



AMPLITUDES 2026

29 June – 3 July 2026



Queen Mary
University of London

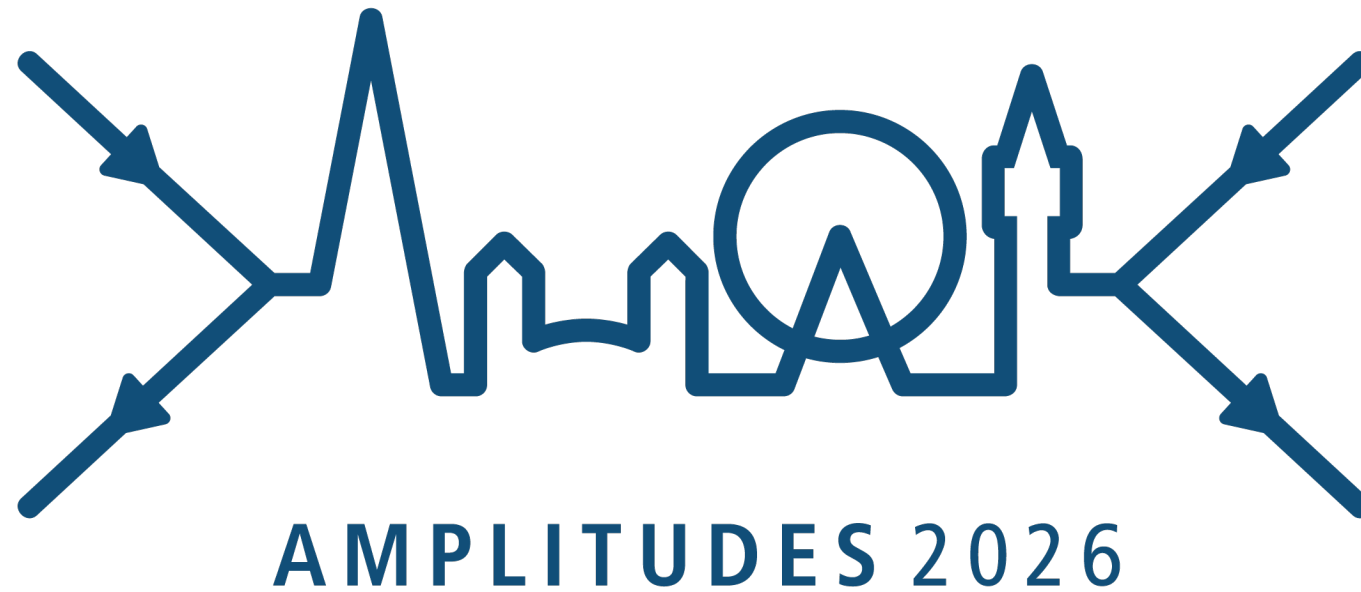
Est.
1785



SAGEX

Scattering Amplitudes:
from Geometry to Experiment

Welcome to the Gong Show: Part II



Yuanche Liu

Next: Carl Jordan Eriksen



Amplitudes 2026 Gong Show
Yuanche Liu@USTC

CHESS

CHEbyshev pSeudo-Spectral transportation
for Feynman Integral Differential Equations



$$\partial_t J^{(r)} = D_m J^{(r)}$$

Differential to Linear

$$|J - J_0| \sim \rho^{-m}$$

Exponentially accurate

$$B(t) \sim \frac{R_c}{t - c} + M_c$$

Semi-Analytic Regularize



$\sim 10x$
faster wall time



100 stable digits
1 minute



734 integrals
Large family capable

Tests based on:

3l5p [Chicherin, Wu, Wu, Xu, Zhang, Zhang, 2025]

2l6p [Liu, Matijasic, Peraro, Xu, Yang, Zhang, 2026]

Yuanche Liu and Yang Zhang @ USTC

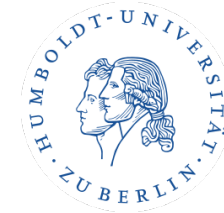
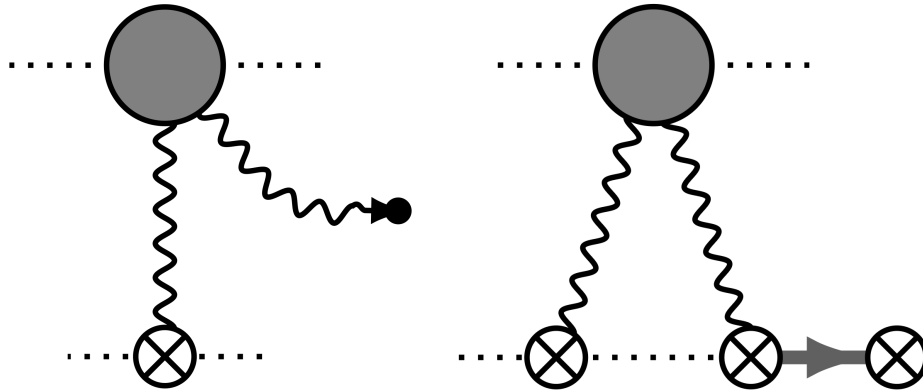
Carl Jordan Eriksen

Next: Yu Wu

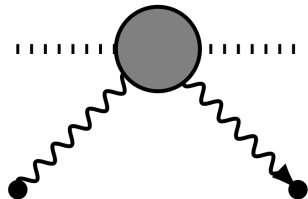
Black hole response theory

A worldline quantum field theory approach to the self-force expansion

Lara Bohnenblust, Carl Jordan Eriksen, Jitze Hoogeveen, Gustav Uhre Jakobsen, Jan Plefka



In a shockwave background



$$\sim \int d^{D-2} \mathbf{x}_\perp e^{-i \mathbf{q}_\perp \cdot \mathbf{x}_\perp} \left[e^{-i 2 G(P \cdot k_1) f(\mathbf{x}_\perp^2)} - 1 \right]$$

Symbols et Periods



<https://indico.global/e/kmpb2026>

KMPB Summer School

$\otimes \Sigma \otimes \dot{v} \otimes \mu \otimes \beta \otimes o \otimes \lambda \otimes$

A. Volovich | Introduction to Symbology

A. Matijašić | Elliptic MPLs and their Symbol

J. Broedel | Periods in Mathematical Physics

V. Fantini | Introduction to Resurgence

Yu Wu

Next: Tobias Scherdin

Giant Correlator at Two loops

$\mathcal{D}(x_i) \equiv \det(Y_i \cdot \phi(x_i))$ Giant Graviton

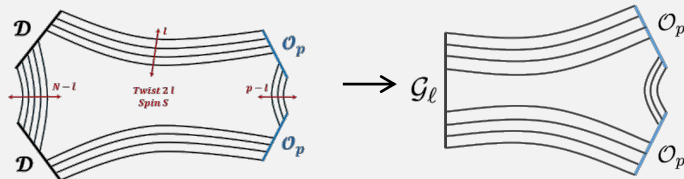
$$G_{\{p,q\}} = \langle \mathcal{D}(x_1, Y_1) \mathcal{D}(x_2, Y_2) \mathcal{O}_p(x_3, Y_3) \mathcal{O}_q(x_4, Y_4) \rangle$$

harmonic superspace

$$\langle \det(\tilde{q}_1^+) \det(q_2) \text{tr}[(\tilde{q}_3^+)^r (q_3^+)^{p-r}] \text{tr}[(\tilde{q}_4^+)^r (q_4^+)^{p-r}] \rangle$$

partial contraction

$$\sum_{\ell=0}^{N_c} (-1)^{\ell+1} \left(\frac{[12]^2}{8\pi^2 x_{12}^2} \right)^{N_c-\ell} \frac{(N_c-\ell)!}{\ell} \langle \text{tr}[(\tilde{q}_1 q_2)^\ell] \mathcal{O}_p \mathcal{O}_p \mathcal{L}_5 \mathcal{L}_6 \rangle$$



