

# Relaxing Lyman- $\alpha$ bounds by self-cooling Dark Sectors

Stefan Lederer

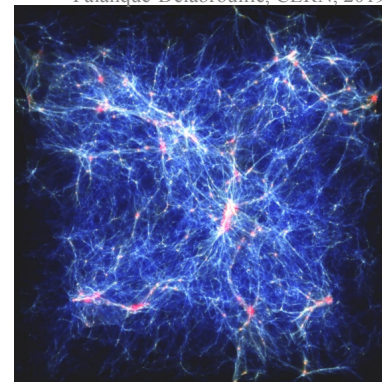
Collaborators:

Andrzej Hryczuk, Esau Cervantes

[publication in preparation]

# Lyman- $\alpha$ constraints on light Dark Matter

Palanque-Delabrouille, CERN, 2019



- Lyman- $\alpha$  observations dictate an upper bound on the free-streaming scale of dark matter.
- “Warm Dark Matter” hydro-simulations:

$$m_{\text{WDM}}^{\text{Ly-}\alpha} \geq \mathbf{5.3 \text{ keV}} \quad [\text{J. Lesgourgues et al., 2020}]$$

(1.6 keV for conservative estimates) [A. Boyarsky et al., 2020]

These bounds must be **carefully translated** for other DM models!

→ e.g.: map  $f_\chi(p, T)$  to WDM via its **velocity dispersion**:

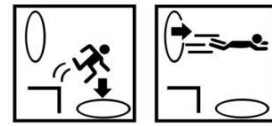
$$m_\chi^{\text{Ly-}\alpha} \sim m_{\text{WDM}}^{\text{Ly-}\alpha} \times \sqrt{\langle p_\chi^2 \rangle} \sim \sqrt{\frac{1}{n_\chi}} \times \int p^2 f_\chi(p)$$

more sophisticated methods exist:

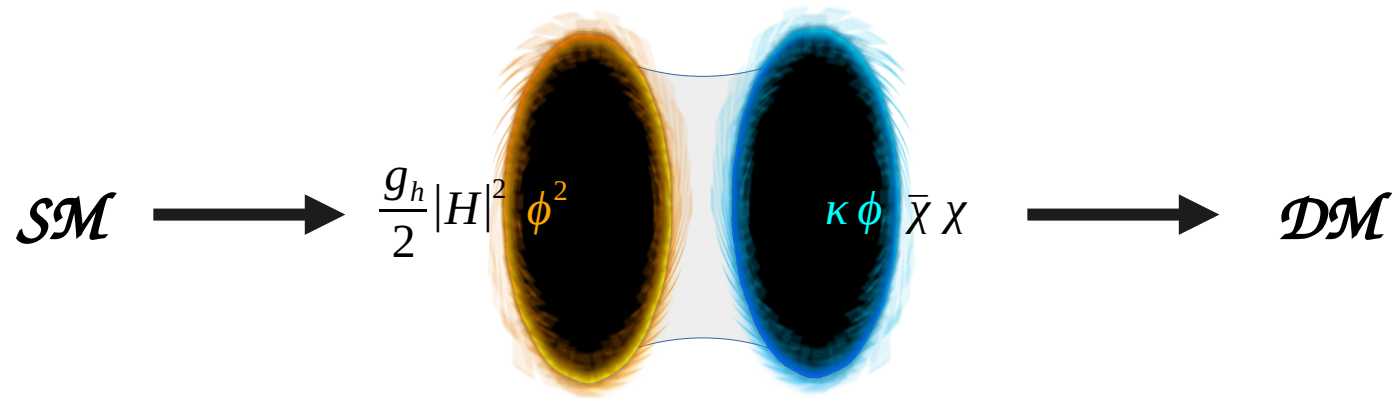
| Probe           | NCDM test                                 | $m_{\text{FI}}^{\text{lim}}$ [keV] | $m_{\text{SW}}^{\text{lim}}$ [keV] |
|-----------------|-------------------------------------------|------------------------------------|------------------------------------|
| Lyman- $\alpha$ | Velocity dispersion, Sec. 3.1.1           | 16                                 | 3.8                                |
|                 | Fits to transfer function, see Sec. 3.1.2 | 15                                 | 3.9                                |
|                 | Area criterion, see Sec. 3.1.3            | 15                                 | 3.8                                |

[Heisig et al., 2021]

