

# Constraining neutron star properties with current and future gravitational wave observations of glitching pulsars

SCALES Ist General Meeting - Superfluid Condensates in Astrophysics and Laboratory Experiments |  
Coimbra - Portugal

Matthew Ball & David Keitel

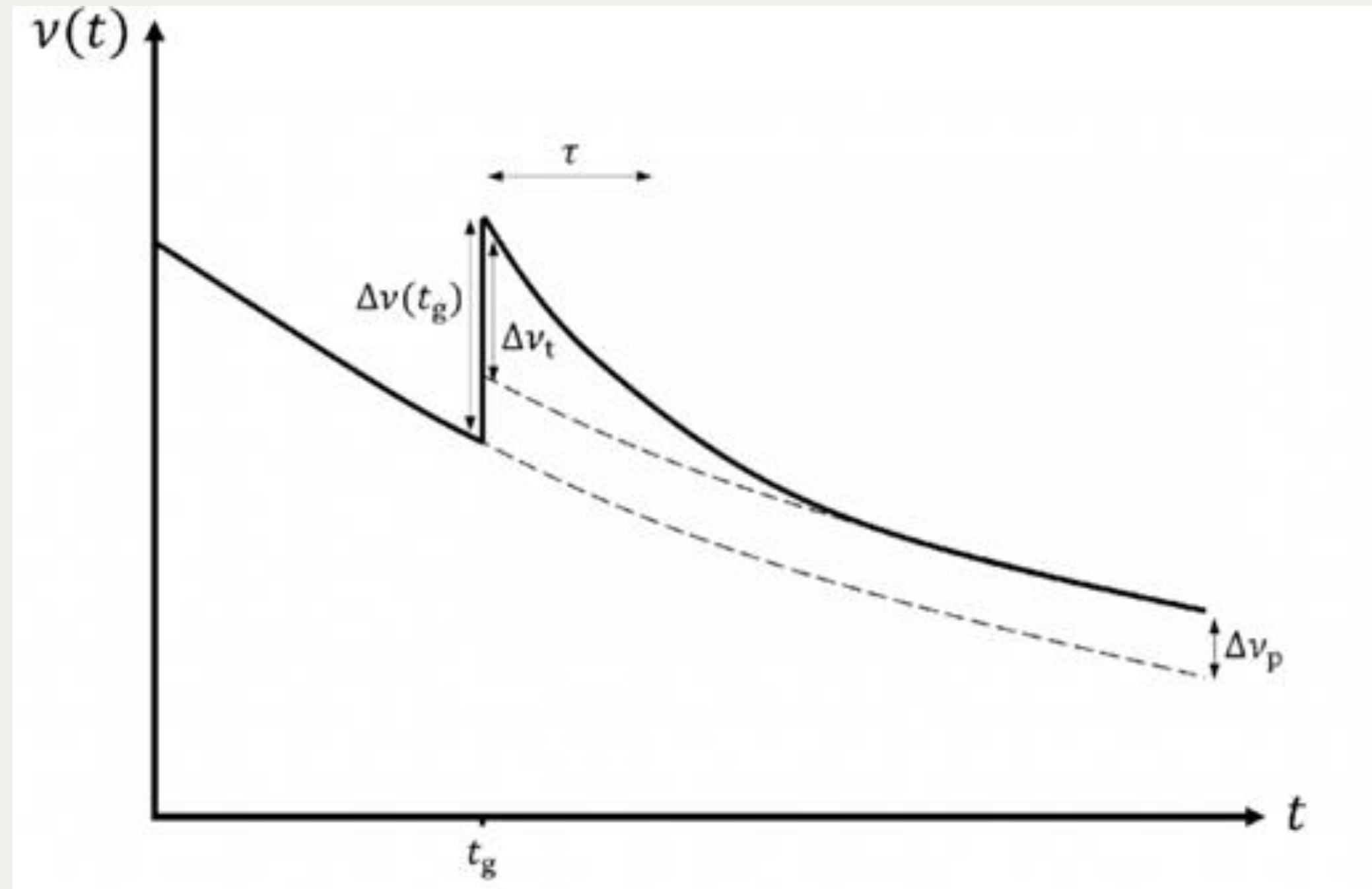
IAC3-IEEC, Universitat de les Illes Balears, E-07122 Palma de Mallorca, Spain

- Search for Gravitational Waves from the 2024 Vela Glitch
  - Details of the search target
  - Results from the search for continuous gravitational waves
  - Results from the search for gravitational wave bursts
  - Astrophysical implications
- Future projections
  - Population-based estimates of future detectability
  - What if the 2024 Vela glitch occurred with different next-generation GW detectors online



# Pulsar glitches

- Sudden increases in rotation speed followed by faster decay (Antonopoulou et al. 2022)
- Believed to be due to exchange of momentum between the crust and a superfluid in the interior (e.g. Haskell & Melatos 2015; Zhou et al. 2022)



Exaggerated diagram of a glitch. Image credit: Yim & Jones 2020

# Gravitational wave signals from a glitch

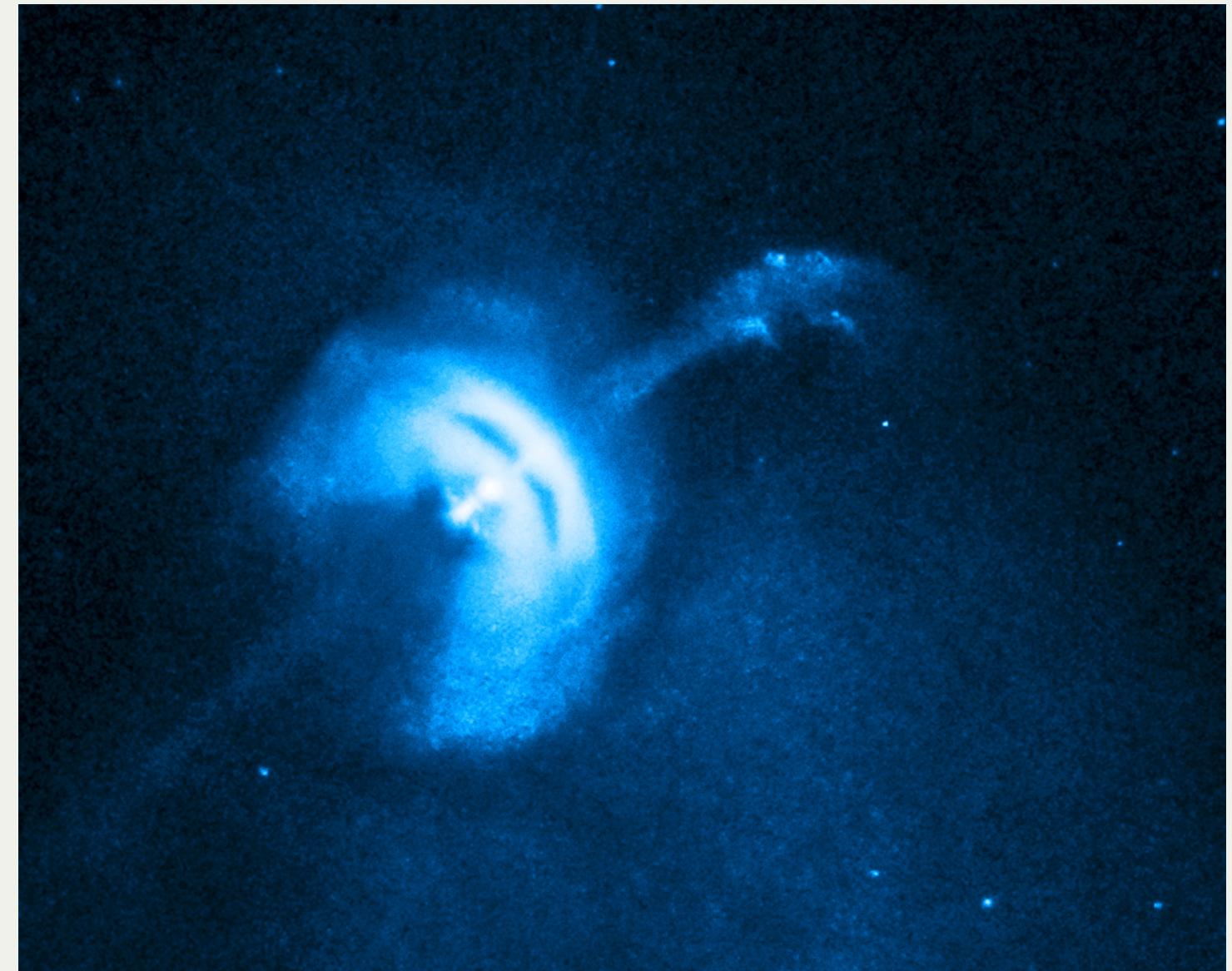
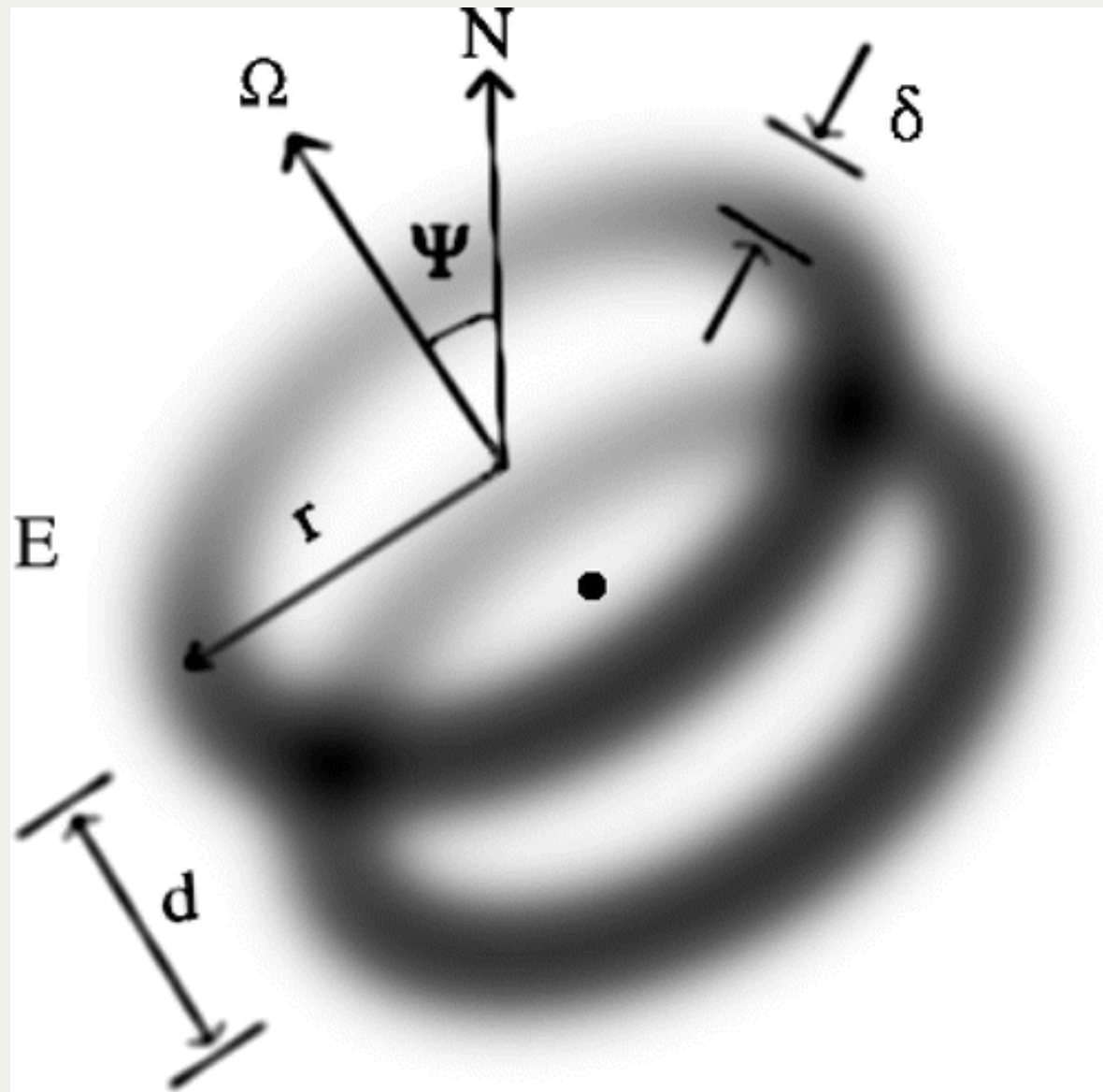
- Small change in moment of inertia may lead to (transient) continuous GW (tCW) emission at  $1\times$  or  $2\times$  the rotation frequency
  - Deformation of the crust (mountains) due to internal mechanisms (such as elastic fracture, superfluid unpinning)
    - Relaxation of this deformation is attributed to the recovery time
- Induced short-duration oscillations during the initial spin-up possibly due to unpinning of superfluid vortices (e.g. Andersson & Kokkotas 1998)
  - Up to a few seconds in duration
  - Hundreds to a few thousand Hz in frequency

