

SEWM, HELSINKI, 20TH AUGUST 2026

PRECISE PREDICTIONS FOR COSMOLOGICAL PHASE TRANSITIONS

BOGUMIŁA ŚWIEŻEWSKA
UNIVERSITY OF WARSAW

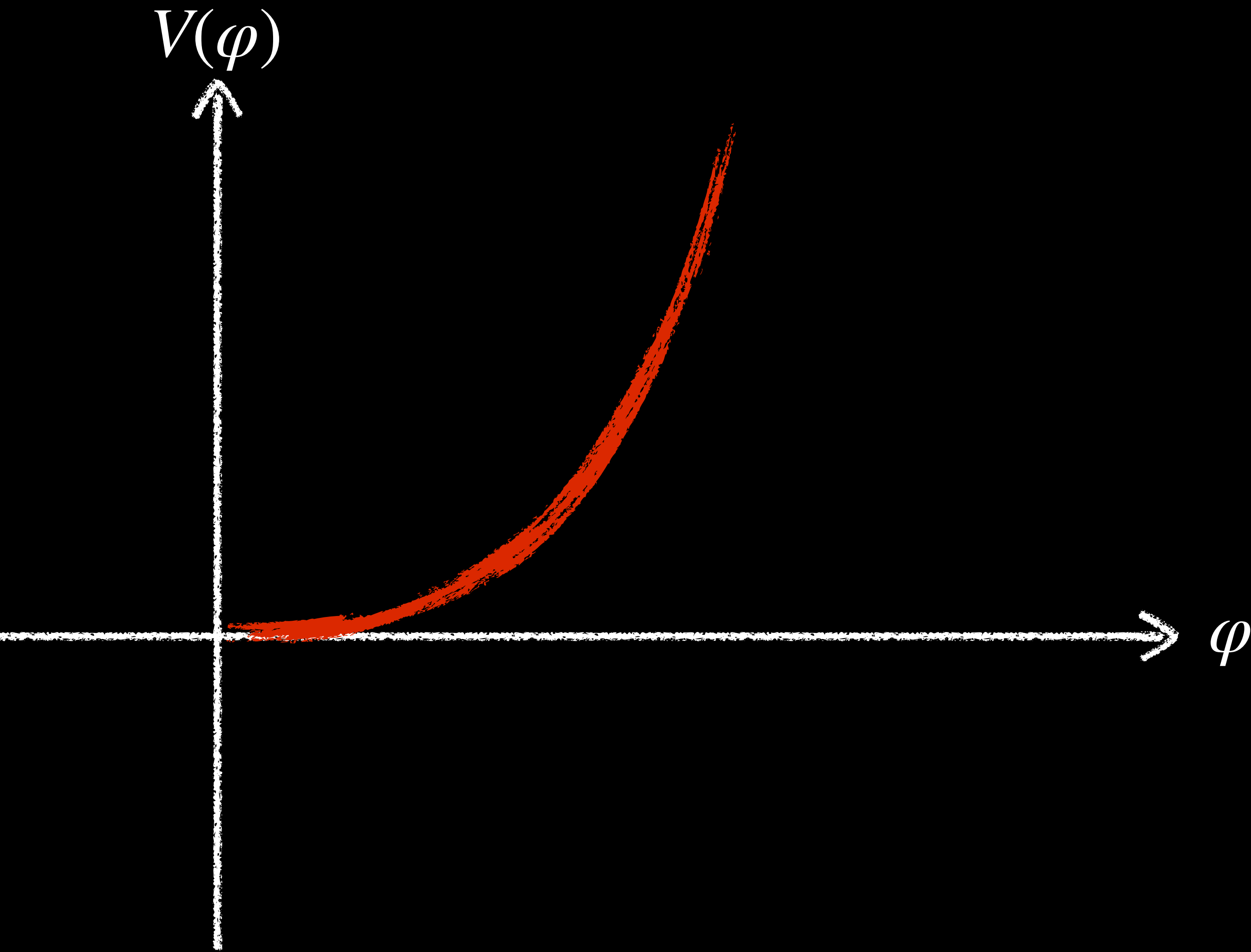
Based on work in collaboration with:

M. Kierkla, T.V.I. Tenkanen, J. van de Vis, P. Schicho, M. Lewicki, D. Schmitt,
JHEP 02 (2024) 234, JHEP 07 (2025) 153, 2607.18233

STOCHASTIC
GRAVITATIONAL-
WAVE BACKGROUND
FROM FIRST-ORDER
PHASE TRANSITIONS

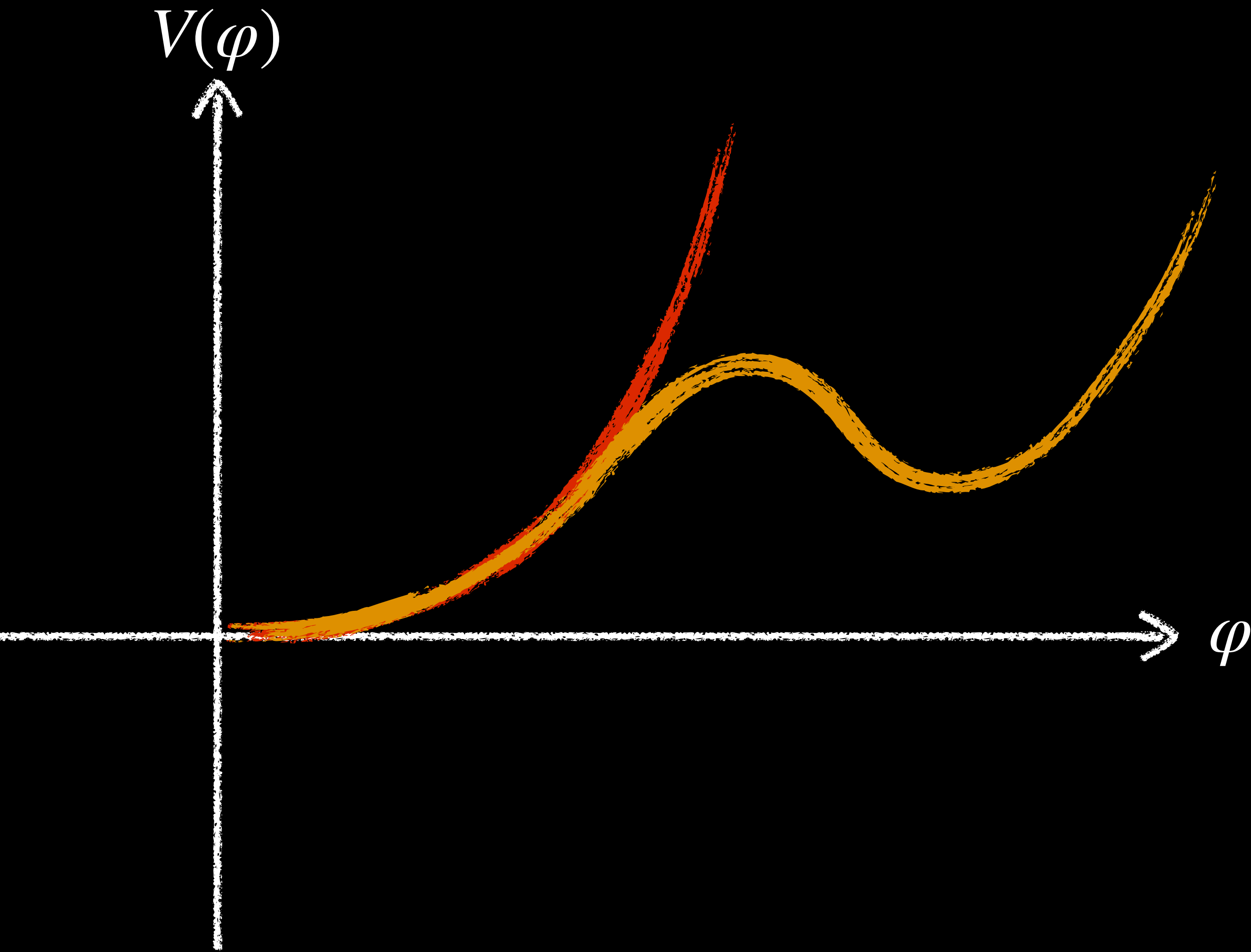


FIRST-ORDER PHASE TRANSITION



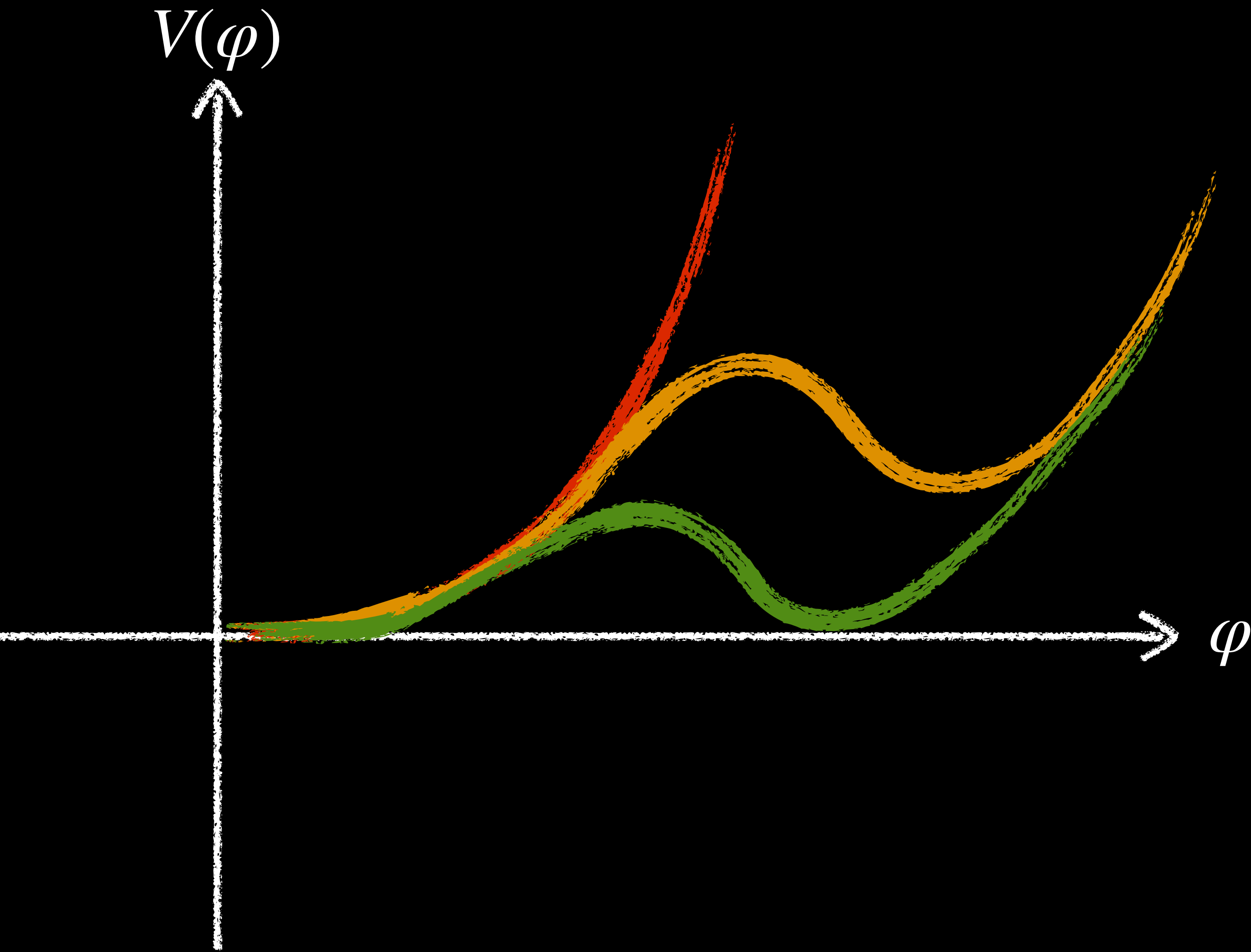
high temperature:
EW symmetry restored

FIRST-ORDER PHASE TRANSITION



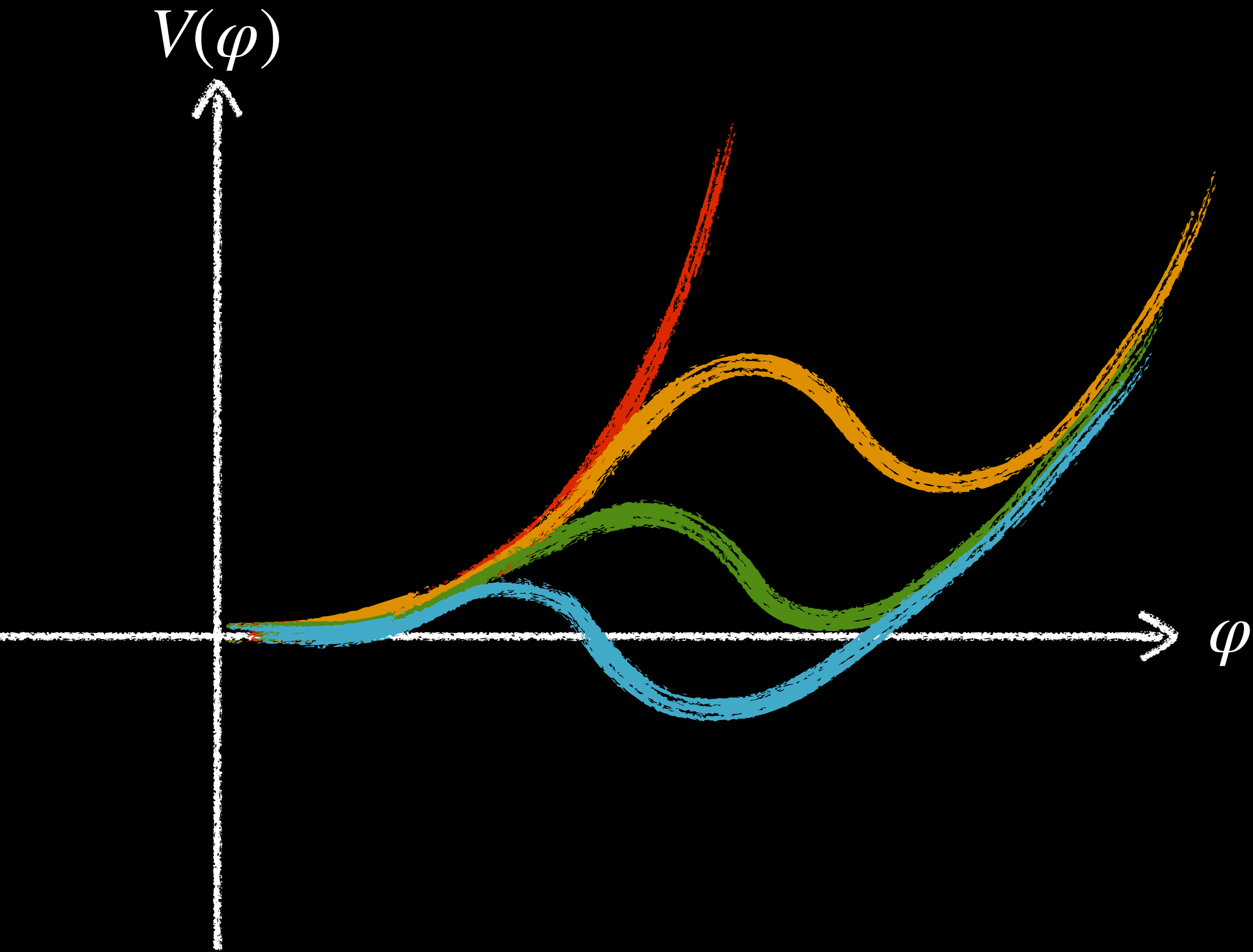
Secondary minimum
forms

FIRST-ORDER PHASE TRANSITION

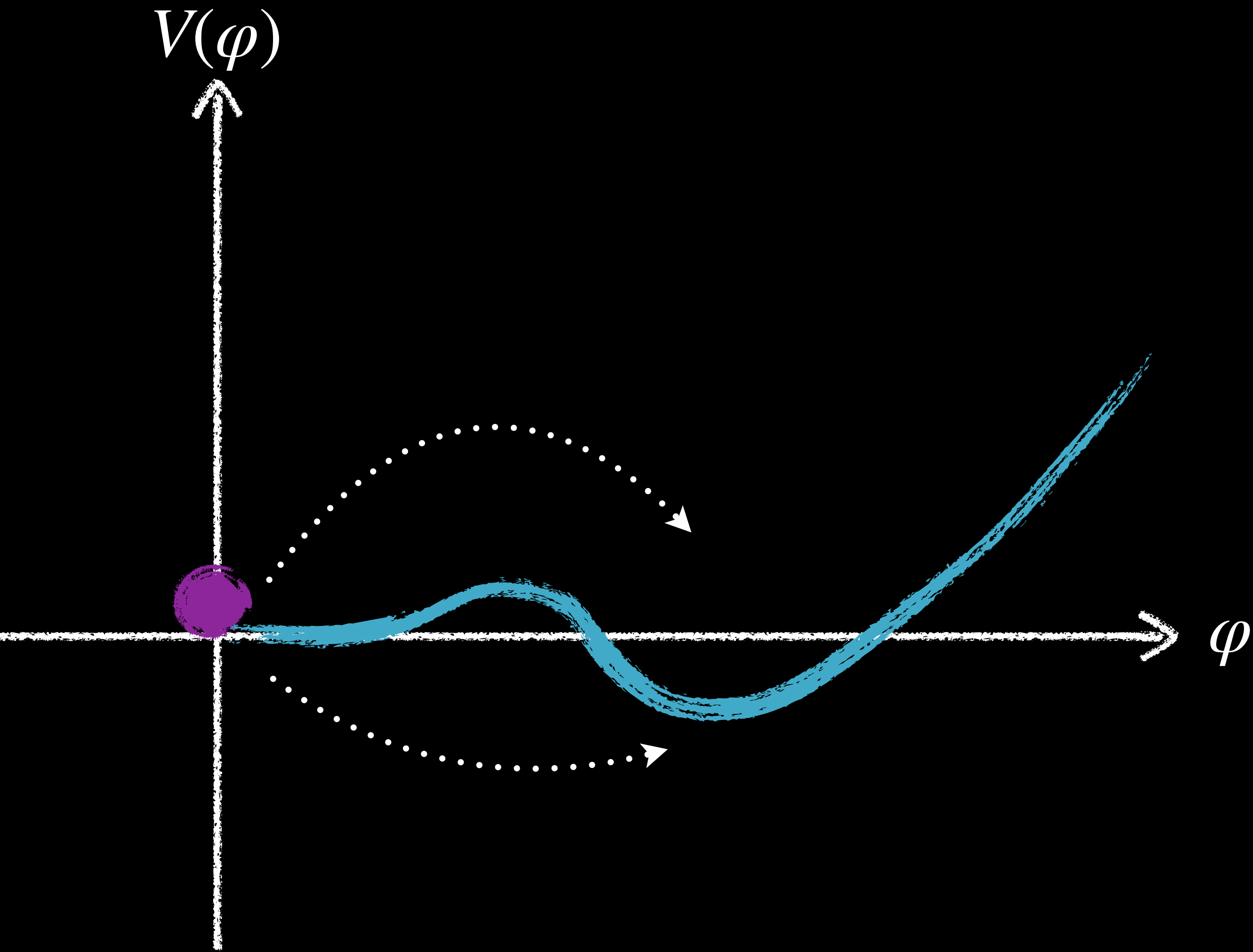


critical temperature:
two degenerate
minima

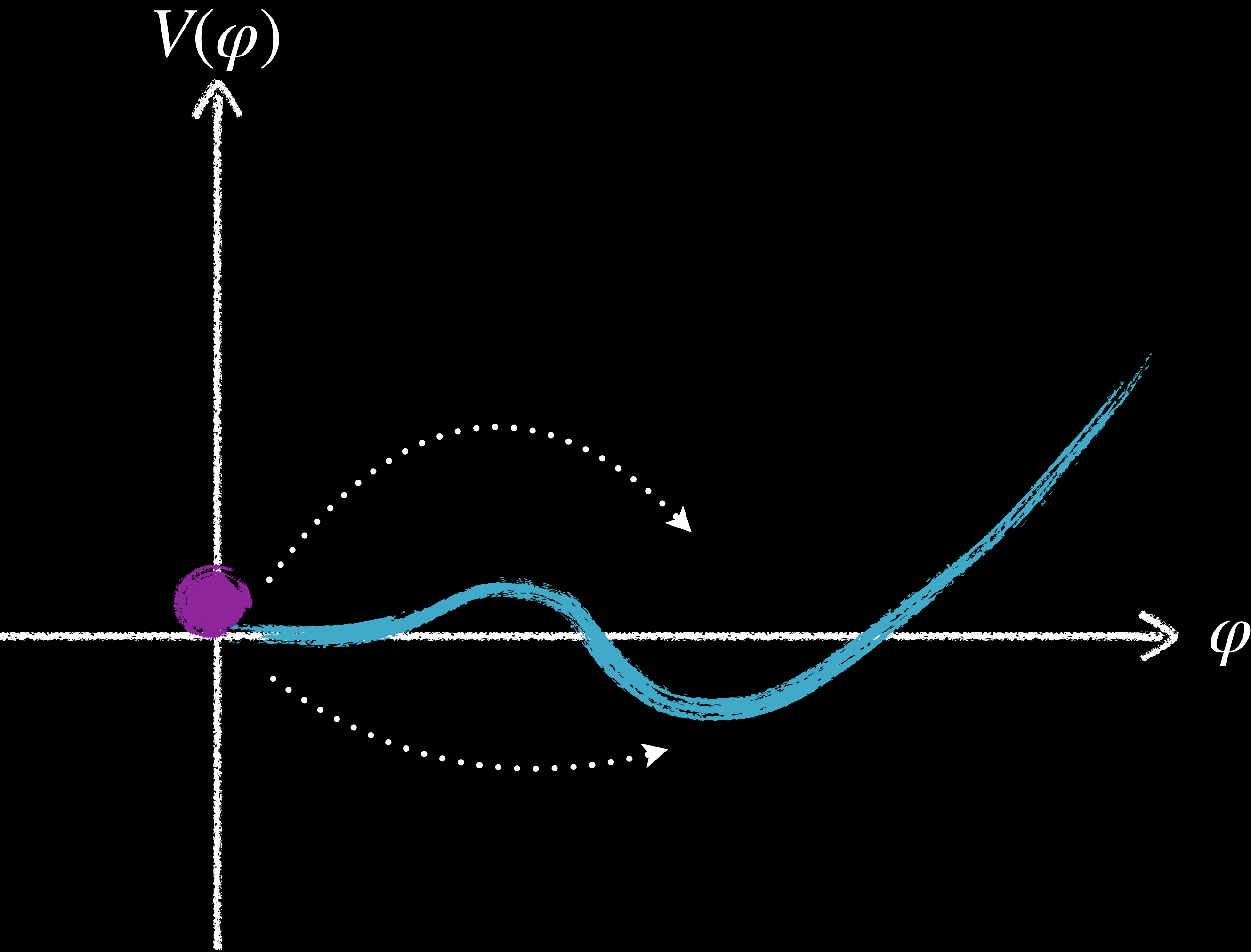
FIRST-ORDER PHASE TRANSITION



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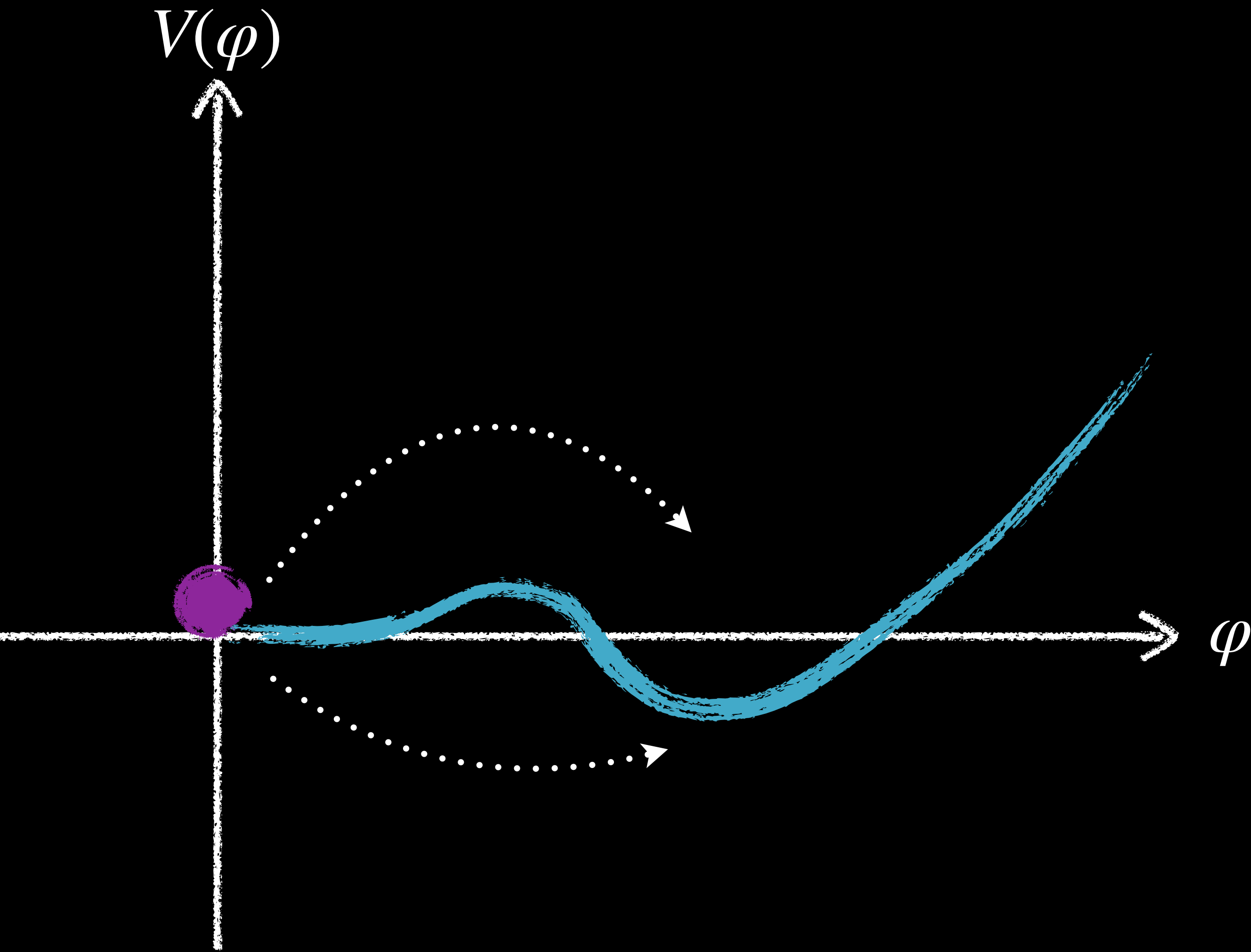
nucleation:
one bubble nucleates
per Hubble volume

