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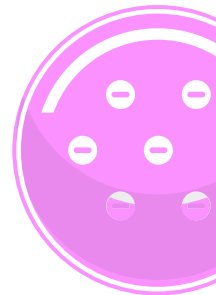
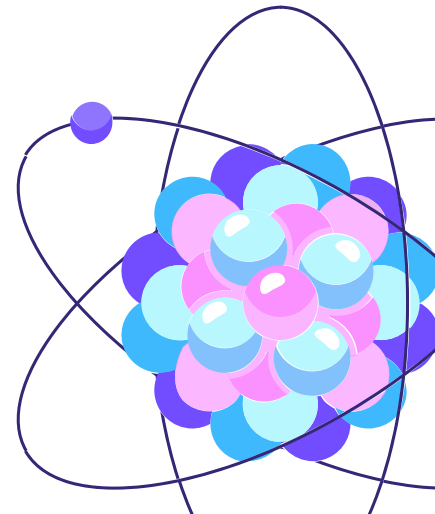
Ciencia y Tecnología

Secretaría de Ciencia, Humanidades, Tecnología e Innovación

Heavy-Light Pseudoscalar Mesons: Structure and Parton Distributions

PhD. Bilgai Almeida-Zamora

Pablo de Olavide University, Spain



1970: Quantum Chromodynamics

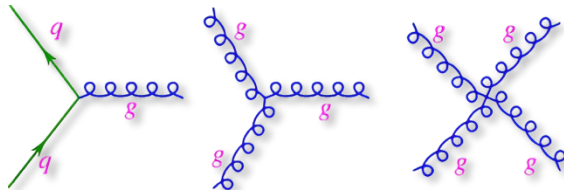
- QCD is a non-Abelian gauge theory with SU(3) color symmetry that describes the strong interaction.

- **Quarks**

Six flavors: up, down, charm, strange, top, bottom
Each quark carries color charge (red, blue, green)

- **Gluons**

Eight gauge fields mediate the interaction
They also carry color charge (self-interactions)



	I	II	III		
mass	$\approx 2.16 \text{ MeV}/c^2$	$\approx 1.273 \text{ GeV}/c^2$	$\approx 172.57 \text{ GeV}/c^2$	0	$\approx 125.2 \text{ GeV}/c^2$
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
	u up	c charm	t top	g gluon	H higgs
	$\approx 4.7 \text{ MeV}/c^2$	$\approx 93.5 \text{ MeV}/c^2$	$\approx 4,183 \text{ GeV}/c^2$	0	
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	d down	s strange	b bottom	γ photon	
	$\approx 0.511 \text{ MeV}/c^2$	$\approx 105.66 \text{ MeV}/c^2$	$\approx 1,77693 \text{ GeV}/c^2$	$\approx 91.188 \text{ GeV}/c^2$	
	-1	-1	-1	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	e electron	μ muon	τ tau	Z Z boson	
	$< 0.8 \text{ eV}/c^2$	$< 0.17 \text{ MeV}/c^2$	$< 18.2 \text{ MeV}/c^2$	$\approx 80.3692 \text{ GeV}/c^2$	
	0	0	0	± 1	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	

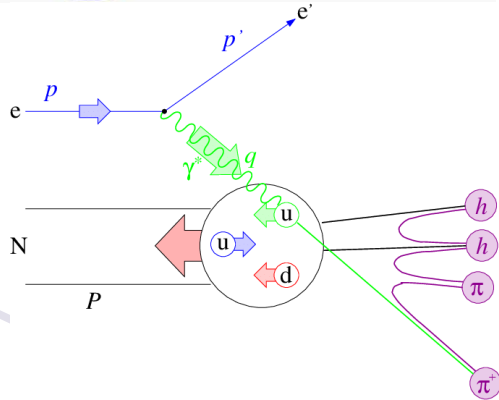
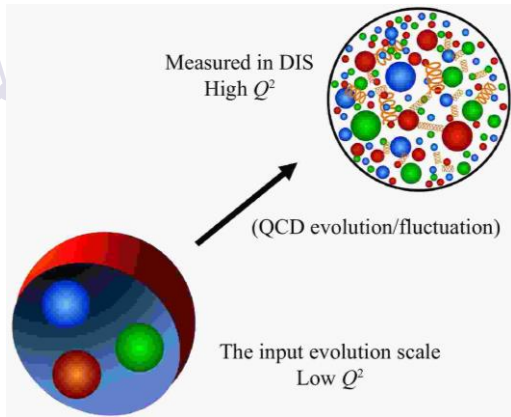
QUARKS

