



Studying N^* and Δ contribution to exclusive pion production in Proton-Proton Collisions using HADES data

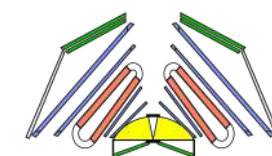
NSTAR 2026

Saket Kumar Sahu^{1,2} for the HADES Collaboration and Deborah Rönchen³

¹Ruhr University Bochum

²GSI Helmholtzzentrum für Schwerionenforschung GmbH

³Forschungszentrum Jülich



HADES

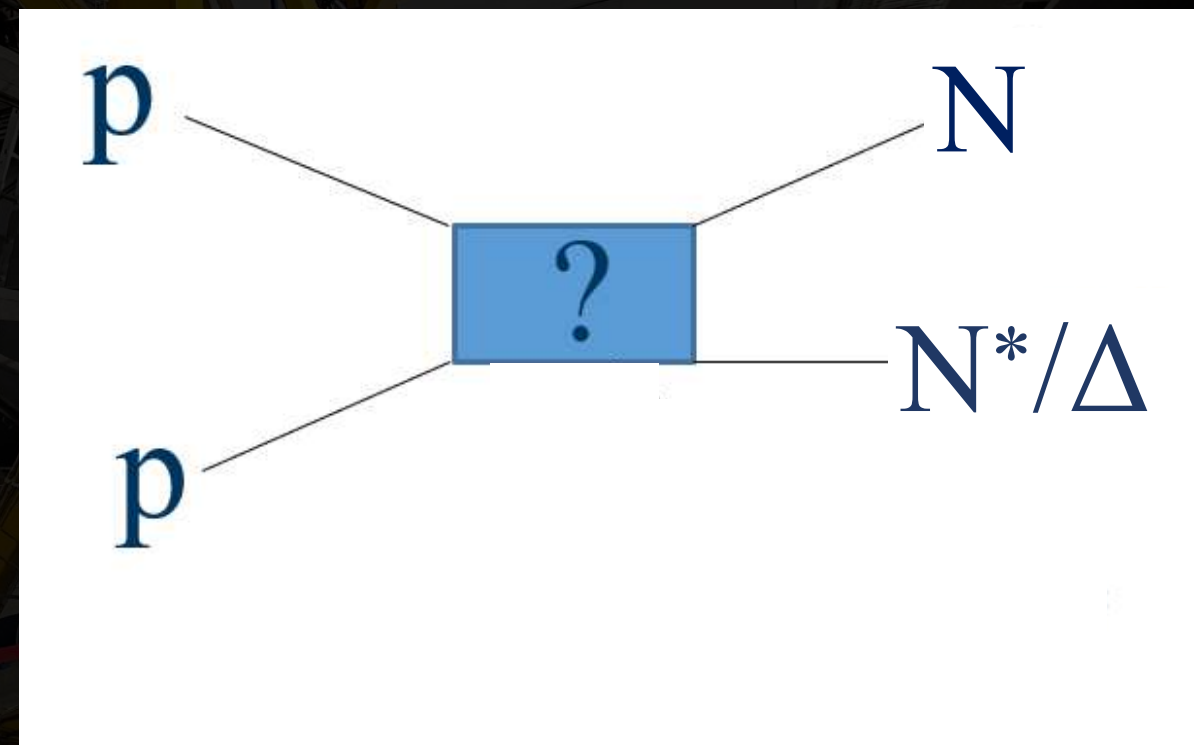
Why N^* and Δ ?

- “They are the simplest system in which the quintessential **non-Abelian character** of QCD is manifest”^[1].

1.N. Isgur, in: V. Burkert, L. Elouadrhiri, J. Kelly, R.M. (eds.) (Eds.), NSTAR2000: Excited Nucleons and Hadronic Structure, Newport News, USA, 2000, pp. 422–445, arXiv:nucl-th/0007008.
2.Volker Burkert, Gernot Eichmann, Eberhard Klempt, Progress in Particle and Nuclear Physics, Volume 146, Part 2, 2026, <https://doi.org/10.1016/j.pnpnp.2025.104214>.

Why N^* and Δ ?

- “They are the simplest system in which the quintessential **non-Abelian character** of QCD is manifest”^[1].
- Understanding the **production mechanisms and dynamical behavior** of these resonances is a key objective of this study.
- What is the relationship between **dynamically generated resonances** and **quark-model states**^[2]?

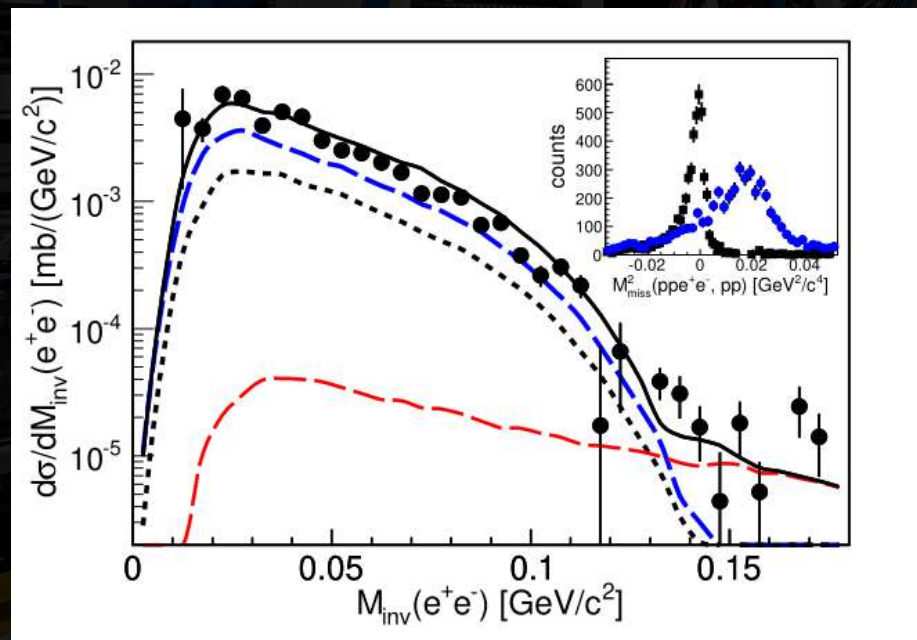


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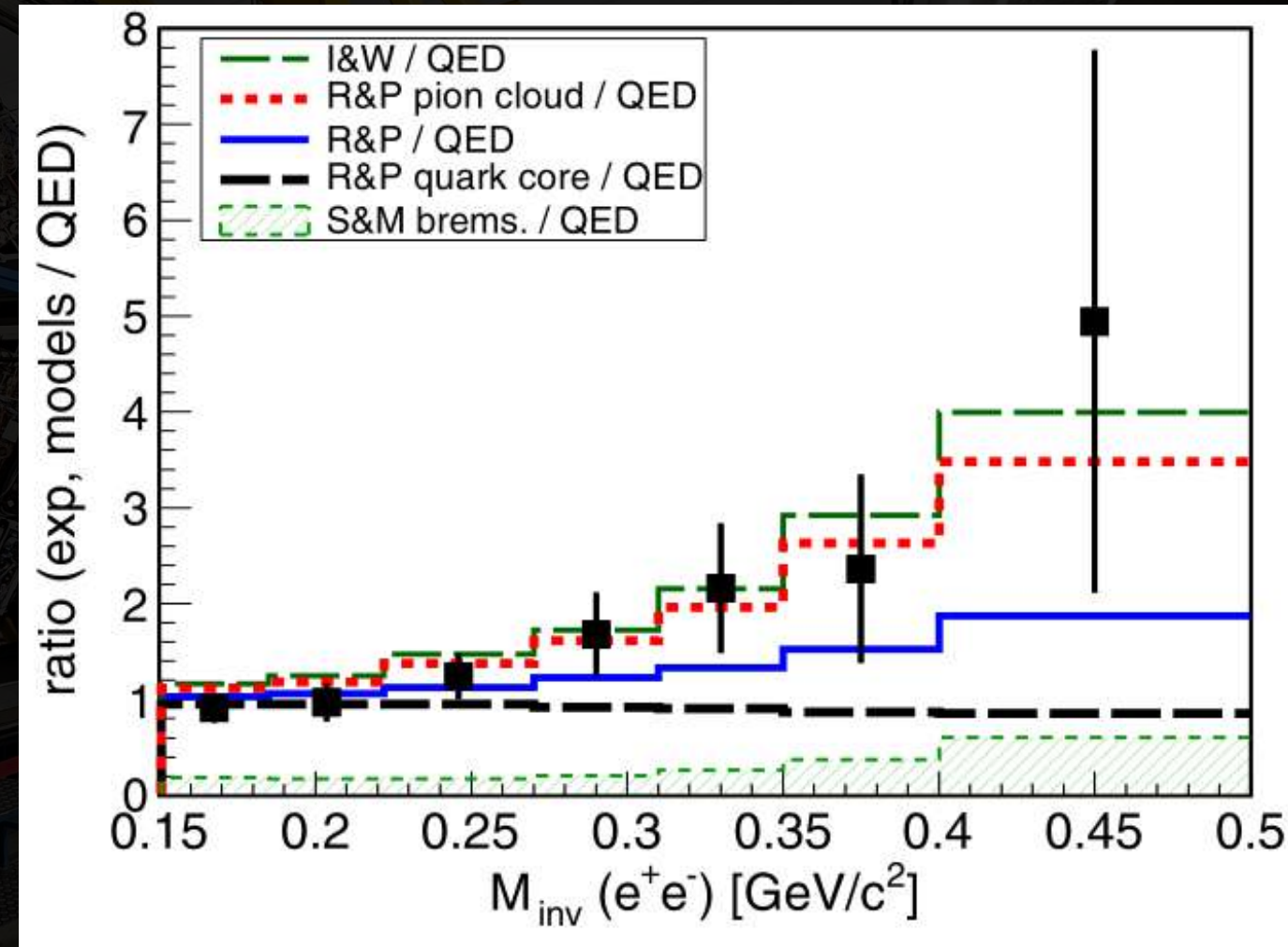
Towards Studying the Electromagnetic Properties of Light Baryons

- **Production mechanisms and reaction dynamics** of N^* and Δ states in $pp \rightarrow NN\pi$ provide access to their **electromagnetic structure** through **dilepton decays**.



contribution of Δ and $N(1440)$ [3]

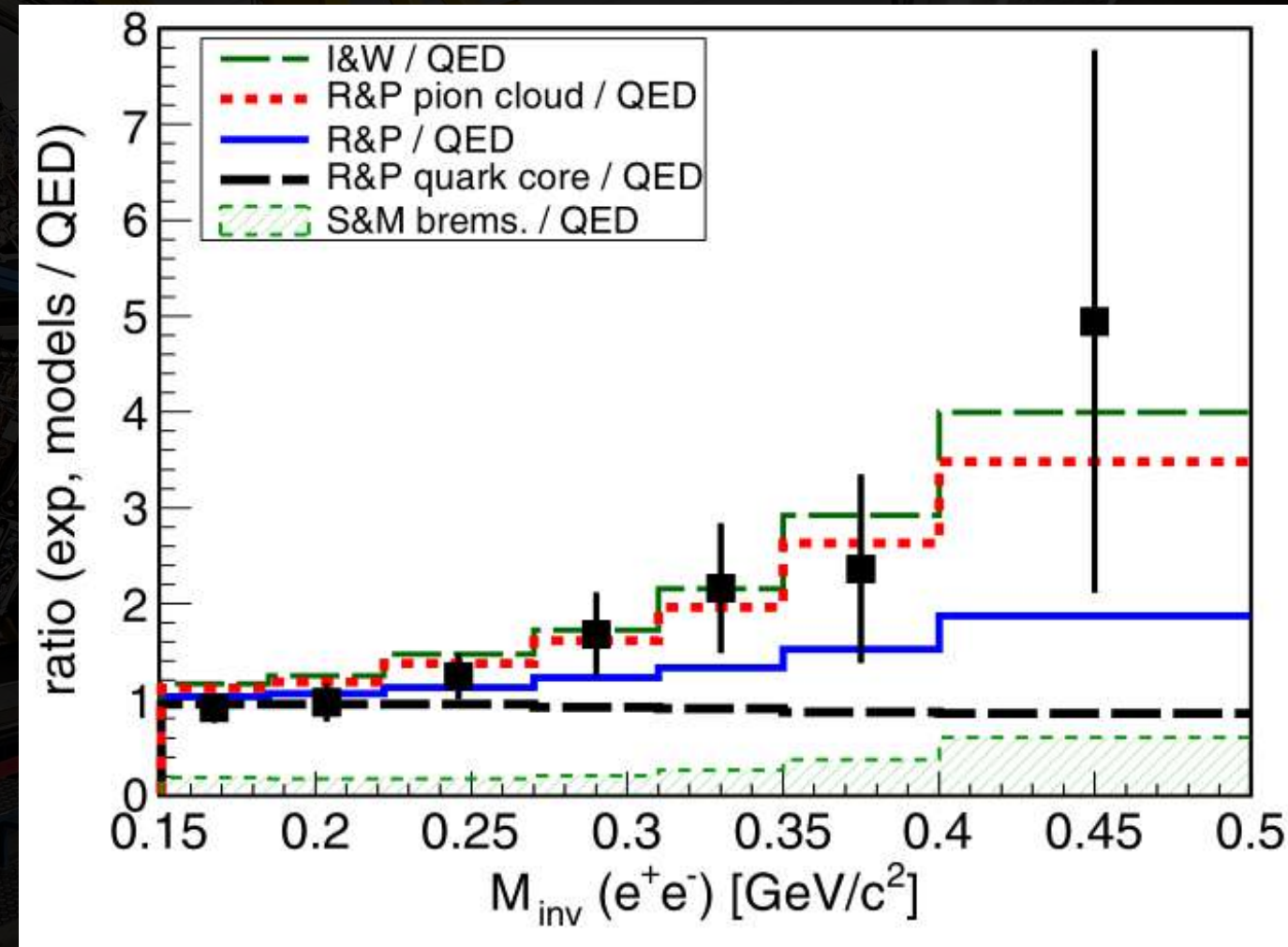
3. Adamczewski-Musch, J. et al. $\Delta(1232)$ Dalitz decay in proton-proton collisions at $T=1.25$ GeV measured with HADES at GSI. *Phys. Rev. C* 95, 065205 (2017).



effective transition form factor for $\Delta \rightarrow pe^+e^-$ [3]

Towards Studying the Electromagnetic Properties of Light Baryons

- **Production mechanisms and reaction dynamics** of N^* and Δ states in $pp \rightarrow NN\pi$ provide access to their **electromagnetic structure** through **dilepton decays**.
- Extract differential cross-sections and also the coupling strengths N^* and Δ resonances.
- How do these measurements improve the baseline for transport models and heavy-ion collisions?