Planarity

Harmonic analyticity

One-loop: only one diagram

Two-loop: 26 diagrams

Manifestly SUSY

Harmonic PCGG Method

Weak-coupling integrands exhibit a defect version of 10D hidden conformal symmetry

generating function

$$\mathbf{I}^{(\ell)}(\lambda_1, \lambda_2) = \left(-\frac{x_{12}^6}{4\pi^2 x_{13}^2 x_{14}^2 x_{23}^2 x_{24}^2 x_{34}^2} \times H_{\{2,2\}}^{(\ell)} \Big|_{x_{ij}^2 \rightarrow \hat{x}_{ij}^2} \right) \Big|_{Y_3 \rightarrow \frac{\lambda_1}{\sqrt{2}} Y_3, Y_4 \rightarrow \frac{\lambda_2}{\sqrt{2}} Y_4}$$

replacement rules

$$\begin{aligned} x_{34}^2 &\rightarrow x_{34}^2 - 2y_{34}^2, \\ \frac{x_{13}^2 x_{23}^2}{x_{12}^2} &\rightarrow \frac{x_{13}^2 x_{23}^2}{x_{12}^2} + \frac{2y_{13}^2 y_{23}^2}{y_{12}^2}, \\ \frac{x_{14}^2 x_{24}^2}{x_{12}^2} &\rightarrow \frac{x_{14}^2 x_{24}^2}{x_{12}^2} + \frac{2y_{14}^2 y_{24}^2}{y_{12}^2}, \\ \frac{x_{13}^2 x_{24}^2 + x_{14}^2 x_{23}^2}{2x_{12}^2} &\rightarrow \frac{x_{13}^2 x_{24}^2 + x_{14}^2 x_{23}^2}{2x_{12}^2} + \frac{y_{13}^2 y_{24}^2 + y_{14}^2 y_{23}^2 - y_{12}^2 y_{34}^2}{y_{12}^2} \end{aligned}$$

4D distances are uplifted to 10D defect distances

Integrability check

OPE analysis $\mathcal{H}(u, v; \tau, \sigma) = \sum_{a=0}^{\infty} g^{2a} \sum_{L=1+n}^{2p-2} \sum_{b=0}^a \sum_{S=0}^a \mathcal{P}_{nm,L,S}^{(a,b)} f_{L,S}^{(b)}(z, \bar{z}, \mu) Y_{nm}(\sigma, \tau)$

Integrability prediction $\sum_{a=0}^{\infty} g^{2a} \sum_{b=0}^a \mu^b \mathcal{P}_{L,S}^{(a,b)} = \sum_{\mathbf{u}} d_{L,S}(\mathbf{u}) c_{L,S}(\mathbf{u}) e^{\delta \Delta_{L,S}(\mathbf{u}) \mu}$
Bethe roots

Perfect agreement with integrability predictions up to twist six

[Yunfeng Jiang, Chang Liu, Yu Wu, Yang Zhang, JHEP 03 (2026) 097, arxiv: 2509.23161]

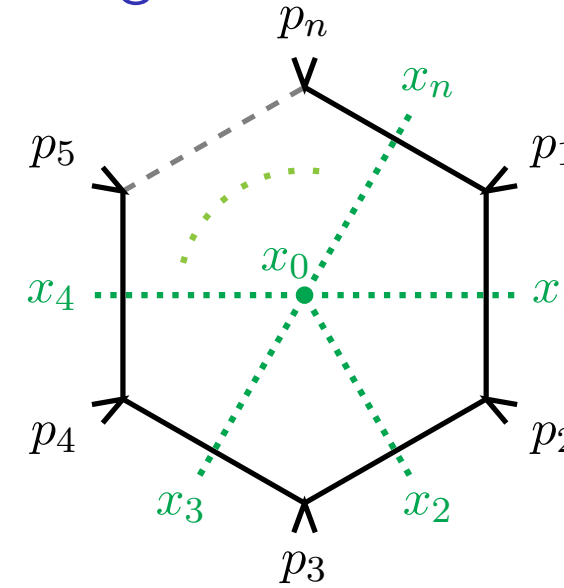
Tobias Scherdin

Next: Michael Reichenberg Ashby

Yangian Symmetry of Polygonic Feynman Integrals

In collaboration with Anne Spiering [260X.XXXXX]

- ▶ we use **Yangian symmetry** to **compute the symbol of star integrals**
- ▶ we find the **angles of these hyperbolic simplices** as solutions to the Yangian differential equations
- ▶ **general interests:** hidden symmetries of amplitudes & loop integrals, symbology, hexagon ansatz in $\mathcal{N} = 4$ SYM, intersection theory, WQFT



We organise the “KMPB School 2026: Symbols & Periods” in Berlin, August 8 – September 4!

Tobias Scherdin, Humboldt-Universität zu Berlin

**Symbols et
Periods**


<https://indico.global/e/kmpb2026>

KMPB Summer School

$\otimes \Sigma \otimes \dot{\nu} \otimes \mu \otimes \beta \otimes o \otimes \lambda \otimes$

A. Volovich | **Introduction to Symbology**
A. Matijašić | **Elliptic MPLs and their Symbol**
J. Broedel | **Periods in Mathematical Physics**
V. Fantini | **Introduction to Resurgence**

Michael Reichenberg Ashby

Next: Marcelo dos Santos

Non-local non-stabiliserness in gluon and graviton scattering:

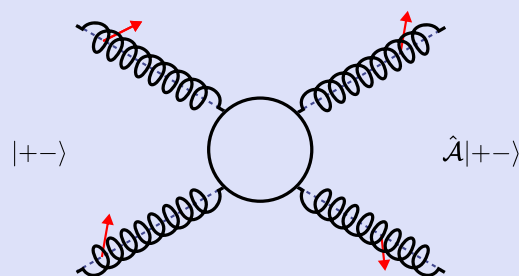
arXiv: 2603.04148

Michael Reichenberg Ashby
Queen Mary University of London, UK

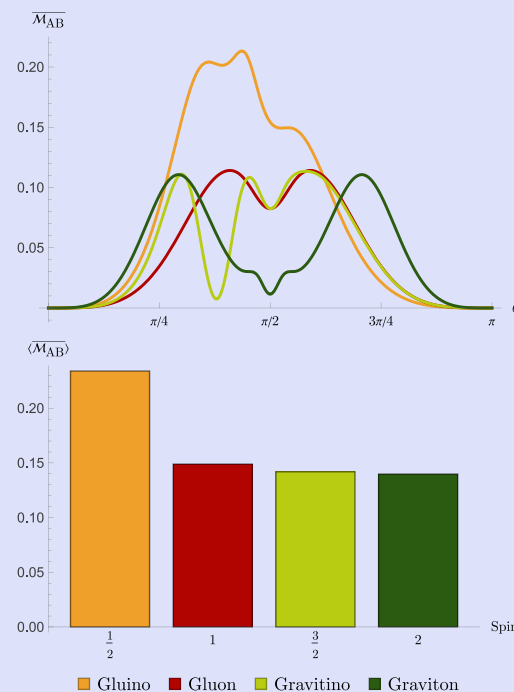
Magic from helicity scattering

$$M_2[|\psi\rangle] = -\log_2 \left(\frac{1}{2^N} \sum_{\hat{P} \in \mathcal{P}^{(N)}} |\langle \psi | \hat{P} | \psi \rangle|^4 \right)$$

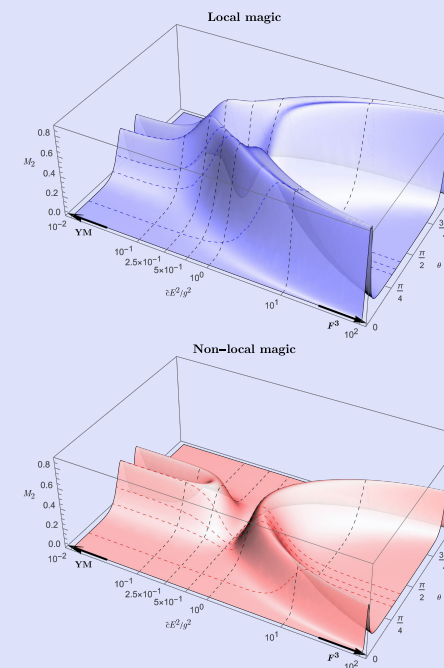
$$\mathcal{M}_{AB} = \min_{U_A \otimes U_B} M_2[(U_A \otimes U_B)|\psi\rangle]$$



Spin vs. Magic



YM + F^3



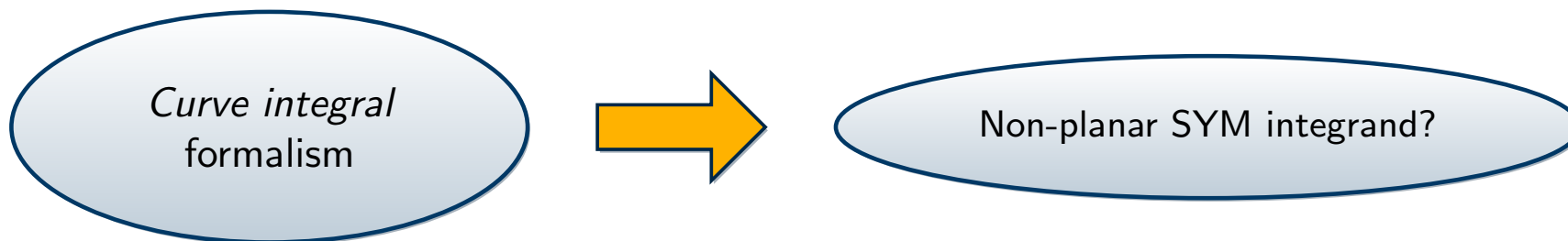
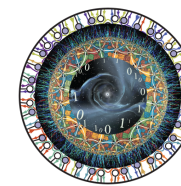
Marcelo dos Santos

Next: Matthew Rochford



Combinatorics of the Scaffolded Superstring

Marcelo dos Santos, UC Davis
Based on work with Jaroslav Trnka



bosonic gluons = SUSY gluons = + - + ...