LEPTONS

GAUGE BOSONS
VECTOR BOSONS

SCALAR BOSONS

The Central Problem of QCD

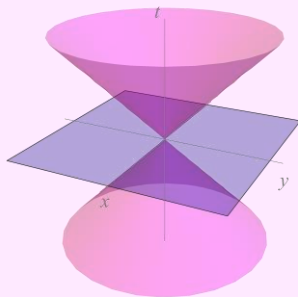


- QCD is highly nonperturbative at low energies.
- Understanding hadron structure from quarks and gluons
 - major challenge.
- Lepton–nucleon DIS provides direct access to quarks and gluons.
- Nonperturbative distributions are required.
- Processes are described in terms of hadron light-front wave functions.
- Phenomenological tools: PDFs, FFs, and GPDs.

CANONICAL QUANTIZATION

Quantum field theory (QFT) provides a quantum-mechanical description of a physical system in four-dimensional Minkowski spacetime

$$g_{\mu\nu} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$



With canonical coordinates:

$$x^\mu = (x^0, x^1, x^2, x^3) = (t, \mathbf{x})$$

$\psi(t, \mathbf{x})$ evolves along the time direction and is solved by fixing boundary conditions $\psi(t_0, \mathbf{x}_0)$ on a spacelike hypersurface at fixed time $t = 0$.

$$i \frac{\partial}{\partial t} \psi(t, \mathbf{x}) = P_0 \psi(t, \mathbf{x})$$

LIGHT-FRONT QUANTIZATION

- The concepts of “time” and “space” are arbitrary.
- A new parameterization of spacetime is introduced through generalized coordinates.

• **Front form:**

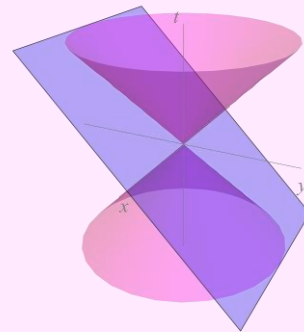
$$x^+ = \frac{1}{\sqrt{2}}(x^0 + x^3), \quad x^- = \frac{1}{\sqrt{2}}(x^0 - x^3), \quad \mathbf{x}_\perp = (x^1, x^2)$$

Light-cone time

Light-cone space

The new metric is:

$$g_{\mu\nu} = \begin{pmatrix} 0 & 0 & 0 & \frac{1}{2} \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ \frac{1}{2} & 0 & 0 & 0 \end{pmatrix}$$

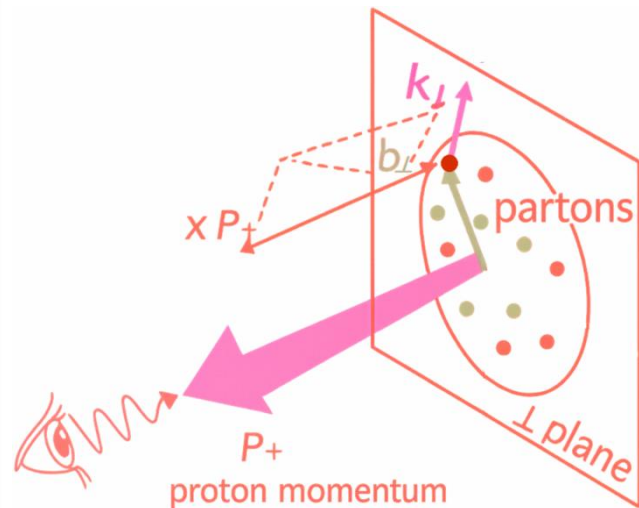


Light-front wave function

In the light-cone Fock decomposition, a pion with momentum $P = (P^+, P_\perp)$ is described by