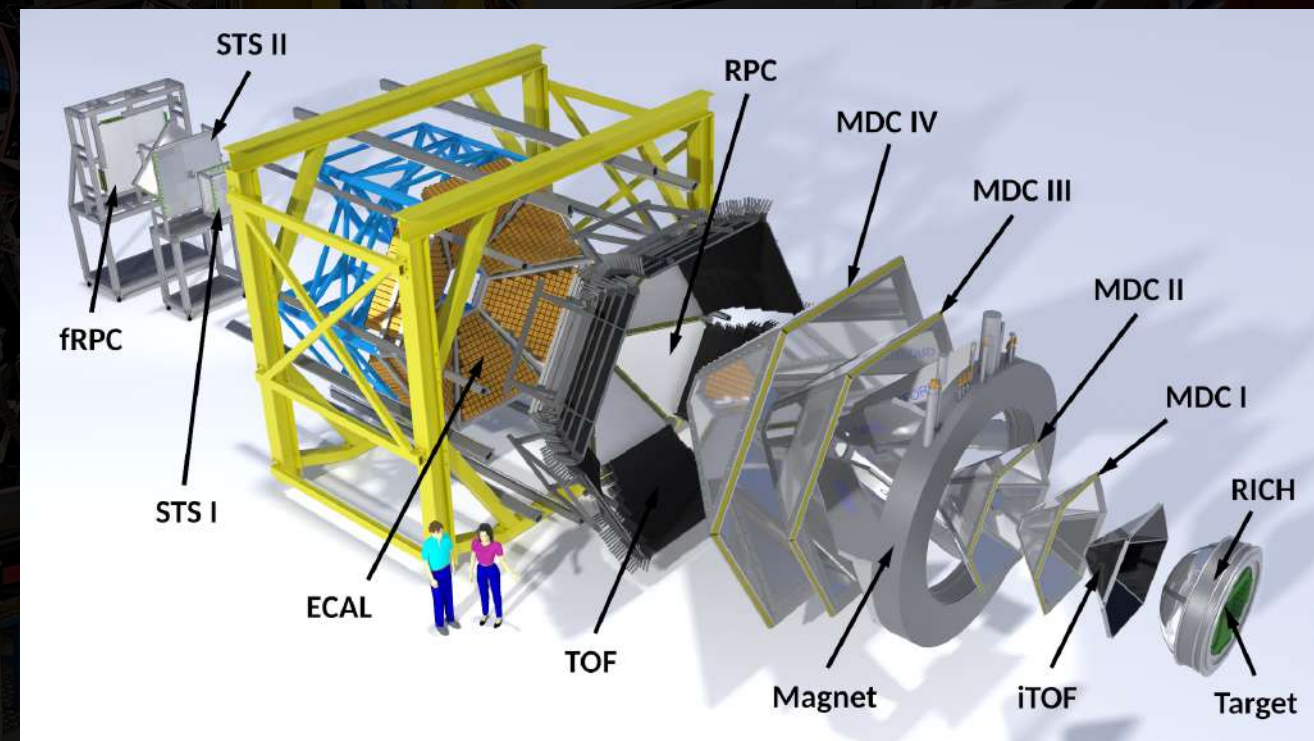
effective transition form factor for $\Delta \rightarrow pe^+e^-$ [3]



work in progress

HADES - High Acceptance DiElectron Spectrometer

- Fixed-target experiment located at GSI Darmstadt
- 6-coil superconducting toroidal magnet providing large acceptance and precise momentum reconstruction.
- Excellent tracking and particle identification (PID) capabilities
- Modular detector design at forward angles
- Additional photon detection capabilities
- Designed for various SIS18 beam ($\pi, p, A, \dots$)

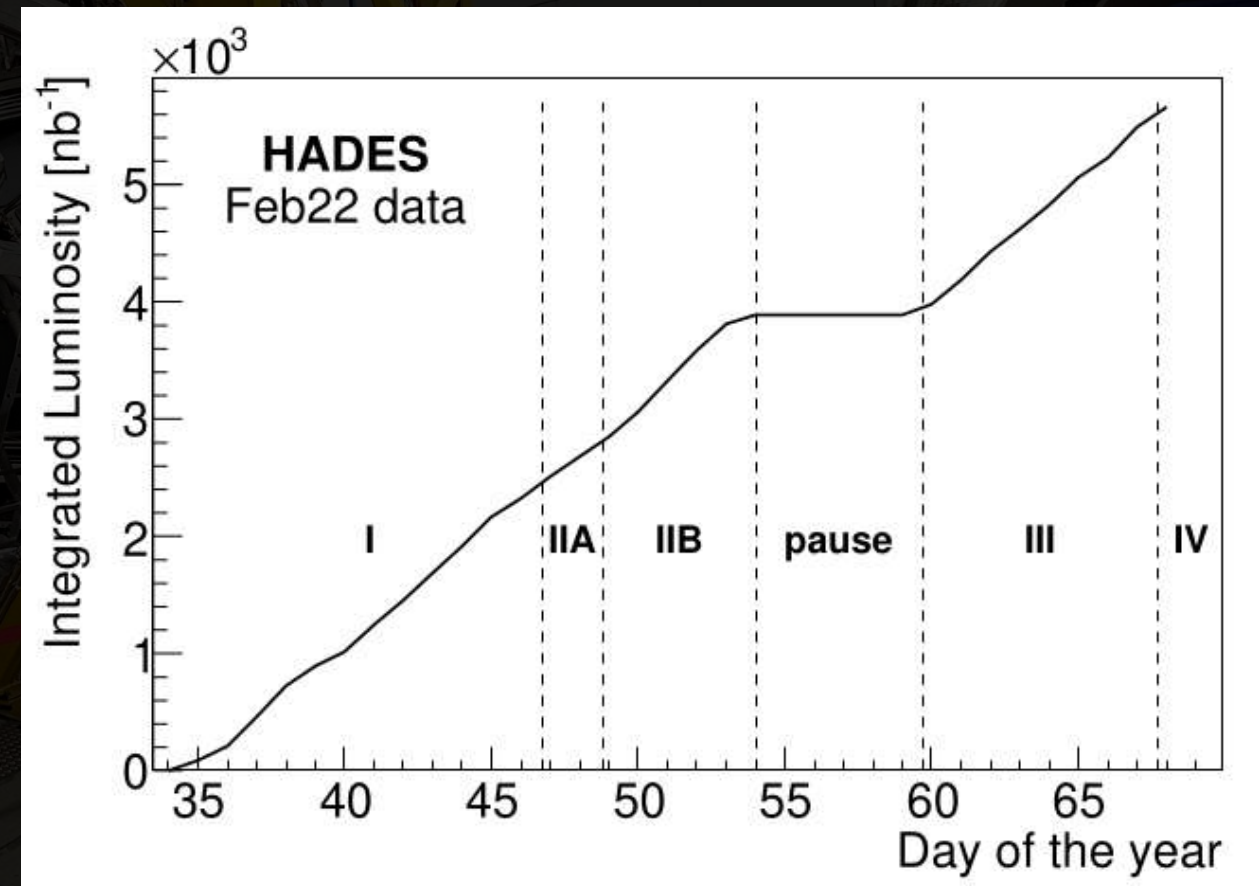


HADES - High Acceptance DiElectron Spectrometer

- Completed pp run in Feb 22.

$$\mathcal{L} = 5660.6 \pm 0.1 \text{ (stat)} \pm 226.0 \text{ (norm)} \pm 180.0 \text{ (sys)} \text{ nb}^{-1}$$

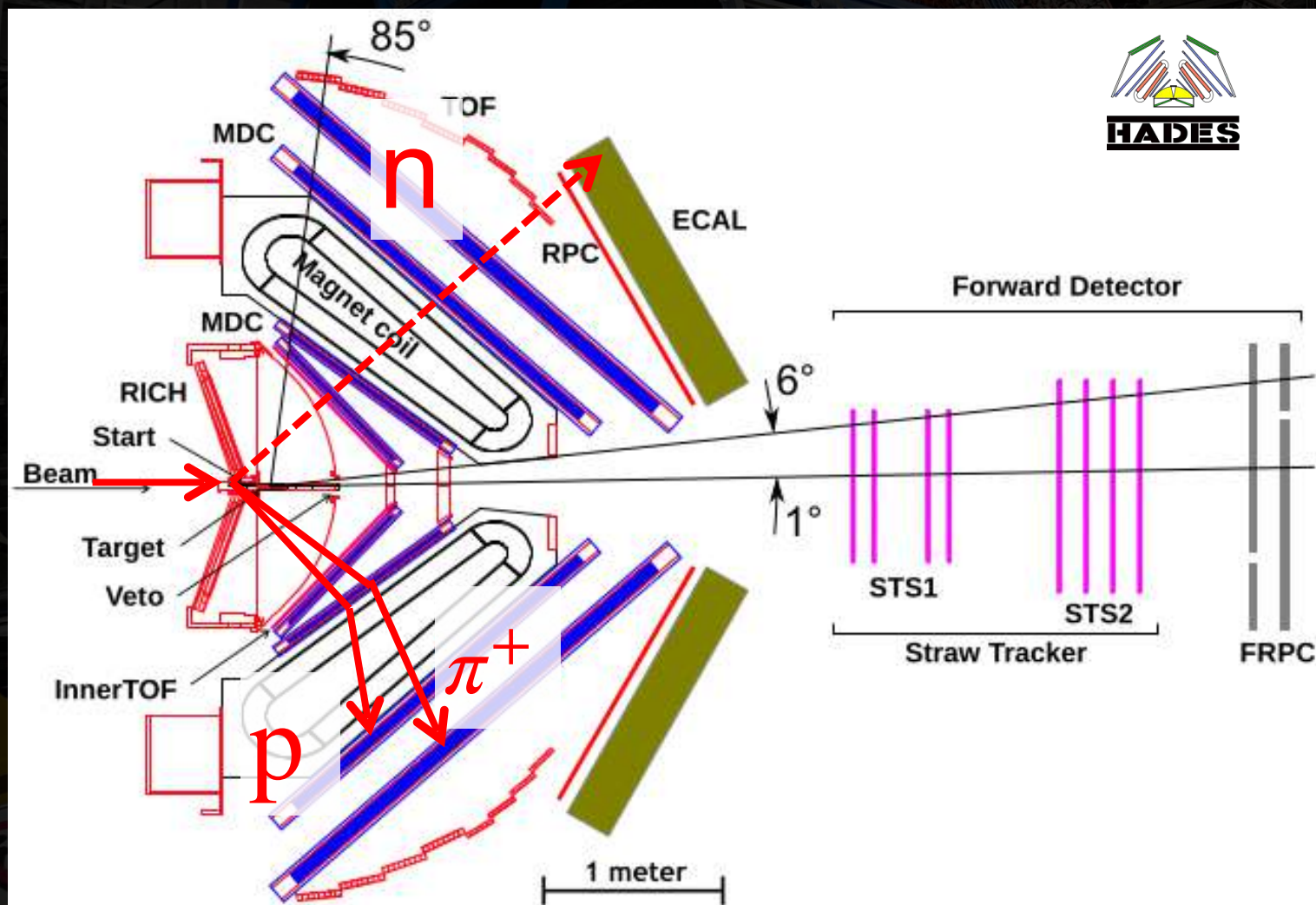
- Pion Beam Run planned to explore the second resonance regime.



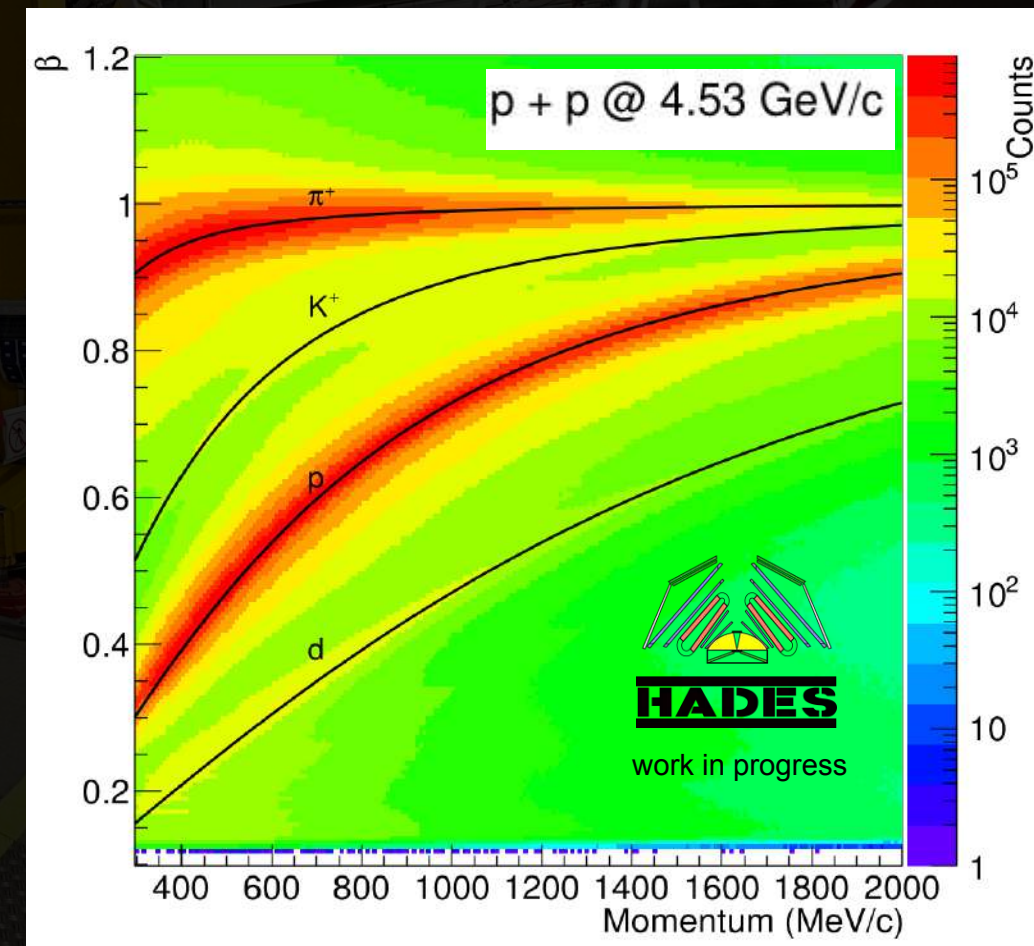
- *Talk by Anna Koperwas- Władyszewska (Wednesday)
- *Talk by Ahmed Marwan Foda (Monday)
- *Talk by Valentin Kladov (Thursday)

Particle Identification

- Reconstruct momenta of proton and π^+ with two track particle identification (PID) procedure.
- Reconstruct neutron momenta with missing mass analysis

