

# Improving Final-State Interaction Modelling with INCL in the NEUT Event Generator

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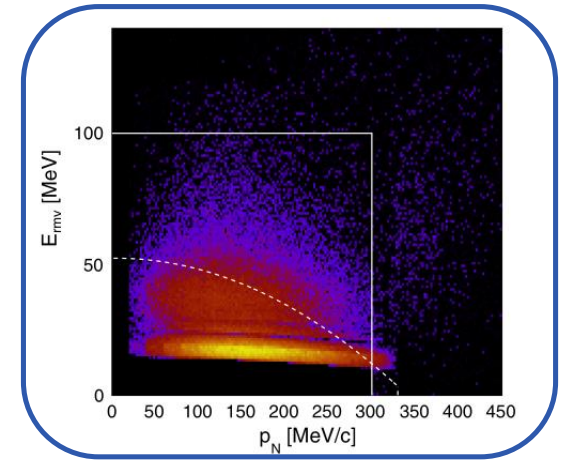
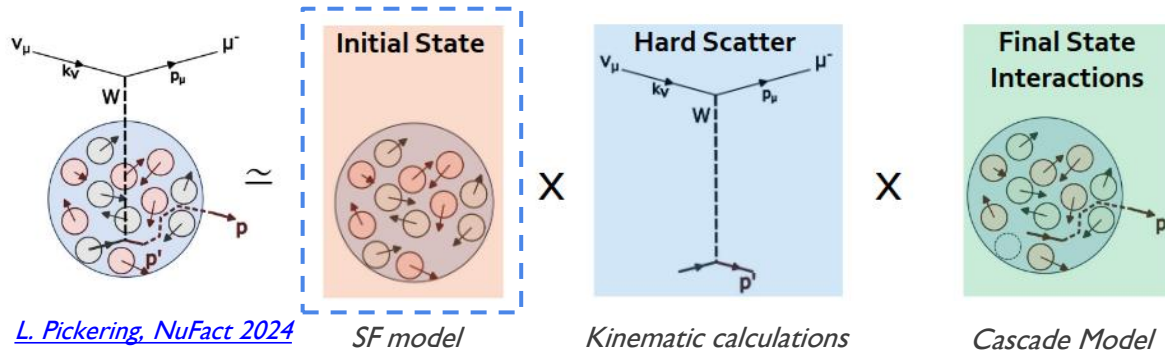


**University of  
Sheffield**

# The NEUT Event Generator

Neutrino-Nucleus interaction simulator, maintained “in-house” by T2K/SK with experimental needs in mind  
 Simulates processes for 100 MeV - few-TeV neutrinos for a range of nuclear targets (H, ..., C, O, ... ,Pb)

In NEUT, neutrino interactions with nuclei are reduced into:



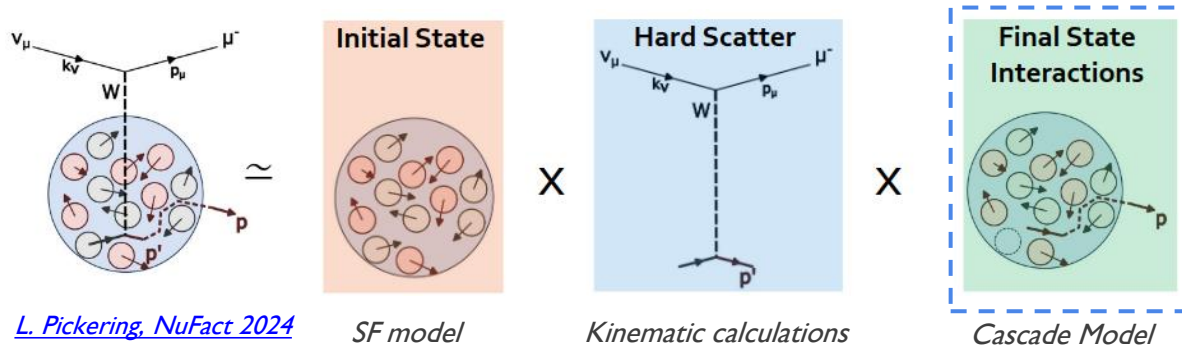
**Spectral function:** Probability of finding a nucleon with an energy  $E_M$  and momentum  $p_M$

Broken into two contributions (both seen here):  
 $P_{MF} + P_{SRC}$

# The NEUT Event Generator

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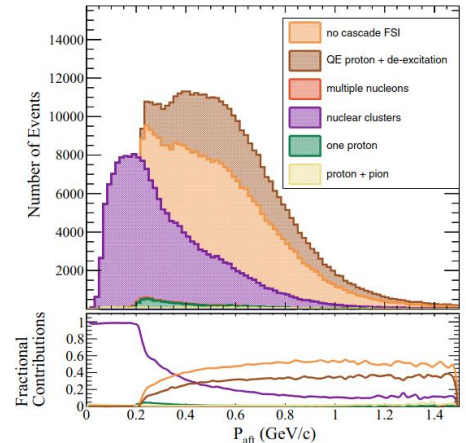


[L. Pickering, NuFact 2024](#)

