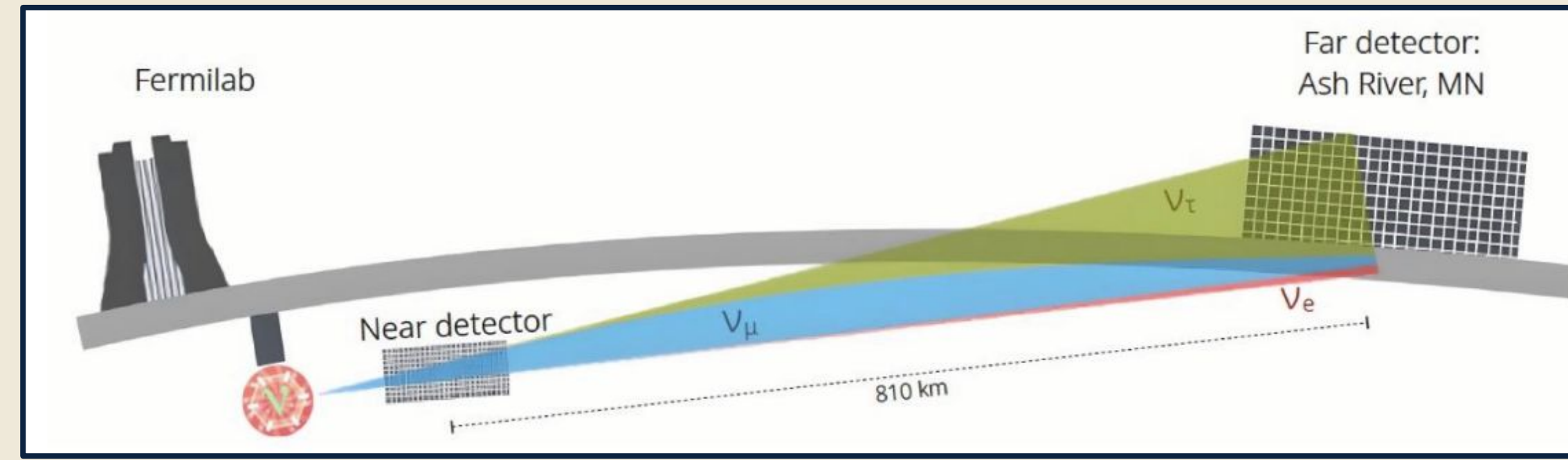
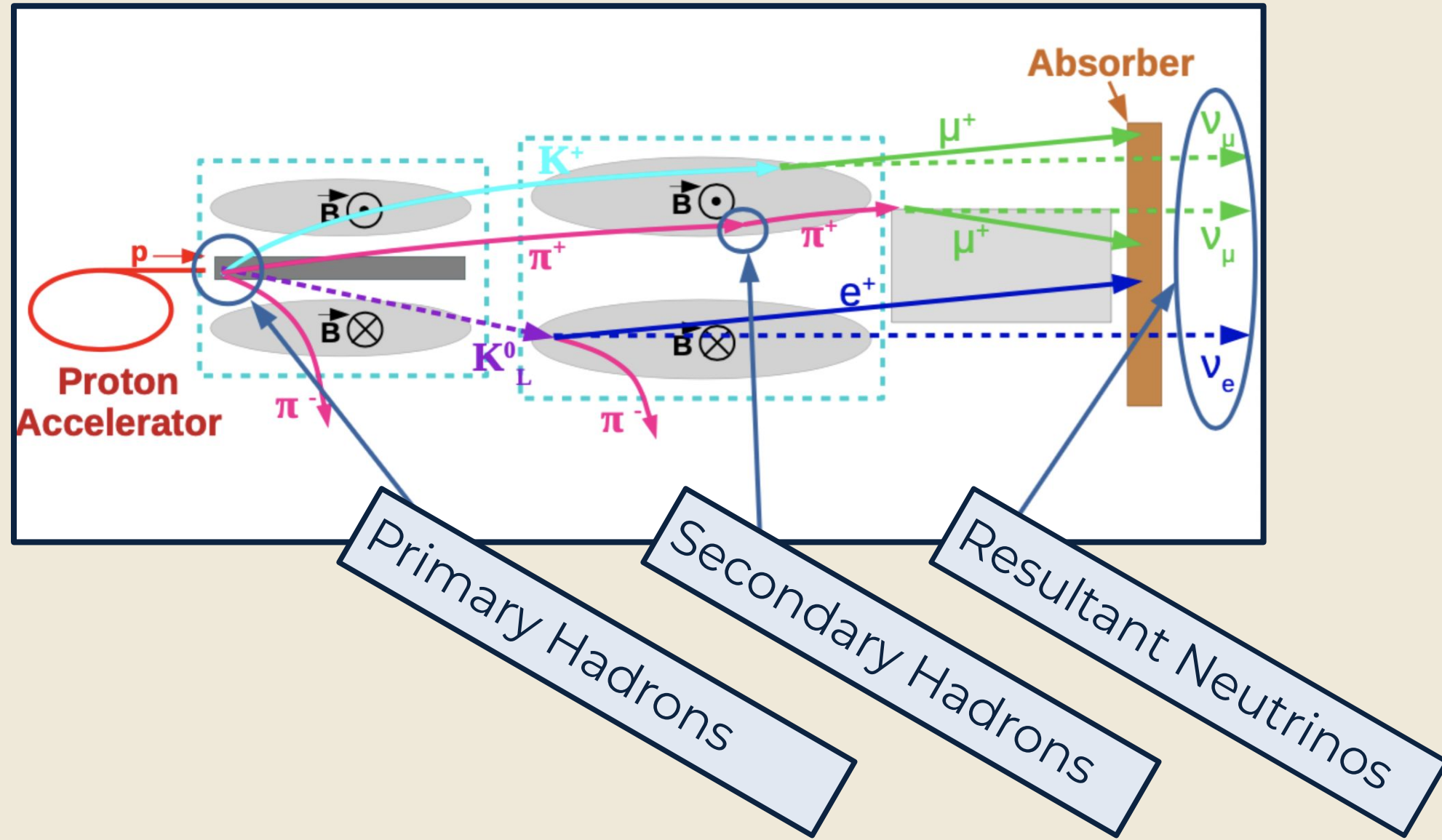