$$\langle \varphi \rangle \neq 0$$

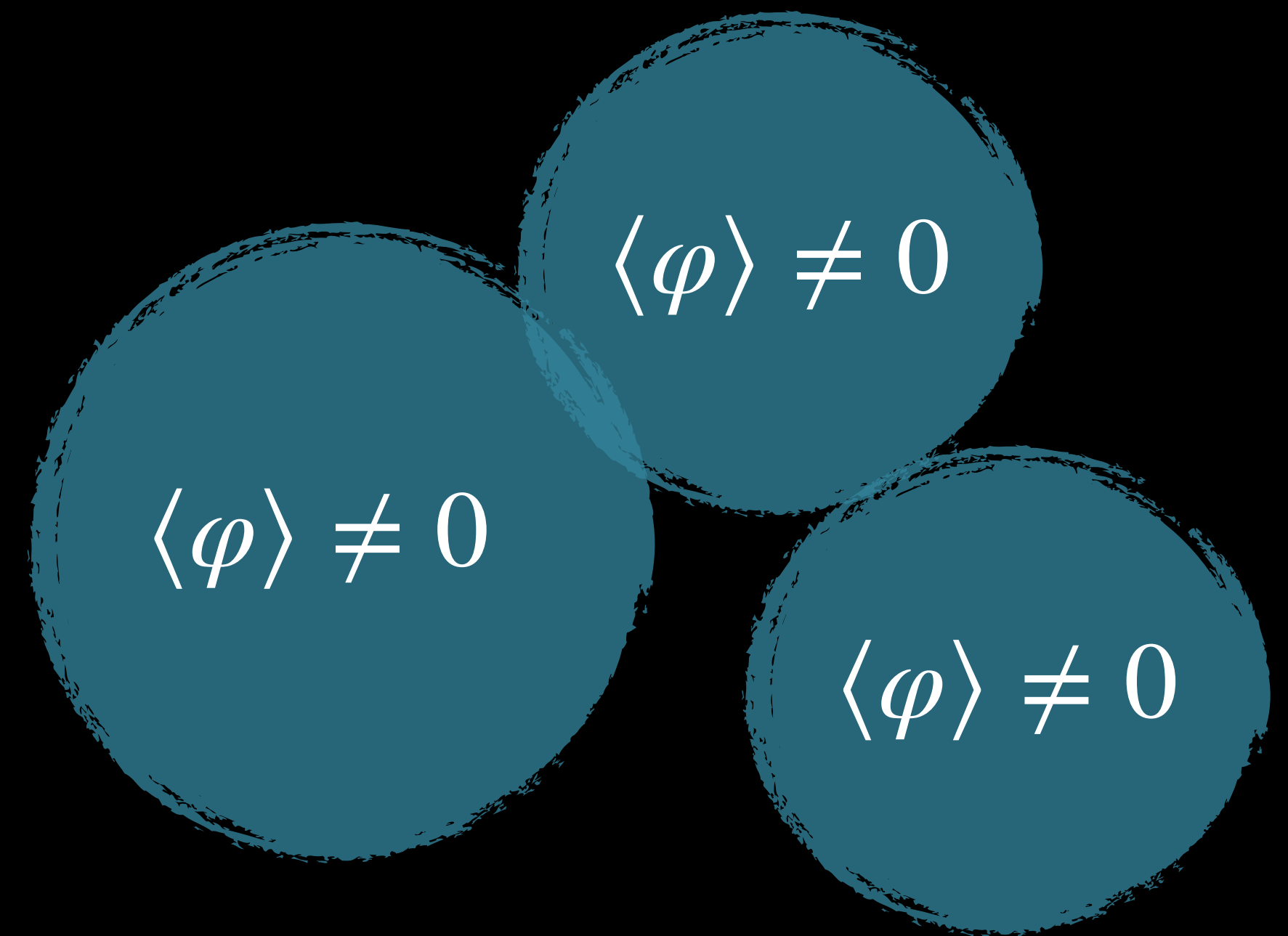
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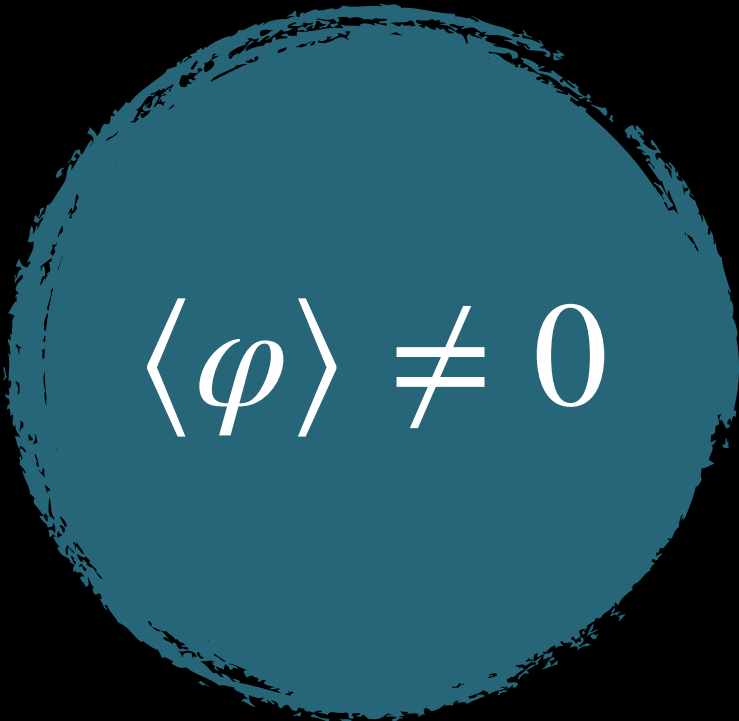
FIRST-ORDER PHASE TRANSITION



percolation: phase
transition completes

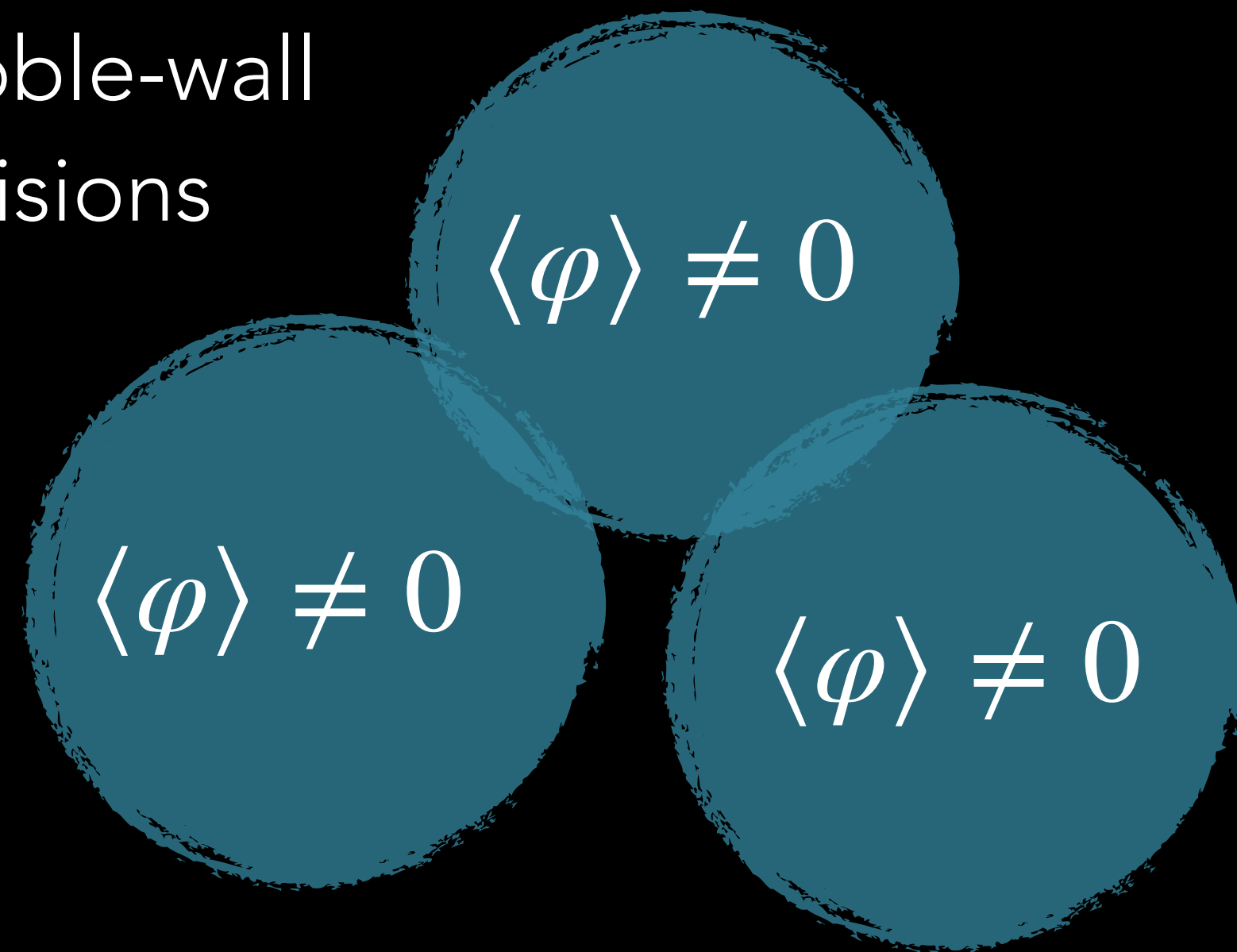


SOURCES OF GRAVITATIONAL WAVES


$$\langle \varphi \rangle \neq 0$$

SOURCES OF GRAVITATIONAL WAVES

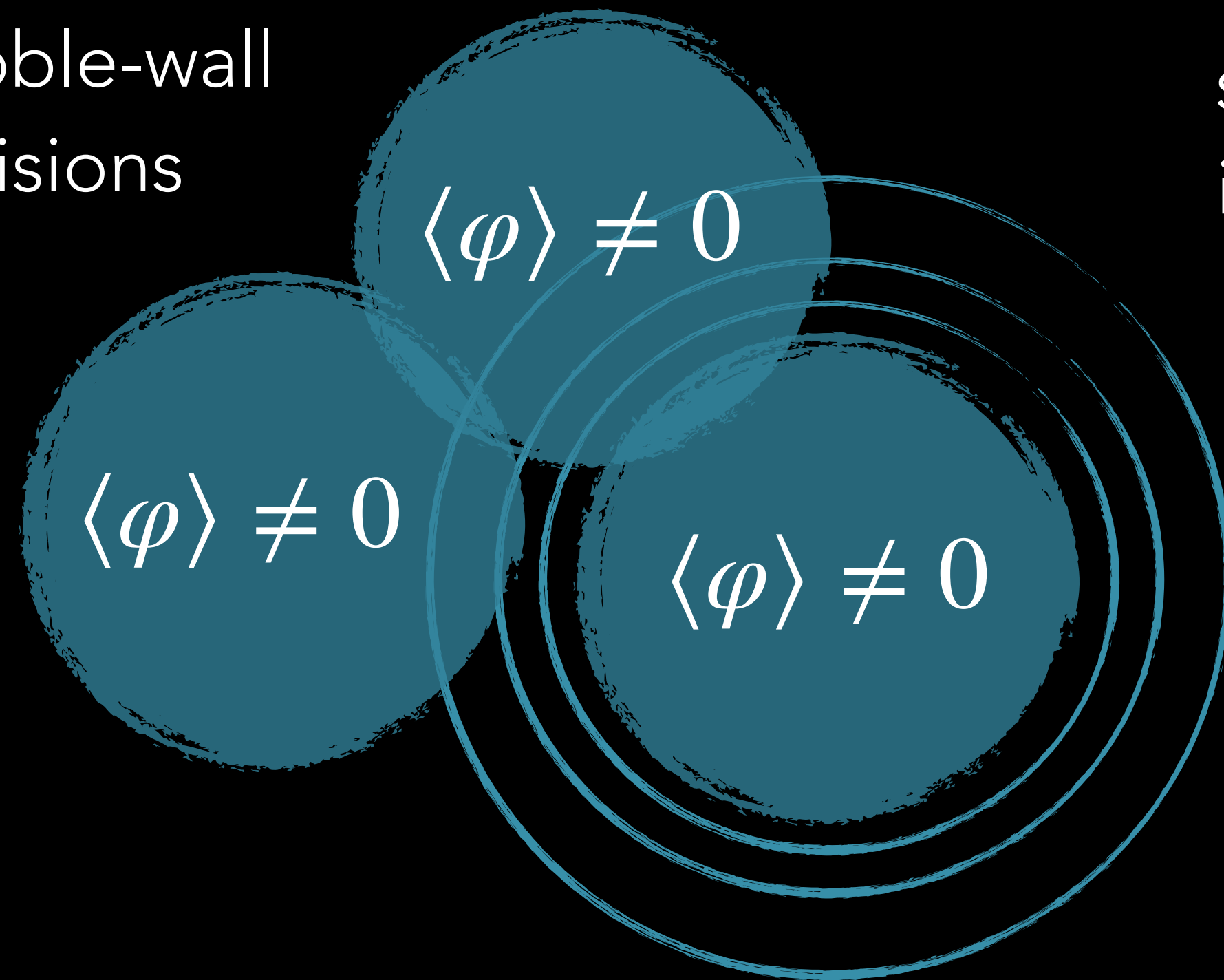
bubble-wall
collisions



SOURCES OF GRAVITATIONAL WAVES

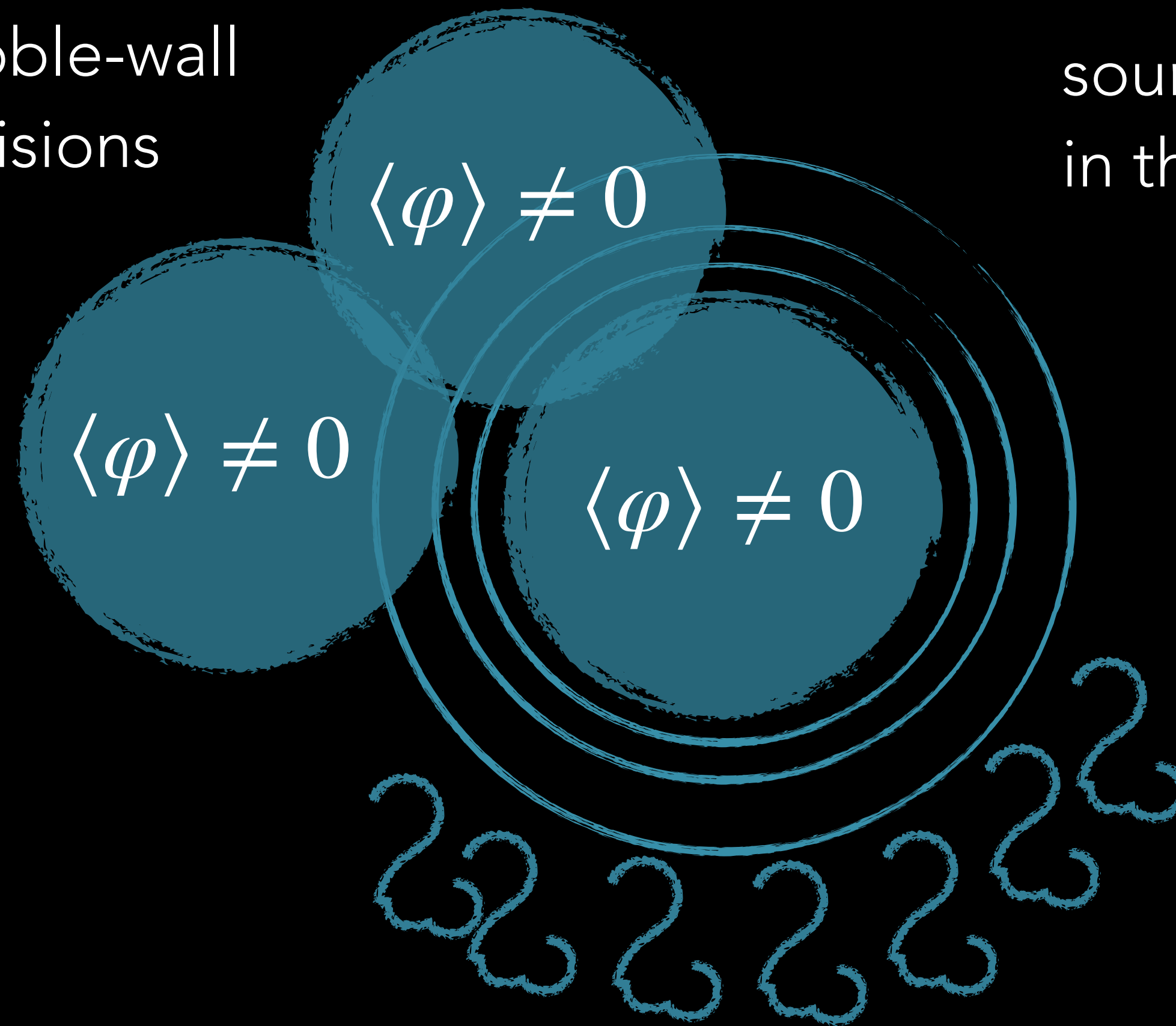
bubble-wall
collisions

sound waves
in the plasma



SOURCES OF GRAVITATIONAL WAVES

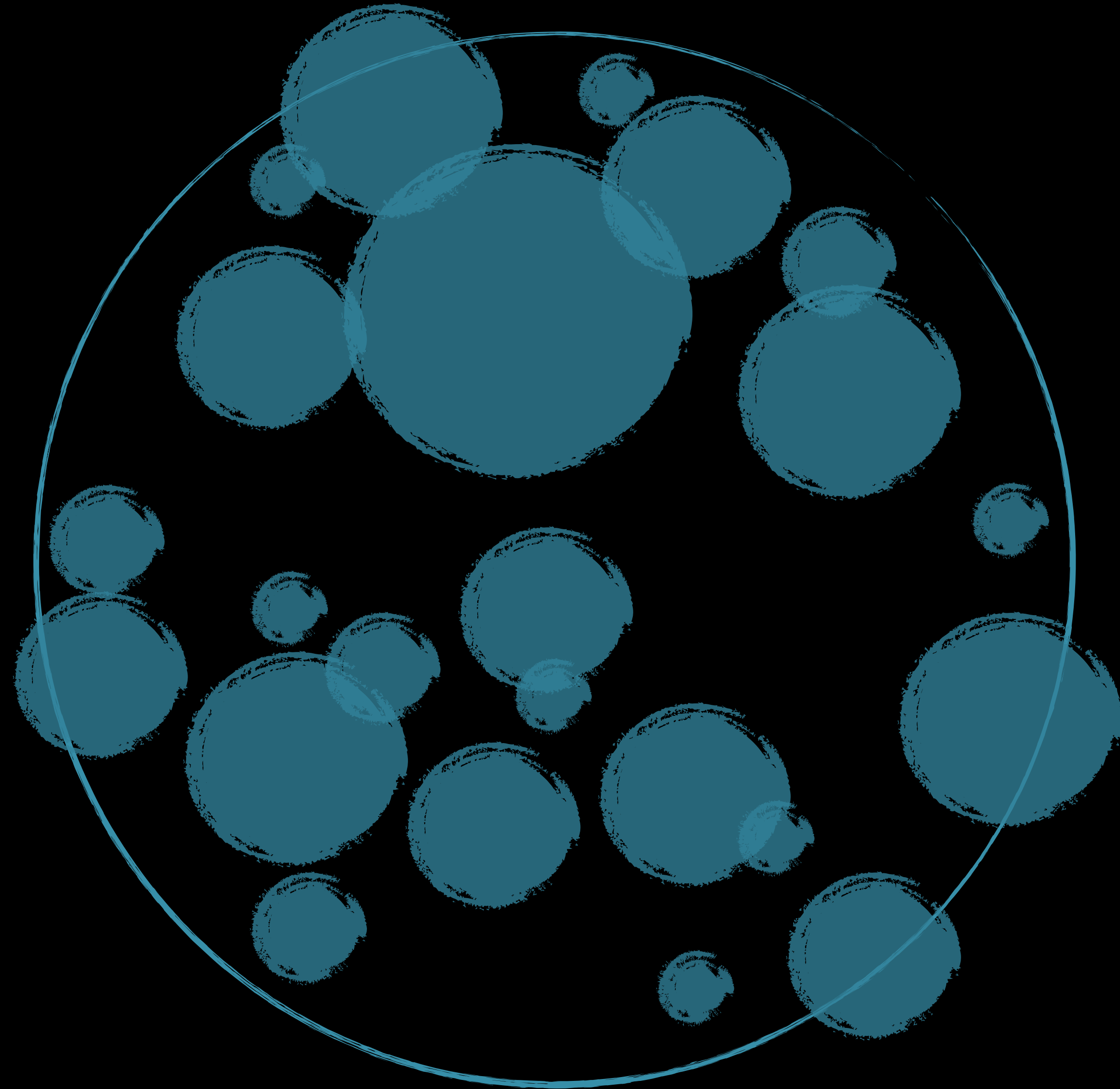
bubble-wall
collisions



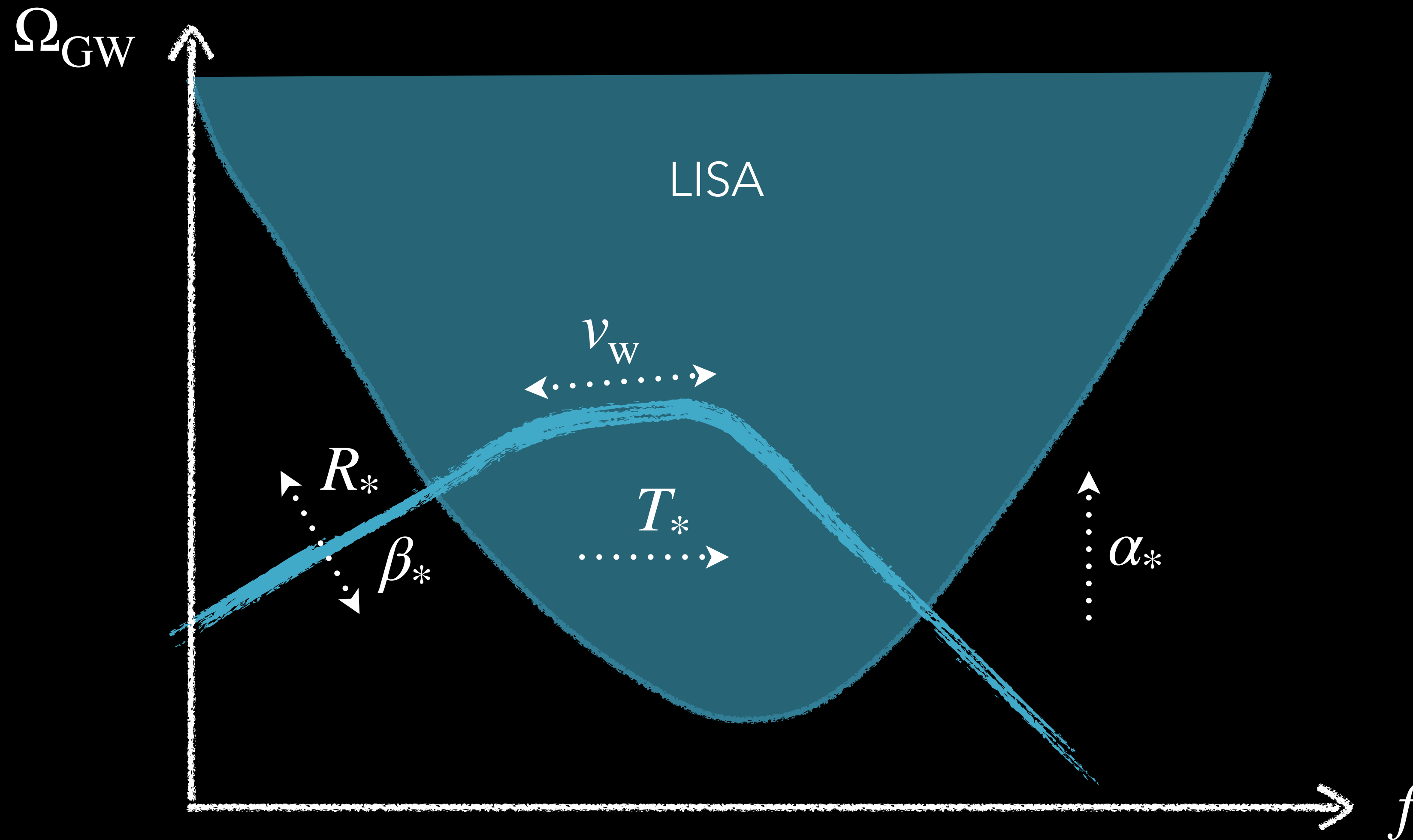
sound waves
in the plasma

turbulence in
the plasma

STOCHASTIC GW BACKGROUND



THERMODYNAMICAL PARAMETERS VS GW



- α_* - phase-transition strength $\approx$ latent heat released
- β_* (R_*) - inverse time (length) scale of the transitions
- T_* - characteristic temperature
- v_w - bubble-wall velocity

GW FROM PT: JOURNEY THROUGH SCALES

Macrophysics

gravitational waves (+baryogenesis, DM)

Intermediate

plasma and bubble dynamics, wall velocity

Microphysics

quantum fields at high T, bubble nucleation

GW FROM PT: JOURNEY THROUGH SCALES

Macrophysics

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data

BUBBLE NUCLEATION RATE

$$\Gamma = A_{\text{dyn}} \cdot A_{\text{stat}} = A_{\text{dyn}} \cdot A_{\text{det}} \cdot \exp(-S_{\text{eff}}[\varphi_b])$$

non-equilibrium
effects

quantum
fluctuations

solution of the classical Euclidean
equation of motion (the bounce)

SOURCES OF UNCERTAINTY

$\Delta\Omega_{\text{GW}}/\Omega_{\text{GW}}$	4d approach	3d approach
RG scale dependence	$\mathcal{O}(10^2 - 10^3)$	$\mathcal{O}(10^0 - 10^1)$
Gauge dependence	$\mathcal{O}(10^1)$	$\mathcal{O}(10^{-3})$
High-T approximation	$\mathcal{O}(10^{-1} - 10^0)$	$\mathcal{O}(10^0 - 10^2)$
Higher loop orders	unknown	$\mathcal{O}(10^0 - 10^1)$
Nucleation corrections	unknown	$\mathcal{O}(10^{-1} - 10^0)$
Nonperturbative corrections	unknown	unknown

[O. Gould, T. V. I. Tenkanen, JHEP 06 (2021) 069]

Two-loop corrections necessary to recover RG-scale invariance of the thermally-corrected effective potential.