Continuation of [1]: native understanding of factorization and F^3 cancellation. **Loops?**

[1] Q. Cao, J. Dong, S. He, C. Zhu, *Superstring amplitudes meet surfaceology*, 2025.

Matthew Rochford

Next: Aakash Kumar

Light-like Wilson loop correlators in $\mathcal{N} = 4$ SYM

Matthew Rochford

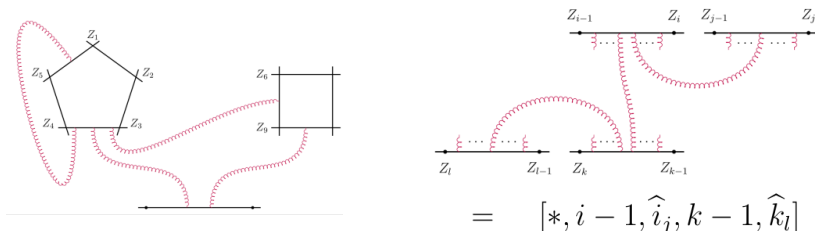
In collaboration with James Drummond, Ömer Gürdoğan and Rowan Wright, based on 2512.12655, 2601.23210, 2602.18423
School of Physics and Astronomy, University of Southampton

MOTIVATION

- Wilson loop definition: $\mathcal{L}(C) = \frac{1}{N} \text{tr} \mathcal{P} \exp i \oint_C dx^\mu A_\mu$
- Wilson loop correlator: $\mathcal{W}_{n_1, \dots, n_m} = \langle \mathcal{L}(C_1) \dots \mathcal{L}(C_m) \rangle$
- Scattering Amplitude/Wilson loop duality: $A(p_1, \dots, p_n) \Leftrightarrow \mathcal{W}_n$
- $\mathcal{W}_n$ satisfies the same properties as scattering amplitudes.
- *Do Wilson loop correlators satisfy analogous properties? Yes!*
- *Why are we interested?* From taking limits of the correlator, we may be able to reproduce Wilson loop-Lagrangian correlators, and they may tell us about the spectrum of operators.

COMPUTING CORRELATORS

Work in twistor space and compute Feynman diagrams of the form:



PROPERTIES OF $\mathcal{W}_{n_1, \dots, n_m}$

- Chiral box expansion and tree-level singularities

$$\mathcal{W}_{n_1, n_2}^{1\text{-loop}} = \sum \left(f_{a,b,c,d}^1 I_{a,b,c,d}^1 + f_{a,b,c,d}^2 I_{a,b,c,d}^2 \right) + \mathcal{W}_{n_1, n_2}^{\text{tree}} \sum I_a^{\text{div}}$$

where f 's are tree-level correlators and I 's are simple integrands/integrals.

- Recursion relation:

$$\begin{aligned} \langle \mathcal{L}[1, 2, 3, 4] \mathcal{L}[\tilde{1}, \dots, \tilde{n}_2] \rangle^c &= \langle \mathcal{L}[1, 2, 3] \mathcal{L}[\tilde{1}, \dots, \tilde{n}_2] \rangle^c \\ &+ \sum_{\tilde{j}} [3, 4, 1, \tilde{j} - 1, \tilde{j}] \langle \mathcal{L}[1, 2, 3, \hat{4}, I_{\tilde{j}}, \tilde{j}, \dots, \tilde{j} - 1, I_{\tilde{j}}] \rangle \end{aligned}$$

- $\bar{Q}$ equation

$$\begin{aligned} \bar{Q}_A' \mathcal{R}_{n_1, n_2}^{(k,1)} &= \int [d^2|3 \mathcal{Z}_{X_1}]_A^{A'} \left[\mathcal{R}_{n_1+1, n_2}^{(k+1,0)} - \mathcal{R}_{n_1, n_2}^{(k,0)} \mathcal{R}_{n_1+1}^{(1,0)} \right] + \text{cyc}_1 \\ &+ \int [d^2|3 \mathcal{Z}_{X_2}]_A^{A'} \left[\mathcal{R}_{n_1, n_2+1}^{(k+1,0)} - \mathcal{R}_{n_1, n_2}^{(k,0)} \mathcal{R}_{n_2+1}^{(1,0)} \right] + \text{cyc}_2 \end{aligned}$$

FUTURE WORK

- Find geometry for $\mathcal{W}_{n_1, n_2}$.
- Reproduce $\langle \mathcal{L}(C_1) \mathcal{O}(x) \rangle$ by taking limit of $\langle \mathcal{L}(C_1) \mathcal{L}(C_2) \rangle$.
- Compute $\mathcal{W}_{n_1, n_2}^{2\text{-loop}}$ using $\bar{Q}$ equation.

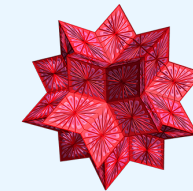
Aakash Kumar

Next: Felix Forner

SMaSH : Simplify Massive Spinor Helicity

Aakash Kumar¹, Arnab Rudra and Rahul Shaw
Indian Institute of Science Education and Research, Bhopal, India

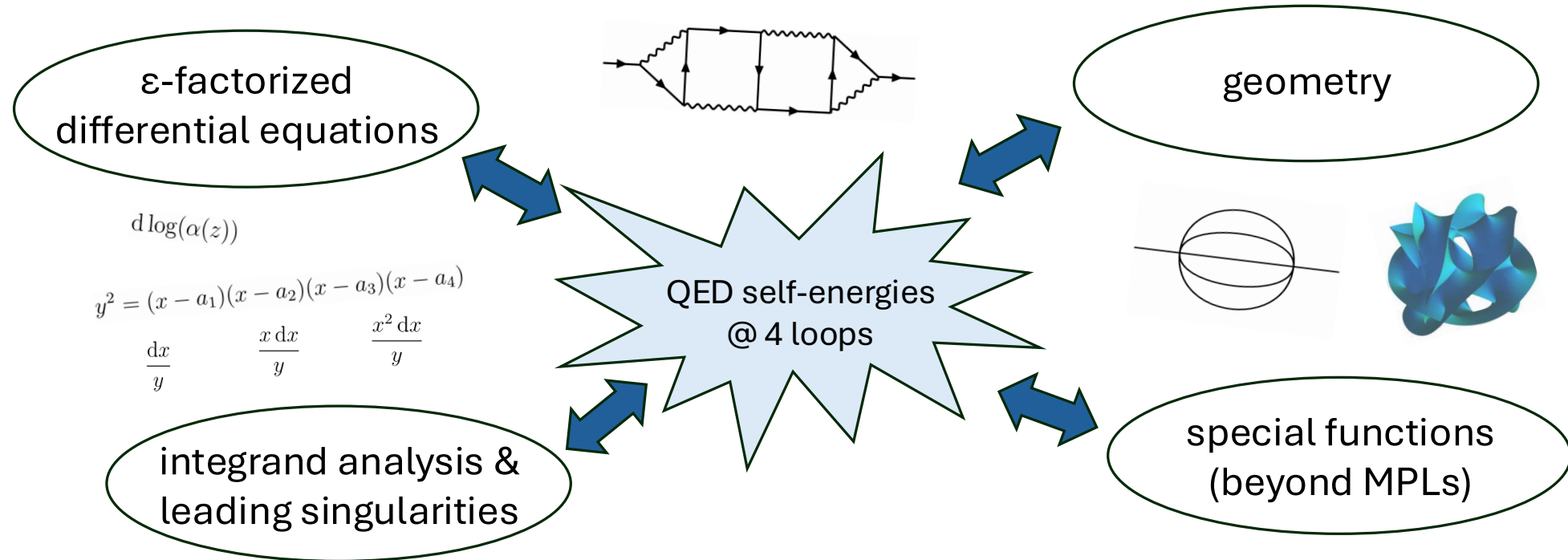
- Explicit massive little group indices
- Index contraction, spinor derivatives, massive & massless helicity scaling operators etc.
- Implementation of RAMBO algorithm to generate numerical kinematics
- High energy behavior and C, P, T transformations
- Computing any n-point higher spin scattering amplitude
- Finding contact terms and manifesting gauge invariance
- Simplification of Mandelstam variables