### Neutrino Flux

- The number of neutrinos passing through a given area in a given time.
- Flux uncertainty is a direct contributor to oscillation uncertainties in long-baseline neutrino experiments.
  - Experiments like DUNE, T2K, NOvA are vital for the future of the field!
- Neutrino beams are produced by decaying beams of hadrons.
- Hadron production uncertainty is **the largest** single source of uncertainty in neutrino flux.

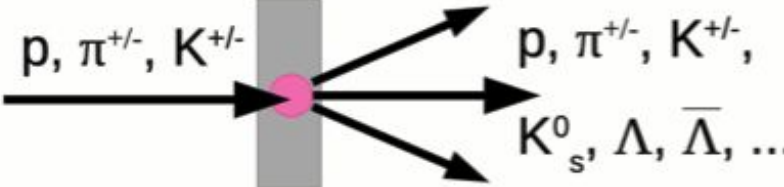


Above: Long-baseline experiments such as NOvA require precise estimations of neutrino flux [1].

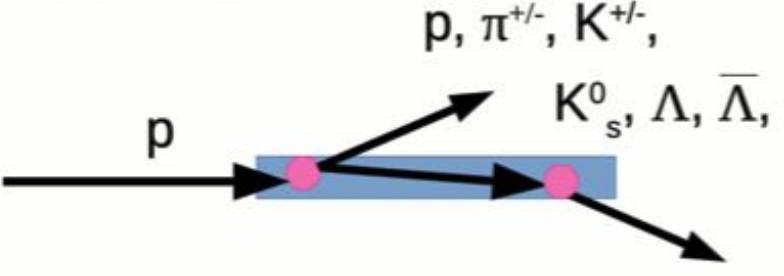
### Why Use a Long Target?

- A thin target is useful for constraining individual types of interaction.
- Long targets, or replica targets, allow a wider ensemble of interactions.
  - Hadrons produced in the target often interact in the target material before exiting.
- They also allow normalization directly to protons on target, whereas thin targets necessitate the study of production cross section in addition to particle yields.
- Other neutrino experiments send us replicas of their targets to study.
  - Data has been taken with replica/prototype targets for T2K, NuMI, and LBNF/DUNE [1].
- These other experiments can use our data to reduce their flux uncertainties!
  - Experiments such as NOvA, MicroBooNE, ICARUS, and MINERvA stand to benefit.
- This methodology has been proven with a T2K replica target [2].