[Table adapted from JHEP 04 (2021) 055, D. Croon, O. Gould, P. Schicho, T. V. I. Tenkanen, G. White]

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[J. Hirvonen, J. Löfgren, M. J. Ramsey-Musolf, P. Schicho, T. V. I. Tenkanen, *JHEP* 07 (2022) 135, Phys.Rev.Lett. 130 (2023) 25, 251801]

Consistent power-counting assures gauge independence, using the LO bounce solution to evaluate NLO contributions to the effective action.

[Table adapted from JHEP 04 (2021) 055, D. Croon, O. Gould, P. Schicho, T. V. I. Tenkanen, G. White]

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[F. Bernardo, P. Klose, P. Schicho, T. V. I. Tenkanen, *JHEP* 08 (2025) 109]

Higher-order operators may significantly affect the predictions — in some cases high- T expansion breaks down entirely.

[P. Navarrete, R. Paatelainen, K. Seppänen, T. V. I. Tenkanen, *JHEP* 01 (2026) 113]

Go beyond high- T expansion with full four-dimensional resummed thermal effective potential.



See the talks by M. Kierkla and A. Dashko

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[A. Ekstedt, P. Schicho, T. V. I. Tenkanen,
Phys.Rev.D 110 (2024) 9, 096006]

Equilibrium thermodynamics of PT
computed to the last perturbative
order. Agreement with lattice in the
region of validity of the EFT.

[Table adapted from JHEP 04 (2021) 055, D. Croon, O. Gould, P. Schicho,
T. V. I. Tenkanen, G. White]

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[O. Gould, J. Hirvonen, Phys.Rev.D 104 (2021) 9, 096015]

Construction of an EFT for nucleation.

[Table adapted from JHEP 04 (2021) 055, D. Croon, O. Gould, P. Schicho,
T. V. I. Tenkanen, G. White]

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[O. Gould, S. Güyer, K. Rummukainen,
Phys.Rev.D 106 (2022) 11, 114507]

Non-perturbative lattice calculation of
PT thermodynamics.

[A. Kormu, O. Gould, D. Weir, Phys.Rev.D 111 (2025) 5, 5;
D. Pîrvu, A. Shkerin, S. Sibiryakov Int.J.Mod.Phys.A 39
(2024) 34, 2445007, J. Hirvonen, O. Gould, Phys.Rev.Lett.
136 (2026) 8, 081601]

Non-perturbative lattice computations
of bubble nucleation rate.

[Table adapted from JHEP 04 (2021) 055, D. Croon, O. Gould, P. Schicho,
T. V. I. Tenkanen, G. White]

SOURCES OF UNCERTAINTY

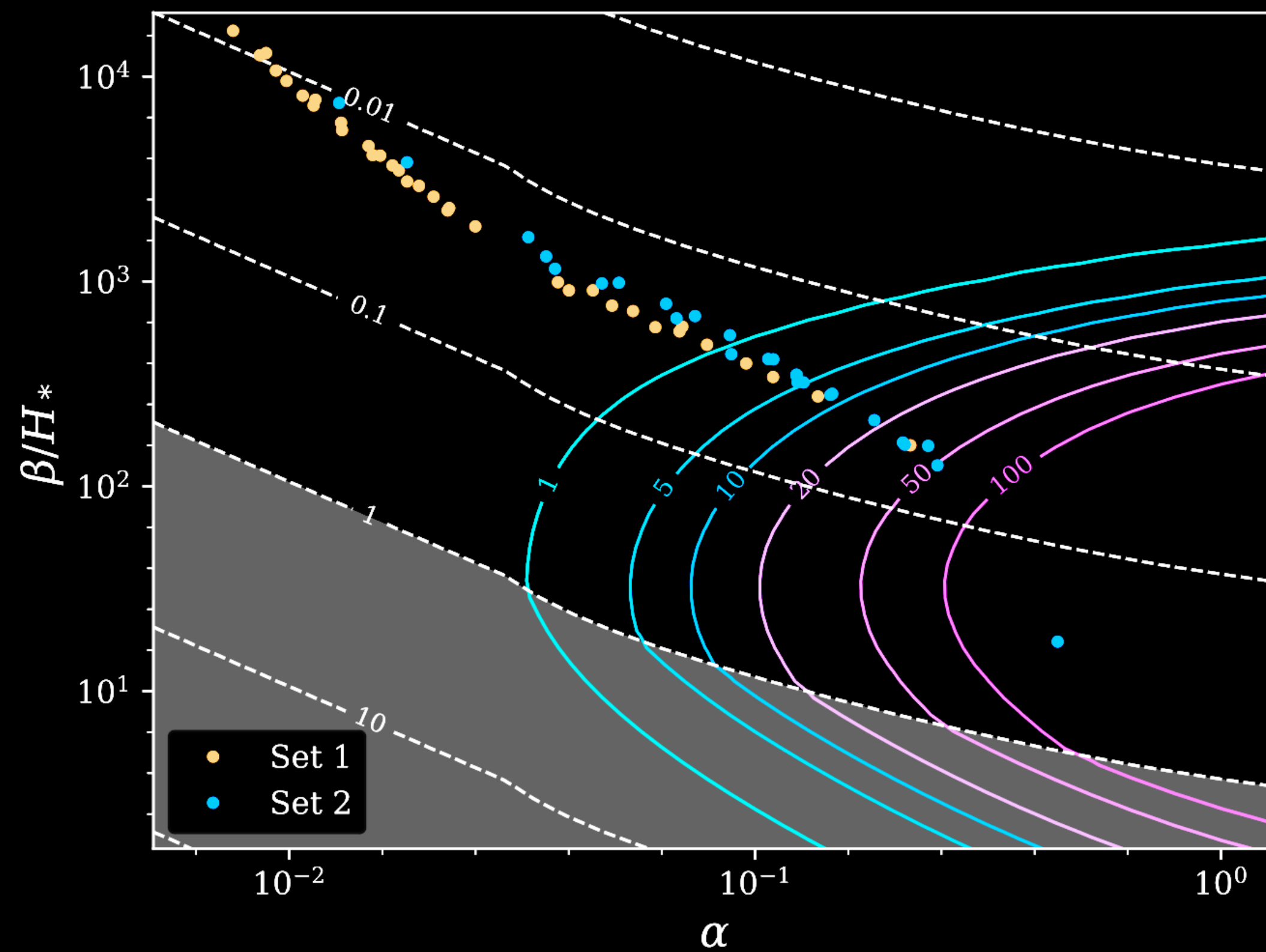
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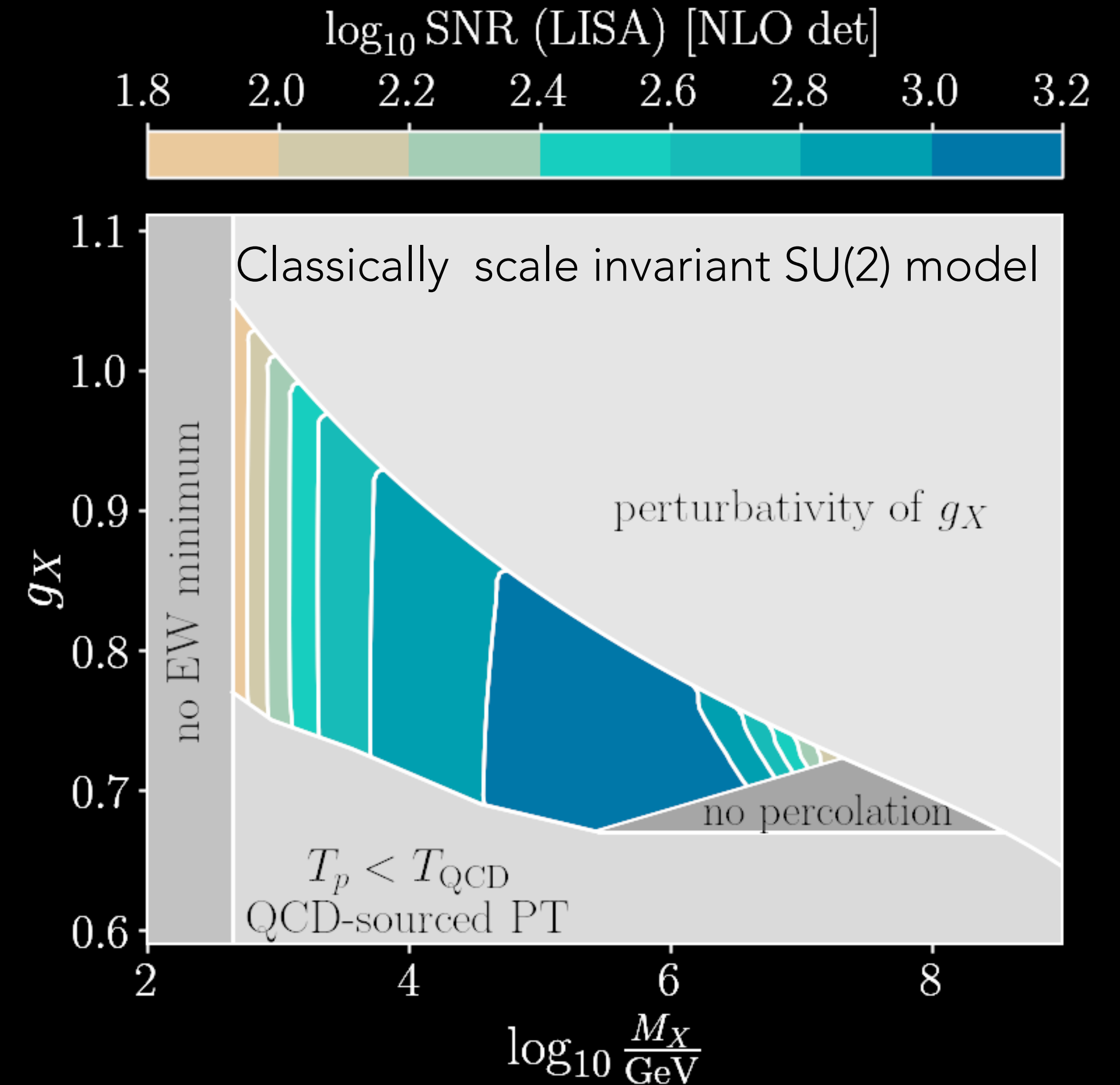
- out-of-equilibrium effects ➡ see the talks by J. Hirvonen and A. Shkerin

VARIOUS MODELS, VARIOUS PROBLEMS

2-Higgs doublet model

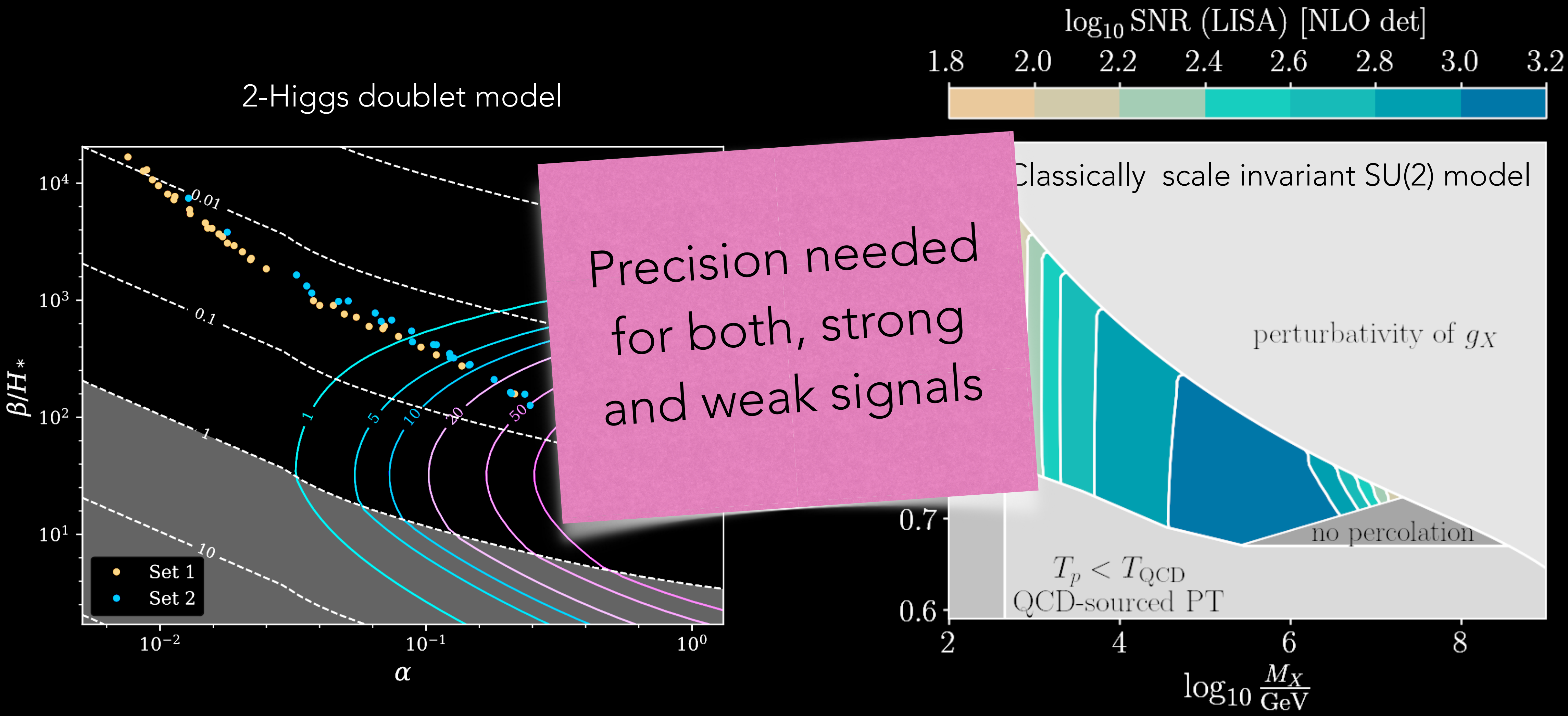


[C. Caprini et al., LISA CosWG, JCAP 03 (2020) 024]



[Image adapted from: M. Kierkla, PhD thesis, University of Warsaw, 2025,
See also M. Kierkla, P. Schicho, BŚ, T.V.I. Tenkanen, J. van de Vis, JHEP 07 (2025) 153]

VARIOUS MODELS, VARIOUS PROBLEMS



[C. Caprini et al., LISA CosWG, JCAP 03 (2020) 024]

[Image adapted from: M. Kierkla, PhD thesis, University of Warsaw, 2025,
See also M. Kierkla, P. Schicho, BŚ, T.V.I. Tenkanen, J. van de Vis, JHEP 07 (2025) 153]

INCREASING THE
PRECISION IN
BUBBLE NUCLEATION



BUBBLE NUCLEATION RATE

$$\Gamma = A_{\text{dyn}} \cdot A_{\text{stat}} = A_{\text{dyn}} \cdot A_{\text{det}} \cdot \exp(-S_{\text{eff}}[\varphi_b])$$

non-equilibrium effects quantum fluctuations solution of the classical Euclidean equation of motion (the bounce)

BUBBLE NUCLEATION RATE - BASIC APPROACH

$$\Gamma = A_{\text{dyn}} \cdot A_{\text{stat}} = A_{\text{dyn}} \cdot A_{\text{det}} \cdot \exp(-S_{\text{eff}}[\varphi_b])$$

non-equilibrium
effects

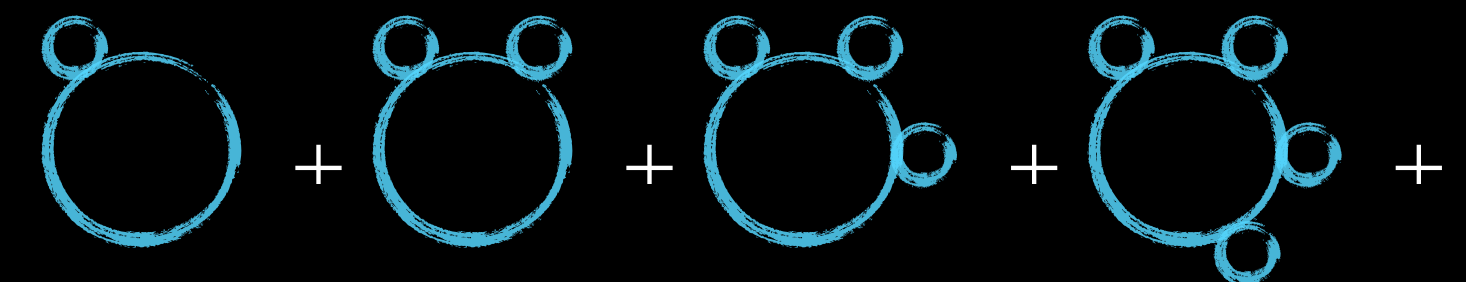
$$\approx T$$

quantum
fluctuations

$$\approx T^3$$

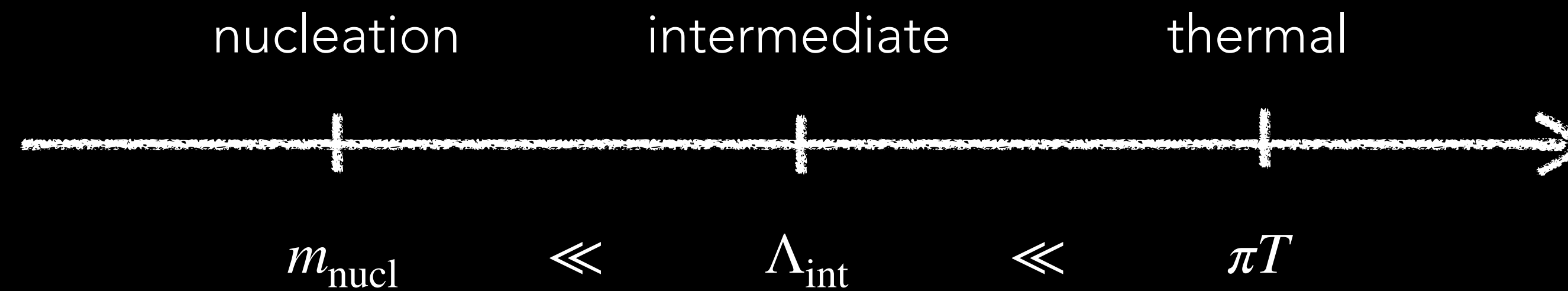
solution of the classical Euclidean
equation of motion (the bounce)

$$S_{\text{eff}} = \int_{\vec{x}} \left[\frac{1}{2} (\partial_i \varphi)^2 + V_{\text{tree}}(\varphi) + V^{(1)}(\varphi) + V_T^{(1)}(\varphi, T) + V^{\text{daisy}}(\varphi, T) \right]$$



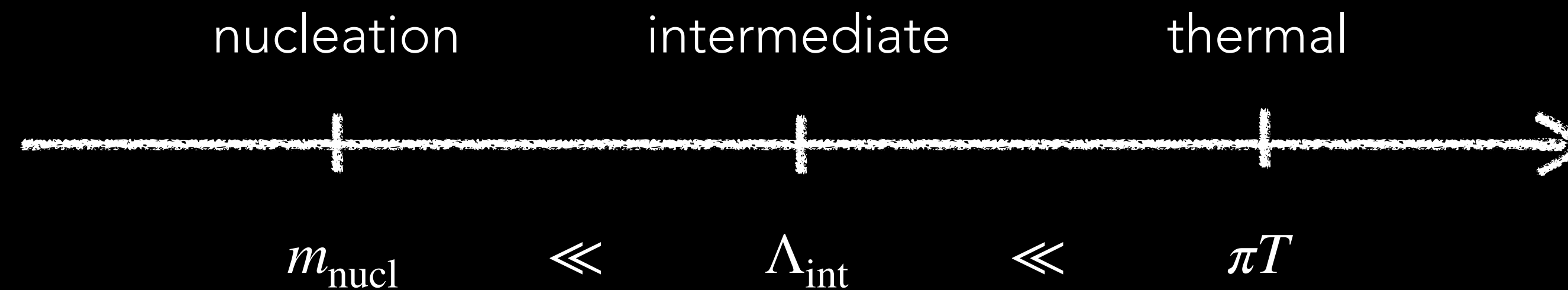
EFFECTIVE FIELD THEORY FOR NUCLEATION

[O. Gould, J. Hirvonen, Phys.Rev.D 104 (2021) 9, 096015]



EFFECTIVE FIELD THEORY FOR NUCLEATION

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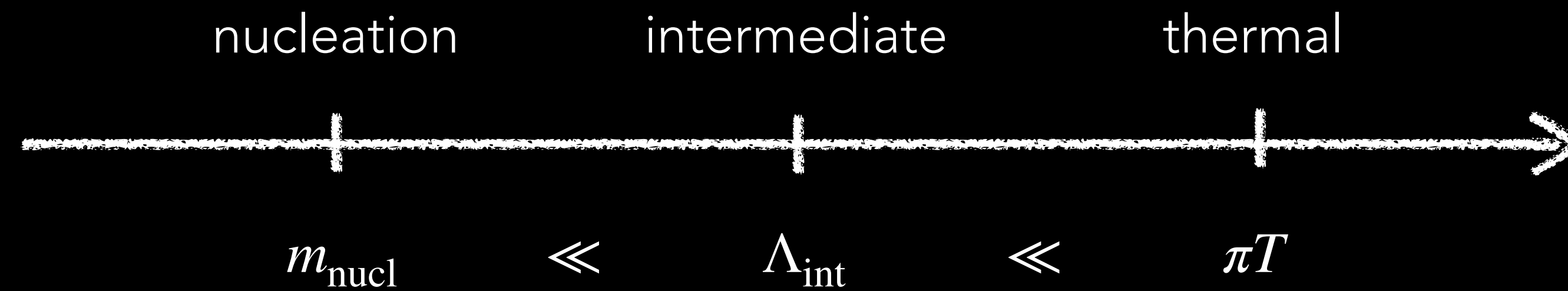


$$\Gamma = A_{\text{dyn}} \cdot A_{\text{stat}} = A_{\text{dyn}} \cdot A_{\text{det}} \cdot \exp(-S_{\text{eff}}[\varphi_b])$$

contributions from
fluctuations of the
fields that are not
integrated out at the
nucleation scale

the effective action at
the nucleation scale

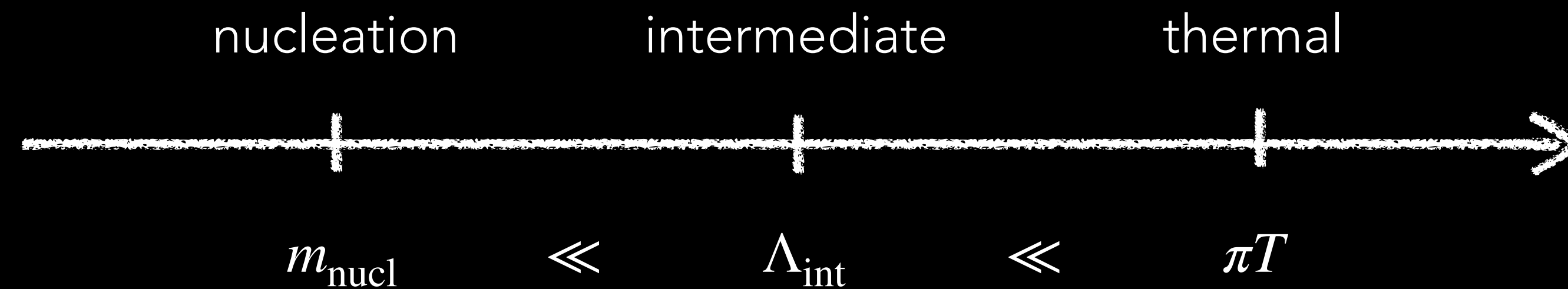
EFFECTIVE FIELD THEORY FOR NUCLEATION



The procedure:

1. Construct the EFT.
2. Compute the effective action consistently in power counting.
3. Solve the LO bounce equation. Use it also in the NLO action.
4. Compute the determinants for the light fields (or use approximations).