¹ github.com/aakash-kmr/SMaSH

Felix Forner

Next: Chanon Hasuwannakit



Chanon Hasuwannakit

Next: Kathrin Stoldt



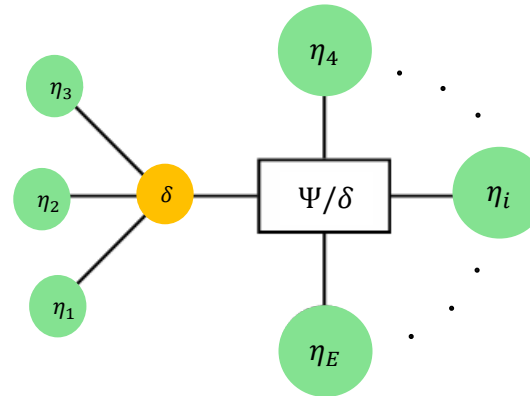
Berends-Giele current for Gravity

Gravity $\rightarrow$ Chiral Einstein-Cartan

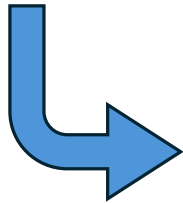
$$S[e, A] = \frac{1}{16\pi G} \int \Sigma^i \wedge (dA^i + \frac{1}{2} \epsilon^{ijk} A^j \wedge A^k)$$

Gravity solution

$J(-++ \dots +)$



$$\sum_{\eta \text{ perms}} \frac{1}{\square} \frac{(q|\eta_1|\Psi|q)}{(1+\Psi)^2} \cdot \prod_{j=1}^{E-2} \frac{(q|\eta_{j+1}|1+\Psi+\eta_1+\dots+\eta_j|\delta_j)}{(1+\Psi+\eta_1+\dots+\eta_j)^2(q\delta_j)} \cdot \frac{(q|\eta_E|\Psi+\eta_1+\dots+\eta_{E-1}|q)}{(1+\Psi+\eta_1+\dots+\eta_{E-1})^2}$$



$$A_{MHV}(01|\mathcal{K}) = (01)^6 \sum_{\Gamma_{\mathcal{K}}} \prod_{i \in \mathcal{K}} (0i)^{\alpha_i-2} (1i)^{\alpha_i-2} \prod_{\langle ij \rangle \in \Gamma_{\mathcal{K}}} \frac{[jk]}{(jk)}$$

Kathrin Stoldt

Next: Enrico Zunino



Radiated Angular Momentum from the Impact Parameter in WQFT

Kathrin Stoldt

Amplitudes 2026



Radiated angular momentum is interesting for gravitational wave modelling

It is non-vanishing only for dissipative effects

$$L^\mu = -\frac{1}{E} \epsilon^\mu_{\nu\alpha\beta} \overbrace{(b_2^\nu - b_1^\nu)}^{b^\nu} p_1^\alpha p_2^\beta$$

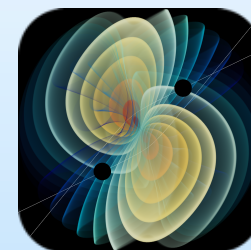
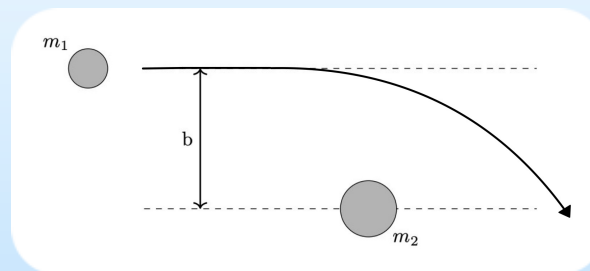
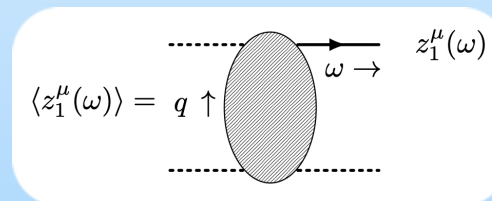


Image credit:
Mathias Driesse

Goal: Use Worldline Quantum Field Theory (WQFT) formalism to compute Δb_i^μ with a new method to obtain ΔL^μ

$$\Delta b_i^\mu = \lim_{\omega \rightarrow 0} \frac{d}{d\omega} \left(i\omega^2 \langle z_i^\mu(\omega) \rangle \right)$$



Systematic organisation of terms related to the wave memory with k -point correlators

Methods:

- Worldline and bulk vertices
- IBPs for three-loop integrals
- Differential equations

Results:

- ΔL^μ at $\mathcal{O}(\alpha^3)$ in Electrodynamics [Jakobsen, KS '26]
- Reproduced $\mathcal{O}(G^3)$ result in gravity

In progress (with Bohnenblust, Eriksen, Jakobsen, Yanovets):

- ΔL^μ at $\mathcal{O}(G^4)$ in gravity

Enrico Zunino

Next: Hector Puerta-Ramisa

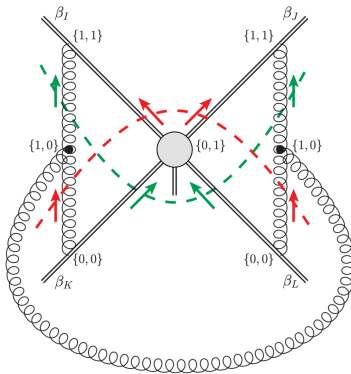
With L. Magnea, ...

Celestial Holography

$$\rho_{ijkq} = \frac{s_{ij}s_{kq}}{s_{ik}s_{jq}} = z\bar{z},$$
$$\rho_{iqjk} = \frac{s_{iq}s_{jk}}{s_{ik}s_{jq}} = (1-z)(1-\bar{z}),$$

Soft QCD

Soft Anomalous Dimension



Enrico Zunino, University of Edinburgh

With E. Gardi, A. McLeod,...

Amplitudes 2026, QMUL

Hector Puerta-Ramisa

Next: Rahul Balaji

Analytic Superspace Methods in (A)dS/(S)CFT

Superior tool for solving constraints from (super)conformal symmetry
→ (S)Conformal group acts linearly
→ Shortening conditions **automatic**

(S)CFT

- Weight shifting operators
[Hansen,Heslop,HPR '25]
- New **non-renormalisation** thms [Bissi,Fardelli,HPR (WIP)]

+ (Super) Conformal tensor products (OPEs) from **very simple combinatorics** [WIP]

Non-SUSY included!

