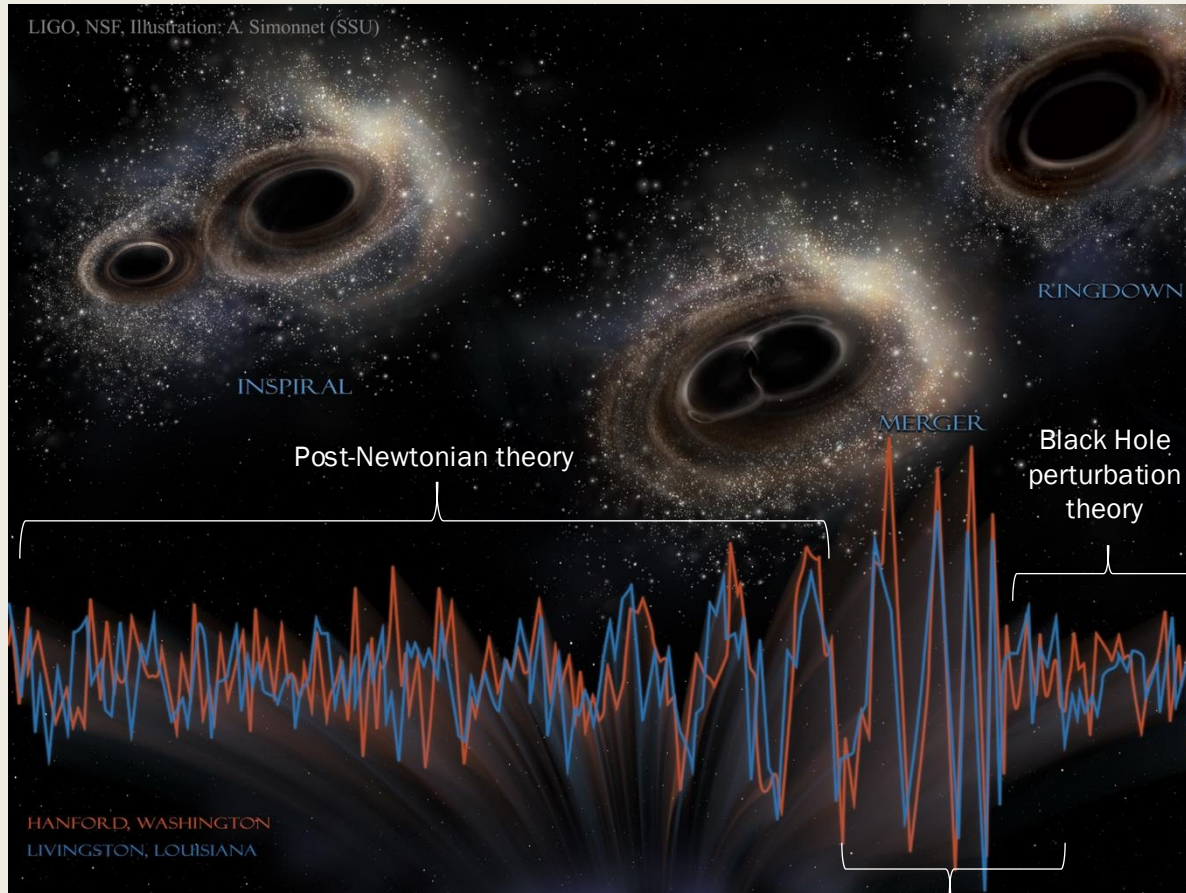


A thick black L-shaped frame is positioned around the text. It starts at the top-left corner, goes right, then down, then right again, and finally down to the bottom-right corner.

# DYNAMICS OF BLACK HOLE BINARIES

Matilde Garcia – BiCoQ conference 17/06



Numerical relativity

# MERGING BINARIES OF COMPACT OBJECTS ACROSS THE COSMOS

10 Years of Detections (2015-2024) of Compact Binary Coalescences with Black Holes and Neutron Stars

O1

O2

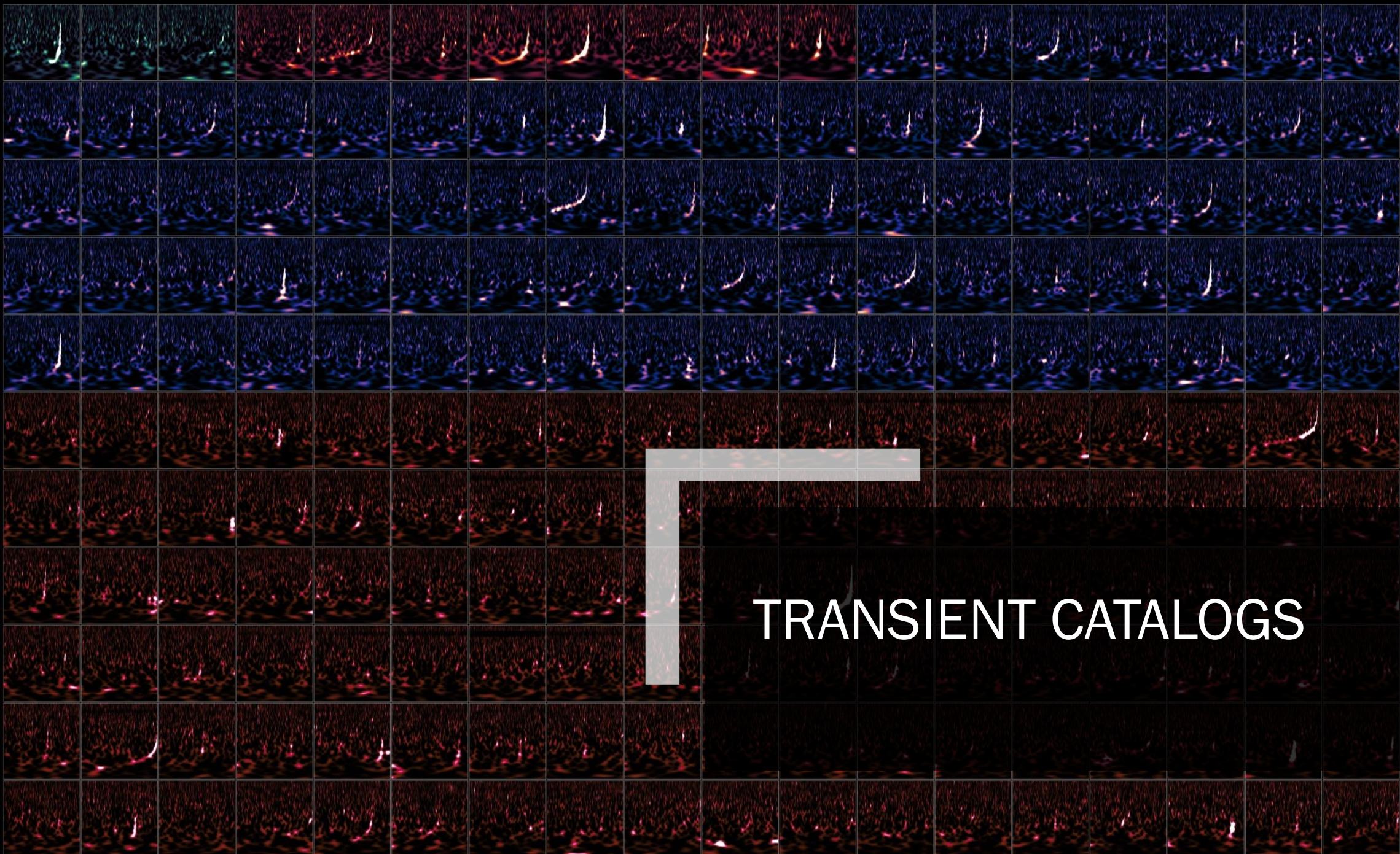
O3

O4a



TRANSIENT CATALOGS

↑



# Where do these binaries come from?

Different formation channels are predicted by theorists

- Dynamical formation channels – can leave imprints on gravitational wave signals
  - Eccentricity is smoking gun evidence that a binary was externally driven to form
- Isolated binaries – expected to circularize by the time they reach LVK's frequency band