EFFECTIVE FIELD THEORY FOR NUCLEATION



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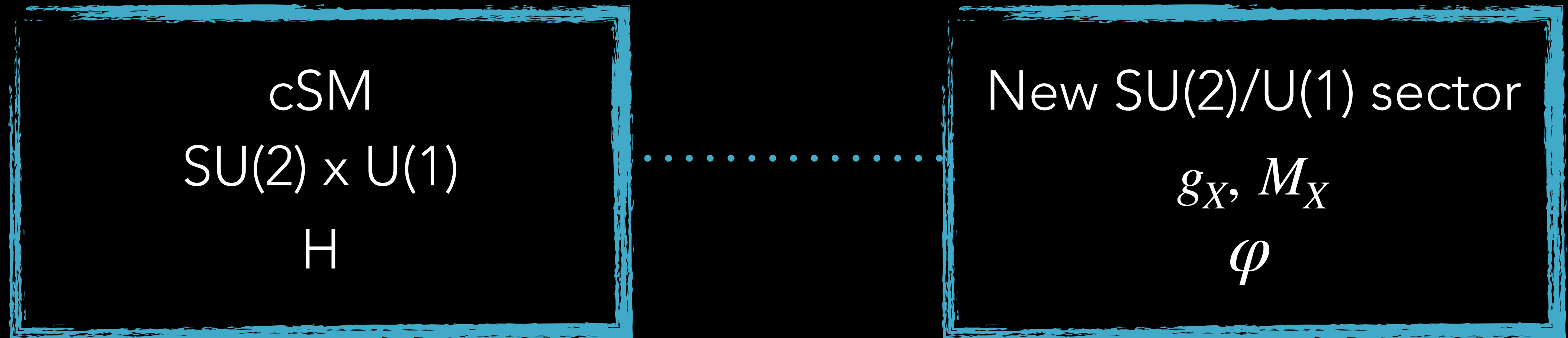
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the effective action at
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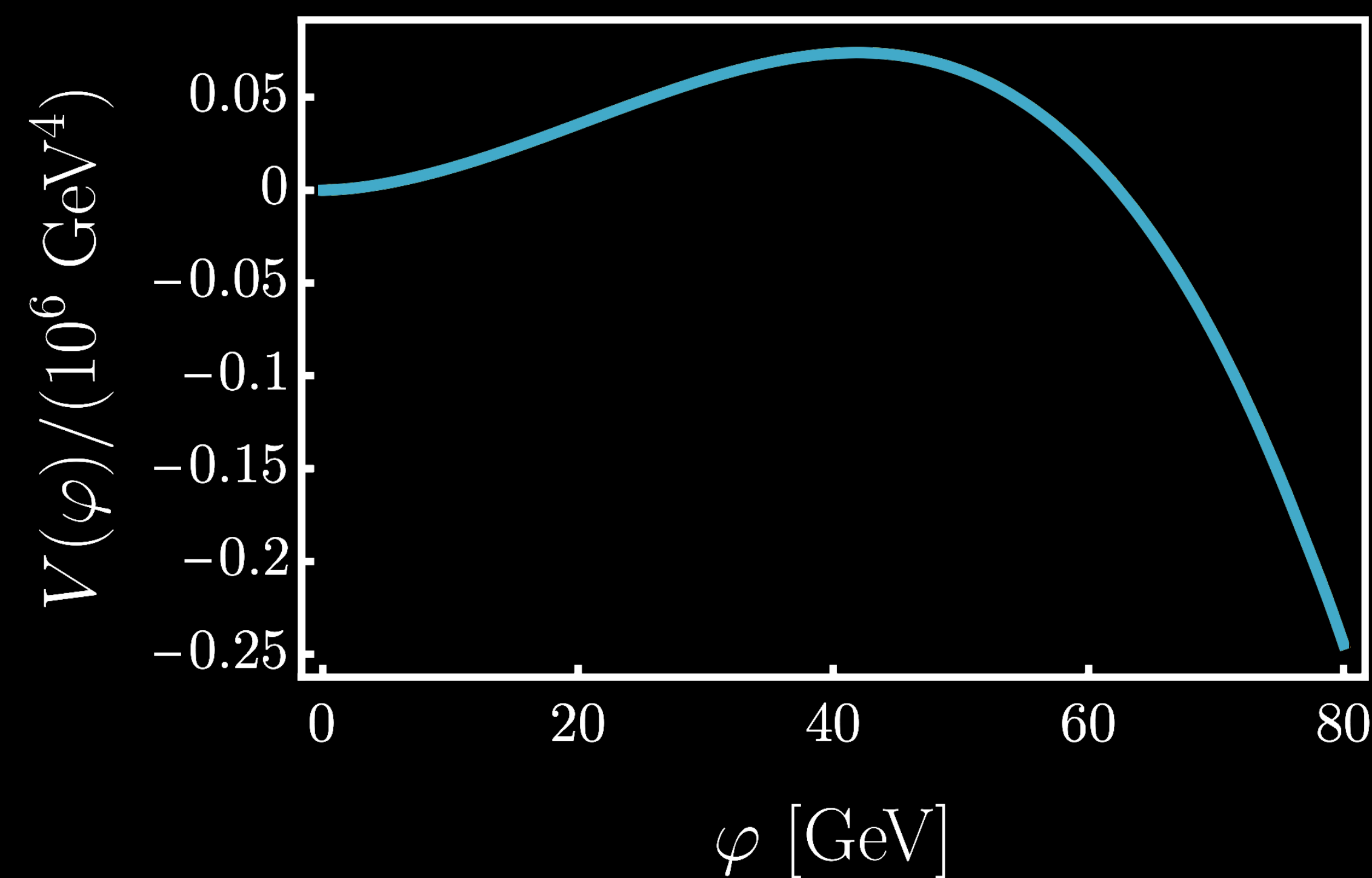
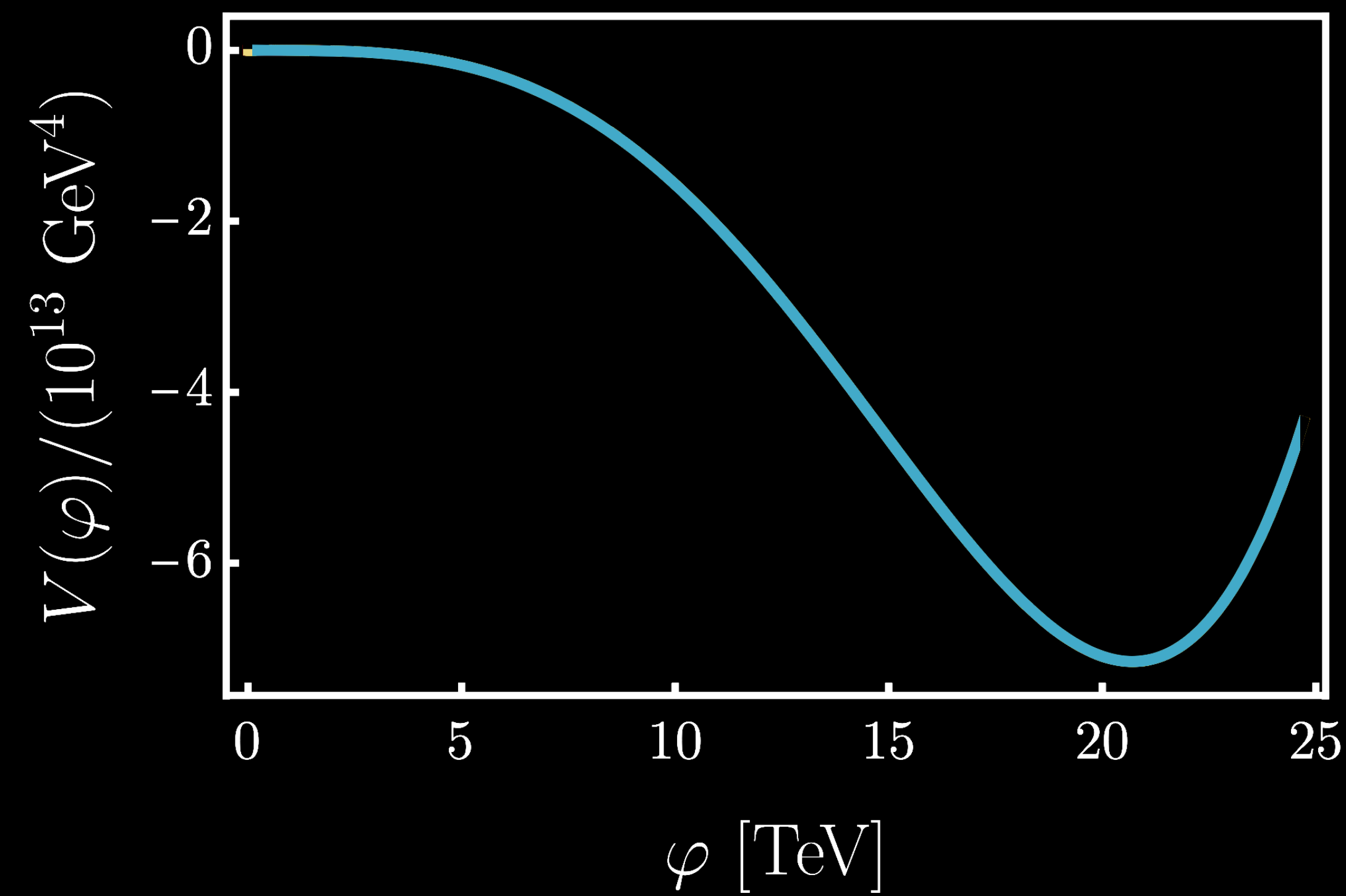
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THE MODEL

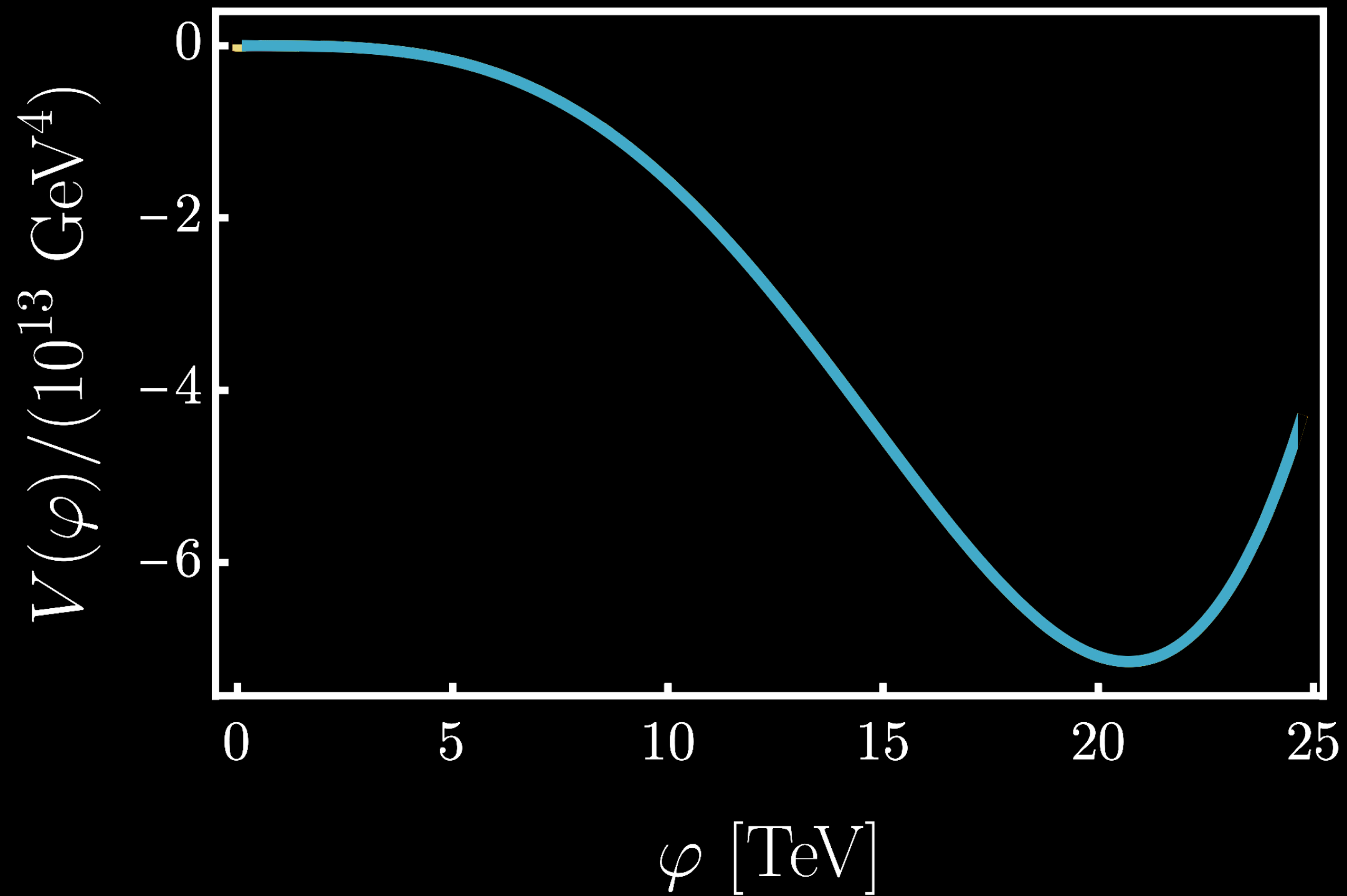


[See also: T.Hambye, A.Strumia, PRD88 (2013) 055022, C.Carone, R.Ramos, PRD88 (2013) 055020, V.V.Khoze, C.McCabe, G.Ro, JHEP 08 (2014) 026, T. Hambye, A.Strumia, D.Teresi, JHEP 1808 (2018) 188, I.Baldes, C. Garcia-Cely, JHEP 05 (2019) 190, T.Prokopec, J.Rezacek, BS, JCAP 02(2019)009, D. Marfaria, P. Tseng, JHEP 02 (2021) 022]

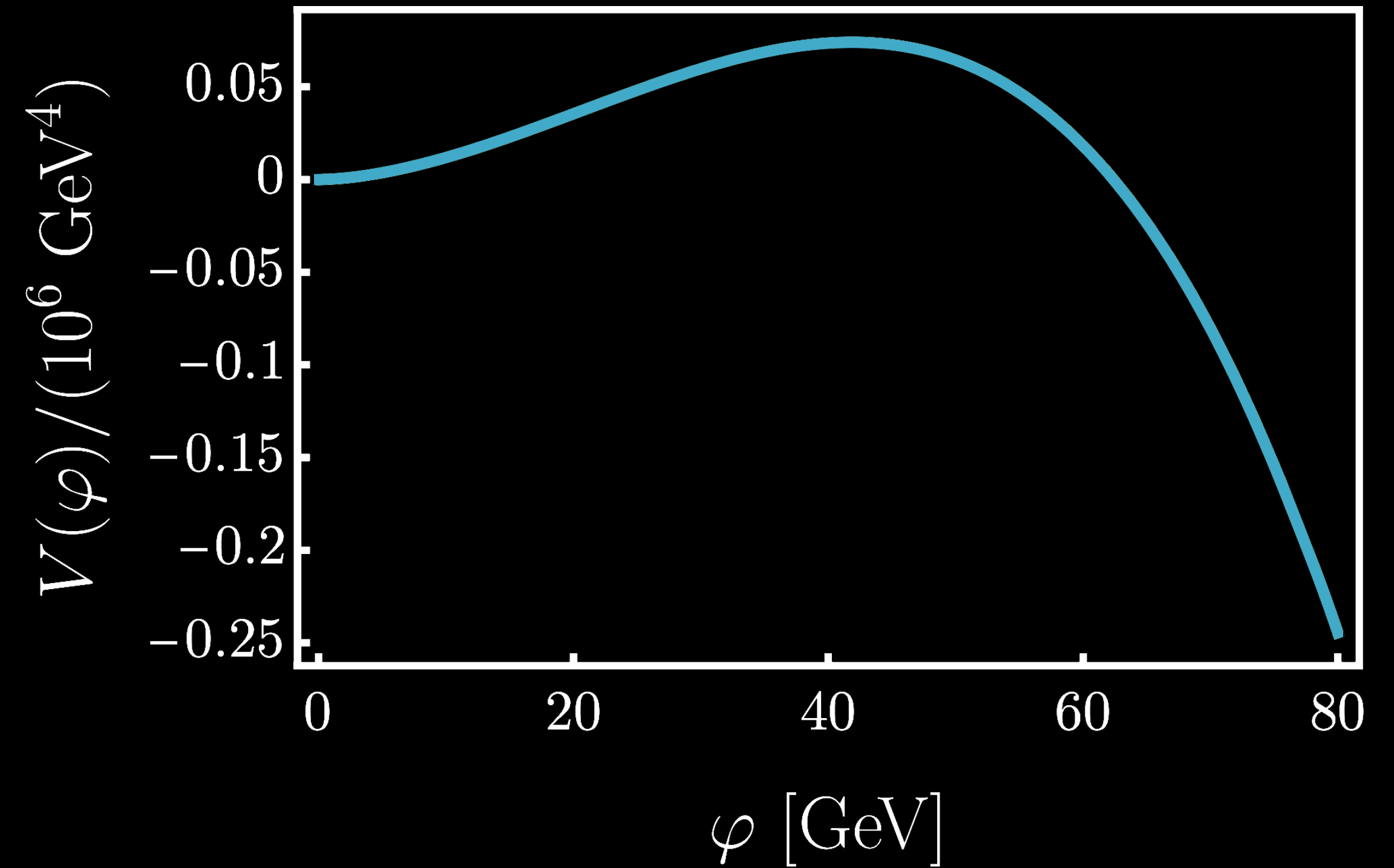
HIGH-T VS LOW-T



HIGH-T VS LOW-T

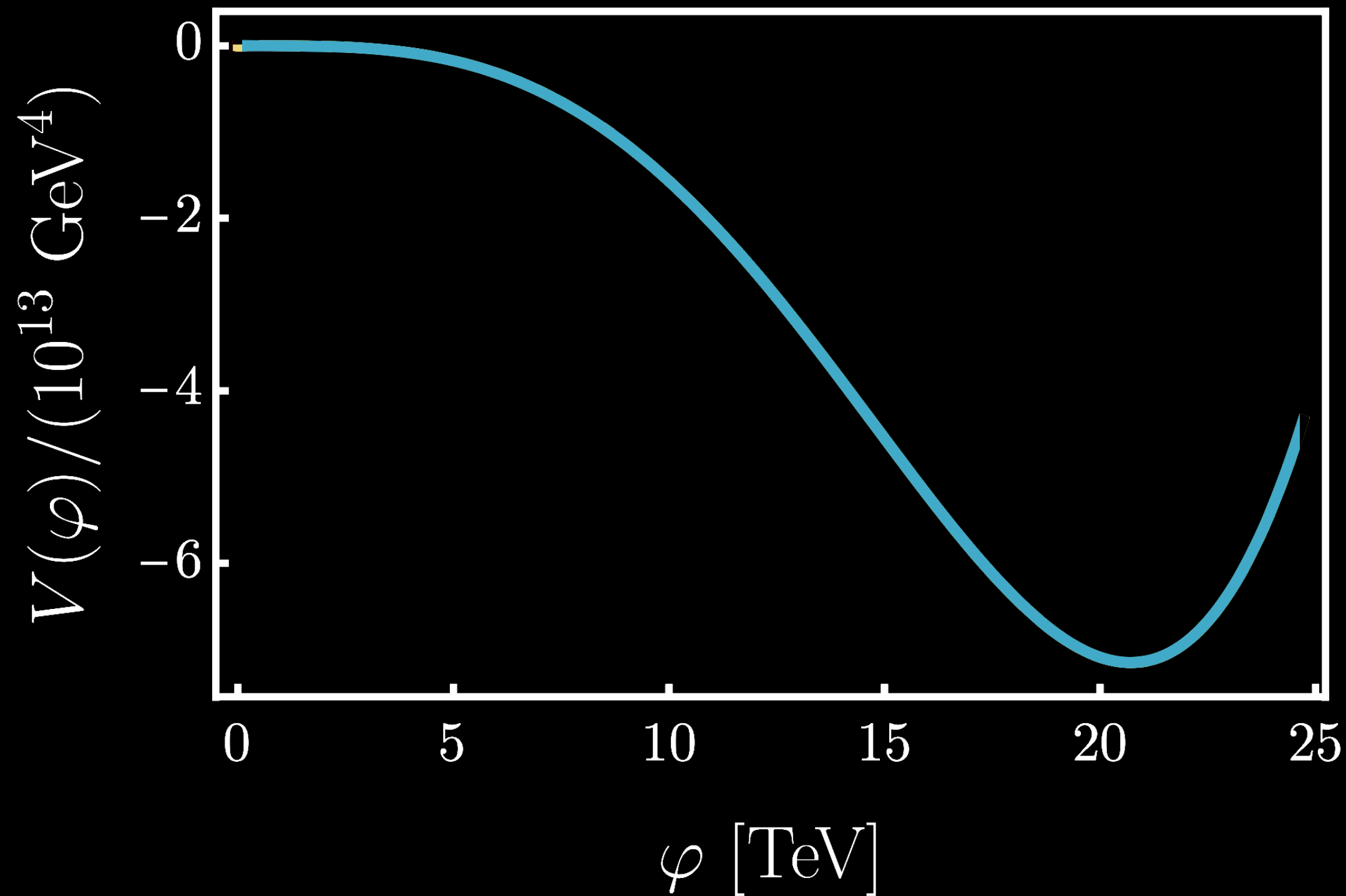


At large fields $M_X(\varphi)/T \gg 1$,
use LT approximation to compute T_{reh} , ΔV

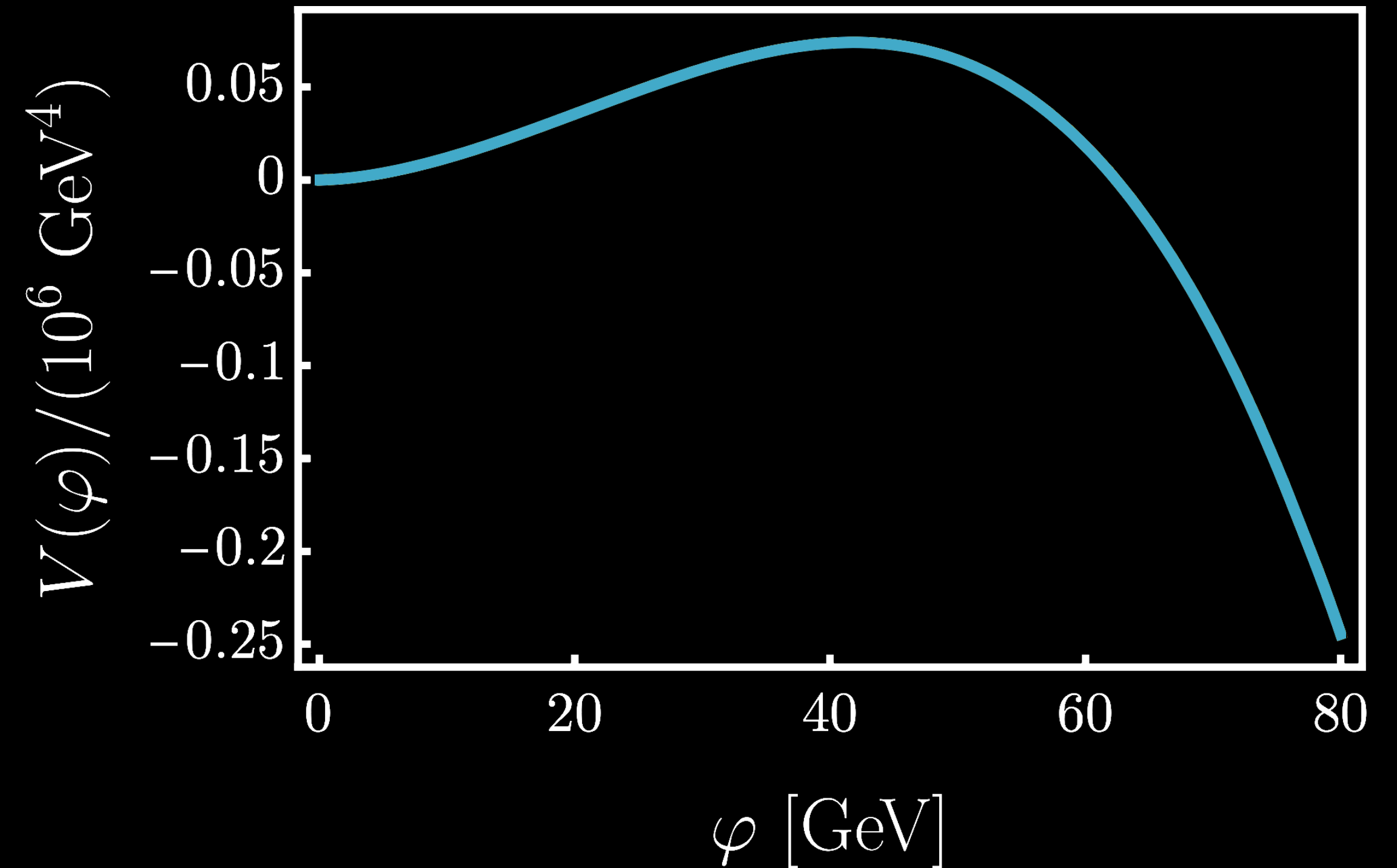


At small fields $M_X(\varphi)/T \lesssim 1$,
use HT approximation to compute T_p , $R_* H_*$

