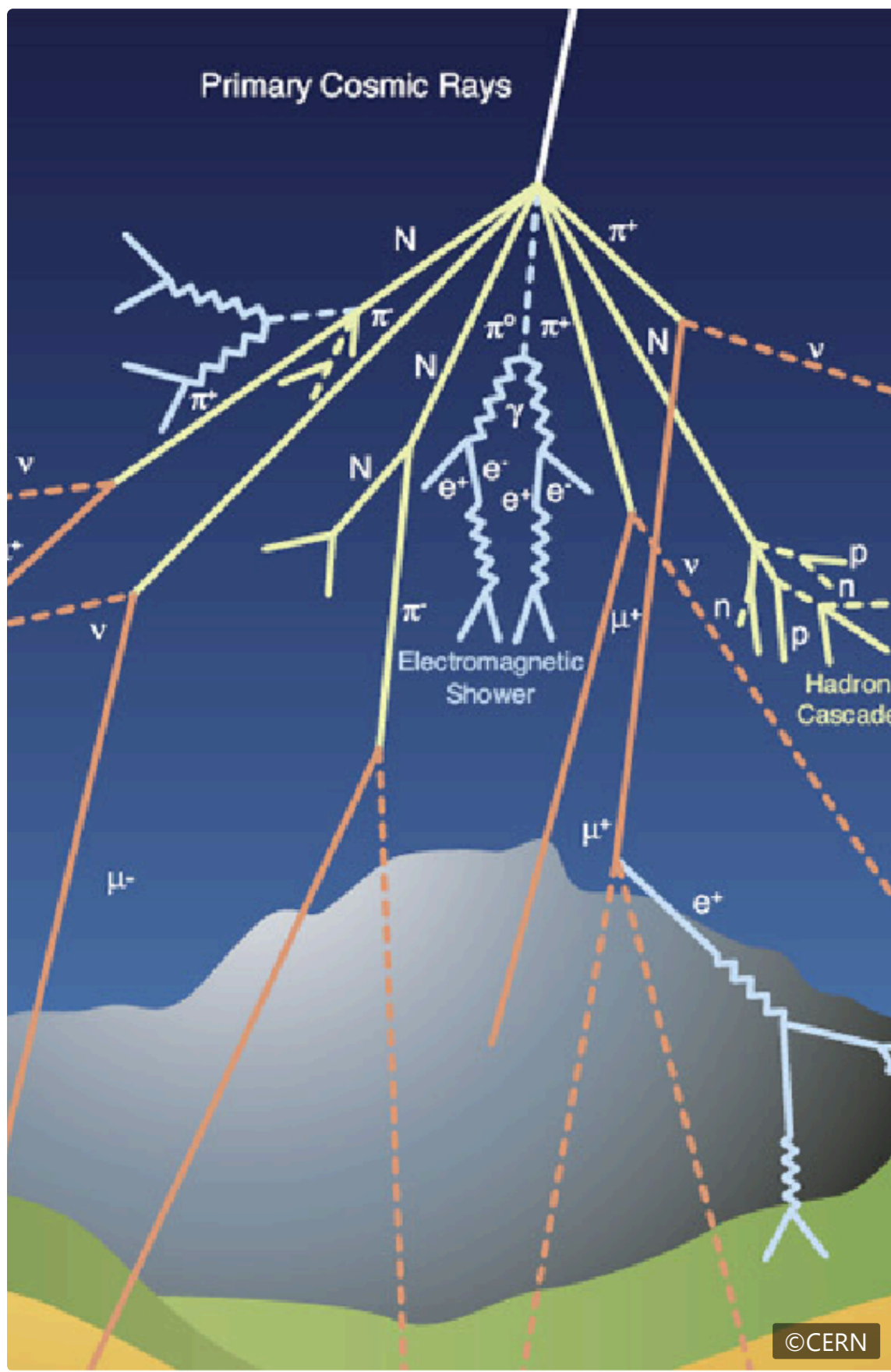


Atmospheric Neutrinos



- **Atmospheric ν** : key signal for oscillations; background for **DSNB, DM, nucleon decay**
- Existing 3D models (HKKMS, Bartol, FLUKA) focus on $E_\nu > 1$ GeV
- The < 100 MeV region — critical for DM searches — remains **unexplored**
- **3D Calculation Framework**

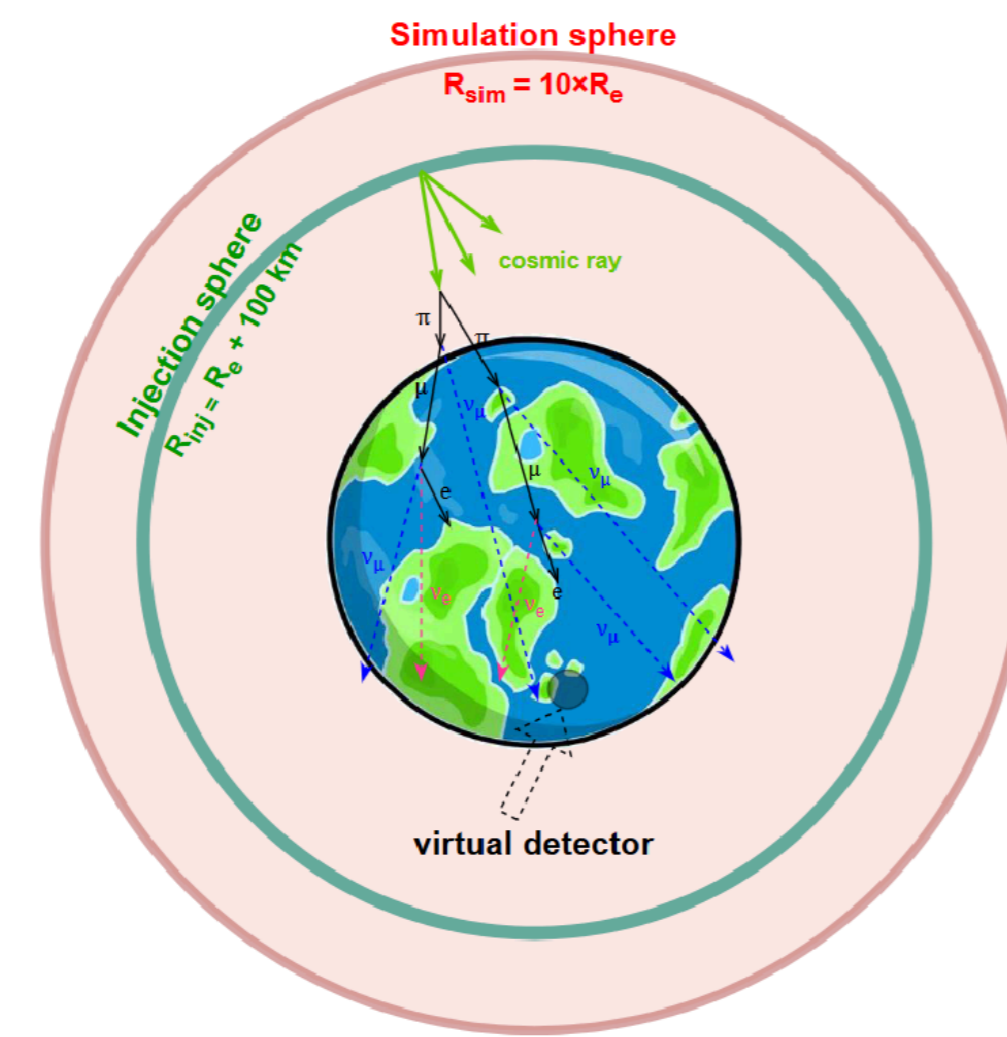
$$\Phi_\nu = \Phi_{CR} \otimes R_{geo} \otimes Y_\nu$$