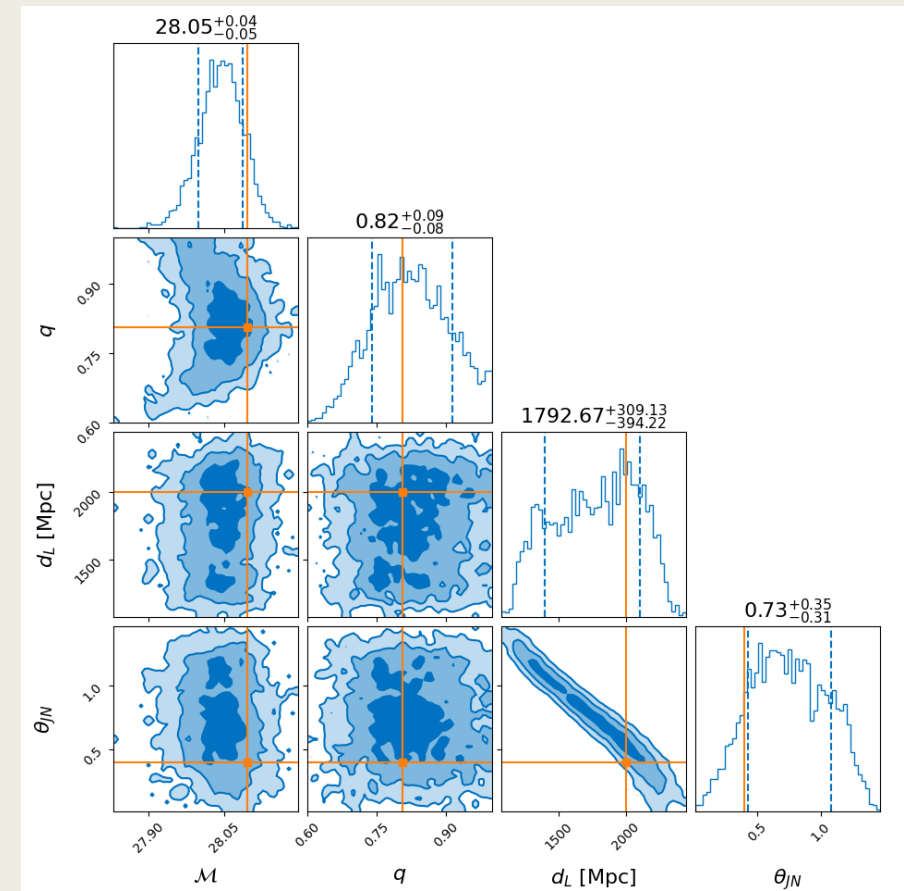
CRASH COURSE  
IN BAYESIAN  
INFERENCE FOR  
GWS



# Gravitational wave data analysis

- $\mathcal{L}(d | \theta) = \frac{1}{2\pi\sigma^2} \exp\left(-\frac{1}{2} \frac{|d - \mu(\theta)|^2}{\sigma^2}\right)$  - Likelihood, introduces a noise and waveform model
- $\pi(\theta)$  - Prior probability on the parameters
- $\mathcal{Z} = \int d\theta \mathcal{L}(d | \theta) \pi(\theta)$  - Evidence, normalizing factor / model comparison
- $p(\theta | d)$  - Posterior probability, ultimate goal of bayesian inference

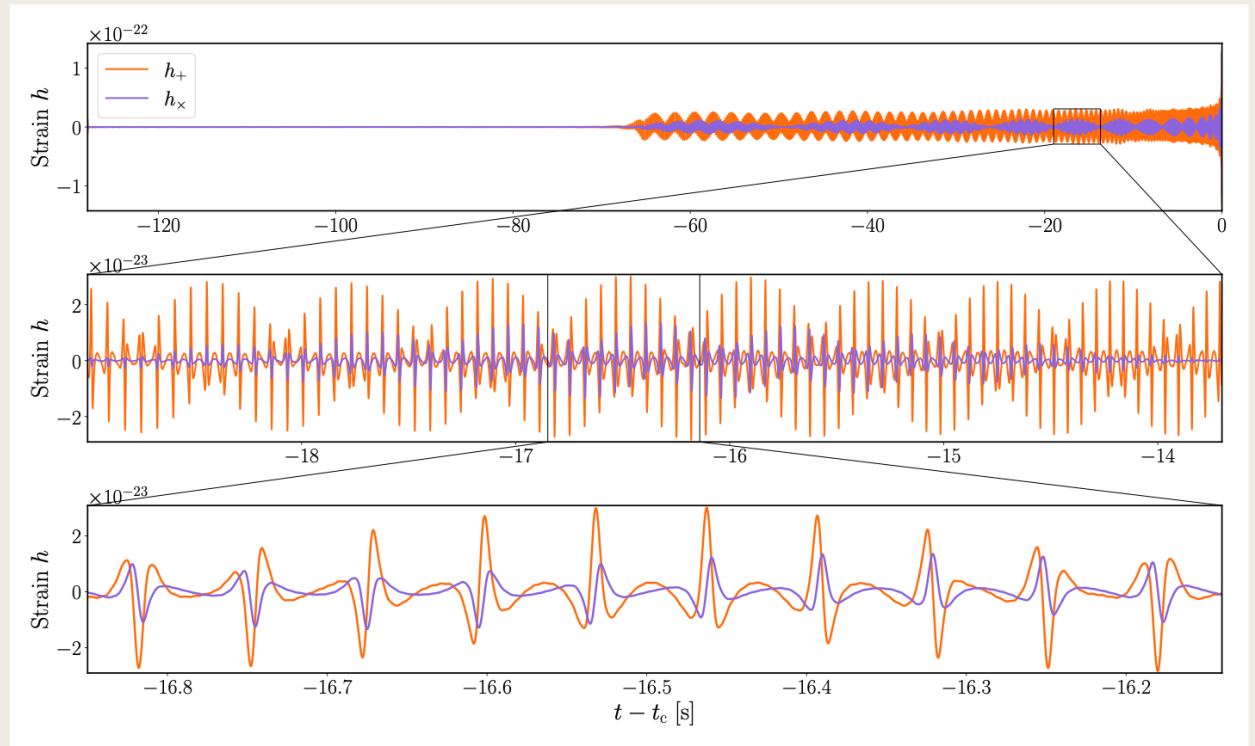
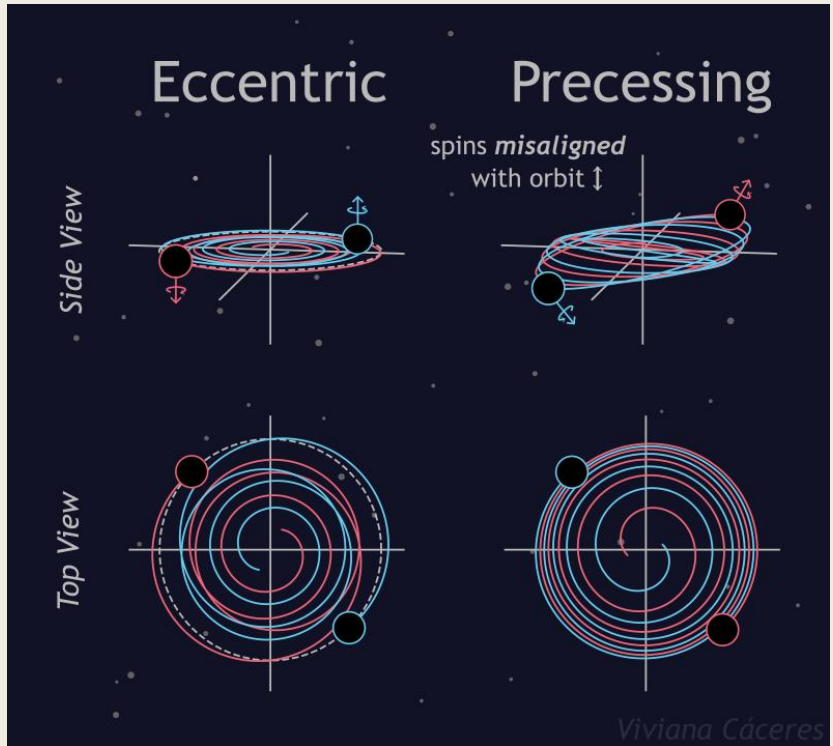
**BAYES THEOREM** 
$$p(\theta | d) = \frac{\mathcal{L}(d|\theta)\pi(\theta)}{\mathcal{Z}}$$