# Simple Scalar Toy Model

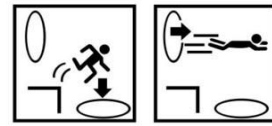


$$\mathcal{L} \supset \frac{g_h}{2} |H|^2 \phi^2 + \kappa \phi \bar{\chi} \chi$$

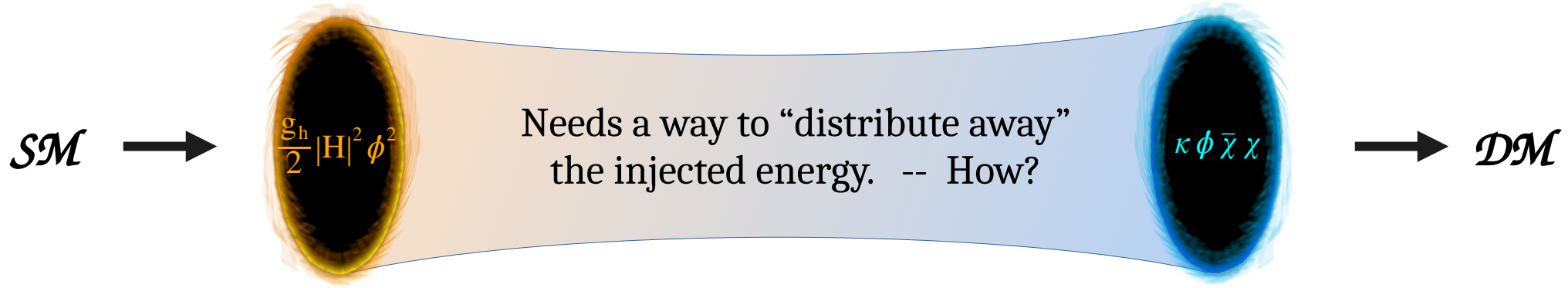


**Problem:** (co-moving) momentum conservation

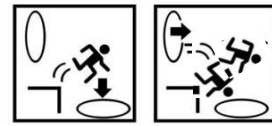
# Simple Scalar Toy Model



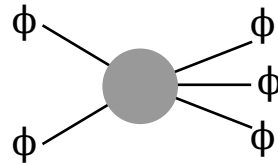
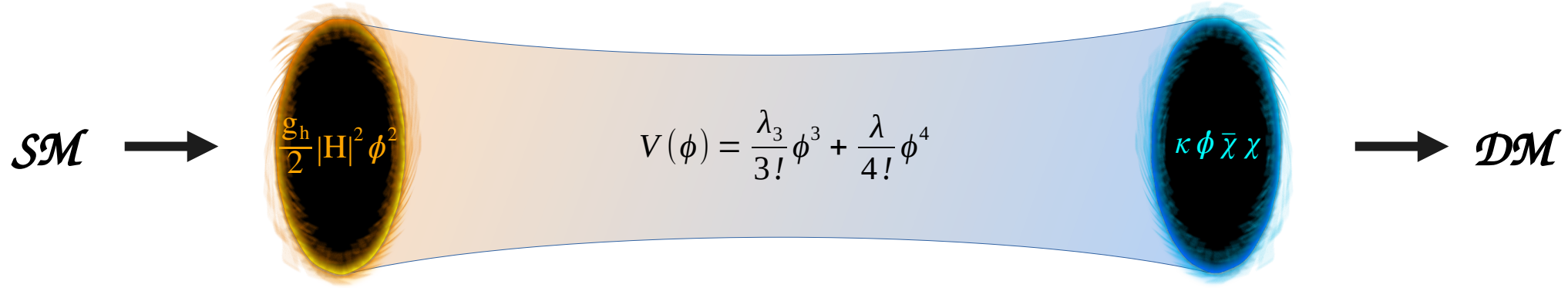
$$\mathcal{L} \supset \frac{g_h}{2} |H|^2 \phi^2 + \kappa \phi \bar{\chi} \chi$$



# Simple Scalar Toy Model



$$\mathcal{L} \supset \frac{g_h}{2} |H|^2 \phi^2 + \frac{\lambda_3}{3!} \phi^3 + \frac{\lambda}{4!} \phi^4 + \kappa \phi \bar{\chi} \chi$$



$\rightarrow$  2-to-3 translate kinetic energy to rest mass.