**FSI:** Re-interactions of the hadron produced at the hard scatter with nucleons in the nucleus

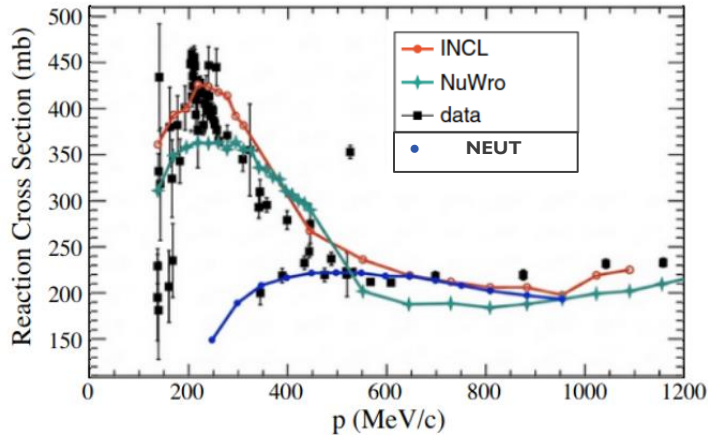
NEUT uses the **Bertini cascade** model, a semi-classical “billiard ball” approach

Other FSI models exist, with previous work integrating the INCL++ cascade into NuWro showing promising results



# INCL++ for Neutrino Generators

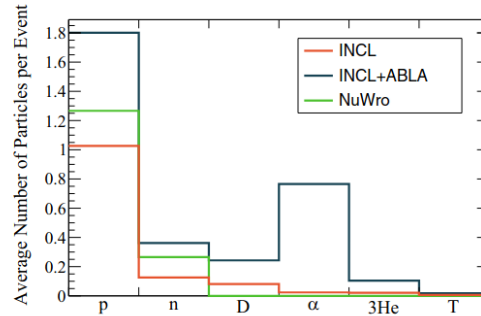
## Improved p-C low momentum proton cross section prediction



Plot from *PHYSICAL REVIEW D* 106, 032009 (2022), with NEUT prediction overlaid

**p-C reaction cross section predictions used to benchmark cascade modelling**

## Introduction of Light Nuclei Production (clustering)

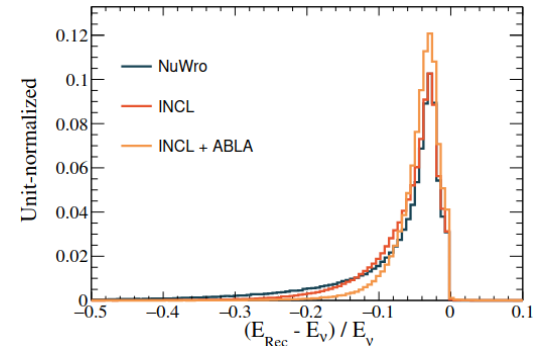


Plot from *PHYSICAL REVIEW D* 108, 112008 (2023)

**INCL + ABLA predicts T2K events on carbon cause fragmentation and produce clusters fairly often**

$$E_{rec} = E_{\mu} + \sum_i T_i$$

**If detectable, introducing clusters in models improves neutrino energy reco**



*A. Ershova, e4nu 2025*

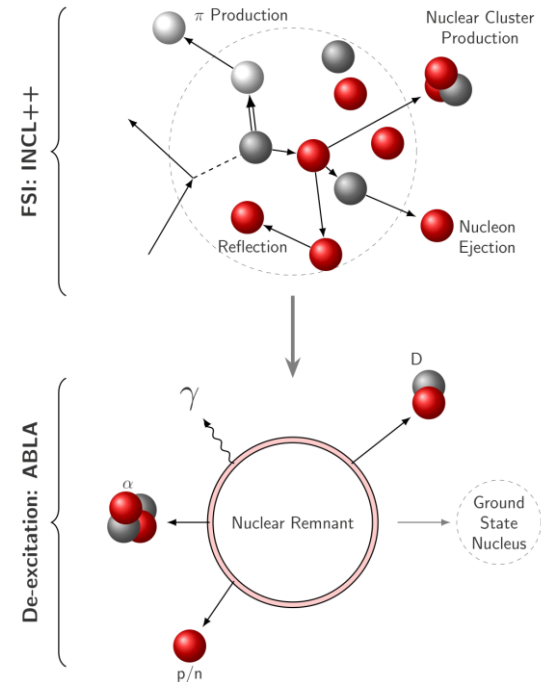
# Intranuclear Cascade Liege ++ (INCL)

**Liege Intranuclear Cascade (INCL):** simulates struck nucleon re-interactions within a target nucleus, designed for hadron/light nucleus-induced reactions on nuclei from a few MeV to 10-20 GeV (ref)

- Evolves entire nucleus through time
- **Nucleons:** reflect off the potential, interact with other nucleons, decay
- **Final states:** hadrons, nuclear clusters (D, T,  $^3\text{He}$ , alpha), and excited nuclear remnants with an excitation energy:

$$E^* = \sqrt{(E_\nu + M_A - E_{\text{lep}} - \sum_N E_{\text{had}})^2 - |\mathbf{p}_\nu - \mathbf{p}_{\text{lep}} - \sum_N \mathbf{p}_{\text{had}}|^2} - M_{A-N}$$

Coupled to a **de-excitation** routine (ABLA), modelling nuclear remnant relaxation after FSI



