



Careless whispers:

A population of sub-threshold post-merger gravitational waves constrains the hot nuclear equation of state

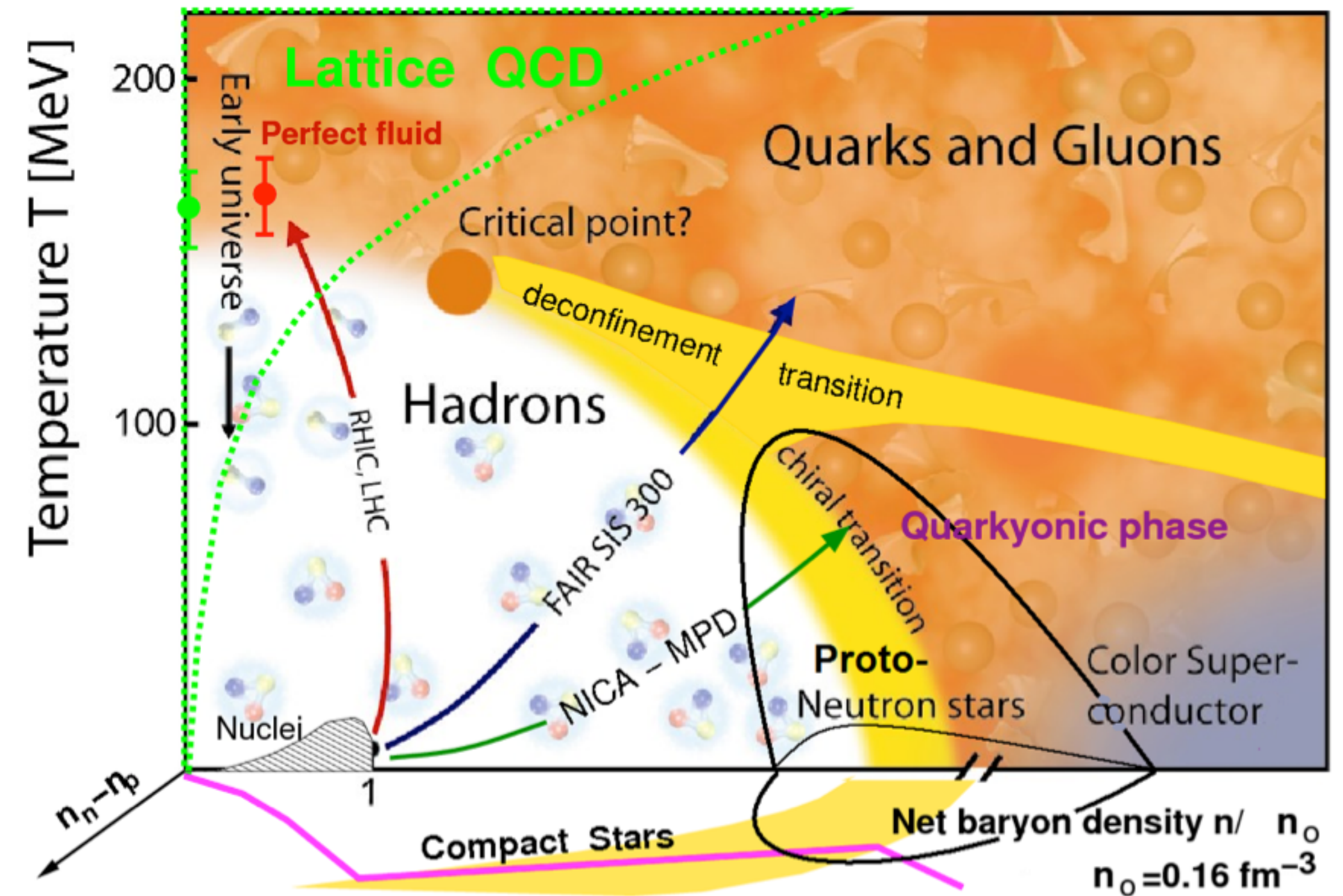
Fiona Panther | University of Western Australia | Forrest Research Foundation

With Paul Lasky | Monash University | OzGrav



Post-merger remnants and the NS maximum mass

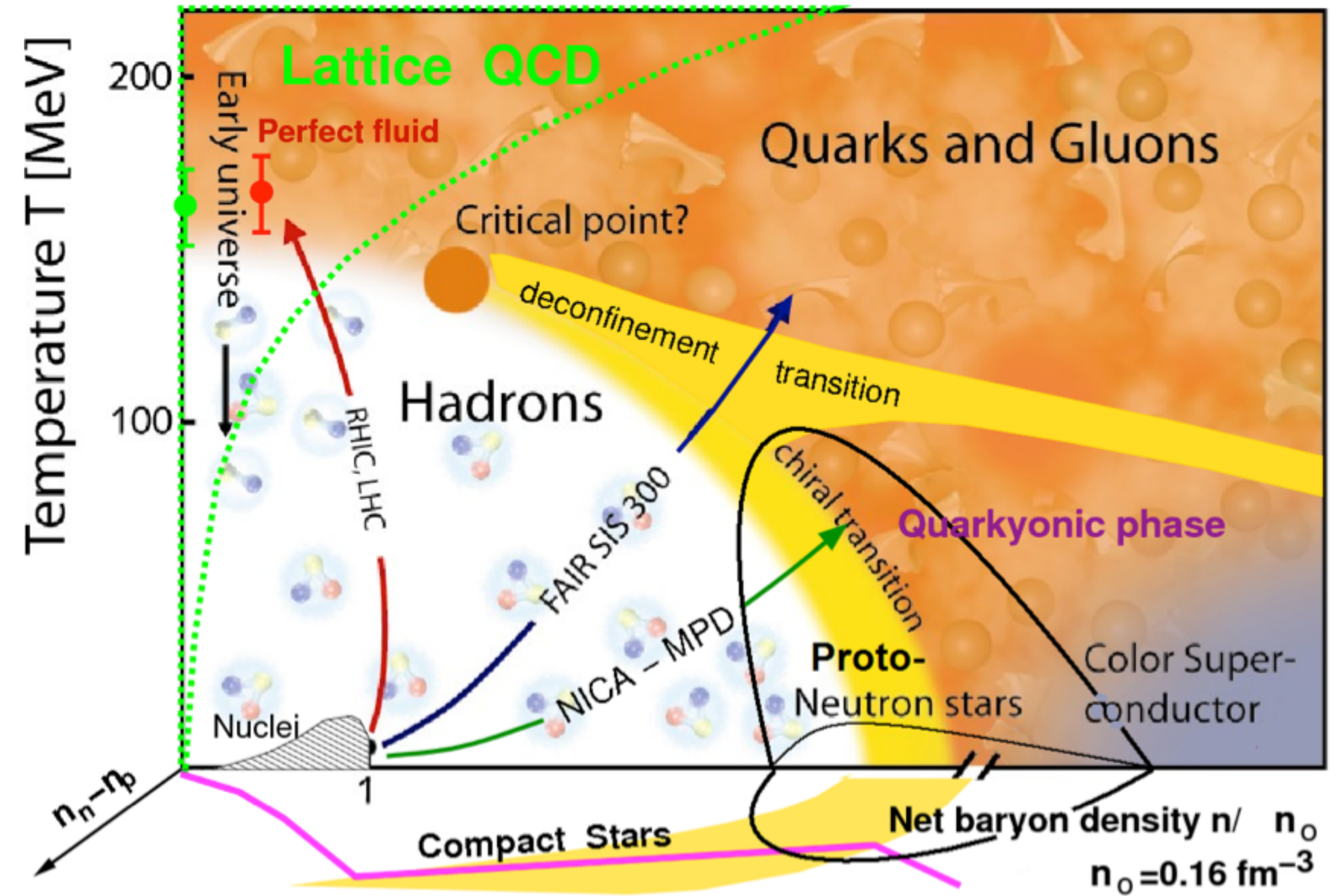
Hypermassive neutron stars that form from BNS mergers can help us constrain the nuclear EoS



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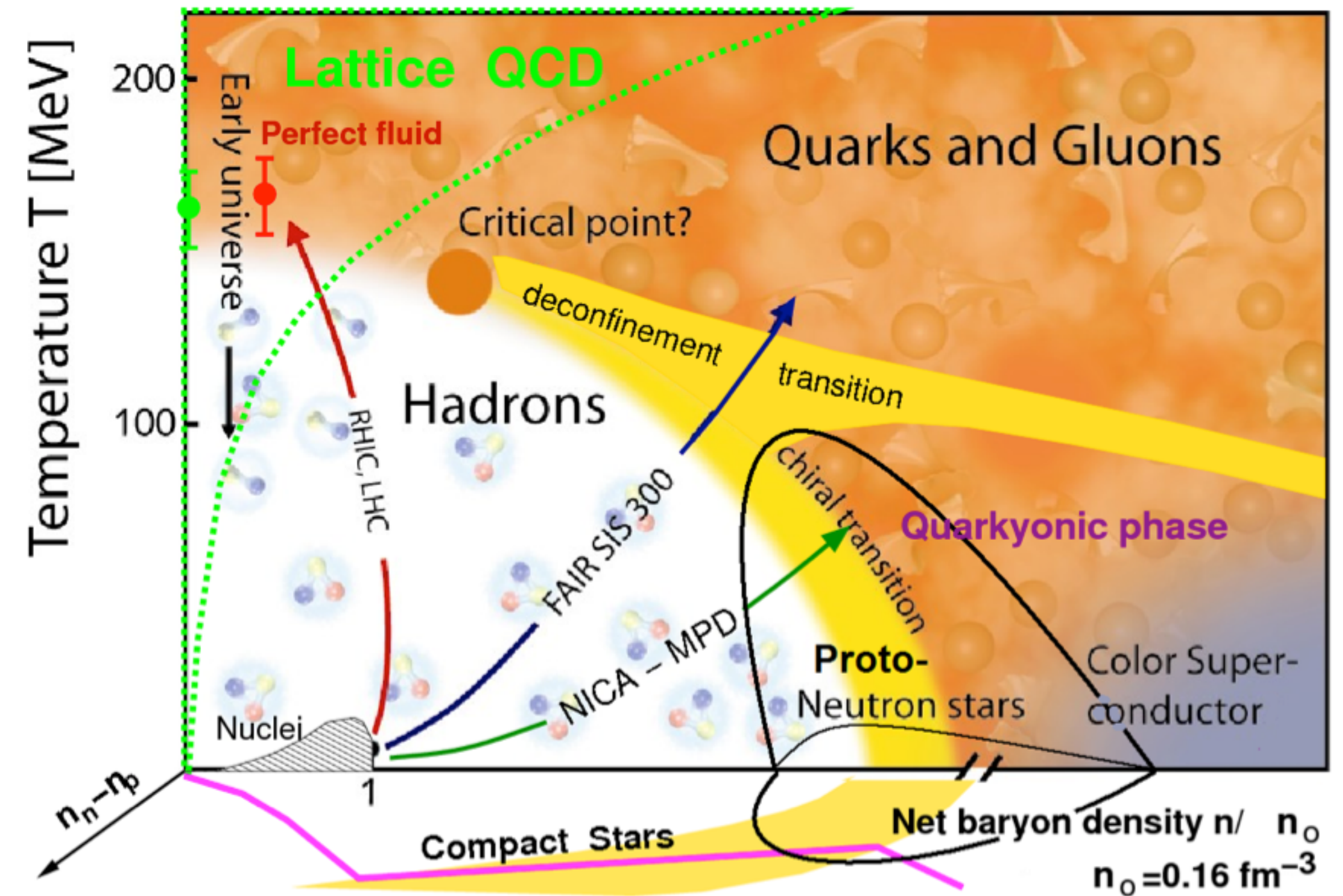
- Most stringent upper limit for a non-rotating neutron star: Tolman-Oppenheimer-Volkoff (TOV) limit



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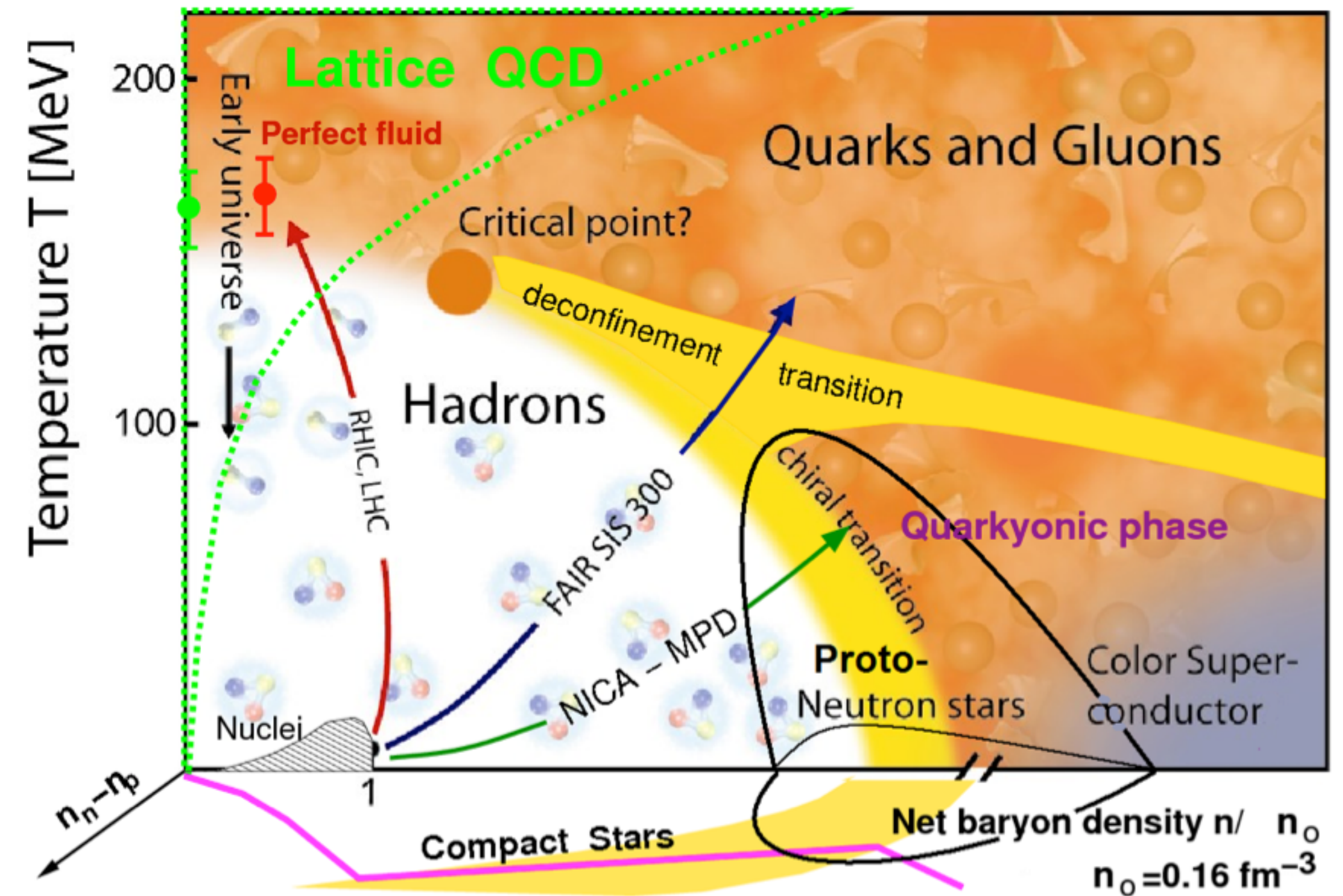
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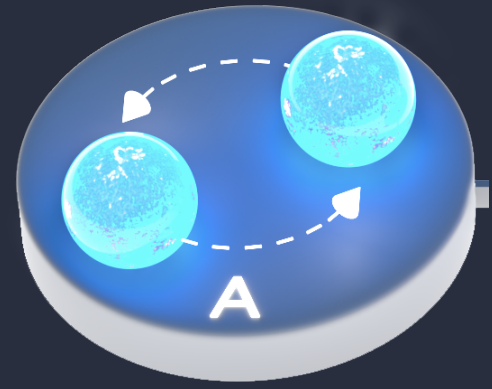
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- Hypermassive NS matter described by the **hot nuclear EoS**, and **NS are differentially rotating** (Sarin+2021 review)
- The hot nuclear EoS can be studied in these objects



Post-merger remnants and the NS maximum mass

Measuring NS properties with GWs

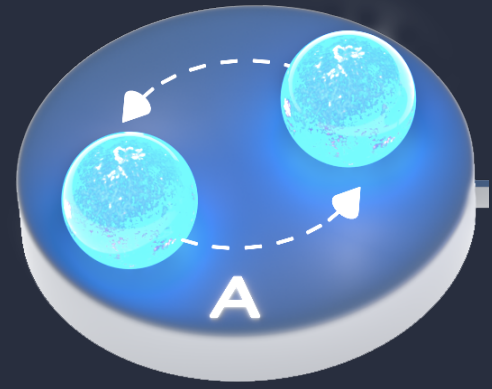


Inspiral: measurement of NS masses
constrains *cold nuclear EoS*

NS & black hole graphics: Sarin & Lasky 2021

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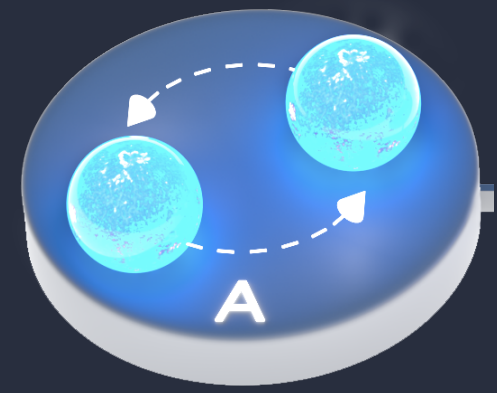


Merger: measurement of tidal
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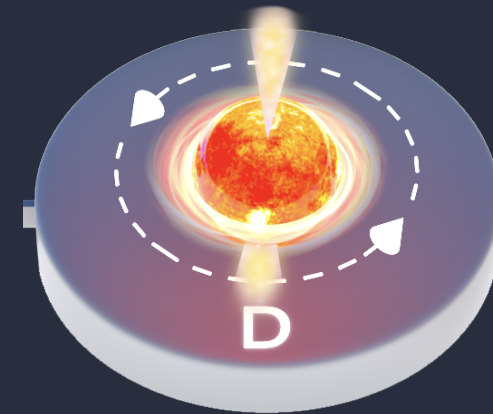
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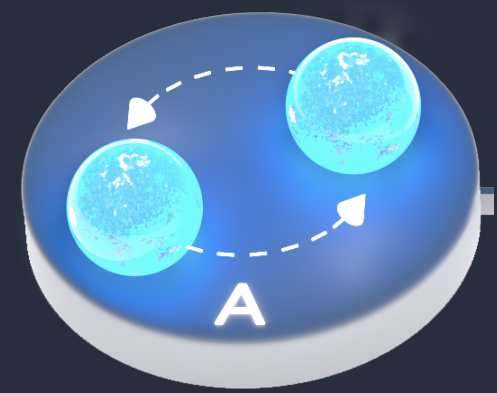