#### Thin-Target Measurements

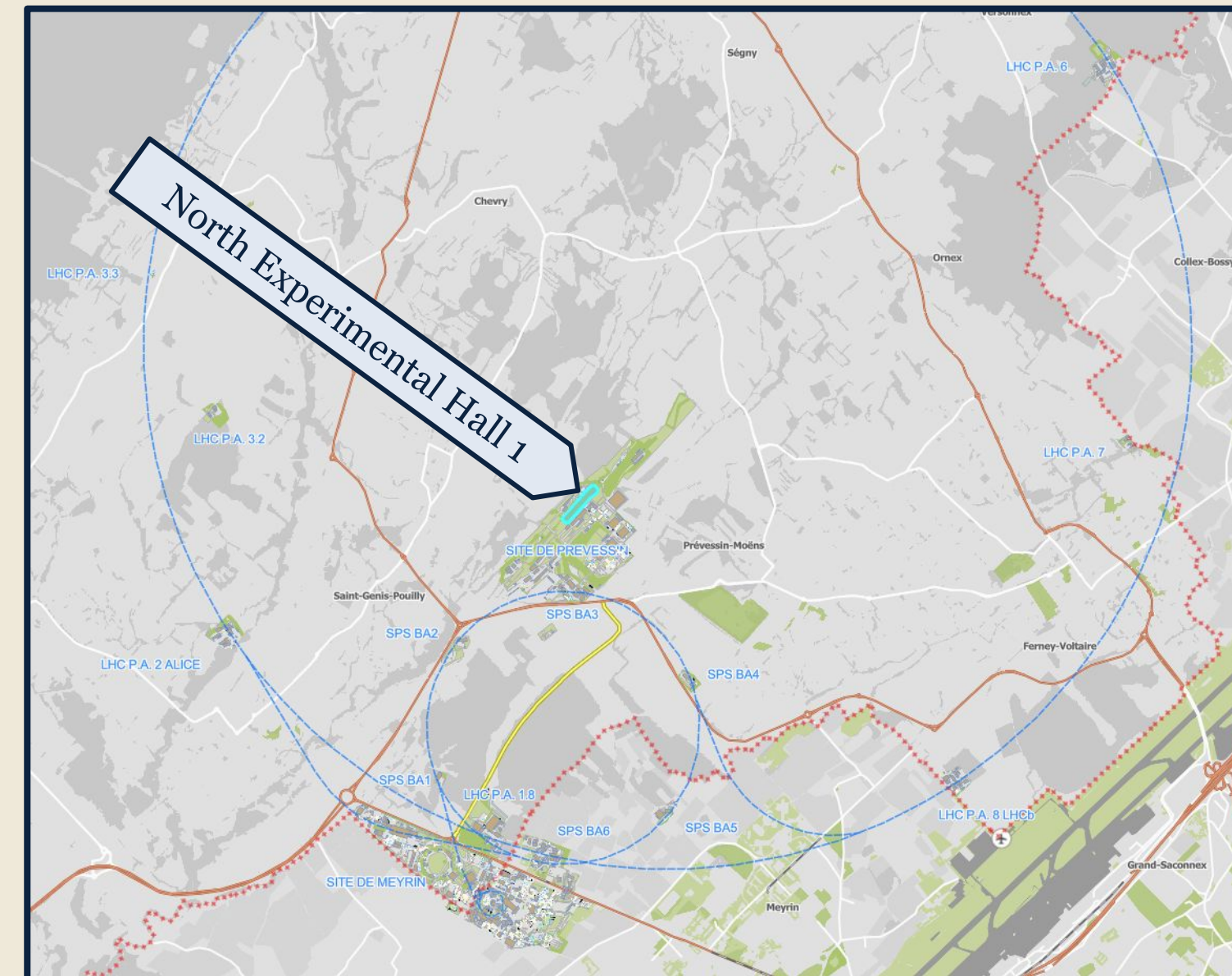


#### Replica-Target Measurements

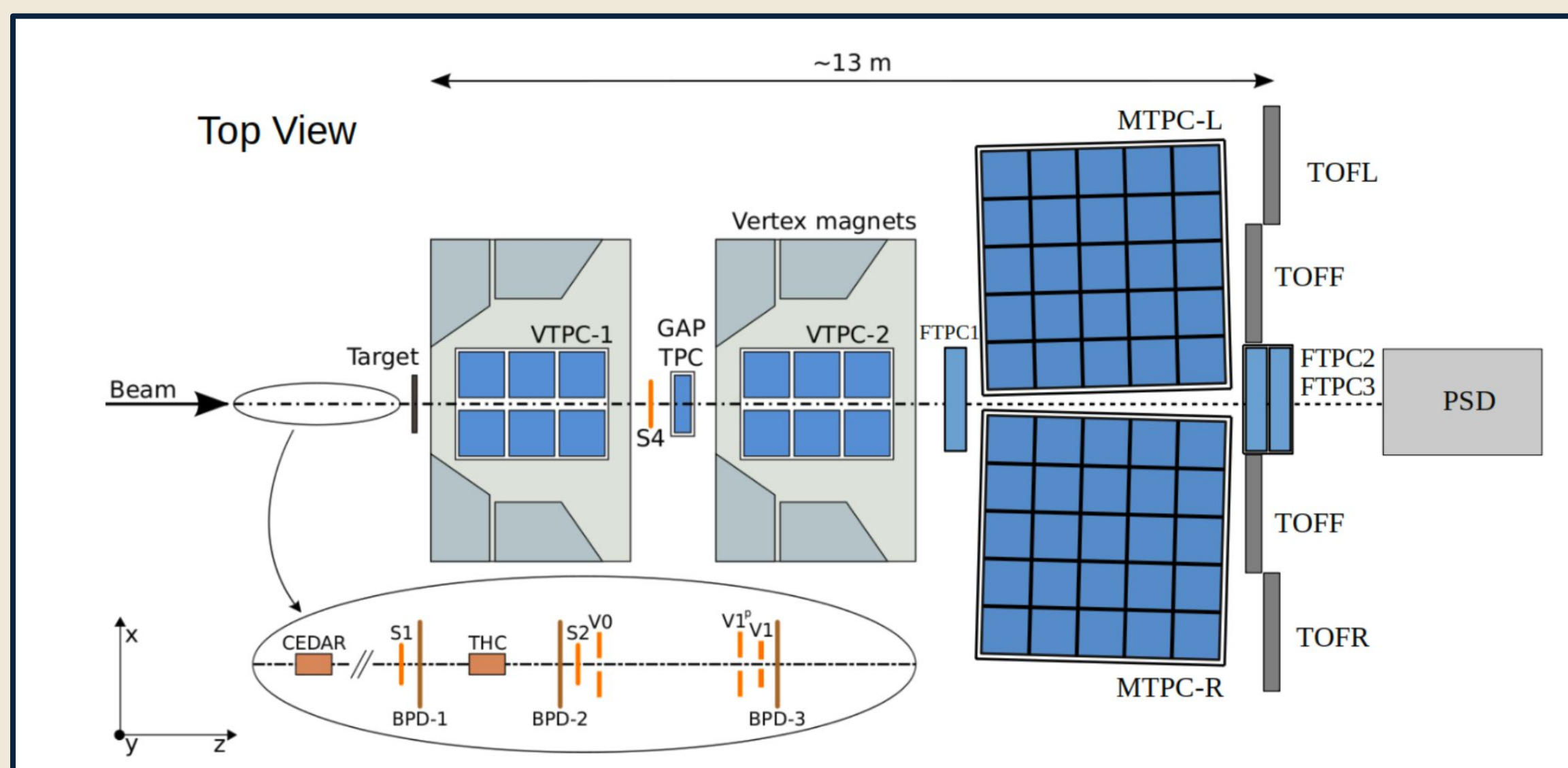


### The NA61/SHINE Experiment

- NA61/SHINE is the 61st experiment in CERN's North Area [3].
- The experiment receives beams from the Super Proton Synchrotron (SPS) [3].
- SHINE stands for SPS Heavy Ion and Neutrino Experiment [1].
- NA61/SHINE has a very broad physics program.
- The experiment's neutrino program studies hadron production relevant for neutrino beam production [1].
- The goal of this study: **Reduce hadron production uncertainties.**



Above: North Experimental Hall 1 receives beams from the Super Proton Synchrotron.