# The Spectral Function and de-excitation

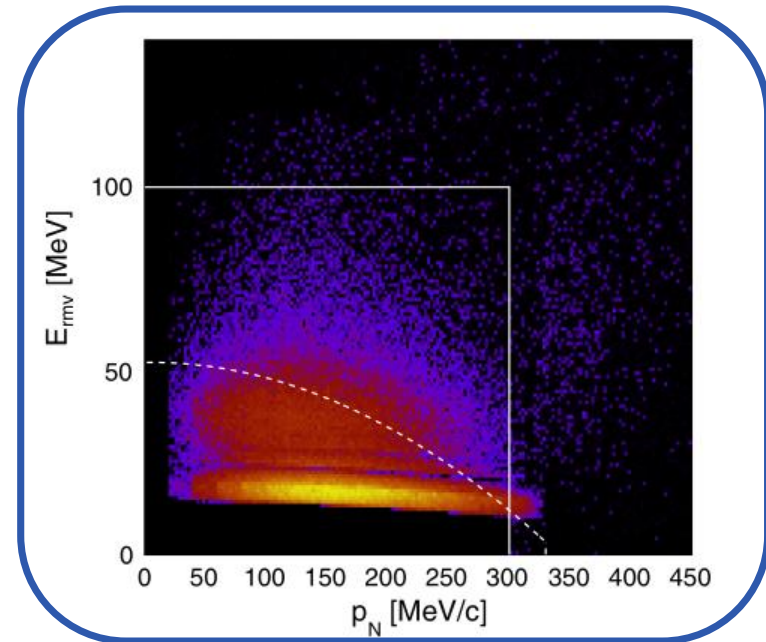
Previous work only looked into Mean Field (MF)  
contribution: simple 1 proton outputs (1p1h)

Spectral function  $E_{miss}$  values directly affect mean field  
excitation energy for 1p1h:

$$E^* = E_{miss} - (M_A - M_{A-1} - M_N) = E_{miss} - 18.4 \text{ MeV}$$

Only considering MF 1p1h

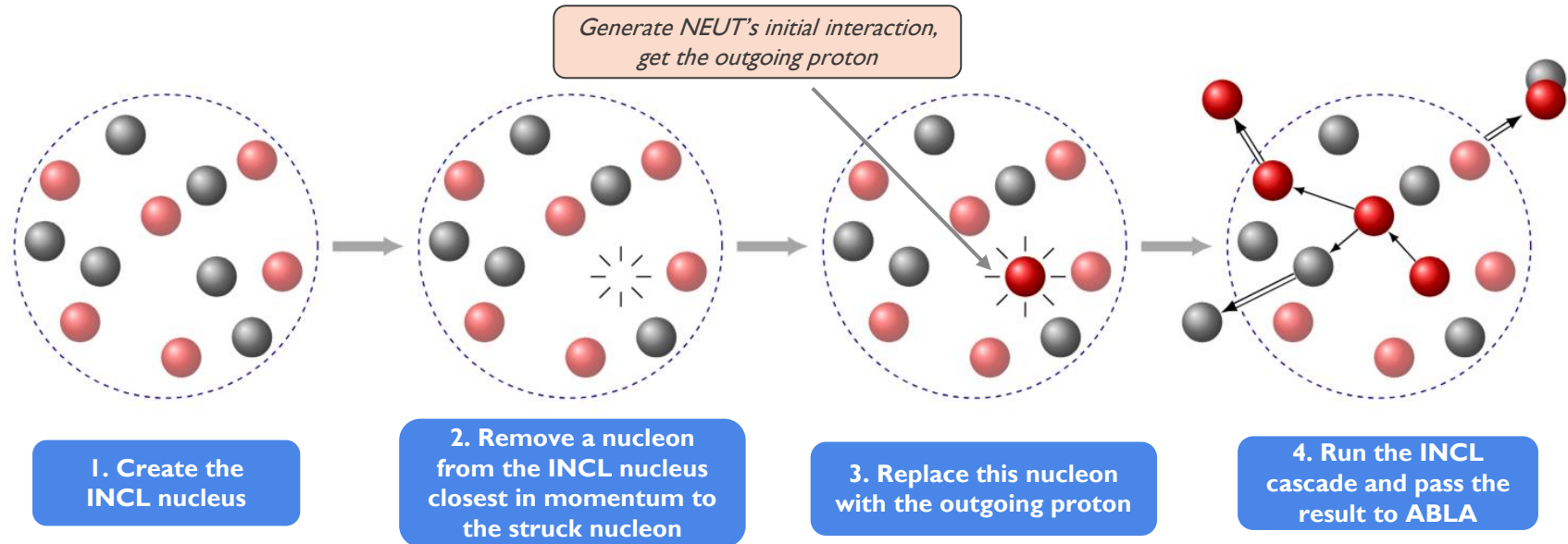
$$P_{sf} = P_{MF} + P_{SRC}$$



Benhar spectral function model, from PHYSICAL  
REVIEW D 109, 072006 (2024)

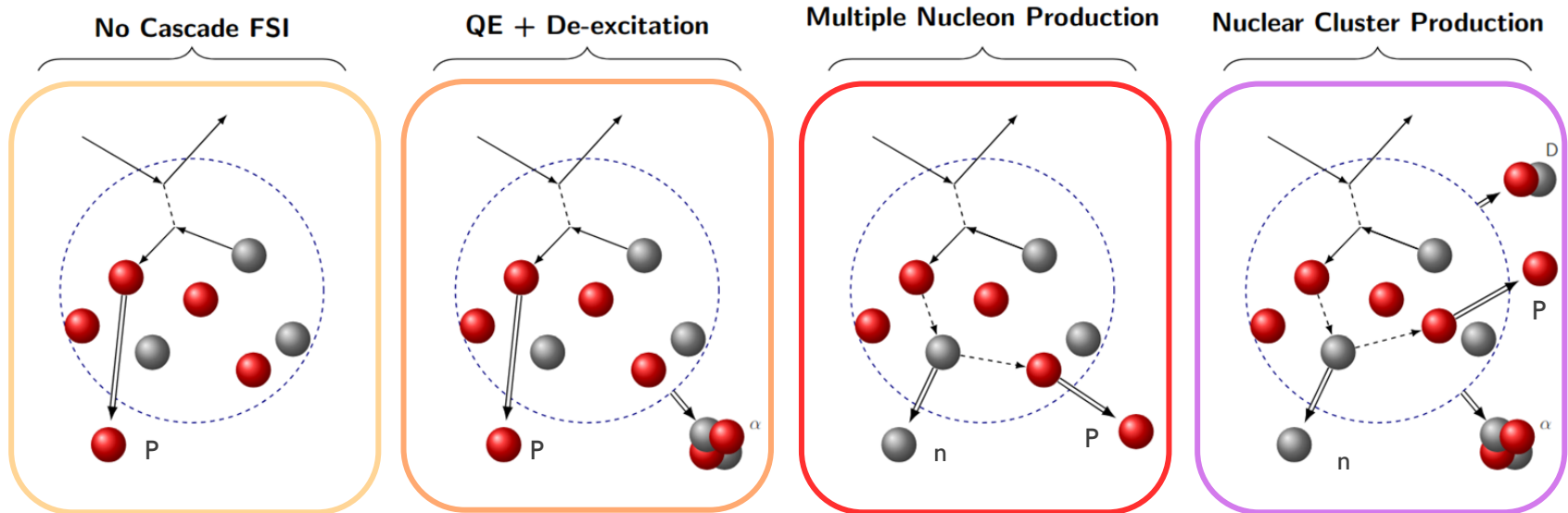
# Using INCL for neutrino FSI (IpIh)