# Constraints on gravitational waves from the 2024 Vela pulsar glitch

Based on A. G. Abac et al 2026 ApJ 1005 12 (arXiv:2512.17990)

# The Vela pulsar

- Rotation rate [Hz]:  $(11.182888898688 \pm 0.0000000000002)$  (IAR; MPRO)
- Distance [pc]:  $287_{-17}^{+19}$  (Dodson et al. 2003)
- Orientation from wind nebula (Ng & Romani 2008)

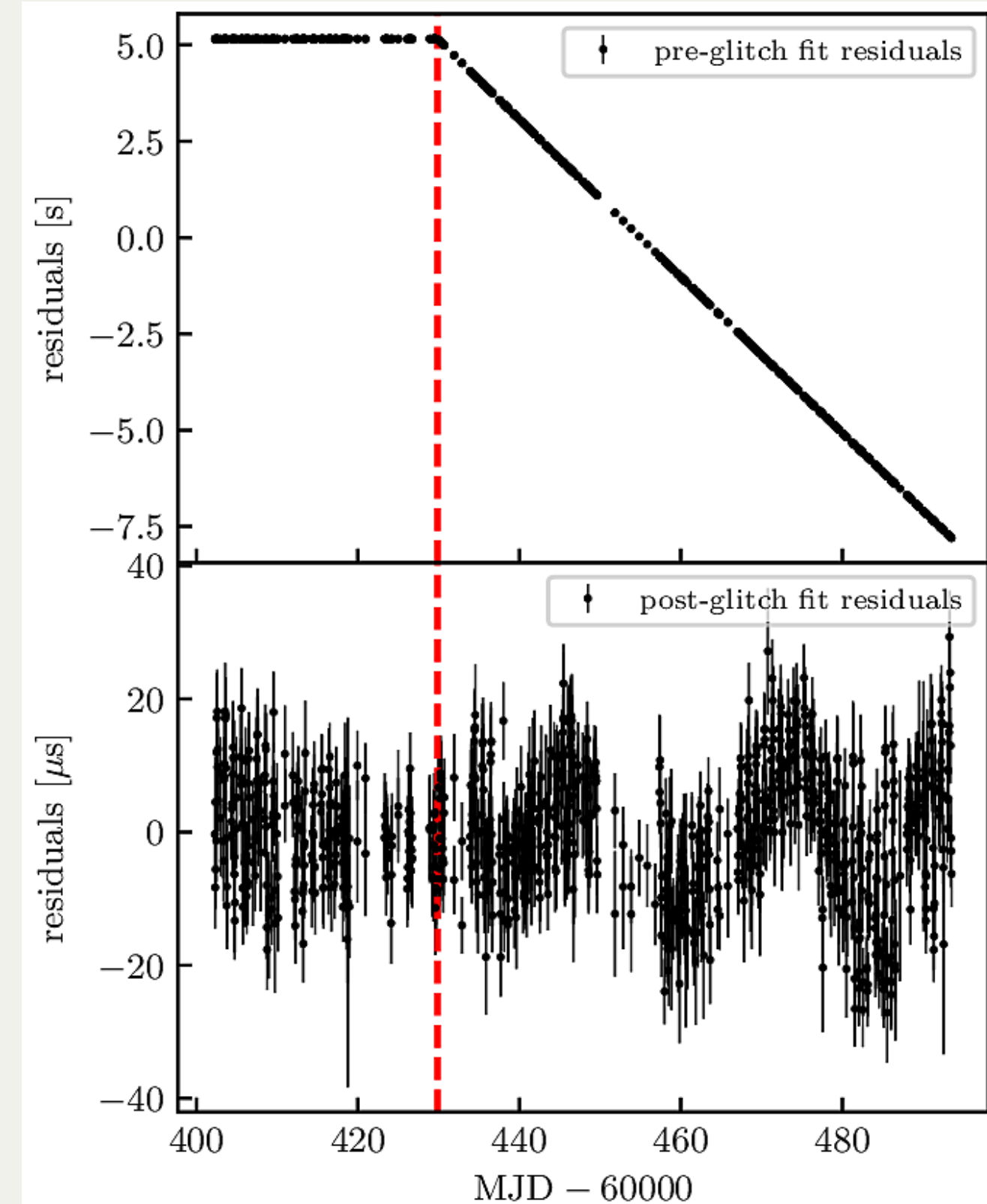


Schematic diagram of wind nebula used to compute Vela orientation. Image credit: Ng & Romani 2008

Vela pulsar jet in x-rays. Image credit: NASA/CXC/Univ. of Toronto/M. Durant, et al.

# Properties of the glitch (IAR; MPRO)

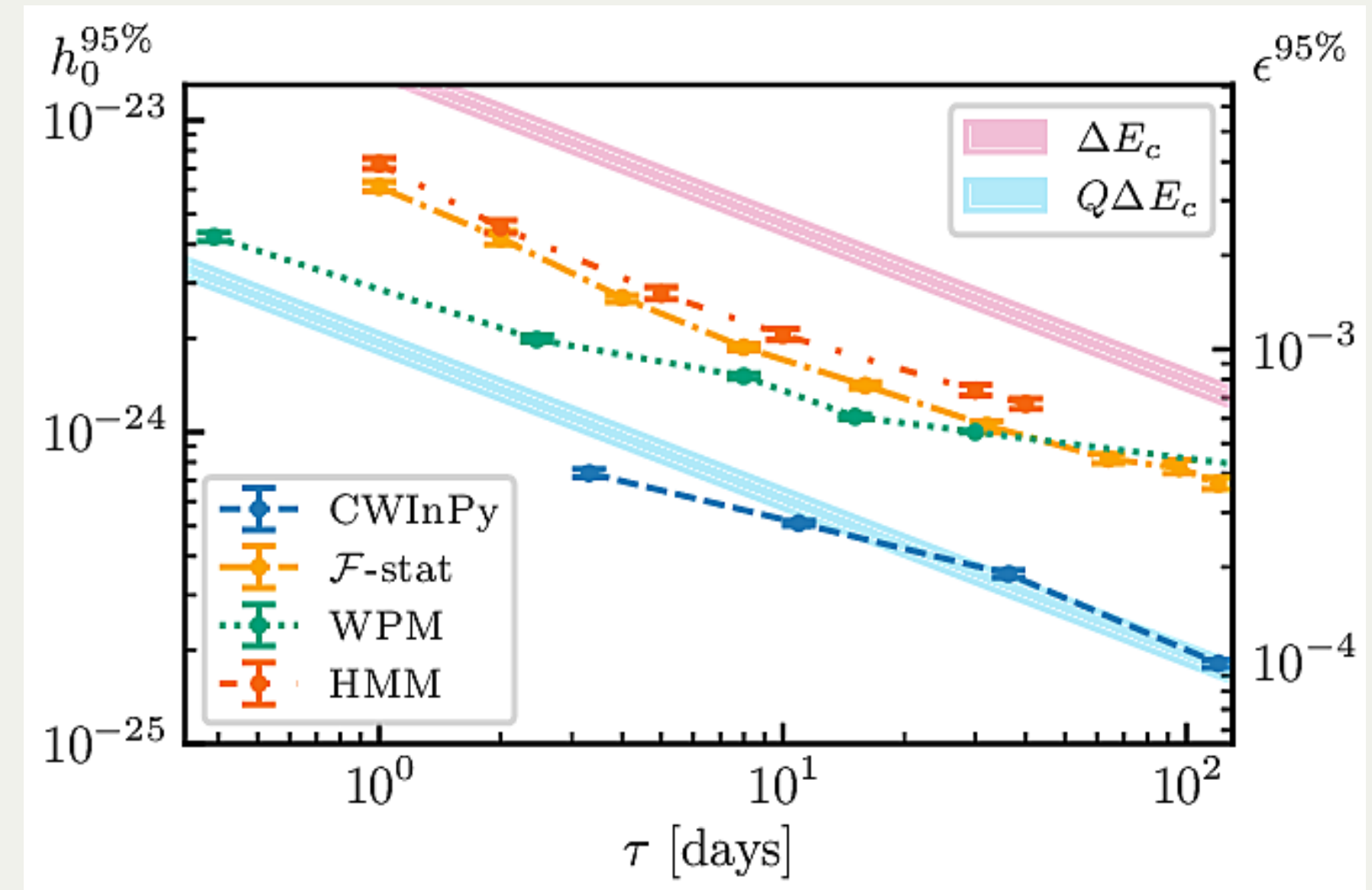
Parameter	Value
$T_{\text{gl}}$ [d] (MJD)	$60429.86975 \pm 0.00139$
$T_{\text{gl}}$ [s] (GPS)	$1398459095.216 \pm 120.096$
$\Delta f_{\text{rot}}$ [Hz]	$(2.65854 \pm 0.00005) \times 10^{-5}$
$\Delta \dot{f}_{\text{rot}}$ [Hz, s <sup>-1</sup> ]	$(-1.0298 \pm 0.0009) \times 10^{-13}$
$\tau_d^1$ [d]	$15.1 \pm 0.1$
$\Delta f_{\text{rot}}^{d,1}$ [Hz]	$(1.501 \pm 0.004) \times 10^{-7}$
$\tau_d^2$ [d]	$2.45 \pm 0.06$
$\Delta f_{\text{rot}}^{d,2}$ [Hz]	$(1.24 \pm 0.03) \times 10^{-7}$
$\tau_d^3$ [d]	$0.39 \pm 0.03$
$\Delta f_{\text{rot}}^{d,3}$ [Hz]	$(1.8 \pm 0.1) \times 10^{-7}$



Glitch fitting residuals (Abac et al. 2026)

# Continuous Wave search results

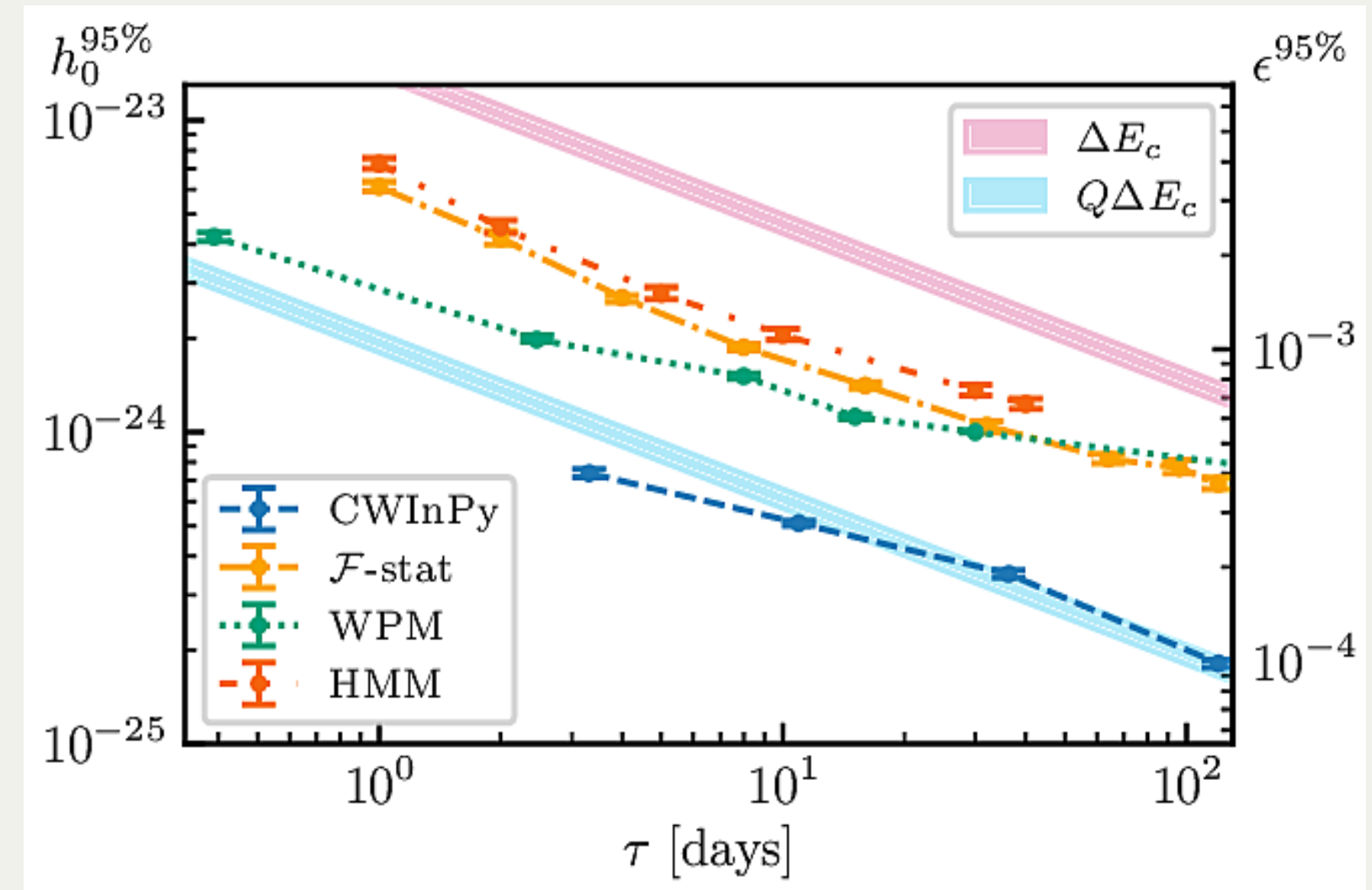
- Searches performed with multiple pipelines:
  - CWInPy (Pitkin 2022)
  - Transient  $\mathcal{F}$ -statistic search (Prix et al. 2011)
  - Weighted peakmap search (WPM) (Astone et al. 2005; Astone et al. 2014; Piccinni et al. 2019)
  - Hidden Markov model (HMM) (Jaranowski et al. 1998; Suvorova et al. 2016; Sun et al. 2018)
- No candidates found