ECENTRICITY  
MEASUREMENTS  
CHALLENGES








# ECCENTRICITY – SPIN PRECESSION DEGENERACY

The two effects, in general, operate on different timescales

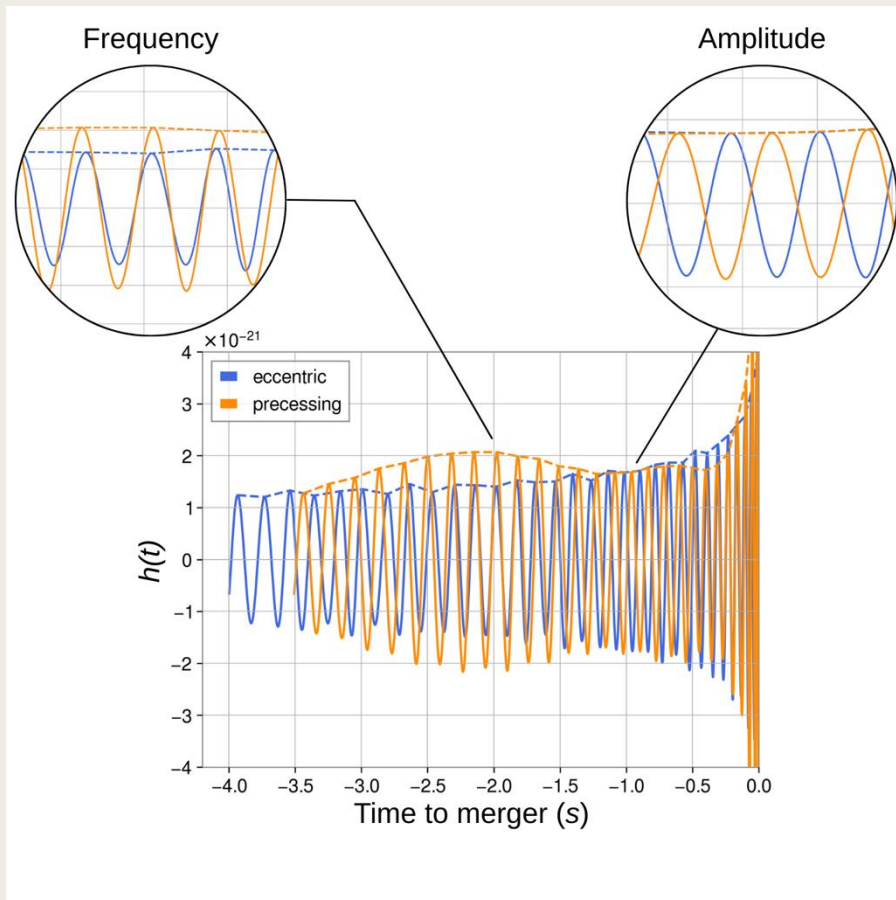
# However...

Eccentricity or spin precession? Distinguishing subdominant effects in gravitational-wave data

Isobel M. Romero-Shaw<sup>\*</sup> <sup>1,2,3</sup>, Davide Gerosa <sup>4,5,6</sup>, Nicholas Loutrel <sup>7</sup>

## Misinterpreting Spin Precession as Orbital Eccentricity in Gravitational-Wave Signals

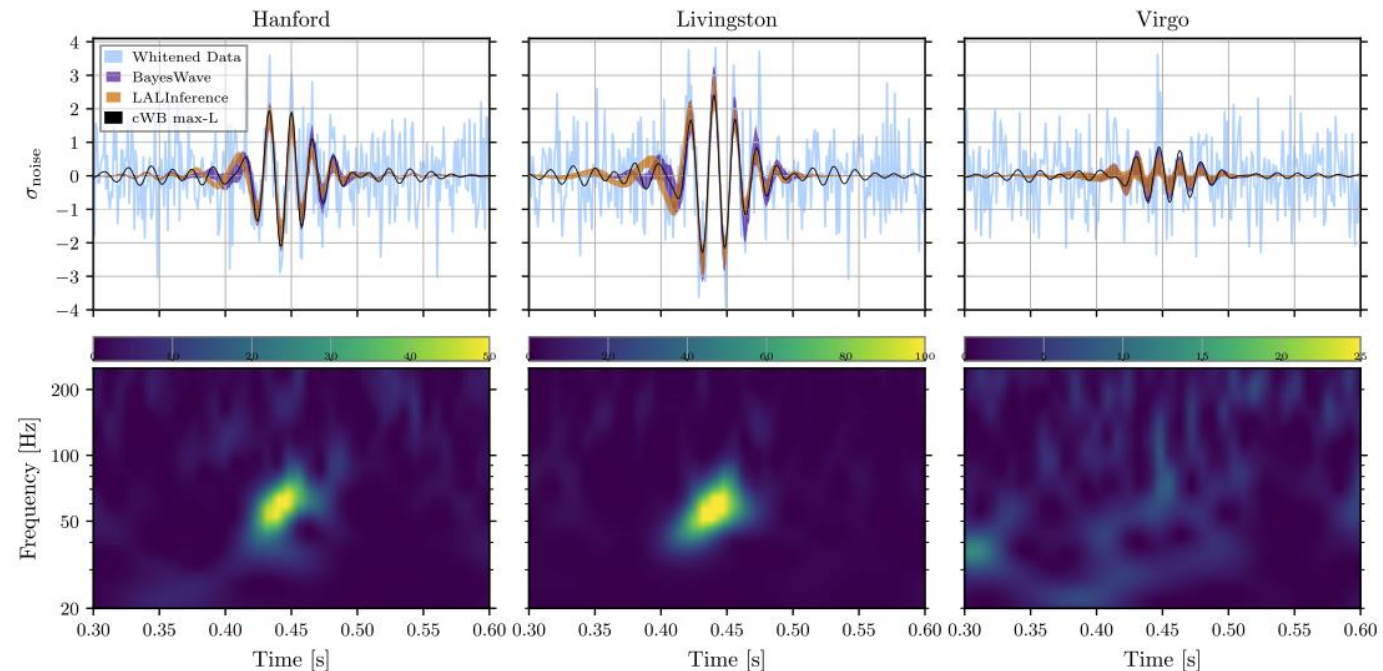
Snehal Tibrewal,<sup>1</sup> Aaron Zimmerman,<sup>1</sup> Jacob Lange,<sup>2,1</sup> and Deirdre Shoemaker<sup>1</sup>