- Unified formalism for any $SU(m, m|2n)$, $OSp(4m|2n)$
- Use **harmonic analyticity** to solve constraints, then turn off SUSY [Heslop,HPR'25 + WIP]

Rahul Balaji

Next: Dhruv Pathak

Towards Open String Integrals on Moduli Space

Rahul K Balaji

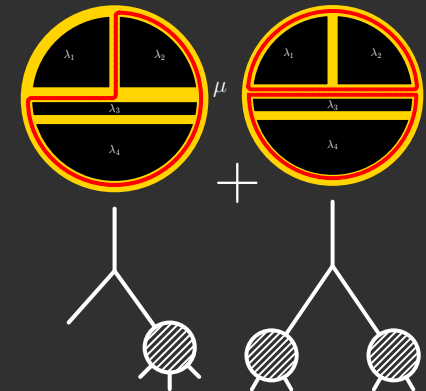
Princeton University, IAS

Amplitudes 2026

$$K_{0,n}(\lambda) = \sum_{\Gamma} \frac{1}{|\text{Aut } \Gamma|} \prod_{e=(ij) \in E(\Gamma)} \frac{2}{\lambda_i + \lambda_j}$$

$$K_{0,4}(\lambda_1, \lambda_2, \lambda_3, \lambda_4) = \begin{array}{c} \text{[diagram 1]} + \text{[diagram 2]} + \\ \text{[diagram 3]} + \text{[diagram 4]} + \\ \text{[diagram 5]} + \text{[diagram 6]} \end{array}$$

$$= \sum_{i=1}^4 \frac{1}{\lambda_i^3} \prod_{j \neq i} \frac{1}{\lambda_j}$$



$$K_{0,5}(\mu, \lambda_1, \dots, \lambda_4)$$

Next up: $A_{g,n}^{\alpha'} = \int_{\mathcal{M}_{g,n}} \Omega_{WP} \prod_C u_C^{\alpha' X_{ij}}$

Information about α' corrections contained in the leading order terms.



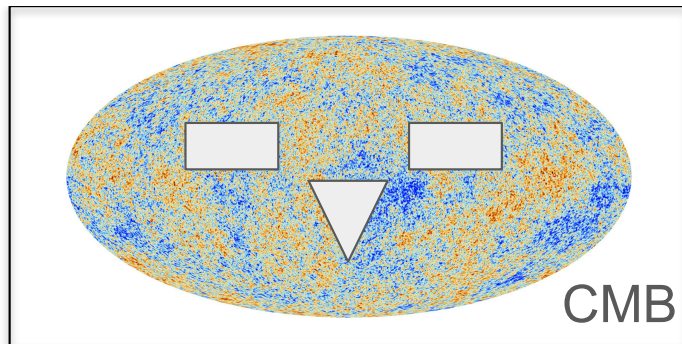
Dhruv Pathak

Next: Gabriel Menezes

Dhruv Pathak
Govardhan



Higher Point Feynman Diagrams



Precision Cosmology Observables

Problem

V vertices $\Rightarrow V$
integrals

One Integral?

$$\text{Diagram with two vertices (grey and blue) connected by a line } k = \frac{1}{2\pi i} \int \frac{d\omega}{\omega^2 - k^2} \left(\text{Diagram with grey vertex and line } \omega \right) \times \left(\text{Diagram with blue vertex and line } -\omega \right) + B_O$$

E.g. Conformal Scalar ϕ^3
Scale factor $a(\tau) = \tau^{j-1}$

$$\text{Diagram with three external lines } k_1, k_2, k_3 \text{ meeting at vertex } j = \frac{-i \Gamma(j)}{(i k_{123})^j} \Rightarrow \text{Diagram with four external lines } k_1, k_2, k_3, k_4 \text{ meeting at vertices } j_0, j_1 = \frac{\Gamma(j_0 + j_1)}{j_0(k_3 + k_4 - k)^{j_0 + j_1}} {}_2F_1 \left(j_0, j_0 + j_1; 1 + j_0; \frac{-(k_1 + k_2) - k}{(k_3 + k_4) - k} \right) + B_O$$

Selects observable
 $\Psi, G_F, \langle \varphi^n \rangle$

Gabriel Menezes

Next: Maegan Anderson



AMPLITUDES 2026

Higher-Spin Soft Charges as Kerr Multipole Dressing

Gabriel Menezes | Based on 2607.XXXXX



Department of Mathematical Physics
USP's Institute of Physics



One-minute message

Kerr scattering selects an exponentiated soft tower

- **VV recovered:** $s = 0$ gives the Veneziano-Vilkovisky supertranslation.
- **Subleading:** only the electric $\text{Diff}(S^2)$ component is fixed, naturally in generalized BMS.
- **Ward/dressing:** charges reproduce the exponentiated Kerr soft kernel and generate the linearized Kerr field.
- **Meaning:** the algebra composes canonical/intrinsic Kerr frame shifts.

Key equations

KERR SOFT MULTIPOLE DRESSING

$$S_{\text{Kerr}}^{\text{cl}}(k) = S_{\eta}^{(0)} e^{-i\omega W_{\eta}(q)}, \quad M_{\ell} + iS_{\ell} = M(ia)^{\ell}$$

CHARGE ALGEBRA

$$\{Q_s^{\text{tot}}(t), Q_{s'}^{\text{tot}}(t')\} = Q_{s+s'-1}^{\text{tot}}([t, t']_{\star}) + \mathcal{K}_{s,s'}[t, t'; C]$$

LOCAL CHIRAL REDUCTION

$$\{F_{m,s}, F_{n,s'}\} = ((s' - 1)m - (s - 1)n)F_{m+n,s+s'-2} \quad \text{local check}$$

Takeaway: the $w_{\{1+\infty\}}$ -like structure is the composition law for Kerr soft frame shifts.

Maegan Anderson

Next: Zhihao Zhang



Conformally flat limit of Quadratic Gravity

Maegan Anderson

University of Edinburgh

with Sam Bateman, Franz Herzog and Neil Turok

Web of related theories

$$\mathcal{S}_{\text{QG}} = - \int d^4x \sqrt{-g} \left(\frac{1}{2\gamma} C^2 + \frac{1}{\xi} R^2 \right)$$

$\gamma \rightarrow 0$

$$\mathcal{S}_{\text{PS}} = -\frac{1}{2} \int d^4x \left(\square\varphi + \lambda(\partial\varphi)^2 \right)^2$$

$$\mathcal{S}_{\Omega\Upsilon} = - \int d^4x \left(\partial\Omega\partial\Upsilon - \frac{\lambda^2}{2}(\Omega\Upsilon)^2 \right)$$

$$\mathcal{S}_{\text{CSQ}} = - \int d^4x \left(\partial\phi\partial\phi^* + g(\phi^*\phi)^2 \right)$$

Beta-functions

All agree given the following relationships between couplings:

$$\xi = 72\lambda^2$$

$$g = -\frac{\lambda^2}{2}$$

(1-loop) $\longrightarrow$ (3-loop) $\longrightarrow$ (6-loop)

Perfect square theory (CFQG)

- Renormalisable, asymptotically free theory of Gravity (albeit without gravitons)
- To all loops is Euclidean IR finite

