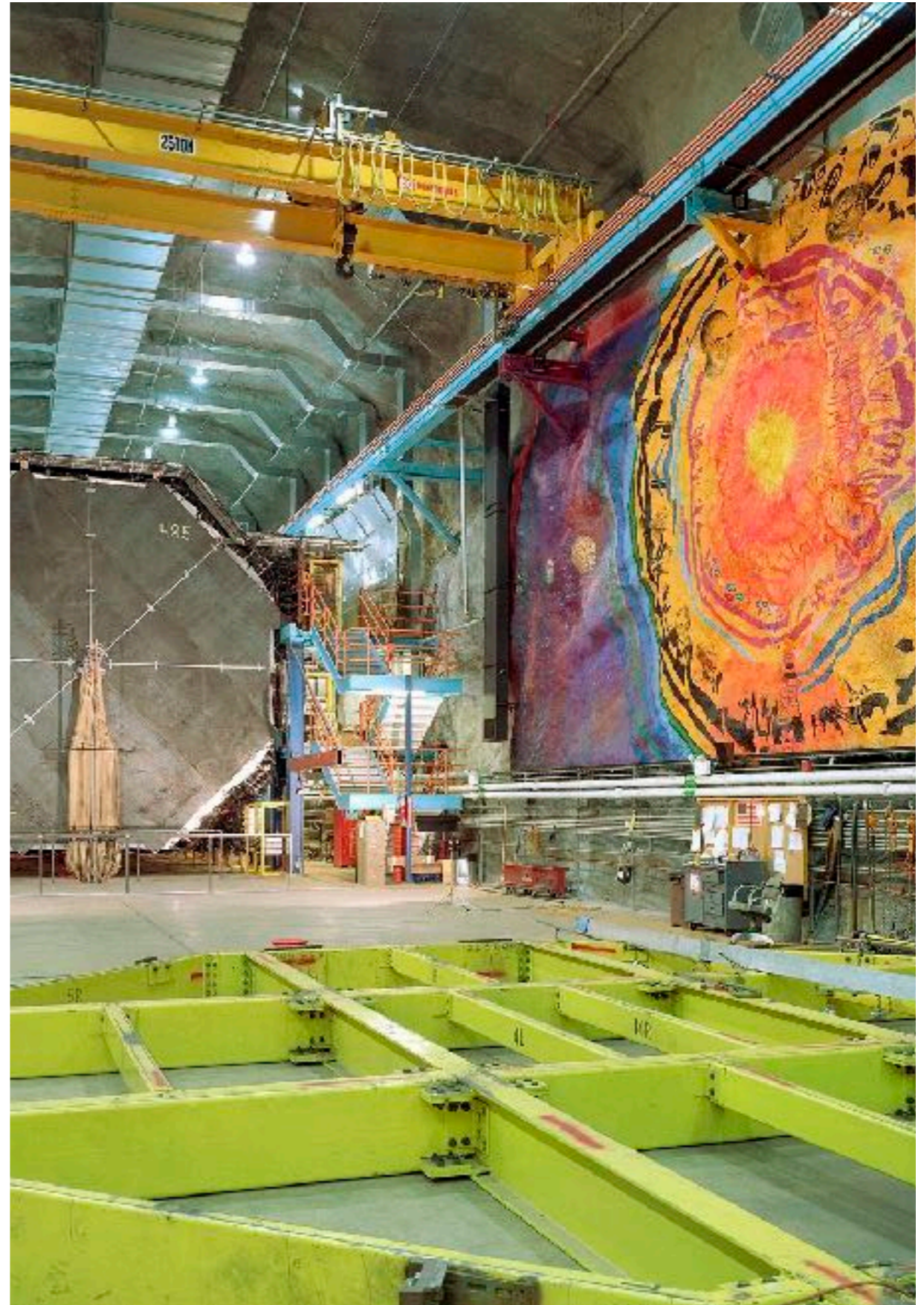


# Refined measurement of $\sin^2\theta_{23}$ from the MINOS Experiment

Jennifer Thomas, UCL  
on behalf of  
**MINOS+ Collaboration**

**Neutrino 2026**

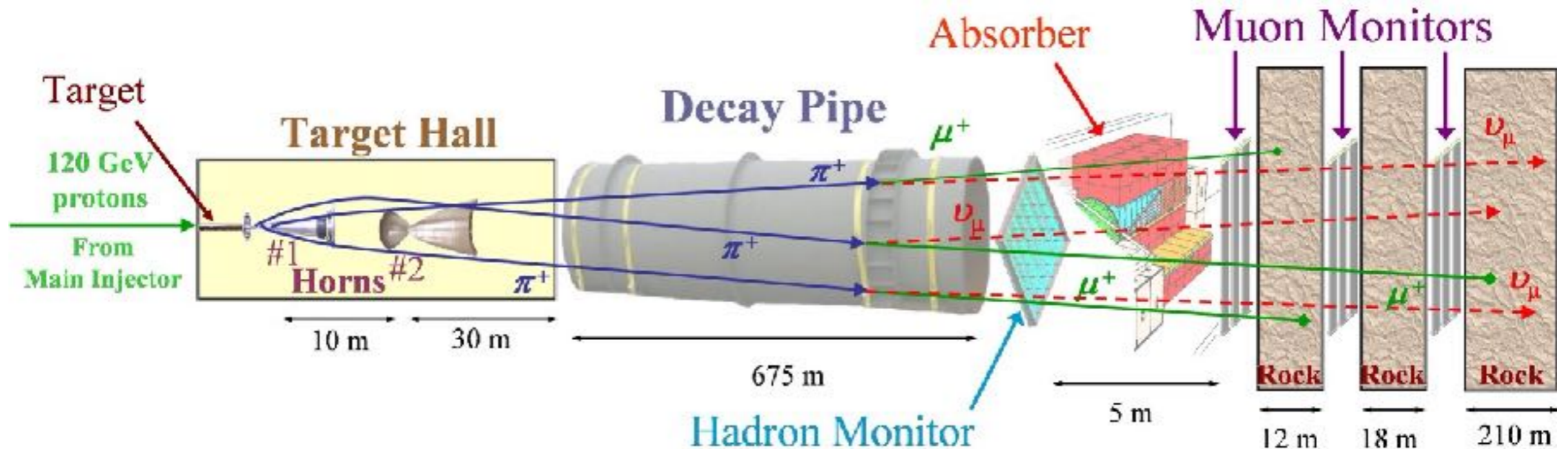


# The Numbers

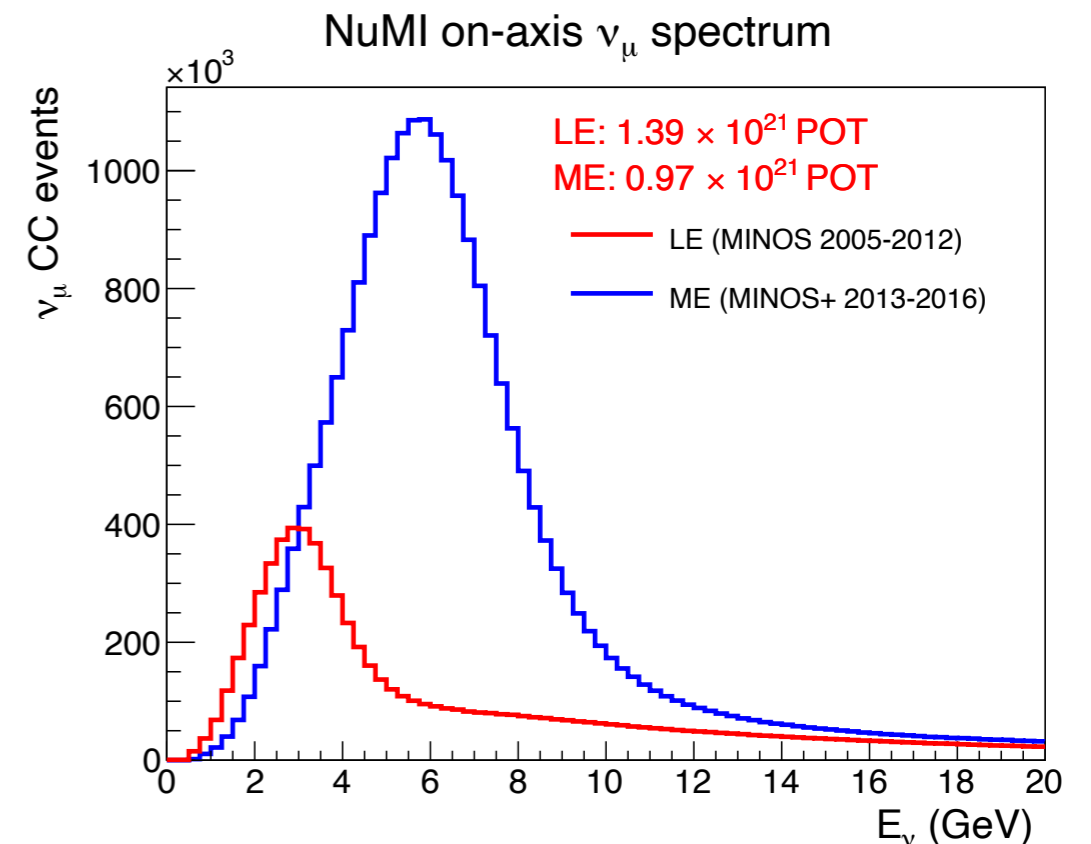
- 250 collaborators (at the peak)
- 10 years from proposal to beam (1995-2005)
- 11 years to collect data (2005-2016)
- 8 Targets (8 MINOS, 1 NOVA)
- 4 horns
- 4 FNAL Directors
- 5 Co-Spokespeople
- 43 papers (so far...) New Sun Shadow  
[arxiv.org/abs/2605.29306](https://arxiv.org/abs/2605.29306)
- 43 students/postdocs went to academia
- \$220,000,000 for 9770 events. (~\$22.5K/event )



# The NuMI Beam at FNAL



- Lowest energy possible was chosen as final LE setting (**just** low enough!)
  - Low Energy configuration, energy peak around 3 GeV (2005-2012)
  - Medium Energy configuration, energy peak at around 7 GeV (2013-2016), result of optimising off-axis flux at NOVA
- Hardware (slow) failings and component changes over time
- Forward Horn Current (FHC,  $\nu$ ) and Reverse Horn Current (RHC)  $\bar{\nu}$

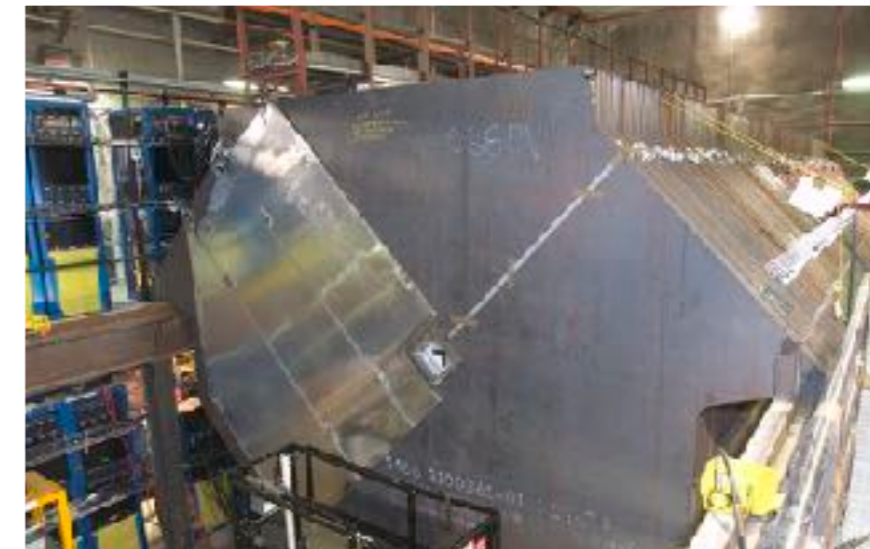
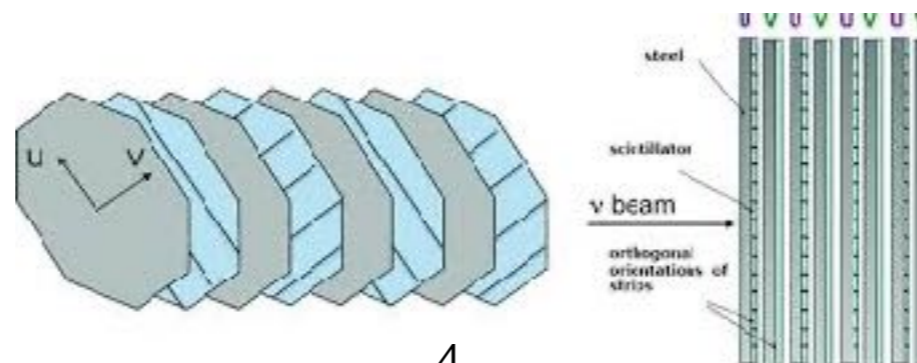
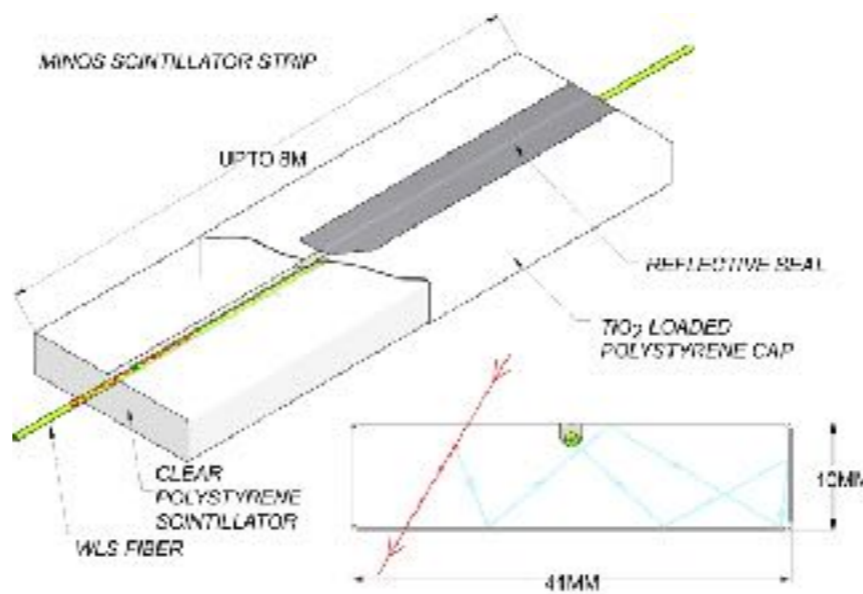


# The MINOS Experiment

- MINOS detectors were two functionally identical, magnetised (1.4T), tracking, sampling calorimeter detectors.
- Oriented for beam  $\nu\mu$ -charged current (CC) events (track orthogonal to planes), full event containment (muon and shower)



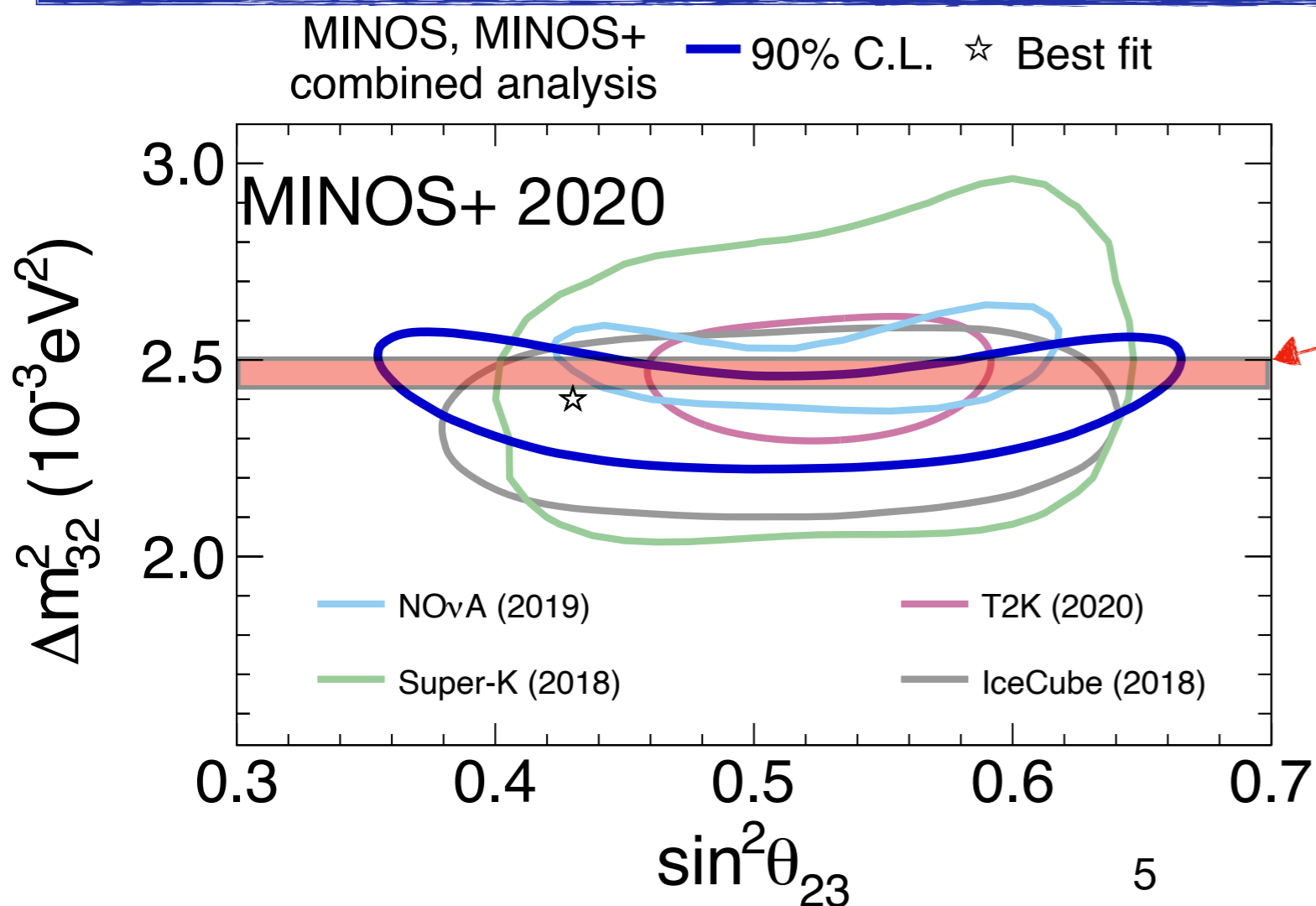
Far Detector  
735 km from beam target  
5.4 kton mass



Near Detector  
1 km from beam target  
1 kton mass

# Motivation

- Reactor experiments' precise measurement of  $\Delta m^2$  independent of  $\sin^2\theta_{23}$
- Increase precision on  $\sin^2\theta_{23}$ , the least well known of the mixing angles
- Focus on MINOS core strengths, use  $\nu_\mu$  wide band beam (WBB) data only
  - exploit **WBB beam  $\nu_\mu$  data** collected at and above oscillation max
  - exploit **detector's strength** of  $\mu$  containment and total energy measurement
  - exploit **experiment's strength** of systematics cancellation between ND and FD



## New Reactor Constraint (2025)

$$\Delta m^2_{32} = 2.48 \pm 0.05 \times 10^{-3} \text{ eV}^2 \text{ (NH)}$$

$$\Delta m^2_{32} = -2.54 \pm 0.05 \times 10^{-3} \text{ eV}^2 \text{ (IH)}$$

$$\text{DayaBay } \Delta m^2_{32} = 2.48 \times 10^{-3} \text{ eV}^2 \pm 0.06 \times 10^{-3} \text{ eV}^2$$

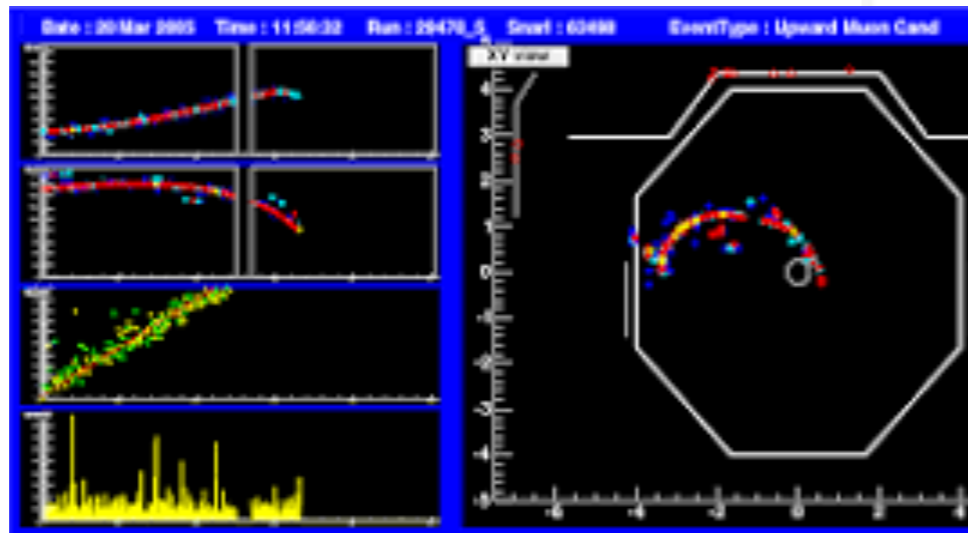
(F. P. A. et al. (Daya Bay), Phys. Rev. Lett. 130, 161802913(2023))

$$\text{RENO } \Delta m^2_{ee} = 2.57 \times 10^{-3} \text{ eV}^2 \text{ } ^{+0.10}_{-0.11} \text{ } ^{+0.05}_{-0.05} \times 10^{-3} \text{ eV}^2$$

(S. Jeon et al. (RENO), Phys. Rev. D 111, 112006(2025))

# Analysis Revisited

- Beam flux simulation improvements
- Neutrino interaction modelling updates
- Hadronic Shower Energy Reconstruction
- ME resolution binning
- Re-evaluation of systematics