HIGH-T VS LOW-T



At large fields $M_X(\varphi)/T \gg 1$,
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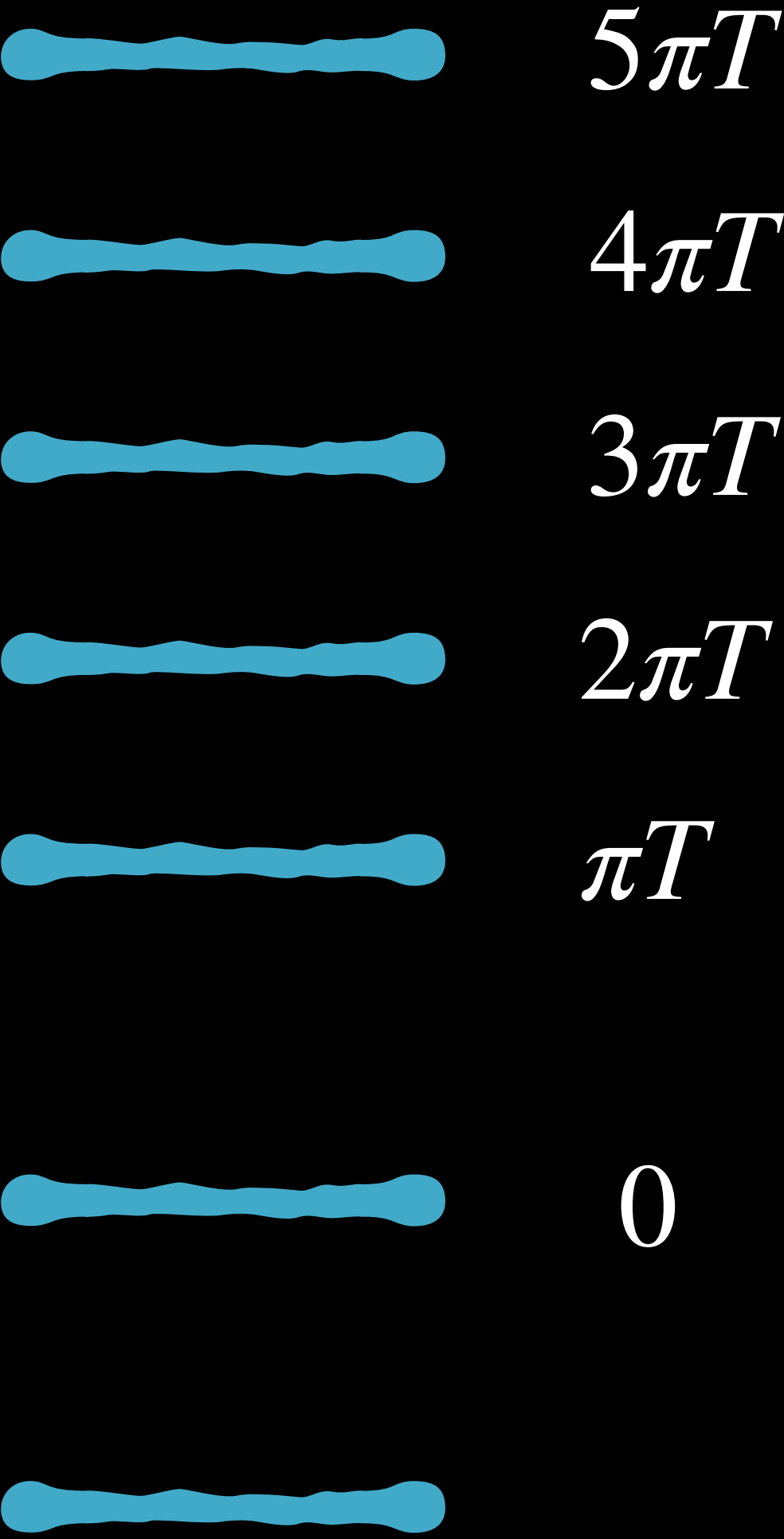


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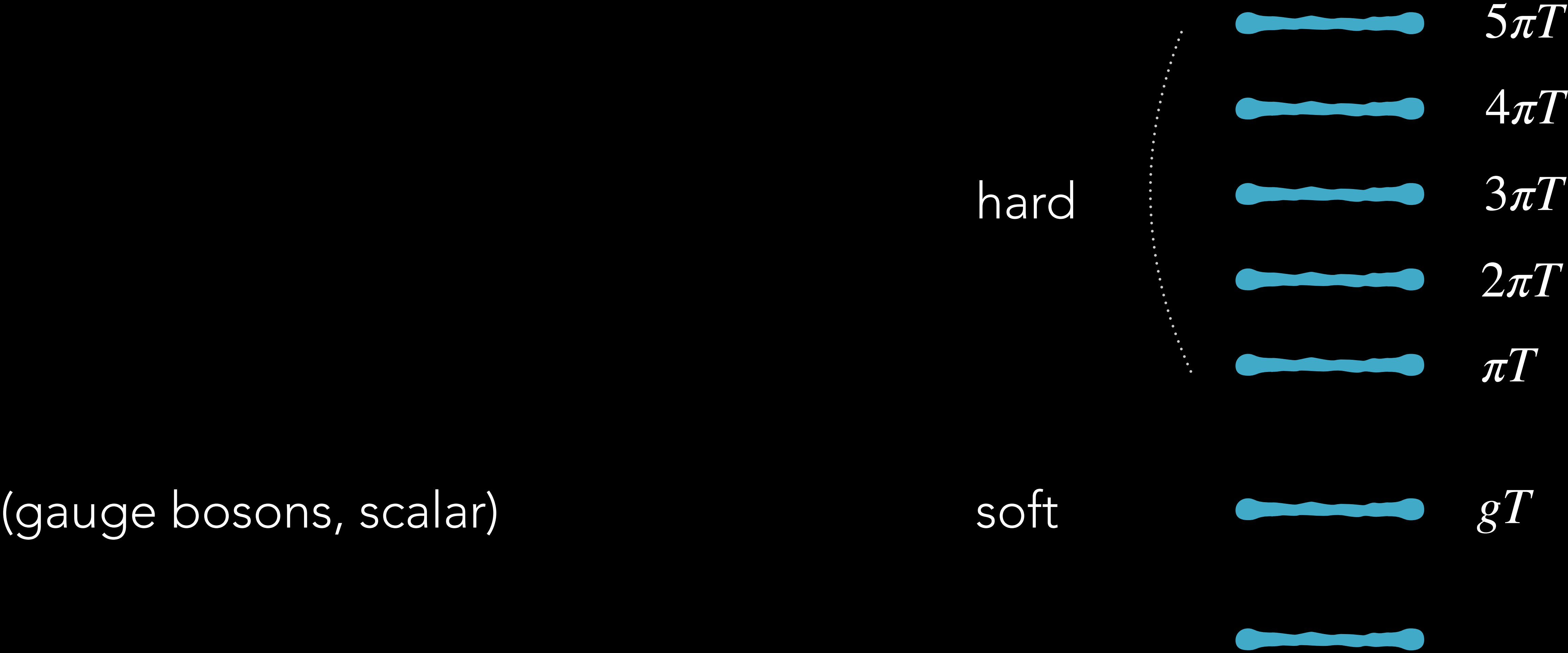
➡ See the talk by M. Kulejewski for particle production from the field evolution

HT EFT CONSTRUCTION

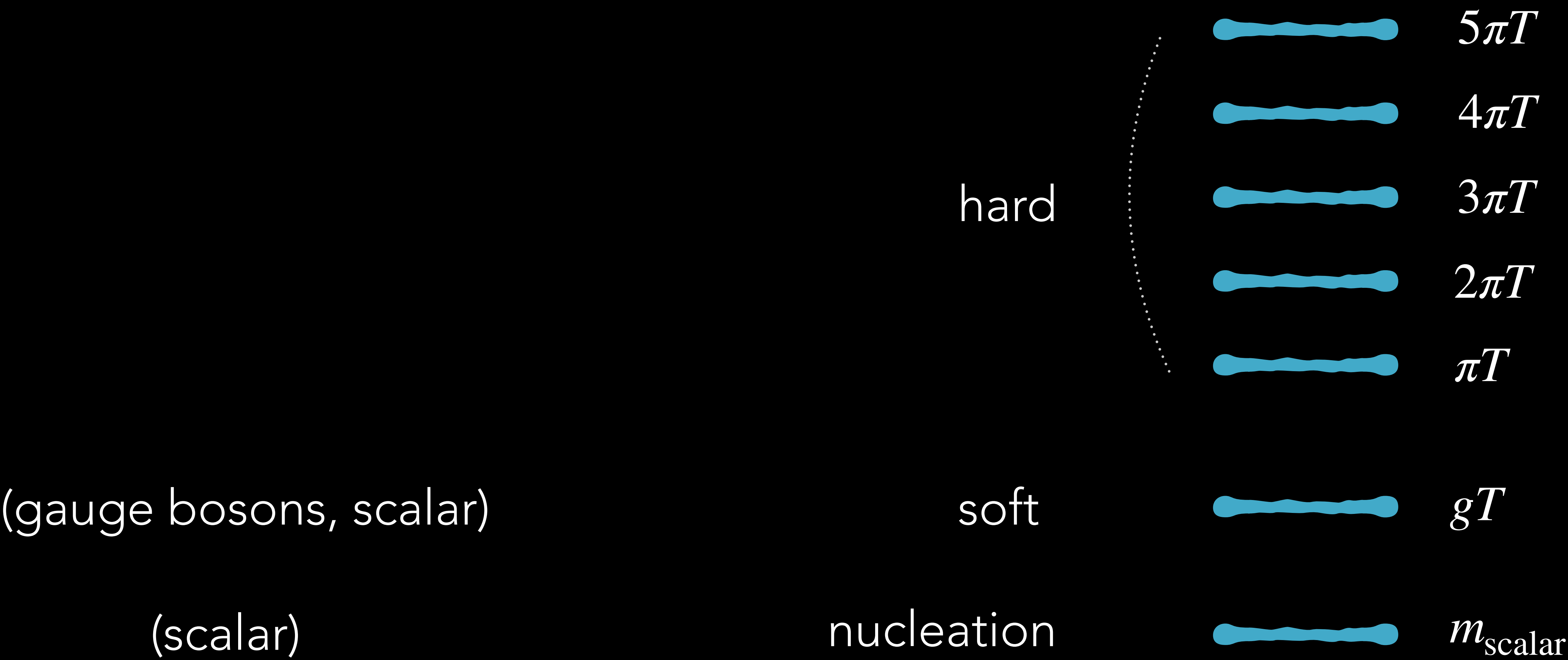
hard



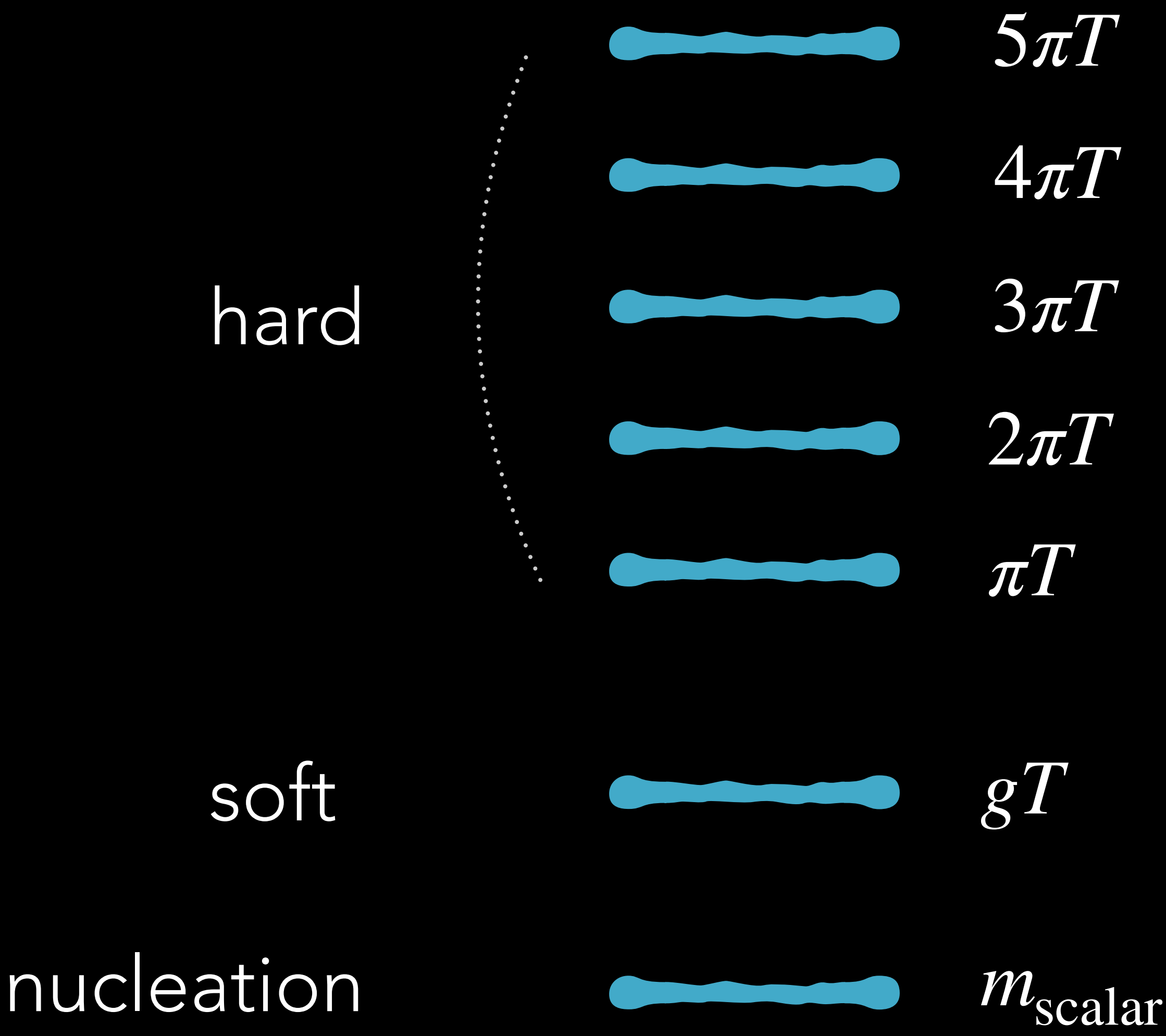
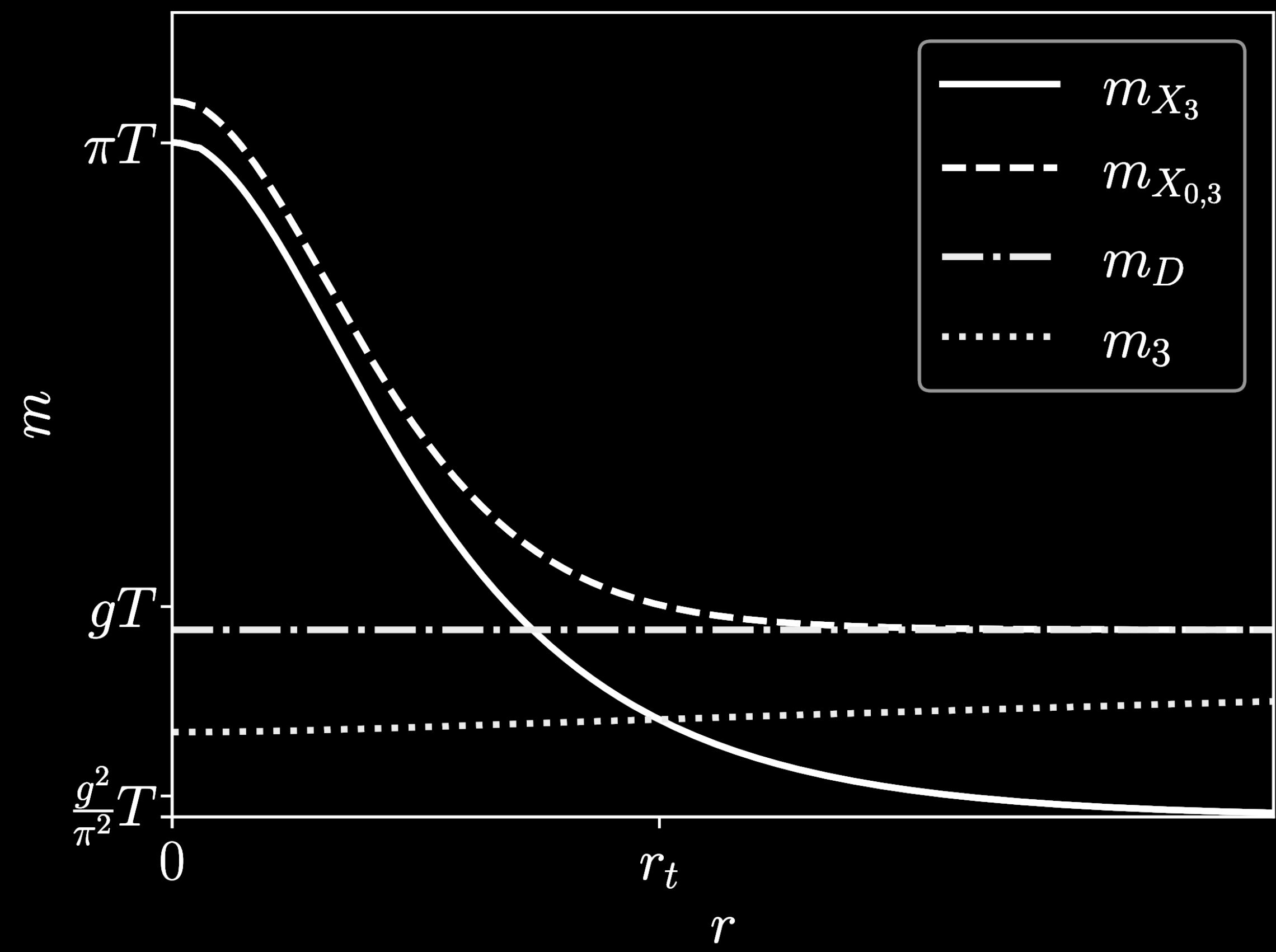
HT EFT CONSTRUCTION



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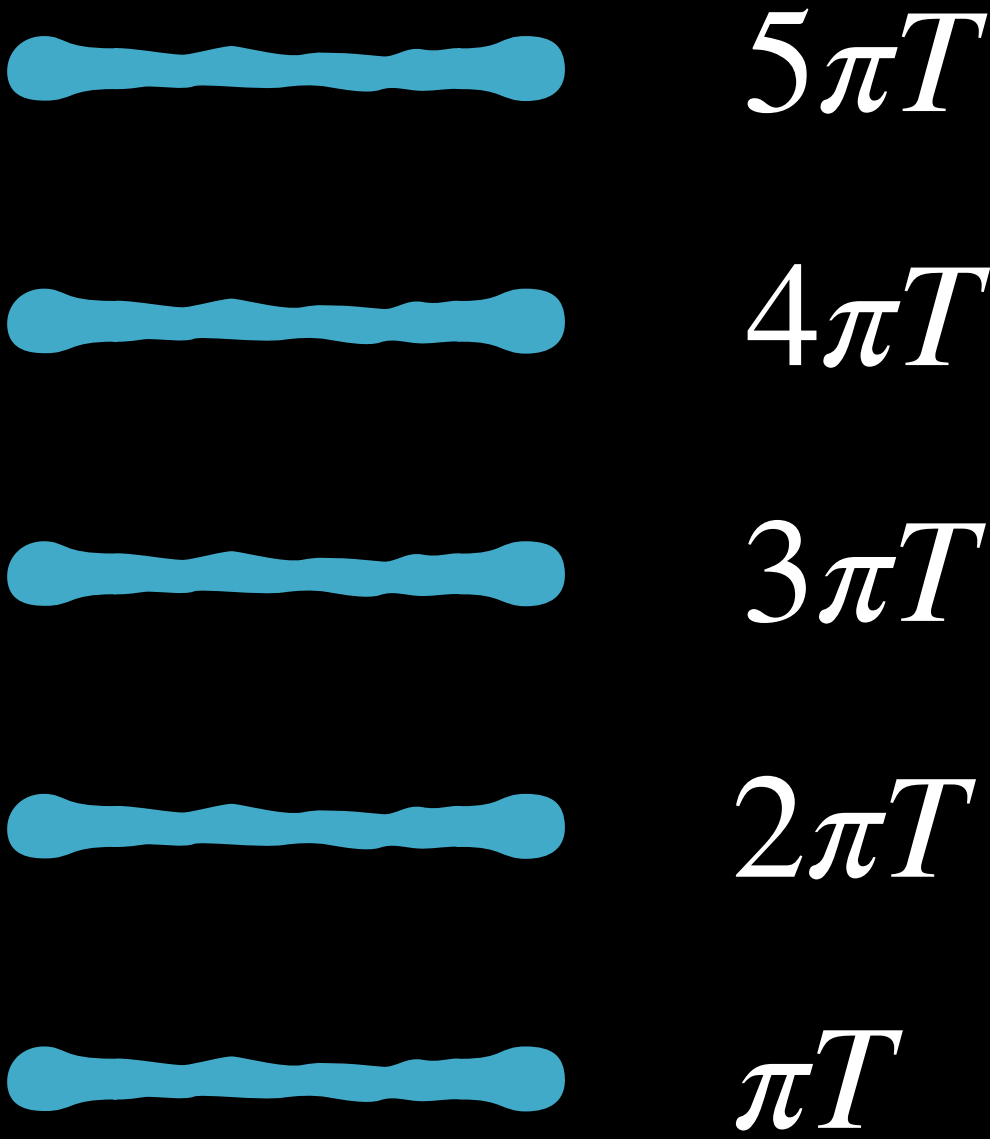
HT EFT CONSTRUCTION

2-loop matching
with DRalgo

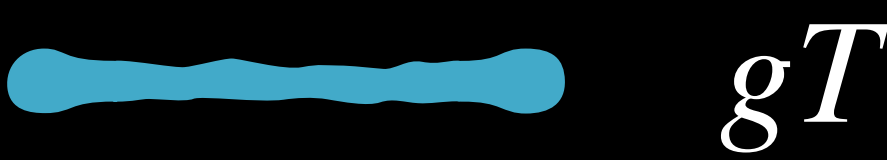
(gauge bosons, scalar)

(scalar)

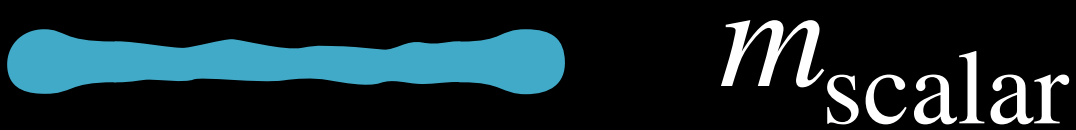
hard



soft



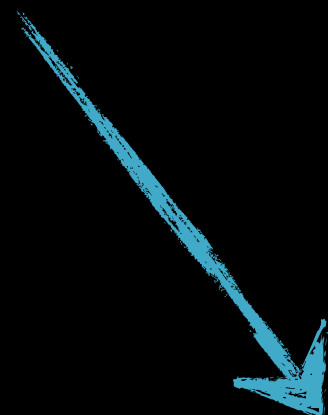
nucleation



WHAT'S NEW AT NLO?

$$S_3^{\text{EFT, NLO}} = 4\pi \int dr \, r^2 \left(\frac{1}{2} Z_3^{\text{NLO}}(v_3) (\partial_i v_3)^2 + V_3^{\text{EFT, NLO}}(v_3) \right)$$

- 
- New effective operator in the kinetic term
 - Behaves badly for $\varphi_3 \rightarrow 0$

- 
- two-loop matching
 - NLO potential
 - Includes missing (4d) RG scale dependence
 - 3d scale invariant

WHAT'S NEW AT NLO?

