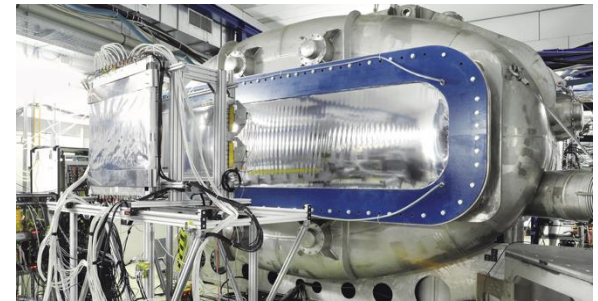
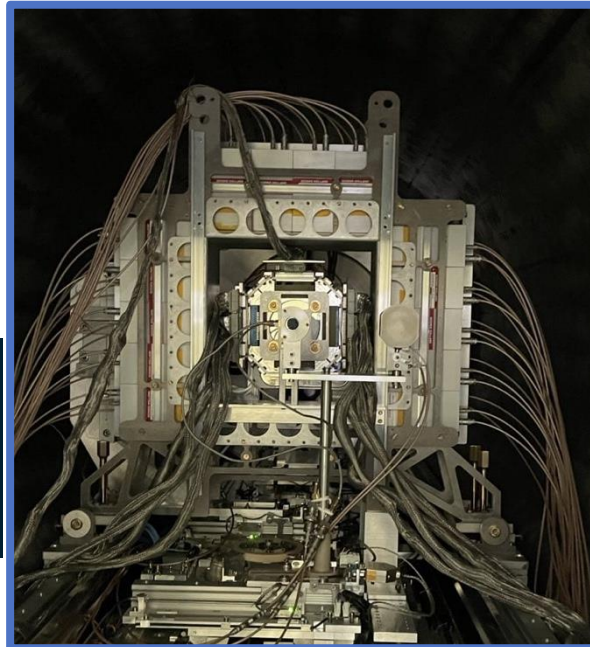
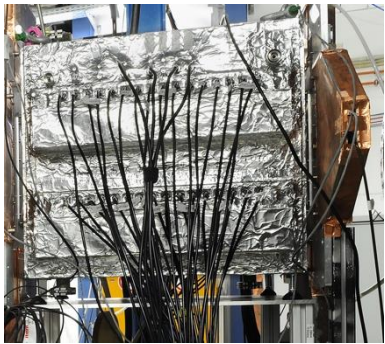


# Fission in inverse kinematics – history, status and outlook

A. Heinz  
Chalmers University of Technology

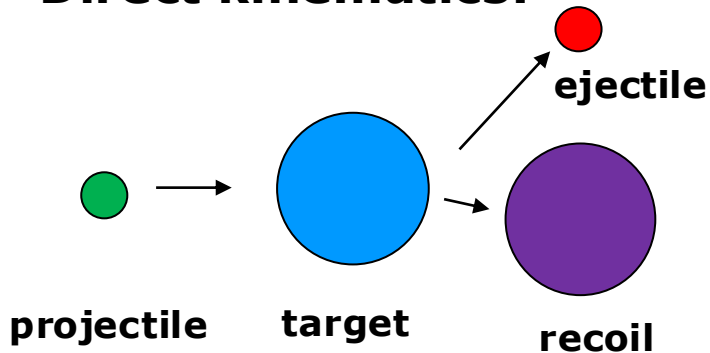


*Knut och Alice  
Wallenbergs  
Stiftelse*

 Vetenskapsrådet

# Direct vs. inverse kinematics

## Direct kinematics:



## Advantages:

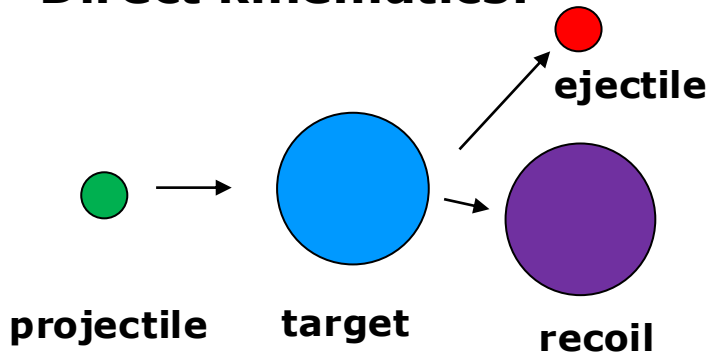
- High beam intensities.
- High angular and energy resolution of the ejectile.

## Disadvantages:

- Needs stable or long-lived beam and target.
- Recoil identification.
- Hard to do complete kinematics.

# Direct vs. inverse kinematics

## Direct kinematics:



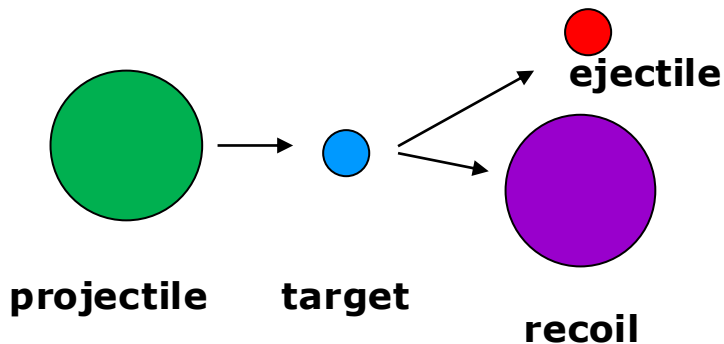
## Advantages:

- High beam intensities.
- High angular and energy resolution of the ejectile.

## Disadvantages:

- Needs stable or long-lived beam and target.
- Recoil identification.
- Hard to do complete kinematics.

## Inverse kinematics:



## Advantages:

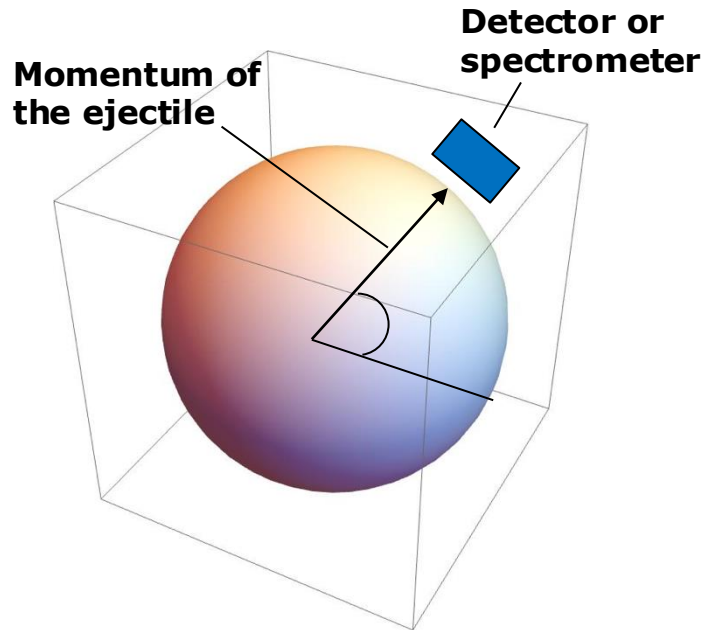
- Works with short lived beams.
- Recoils identification.
- Possible to do complete kinematics.

## Disadvantages:

- Energy and angular resolution of the ejectile.
- Low beam intensities.

# Kinematics

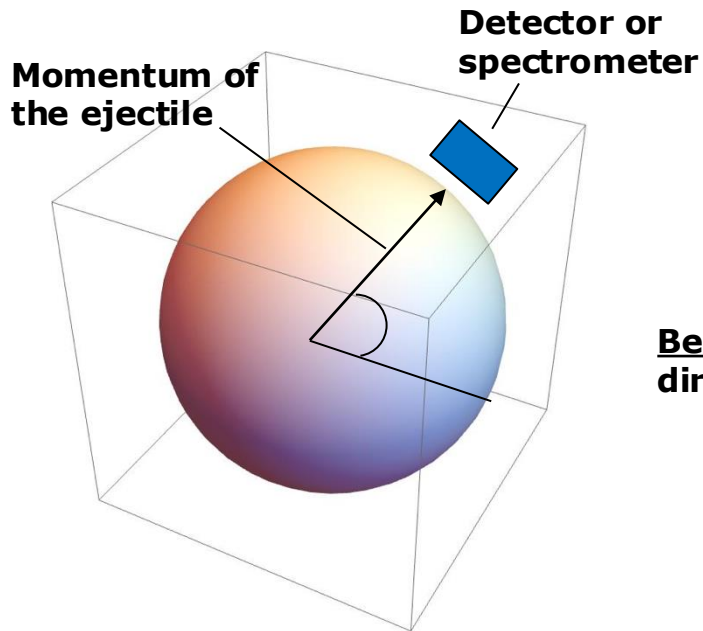
## Direct kinematics:



- Possible to get very good **energy and angular resolution**.
- Hard to cover  **$4\pi$** .

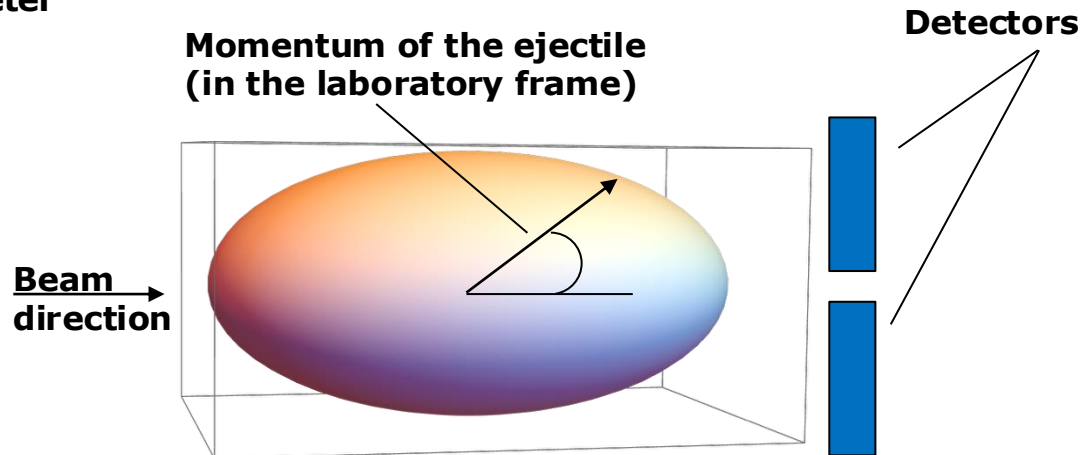
# Kinematics

## Direct kinematics:



- Possible to get very good **energy and angular resolution**.
- Hard to cover  **$4\pi$** .