Primary CR Flux

Geomagnetic Cutoff

Hadronic Interaction

$\pi/K/\mu$ Decay



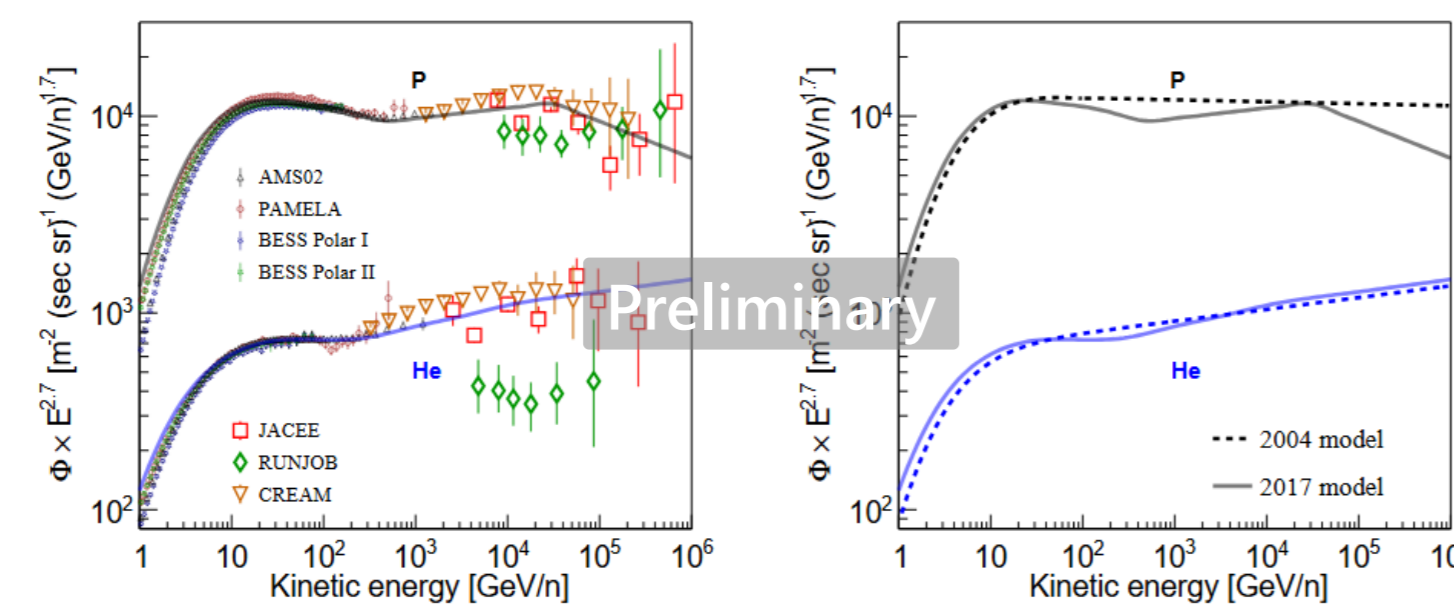
Based on the calculation scheme by Honda-san^{[1][2]}

- **3D geometry**: Earth sphere (R_E) → Injection sphere ($R_E + 100$ km) → Simulation sphere ($10 \times R_E$)
- **Virtual detector** with size correction for each site
- **Backward ray-tracing** for geomagnetic rigidity cutoff