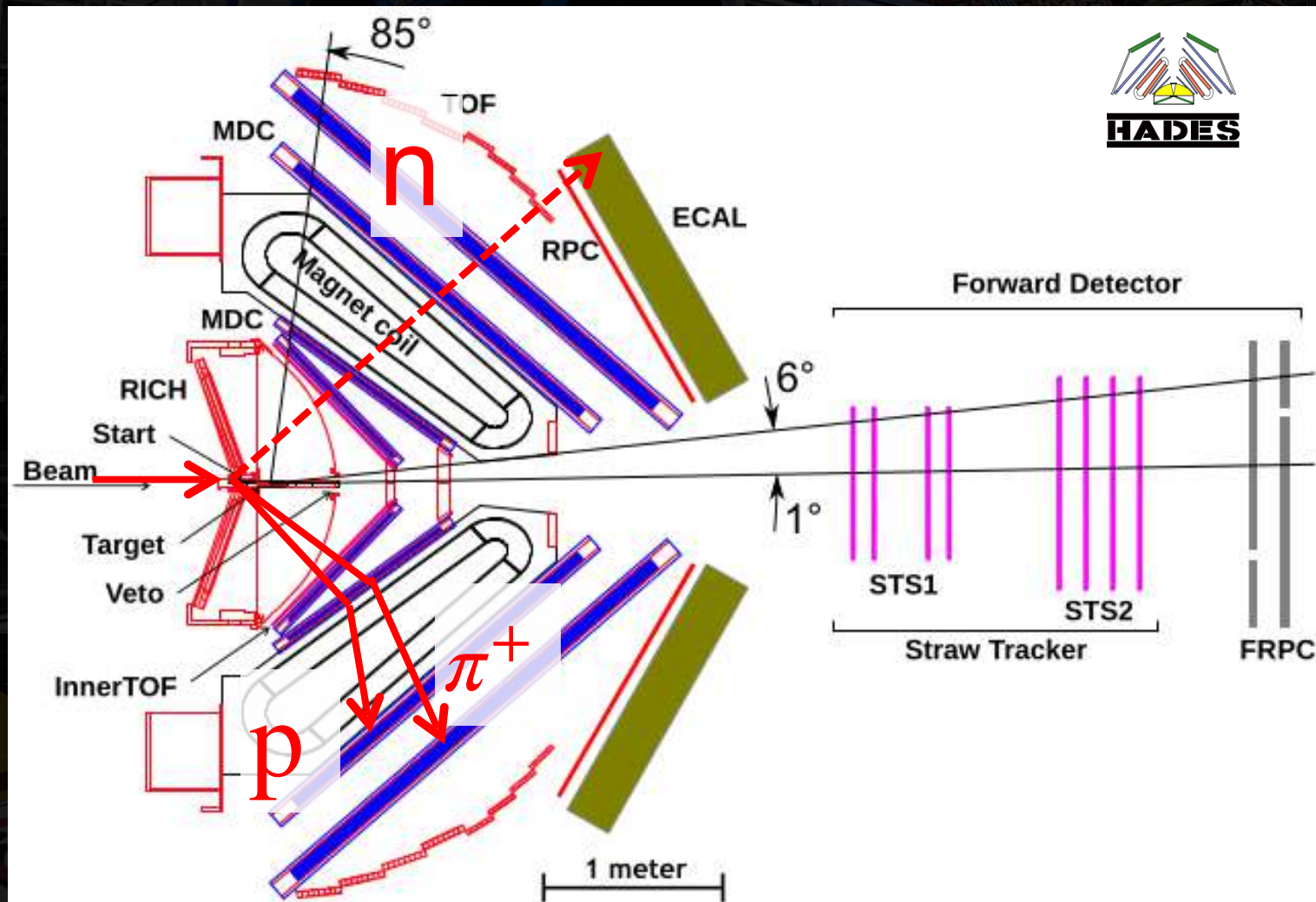


Particle Identification

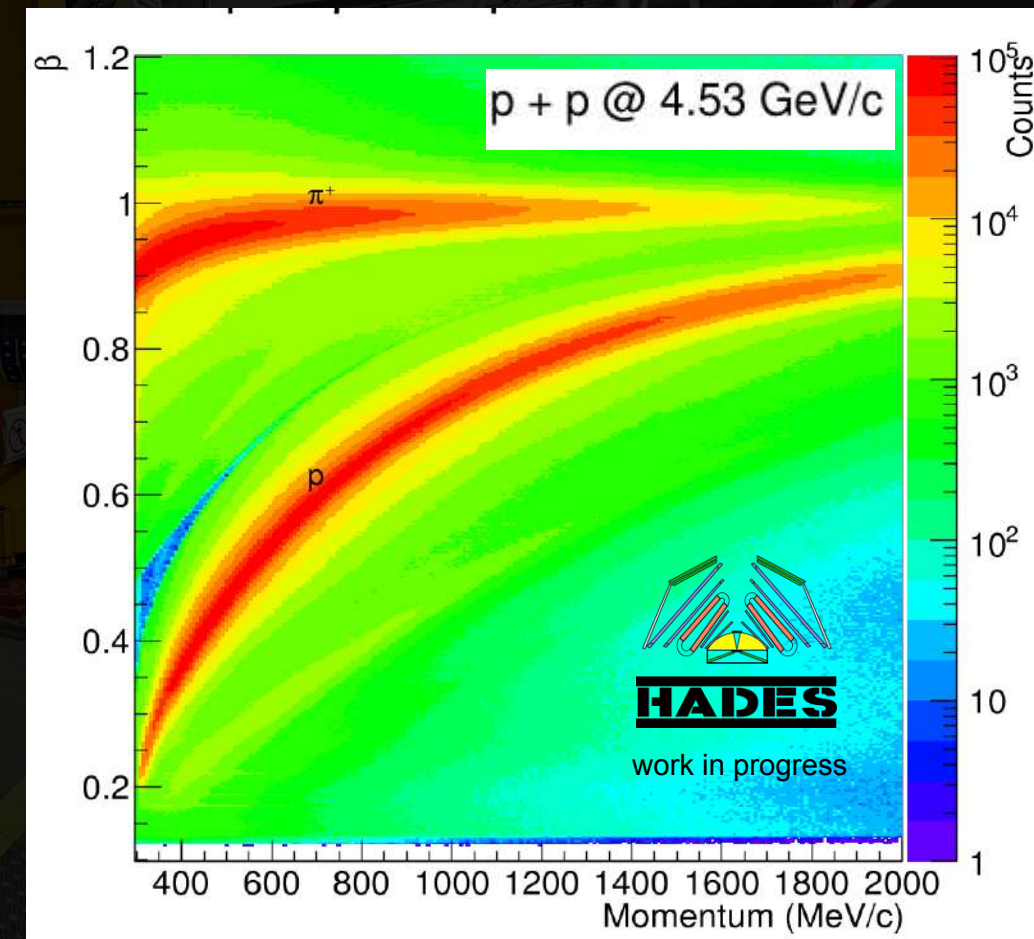


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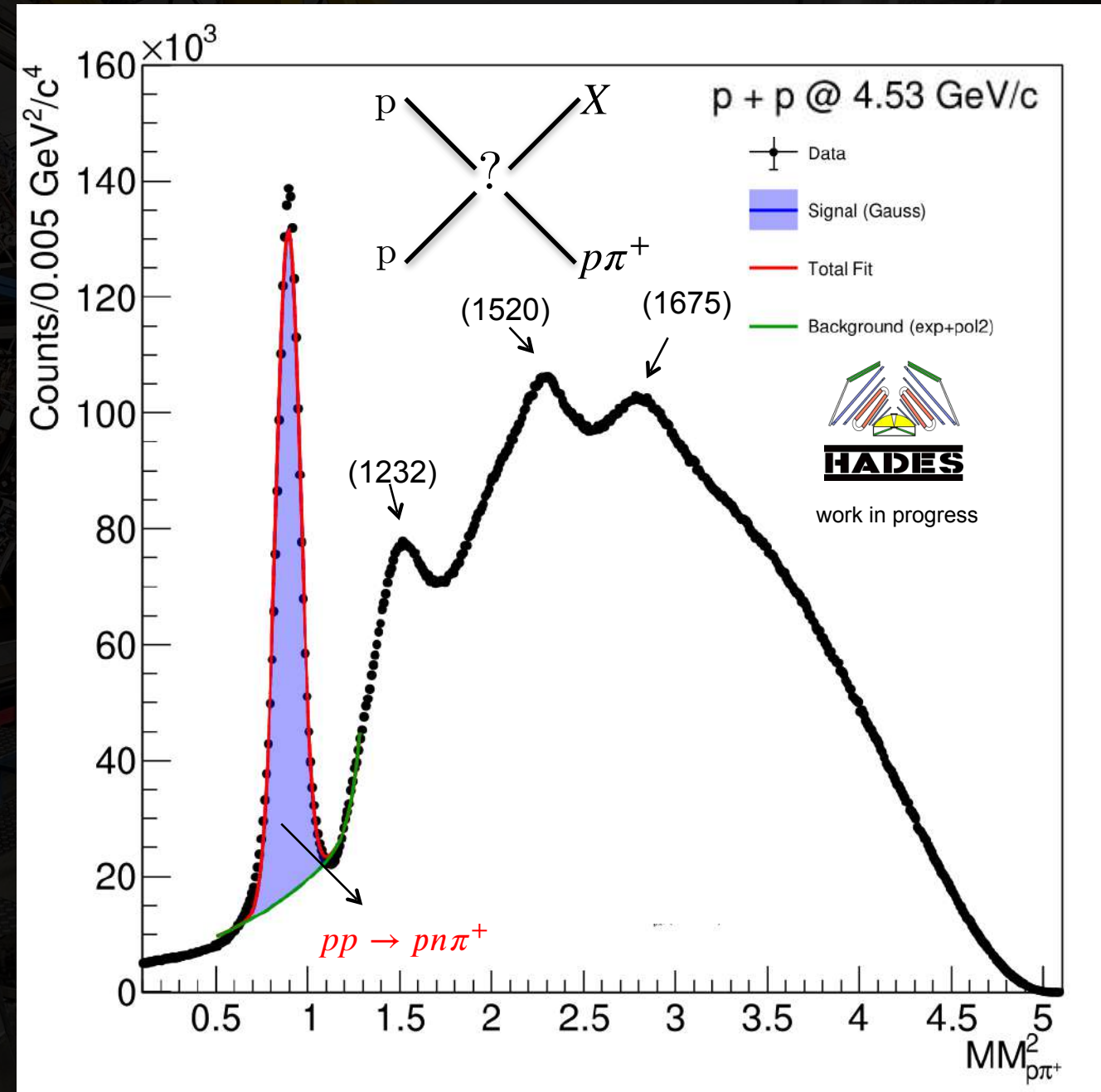


After Multiplicity and Vertex cuts



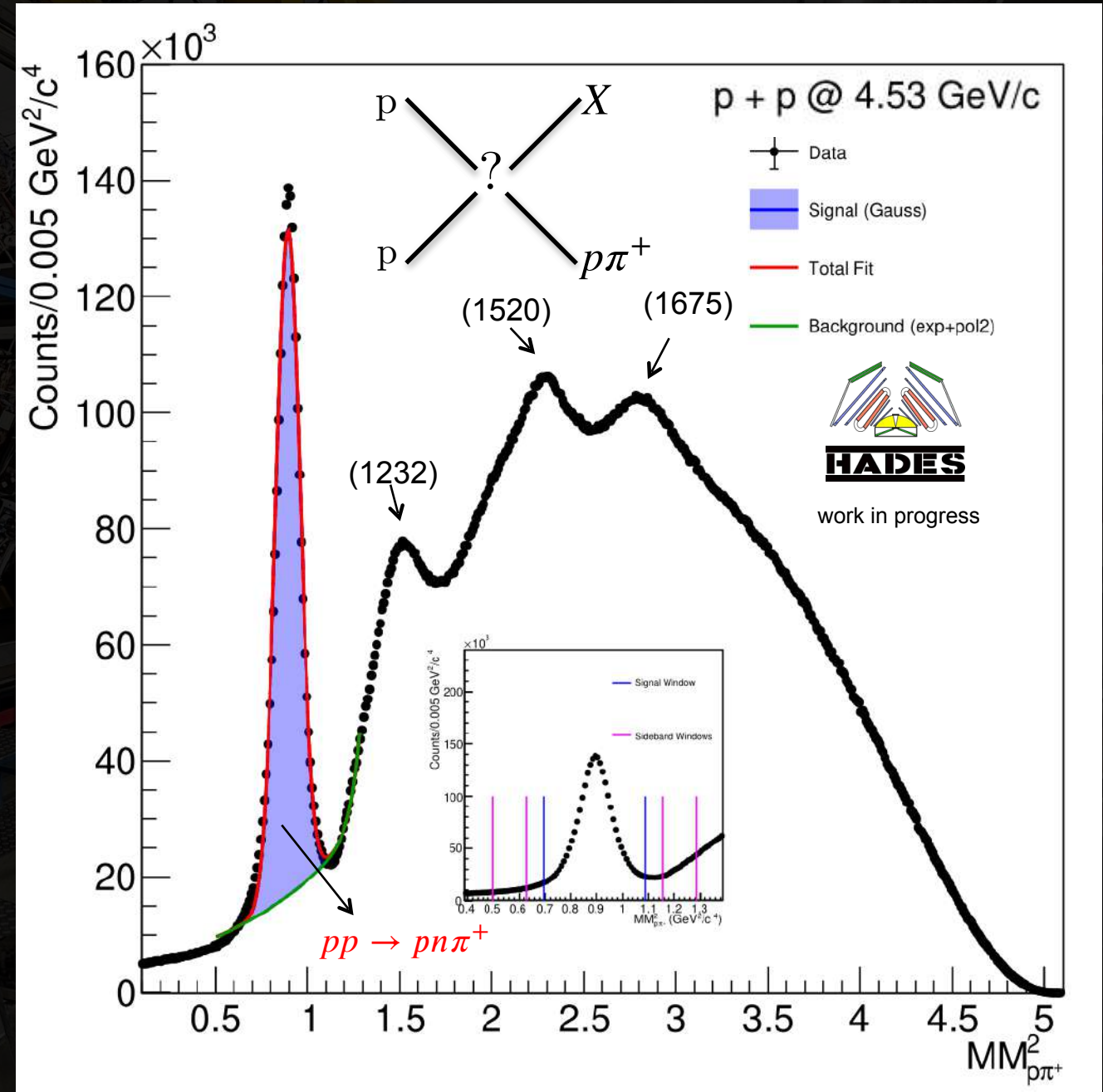
Missing Neutron Identification

- Select missing neutron by applying mass window for further analysis.

