

# Anomaly mediation and Seiberg Witten theory

Cyrus Robertson Orkish  
Daniel Stolarski



**Carleton**  
University

Big picture:

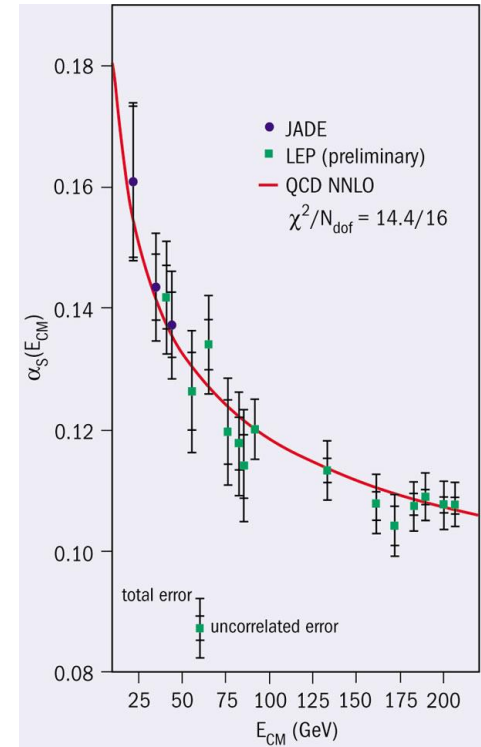
Understanding the IR structure  
of asymptotically free gauge  
theories

# Example: chiral QCD

- Gauge group  $SU(3)$
- 3 massless quarks.
- Global symmetry group  $SU(3)_L \times SU(3)_R$
- Classically conformal

# Example: chiral QCD

- Gauge group  $SU(3)$
  - 3 massless quarks.
  - Global symmetry group  $SU(3)_L \times SU(3)_R$
  - Classically conformal
- 
- Running coupling: conformal anomaly
  - At  $\Lambda_{QCD}$ , perturbation theory breaks



Renormalization group flow

UV

Renormalizable perturbative  
theory of quarks and gluons

$\Lambda_{QCD}$

IR

Pions - sigma model on  
symmetric space

Renormalization group flow

UV

Renormalizable perturbative  
theory of quarks and gluons

$\Lambda_{QCD}$

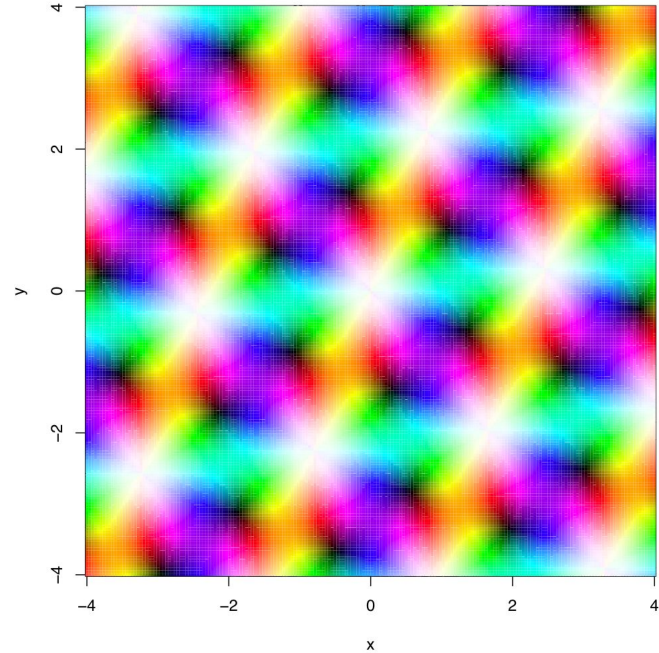
IR

Pions - sigma model on  
symmetric space

Most everyone believes this. Noone  
knows how to prove it.