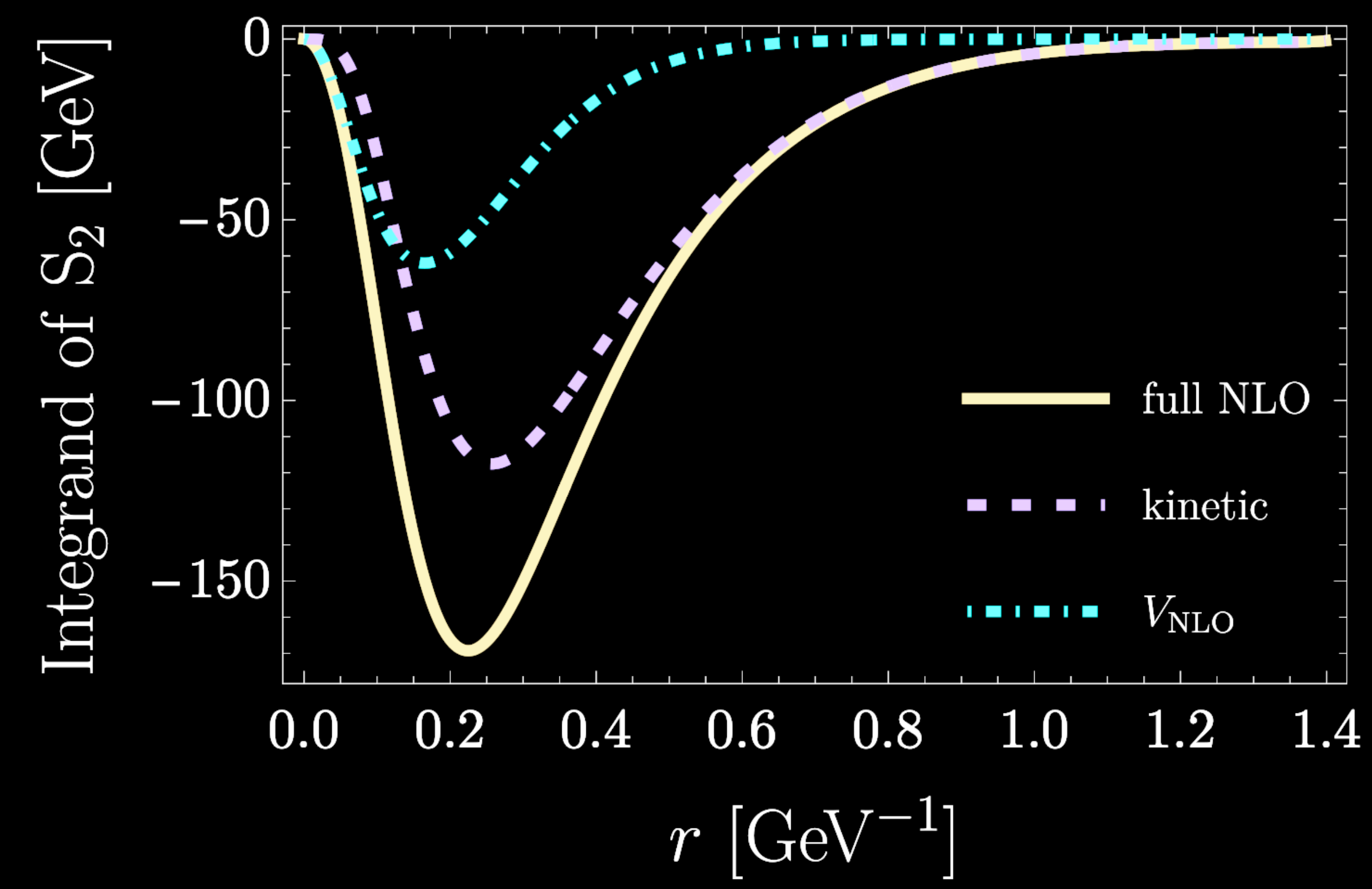
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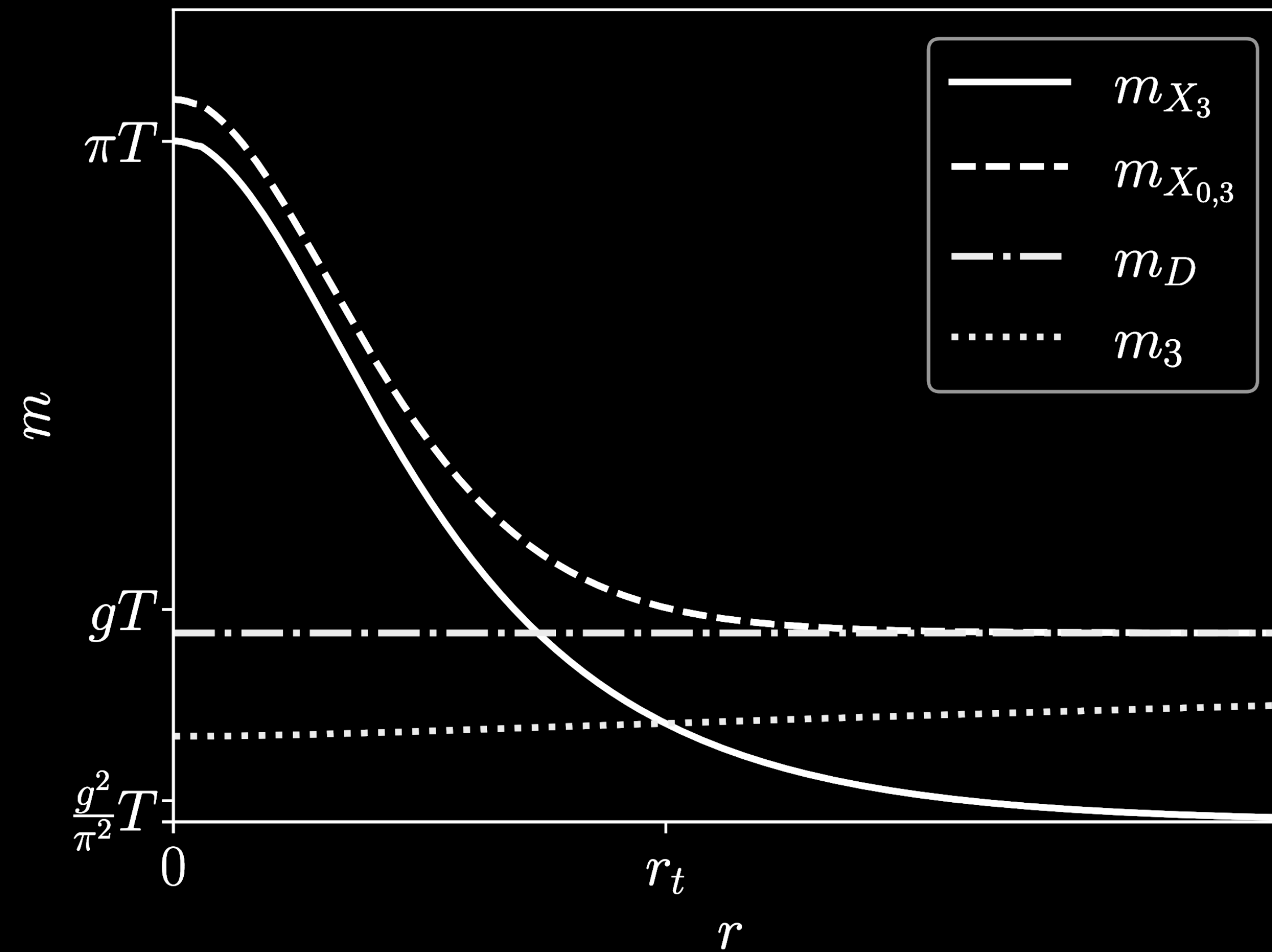
Up to 100% corrections to percolation temperature!

MOMENTUM EXPANSION



[M. Kierkla, BŚ, T.V.I. Tenkanen, J. van de Vis, JHEP 02 (2024) 234]

VALIDITY OF EFT — SCALE-SHIFTERS



[M. Kierkla, BŚ, T.V.I. Tenkanen, J. van de Vis, JHEP 02 (2024) 234]

NUCLEATION RATE BEYOND LEADING ORDER

$$\Gamma = A_{\text{dyn}} \cdot A_{\text{stat}}$$

$$A_{\text{stat}} = \prod_a \mathcal{J}_a \mathcal{V}_a \sqrt{\frac{\det \mathcal{O}_a(\varphi_F)}{\det' \mathcal{O}_a(\varphi_b)}} \mathcal{J}_\phi \sqrt{\left| \frac{\det \mathcal{O}_\phi(\varphi_F)}{\det' \mathcal{O}_\phi(\varphi_b)} \right|} e^{-(S[\varphi_b] + C[\varphi_b])}$$

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Inclusion of fluctuations
from the scale-shifting fields

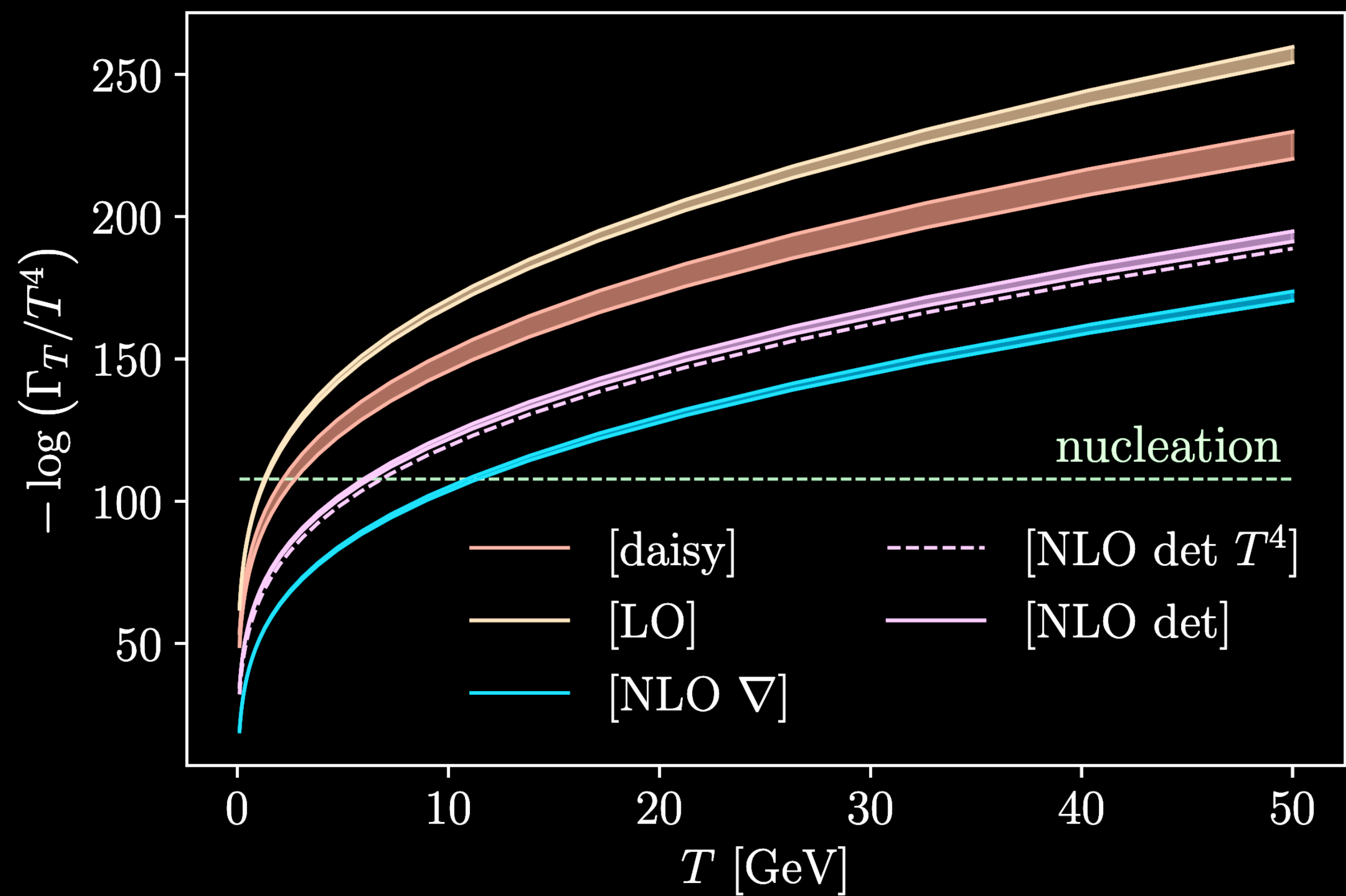
Test of validity of the
momentum expansion

Test of the
approximations for the
scalar prefactor &
quantum fluctuations

Remove the
contribution from the
scale shifting fields

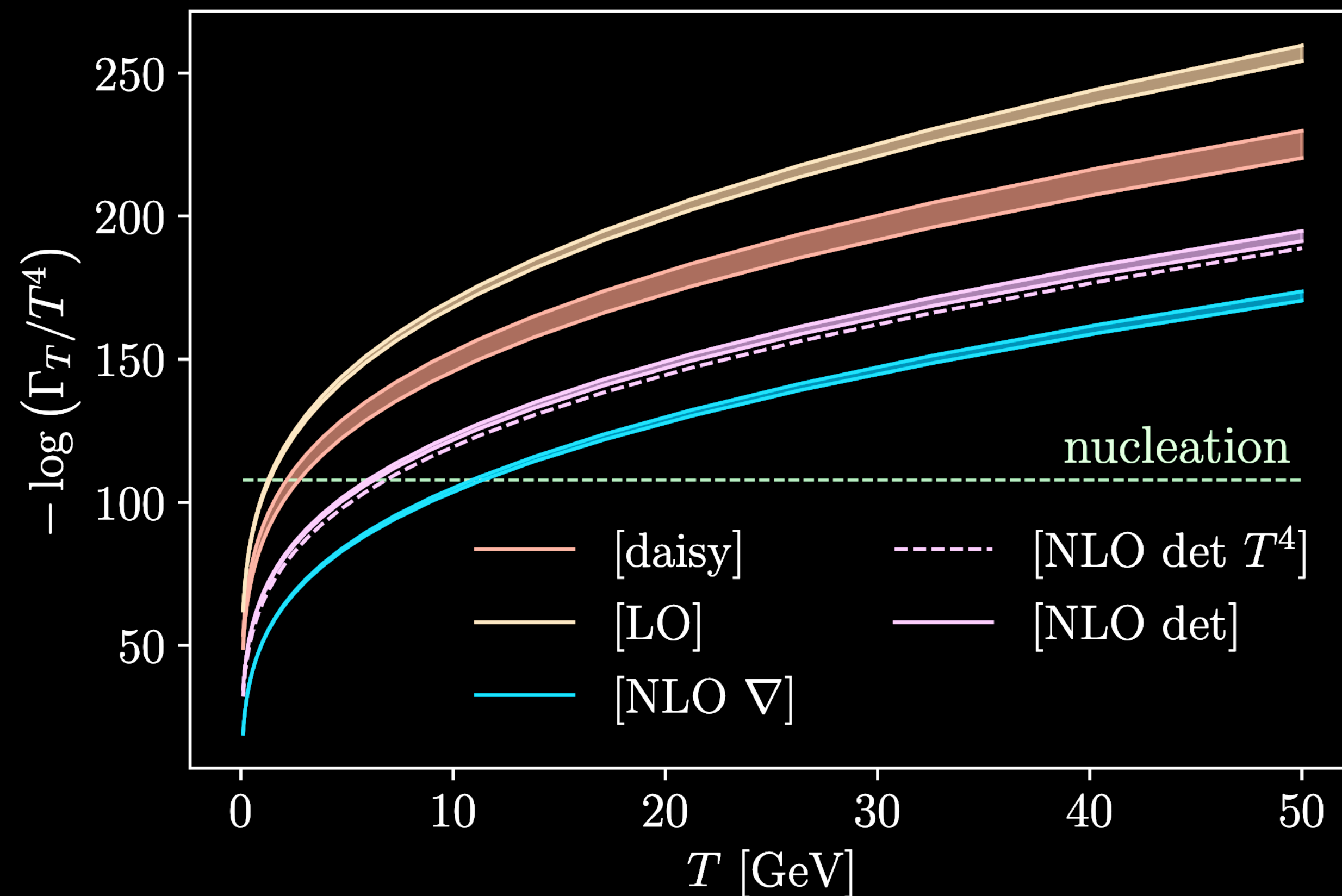
COMPARISON OF DIFFERENT APPROXIMATIONS

$$\Gamma = A_{\text{dyn}} \cdot A_{\text{stat}} \quad A_{\text{stat}} = \prod_a \mathcal{J}_a \mathcal{V}_a \sqrt{\frac{\det \mathcal{O}_a(\varphi_F)}{\det \mathcal{O}_a(\varphi_b)}} \mathcal{J}_\phi \sqrt{\left| \frac{\det \mathcal{O}_\phi(\varphi_F)}{\det \mathcal{O}_\phi(\varphi_b)} \right|} e^{-(S[\varphi_b] - S[\varphi_F])}$$



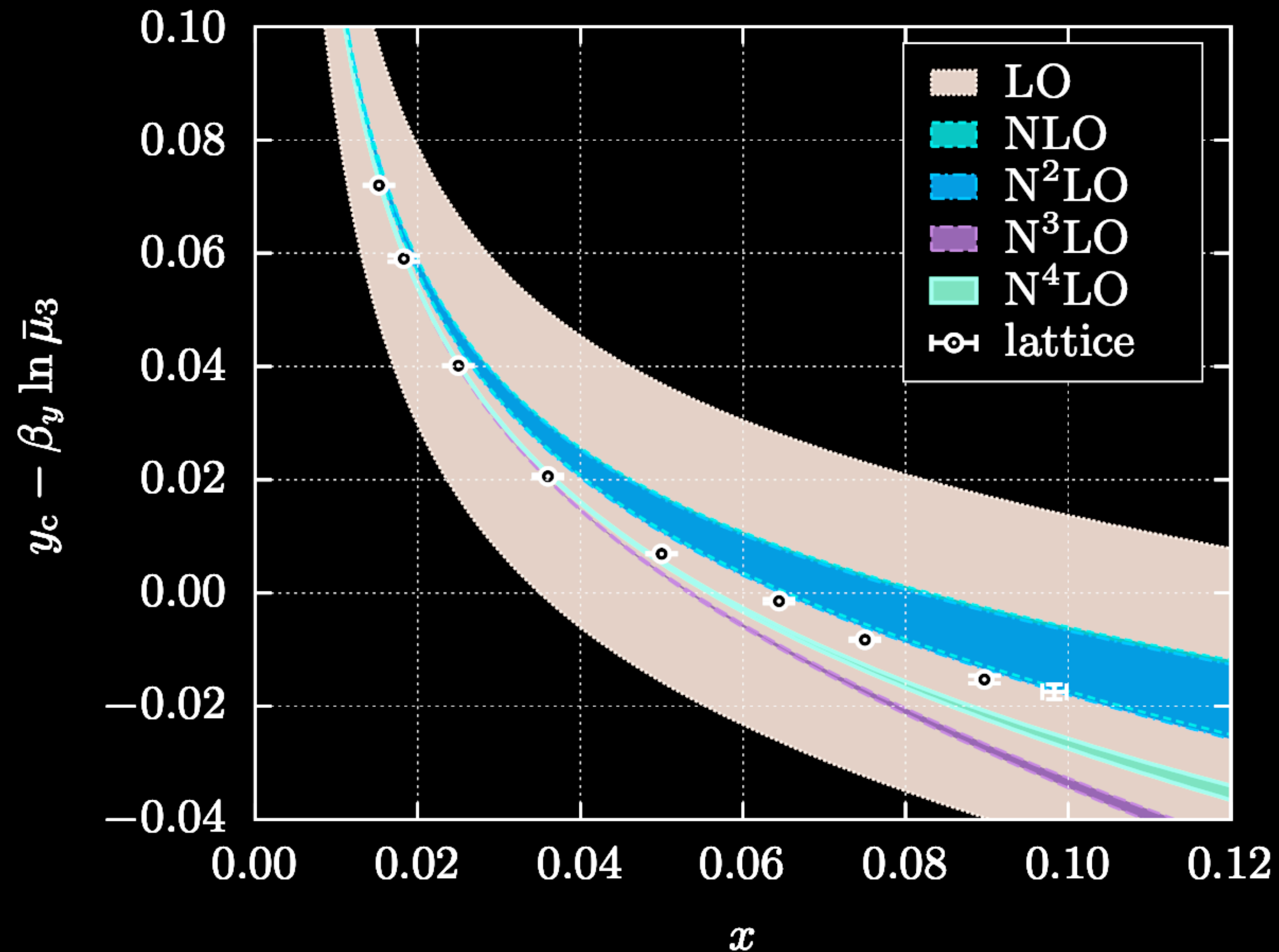
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- Up to 300% difference in percolation temperature
- 30% difference in the bubble radius

IS THE PERTURBATIVE APPROACH RELIABLE?



- Convergence in thermodynamical studies
- No lattice computation with $\lambda < 0$

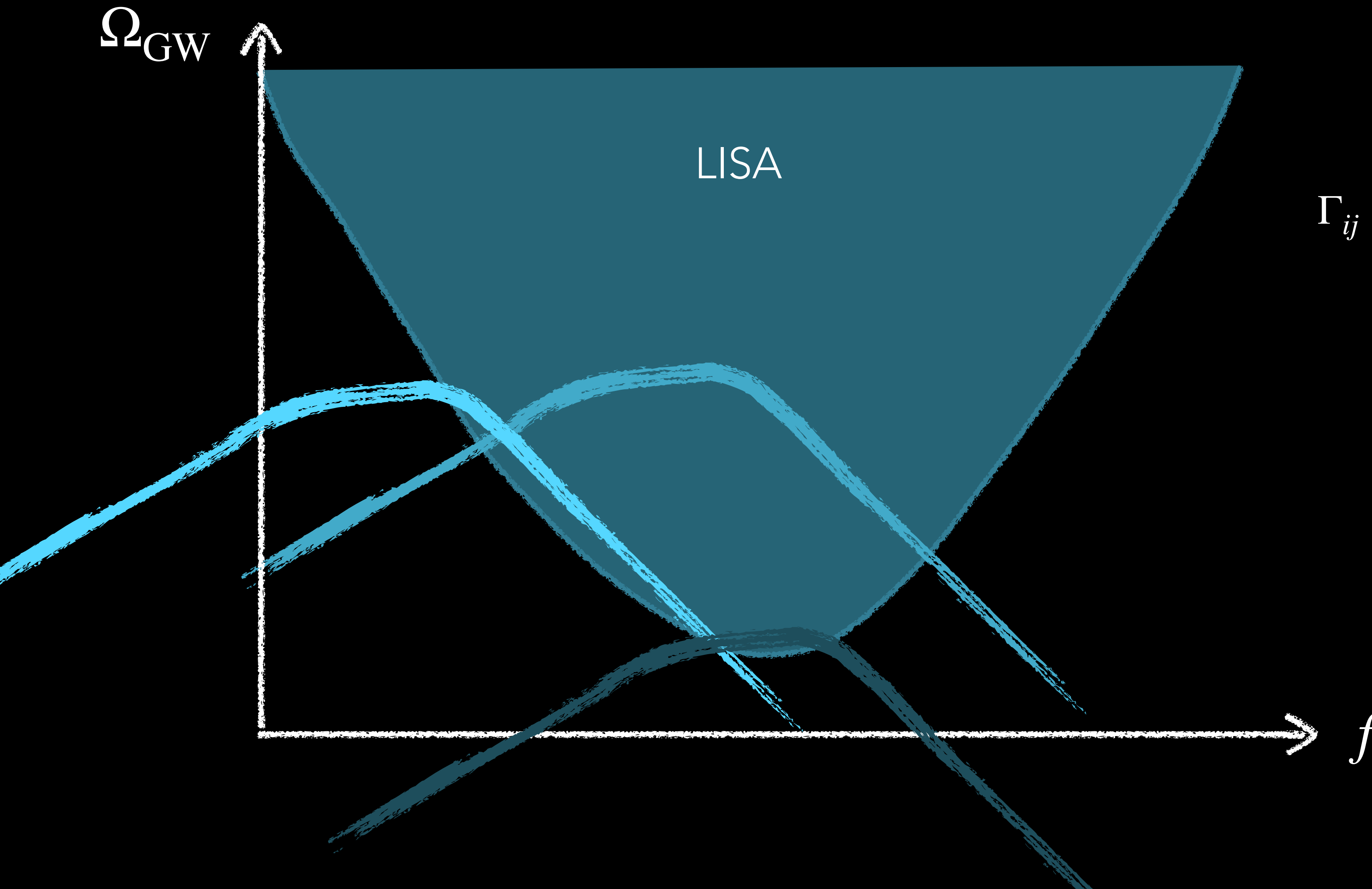
[figure adapted from: A. Ekstedt, P. Schicho, T. V. I. Tenkanen, Phys.Rev.D 110 (2024) 9, 096006]

[See also: O. Gould and T. V. I. Tenkanen, JHEP 01 (2024) 048, L. Niemi et al. PRL 126 (2021) 171802, PRD 110 (2024) 115016]

THE INVERSE PROBLEM



EXTRACTING INFORMATION FROM GW SPECTRUM



$$\Gamma_{ij} = T \int \frac{df}{\Omega_{\text{tot}}(f)^2} \frac{\partial \Omega_{\text{GW}}}{\partial \theta_i} \frac{\partial \Omega_{\text{GW}}}{\partial \theta_j}$$