INCL is designed for nucleon-nucleus reactions, and is not designed for neutrino projectiles (yet!) so we must adapt both our generator and INCL to accommodate this:



# INCL++ Interaction Channel Table

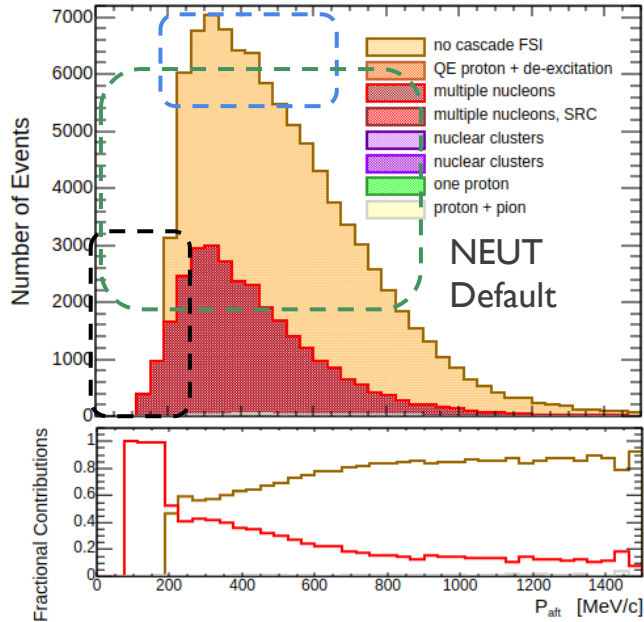
Due to the introduction of clusters and native de-excitation, study the FSI output channels based off numbers and types of ejected channels



*Channels with dominant contributions. Also see pion production and single inelastically scattered protons*

# NEUT comparisons: CCQE |p|h - I

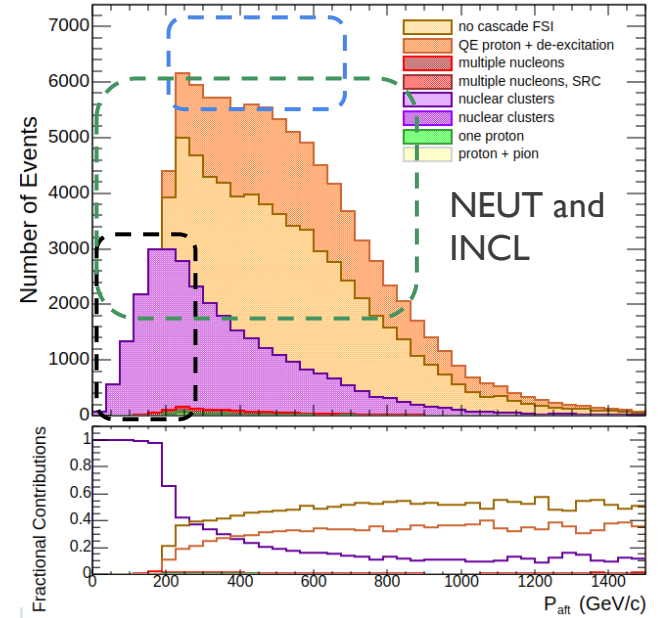
## Leading proton distributions post FSI, broken down by channel



*Lower peak when using INCL due to events with no final state protons*

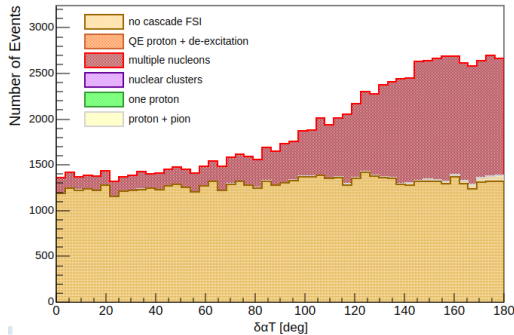
*“Transparent” protons in INCL can be produced alongside nuclear clusters if the remnant de-excites*

*Increase in leading protons below  $p_f$ , almost always emitted alongside nuclear clusters*