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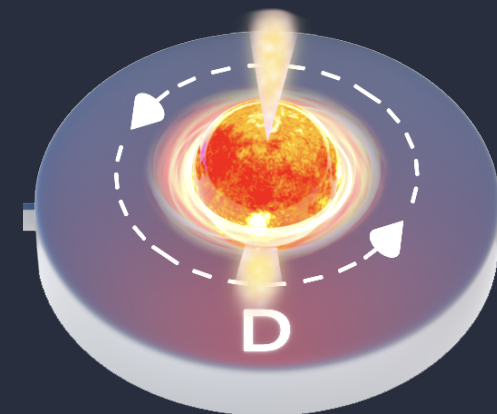
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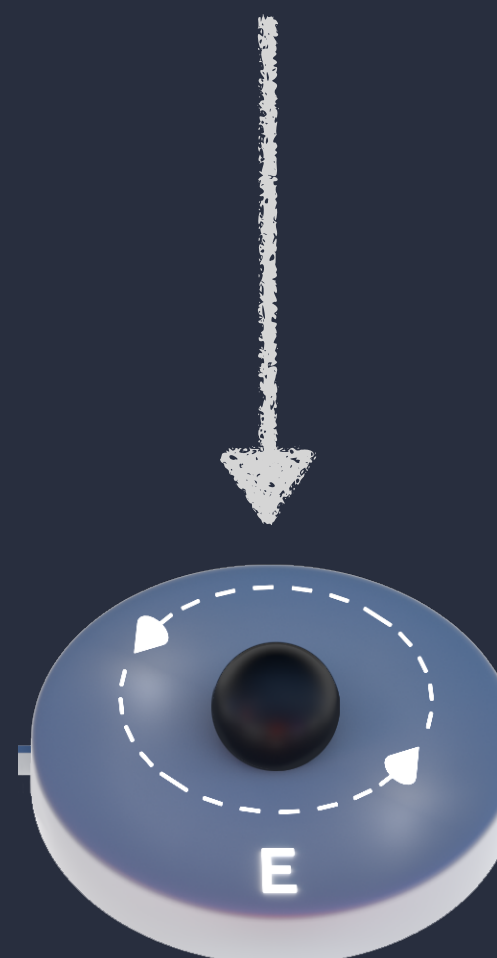
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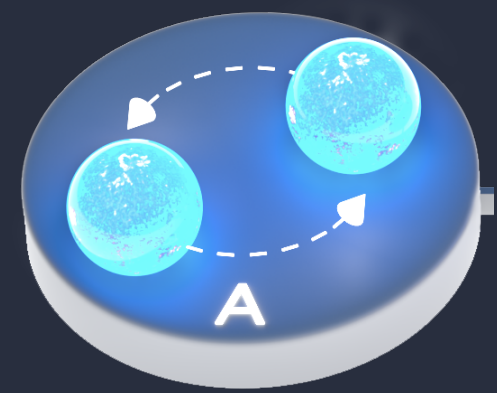


BH formation: Collapse to BH if rotational support is lost and EoS insufficiently stiff

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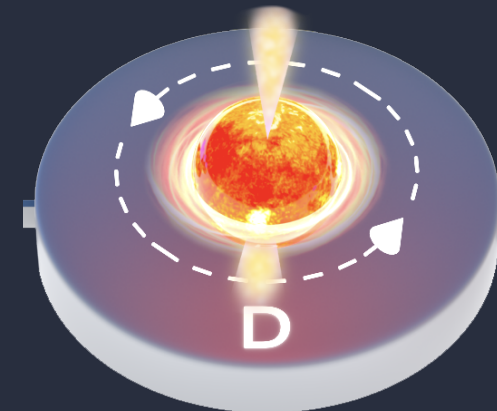
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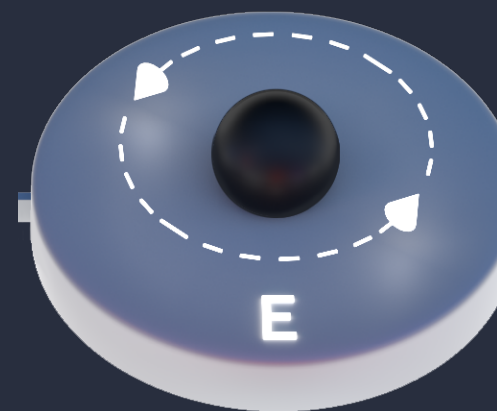
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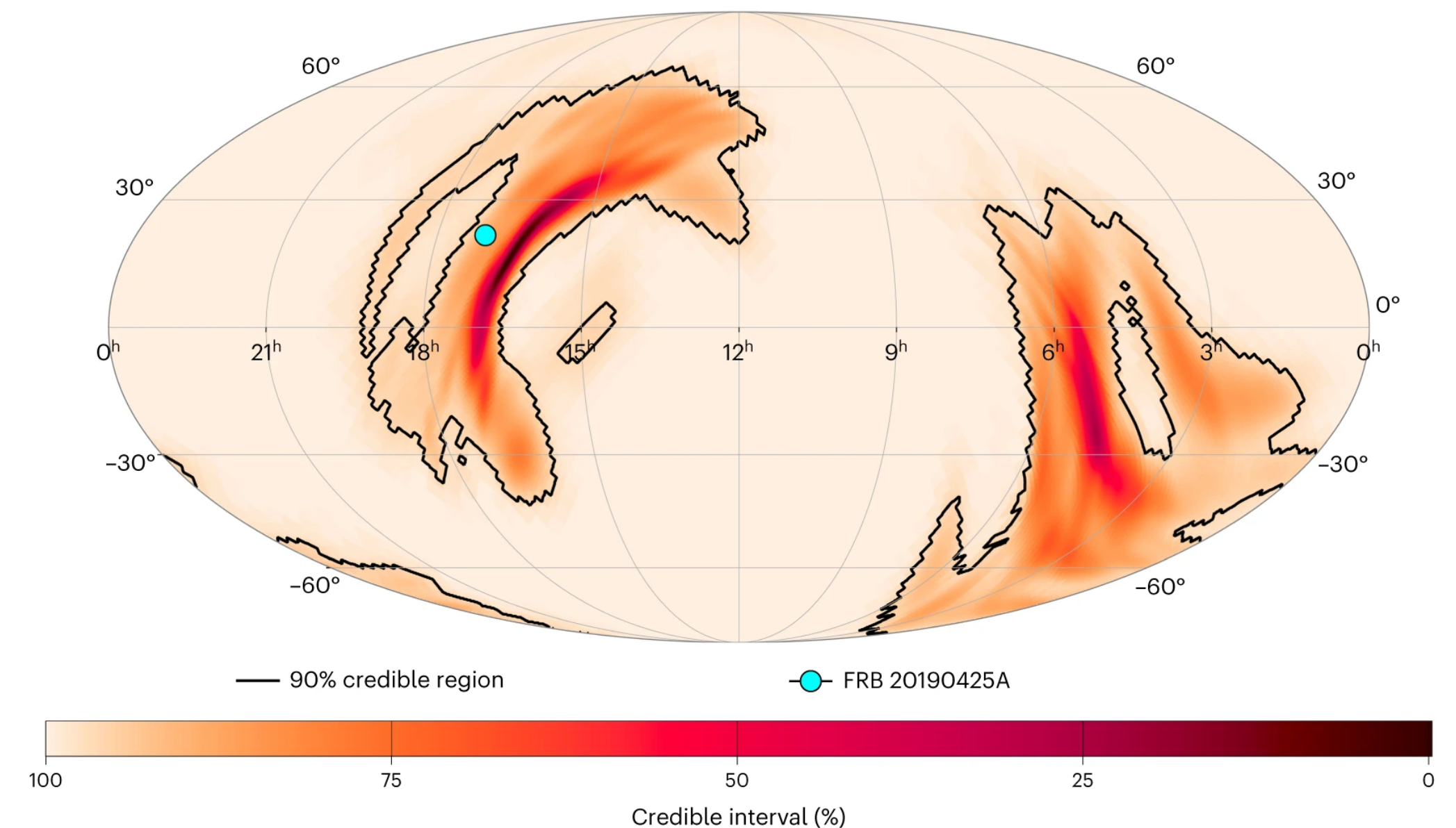
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Post-merger remnants and the NS maximum mass

An FRB* 2.5 hours AFTER a BNS merger resulting from a hypermassive neutron star formed in GW190425

$> 2.63^{+0.39}_{-0.23}$ solar masses ($> 2.31^{+0.24}_{-0.08}$ solar masses)



Moroianu+2022 Nat. Astron. (MSc student, now PhD at UvA)

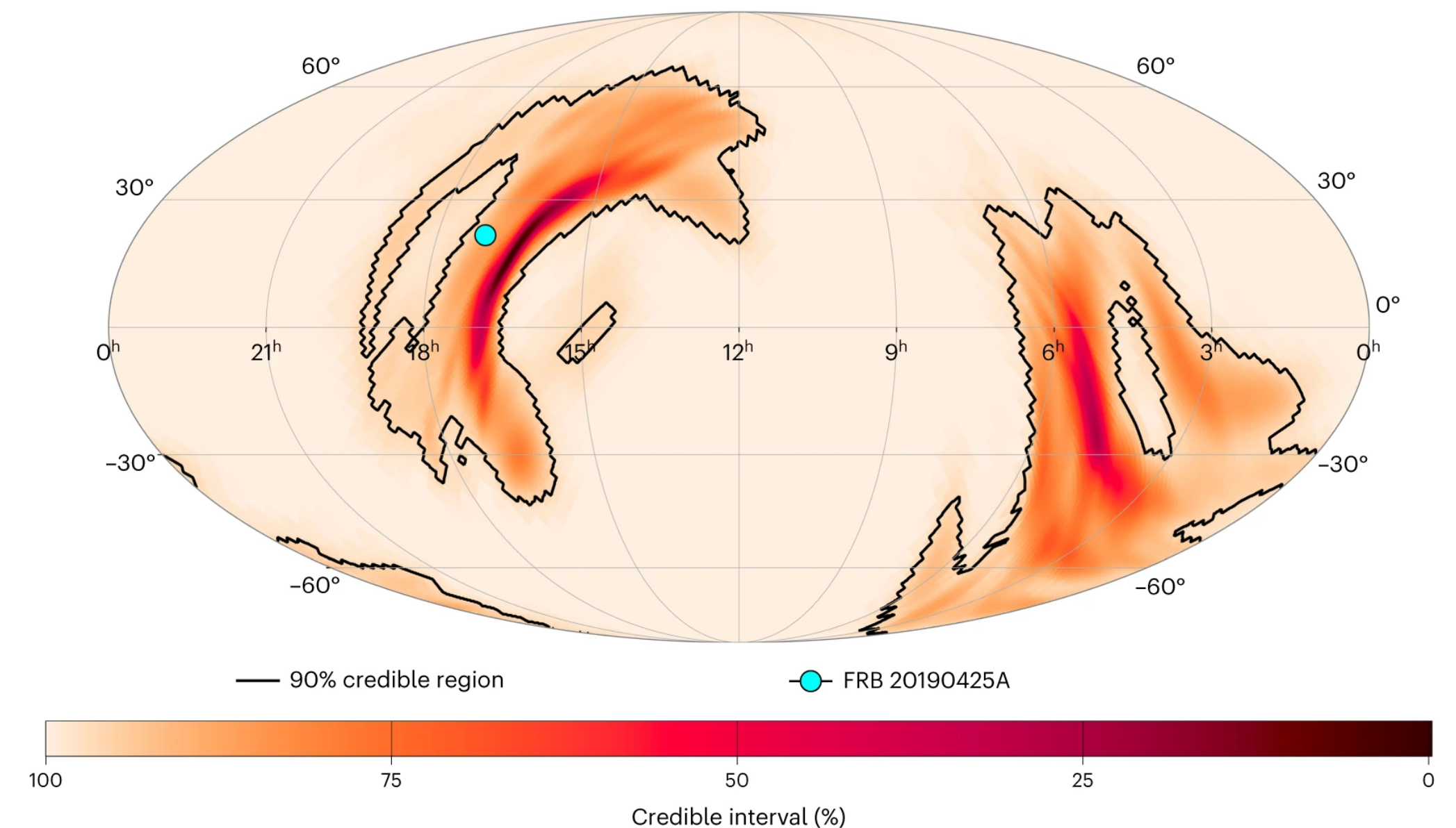
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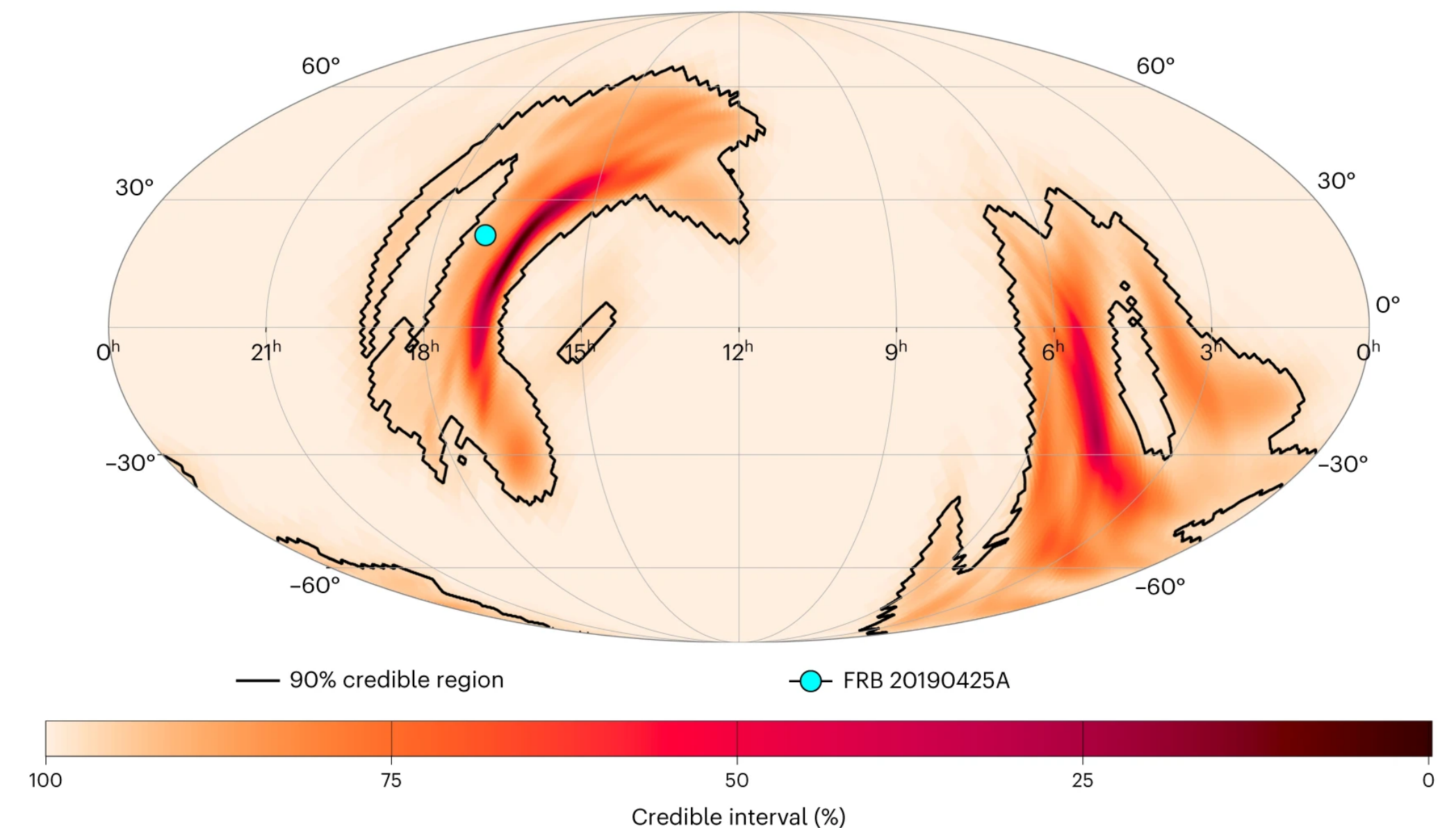
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- Emission from collapse of a hypermassive remnant that occurs after the GW emission could be a smoking gun (e.g. delayed sGRB jet, magnetar collapse producing a fast radio burst, see Sarin & Lasky 2021 for a review)
- There is no conclusive electromagnetic signature of post-merger remnants that can allow us to measure the NS mass and probe the hot nuclear EoS

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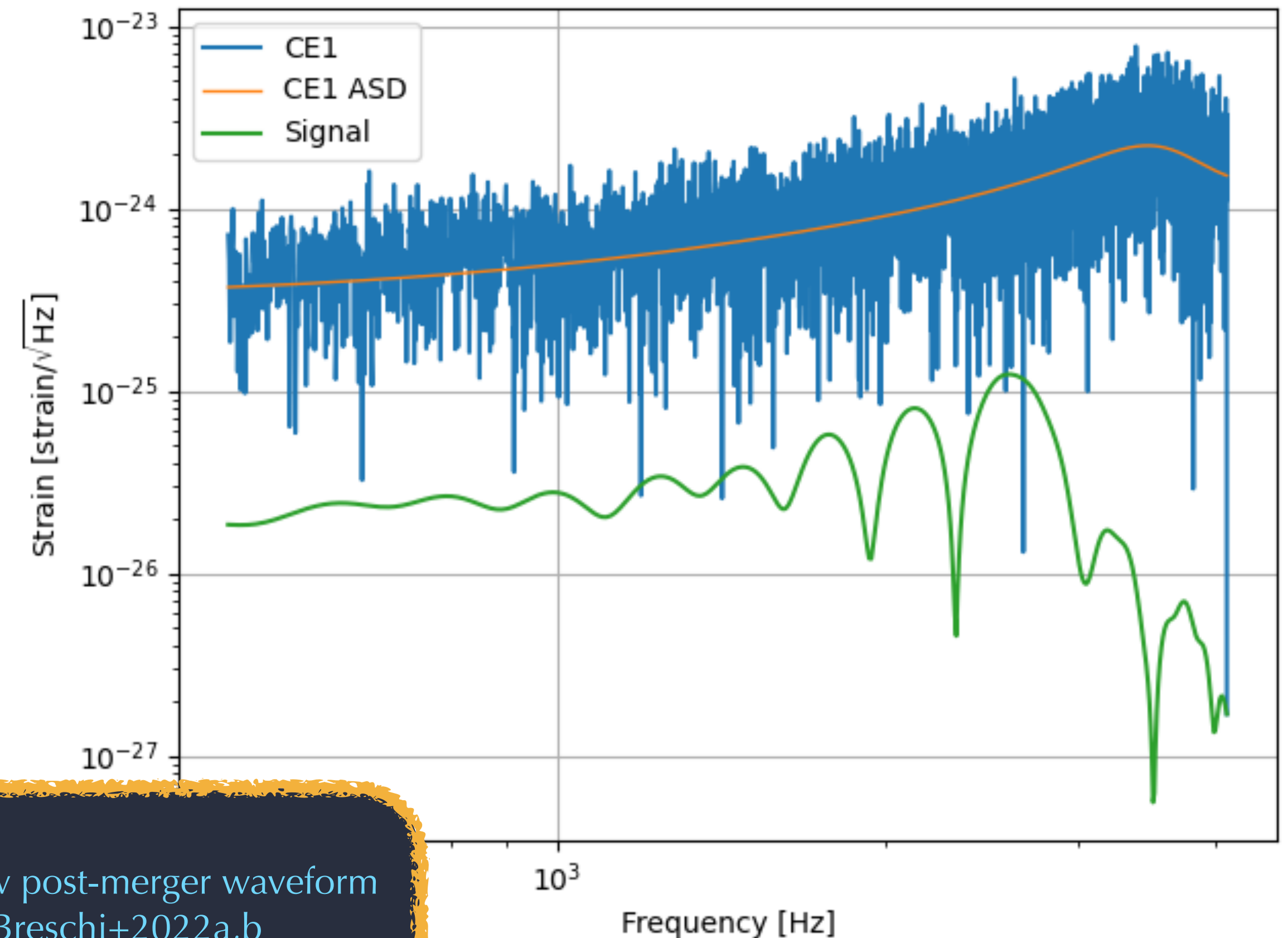