## Inverse kinematics:

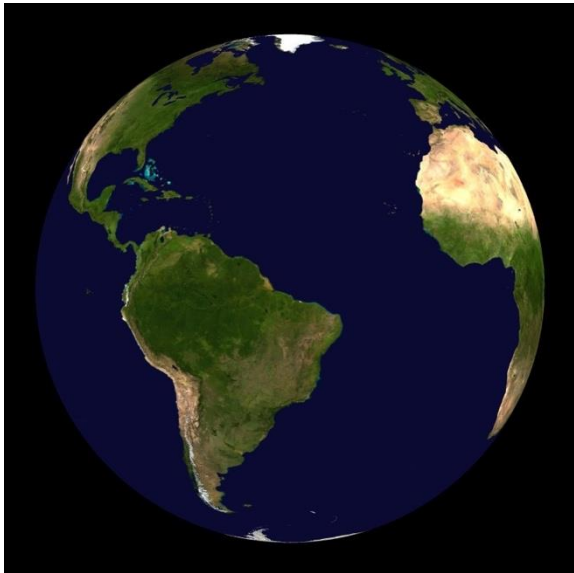


- Possible to get very good **solid angle coverage**.
- Limited **energy and angular resolution**.

---

# A problem known from geography

---



**Projection**

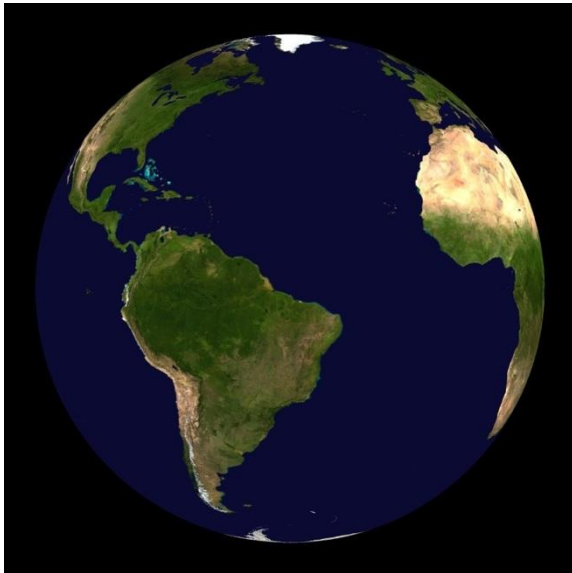


**Images from Wikipedia**

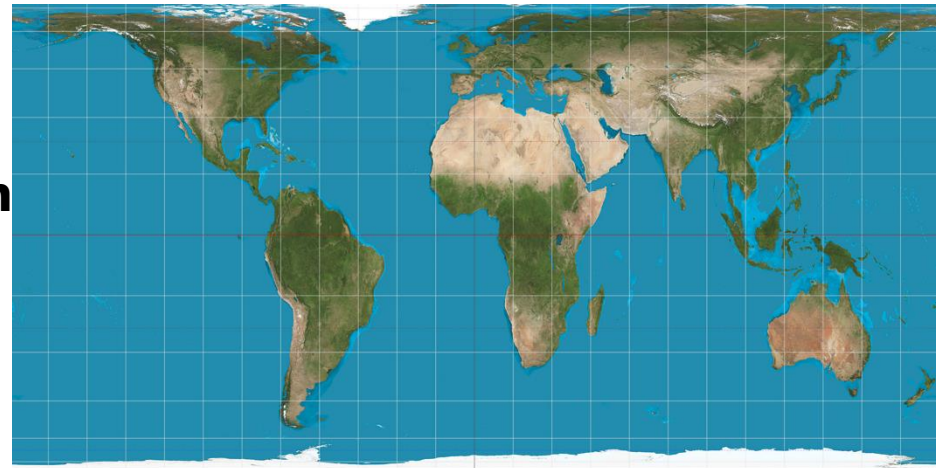
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# A problem known from geography

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**Projection**  
→

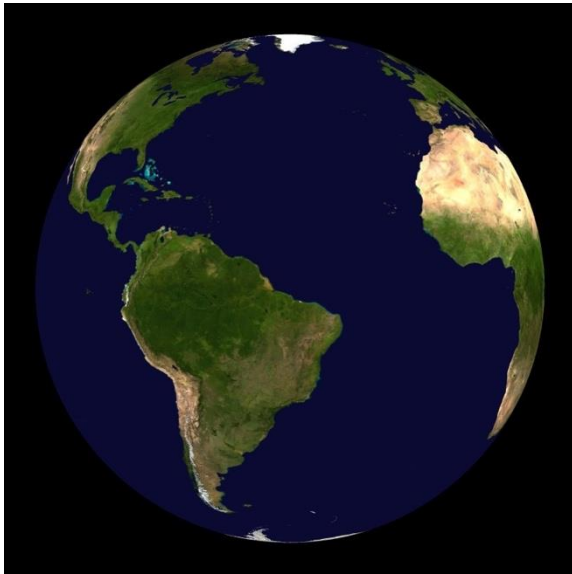


**Images from Wikipedia**

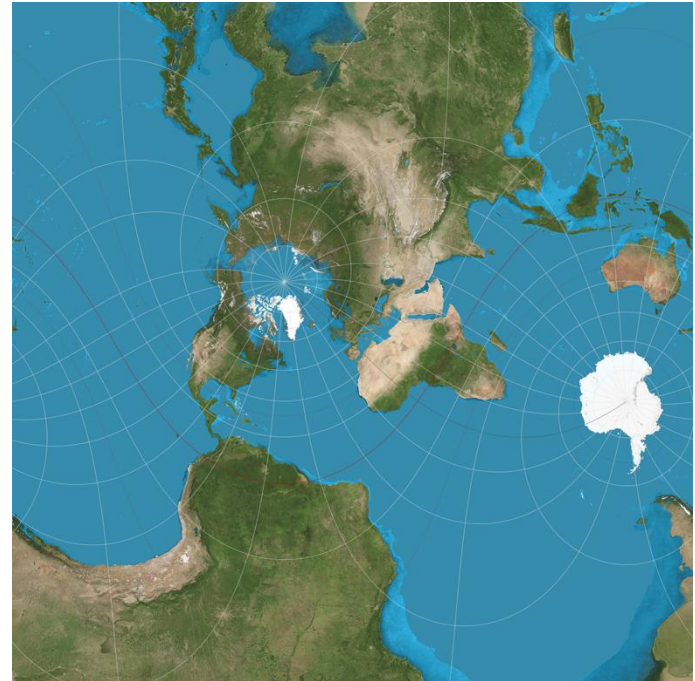
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# A problem known from geography

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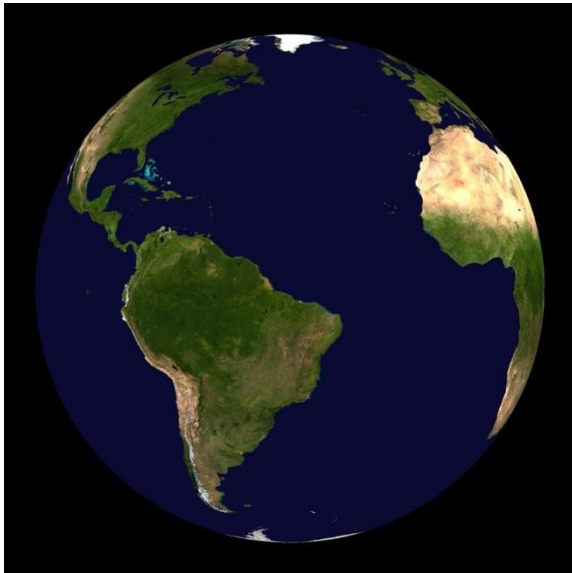