(Abac et al. 2026)

# Continuous wave search implications

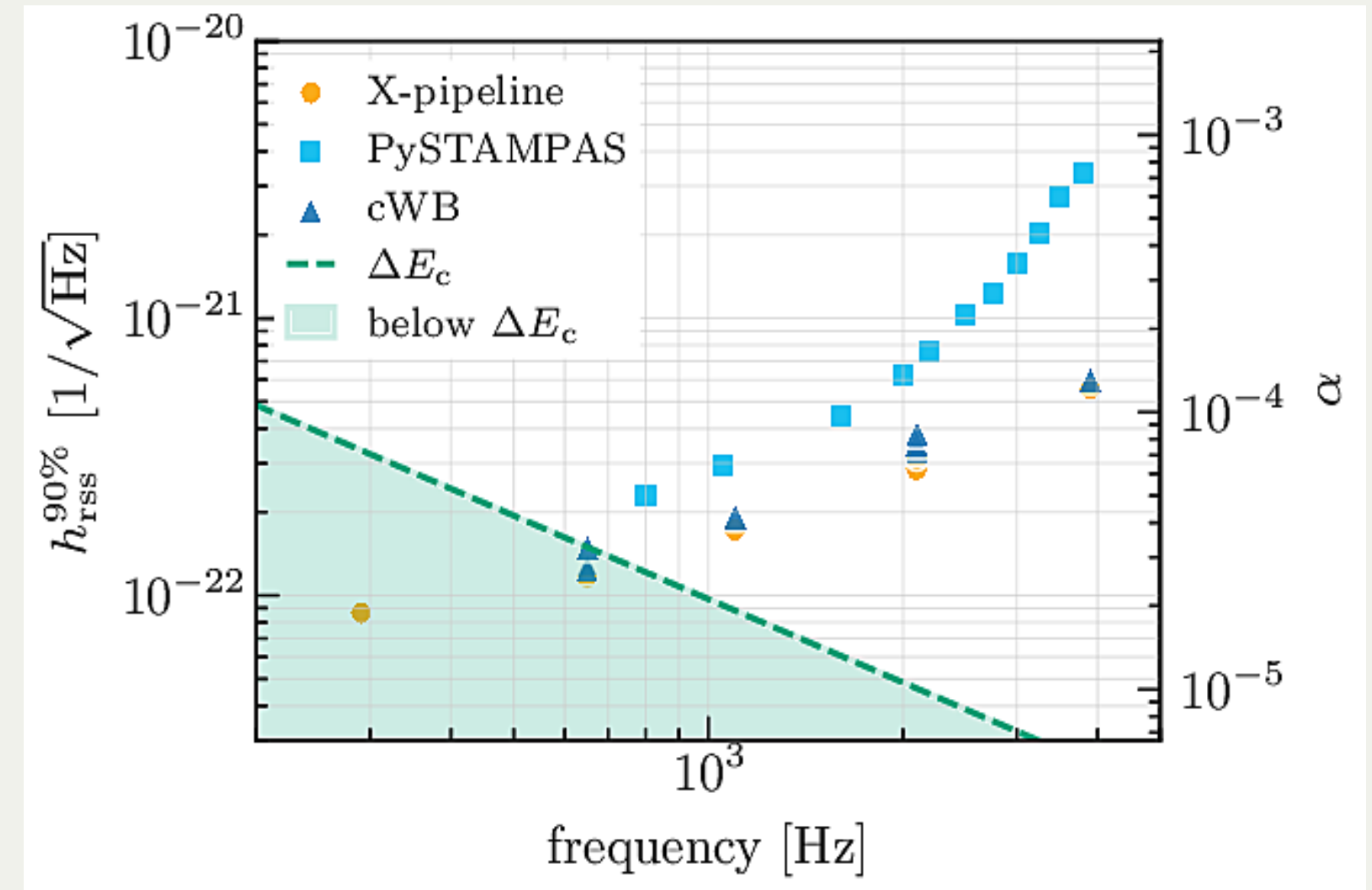
- Transient mountain model still below upper limits by most searches when including healing parameter  $Q$  (Yim & Jones 2020)
  - Barely probed by most restrictive CWInPy analysis
  - All analyses probe below characteristic energy  $\Delta E_c$



(Abac et al. 2026)

# GW burst search results

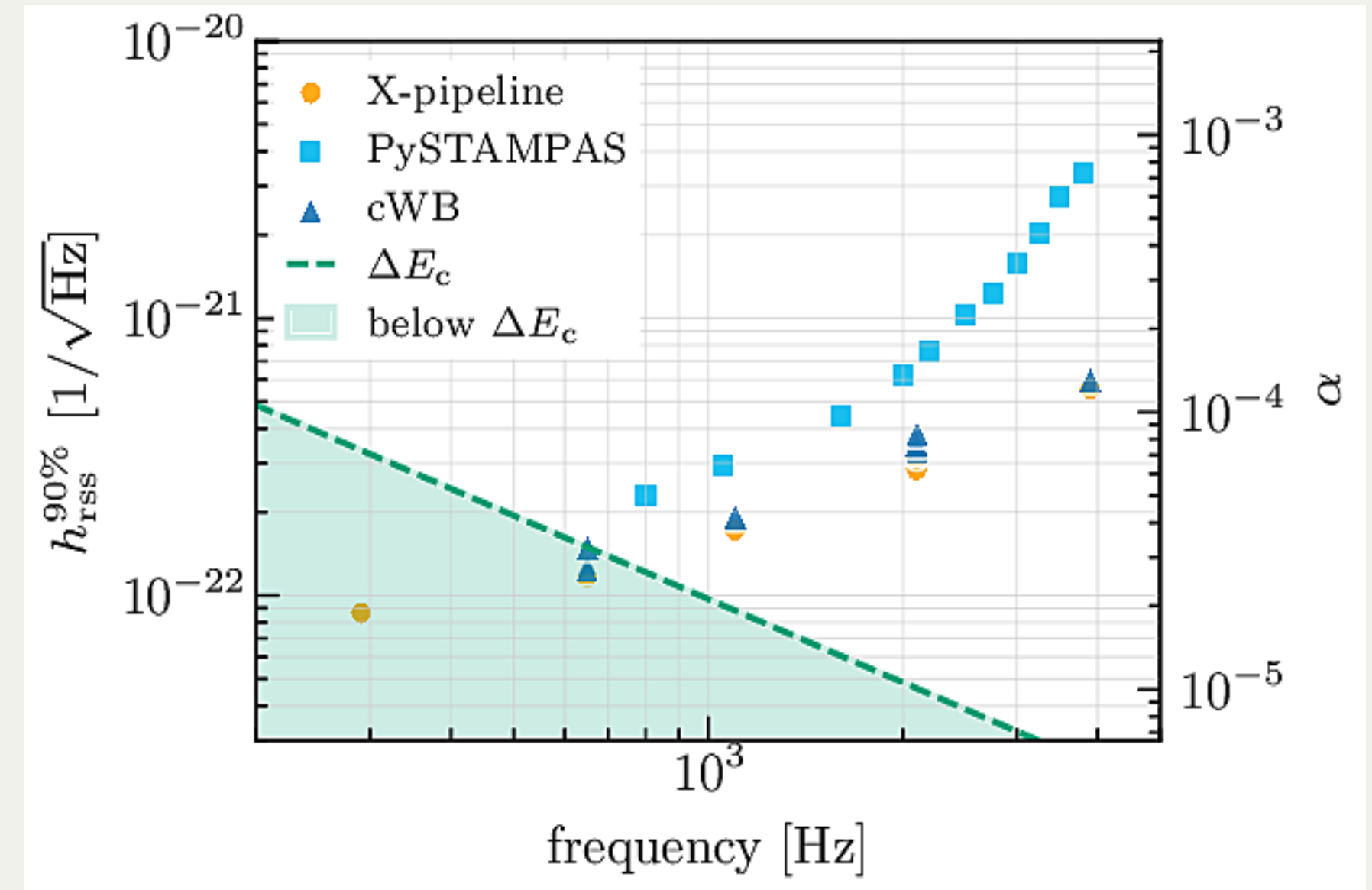
- Searches performed with multiple pipelines:
  - Coherent Wave Burst (cWB) (Klimenko et al. 2016; Drago et al. 2021; Martini et al. 2025)
  - pySTAMPAS (Macquet et al. 2021)
  - X-Pipeline (Sutton et al. 2010; Was et al. 2012)
- No candidates found



(Abac et al. 2026)

# GW burst search implications

- Searches probe below characteristic strain below about 800 Hz
- f-mode emission very unlikely at these low frequencies (Wilson & Ho, 2024)
- Upper limits can be converted into a limit on the physical deformation of the surface of the NS (Yim & Jones 2023)
  - For  $M = 1.4M_{\odot}$  and  $R = 10^6$  cm, the surface deformation is constrained to  $\lesssim 70$  cm

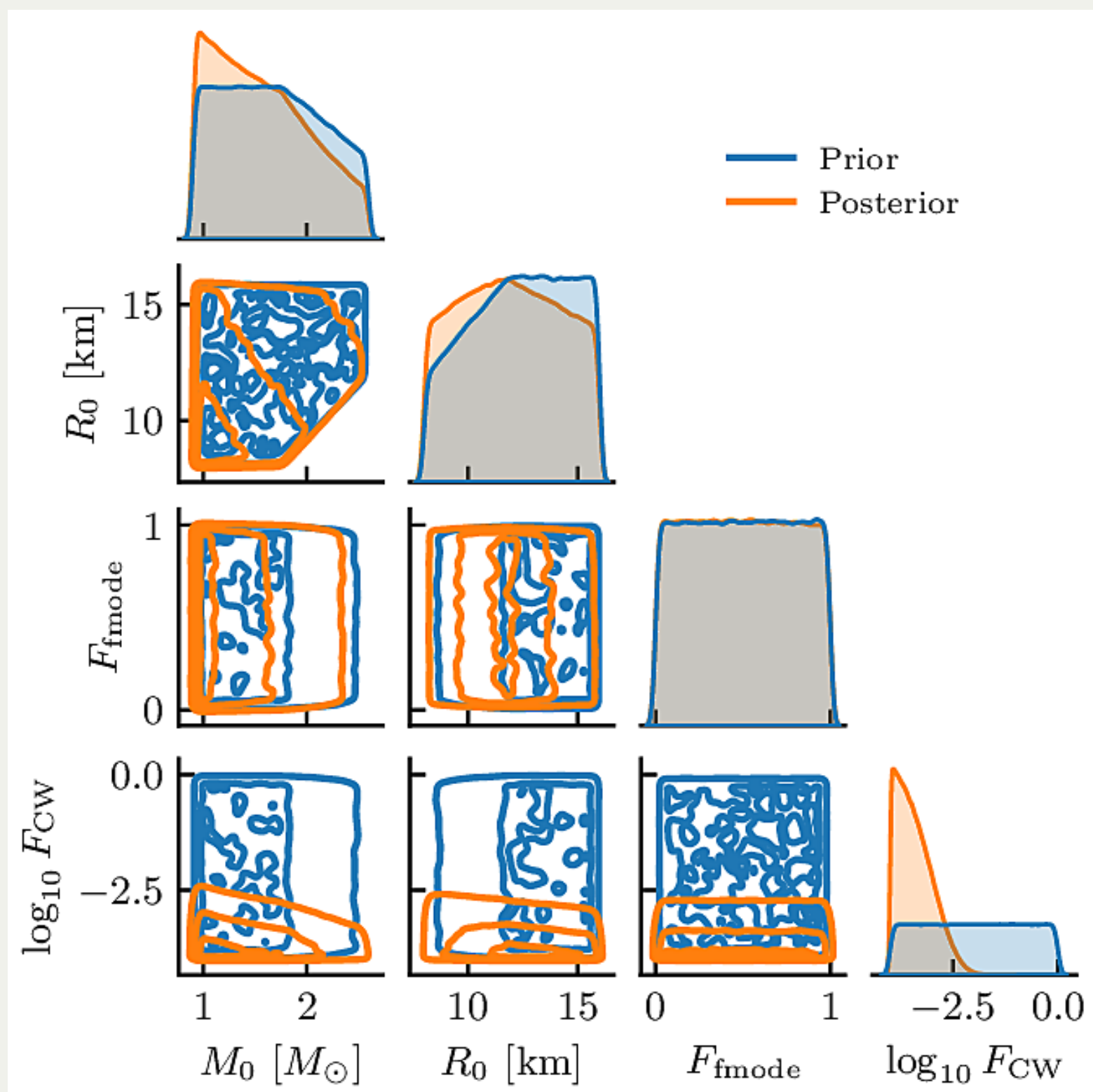


(Abac et al. 2026)