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Detecting post-merger GWs

Making a detection* of PMGWs is a significant challenge:

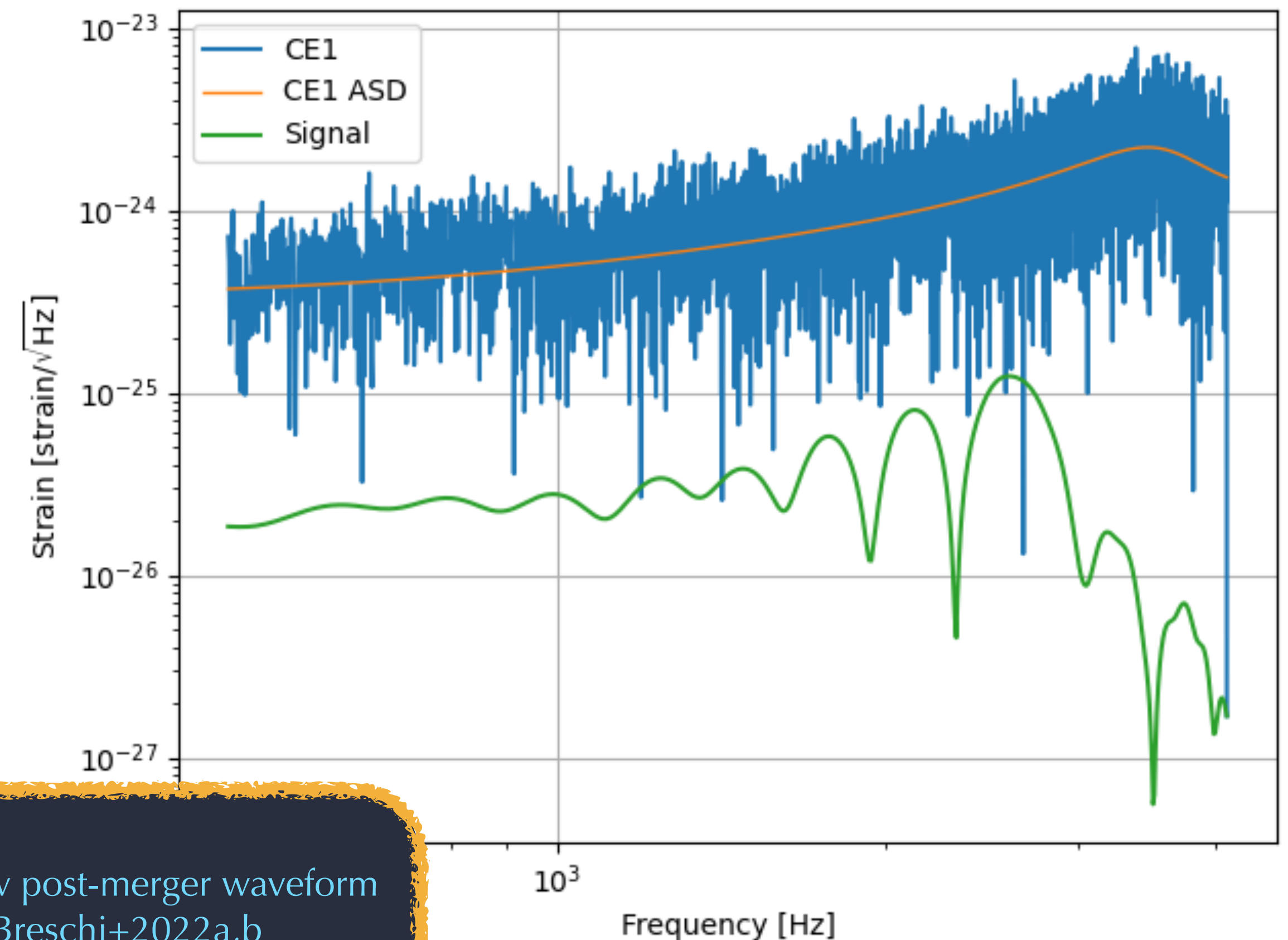


In this work I am using the NRPMw post-merger waveform approximant developed in Breschi+2022a,b

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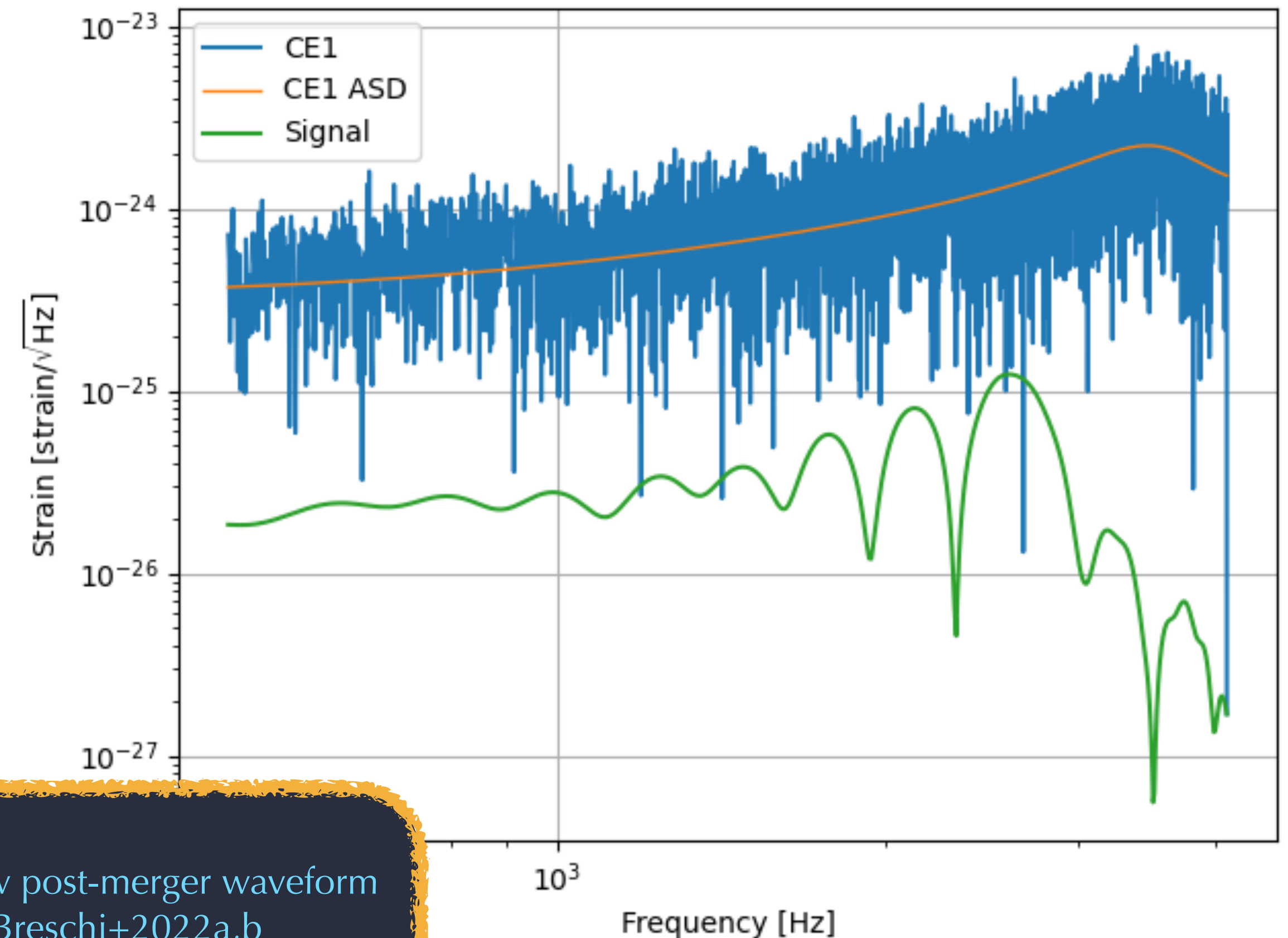


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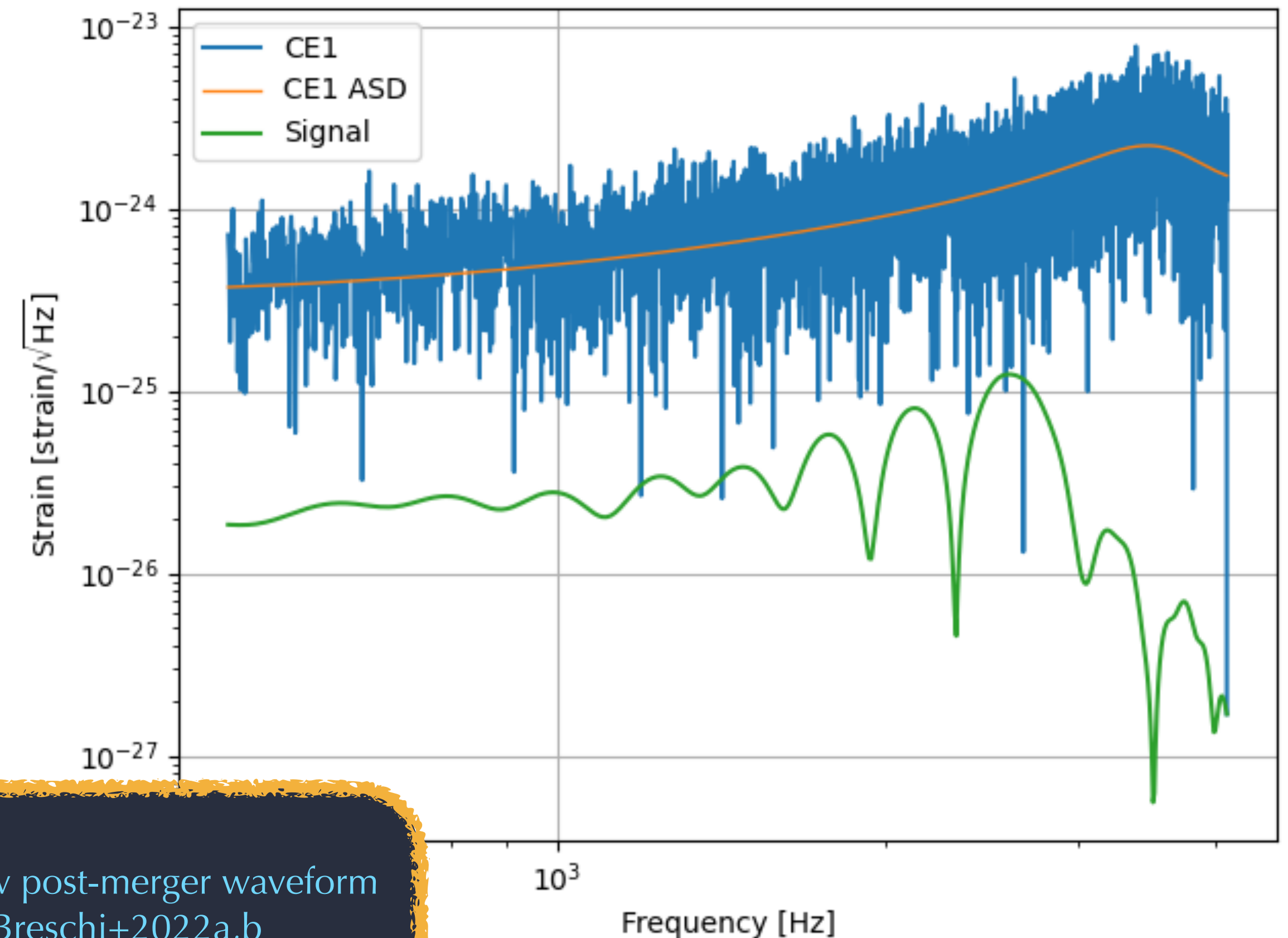


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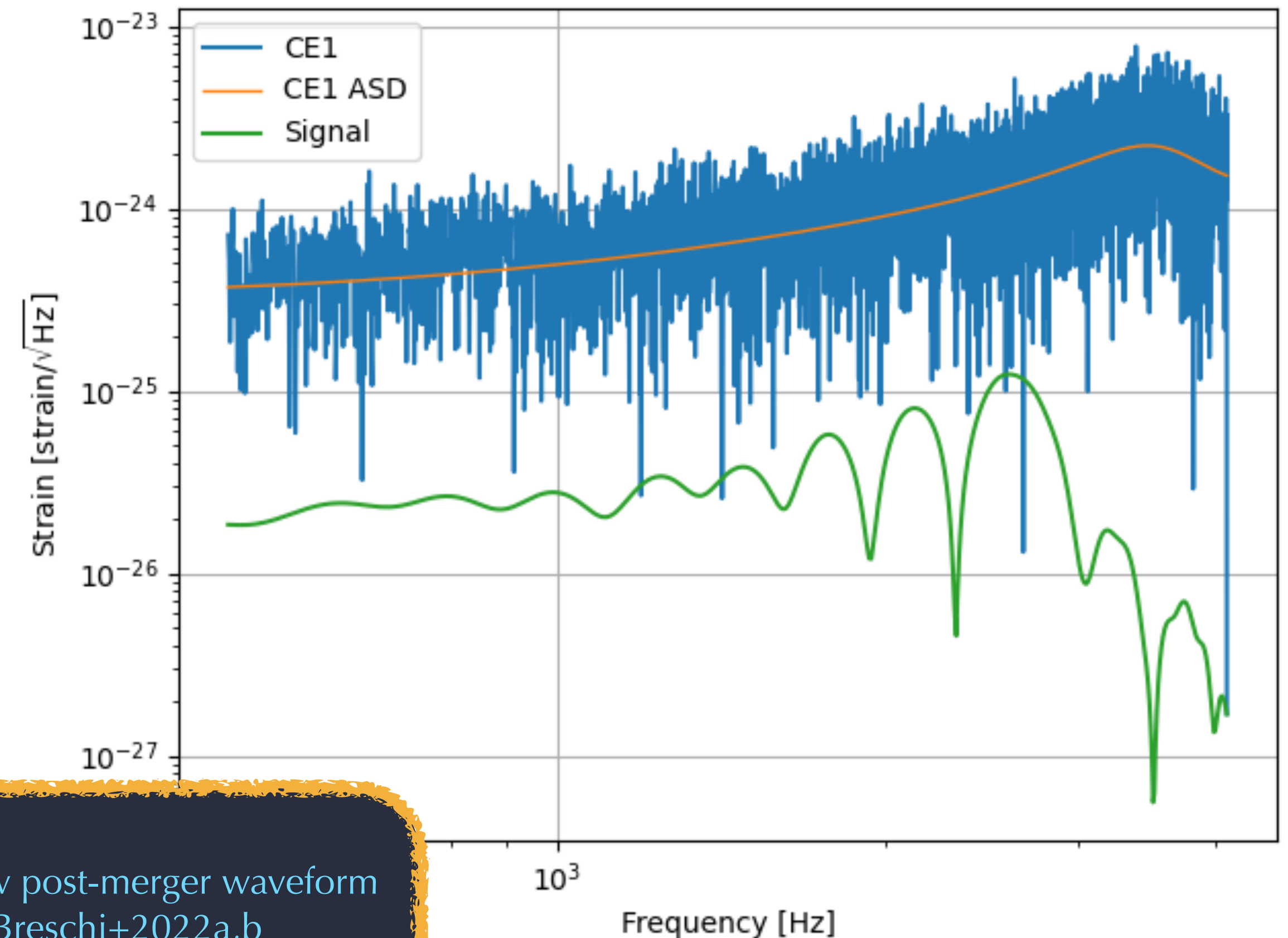


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- Lots of model uncertainty!!



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A solution for faint sources: stacking

- Stacking data common in astronomy when we have a faint source and need to boost our SNR.
- How can we combine many observations of PMGWs? We cannot naively stack them in the data space.
- Stack observations of heterogeneous sources in the **model space** by creating a 'stacked signal likelihood' instead!

Stacking in the data space with optical images



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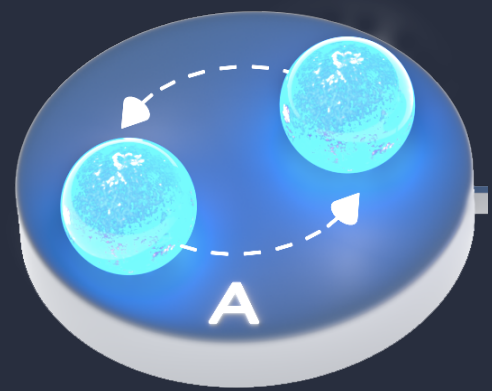
Stacking in the data space with optical images



Stacking increases the **contrast** of the image: noise level grows at a slower rate to the signal level, so by combining many exposures to lengthen the observing time we can maximise the ratio of the signal to the noise.

