

Classification of proto-neutron star oscillation modes

Guillem Fernández-Rodríguez

Phd Student in Mathematics at University of Valencia



VNIVERSITAT
ID VALÈNCIA

Collaborators:

Isabel Cordero-Carrión (University of Valencia)

Dimitra Tseneklidou (University of Valencia)

Introduction

In CCSNe, we are interested in the PNS oscillation modes. We can classify them based on a:

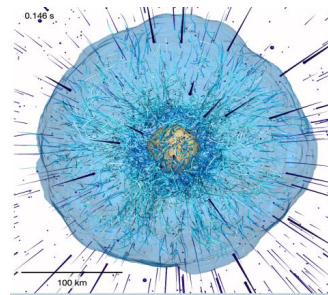
- Physically motivated way, based on the energy of the restoring forces of the modes.

Previous Dimitra's talk

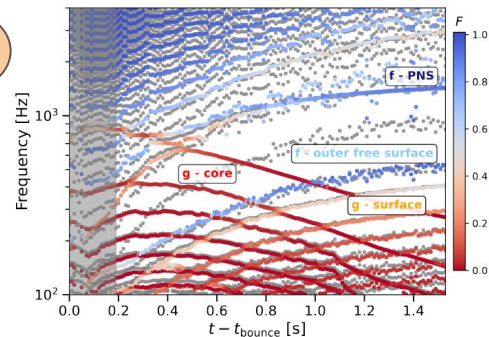
- Data-driven way, by using similarity based criteria between discovered modes.

simulations

observations



Burrows et al (2021)



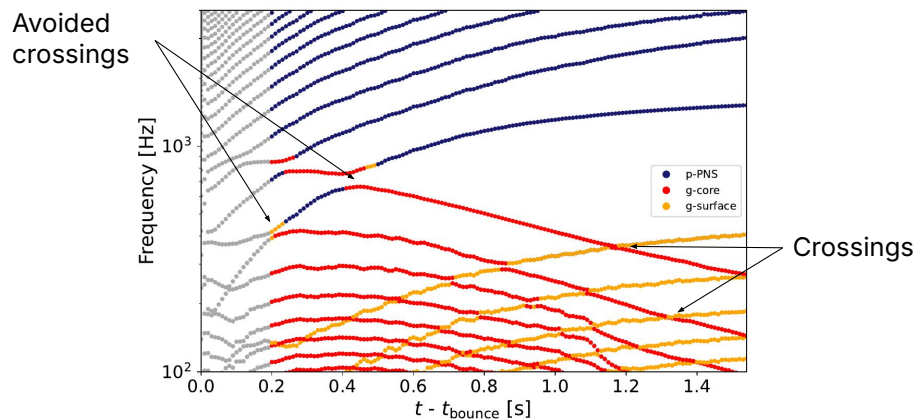
D. Tseneklidou et al (2026)

 [arXiv:2608.10264](https://arxiv.org/abs/2608.10264)

Introduction

Assumptions

- 1 Modes of the same family are (linearly) similar
- 2 There is a separation between modes of the same family
- ? At certain small x axis intervals, the modes behave linearly (*)



Simulation Data

2D Simulation S20 LS220
from M. Obergaulinger

Perturbative analysis done until
surface

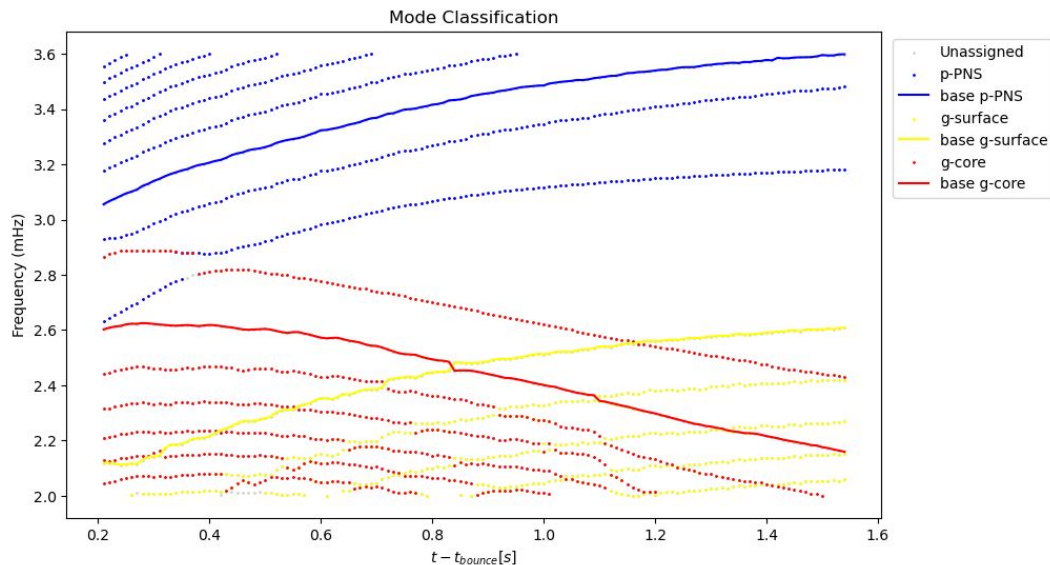
D. Tseneklidou et al (2026)

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Introduction

Objectives

- ☒ Mode classification method given a single member from each family.
- ☐ Classification given no known base modes.