For short signals, with only a few cycles in band, the two effects can become indistinguishable

## GW190521: A Binary Black Hole Merger with a Total Mass of $150 M_{\odot}$

R. Abbott *et al.*<sup>\*</sup>  
(LIGO Scientific Collaboration and Virgo Collaboration)



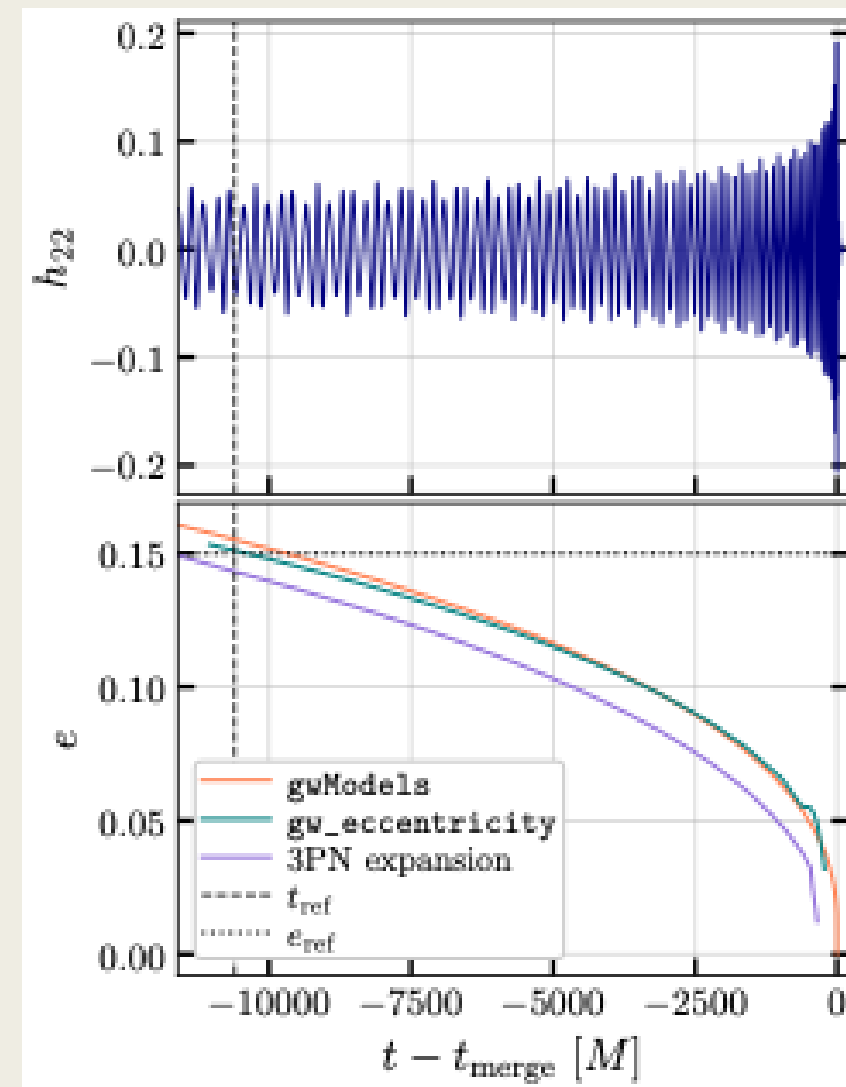
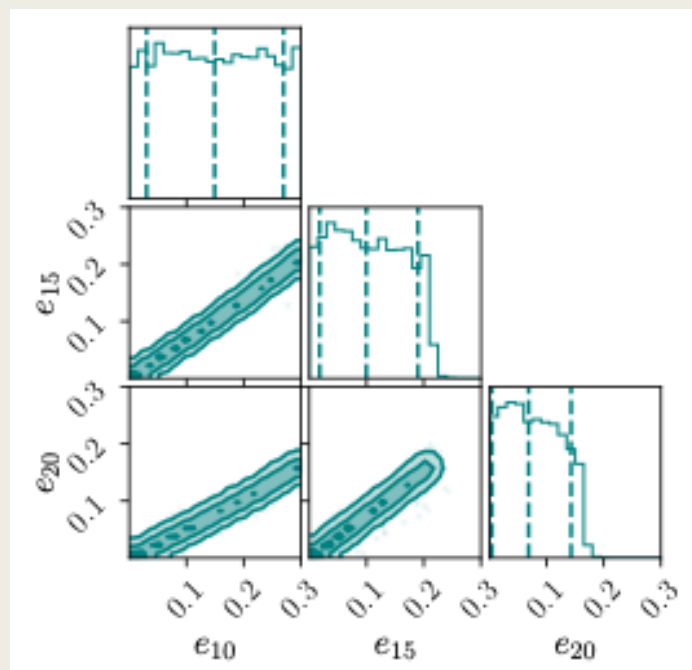
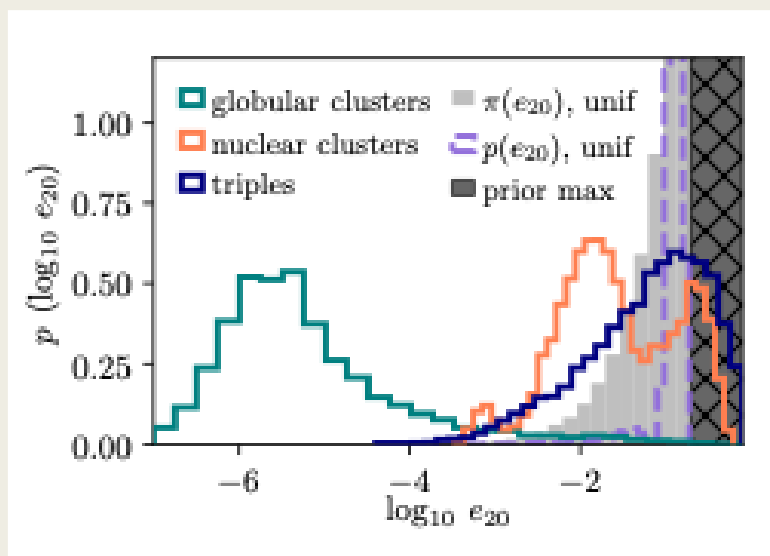
# Furthermore...

Recovered results are extremely prior dependent

Choice of eccentricity reference frequency

Ambiguous definitions of eccentricity

...