A mixture model formalism to 'stack' GWs

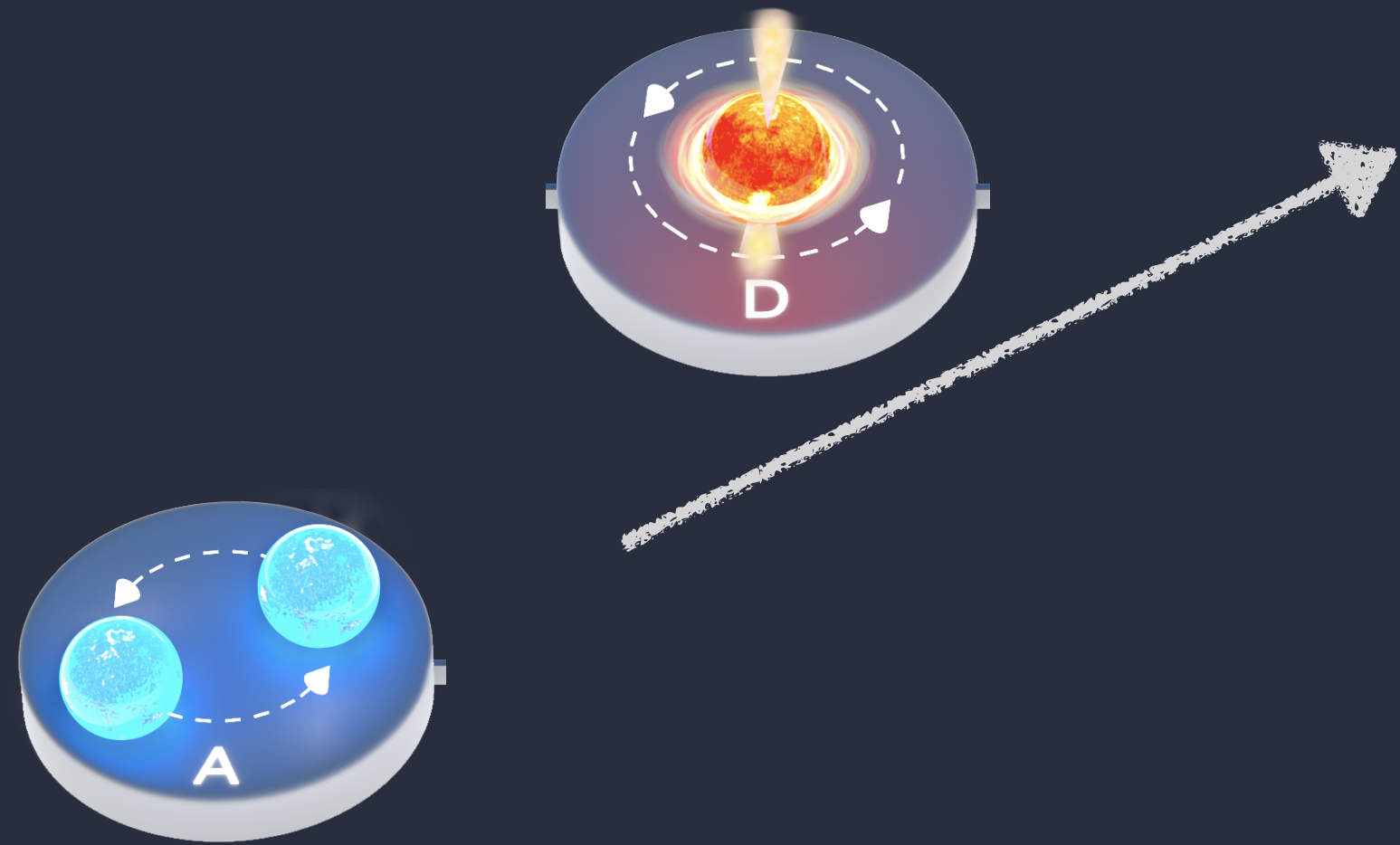
Develop a mixture model formalism based on Smith & Thrane 2018 (An Optimal Search for a GW background) to search for PMGWs



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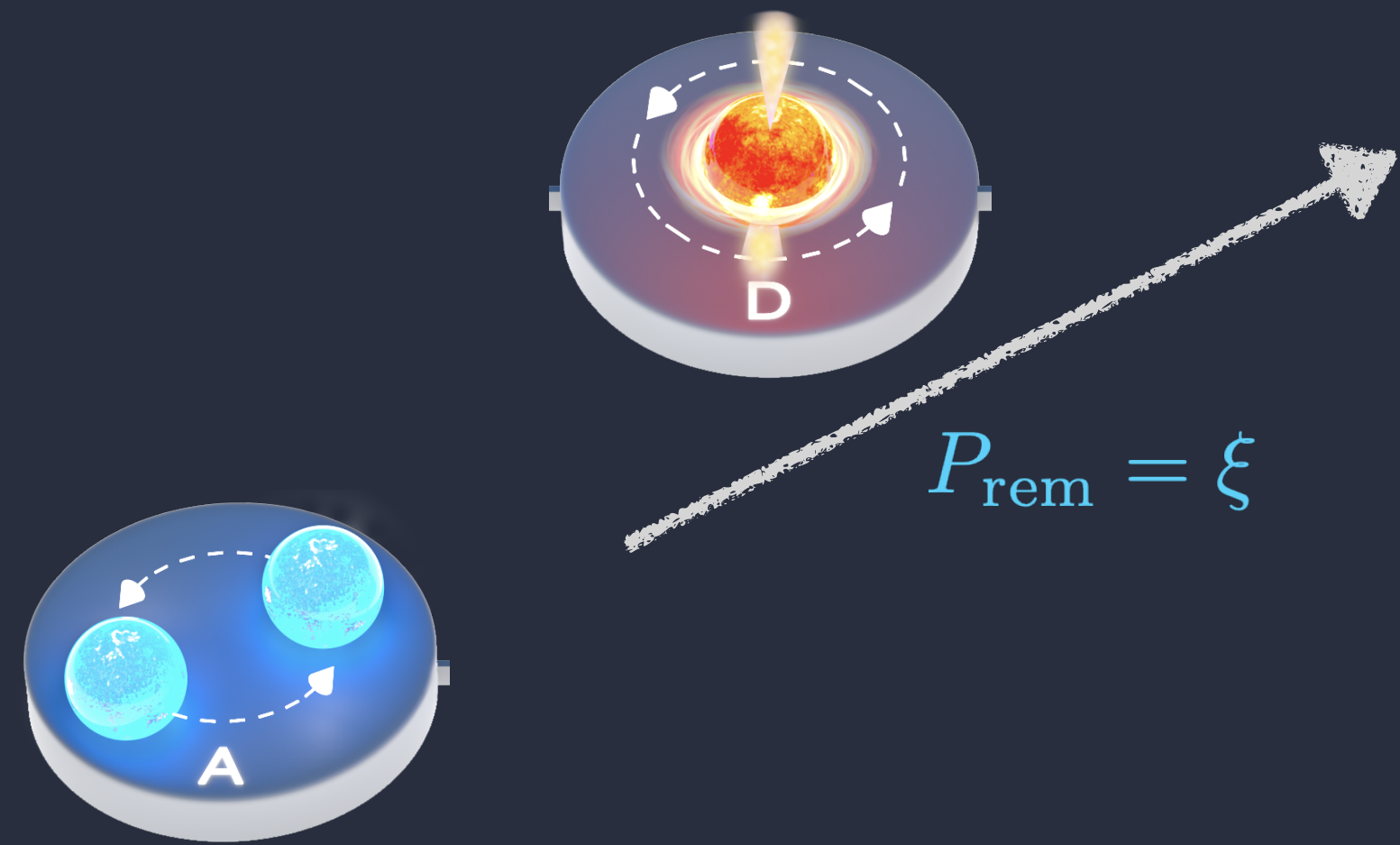
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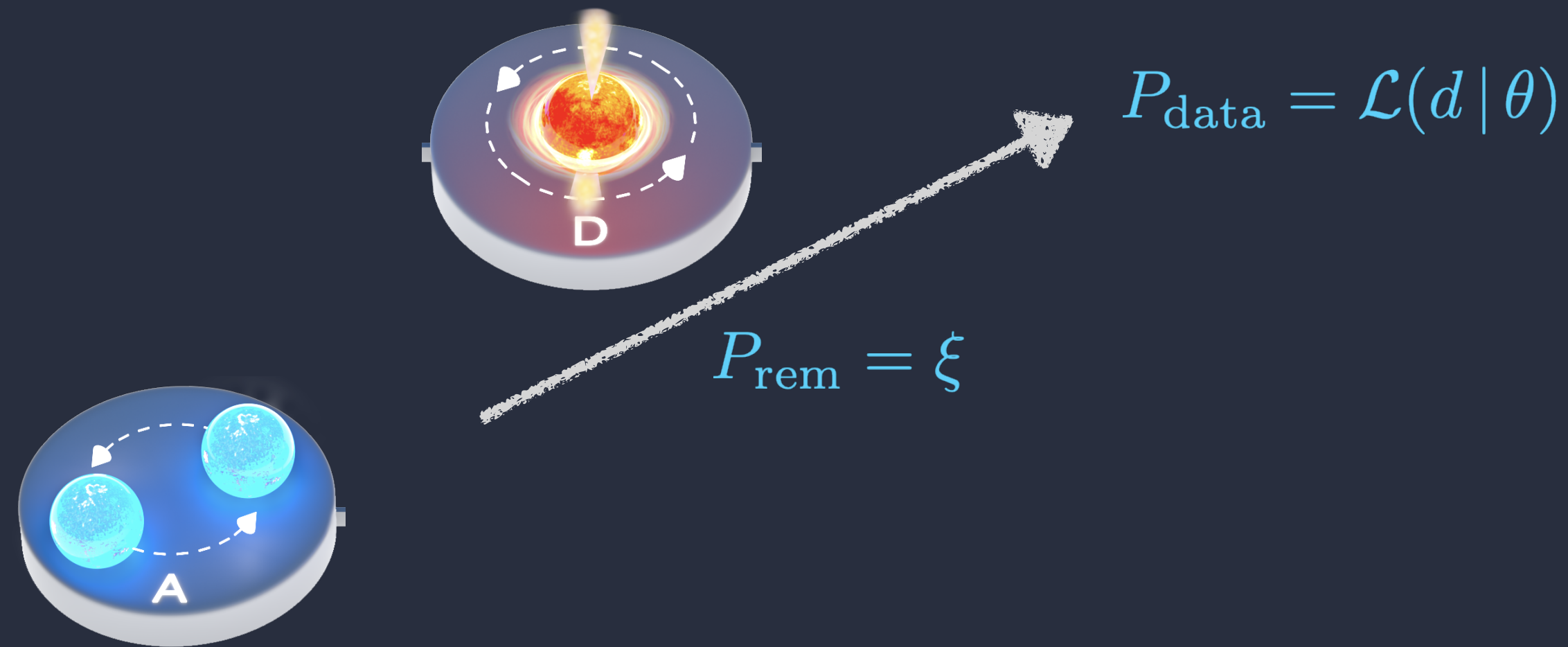
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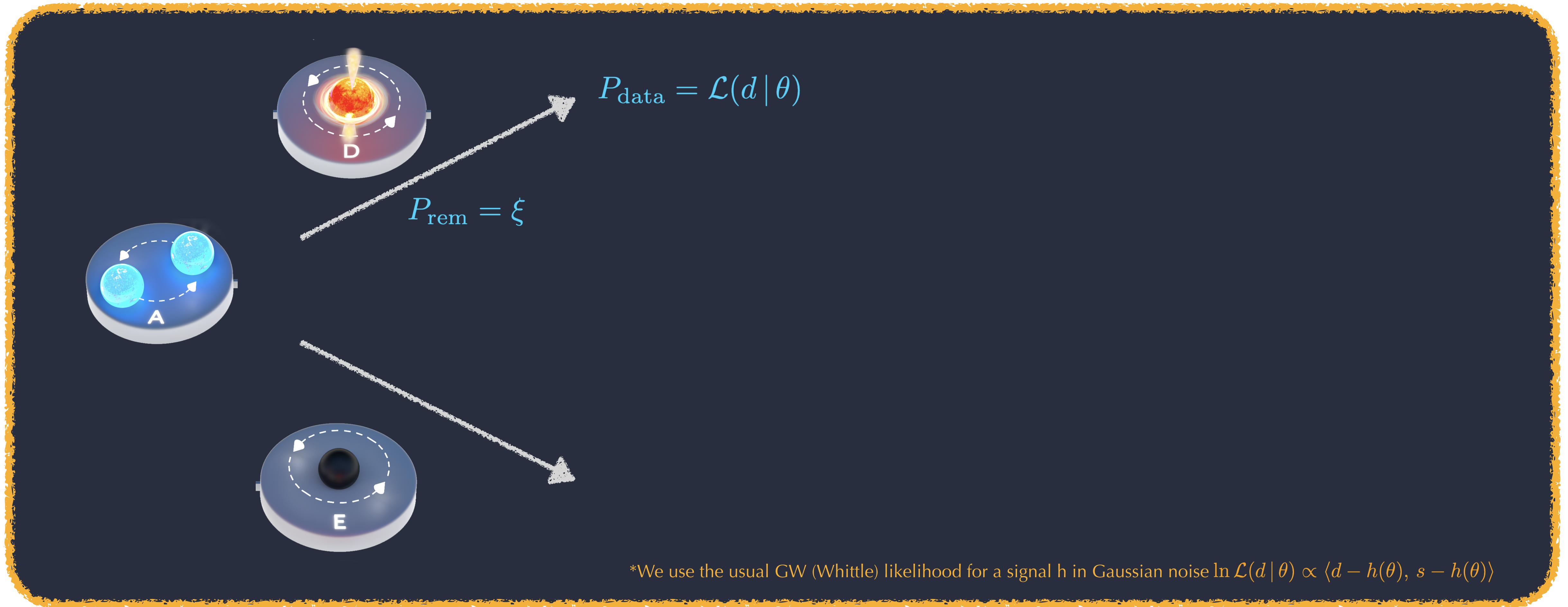
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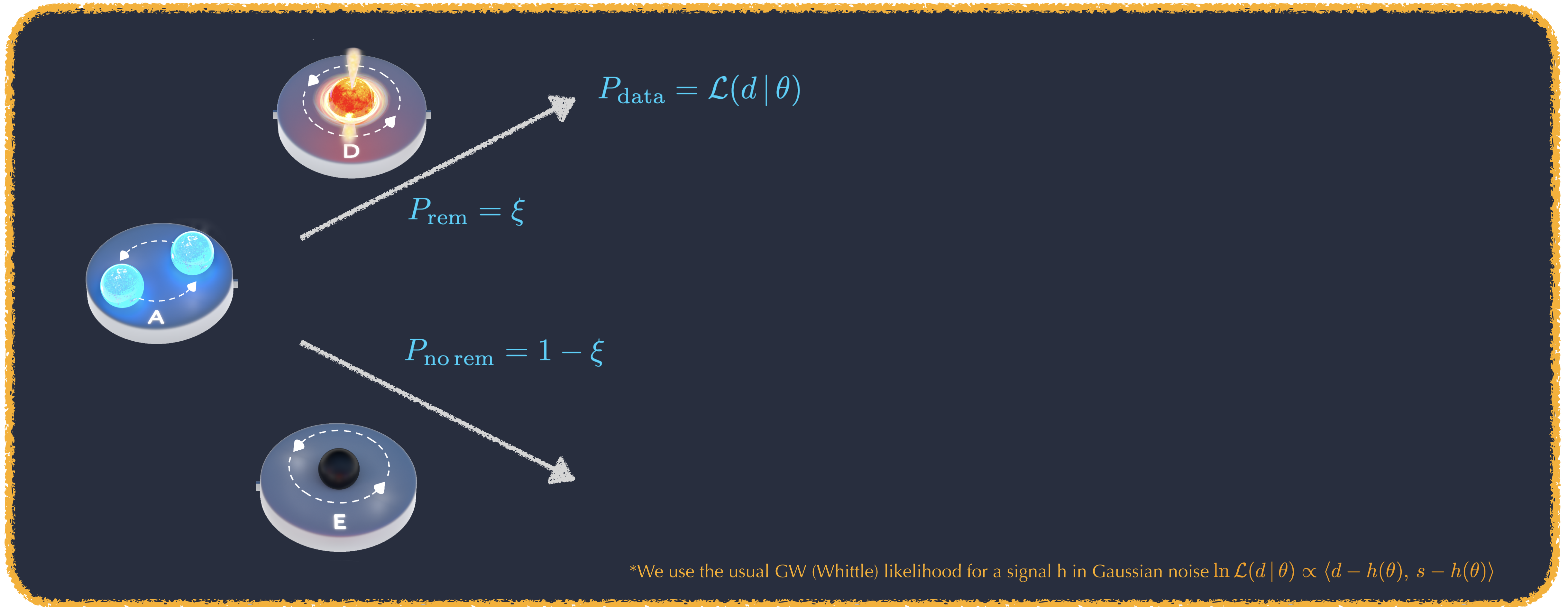
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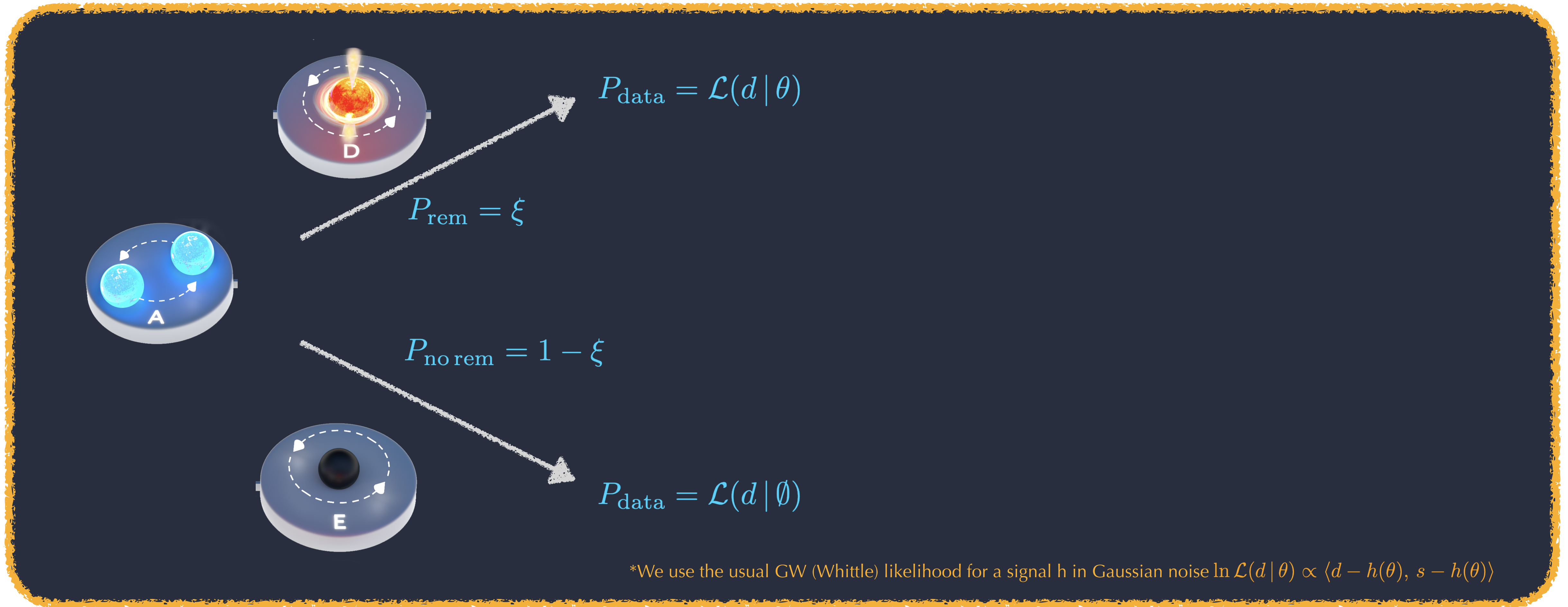
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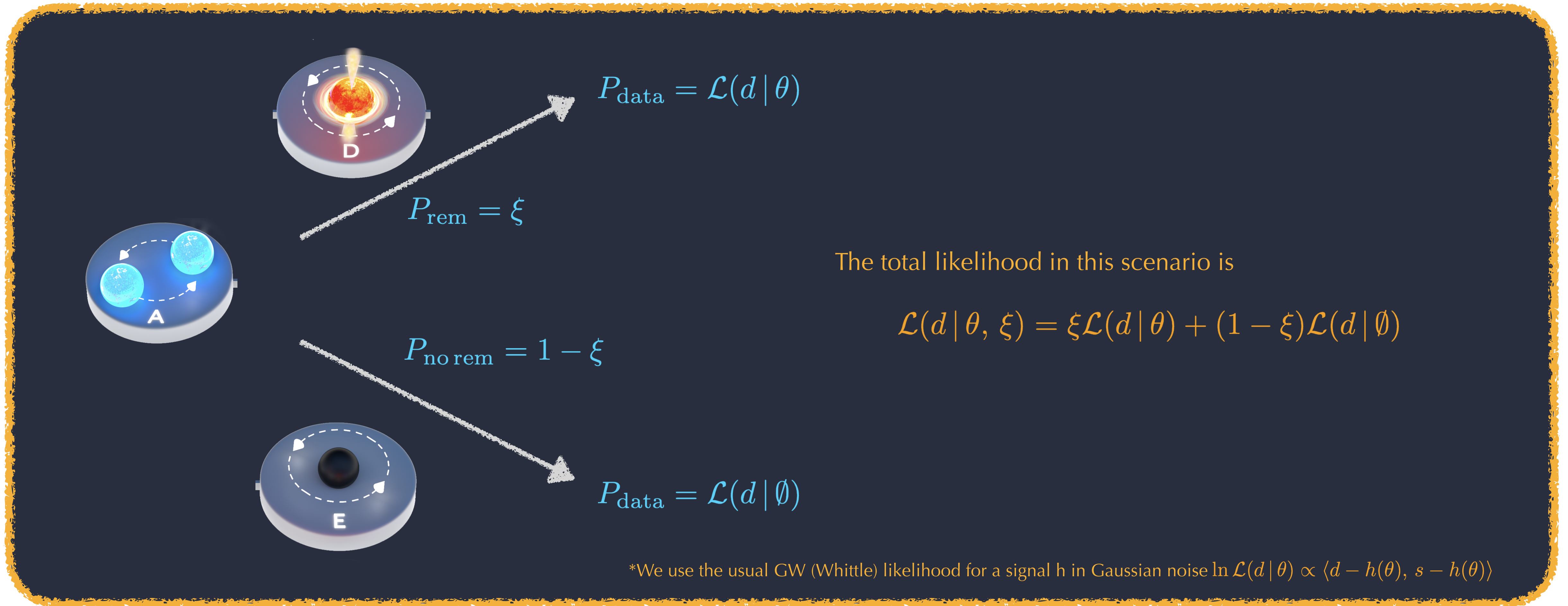
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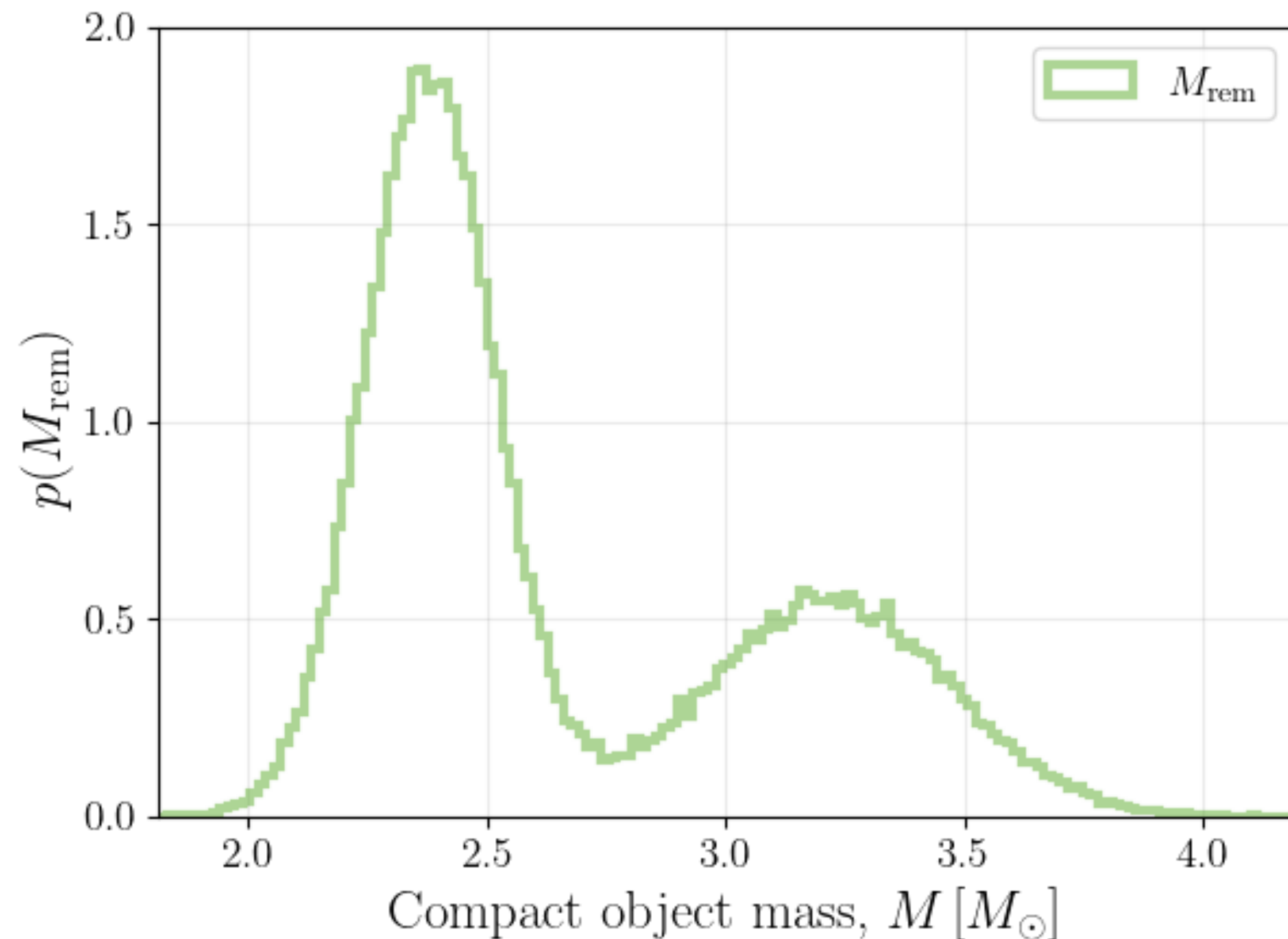
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What's in the mixing fraction?