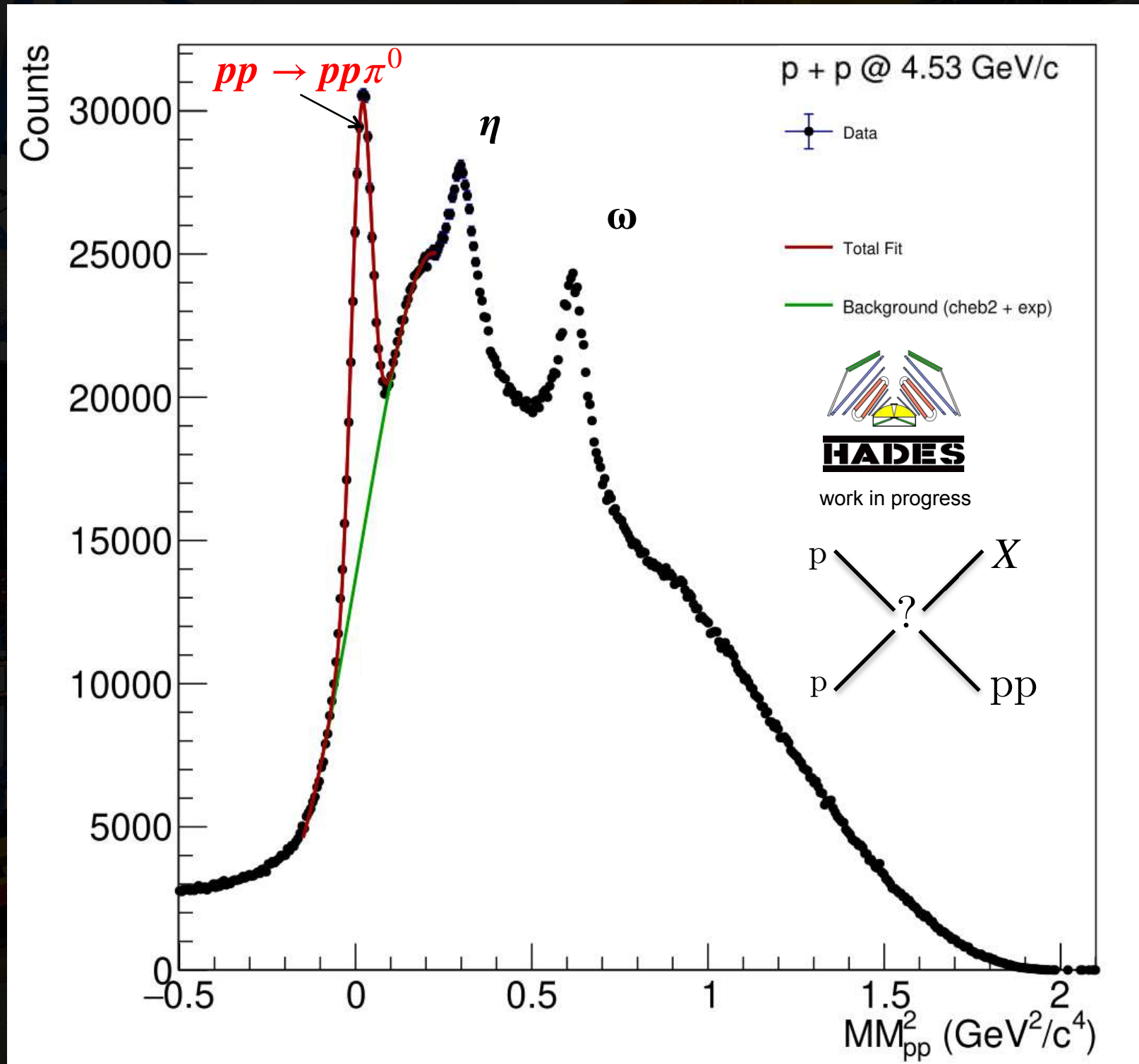


Missing Neutron Identification

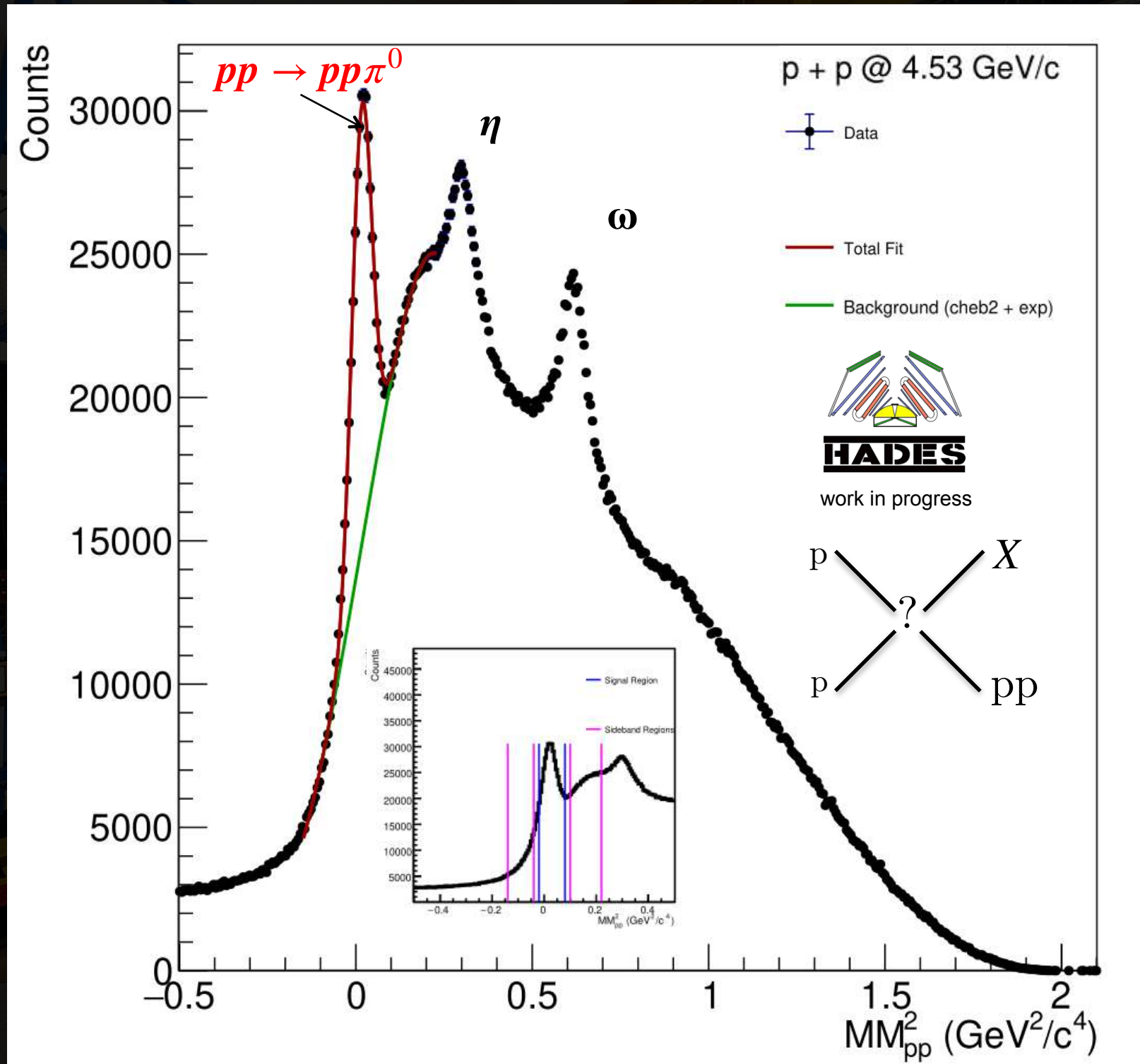
- Select **missing neutron** by applying mass window for further analysis.
- Kinematic fit is applied to signal and sideband regions.



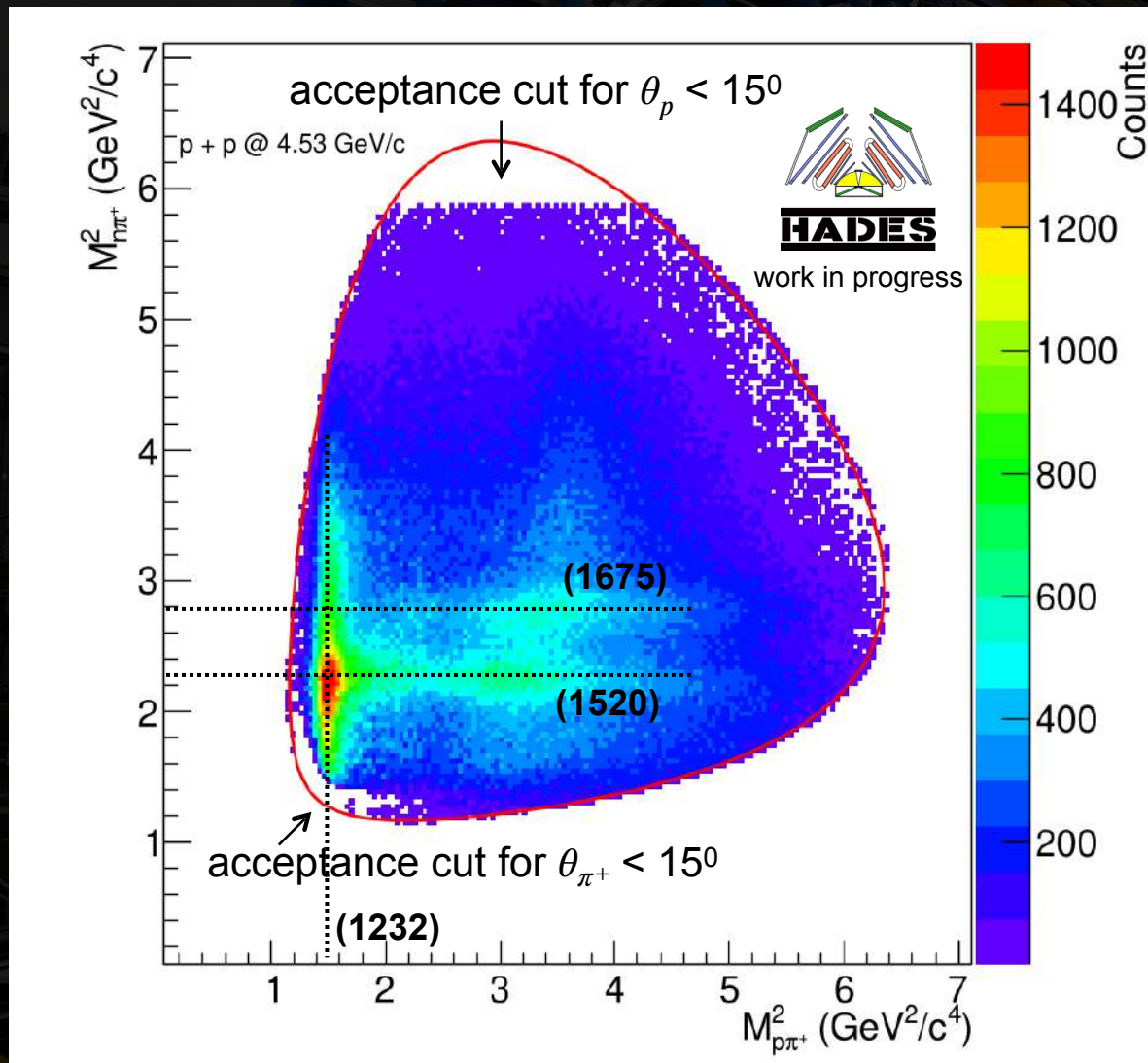
$$pp \rightarrow pp\pi^0$$



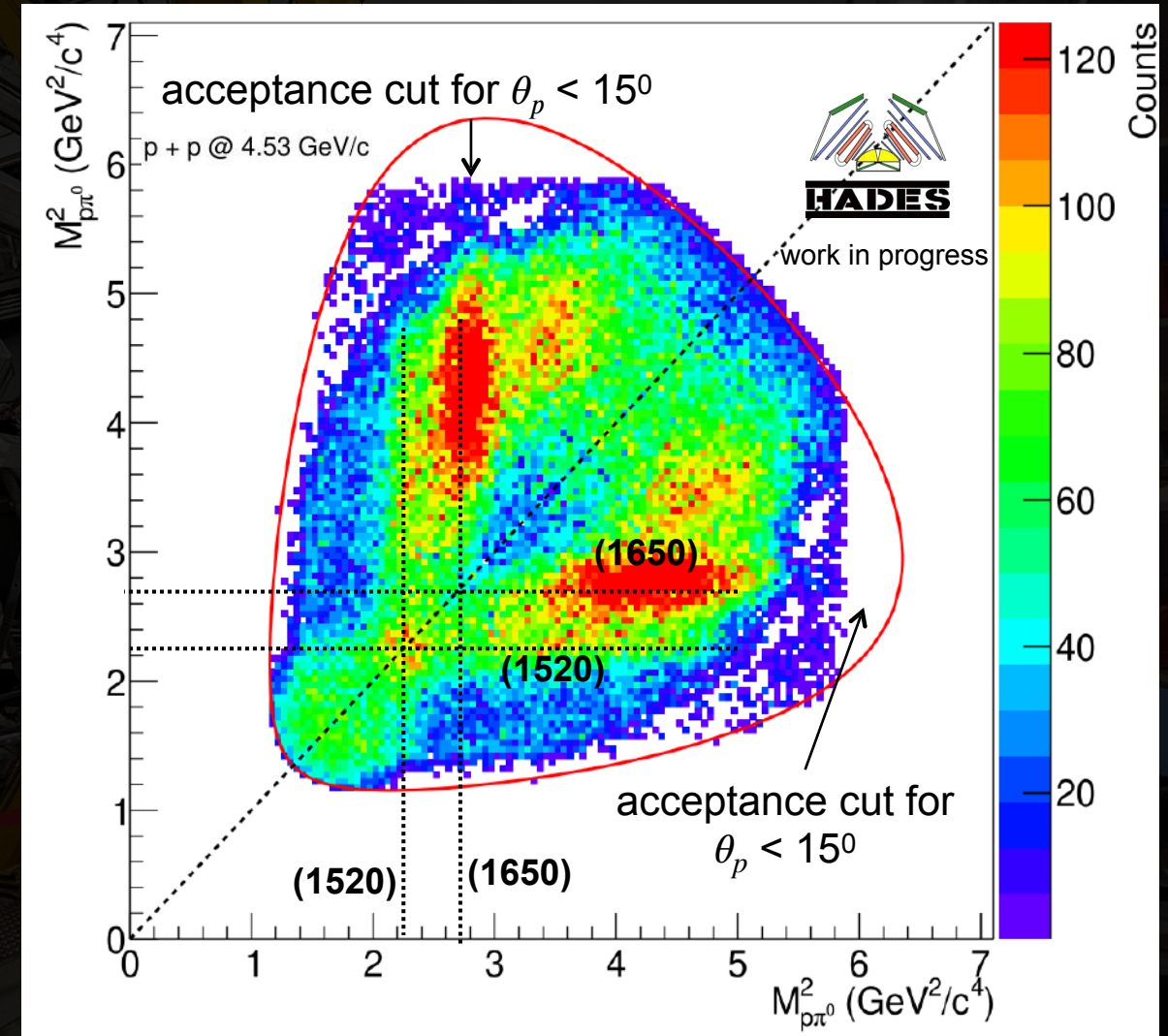
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Sideband Subtracted Dalitz Plots

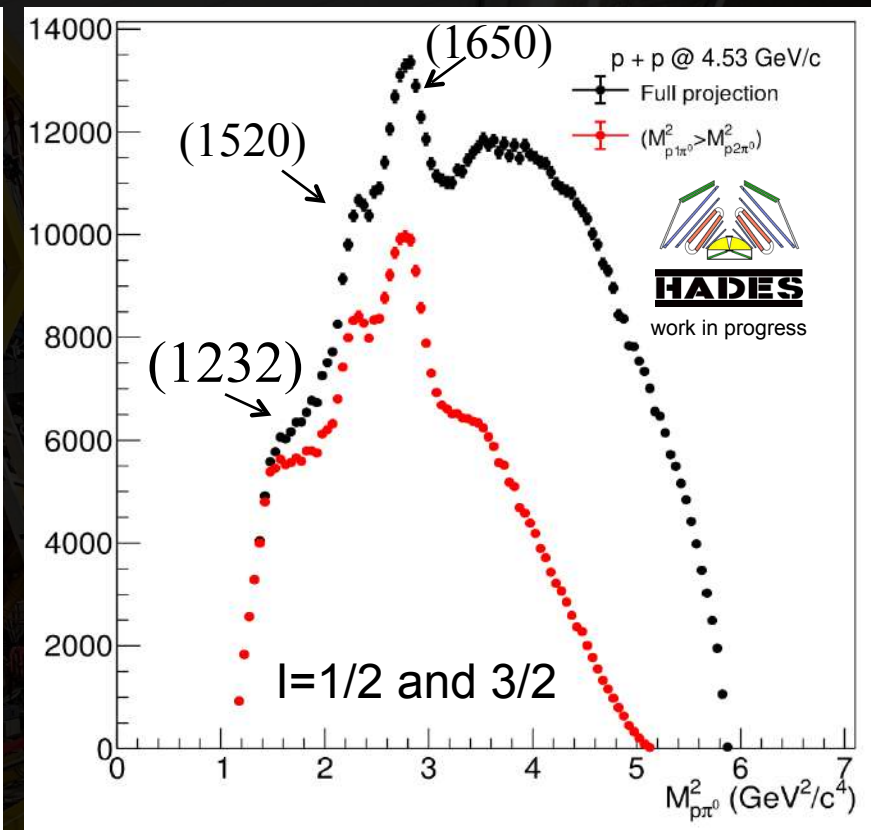
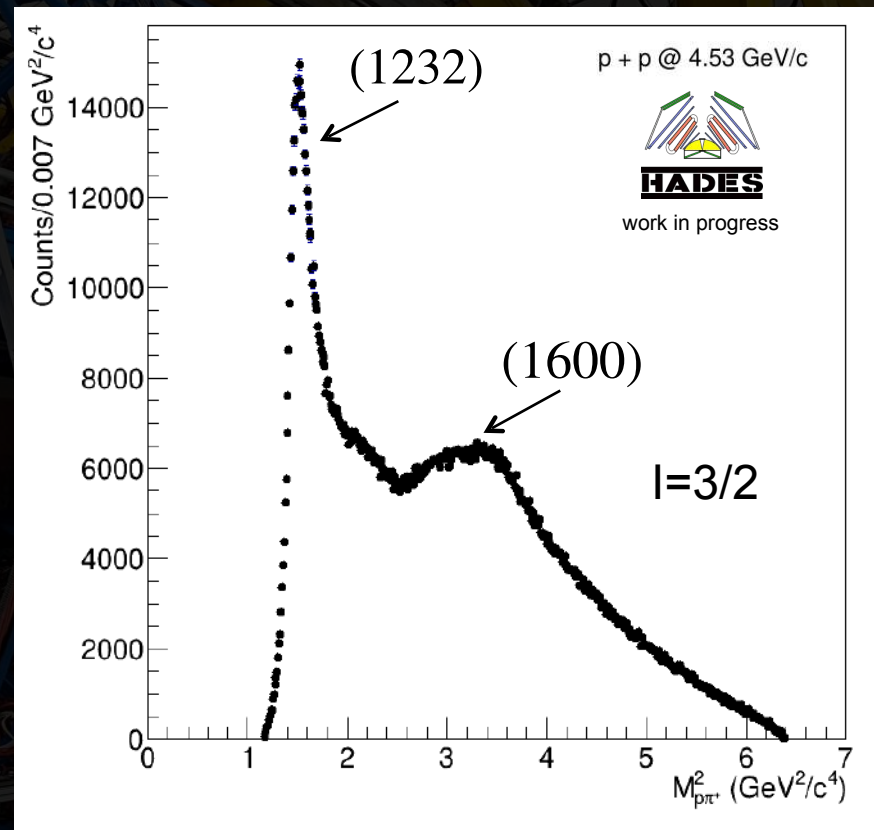
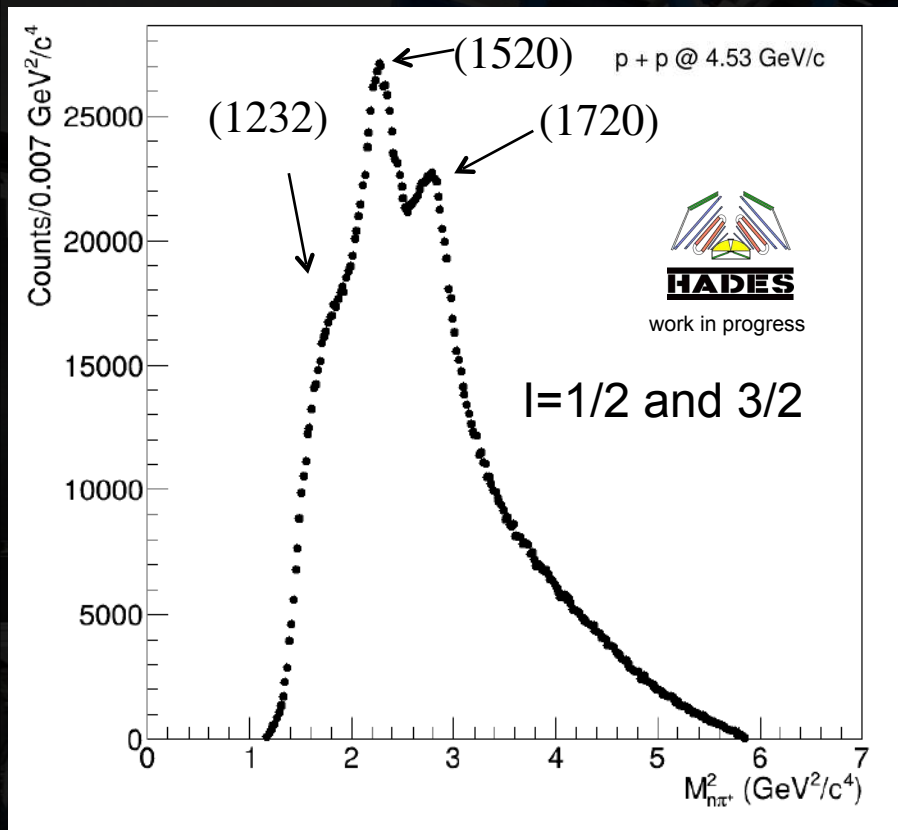