(reverse) “cannibal process”

# Boltzmann equations

- assume kinetic equilibrium:  $f_\phi(p, T_\phi) \sim e^{-\omega_p/T_\phi}$
- Solve coupled BME up to **second** moment:  $n_\phi(x)$  &  $T_\phi(x)$

Abundance  $Y=n/s$ :

$$x \text{ H } \frac{d Y_\phi}{d x} = + 2 \Gamma_{H \rightarrow \phi \phi} Y_H^{\text{eq}} + \langle \sigma v \rangle_{2 \rightarrow 3} s Y_\phi (Y_\phi - Y_\phi^{\text{eq}}) - \Gamma_{\phi \rightarrow \bar{\chi} \chi} Y_\phi$$

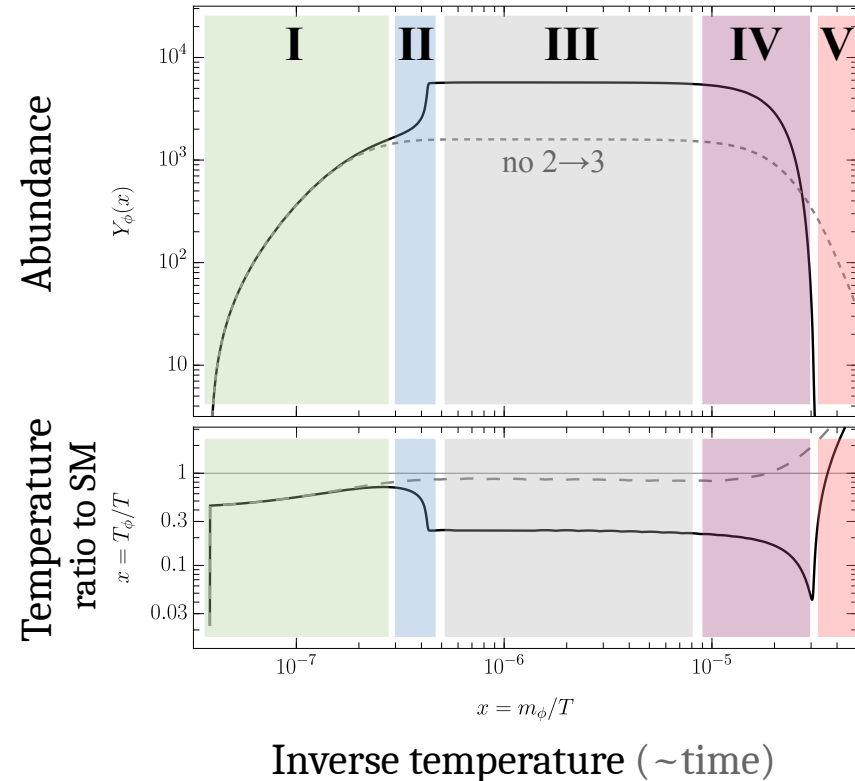
Temperature:

$$\frac{d T_\phi}{d x} = \dots$$

- Simplify model:  $\lambda_3 \sim \lambda^{1/2} \rightarrow (\sigma v)_{2 \rightarrow 3} \sim \lambda^3$

# Dark sector evolution

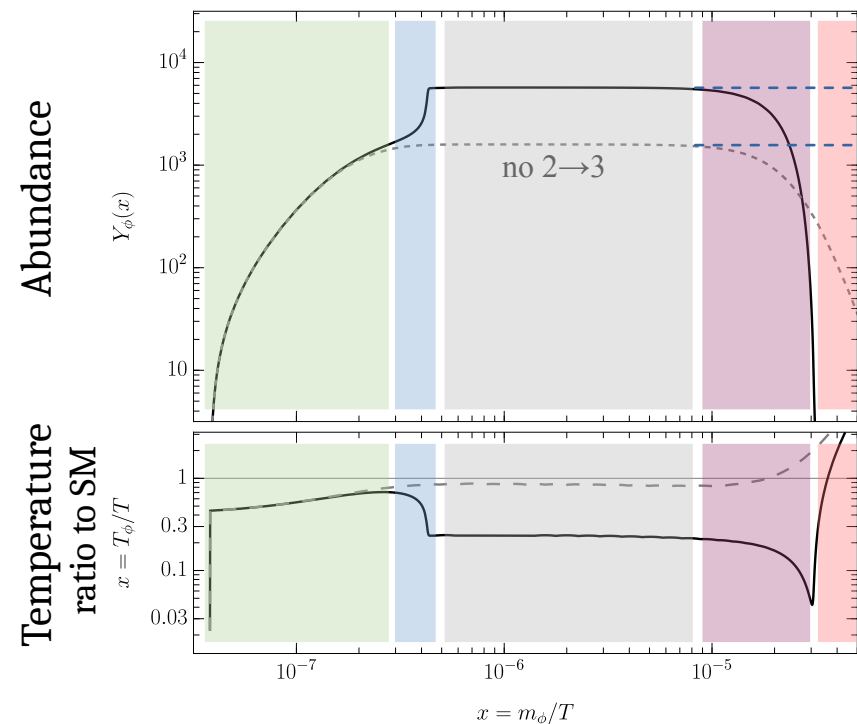
$$x H \frac{dY_\phi}{dx} = 2 \Gamma_{H \rightarrow \phi\phi} \times Y_H^{\text{eq}} + \langle \sigma v \rangle_{2 \rightarrow 3} s Y_\phi \times (Y_\phi - Y_\phi^{\text{eq}}) - \Gamma_{\phi \rightarrow \bar{\chi}\chi} \times Y_\phi$$