Last CoConut meeting: We manually gave the continuous lines as base modes of each family to the algorithm and classified the others.

The two key points



1 Use **correlation**
between modes



2 Prolong based on
**separation
distance**

The two key points and the one who survived



1 Use **correlation**
between modes



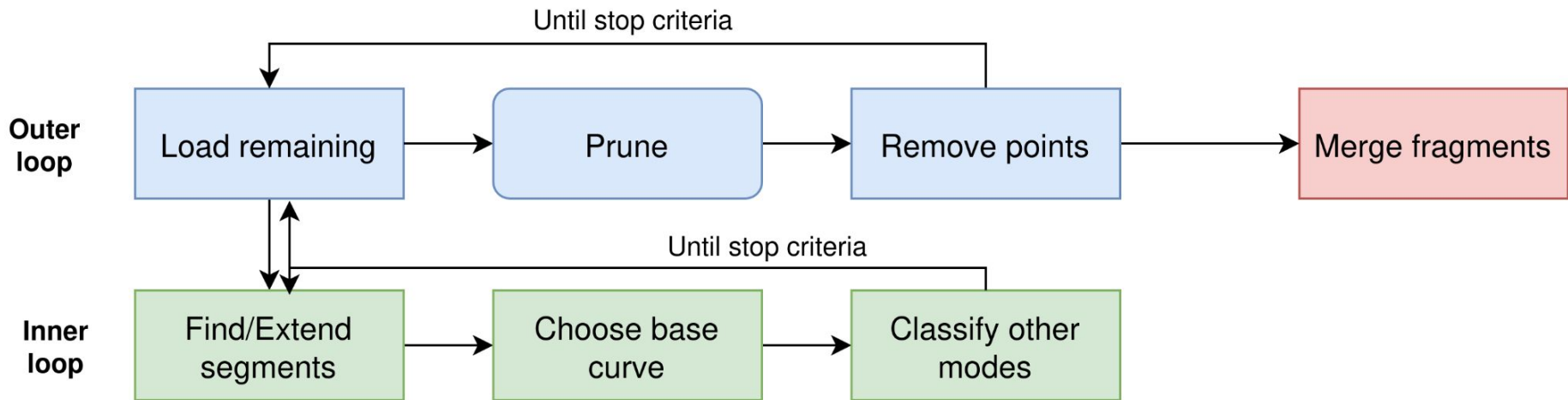
2 Prolong based on
**separation
distance**



? Find lines in short
segments

And the technical story is...