Physics determines the fraction of BNS mergers that leave behind a remnant

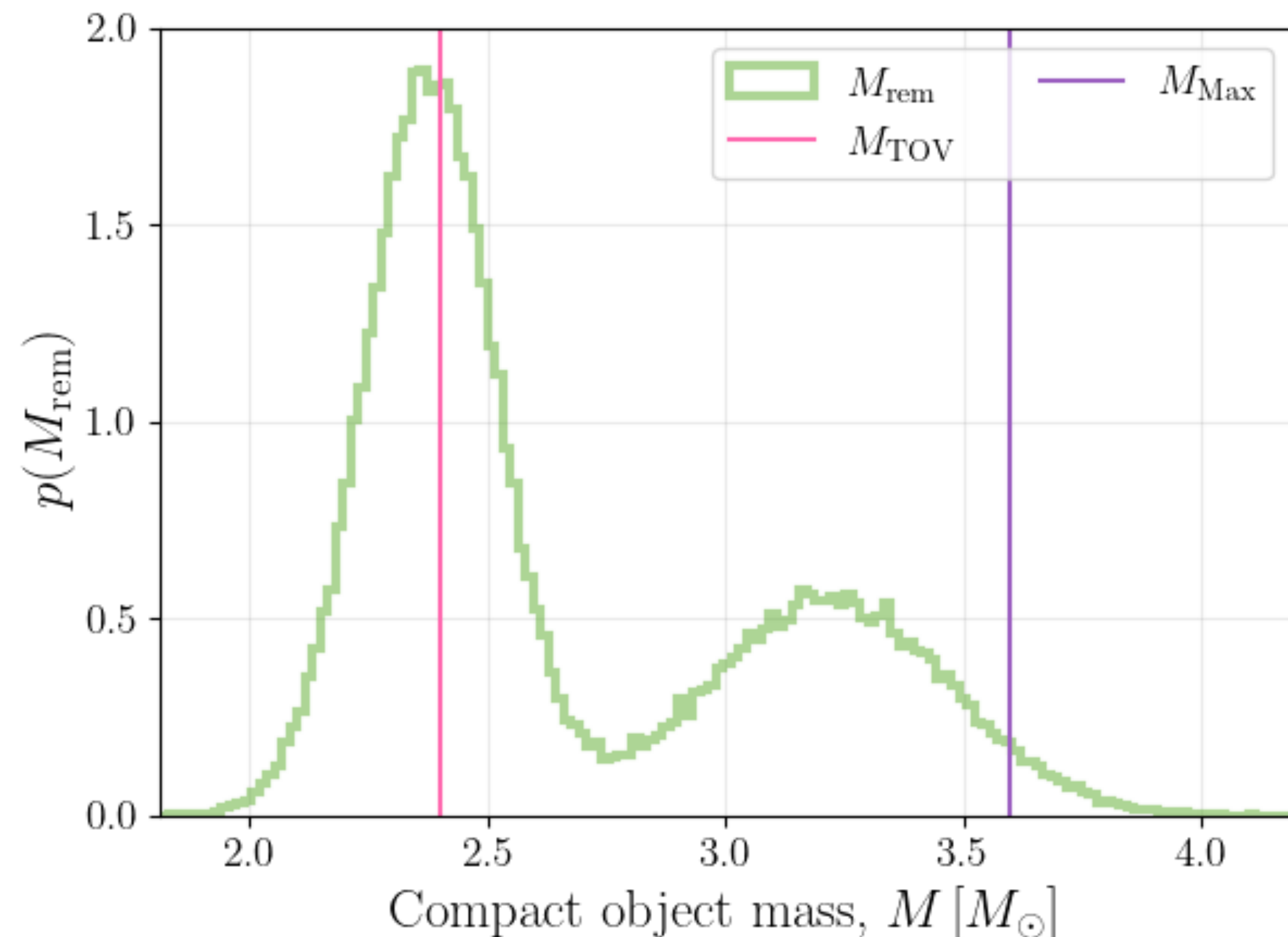


NS masses: we assume a bimodal Gaussian distribution of component masses m_1 and m_2 based on the Galactic NS population and the masses of GW170817 and GW190425

Remnant mass: The remnant mass is the sum of the **rest masses** of the individual neutron stars, minus the mass lost ($0.1 M_{\text{Sun}}$). The rest mass is conserved in the merger

