

Fluctuating Proton Geometry: Constraints from Charge Radius, Diffraction, and Flow

Wenbin Zhao

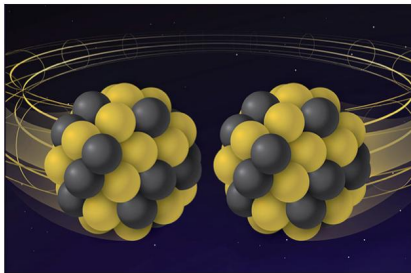
Central China Normal University

5th edition of the International Small Systems workshop

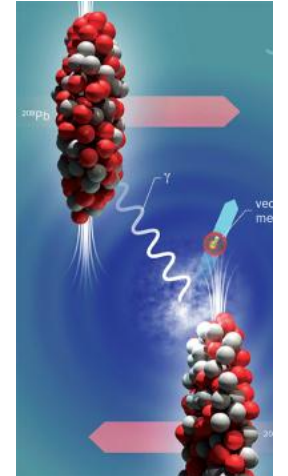
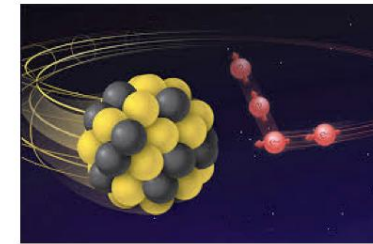
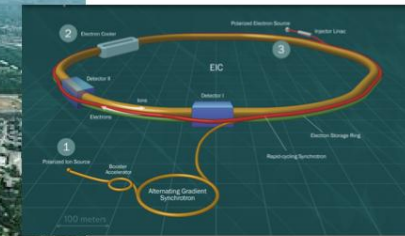
2026.07.02 (Online)



Heavy-ion Collisions and DIS/UPC



- **Heavy-ion Collisions:** High center-of-mass energies available.
- **Multi-Stage process:**
Initial state $\Rightarrow$ QGP $\Rightarrow$ Hadronic Scatter



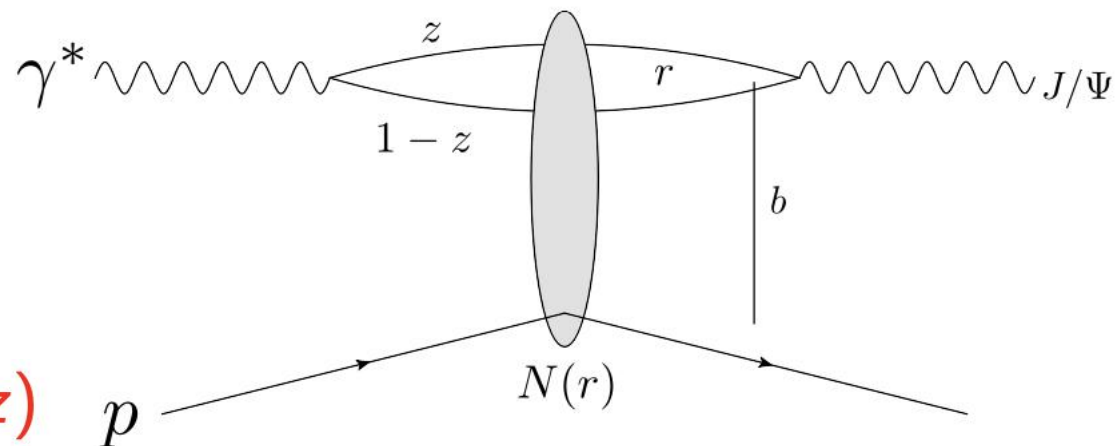
- **DIS/UPC:**
- Pin down kinematics, clean probes of QCD dynamics.
- Collision energy is limited.

- It is the same nucleus at small x: probe the initial state in DIS/UPC, then apply to heavy ion simulations.

Imaging nuclei with photon-nucleus reactions

High energy factorization:

- ① $\gamma^* \rightarrow q\bar{q}$ splitting, wave function $\Psi^\gamma(r, Q^2, z)$
- ② $q\bar{q}$ dipole scatters elastically $N(r, x, b)$
- ③ $q\bar{q} \rightarrow J/\psi$, wave function $\Psi^V(r, Q^2, z)$



Diffractive scattering amplitude

$$\mathcal{A}^{\gamma^* p \rightarrow V p} \sim \int d^2 b dz d^2 r \Psi^{\gamma^*} \Psi^V(r, z, Q^2) e^{-i b \cdot \Delta} N(r, x, b)$$

Impact parameter, b , is the Fourier conjugate of the momentum transfer, $\Delta \approx \sqrt{-t}$, $N(r, x, b)$ dipole-target scattering amplitude.

$\mathbf{A} \sim$ Fourier transform of the spatial structure function of target ($T_{p/A}$).

Miettinen, Pumplin, PRD 18, 1978; Caldwell, Kowalski, 0909.1254; Mäntysaari, Schenke, 1603.04349; Mäntysaari, 2001.10705

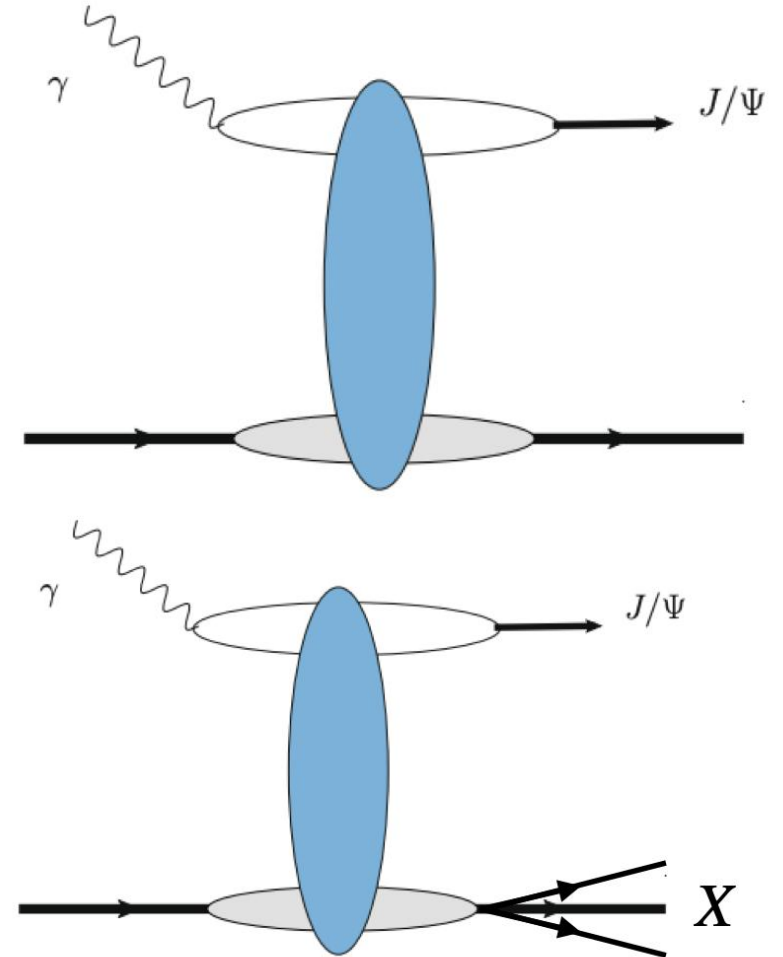
Coherent and incoherent processes

- **Coherent** $\sigma_{\text{coherent}} \sim |\langle \mathcal{A} \rangle_{\Omega}|^2$

Target stays intact, ($|\text{initial state}\rangle = |\text{final state}\rangle$)
Probes the average shape of the target.

- **Incoherent** $\sigma_{\text{incoherent}} \sim \langle |\mathcal{A}|^2 \rangle_{\Omega} - |\langle \mathcal{A} \rangle_{\Omega}|^2$

Target breaks apart, ($|\text{initial state}\rangle \neq |\text{final state}\rangle$)
Probes the variance of event-by-event initial state fluctuations in target structure.



Proton geometry fluctuations (hot spot)

- Proton's event-by-event fluctuating density profile:

$$T_p(\mathbf{b}_\perp) = \frac{1}{N_q} \sum_{i=1}^{N_q} p_i T_q(\mathbf{b}_\perp - \mathbf{b}_{\perp,i}), \quad P(\ln p_i) = \frac{1}{\sqrt{2\pi}\sigma} \exp \left[-\frac{\ln^2 p_i}{2\sigma^2} \right].$$

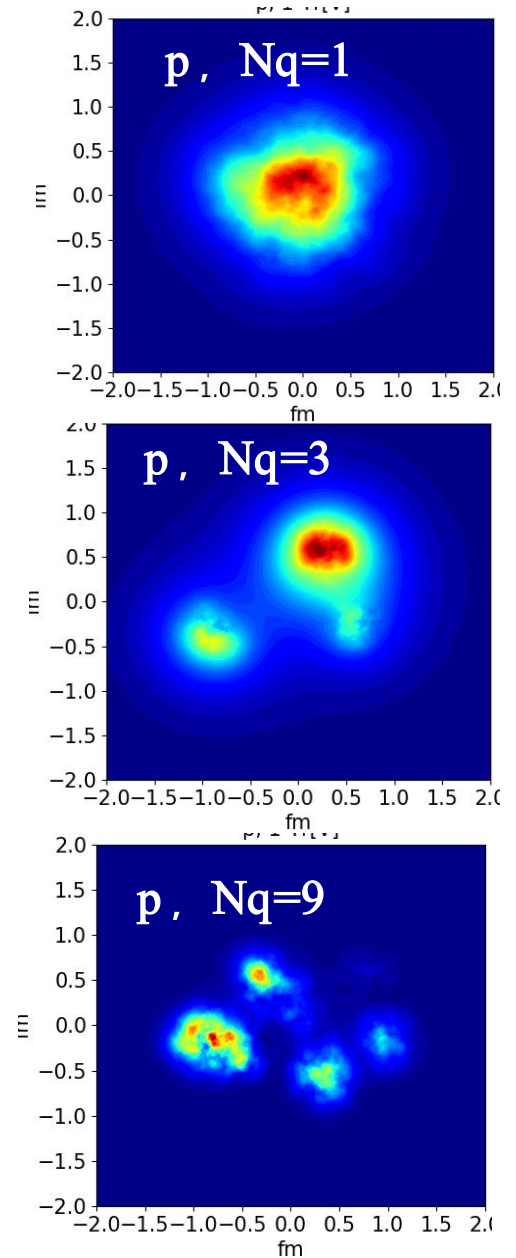
- The density profile of each spot is:

$$T_q(\vec{b}) = \frac{1}{2\pi B_q} e^{-b^2/(2B_q)}$$

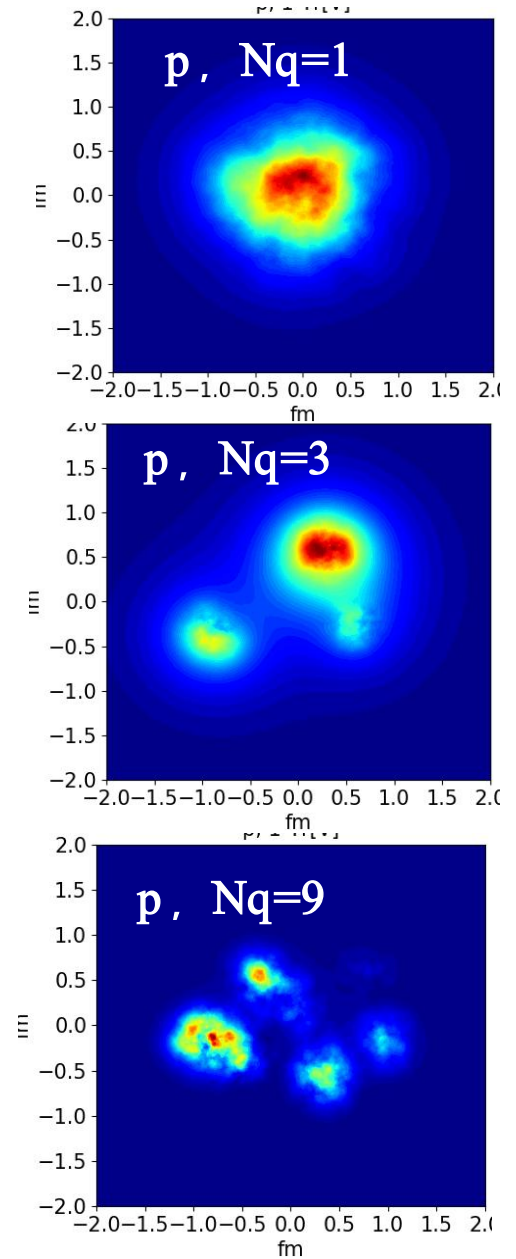
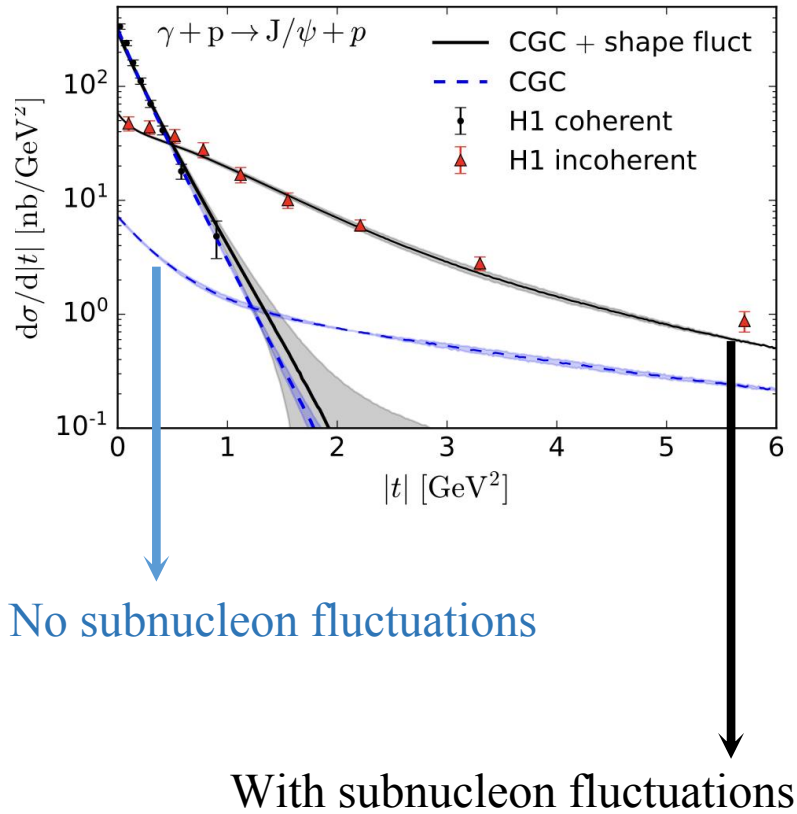
- The spot positions $\vec{b}_i$ are sampled from:

$$P(b_i) = \frac{1}{2\pi B_{qc}} e^{-b_i^2/(2B_{qc})}$$

Schenke , etc.al. PhysRevLett.108.252301 ,
PhysRevC.86.034908, Mäntysaari, Schenke, 1603.04349;

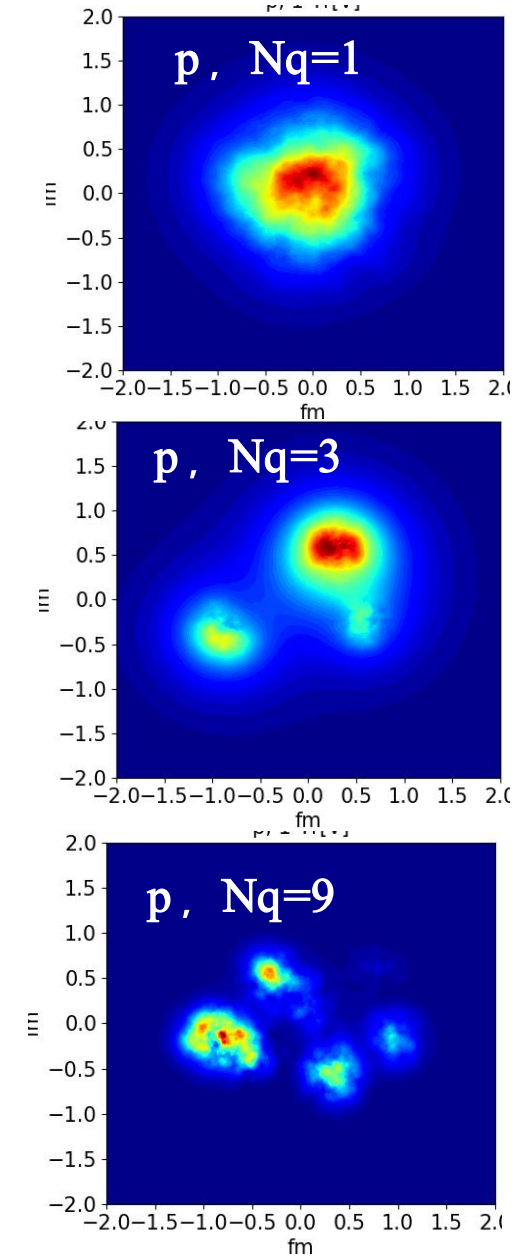
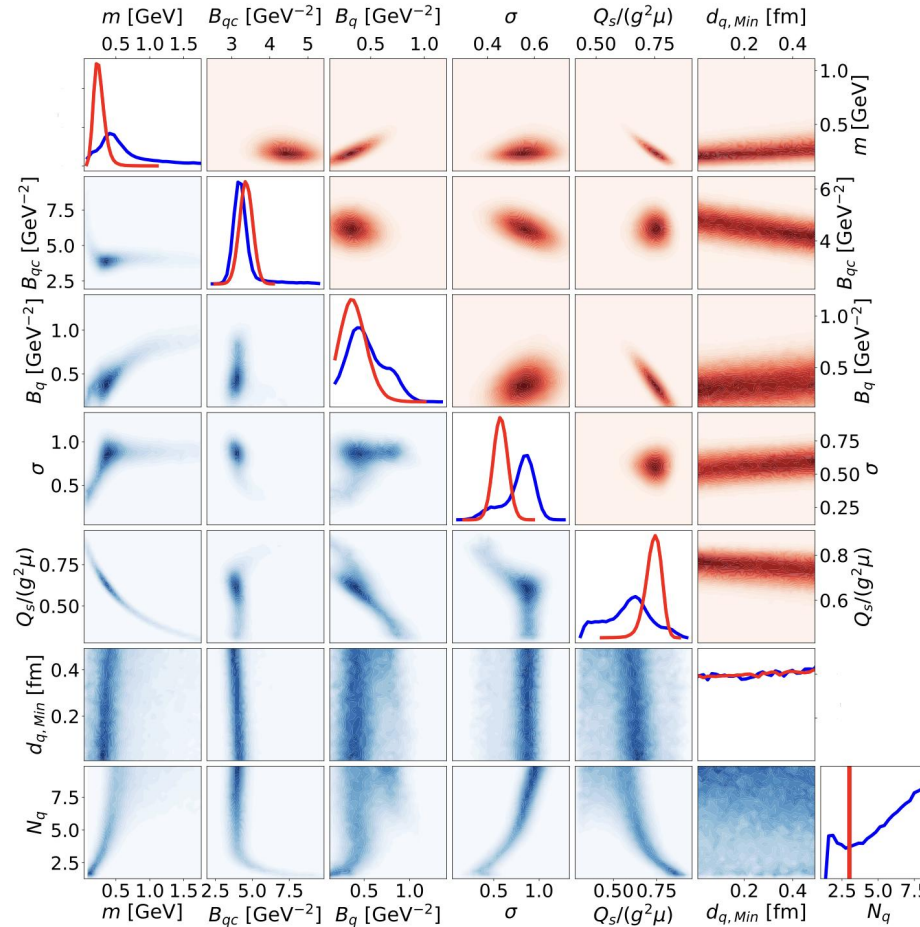
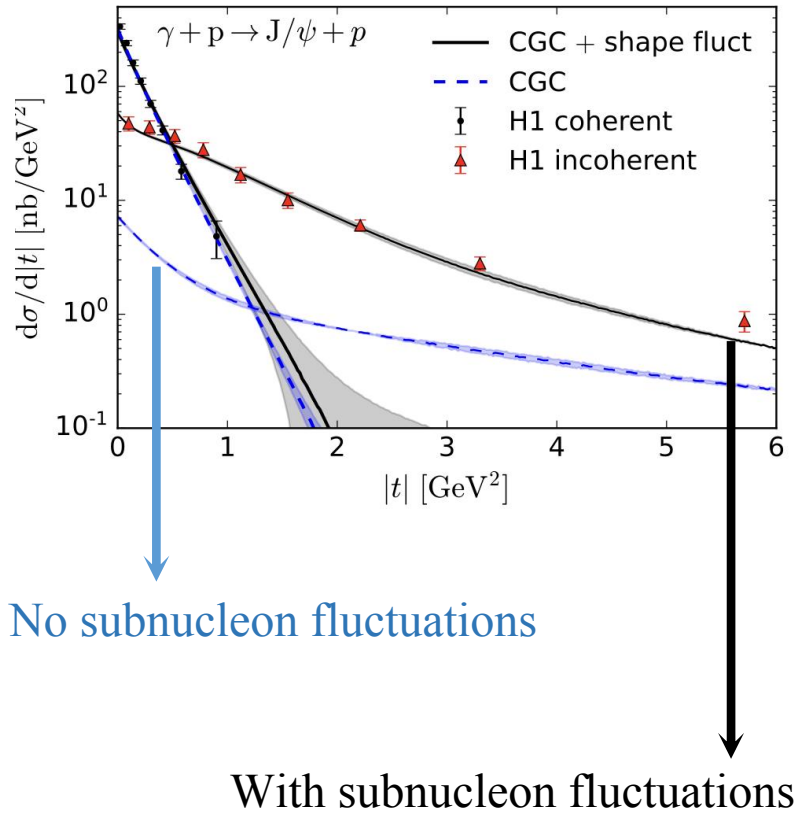


Proton geometry fluctuations



H. Mäntysaari, Schenke, PhysRevLett.108.252301, PhysRevC.86.034908;
 H. Mäntysaari, F. Salazar and B. Schenke, Phys. Rev. D 106, 074019 (2022).
 H. Mäntysaari, B.Schenke, C. Shen and W. Zhao, Phys. Lett. B 833 (2022), 137348.