# The NuMI Beam Simulation

- Extensive ( $\sim 10^7$  events) ND data used to inform the flux simulation
- Beam simulation : FLUGG package which is GEANT4 (geometry)+FLUKA (hadron production)
- Multi parameter fit to ND data
  - includes warping function for hadron production in FLUKA
  - Hardware changes tracked and modelled over time
  - RHC and FHC simultaneously fit
- Updated hadron production model between  $p_T$  0.1-0.5 GeV changes FLUKA prediction
- The combination of hadron production modelling and better geometry modelling has significantly improved the agreement between data and MC

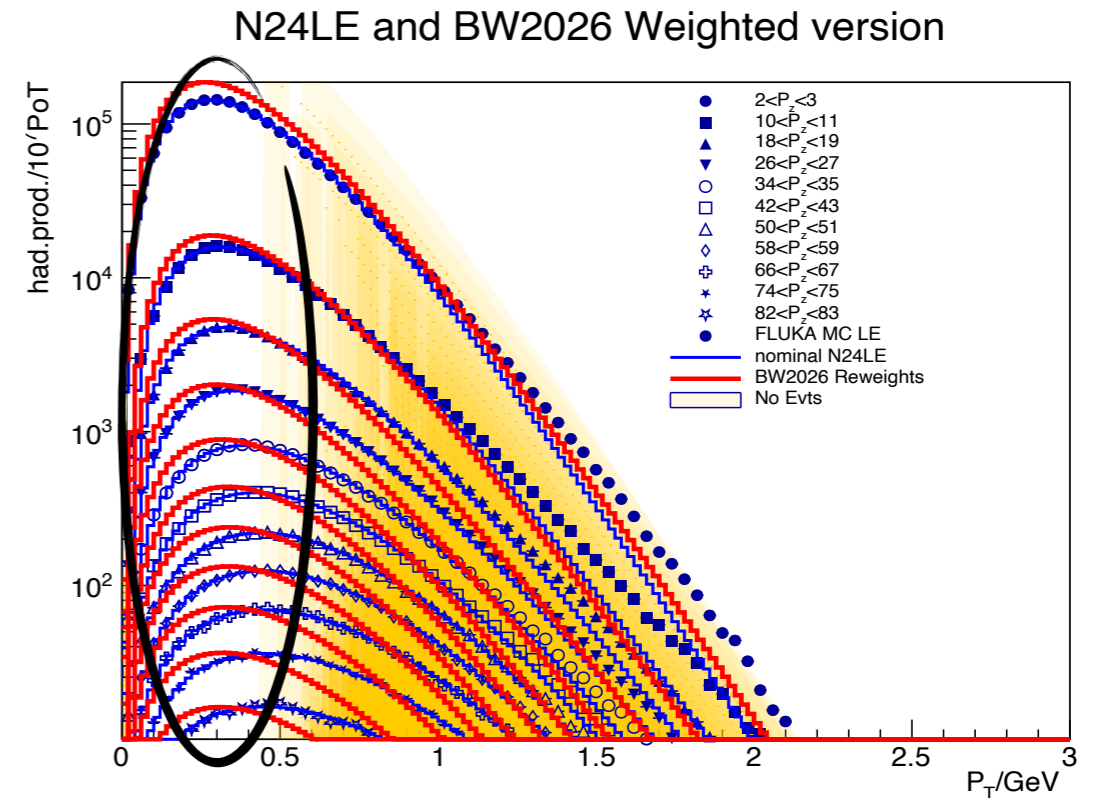
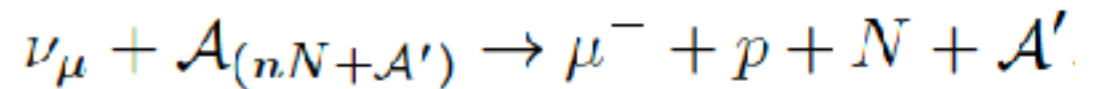
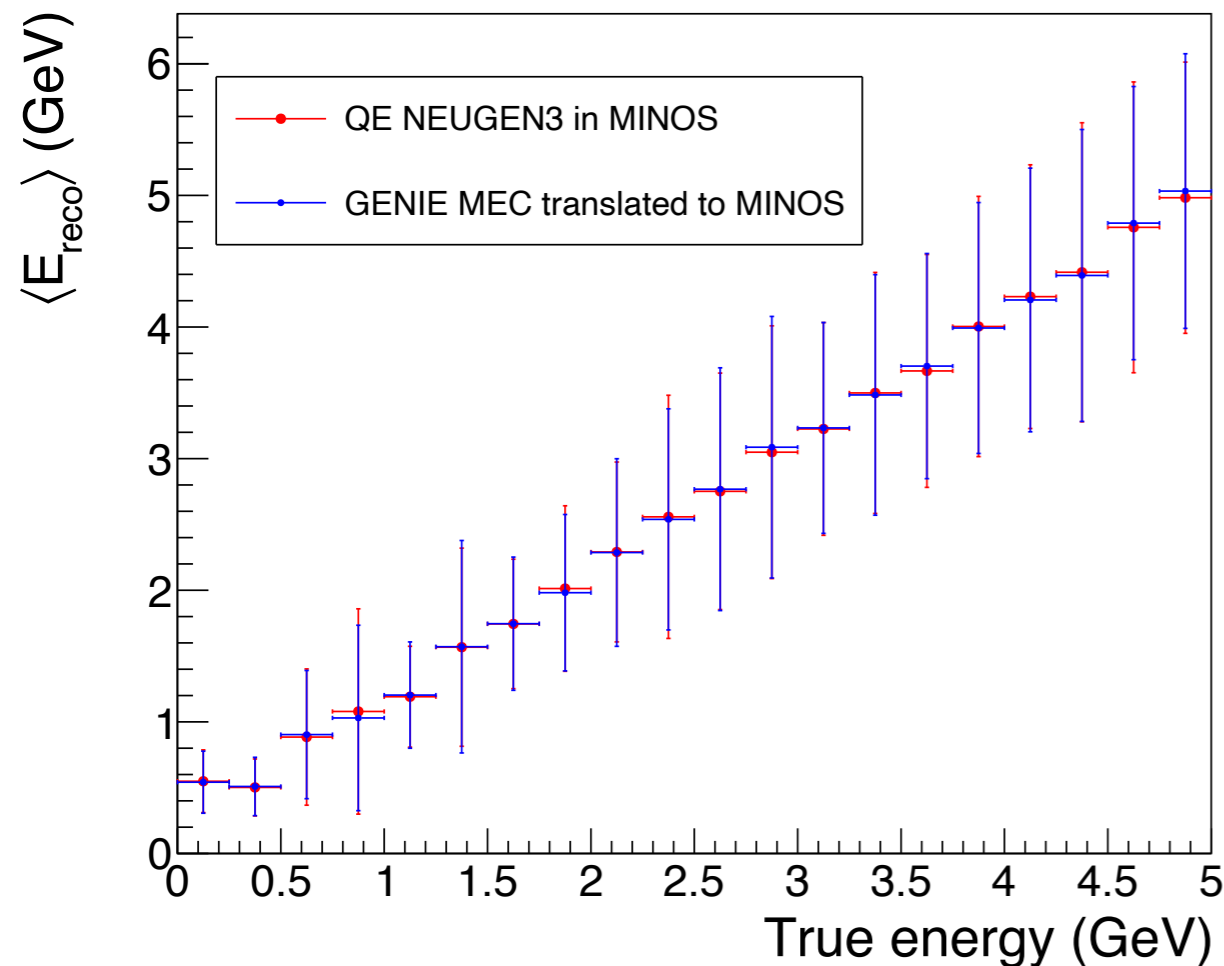


Figure 12: Original and improved warping functions compared to FLUKA predictions

$$\frac{d^2 N}{dx_F dp_T} = [B(x_F)p_T + C(x_F)p_T^2] \exp(-D(x_F)p_T^{E(x_F)})$$

# Neutrino Interaction Modelling

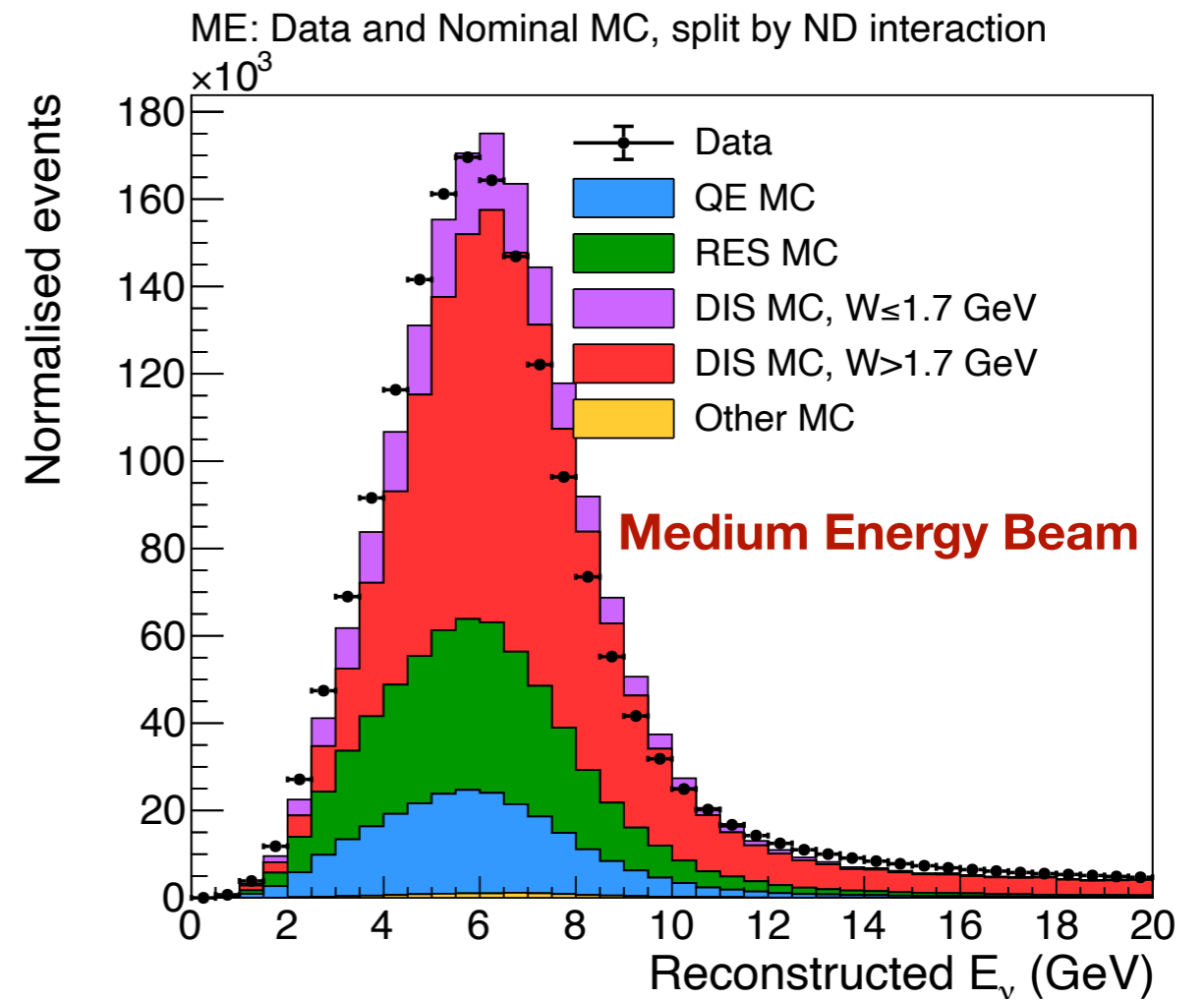
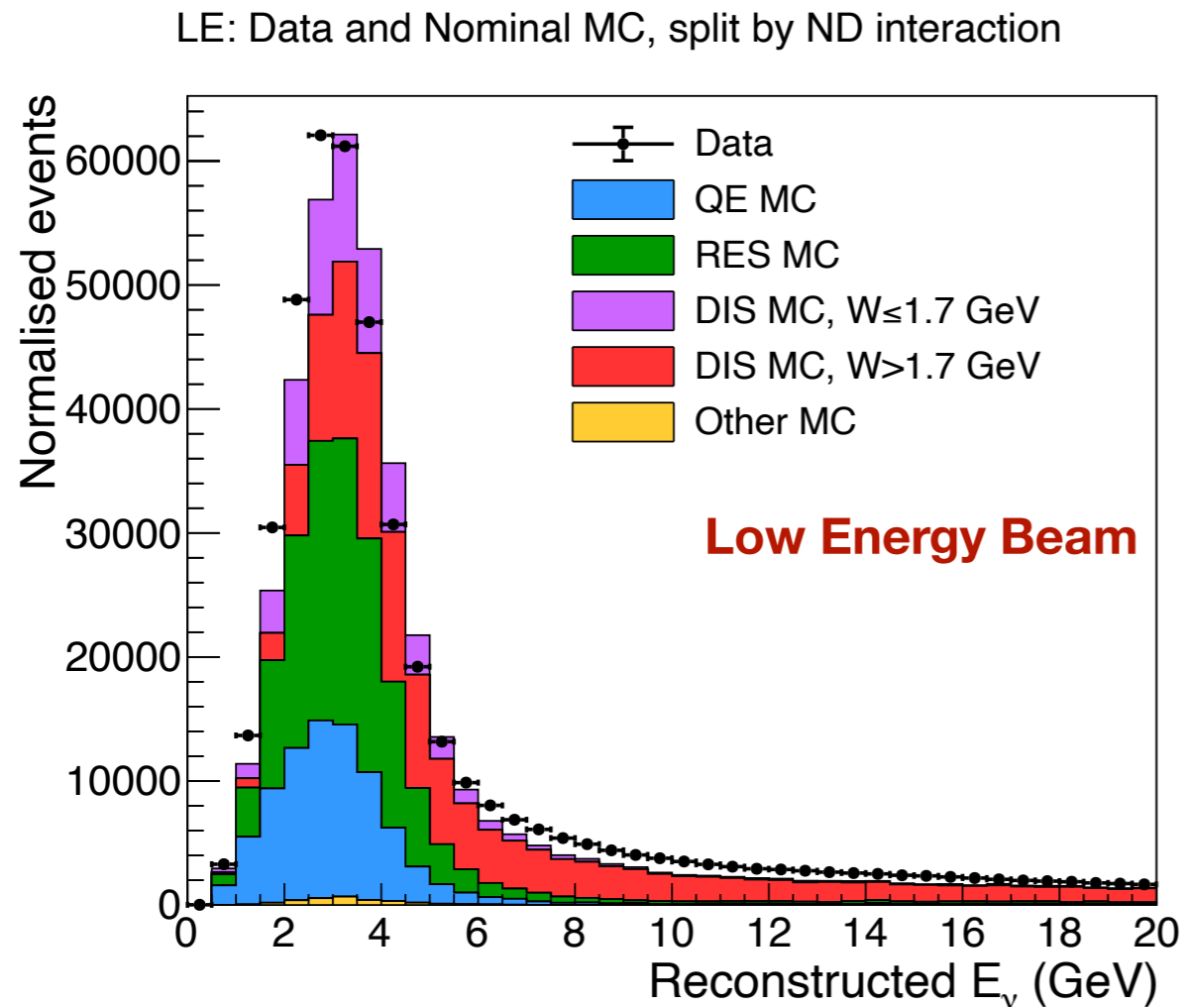
- Since MINOS finished running, two pertinent developments in  $\nu\mu$ CC interactions
- new work has shone spotlight on 2p2h-Meson Exchange Current
- new phenomenological fits of resonant  $\pi$  production to bubble chamber data ( $W < 1.7\text{GeV}$ )



- MEC events produced in MINOS detector simulation via matching of NEUGEN3 truth #neutrons,  $E_{\mu}$  and  $E_{\text{had}}$  using GENIE on Fe
- No discernable difference from QE events

\*D. Ruterbories et al (MINERvA Collaboration) *Simultaneous measurement of proton and lepton kinematics in quasielastic-like  $\nu_{\mu}$  - hydrocarbon interactions from 2 to 20 GeV*, *Phys. Rev. Lett.* **129**, 021803 (2022); *arXiv:2203.08022*.

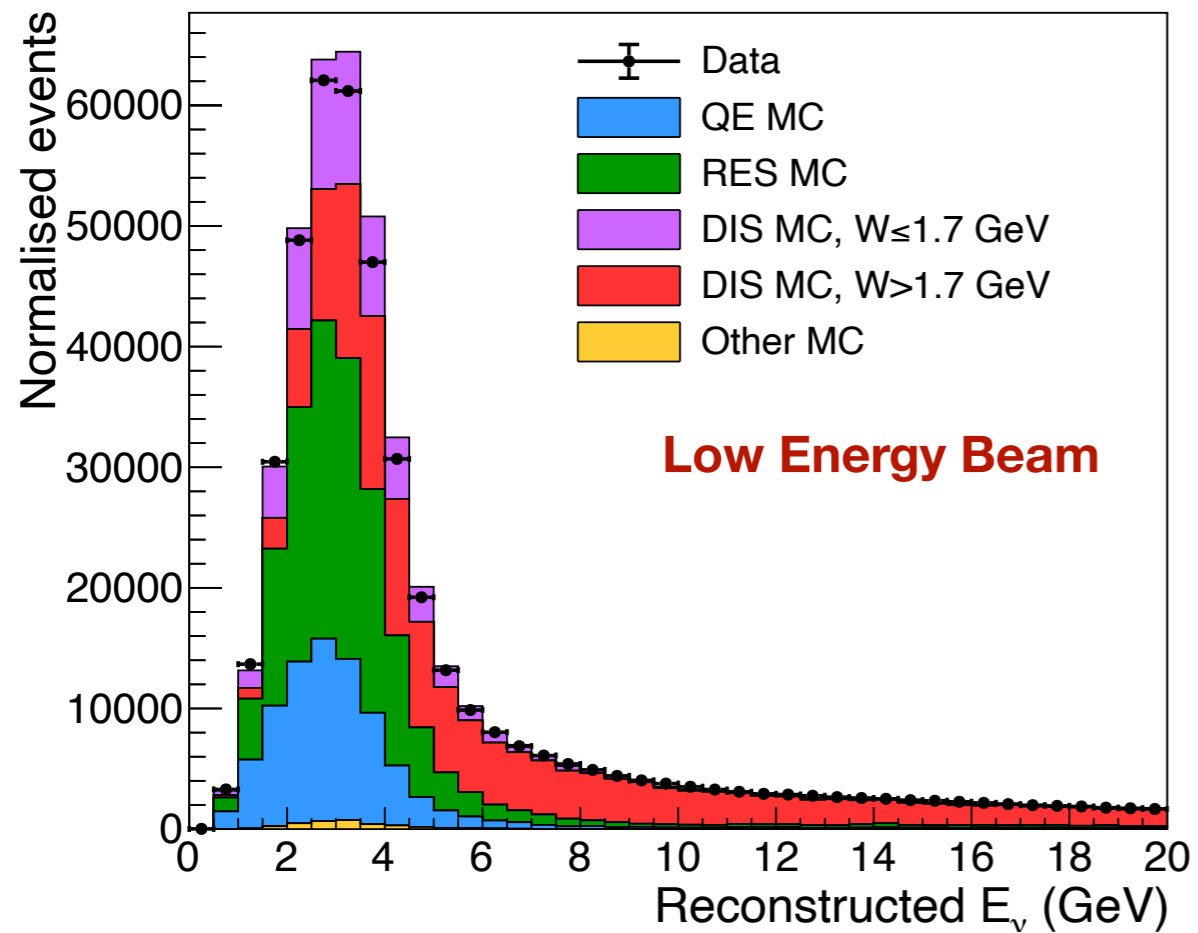
# Beam Modelling Improvements



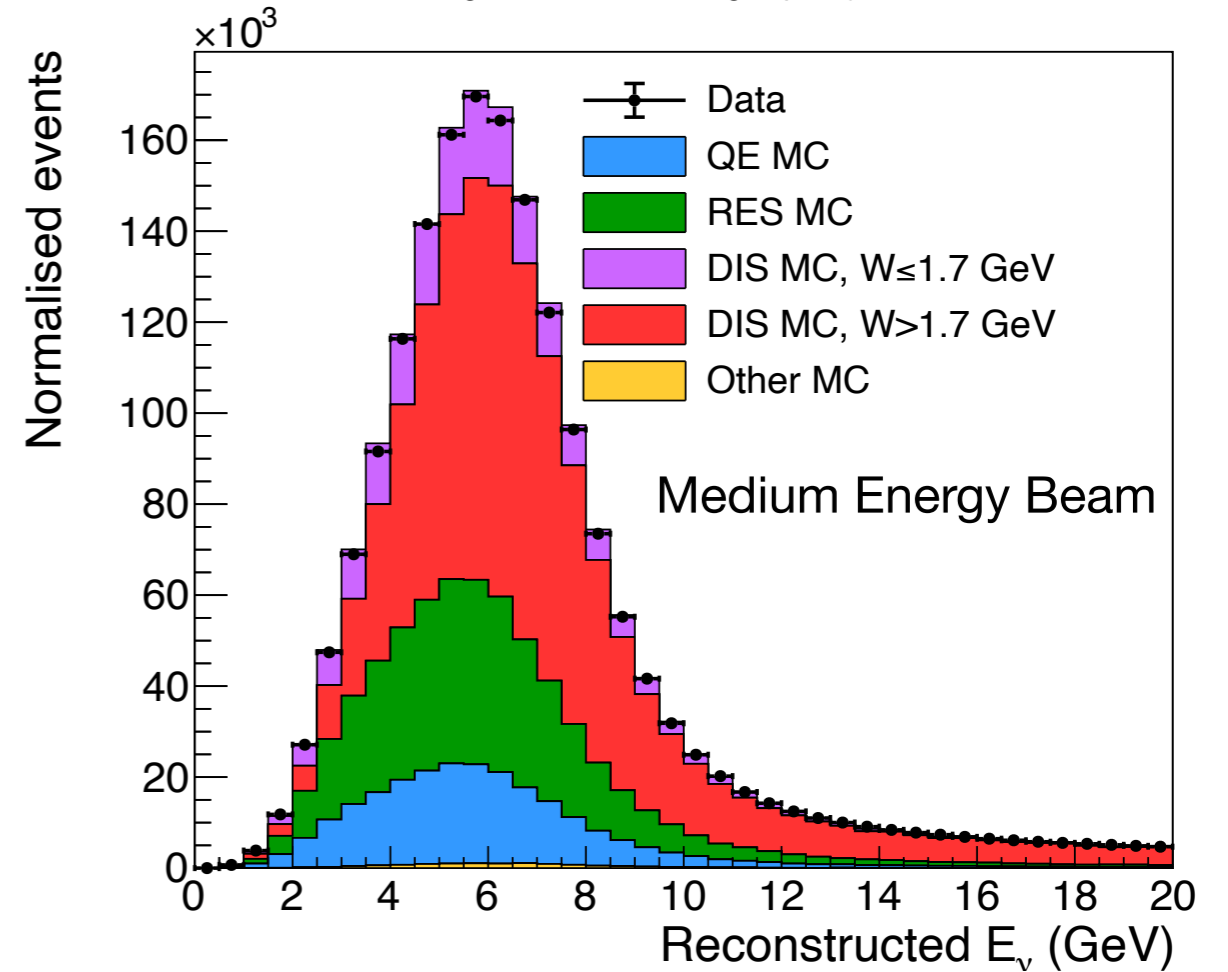
Original Neugen3 + out-of-the-box beam simulation (FLUGG)