$$|\pi : P\rangle = \sum_{n, \lambda_i} \int \prod_i \frac{dx_i d^2 \vec{k}_{\perp i}}{\sqrt{x_i} 16\pi^3} \left| n : x_i P^+, x_i \vec{P}_\perp + \vec{k}_{\perp i}, \lambda_i \right\rangle \psi_{n/\pi}(x_i, \vec{k}_{\perp i}, \lambda_i)$$

- $\psi(x_i, k_{\perp i}, \lambda_i)$ is the light-front wave function.
- $x_i = k_i^+/P^+$ is the longitudinal momentum fraction carried by the i th parton.
- k_i^+ is the longitudinal momentum.
- $k_{\perp i} = p_{\perp i} - x_i P_\perp$ is the transverse momentum relative to the meson direction.
- λ_i is the light-front helicity of the i th parton.



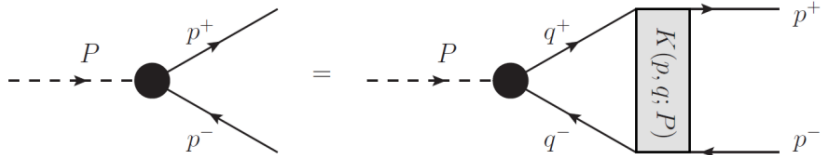
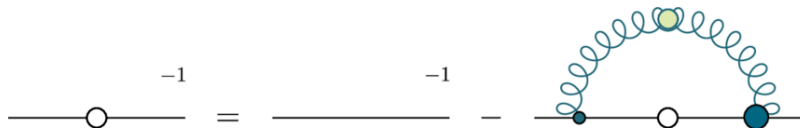
$\psi(x_i, k_\perp, \lambda_i)$ is the probability amplitude for finding partons (quarks and gluons) with momenta k^+ and $p_\perp$ inside a hadron with momentum P^+ and transverse momentum $P_\perp$.

Light-front wave function

$$\psi_M^q(x, k_\perp^2) = \text{Tr} \int \frac{d^2 k_\parallel}{\pi} \delta(n \cdot k - x n \cdot P) \gamma_5 \gamma \cdot n \chi_M(k_-, P)$$

Bethe-Salpeter wave function

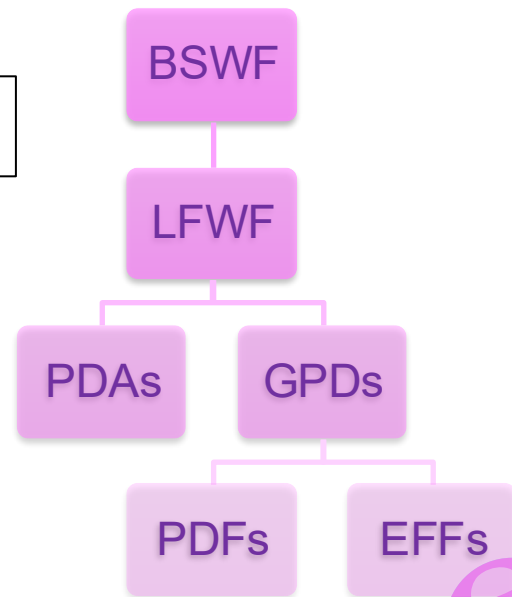
$$S_q(k) \Gamma_M(k_-, P) S_{\bar{h}}(k - P)$$



