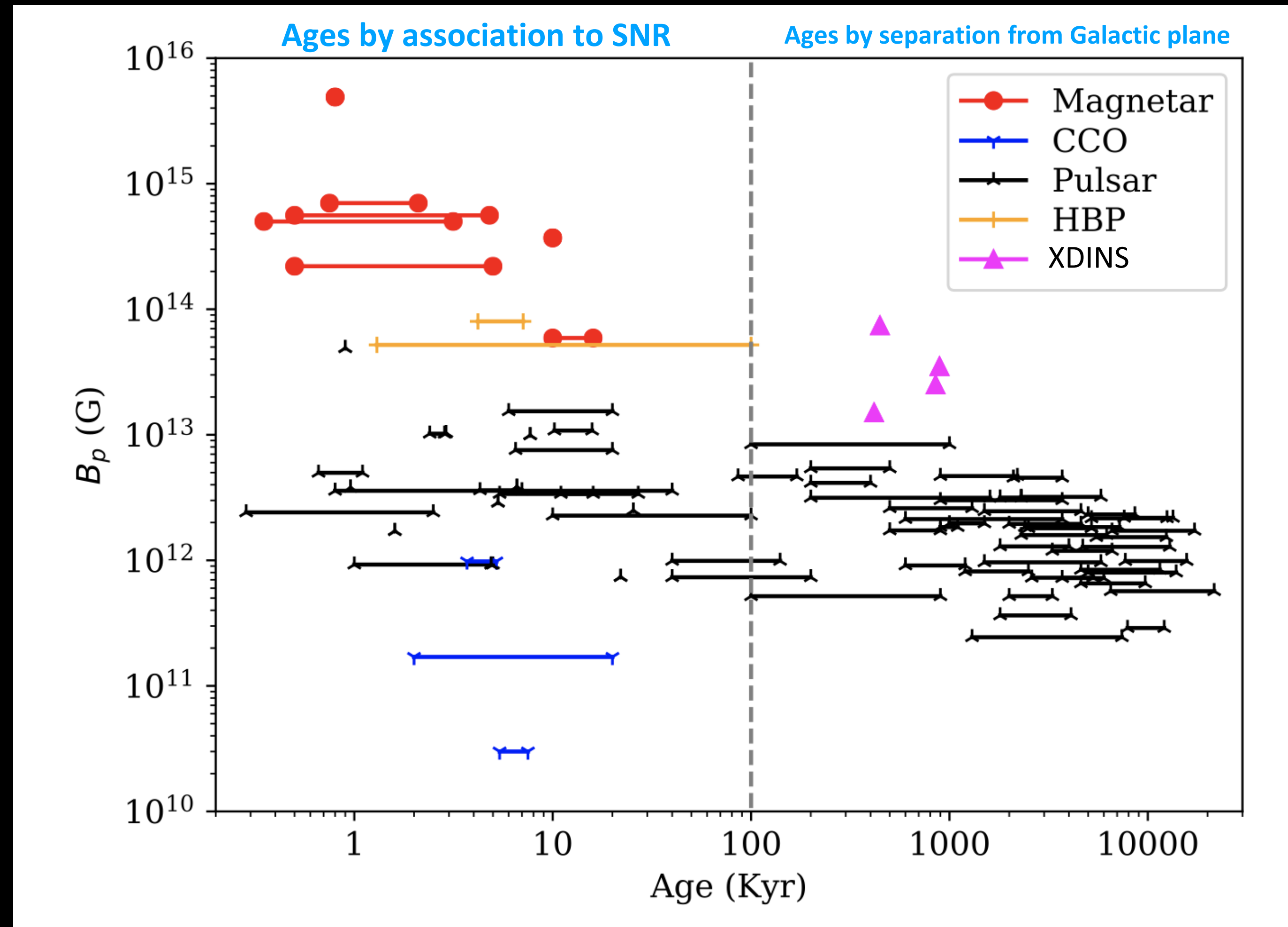


Gourgouliatos et al. (2020)

# Magnetic fields of neutron stars are complex

- ★ Magnetars probably have strong toroidal fields in the crust.
- ★ Some low-B magnetars as well as some X-ray Dim Isolated Neutron Stars have individual arcs of strong poloidal magnetic fields.
- ★ CCOs have hidden magnetic fields which are either buried or small scale poloidal.

# Magnetic field evolution problem

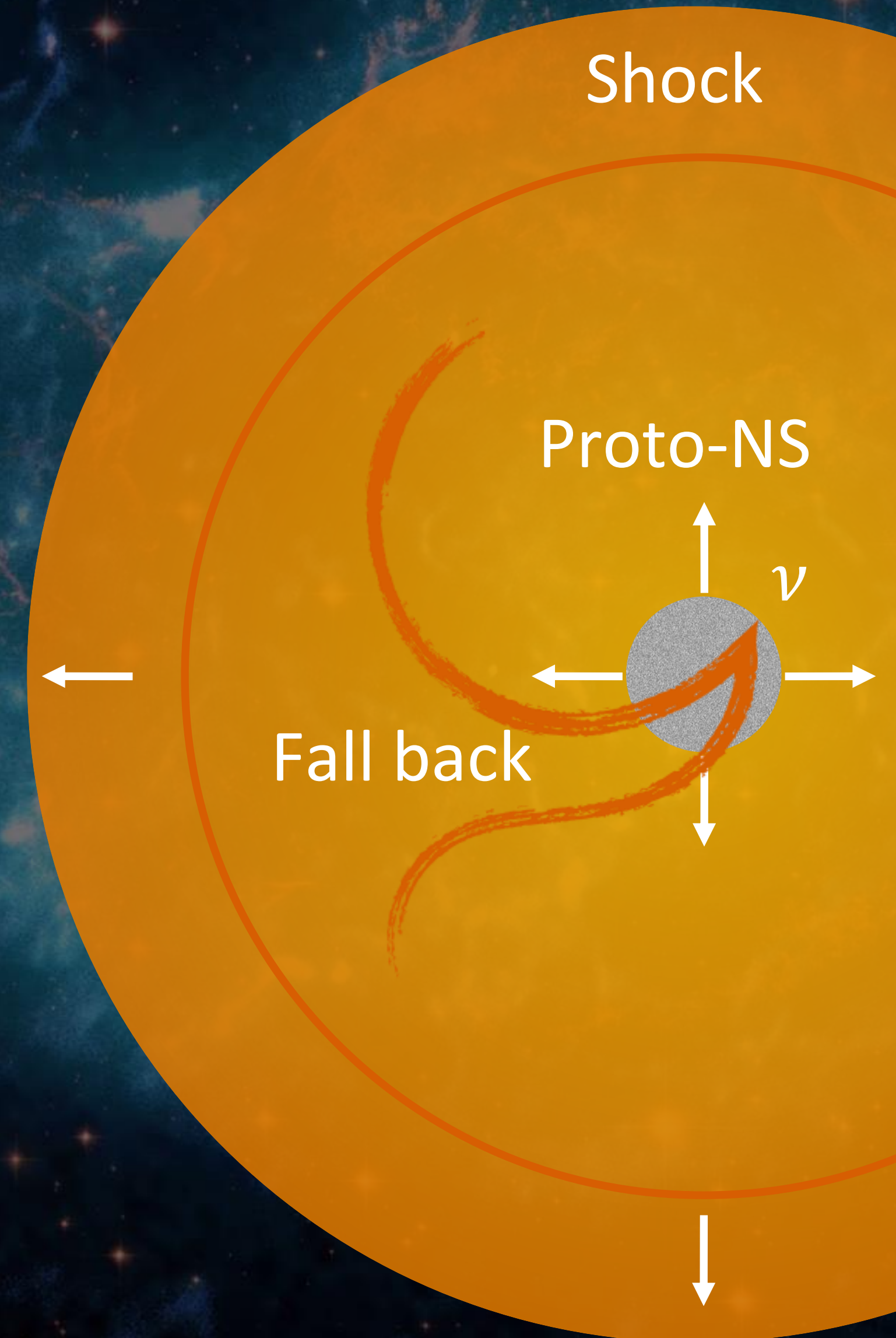
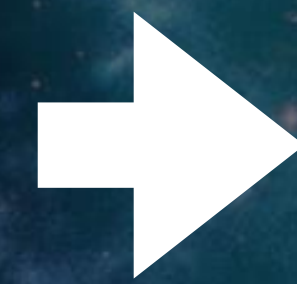
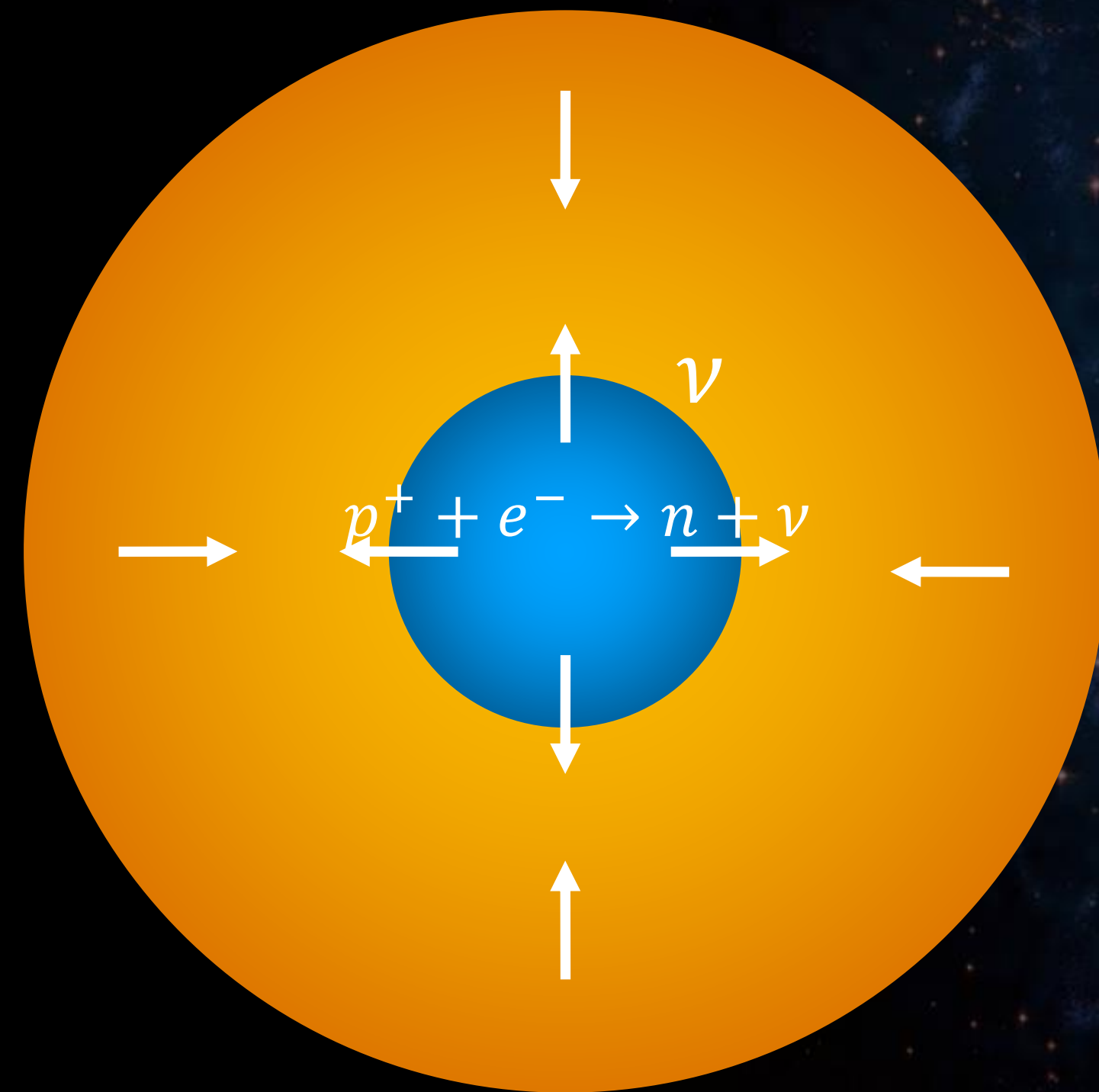
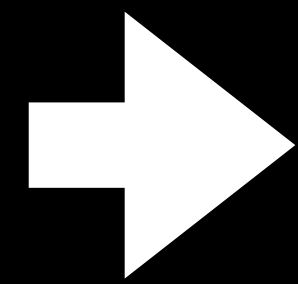
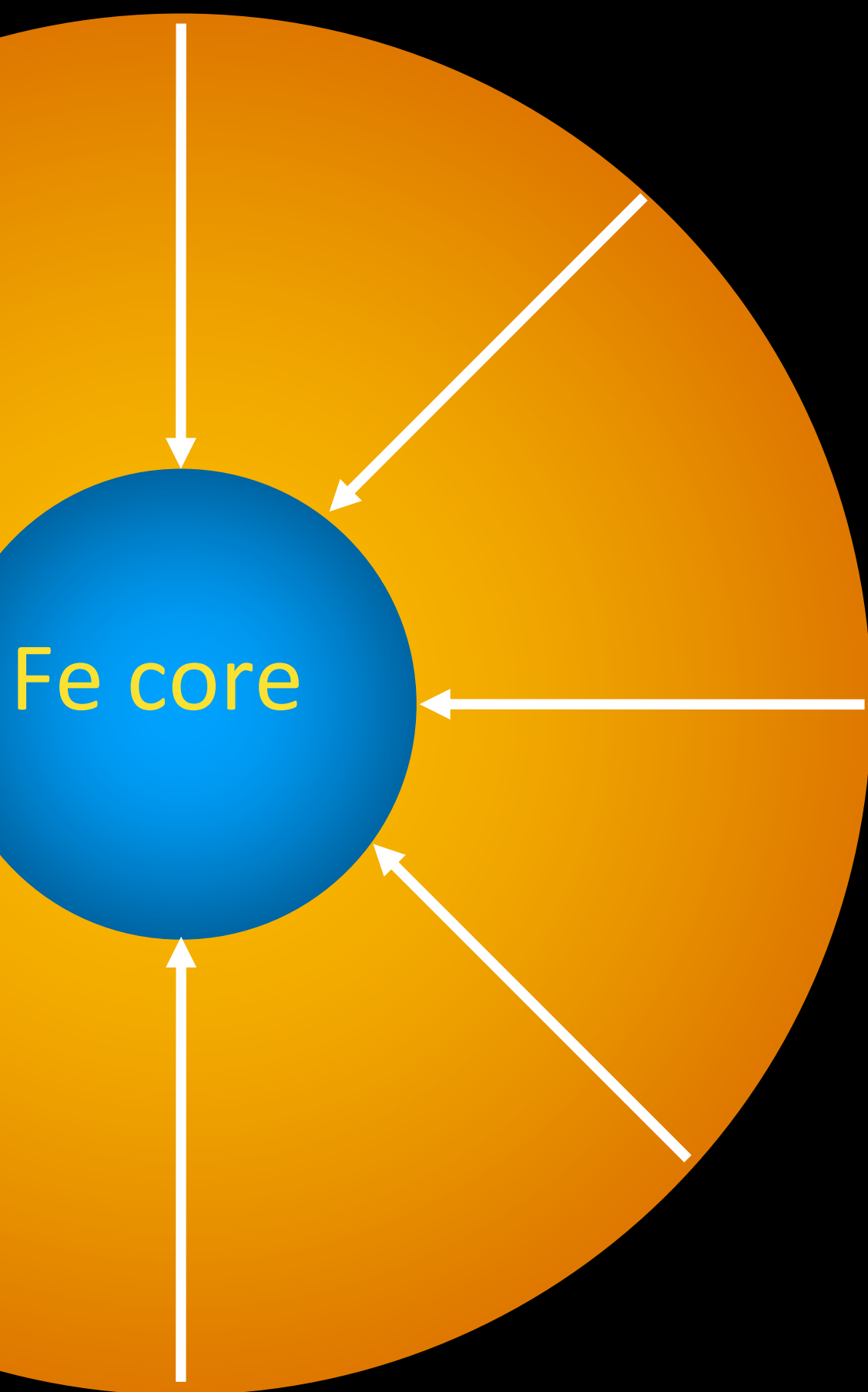


# Formation of magnetic fields

The background of the slide features a dark gray, textured pattern of magnetic field lines. The lines are arranged in two primary regions, one on the left and one on the right, each radiating from a central point. The left region is labeled with a small 'N' and the right with a small 'S', representing North and South magnetic poles. The lines between these two regions curve inward, creating a dipole-like field structure. The overall texture is dense and fibrous, with the lines appearing to flow from the poles towards the center.