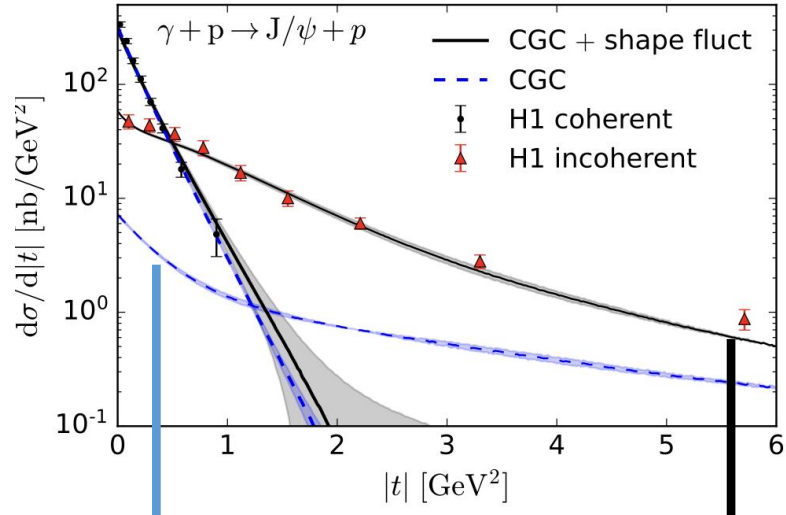
Proton geometry fluctuations



- The extracted proton radius **$R \sim 0.6$ fm**.

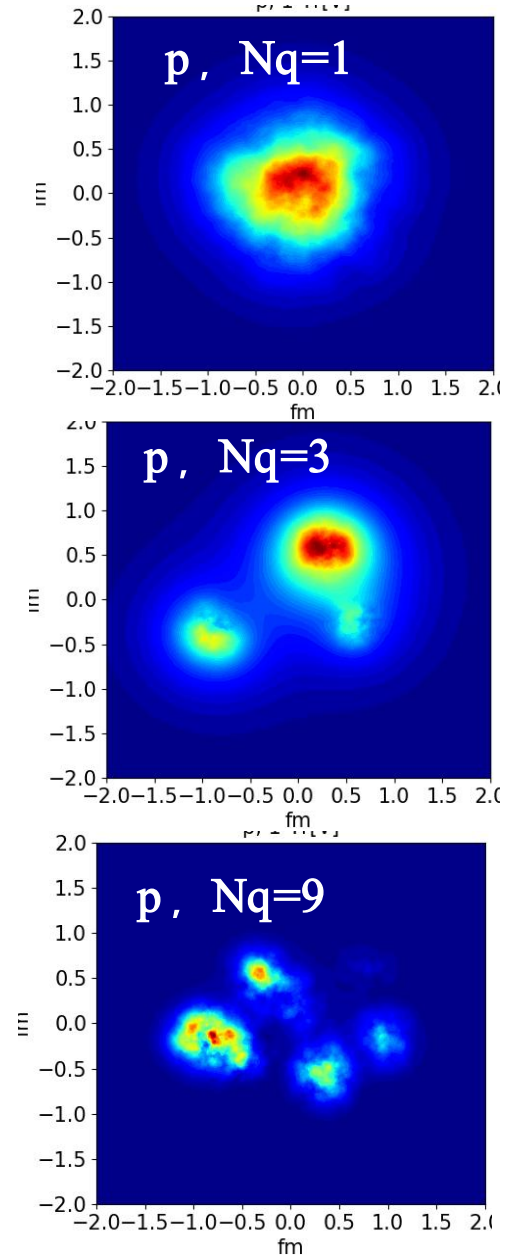
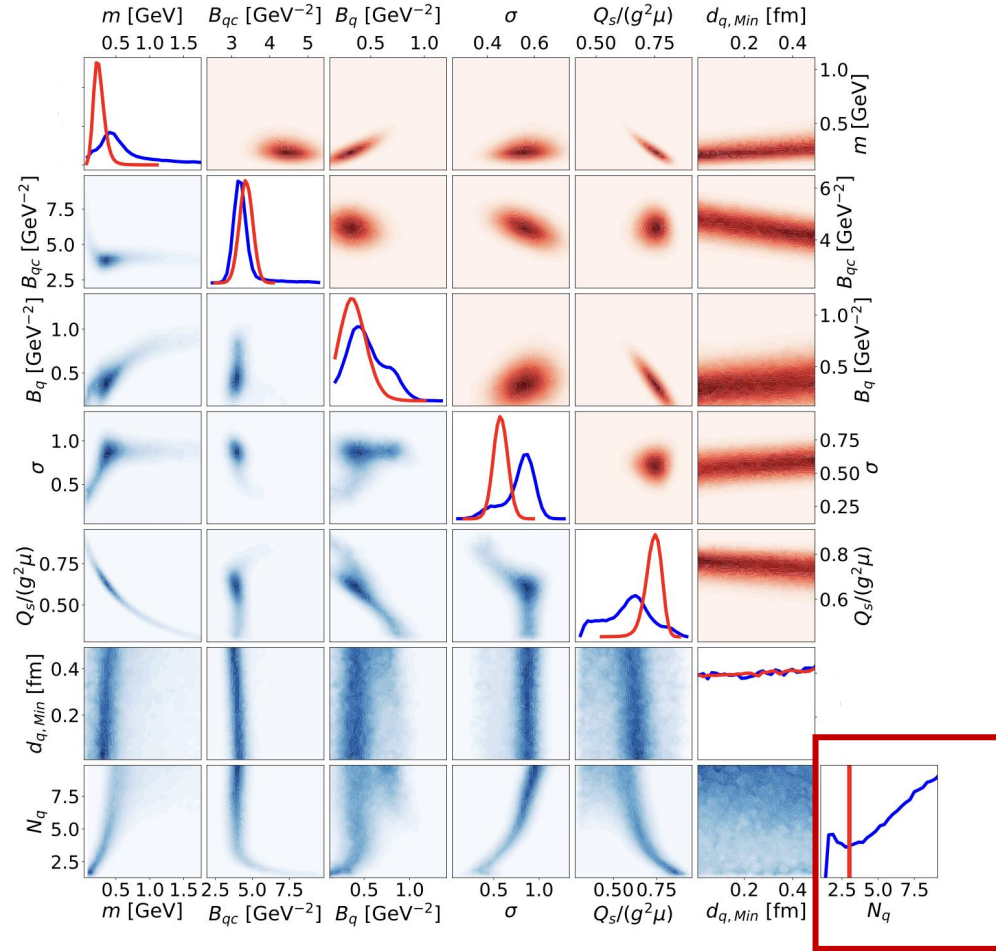
H. Mäntysaari, Schenke, PhysRevLett.108.252301, PhysRevC.86.034908;
H. Mäntysaari, F. Salazar and B. Schenke, Phys. Rev. D 106, 074019 (2022).
H. Mäntysaari, B.Schenke, C. Shen and W. Zhao, Phys. Lett. B 833 (2022), 137348.

Proton geometry fluctuations



No subnucleon fluctuations

With subnucleon fluctuations

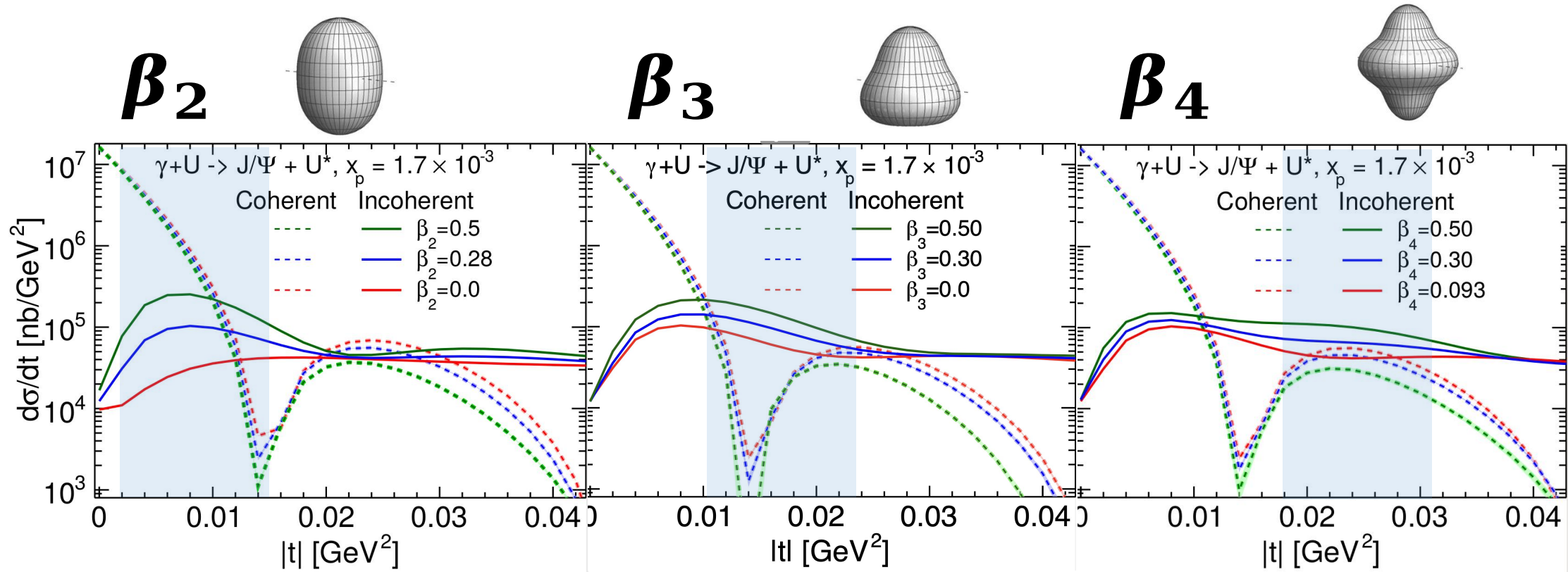


- The extracted proton radius **$R \sim 0.6$ fm**.
- $Nq = 1$ (no sub-nucleonic structure) is **excluded** by data.

H. Mäntysaari, Schenke, PhysRevLett.108.252301, PhysRevC.86.034908;
H. Mäntysaari, F. Salazar and B. Schenke, Phys. Rev. D 106, 074019 (2022).
H. Mäntysaari, B.Schenke, C. Shen and W. Zhao, Phys. Lett. B 833 (2022), 137348.

Multi-scale imaging of Nuclear shape

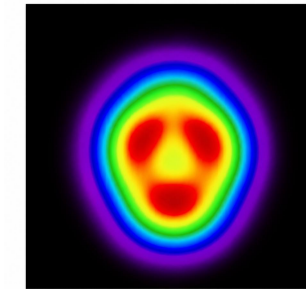
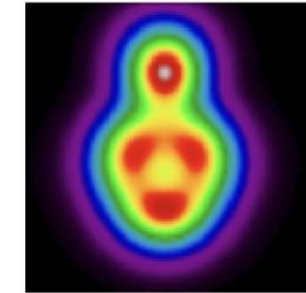
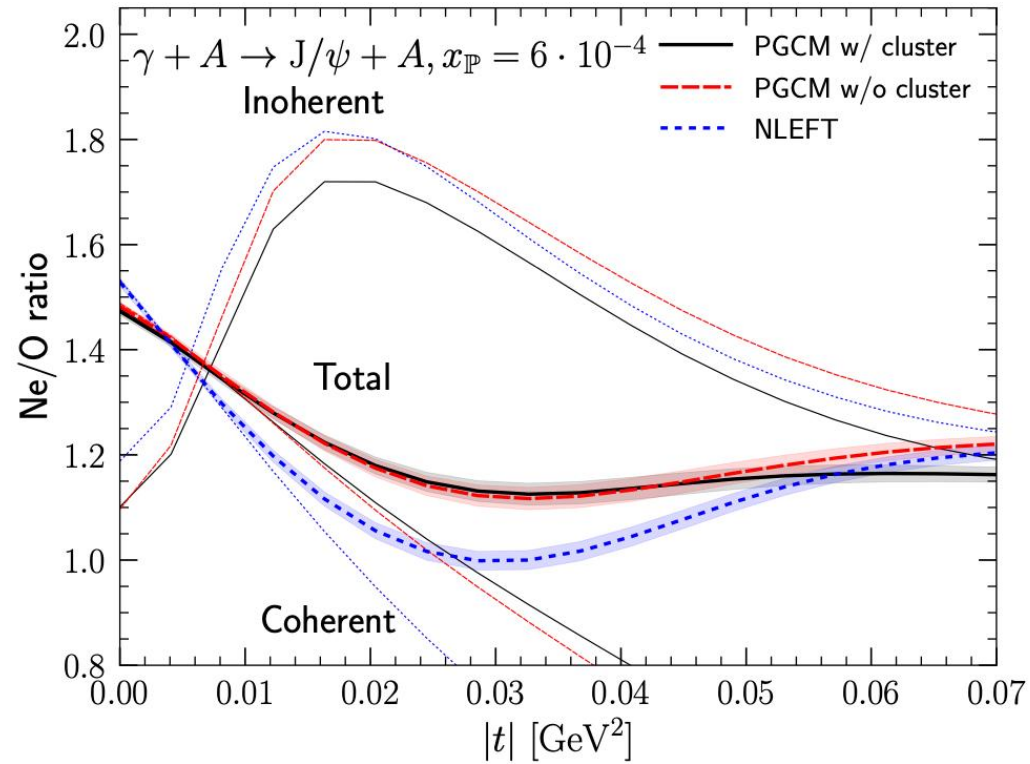
$$\rho(r, \Theta, \Phi) \propto \frac{1}{1 + \exp([r - R(\Theta, \Phi)]/a)} , \quad R(\Theta, \Phi) = R_0 \left[1 + \underline{\beta_2} \left(\cos \gamma Y_{20}(\Theta) + \sin \gamma \underline{Y_{22}}(\Theta, \Phi) \right) + \underline{\beta_3} Y_{30}(\Theta) + \underline{\beta_4} Y_{40}(\Theta) \right]$$



H. Mäntysaari, B. Schenke, C. Shen and W. Zhao, PhysRevLett.131.062301.

- “**X-ray vision**” for atoms.

Imaging of Light Nuclei Shape

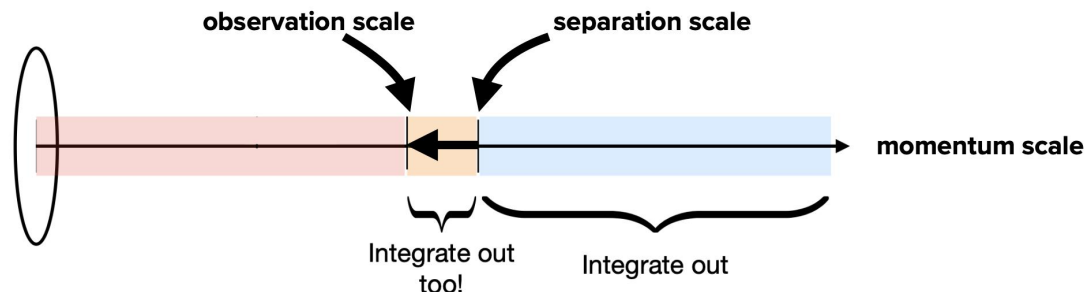


H. Mantysaari, H. Roch, B. Schenke, C. Shen and W. Zhao, [arXiv:2605.00454 [hep-ph]].

H. Mäntysaari, B. Schenke, C. Shen and W. Zhao, PhysRevLett.131.062301.

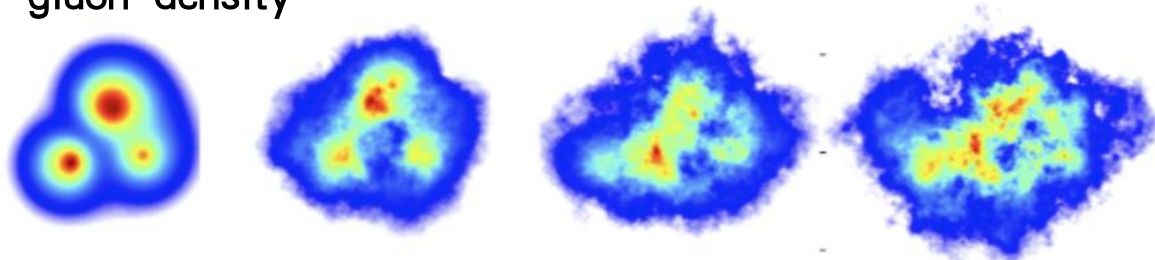
- Probing the bowling-pin shape of Ne-20 in UPCs

Energy evolution of initial state



A. Morreale and F. Salazar, Universe 7, no.8, 312 (2021).

gluon density



Low energy
(UPC/DIS)

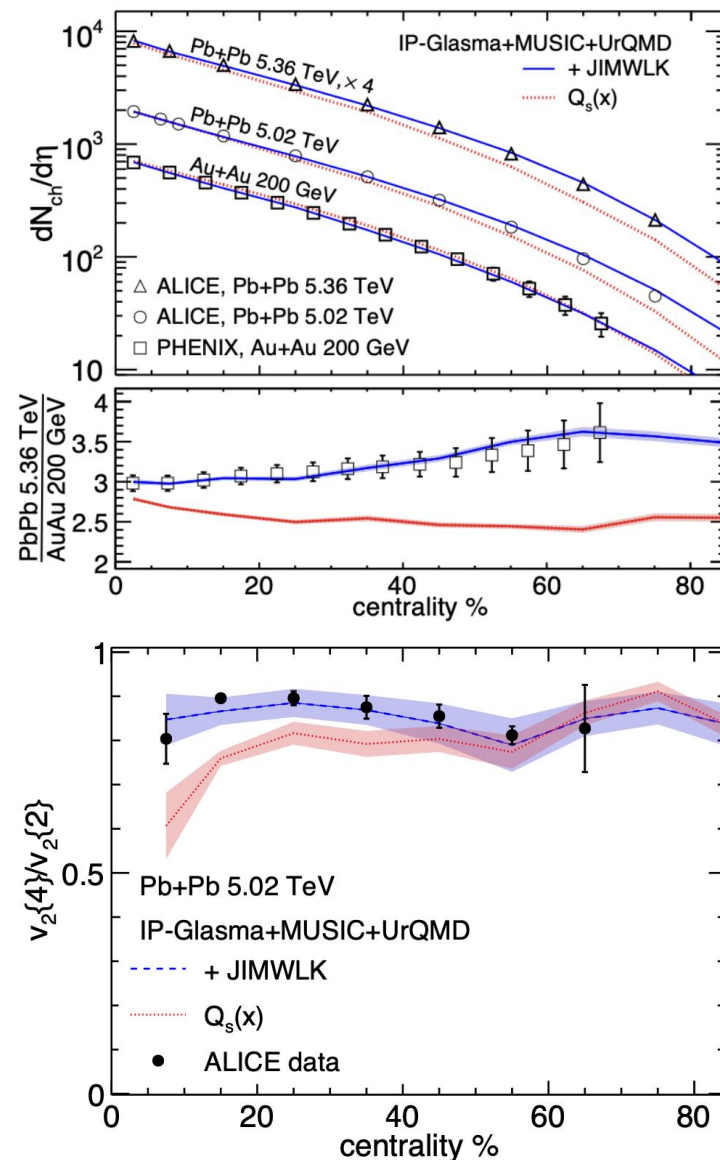


High energy
(LHC)

- Energy evolution of the initial state is important to final state observables.