# Supersymmetry

- Lorentz invariance is powerful. SUSY is even more powerful.
- Allows derivation of exact, nonperturbative results.
- We'll see an example as we proceed.



SUSY = 0th order approximation. Can we get to 1st order?

Possible answer: Anomaly mediated  
supersymmetry breaking (AMSB)

# Anomaly mediated SUSY breaking (AMSB)

- Rotate conformal anomaly into superspace: superconformal anomaly
- This is AMSB
  
- Only 1 parameter,  $m_{3/2}$
- + Lagrangian + beta functions ->

$$V_{tree} = m_{3/2} \left( \partial_i W h^{i\bar{j}} \bar{\partial}_{\bar{j}} K - 3W \right) + \text{h.c.} + |m_{3/2}|^2 \left( \partial_i K h^{i\bar{j}} \bar{\partial}_{\bar{j}} K - K \right)$$

$$m_\lambda = \frac{-\beta(g)}{g} m_{3/2}$$

$$m_i^2 = \frac{-1}{4} \dot{\gamma}_i |m_{3/2}|^2$$

$$A_{ijk} = \frac{-1}{2} (\gamma_i + \gamma_j + \gamma_k) m_{3/2}$$

# AMSB for non-SUSY gauge theory

- [arXiv:2104.01179](https://arxiv.org/abs/2104.01179)
- Hitoshi Murayama - Introduces AMSB to SQCD
- Many similar studies since.

Renormalization group flow

UV

Large  $m_{3/2}$ , apply AMSB to perturbative UV theory -> squarks+gaugino decouple

$\Lambda$

Small  $m_{3/2}$ , apply AMSB to low-energy description -> candidate vacuum has massless spectrum and symmetries like chiral QCD

IR

Renormalization group flow

UV

Large  $m_{3/2}$ , apply AMSB to perturbative UV theory -> squarks+gaugino decouple

$\Lambda$

Small  $m_{3/2}$ , apply AMSB to low-energy description -> candidate vacuum has massless spectrum and symmetries like chiral QCD

IR

**\$1,000,000 question:  
Far IR at large SUSY-breaking**

# Phase transitions as $m_{3/2} \rightarrow \infty$

- arXiv: 211.11214
- Bai & Stolarski,  
Georgi-Glashow like SU(5)  
theory
- Phase transition guaranteed  
(t'Hooft anomaly matching)

# Our project

- Seiberg Witten theory + AMSB
- arXiv:xxxx.xxxxx

# Our project

- Seiberg Witten theory + AMSB
- arXiv:xxxx.xxxxx
- Examine AMSB in a more controlled setting. What can we learn about the flow from small to large SUSY-breaking?

# Seiberg Witten theory

# Seiberg Witten theory

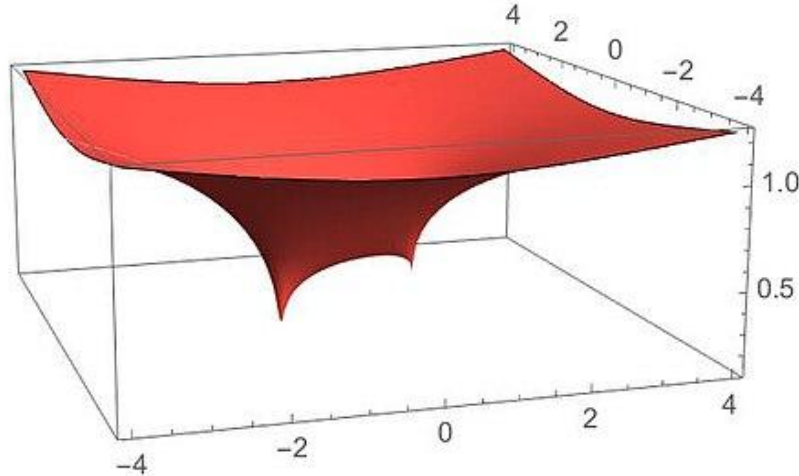
- N=2 supersymmetric gauge theory, gauge group SU(2), up to 3 flavours (4 flavours is conformal)