# From supernova to NS

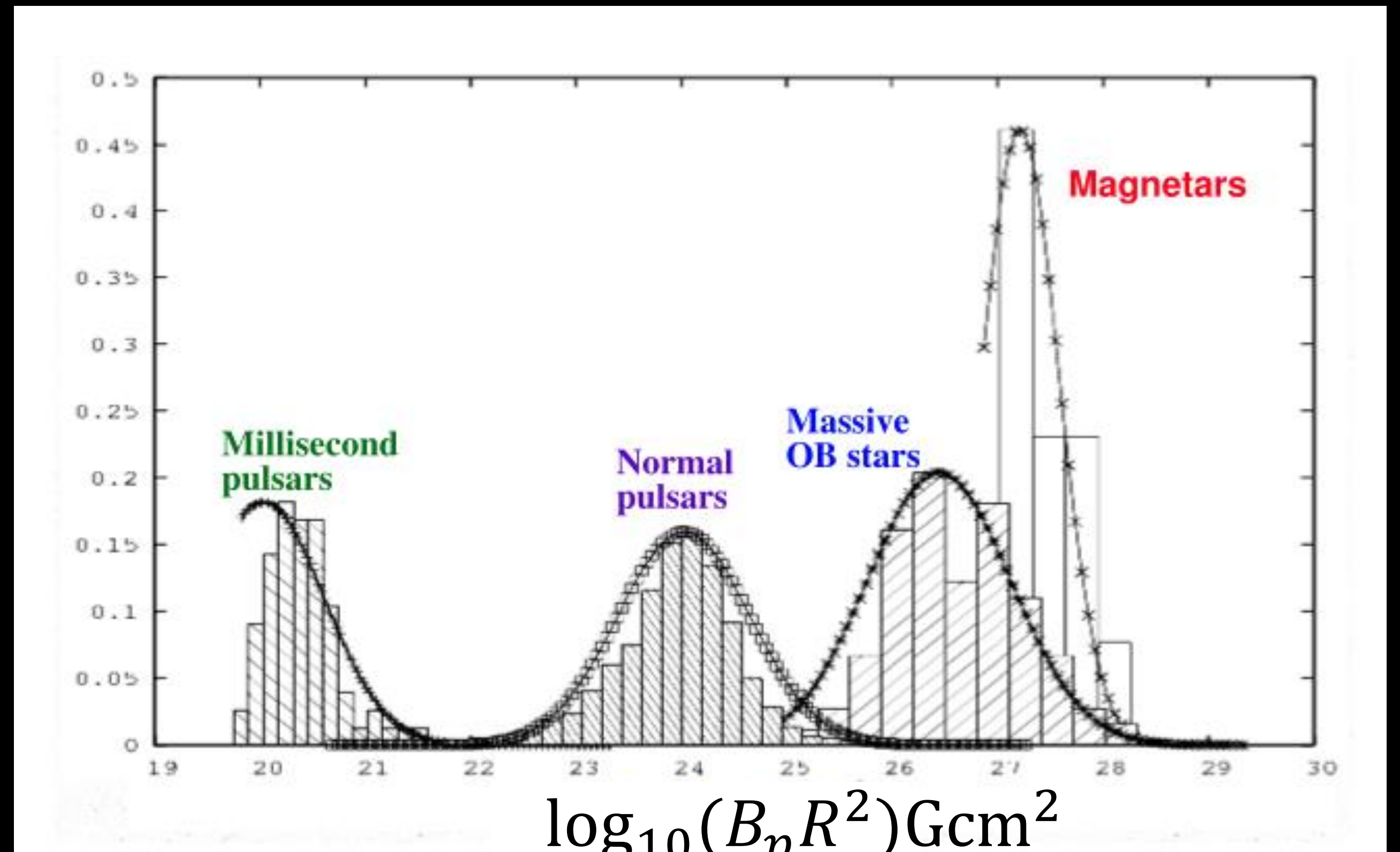
Massive star



# Formation of strong magnetic fields

**Fossil hypothesis:** magnetic field of a massive star (NS progenitors) is amplified when the magnetised core collapses.

**Dynamo hypothesis:** there are two regions in the proto-neutron star where convection is possible. The cooling of neutron star proceed slow enough which allows multiple dynamical overturns. (See e.g. Thompson & Murray 2001)



Ferrario and Wickramasinghe (2006)

Igoshev & Kholtygin (2011)

Makarenko, Igoshev & Kholtygin (2021)

# Dynamo in MHD

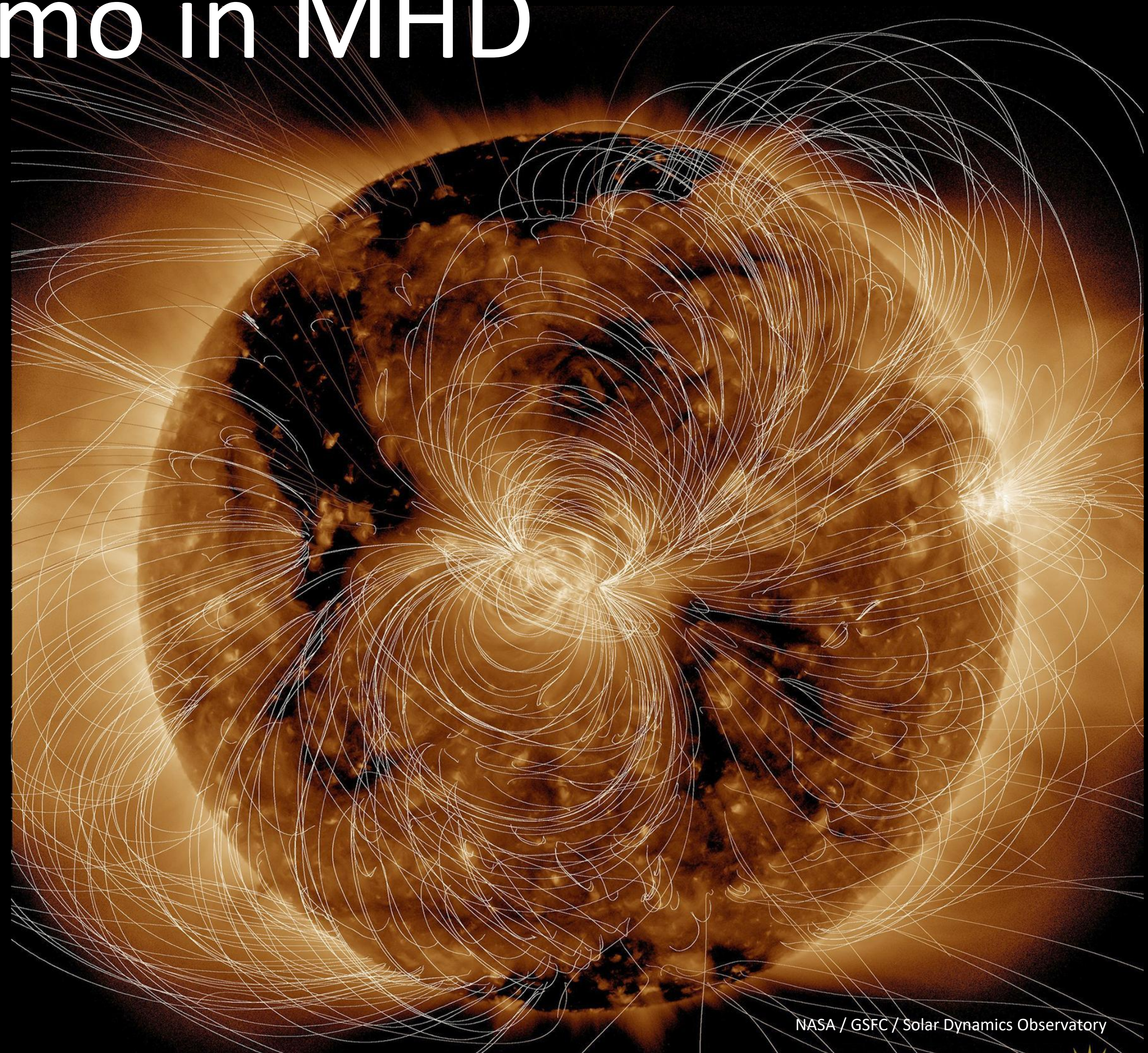
Induction equation:

$$\frac{\partial \vec{B}}{\partial t} = \nabla \times (\vec{u} \times \vec{B}) + \eta(\nabla^2 \vec{B})$$

Some fluid velocity  $\mathbf{u}$  which advects fields amplifying it.

Large regular velocities develop as a result of an instability:

1. Convective
2. Magneto-rotational
3. Tayler-Spruit



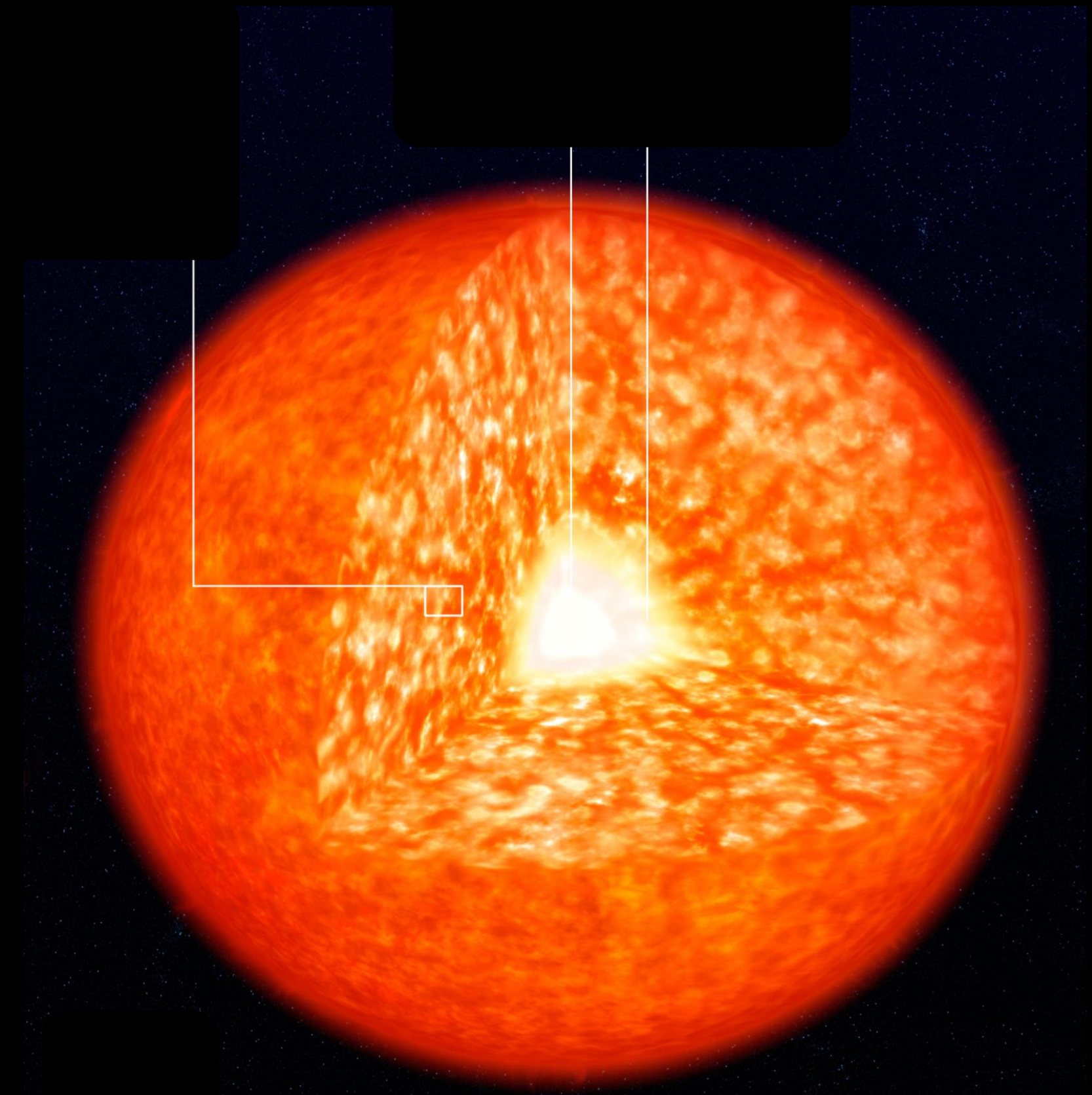
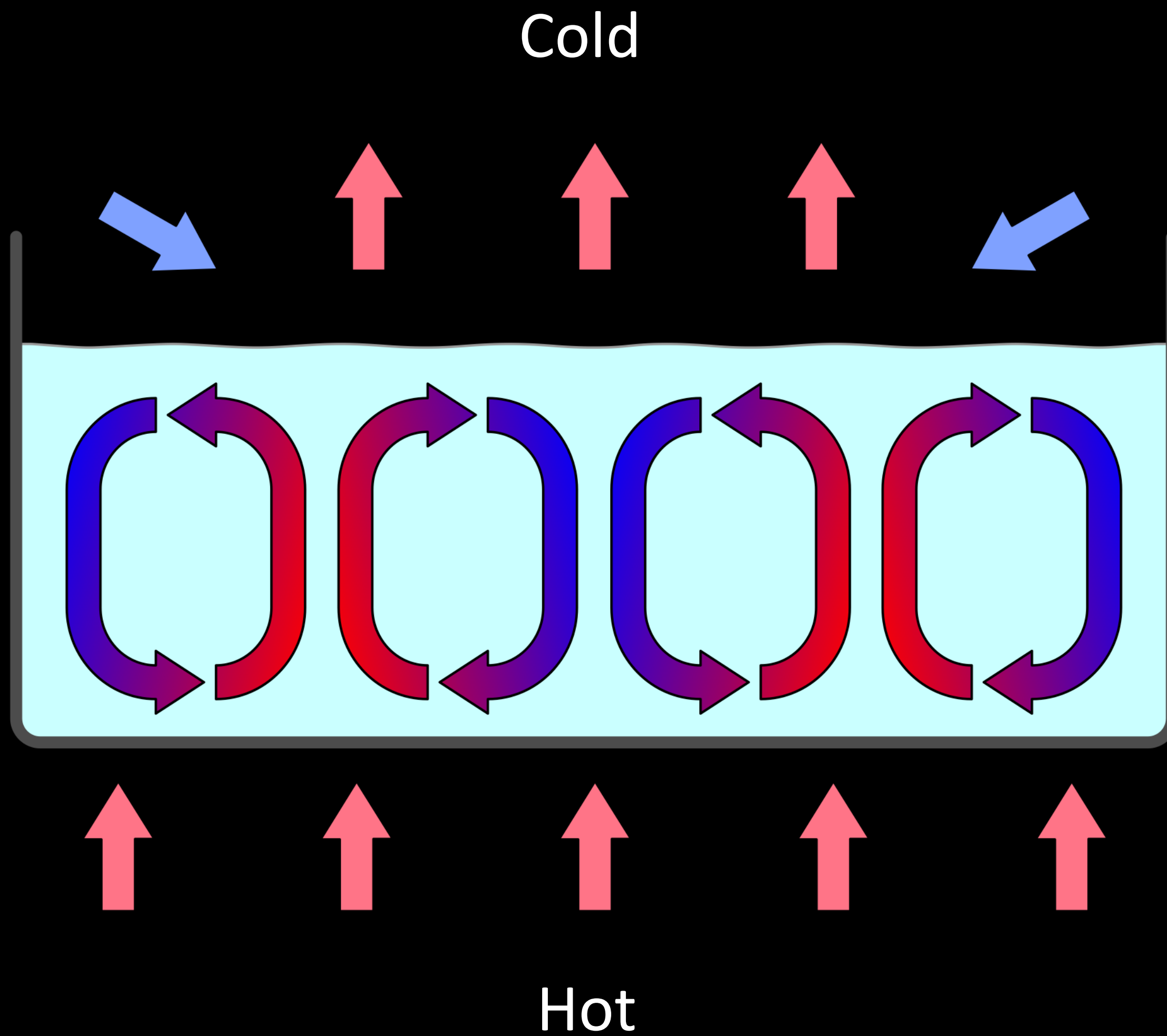
# Proto-NS simulation: Boussinesq approximation