**Projection**

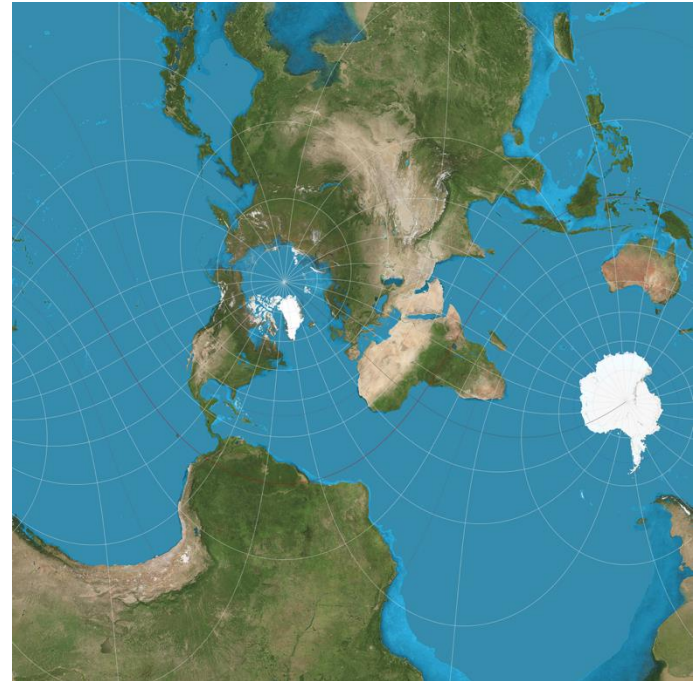


**Images from Wikipedia**

# A problem known from geography



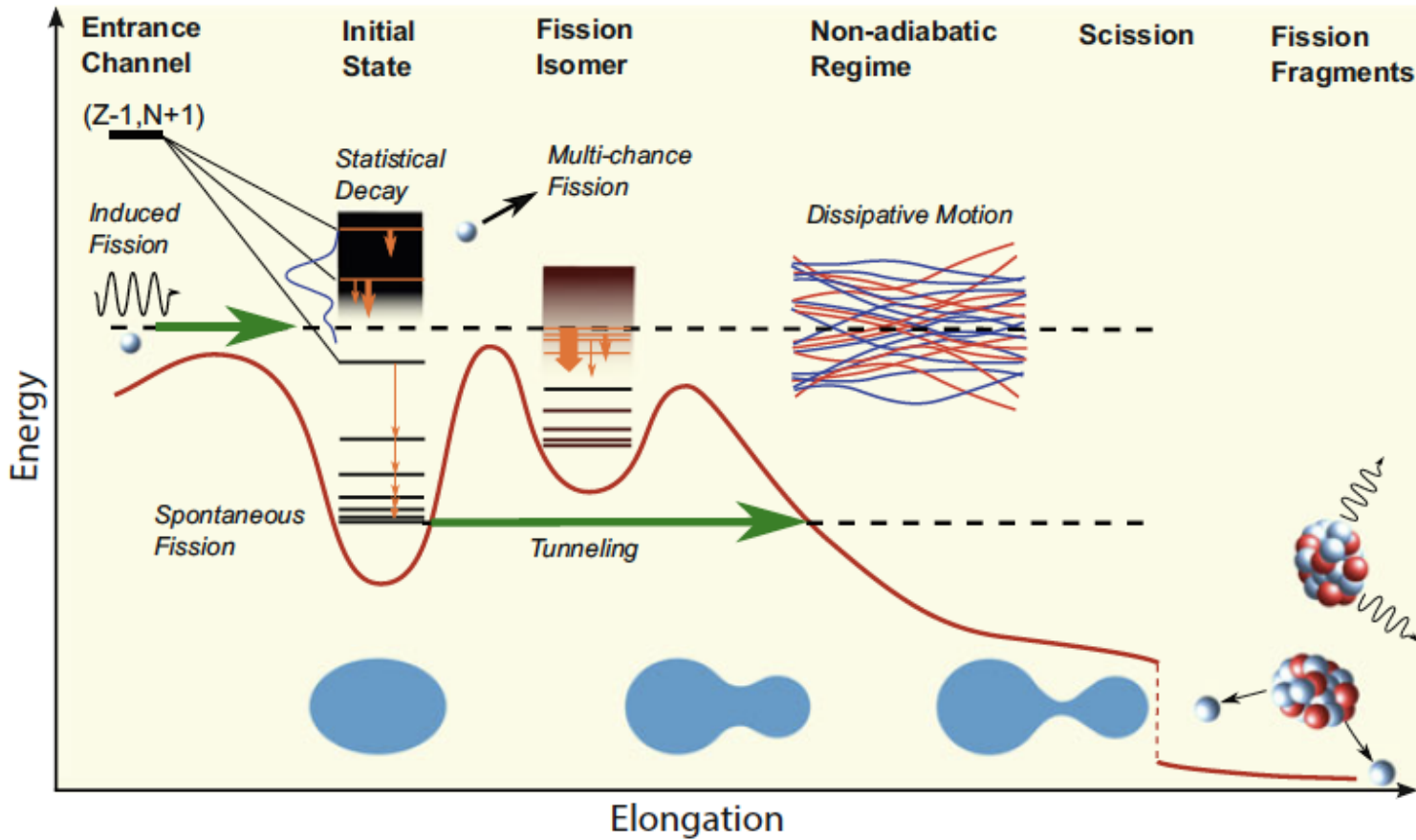
Projection



**The “solution” for inverse kinematics: don’t project on 2D  
→ listen to the talk of Maria Vittoria.**

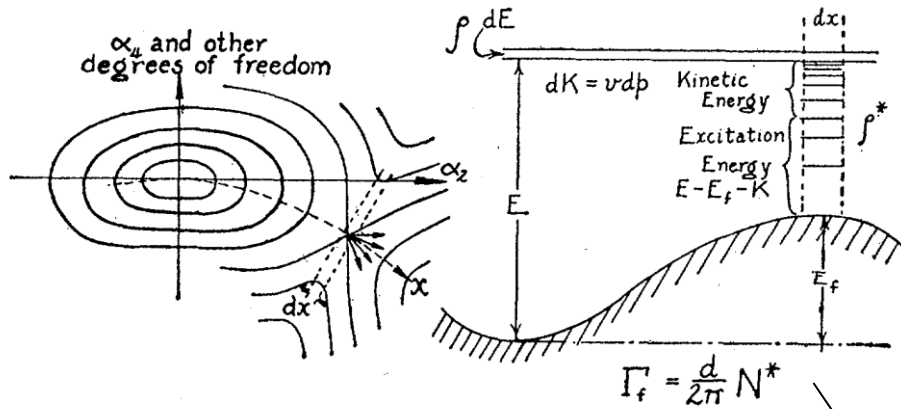
**Images from Wikipedia**

# Nuclear fission



N. Schunck, *Microscopic Theory of Nuclear Fission* in *Handbook of Nuclear Physics*, Springer Nature Singapore (2023)

# Potential Energy Surface



The **potential energy surface** and the relation to the **level density, i.e. available phase space, above it.**



Disintegration of Uranium by Neutrons: a New Type of Nuclear Reaction

ON bombarding uranium with neutrons, Fermi and collaborators<sup>1</sup> found that at least four radioactive substances were produced, to two of which atomic numbers larger than 92 were ascribed. Further investigations<sup>2</sup> demonstrated the existence of at least

Meitner, O. Frisch, *Nature* 143, 239 (1939)



SEPTEMBER 1, 1939

PHYSICAL REVIEW

VOLUME 56

The Mechanism of Nuclear Fission

NIELS BOHR

*University of Copenhagen, Copenhagen, Denmark, and The Institute for Advanced Study, Princeton, New Jersey*

AND

JOHN ARCHIBALD WHEELER

*Princeton University, Princeton, New Jersey*

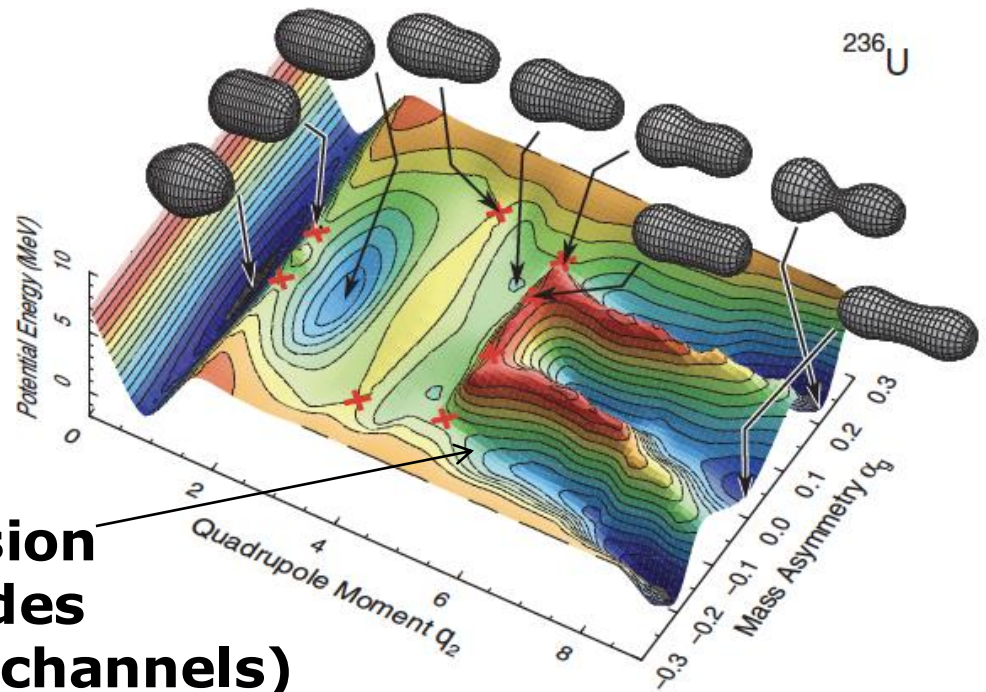
(Received June 28, 1939)

# Fission modes

Valleys and passes in the potential energy surface.

- ⇒ **Fission modes** characterized by:
  - ⇒ **asymmetry** and
  - ⇒ **deformation** at scission.
- ⇒ **Experimental signatures:**
  - ⇒ **Fission fragment mass and charge distributions.**
  - ⇒ **Total kinetic energy release.**
- ⇒ **Mapping** of the potential energy surface with data.

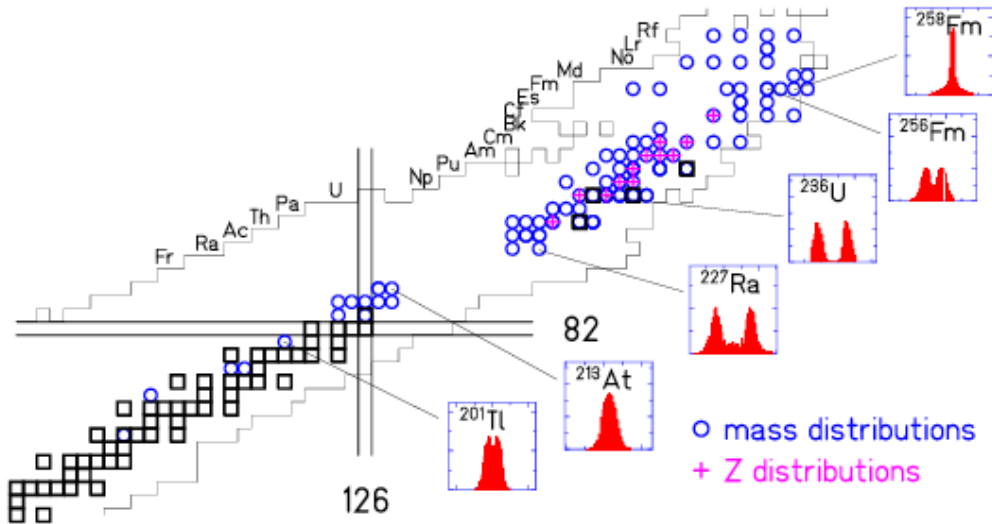
**Fission modes (or channels)**



T. Ichikawa et al., Phys. Rev. C 86, 024610 (2012)

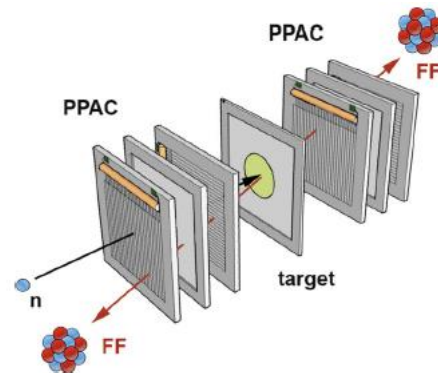
The available **phase space** is the key to understand the fission fragment **yields**.