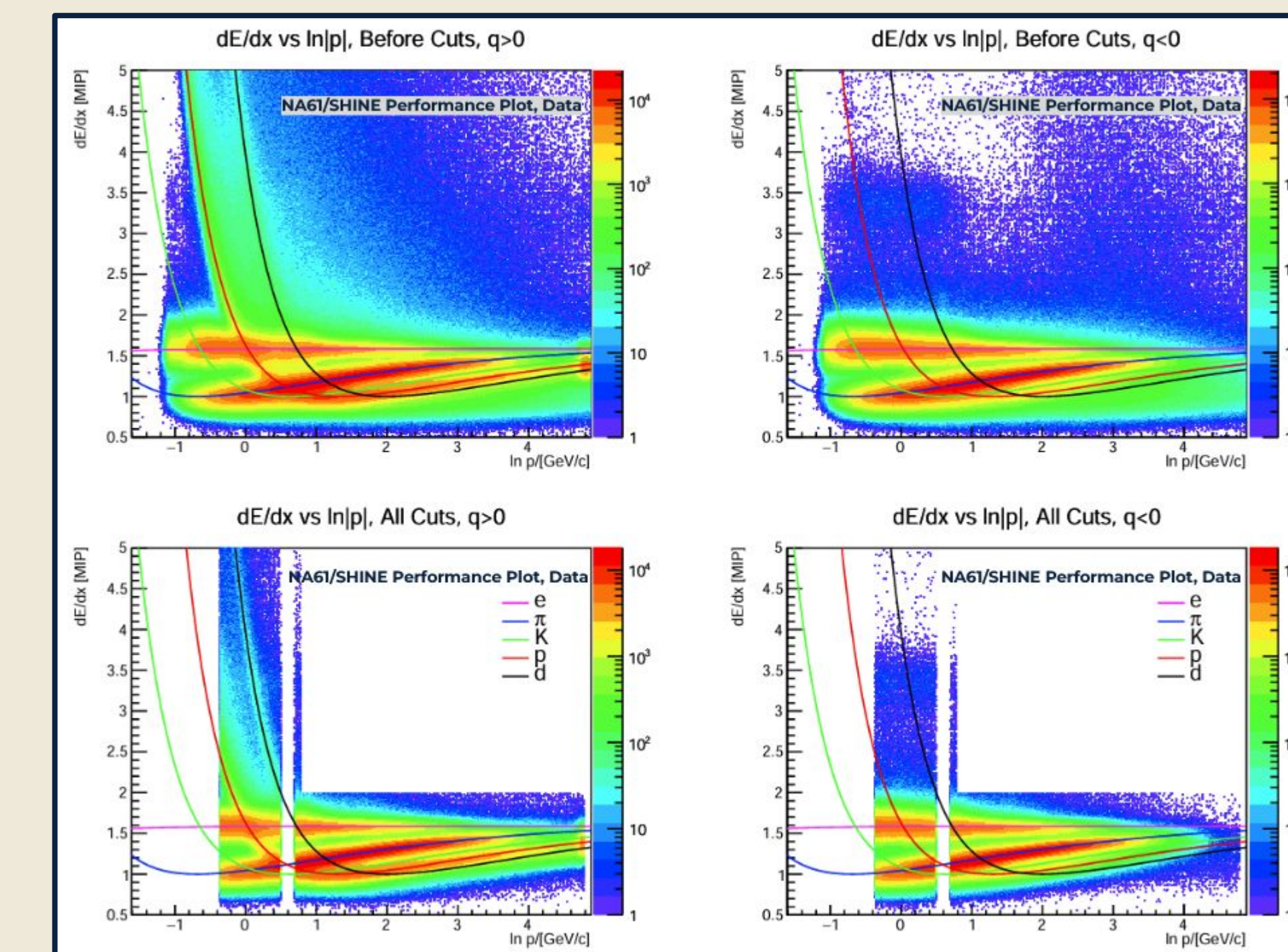


Left: The NA61/SHINE experimental setup as it was during 2018 NuMI data taking.

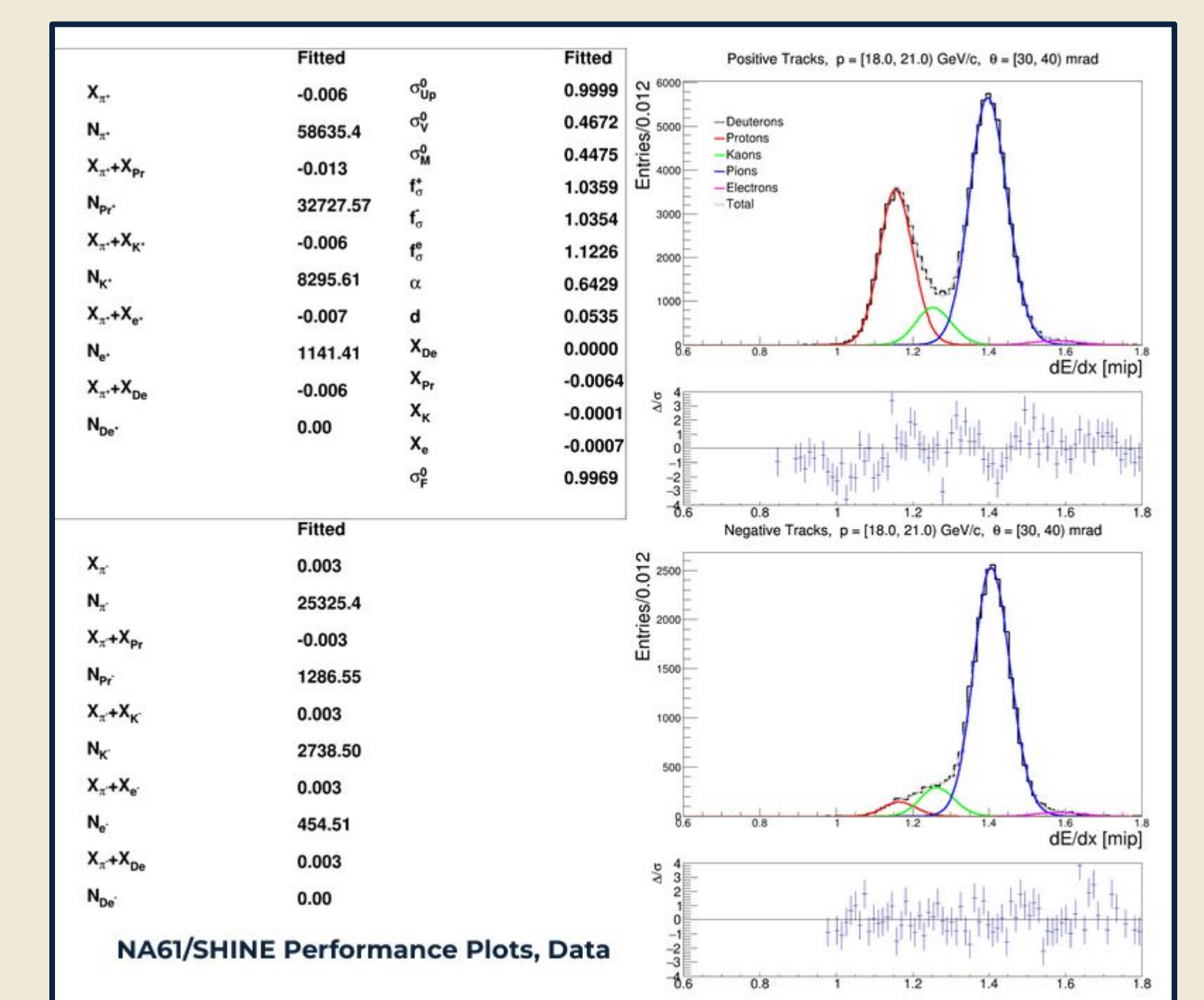
$$\frac{d^2n_i}{dp d\theta} = \frac{c_i^{\text{total}}}{\Delta p \Delta \theta N_{\text{POT}}} y_i$$