ECENTRICITY  
MEASUREMENTS  
ATTEMPTS



# Eccentric VS Spin precessing hypothesis testing

■  $\mathcal{Z} = \int d\theta \mathcal{L}(d | \theta) \pi(\theta)$  - Evidence, normalizing factor / model comparison

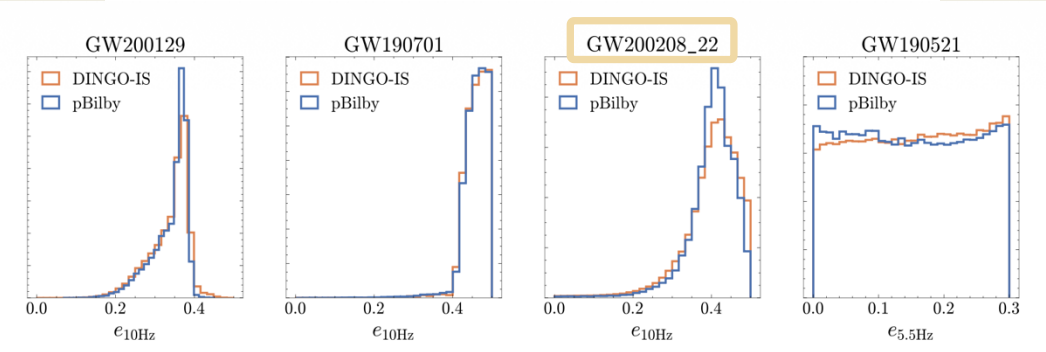
$\mu_1(\theta) \Rightarrow \mathcal{Z}_1$   
eccentric, spin aligned hypothesis

$\mu_2(\theta) \Rightarrow \mathcal{Z}_2$   
Quasi-circular, spin precessing hypothesis

Bayes factor  $\mathcal{Z}_1 / \mathcal{Z}_2$

Evidence for eccentricity in the population of binary black holes observed by LIGO-Virgo-KAGRA

Nihar Gupte,<sup>1,2</sup> Antoni Ramos-Buades,<sup>3,1</sup> Alessandra Buonanno,<sup>1,2</sup> Jonathan Gair,<sup>1</sup> M. Coleman Miller,<sup>4</sup> Maximilian Dax,<sup>5</sup> Stephen R. Green,<sup>6</sup> Michael Pürrer,<sup>7,8</sup> Jonas Wildberger,<sup>5</sup> Jakob Macke,<sup>5</sup> Isobel M. Romero-Shaw,<sup>9,10</sup> and Bernhard Schölkopf<sup>5</sup>



FOUR ECCENTRIC MERGERS INCREASE THE EVIDENCE THAT LIGO-VIRGO-KAGRA'S BINARY BLACK HOLES FORM DYNAMICALLY

Isobel Romero-Shaw,<sup>1,2,3</sup> Paul D. Lasky,<sup>1,2</sup> and Eric Thrane<sup>1</sup>

Event	$\ln \mathcal{B}_{E/P}(e_{10} \geq 0.1)$	$\ln \mathcal{B}_{E/P}(e_{10} \geq 0.05)$
GW190521	3.06	2.30
GW190620	2.52	2.10
GW191109	-1.74	-2.14
GW200208_22	1.51	0.96

# Accurate inspiral-only waveform models

- In theory:

Long enough signal (many inspiral cycles)

Accurate waveform models  $\mu(\theta)$  – both eccentric and spin precessing

Appropriate choice of priors, data glitch mitigation ...

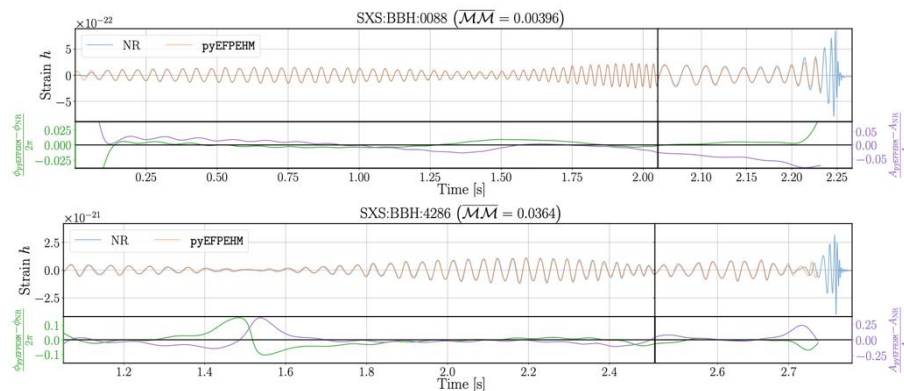
Somehow confident eccentricity measurement

- It has been done!

(For very light systems of NS and BHNS)

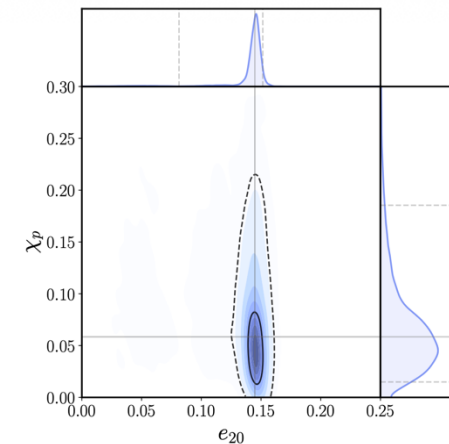
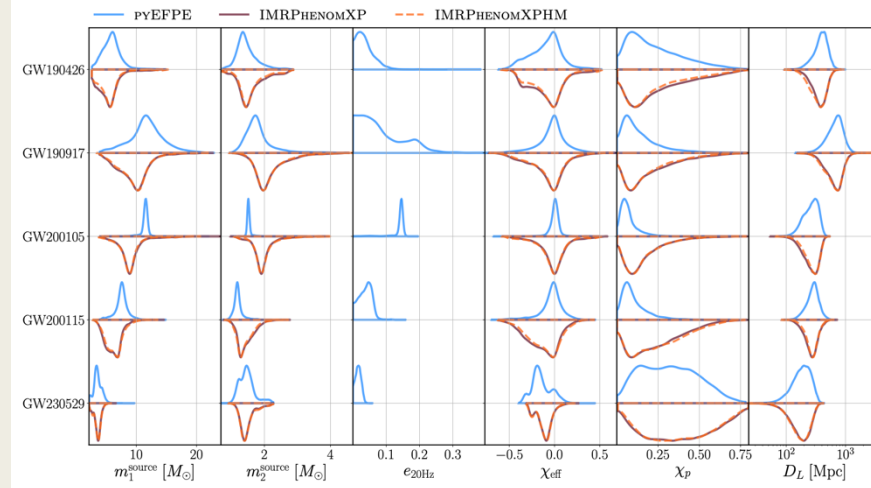
Post-Newtonian inspiral waveform model for eccentric precessing binaries with higher-order modes and matter effects

Gonzalo Morras <sup>1,2,\*</sup>, Geraint Pratten <sup>3</sup>, Patricia Schmidt <sup>3</sup> and Alessandra Buonanno <sup>1,4</sup>



Impact of eccentricity on the population properties of neutron star – black hole mergers

GONZALO MORRAS <sup>1,2</sup>, GERAINT PRATTEN <sup>3</sup> AND PATRICIA SCHMIDT <sup>3</sup>



# Accurate inspiral-only waveform models

- For NS and BH-NS binaries, there are a lot of inspiral cycles within band

(in fact, the merger is often too high-frequency to be visible)



Using inspiral-only waveforms is not a problem

- For BBH binaries ...