- I. Freeze-in
- II. Thermalization of  $\phi$
- III. (Redshifting in equilibrium)
- IV. Decay in thermal equilibrium
- V. Decay:
  - a) in kinetic equilibrium
  - b) after kinetic decoupling

# Dark sector evolution

$$x H \frac{dY_\phi}{dx} = 2 \Gamma_{H \rightarrow \phi\phi} Y_H^{\text{eq}} + \langle \sigma v \rangle_{2 \rightarrow 3} s Y_\phi (Y_\phi - Y_\phi^{\text{eq}}) - \Gamma_{\phi \rightarrow \bar{\chi}\chi} Y_\phi$$



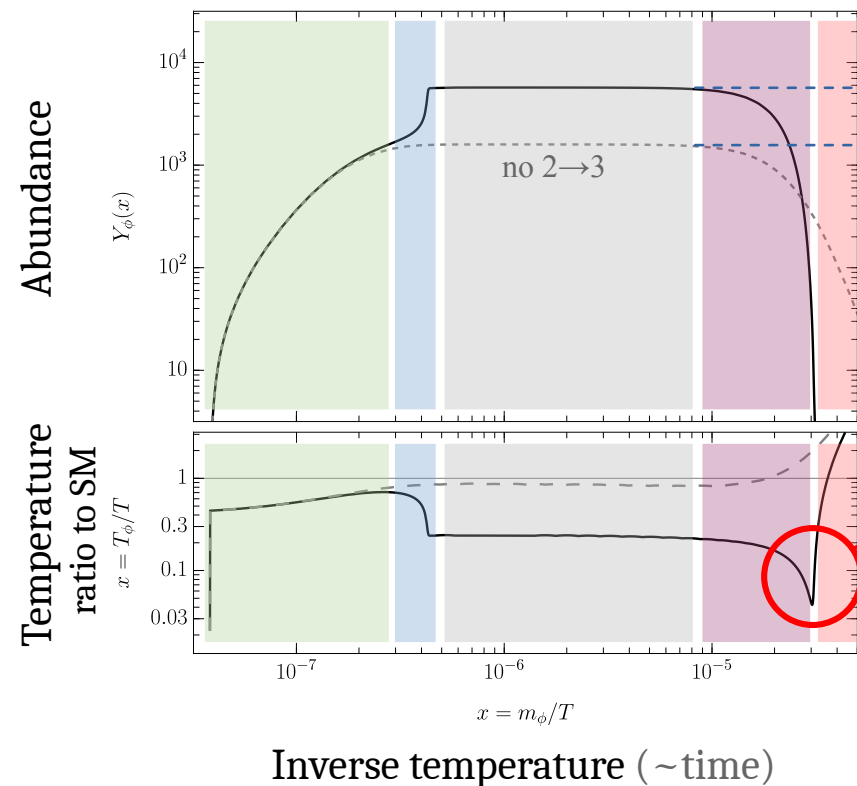
Change in abundance from self-thermalization:  $\sim g_h^{-1/2}$

$$\left. \begin{aligned} \rho^{\text{FI}} &= \rho^{\text{eq}} \\ n_\phi^{\text{eq}} \Big|_{T_\phi \gg m_\phi} &\approx \sqrt[4]{\pi^2 n_\phi^{\text{FI}} T_\phi^{\text{FI} 3}} \\ n_\phi^{\text{FI}} &\sim \Gamma_{h \rightarrow \phi\phi} \sim g_h^2 \\ T_\phi^{\text{FI}} &\approx T_\phi^{\text{FI}} \left( \frac{m_h}{m_\phi} \right) \end{aligned} \right\} n_\phi^{\text{FI}} / n_\phi^{\text{eq}} \sim \sqrt{g_h}$$

Inverse temperature ( $\sim$  time)

# Dark sector evolution

$$x H \frac{dY_\phi}{dx} = 2 \Gamma_{H \rightarrow \phi\phi} \times Y_H^{\text{eq}} + \langle \sigma v \rangle_{2 \leftrightarrow 3} s Y_\phi \times (Y_\phi - Y_\phi^{\text{eq}}) - \Gamma_{\phi \rightarrow \bar{\chi}\chi} \times Y_\phi$$