H. Mäntysaari and B. Schenke, PRD 98 (2018) 034013.

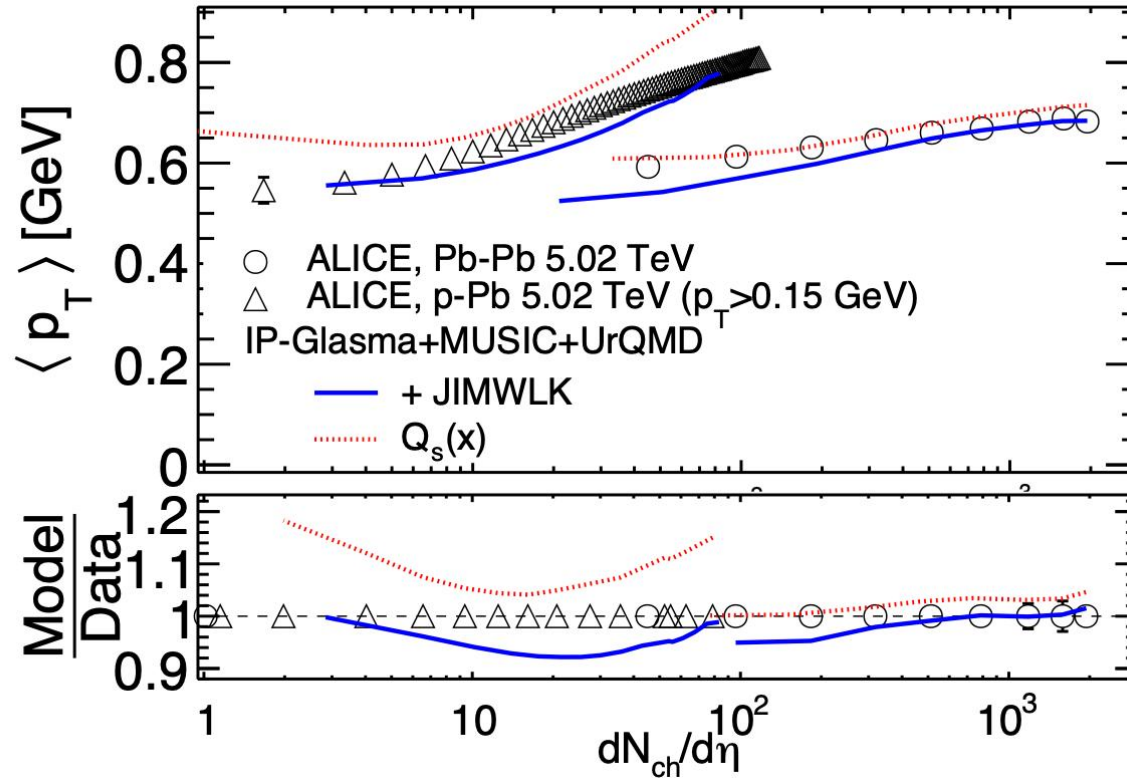
H. Mäntysaari, B. Schenke, C. Shen and W. Zhao, PRL. 135, 022302 (2025)



+ **JIMWLK**: CGC + energy evolution

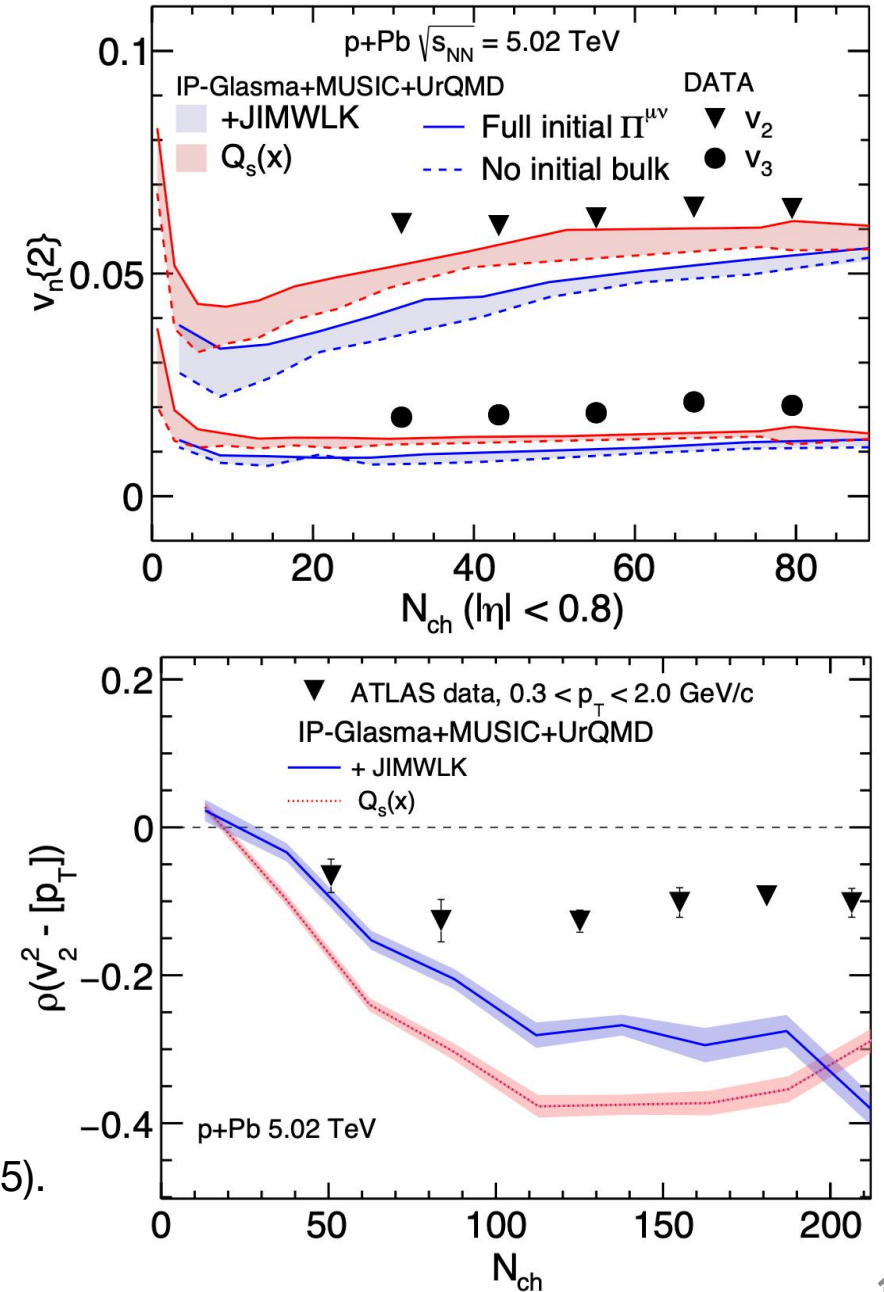
$Q_s(x)$: CGC (change the $Q_s(x)$ only)

Energy evolution of initial state

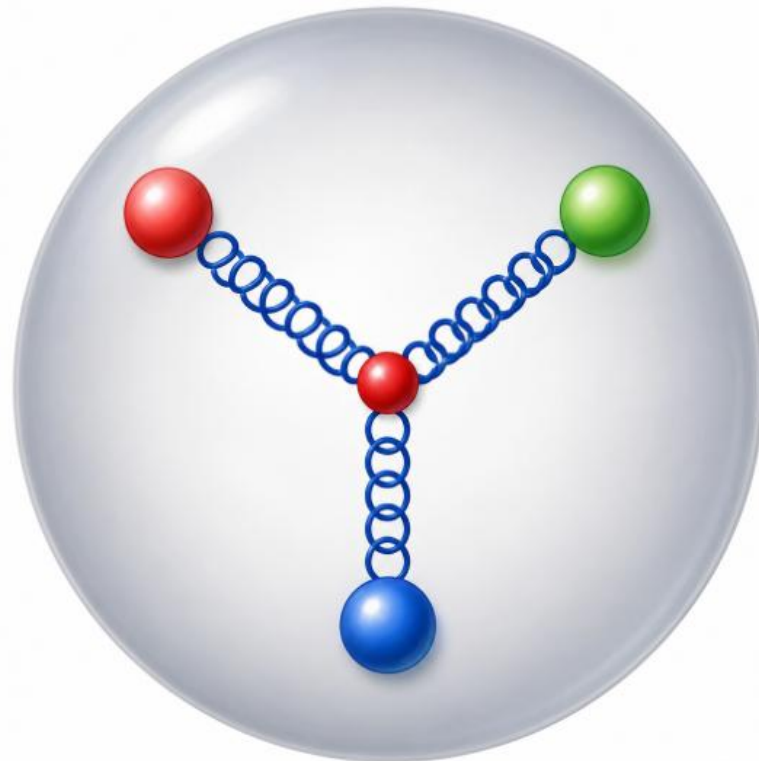


- Energy evolution will **reduce the mean p_T** .
- Energy evolution is more important for small systems.

H. Mäntysaari, B. Schenke, C. Shen and W. Zhao, PRL. 135, 022302 (2025).
H. Mäntysaari, B. Schenke, C. Shen and W. Zhao, [arXiv: 2511.03588].



Stringy Proton



Proton geometry fluctuations (stringy proton)

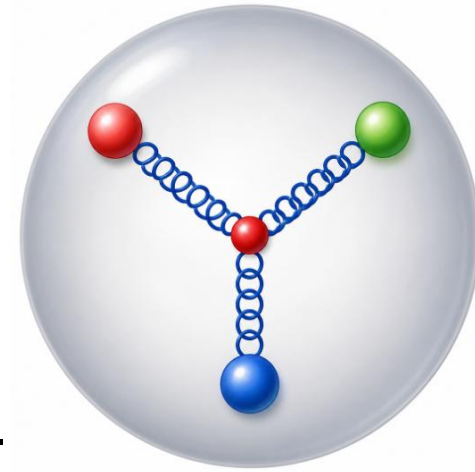
- Sample 3 valence quarks with Gaussian, $\mathbf{B}_q = \mathbf{R}_{ch} \approx 0.87\text{fm}$ (not a free parameter anymore).

$$T_q(\vec{b}) = \frac{1}{2\pi\mathbf{B}_q} e^{-b^2/(2\mathbf{B}_q)}$$

- Construct Y-shaped geometry, connect via Fermat point
- Place gluons along strings: Sample points on strings; Add Gaussian gluonic hot spot.
- Add log-normal Q_s fluctuations:

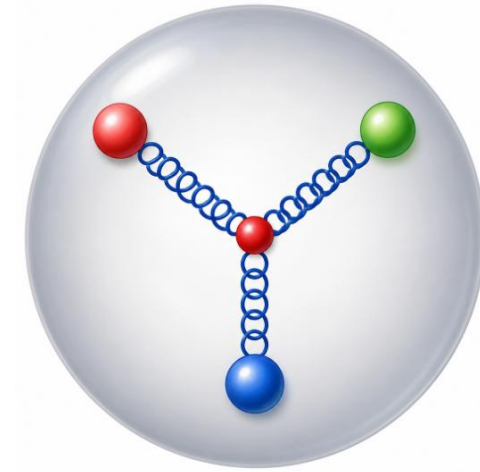
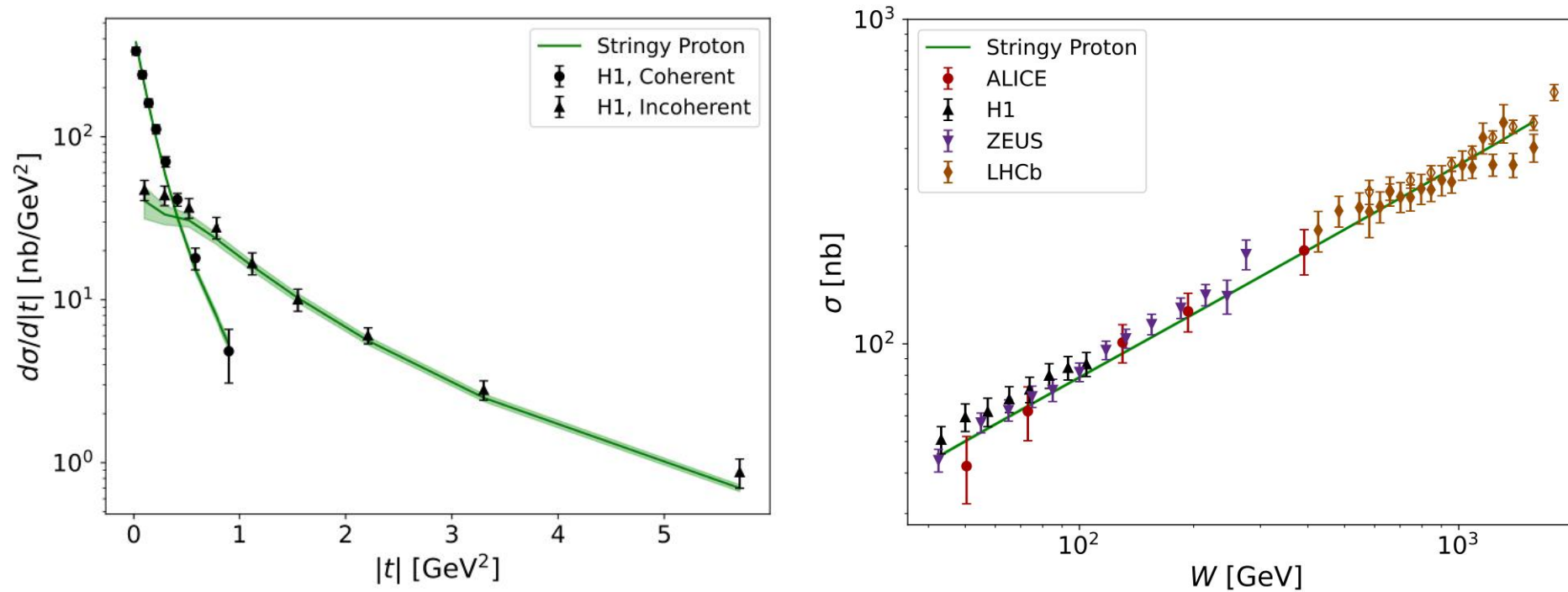
$$T_p(\mathbf{b}_\perp) = \frac{1}{N_q} \sum_{i=1}^{N_q} p_i T_q(\mathbf{b}_\perp - \mathbf{b}_{\perp,i}), \quad P(\ln p_i) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left[-\frac{\ln^2 p_i}{2\sigma^2}\right].$$

⇒ Event-by-event shape + density fluctuations.
 ⇒ Automatically get: $\mathbf{R}_g \leq \mathbf{R}_{ch}$.



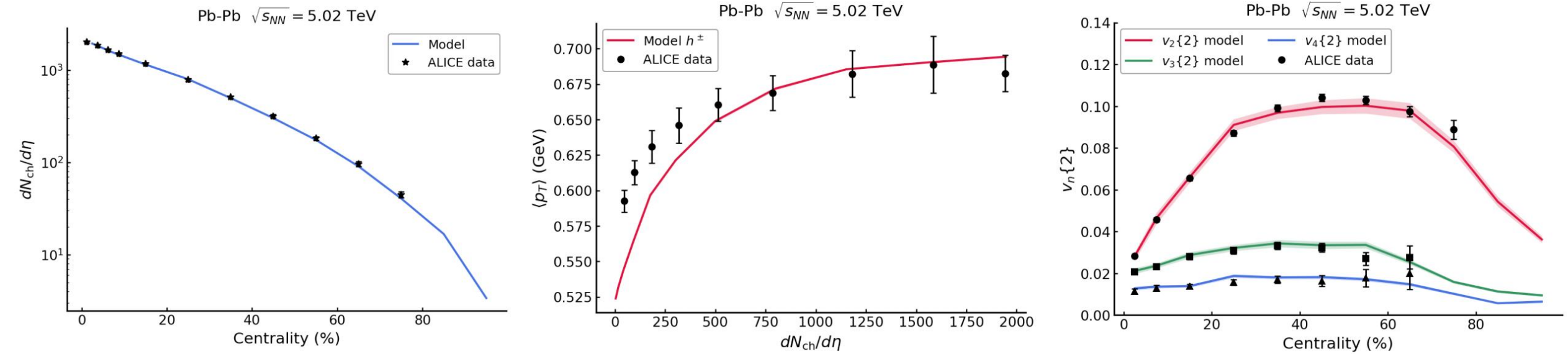
- Lattice QCD : Y-shaped flux tubes (Bissey et al., PRD 76 (2007));
- Baryon junction picture : Rossi, Veneziano, Nucl. Phys. B 123 (1977); D. Kharzeev, Phys.Lett. B 378, 238–246 (1996)).
- Proton = 3 valence quarks connected by gluonic strings.