GW200208\_222617 as an eccentric black-hole binary merger: properties and astrophysical implications

Isobel Romero-Shaw<sup>1,2,3,\*</sup> Jakob Stegmann<sup>4</sup> Hiromichi Tagawa,<sup>5</sup> Davide Gerosa<sup>6,7</sup> Johan Samsing,<sup>8</sup> Nihar Gupta<sup>9,10</sup> and Stephen R. Green<sup>11</sup>

- Relatively low mass
- Many visible inspiral cycles
- No (known) data issues (glitch-free)



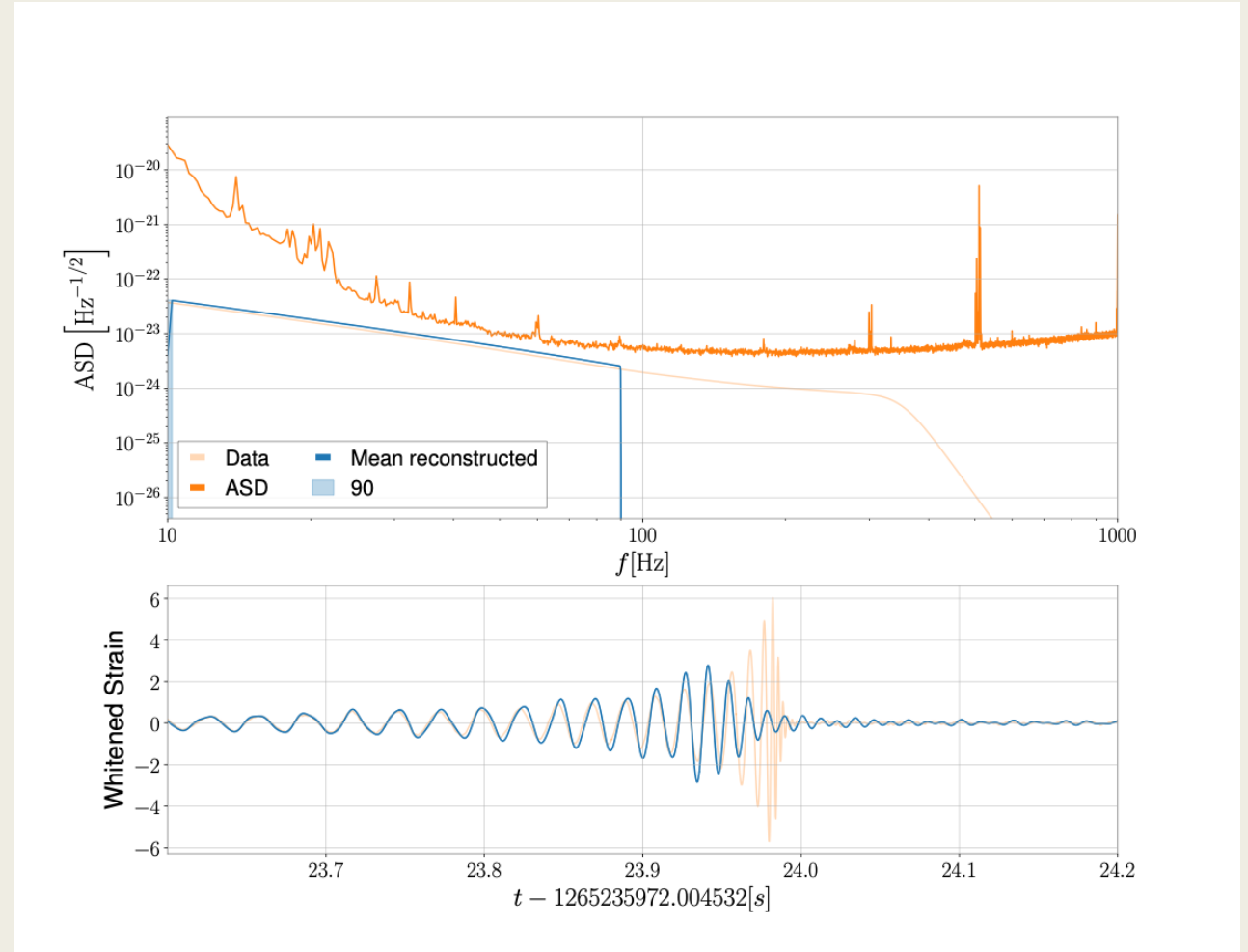
Using inspiral-only waveforms is a problem!!

# The problem of inspiral-only waveforms

- Even for relatively light BBH– in the same frequency range, we have inspiral-merger-ringdown data, but only inspiral model...

$$\mathcal{L}(d | \theta) = \frac{1}{2\pi\sigma^2} \exp\left(-\frac{1}{2} \frac{|d - \mu(\theta)|^2}{\sigma^2}\right)$$

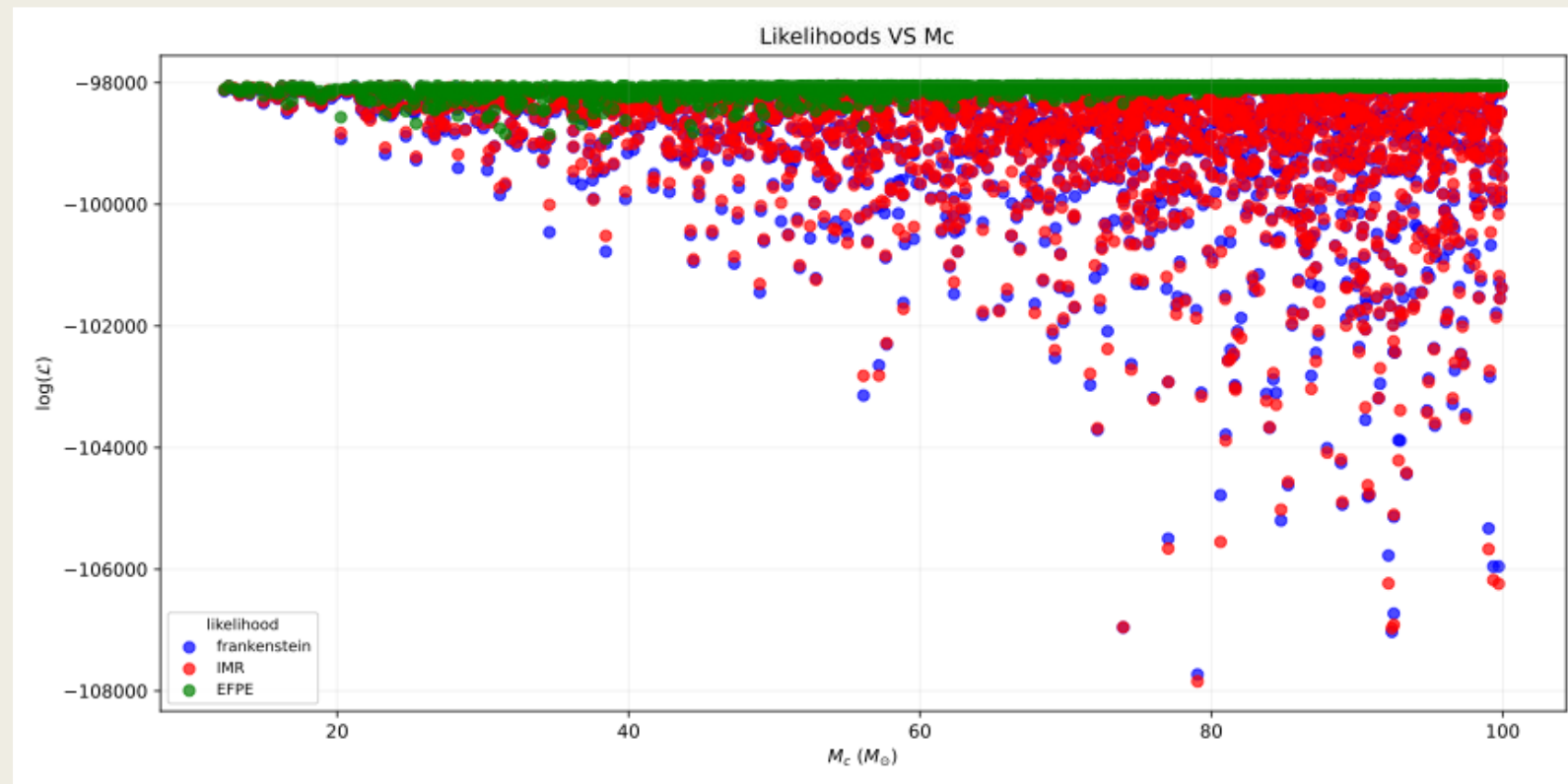
an integral across frequencies of the noise weighted inner product of the signal with the model