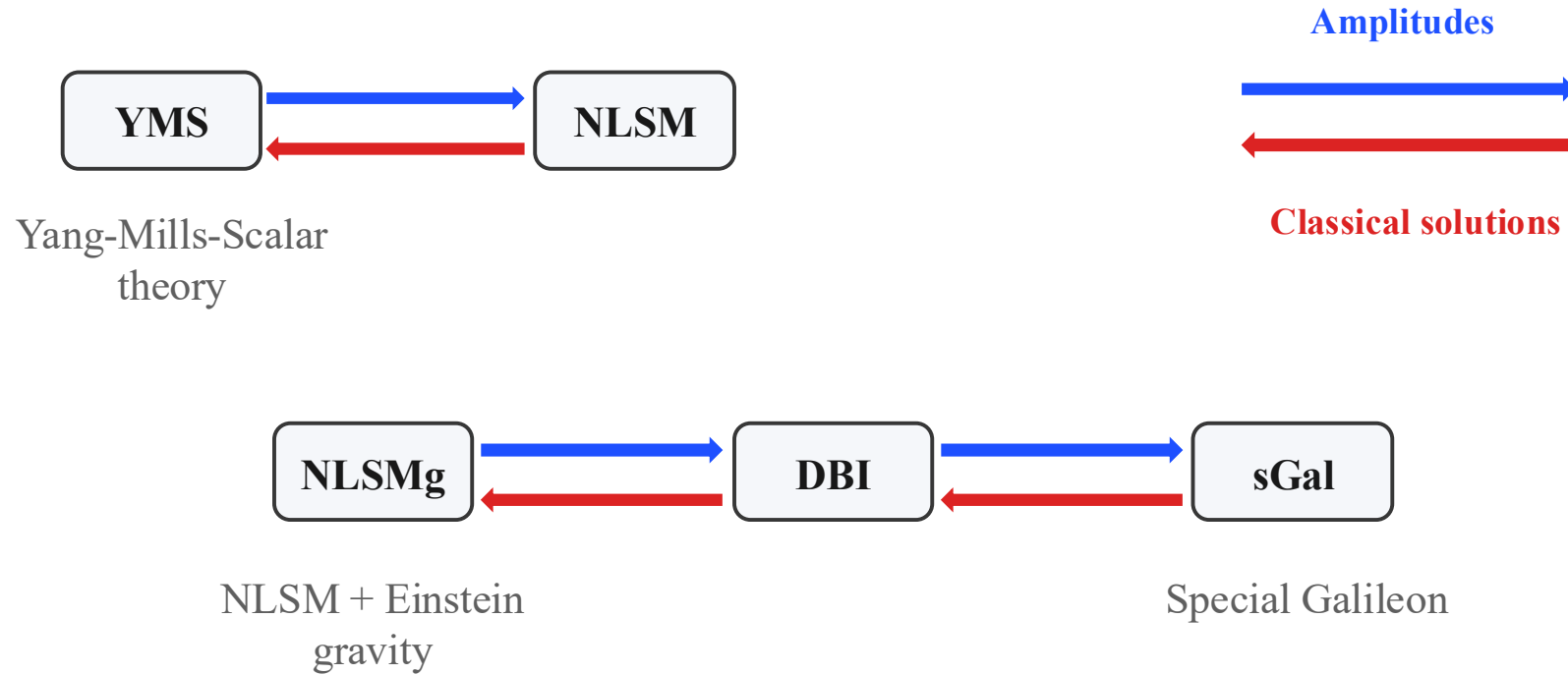
Zhihao Zhang

Next: Sebastien Timothy MacDonald

Geometric duality between effective field theories

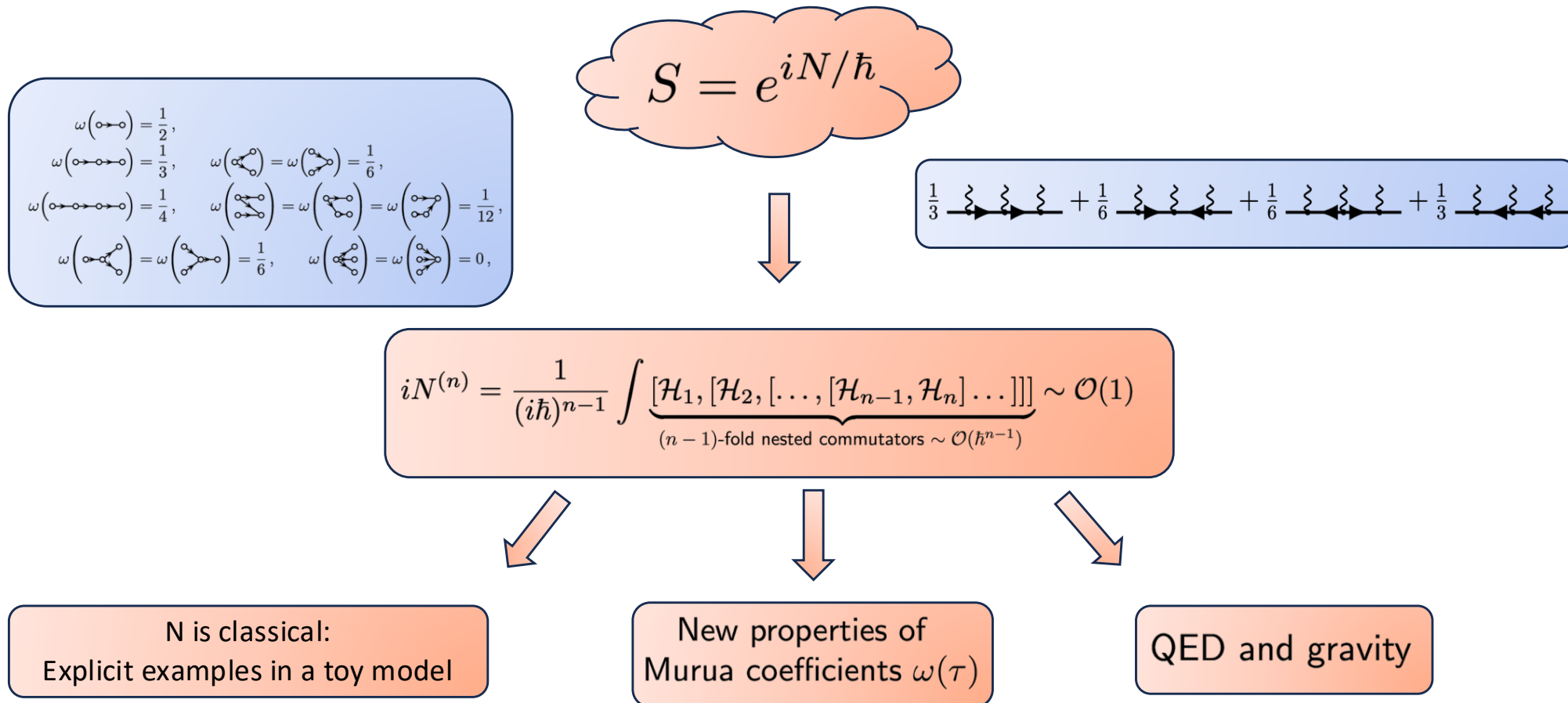
Speaker: Zhihao Zhang

Working with: Tomas Brauner, Diederik Roest, Tianzhi Wang, Yang Li



Sebastien Timothy MacDonald

Next: Francesco Campanella

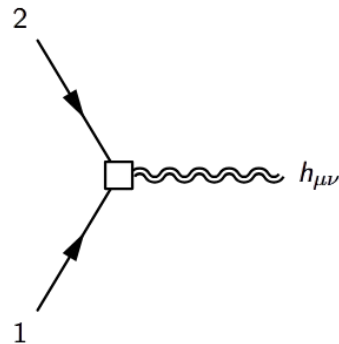


Francesco Campanella

Next: Sebastiano Bocchia

Gravitational Multipoles in Higher Dimensions from Scattering Amplitudes

Francesco Campanella
La Sapienza, University of Rome



References:

- 2605.05067 FC, Riccioni
- 2412.01771 Bianchi, Gambino, Riccioni
- 1812.08752 Chung, Huang, Kim, Lee
- 2403.16574 Gambino, Pani, Riccioni
- 1709.06016 Vines
- 2605.29831 Cangemi, Surubaru

- Three-point function involving a massive spinning field and gravity in arbitrary dimensions to study **stress-energy tensor structure in momentum space**;
- In four dimensions, there are two types of gravitational multipole moments: **Mass** and **Current** moments;
- In four dimensions, the minimal coupling reproduces the Kerr multipolar structure;
- In higher dimensions, additional multipole moments appear: the **Stress** moments;
- In dimensions higher than four, Spin universality is **lost** and the **minimal coupling does not reproduce** Myers-Perry multipolar structure, which is

$$T^{\mu\nu}(q)|_{\text{MP}} = m\Omega(d)\zeta^{-\frac{d-2}{2}} \left[u^\mu u^\nu \left(J_{\frac{d-2}{2}} \left(\frac{d-1}{2} \zeta \right) - \frac{\zeta}{2} J_{\frac{d}{2}} \left(\frac{d-1}{2} \zeta \right) \right) \right. \\ \left. - \frac{1}{2\zeta} (S \cdot q)^\mu (S \cdot q)^\nu J_{\frac{d}{2}} \left(\frac{d-1}{2} \zeta \right) \right. \\ \left. - \frac{i}{2} \left(u^\mu (S \cdot q)^\nu + u^\nu (S \cdot q)^\mu \right) J_{\frac{d-2}{2}} \left(\frac{d-1}{2} \zeta \right) \right]$$

with

$$\zeta \equiv \sqrt{q \cdot S \cdot S \cdot q} = \sqrt{q^\mu S_\mu{}^\nu S_\nu{}^\sigma q_\sigma}$$