Fix the Proton geometry by diffractive J/ψ



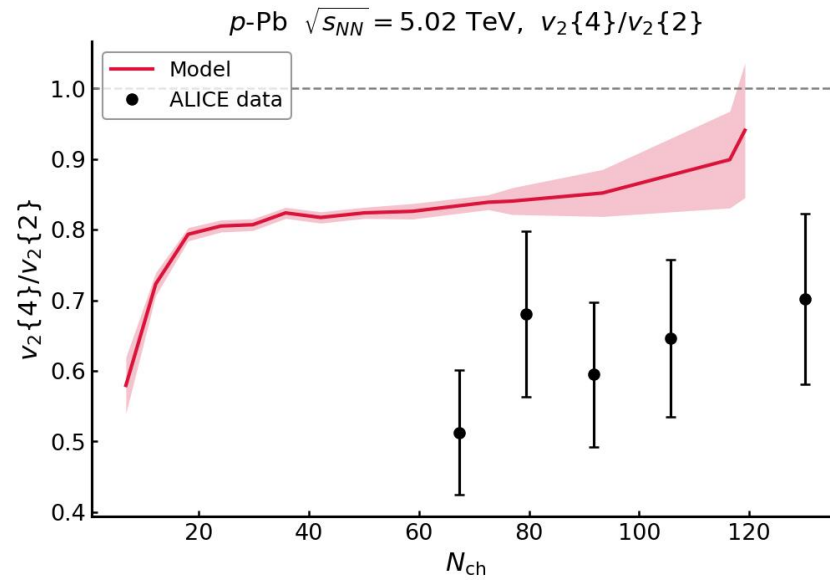
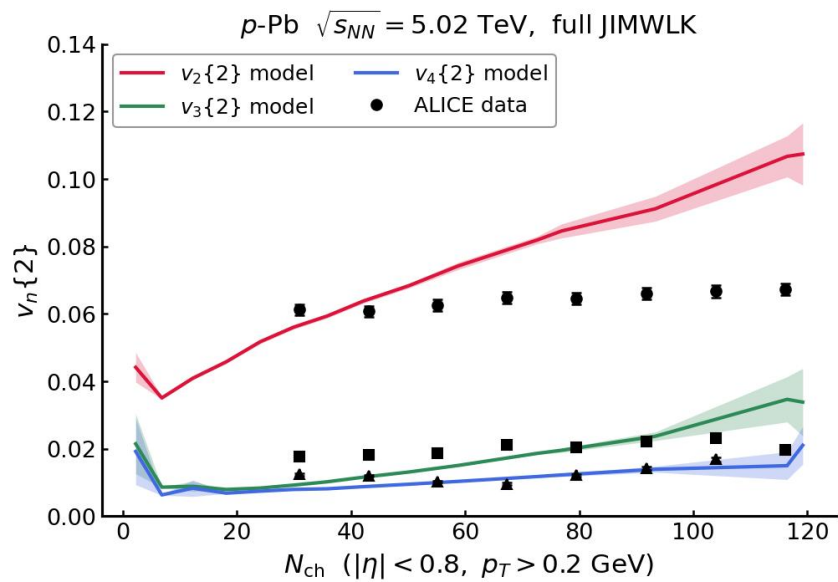
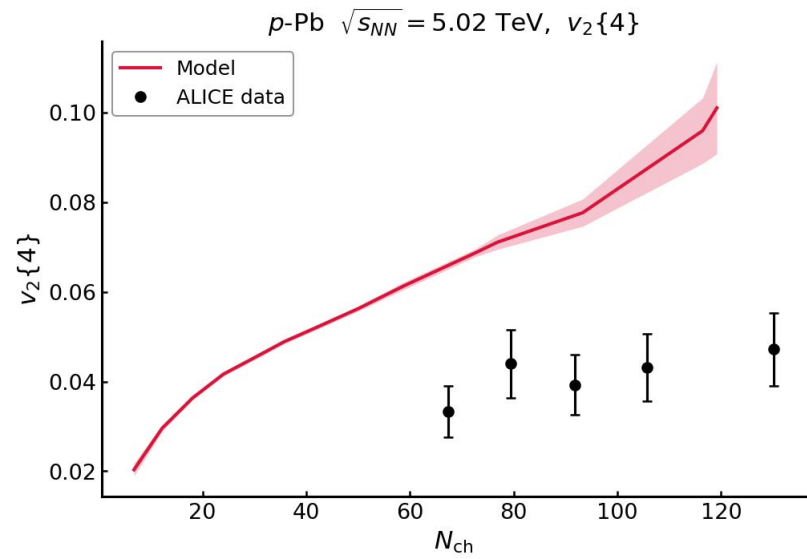
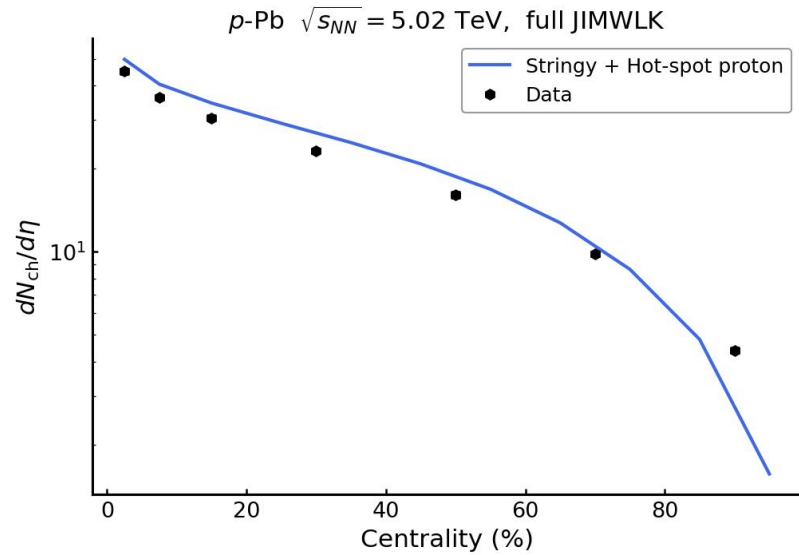
- The t -differential and integrated J/ψ cross sections show good agreement with the data.
- **With the charge radius fixed** and the remaining parameters fitted to diffractive data, the model gives a consistent description of the proton structure.

From DIS to heavy-ion collisions

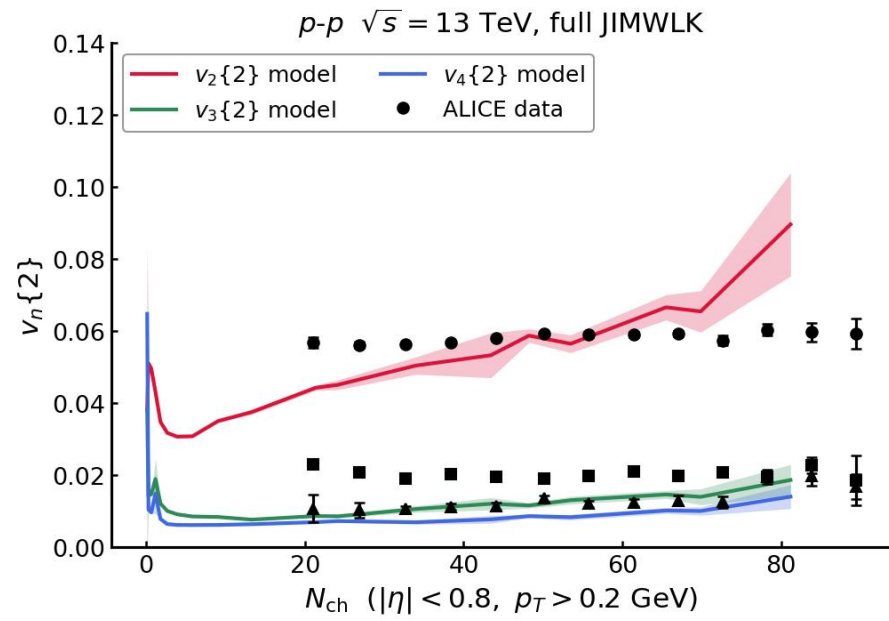


- Apply the stringy proton implemented in IP-Glasma to HIC systems with MUSIC+UrQMD.
- Well describe the flow observables in the heavy-ion collisions.

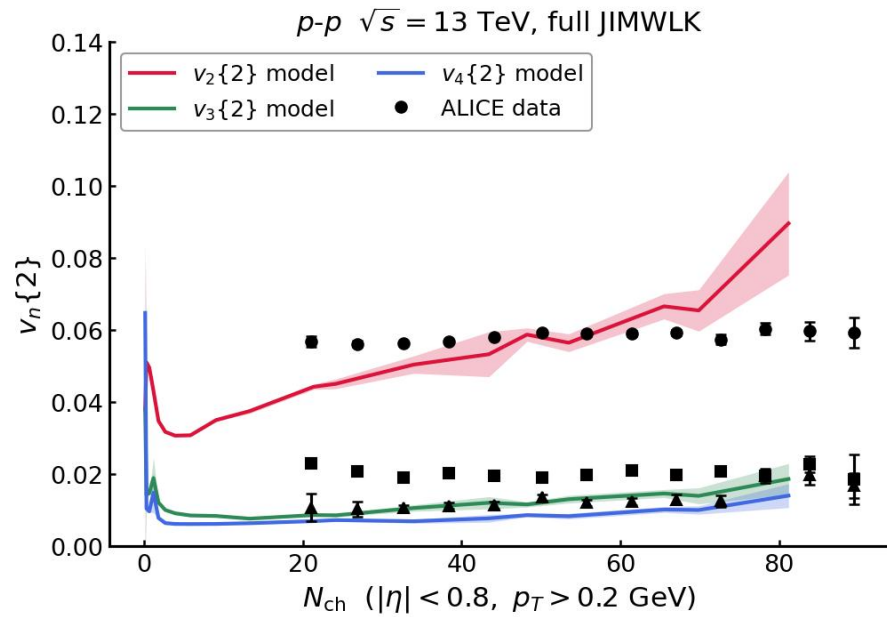
p-Pb collisions



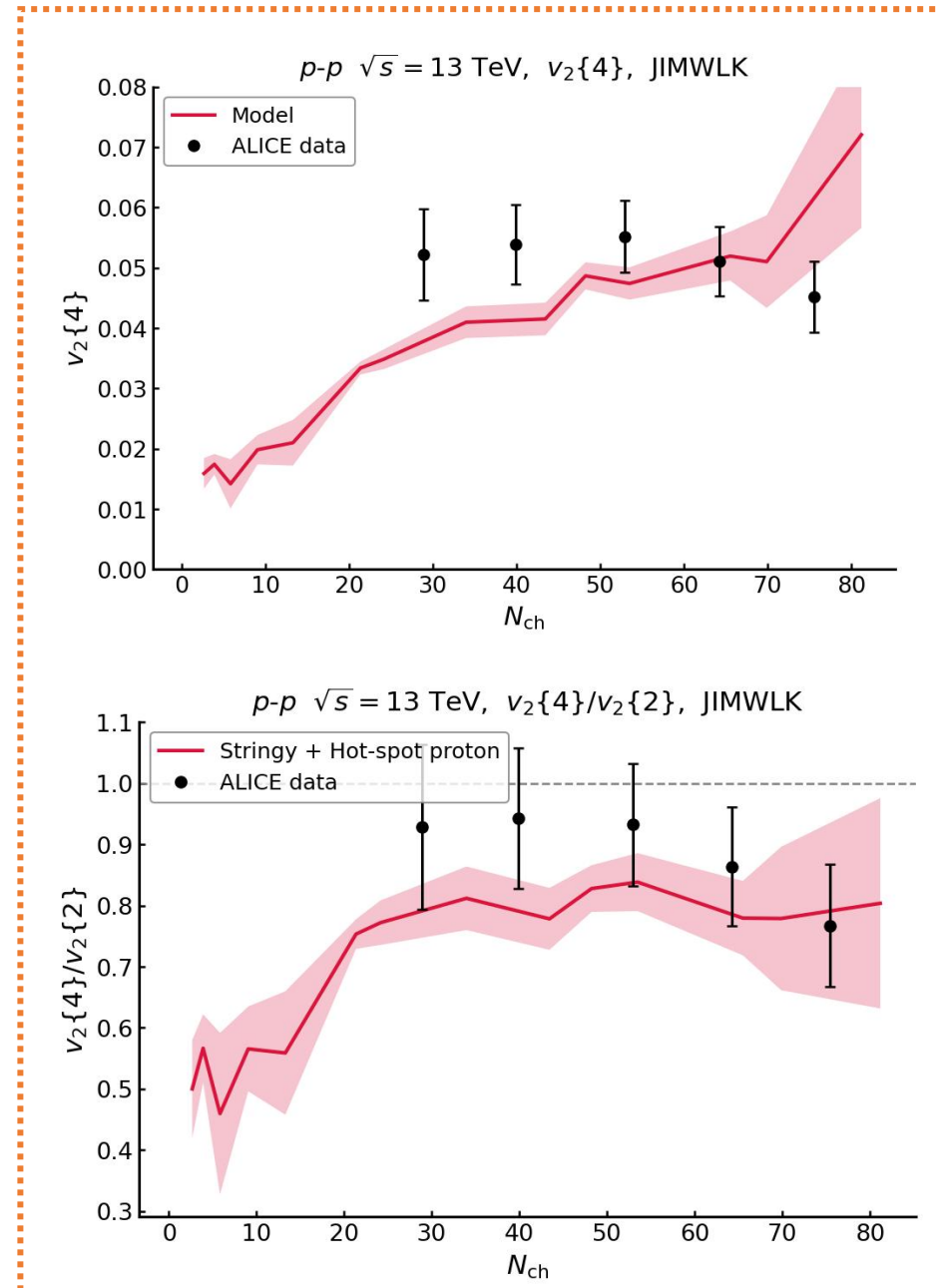
p-p collisions



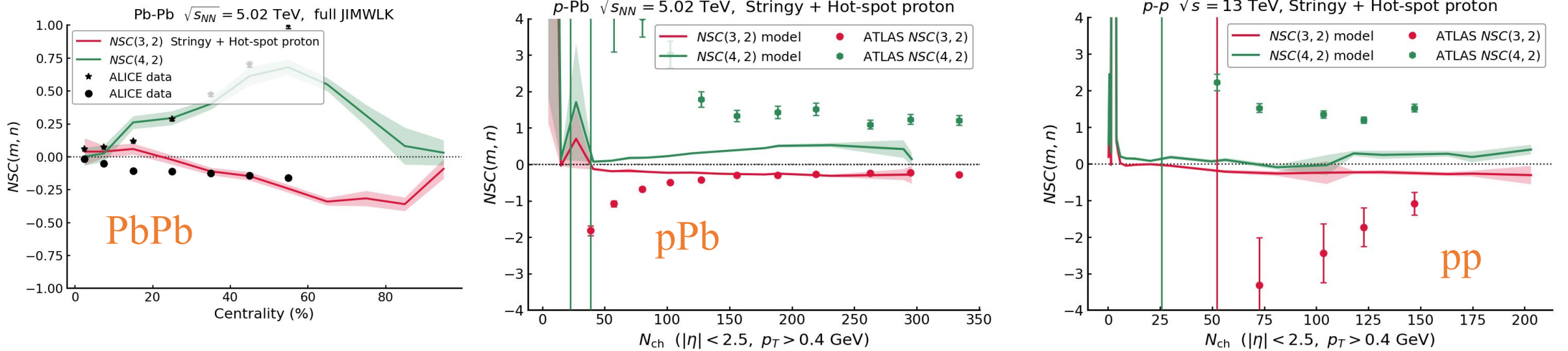
p-p collisions



- **Real $v_2\{4\}$** in p-p from hydro simulations!



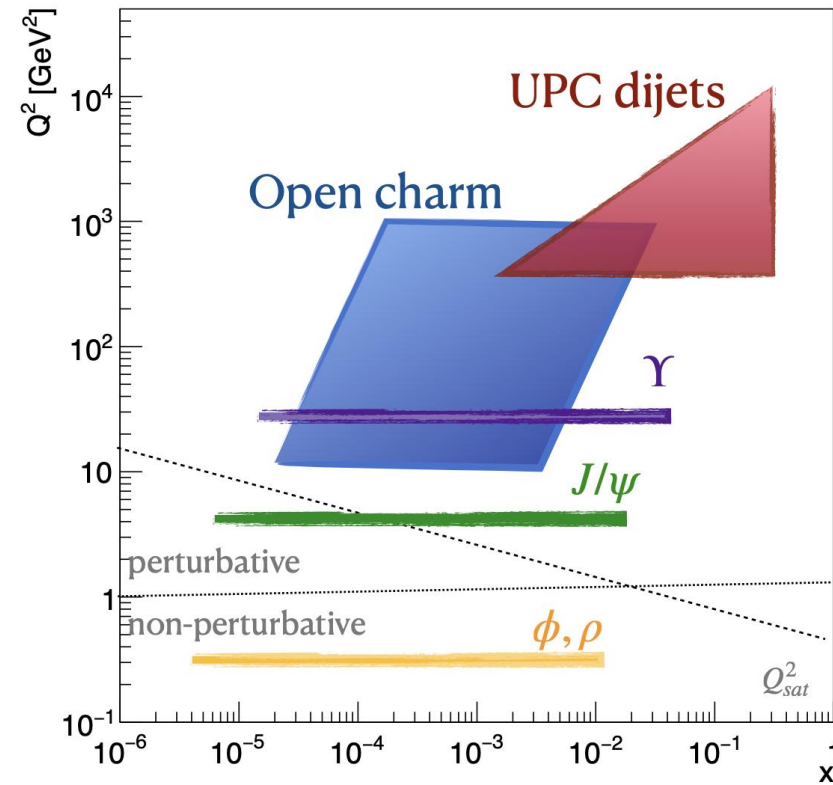
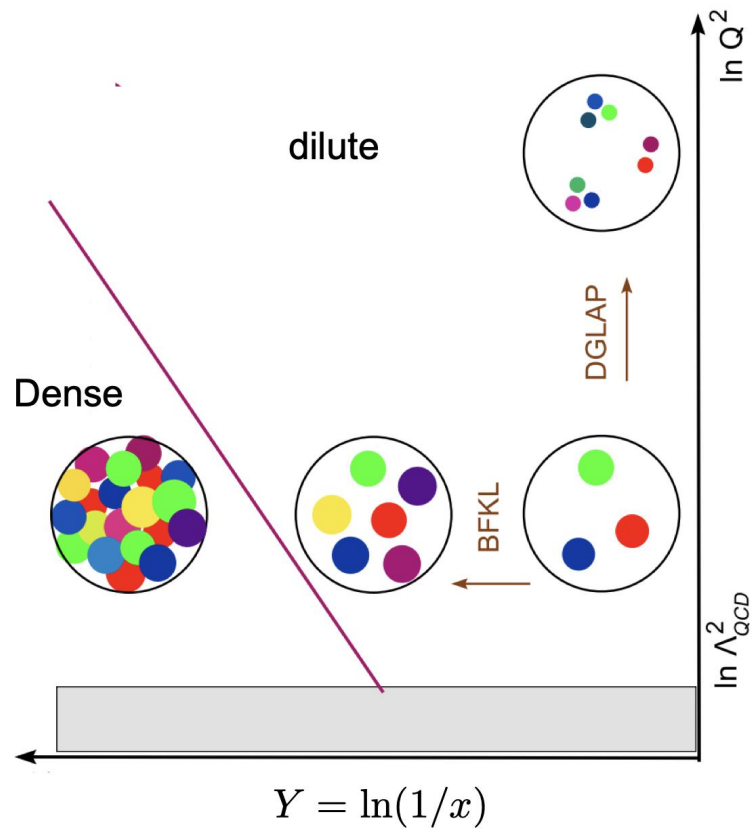
Normalized Symmetric Cumulant



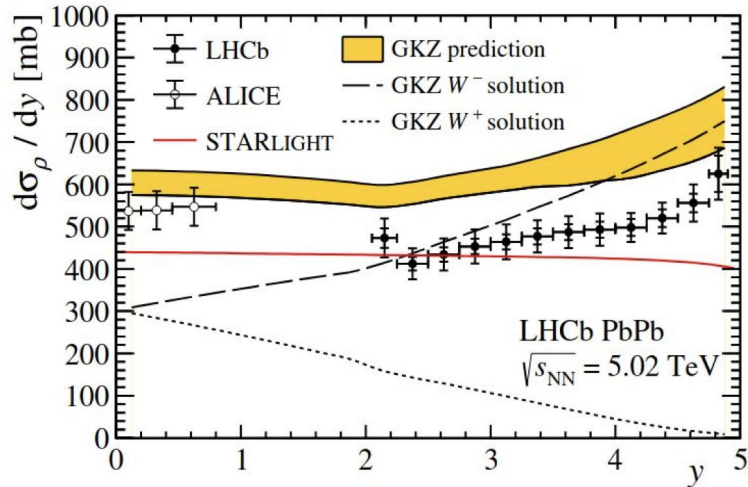
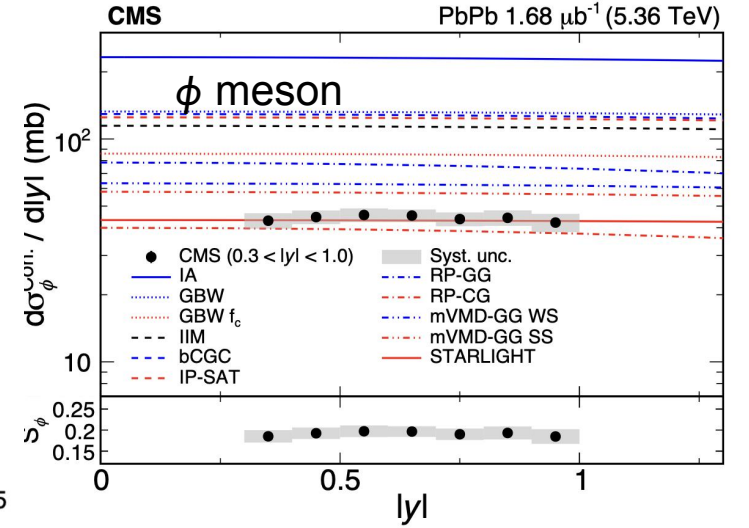
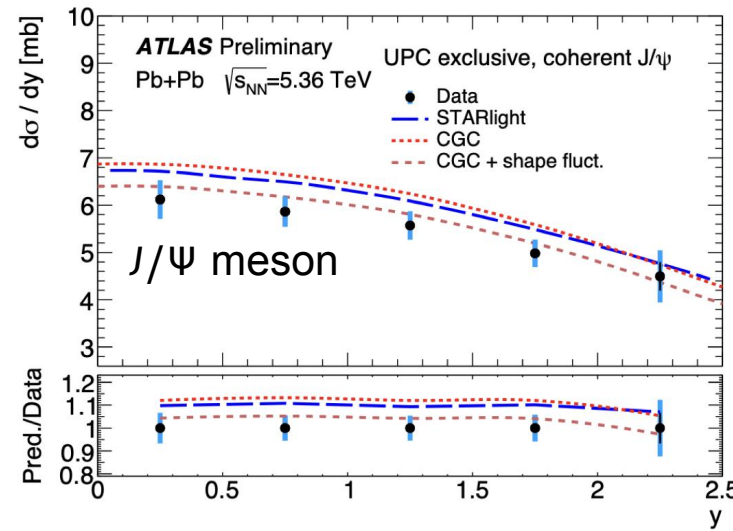
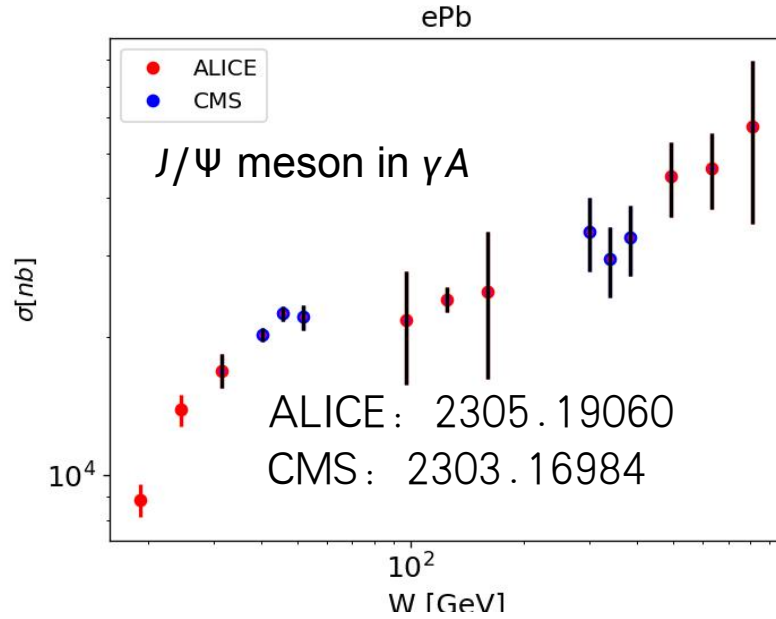
$$NSC^v(m, n) = \frac{SC^v(m, n)}{\langle v_m^2 \rangle \langle v_n^2 \rangle} = \frac{\langle v_m^2 v_n^2 \rangle - \langle v_m^2 \rangle \langle v_n^2 \rangle}{\langle v_m^2 \rangle \langle v_n^2 \rangle}$$

- **Correct sign** of the NSC(4,2) and NSC(3,2) in PbPb, pPb, and **in pp** from hydro simulations.
- If correlations are caused by long-range collective correlations, then **$|NSC(4,2)| < 1$** and **$|NSC(3,2)| < 1$** should hold.