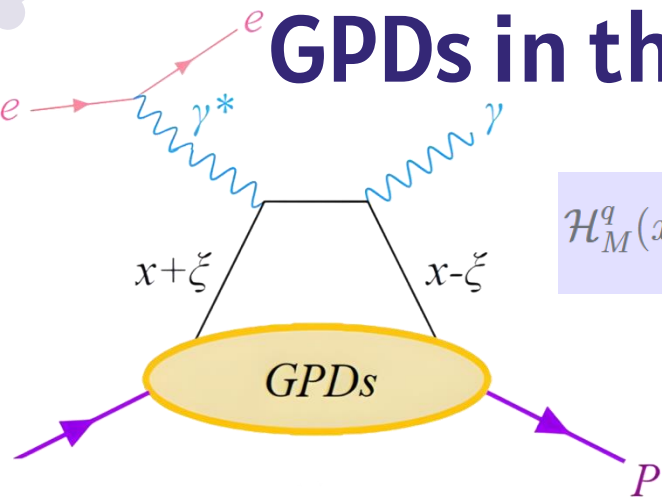
Inputs:
Solutions from
quark DSE
and meson BSE

Idea:

Compute **everything**
from the **LFWF**.

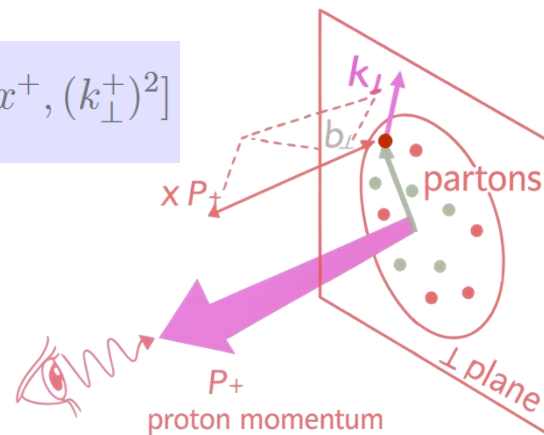


GPDs in the Light-Front Formalism



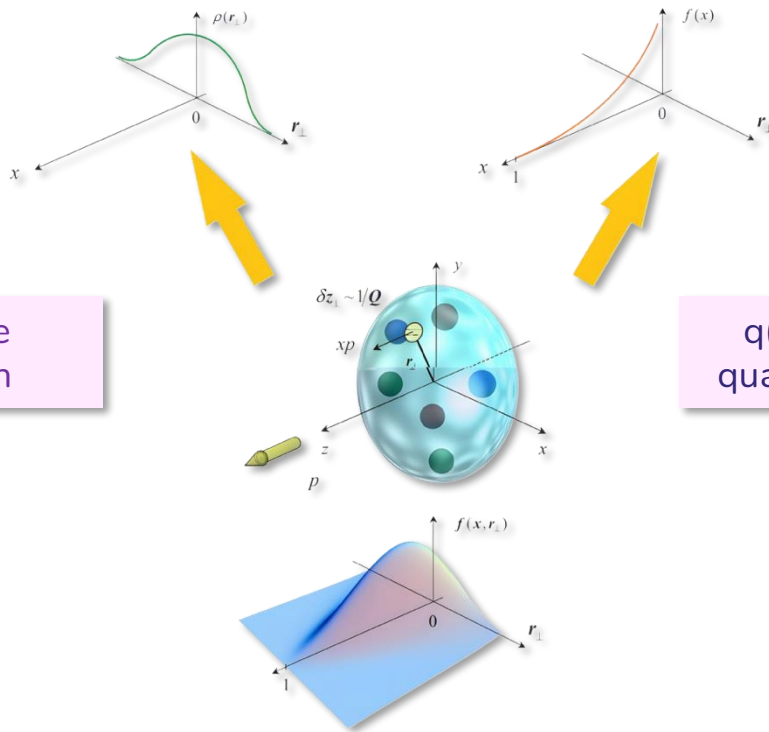
$$\mathcal{H}_M^q(x, \xi, t) = \int dk_{\perp} \psi_M^{q*}[x^-, (k_{\perp}^-)^2] \psi_M^q[x^+, (k_{\perp}^+)^2]$$

- ψ are the parton LFWFs in the hadronic state.
- x_i and $k_{\perp i}$ are the partons' longitudinal and transverse momentum variables.
- ξ is the skewness.
- $t = \Delta^2$ is the momentum transfer.