# Beam Modelling Improvements

LE: Data and reweighted MC, no ND wgt, split by ND interaction

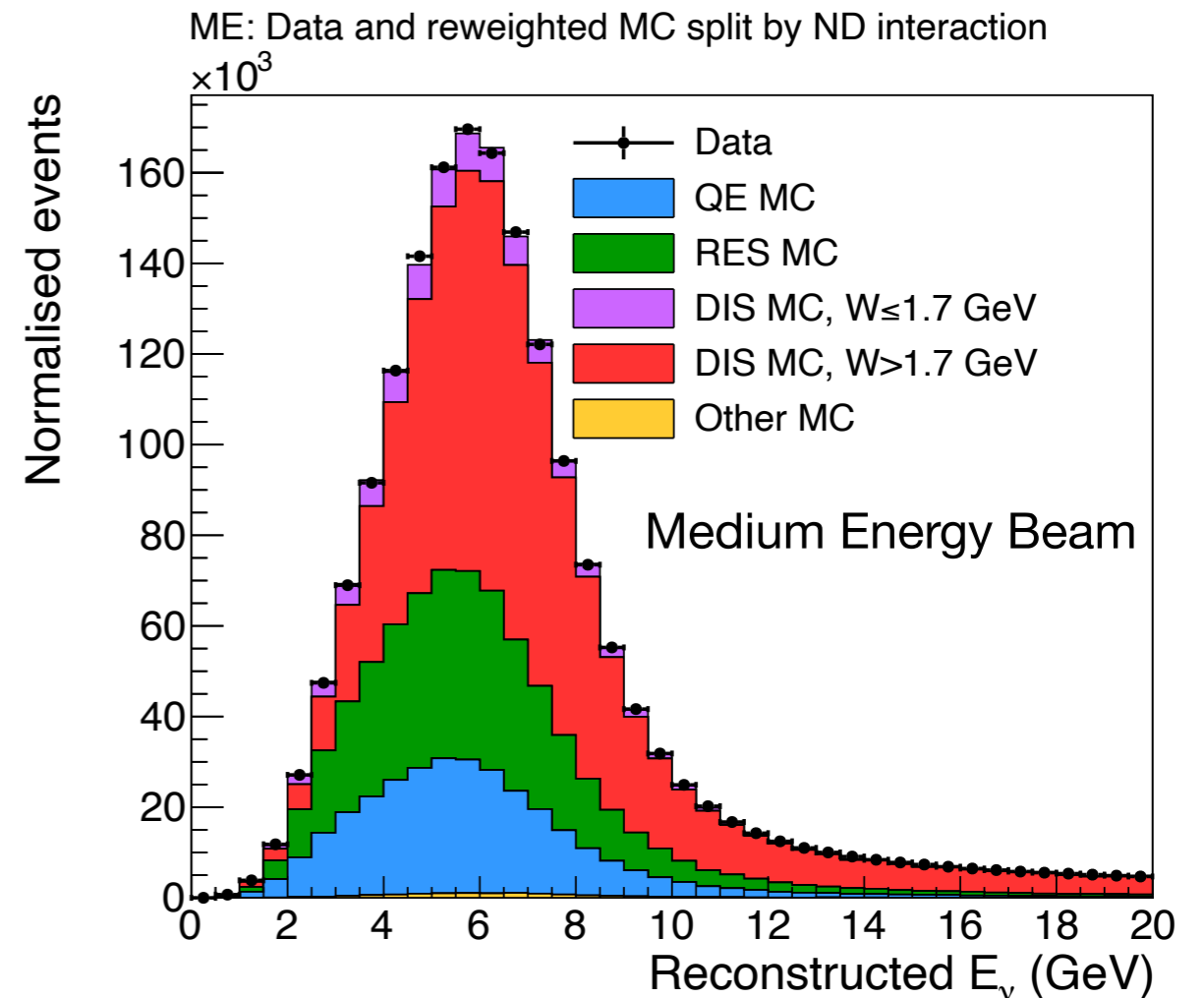
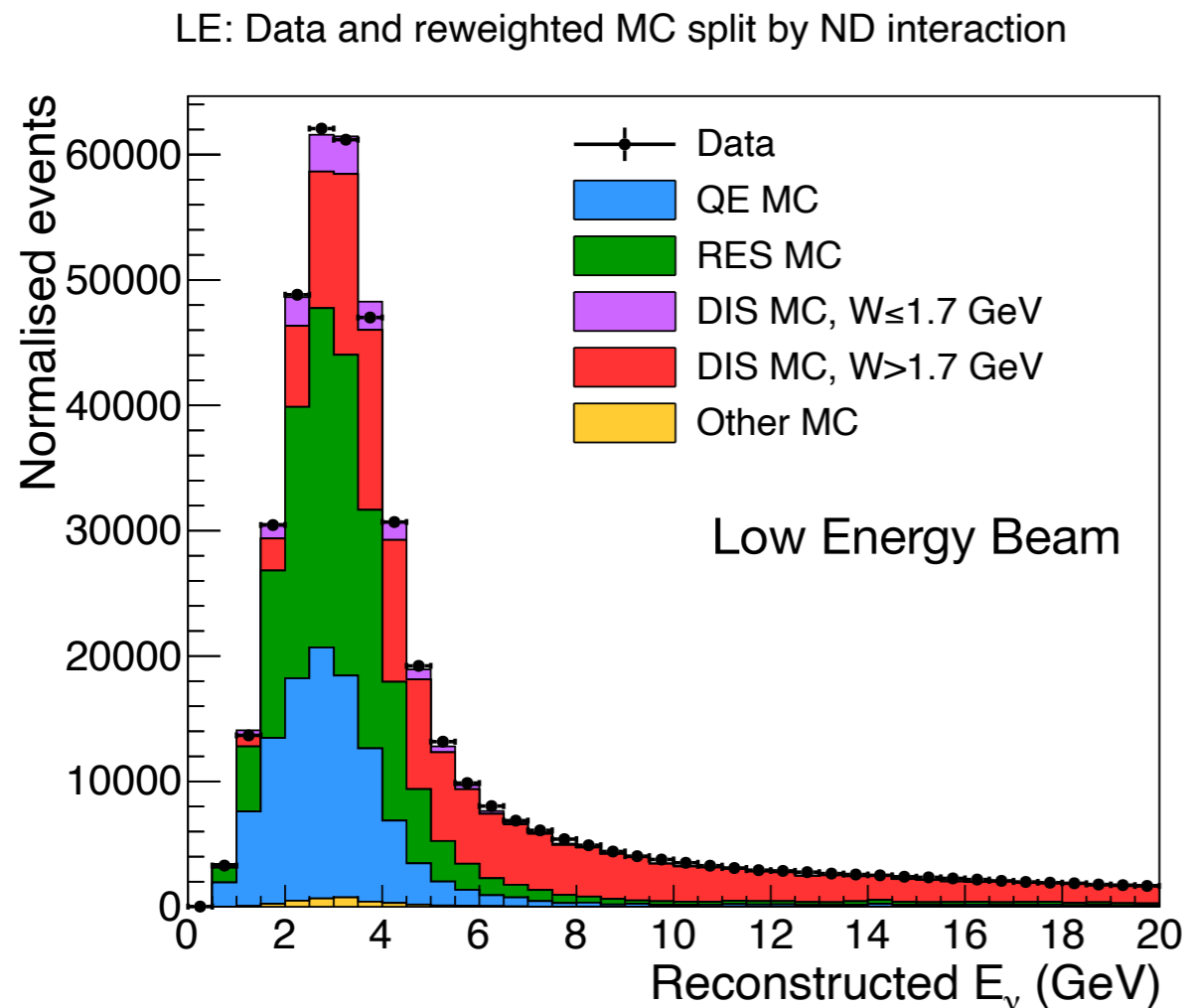


ME: Data and reweighted MC, no ND wgt, split by ND interaction



After FLUKA re-weighting of hadron production parameters

# Modelling Improvements



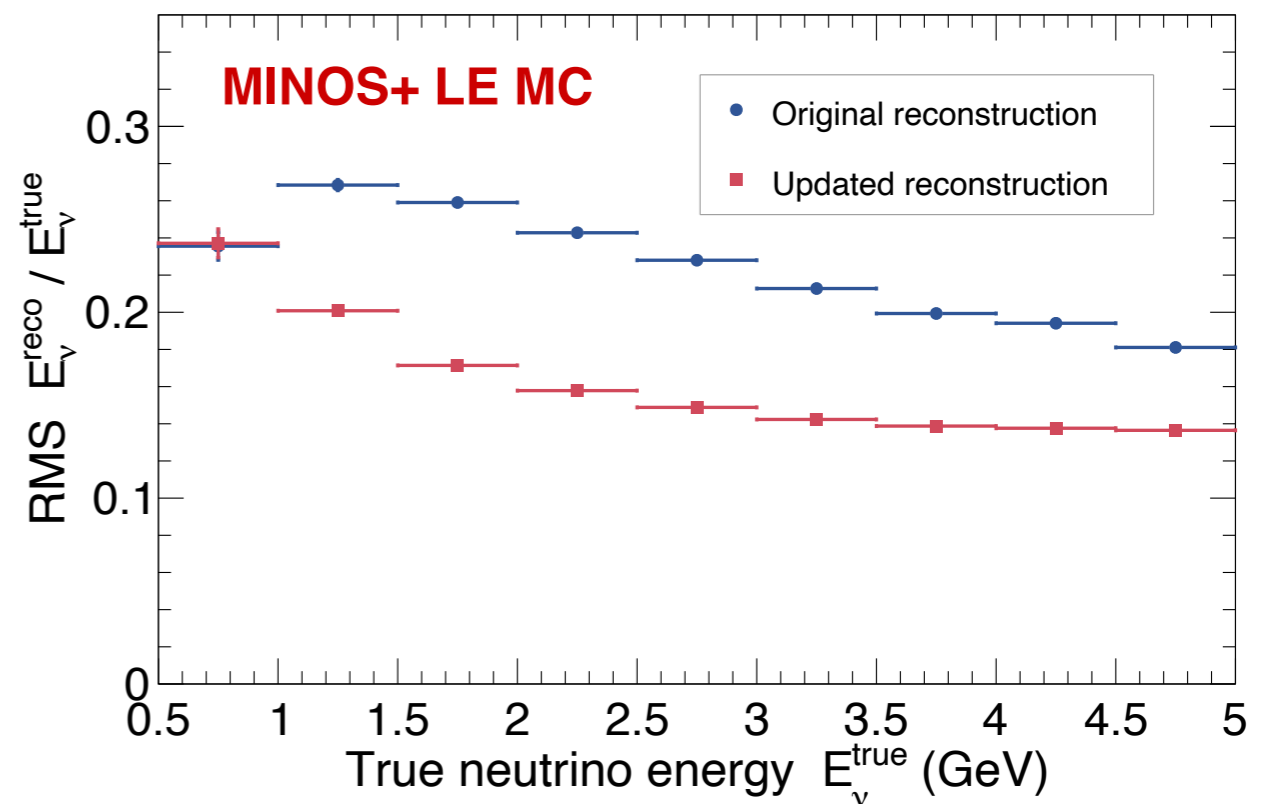
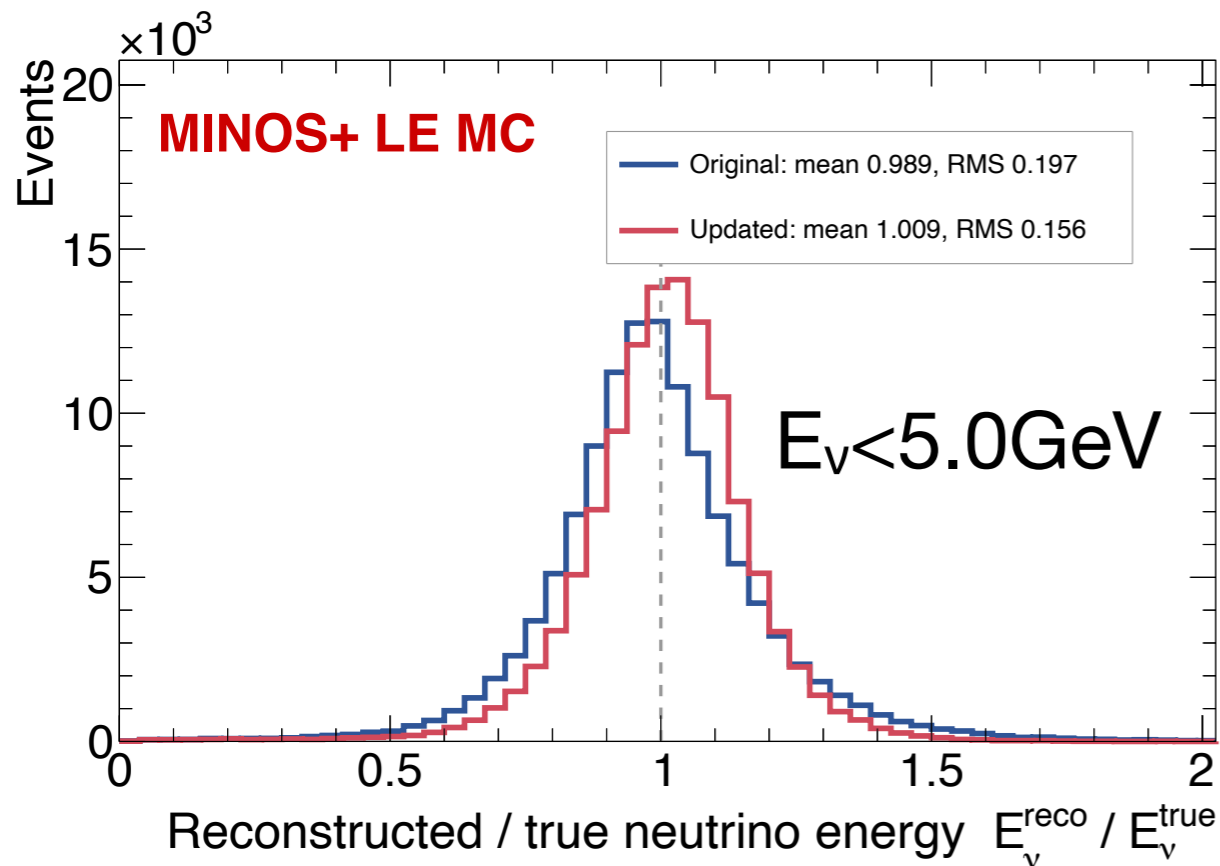
After QE and non-resonant pion production ( $W < 1.7$  GeV) re-weighting

In line with eg: Minerva estimates (QE up 30%,  $W < 1.7$  down 60%)

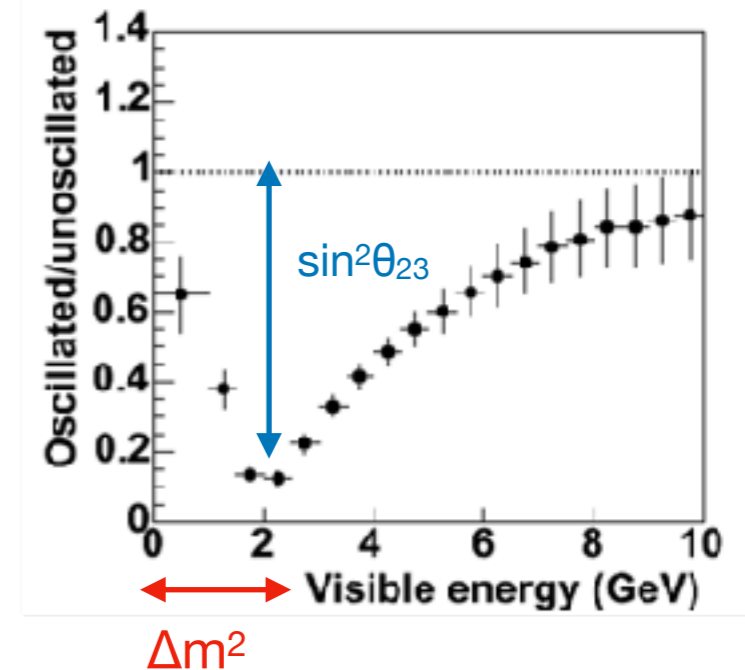
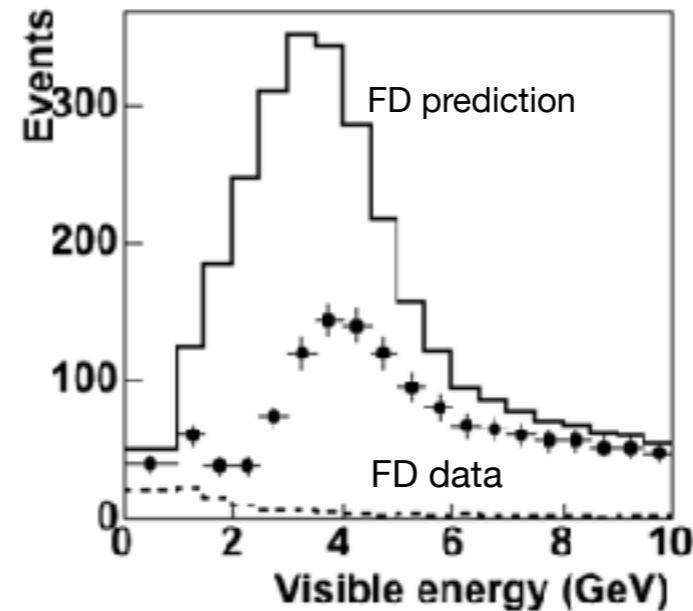
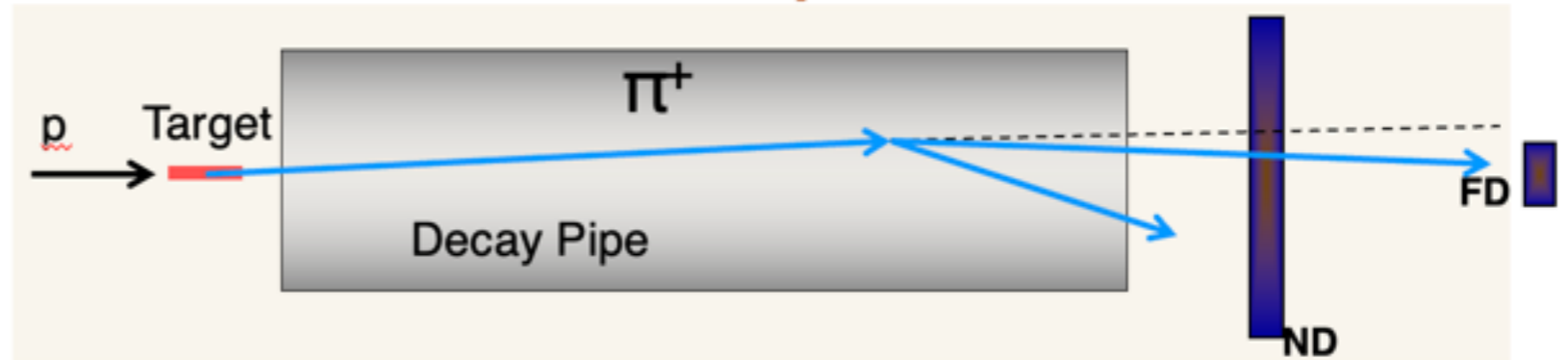
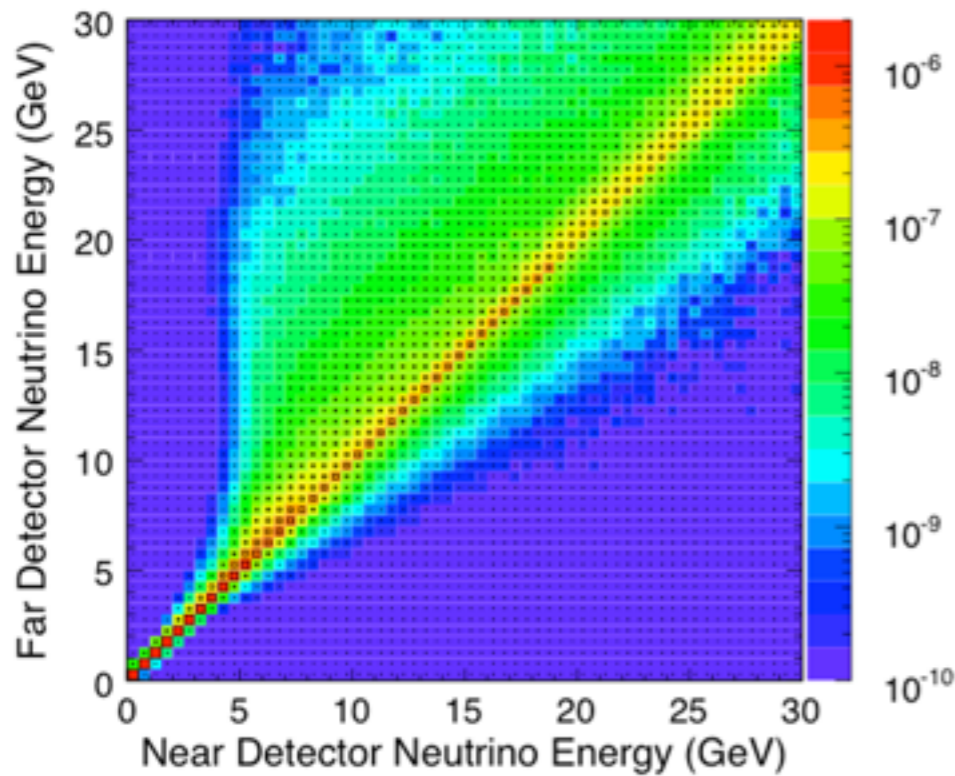
# Hadronic Shower Energy Estimator