# Experimental status around 1995



A.N. Andreyev et al., Rep. Prog. Phys. 81, 016301 (2018)

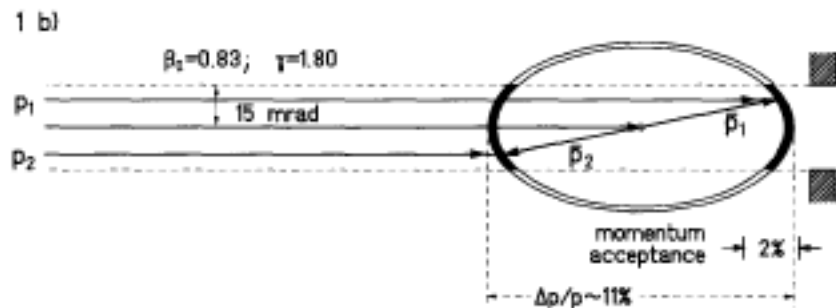
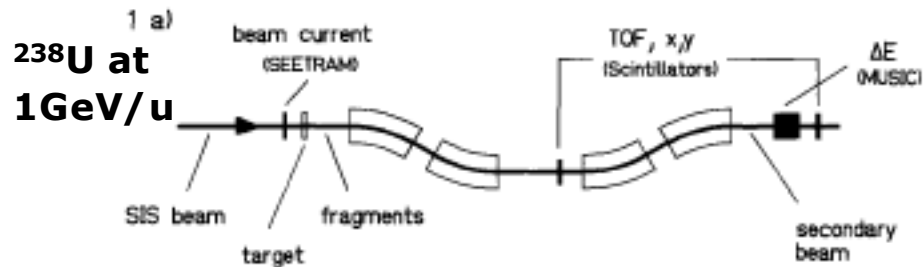
## Schematic layout of an experiment (n\_TOF):



N. Colonna et al., Eur. Phys. J. A. 56, 48 (2020)

- **Limited number of isotopes studied mostly in direct kinematics.**
- **Three main approaches to induce fission: neutrons, light charged particles, spontaneous fission.**
- **Challenging to identify fission fragments in A and Z.**

# Fission in **inverse kinematics**: isotopic resolution of fission fragments



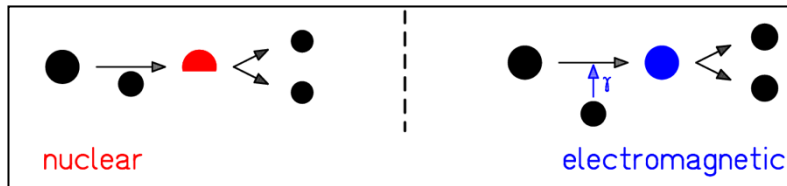
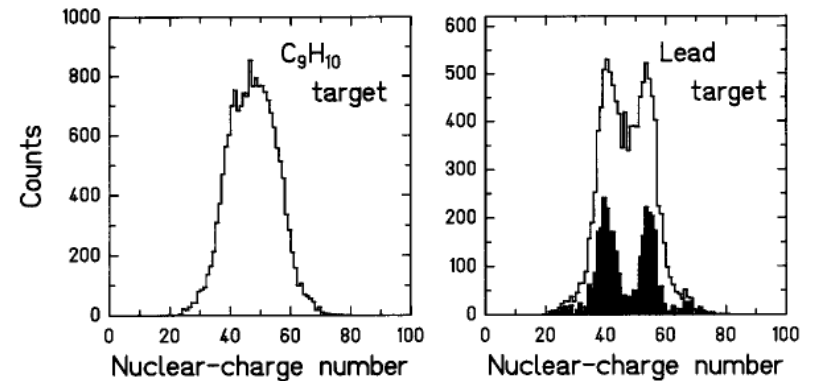
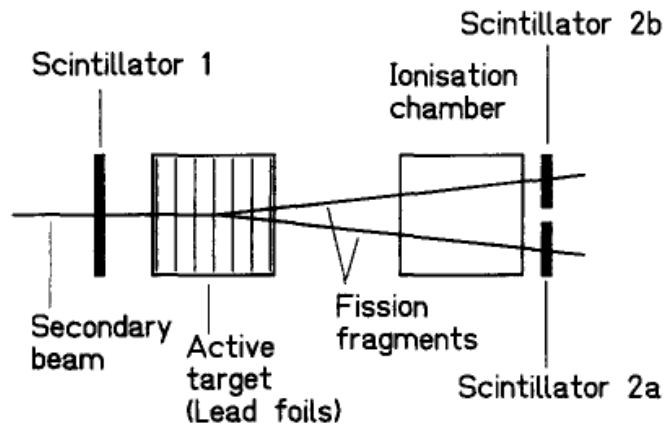
Nuclear Charge $Z \Rightarrow$ ionization chamber	} $\Rightarrow \frac{B\rho \cdot Z}{\gamma\beta} = A$
Bending $\rho \Rightarrow$ positions	
Velocity $\gamma\beta \Rightarrow$ ToF	
Magnetic field $B \Rightarrow$ Hall probes	

- The **beam fissions**, not the target.
- **Event-by-event identification of one fission fragment!**
- Only for **stable** beams!
- **Widely used to produce neutron-rich beams.**

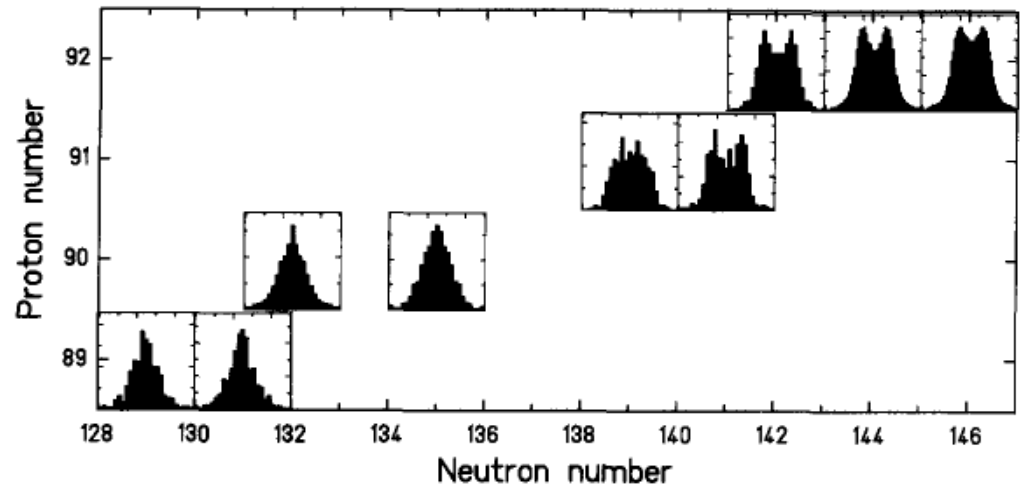
M.Bernas et al., Phys. Lett. B 331, 19 (1994)

**Talk of S. Pietri**

# Fission of **radioactive beams** in **inverse kinematics** (first attempt)

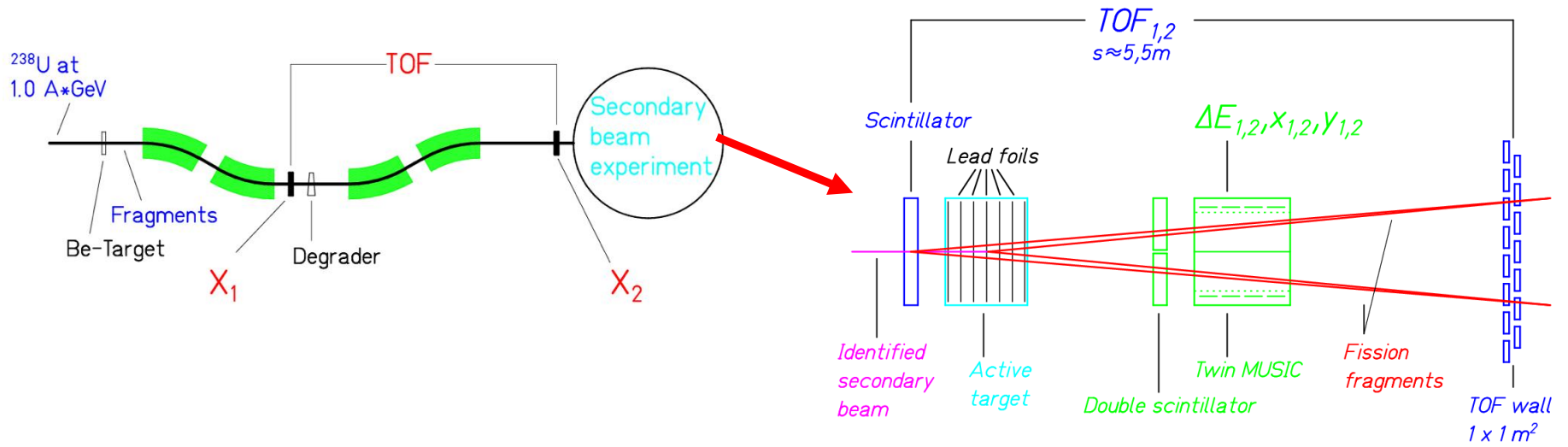


Use radioactive (secondary) beams in inverse kinematics at **relativistic energies** (about **500 MeV/u**)