$pn\pi^+$



$pp\pi^0$

Dalitz Plot Projections

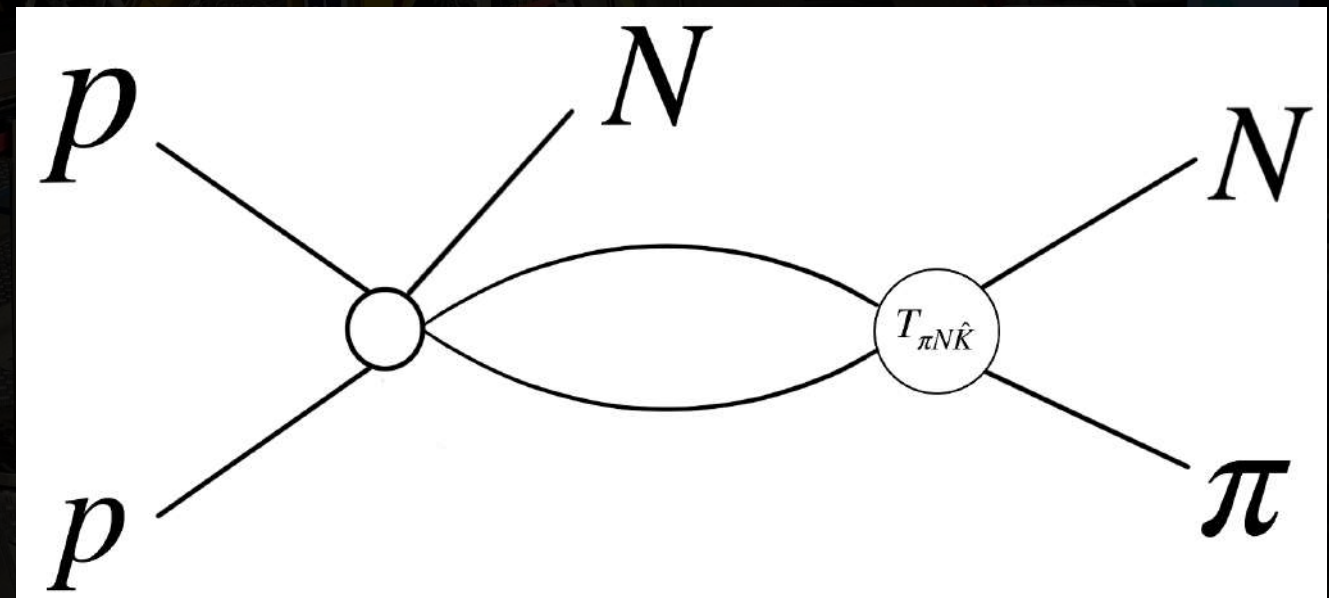


$p n \pi^+$

$p p \pi^0$

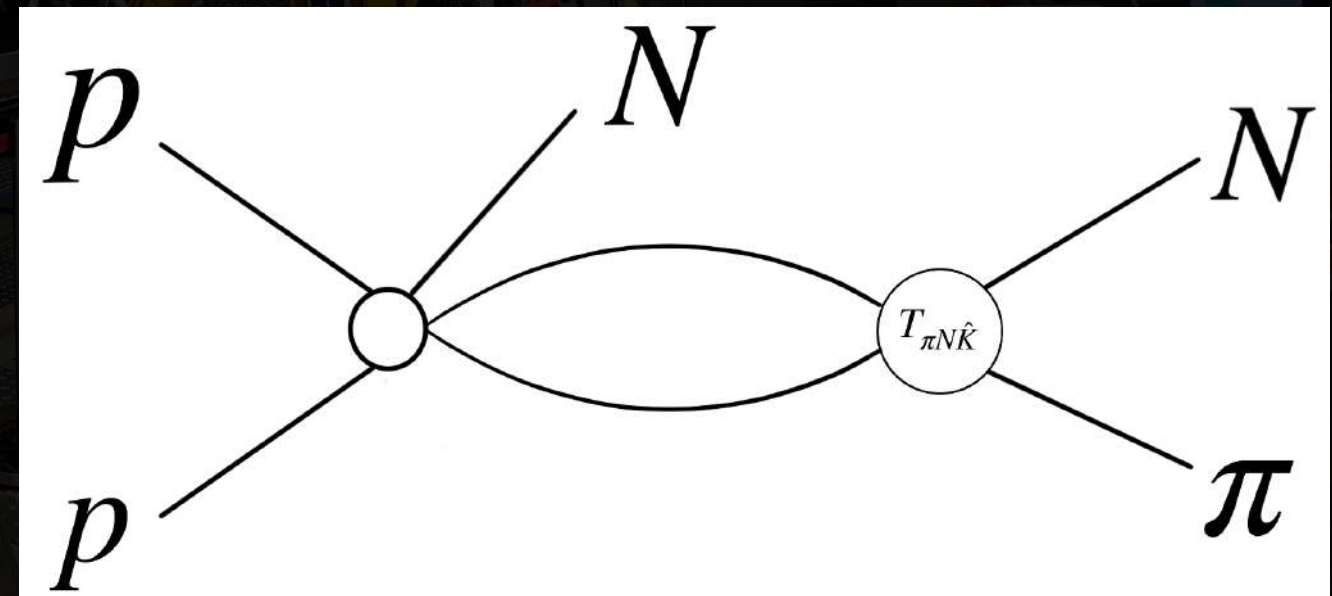
$pp \rightarrow NN\pi$ with Jülich-Bonn Dynamic Coupled Channel Approach

- Dynamical Coupled Channel (DCC) [4] approach : simultaneous analysis of different reactions.
- Allows for extracting the coupling strength of the resonances to final states.



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- $\mathcal{M}$ is the invariant matrix element for calculating the invariant mass distribution and $T_{\pi p \hat{K}}$ is the full JüBo T-Matrix for different channels ($\hat{K} \rightarrow \pi N$), includes s-channel and dynamically generated resonances.



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$$\mathcal{M}_{\mu\nu}(q, p', \epsilon) = V_{\mu\nu}(q, p', \epsilon) + \sum_{\hat{K}} \int_0^\infty dp p^2 T_{\mu\hat{K}}(q, p, \epsilon) G_{\hat{K}}(p, \epsilon) V_{\hat{K}\nu}(p, p', \epsilon)$$

↑
Kernel which contains the
coupling information
of the resonances
to the final state

↑
all possible meson
baryon channels

ϵ - C.M energy of $pp \rightarrow pn\pi^+$

- MB $\rightarrow$ MB interactions (e.g. FSI) are incorporated by Jülich-Bonn model (fitted through lots of data) within SU(3) dynamics.

$pp \rightarrow NN\pi$ with Jülich-Bonn Dynamic Coupled Channel Approach

- Dynamical Coupled Channel (DCC) [4] approach : simultaneous analysis of different reactions.
- Allows for extracting the coupling strengths to different final states.
- $\mathcal{M}$ is the invariant matrix element for the transition from the initial state to the final state. It includes s-channel, t-channel and u-channel exchanges.

Can we decouple final-state interactions from the production mechanism?

$$\mathcal{M}_{\mu\nu}(q, p, \epsilon)$$

$$= \mu_{\hat{K}}(q, p, \epsilon) G_{\hat{K}}(p, \epsilon) V_{\hat{K}\nu}(p, p', \epsilon)$$

ϵ - C.M energy of $pp \rightarrow pn\pi^+$

all possible NSTAR baryon channels

- MB $\rightarrow$ MB interactions (e.g. FSI) are incorporated by Jülich-Bonn model (fitted through lots of data) within SU(3) dynamics.

AmpTools – Framework for Amplitude Analysis

Purpose:

- Toolkit for performing Partial Wave Analysis (PWA)^[5].
- Fits complex amplitudes for exclusive reactions.

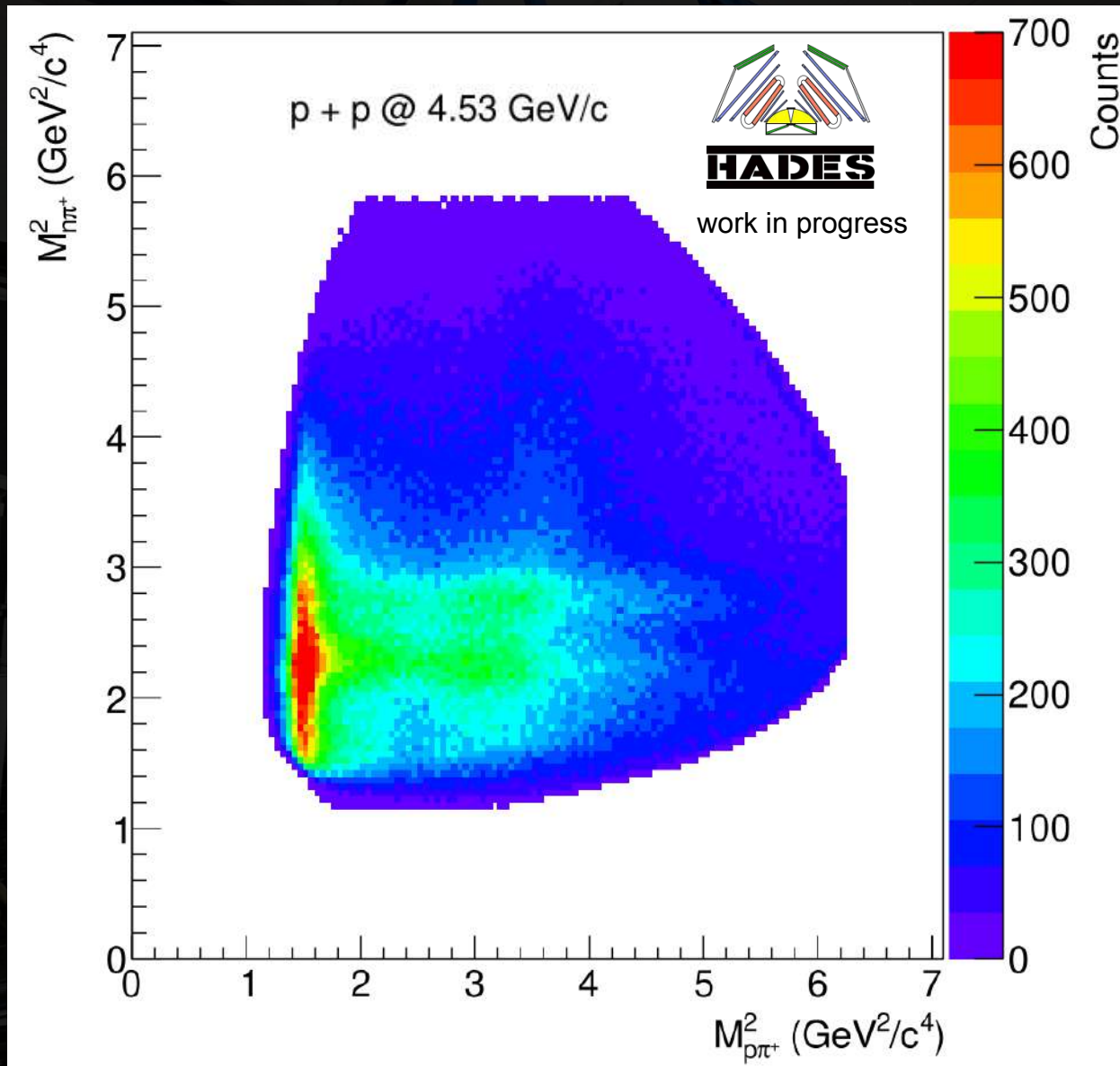
Key Features

- Flexible physics model definitions (resonances, backgrounds).
- Coherent and incoherent amplitude combinations.
- Event-based maximum likelihood fitting.

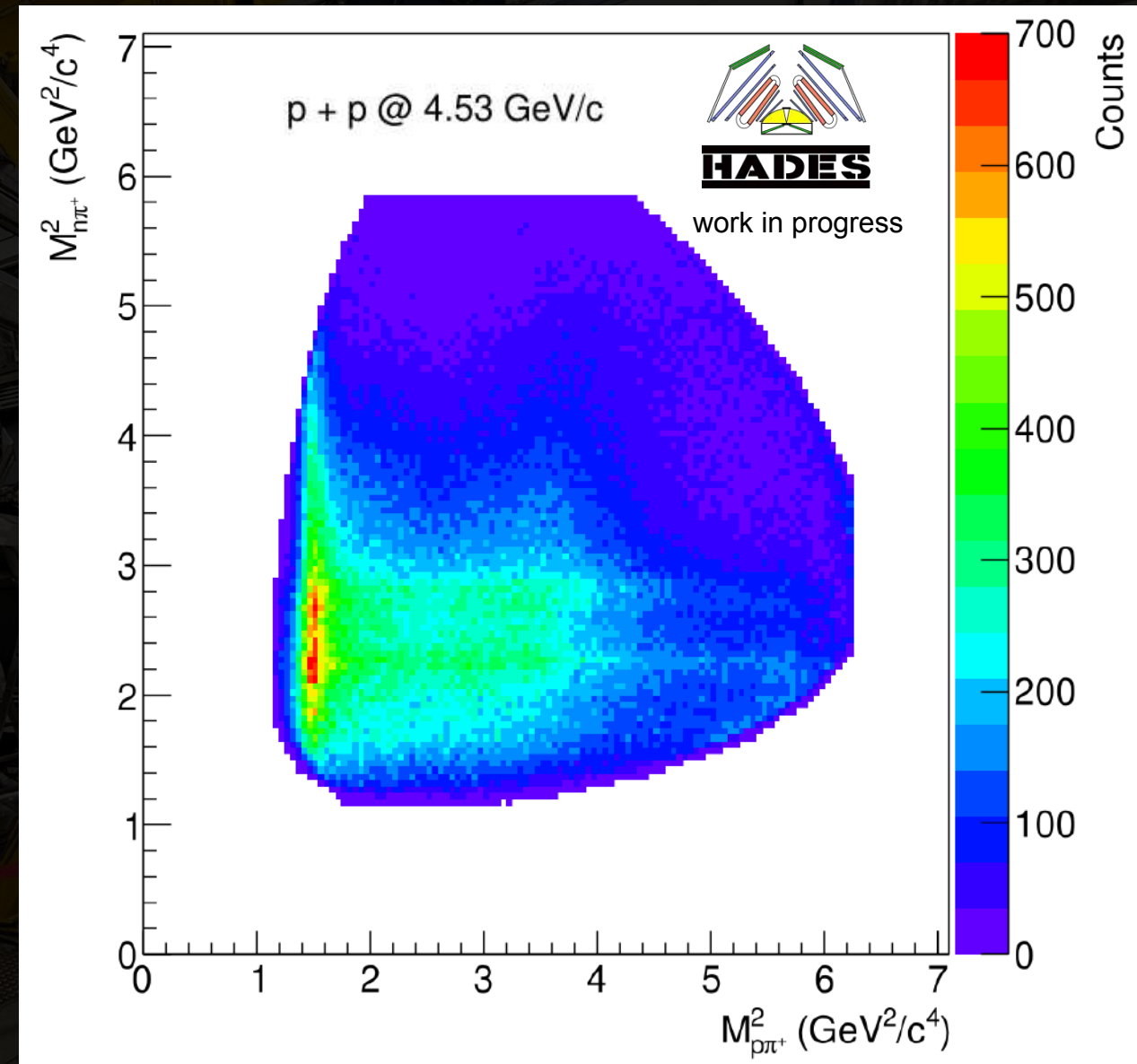
$$-2 \ln \mathcal{L}(\theta) = -2 \left(\sum_{i=1}^N \ln I(x_i; \theta) - \int I(x; \theta) \eta(x) dx \right) + c_1$$

- GPU acceleration for fast computations.
- Interfaces with ROOT.