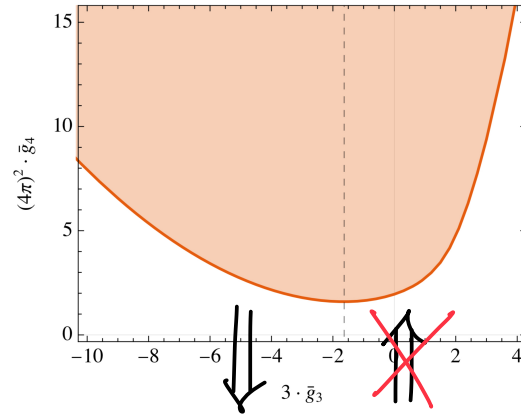


Sebastiano Bocchia

Next: Melvyn Nabavi

Bootstrapping the Spectra of Neutral Goldstones in 4d

General Problem

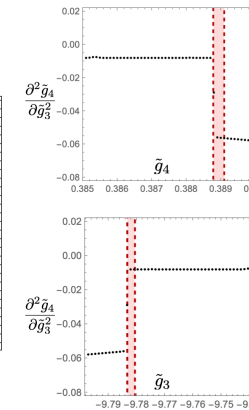
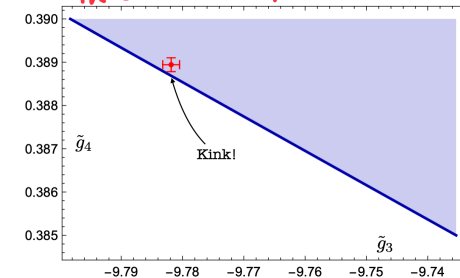


$\tilde{g}_2$ - cutoff

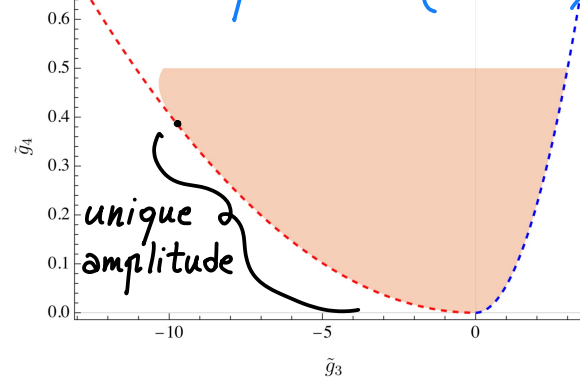
$$M(s, t, u) = \tilde{g}_2 (s^2 + t^2 + u^2) + \tilde{g}_3 (stu) + \tilde{g}_4 (s^2 + t^2 + u^2)^2 + \dots$$

$$- \frac{\tilde{g}_2^2}{480\pi^2} (s^2(4s^2 + t^2 + u^2) \log(-s\sqrt{\tilde{g}_2}) + (s \rightarrow t) + (s \rightarrow u)) + \dots$$

Verified the presence of a kink in the EFT problem

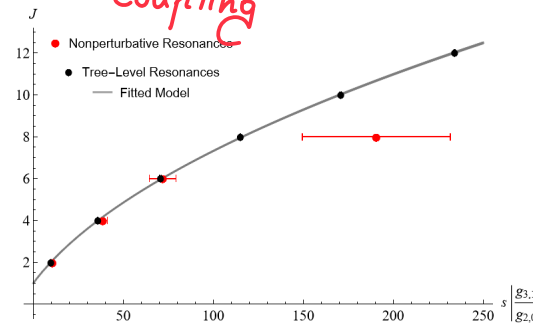


EFT problem (weakly coupled)



M - cutoff

Only one trajectory survives at weak coupling



SEBASTIANO BOCCHIA

based on the work with A. Guerrieri, K. Häring and D. Karateev



Melvyn Nabavi

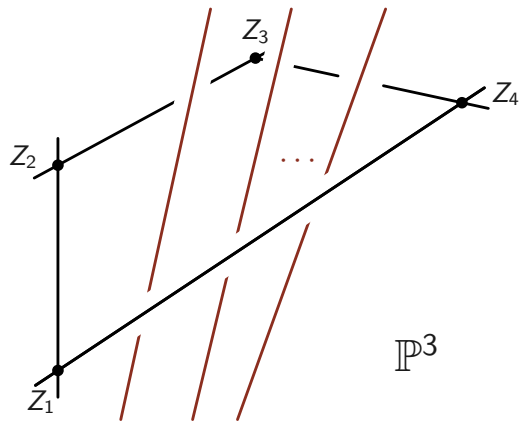
Next: Daniel Longenecker

The deformed Amplituhedron at higher loops

Melvyn Nabavi

Johannes Henn, Rourou Ma and Jaroslav Trnka

$\mathcal{N} = 4$ sYM integrand



"canonical form" in $G(2, 4)^L$

deforming Z'_i s
 $\longrightarrow$
 to "fat lines"

Conjecture:

deformed Amplituhedron:

$\mathcal{N} = 4$ sYM on the Coulomb branch.

IR finite

► 1,2,3 loops ✓ :

$$d\Omega_3 = \sum_i \alpha_i \left[\text{diagram 1} \right] + \sum_i \beta_i \left[\text{diagram 2} \right]$$

► Generalizing to all-loops?



UC DAVIS
 UNIVERSITY OF CALIFORNIA

Daniel Longenecker

Next: Leonardo Sartori

Uncolored Scalar Kinematics

Daniel Longenecker

The X_{ij} variables trivialize momentum conservation for theories with color.

What about uncolored, permutation-invariant theories? For example, ϕ^3 .

Here is a prescription:

Momentum conservation ($\sum_i s_{ij} = 0$) is linear in the space of mandelstams, so we can do an orthogonal projection to kinematic space.

For example, at 4pts, $s \rightarrow s - \frac{1}{3}(s+t+u) = \frac{2}{3}s - \frac{1}{3}t - \frac{1}{3}u$.

Using this prescription, we can modify the Koba-Nielsen factor and discover new, permutation covariant coordinates on $M_{0,n}$ (the integration domain for string tree amps).

Leonardo Sartori

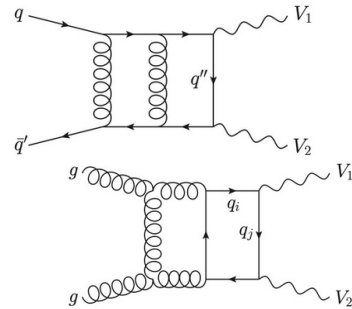
Next: Marko Beocanin

Preliminary: Two-loop Massive Top Corrections to Di-Boson Production



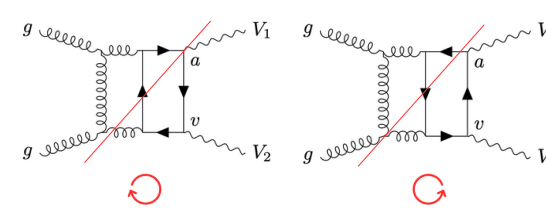
Leonardo Sartori based on current work with **A. Ghira, L. Tancredi** and **G. Zanderighi**

only massless
quarks in loops:



$$\begin{aligned}\tilde{T}_1^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)p_1^\mu p_1^\nu, \\ \tilde{T}_2^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)p_1^\mu p_2^\nu, \\ \tilde{T}_3^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)p_2^\mu p_1^\nu, \\ \tilde{T}_4^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)p_2^\mu p_2^\nu, \\ \tilde{T}_5^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_A u(p_1)p_1^\mu p_1^\nu, \\ \tilde{T}_6^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_A u(p_1)p_2^\mu p_1^\nu, \\ \tilde{T}_7^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_A u(p_1)p_1^\mu p_2^\nu, \\ \tilde{T}_8^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_A u(p_1)p_2^\mu p_2^\nu, \\ \tilde{T}_9^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)v_A^\mu v_A^\nu,\end{aligned}$$

[Gehrmann, von Manteuffel, Tancredi, 2015]
[Caola, Henn, Melnikov, Smirnov, Smirnov, 2015]