Above: Double-differential multiplicity.  $c_i^{\text{total}}$  is the product of correction factors,  $y_i$  is the yield of a particle species in bin  $i$ ,  $N_{\text{POT}}$  is the number of protons on target.  $\Delta p$  and  $\Delta \theta$  are the sizes of the  $p$  and  $\theta$  bins [1].

Below: Plots of energy loss ( $dE/dx$ ) vs momentum ( $\ln|p|$ ) for positive and negative charge, before and after all cuts. Bethe-Block lines for common particles are overlaid. NA61/SHINE Performance.



Below: Example  $dE/dx$  fits for one bin of data, positively- and negatively-charged tracks. Fit parameters, fit peaks, and ratio plots are shown. NA61/SHINE Performance.

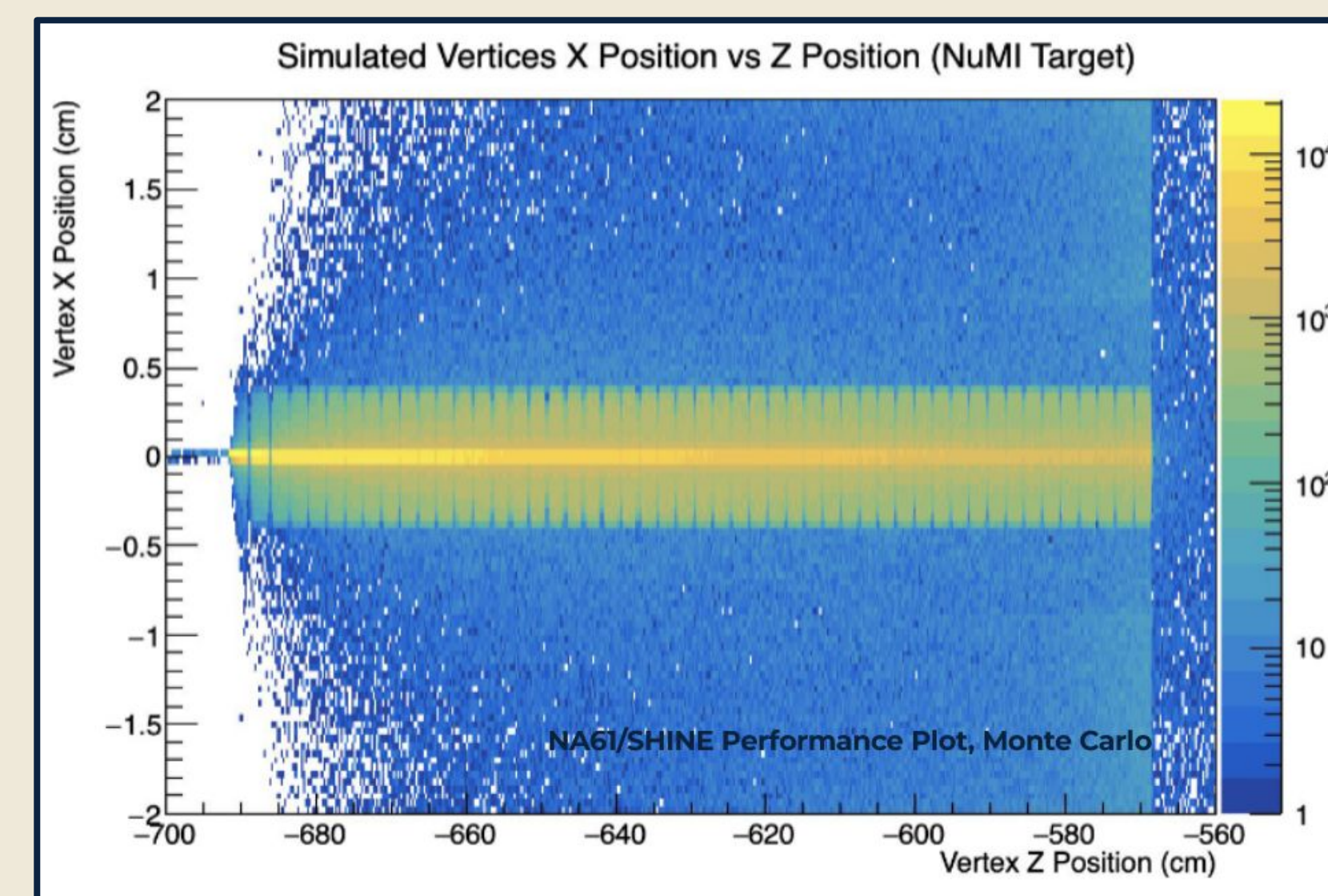
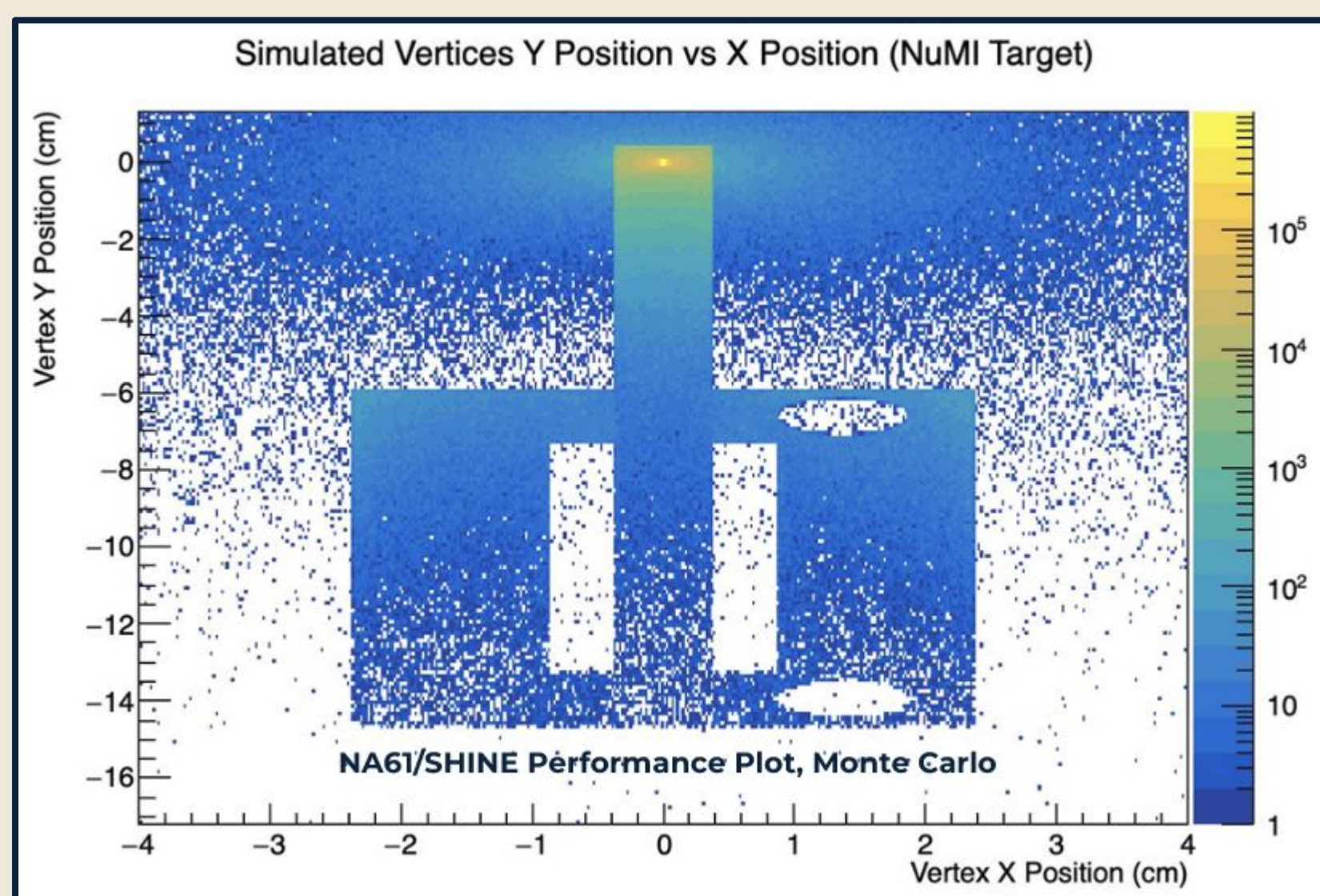


### NuMI Replica Target Data Taking

- Data was taken on a NuMI replica target during the summer and fall of 2018 [1].
  - NuMI: Neutrinos at the Main Injector; a neutrino beamline at Fermilab.
- This target is a 123 cm graphite rectangle, with fins cut out along its length [1].
- The experiment received a beam of protons at 120 GeV/c [1].