$$\frac{D\mathbf{v}}{Dt} + \frac{2}{E}\vec{e}_z \times \vec{v} = -\nabla\Pi + \frac{Ra}{Pr}T\vec{e}_r + \frac{1}{EPm}(\nabla \times \vec{B}) \times \vec{B} + \Delta\vec{v}$$

$$\frac{\partial\vec{B}}{\partial t} = \nabla \times (\vec{v} \times \vec{B}) + \frac{1}{Pm}\Delta\vec{B}$$

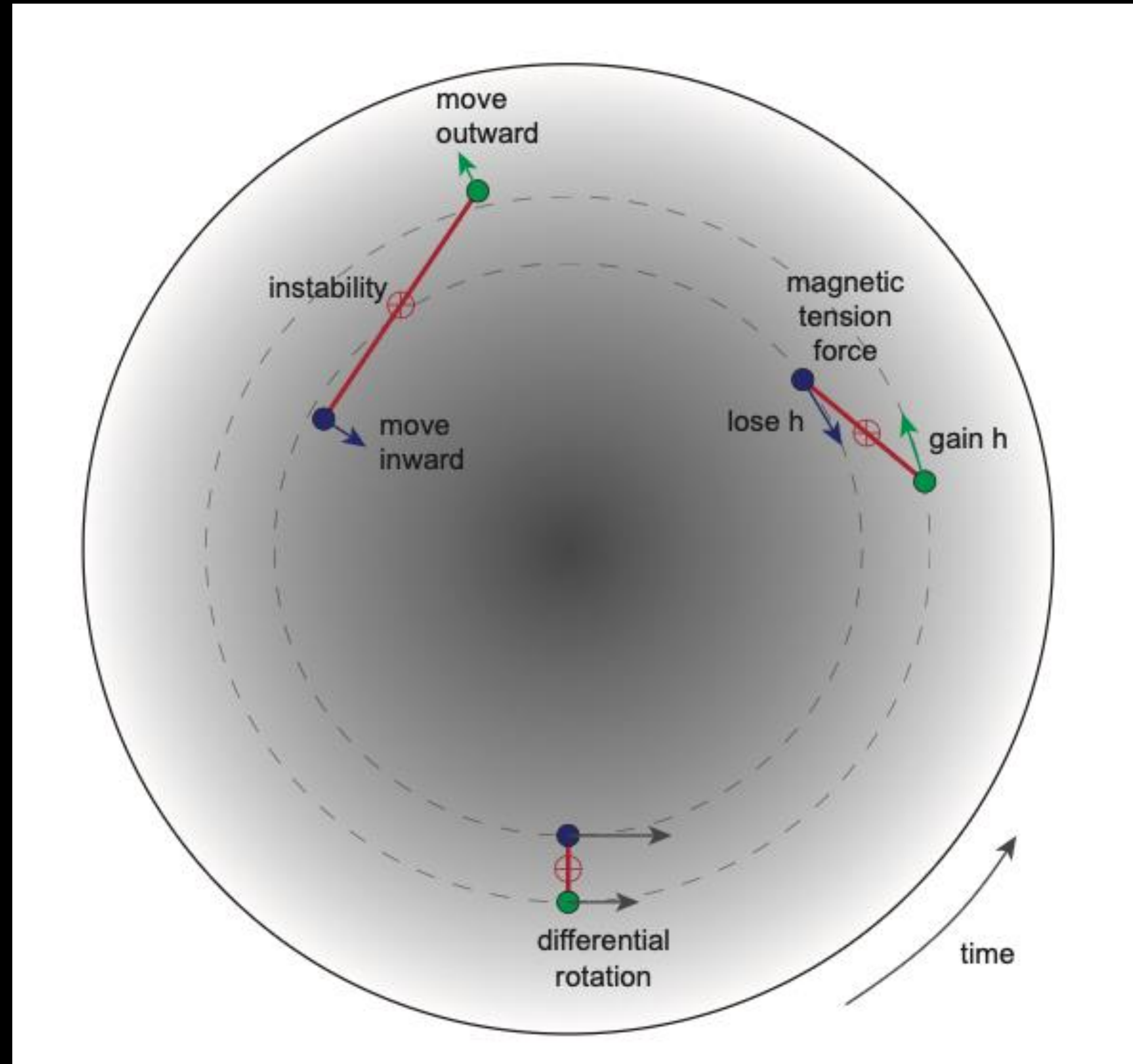
$$\frac{DT}{Dt} = \frac{1}{Pr}\Delta T \quad \nabla \cdot \vec{B} = 0 \quad \nabla \cdot \vec{u} = 0$$

# Convective instability



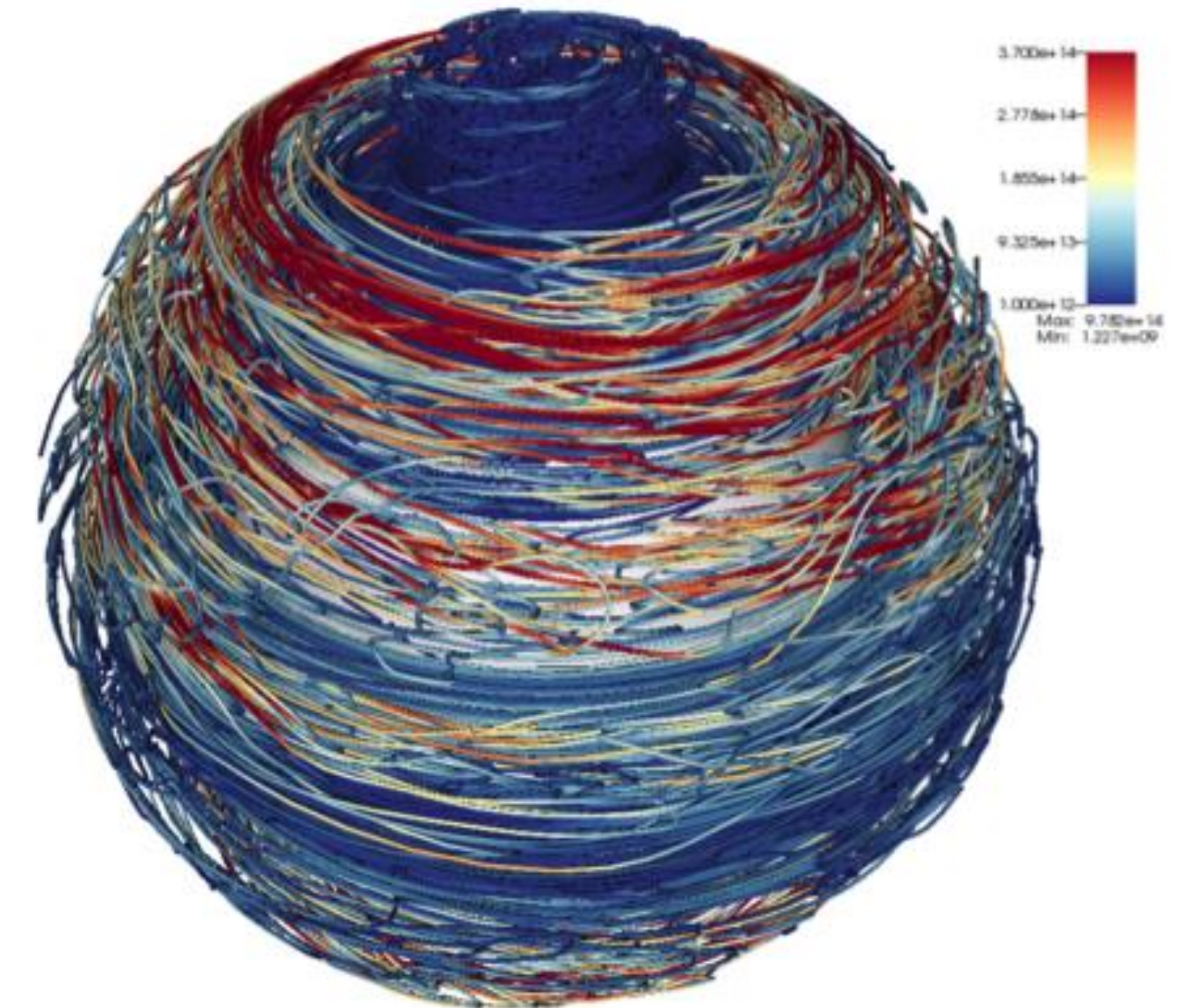
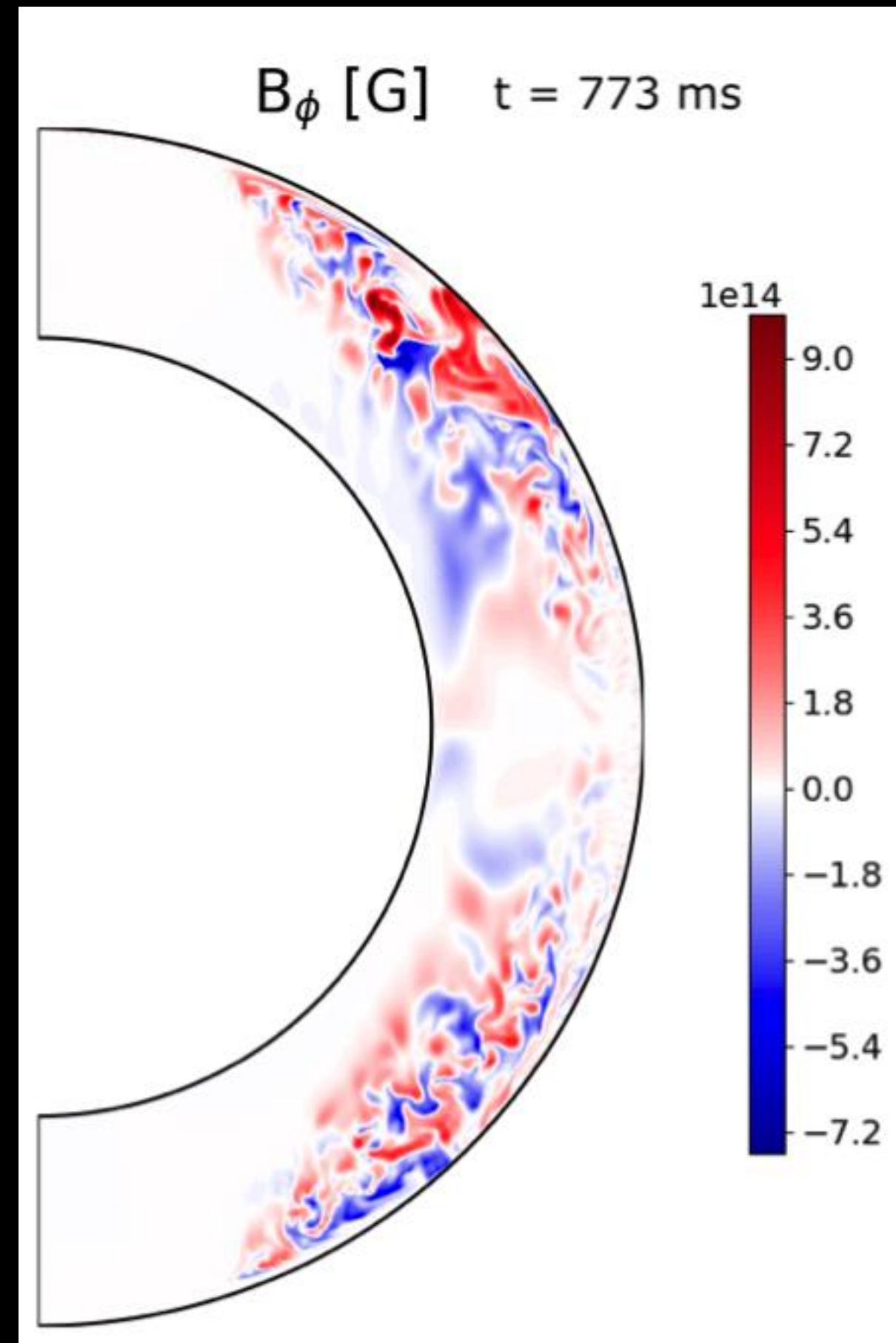
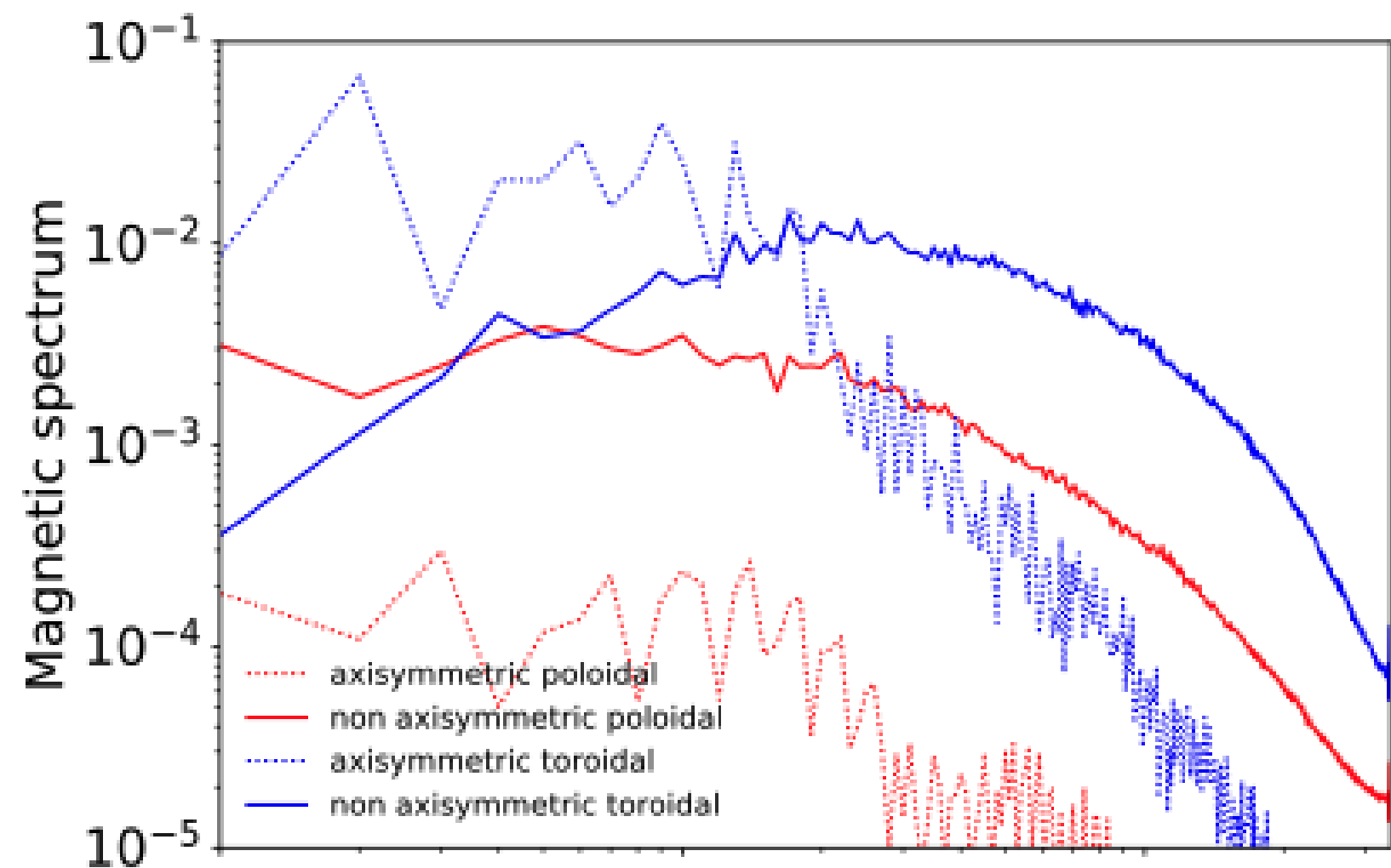