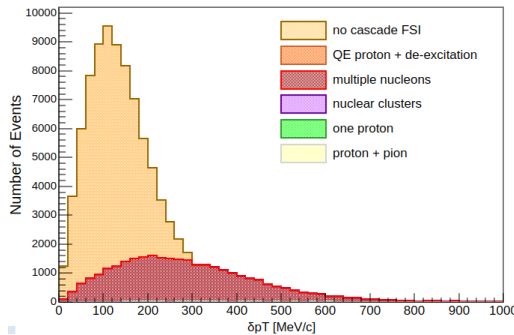
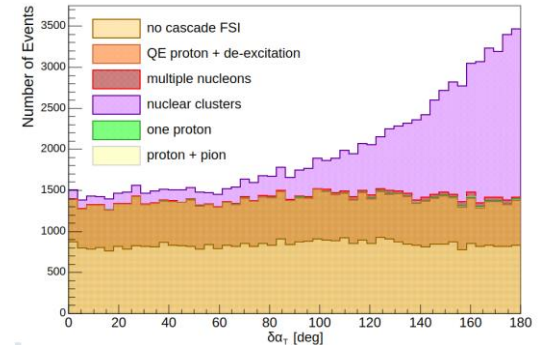
$P_{aft}$  [MeV/c]

## Transverse kinematic imbalance distributions, broken down by channel



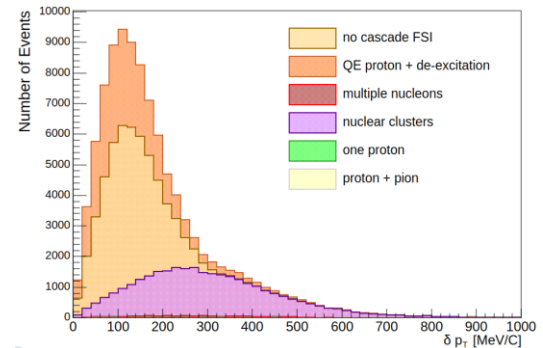
$$|\delta\vec{\alpha}_T| = \arccos\left(\frac{-\vec{p}_T^\mu \cdot \delta\vec{p}_T}{p_T^\mu \cdot \delta p_T}\right)$$

More cluster events at higher angles:  
decelerated de-excitation  
protons are emitted alongside  
clusters



$$|\delta\vec{p}_T| = |\vec{p}_T^p + \vec{p}_T^\mu|$$

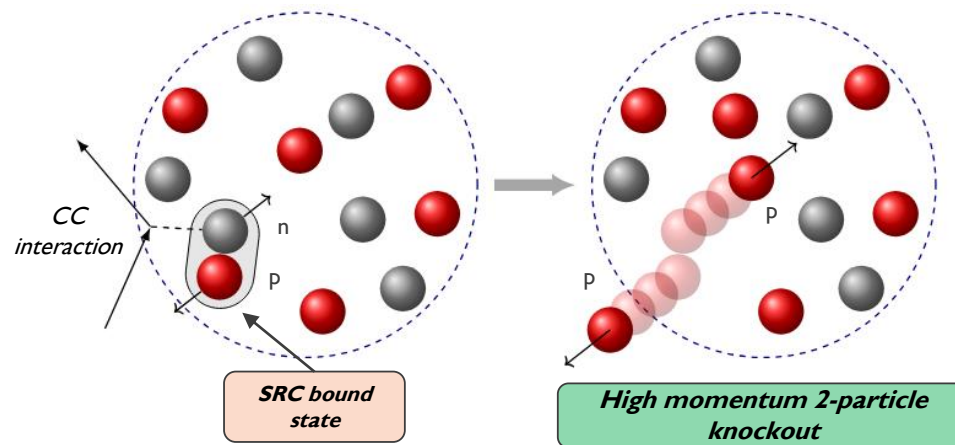
Similar shape, but with INCL:  
-transparent events split into  
two channels  
-multiple nucleon events now  
form with clusters



**Short Range Correlations (SRCs):** Bound pairs of high momentum nucleons found within the nucleus.

- SRCs form the other contribution to the spectral function
- The contribution to the spectral function from SRCs is not separable from the mean field (yet...)
- Freedom in how to define the SRC contribution in generators

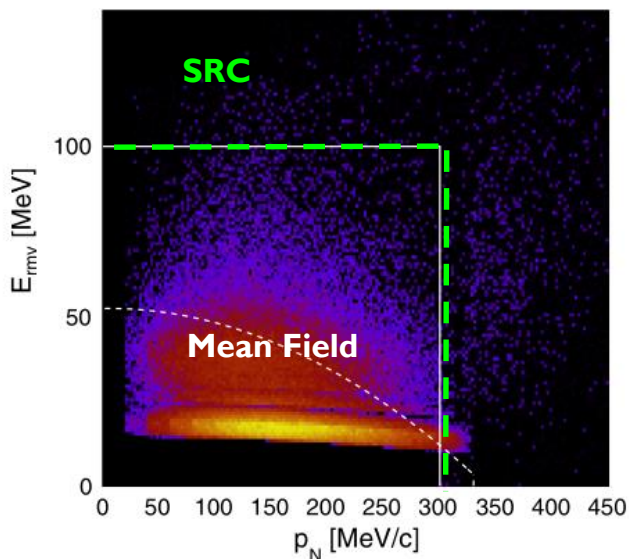
**Excitation energy of the nucleus is very dependent on SRC definition**



*To simulate SRC events, if an event is within the SRC region, place a nucleon of equal and opposite momentum to the struck nucleon into the nucleus*