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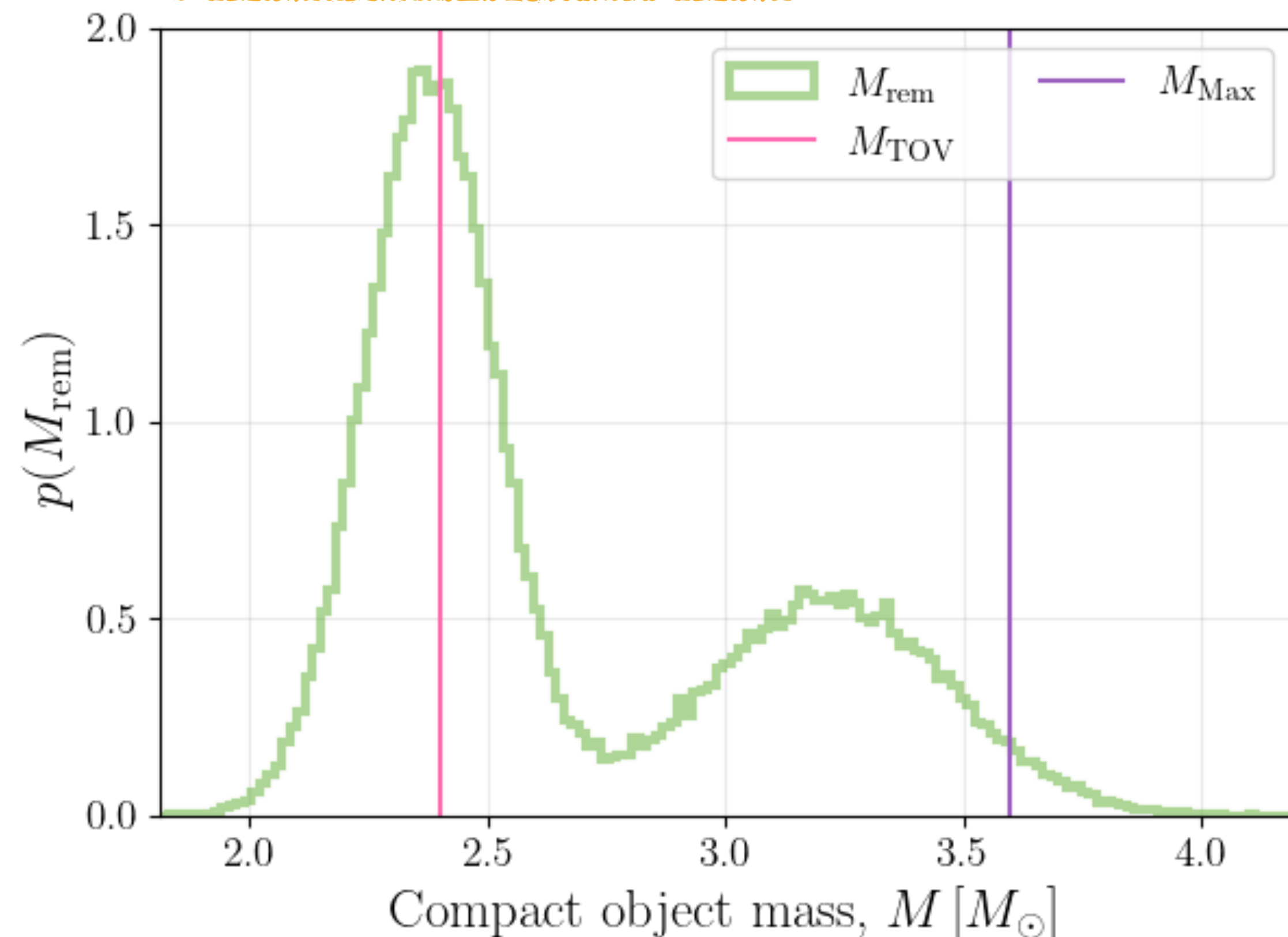
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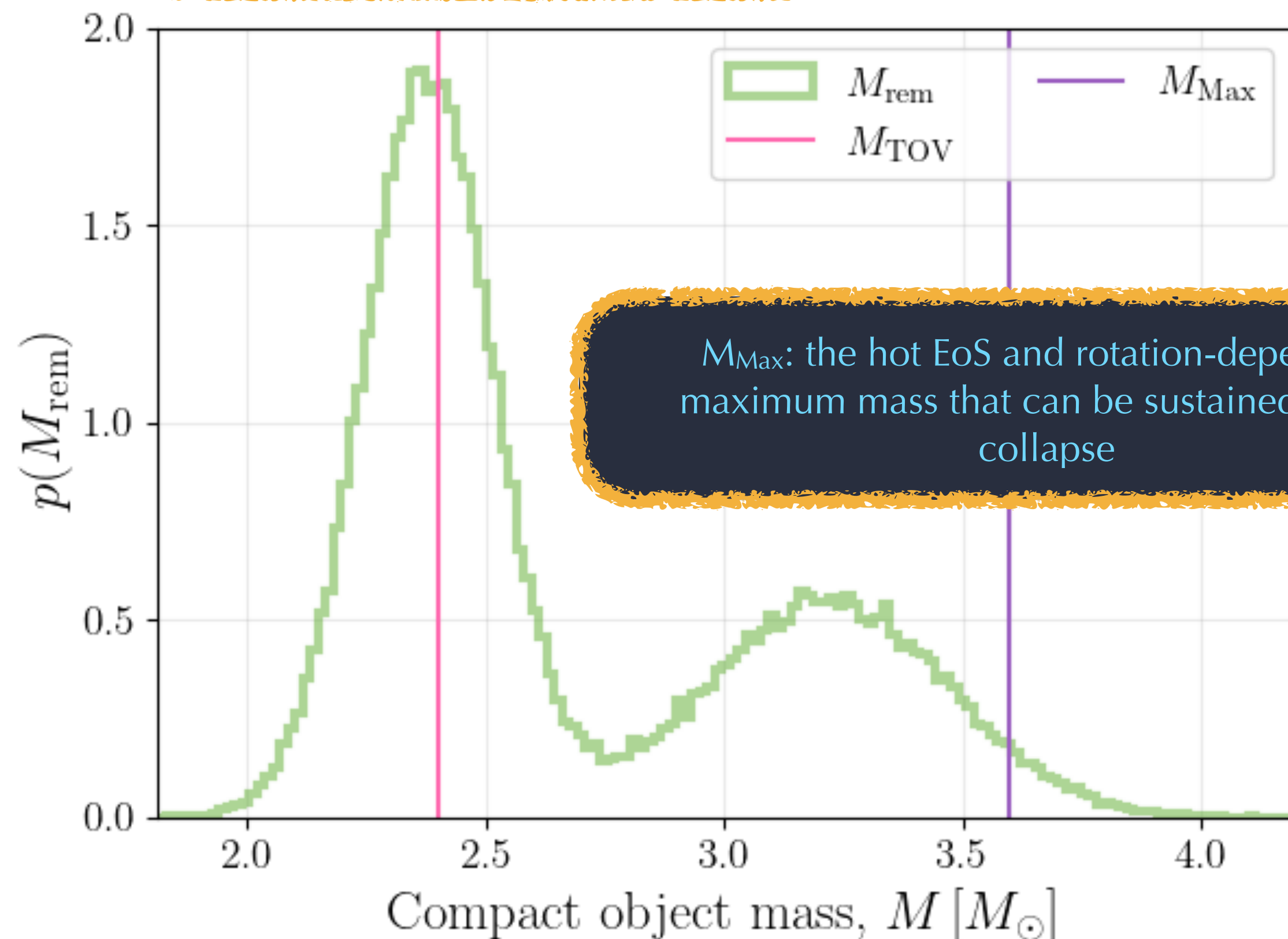
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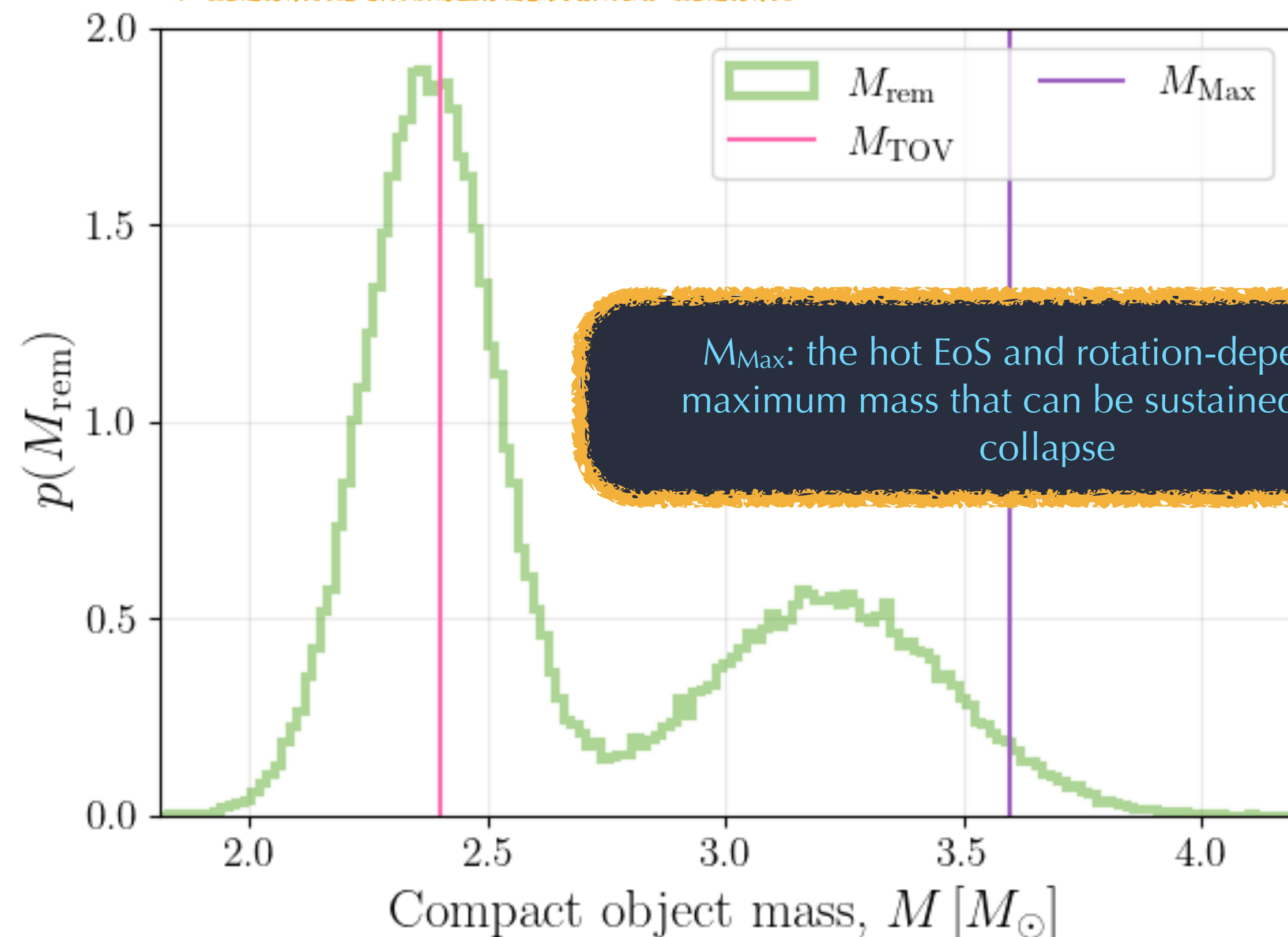
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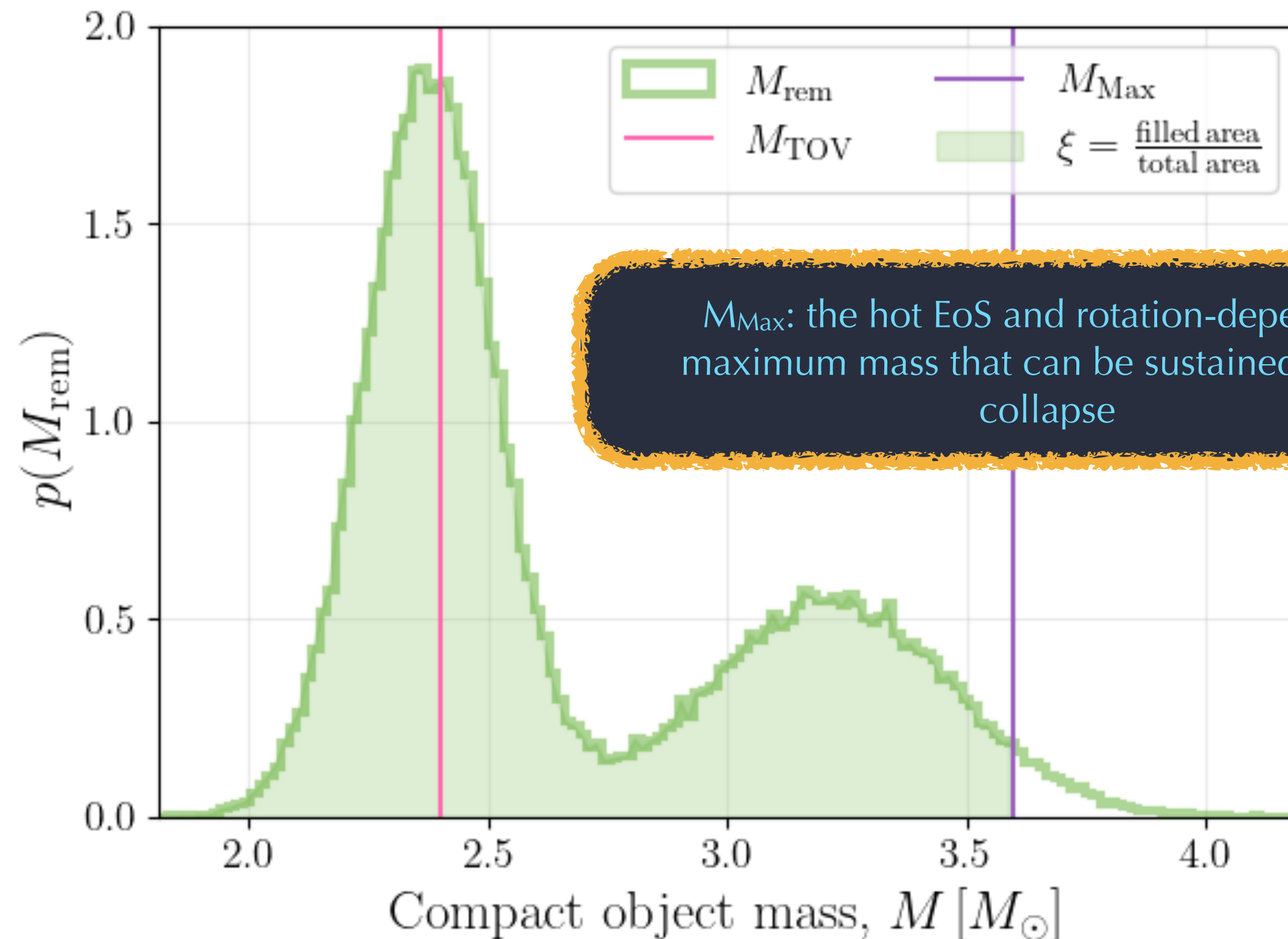
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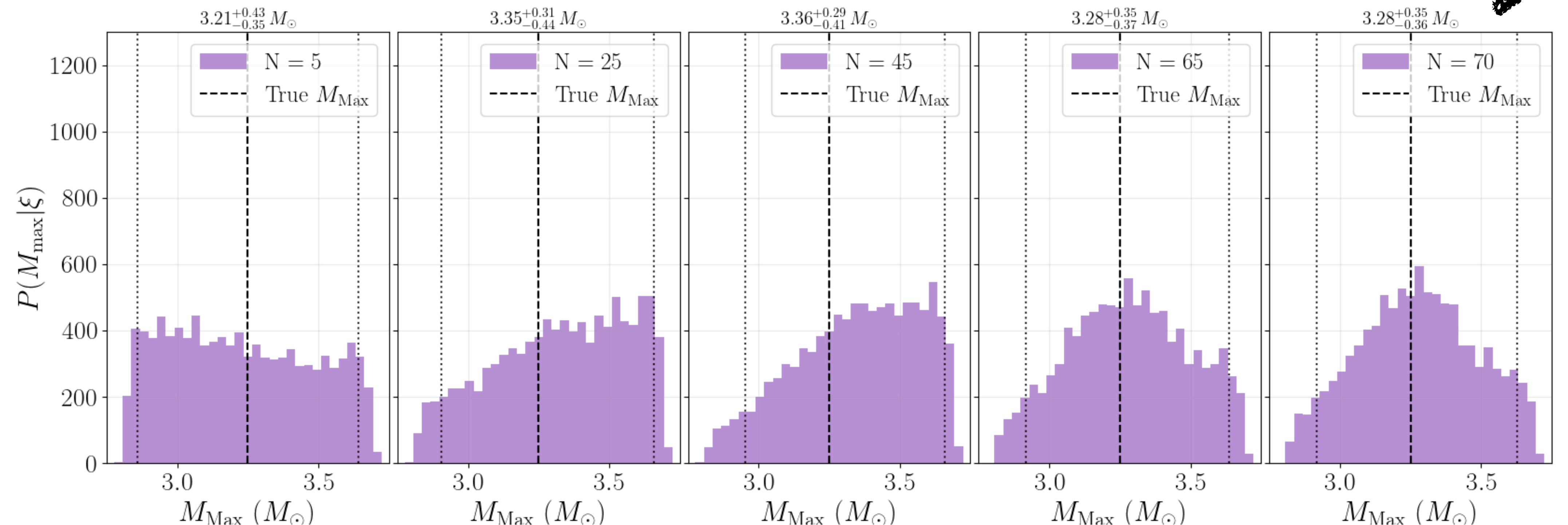
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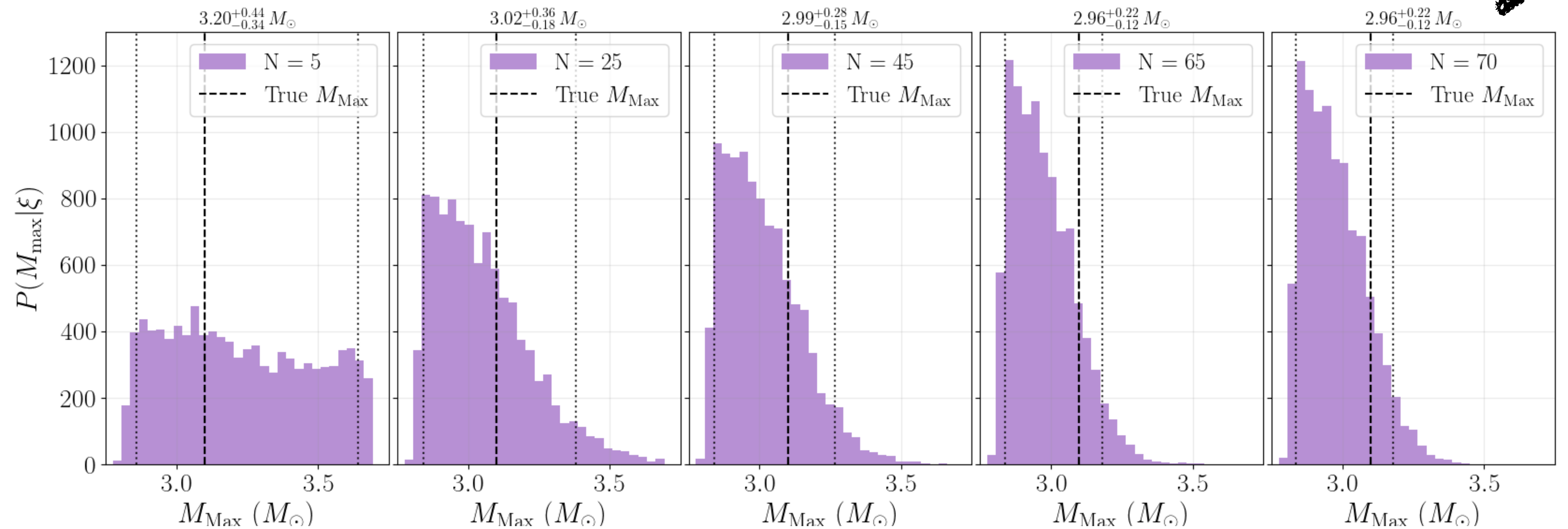
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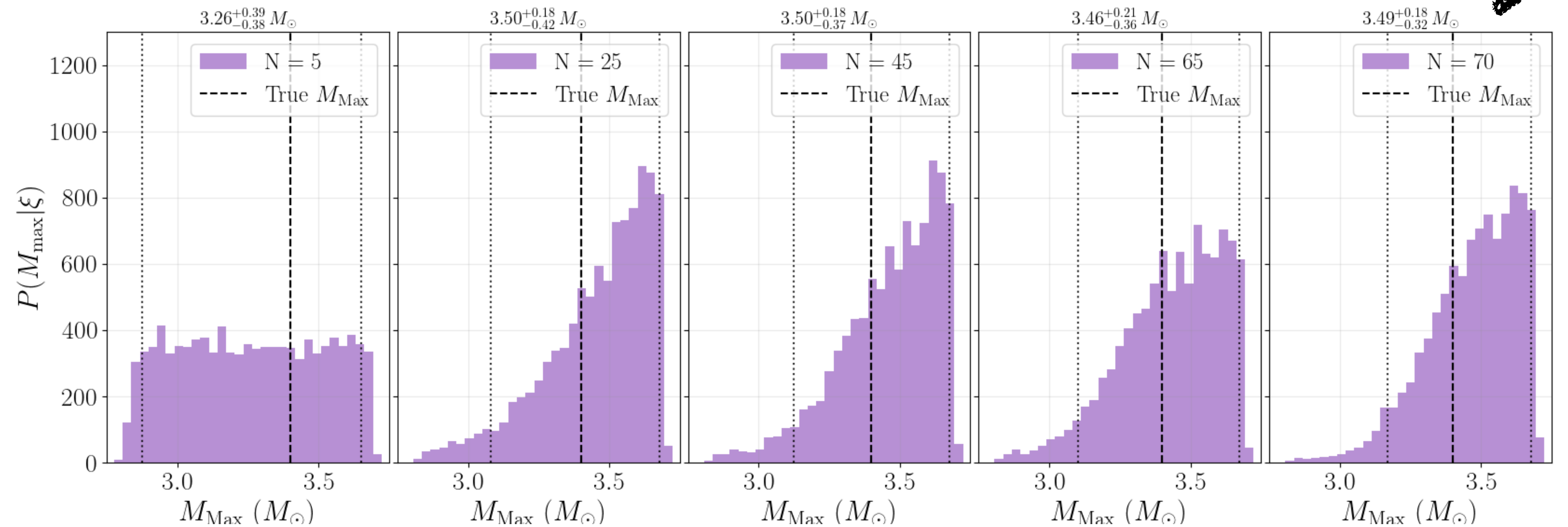
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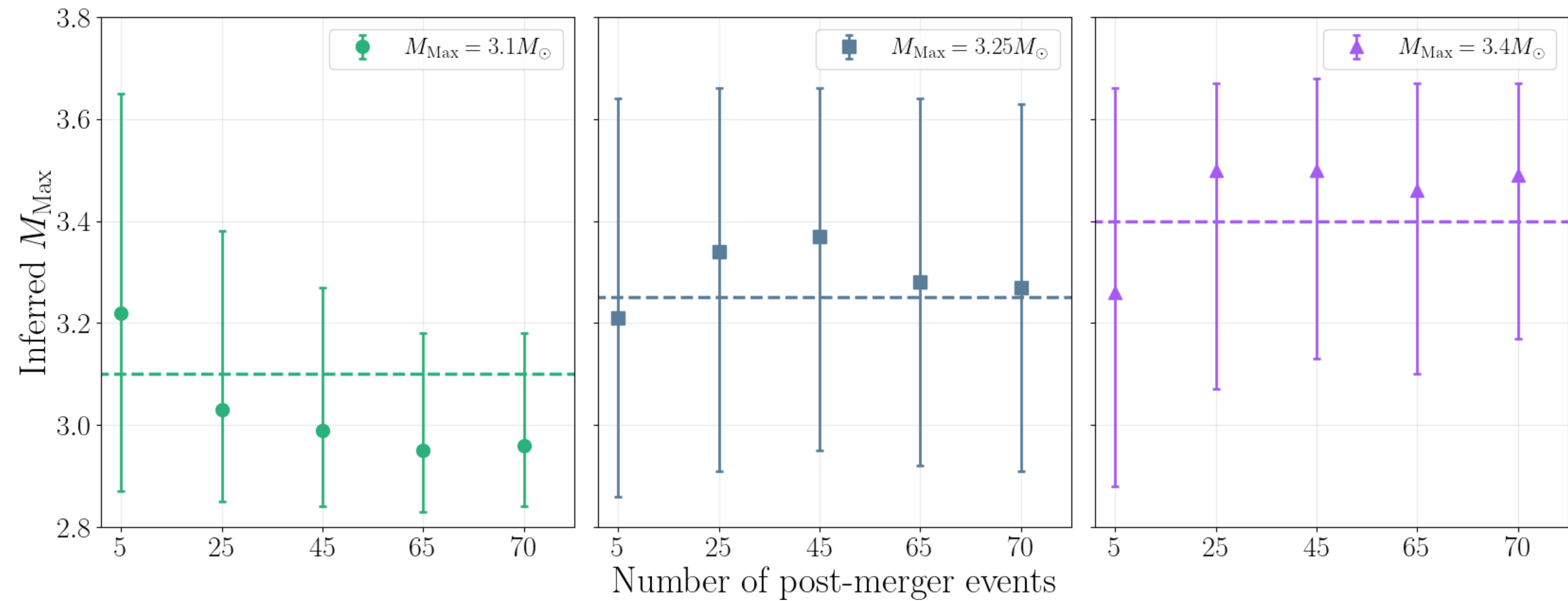
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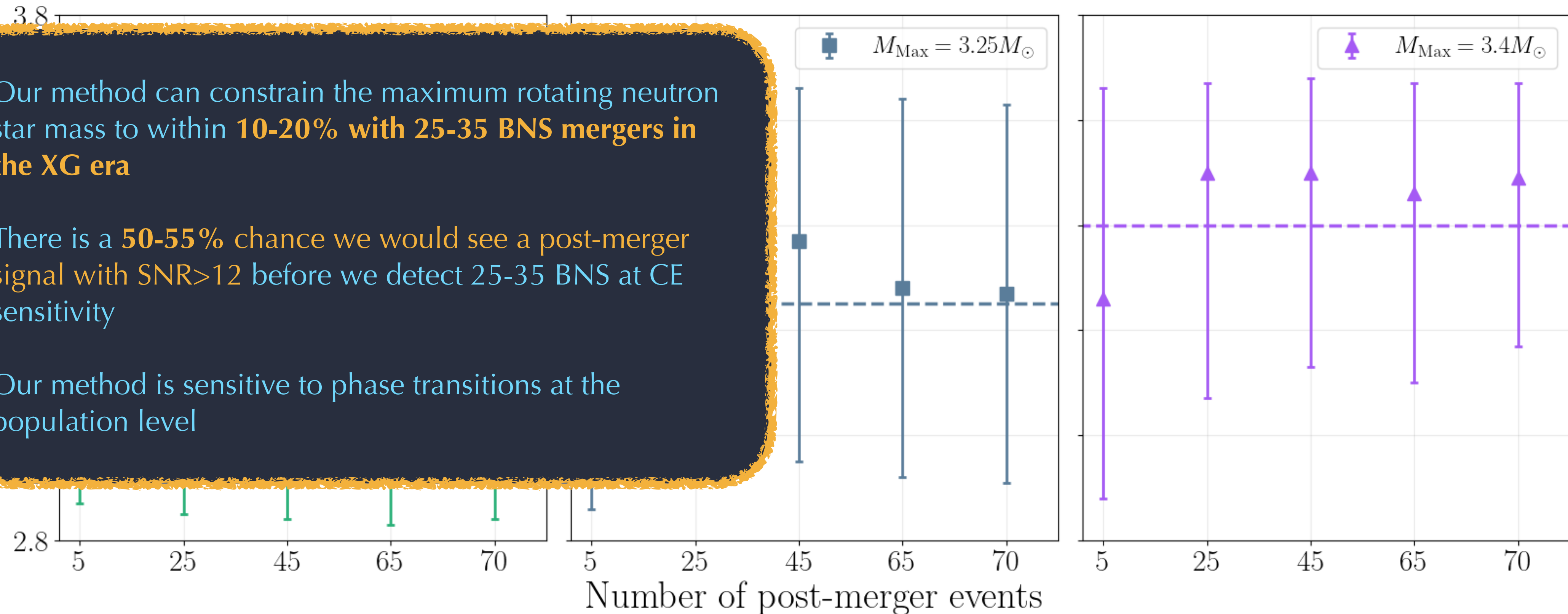
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Our method can constrain the maximum rotating neutron star mass to within **10-20%** with **25-35 BNS mergers in the XG era**