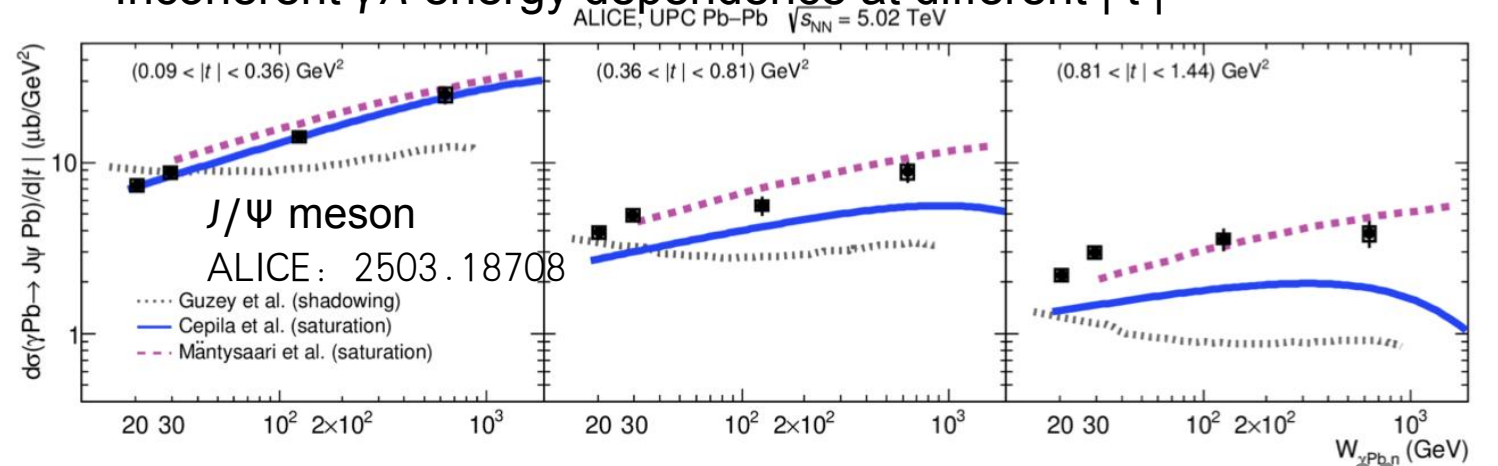
Probing gluon saturations in UPC



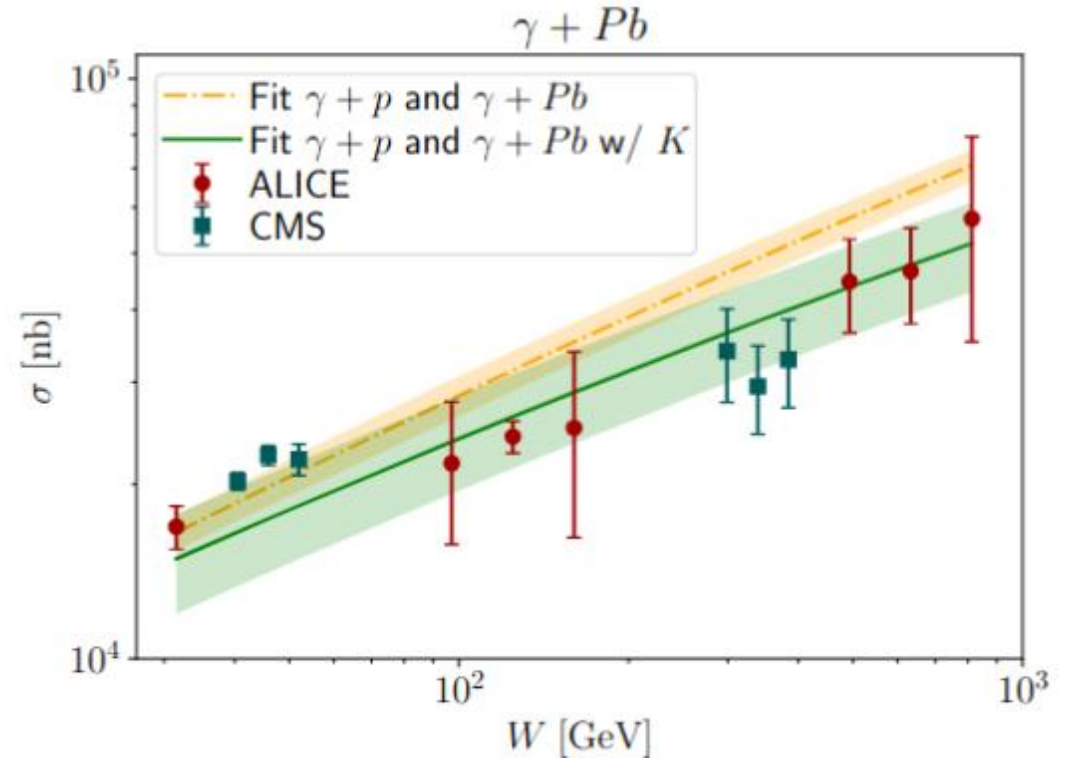
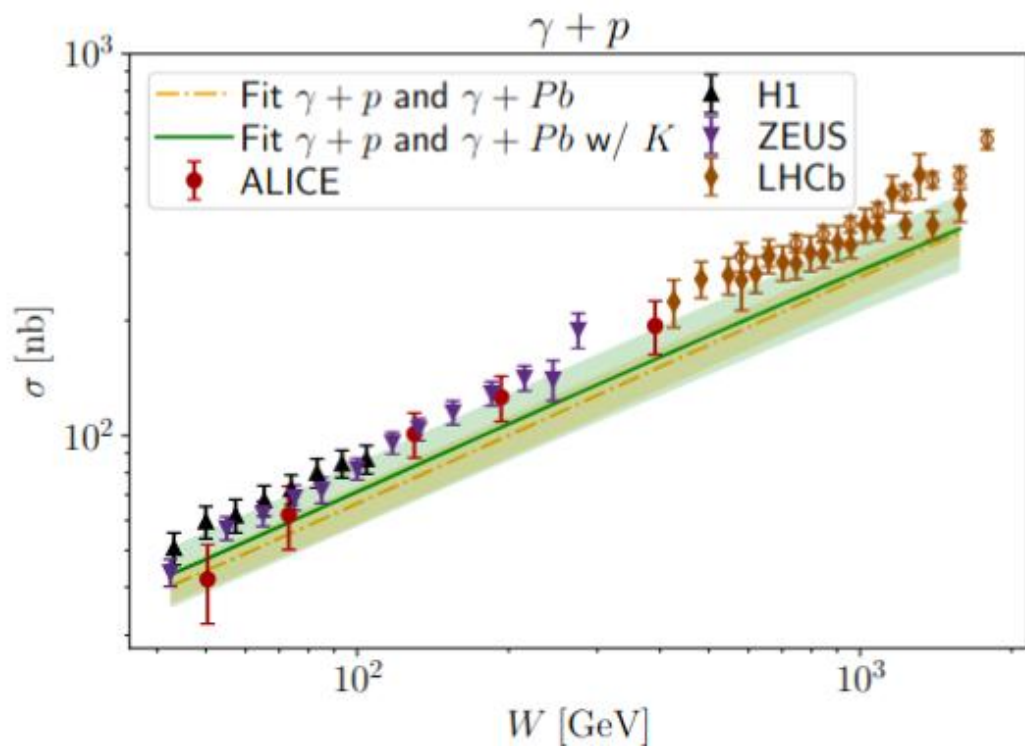
Wealth of vector meson productions in UPCs



- Incoherent γA energy dependence at different $|t|$



Global Bayesian analysis of J/ψ photoproduction on proton and Pb



H. Mantysaari, H. Roch, F. Salazar, B. Schenke, C. Shen and W. Zhao, Phys. Rev. D 113 (2026), 014038.

- CGC model has **tension** to fit the γp and γPb data simultaneously. (See also: J. Penttala and C. Royon, PLB. 864, 139394 (2025).)
- $K \sim 0.3$ here for the green lines.

Corrections for Electromagnetic Ion Dissociation (EMD) in UPC

A First Account of the Impact of Ion Electromagnetic Dissociation on Event Exclusivity in Ultraperipheral LHC Collisions

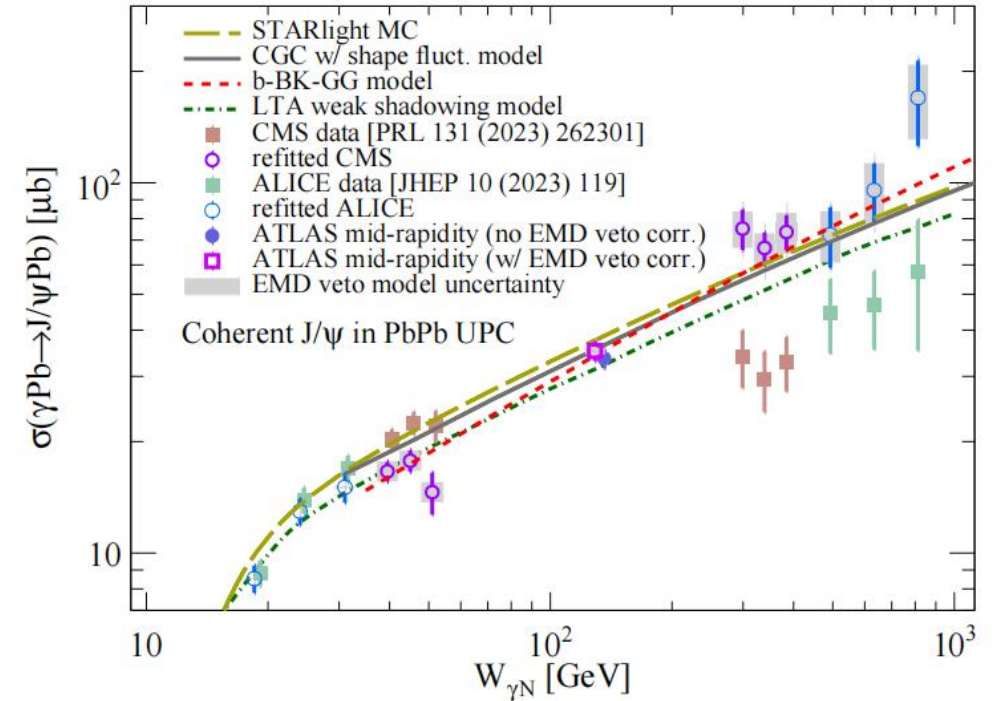
M. Dyndal*

AGH University of Krakow, Faculty of Physics and Applied Computer Science, al. Mickiewicza 30, 30-059 Krakow, PL

L. A. Harland-Lang†

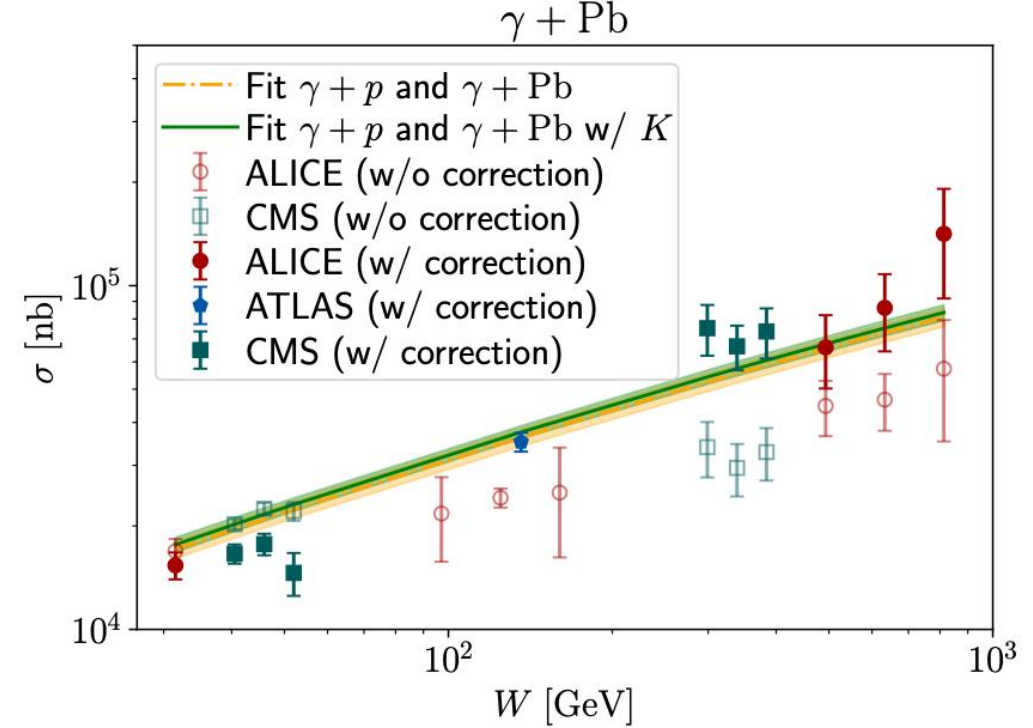
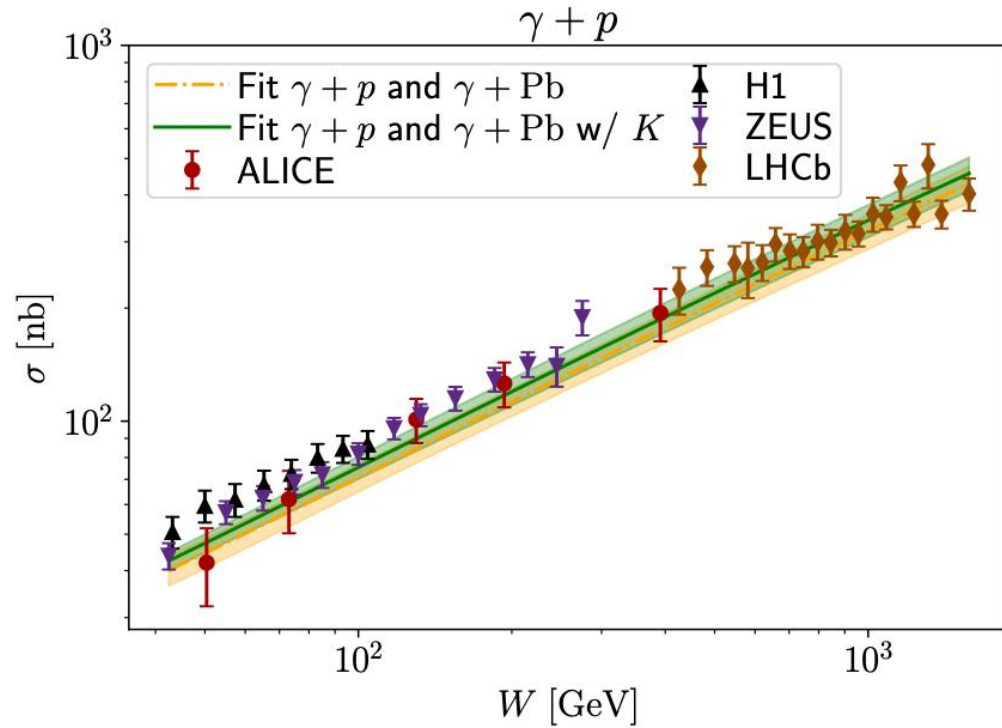
Department of Physics and Astronomy, University College London, London, WC1E 6BT, UK

[M. Dyndal and L. A. Harland-Lang, [arXiv:2604.19879]].



- EMD occurs when photon excites the ion, which de-excites by emitting particles.
- It usually forward neutrons, but at high photon energies it produces mid-rapidity hadrons.
- It can trigger the experimental exclusivity veto and reduce the J/ψ photoproduction.

Revisiting the EMD-corrected J/ψ Production

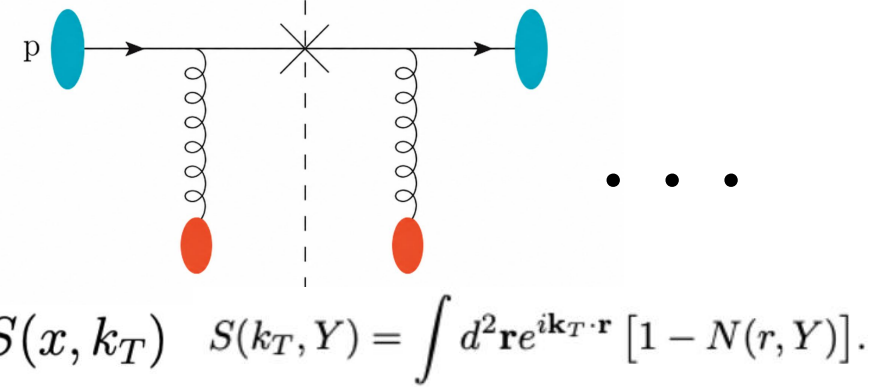
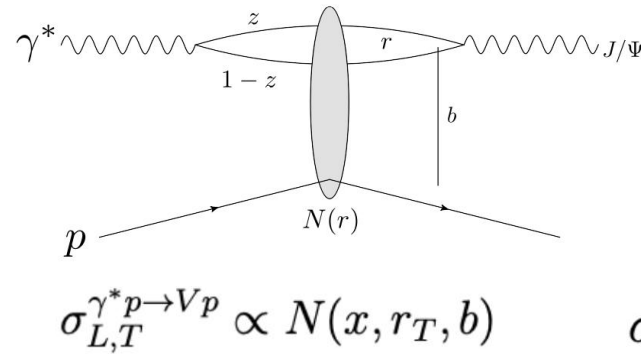
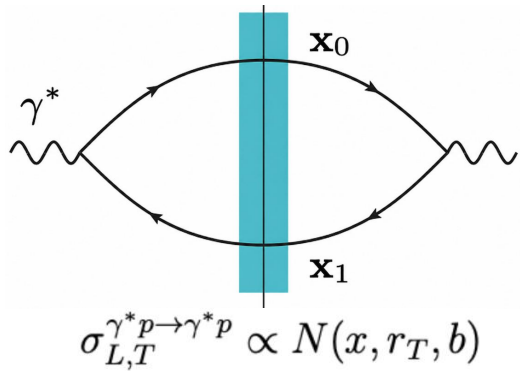


H. Mantysaari, H. Roch, B. Schenke, C. Shen and W. Zhao, arXiv:2606.20362.

- The **tension** between the CGC model and the simultaneous description of the γp and EMC-corrected γPb data has **disappeared**.
- $K \sim 0.94$ here for the green lines.