Probability amplitude for finding a parton at a given position in the transverse plane carrying a fraction x of the hadron momentum

Generalized Parton Distributions

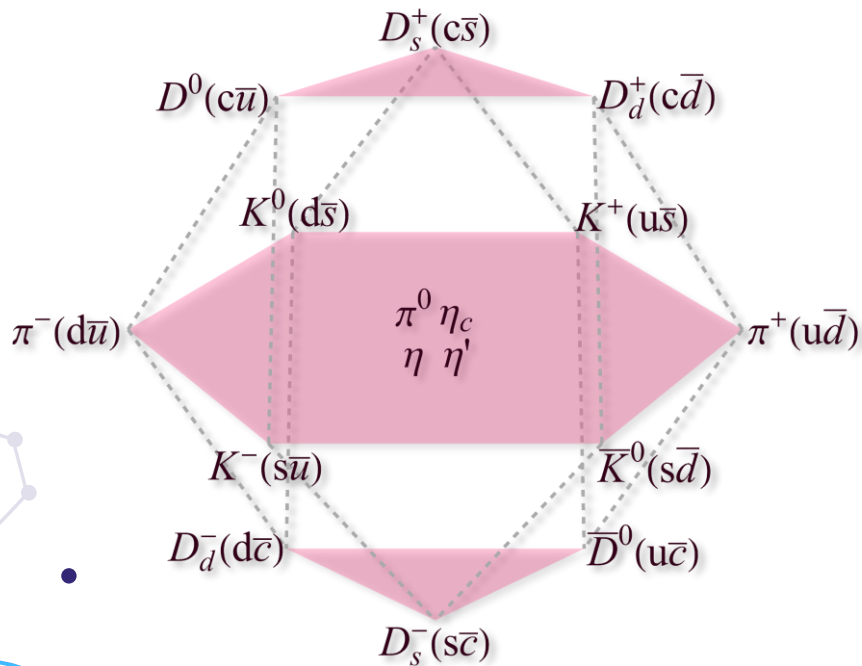


$F(t) \Rightarrow$ encode the charge distribution in the hadron

$q(x) \Rightarrow$ probability of finding a quark with momentum fraction x

$H(x, \xi, t) \Rightarrow$ unify PDFs and FFs

Pseudoscalar Mesons

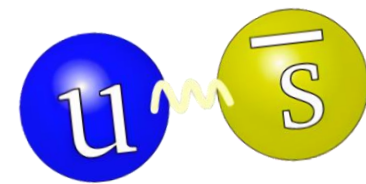


- Mesons with spin 0
- **Negative parity ($J^P = 0^-$)**
- Composed of a quark and an antiquark
- Composed of light (u, d, s) and heavy (c, b) quarks.
- **Relevance to internal structure:** all allow us to explore PDFs, FFs, and GPDs, although heavy mesons exhibit more pronounced momentum asymmetries.