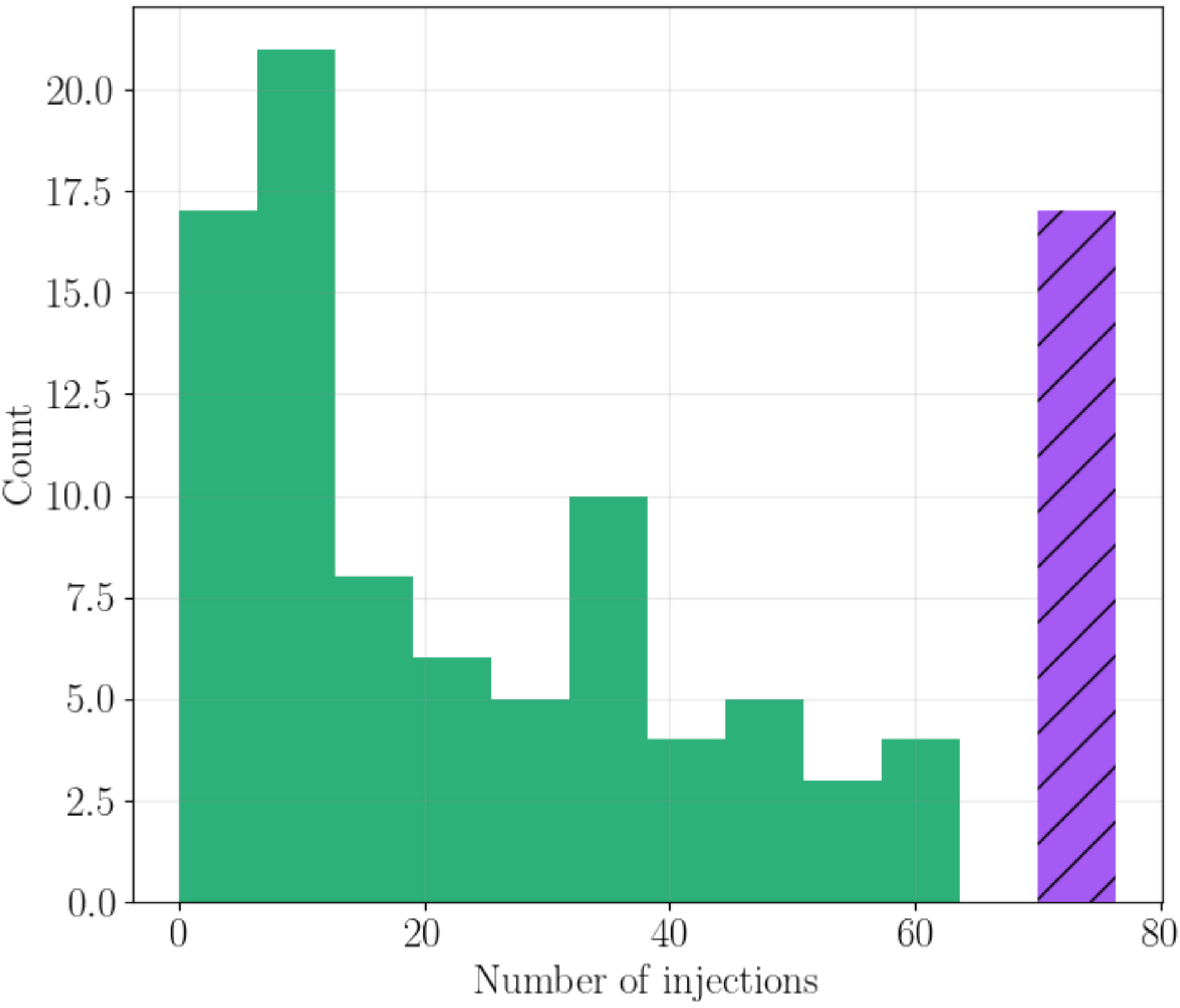
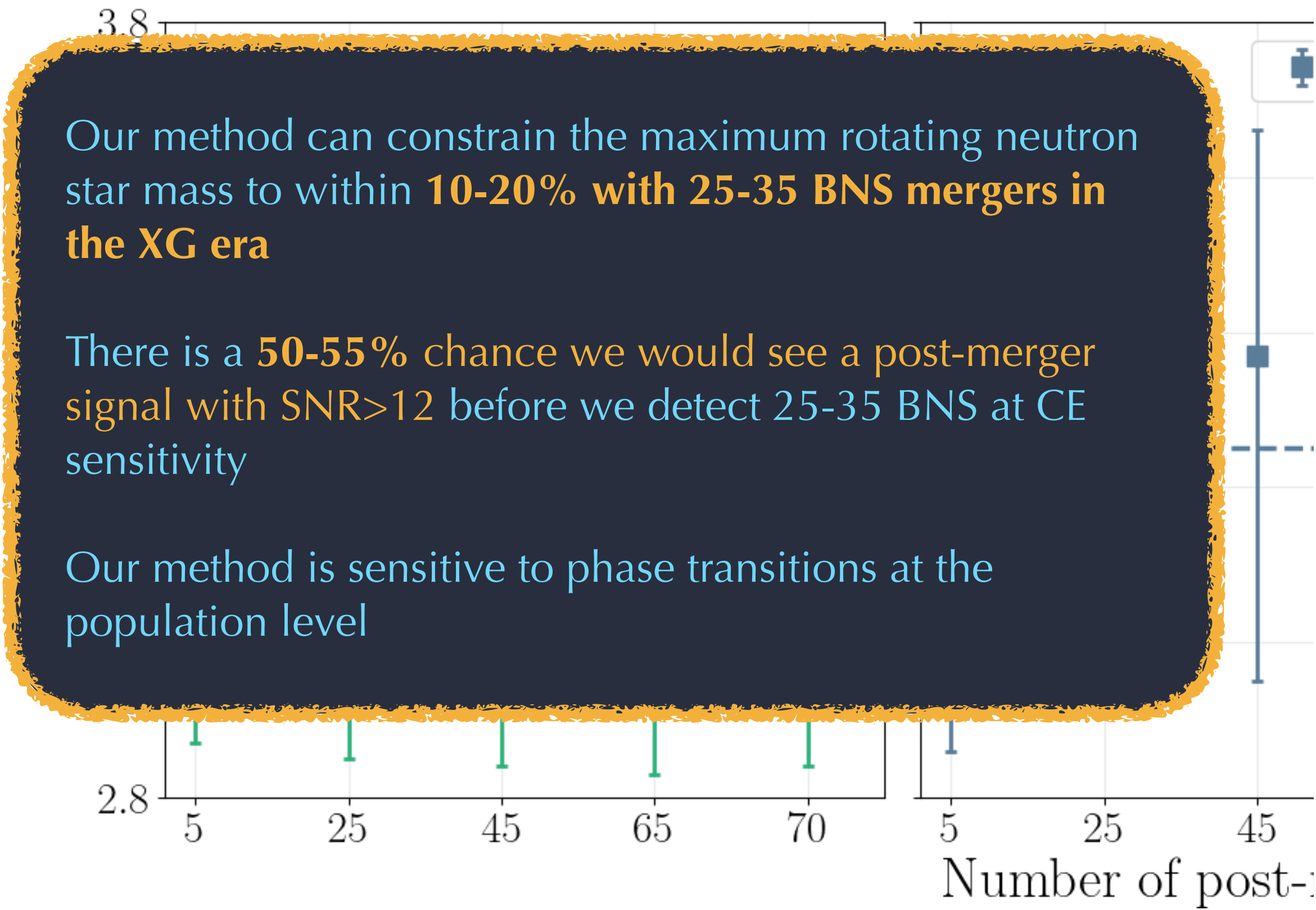
There is a **50-55%** chance we would see a post-merger signal with $\text{SNR} > 12$ before we detect 25-35 BNS at CE sensitivity

Our method is sensitive to phase transitions at the population level



Panther & Lasky 2026

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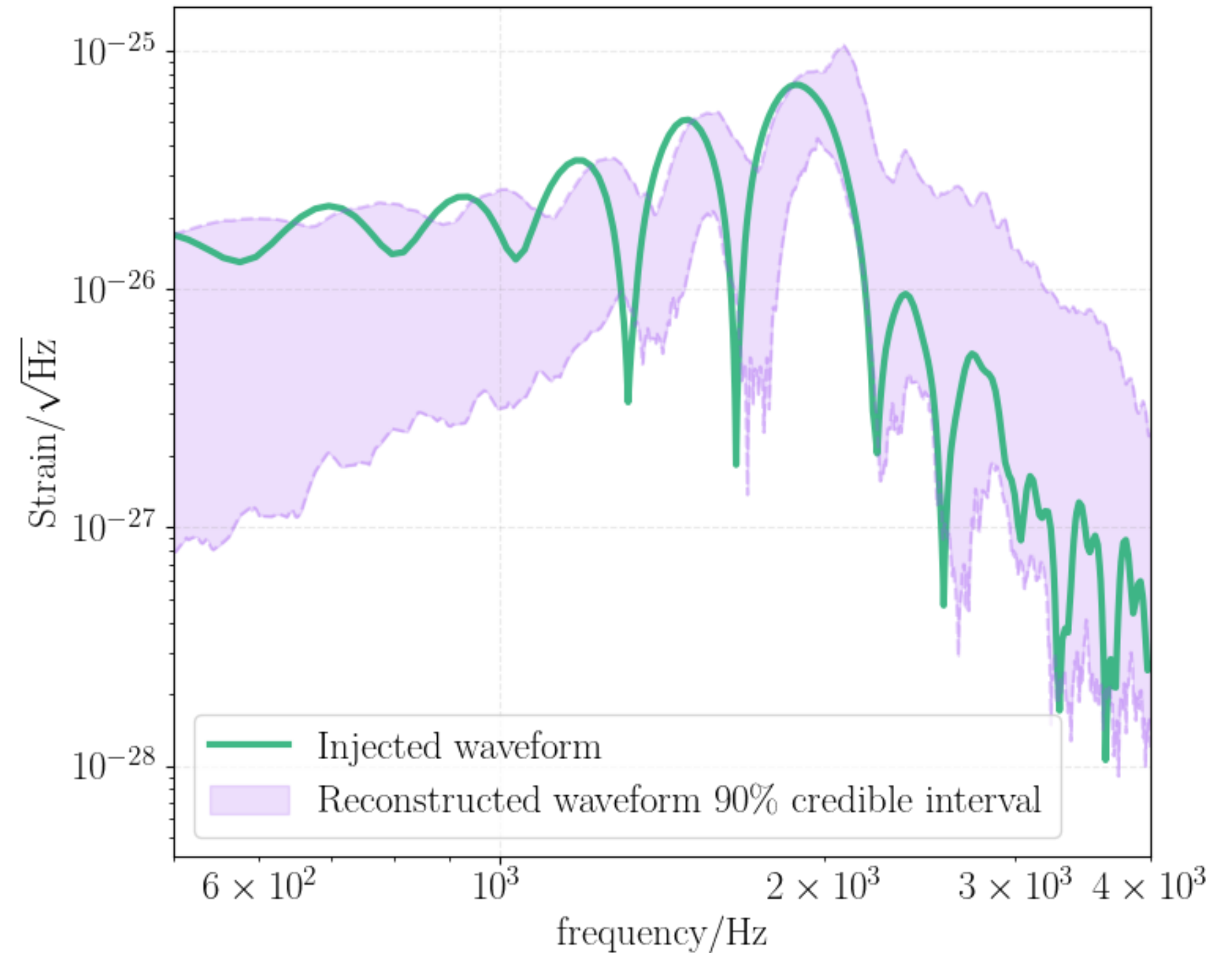
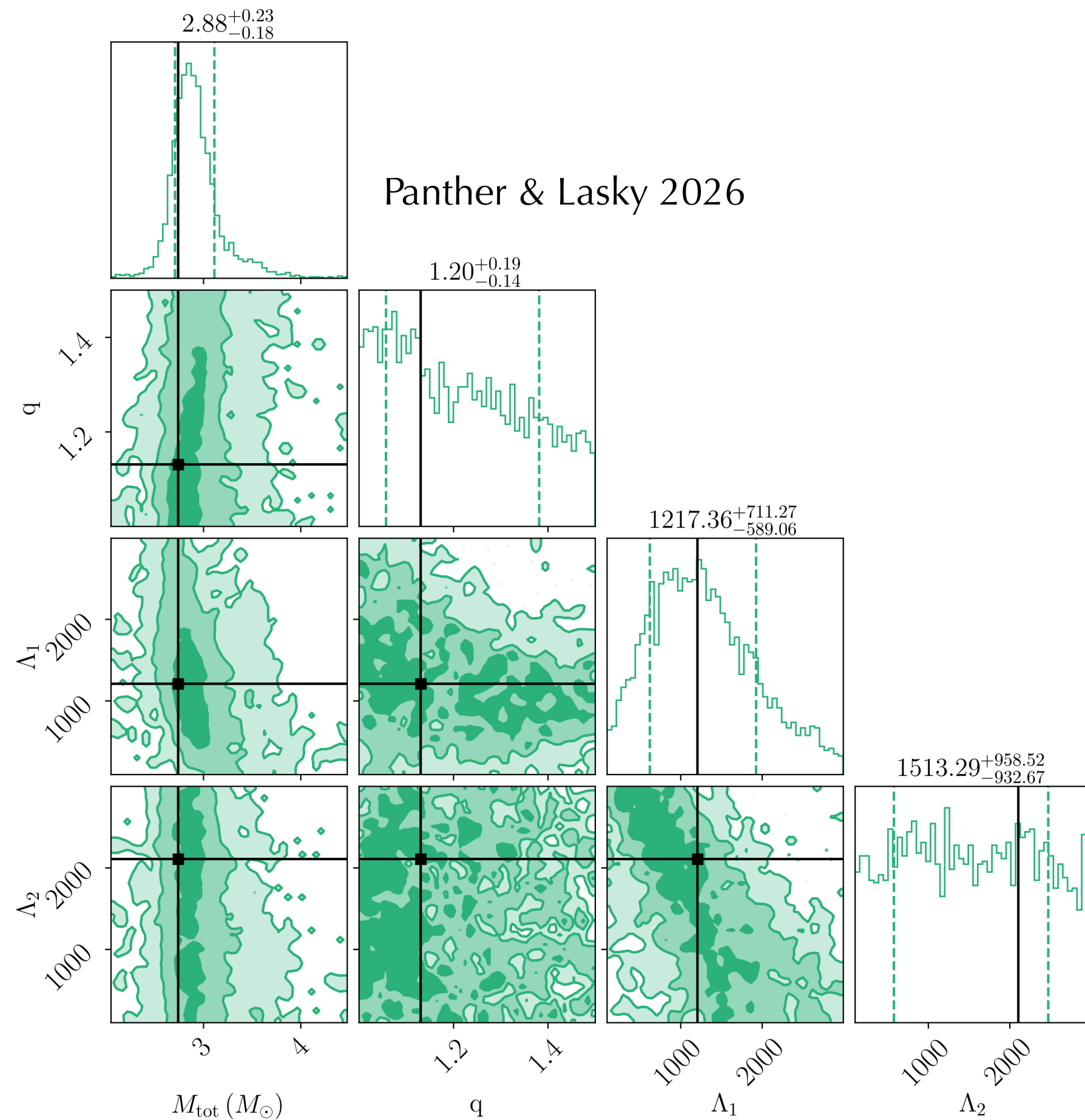
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- Inconsistencies in MTOV measured between post- and pre-merger can provide evidence for phase transitions between hadronic matter and QGP in extreme spacetime environments