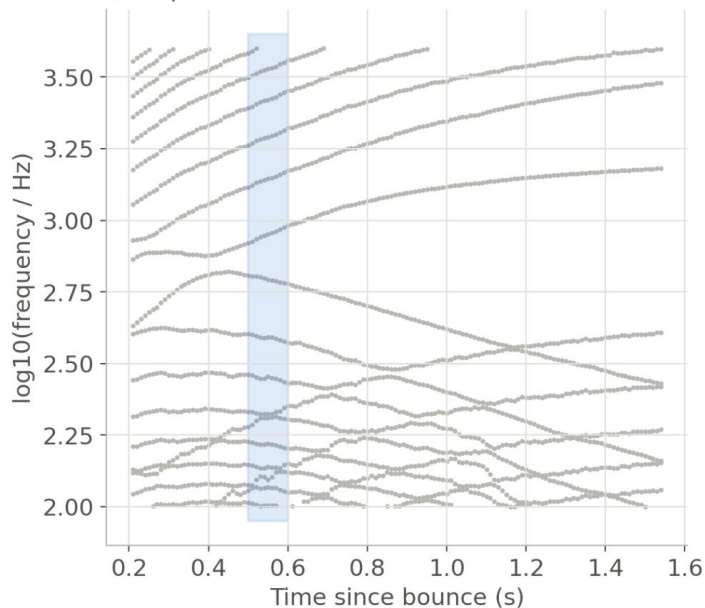
Algorithm



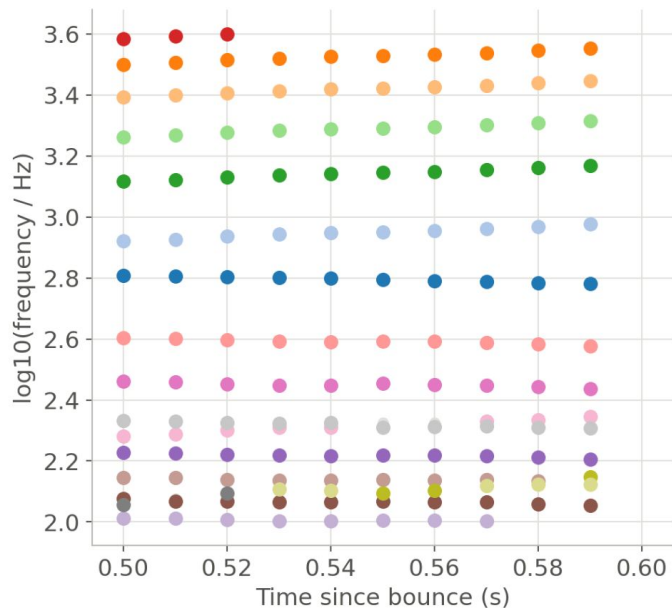
Inner loop: find initial segments

Select a window

1806 points



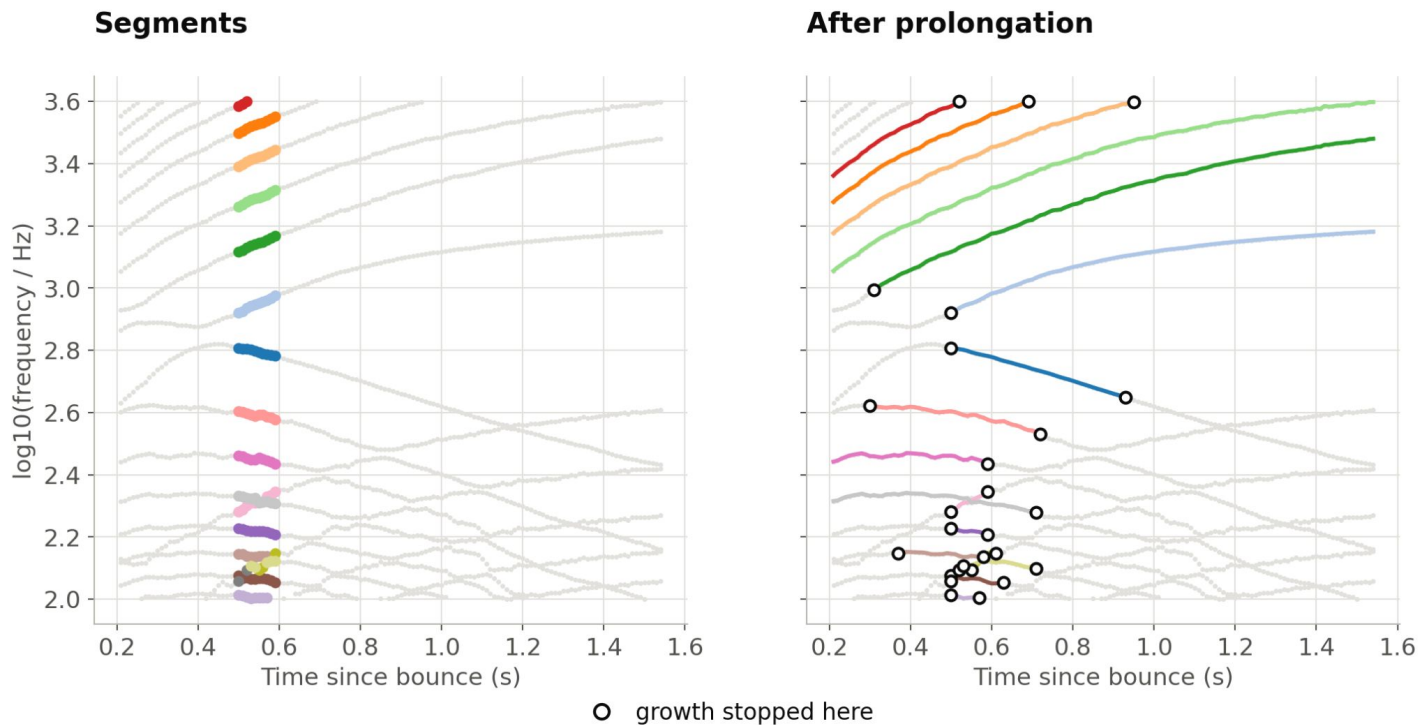
Find lines inside the window: 18 segments