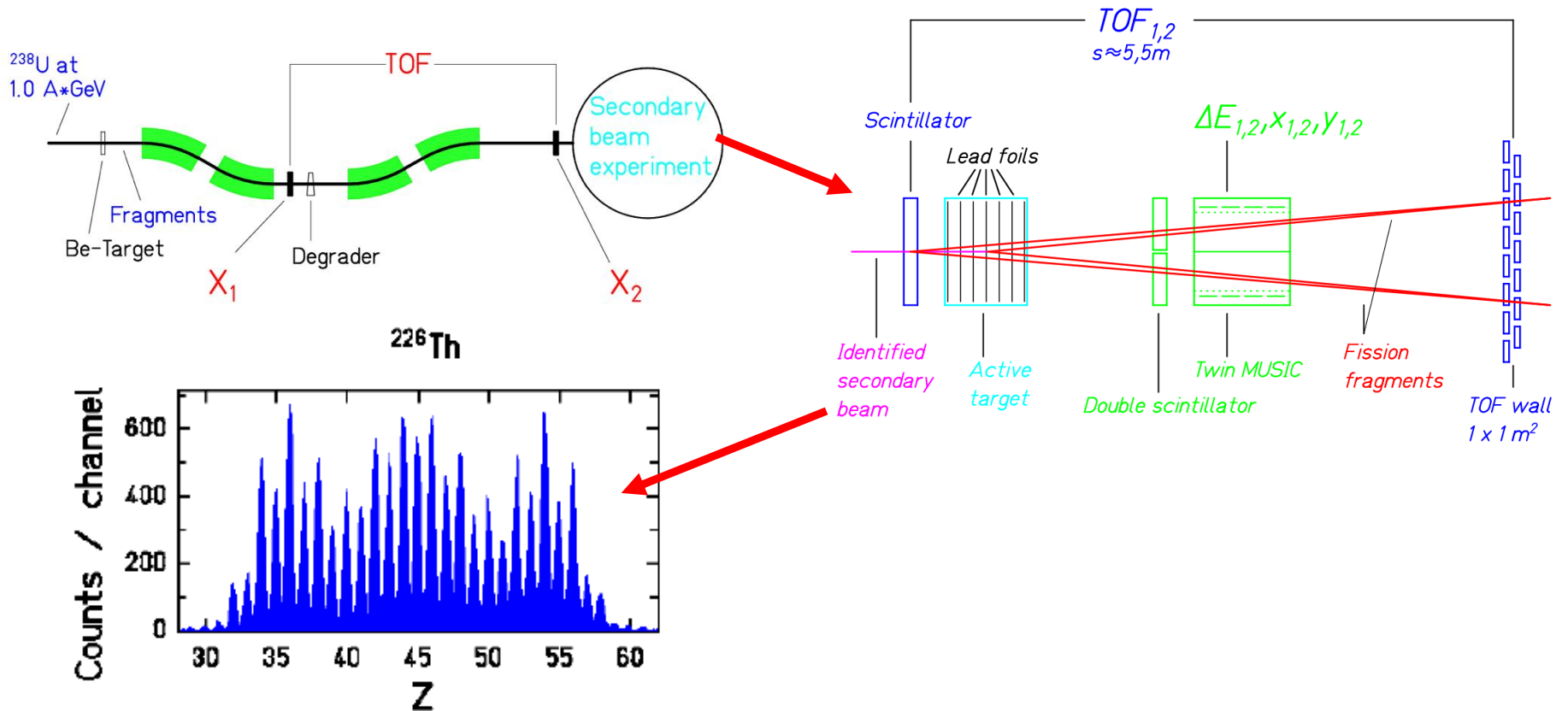
K.-H. Schmidt, A. Heinz, et al., Phys. Lett. B 325, 330 (1994)

# The third attempt



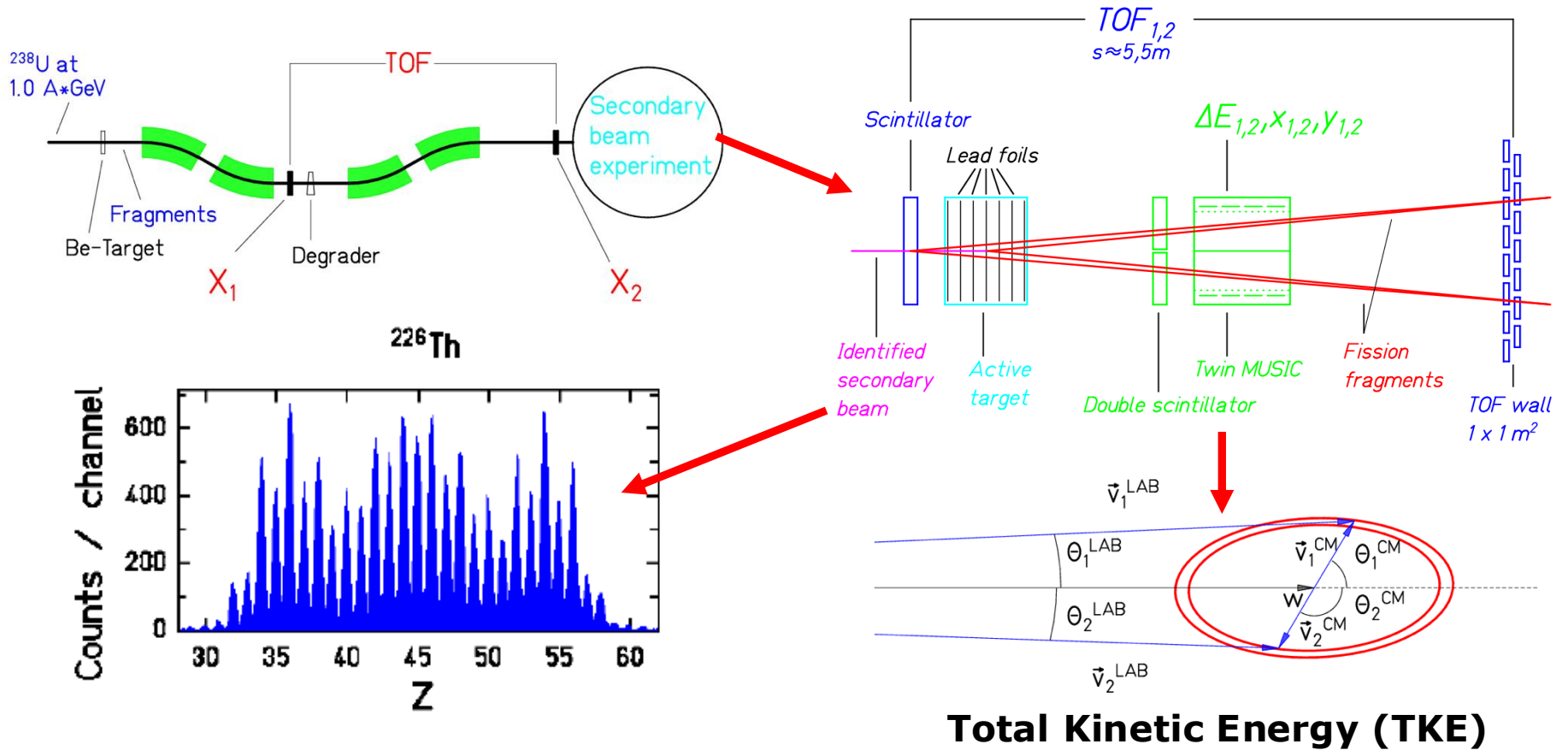
K-H. Schmidt et al., Nucl. Phys. A 665, 221 (2000)

# The third attempt



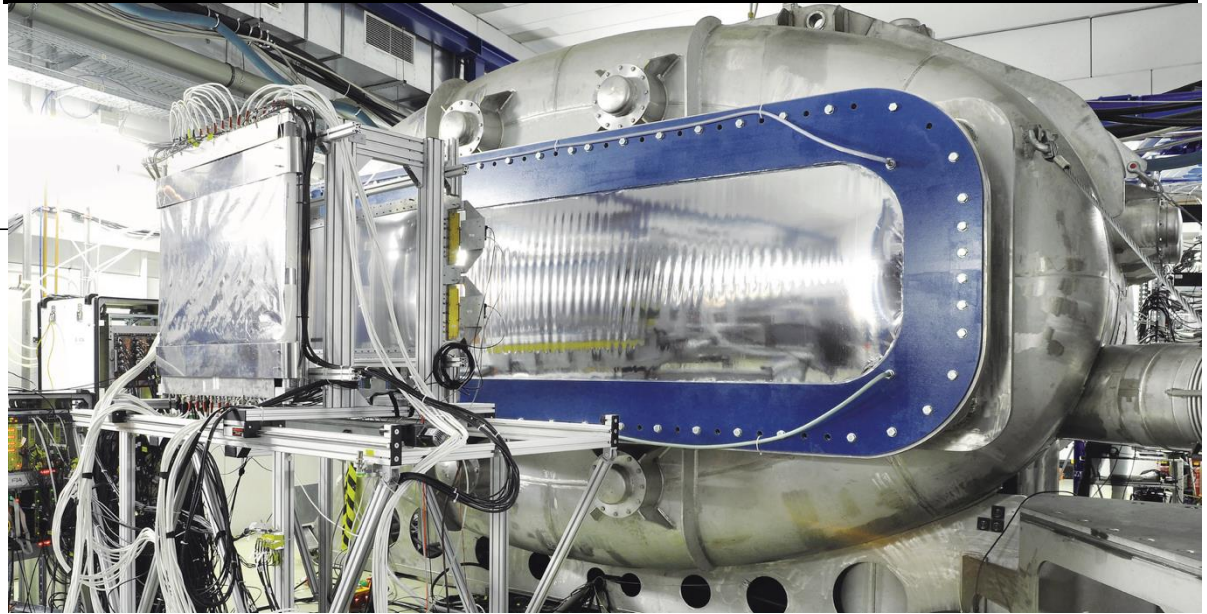
K-H. Schmidt et al., Nucl. Phys. A 665, 221 (2000)

# The third attempt



K-H. Schmidt et al., Nucl. Phys. A 665, 221 (2000)

C. Böckstiegel et al., Phys. Lett B 398, 259 (1997)



**Goal:**

Measure **A** and **Z** of **both fission fragments in coincidence** for fission of radioactive beams.

