

Primordial Features and Their Impact on Structure Formation

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Based on ongoing work with:
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Yuhsin Tsai, Fengwei Yang, Chris Jungkind (26???.XXXXX)

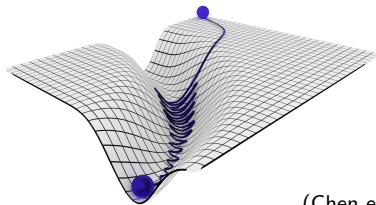
- 1 Primordial Features
- 2 Impact on Structure Formation

1 Primordial Features

2 Impact on Structure Formation

Features in Inflaton Trajectory

- The presence of other (heavy) fields during inflation may result in features in inflaton potential/trajectory



(Chen et al 2015)

- Motivation:
 - multi-field scenarios are likely (even effective single-field case)
 - gives rise to non-gaussianities
 - **results in features in primordial power spectrum**

(see also Chen 2010-2014++, Chluba et al 2015, Slosar et al 2019, ++)

Features in Primordial Spectrum

- Single-field slow-roll inflation predicts nearly scale invariant primordial spectrum

$$P_{\zeta 0} = A_s \left(\frac{k}{k_0} \right)^{n_s - 1} \quad (1)$$

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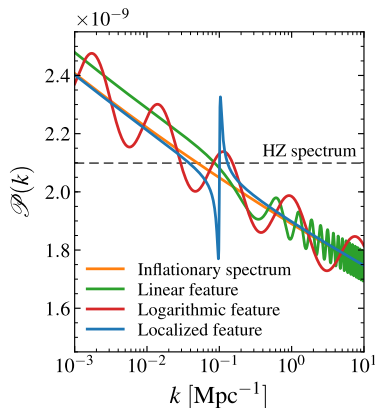
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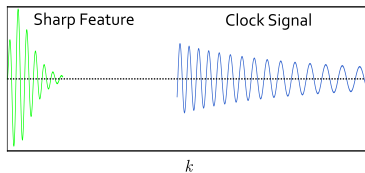


(Slosar et al 2019)

Primordial Clock Signal

- Massive field \rightarrow 2-part signal

Primordial Clock Signal

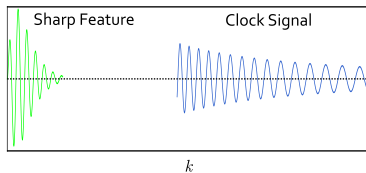


(Chen et al 2015)

- Massive field \rightarrow 2-part signal
- Sharp Feature: excitation of massive field

$$\Delta P_\zeta \sim \text{envelope} \times \cos k/k_0 \quad (3)$$

Primordial Clock Signal



(Chen et al 2015)

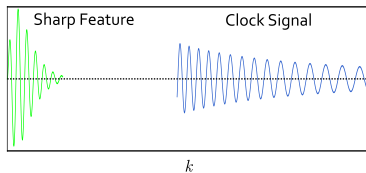
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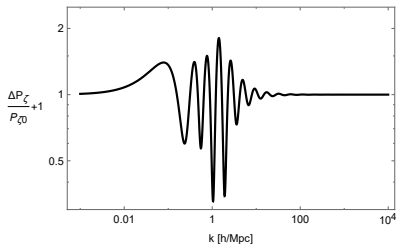
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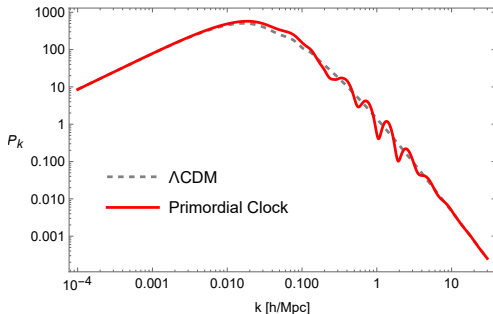
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Sensitivity to Matter Fluctuations

- Changes in the primordial spectrum
→ changes spectrum of matter fluctuations

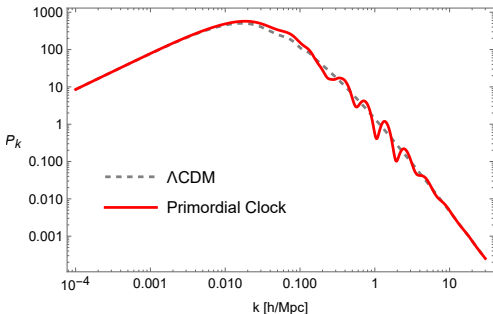
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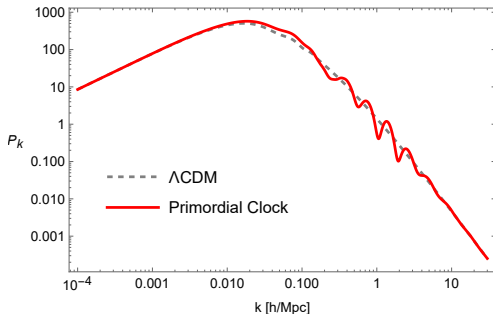
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(See Braglia et al 2021, 2022)