- k-Nearest Neighbours (kNN)
  - Shower PH, #planes in shower, PH around track
- reduced k from 400 to k=70, simplified calibration
- Improvement in region of interest in reconstructed energy

## Far Detector Energy Reconstruction



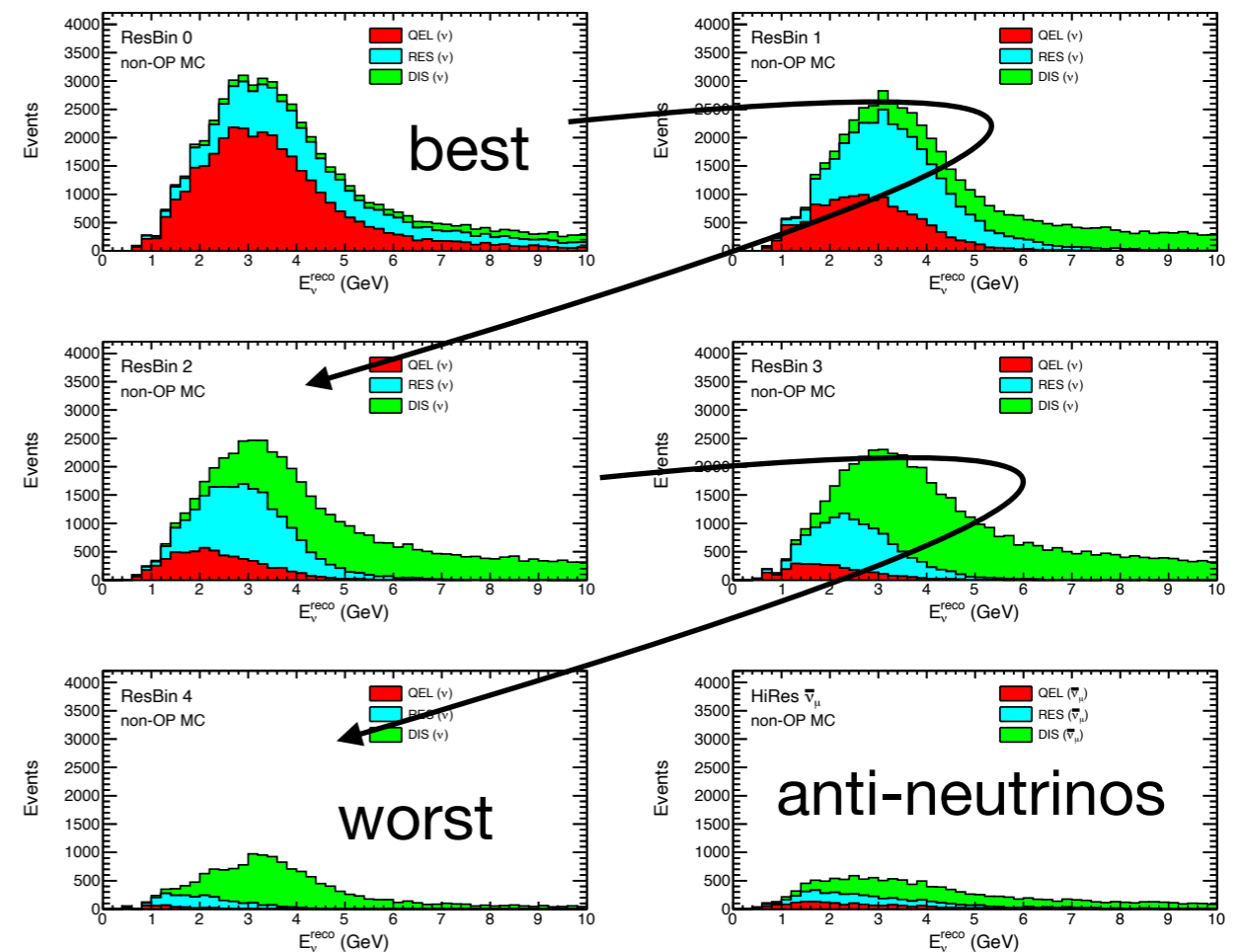
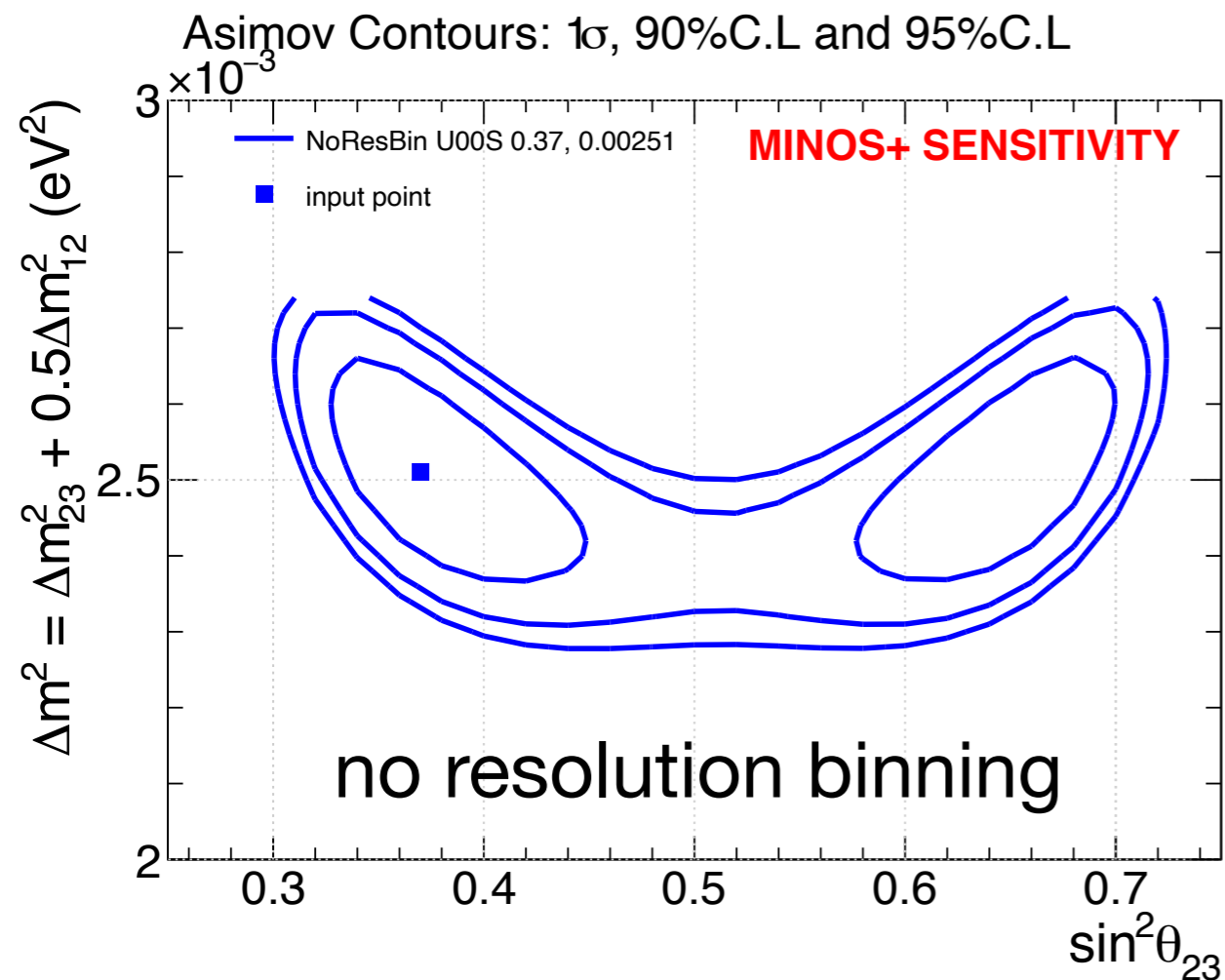
# Basics of Oscillation Parameter Measurement



- Good model now of pions in the decay pipe, now add kinematics
- Push ND data through the ND->FD matrix
- FD prediction then compared to FD data

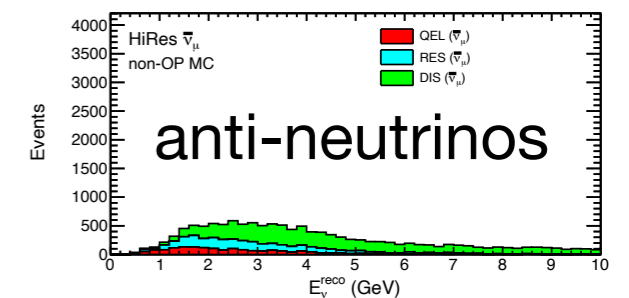
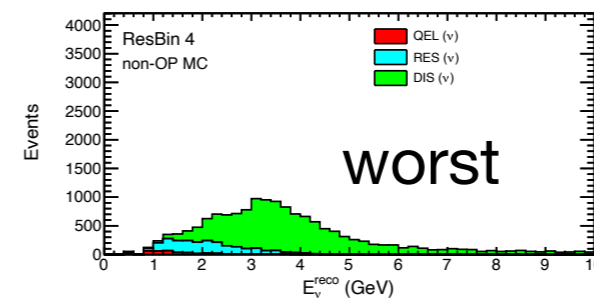
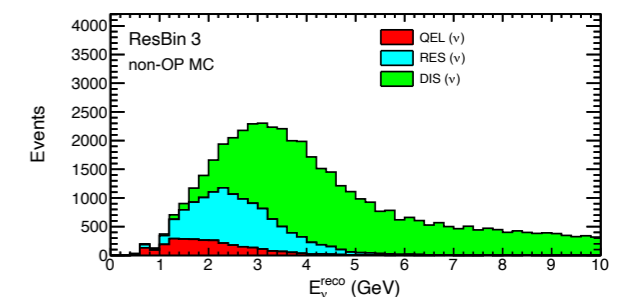
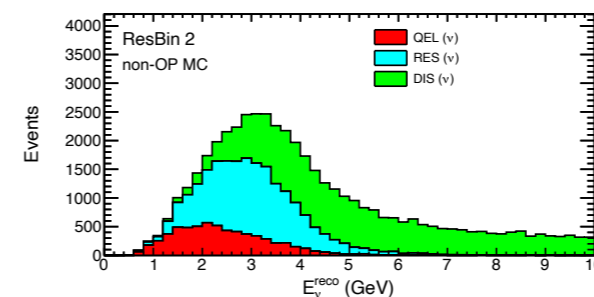
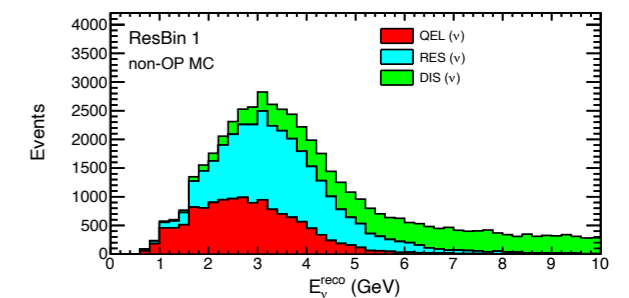
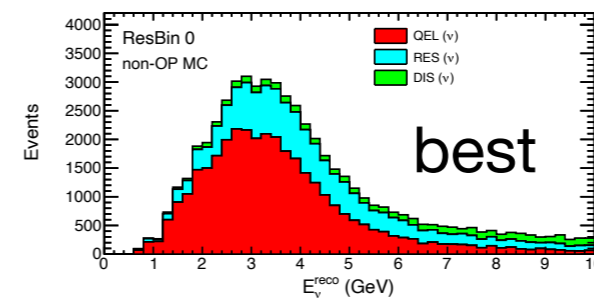
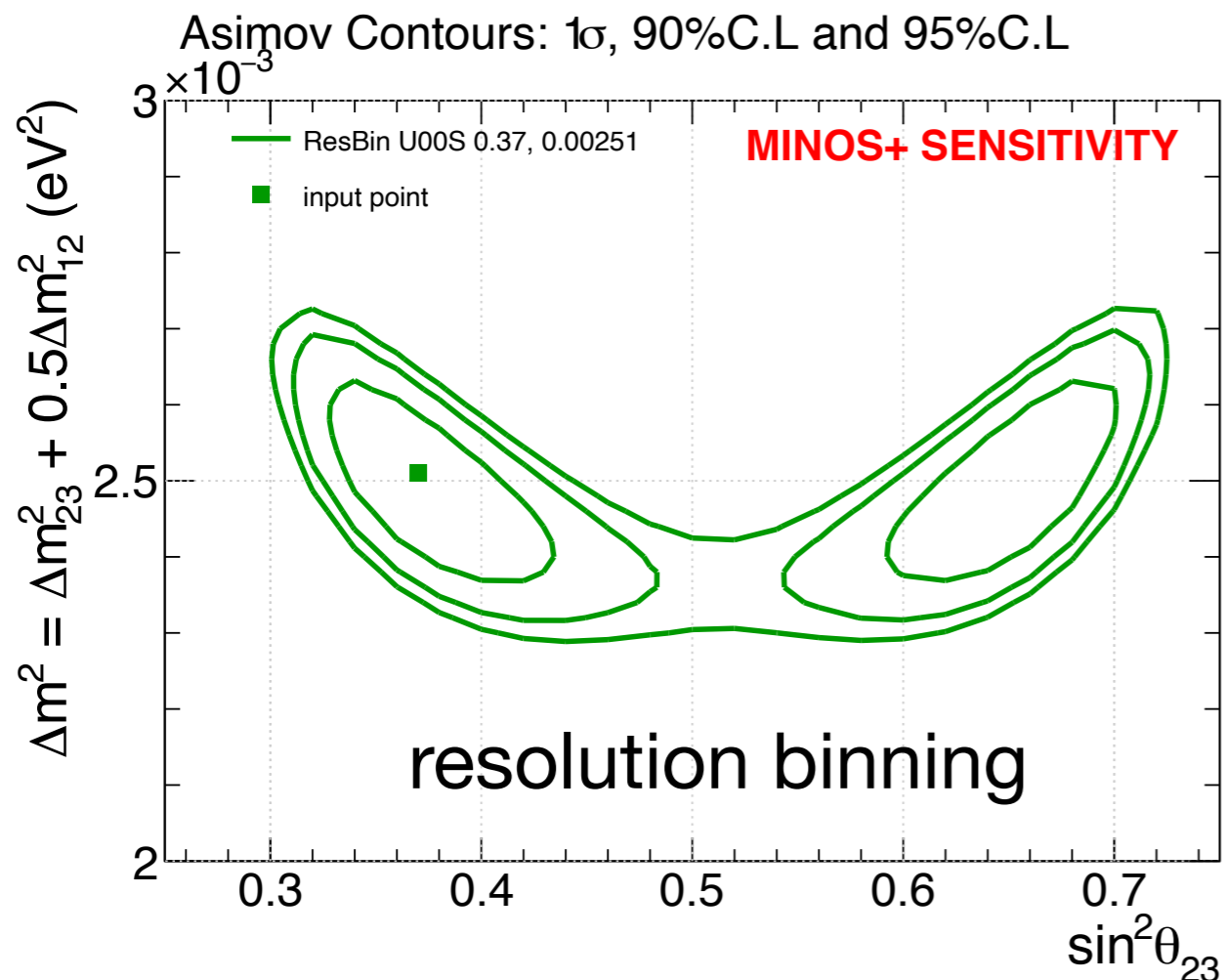
# Resolution Binning

- The extrapolated ND spectrum is compared with the FD Data to find the best parameter fit values
- Resolution binning is used to group events together in the fit of similar resolution



# Resolution Binning

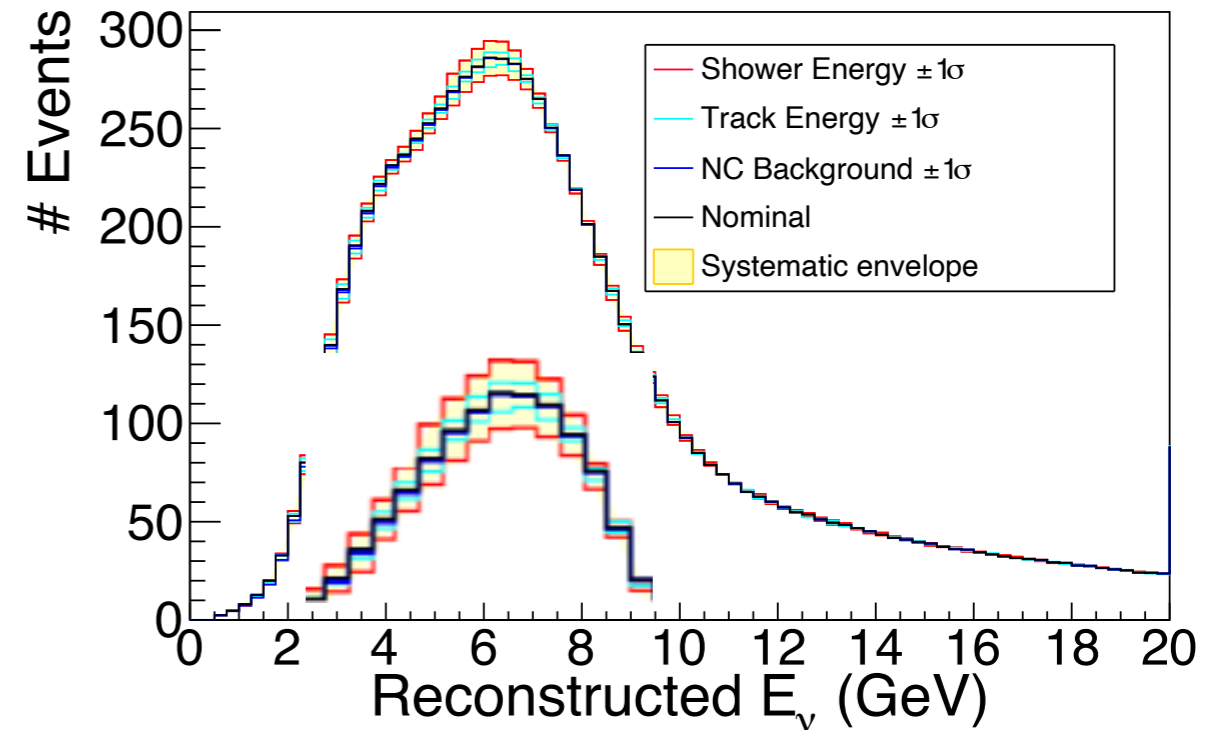
- The extrapolated ND spectrum is compared with the FD MC to find the best parameter fit values
- Resolution binning is used to group events together in the fit of similar resolution
- This improves sensitivity to  $\Delta m^2$  and  $\sin^2\theta_{23}$



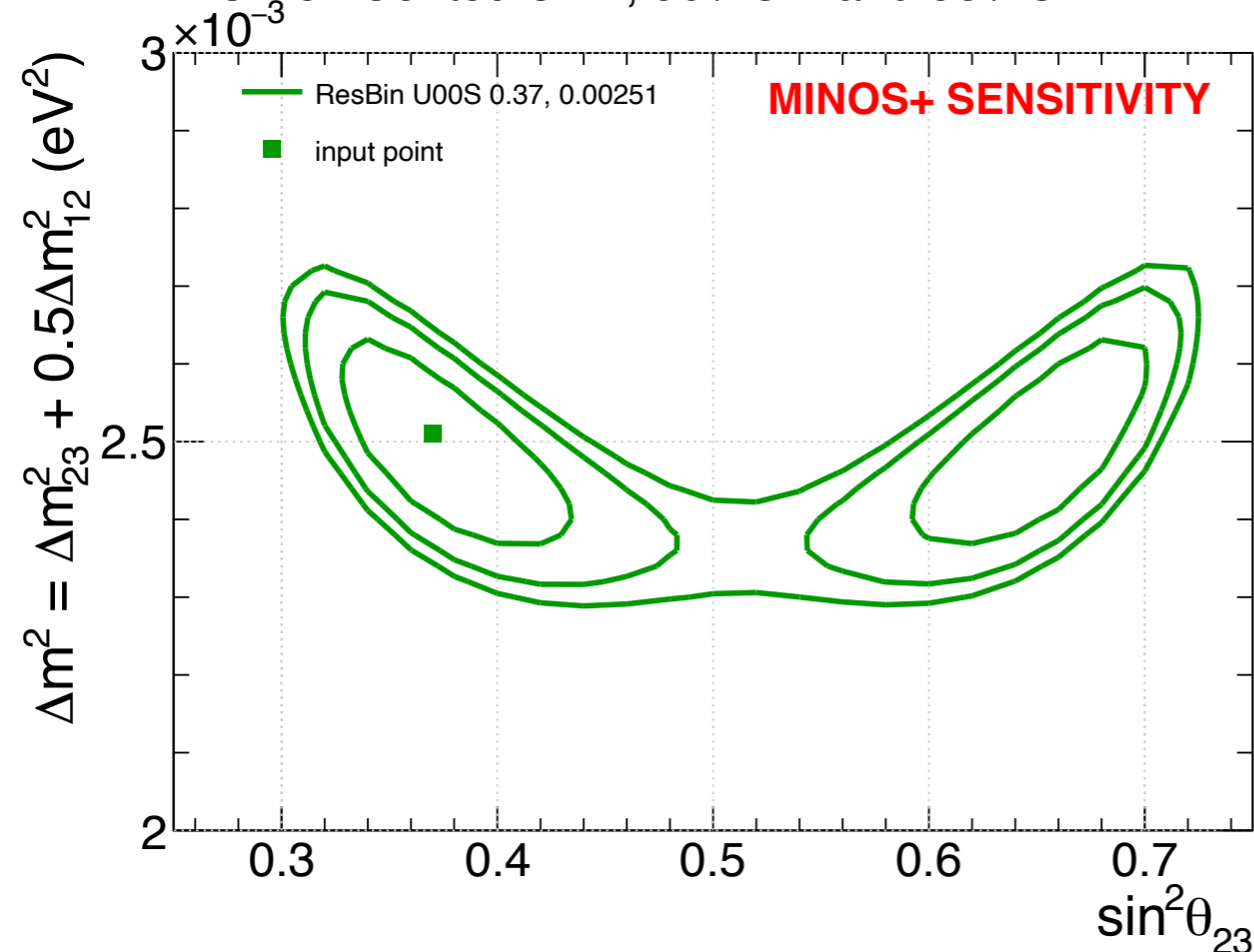
# Systematic Studies Revisited

- Dominant systematics are Eshw, Etrk, NC Bkg and Normalisation
- The raw systematic envelope shows +/- 5-7% changes in region of interest for  $1\sigma$  errors