Above: The NuMI Replica Target on a table. Arrow added to show beam direction.

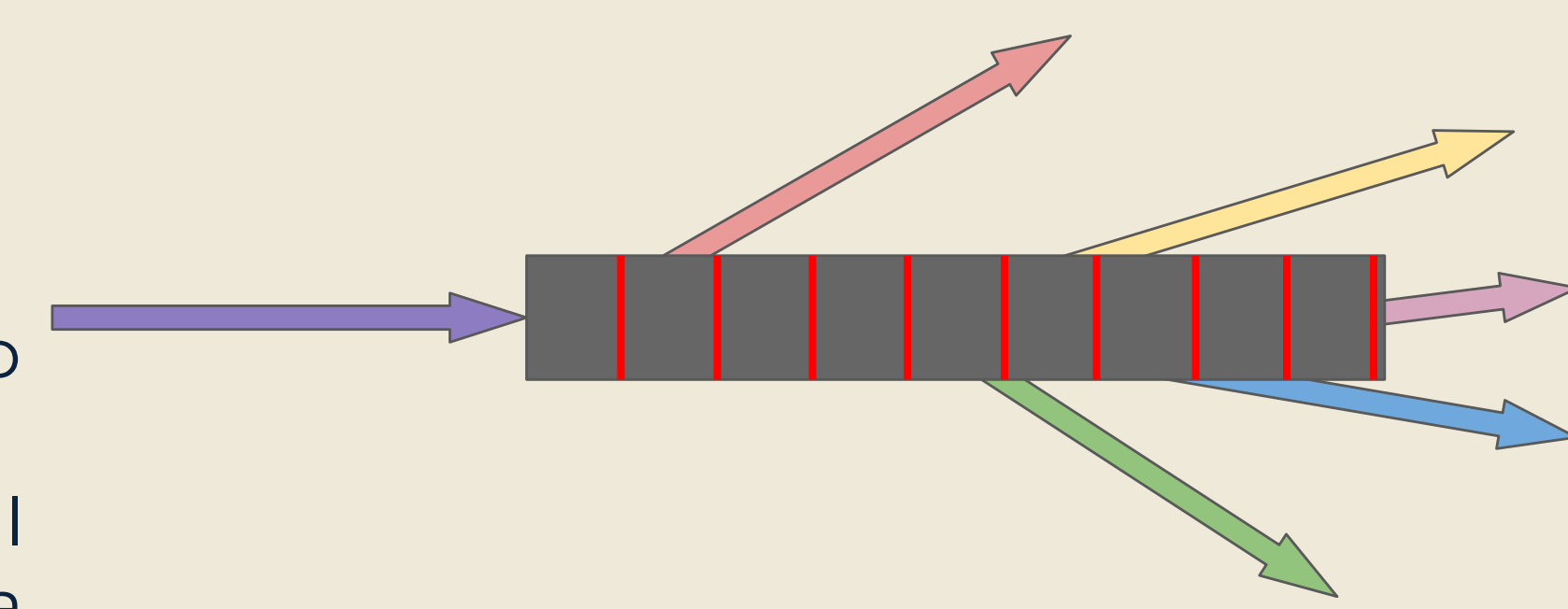


Left: Simulated exit positions of tracks, ZX plane. The graphite fins of the target are visible, viewed from above. NA61/SHINE Performance.

Leftmost: Simulated exit positions of tracks, XY plane. The target profile is visible, including various supporting structures. NA61/SHINE Performance.

### Next Steps

- The analysis software was built to handle thin-target data.
- Thin targets can be modeled as a plane.
- For replica targets, the geometry becomes relevant.
- Adaptation of the code is required to account for this.
- Current work focuses on dividing the target into longitudinal "z-bins" along the beam axis.
- Once this adaptation has been completed for the NuMI replica target, it can be applied for a future analysis with a DUNE prototype target (data taken in 2024/2025).



Above: Cartoon illustration of z-bin divisions.

[1] D. Battaglia, Constraining Hadron Production Uncertainty with NA61 Proton-NuMI Replica Target Data, Ph.D. thesis, University of Notre Dame (2026). Forthcoming.

[2] N. Abgrall et al. Measurements of  $\pi^{\pm}$ ,  $K^{\pm}$  and proton double differential yields from the surface of the T2K replica target for incoming 31 GeV/c protons with the NA61/SHINE spectrometer at the CERN SPS, *Eur. Phys. J. C* **79**, 100 (2019), doi:10.1140/epjc/s10052-019-6583-0.

[3] N. Abgrall et al. NA61/SHINE facility at the CERN SPS: beams and detector system, *JINST* **9**, P06005 (2014), doi:10.1088/1748-0221/9/06/P06005.