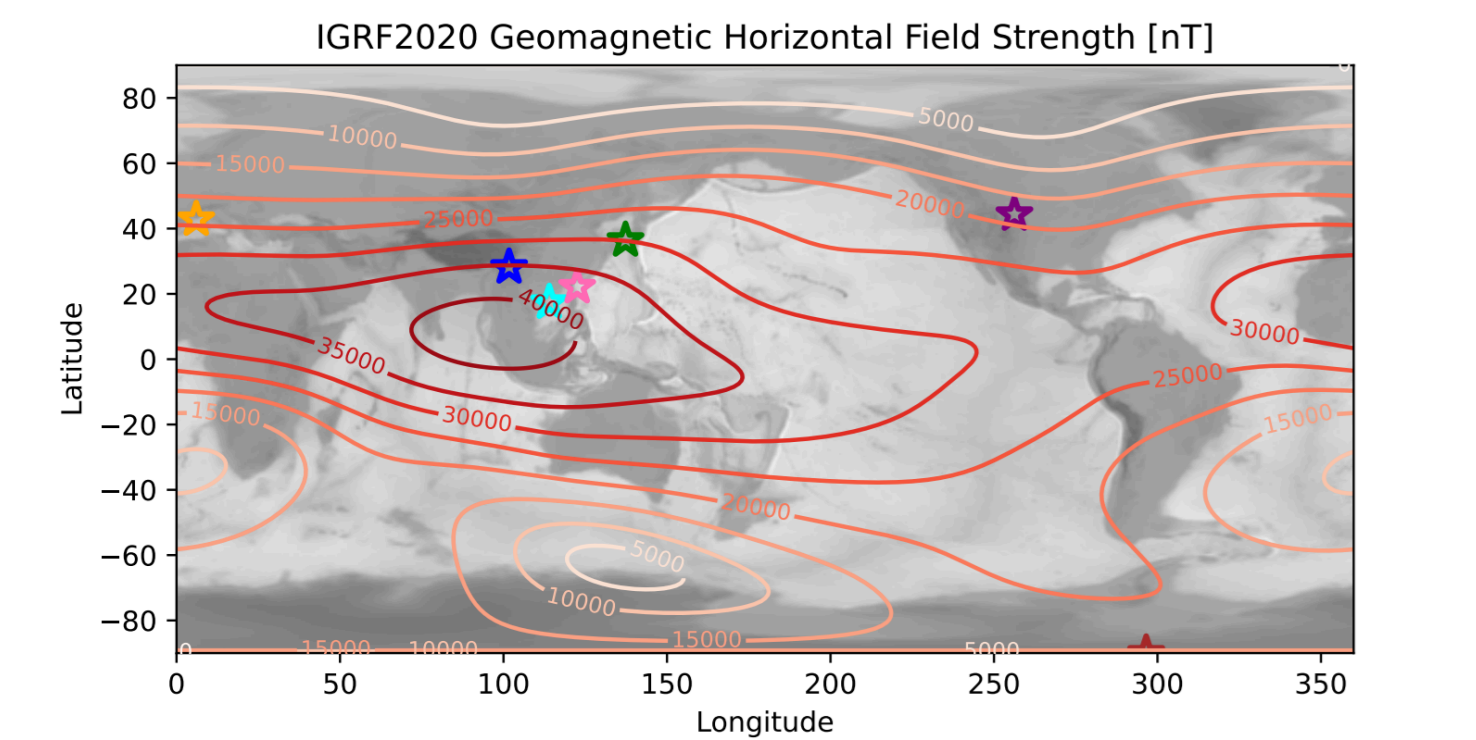
Model Updates

Component	HKKMS15	This Work
CR Model	2004	2017 (AMS02)
Geomagnetic	IGRF2010	IGRF2020
Atmosphere	NRLMSISE-00	NRLMSISE-00
Hadronic	JAM+DPMJET	Recalibrated
μ in Earth	X	✓

Updated Primary Cosmic Ray Model

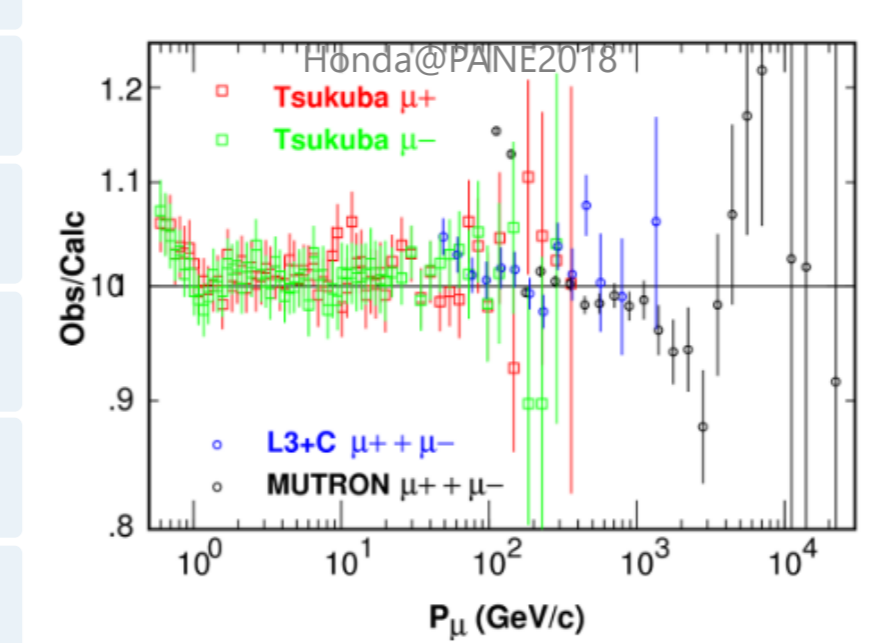


Geomagnetic Field (IGRF2020) & Sites



JUNO ~23°N
Super-K ~36°N
CJPL ~28°N
TRIDENT ~15°N
IceCube ~90°S
DUNE ~42°N
ORCA ~43°N