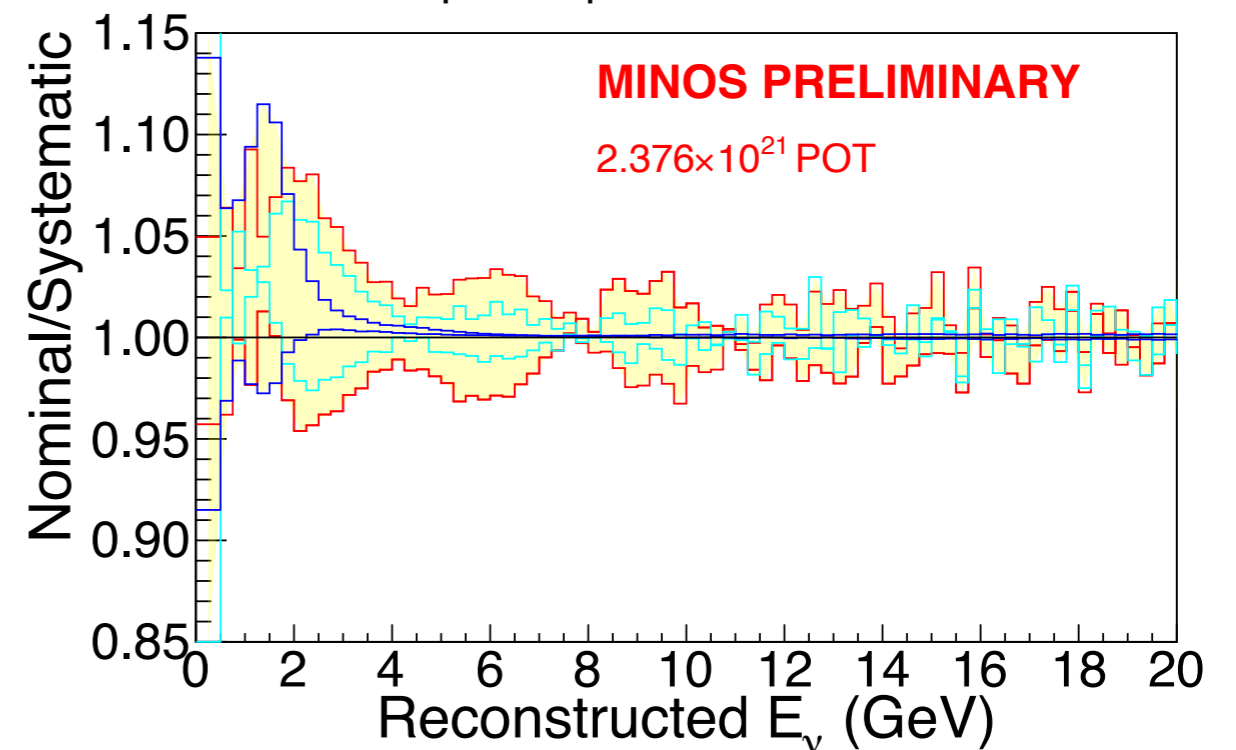
Neutrino Energy Spectrum



Asimov Contours:  $1\sigma$ , 90%C.L and 95%C.L



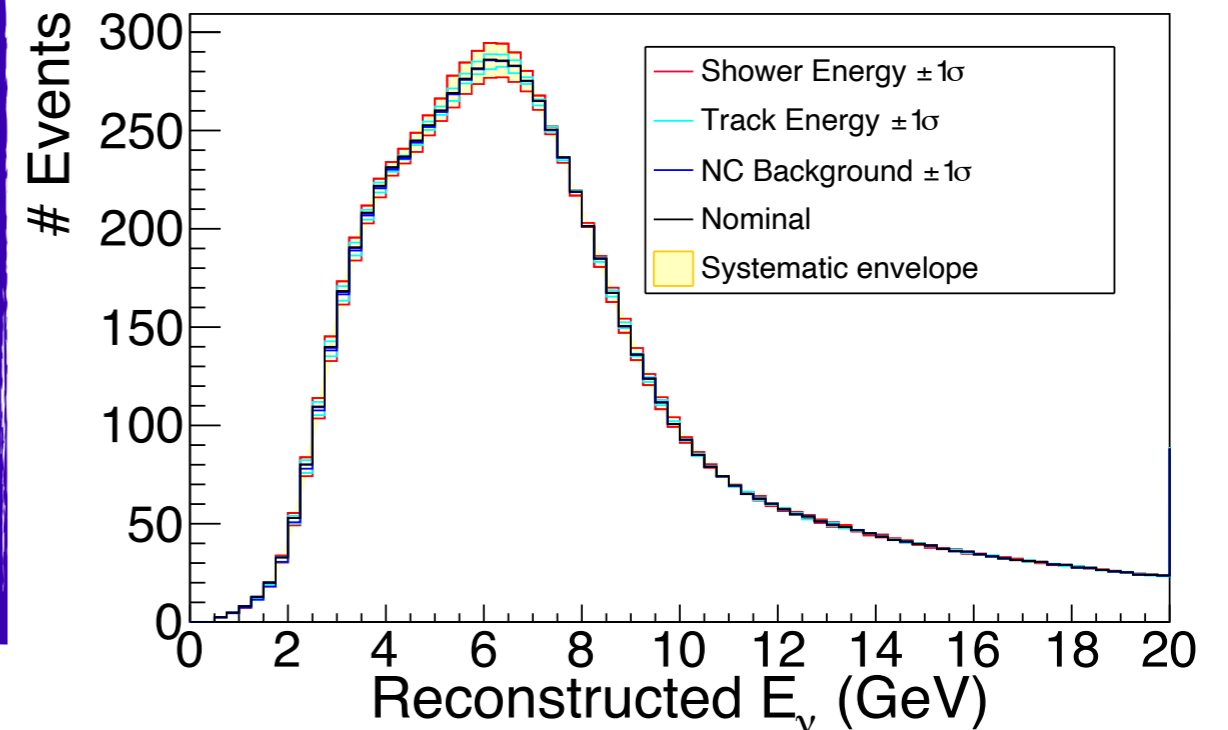
Template Spectrum Ratios



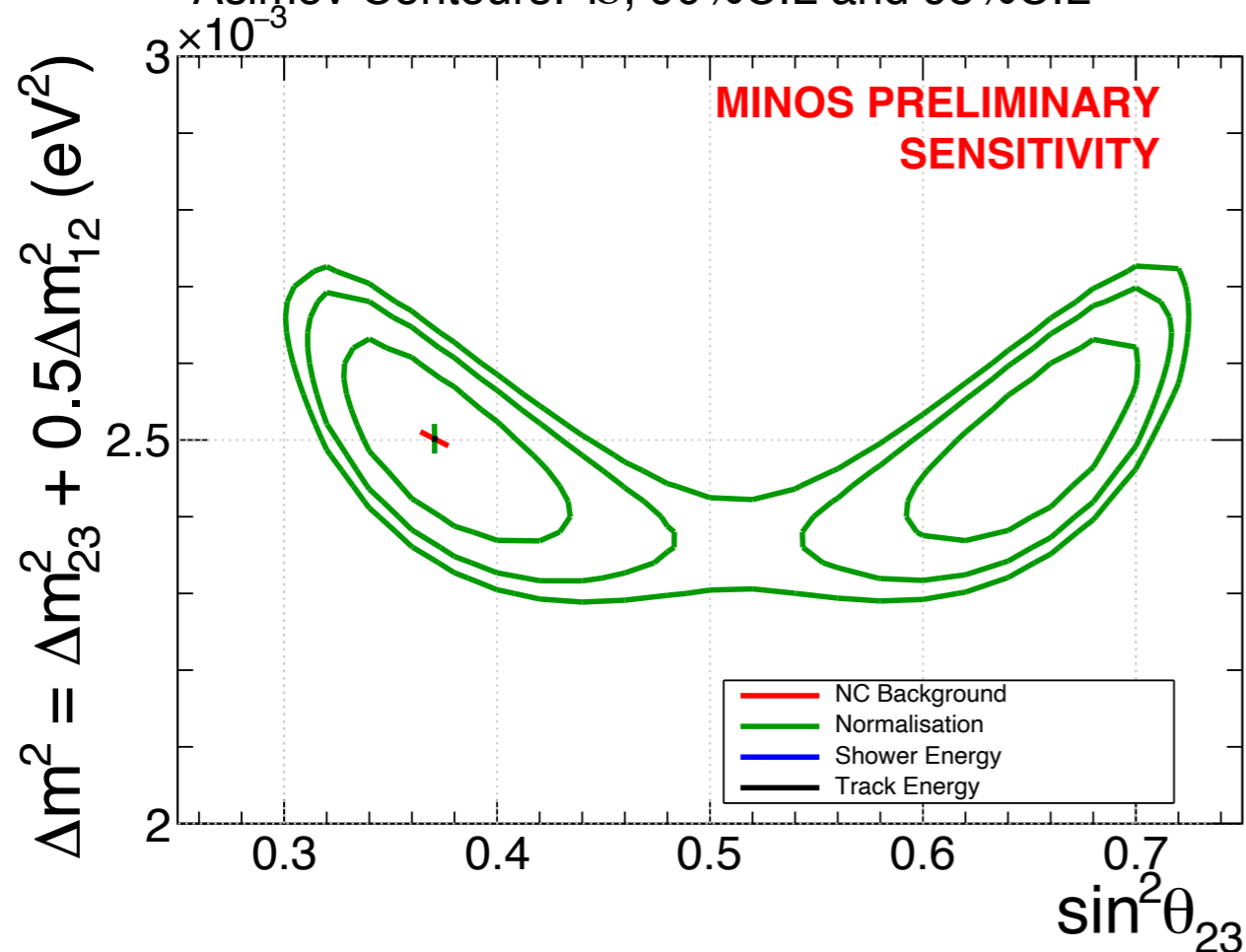
# Systematic Studies Revisited

- Dominant systematics are Eshw, Etrk, NC Bkg and Normalisation
- F/N shows  $\sim 2\%$  errors in region of interest
- Impact of systematics very small compared to statistics after fitting for systematics

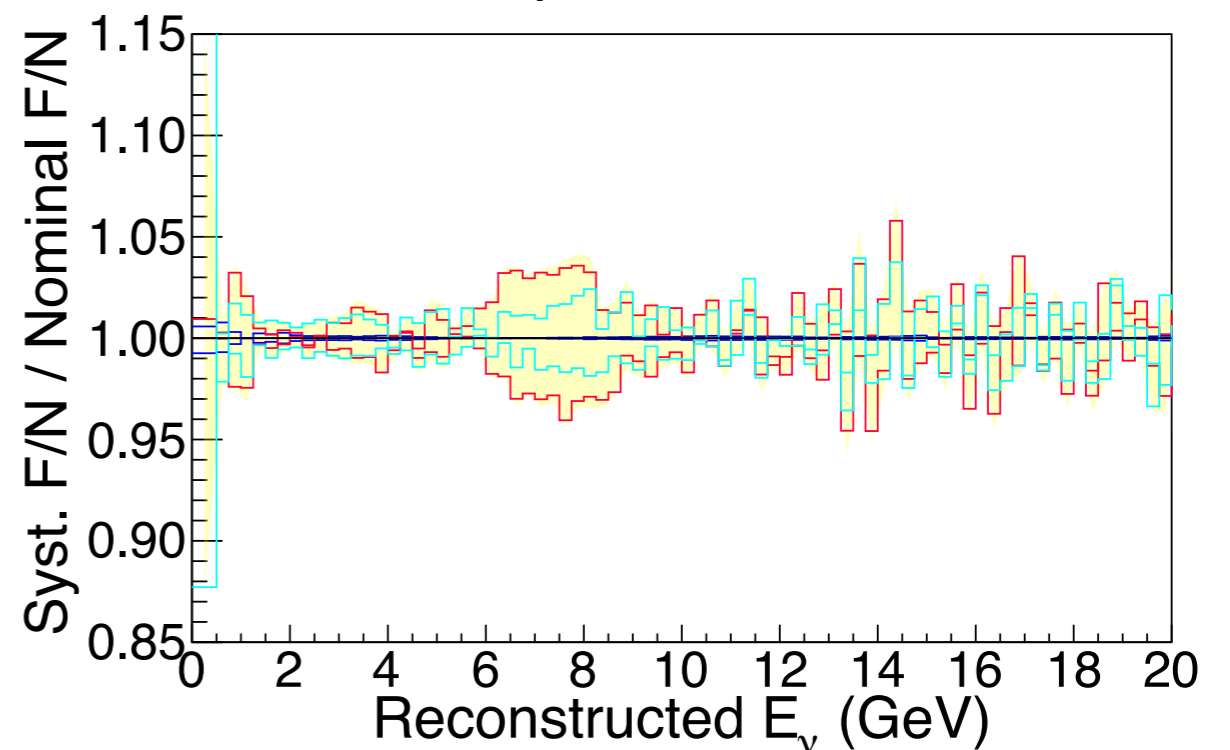
Neutrino Energy Spectrum



Asimov Contours:  $1\sigma$ , 90%C.L and 95%C.L



All Runs F/N Systematic Double Ratios



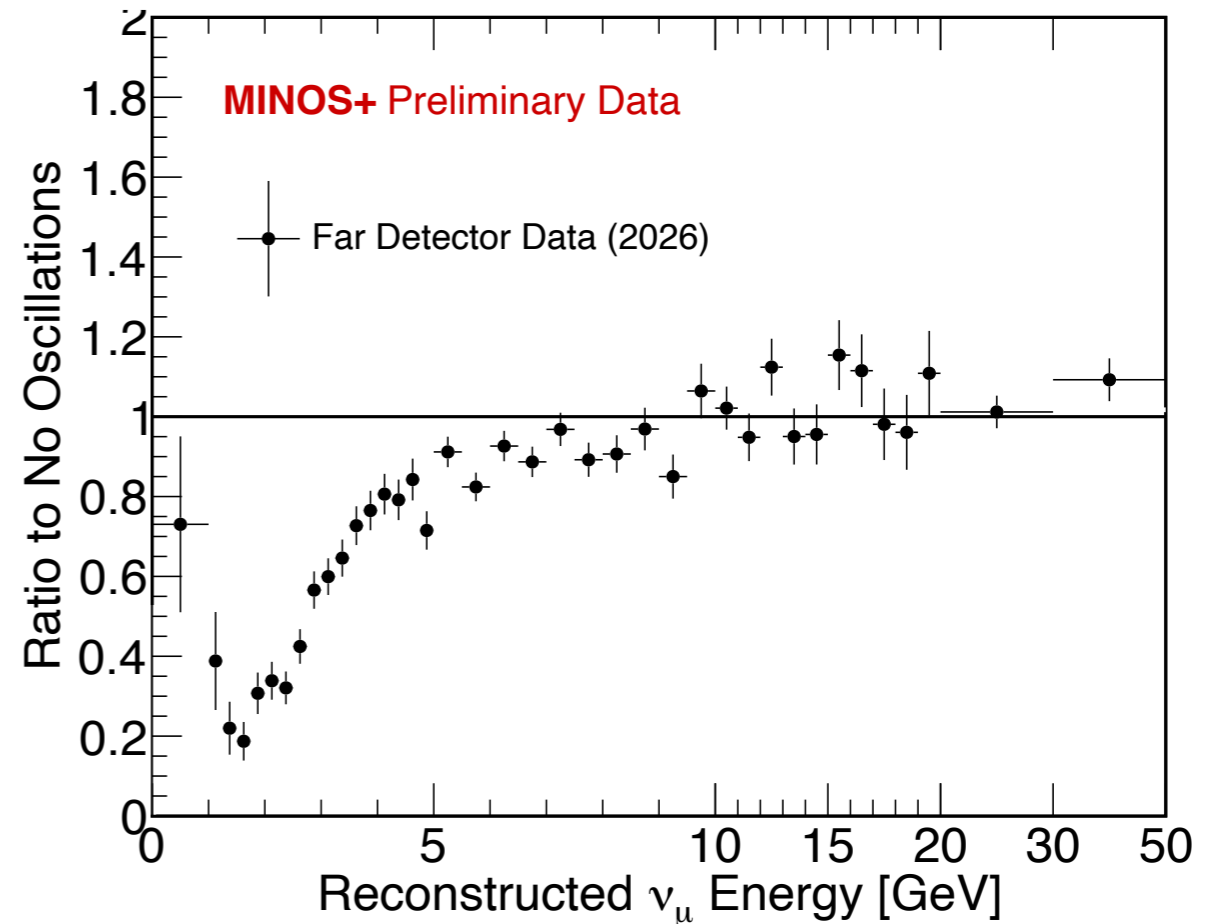
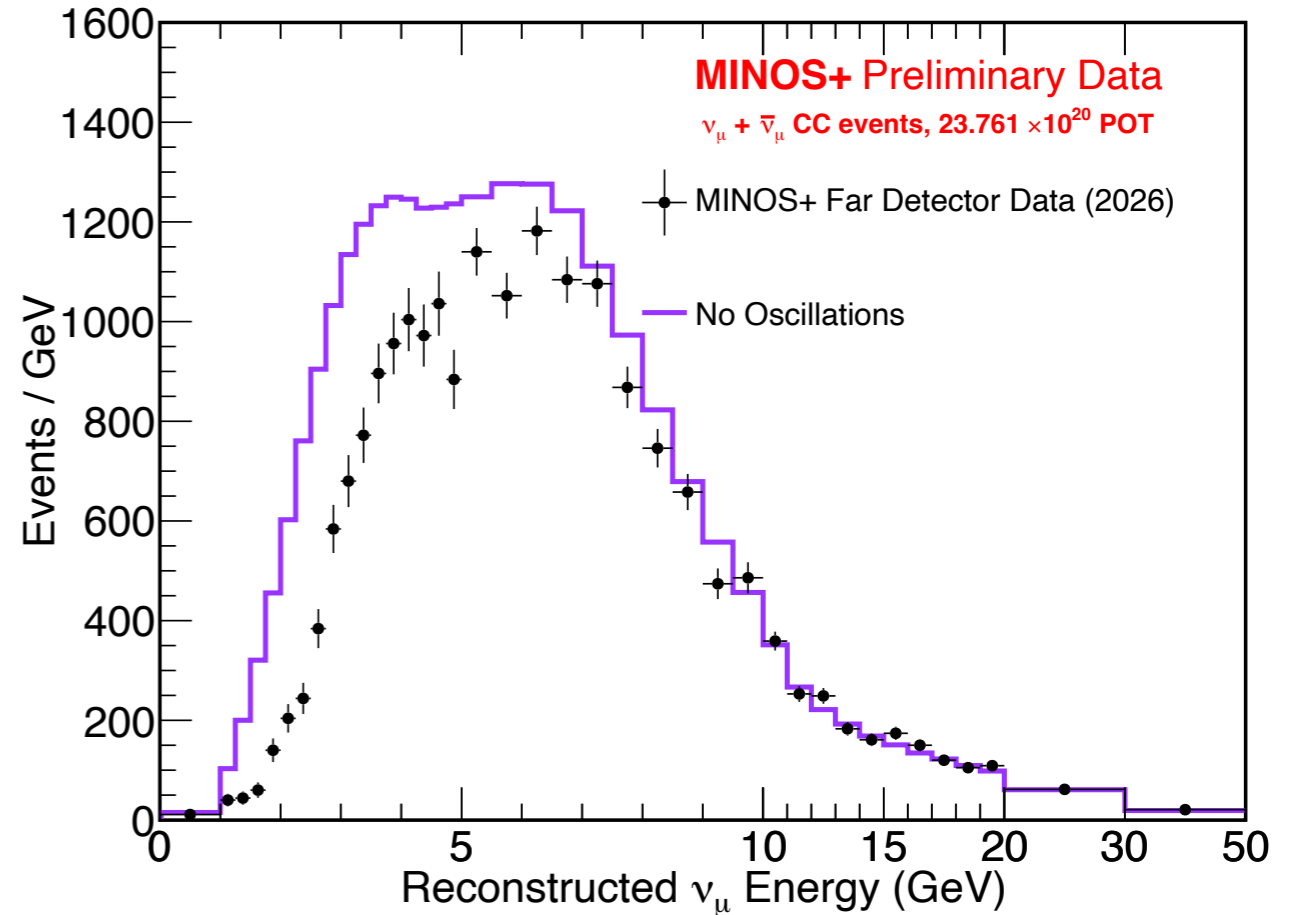
# Results