Preliminary Fit Results

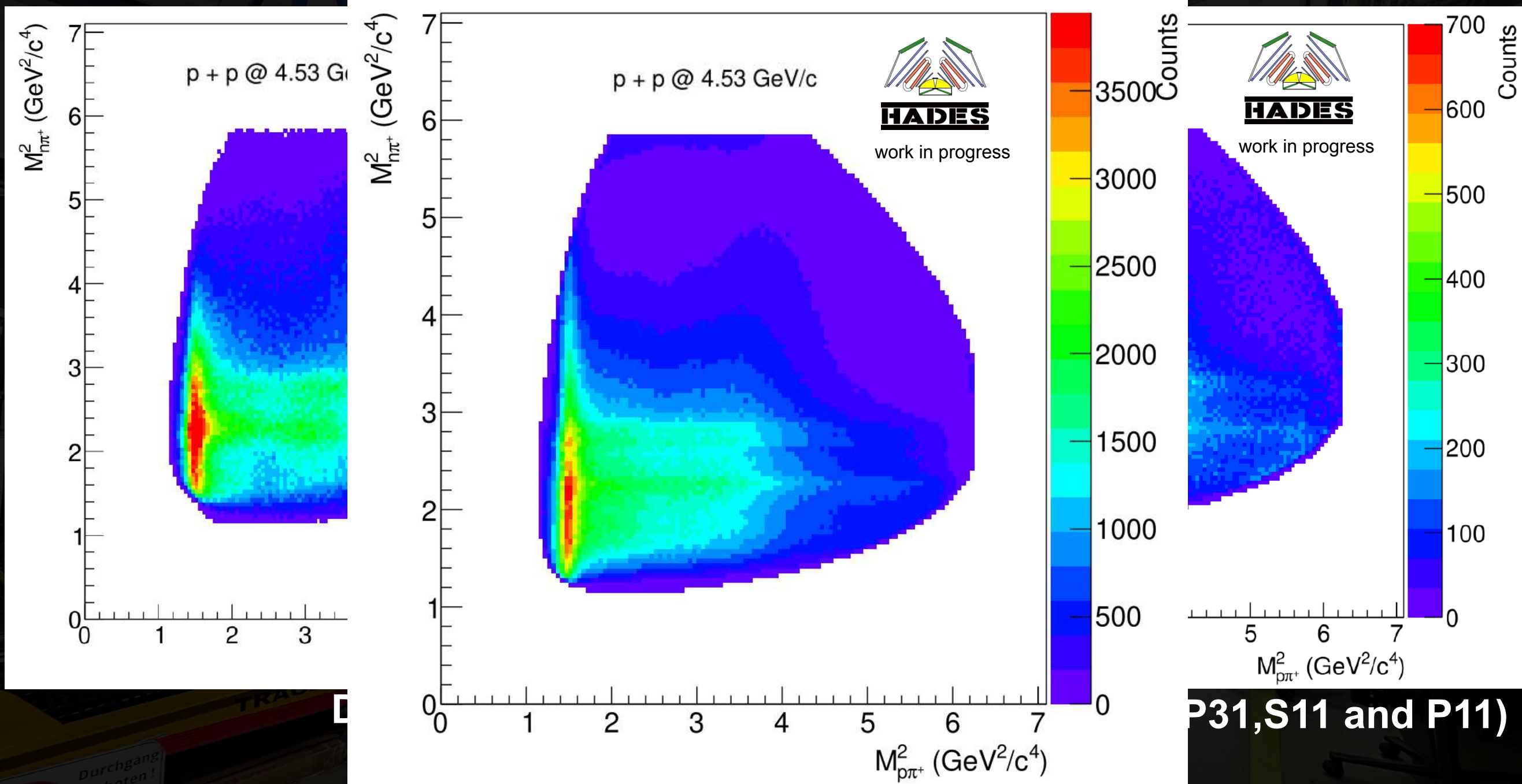


Data



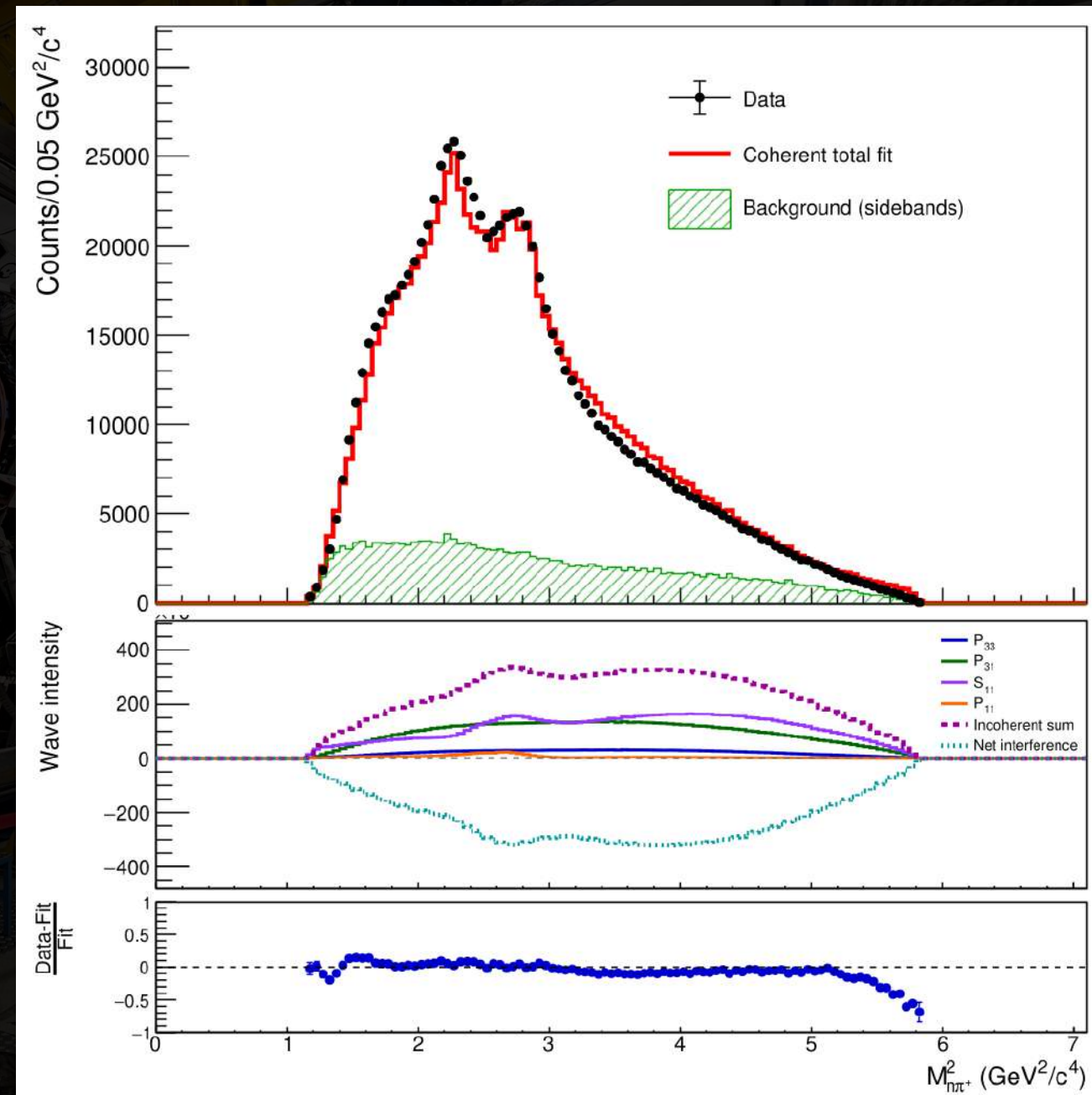
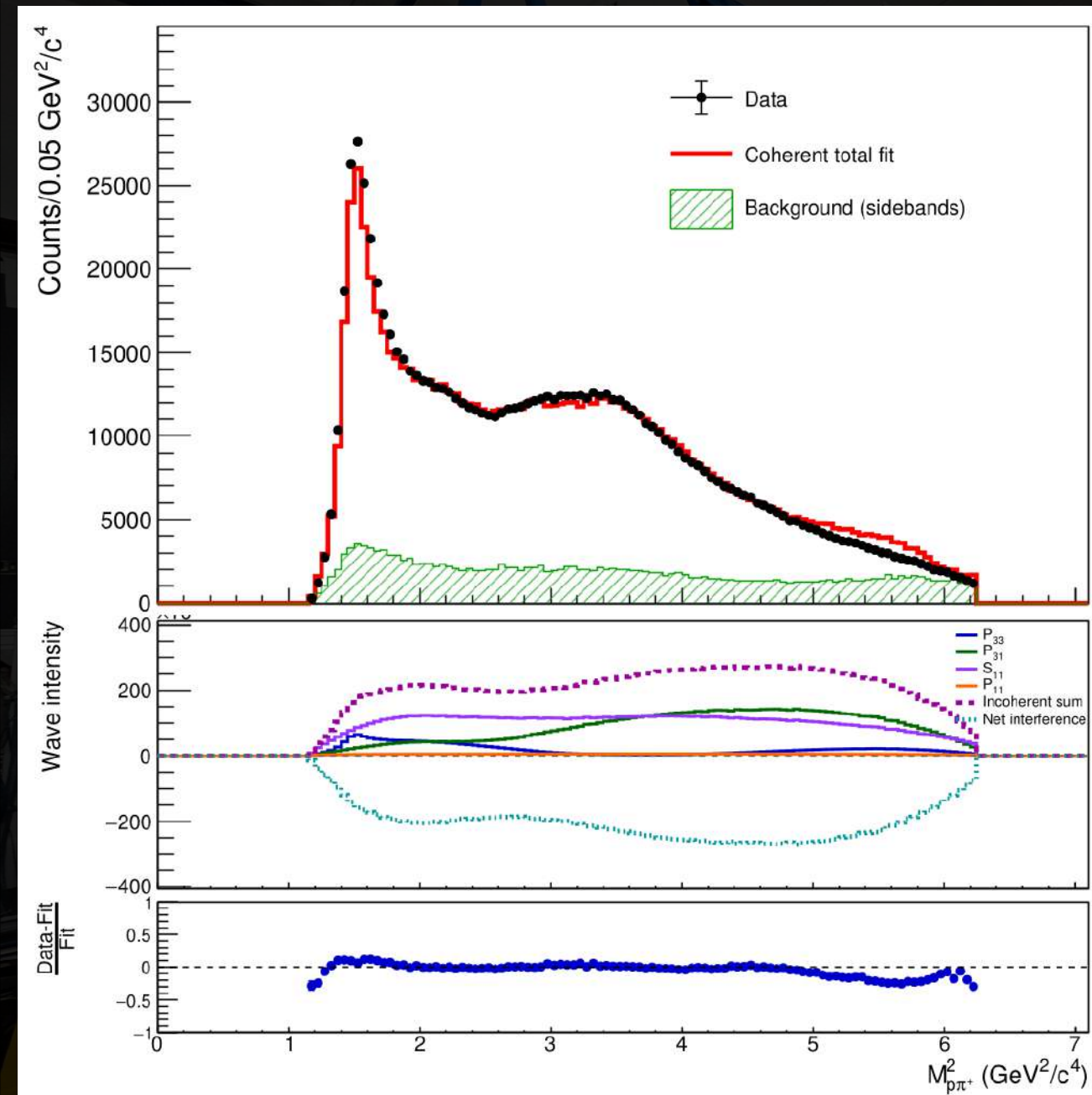
Fit Result (P33,P31,S11 and P11)

Preliminary Fit Results



Acceptance and Efficiency Corrected, can be used as a generator

Preliminary Fit Results



Fit Result (P33,P31,S11 and P11)

Conclusion and Outlook

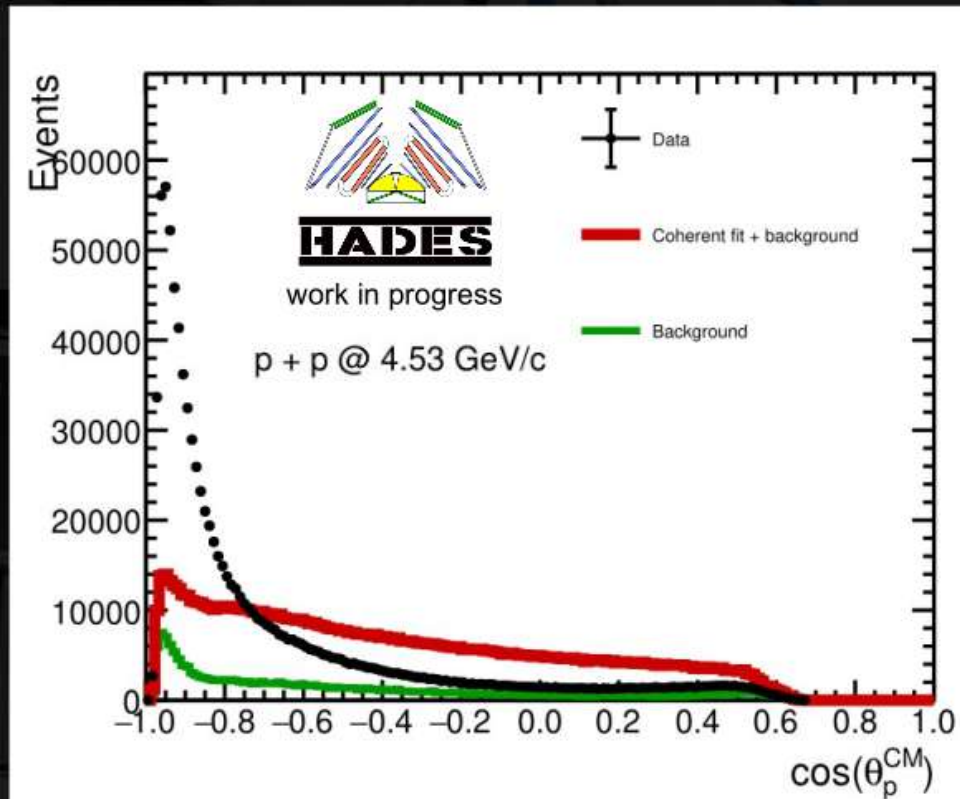
- The data provides valuable constraints for improving the implementation of baryon-resonance dynamics in transport models.
- Preliminary fit to the $pp \rightarrow pn\pi^+$ case shows the coupled channel machinery works.
- A good benchmark case to validate this machinery and assess whether it can be used to compute the FSI for other channels involving $K\Lambda$ and $K\Sigma$.
- Once the fit for $pp \rightarrow pn\pi^+$ case is finalised, quantify the different MB contribution.
- Also do a combined fit of the $pp \rightarrow pn\pi^+$ and $pp \rightarrow pp\pi^0$ channels.
- Extract cross-sections for $pp \rightarrow pn\pi^+$ and $pp \rightarrow pp\pi^0$ channels