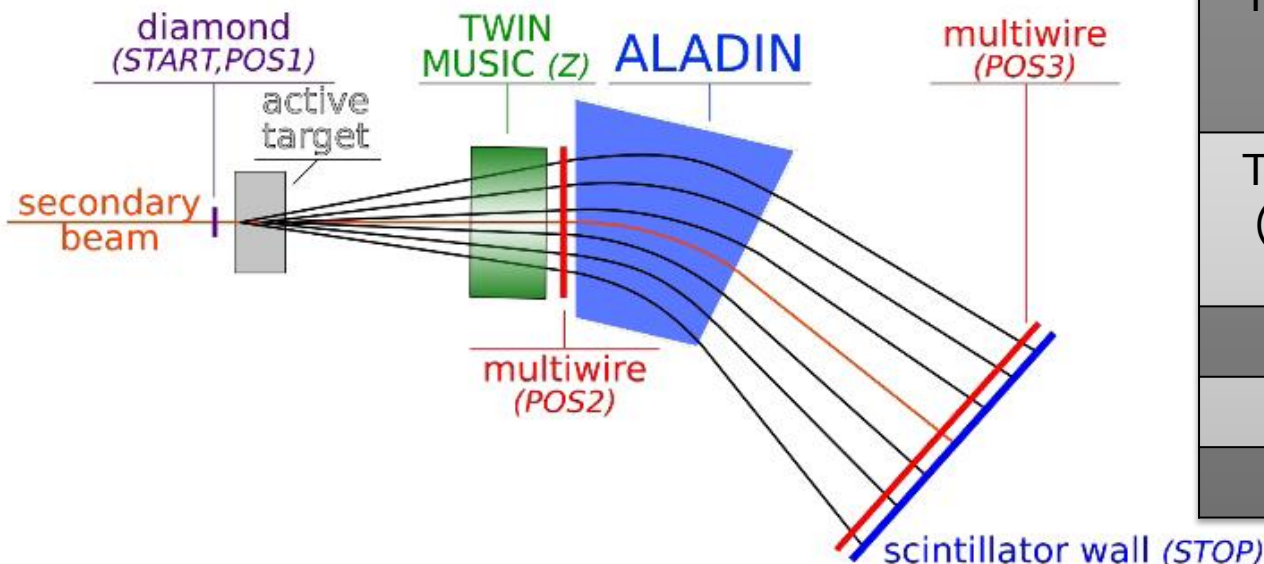
**Method:**

Add a **large dipole magnet** to the setup.

**Disadvantage:**

**No measurement of  $E^*$**  before fission.

# SOFIA – Set-up



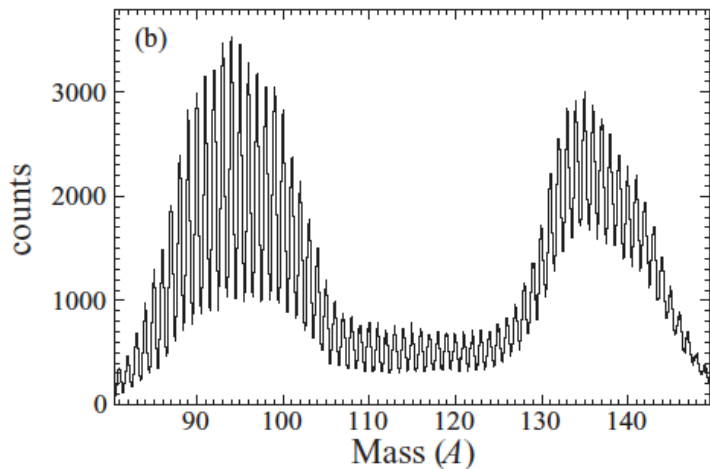
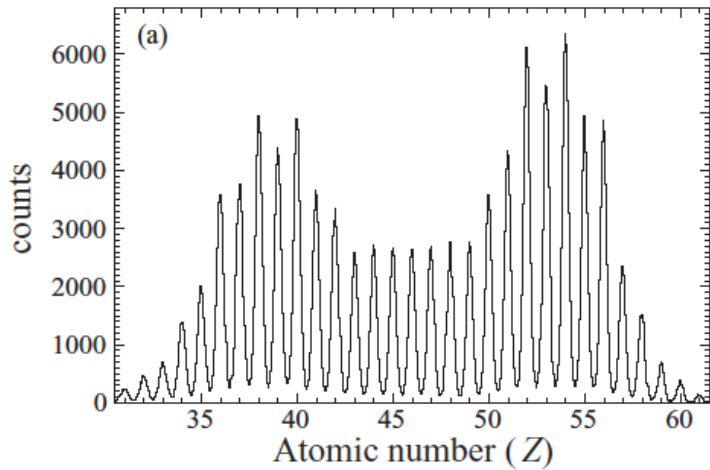
Detector	Resolution (FWHM)
Twin MUSIC (energy)	< 1 % (0.2 in charge units)
Twin MUSIC (position & angle)	≈ 60 μm ≈ 0.1 mrad
MWPC 1	≈ 200 μm
MWPC 2	≈ 300 μm
ToF wall	≈ 40 ps

**Major improvement: masses and charges of the fission fragments!**

**Major challenge: straggling → mass, total kinetic energy resolution.**

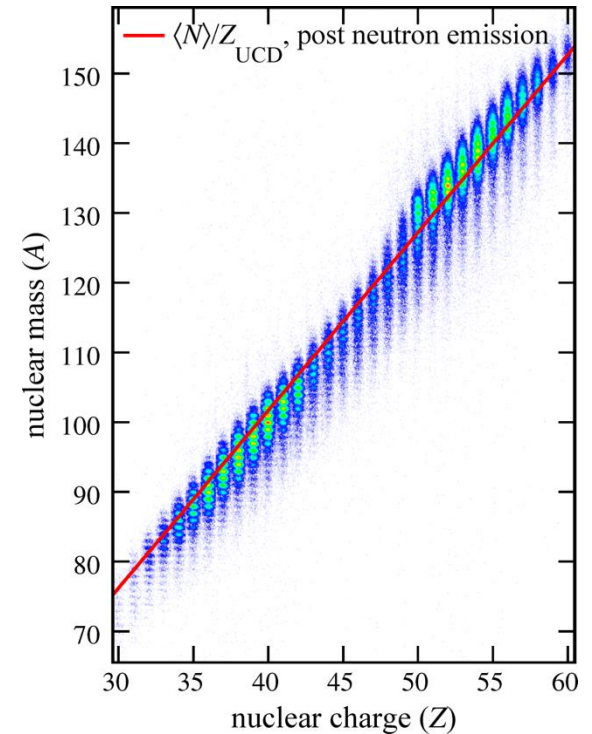
G. Boutoux et al.