Sensitivity to Matter Fluctuations

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- Larger scales (smaller k) constrained by the CMB
(See Braglia et al 2021, 2022)
- Primordial feature signal in scales of structure formation?

1 Primordial Features

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Targets in Structure Formation

- Many upcoming observations of structure becoming available



Targets in Structure Formation

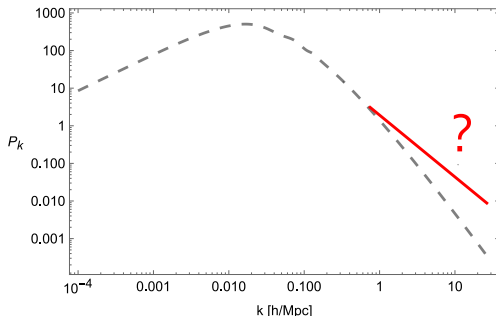
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- Interesting new results already in JWST
 - e.g. high redshift galaxies, little red dots

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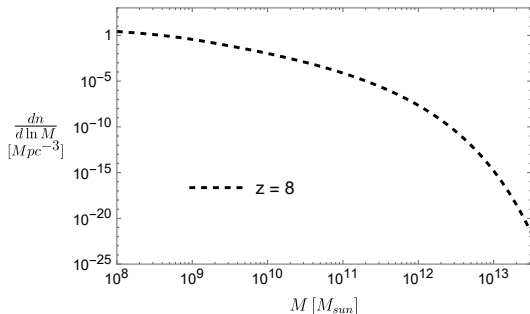
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- Emerging picture of more structure at smaller scales

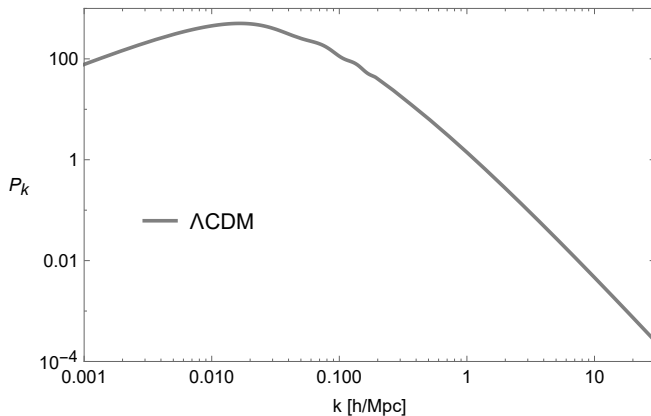
Halo Mass Function (HMF)

- Distribution of haloes predicted using excursion set theory (extended Press-Schechter)
- Using linear matter power spectrum, estimate collapse of structure
- Predict number density of haloes per mass interval $\frac{dn}{d \ln M}$