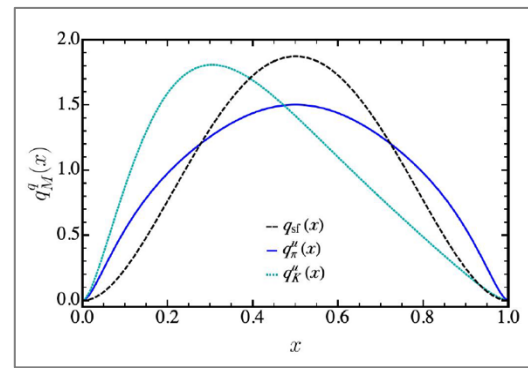


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Pion and Kaon



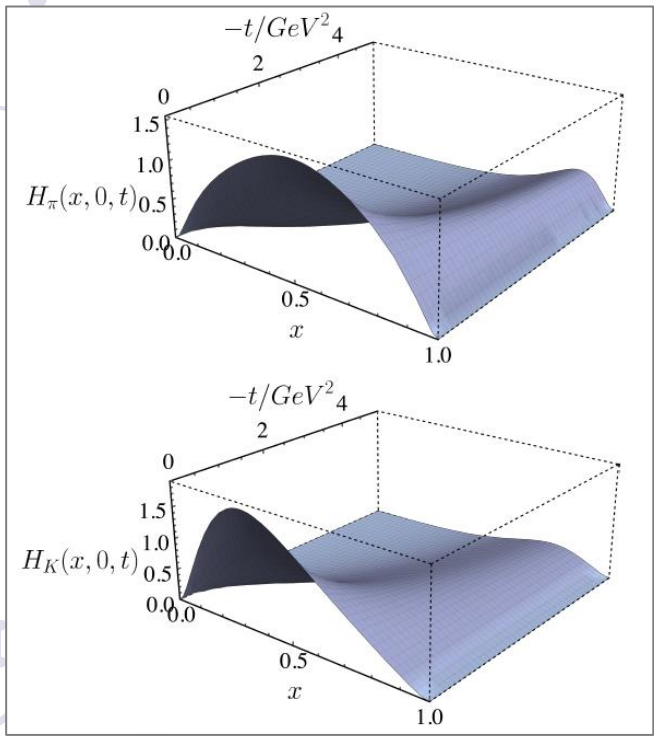
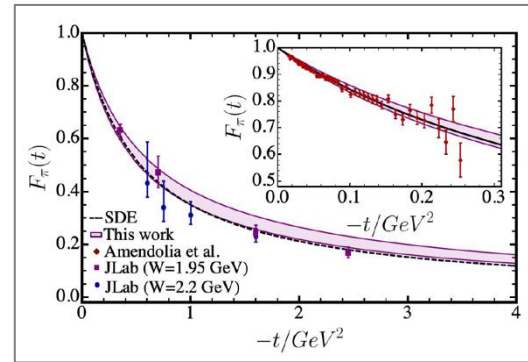
Forward limit:
 $\xi = 0, t = 0$
 PDF