# Charge and mass resolution



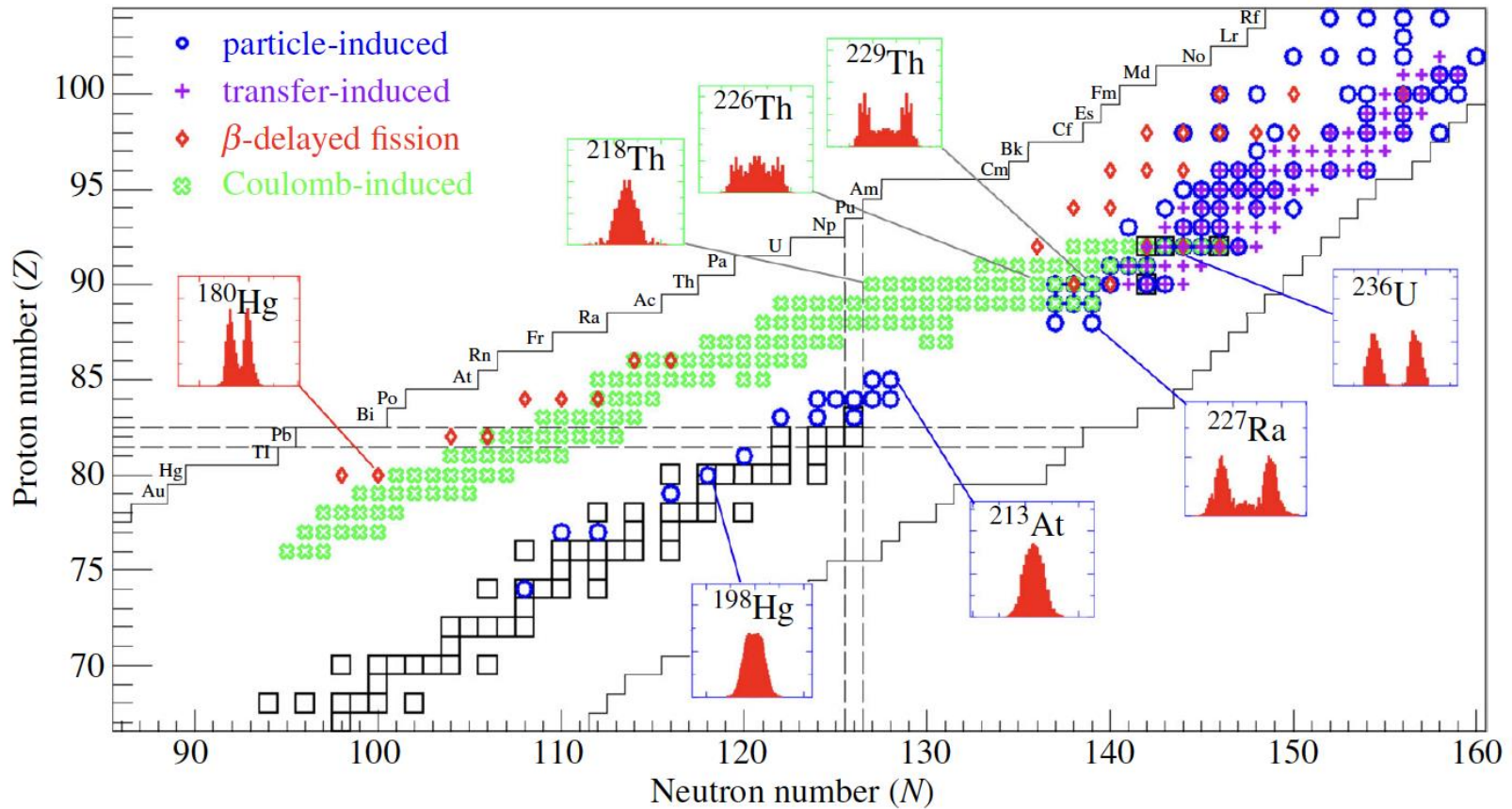
**It works!**

**$^{238}\text{U}$**



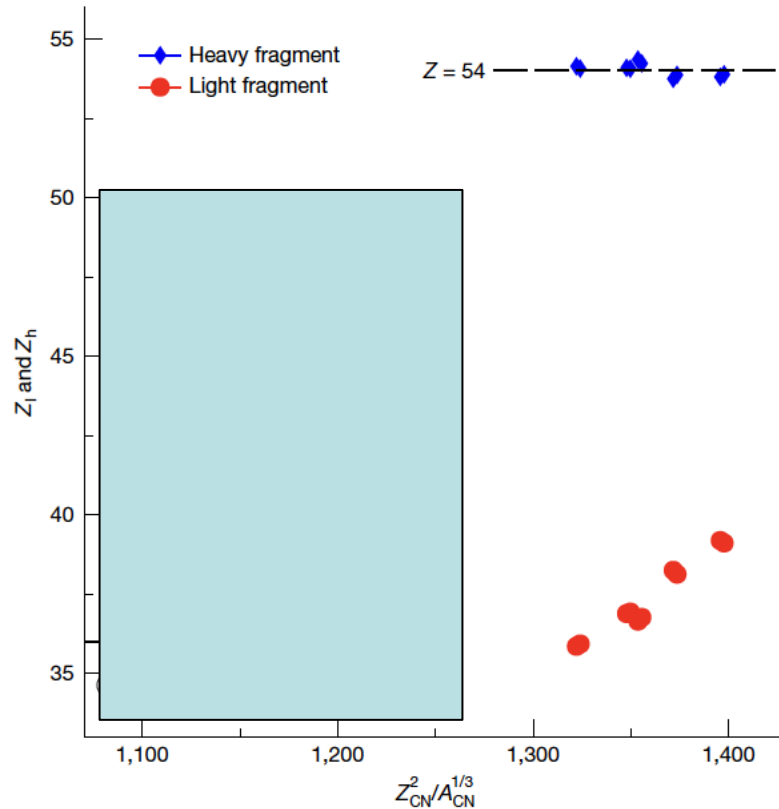
E. Pellerau et al.,  
Phys. Rev. C 95,  
054603 (2017)

# Status in 2023



T. Aumann et al., Phyl Trans. R. Soc. A 382, 20230121 (2024)

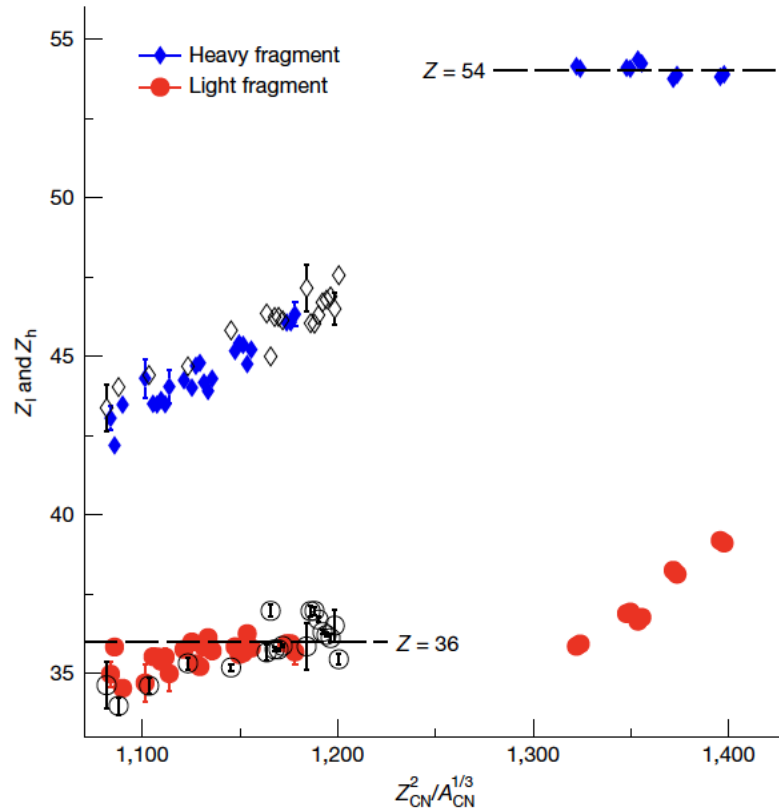
# Asymmetric fission



⇒ Looks like the  $Z$  of the heavy fragment is **always constant**.

P. Morfouace et al., Nature 641, 339 (2025)

# Asymmetric fission



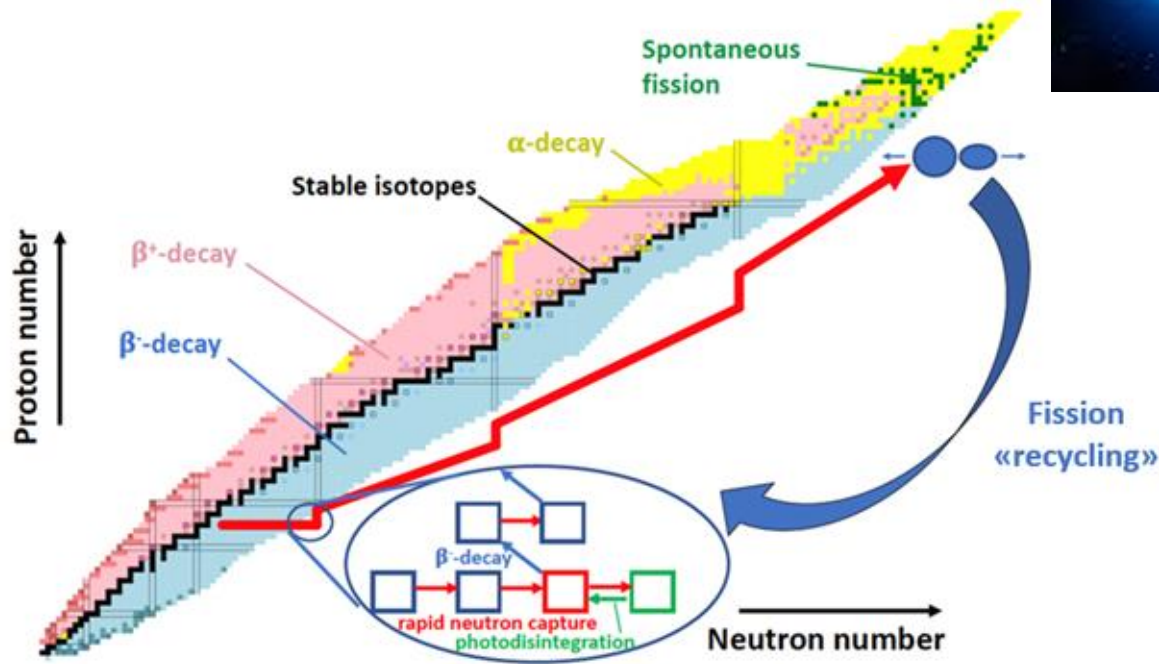
⇒ **(Deformed) Proton shells are responsible for the observed behavior.**

P. Morfouace et al., Nature 641, 339 (2025)

# Fission and nucleosynthesis



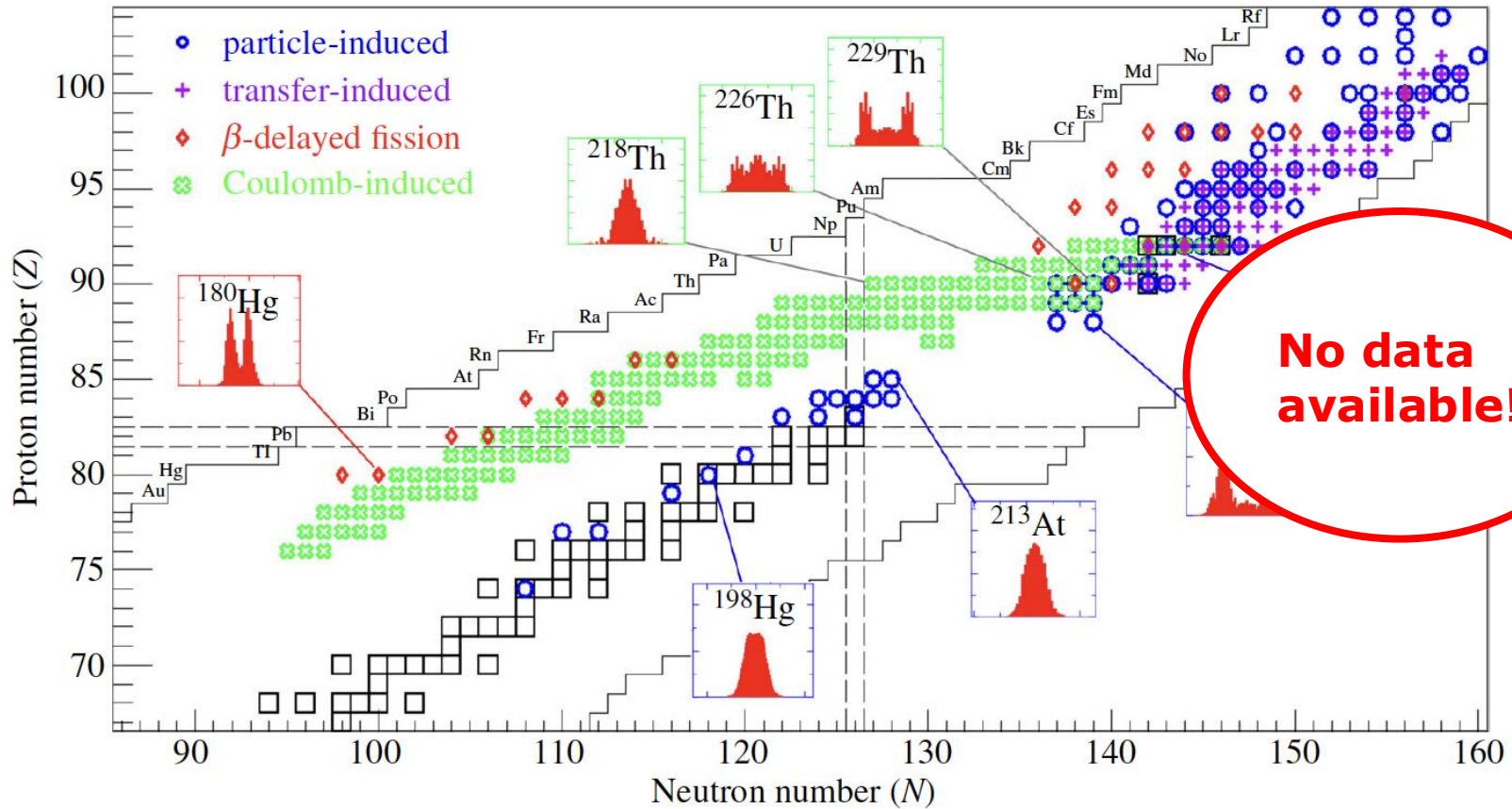
ESO/Univ. Warwick, Mark Garlick



- **Open questions:**
- **Fission probability of n-rich nuclei?**
- **What is the role of fission recycling in the r-process?**

Fission determines the **mass limit** of the nuclei which can be produced in the astrophysical **r-process**.