## MINOS Results



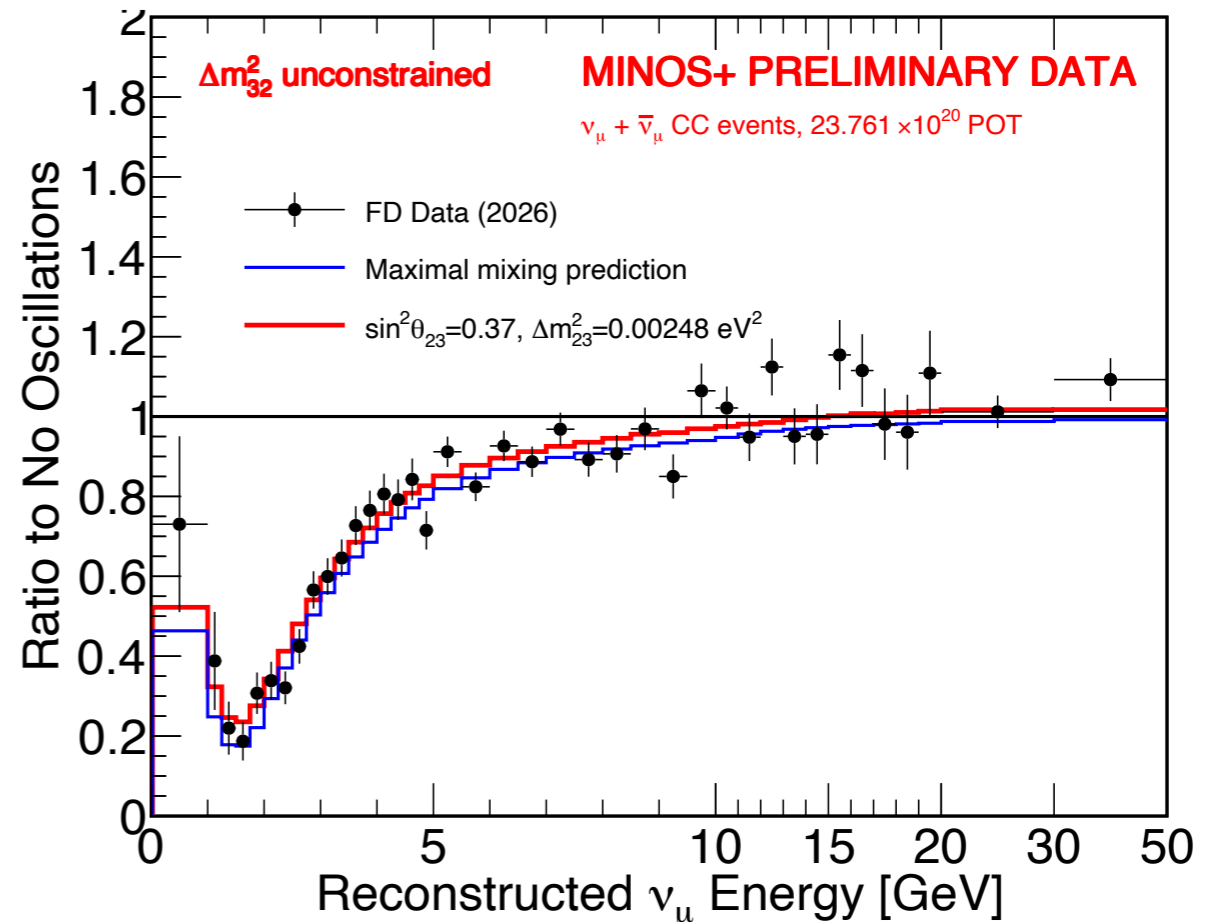
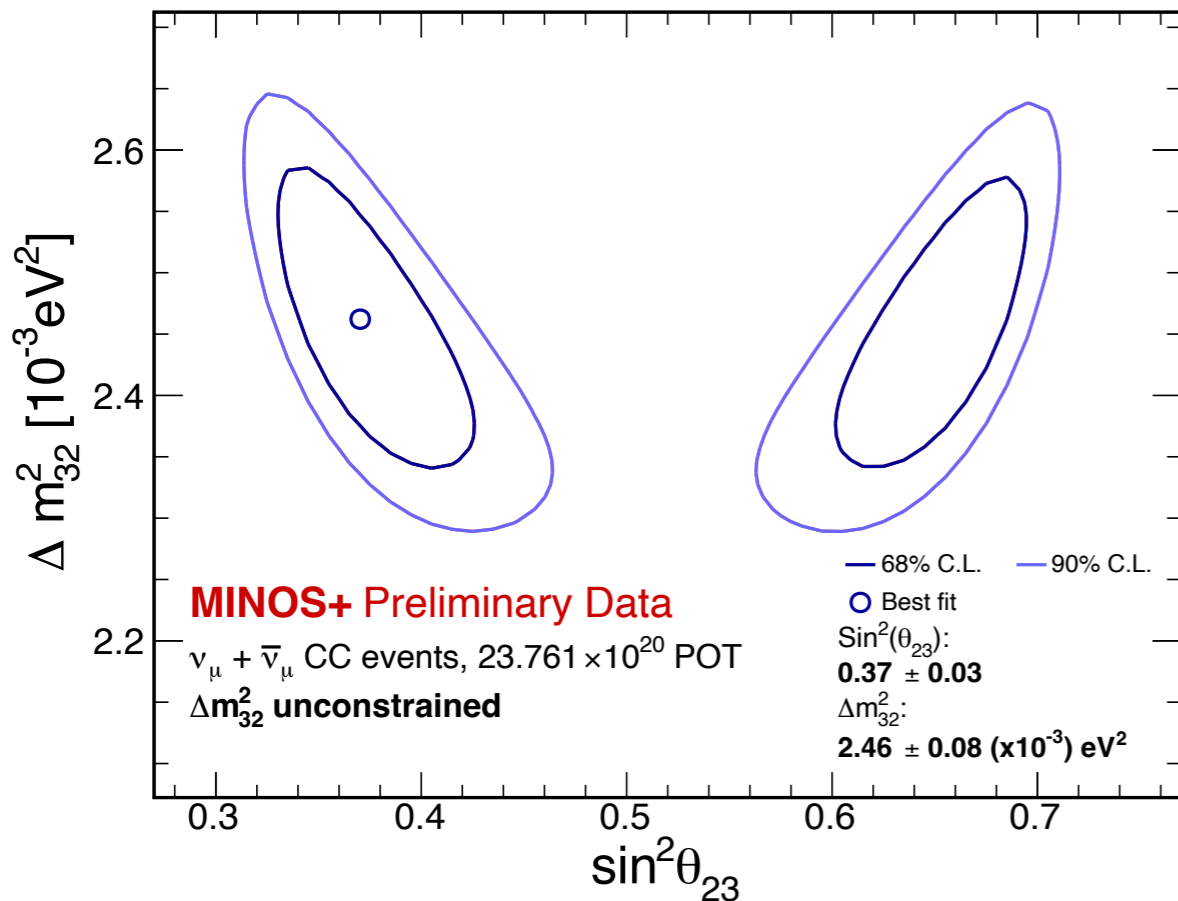
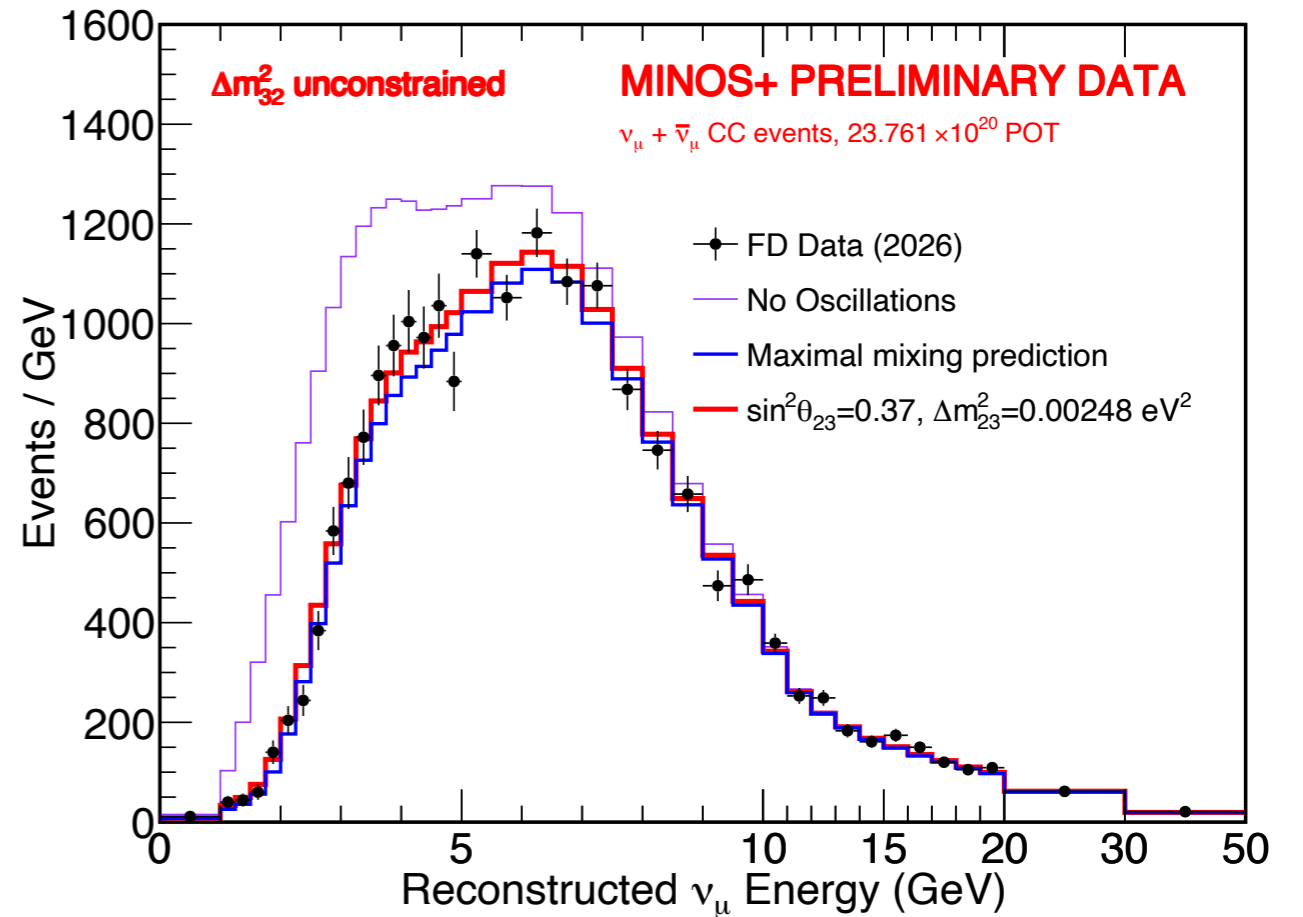
# MINOS+ Results

- Standard (three-flavour) fit to  $\Delta m^2$  and  $\sin^2\theta_{23}$
- Disappearance only, no  $\nu_e$  appearance: no  $\delta CP$ , no octant information



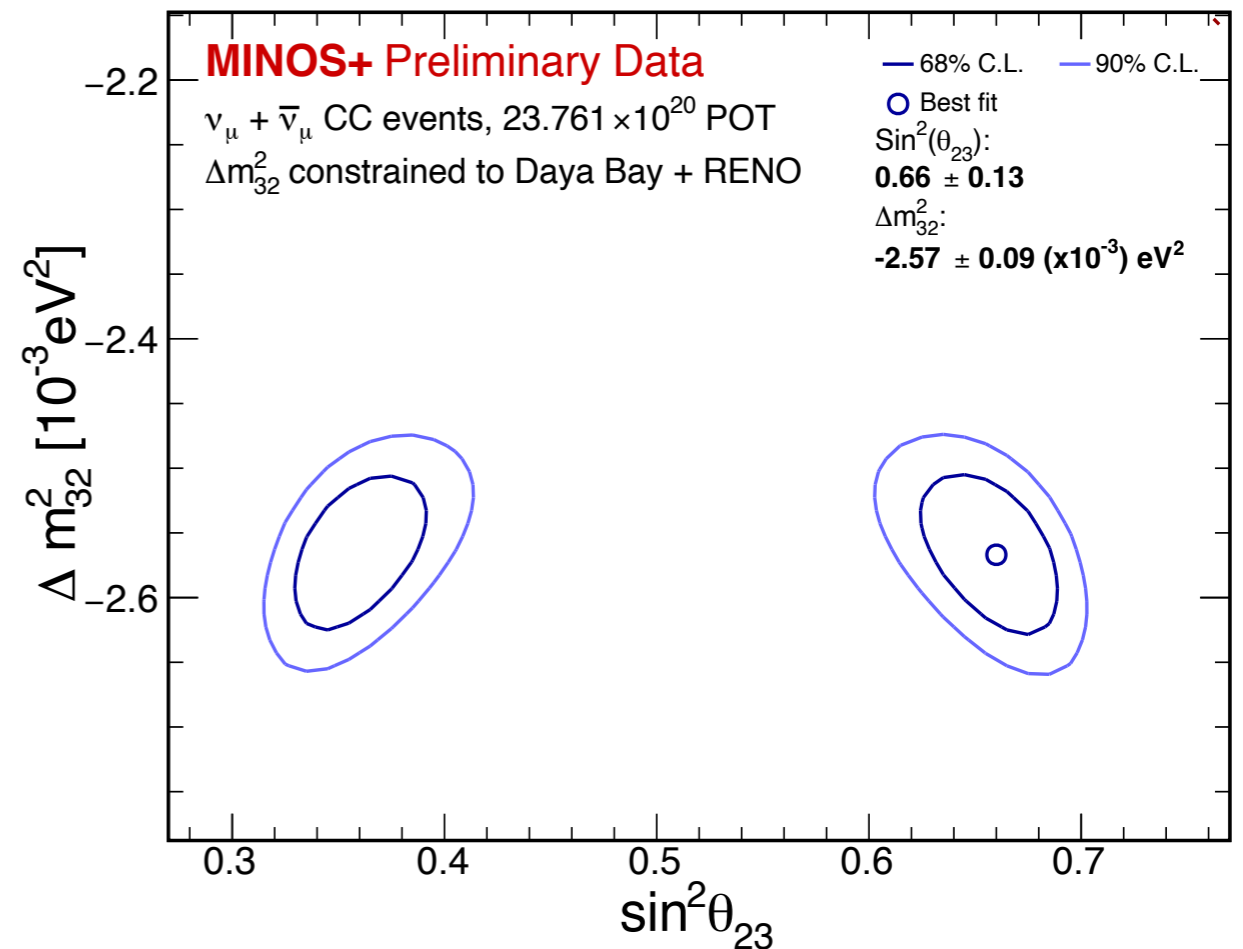
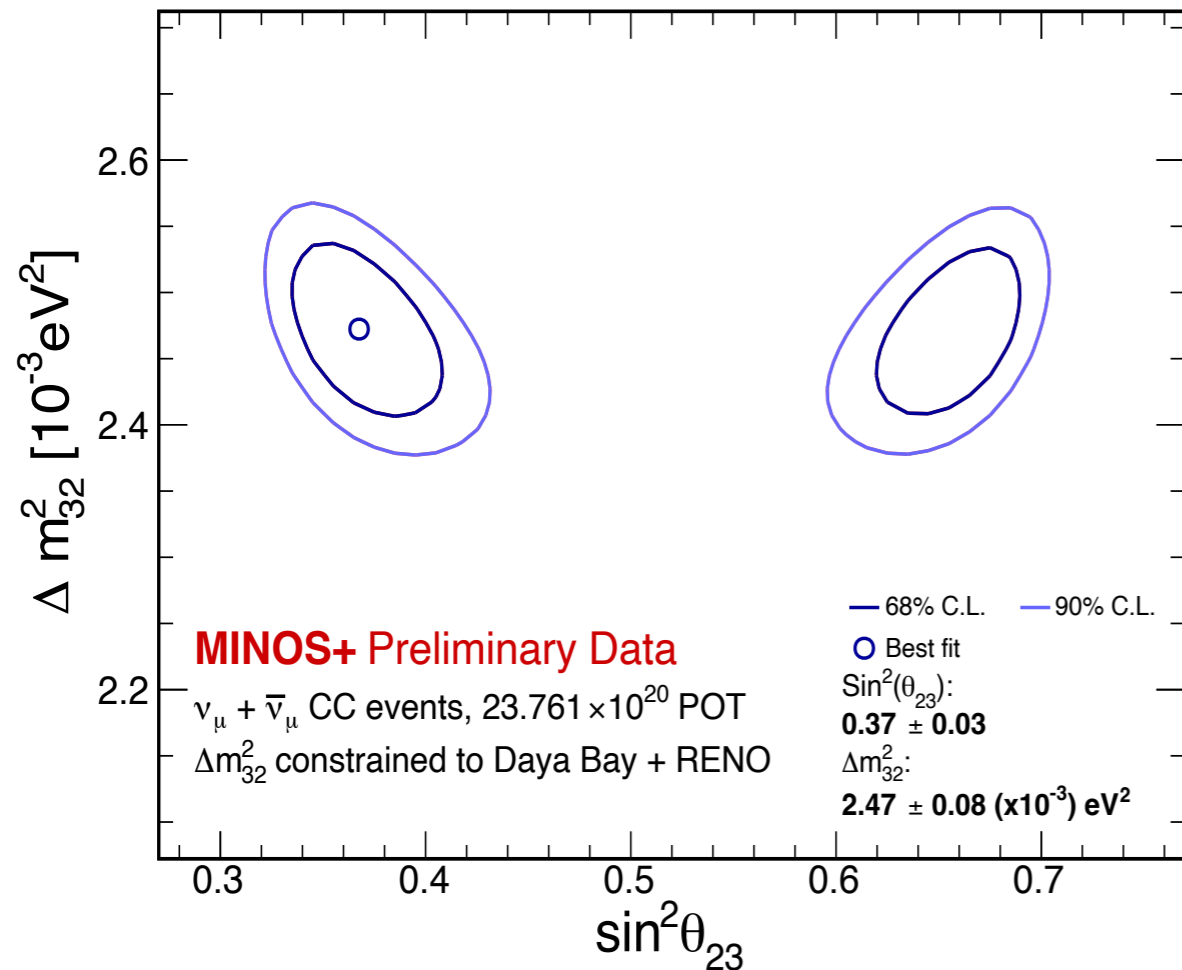
# MINOS+ Results

- 3 flavour fit produces symmetrical contour (only disappearance)
- Unconstrained fit with both parameters excludes maximal mixing solution at 90% C.L.