# Magneto-rotational instability



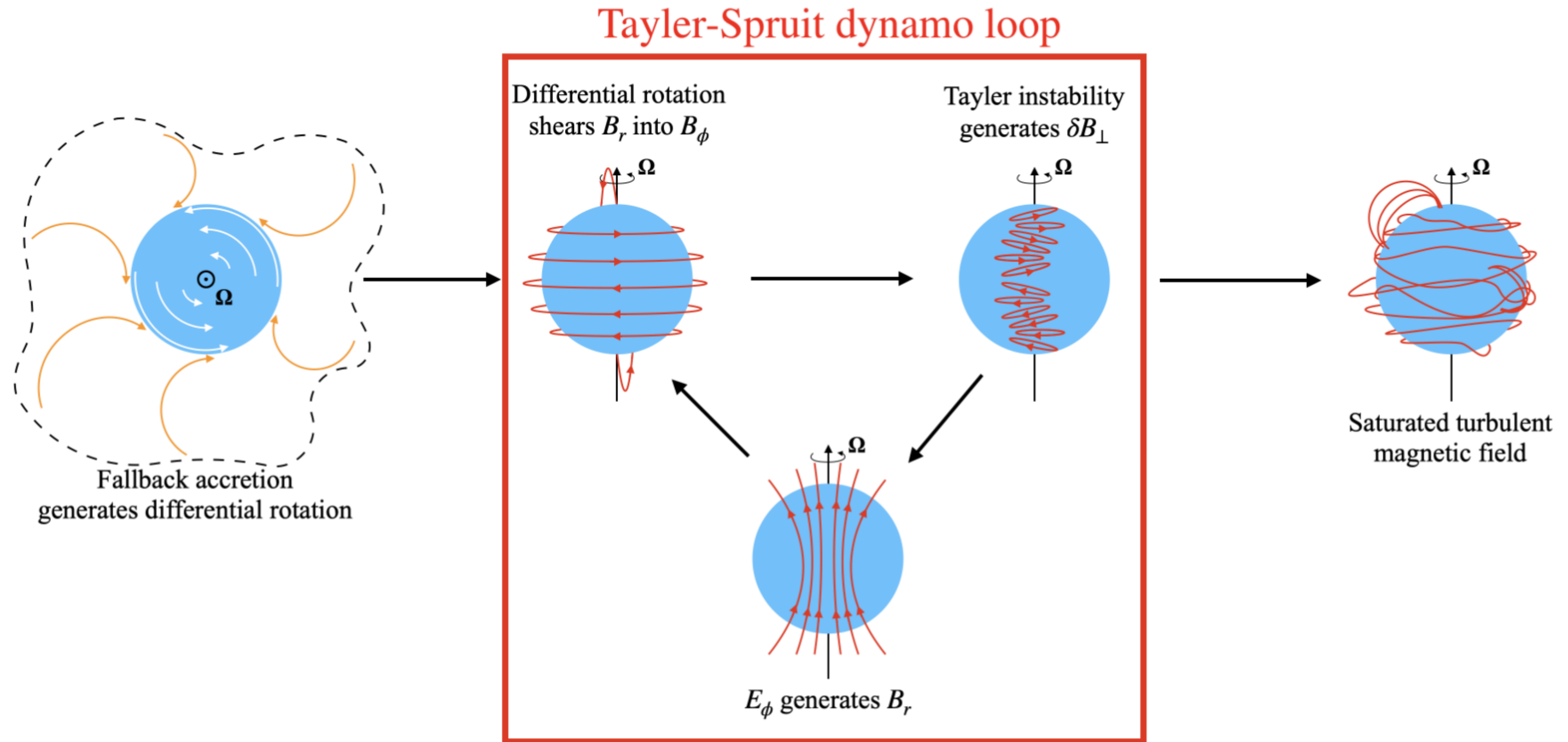
# Magneto-rotational instability

Small-scale magnetic field predominantly toroidal.



**Fig. 4.** 3D rendering of the magnetic field lines in simulation Standard at  $t = 773$  ms. The color represents the magnetic field amplitude in Gauss.

# Taylor-Spruit instability



**Fig. 1.** Schematic representation of the different stages of our magnetar formation scenario. The dashed line encloses the region of the fallback (orange arrows). Red and white lines represent the magnetic field lines and fluid motions, respectively.  $\Omega$  and  $E_\phi$  stand for the angular rotation frequency and the azimuthal component of the electromotive force, respectively.  $B_\phi$  and  $B_r$  are the axisymmetric azimuthal and radial magnetic fields, and  $\delta B_\perp$  is the non-axisymmetric perpendicular magnetic field.

# Proto-NS simulation: Boussinesq approximation

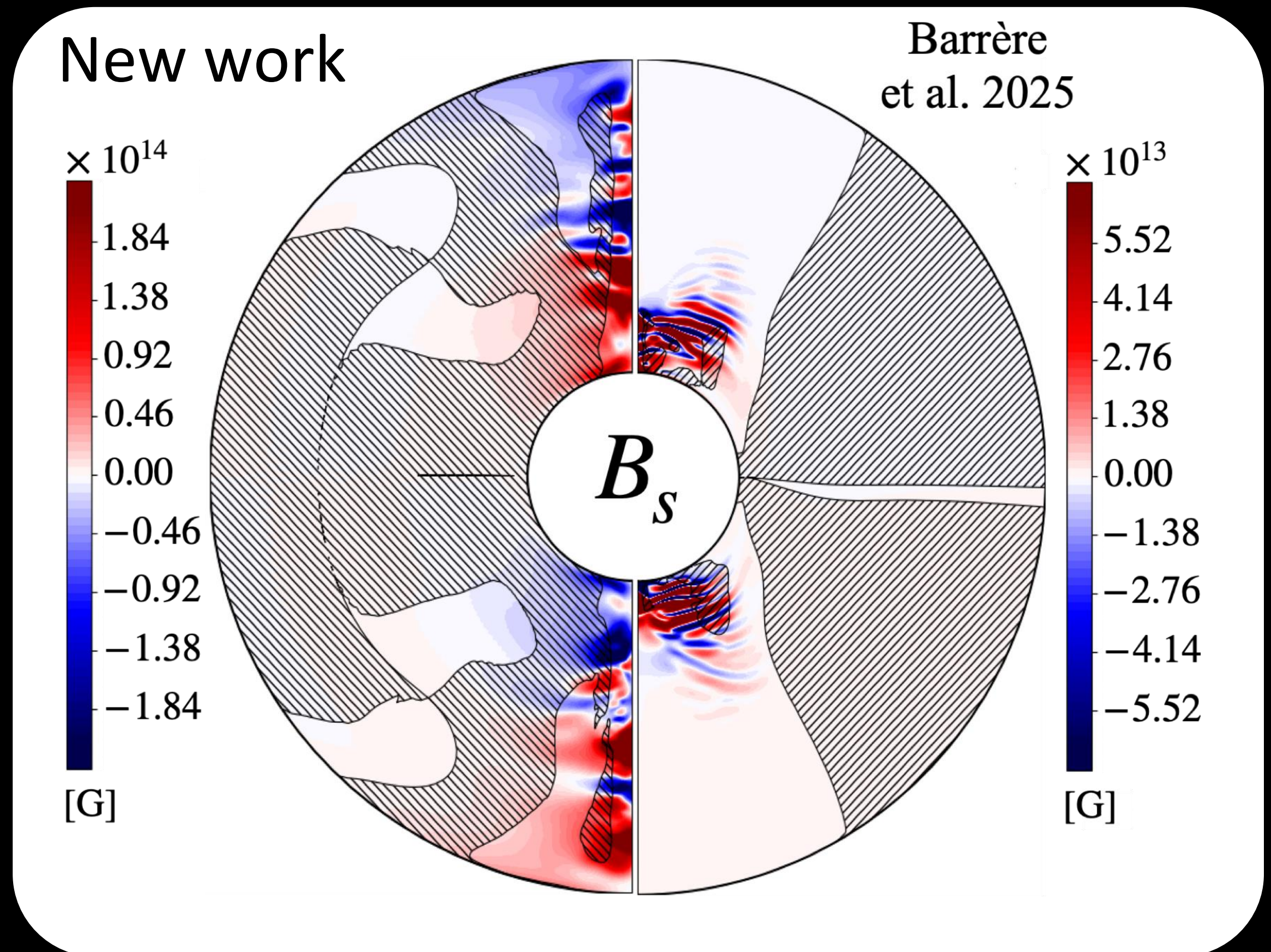
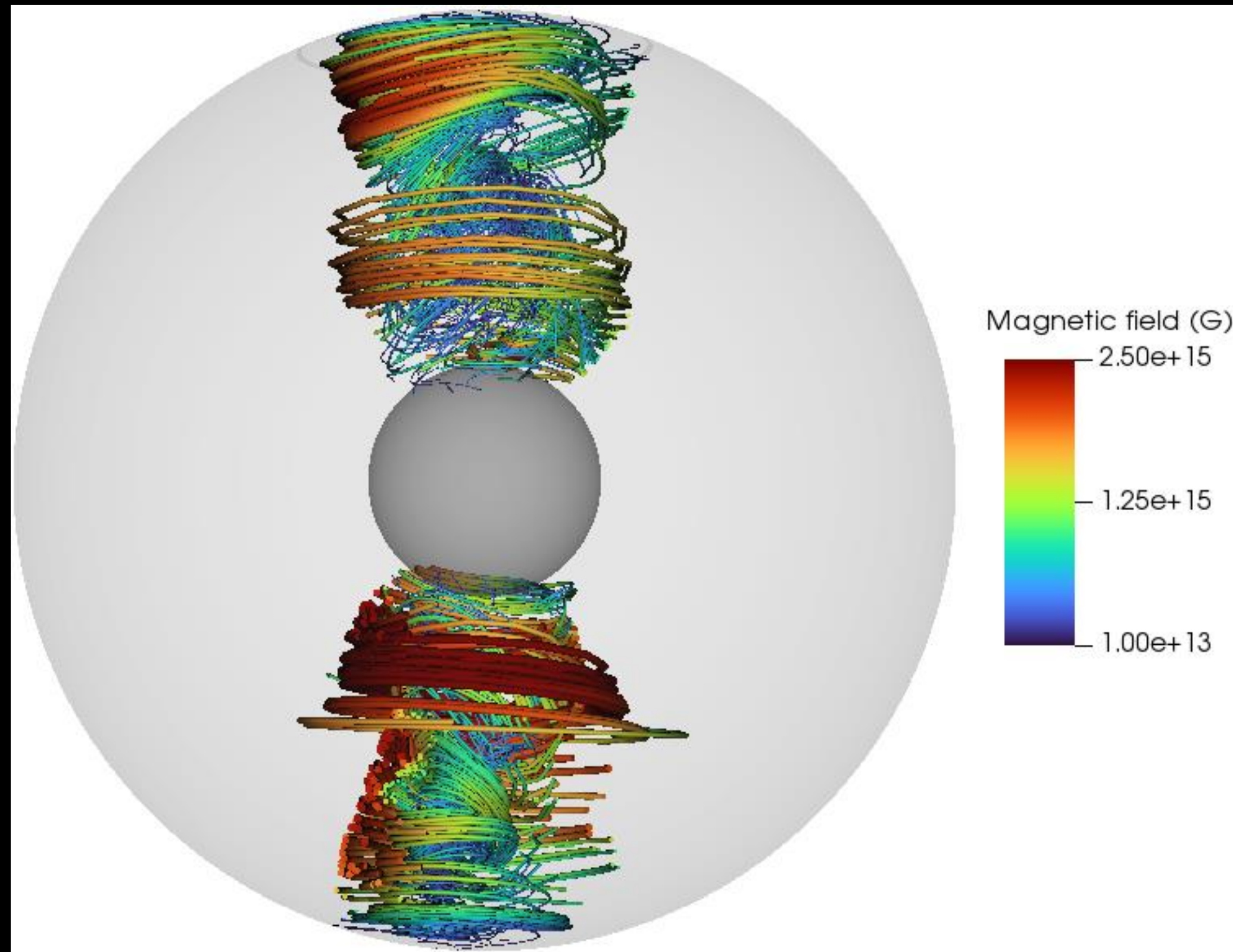
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$$\frac{\partial \vec{B}}{\partial t} = \nabla \times (\vec{v} \times \vec{B}) + \frac{1}{Pm}\Delta\vec{B}$$

$$\frac{DT}{Dt} = \frac{1}{Pr}\Delta T \quad \nabla \cdot \vec{B} = 0 \quad \nabla \cdot \vec{u} = 0$$

- DNS simulation with stable stratification in Boussinesque approximation.
- Spherical Taylor-Couette configuration with positive shear
- No-slip and insulating boundary conditions.
- Ekman number  $E = 10^{-5}$ , magnetic Prandtl number  $Pm = 1$ .
- Ratio of Brunt-Väisälä frequency to the outer angular frequency  $N/\Omega_0 = 0.1$
- Rossby number  $Ro = 1 - \Omega_i/\Omega_o = 0.75$

# Taylor-Spruit dynamo for proto-NS



Barrère, Guilet, Raynaud & Reboul-Salze (2023)

Barrère et al. (2025)