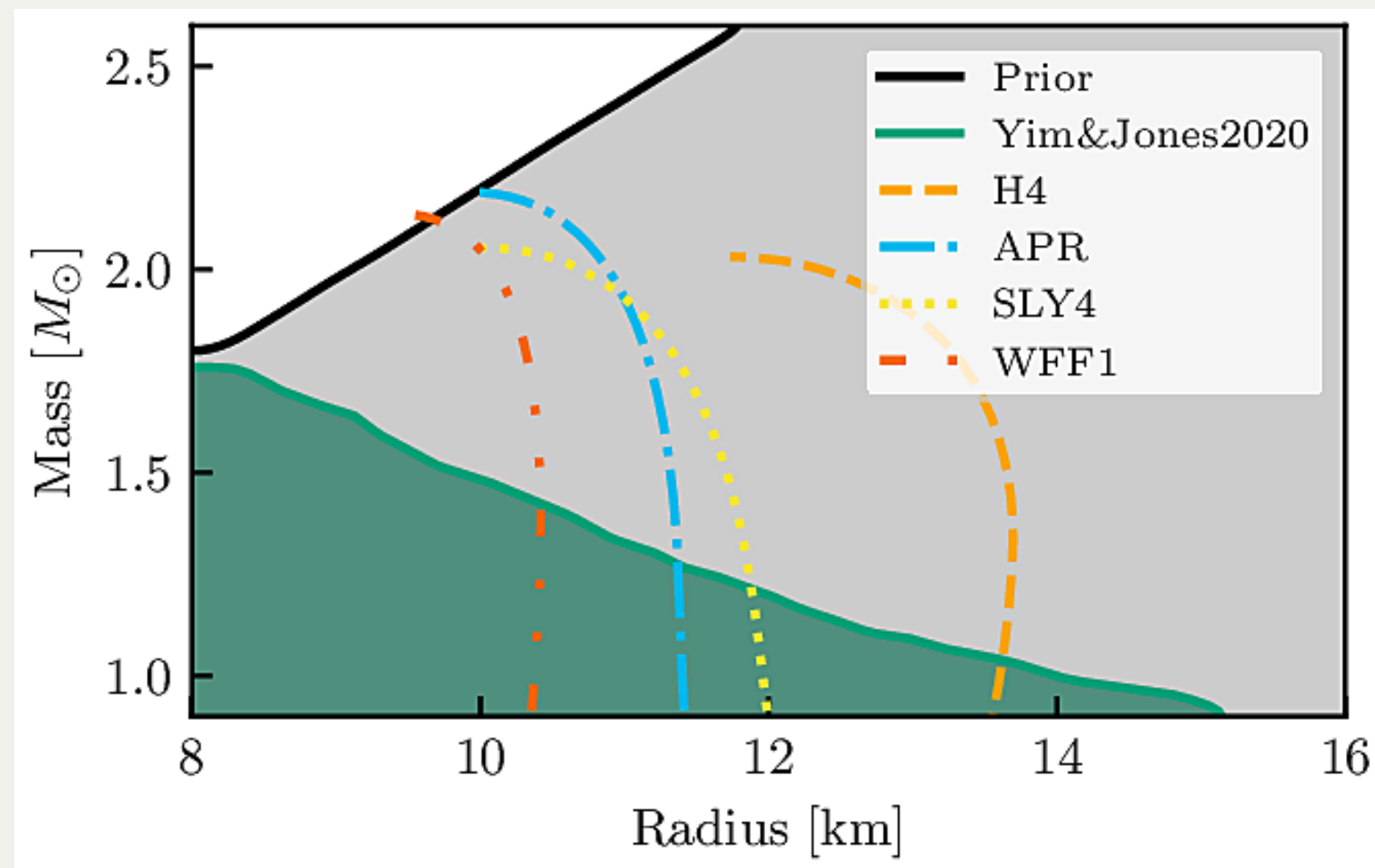
# Joint implications from non-detection

- Assume both a tCW and short GW burst were emitted but not detected
- Assume more parameterized model:
  - Transient mountain model for tCW
  - f-mode for burst
  - Energy in each channel given by fractions  $F_{\text{fmode}}$  and  $F_{\text{CW}}$  relative to characteristic energy
 
$$\Delta E_c = 4\pi^2 I_{zz} \nu_s \Delta \nu_s$$
- Use results from most sensitive (optimistic) pipeline from each search
  - CWInPy for tCW
  - X-Pipeline for burst
- Use equation-of-state independent universal relations to connect mass and radius to the moment of inertia (Yagi & Yunes, 2017) and f-mode frequency & damping time (Pradhan et al. 2022)

# Joint implications from non-detection



Allowing  $F_{\text{fmode}}$  and  $F_{\text{CW}}$  to freely vary (Abac et al. 2026)



Constraining  $F_{\text{fmode}} = 0.8$  and  $F_{\text{CW}} = Q$  (Abac et al. 2026)

# Prospects for Simultaneously Detecting Long and Short Duration Gravitational Waves from Pulsar Glitches with Current and Future Detectors

Work in progress

# Future detector networks

- Expect both Cosmic Explorer (Evans et al. 2021; Srivastava et al. 2022) and the Einstein Telescope (Branchesi et al. 2023) in the next few decades
- Anticipate an order of magnitude increase in sensitivity over current generation