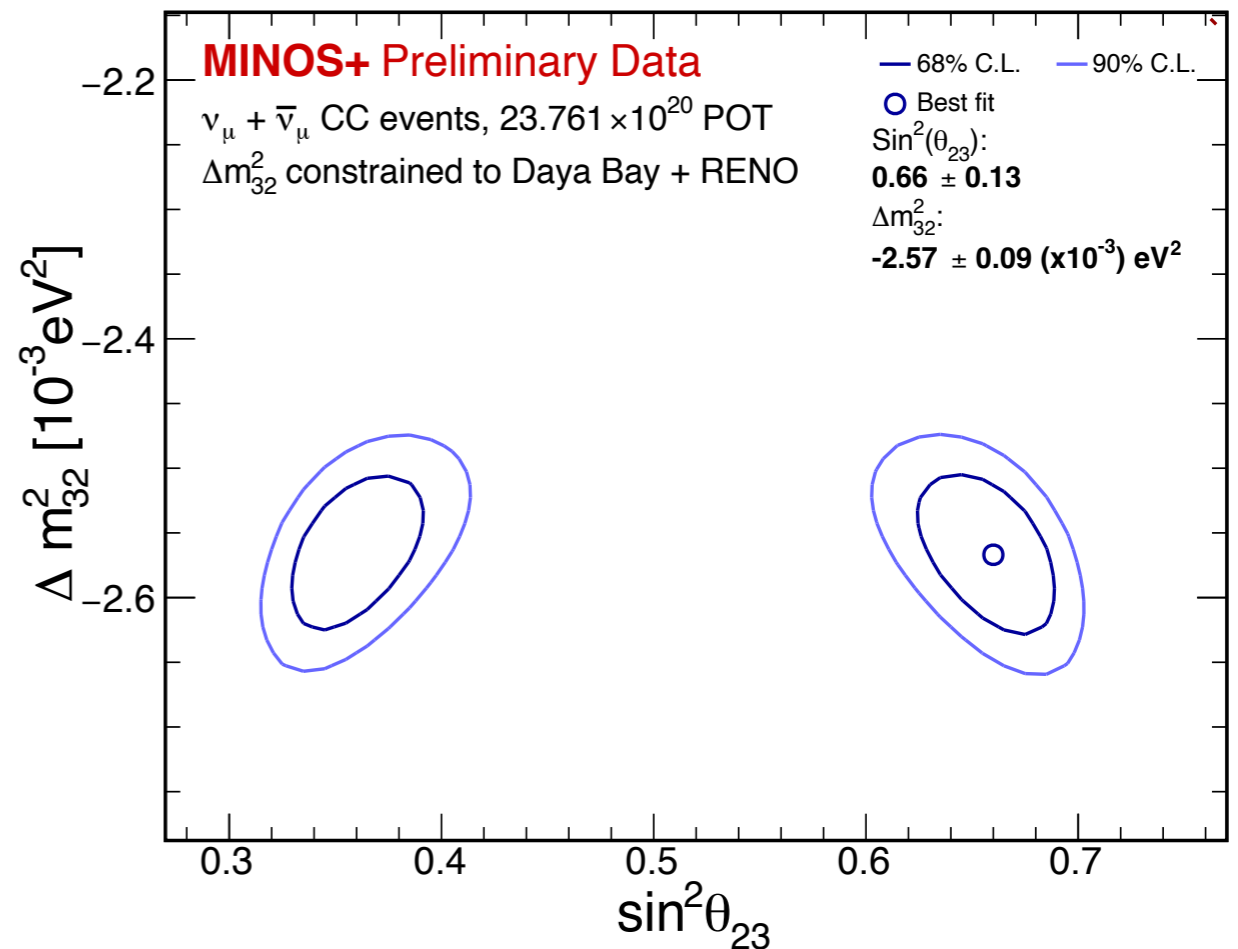
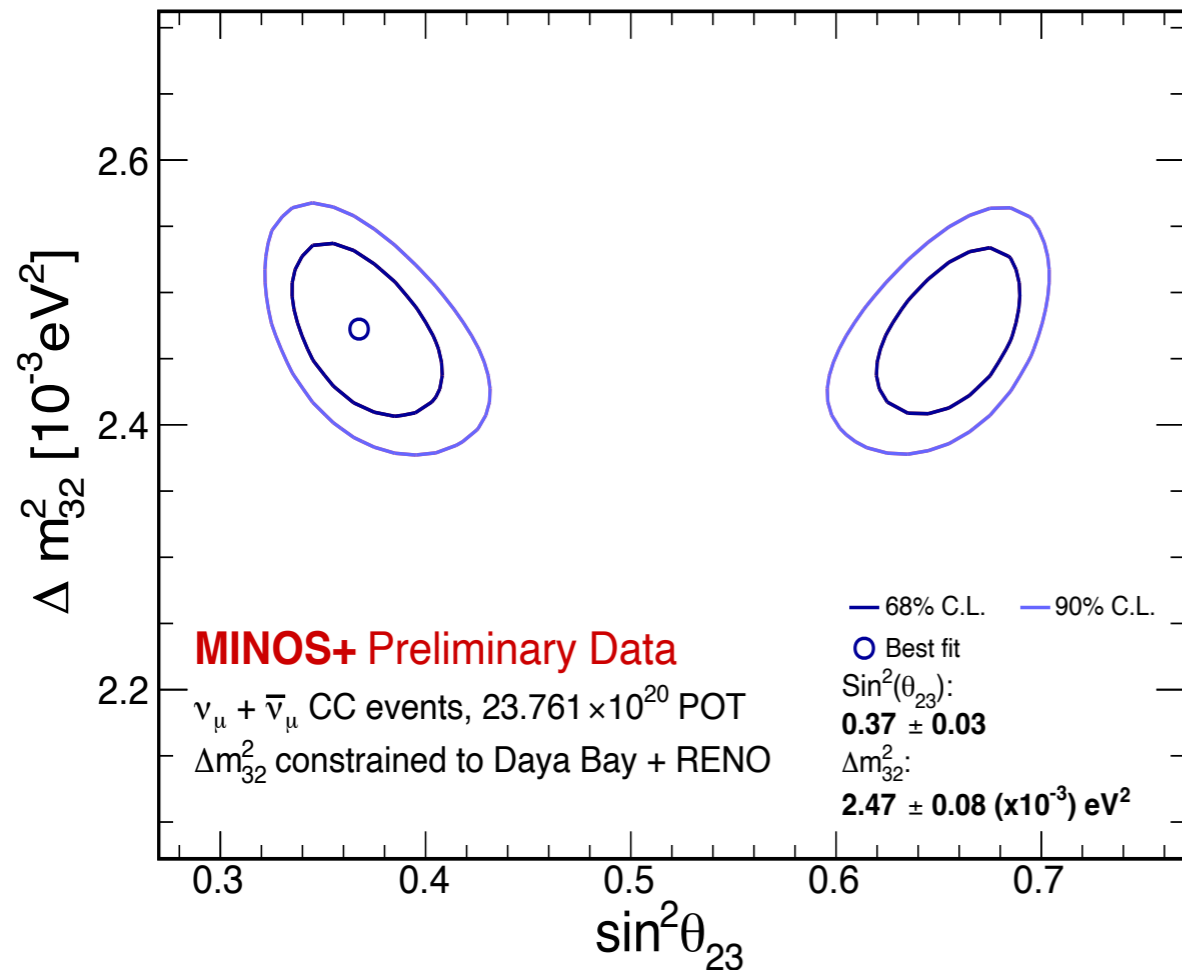
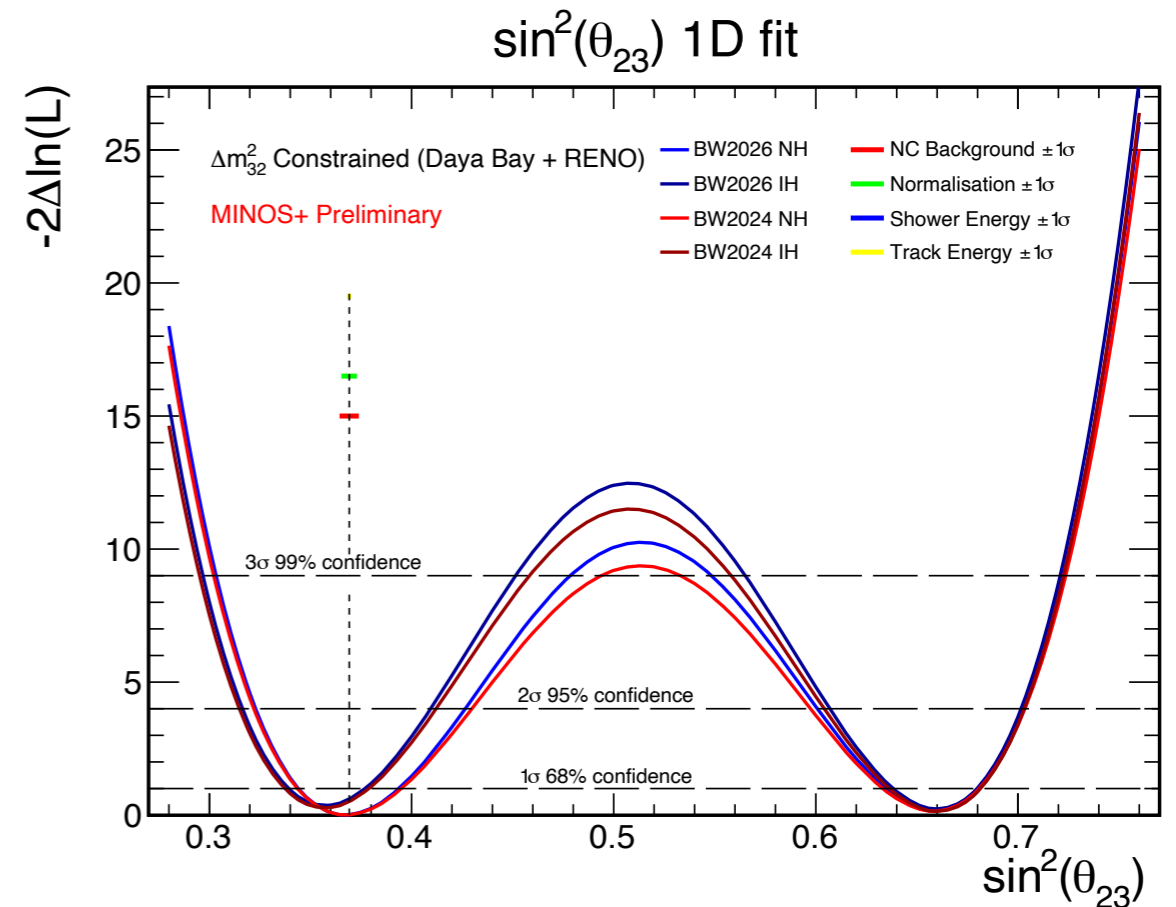
# MINOS Results

- **Constrain  $\Delta m^2$**  with Reactor value



# MINOS Results

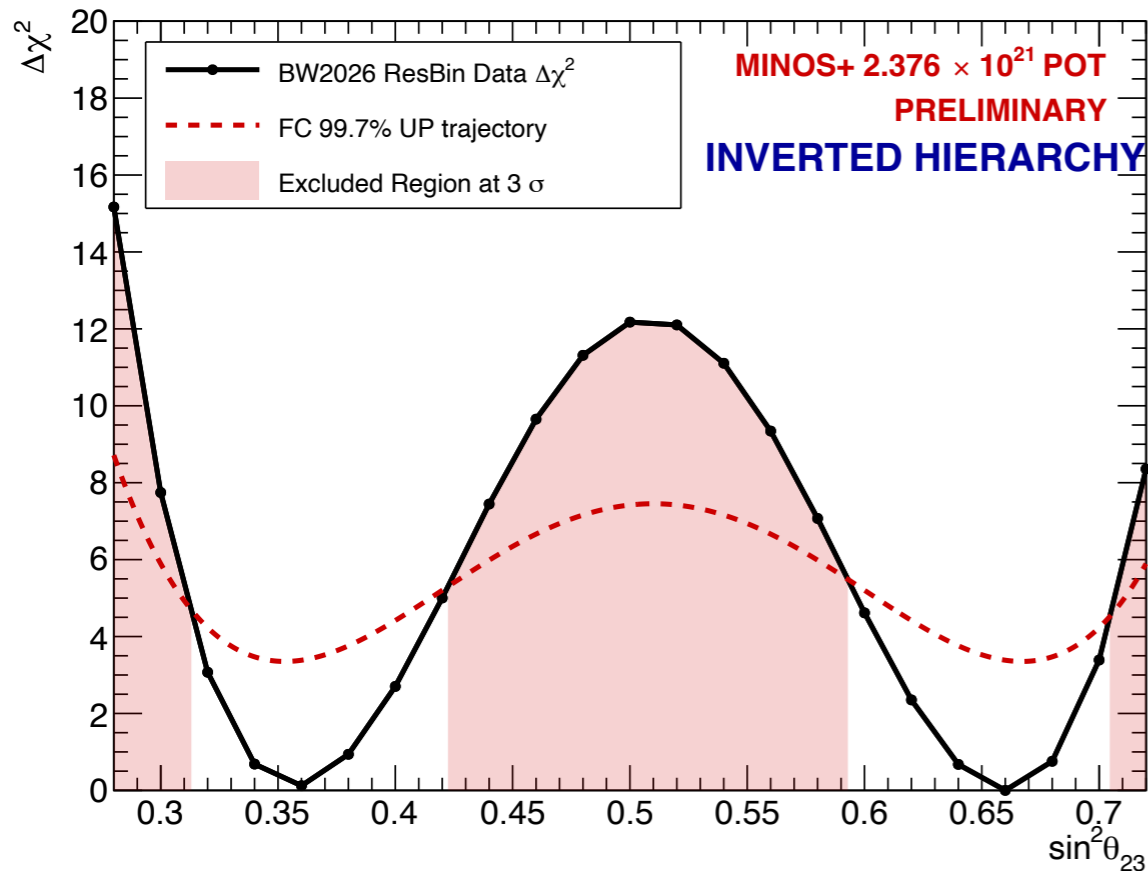
- **Constrained  $\Delta m^2$**  with Reactor Constraint excludes maximal mixing at  $3\sigma$
- FC Corrections important with a constrained fit



# MINOS Results (Feldman Cousins Corrected)

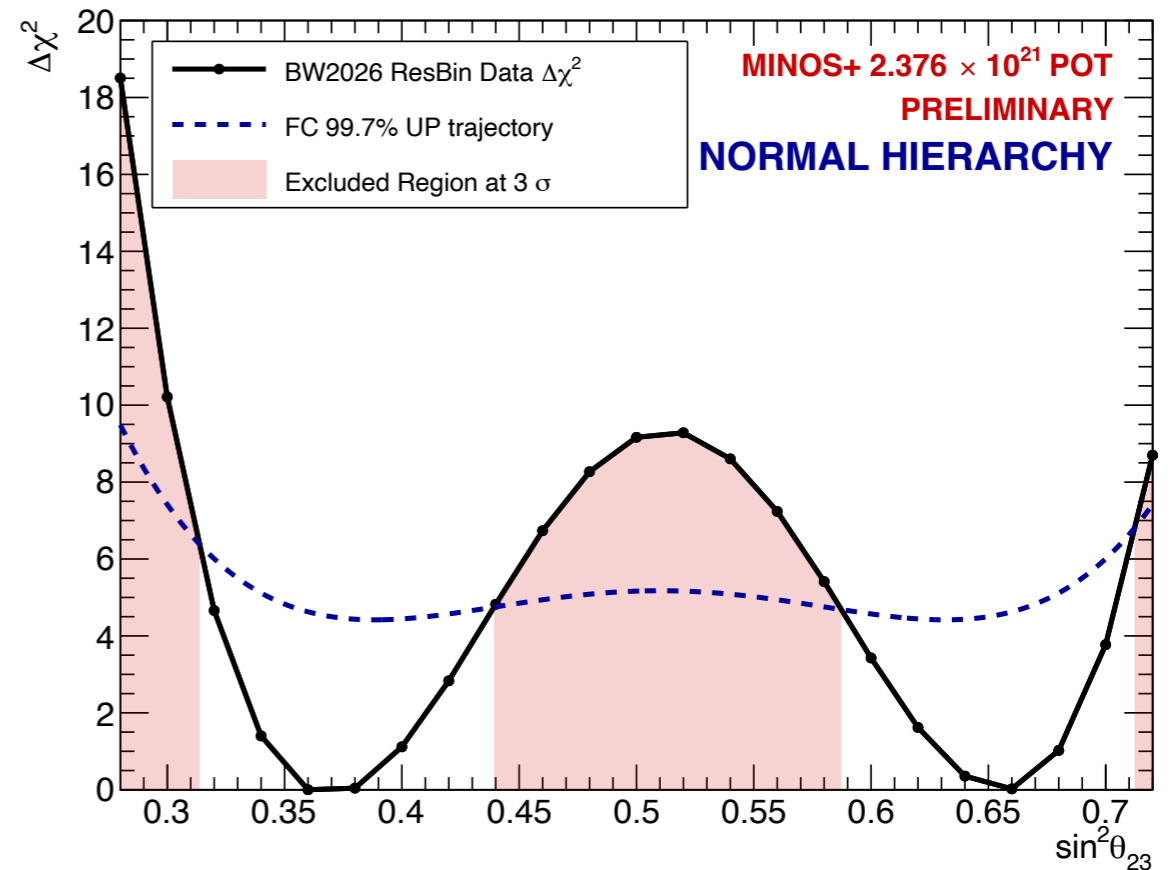
MINOS+ Data  $3\sigma$  exclusion

Excluded at  $3\sigma$ :  $<0.31, 0.42-0.59, \text{ and } >0.70$

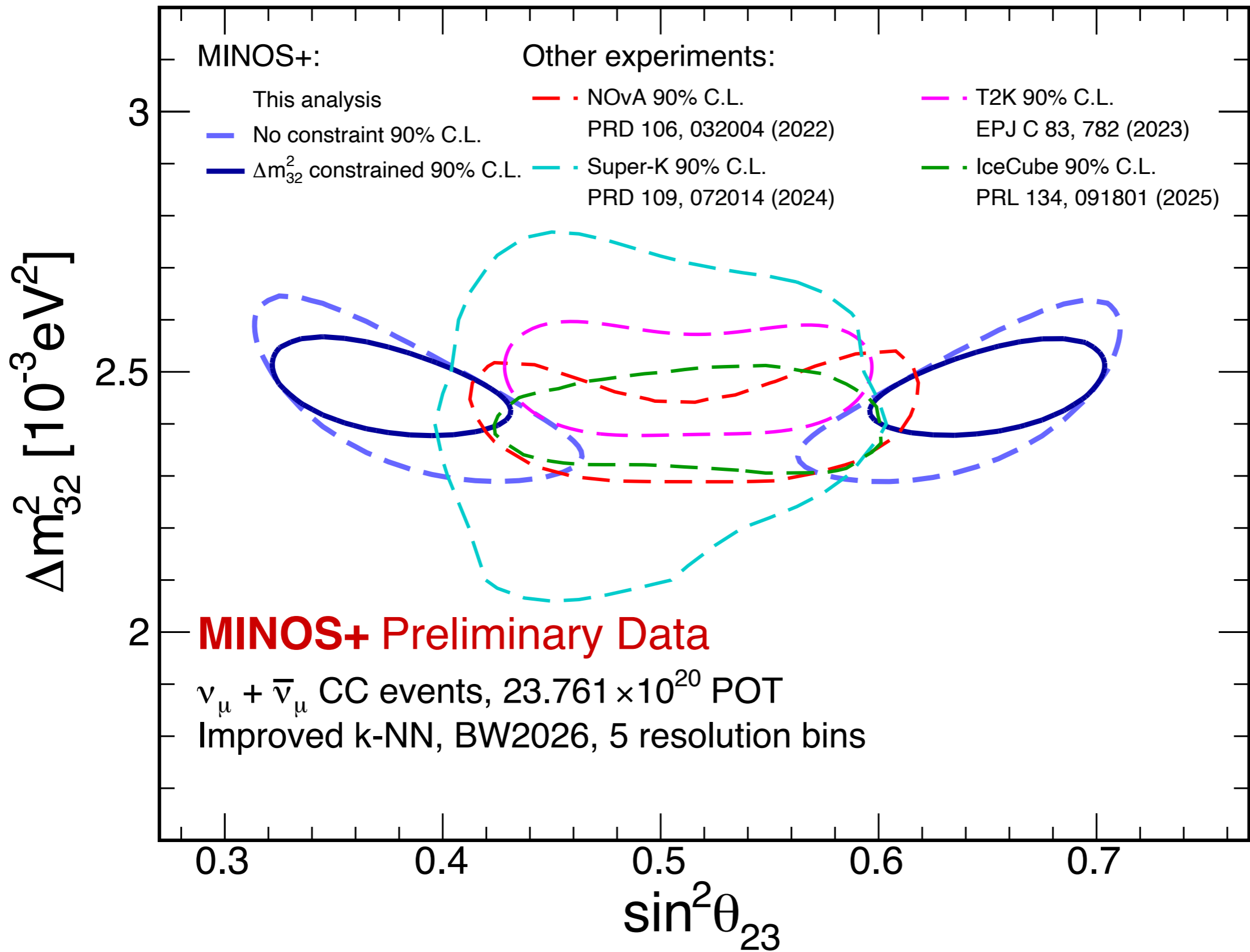


MINOS+ Data  $3\sigma$  exclusion

Excluded at  $3\sigma$ :  $<0.31, 0.44-0.59, \text{ and } >0.71$



- MINOS data with **reactor constrained  $\Delta m^2$**  excludes maximal mixing at  $3\sigma$
- IH : 0.42-0.59 excluded at  $3\sigma$
- NH : 0.44-0.59 excluded at  $3\sigma$



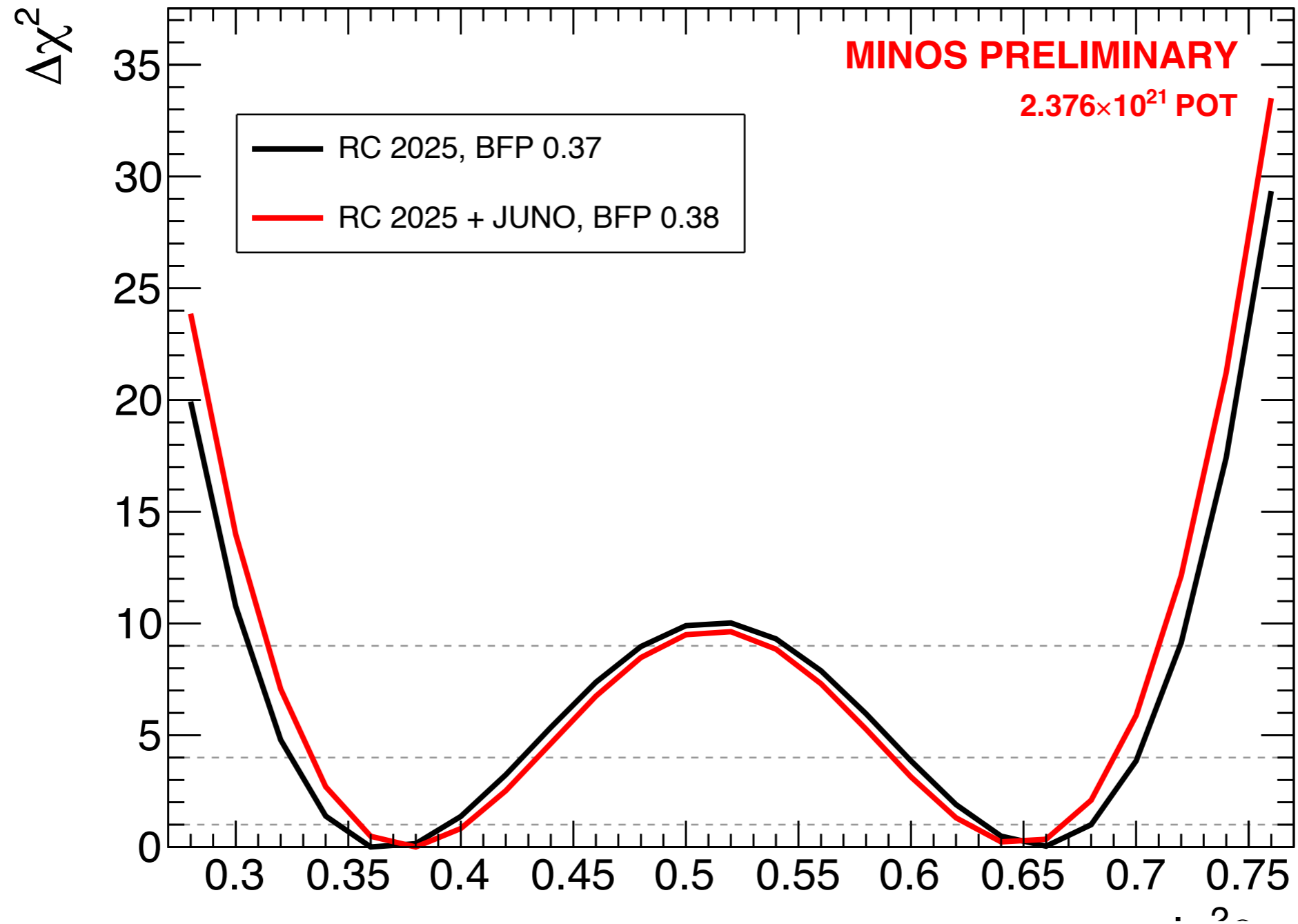
# Looking to the future

- MINOS on-axis data set will be curated
  - Keep it in a raw form that can be used easily with ML : this will become an industry
  - Keep current in light of new modelling developments \$\$\$\$\$\$ - curate the MC too!
- Conference rush means there are always things left on the table
  - Come back to them!
- New experiments coming soon (when?) but existing data will be a spring board to get quickly to the remaining unknowns