Proto-neutron star - exists  $\sim 30$  seconds

Could have dynamo operating

Neutron star - evolves on Myr timescale

Cooling from inside via neutrino emission - no dynamo



# Magnetic field evolution in neutron star crust

# Magneto-thermal evolution of neutron stars

## PARODY code

- We use the modified PARODY code to solve two equations simultaneously using the spectral decomposition for angular variables and finite difference scheme for radial direction.
- The equations are solved in a spherical shell which represents the neutron star crust. The shell extends for approximately 1 km in depth.

$$\frac{\partial \vec{B}}{\partial t} = Se \nabla \left( \frac{1}{\mu} \right) \times \nabla T^2 + Ha \nabla \times \left[ \frac{1}{\mu^3} \vec{B} \times (\nabla \times \vec{B}) \right] - \nabla \times \left[ \frac{1}{\mu^2} \nabla \times \vec{B} \right] \quad \text{Magnetic induction}$$

$$\frac{1}{Ro} \frac{C_v}{T} \frac{\partial T^2}{\partial t} = \nabla \cdot (\mu^2 \hat{\chi} \cdot \nabla T^2) + \frac{Pe}{Se} \frac{|\nabla \times \vec{B}|^2}{\mu^2} + Pe \mu (\nabla \times B) \cdot \nabla \left( \frac{T^2}{\mu^2} \right) \quad \text{Thermal diffusion}$$

De Grandis et al. (2020)

Igoshev et al. (2021), Nature Astronomy

Igoshev et al. (2021), ApJ

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$$\frac{1}{Ro} \frac{C_v}{T} \frac{\partial T^2}{\partial t} = \underbrace{\nabla \cdot (\mu^2 \hat{\chi} \cdot \nabla T^2)}_{\text{Thermal diffusion}} + \frac{Pe}{Se} \frac{|\nabla \times \vec{B}|^2}{\mu^2} + Pe \mu (\nabla \times B) \cdot \nabla \left( \frac{T^2}{\mu^2} \right) \quad \text{Thermal diffusion}$$

# Initial and boundary condition

- Upper boundary condition:

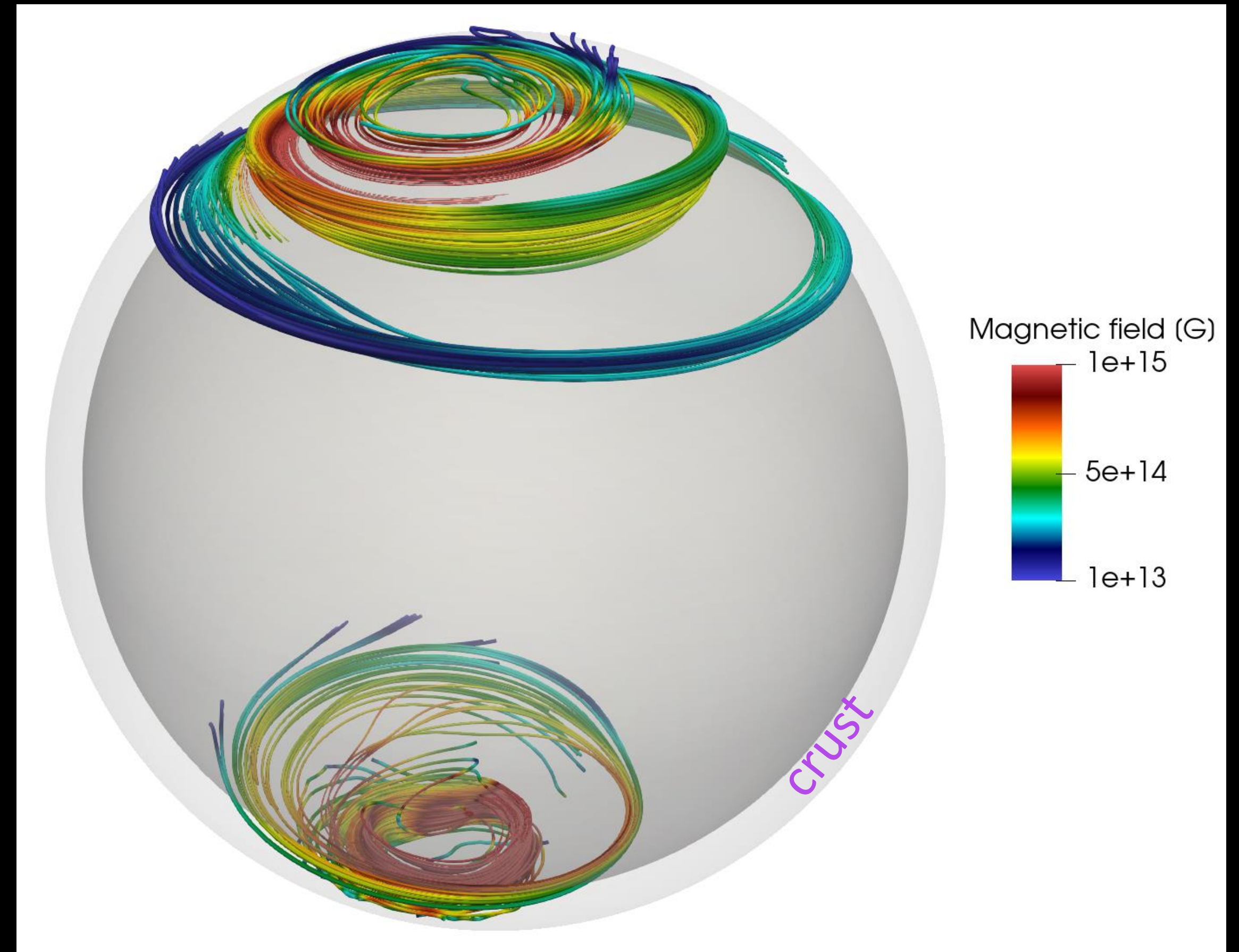
- ▶  $\nabla \times B = 0$  Force-free

- ▶  $\frac{\pi^2 k_B^2}{6e^2} \vec{r} \cdot \hat{\chi} \cdot \nabla T_b^2 = \sigma_B T_s^4$  where  $\left(\frac{T_s}{10^6}\right)^2 = \left(\frac{T_b}{10^8}\right)$   
Blackbody emission from the atmosphere

- Lower boundary condition

- ▶  $B_r = 0$  the Meissner condition

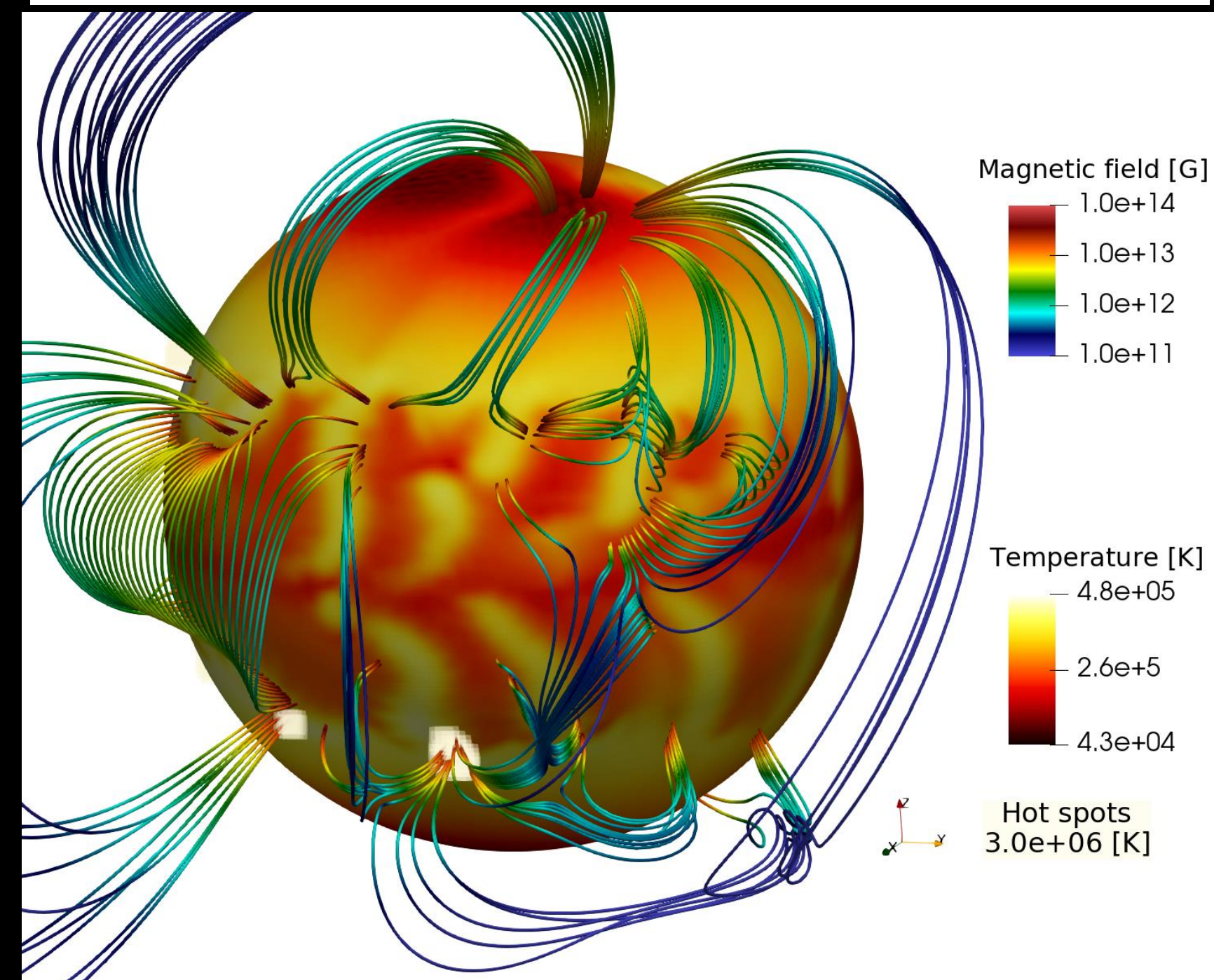
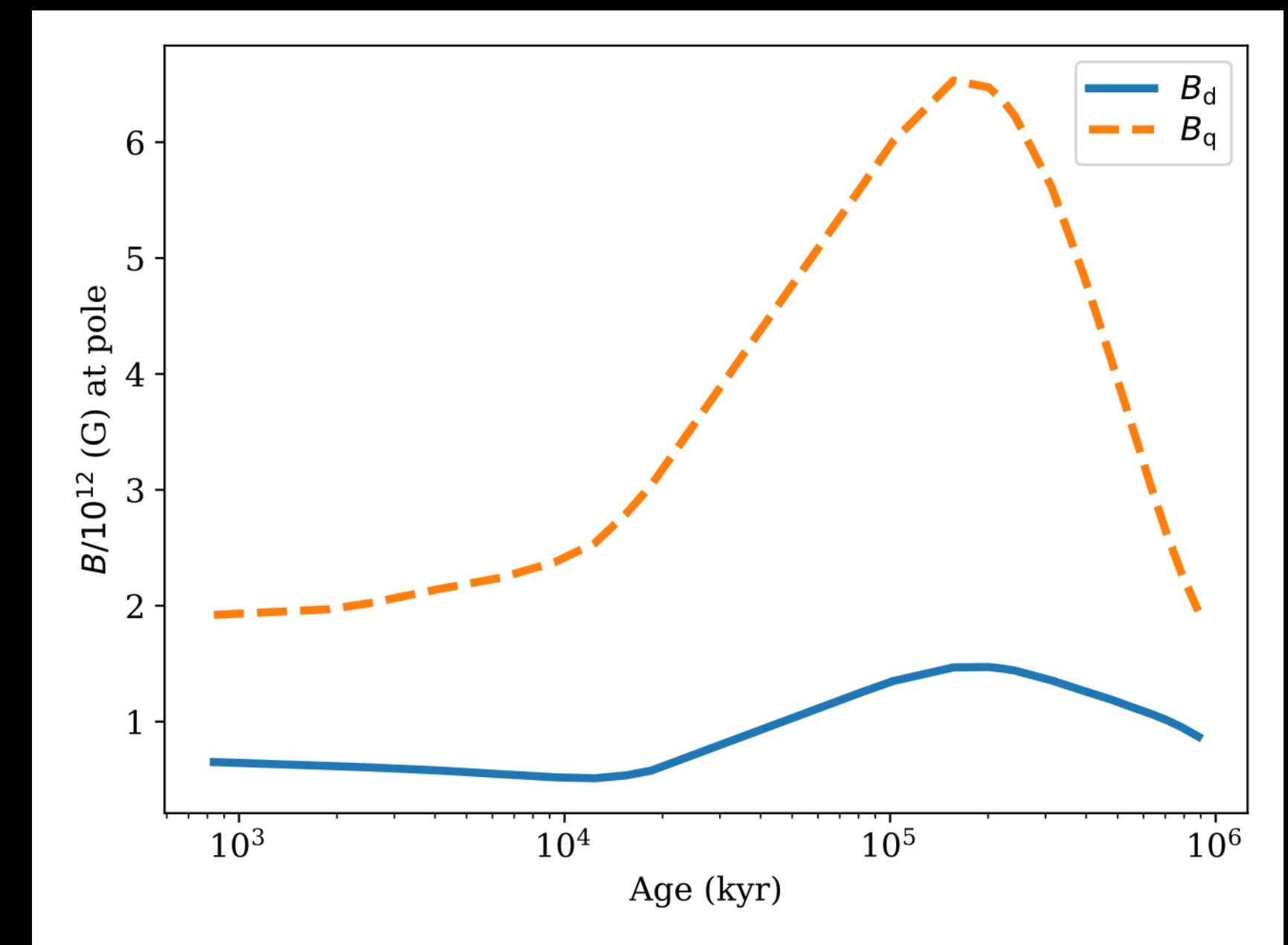
- ▶  $\frac{\partial T}{\partial t} = 0$  no cooling



# External magnetic field

Age 200 kyr

- Magnetic field structure is dominated by small scale fields. A system of magnetic arcs is formed.
- Magnetic field strength at the footpoints of individual arcs reaches  $10^{14}$  G, the dipolar field stays low  $\approx 10^{12}$  G.
- Hot regions are large and have insufficient temperature to be detected as quiescent emission.
- Surface can be heated by magnetospheric currents  $\vec{J} = \nabla \times \vec{B}$ , force-free condition  $\nabla \times \vec{B} = \mu \vec{B}$  which means  $J_r \propto B_r$ . Regions with the strongest radial magnetic field can be heated by magnetospheric currents. Detailed future modelling is necessary.