# Short-range Correlation Modelling - Mo' Protons Mo' Problems

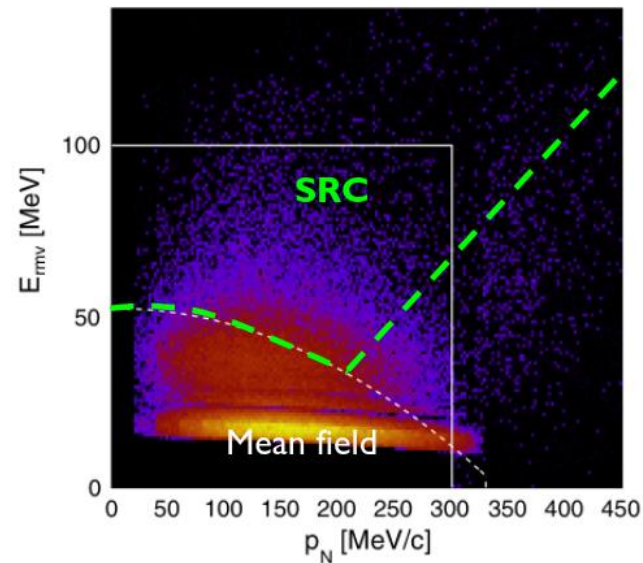
*NEUT SRC - MF and SRC contribution*



NEUT's SRC events are defined as:

- $p_N > 300$  MeV
- $E_{miss} > 100$  MeV

*NuWro SRC - MF and SRC contribution*



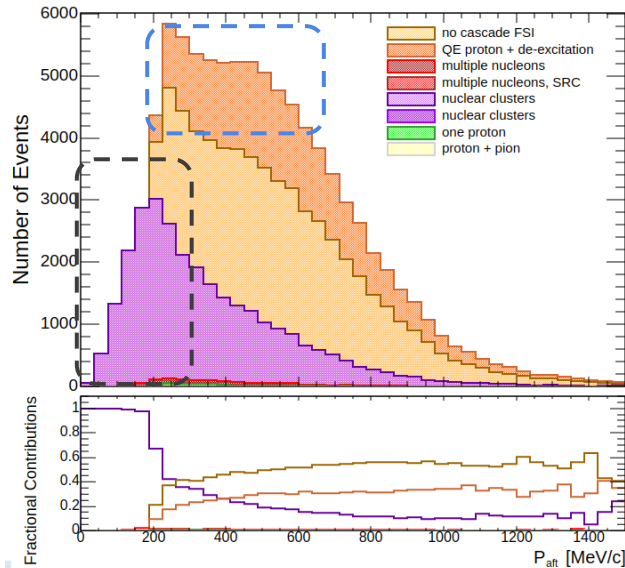
NuWro defines SRC with a function and a cut:

$$p_N > 330 \text{ or } E_{miss} > (52.27 + 0.0048 p_N - 0.0004618 p_N^2)$$

$$E_\nu - E_{lep} - T_p - T_{src} > 14 \text{ MeV}$$

## Leading proton distributions highlight effect of SRC modelling on FSI with INCL

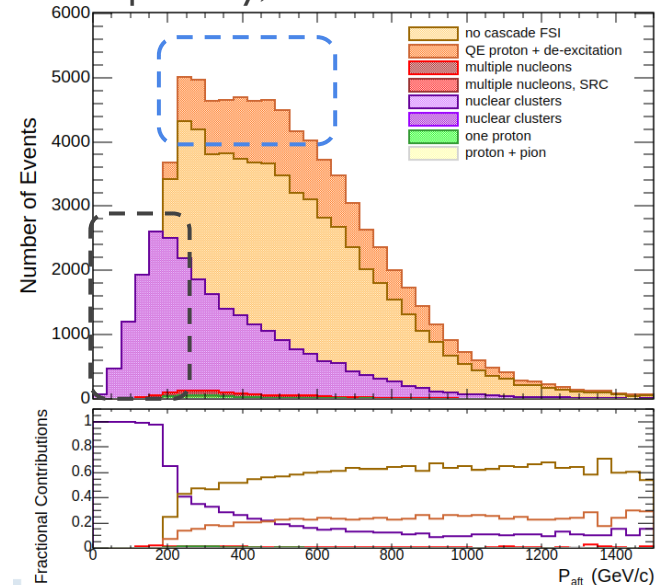
1p1h only, NEUT SRC model



Fewer *transparent + de-excitation* events:  
fewer high missing energy,  
lower momentum protons in  
the NuWro MF distribution

Fewer events with nuclear clusters  
with NuWro SRC model:  
excitation energies are lower  
due to change in MF missing  
energy distribution

1p1h only, NuWro SRC model



Total number of MF CCQE events has reduced as **SRC contribution to SF is greater for NuWro SRC**

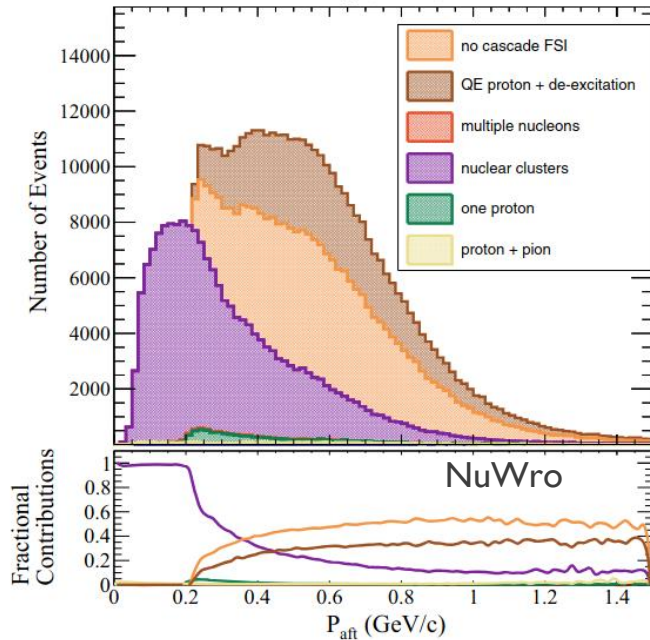
*INCL++ is an FSI model which introduces nuclear clustering and a better handling of low energy nucleon interactions.*