! No non-trivial axial-vector
contributions

! Double-axial
= Double-vector

Only Multi-polylog appear

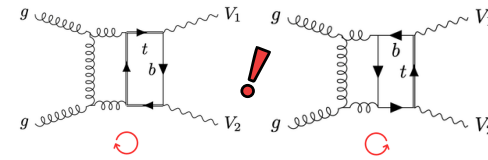
$$G(w_1, w_2, \dots, w_n; z) \equiv \int_0^z dt \frac{1}{t - w_1} G(w_2, \dots, w_n; t),$$

accounting for
massive top quark:

$$\begin{aligned}\tilde{T}_1^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)p_1^\mu p_1^\nu, \\ \tilde{T}_2^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)p_1^\mu p_2^\nu, \\ \tilde{T}_3^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)p_2^\mu p_1^\nu, \\ \tilde{T}_4^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)p_2^\mu p_2^\nu, \\ \tilde{T}_5^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_A u(p_1)p_1^\mu p_1^\nu, \\ \tilde{T}_6^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_A u(p_1)p_2^\mu p_1^\nu, \\ \tilde{T}_7^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_A u(p_1)p_1^\mu p_2^\nu, \\ \tilde{T}_8^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_A u(p_1)p_2^\mu p_2^\nu, \\ \tilde{T}_9^{E,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)v_A^\mu v_A^\nu, \\ \tilde{T}_1^{O,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)p_1^\mu v_A^\nu, \\ \tilde{T}_2^{O,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)p_2^\mu v_A^\nu, \\ \tilde{T}_3^{O,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)p_1^\nu v_A^\mu, \\ \tilde{T}_4^{O,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)p_2^\nu v_A^\mu, \\ \tilde{T}_5^{O,\mu\nu} &= \bar{u}(p_2)\not{p}_A u(p_1)p_1^\mu v_A^\nu, \\ \tilde{T}_6^{O,\mu\nu} &= \bar{u}(p_2)\not{p}_A u(p_1)p_2^\mu v_A^\nu, \\ \tilde{T}_7^{O,\mu\nu} &= \bar{u}(p_2)\not{p}_A u(p_1)p_1^\nu v_A^\mu, \\ \tilde{T}_8^{O,\mu\nu} &= \bar{u}(p_2)\not{p}_A u(p_1)p_2^\nu v_A^\mu, \\ \tilde{T}_9^{O,\mu\nu} &= \bar{u}(p_2)\not{p}_3u(p_1)v_A^\mu v_A^\nu,\end{aligned}$$

[Melnikov, Dowling, 2015]
[Brønnum-Hansen, Wang, 2020]
[Agarwal, Jones, von Manteuffel, 2020]
(Numerical results)

Axial-vector contributions
don't cancel anymore



! Double-axial and double-vector
contributions even
have different scalings

! Need schemes to handle γ_5 in
dimensional regularisation

$$\begin{aligned}v^2 &\sim m_t^{-4} \\ a^2 &\sim m_t^{-2}\end{aligned}$$

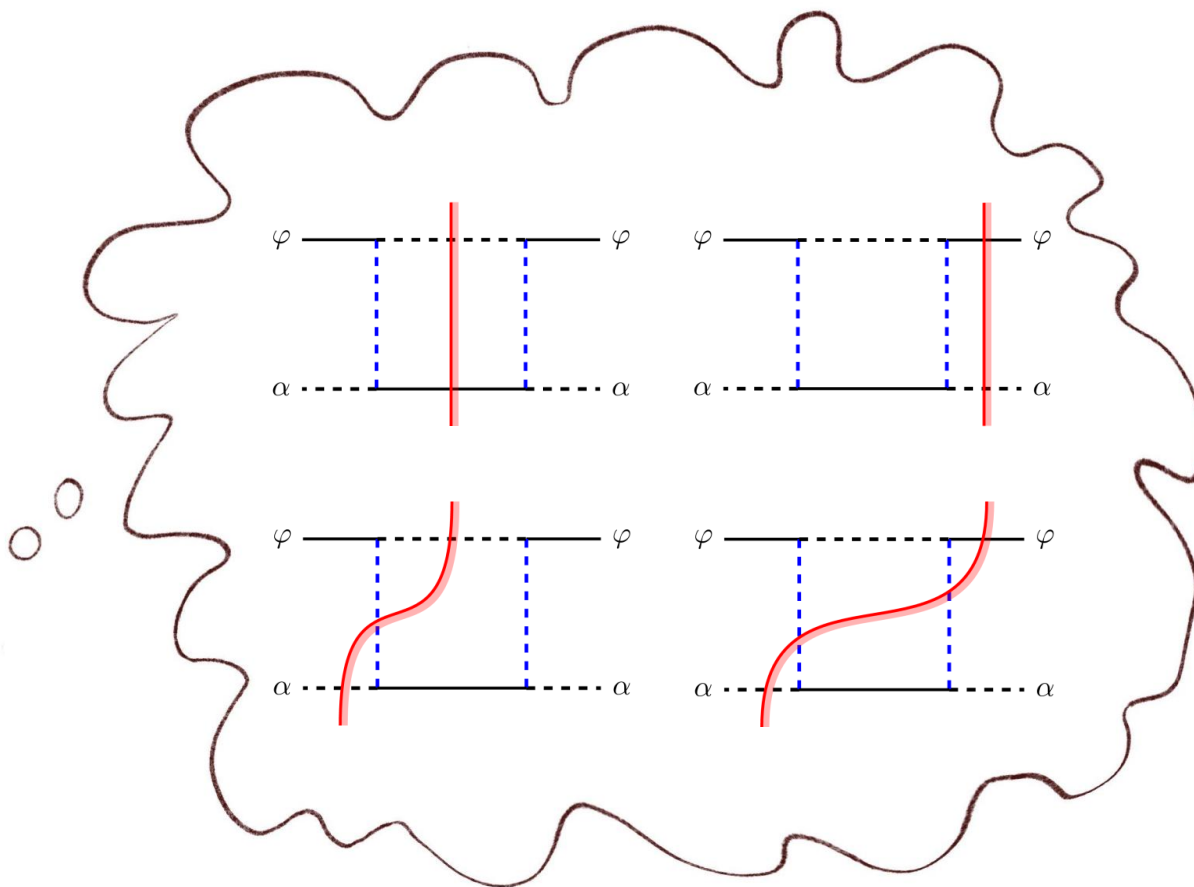
! Elliptic integrals start
appearing, new techniques
needed

$$I_n^C(a, \epsilon) = \frac{1}{2\sqrt{\pi}} \int_C dx \frac{x^n}{\sqrt{x(1-x)(1-ax)}} (x(1-x)(1-ax))^\epsilon$$

[Forner, Mella, Nega, Tancredi, Wagner, 2026]

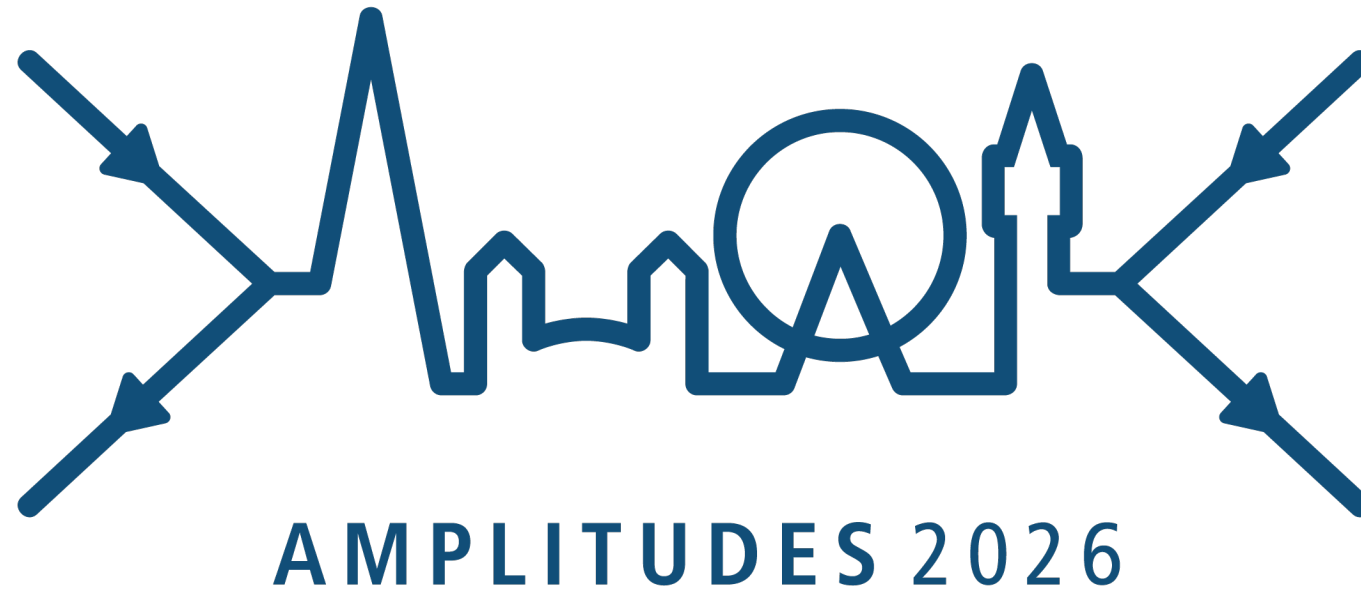
Marko Beocanin

Next: the end



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Thank you for all your
wonderful contributions!