Conclusion and Outlook

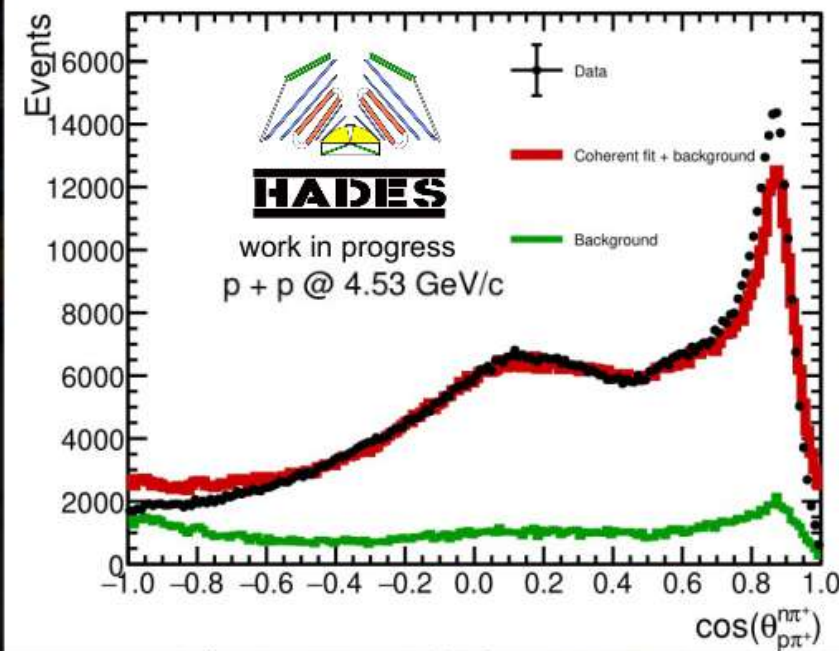
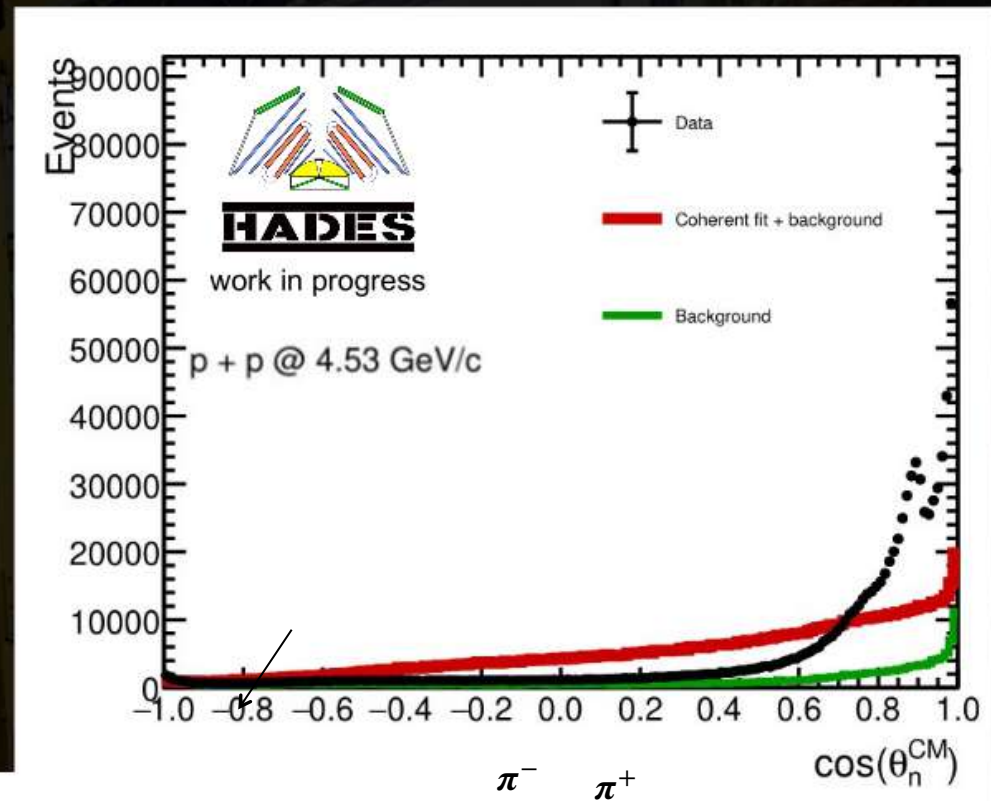
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Δ Thank You Δ

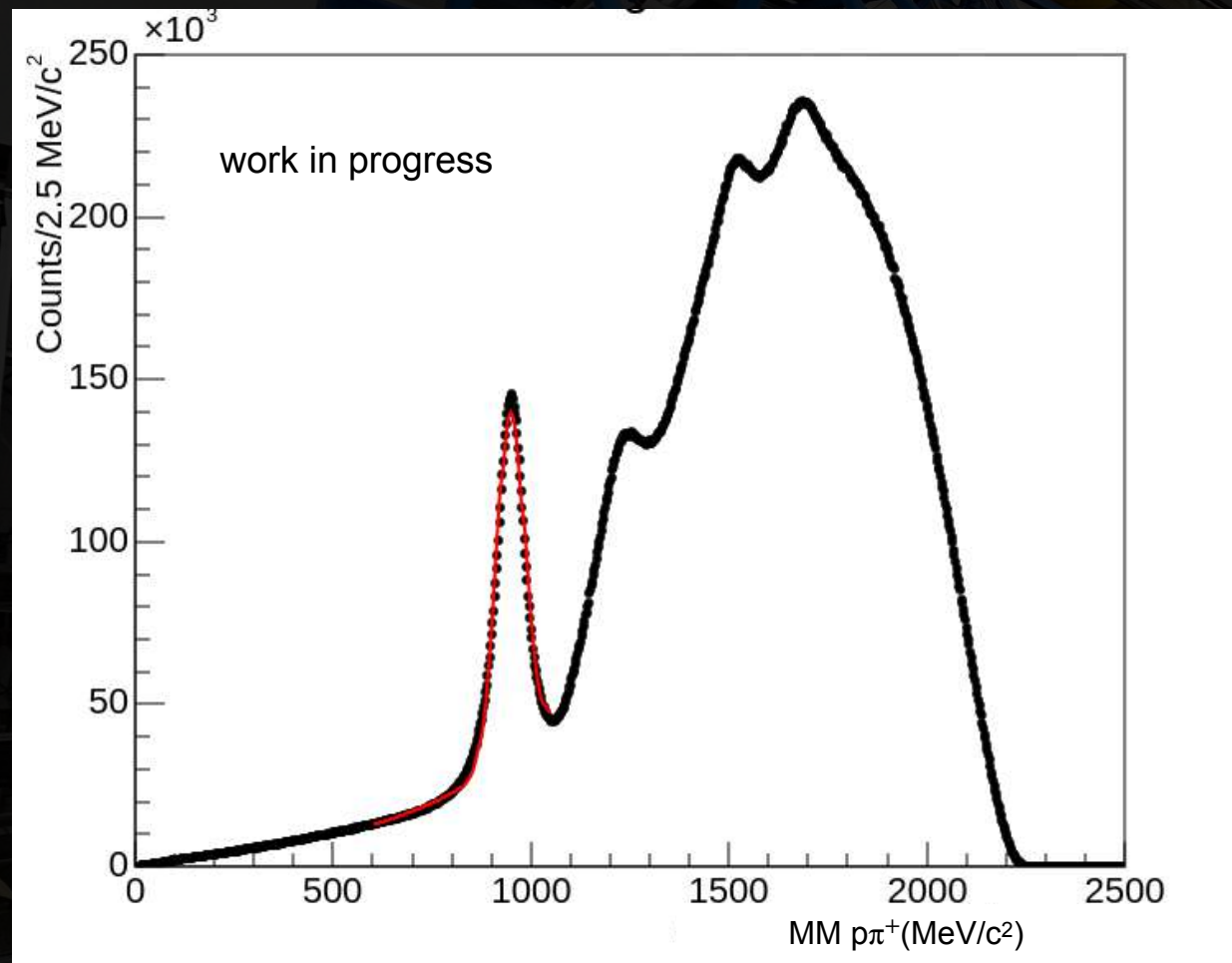
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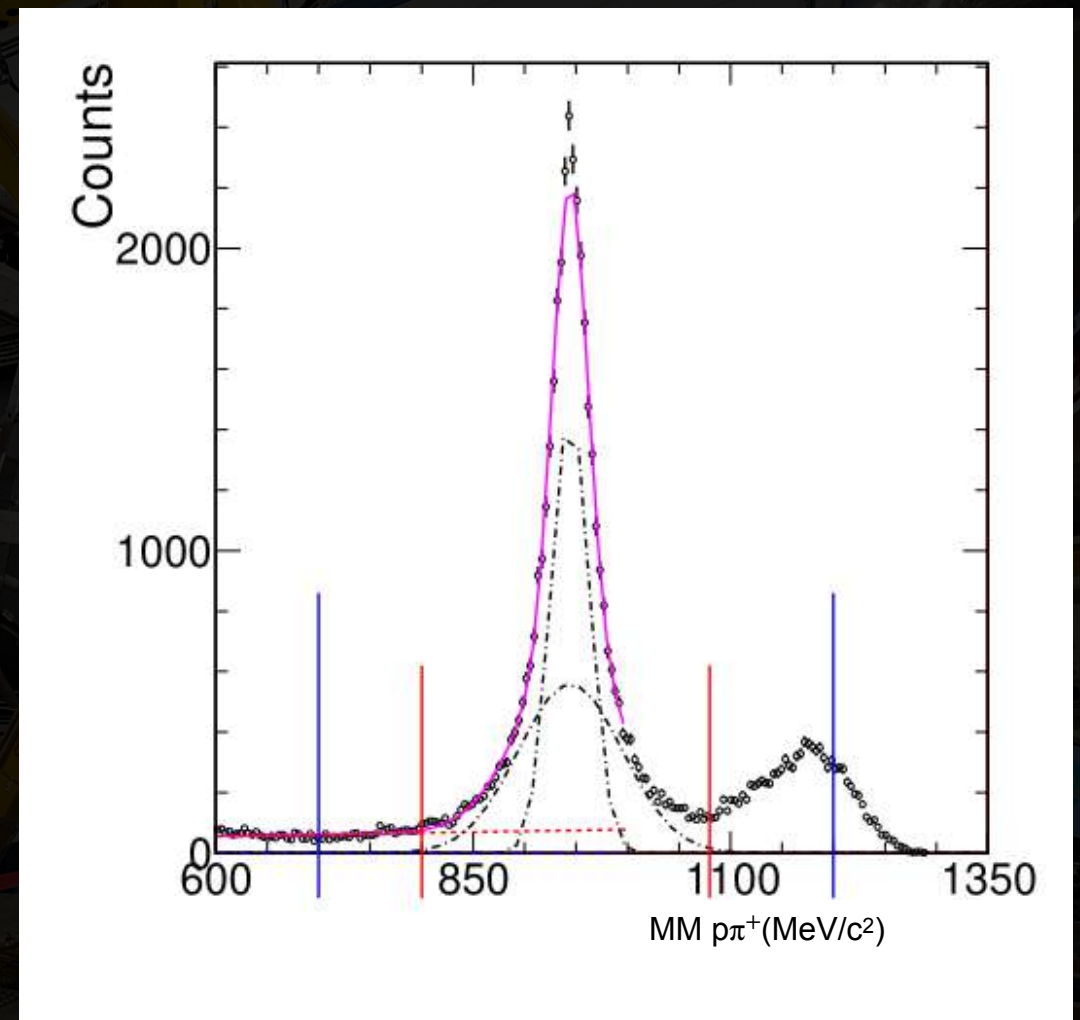
Angular
dependence
not
implemented



Missing Mass Resolution



Neutron Peak Resolution ~ 35 MeV/c²



pp at $T = 1.25$ GeV
T. Liu, PhD Thesis 2010.

Neutron Peak Resolution ~ 12 MeV/c²

Normalization and Barrier Factors

The amplitude is normalized and multiplied by a barrier factor:

$$A_{JuBo}(L, I, J) = B_L(q) \sqrt{\frac{\rho(s, m_1, m_2) K_f}{K_i}} A_{L, I, J}(\alpha, \gamma)$$

$B_L(q)$ is the Blatt-Weisskopf barrier factor for a spectator with the orbital angular momentum L .

K_i, K_f are initial and final momenta in the CM frame.

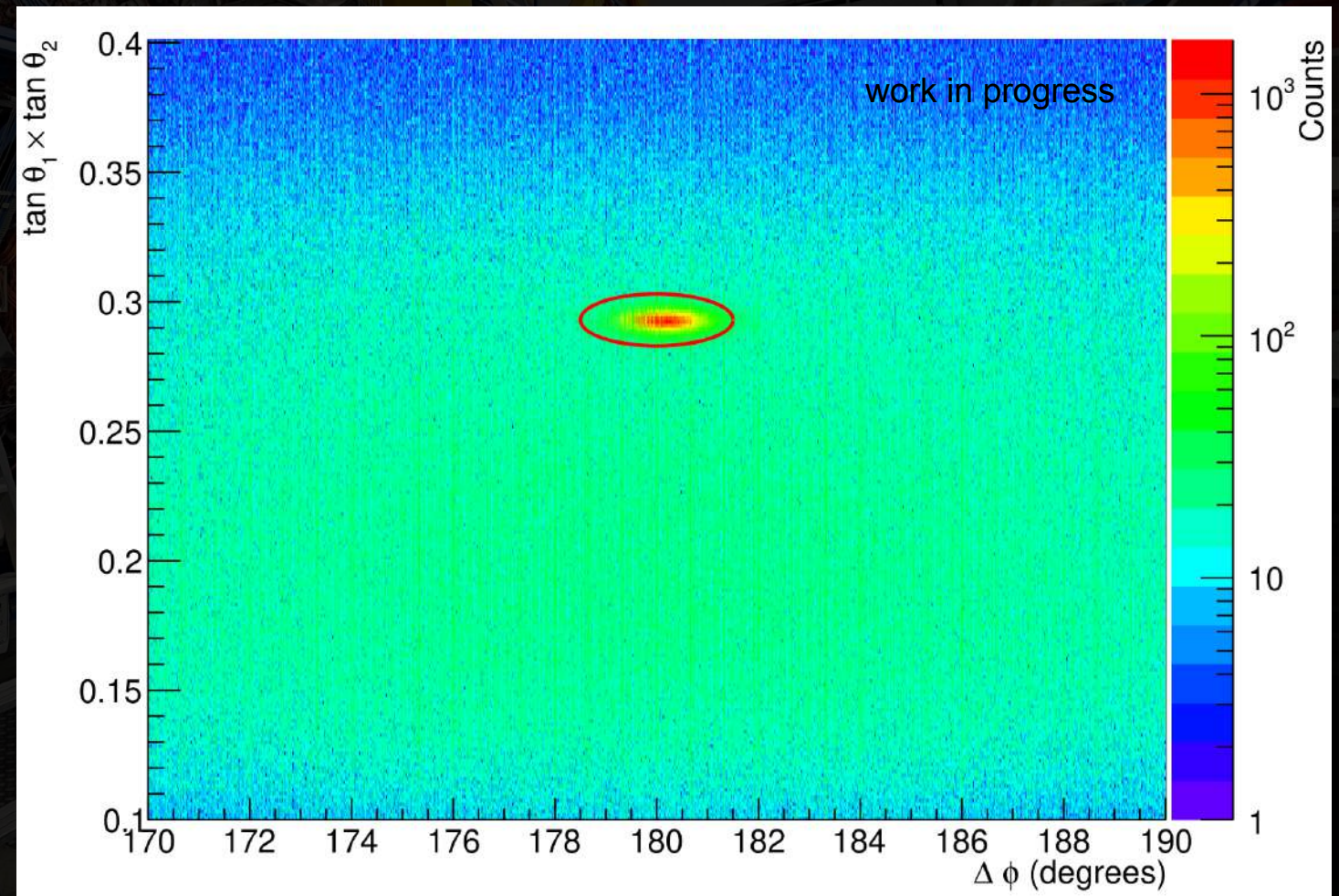
ρ is the NSTAR-Baryon phase space volume.