Find/Extend
segments

1. Find densest segment
2. Look for local lines with j-linkage

Inner loop: extend segments



Find/Extend
segments

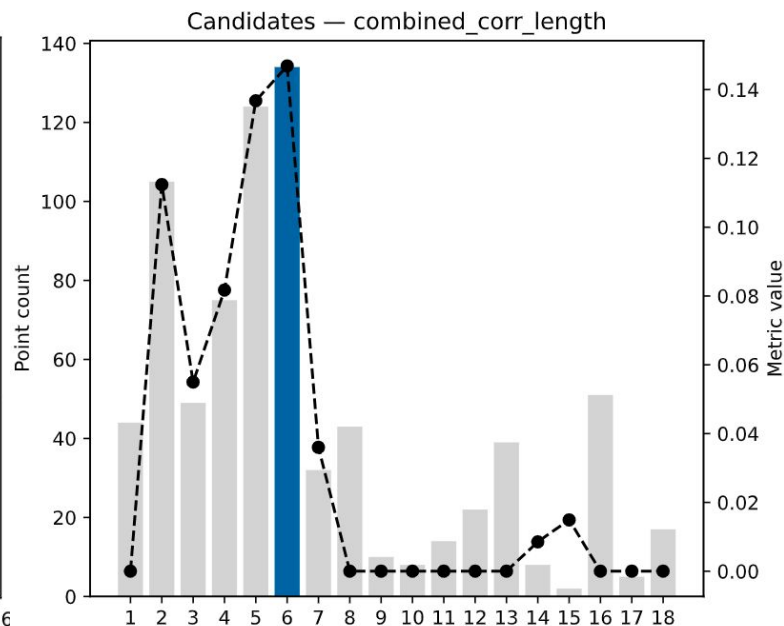
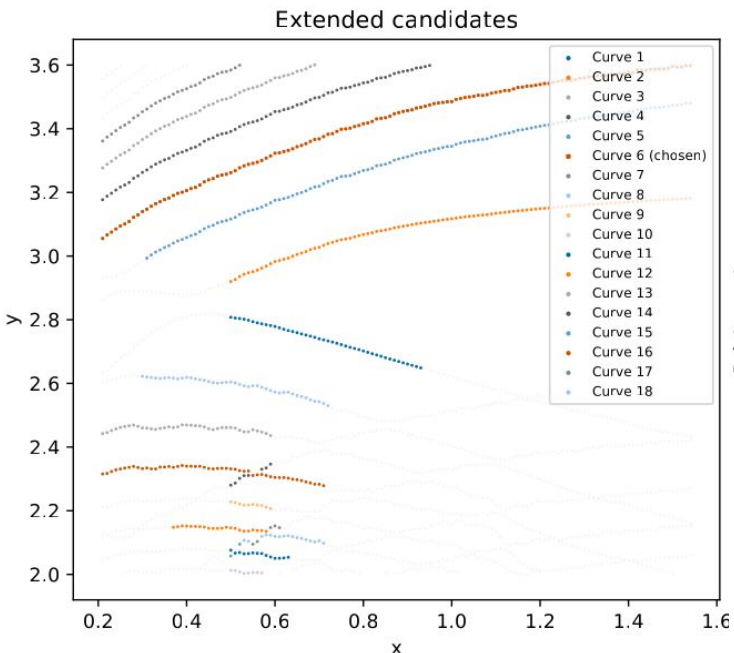
Prolongation algorithm

Extend while:

$$d_j < w_i d_i$$

d_i : distance to higher and lower points

Inner loop: choose base curve

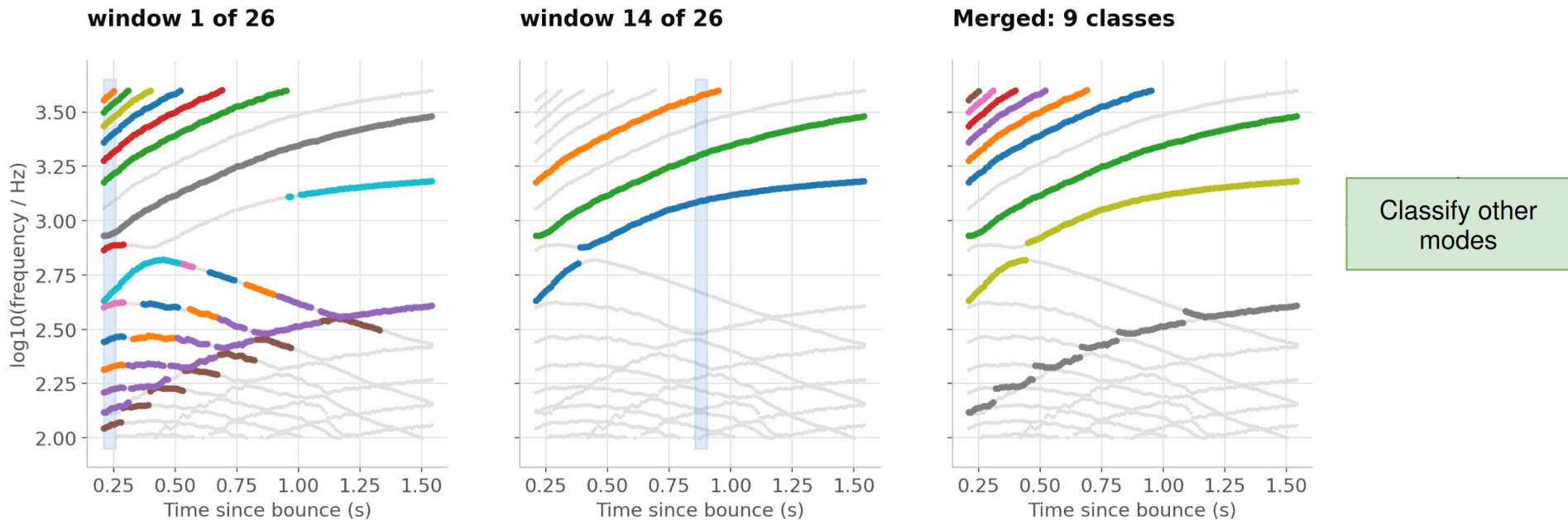


Choose base
curve

Score is combination
of:

- Length
- Correlations

Inner loop: classify other modes



Importance of inner loop

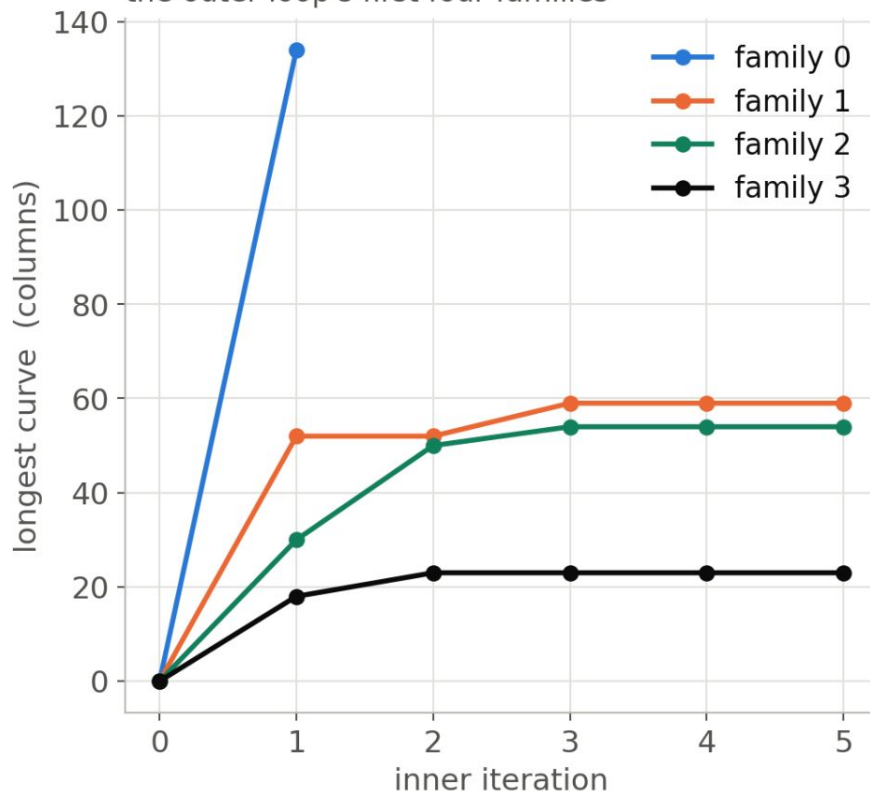
In the inner loop:

→ We classify modes using the base curve and use the previous classification to find a better base curve.

→ Consider at least 3-4 iterations.