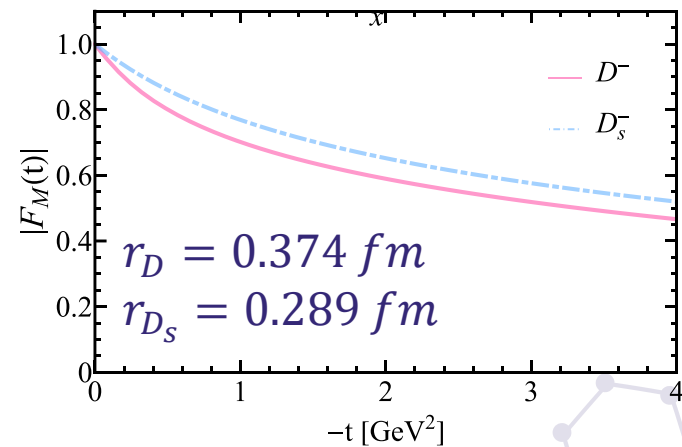
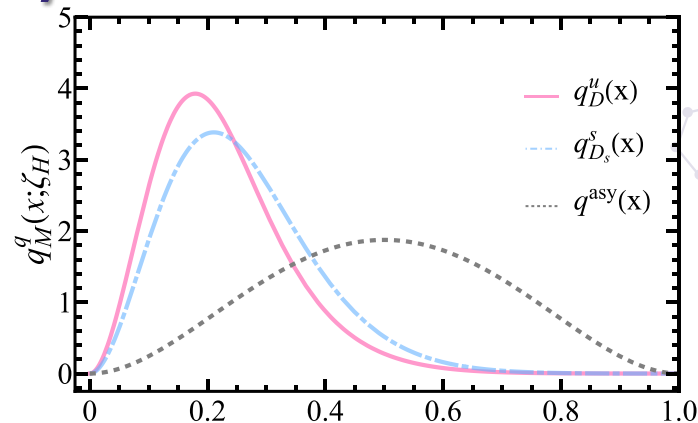
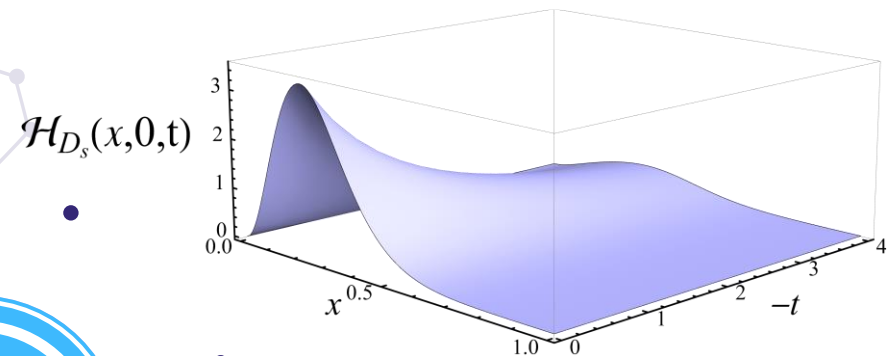
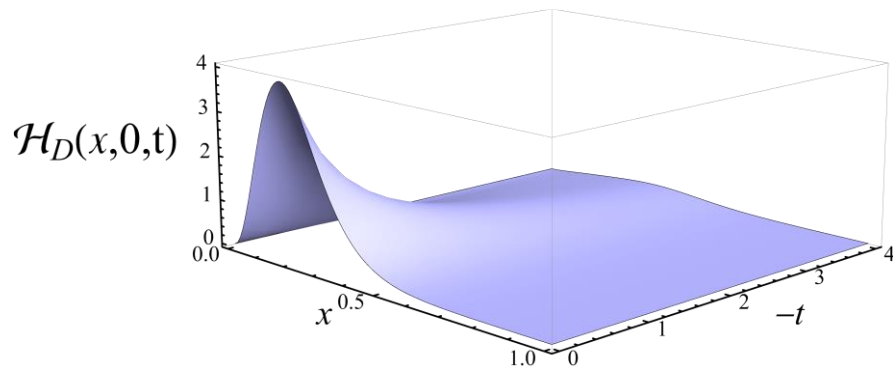
Zeroth moment:
 (integral over x)
 EFFs

$$r_\pi = 0.660 \text{ fm}$$

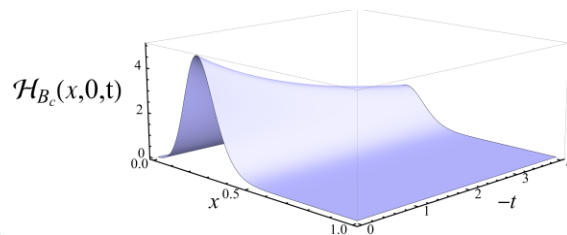
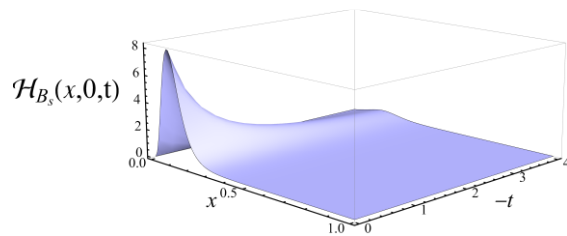
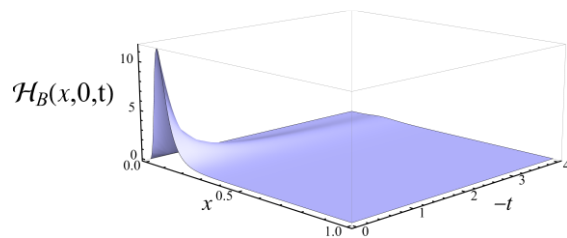
$$r_K = 0.560 \text{ fm}$$