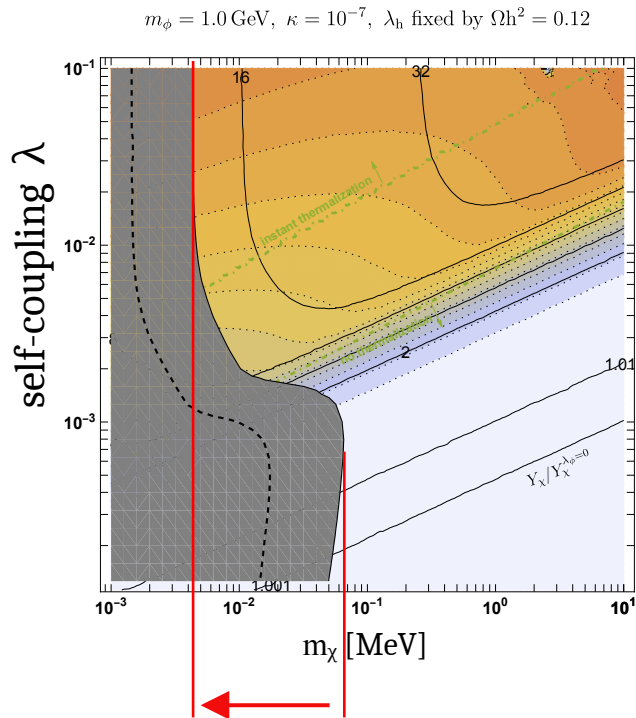
- Change in abundance from self-thermalization:  $\sim g_h^{-1/2}$
- Decay starts *during* efficient  $2 \leftrightarrow 3$ :  
decaying modes are rapidly replenished.  
→ strong secondary cooling.

# Lyman- $\alpha$ exclusion bounds



## procedure

- Pick mass-scale ( $m_\phi$ )
- Fix decay time ( $\kappa$ )
- match  $\Omega h^2 = 0.12$  ( $g_h$ )
- Plot Lyman- $\alpha$  exclusion bounds in  $\lambda$  and  $m_\chi$ .

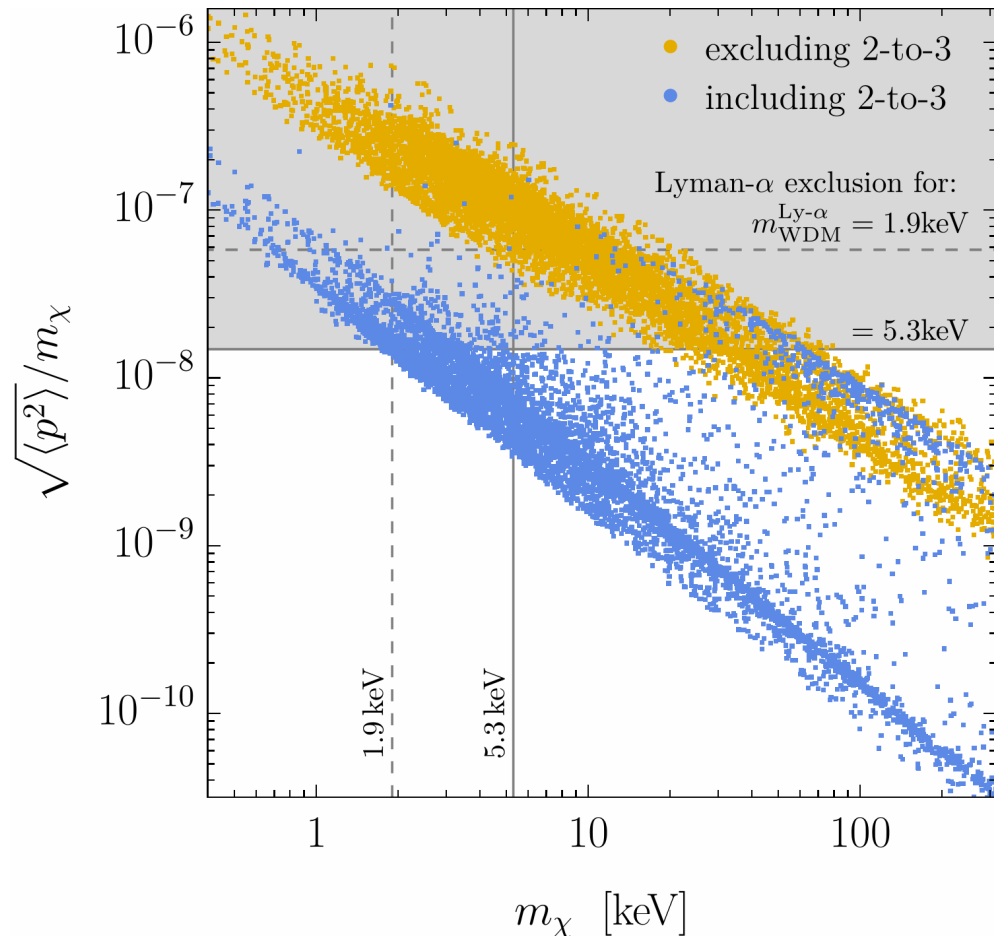


# Model Exploration via MCMC



MCMC results for 5D-scan (still ongoing)