Hadronic model calibrated to muon observations



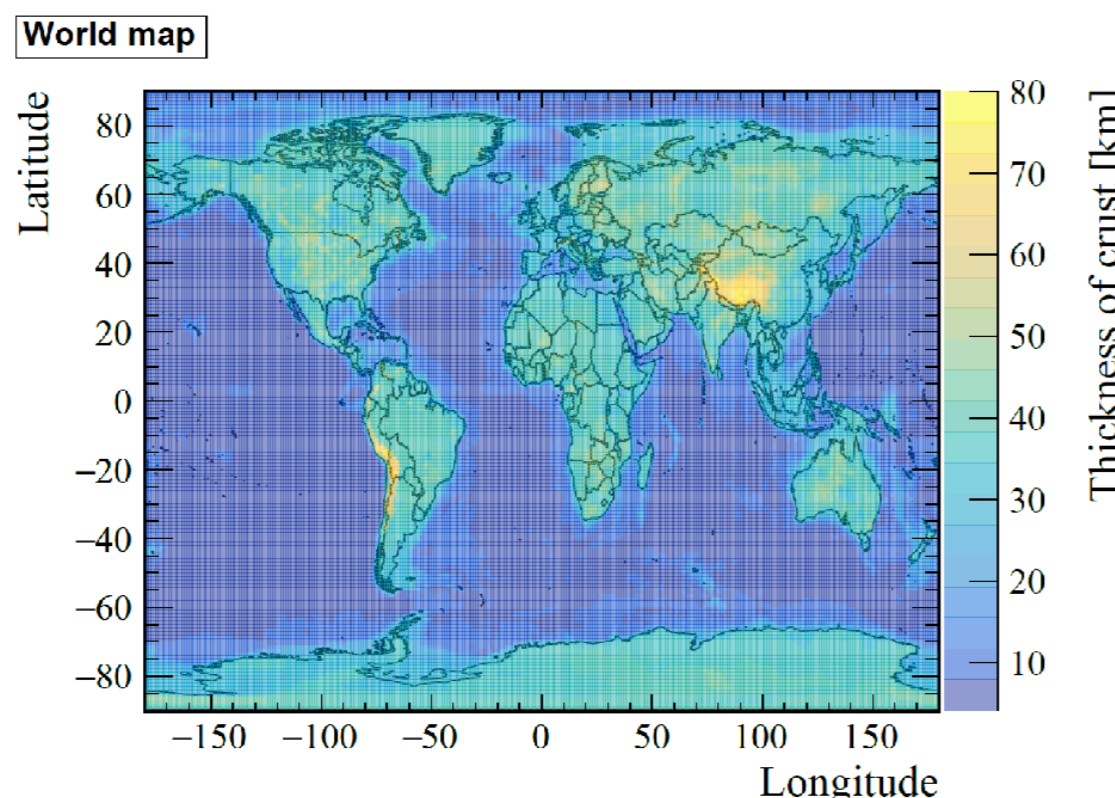
μ Propagation in Earth

Physical processes of muons inside the Earth — **New contribution at $E_\nu < 100$ MeV**

- μ^+ : stop and decay → $e^+ + \nu_e + \bar{\nu}_\mu$
- μ^- : stop and captured by atom
- decay inside atom (→ $e^- + \nu_\mu + \bar{\nu}_e$)
- nuclear capture ($\mu^- + p \rightarrow \nu_\mu + n$)

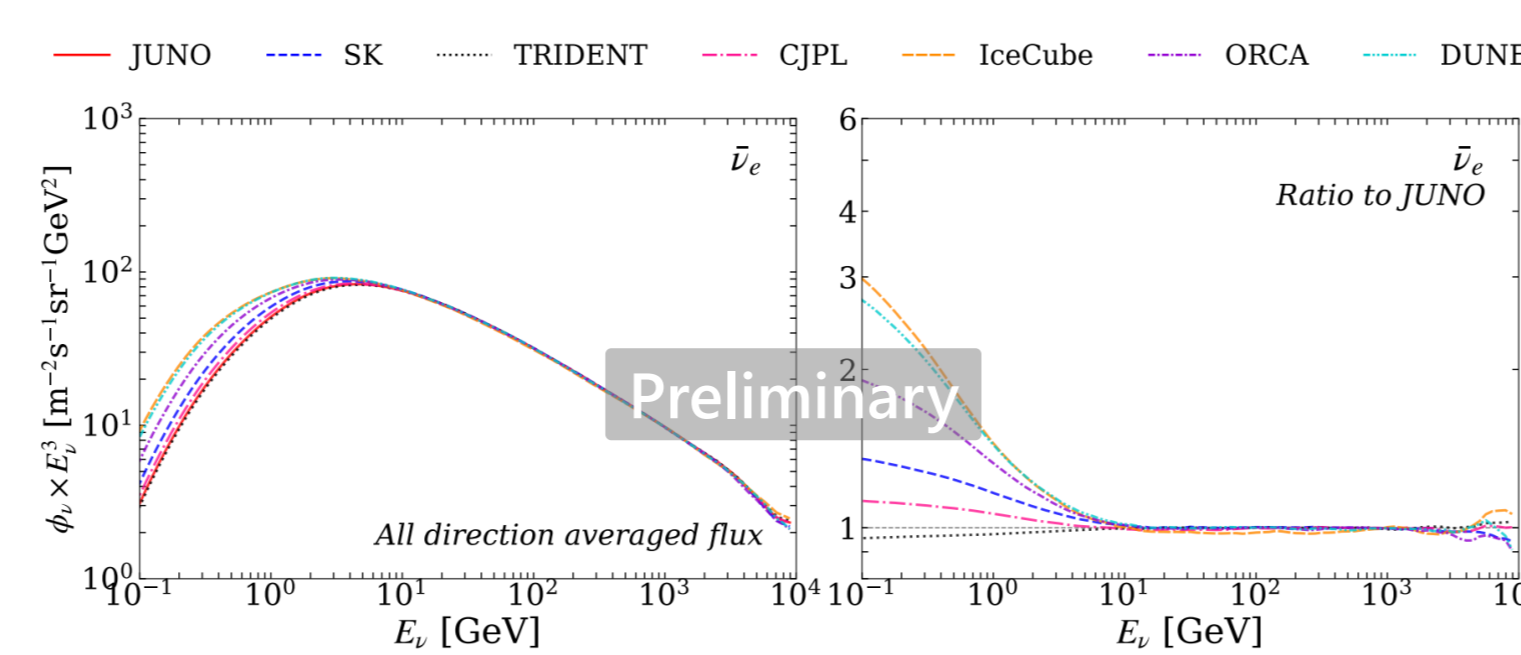
Atomic absorption probability and nuclear capture probability for μ^- considered