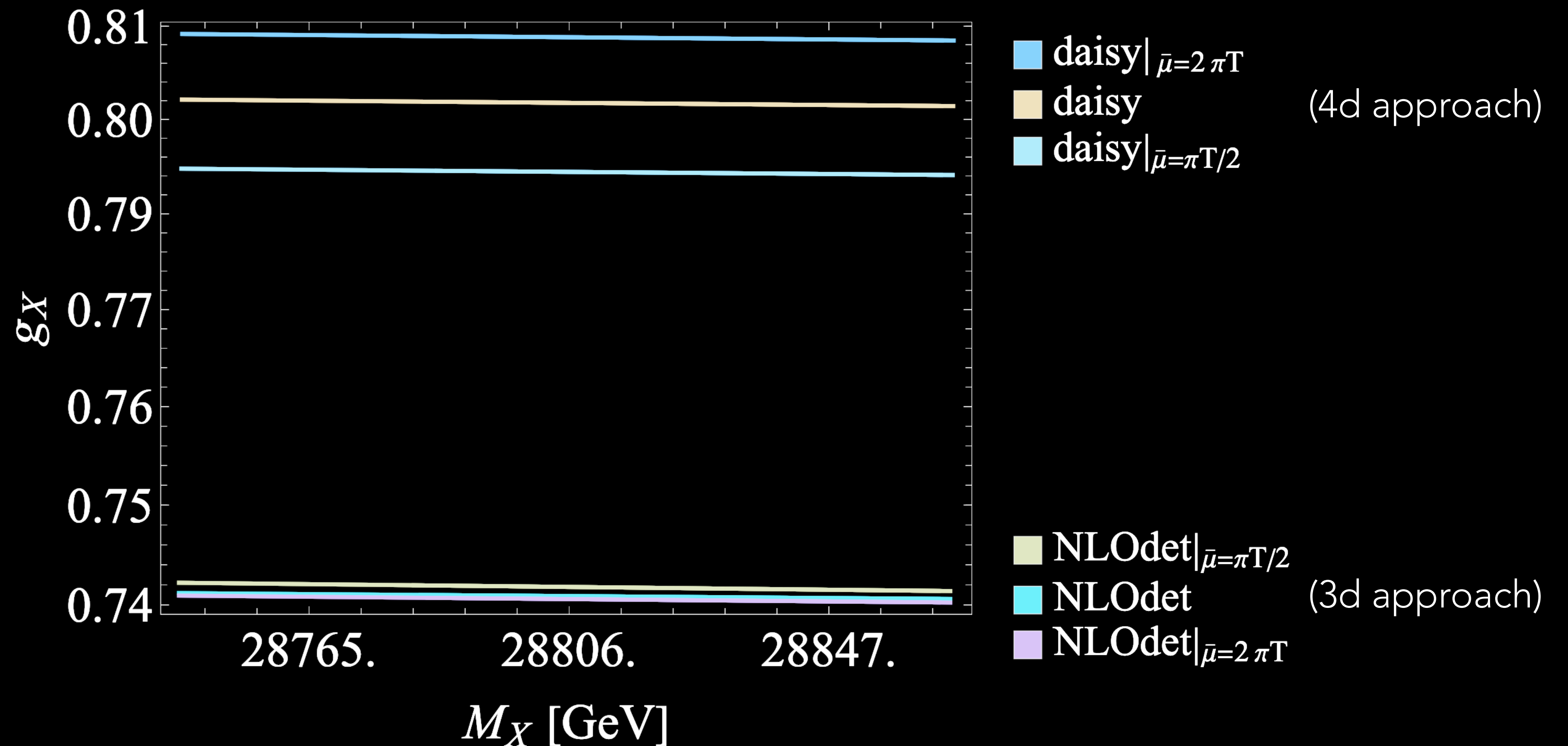
$$\sigma_{ij}^2 = (\Gamma^{-1})_{ij}$$

$$\sigma_{g_X} = \sqrt{\sigma_{g_X g_X}^2}$$

$$\sigma_{M_X} = \sqrt{\sigma_{M_X M_X}^2}$$

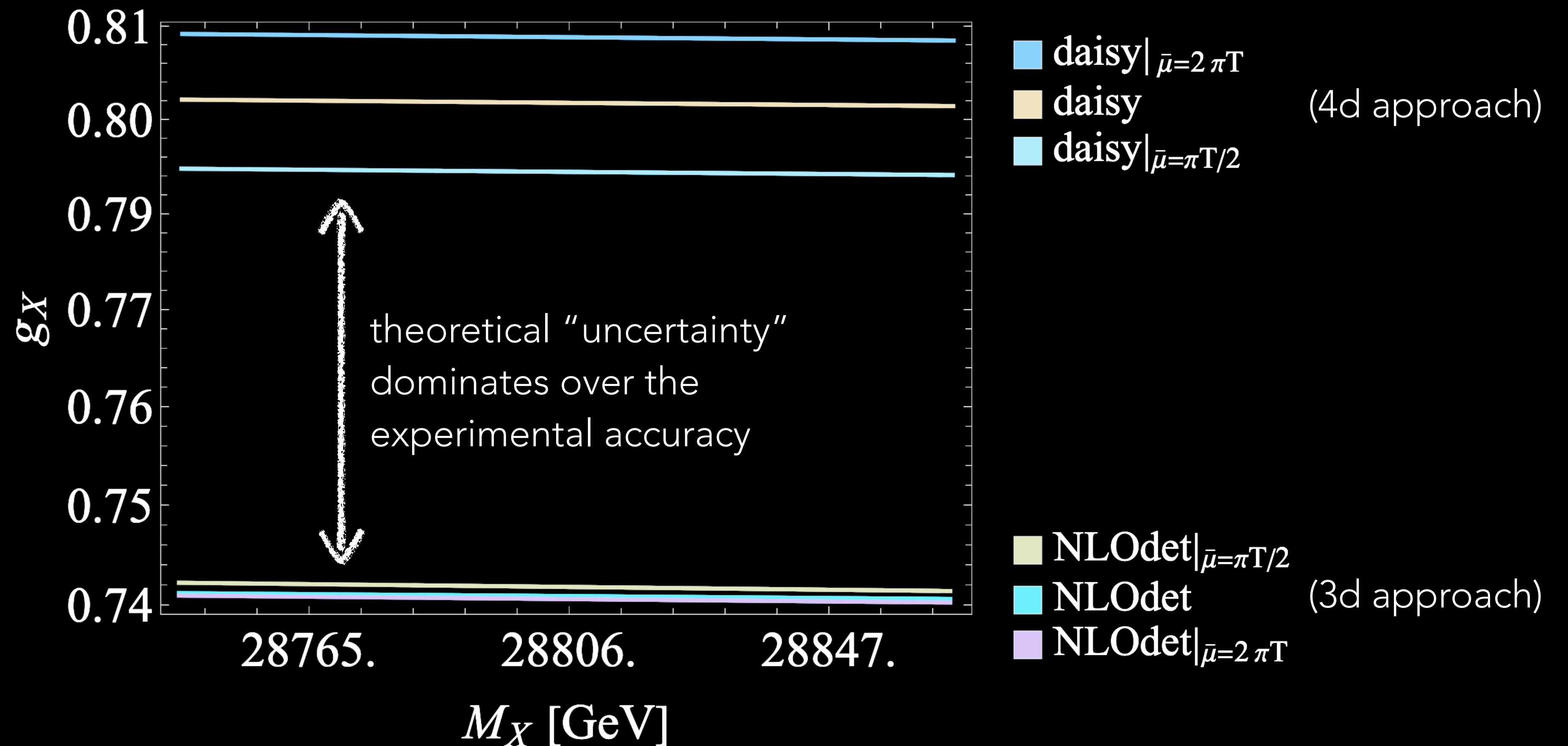
RECONSTRUCTION OF U(1) MODEL PARAMETERS

S1: $\Omega_p = 10^{-9.3}$, $f_p = 10^{-2.7}$ Hz



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HIERARCHY OF ERRORS FOR STRONG TRANSITIONS

experimental error $\sim$ residual scale dependence in 3d NLOdet approach

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scale dependence in the 3d daisy approach

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HIERARCHY OF ERRORS FOR STRONG TRANSITIONS

experimental error $\sim$ residual scale dependence in 3d NLOdet approach



scale dependence in the 3d daisy approach



difference between 3d daisy and 4d NLOdet

SUMMARY



CONCLUSIONS

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Strong GW
signals need
strong theory.

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Strong GW
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strong theory.
And weak as well

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Theoretical
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CONCLUSIONS

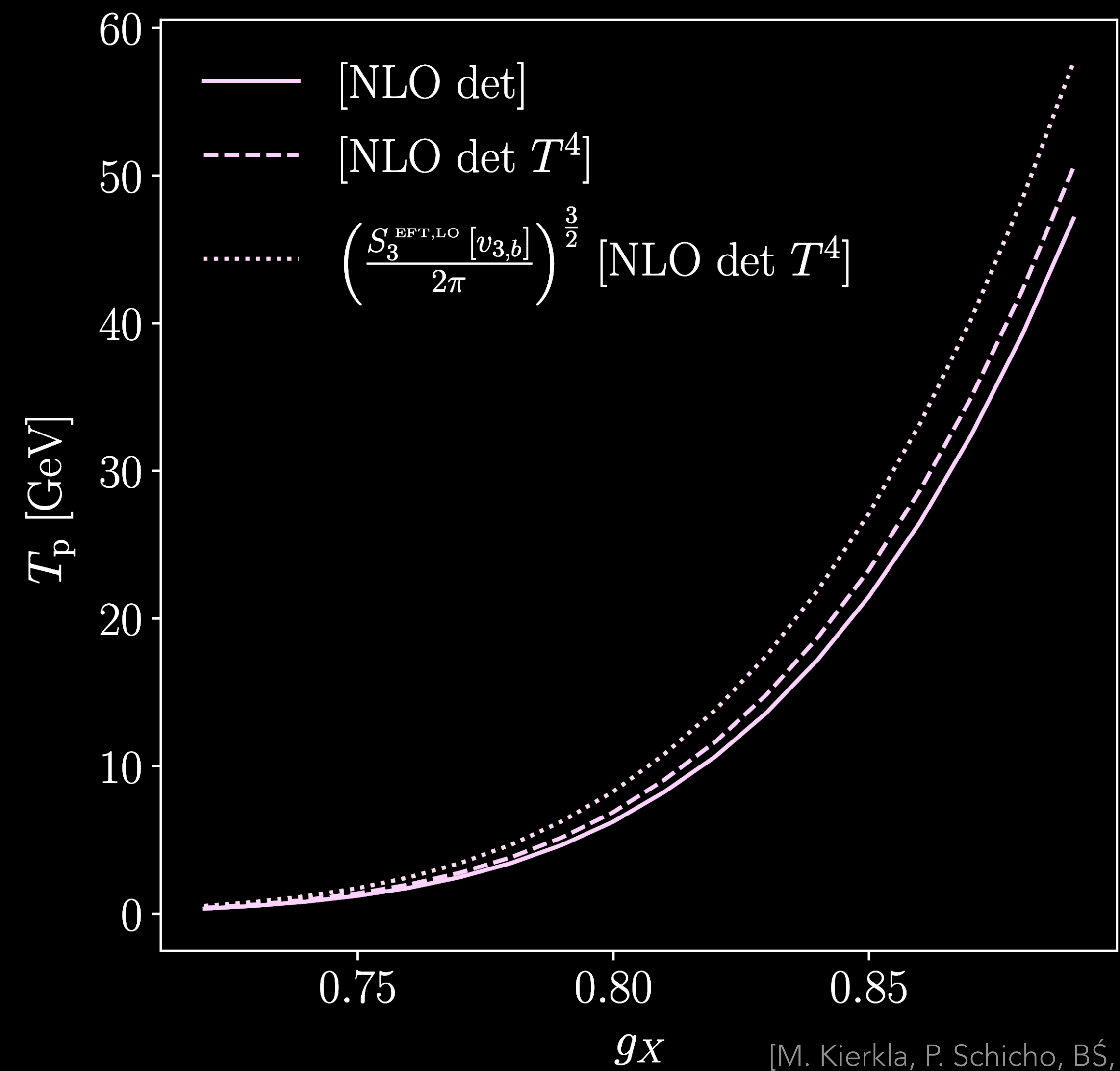
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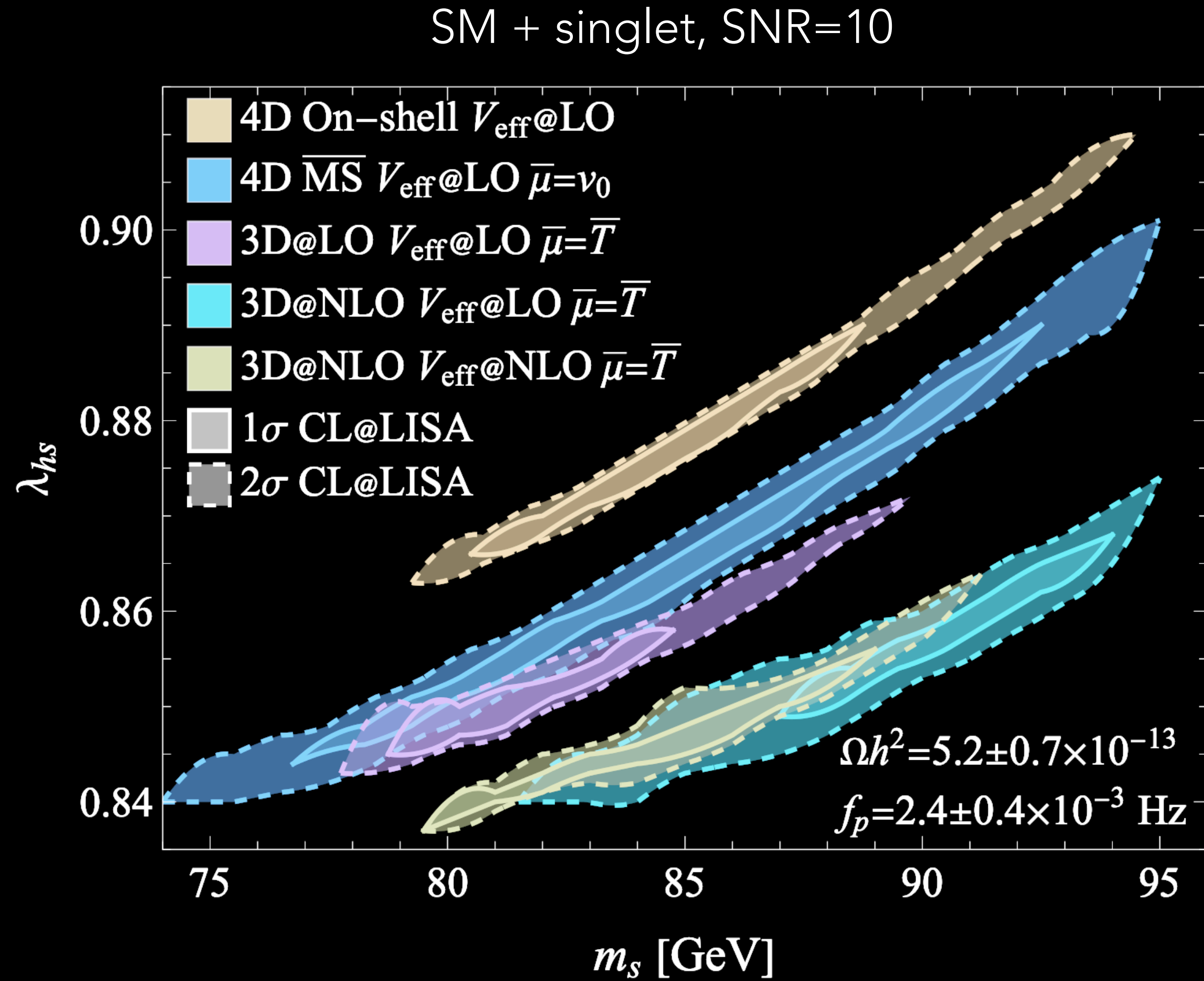
but also to
ensure the
procedures are
well-defined.

THANK YOU

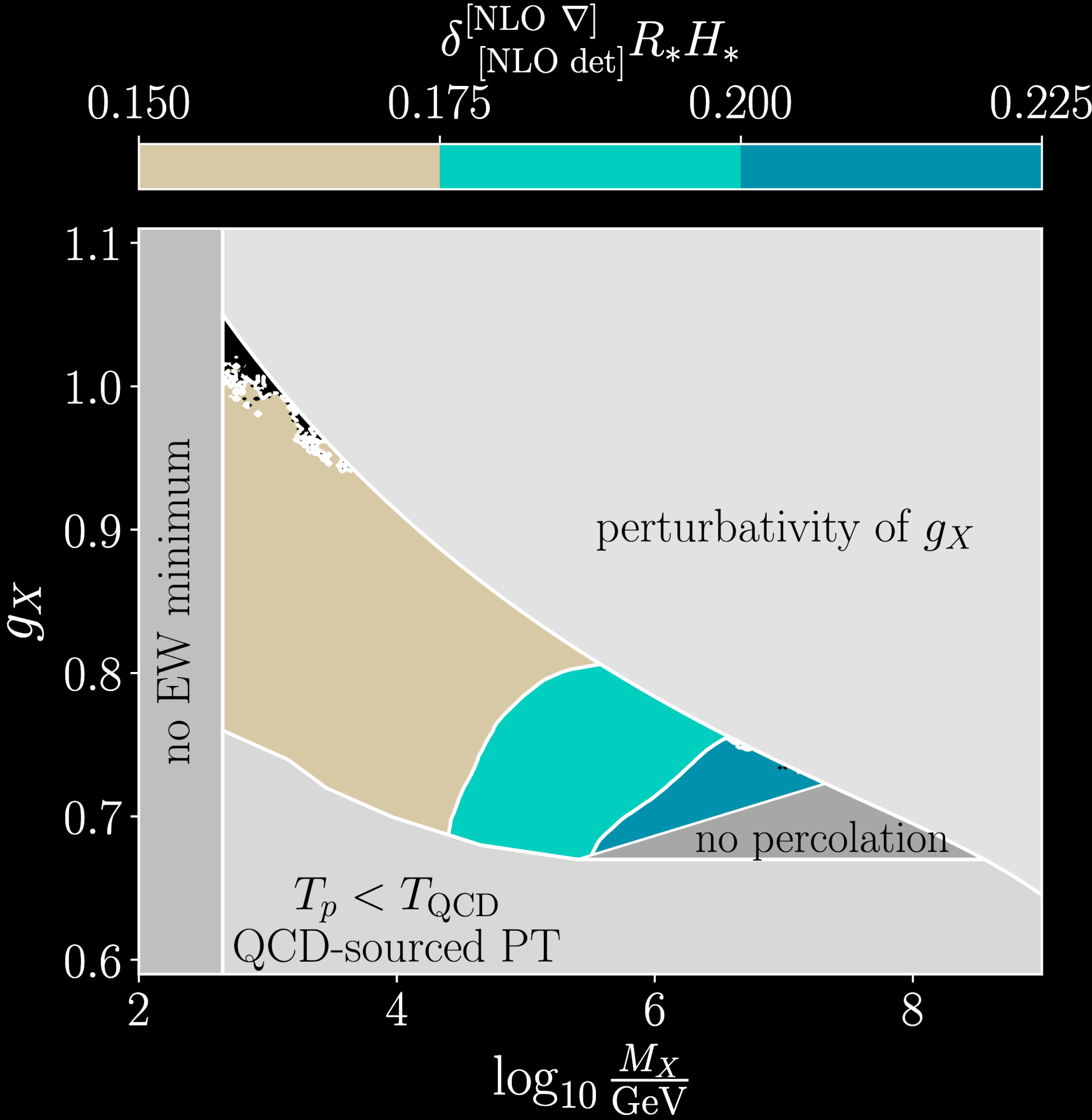
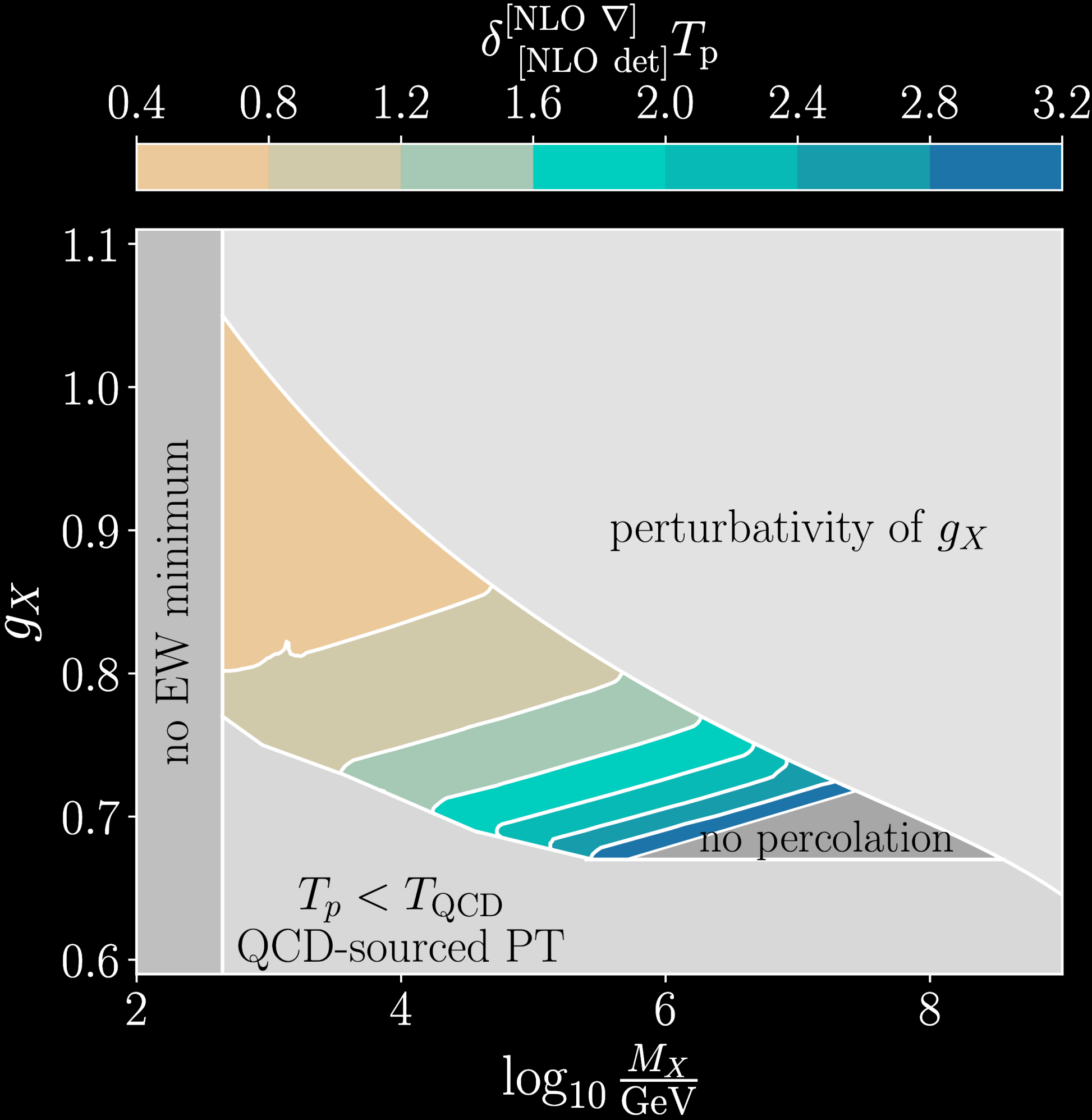
SCALAR DETERMINANT