- 2-to-3 reactions **included**
- 2-to-3 reactions **disregarded**
- **DS-Cooling** reduces  $\langle v_\chi^2 \rangle$  in a given model

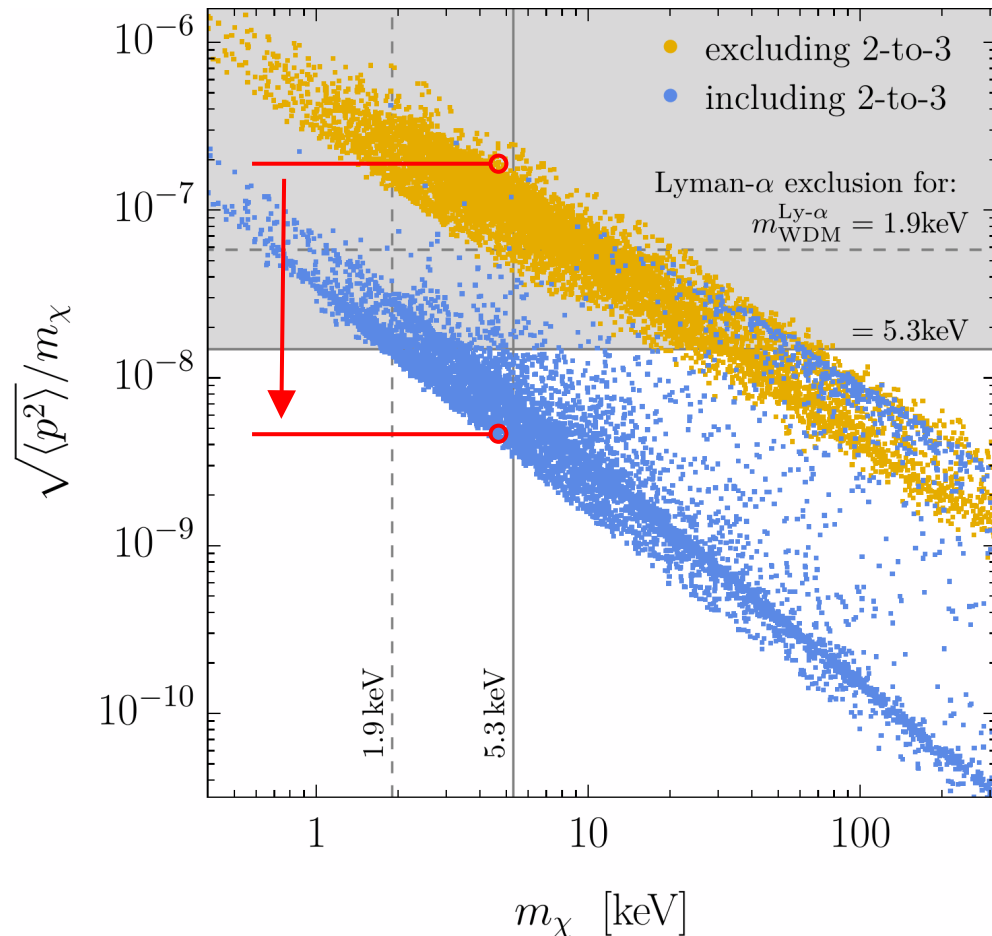


# Model Exploration via MCMC

preliminary

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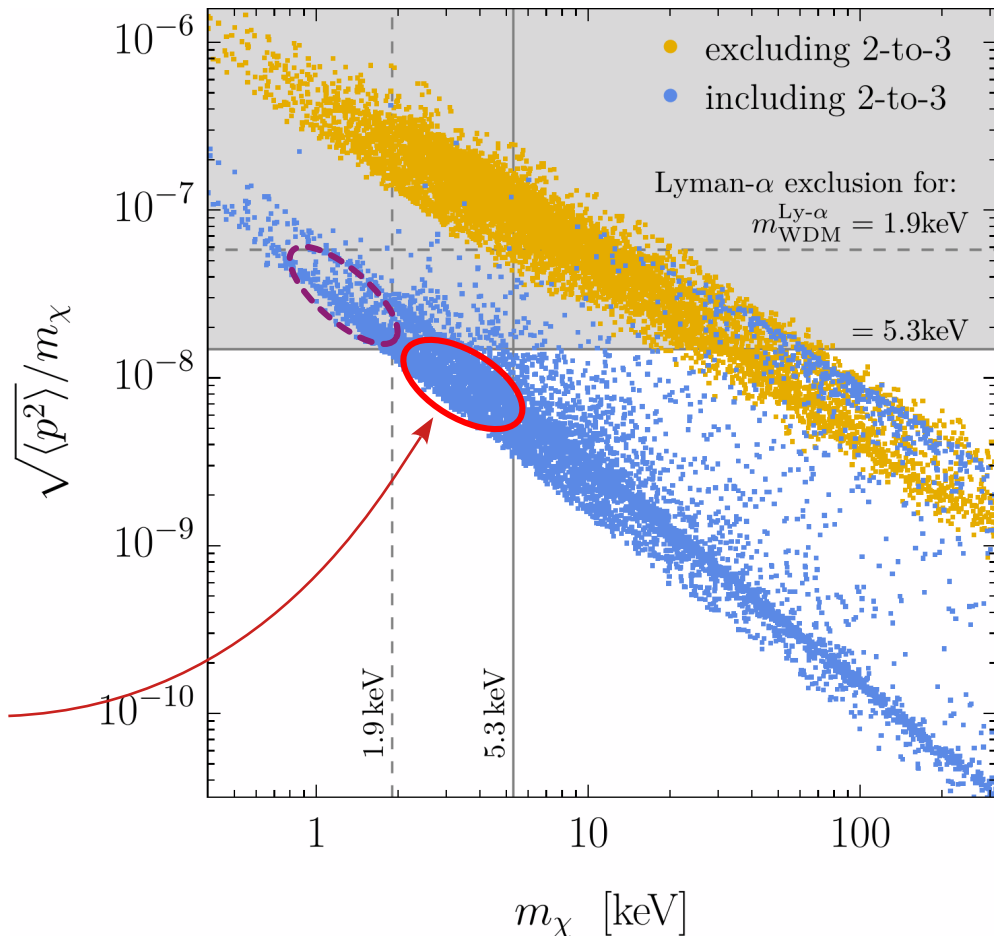
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**Models allowed but below the WDM limit.**