# Conclusion

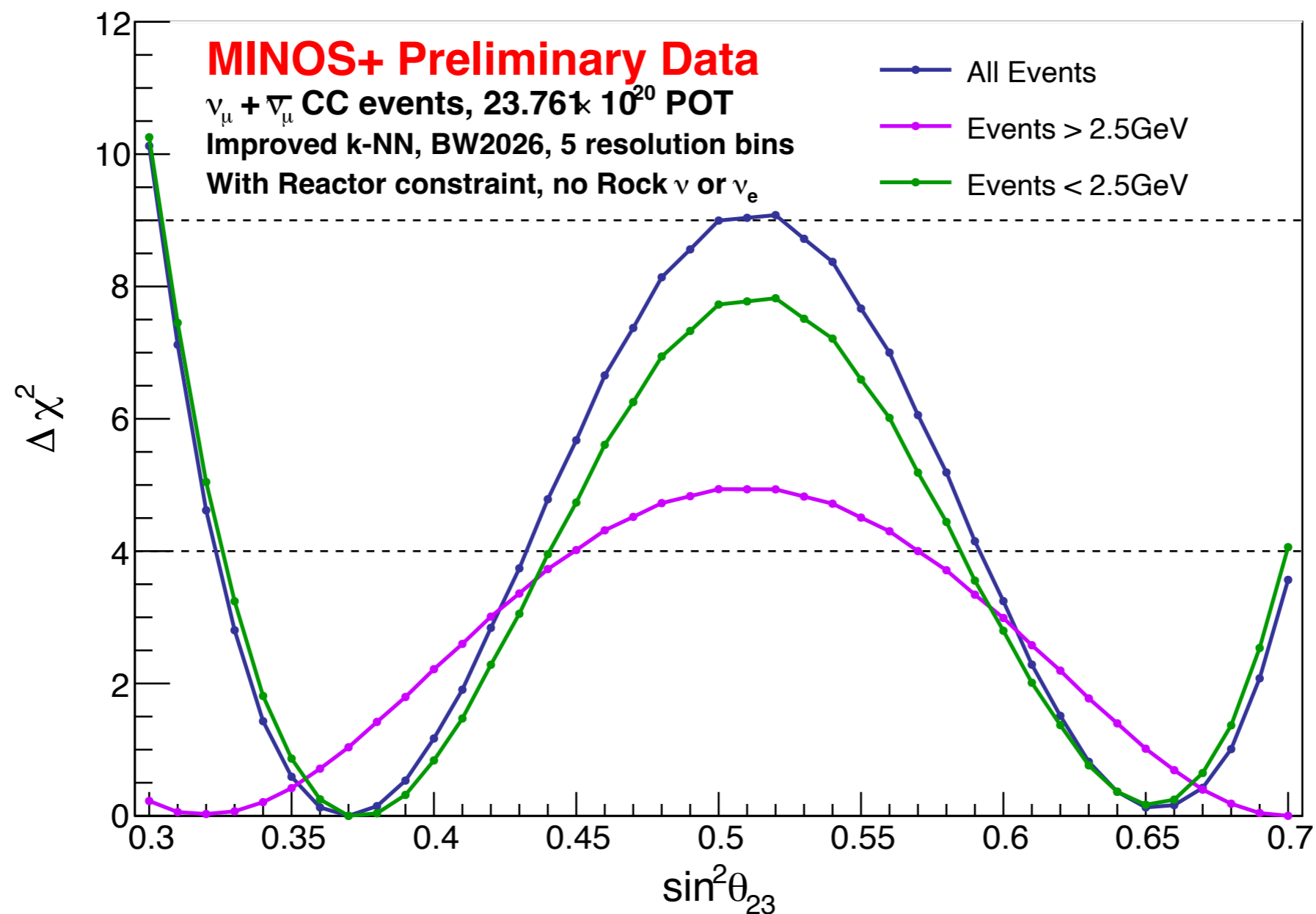
- The MINOS analysis has been renovated and polished
- MINOS rules out maximal mixing at the  $3\sigma$  level with reactor constraint
- Excluded region extends from 0.44 to 0.59 in  $\sin^2\theta_{23}$
- Potentially important tension with off-axis LBL experiments must be understood
- Until DUNE, MINOS is still the only 2-detector on axis experiment in town!

# MINOS+ Results (JUNO + RC constraint)



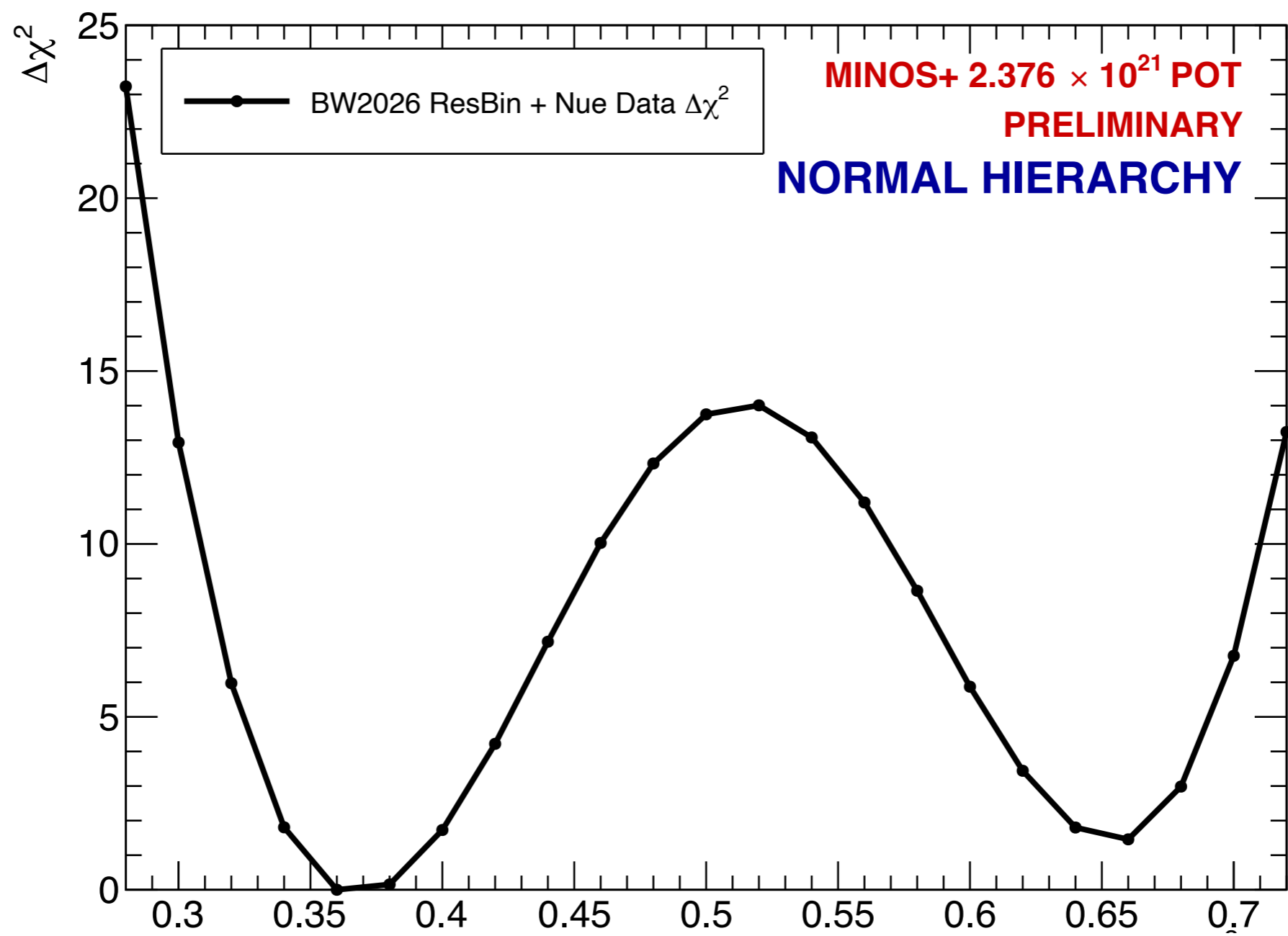
# MINOS+ Results (Cross checks)

- Sanity check at below and above 2.5 GeV renders similar trend



# MINOS+ Results (Cross checks)

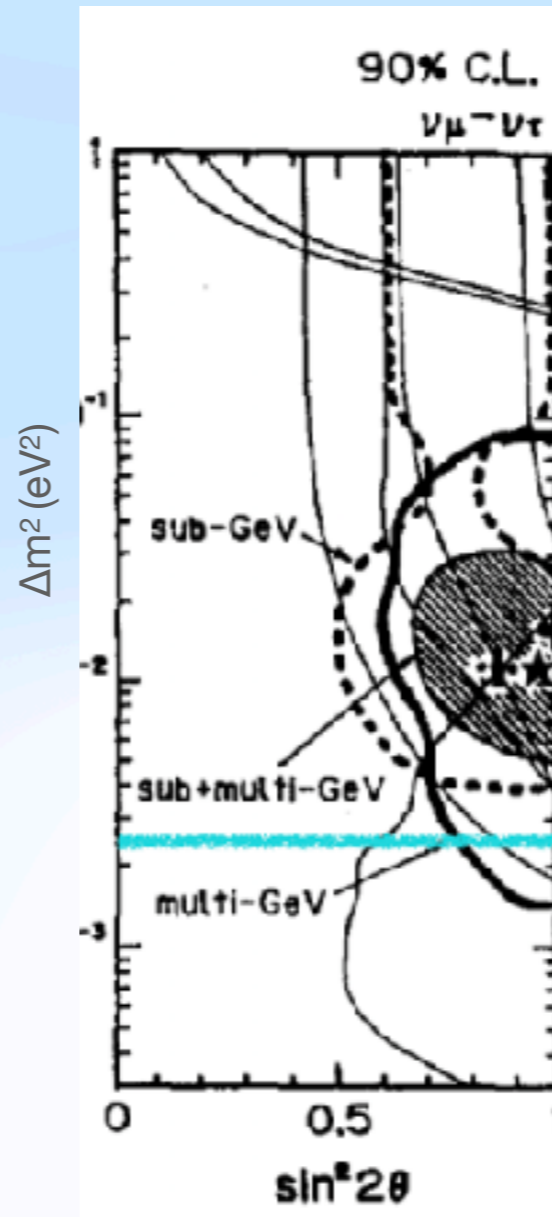
- Including  $\nu_{e\mu}$  chi



# The conventional wisdom at the time

## The Kamiokande Experiment

- In 1991 Kamiokande had shown that if neutrino oscillations were the cause of the missing atmospheric neutrinos in their water Cherenkov detector, then the  $\Delta m^2$  (difference in mass squared of the two types of neutrinos) was  $\sim 10^{-2} \text{ eV}^2$



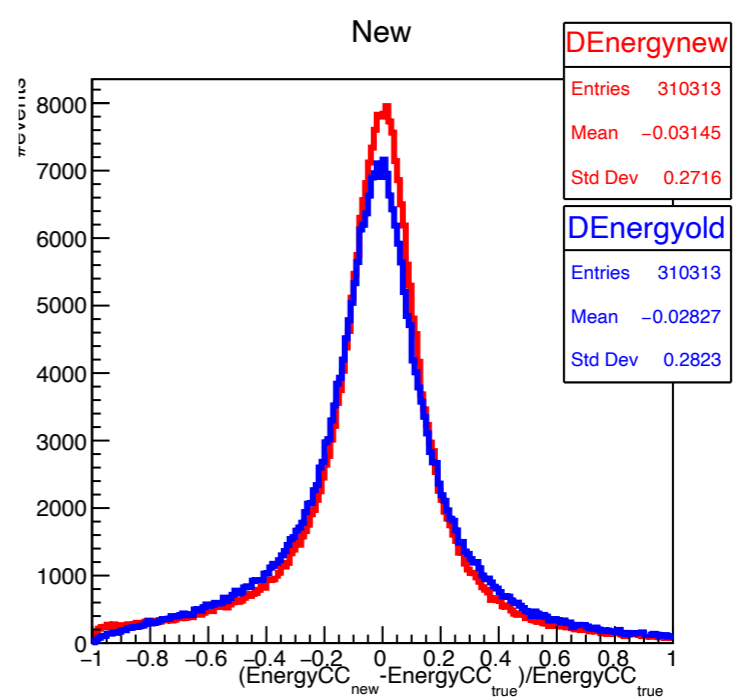
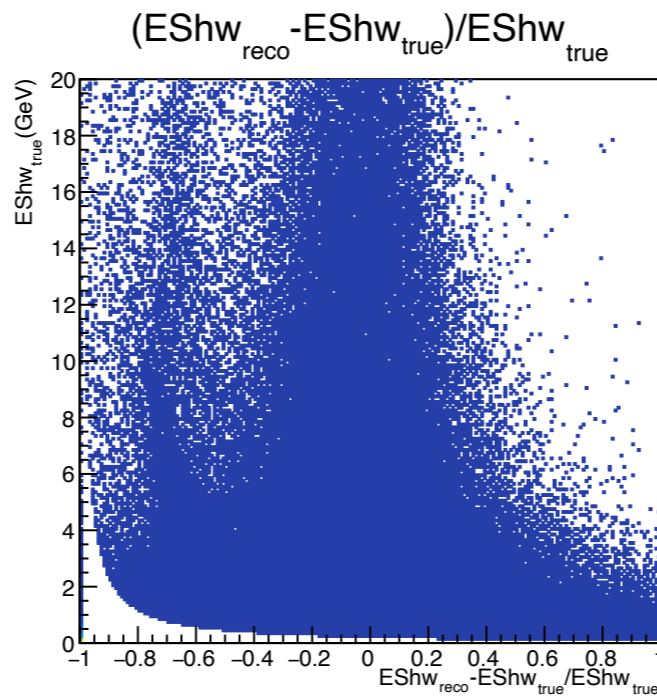
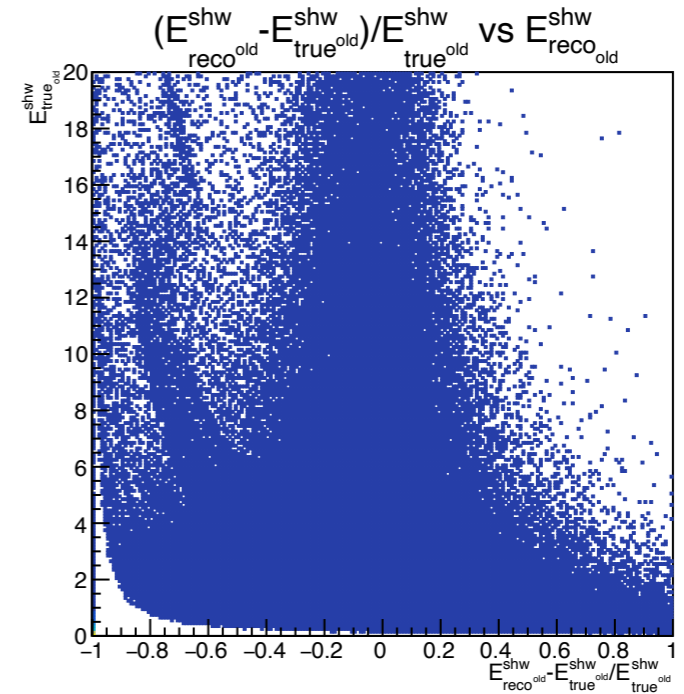
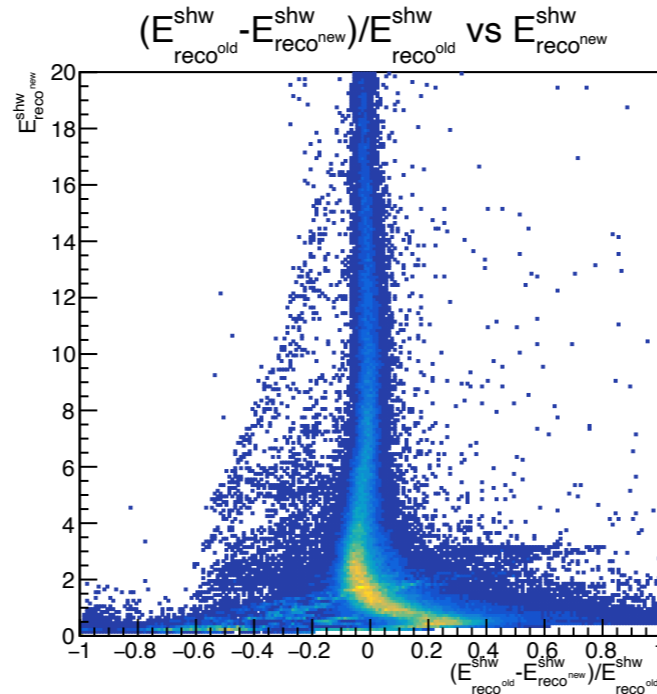
- The Japanese funding agency took it seriously....

“The Super-Kamiokande project was approved by the Japanese Ministry of Education, Science, Sports and Culture in 1991 for total funding of approximately \$100 million.”

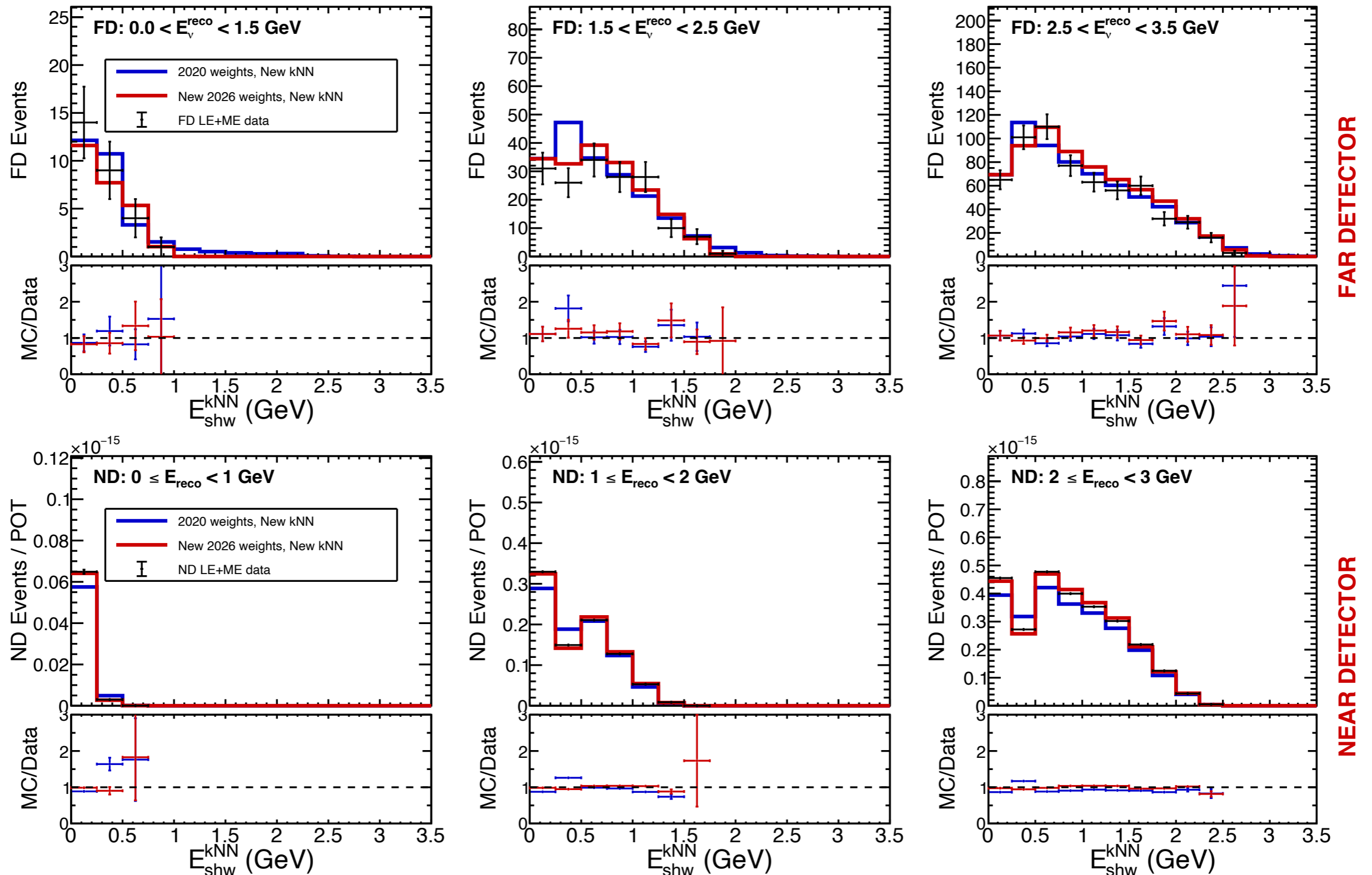
$$P(\nu_{\mu} \rightarrow \nu_{\mu}) = 1 - \sin^2 2\theta \sin^2 (1.267 \Delta m^2 L / E)$$

# Shower Energy Estimator

- The shower energy estimator uses three variables
  - raw PH in shower
  - PH along identified track
  - #planes in shower
- Previous calibration step was removed
- Movement in energy between new and old approaches is shown
- Overall, total fractional reconstructed energy distribution marginally improved



# Hadronic Shower Energy MC/Data



Hadronic energy in bins of total reconstructed neutrino energy : LE+ME

# The extrapolation procedure