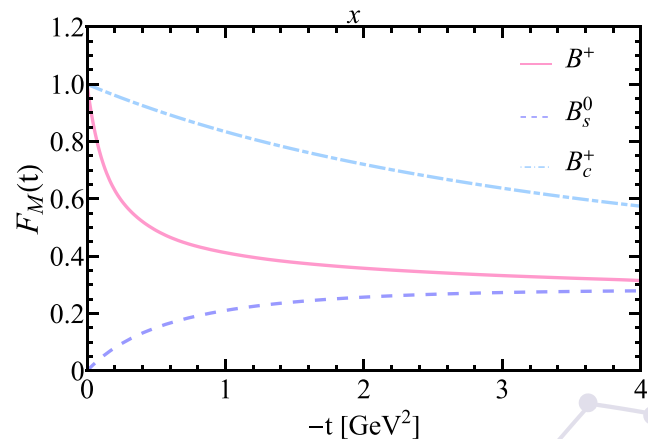
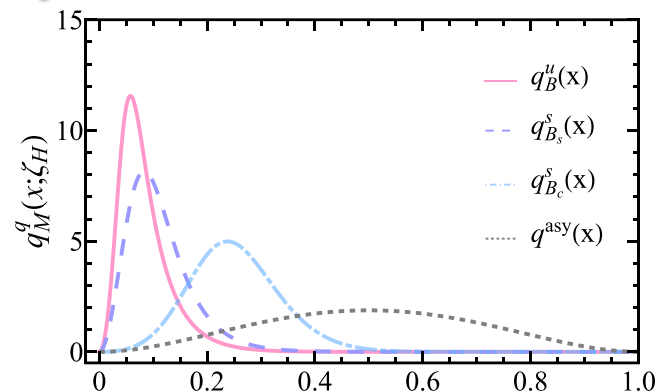
D Mesons: GPDs, PDFs, and EFFs



B Mesons: GPDs, PDFs, and EFFs



$$\begin{aligned} r_B &= 0.478 \text{ fm} \\ r_{B_s} &= 0.264 \text{ fm} \\ r_{B_c} &= 0.217 \text{ fm} \end{aligned}$$



Charge radii: Comparison with Other

		D^-	D_s^-	B^+	B_s^0	B_c^+
$ r_{0-} $		0.374	0.289	0.478	0.264	0.217
Covariant CQM	[97]	0.505	0.377	–	–	–
PM	[98]	–	0.460	0.730	0.460	–
LFQM	[99]	0.429	0.352	0.615	0.345	0.208
CI	[100]	–	0.260	0.340	0.240	0.170
Lattice	[101]	0.450(24)	0.465(57)	–	–	–
Lattice	[102]	0.390(33)	–	–	–	–

- Our predictions follow the general trends obtained with other theoretical approaches.
- A similar hierarchy is observed: $r_D > r_{D_s}$ and $r_B > r_{B_s} > r_{B_c}$.

Summary

- Hadron structure is governed by nonperturbative QCD dynamics.
- The light-front formalism provides a natural framework to describe the internal structure of hadrons.
- Light-front wave functions give access to different observables, such as PDFs, GPDs and electromagnetic form factors.
- GPDs connect information on the longitudinal momentum and spatial distribution of partons.
- Heavy-light pseudoscalar mesons exhibit strong momentum asymmetries due to the large difference between the quark masses.
- Within each meson family, heavier quark content leads to smaller charge radii.
- These results follow the same general trends found in other theoretical approaches.

Thank you.