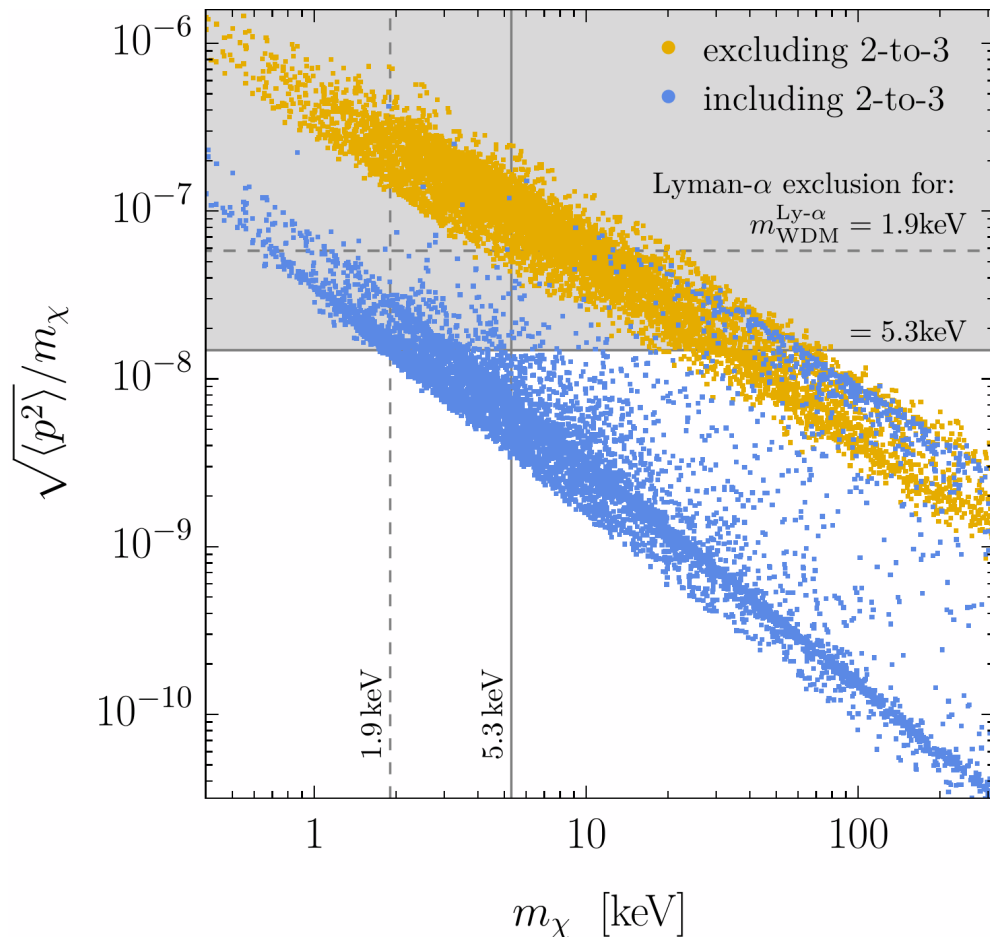


# Model Exploration via MCMC

preliminary

MCMC results for 5D-scan (still ongoing)

- 2-to-3 reactions **included**
- 2-to-3 reactions **disregarded**
- **DS-Cooling** reduces  $\langle v_\chi^2 \rangle$  in a given model
  - lowest  $m_\chi = \mathbf{1.7\text{keV}}$  ( $m_{\text{WDM}} = 5.3\text{keV}$ )
  - Lyman- $\alpha$  corrections as large as  $\mathbf{O(10^2)}$   
→ decay-cooling is also large!
  - Cooling present even at **low**  $\lambda \sim \mathbf{O(10^{-4})}$  !



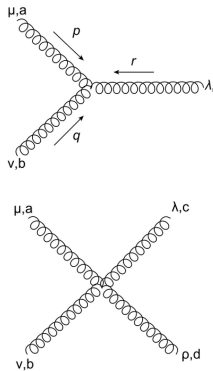