# Seiberg Witten theory

- N=2 supersymmetric gauge theory, gauge group  $SU(2)$ , up to 3 flavours (4 flavours is conformal)
- Scalar potential  $\rightarrow$  VEV breaks  $SU(2) \rightarrow U(1)$

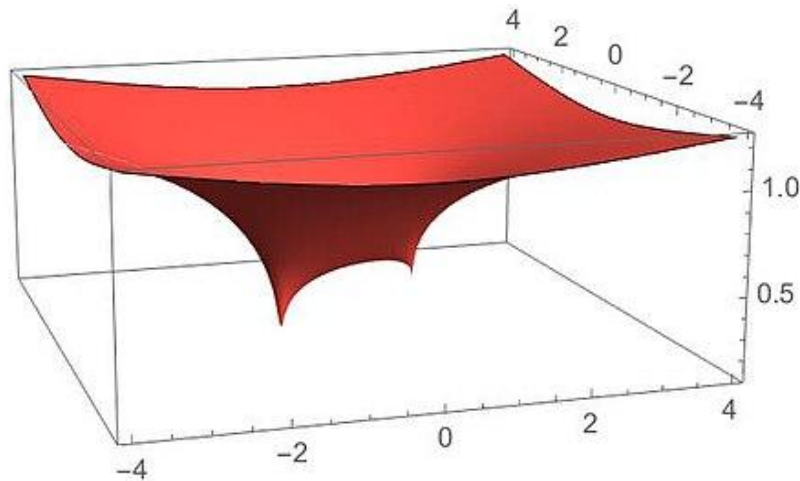
# Seiberg Witten theory

- N=2 supersymmetric gauge theory, gauge group  $SU(2)$ , up to 3 flavours (4 flavours is conformal)
- Scalar potential  $\rightarrow$  VEV breaks  $SU(2) \rightarrow U(1)$
- A moduli space of vacua (like goldstones, but space not symmetric)