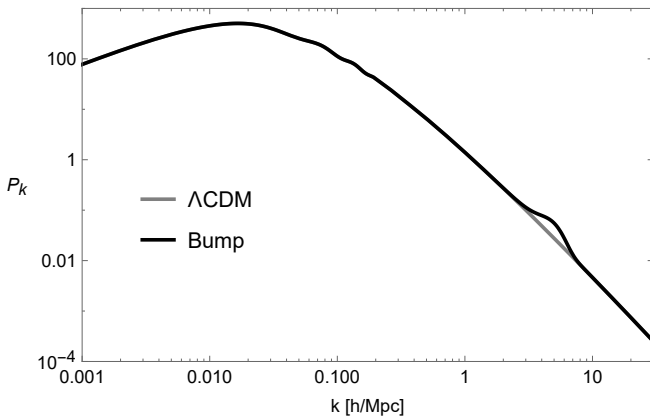
HMF from Simplified Behaviors

Try simple behaviors in matter power spectrum



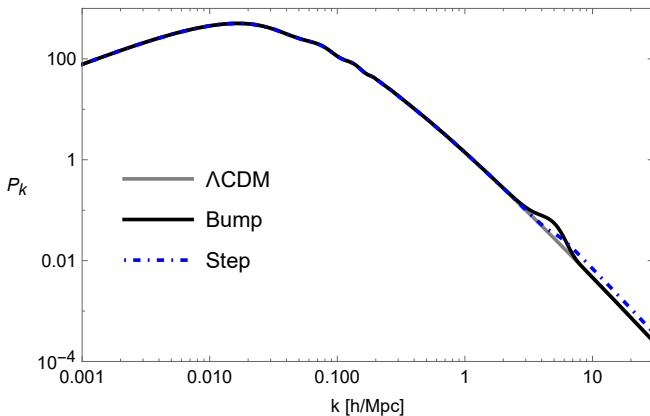
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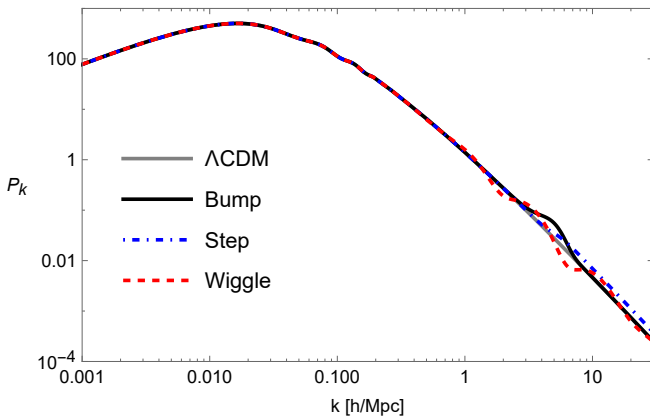
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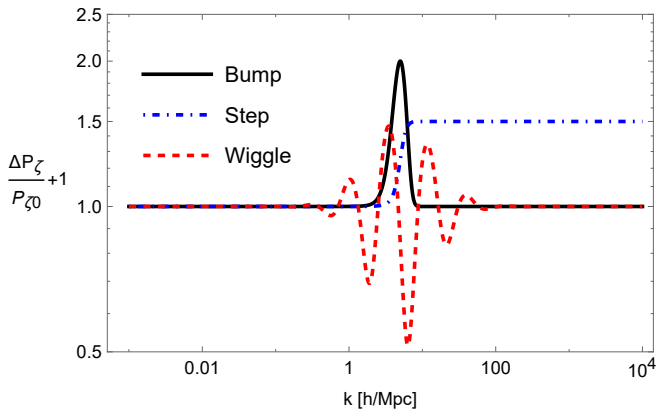
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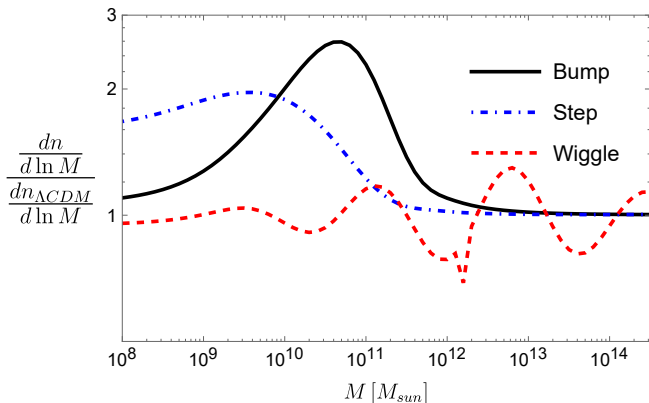
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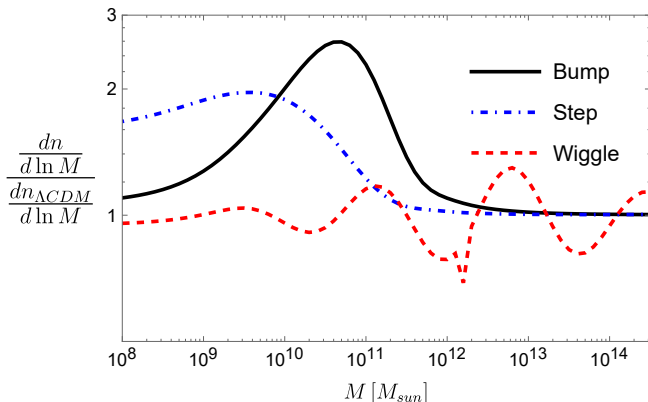
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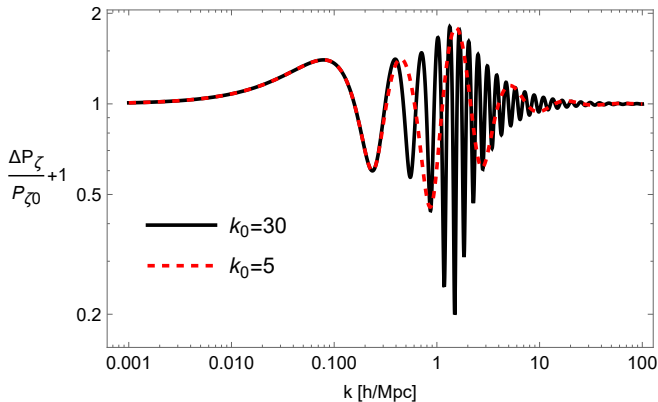
Try simple behaviors in matter power spectrum