# Summary

## Already for the simplest toy model:

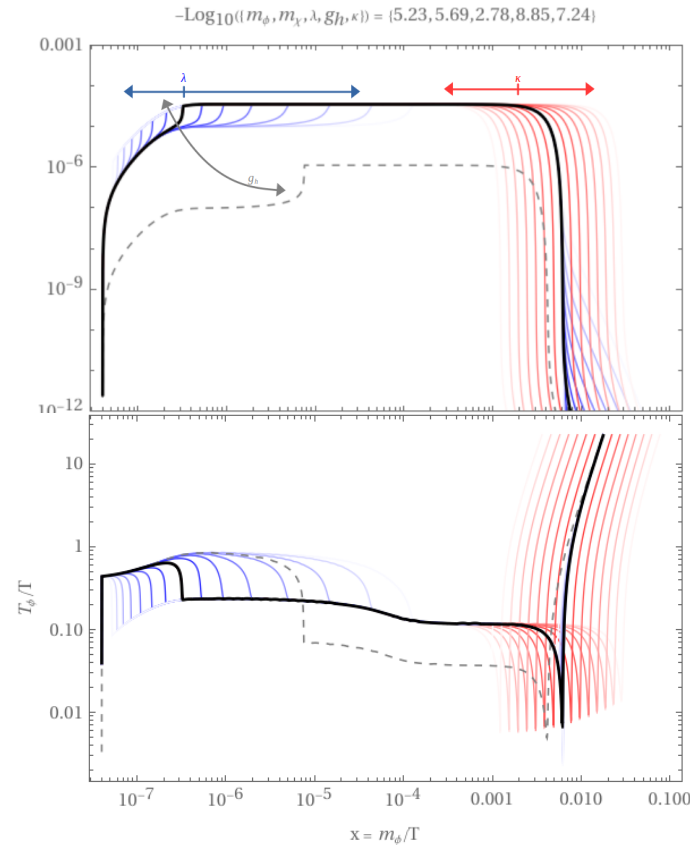
- Self-cooling non-thermal dark sectors allow for  $\mathbf{m_\chi \approx 1 keV}$ .
- Already for small self-interactions ( $\sim 10^{-2}$ ).
- Cooling during decay-onset important.

## Outlook:

- Mechanism also possible in (broken)  $\mathbf{SU(N)_d}$  models:  $\phi \rightarrow A_{\mu,a}$   
( $\rightarrow$  momentum dependent vertices. Qualitatively identical results)



# Parameter dependence of DS evolution



# Lyman- $\alpha$ -bounds shift vs. self-coupling

MCMC-scan of parameter space. (8240 points converged to  $\Omega h^2=0.12$ )