# What now?

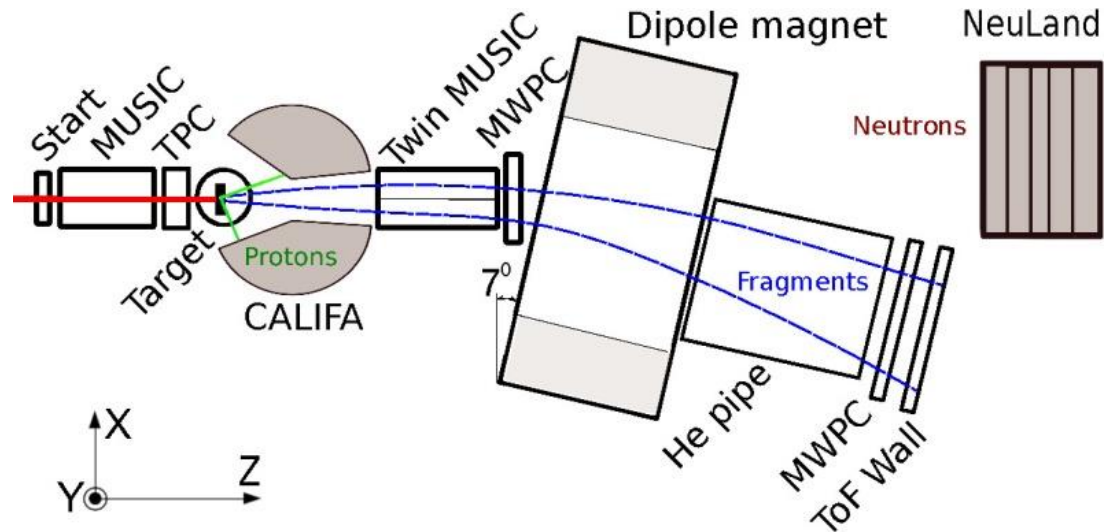


T. Aumann et al., Phyl Trans. R. Soc. A 382, 20230121 (2024)

# Fission after quasi-elastic scattering

**Reaction:**  
**(p,2pF) using a liquid H<sub>2</sub> target; relativistic energies.**

**Advantage:**  
**Measure fission observables**  
(masses, charges of fission fragments, total kinetic energy release) as **function of the excitation energy E\***.

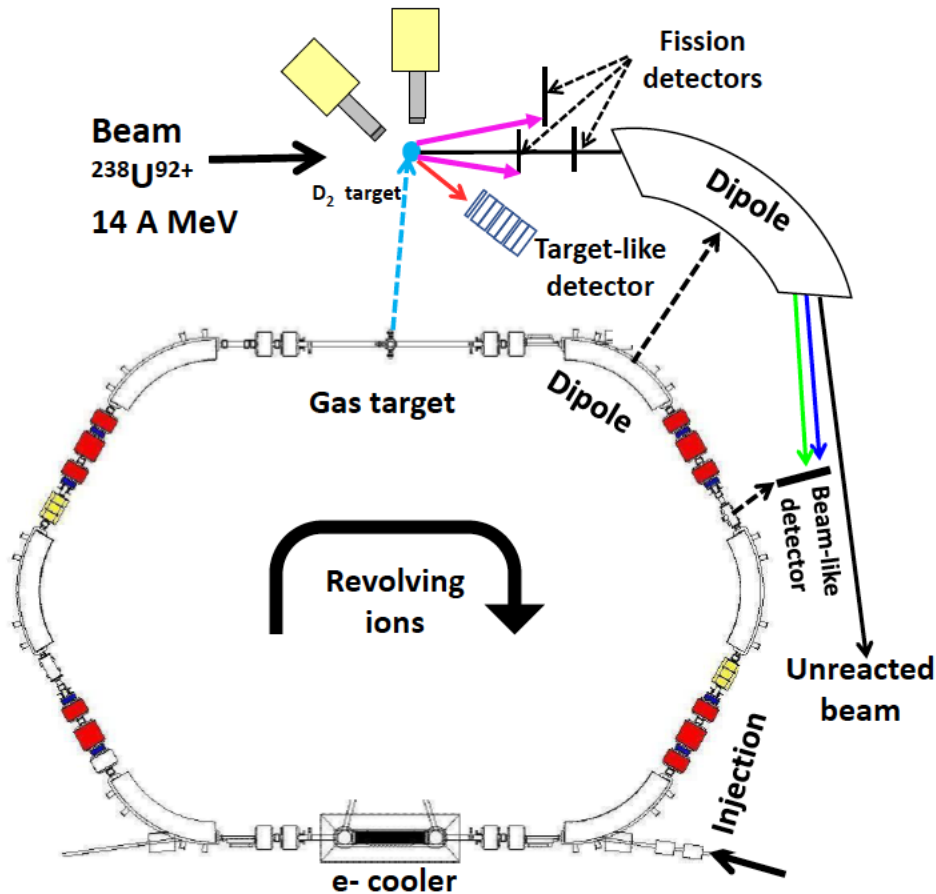


J. Taieb et al.

**Challenges:**

- **Background from delta-electrons.**
- **Lower cross sections.**
- **Limited E\* resolution.**

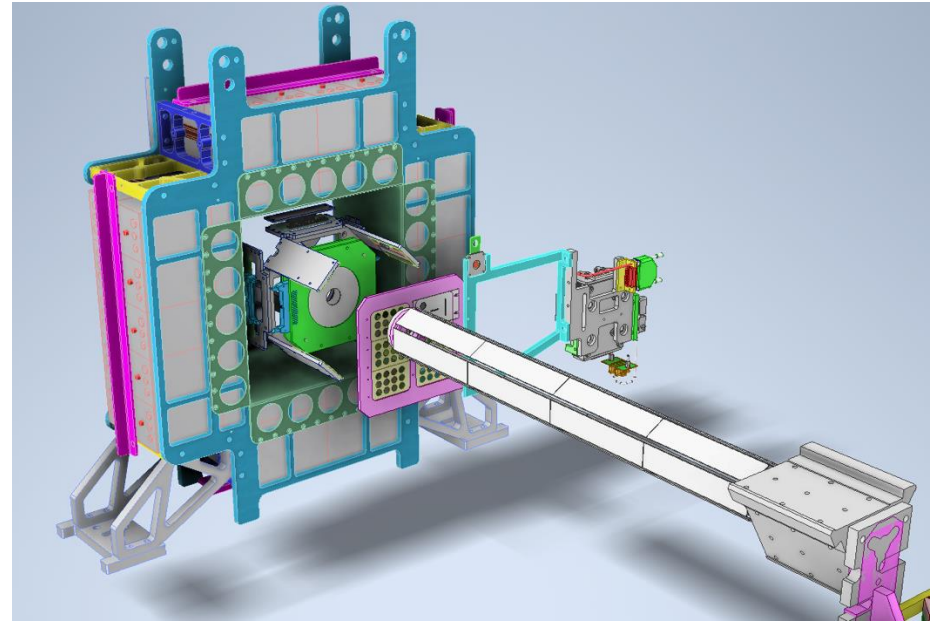
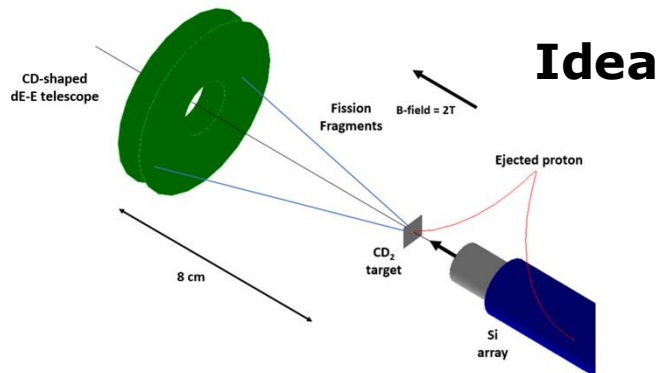
# Fission in storage rings



- **Proof-of-principle** experiment in the ESR at GSI in Summer 2024.
- **Tin target** => very **"clean"** conditions.
- Measure **excitation energy** and fission fragment **masses**.
- Measure **all competing decay channels** simultaneously.

B. Jurado et al.

# Fission using the ISOLDE Solenoidal Spectrometer (ISS)



Measured quantities	Observables
Back-scattered protons	$E^*, P_f$
Fission fragments (FFs)	$P_f$
Deuterons (for normalisation)	$\sigma_f$
$\gamma$ -rays from FFs	Total $E_\gamma, (m_\gamma)$

**Exploit the (d,pF) surrogate reaction with a radioactive beam.**

**⇒ Talk of Maria Vittoria!**

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# What do we need?

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- **A and Z of fission fragments.**
- **Total kinetic energy** released.
- **Neutron** energies and multiplicities.
- **Excitation energies.**
- **Gamma-ray** multiplicities and energies
- ...

**But most importantly: the ability to correlate as many of those observables as possible!**

---

# Conclusions

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- **Inverse kinematics comes with advantages and challenges.**
- **For radioactive beam experiments we have (often) no alternative.**
- **Fission studies in inverse kinematics are (one) way to extend the scope of fission studies.**
- **Different (complementary) experimental approaches have improved our understanding of fission! More is to come!**

**Thank you for your attention!**

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