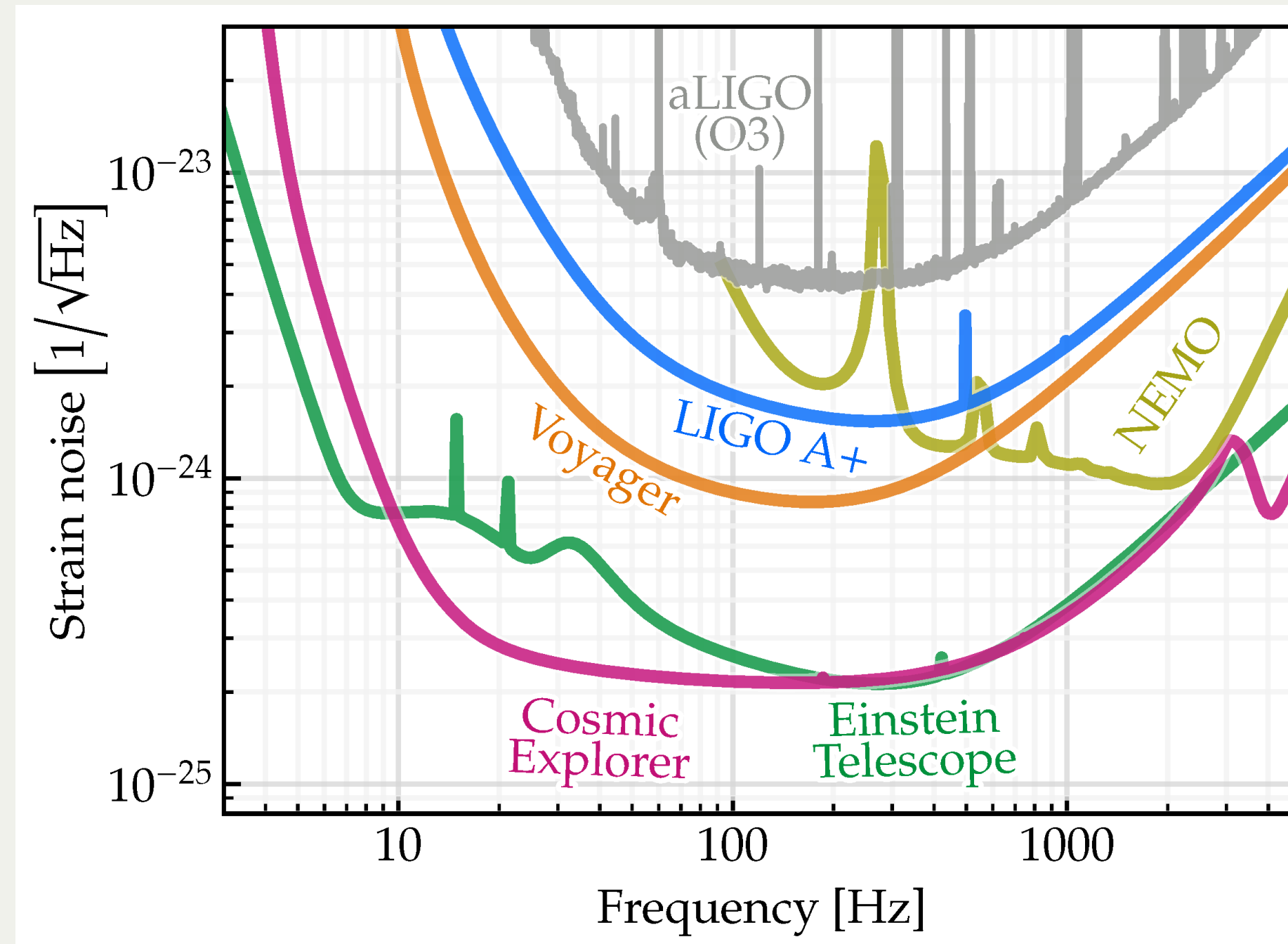


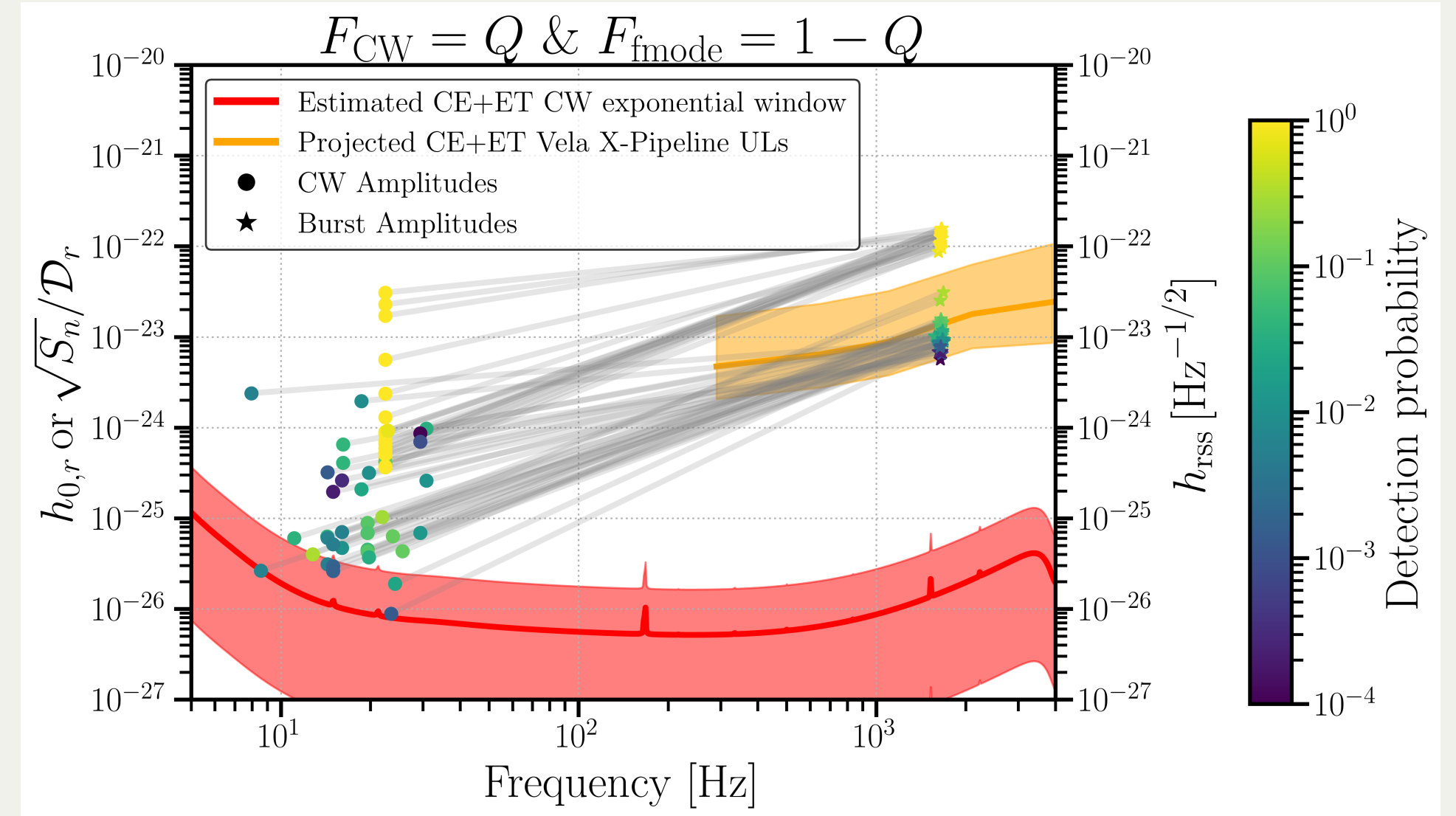
Figure credit: Evan Hall, 2022

# Projecting results to future detectors

- Estimating CW limits for future observing runs & detectors via sensitivity depth
  - Sensitivity depth defined as  $\mathcal{D} = \sqrt{S_n}/h_0$
  - Sensitivity depth of O5, CE, ET from Moragues et al. (2023)
  - Repeat their method for CE+ET network with cows3 infrastructure (Mirasola & Tenorio 2024)
- Projecting Burst  $h_{\text{rss}}$  limits to future observing runs & detector networks
  - Assume that detectors have similar degrees of non-gaussianity
  - Assume that pipelines place limits at the same network SNR values
  - Geometric factor of sky location/source orientation/antenna pattern and detector ASD (Sutton 2013)

# Prospects of detection in future detectors

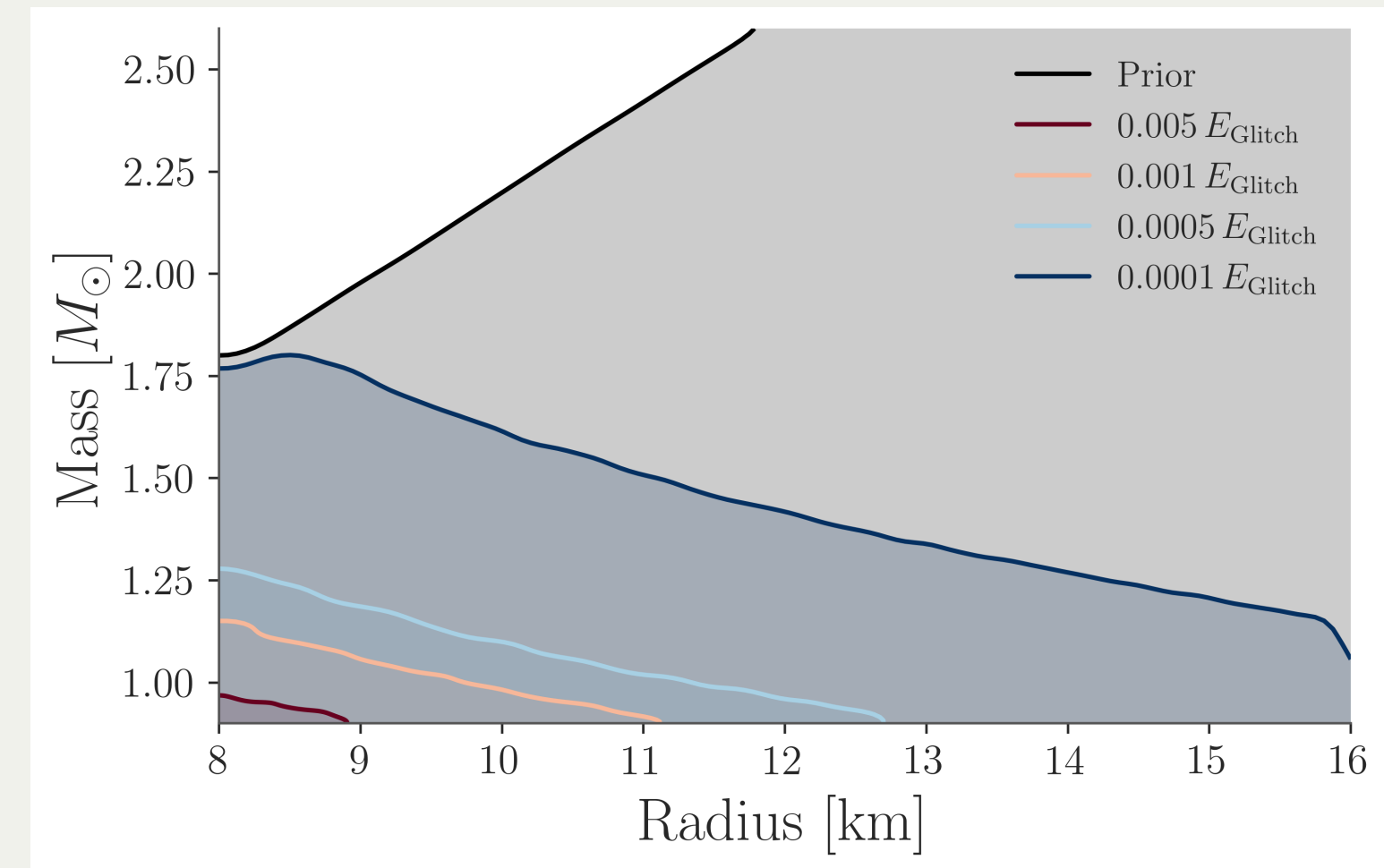
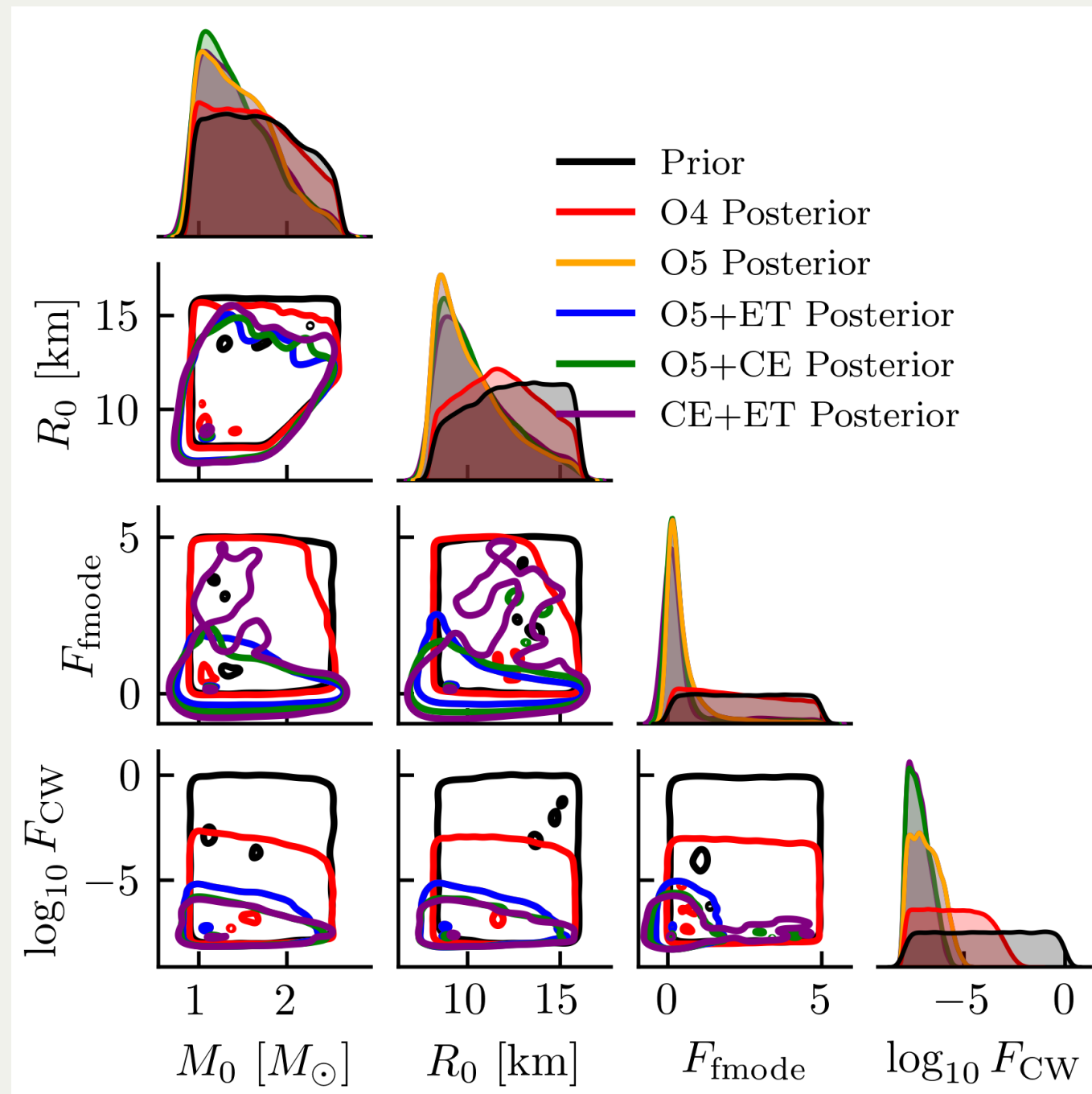
- Catalog of past ATNF pulsar glitches with measured healing parameters (Manchester et al. 2005; ATNF 2026)
- Monte Carlo samples of astrophysical parameters for each glitch & compute fraction of samples that give characteristic amplitude above projected O4 search limits
  - Require both tCW and f-mode GW amplitude to exceed respective search limits
  - Fraction of samples reported as a probability of double-detection
- Fix energy fractions in different scenarios:
  - Equal energy:  $F_{CW} = Q$  and  $F_{fmode} = Q$
  - Both channels add up to characteristic energy:  $F_{CW} = Q$  and  $F_{fmode} = 1 - Q$



# Implications of non-detection in future detectors

- Uninformed prior on the energy fractions
- Little to learn without limits on energy fractions

- Fixed energy fractions but with a global factor  $F_{\text{tot}}$  limiting the total GW energy such that  $F_{\text{CW}} + F_{\text{fmode}} = F_{\text{tot}}$ . Thus, we have  $F_{\text{CW}}/F_{\text{tot}} = Q = 0.017$  and  $F_{\text{fmode}}/F_{\text{tot}} = 1 - Q$