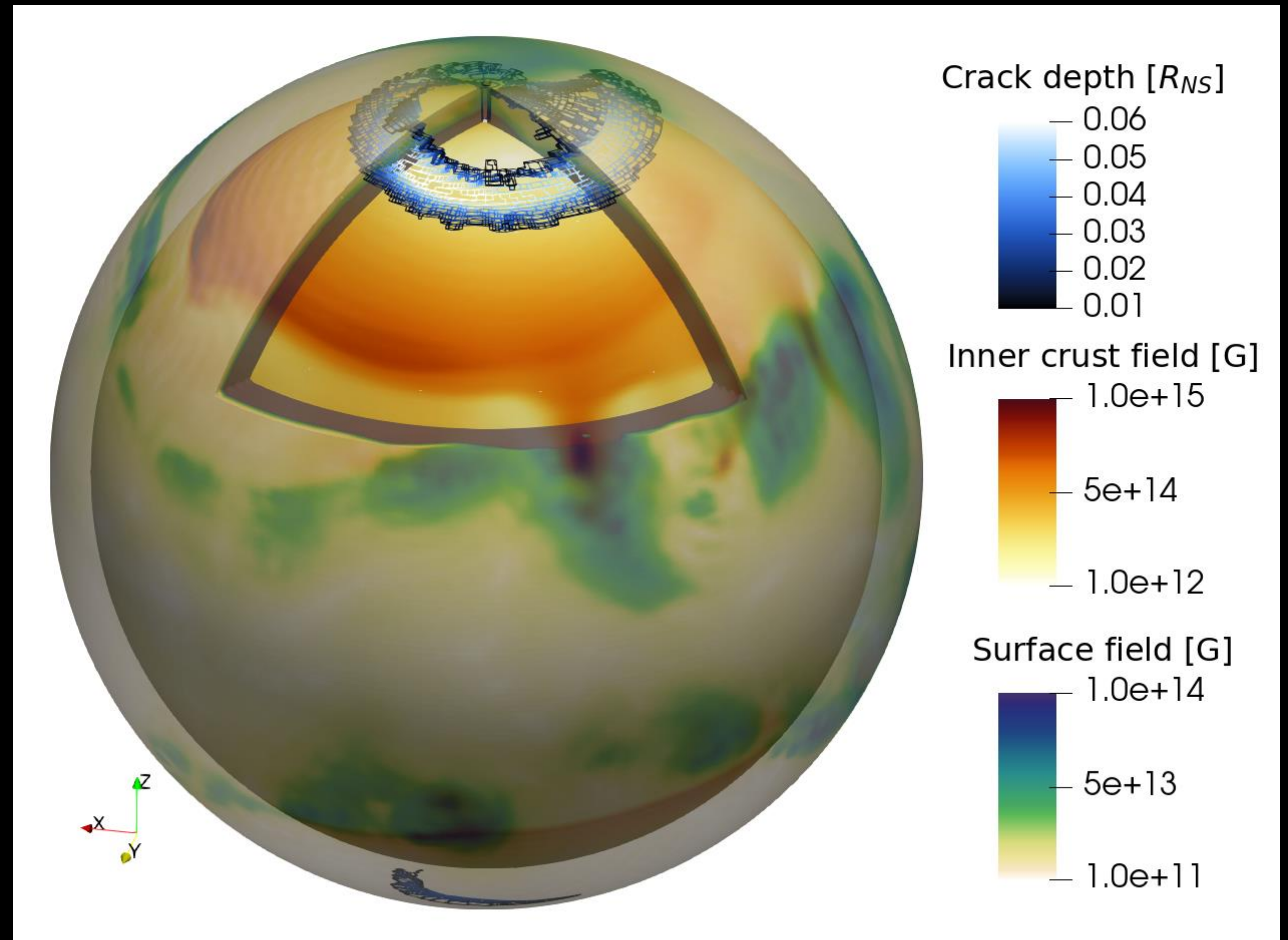


# Is it a magnetar?

## Crust yielding criterion

- Crust will fail near the original magnetic pole and can trigger outbursts similar to magnetar outburst with energies up to  $2 \times 10^{39}$  erg.

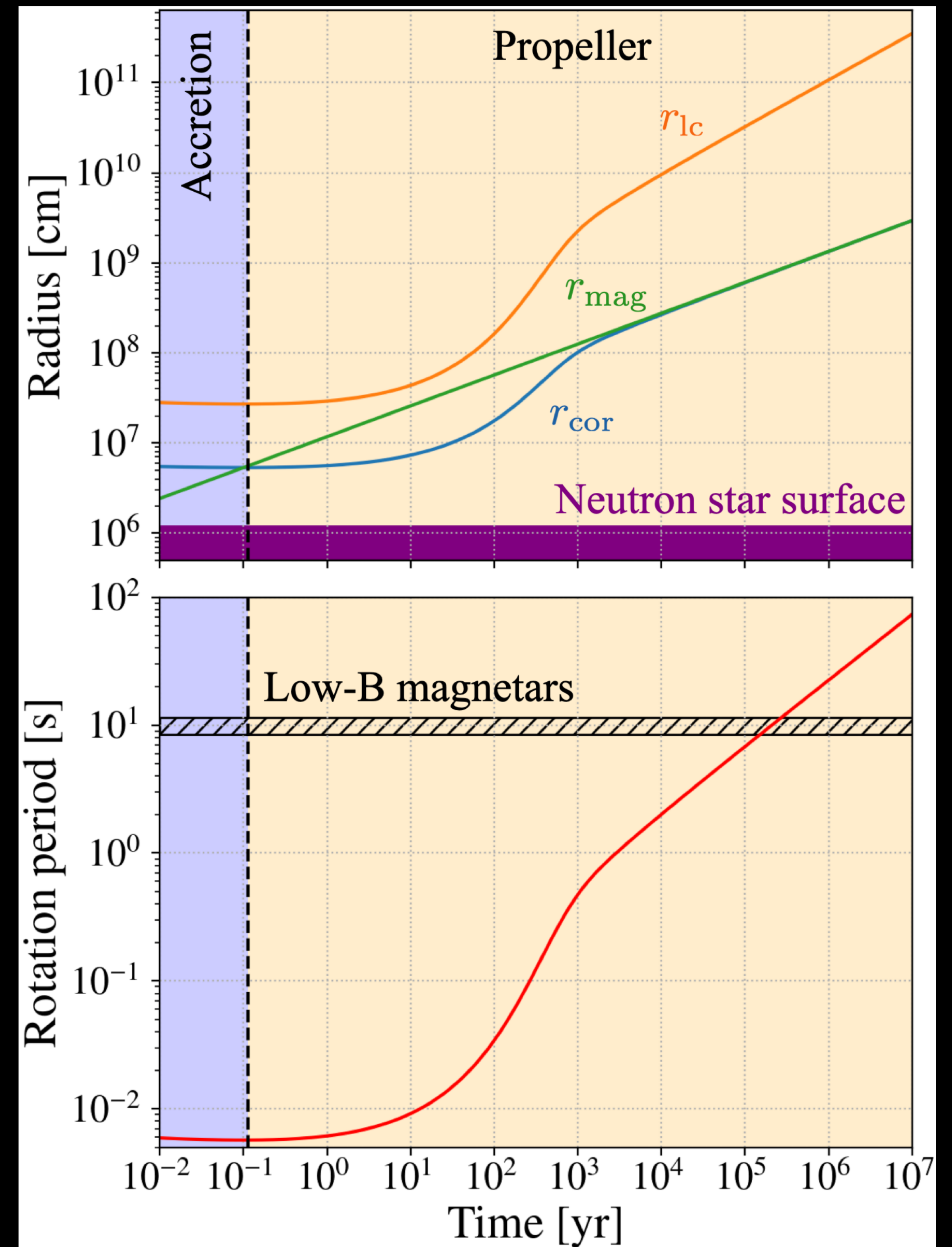
Lander & Gourgouliatos (2019) model



# Spin period

## Fallback disk

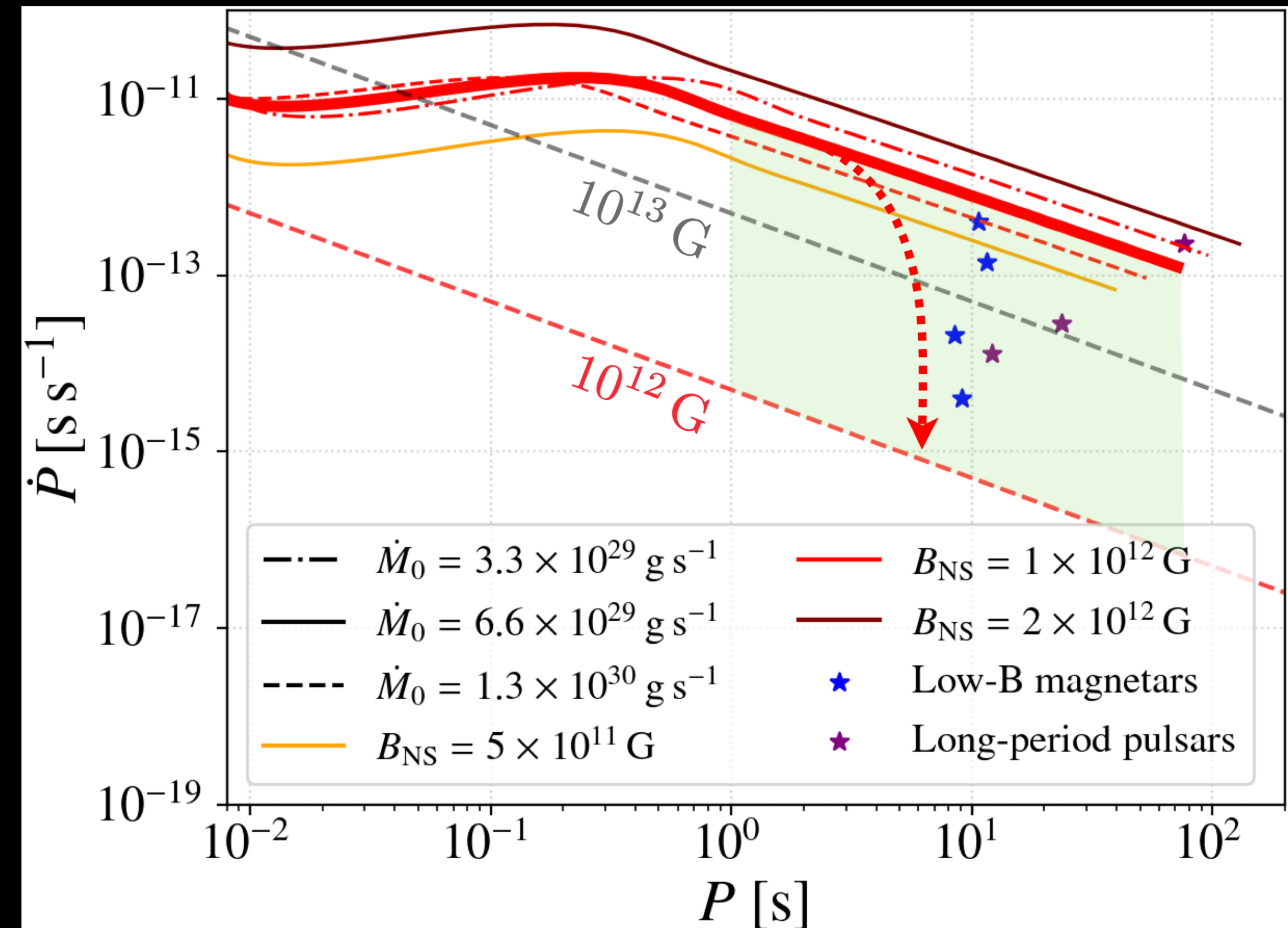
- Long periods  $> 1$  sec cannot be reached using the dipolar braking.
- Tayler-Spruit dynamo requires significant fallback accretion to operate.
- If fallback continues, it will decelerate neutron star in the propeller regime. The neutron star reaches spin periods  $\sim 10$  sec by 200 kyr.
- Simulations based on Gompertz et al. (2014) and Ronchi, Rea, Graber et al. (2022) but with  $\dot{M}_0 = 6.5 \times 10^{29}$  g/s based on TS dynamo simulations.



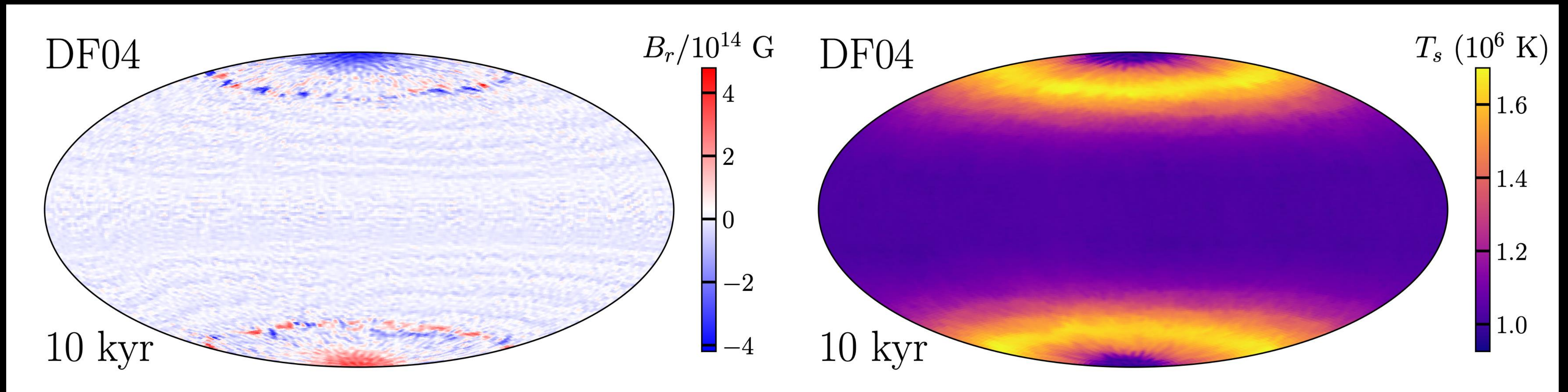
# Spin period

## Fallback disk

- The period derivative depends on the state of the fallback disk. If the fallback disk is partially (completely) depleted, the period derivative is closer to magnetospheric spin-down.
- At older ages these objects could turn into long-period pulsars.