World map for muon hit point on the Earth



Flux with $E_\nu > 100$ MeV

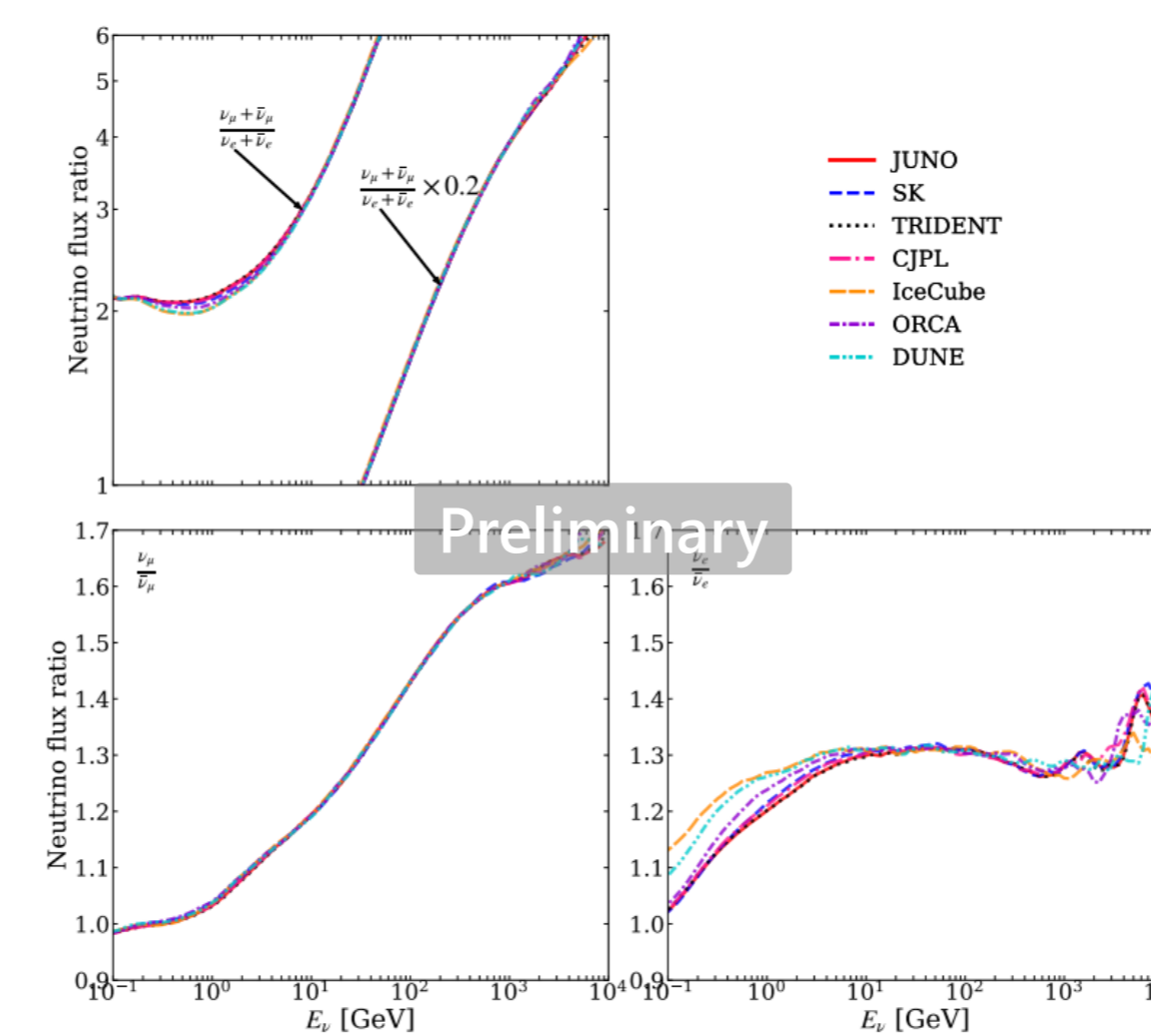
All-Direction Fluxes



($\bar{\nu}_e$ shown as example; patterns similar for other flavors)

- $E_\nu > 10$ GeV: all sites converge → location-independent
- $E_\nu < 1$ GeV: site-dependent deviations up to $3\times$
- IceCube & DUNE show $\sim 3\times$ higher flux vs JUNO at low E