# The problem of inspiral-only waveform models

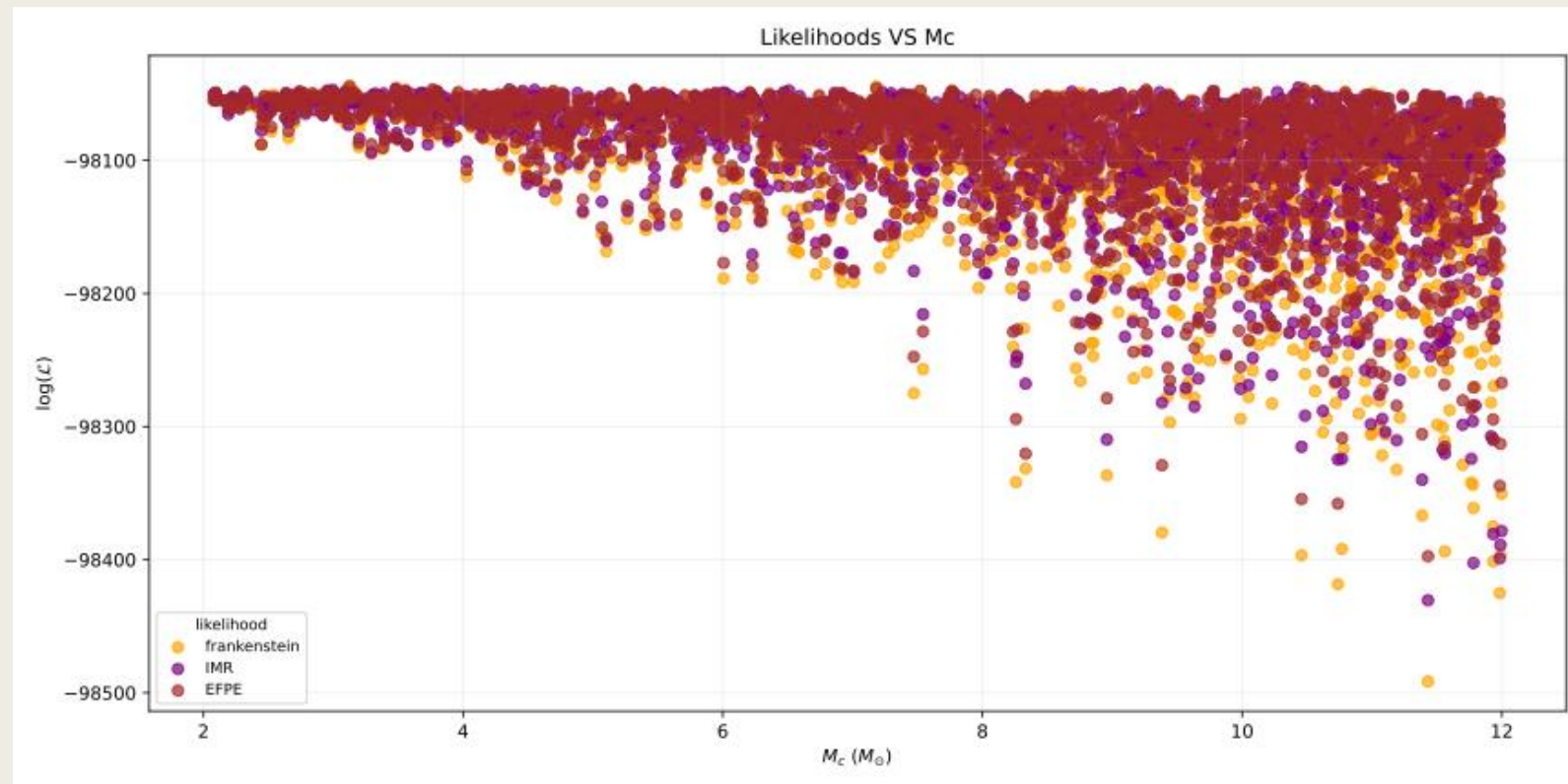
$$\mathcal{L}(d | \theta) = \frac{1}{2\pi\sigma^2} \exp\left(-\frac{1}{2} \frac{|d - \mu(\theta)|^2}{\sigma^2}\right)$$

- A large amount of the frequency range has model  $\mu = 0$  for BBH
- $\mathcal{L}(d_1 | \mathcal{M}_c)$  - BBH data set, inspiral only model



# The problem of inspiral-only waveform models

- For lighter binaries – in the same frequency range, we have only inspiral data, and only inspiral model...
- $\mathcal{L}(d_2 | \mathcal{M}_c)$  - BNS data set, inspiral only model