Global Extraction of the Universal Dipole Amplitude from an **Unbiased Initial Condition**

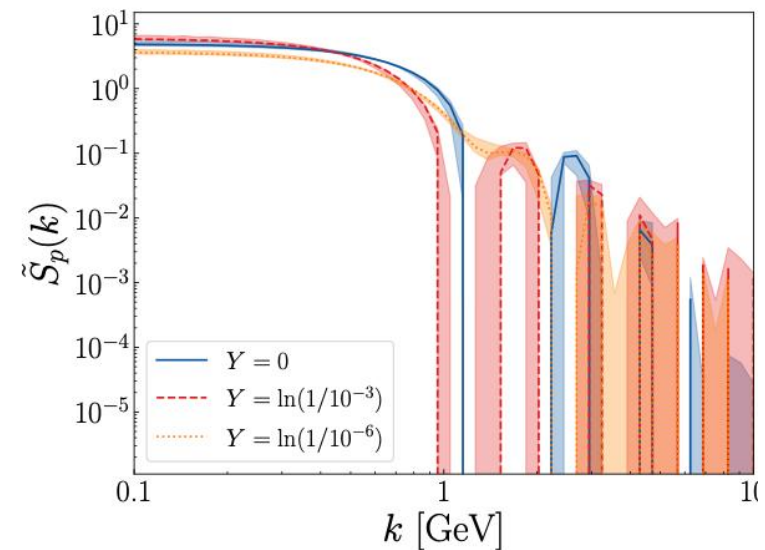
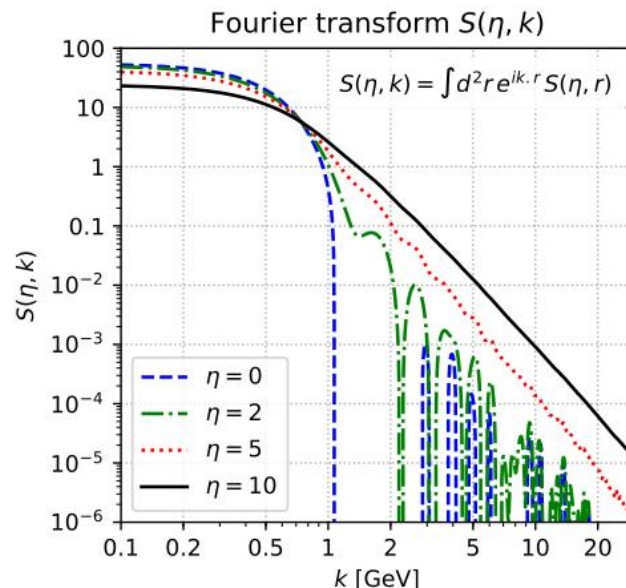
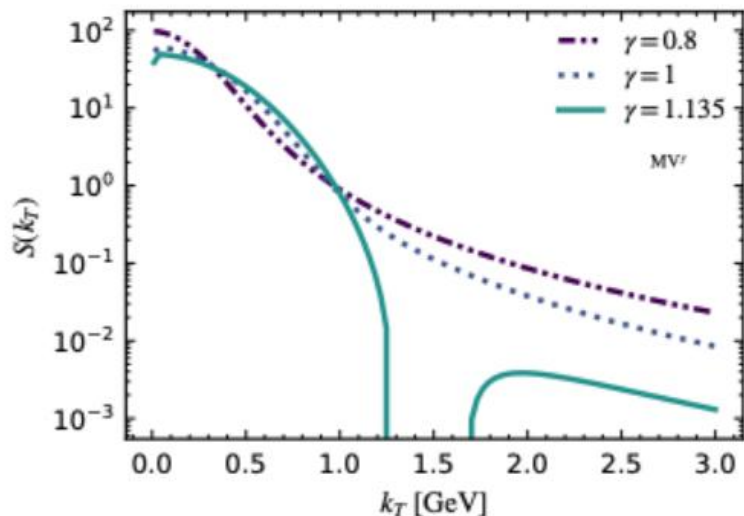
Universal Dipole Amplitude



$$\frac{d\sigma^{pA \rightarrow hX}}{d^2 p_{\perp} dy} = \frac{1}{(2\pi)^2} \int_{x_F}^1 \frac{dz}{z^2} \left[\sum_q x_1 q(x_1, \mu^2) \tilde{S}_F\left(\frac{p_{\perp}}{z}, x_2\right) D_{h/q}(z, \mu^2) \right. \\ \left. + x_1 g(x_1, \mu^2) \tilde{S}_A\left(\frac{p_{\perp}}{z}, x_2\right) D_{h/g}(z, \mu^2) \right]$$

- The small-x dipole amplitude is **universal** across several processes.
- The dipole amplitude should be **positive** in both coordinate and momentum space.

Problem for ~ 20 Years



$$S(k_T, Y) = \int d^2\mathbf{r} e^{i\mathbf{k}_T \cdot \mathbf{r}} [1 - N(r, Y)].$$

- Using MV-type parametrization, no one can fit the ep data while keeping the $S(k_T)$ positive.

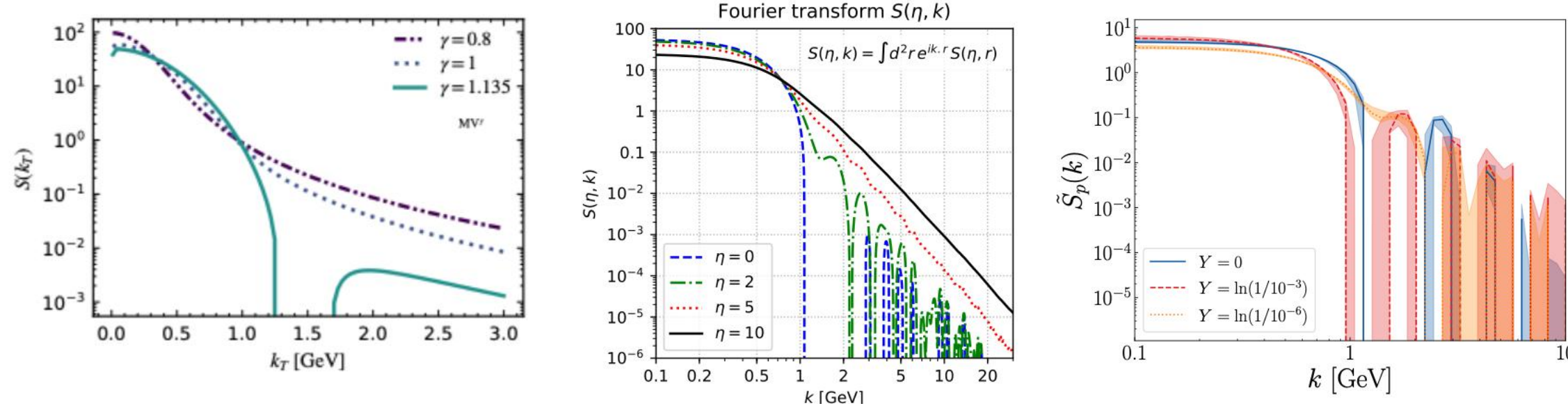
AAMQS: EPJC, 771 (2011), 1705;

B. Duclouw, E. Iancu, G. Soyez and D. N. Triantafyllopoulos, PLB 803 (2020), 135305

C. Casuga, H. Hanninen and H. Mantysaari, PRD 112 (2025), 034003;

References	$\chi^2/\text{d.o.f.} (\sigma_r^{\text{total}})$	$\chi^2/\text{d.o.f.} (\sigma_r^{\text{cE}})$	$\chi^2/\text{d.o.f.} (J/\psi)$	$S(k_T) > 0?$	Universal $N?$
Albacete <i>et al.</i> [Albacete:2010sy] (LO BK + LO Impact Factor)	~ 1.1	~ 1.3	N/A	No	No
B. Duclouw <i>et al.</i> [Ducloue:2019jmy] (ciBK + LO Impact Factor)	~ 1.0	N/A	N/A	No	No
Casuga <i>et al.</i> [Casuga:2025etc] (KCBK + NLO Impact Factor, Bayesian)	~ 1.2	~ 2.7	N/A	No	Yes
Casuga <i>et al.</i> [Casuga:2026xxt] (NLO+NLL BK + NLO Impact Factor, Bayesian)	~ 1.2	~ 2.4	N/A	No	Yes
This work, without " $S(k_T) > 0$ " constraint (ciBK + LO Impact Factor, PINN)	0.868	1.160	0.691	No	Yes
This work, with "$S(k_T) > 0$" constraint (ciBK + LO Impact Factor, PINN)	1.48	1.56	1.13	Yes	Yes

Problem for ~ 20 Years



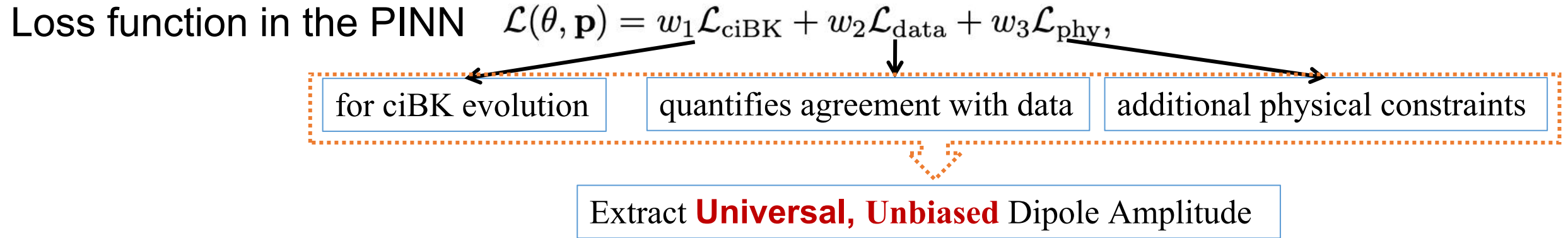
$$S(k_T, Y) = \int d^2 \mathbf{r} e^{i \mathbf{k}_T \cdot \mathbf{r}} [1 - N(r, Y)].$$

- Using MV-type parametrization, no one can fit the ep data while keeping the $S(k_T)$ positive.

AAMQS: EPJC, 771 (2011), 1705;
B. Duclouw, E. Iancu, G. Soyez and D. N. Triantafyllopoulos, PLB 803 (2020), 135305
C. Casuga, H. Hanninen and H. Mantysaari, PRD 112 (2025), 034003;

References	$\chi^2/\text{d.o.f. } (\sigma_r^{\text{total}})$	$\chi^2/\text{d.o.f. } (\sigma_r^{c\bar{e}})$	$\chi^2/\text{d.o.f. } (J/\psi)$	$S(k_T) > 0?$	Universal N ?
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This work, without “ $S(k_T) > 0$ ” constraint (ciBK + LO Impact Factor, PINN)	0.868	1.160	0.691	No	Yes
This work, with “ $S(k_T) > 0$ ” constraint (ciBK + LO Impact Factor, PINN)	1.48	1.56	1.13	Yes	Yes

Physics-Informed Global Extraction of the Universal Dipole Amplitude

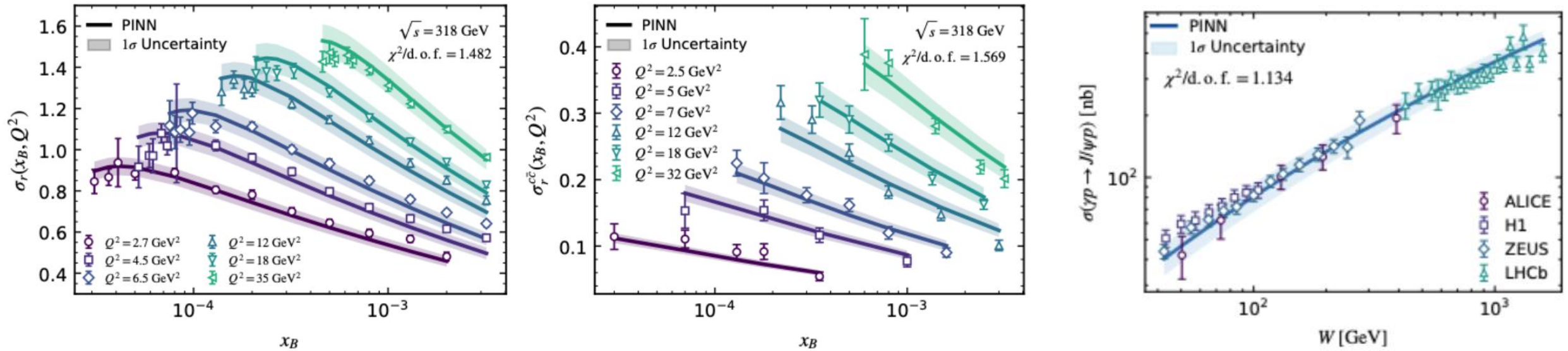


- PINN extracts an **universal** amplitude constrained by the **collinear improves BK**.
- **Without imposing** a priori MV-type parametrization of the initial condition.

S. W. Dai, F. P. Li, L. G. Pang, G. Y. Qin, S. Y. Wei, H. Z. Zhang and W. Zhao, arXiv:2603.08008.

The dipole amplitude is available: <https://doi.org/10.5281/zenodo.18826120>

Physics-Informed Global Extraction of the Universal Dipole Amplitude

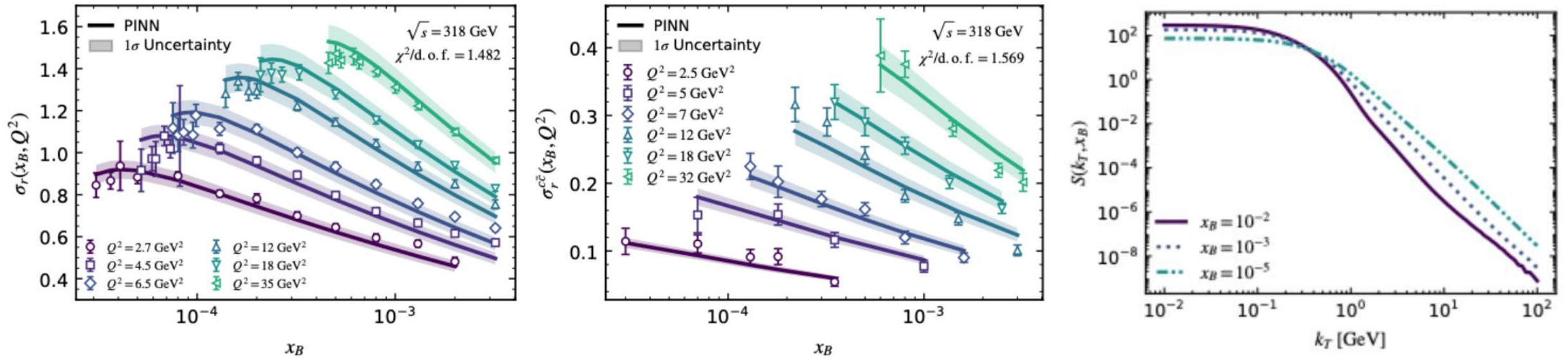


- PINN extracts an **universal** amplitude constrained by the **CiBK**.
- **Simultaneously** constrained by reduced **total** and **charm quark** DIS cross sections, exclusive **J/ψ data**.

S. W. Dai, F. P. Li, L. G. Pang, G. Y. Qin, S. Y. Wei, H. Z. Zhang and W. Zhao, arXiv:2603.08008.

The dipole amplitude is available: <https://doi.org/10.5281/zenodo.18826120>

Physics-Informed Global Extraction of the Universal Dipole Amplitude

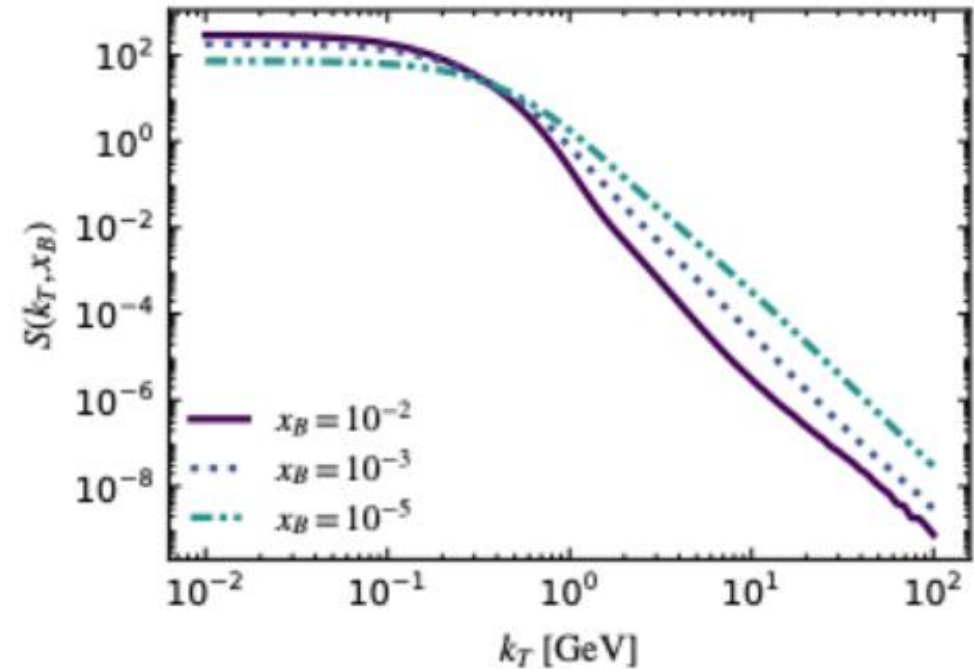
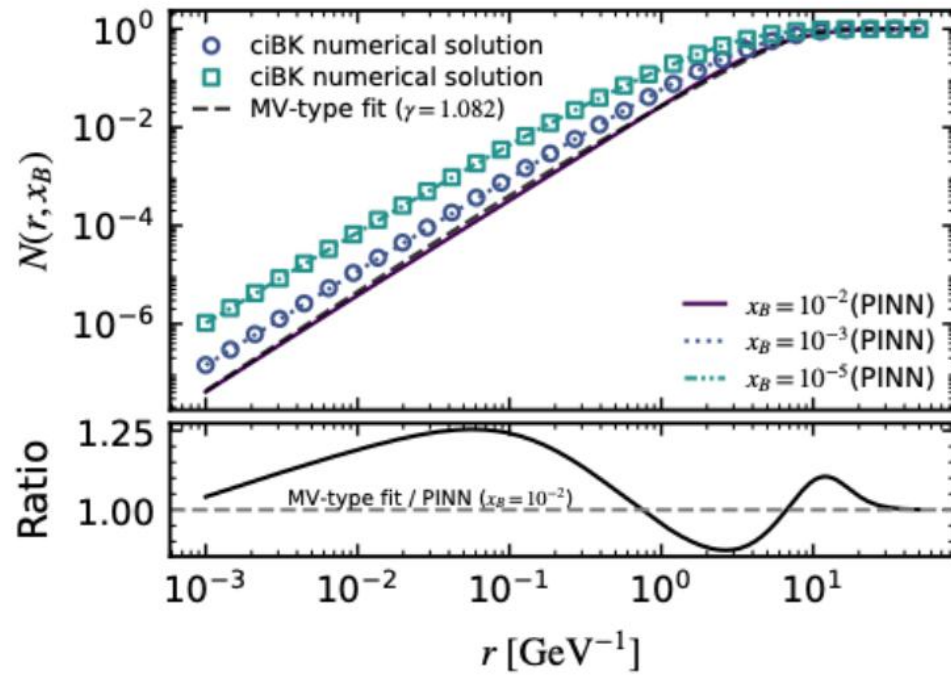


- PINN extracts an **universal** amplitude constrained by the **CiBK**.
- **Simultaneously** constrained by reduced **total** and **charm quark** DIS cross sections, exclusive **J/ ψ data**.
- Keep the **positivity for the momentum-space amplitude**.