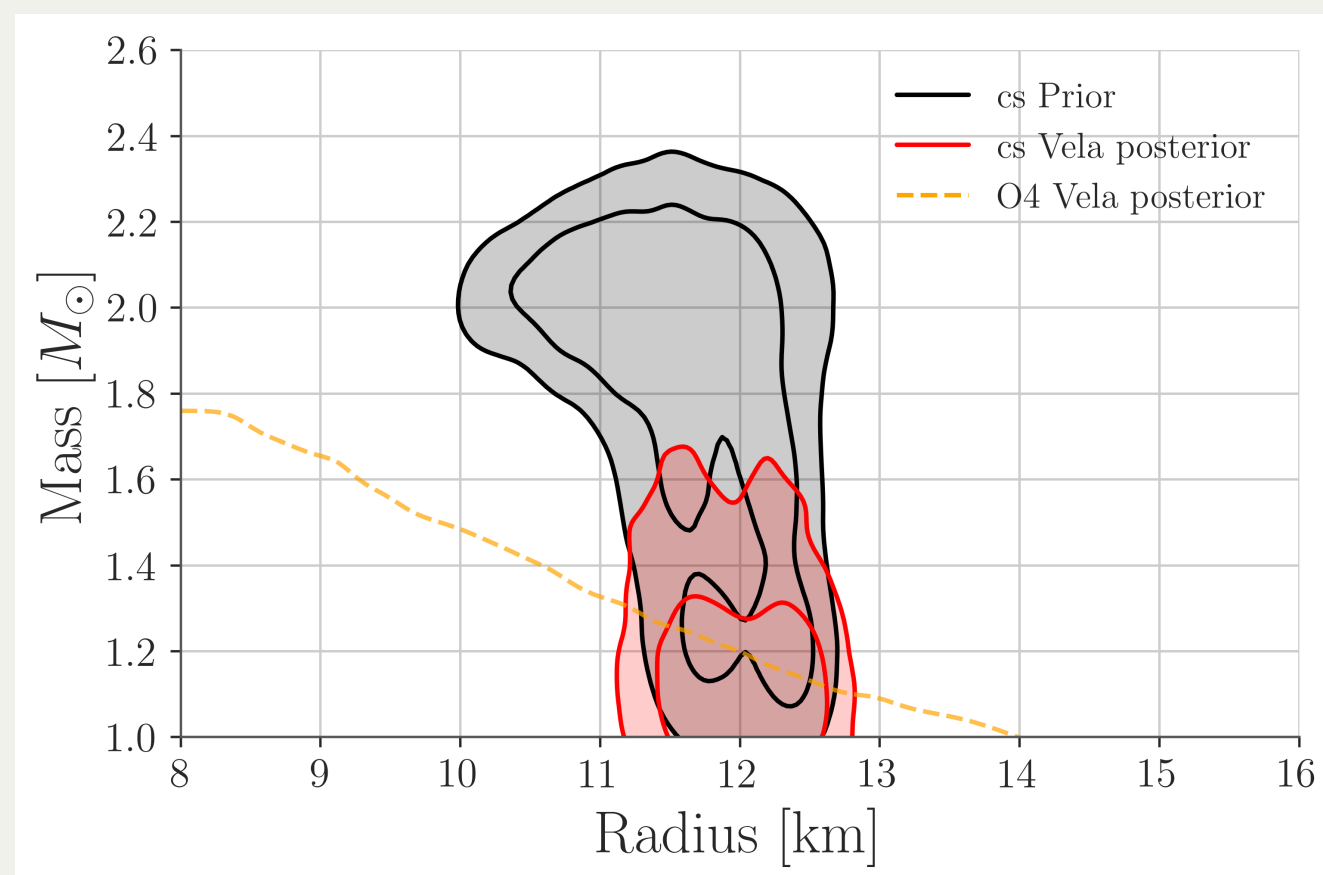
An ET + CE network would match the O4 constraints if the available GW energy was a factor of  $10^4$  lower than the characteristic glitch energy

# Including constraints on the EoS from NICER

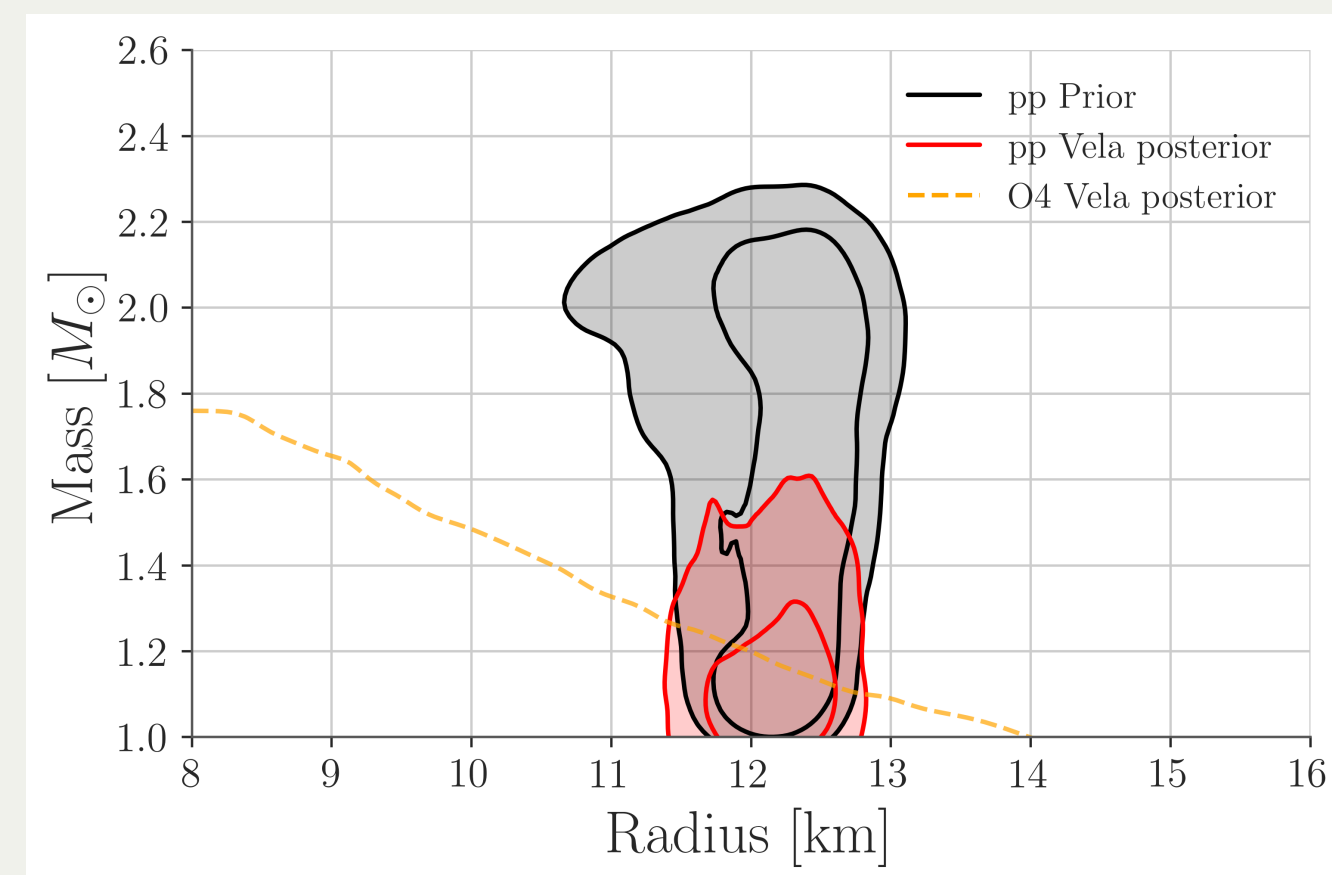
- Work with Melissa Mendes (Technische Universität Darmstadt)
- Construct mass/radius prior from NICER posterior (Lucien Mauviard et al 2025)
- Two different priors use different high-density parameterizations to minimize prior dependence
- Re-analyze 2024 Vela glitch under joint analysis framework
  - Greatly restricts allowed mass/radius parameter space
  - Under (many) assumptions, upper limit on the mass could be placed



Recent STSM funded by SCALES



NS speed of sound model



Piecewise-polytropic model

# Conclusions/Summary

- O4 search on Vela probes close to model limits for CW emission
  - burst still a ways off
- 3rd generation detectors massively improve detection probability for several pulsars
  - Still will not observe all pulsar glitches
  - Vela still a priority target
- Future searches will either detect something, likely with both CW and burst (assuming targeted searches on every glitch), or start disproving models
- Need more parameterized models to better inform future upper limits

# Acknowledgements

This material is based upon work supported by NSF's LIGO Laboratory which is a major facility fully funded by the National Science Foundation. The authors are grateful for computational resources provided by the LIGO Laboratory and supported by National Science Foundation Grants PHY-0757058 and PHY-0823459

This work was supported by the Universitat de les Illes Balears (UIB) with funds from the Programa de Foment de la Recerca i la Innovació de la UIB 2024-2026 (supported by the yearly plan of the Tourist Stay Tax ITS2023-086); the Spanish Agencia Estatal de Investigación grants PID2022-138626NB-I00, RED2024-153978-E, RED2024-153735-E, funded by MICIU/AEI/10.13039/501100011033 and the ERDF/EU; and the Comunitat Autònoma de les Illes Balears through the Conselleria d'Educació i Universitats with funds from the European Union - European Regional Development Fund (ERDF) (SINCO2022/18146 - Plataforma HiTech-IAC3-BIO); and by COST action SCALES CA24139, supported by COST (European Cooperation in Science and Technology).



# Extra slides

# Details on estimating CW sensitivity for future detectors

- Follow methodology detailed in Moragues et al. (2023)
- Use COWS3 python package (Mirasola & Tenorio, 2024)
- Select Crab & Vela pulsars as representative targets
- Network sensitivity is the harmonic mean of the detectors in network
- Generate a distribution of SNR values for a unit sensitivity depth signal for 120 days of observation with 1800s segments for each detector in the network
- Generate a distribution of the  $\chi^2$  random variable  $2\mathcal{F}$  outliers based on the number of templates used in the original analysis ( $3.9 \times 10^6$  for the Crab pulsar and  $3.6 \times 10^5$  for the Vela pulsar)
- Fit to a Gumbel distribution, and we take the 99th percentile for this outlier distribution
- Compute the false-dismissal probability for different sensitivity depths using our  $2\mathcal{F}$  threshold and unit-depth SNR distribution
- Take the sensitivity depth that gives a false-dismissal probability of 0.05
- This process gives  $\mathcal{D} = 30.4/\sqrt{\text{Hz}}$  (Crab) and  $\mathcal{D} = 36.7/\sqrt{\text{Hz}}$  (Vela) for CE+ET
- Take the average of  $\mathcal{D} = 33.6/\sqrt{\text{Hz}}$  as sky-averaged sensitivity depth

# Details on projecting burst results to future detectors

- Sutton, 2013 showed that the relation between the signal-to-noise ratio  $\rho$  and  $h_{\text{RSS}}$  for a short-duration, monochromatic signal is

$$\rho^2 = \Theta^2 \frac{h_{\text{RSS}}^2}{S_n(f_0)}$$

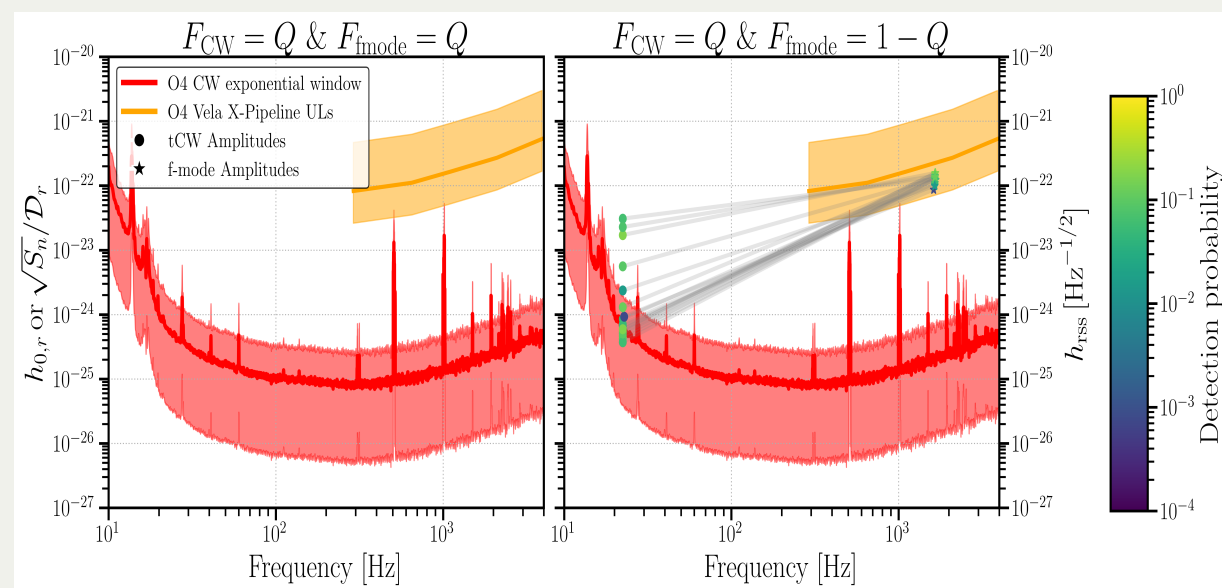
where  $\Theta$  is a geometric term defined in terms of the detector antenna pattern and source inclination angle for different polarization cases:

$$\Theta^2 \equiv \begin{cases} F_+^2(\theta, \phi, \psi) + F_\times^2(\theta, \phi, \psi) & \text{Unpolarized} \\ F_+^2(\theta, \phi, \psi) \left( \frac{1 + \cos^2(\iota)}{2} \right)^2 + F_\times^2(\theta, \phi, \psi) \cos^2(\iota) & \text{Elliptical} \\ F_+^2(\theta, \phi, \psi) 2 \sin^4(\iota) & \text{Linear} \end{cases}$$