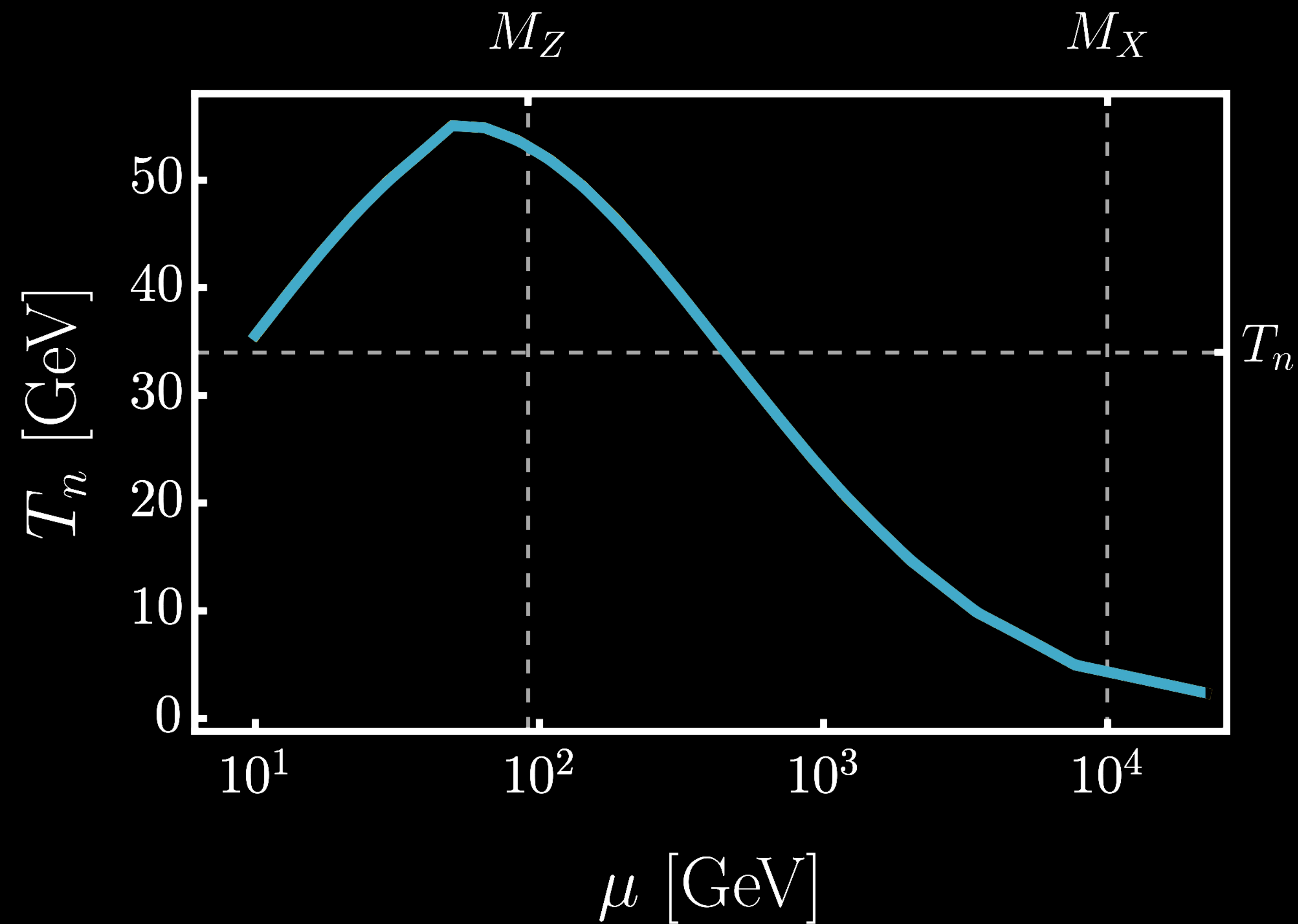
PRECISION FOR WEAKER SIGNALS



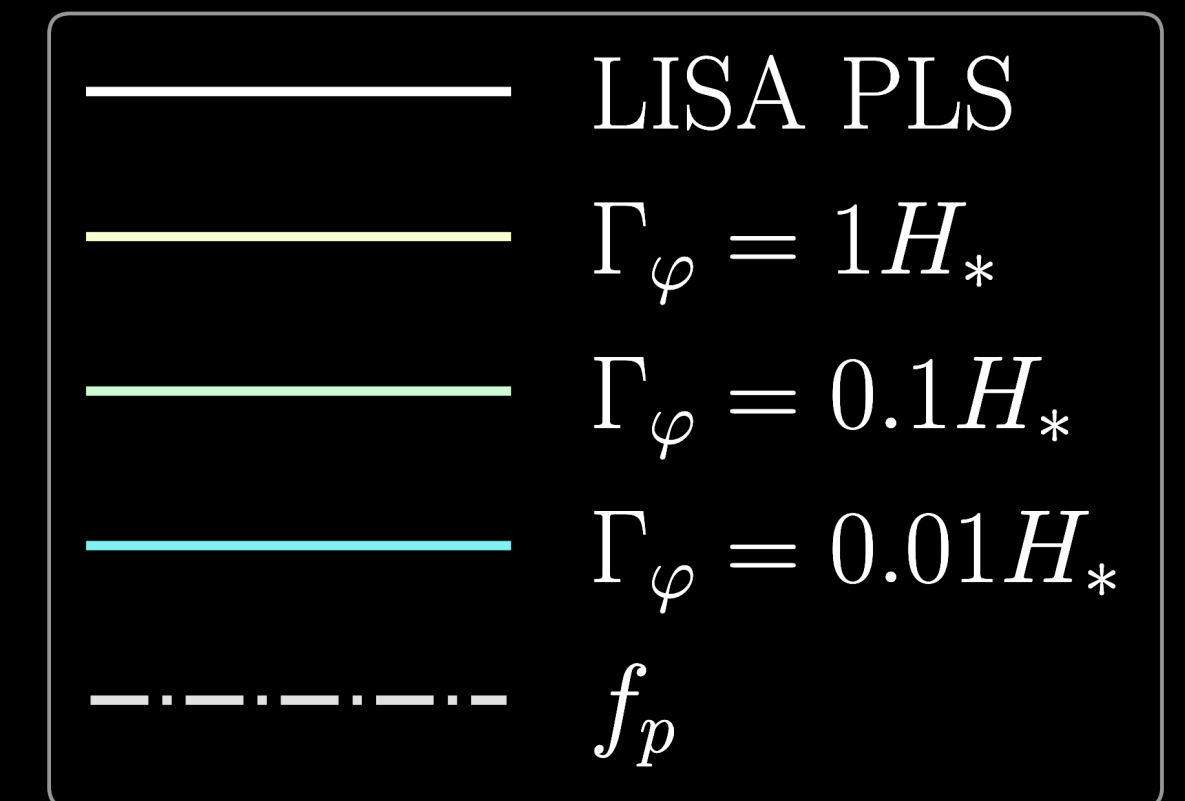
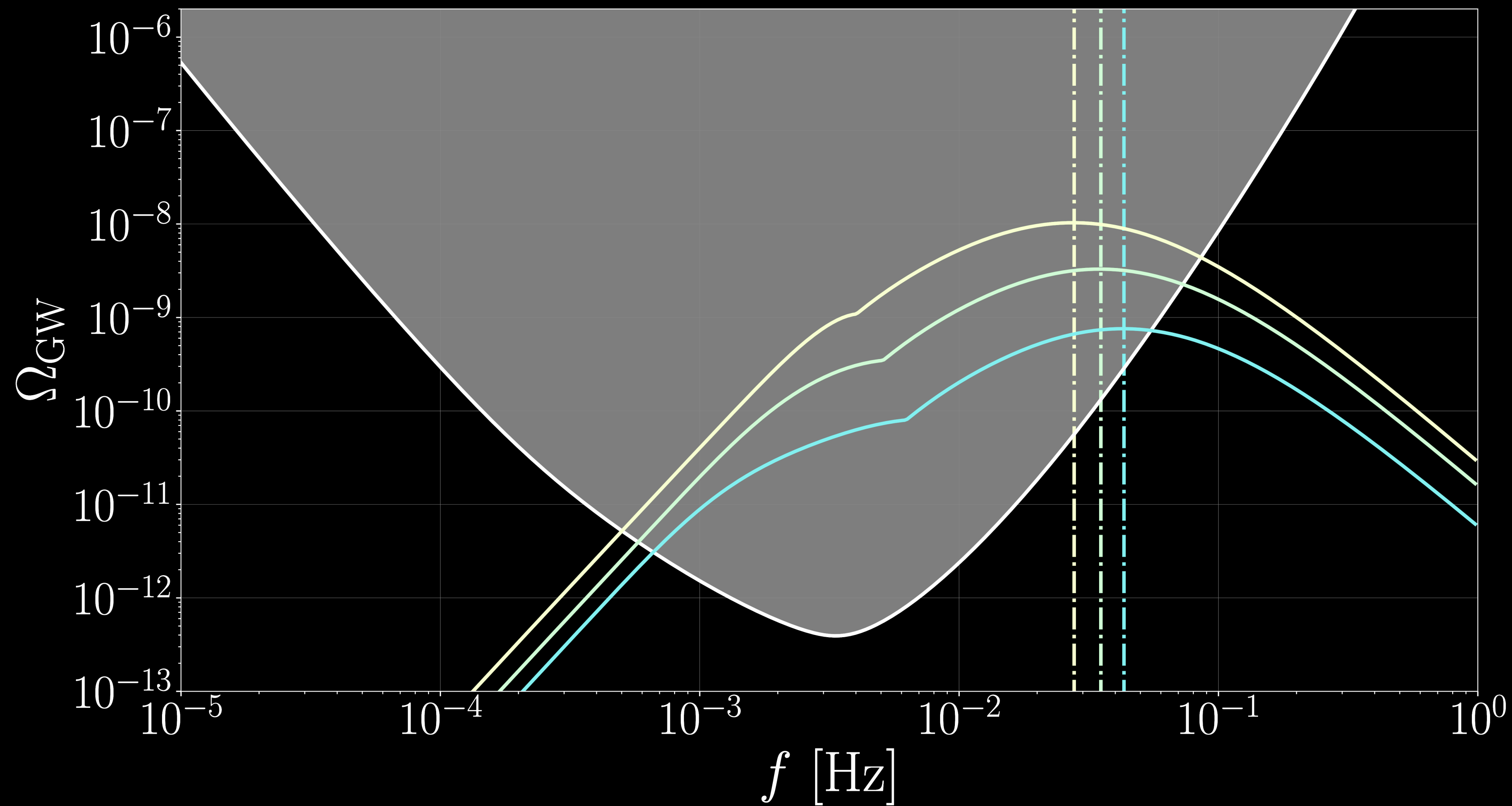
ACCURACY OF PREDICTIONS



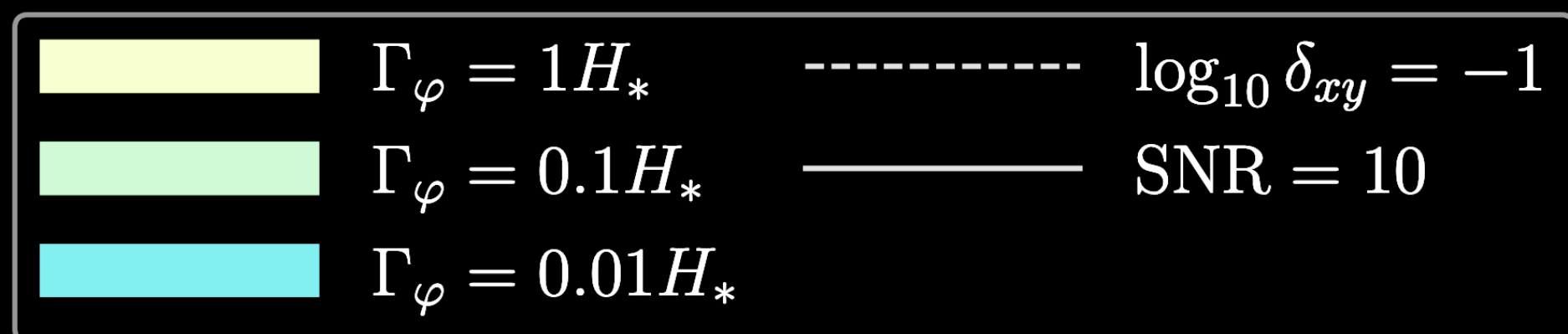
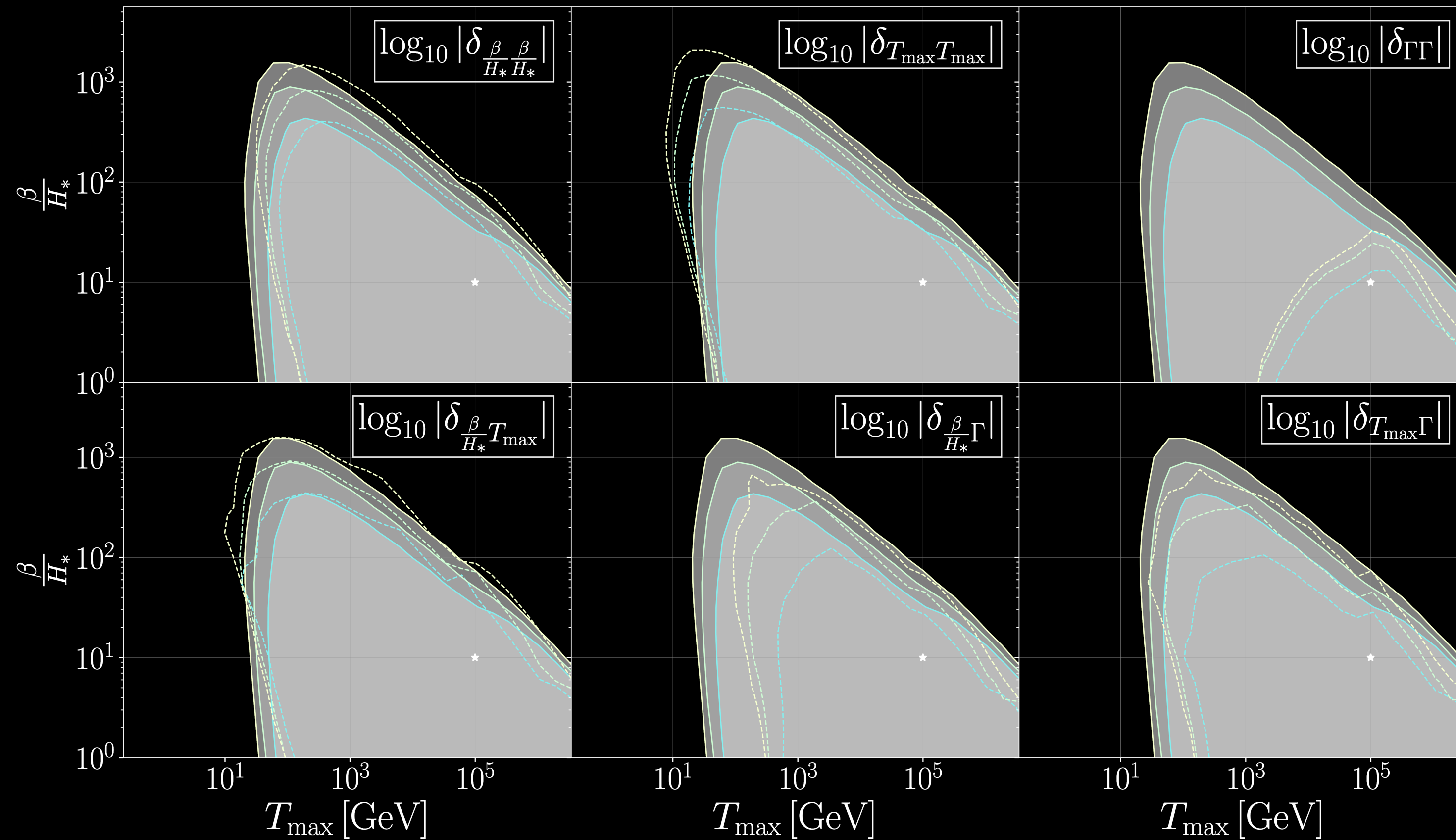
SCALE DEPENDENCE - SOURCE OF UNCERTAINTY



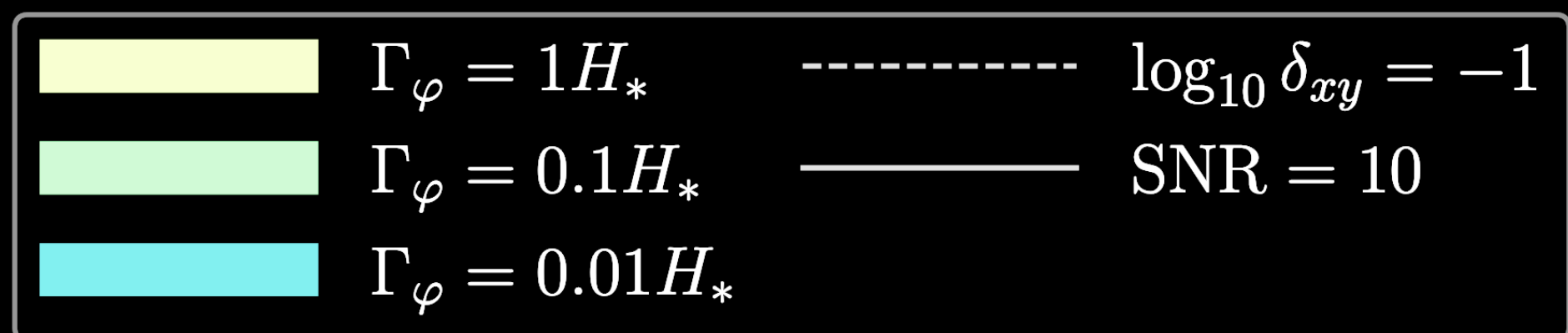
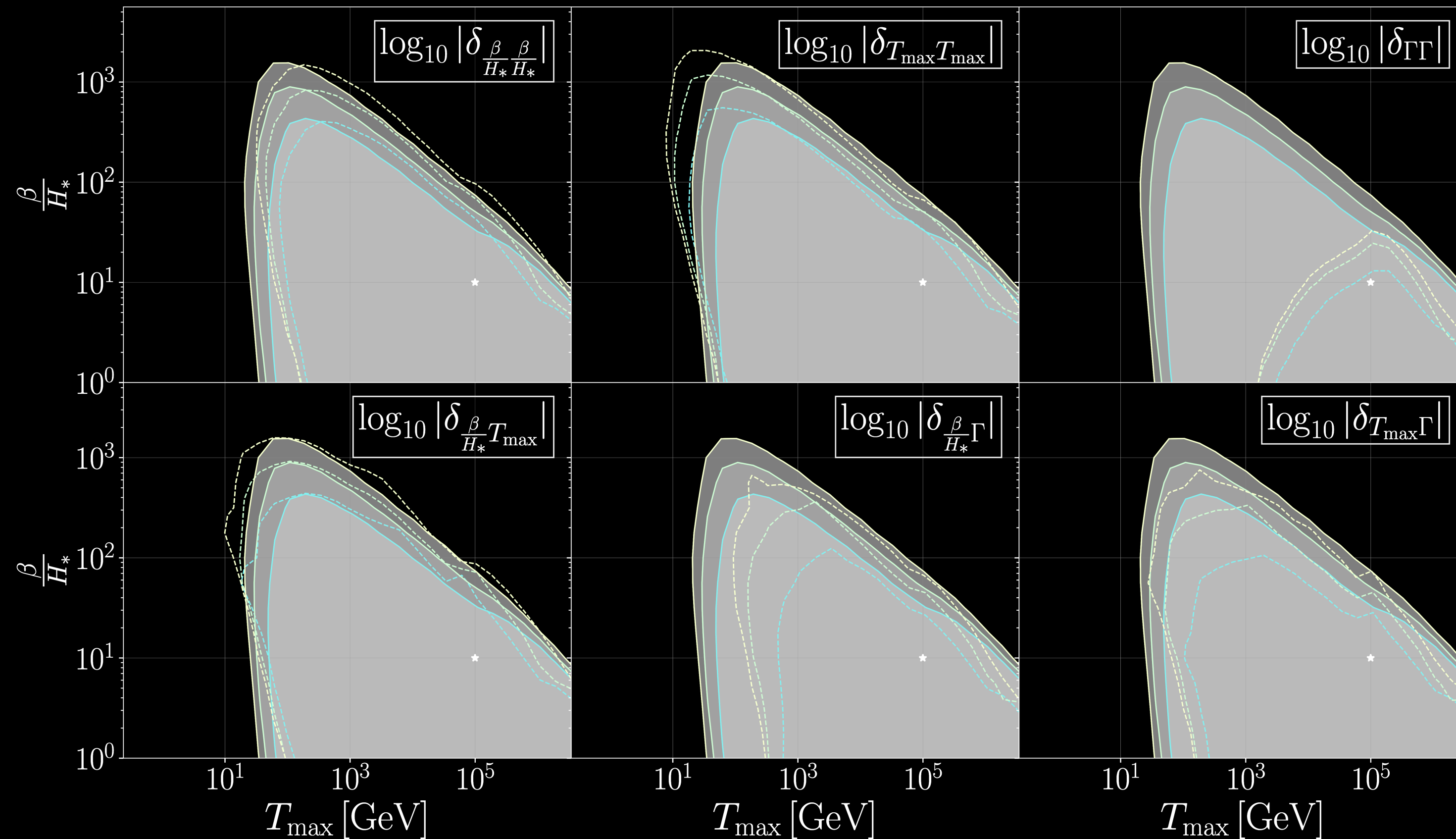
MODIFIED EXPANSION AFFECTS THE SIGNAL



WHAT CAN WE LEARN FROM THE SIGNAL?

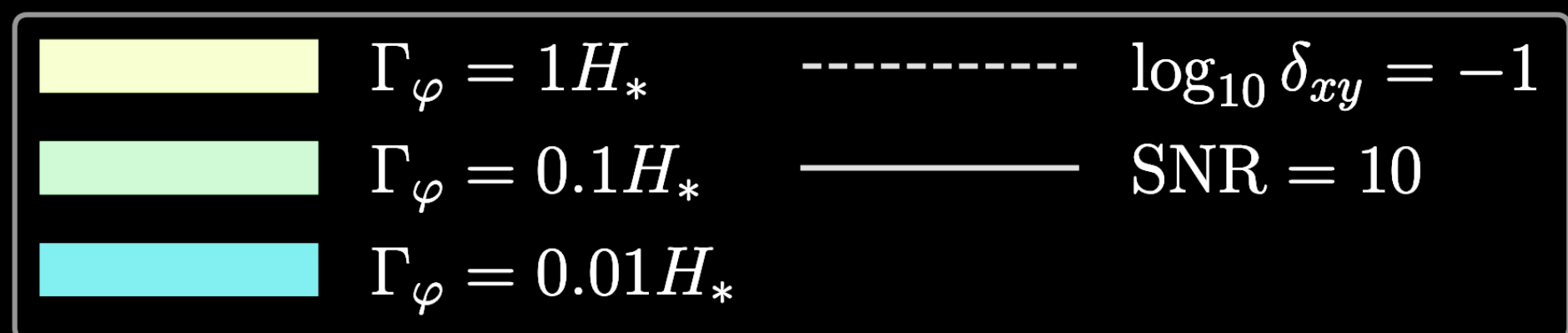
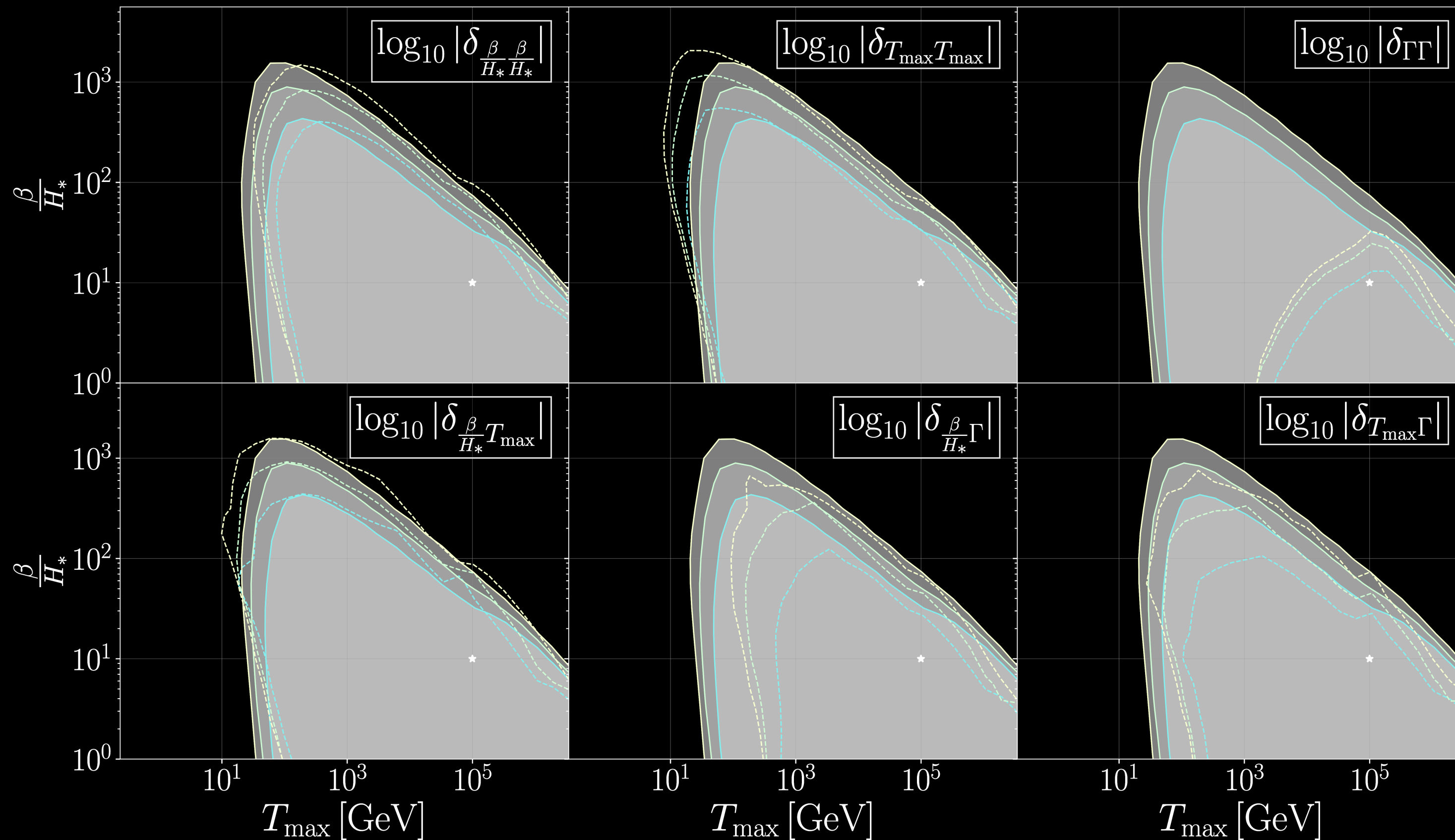


WHAT CAN WE LEARN FROM THE SIGNAL?



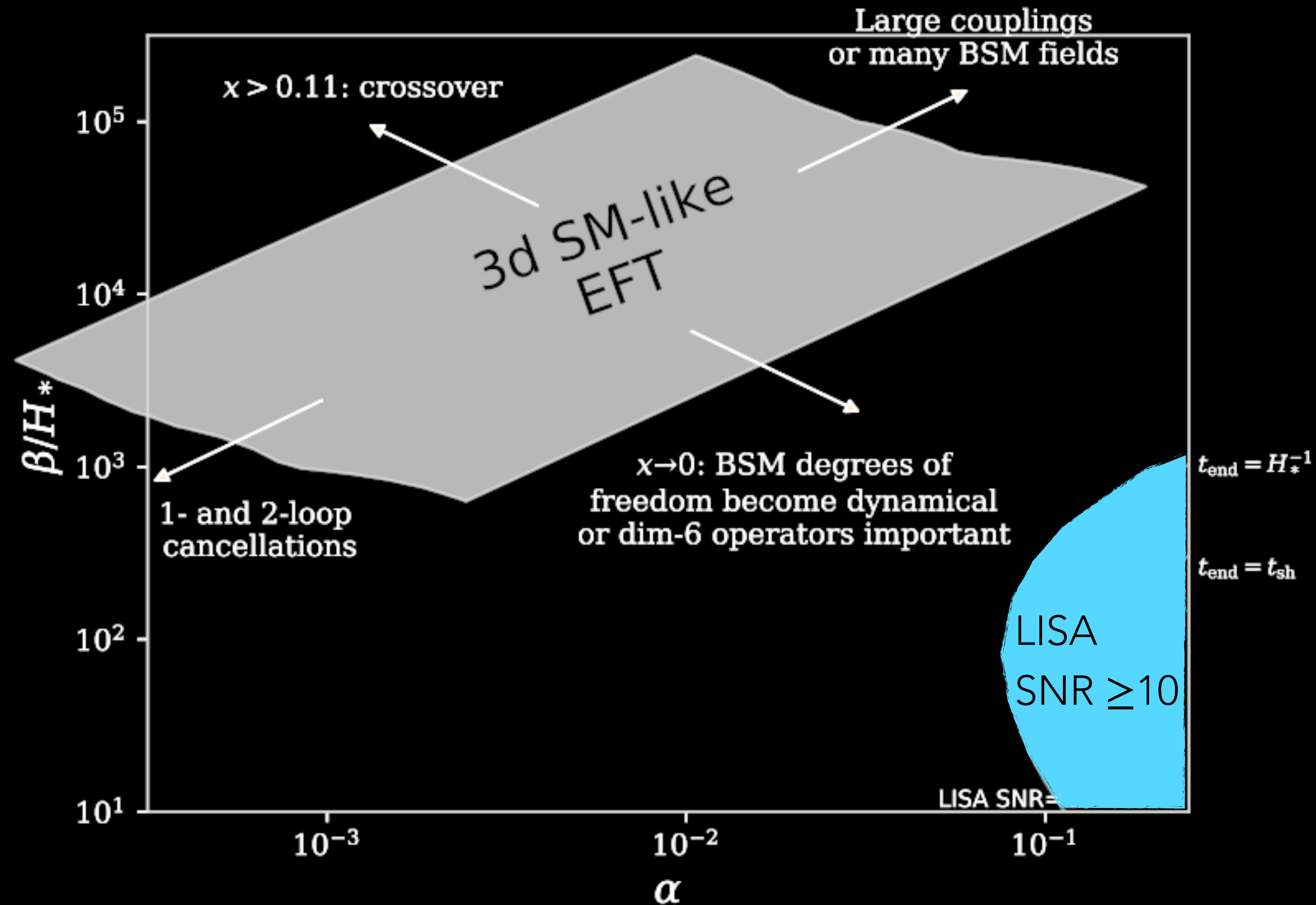
- Decay rate of the scalar (inaccessible at colliders?) can be determined from the spectrum

WHAT CAN WE LEARN FROM THE SIGNAL?



- Decay rate of the scalar (inaccessible at colliders?) can be determined from the spectrum
- Individual parameters can be determined with an accuracy better than 10%

WHAT KIND OF PT CAN BE OBSERVABLE?



[Figure adapted from: Phys.Rev.D 100 (2019) 11, 115024, O. Gould, J. Kozaczuk, L. Niemi, M. J. Ramsey-Musolf, T. V.I. Tenkanen, D. J. Weir]