

EMERGENT HADRON MASS



ECT*
EUROPEAN CENTRE
FOR THEORETICAL STUDIES
IN NUCLEAR PHYSICS AND RELATED AREAS
FONDAZIONE BRUNO KESSLER

and PION/KAON/NUCLEON FORM FACTORS

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ECT* - FONDAZIONE BRUNO KESSLER



NSTAR 2026

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QCD

(classical)

LAGRANGIAN

$$\mathcal{L}_{\text{QCD}} = \sum_{j=u,s,d,\dots} \bar{q}_j \left[\gamma_\mu D_\mu + m_j \right] q_j + \frac{1}{4} G_{\mu\nu}^a G_{\mu\nu}^a$$
$$D_\mu = \partial_\mu + ig \frac{1}{2} \lambda^a A_\mu^a$$
$$G_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + gf^{abc} A_\mu^b A_\nu^c$$

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GLUON SELF-INTERACTION

pure-gluon QCD displays a
mass gap

$$m_g \sim 0.5 \text{ GeV}$$

Cornwall, PRD 26 (1982)

GAUGE SYMMETRY IS FINE

2-point STI can be still satisfied with

$$\Delta_{\mu\nu}(q) = \frac{P_{\mu\nu}(q)}{q^2[1 + \Pi(q^2)]}, \quad q^\mu P_{\mu\nu}(q) = 0$$

$$\lim_{q^2 \rightarrow 0} q^2 \Pi(q^2) = m_g$$

(“only” requires the presence of
longitudinally coupled massless poles)

Schwinger, PR 125 and 128 (1962)

STRESS-ENERGY TENSOR IS ANOMALOUS

$$T_{\mu\mu} = \frac{\beta}{4} G_{\mu\nu}^a G_{\mu\nu}^a$$

but no size prescribed...

QCD

LAGRANGIAN

$$\mathcal{L}_{\text{QCD}} = \sum_{j=u,s,d,\dots} \bar{q}_j \left[\gamma_\mu D_\mu + m_j \right] q_j + \frac{1}{4} G_{\mu\nu}^a G_{\mu\nu}^a + \underbrace{\frac{1}{2\xi} (\partial_\mu A_\mu^a)^2}_{\text{(linear) gauge fixing}} + \underbrace{\partial_\mu \bar{c}^a \partial_\mu c^a + g f^{abc} (\partial_\mu \bar{c}^a) A_\mu^b c^c}_{\text{Faddeev-Popov ghost term}}$$
$$D_\mu = \partial_\mu + ig \frac{1}{2} \lambda^a A_\mu^a$$
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QCD LAGRANGIAN

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(linear) gauge fixing Faddeev-Popov ghost term

$$D_\mu = \partial_\mu + ig \frac{1}{2} \lambda^a A_\mu^a$$
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1 RGI MASSES

40 years+ non-perturbative methods uncover the size of
the gluon mass

$$m_g = 0.43(1) \text{ GeV}$$

Aguilar et al., EP

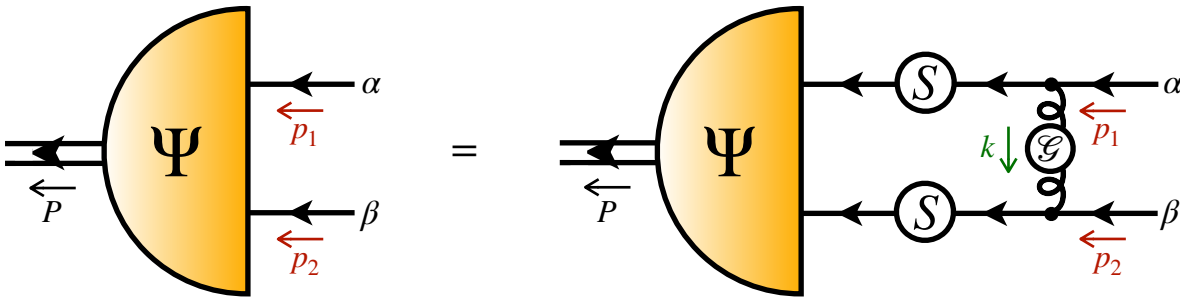
π/K

ELECTROMAGNETIC

FORM FACTORS

Yao, DB, Roberts, PLB 855 (2024)

BETHE-SALPETER
EQUATION

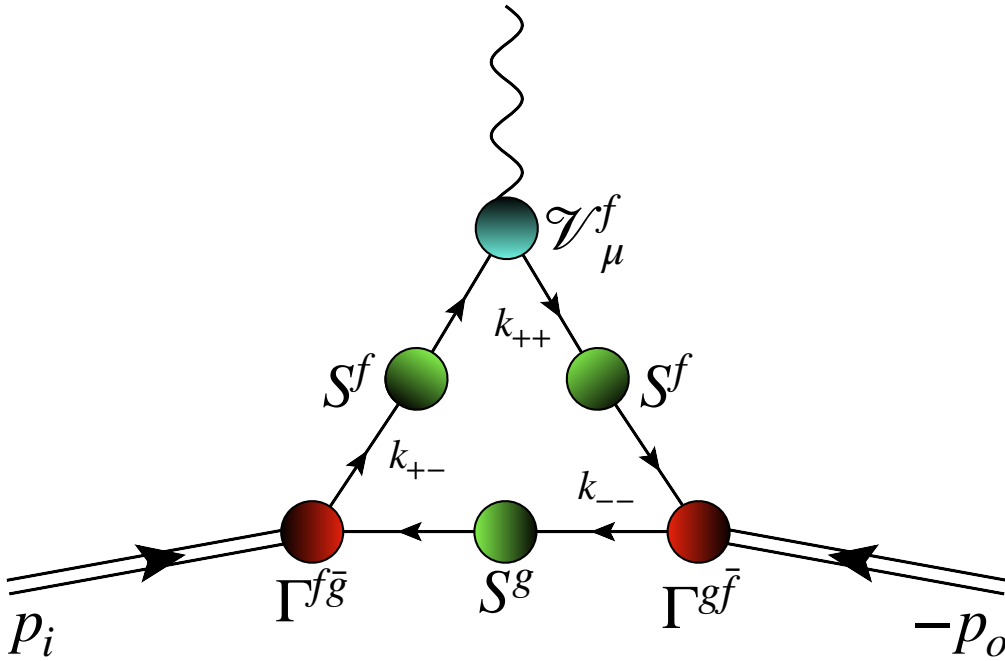


dressed-quark propagators singularities
limit mass of bound-state

singularities move in the complex k^2 domain
sampled by the bound-state equations

Q^2_{max}

TRIANGULAR DIAGRAM



SPM INTERPOLATION

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