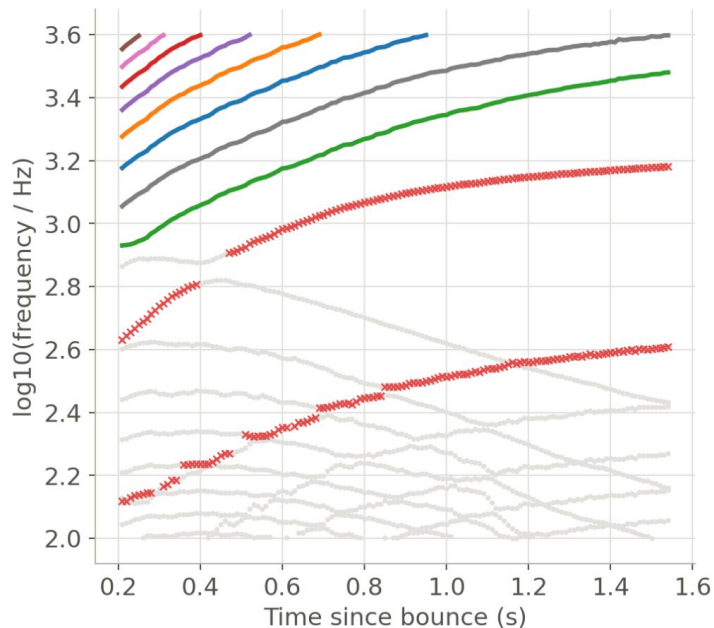
Reach grows with each pass

the outer loop's first four families



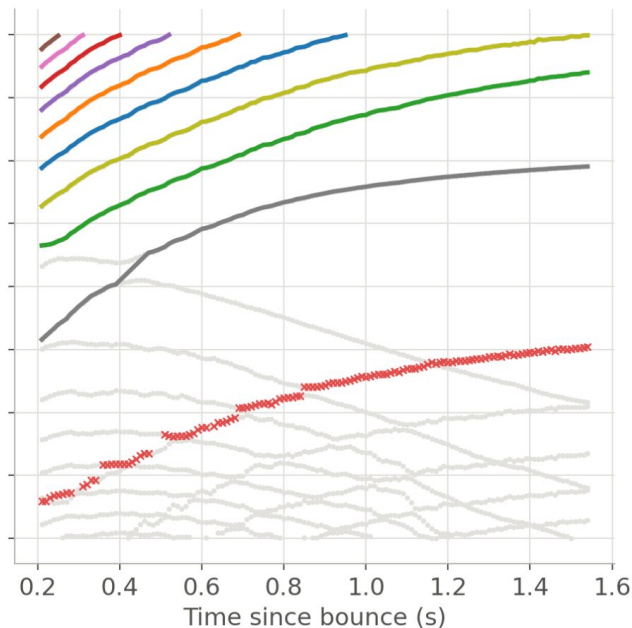
Outer loop: prune

mult = 1.5



— kept in the family

mult = 2

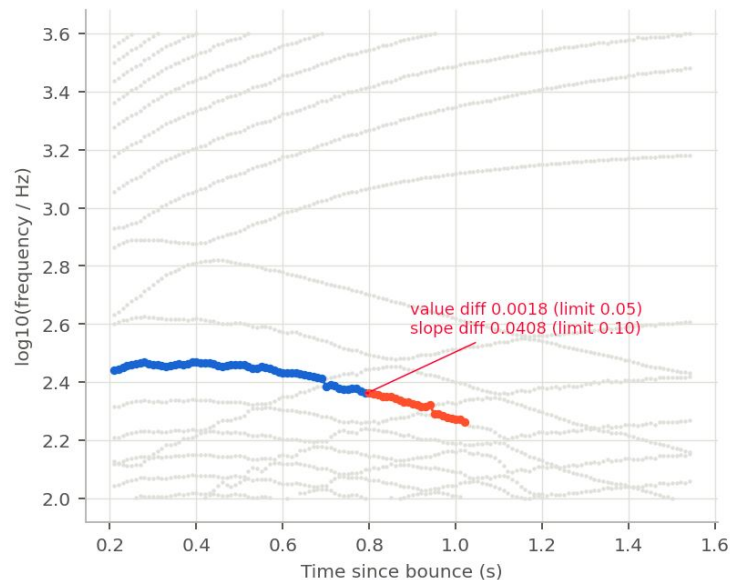
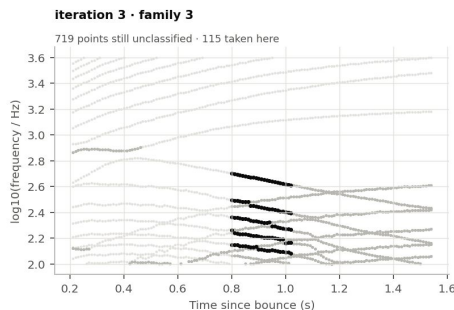
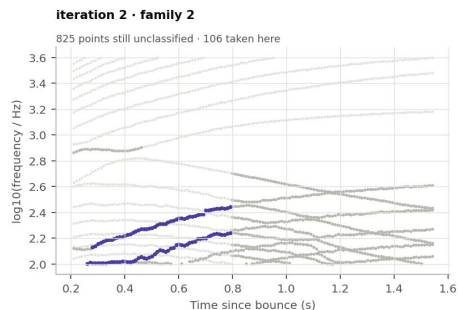
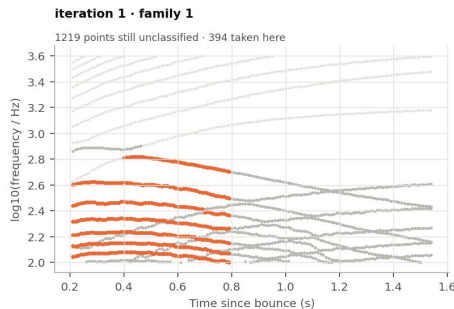
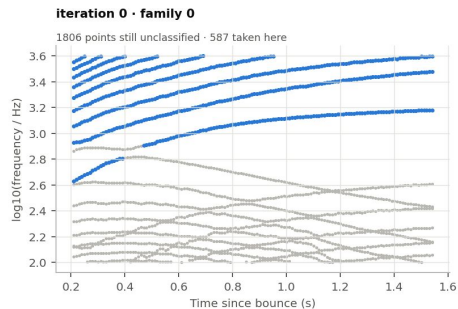