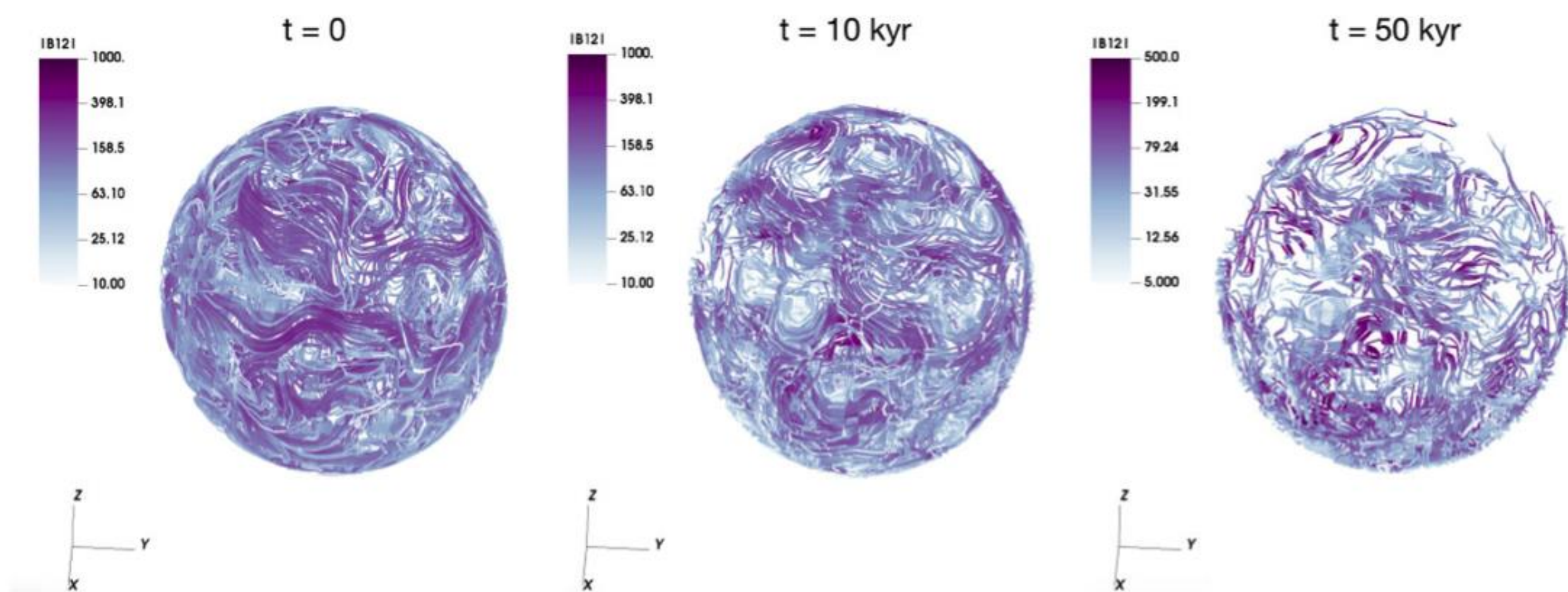
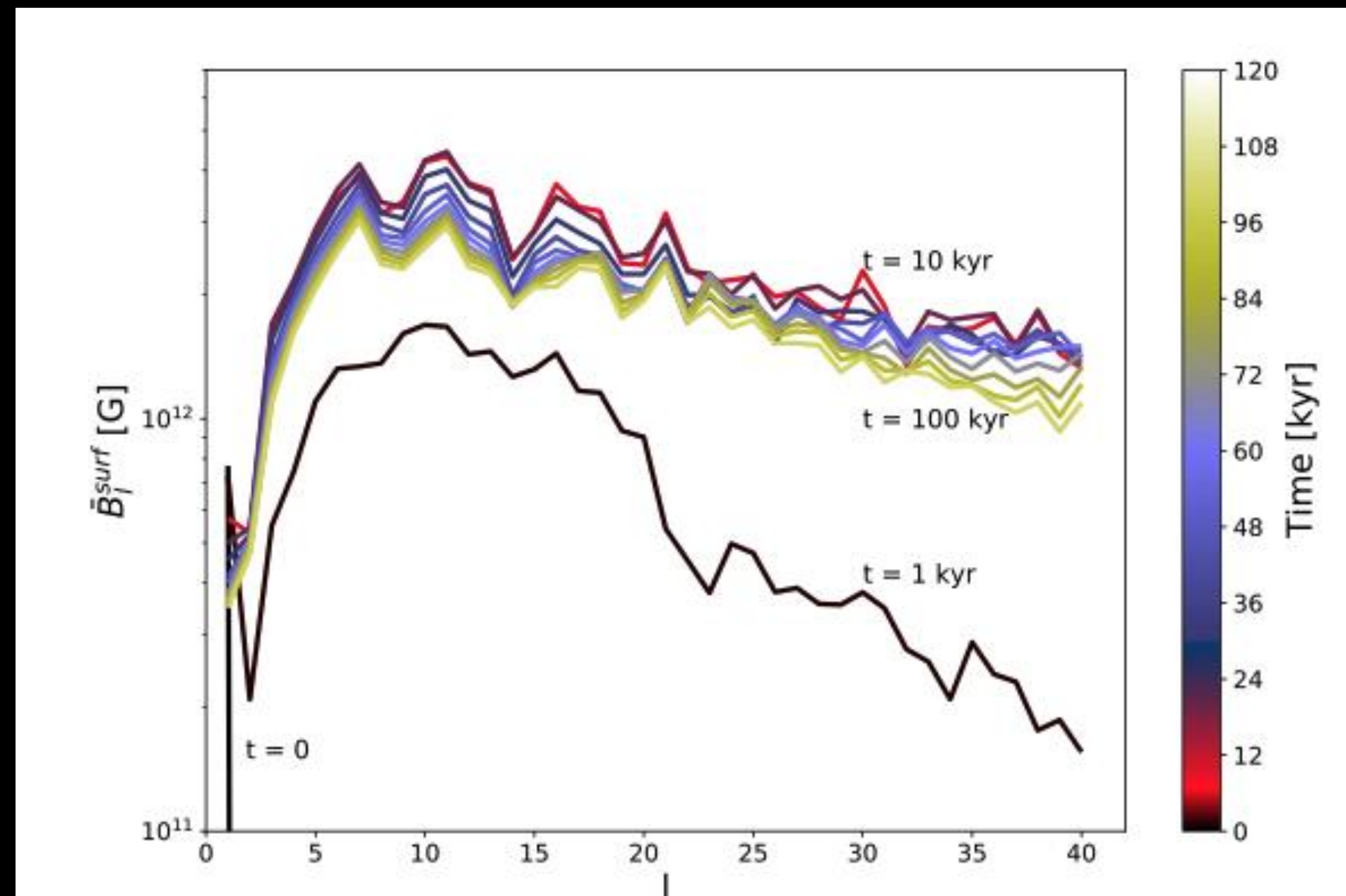


# New volumetric forcing

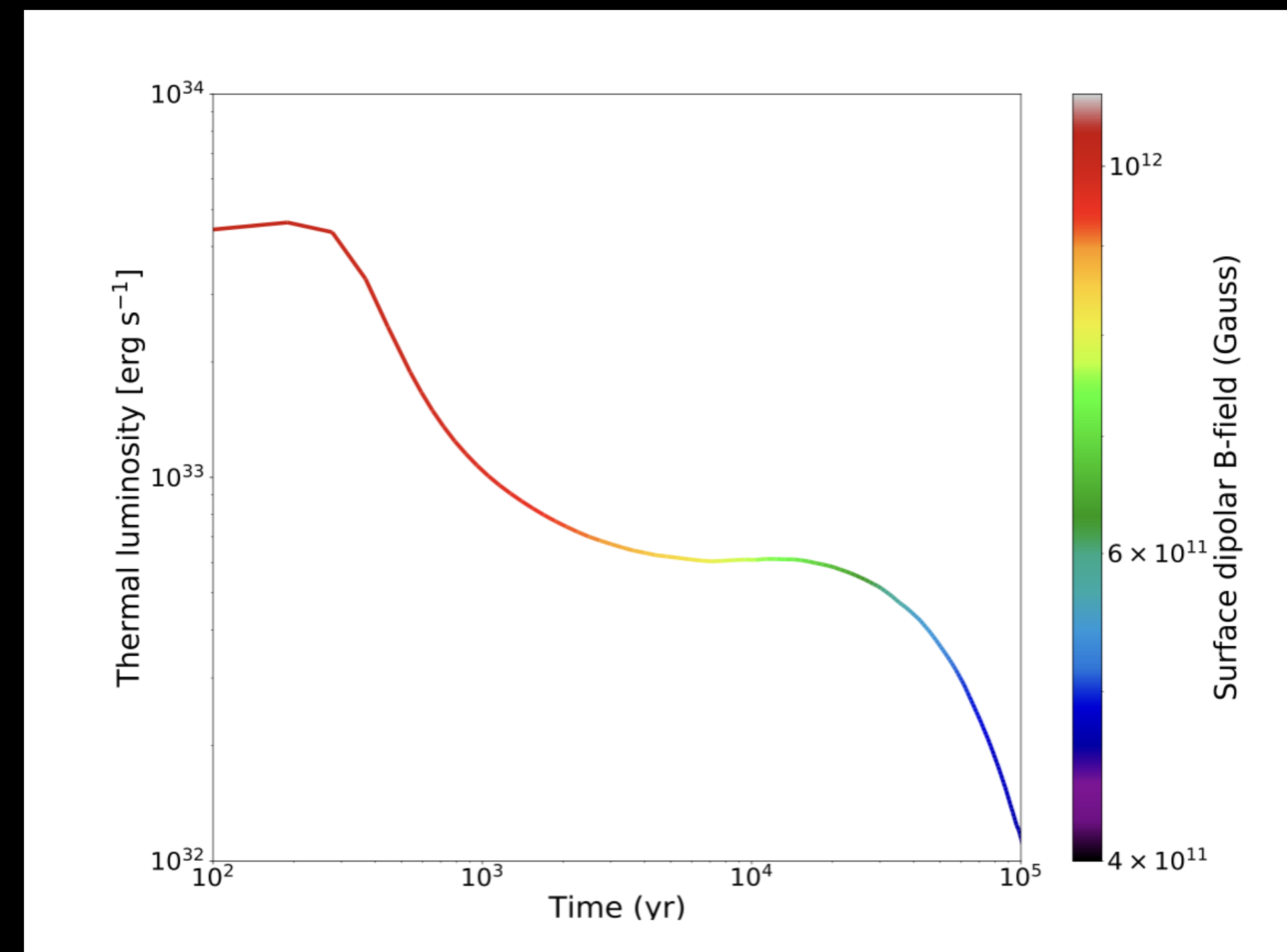


# MRI dynamo

- Dehman et al. (2023) found no growth of dipolar magnetic field, however X-ray luminosities are enhanced and could explain CCOs.



**Figure 4.** Field lines in the crust of an NS at  $t = 0$  (on the left),  $t = 10$  kyr (in the centre), and  $t = 50$  kyr (on the right). The colour scales indicates the local field intensity in units of  $10^{12}$  G.



# Core superconductivity

The background of the slide features a complex, dark gray pattern of magnetic field lines. These lines are arranged in a series of concentric, roughly circular loops that appear to emanate from a central point. The lines are more densely packed in some areas and more spread out in others, creating a textured, almost crystalline appearance. In the lower-left and lower-right quadrants, there are faint, light-colored labels 'N' and 'S' respectively, which likely represent the North and South poles of a magnetic field source. The overall effect is that of a magnetic field visualization, possibly from a scanning tunneling microscope or a similar high-resolution imaging technique.

# MHD-like approach

- Our model rely on Hall-Vinen-Bekharevich-Khalatnikov (HVBK) two-fluid model for describing superfluid/superconductor as a sum of a few fluids. We closely follow prescription developed by Glampedakis, Andersson & Samuelsson (2011) with simplifications by Graber, Andersson, Glampedakis & Lander (2015).

# Single fluid system

$$\frac{\partial \vec{u}_c}{\partial t} = -\nabla \delta\mu_c + \frac{(\vec{\nabla} \times \vec{H}_{c1}) \times \vec{B}}{n_c} + \nu f(u_c)$$

$u_l$  is the vortex velocity  
Ohmic term is for numerical stability

$$\frac{\partial \vec{B}}{\partial t} = \vec{\nabla} \times (\vec{u}_l \times \vec{B}) + \frac{\vec{\nabla}^2 \vec{B}}{\text{Rm}}$$

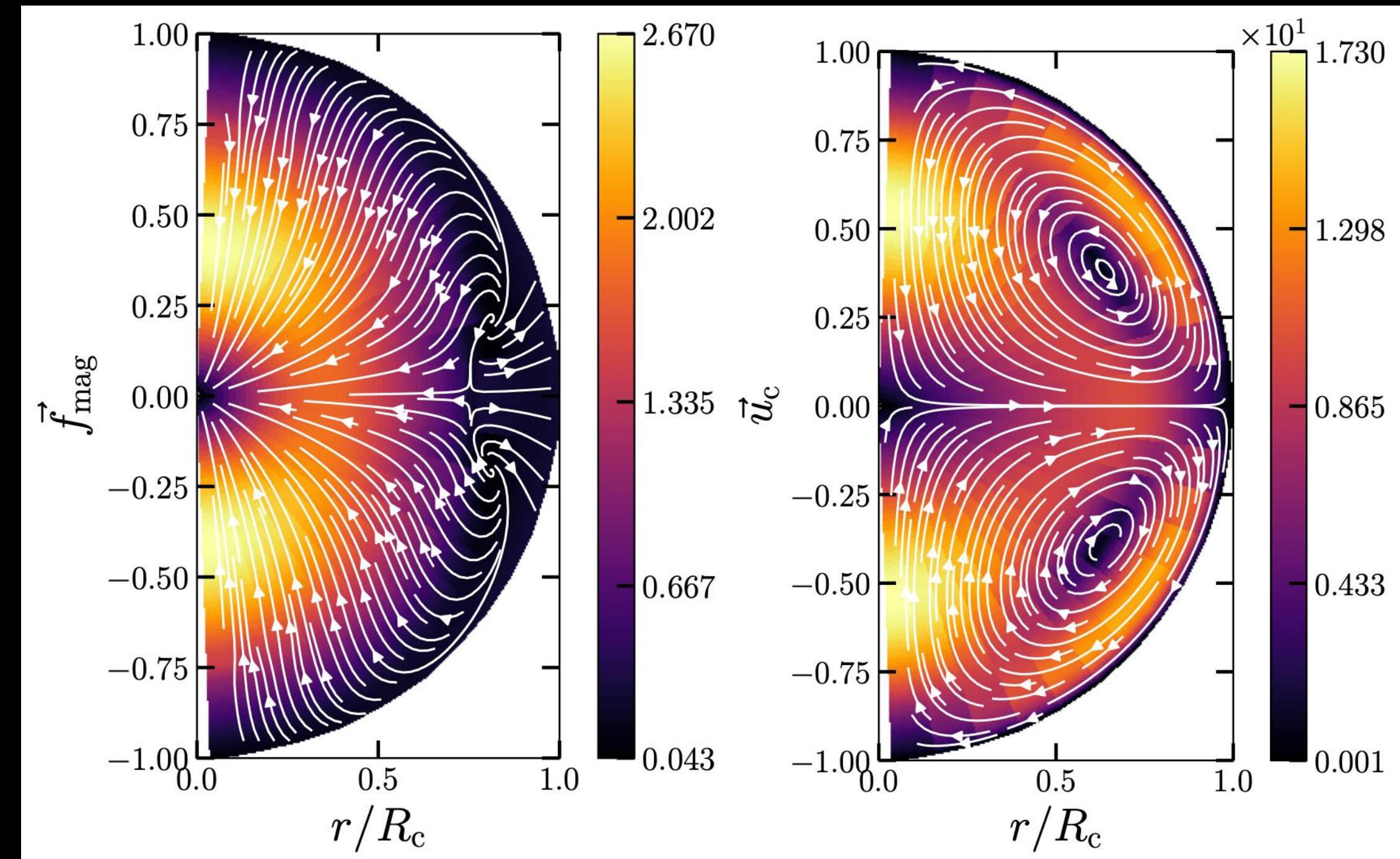
Viscosity due to electron - electron scattering

$$\vec{\nabla} \cdot (n_c \vec{u}_c) = 0 \quad \vec{\nabla} \cdot (\vec{B}) = 0$$

$$\left. \frac{\partial B^l}{\partial r} + \frac{l+1}{r} B^l \right|_{r=R_{\text{NS}}} = 0 \quad J_r = 0$$

Stress-free boundary condition

$$\int \delta\mu_c dV = 0$$



# Boundary conditions

Vacuum

$$\frac{\partial B^l}{\partial r} + \frac{l+1}{r} B^l \Big|_{r=R_{\text{NS}}} = 0$$