Elastic Cut

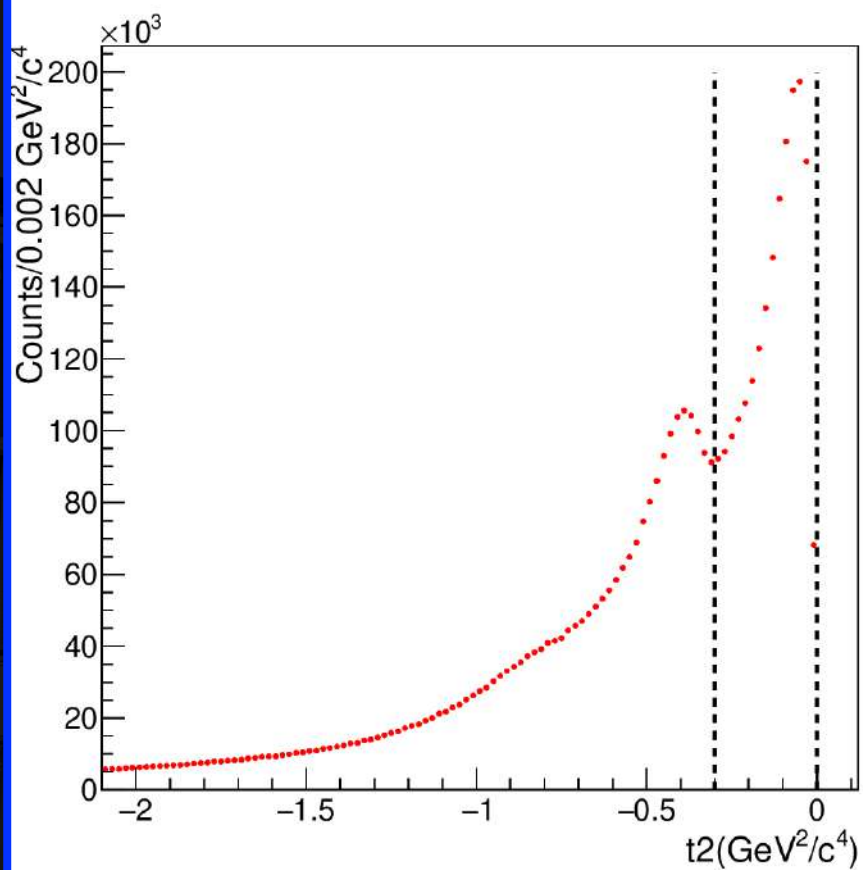
- Inelastic events are selected by applying cuts based on the expected kinematics of elastic scattering.

$$\Delta\phi = |\phi_1 - \phi_2| = 180^\circ$$

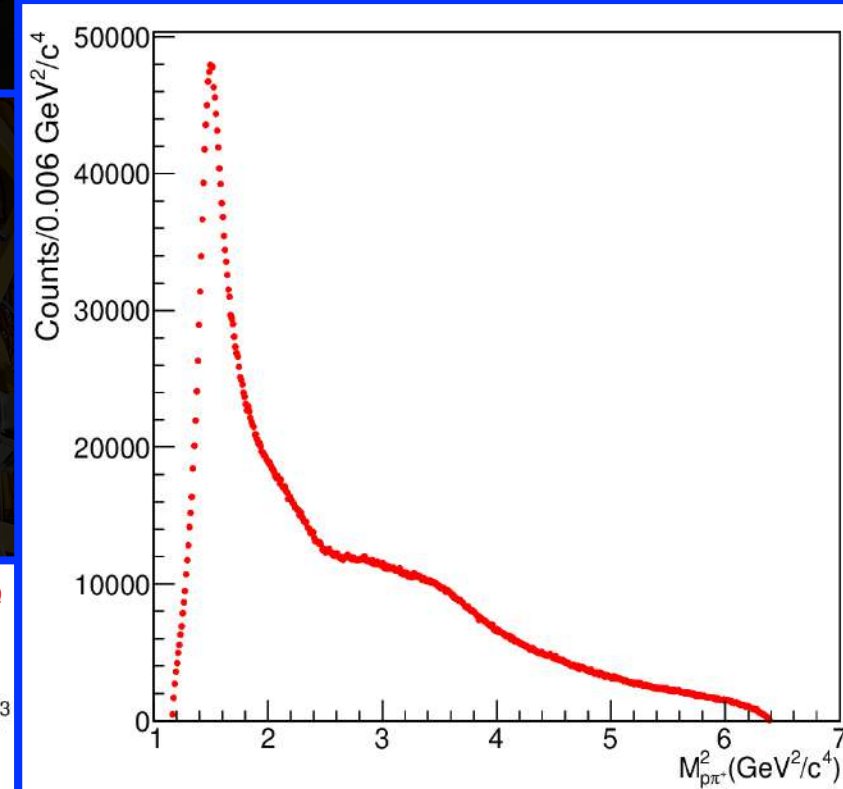
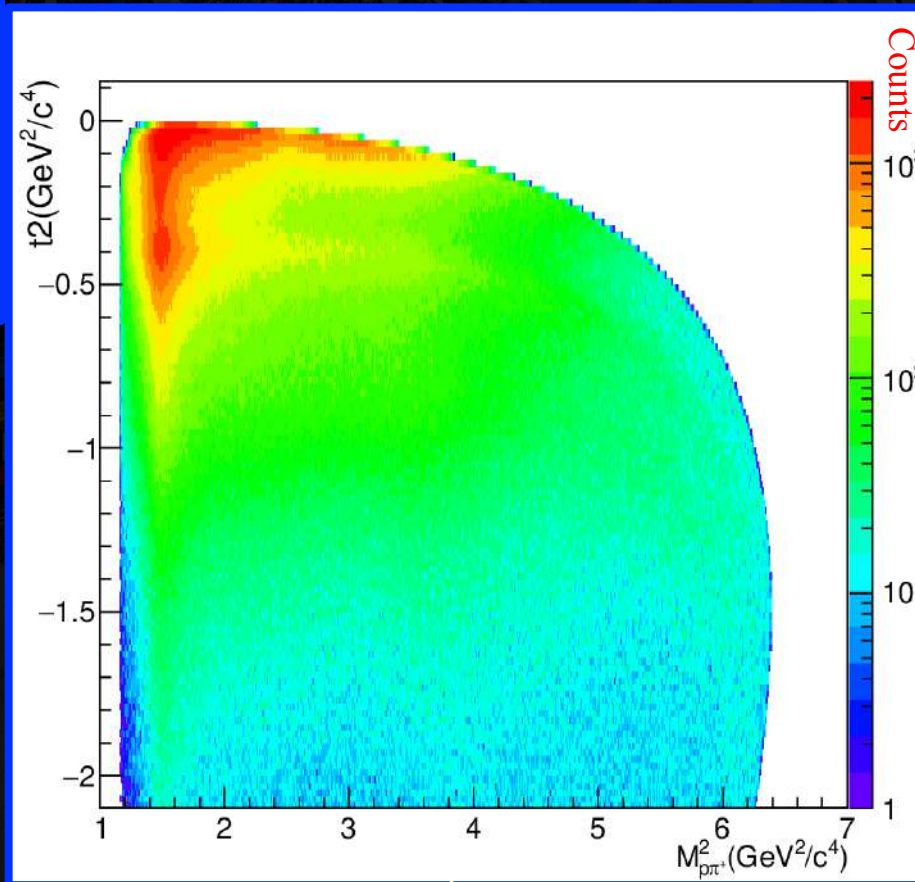
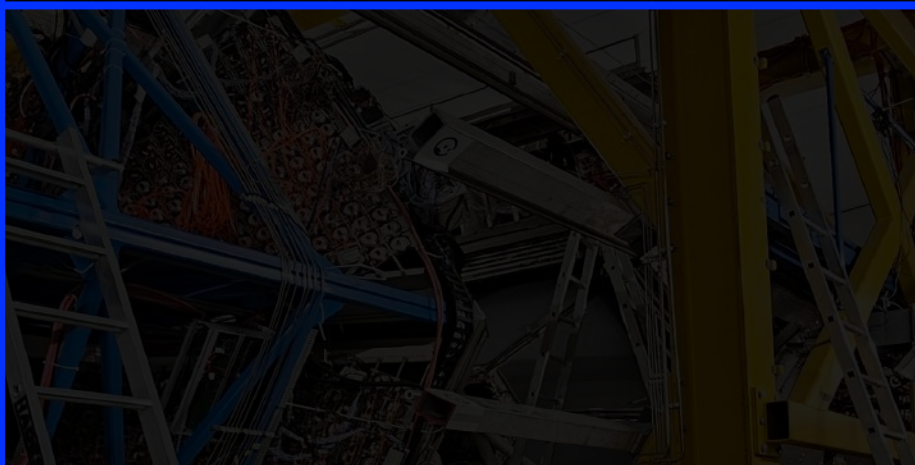
$$\tan\theta_1 \times \tan\theta_2 = \frac{1}{\gamma_{CM}^2}$$



$M_{p\pi^+}^2$ vs t_2



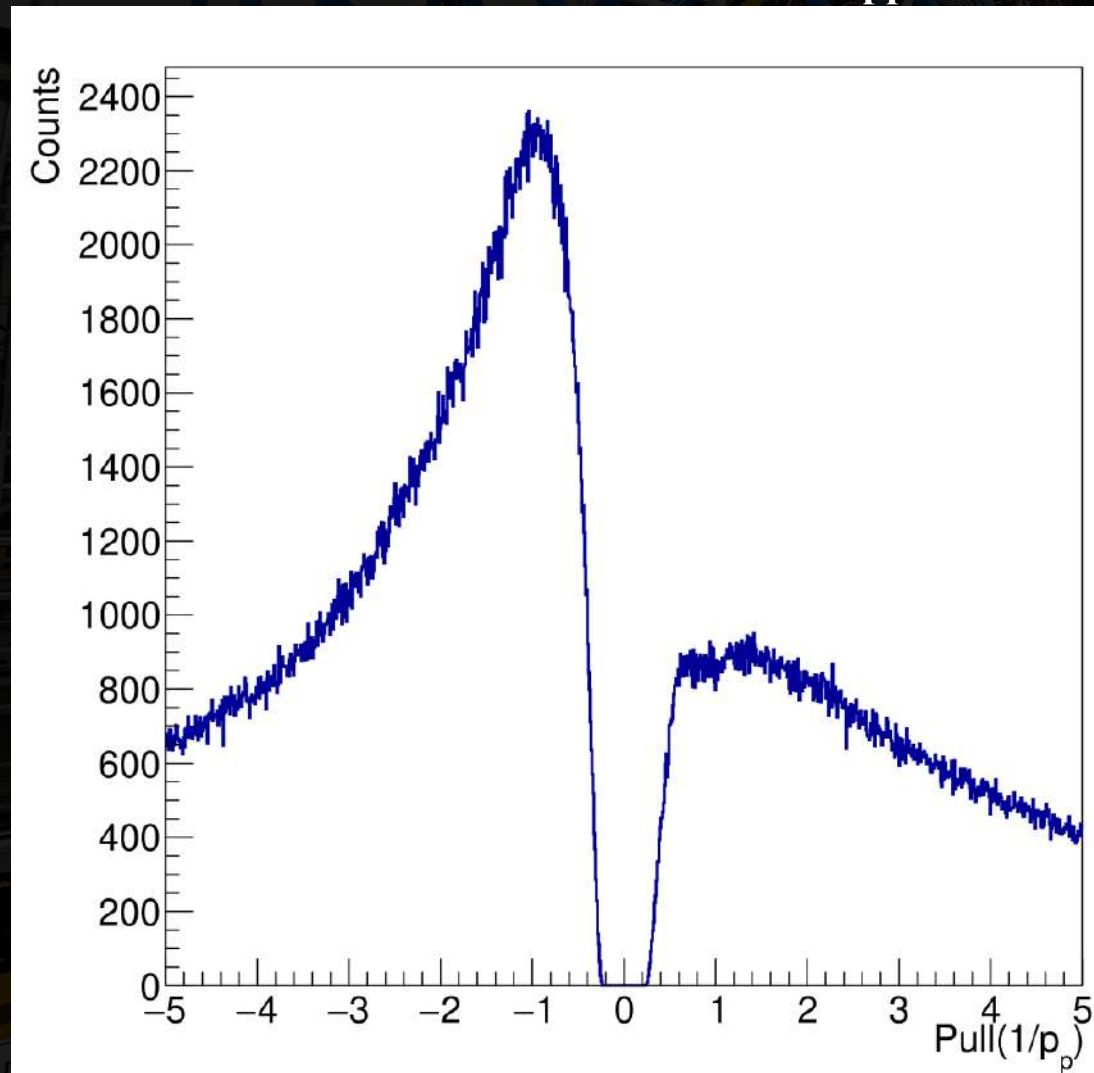
Y projection



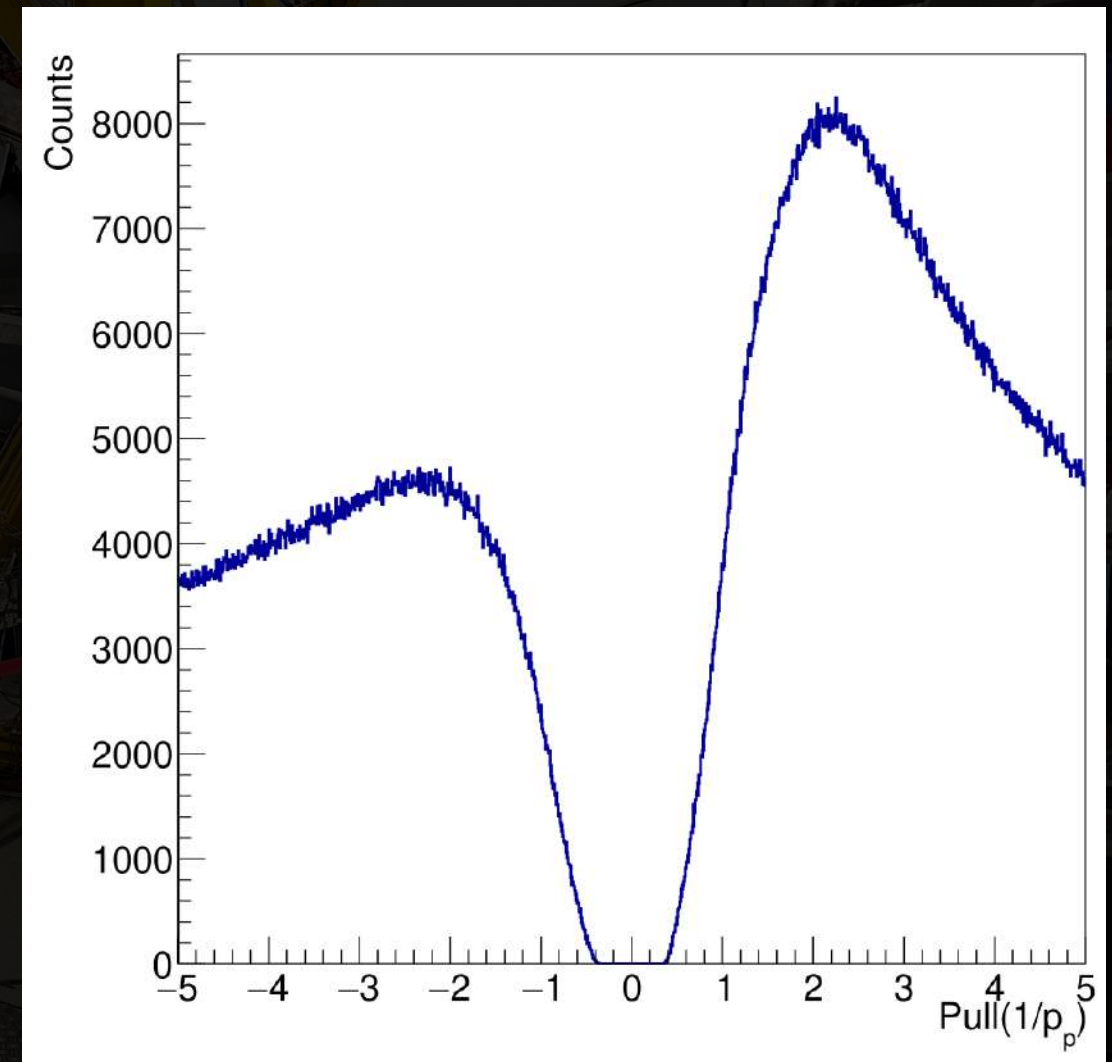
X projection

Kinfit Missing Mass Constraint

Can be thought as the 1C fit is shrinking the momentum of lower sideband to lower values and stretching the momentum of the upper sideband to higher values.



lower sideband



upper sideband