S. W. Dai, F. P. Li, L. G. Pang, G. Y. Qin, S. Y. Wei, H. Z. Zhang and W. Zhao, arXiv:2603.08008.

The dipole amplitude is available: <https://doi.org/10.5281/zenodo.18826120>

Dipole Amplitude of Proton

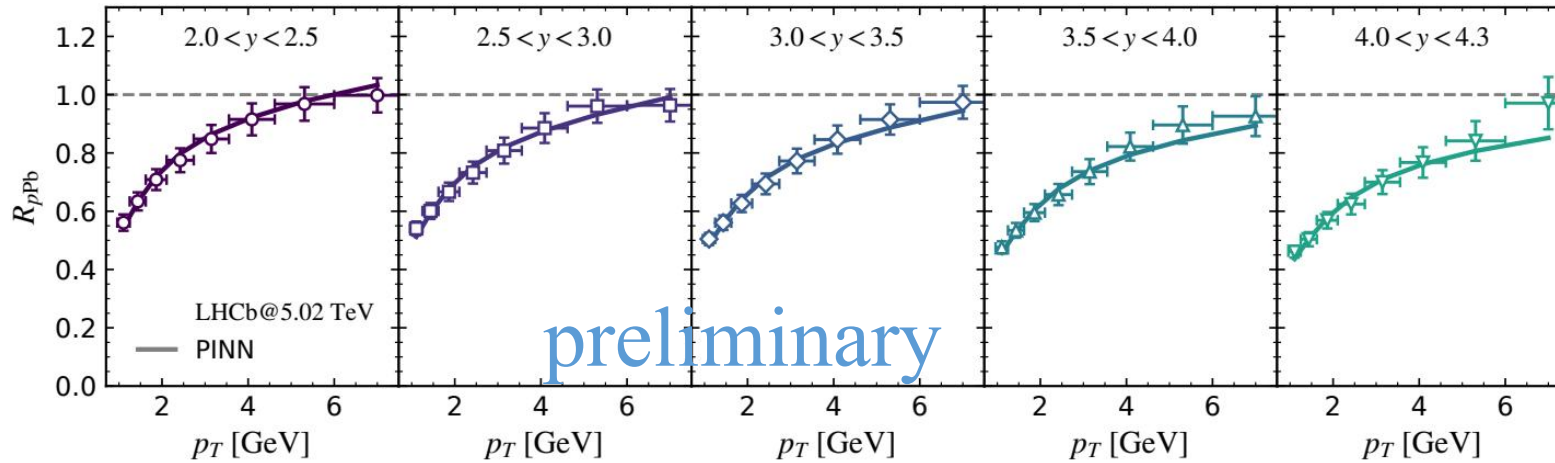


- To solve this problem, which has persisted for 20 years, we need to **go beyond** the MV parametrization.

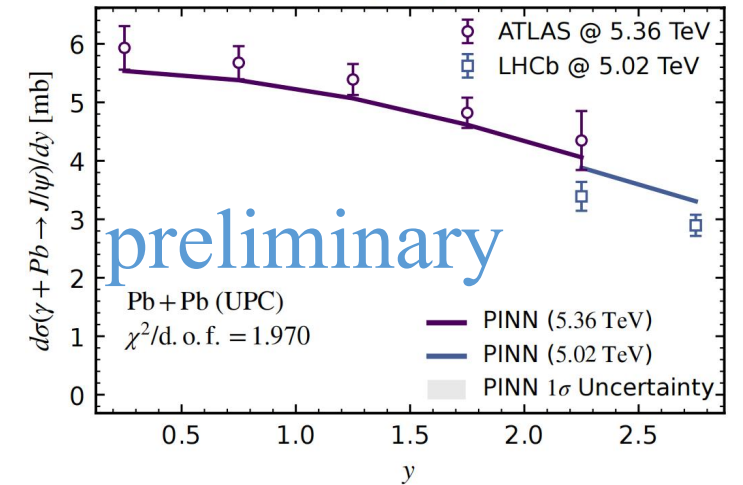
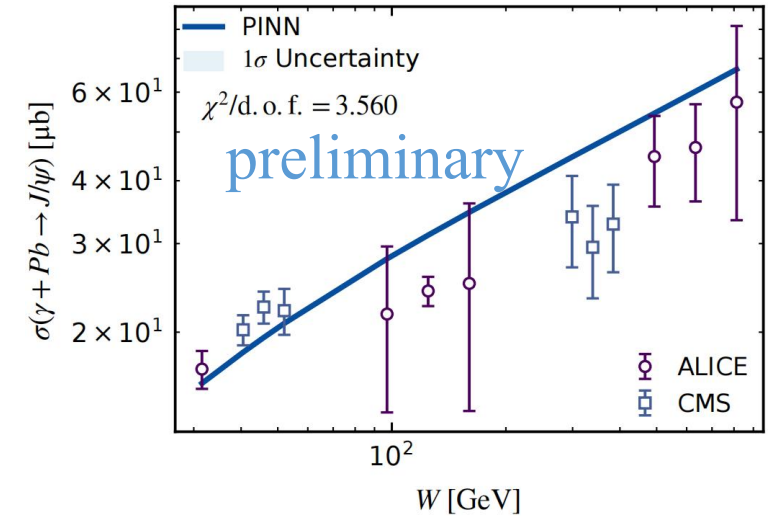
S. W. Dai, F. P. Li, L. G. Pang, G. Y. Qin, S. Y. Wei, H. Z. Zhang and W. Zhao, arXiv:2603.08008.

The dipole amplitude is available: <https://doi.org/10.5281/zenodo.18826120>

Global Extraction of the Nuclear Dipole Amplitude



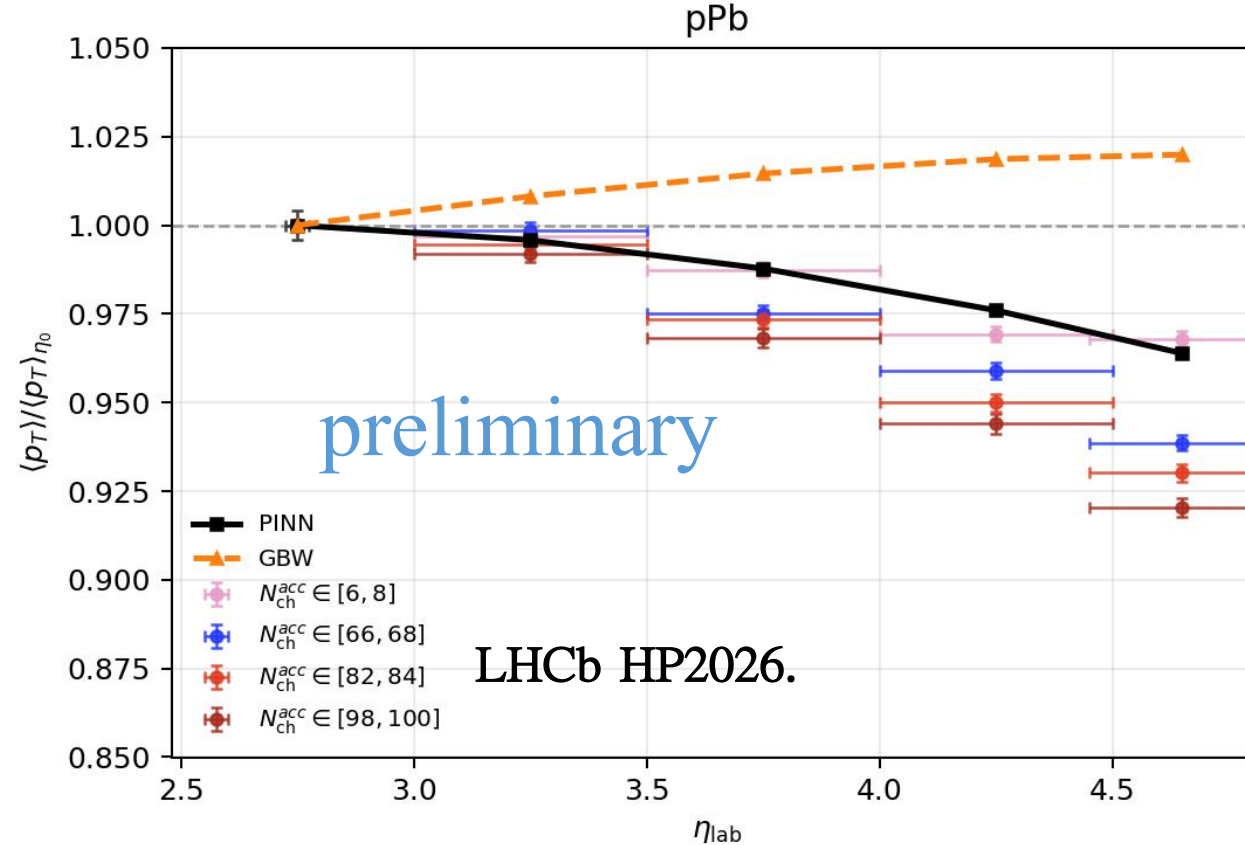
- RpPb greatly **suppresses the uncertainty** from the FF and PDF.
- Every parameter **plays two roles**.
- There is some **tension** between the RpPb and J/ψ data. (EMD correction for J/ψ data?)



S. W. Dai, F. P. Li, L. G. Pang, G. Y. Qin, S. Y. Wei, H. Z. Zhang and W. Zhao, arXiv:2603.08008 and in progress.

The dipole amplitude is available: <https://doi.org/10.5281/zenodo.18826120>

Mean p_T ratio v.s. η

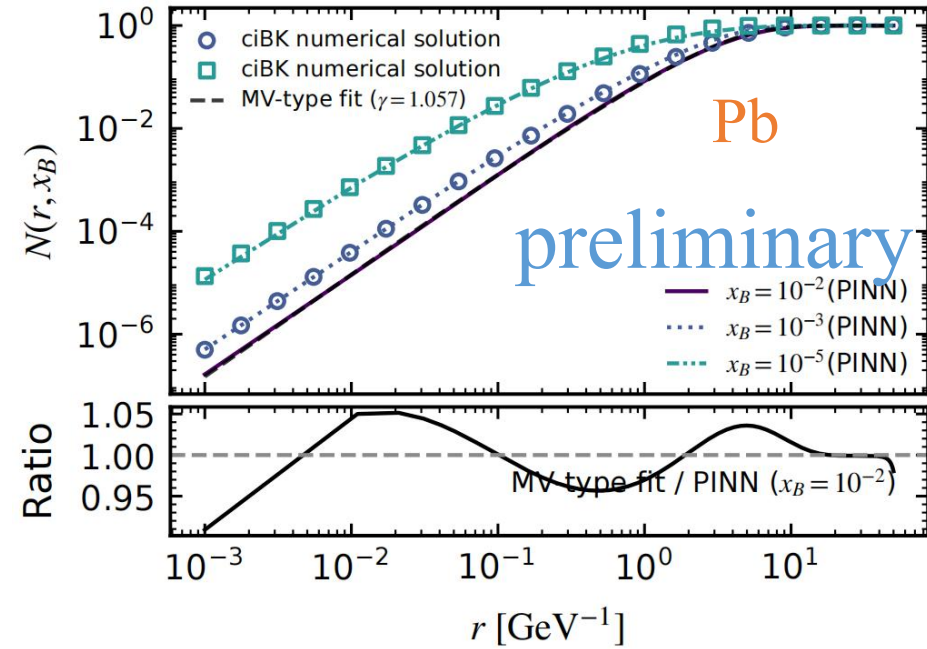
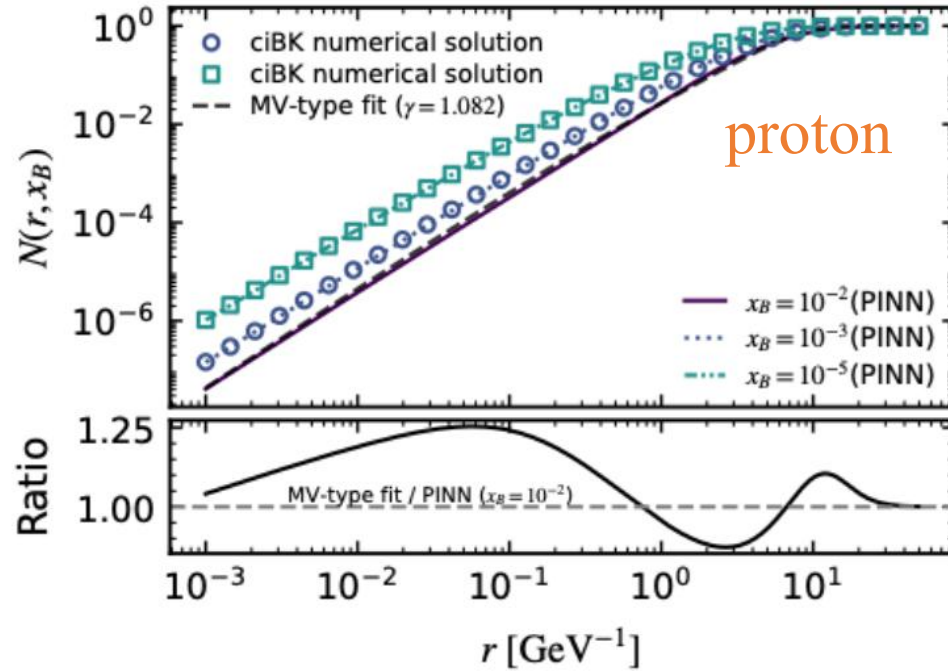


- Our CGC calculation of Mean p_T ratio v.s. η is **consistent** with the LHCb measurements at low Nch.
- In pPb, high Nch implies hydrodynamic behavior, while **low Nch results in CGC dominance**.

S. W. Dai, F. P. Li, L. G. Pang, G. Y. Qin, S. Y. Wei, H. Z. Zhang and W. Zhao, arXiv:2603.08008 and in progress.

The dipole amplitude is available: <https://doi.org/10.5281/zenodo.18826120>

Dipole Amplitude of Pb

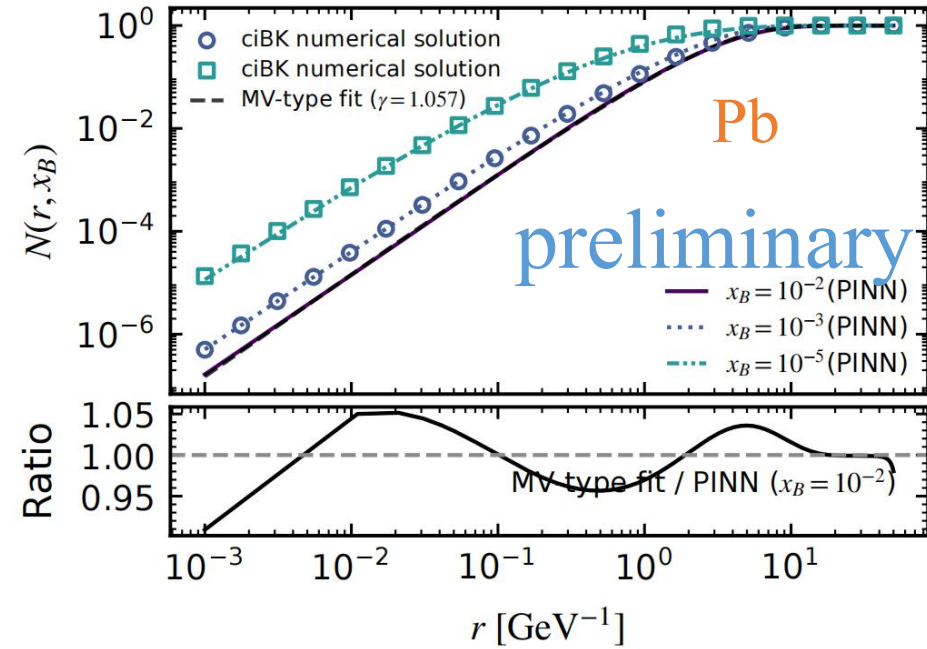
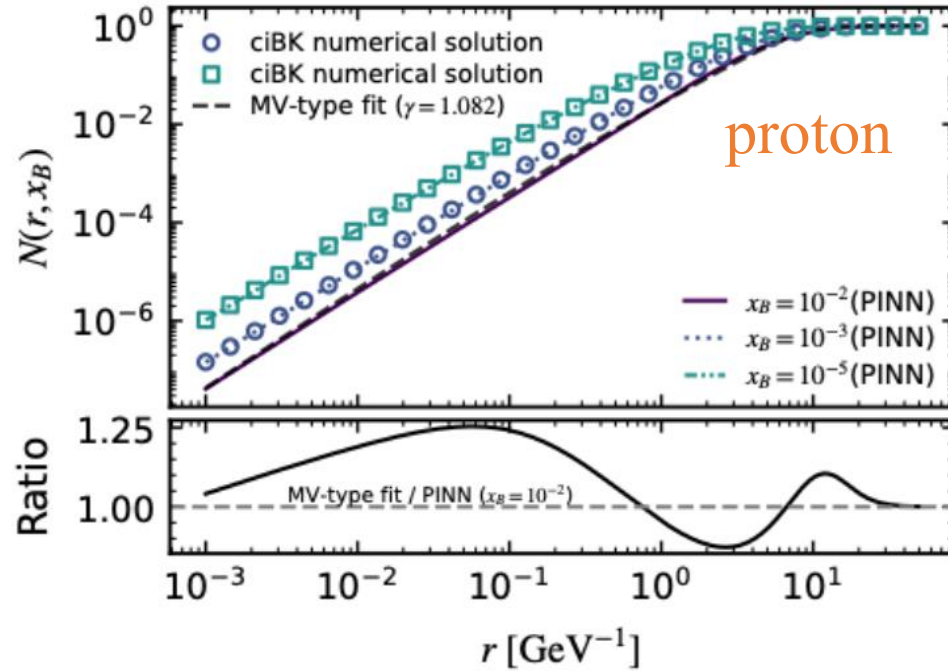


- The MV-type fit works better for Pb than for proton. (**MV model is designed for large nuclei.**)

S. W. Dai, F. P. Li, L. G. Pang, G. Y. Qin, S. Y. Wei, H. Z. Zhang and W. Zhao, arXiv:2603.08008 and in progress.

The dipole amplitude is available: <https://doi.org/10.5281/zenodo.18826120>

Dipole Amplitude of Pb



- The MV-type fit works better for Pb than for proton. (**MV model is designed for large nuclei.**)
- From the **unbiased** global fit, we obtain a ratio of $\frac{Q_{s0,Pb}^2}{Q_{s0,p}^2} \sim 3.1$.

S. W. Dai, F. P. Li, L. G. Pang, G. Y. Qin, S. Y. Wei, H. Z. Zhang and W. Zhao, arXiv:2603.08008 and in progress.

The dipole amplitude is available: <https://doi.org/10.5281/zenodo.18826120>

Summary

- A comprehensive analysis of UPC/DIS and heavy-ion collision data across various energies will provide a precise understanding of **gluon saturation**, the **initial conditions** of heavy-ion collisions, and the **QGP properties**.
- The neural network method offers a novel approach to solving problems in the small-x area.
- From the **unbiased** global fit, we obtain a ratio: $\frac{Q_{s0,Pb}^2}{Q_{s0,p}^2} \sim 3.1$.