- The interface developed allows for straight integration of the INCL++ cascade into NEUT, allowing for data comparisons and fake data studies to be performed, with potential for reweightability in the future
- The introduction of nuclear clusters in FSI can lead to a better understanding of nuclear effects and improved neutrino energy reconstruction
- Introducing the INCL cascade with ABLA into NEUT increases number of final state channels and greatly reduces the number of purely transparent events through de-excitation
- SRC model choice affects FSI in INCL due to changes in the excitation energy calculation and the ratio of MF |p|h to SRC events

*Special thanks to Anna Beever for her invaluable support in getting this work to this point!*

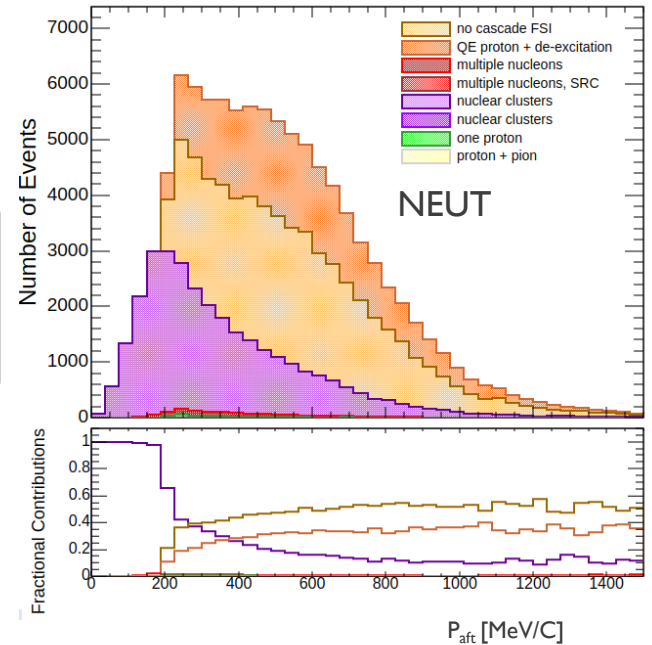
*Also, thanks to Patrick Stowell, Sara Bolognesi, and Jean Davide-Christophe for INCL physics input and to Jake McKean and other members of the T2K NIWG for neutrino physics and NEUT input.*

## Leading proton distributions post FSI, broken down by channel



Plot from PHYSICAL REVIEW D 108, 112008 (2023)

*Implementation in NEUT matches prior work, with some differences from initial interaction modelling*

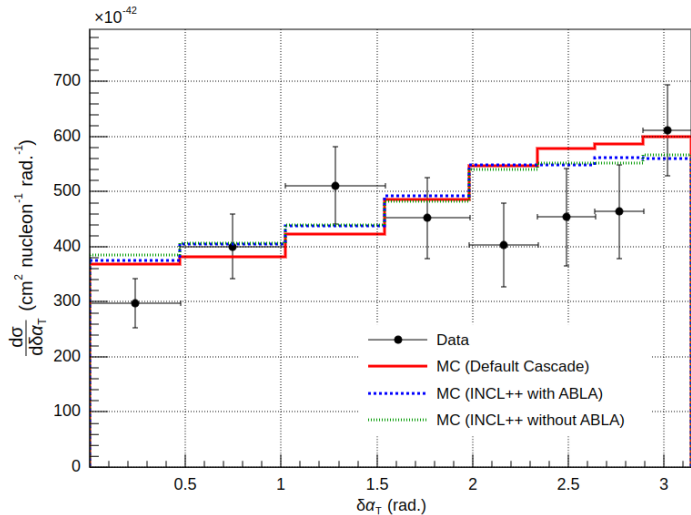


## Annas comments

BACKUPS

# Preliminary Data Comparisons - T2K TKI

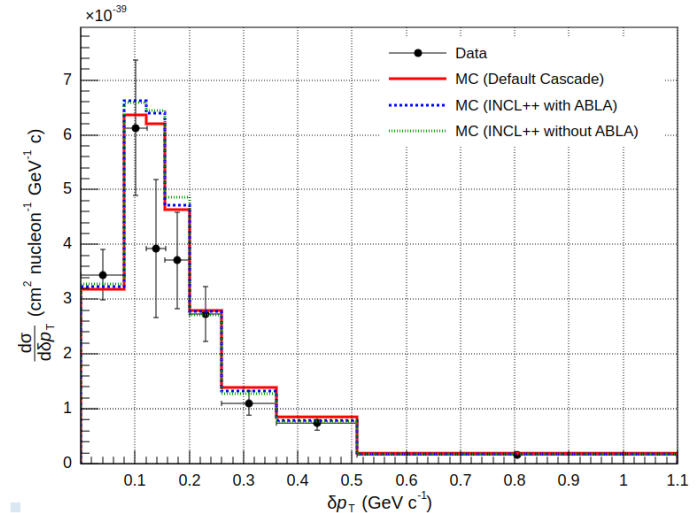
INCL++ can only use CCQE events at present, so using NEUT data for other channels



Apparent “reduction”  
in FSI strength for  
INCL is due to  
presence of non  
proton events in INCL