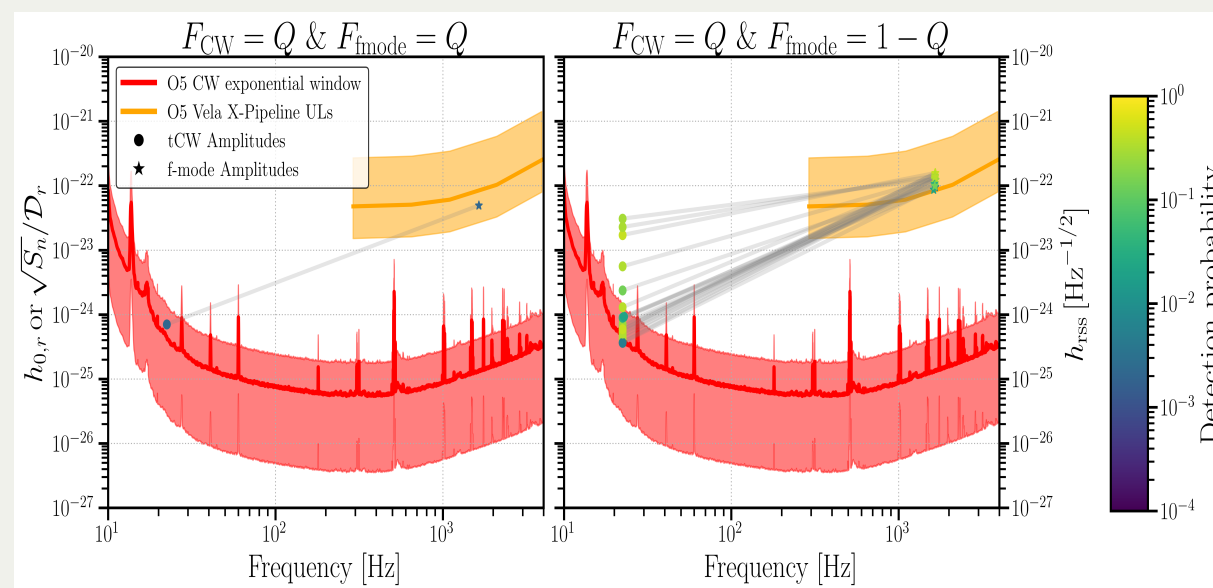
- Assuming that a pipeline reaches “detectability” at similar  $\rho$  for different noise realizations, we equate  $\rho$  for different detectors and solve for  $h_{\text{RSS}}$ , using the respective detector details for the geometric term  $\Theta$ .



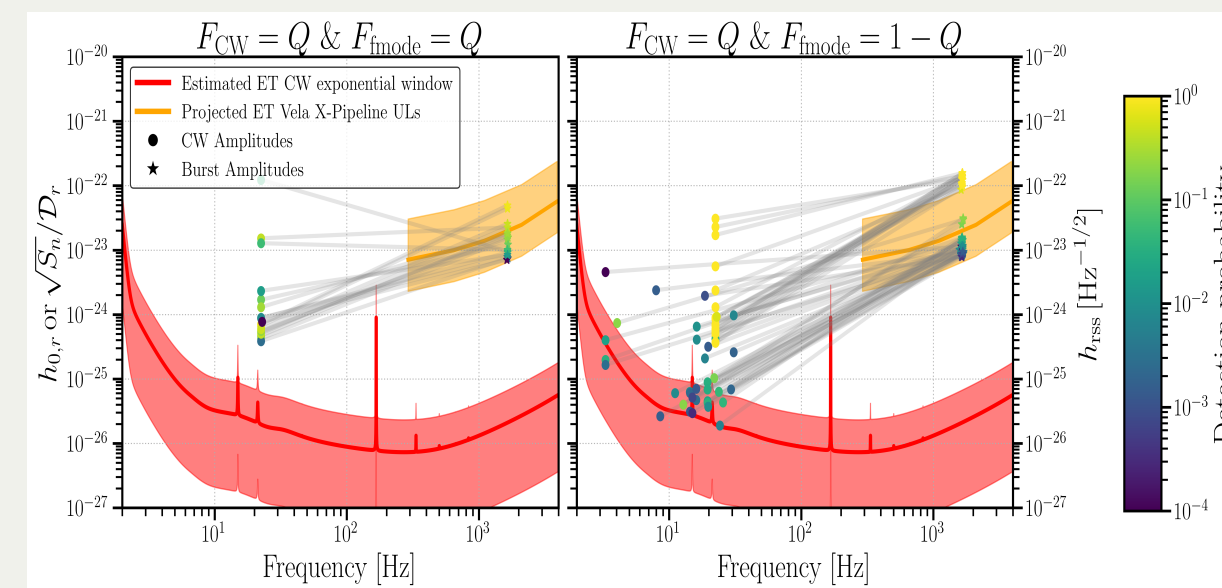
# Pulsar glitch dual-detection plots for other detector networks