Everything is smeared, BUT oscillations may survive!

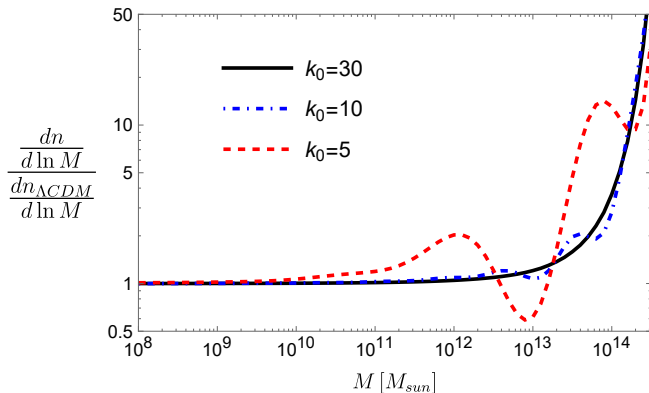
HMF from Sharp Feature + Clock

Simplified Sharp Feature + Clock, with different frequencies (mass)



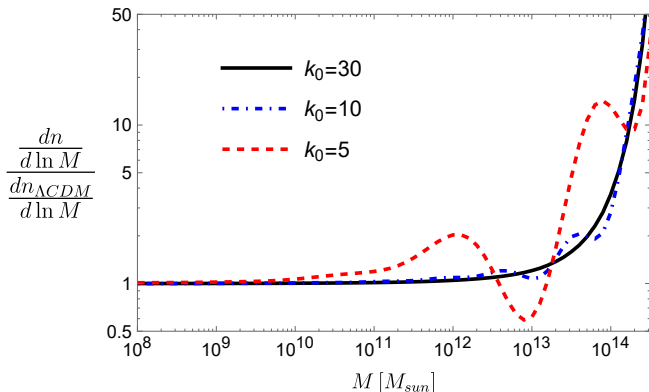
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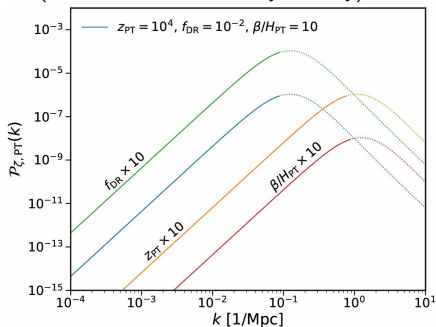
High, low frequency lose oscillations

(see also Acharya 2026)

→ intermediate frequency oscillations remain!

Bonus: First Order Phase Transitions

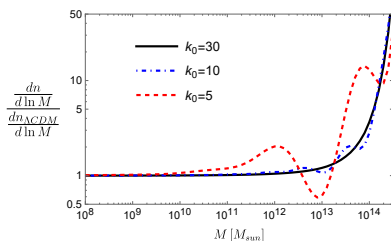
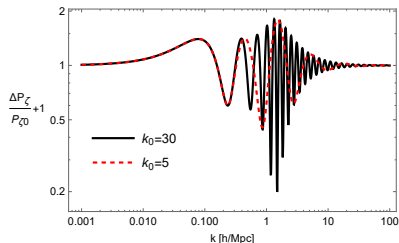
(From Daven Ho's Talk yesterday)



- First order PT modifies spectrum of perturbations
- Impact on *subhalo* mass function

- Ongoing work: understand sensitivity to substructure of pulsar timing arrays
(based on Dror et al, Ramani et al, Lee et al ++)

Summary



- Oscillatory primordial features → maybe oscillations in HMF
- Important questions
 - Constraints from data e.g. UVLF from HST/LWST
 - Do oscillations remain after later galaxy mergers?
- Stay tuned for upcoming results!