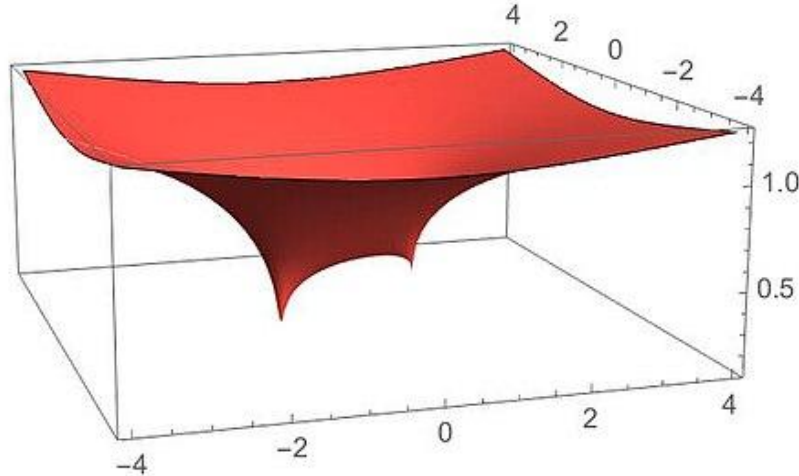
# Seiberg Witten theory

- Can exactly calculate metric



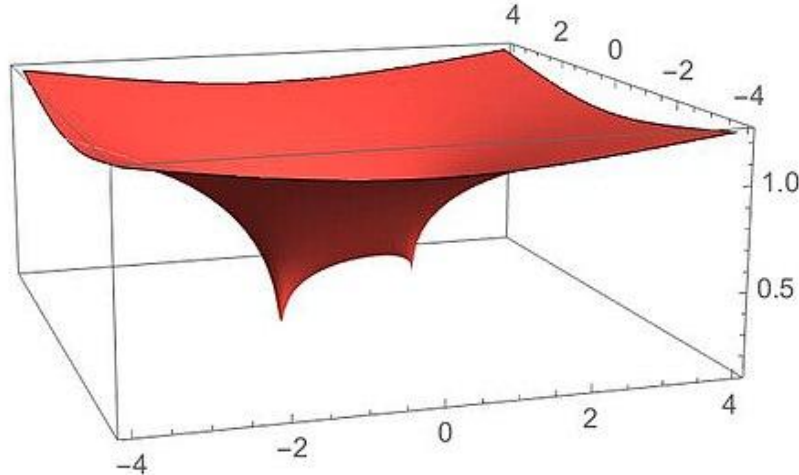
# Seiberg Witten theory

- Can exactly calculate metric
- Singularities = newly massless particles  $\rightarrow$  monopoles!!



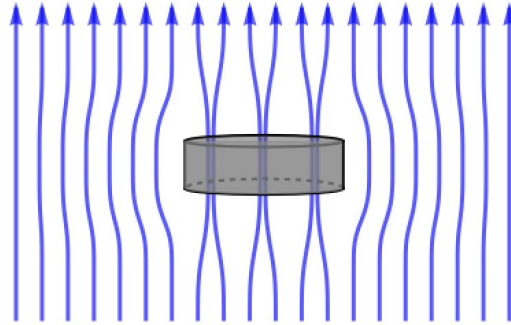
# Seiberg Witten theory

- Can exactly calculate metric
- Singularities = newly massless particles  $\rightarrow$  monopoles!!
- Exact electromagnetic duality  $\rightarrow$  weakly coupled 'elementary' monopoles.



# Seiberg Witten deformation

- N=1-preserving mass term
- Kills moduli space, but singularities survive



- Monopoles condense -> dual Meissner effect, confinement!!

# AMSB + Seiberg Witten

- UV (large  $m_{3/2}$ ) reproduces Seiberg Witten deformation in perturbation theory

# AMSB + Seiberg Witten

- UV (large  $m_{3/2}$ ) reproduces Seiberg Witten deformation in perturbation theory
- IR is different! Coulomb branch still flows to singularities, and monopoles still condense. But SUSY is broken, condensate doesn't match.

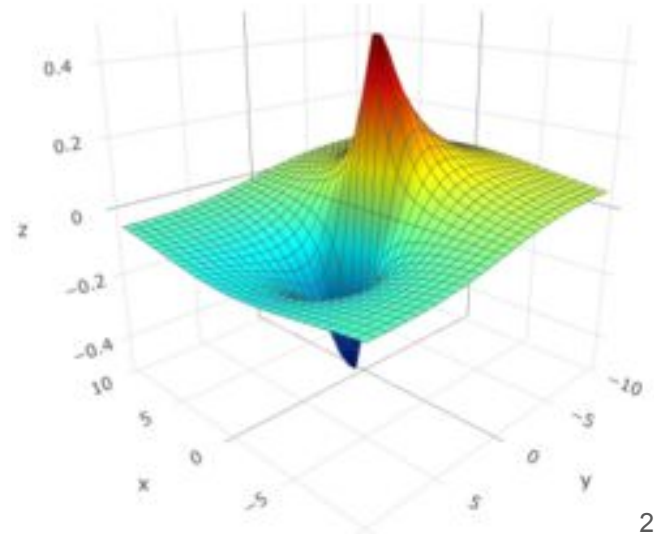
# AMSB + Seiberg Witten

$$\beta = Ag^3 + B \exp\left(-\frac{8\pi^2}{g^2}\right) + \dots$$

1 - loop

Instantons

AMSB mass-splitting  $\rightarrow$  all SUSY broken.