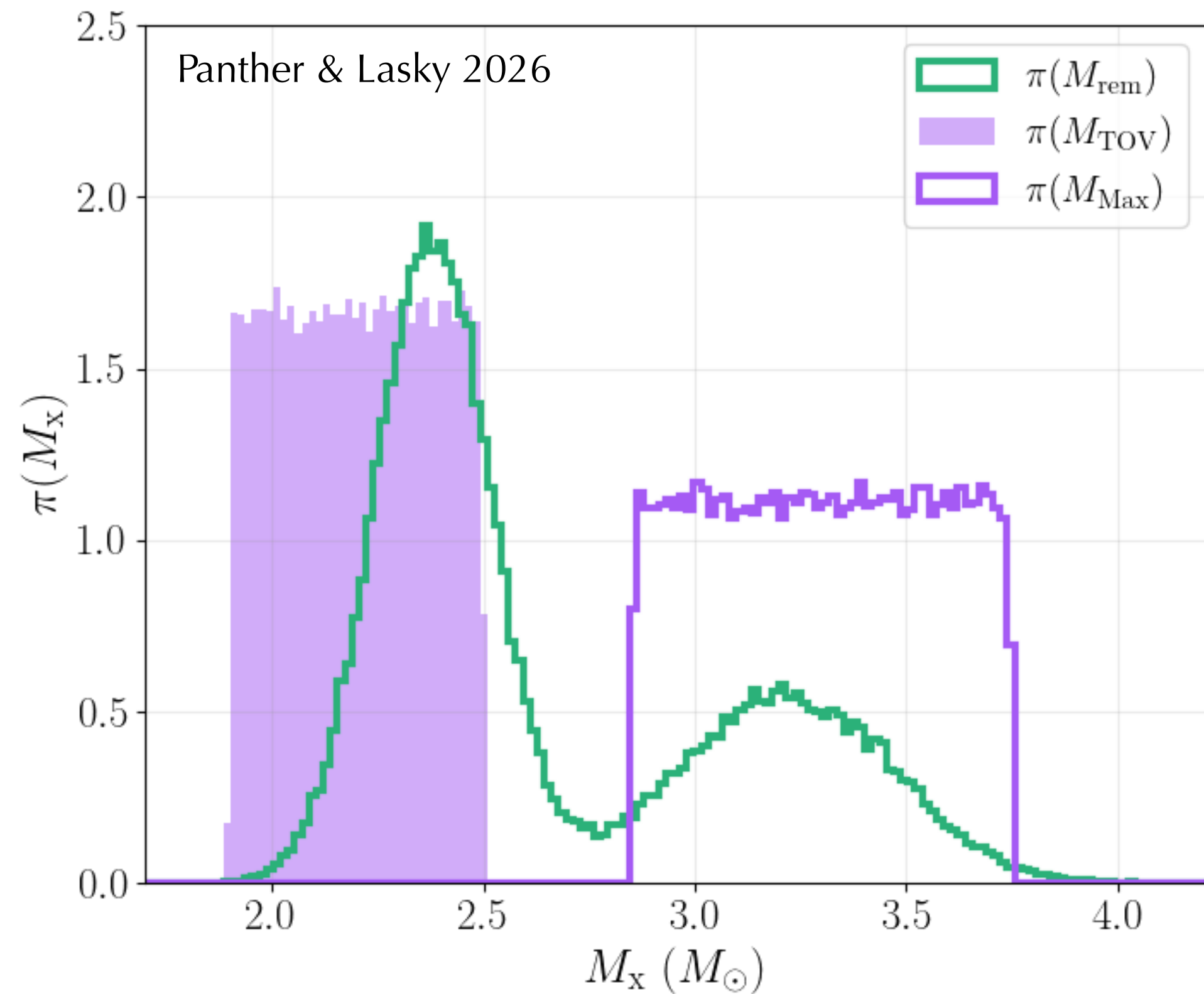
Individual PMNS parameter estimation

PE for individual events does not yield strong evidence for a signal being present, nor are the posteriors particularly informative



A mixture model formalism

We can obtain a posterior distribution on the mixing fraction - and hence M_{Max} - by using Bayes theorem

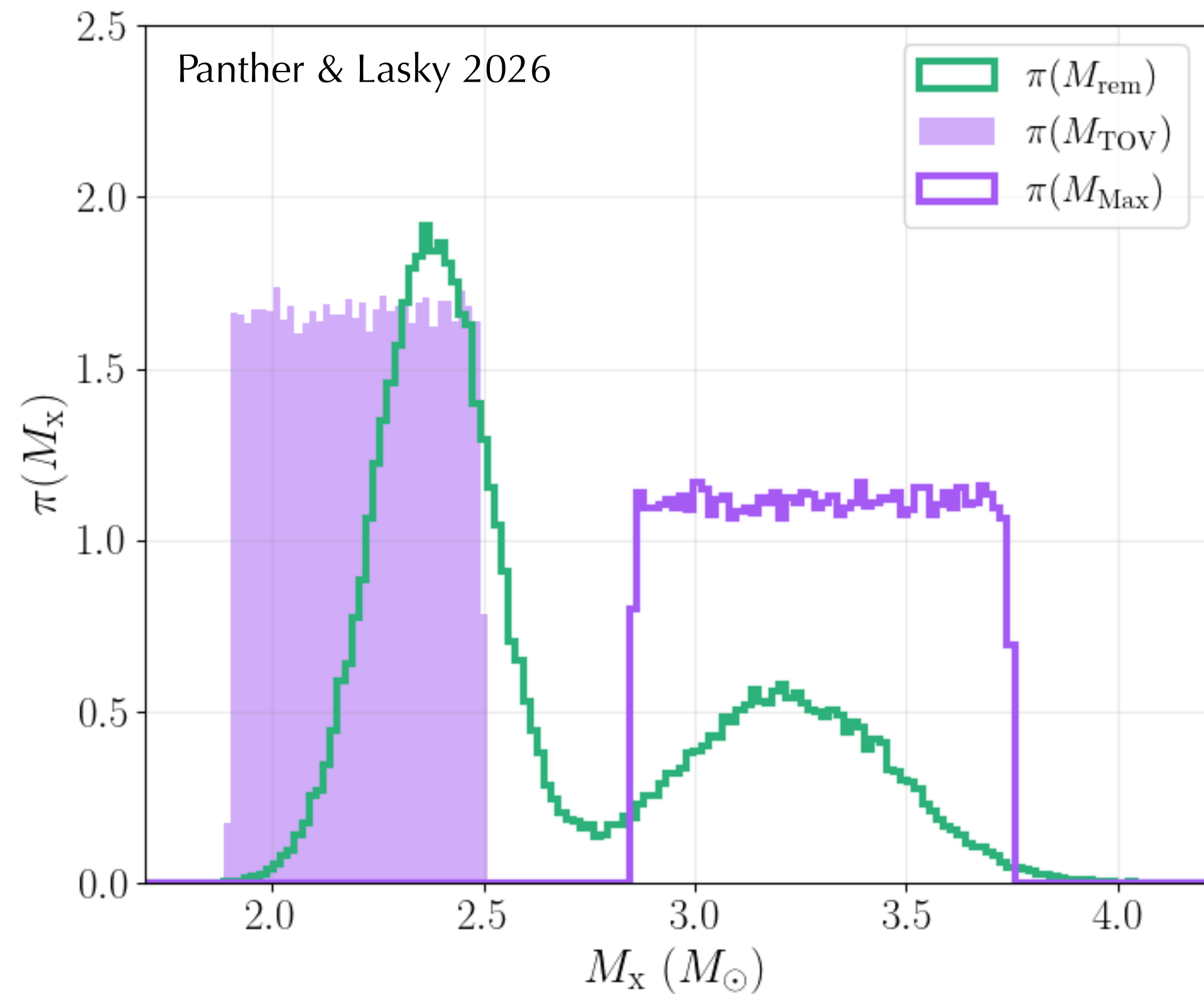


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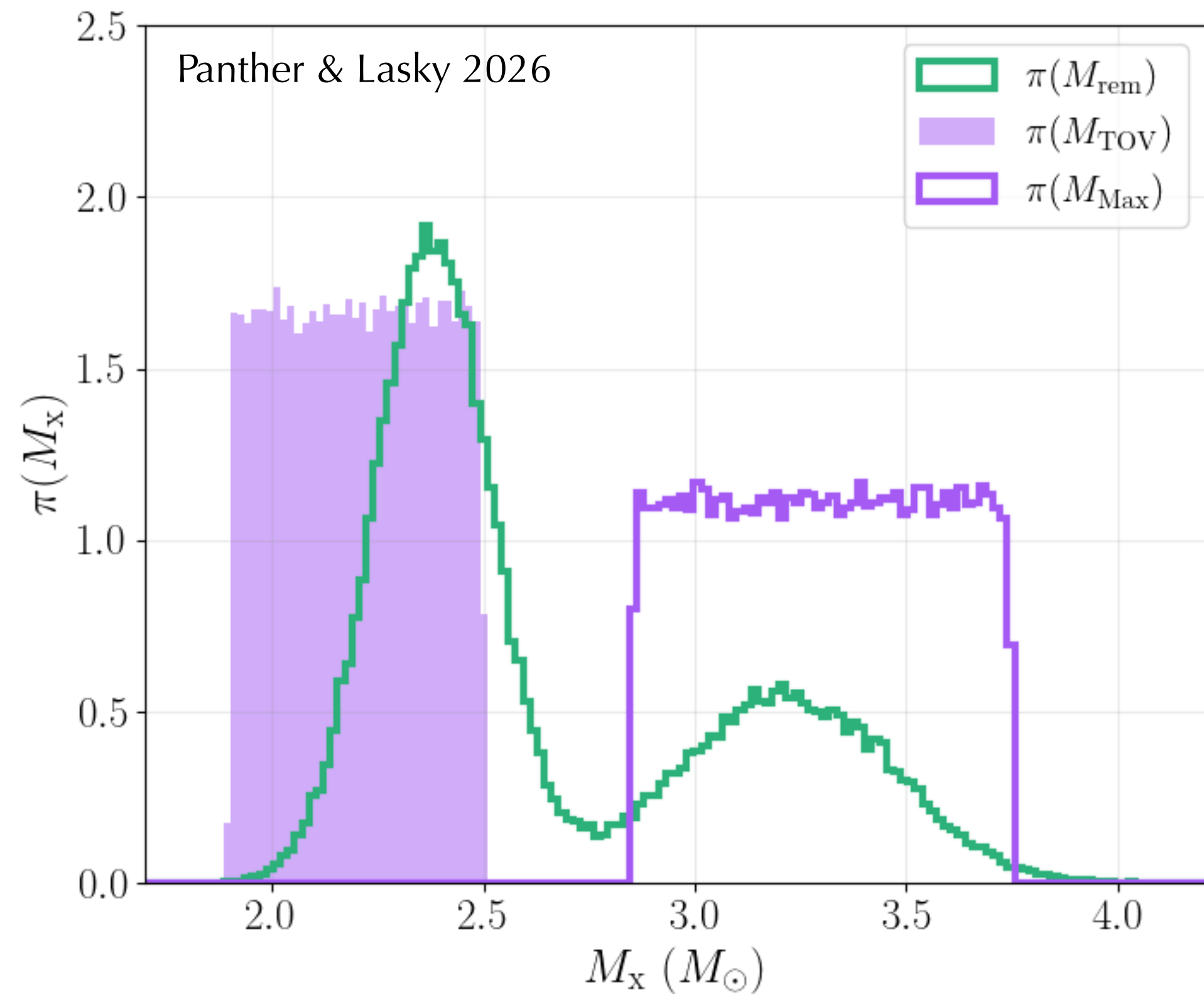
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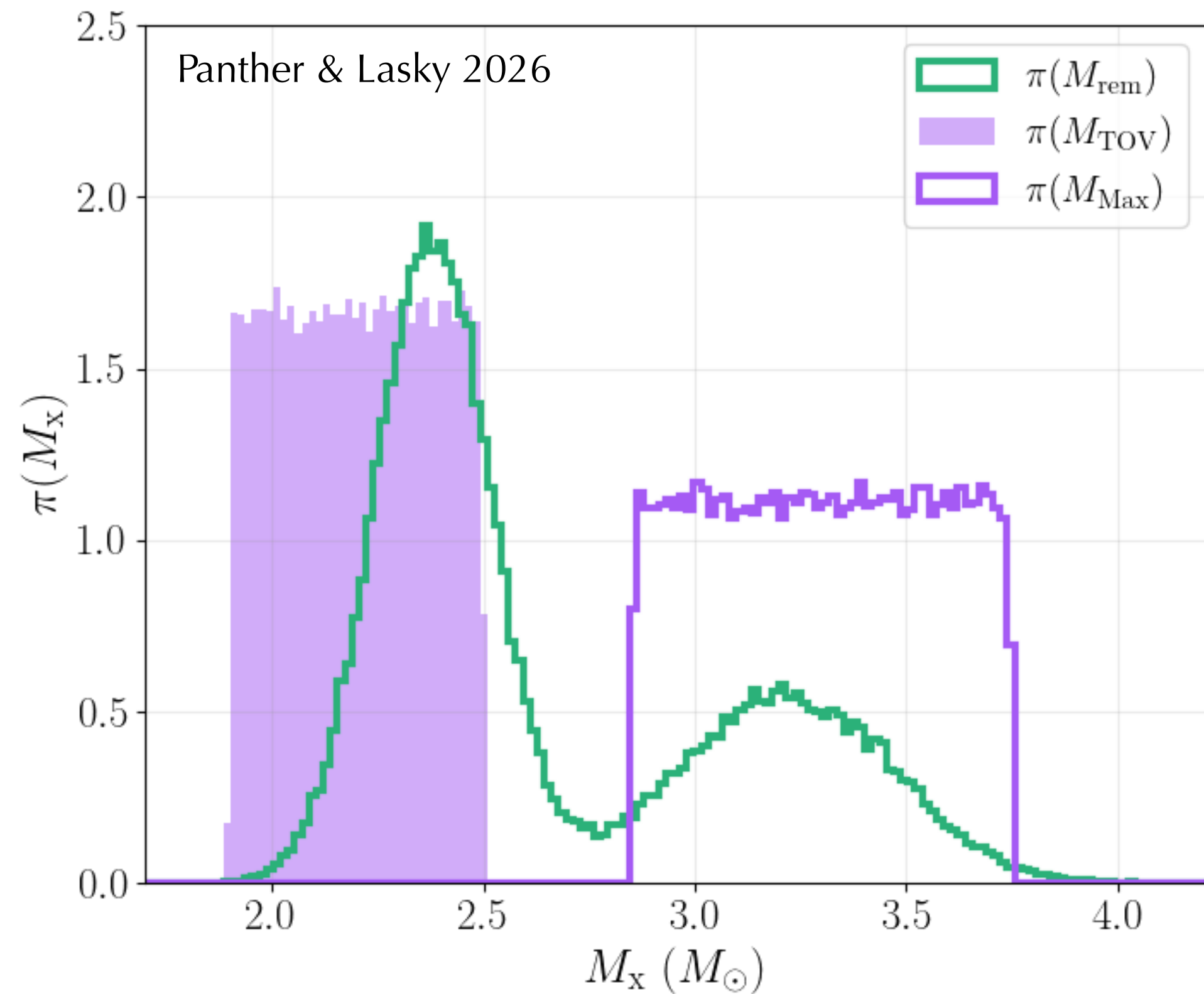
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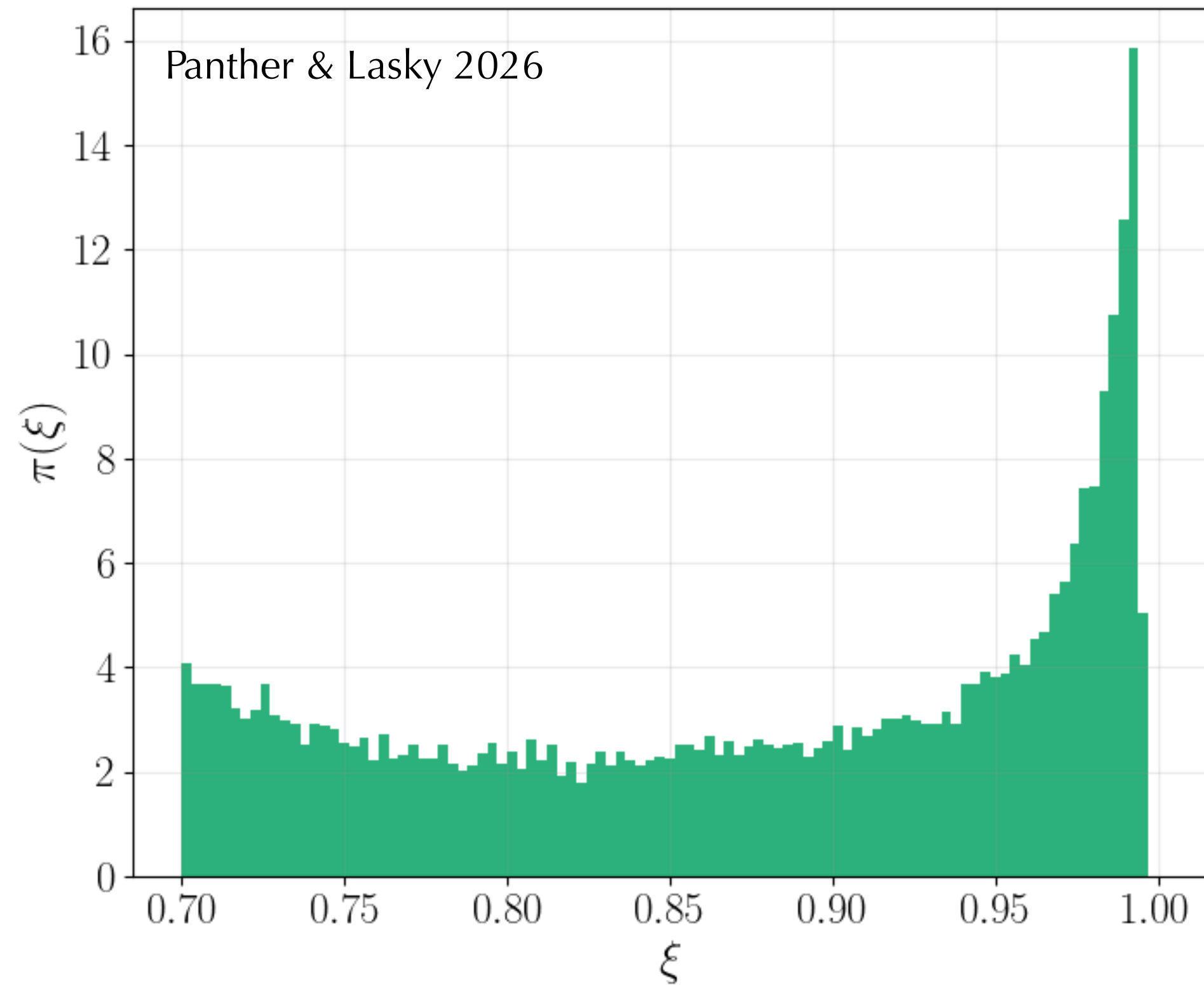
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$$\pi(\xi) = \frac{\int_0^{\pi(M_{\text{max}})} dM_{\text{rem}} \pi(M_{\text{rem}})}{\int_0^\infty dM_{\text{rem}} \pi(M_{\text{rem}})}$$

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Simulated data

We simulate a sample of 70 post-merger remnants for our ‘injection set’ and add them to coloured Gaussian noise