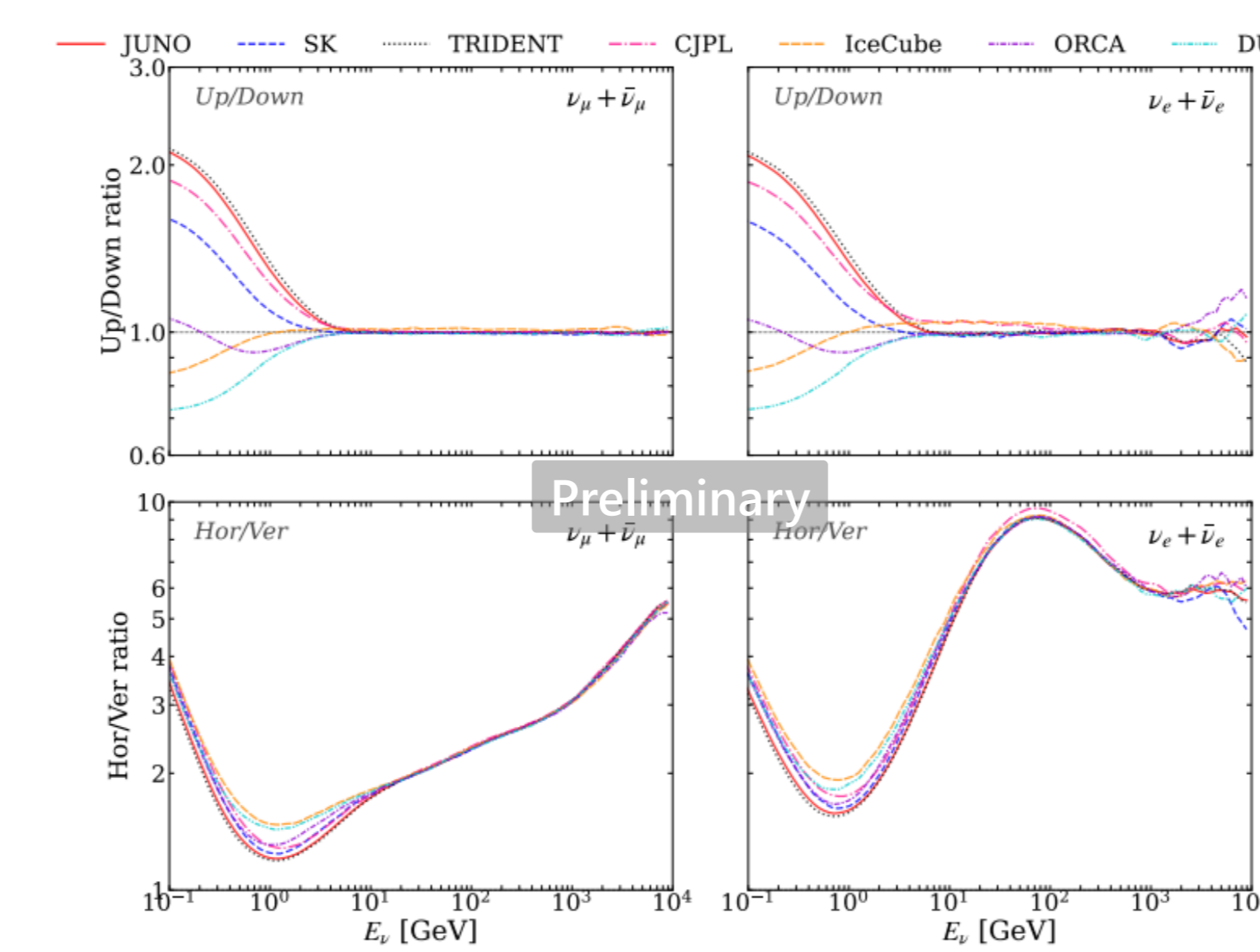
Neutrino flavor ratios



$\nu_e/\bar{\nu}_e$ reflects μ^+/μ^- production asymmetry

Zenith-Angle Dependence

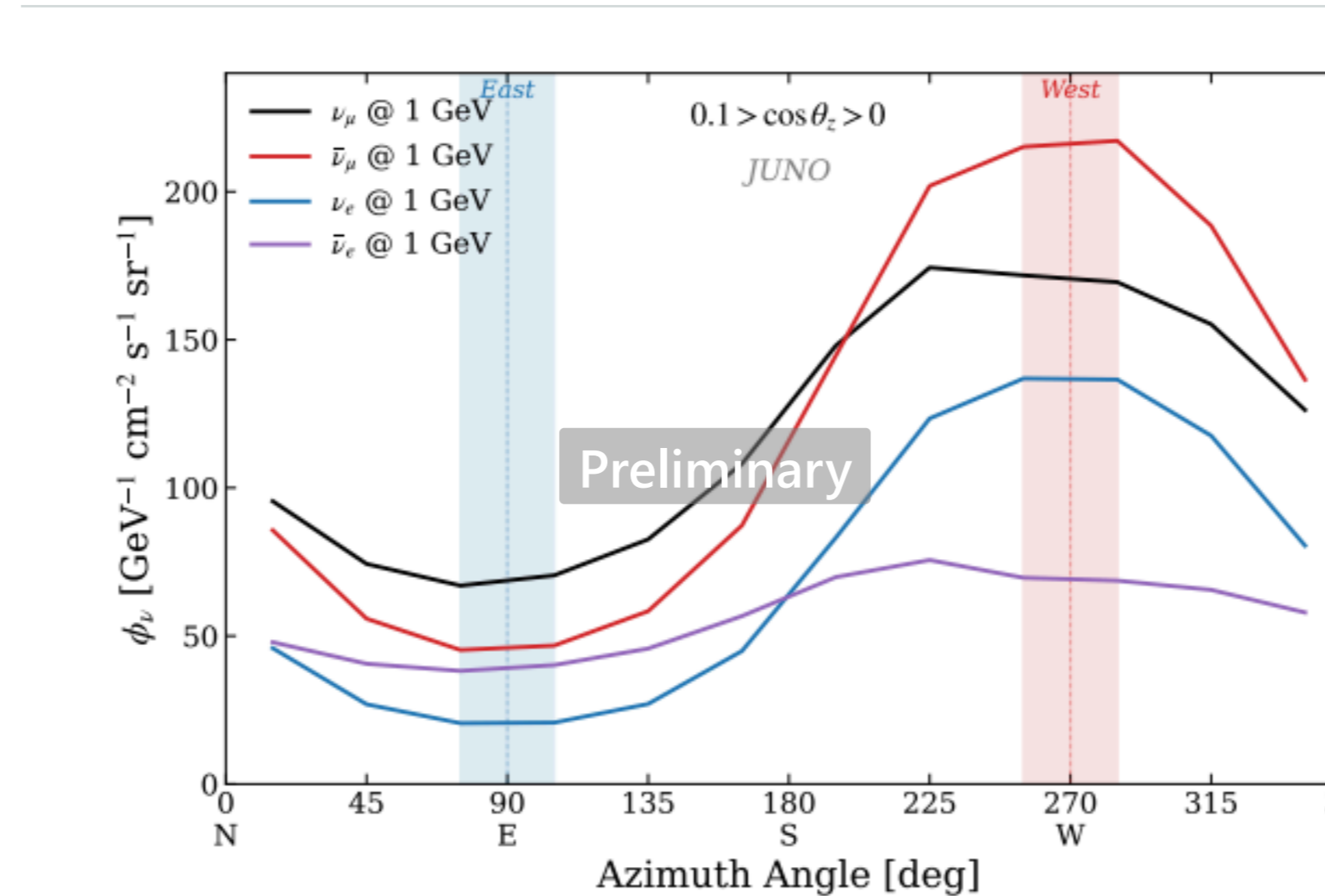
Hor: $0.1 > \cos\theta_z > 0$ | Ver (down): $1 > \cos\theta_z > 0.9$ | Average all azimuth angles



- **Downward**: compact production region above detector
- **Horizontal**: max enhancement at 1–100 GeV (μ decay length effect)
- **Upward**: broad antipodal production, dilution
- **Up/Down ratio** spans ~ 0.7 (DUNE) to ~ 2.2 (TRIDENT) at 0.1 GeV

At 5–100 GeV, downward fluxes at **IceCube** (cold → low air density) and **CJPL** (1580 m → smaller production area) are lower than at other sites.