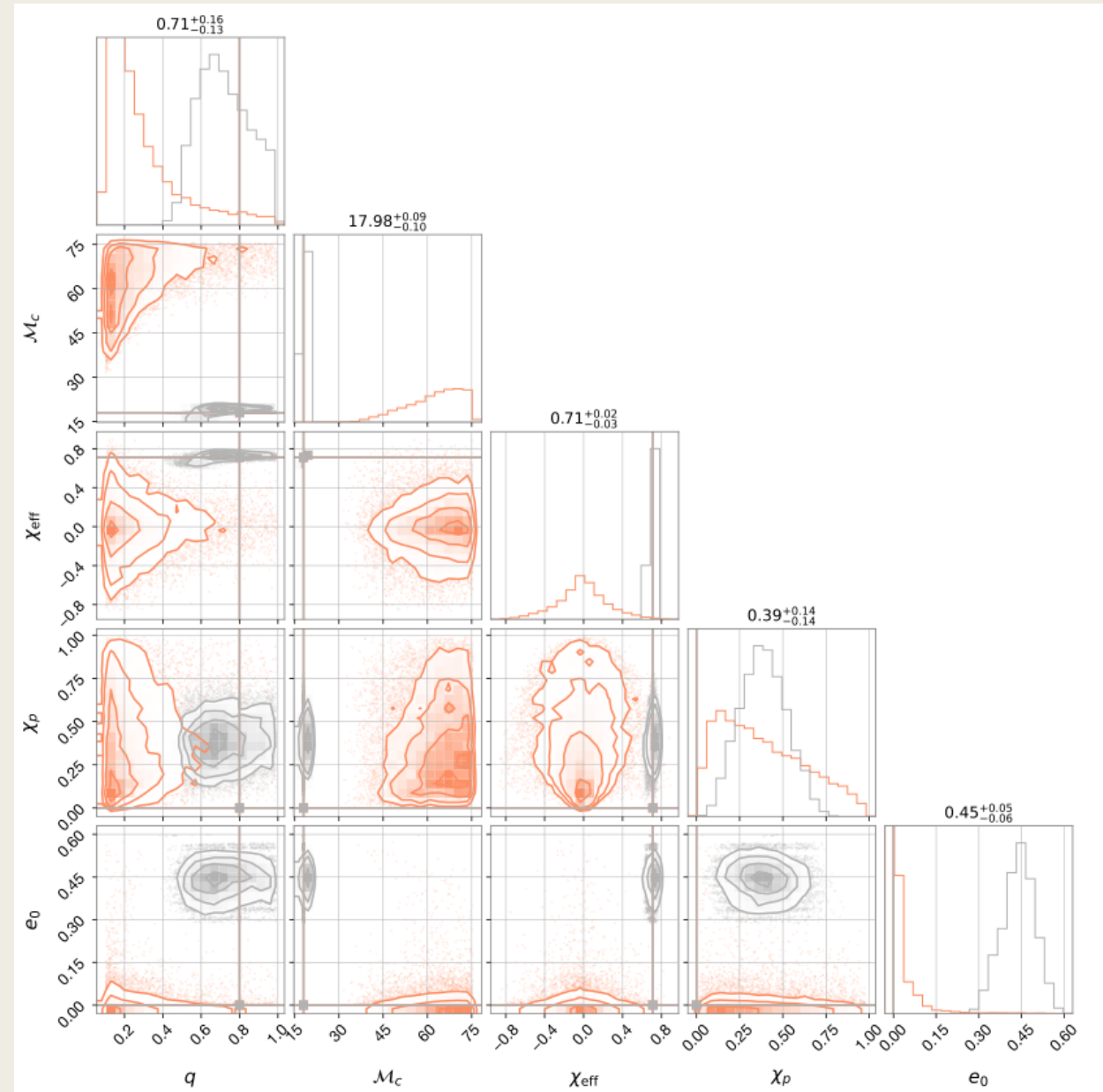


# Possible solutions

1. Cropping the high frequency content of the data (questionable approach)
2. “Patching” a similar but non eccentric waveform to analyze the merger-ringdown part of the signal (to be determined, biased results?)
3. “Patching” a non physical model (spline) (to be determined, model complexity?)

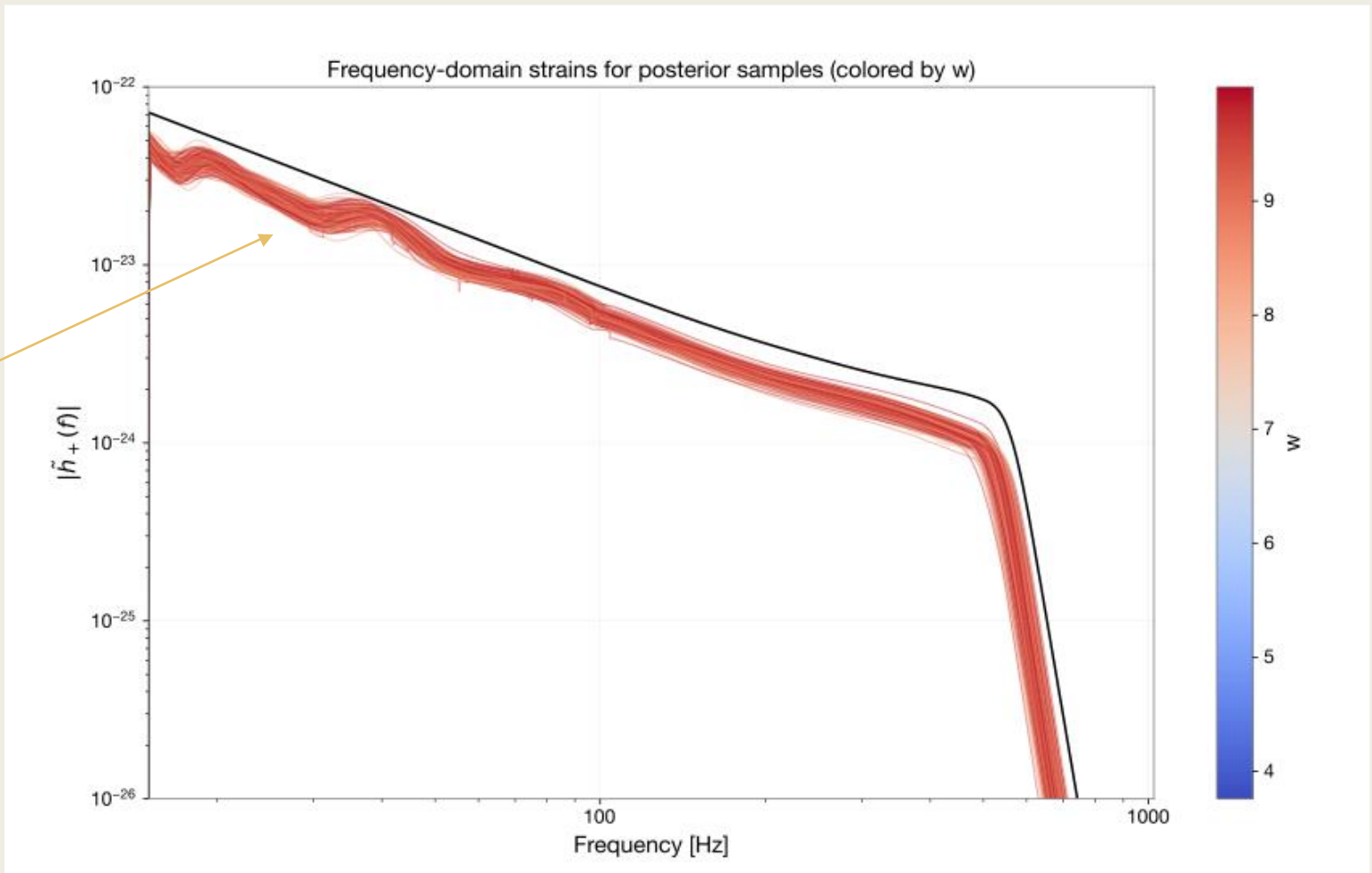
# Preliminary results

- Patching a precessing (non eccentric) waveform to our waveform model for the Merger-Ringdown part of the signal
- Biased results - common inspiral-merger-ringdown parameters are extremely different from the **inspiral parameters** of the inspiral + merger ringdown model



# Preliminary results – bad news

- Inspiral model seems to prefer precessing dynamics





HOPEFULLY, MORE  
AND BETTER  
RESULTS TO COME

...

# Conclusions

- Eccentricity is smoking gun evidence of dynamical formation of binary black holes
- It's very hard to measure it in GW signals (for several other reasons, but):
  - *We can have IMR (inspiral-merger-ringdown) + only eccentric analysis*
  - *We can have IMR + only precessing analysis*
  - *We can have eccentric + precessing but no MR analysis*
- Attempts have been and are being made, but so far there has not been an eccentricity claim on a BBH signal that directly tackled the eccentricity – spin precession degeneracy



**THANK  
YOU!**