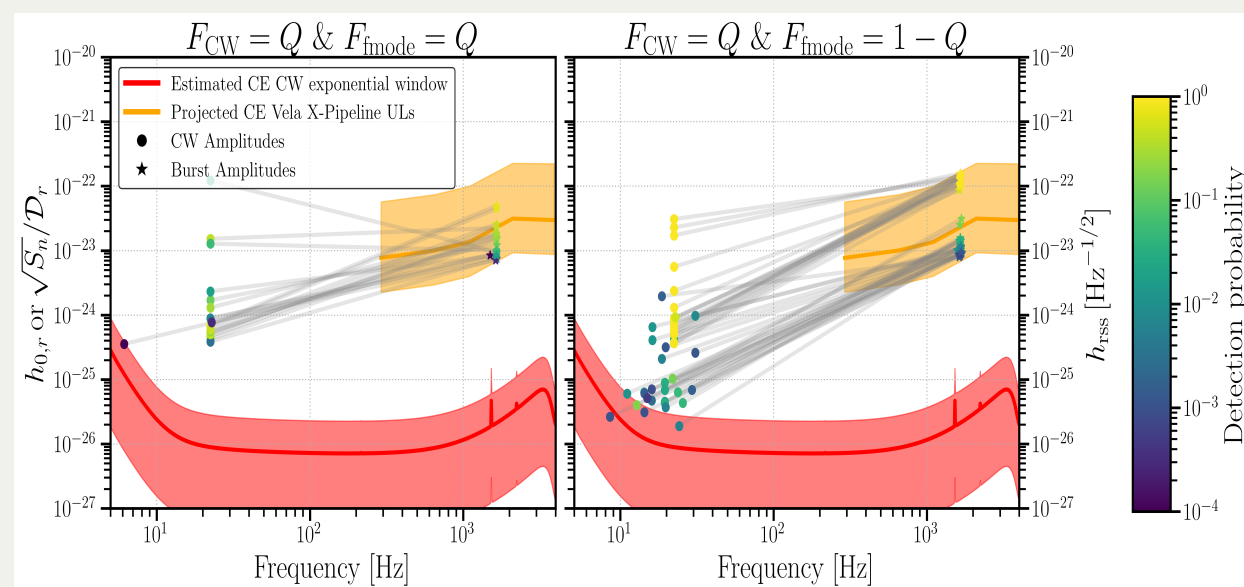
O4 network



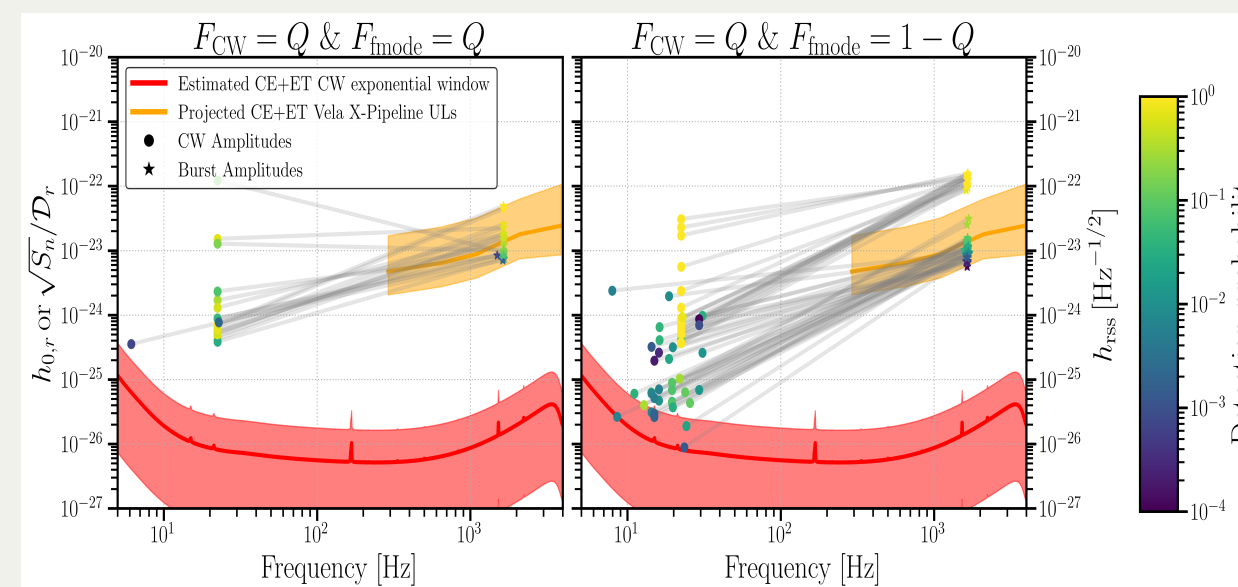
O5 network



ET &amp; O5 network



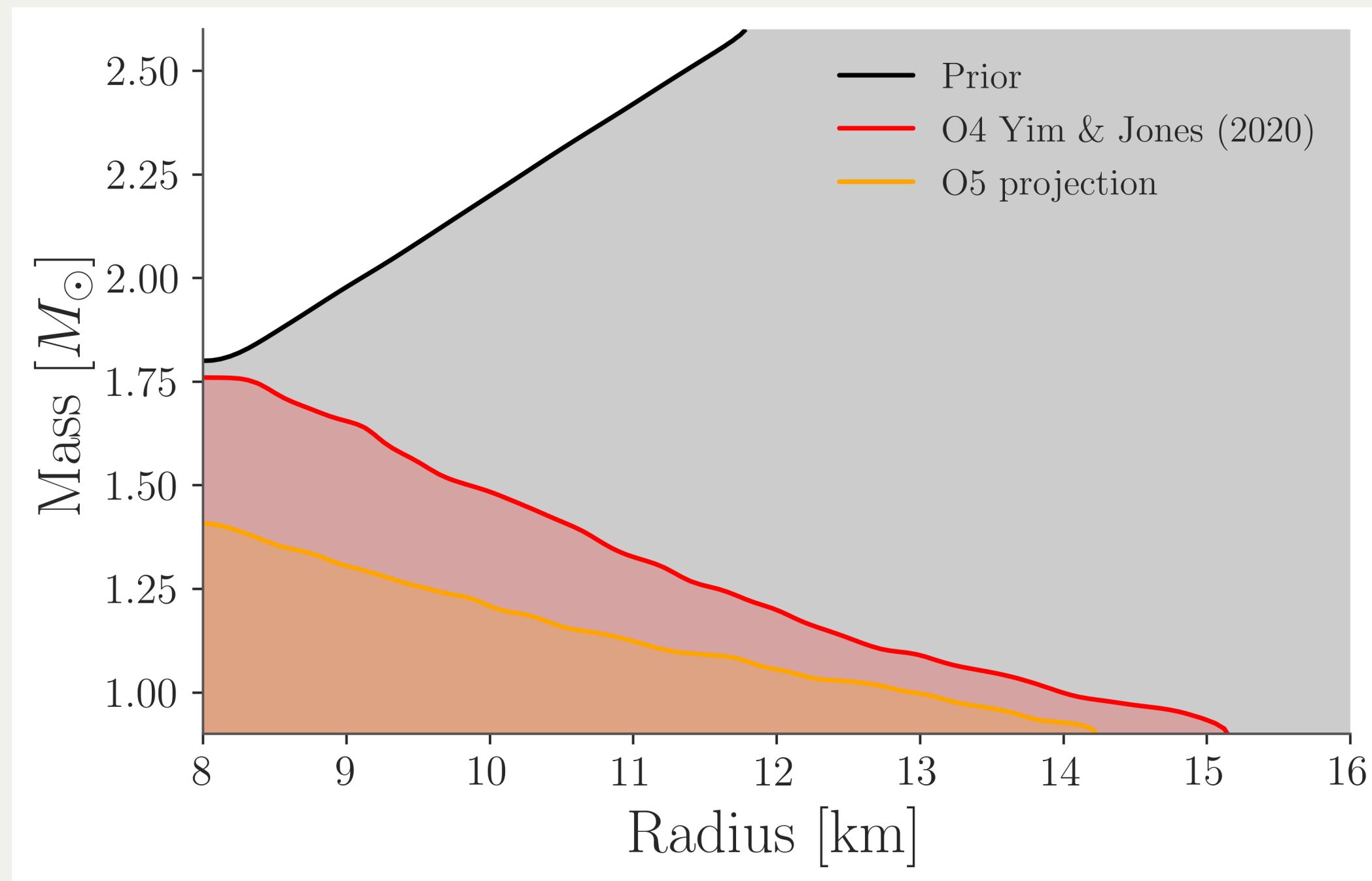
CE &amp; O5 network



ET &amp; CE network

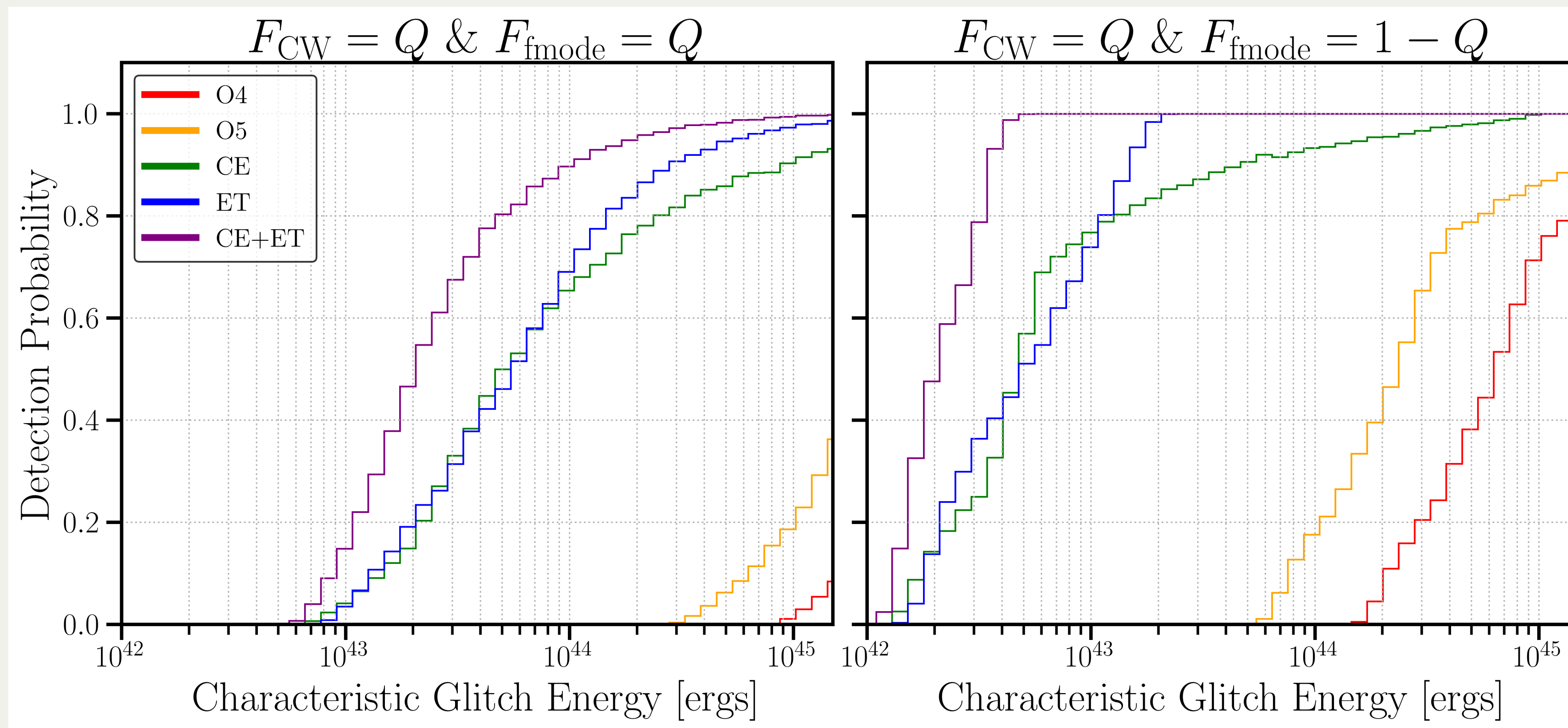
# O4 & O5 projected Vela non-detection fixed energy plots

- Repeating the non-detection CW+Burst analysis performed in Abac et. al. (2026) with the projected sensitivity of future detectors
- Using  $F_{CW} = Q = 0.017$  and  $F_{mode} = 0.8$
- 3rd generation detector sensitivities not compatible with a non-detection under the Yim & Jones (2020) model



# Vela detectable energy

- Mass and radius are fixed to  $2 M_{\odot}$  and 15 km (frequency of peak f-mode detectability)
- $Q$  constrained to below 0.2



# Universal relations

- Moment of inertia relation (Yagi & Yunes, 2017)

$$\log\left(\frac{I_{zz}}{M^3}\right) = -1.261 \log\left(\frac{M}{R}\right) + 0.277$$

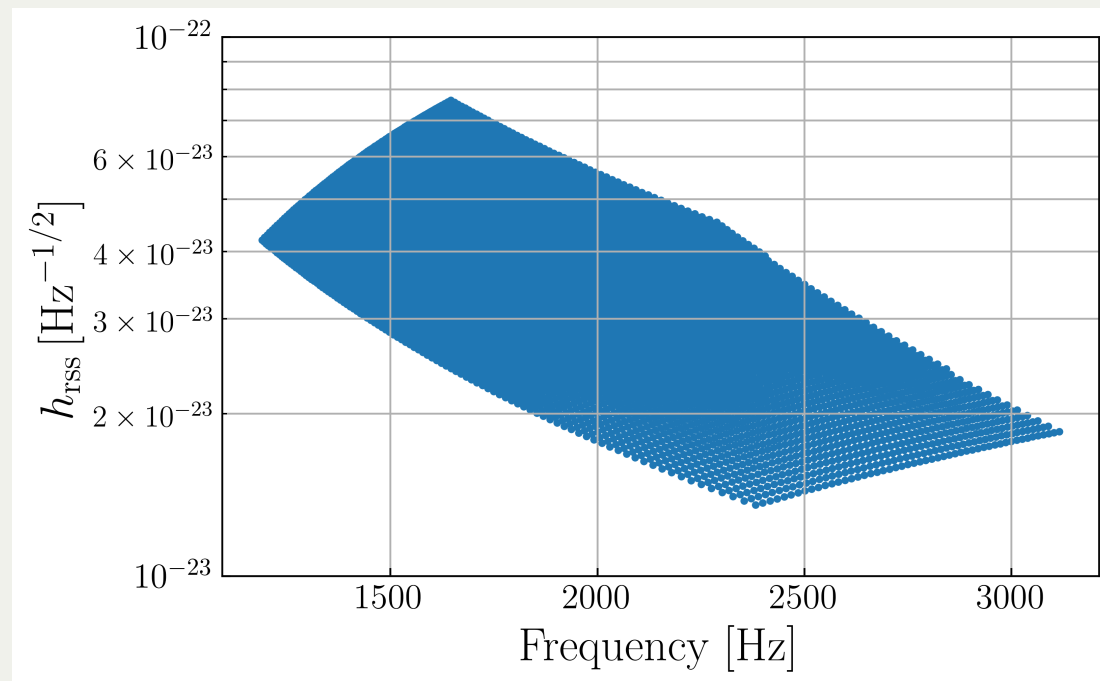
- f-mode frequency and damping time relations (Pradhan et al. 2022)

$$\nu_{f,0}(\text{kHz}) \approx 0.535 + 1.646 \left(\frac{\overline{M}}{\overline{R}^3}\right)^{1/2}$$

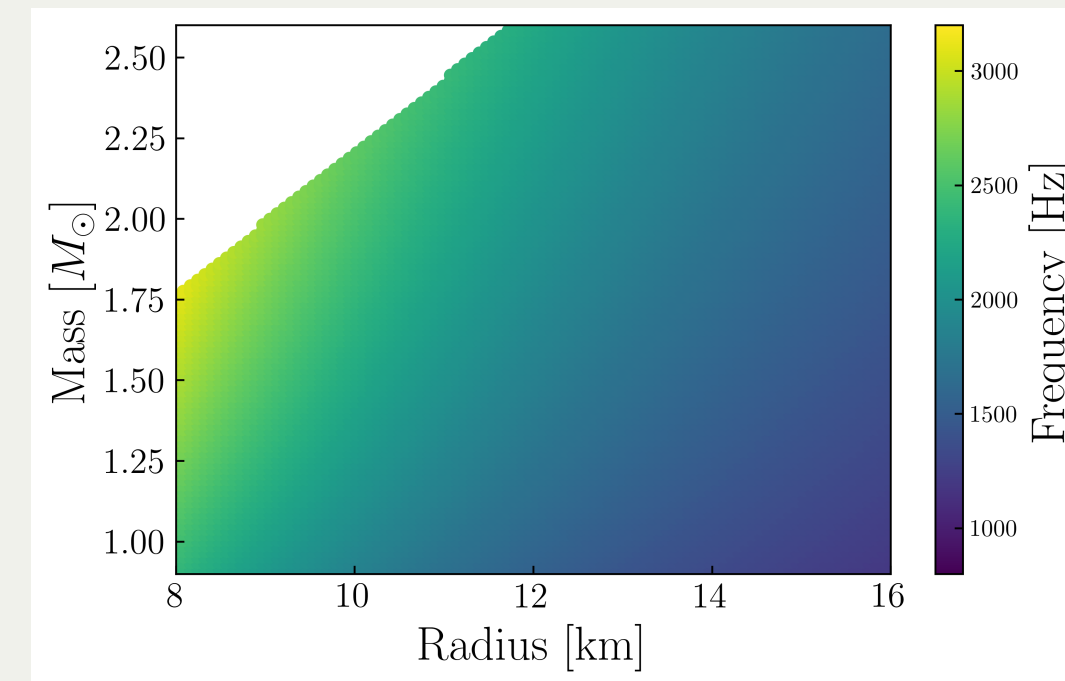
$$\frac{1}{\tau_f(s)} \approx \frac{\overline{M}^3}{\overline{R}^4} \left[ 21.19 - 13.41 \left(\frac{\overline{M}}{\overline{R}}\right) \right]$$



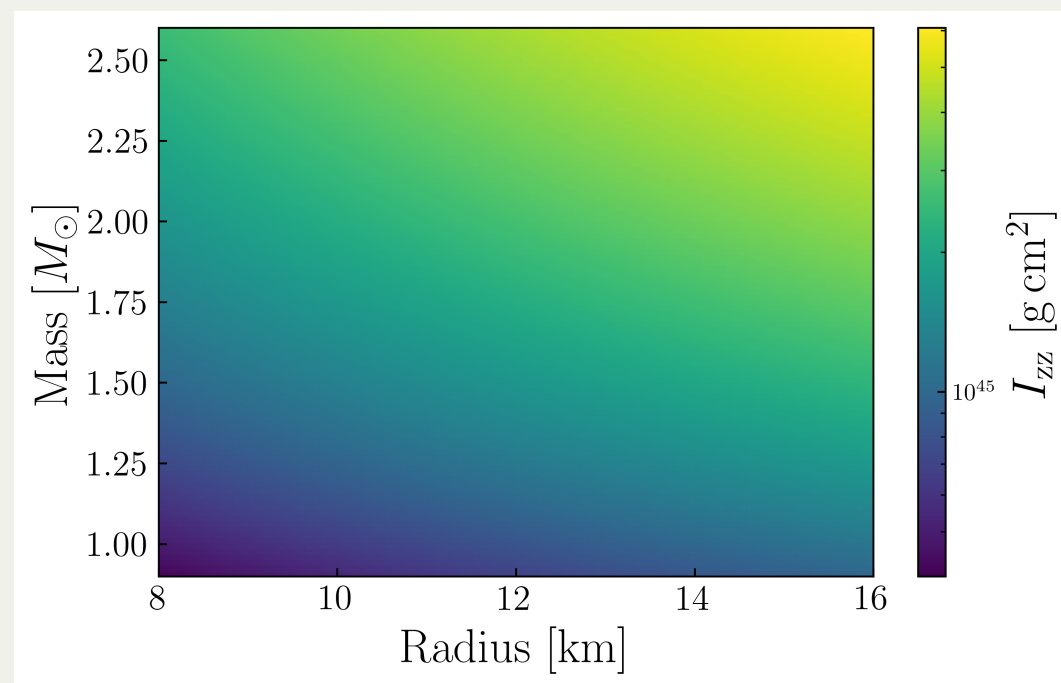
# Some limits of the universal relations



f-mode frequency compared to  $h_{\text{rss}}$



f-mode frequency as function of mass and radius



Moment of inertia