East-West Effect



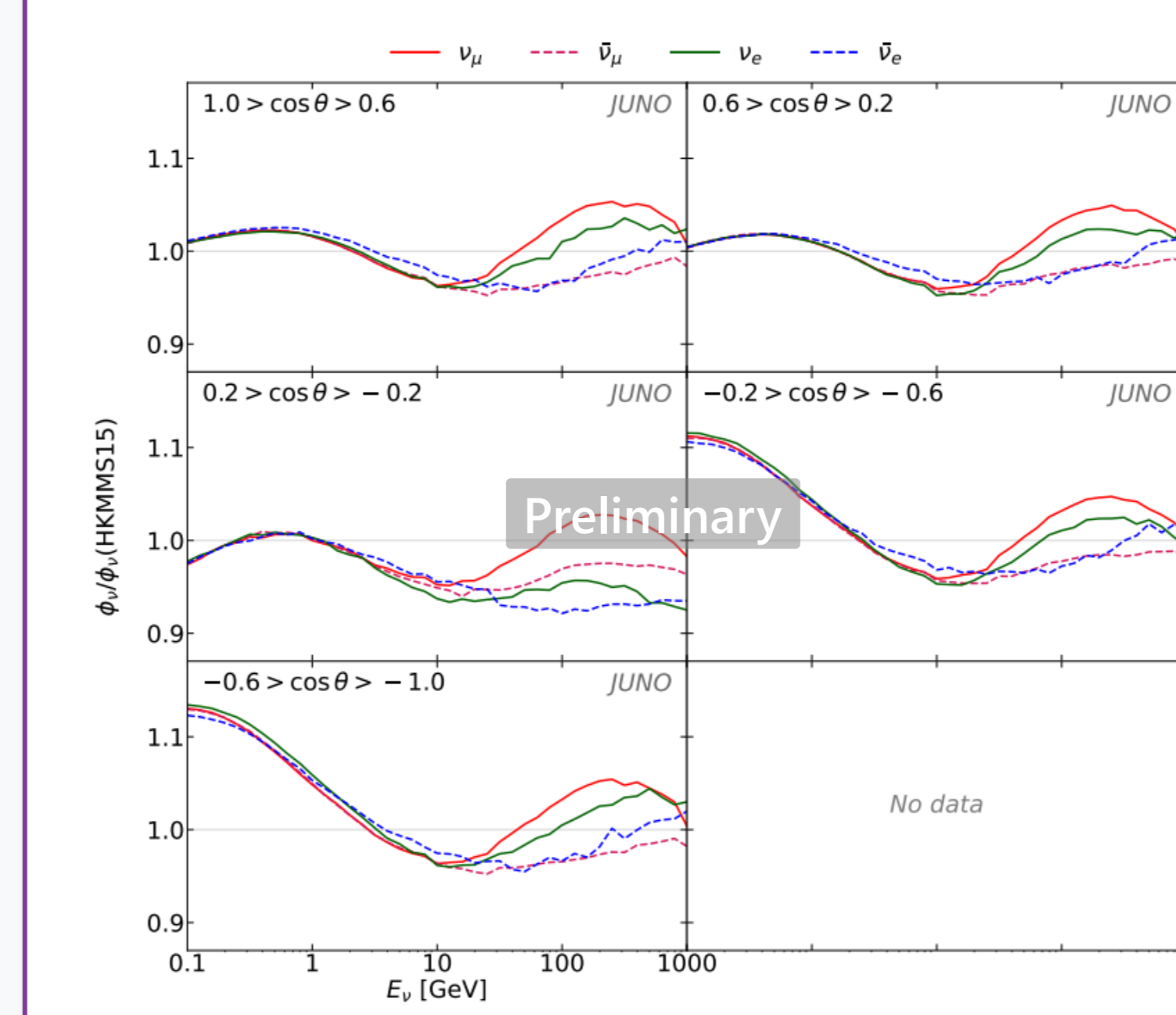
- **JUNO at 1 GeV (horizontal)**: flux peaks at **West** ($\sim 270^\circ$), minimum at **East** ($\sim 90^\circ$)
- Earth's magnetic field acts as a **rigidity filter**: CR from **East** need higher rigidity to penetrate
- **Proton-dominated CR spectrum** → **excess from West, deficit from East**

- **Flavor-dependent**: μ^+/μ^- geomagnetic bending introduces $\nu/\bar{\nu}$ asymmetry (ν_μ vs $\bar{\nu}_\mu$ differ slightly)

References

- [1] HKKMS11: Phys. Rev. D 83, 123001 (2011)
- [2] HKKMS15: Phys. Rev. D 92, 023004 (2015)
- [3] Honda et al. (μ constraint): Phys. Rev. D 100 (2019) no.12, 123022
- [4] HKKMS06: Phys. Rev. D 75 (2007), 043006

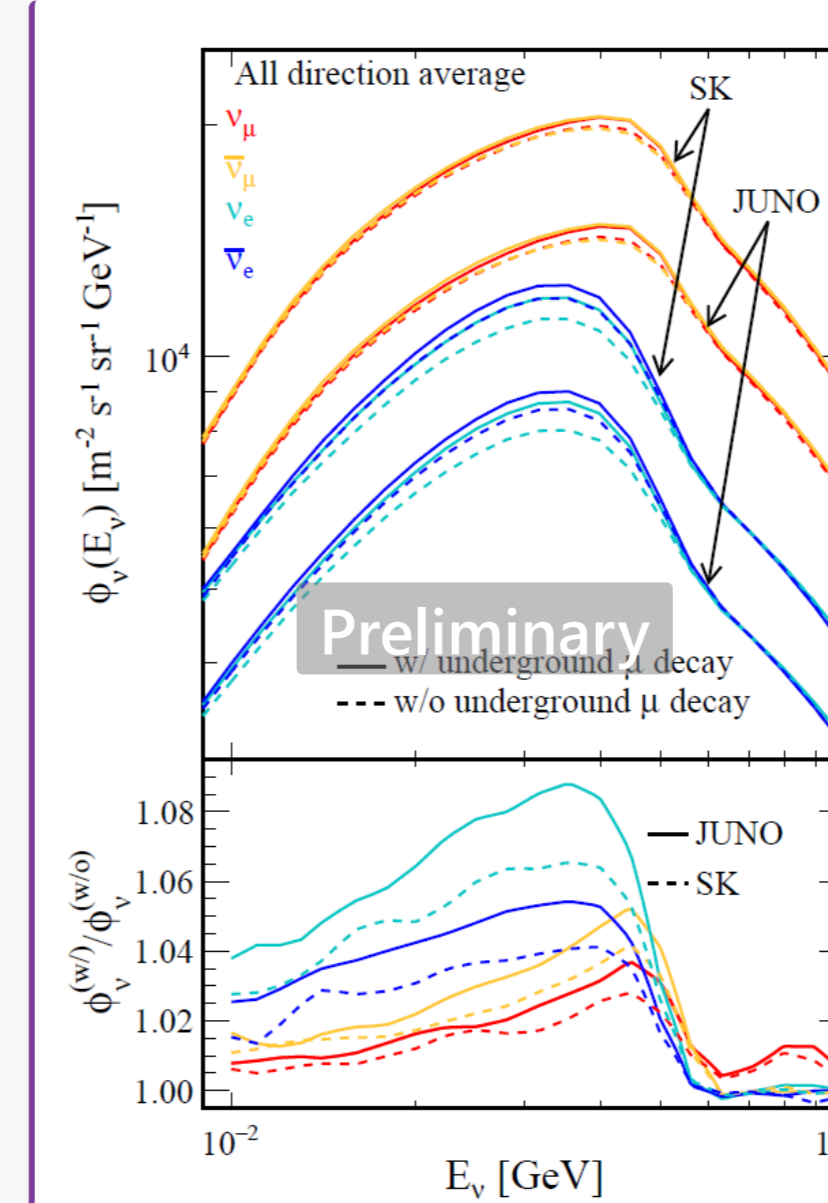
Comparison with HKKMS15



Illustrated with JUNO site results; comparison between this work and HKKMS15:

- $E_\nu < 10$ GeV: upward ν enhanced (2017 CR model → more low-E CR through opposite-side low-cutoff regions)
- $E_\nu > 10$ GeV: ratios ~ 1 , $\nu/\bar{\nu}$ split 1–3% (CR charge asymmetry + hadronic recalibration)
- All within **HKKMS uncertainties** ($\sim 10\%$ for $E_\nu > 1$ GeV, ~ 15 – 25% for < 1 GeV)

Flux with $E_\nu < 100$ MeV

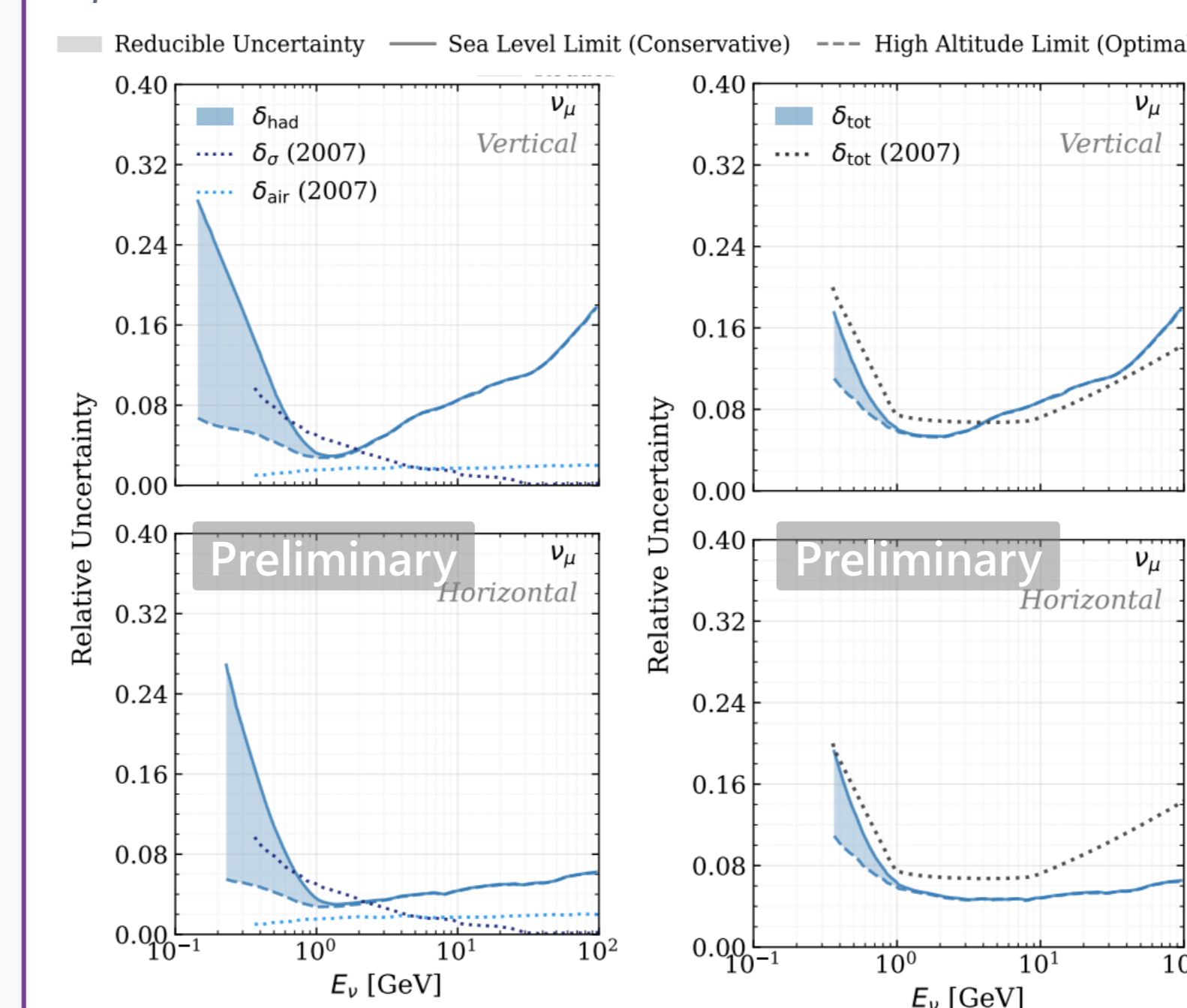


Results computed for all 7 sites; JUNO & SK shown as examples.

- μ propagation in Earth adds ν flux below ~ 100 MeV
- **JUNO vs SK**: absolute enhancement \sim site-independent; relative enhancement larger at JUNO (lower baseline flux from higher geomagnetic cutoff)
- **Flavor hierarchy of μ propagation enhancement**: $\nu_e \approx \bar{\nu}_\mu > \nu_\mu > \bar{\nu}_e$ (μ^+ decay dominates; μ^- captured by nuclei)
- Previously ignored by HKKMS, Bartol & FLUKA — **critical for DSNB & low-mass DM searches**

Flux Model Uncertainty Estimation

(ν_μ shown as example; results for all flavors computed)



- **Method**: hadronic uncertainty (δ_{had}) constrained by atmospheric μ data (Honda et al.^[3])
- Shaded bands: **reducible uncertainty range**
- **Upper solid**: conservative constraint from **sea-level μ observations** (Fig. 9 of Ref. [3])
- **Lower dashed**: optimal constraint from **high-altitude observations at Hanle**, 4500 m a.s.l. (Fig. 12 of Ref. [3])
- **Production cross-section (δ_σ)** and **atmospheric density (δ_{air})**, inherited from **HKKMS06^[4]**
- δ_{tot} : total relative uncertainty of atmospheric ν flux
- Shaded bands: updated total uncertainty combining μ -constrained δ_{had} with δ_σ and δ_{air}
- Band width: **conservative (sea-level)** vs **optimal (high-altitude)** scenarios
- Dotted black lines: historical $\delta_{tot}(2007)$ from **HKKMS06^[4]**