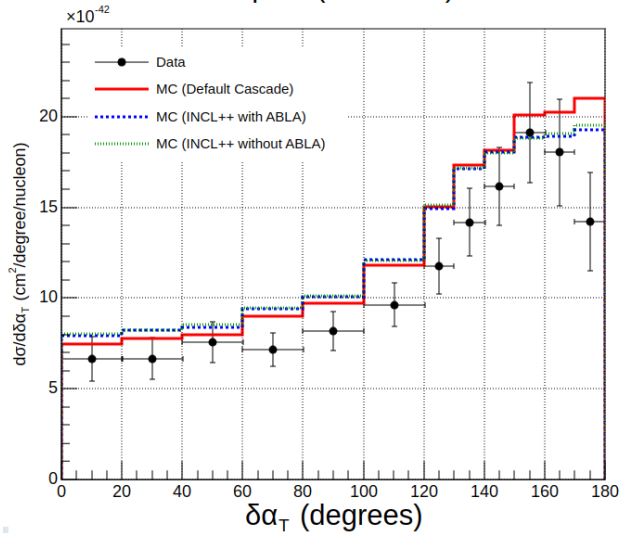
T2K’s proton tracking  
threshold is 500MeV

NEUT Cascade: 12.01 / 8  
NEUT + INCL 10.85 / 8  
NEUT + INCL + ABLA 10.73 / 8



NEUT Cascade: 8.47 / 8  
NEUT + INCL 7.28 / 8  
NEUT + INCL + ABLA 7.09 / 8

# Preliminary Data Comparisons - MiNERva TKI

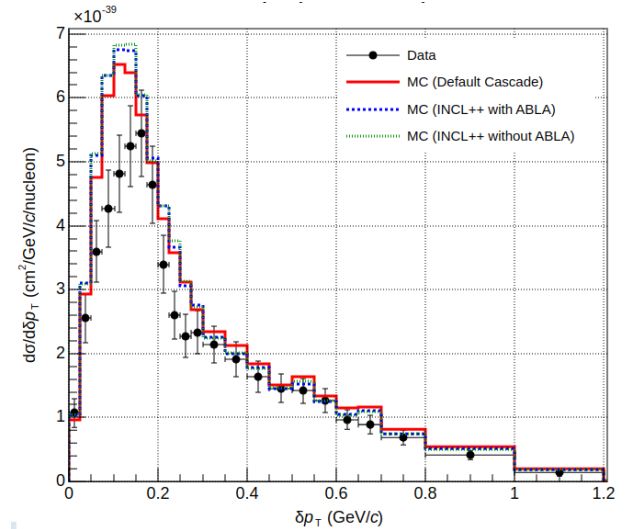


DaT

Neut cascade: 24.55 / 12

NEUT + INCL: 26.38 / 12

NEUT + INCL + ABLA 27.79 / 12



DpT

NEUT Cascade: 53.72 / 24

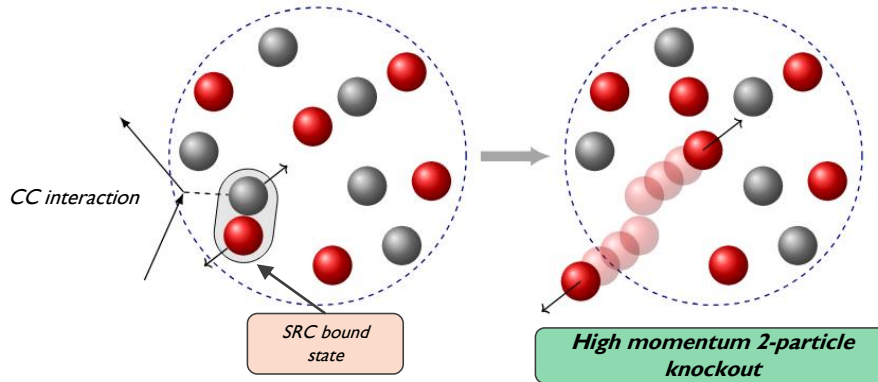
NEUT + INCL: 61.92 / 24

NEUT + INCL + ABLA: 65.79 / 24

Plot of nuisance generated total pN, overlaid  
and normalised, for bertini, INCL and  
INCL+ABLA

# Short-range Correlation Modelling

**SRC:** High momentum nucleons ( $> p_f$ ) existing in correlated bound pairs in the nucleus

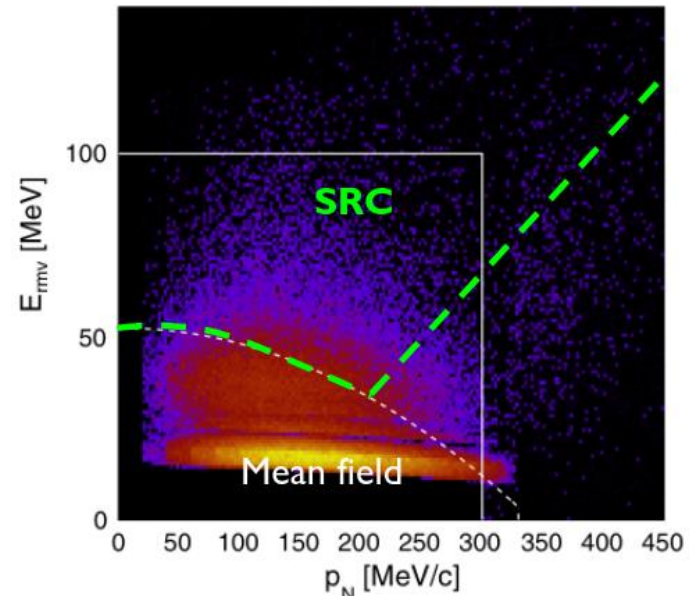


The contribution to the spectral function from SRC is not separable - event generators model this by using cuts on the total SF distribution

NuWro uses:

$$p_N > 330 \text{ or } E_{\text{miss}} > (52.27 + 0.0048 p_N - 0.0004618 p_N^2)$$

- $E_{\text{miss}} > 100 \text{ MeV}$



Plot originally from PHYSICAL REVIEW D 109, 072006 (2024)

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rgba(255, 47, 47)
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