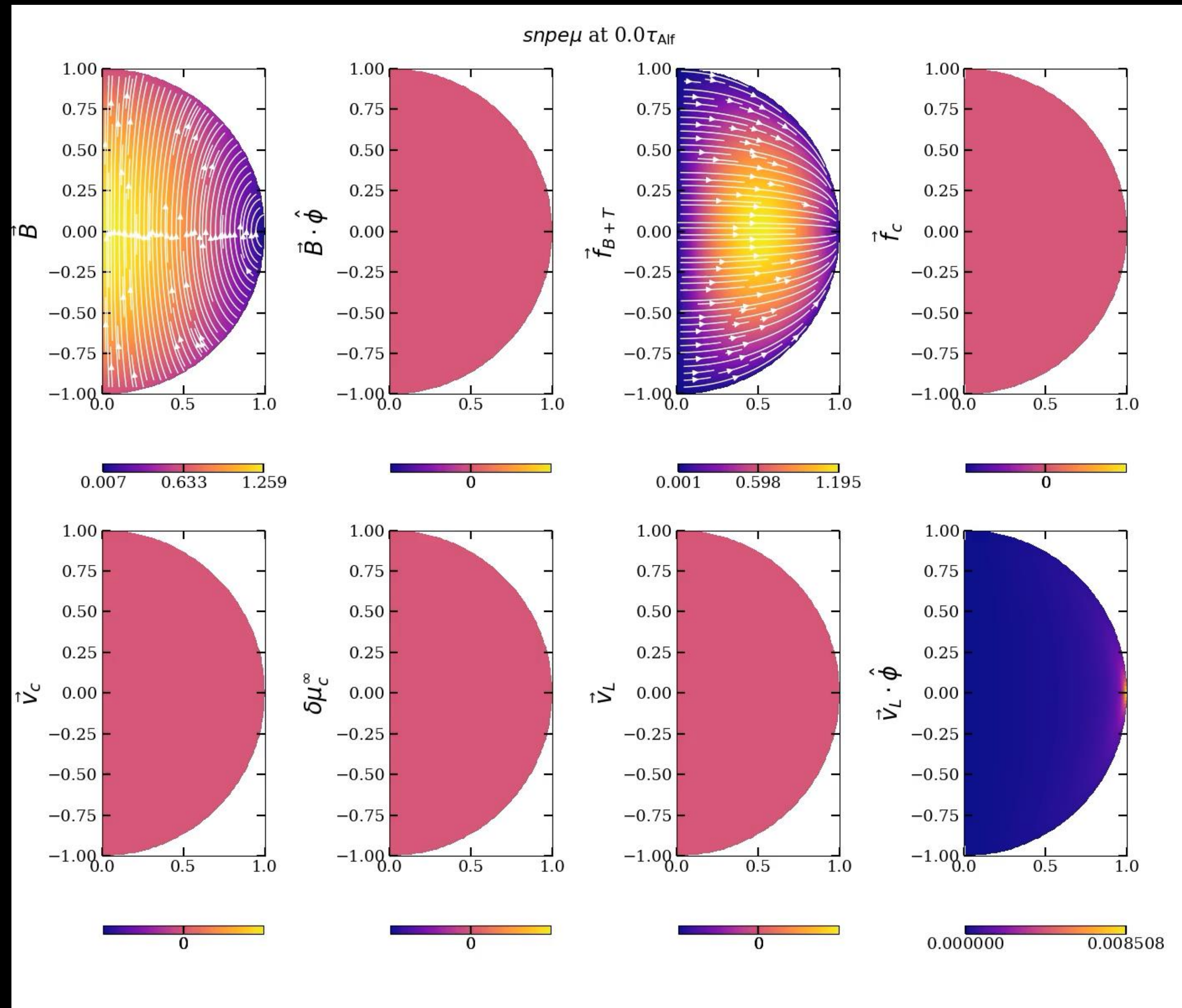
Pseudo-vacuum

$$B_\phi = B_\theta = 0$$

Field lines approaches surface orthogonally

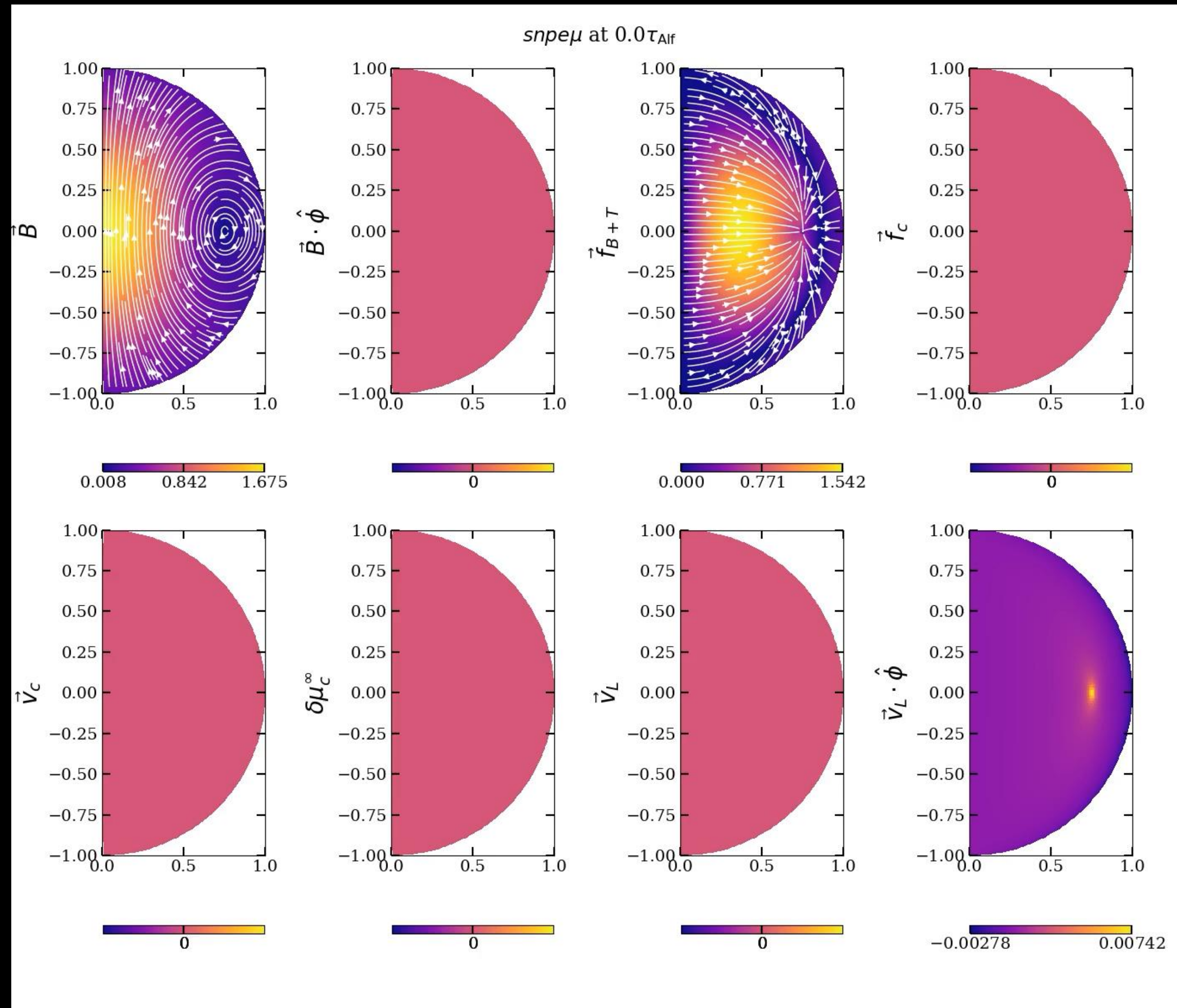
# 2D axial symmetry

Evolution towards stable configurations

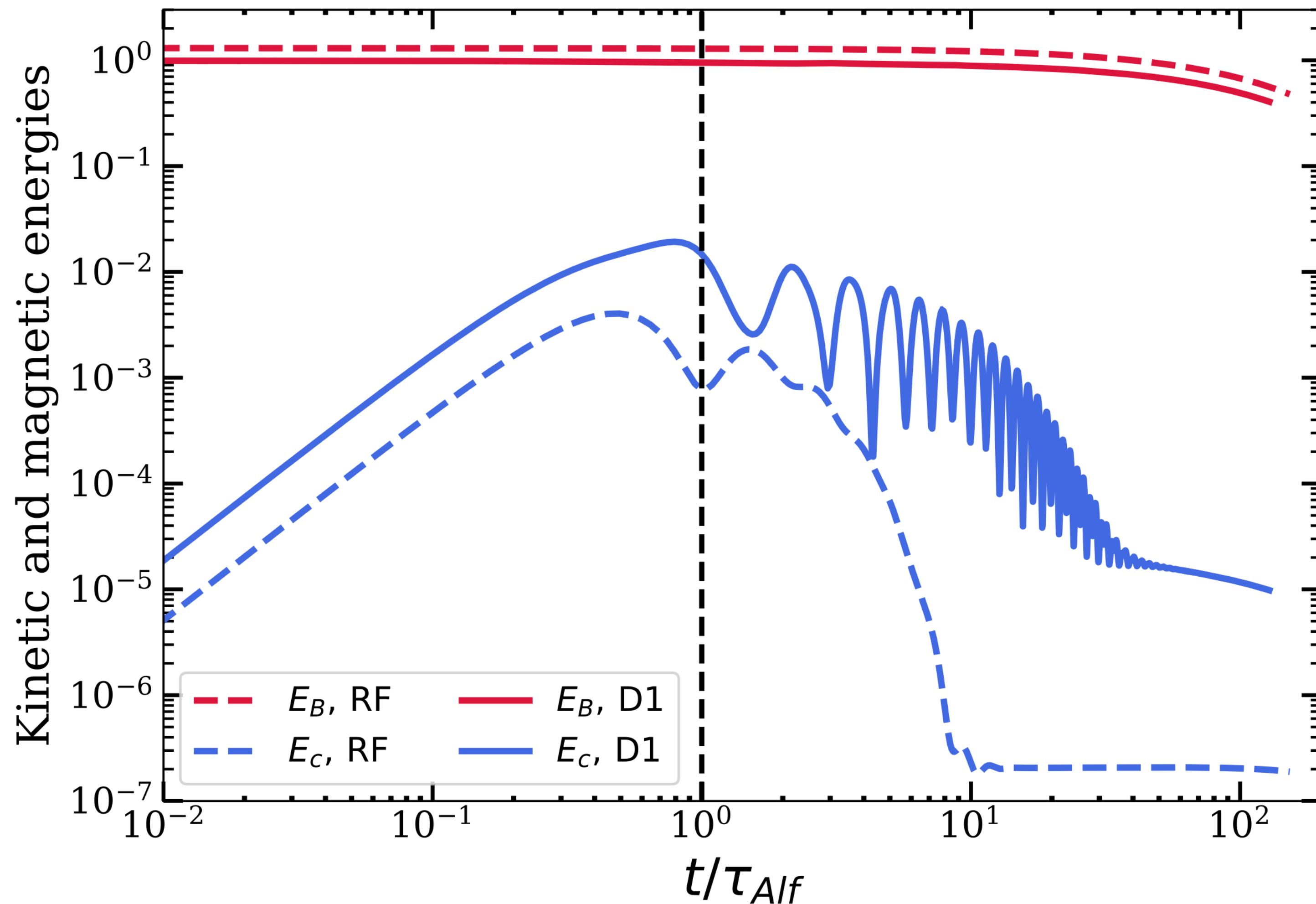


# 2D axial symmetry

Evolution towards stable configurations

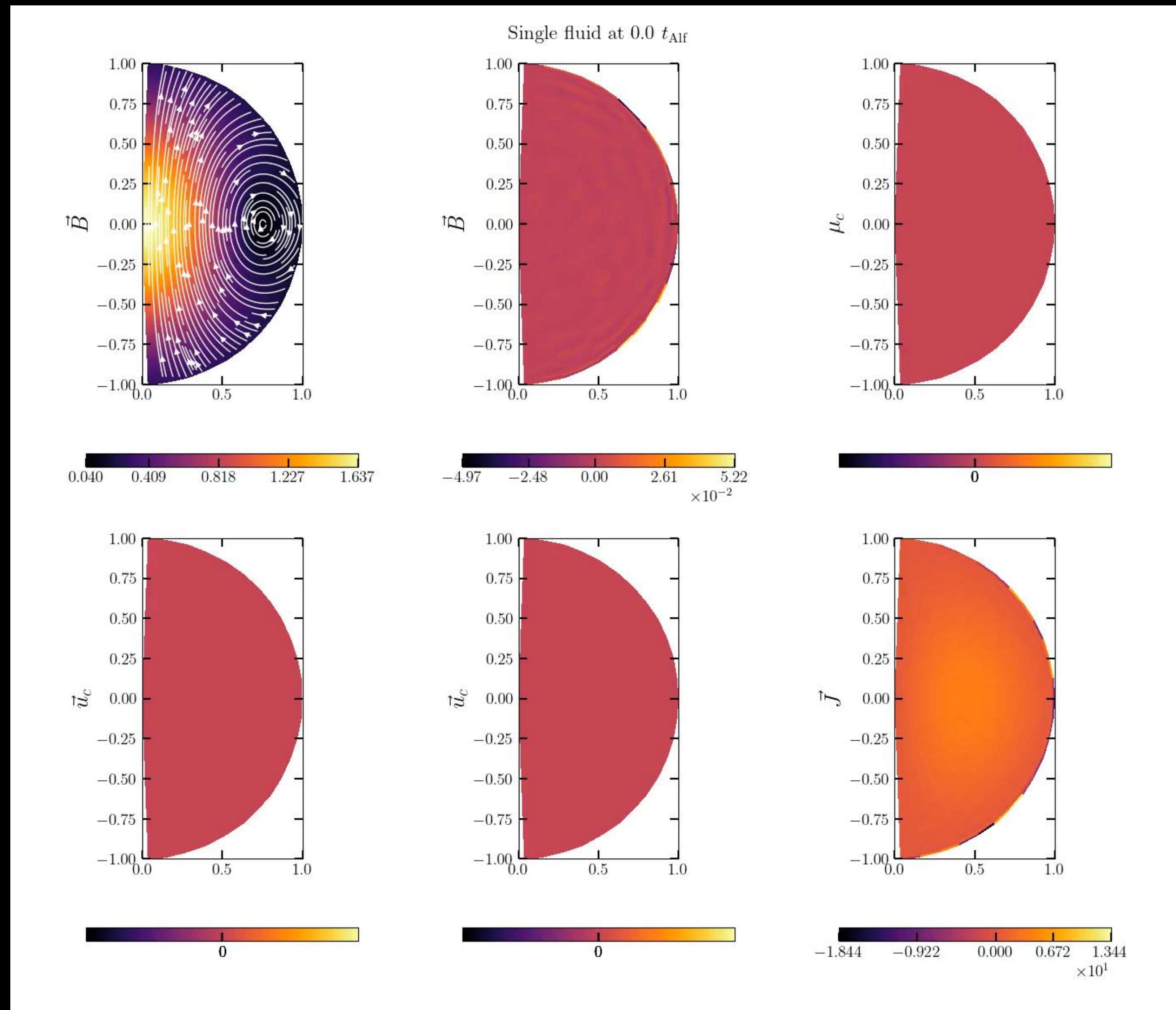


# Energy evolution



# 3D simulations

$$v_l = v_c$$



# Summary and future work

- Magnetic fields of neutron stars are very complicated and might be the key to understand the NS diversity.
- Different types of neutron stars such as magnetars, XDINS, CCOs might be produced due to different type of dynamo mechanisms active at the proto-NS stage
- Convective dynamo combined with fast rotation might be responsible for classical magnetars; Tayler-Spruit for low-B magnetars and MRI for Central Compact Objects.
- Magnetic field evolution in the core is just started to be explored. Non-trivial interactions between the core and crust might lead to different energetic phenomena