× cut

Prune

→ after consecutive
median distance
passes a threshold

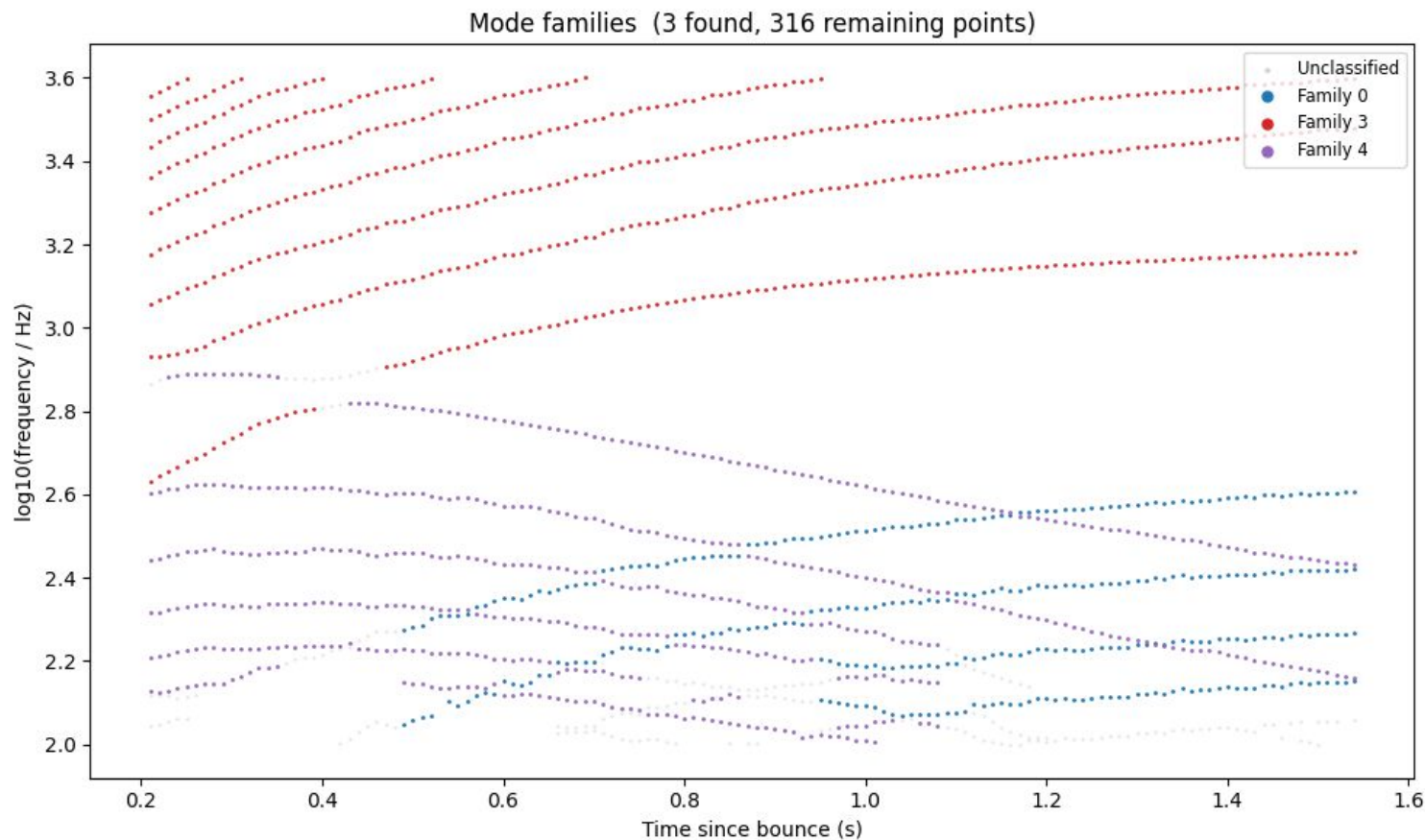
Post loops: Merging families



Merge fragments

After outer iterations finish, we try to merge them based on the slope at the connection.

Results

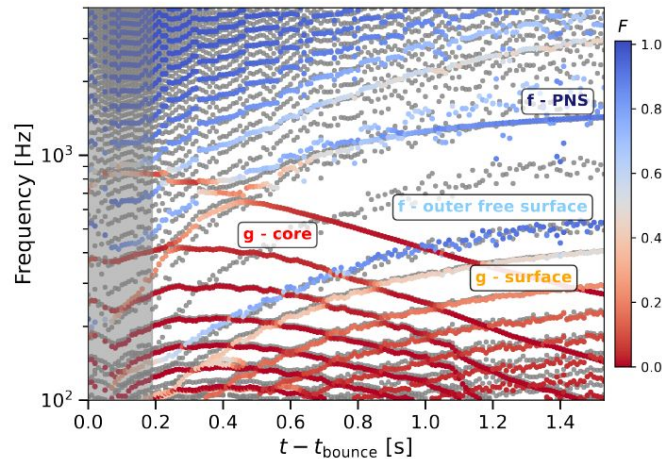


Mixed modes near the boundary are very difficult to classify.