Renormalization group flow

UV

Large  $m_{3/2}$  perturbative  $\rightarrow$  AMSB =  
Seiberg Witten

+Instantons  $\neq$  Seiberg Witten

$\Lambda$

Small  $m_{3/2}$   $\rightarrow$  VEV rolls to singularities.  
Monopoles condense, but theory  $\neq$  Seiberg  
Witten

IR

Renormalization group flow

UV

Large  $m_{3/2}$  perturbative  $\rightarrow$  AMSB =  
Seiberg Witten

+Instantons  $\neq$  Seiberg Witten

AMSB  $\rightarrow$  Seiberg  
Witten deformation

$\Lambda$

Small  $m_{3/2}$   $\rightarrow$  VEV rolls to singularities.  
Monopoles condense, but theory  $\neq$  Seiberg  
Witten

AMSB  $\neq$  Seiberg  
Witten deformation

IR

Flow of  $m_{3/2}$

## Phase transition as $m_{3/2}$ flows to UV?

- Not a phase transition. Spectrum of massless particles and global symmetry breaking pattern do not change

# Phase transition as $m_{3/2}$ flows to UV?

- Not a phase transition. Spectrum of massless particles and global symmetry breaking pattern do not change
- But monopole condensate and spurious charge assignment do.

# A cautionary tale

- No sign of this (non-phase) transition in IR calculation. Solutions are exact.

# A cautionary tale

- No sign of this (non-phase) transition in IR calculation. Solutions are exact.
- In UV, can integrate out massive particles  $\rightarrow$  vacua should match Seiberg Witten. Again no sign of a transition.

# A cautionary tale

- No sign of this (non-phase) transition in IR calculation. Solutions are exact.
- In UV, can integrate out massive particles  $\rightarrow$  vacua should match Seiberg Witten. Again no sign of a transition.
- Transition can only take place when  $m_{3/2} \sim \Lambda$

# A cautionary tale

- No sign of this (non-phase) transition in IR calculation. Solutions are exact.
- In UV, can integrate out massive particles  $\rightarrow$  vacua should match Seiberg Witten. Again no sign of a transition.
- Transition can only take place when  $m_{3/2} \sim \Lambda$
  
- Regime involves interactions of mutually nonlocal degrees of freedom. No weakly coupled Lagrangian description.

# A cautionary tale - hidden phase transitions?

- In this theory, there was no phase transition per se.
- But a VEV was altered, as were its spurious transformation properties.
- Easy to imagine this type of behaviour causing phase transitions

# A cautionary tale - fictitious phase transitions?

- A global symmetry (N=1 supersymmetry) is broken at all  $m_{3/2}$
- Invisible in UV perturbation theory, much clearer in IR.
- Could there be situations where nonperturbative breaking of a symmetry in UV makes e.g. anomaly matching arguments fail?

## On a positive note...

- This talk is rather critical of AMSB. Never trust an extrapolated near-SUSY calculation. But...

## On a positive note...

- This talk is rather critical of AMSB. Never trust an extrapolated near-SUSY calculation. But...
- Valuable hints at how this all might work.

## On a positive note...

- This talk is rather critical of AMSB. Never trust an extrapolated near-SUSY calculation. But...
- Valuable hints at how this all might work.
- Story for another time -> (chiral, super, conformal)

## On a positive note...

- This talk is rather critical of AMSB. Never trust an extrapolated near-SUSY calculation. But...
- Valuable hints at how this all might work.
- Story for another time -> (chiral, super, conformal)
- Possibility of extending exact SUSY results to AMSB (nonperturbatively?)

# Summary

- AMSB + SUSY = way to study non-SUSY
- Extrapolating from small to large SUSY breaking -> dangerous.
- We applied AMSB to Seiberg Witten
- Large AMSB = Seiberg Witten deformation + instanton corrections
- Small AMSB  $\neq$  Seiberg Witten deformation (but qualitatively similar)
- No phase transition, but change in VEV and spurion assignment
- Invisible in perturbation theory.
- Vague hints of potentially fruitful future lines of inquiry.