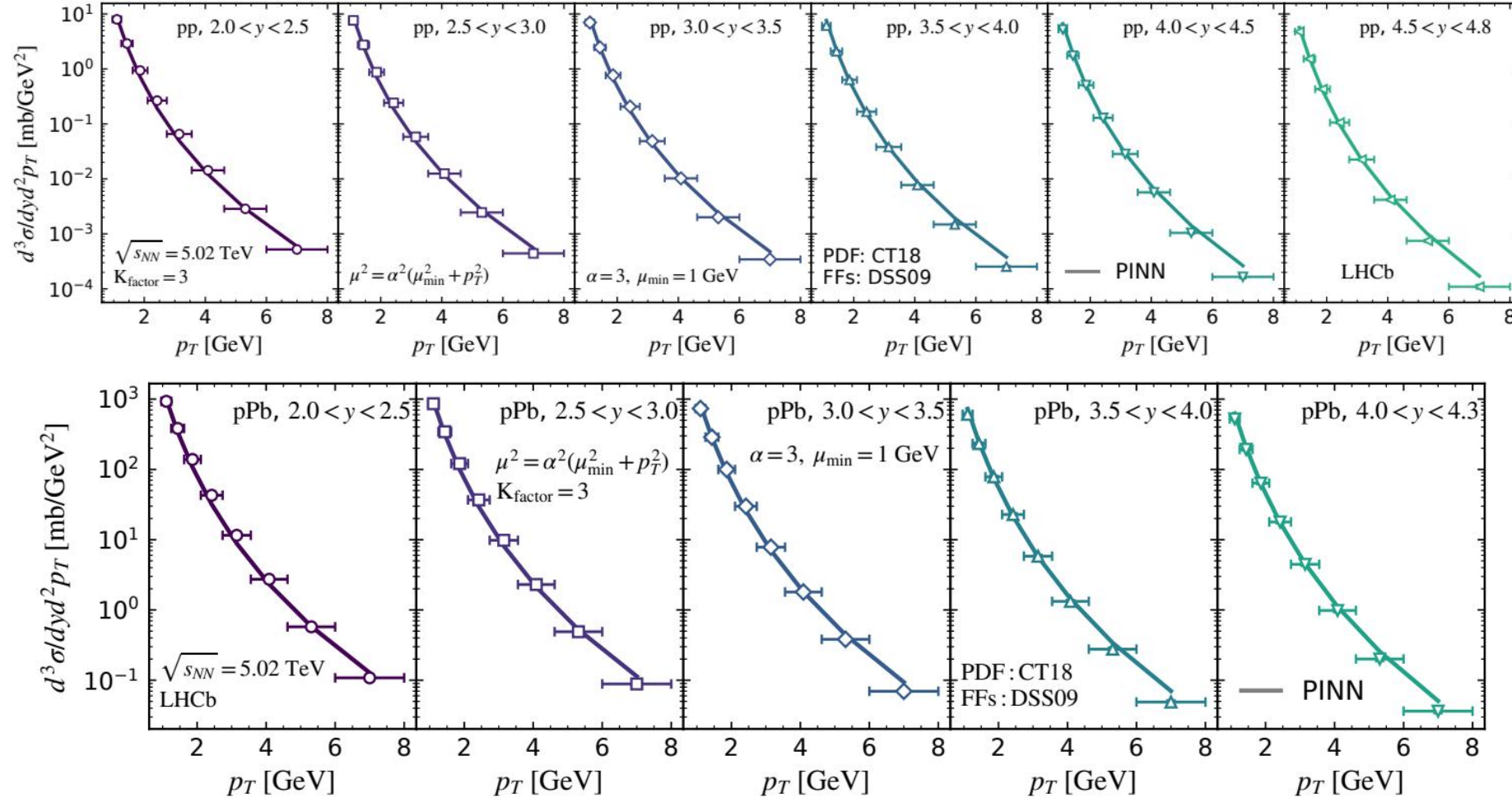
(The dipole amplitude is available: <https://doi.org/10.5281/zenodo.18826120>)

Thanks for Your attentions.

Back Up

Back Up

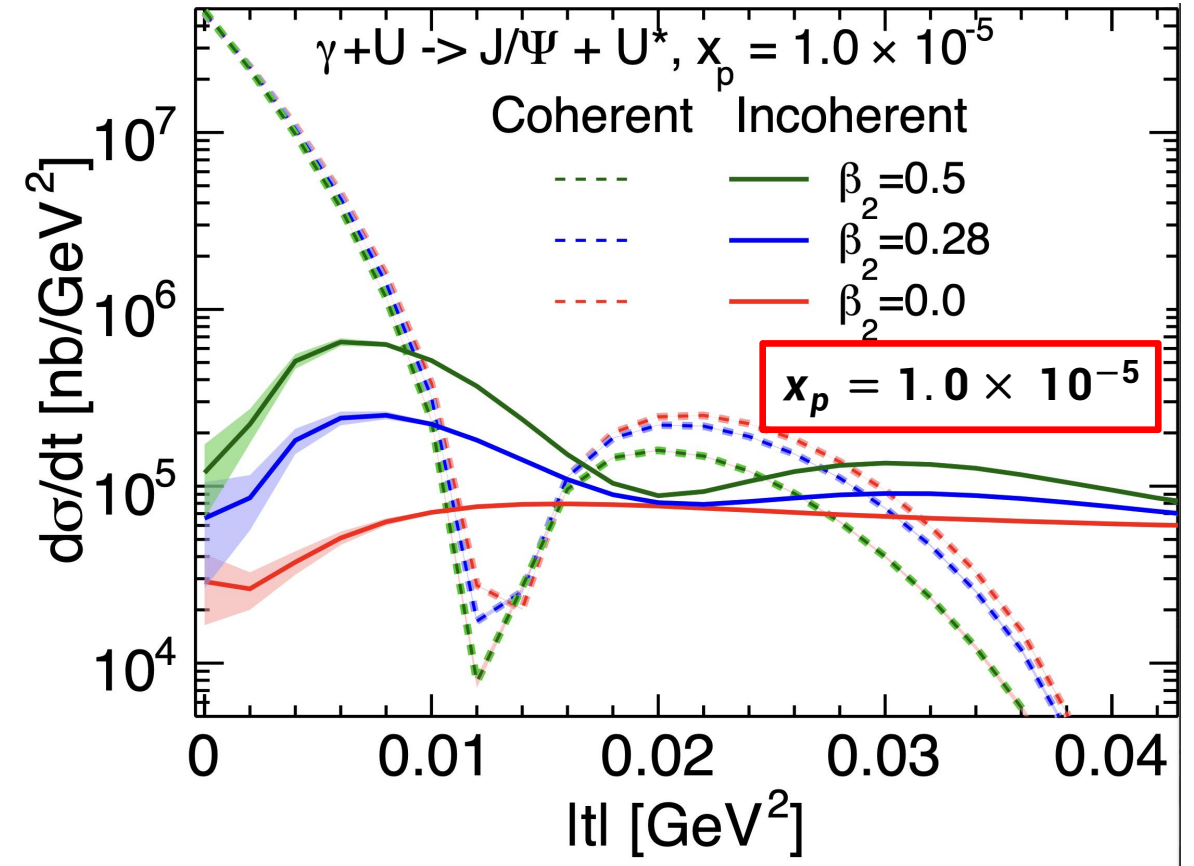
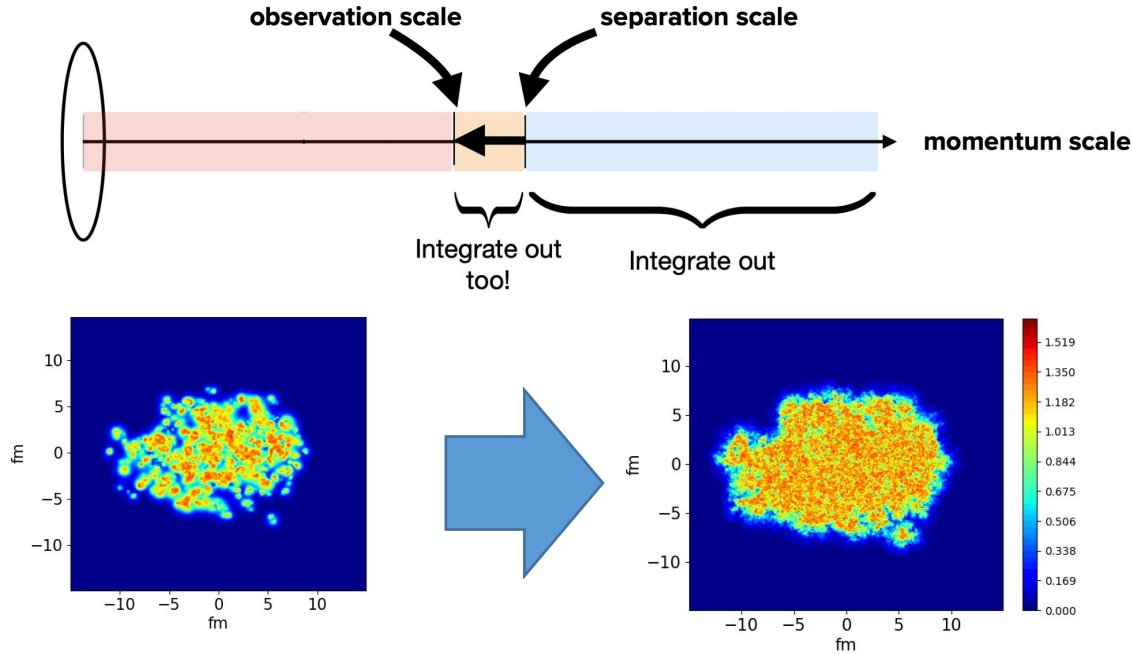
dN/dpT for pp and pPb



S. W. Dai, F. P. Li, L. G. Pang, G. Y. Qin, S. Y. Wei, H. Z. Zhang and W. Zhao, arXiv:2603.08008 and in progress.

The dipole amplitude is available: <https://doi.org/10.5281/zenodo.18826120>

Energy evolution to smaller x



- Energy evolution **doesn't wash out** these effects.

H. Mantysaari, B. Schenke, C. Shen and W. Zhao PhysRevLett.131.062301.

H. Mantysaari, B. Schenke PRD, 98, 034013.

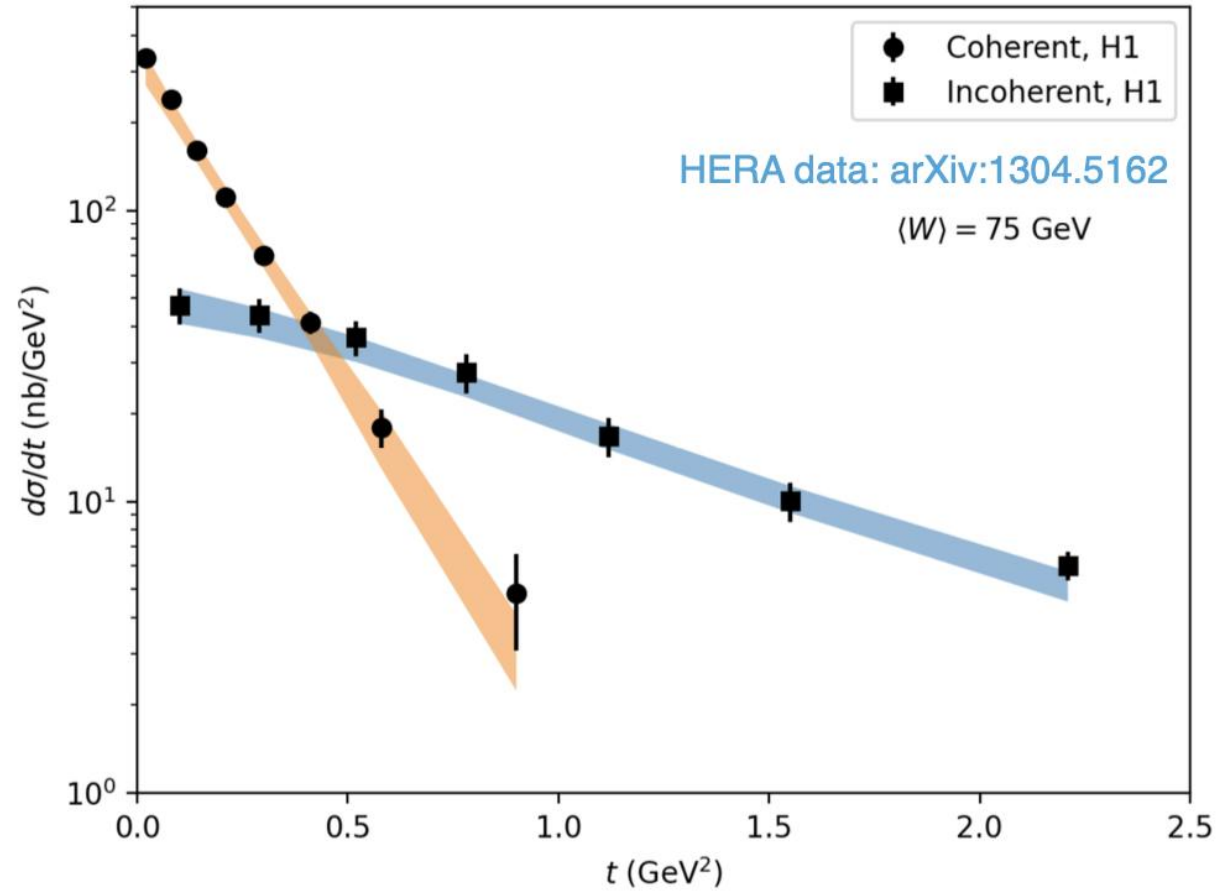
T. Lappi and H. Mantysaari, EPJC 73, 2307 (2013).

Yuri V. Kovchegov, QUANTUM CHROMODYNAMICS AT HIGH ENERGY

Model parameters and the Exp. Data ($\gamma^* + p \rightarrow J/\psi + p^*$)

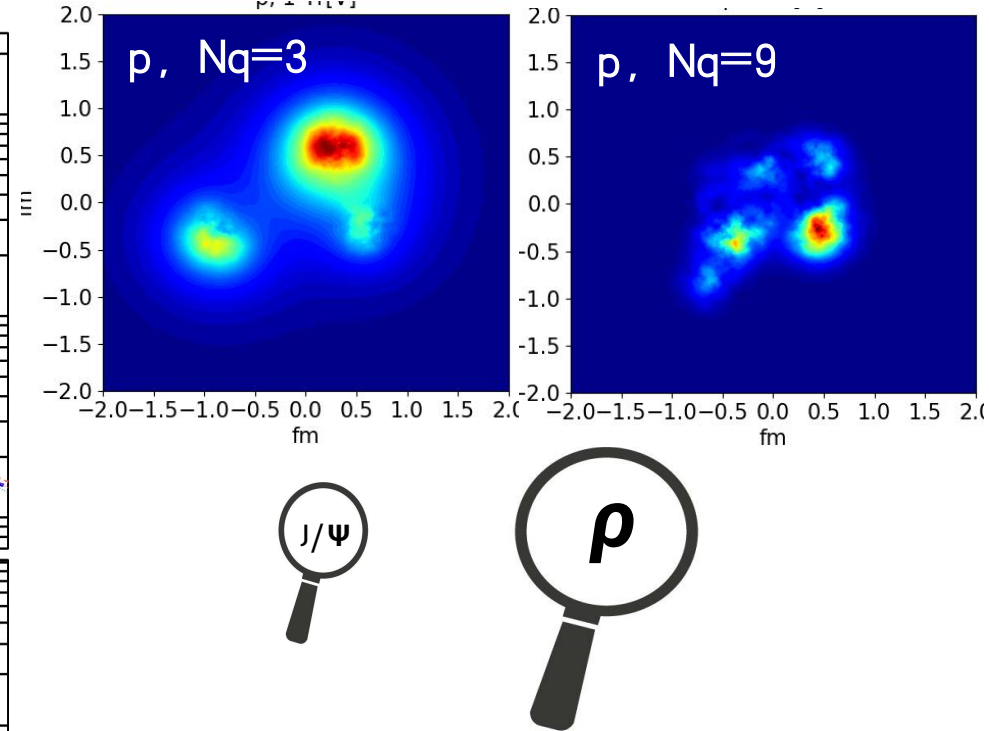
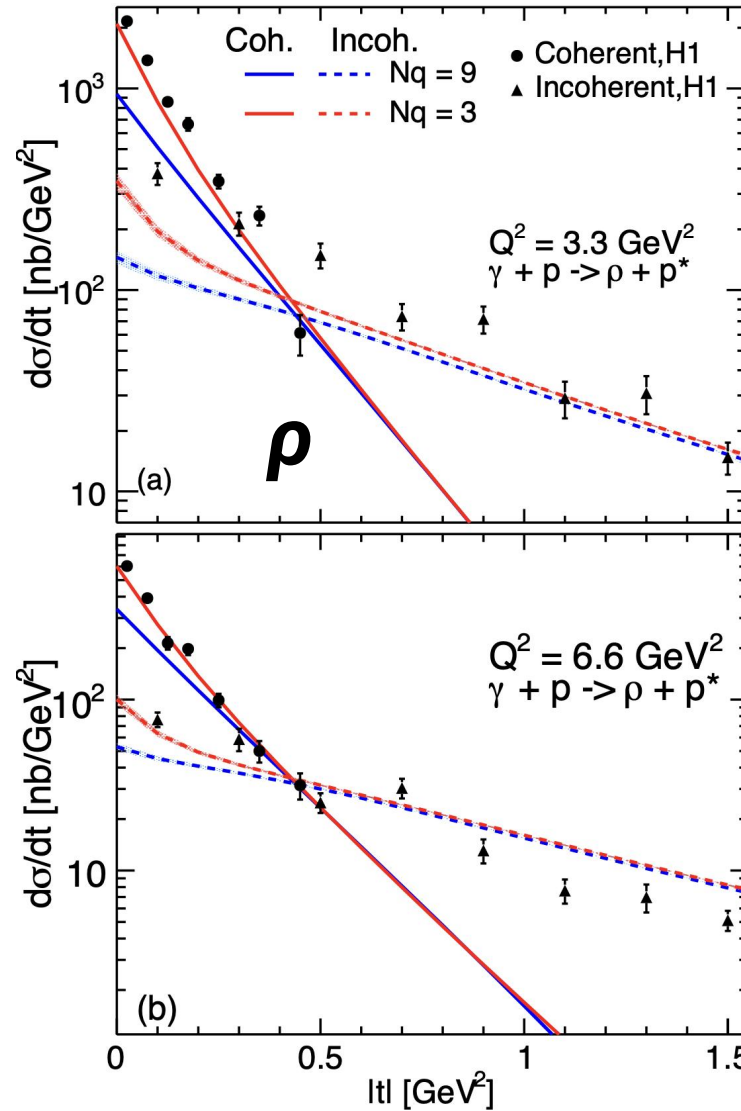
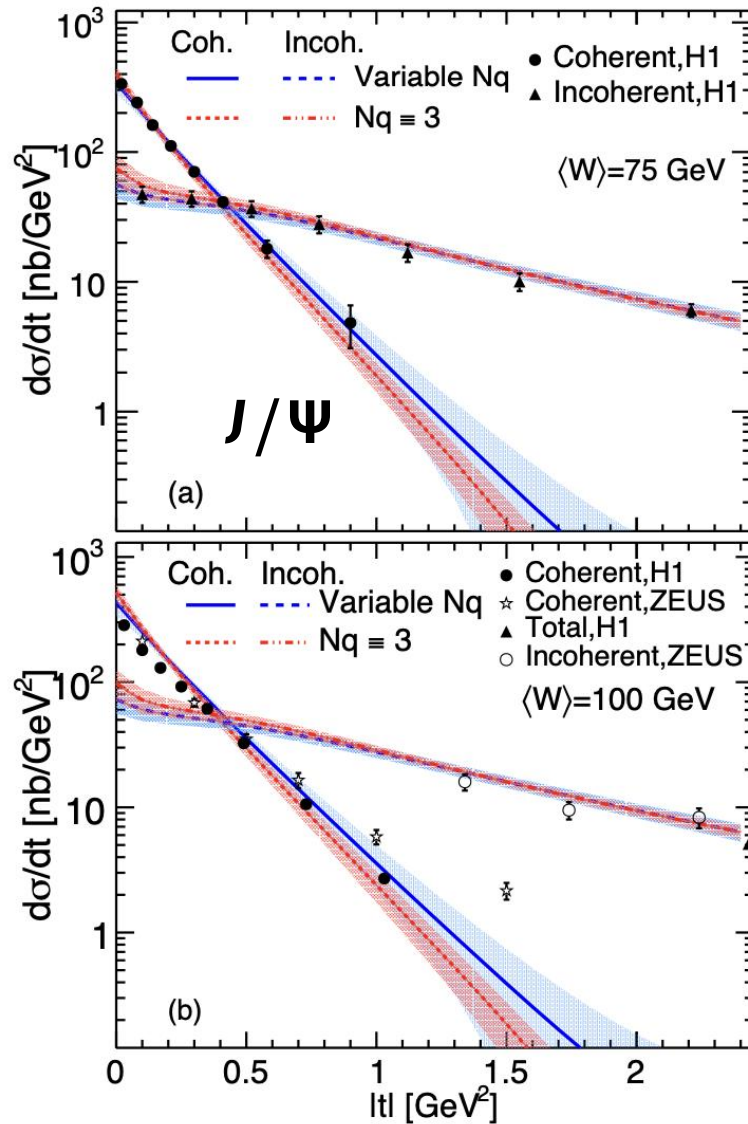
Parameterize proton shape (T_p)

- Number of hot spots N_q
- Proton size B_{qc}
- Hot spot size B_q
- Hot spot density fluctuations σ
- Min. distance between hot spots $d_{q,min}$
- Overall color charge density: $Qs(x)/g^2\mu$
- Infrared regulator m



- 7D parameter space; generated 1000 training points for the model emulator

Probing nucleon at different resolutions



- The ρ mesons probe proton fluctuations at large length scales.
- Sizeable differences observed for ρ productions between $Nq=3$ and $Nq=9$ MAPs.