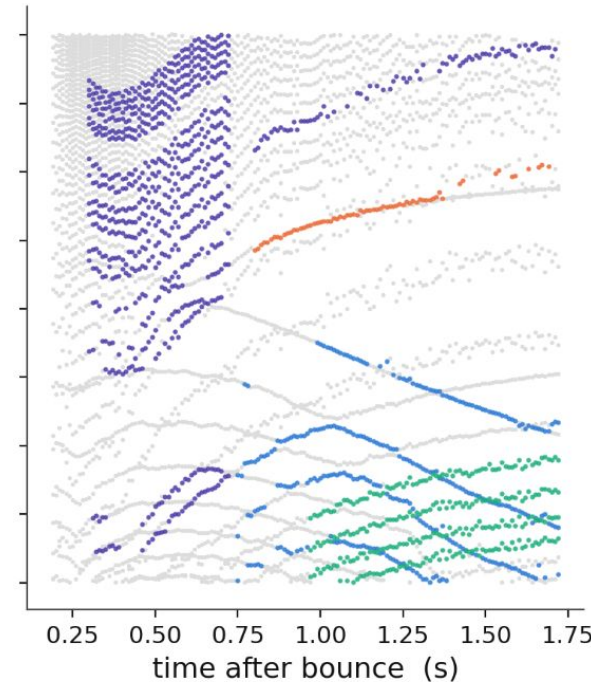
→ Scoring method
→ Separation factor

Application to other datasets

Oscillatory dataset (🏗️ Work in progress)
with boundary conditions at the shock, and 4 families
→ Separation between modes is much smaller
→ Last assumption is not true



Results



Conclusions



Pros

- Data-driven method useful for observation only applications
- Fast *low-tech* algorithm
- Fully automatic except some parameter tuning
- Robust method to crossings and avoided crossings



Cons

- Classification is limited near noisy boundaries
- Not robust to non-smooth oscillation modes

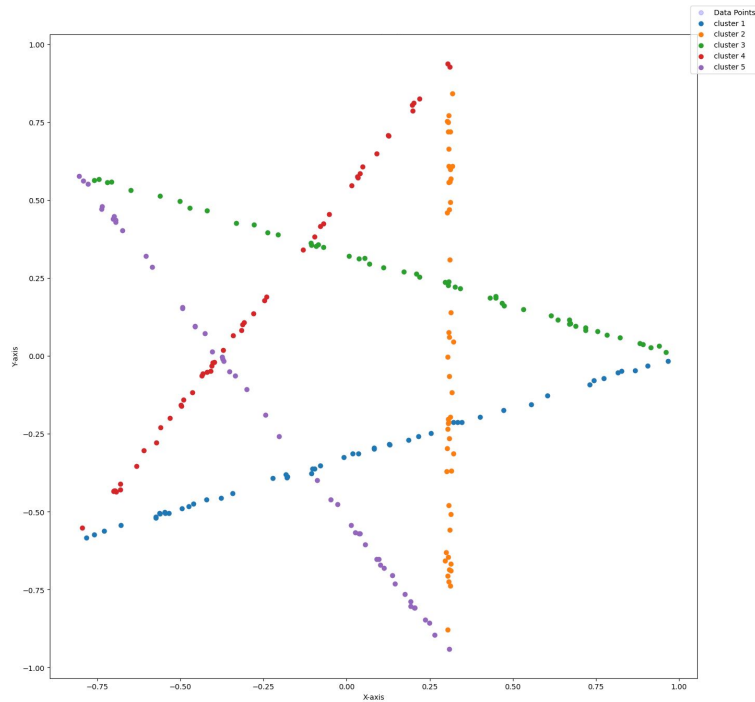


Future work

- Method robust to oscillatory modes
- Application to other datasets

THANK YOU

Extra: Line classification with J-Linkage



Toldo, R. (2008)

[DOI:10.1007/978-3-540-88682-2_41](https://doi.org/10.1007/978-3-540-88682-2_41)

- Minimal Sample Sets

$$P(\mathbf{x}_j|\mathbf{x}_i) = \begin{cases} \frac{1}{Z} \exp -\frac{||\mathbf{x}_j - \mathbf{x}_i||^2}{\sigma^2} & \text{if } \mathbf{x}_j \neq \mathbf{x}_i \\ 0 & \text{if } \mathbf{x}_j = \mathbf{x}_i \end{cases}$$

- Each point is represented by which models it belongs to.
- Model ownership is determined by distance to it.
- Clustering using Jaccard distance

$$d_J(A, B) = \frac{|A \cup B| - |A \cap B|}{|A \cup B|}.$$