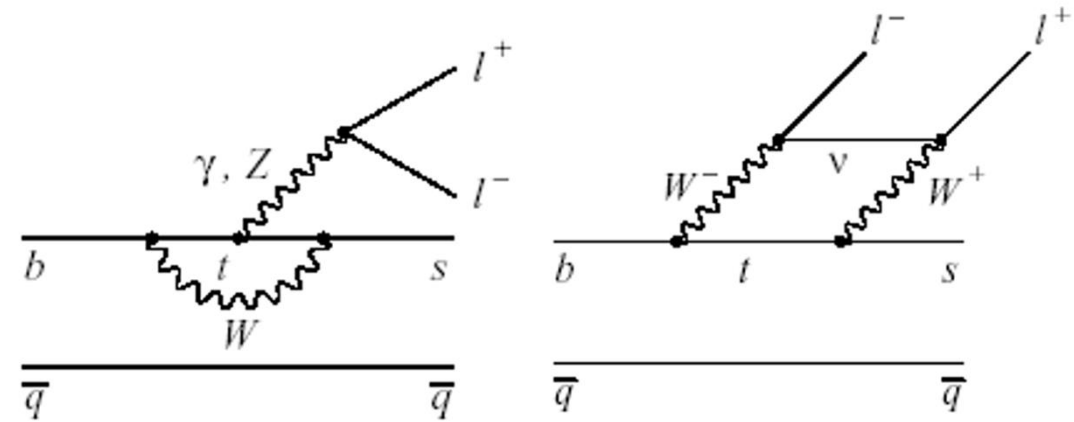


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PROBING NEW PHYSICS: VECTOR LIKE QUARKS IN RARE B-DECAYS



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OVERVIEW

- Motivation
- Standard Model
- Rare B-Decays
- Physics Beyond Standard Model
- Rare B-Decays in VQM
- Results & Conclusion
- References

MOTIVATION

- Rare B-decays are highly suppressed in the SM -- sensitive probes of New Physics (NP)
- Anomalies in Rare B-decays have been observed and by studying Rare B-decays in the presence of vector-like quarks, we aim to understand their impact on the observed experimental results and test the validity of this theoretical extension beyond Standard Model.

STANDARD MODEL AND ITS LIMITATIONS

	mass →	charge →	spin →																									
QUARKS	$\approx 2.3 \text{ MeV}/c^2$	$2/3$	$1/2$	u	up	$\approx 1.275 \text{ GeV}/c^2$	$2/3$	$1/2$	c	charm	$\approx 173.07 \text{ GeV}/c^2$	$2/3$	$1/2$	t	top	0	0	1	g	gluon	$\approx 126 \text{ GeV}/c^2$	0	0	0	H	Higgs boson		
	$\approx 4.8 \text{ MeV}/c^2$	$-1/3$	$1/2$	d	down	$\approx 95 \text{ MeV}/c^2$	$-1/3$	$1/2$	s	strange	$\approx 4.18 \text{ GeV}/c^2$	$-1/3$	$1/2$	b	bottom	0	0	1	γ	photon								
	$0.511 \text{ MeV}/c^2$	-1	$1/2$	e	electron	$105.7 \text{ MeV}/c^2$	-1	$1/2$	μ	muon	$1.777 \text{ GeV}/c^2$	-1	$1/2$	τ	tau	0	0	1	Z	Z boson								
	$< 2.2 \text{ eV}/c^2$	0	$1/2$	ν_e	electron neutrino	$< 0.17 \text{ MeV}/c^2$	0	$1/2$	ν_μ	muon neutrino	$< 15.5 \text{ MeV}/c^2$	0	$1/2$	ν_τ	tau neutrino	$80.4 \text{ GeV}/c^2$	± 1	1	1	W	W boson							

- SM doesn't provide explanation for
 - Dark Matter and Dark Energy
 - Neutrino Masses
 - Matter-antimatter Asymmetry
 - Cannot explain observed lepton flavor universality violation (LFUV)
 - Fails to explain B-anomalies
 - Flavor Physics puzzles

STANDARD MODEL

- Standard Model Lagrangian, $\mathcal{L}_{SM} = \mathcal{L}_{K+G} + \mathcal{L}_H + \mathcal{L}_Y$

- After Symmetry Breaking, Fermion Mass term is

$$-\overline{\psi}_L^u \widehat{M}_1 \psi_R^u - \overline{\psi}_R^u \widehat{M}_1^\dagger \psi_L^u - \overline{\psi}_L^d \widehat{M}_2 \psi_R^d - \overline{\psi}_R^d \widehat{M}_2^\dagger \psi_L^d.$$

Where, $\widehat{M}_1 = \frac{v}{\sqrt{2}} \widehat{Y}_u$, $\widehat{M}_2 = \frac{v}{\sqrt{2}} \widehat{Y}_d$

- Rotation to Mass Eigenstates, $\psi^u = A_1 \psi^u$ and $\psi^d = A_2 \psi^d$ with $A_1^\dagger A_1 = A_2^\dagger A_2 = 1$

- Hence Mass Matrices are diagonalized, $A_1^\dagger \widehat{M}_1 A_1 = \begin{pmatrix} m_u & & \\ & m_c & \\ & & m_t \end{pmatrix}$

STANDARD MODEL

- CKM-Matrix is a unitary matrix, it connects the weak eigenstates with the mass eigenstates.

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = V_{\text{CKM}} \begin{pmatrix} d \\ s \\ b \end{pmatrix}, \quad V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

- CKM-Matrix allows non-diagonal couplings of the charged currents.
- $V_{\text{CKM}} = A_1^\dagger A_2$, $V_{\text{CKM}}^\dagger V_{\text{CKM}} = \mathbb{I}$
- The unitarity of the CKM matrix assures the absence of elementary FCNC vertices. Hence, No flavor changing neutral currents (FCNC) in the standard model at tree-level, (require Loop process).

RARE B-DECAYS

- Loop-level decays mediated by weak interaction. (Flavor Changing Neutral Currents)
- Transition strongly suppressed: (loops, CKM elements, sometimes GIM mechanism)

Q: How are rare decays of B mesons connected to NP (New Physics) ?

- FCNCs are forbidden at tree level due to GIM mechanism, but occur at loop level in the penguin and box diagrams, transitions like $b \rightarrow s$ and $s \rightarrow d$ are possible and they are perfect for indirect discovery: even small contributions have large effects on rare decays.
- The rare radiative decays like $B \rightarrow X_s \gamma$ and semi-leptonic decays $B \rightarrow X_s l^+ l^-$, more specifically $B \rightarrow K \nu \bar{\nu}$ are sensitive probes of new Physics.
- In the SM at the one-loop level they can be described by a set of basic effective vertices.
- Effective Hamiltonian

$$\mathcal{H}_{eff} = \frac{G_F}{\sqrt{2}} \sum_i V_{CKM}^i C_i O_i$$

EFFECTIVE VERTICES

- Using the Feynman rules, we can get effective vertices for a particular process, eventually leading to Wilson coefficients.

$$\bar{s} Z b = i\lambda_i \frac{G_F}{\sqrt{2}} \frac{e}{2\pi^2} M_Z^2 \frac{\cos \theta_W}{\sin \theta_W} C_0(x_i) \bar{s} \gamma^\mu (1 - \gamma^5) b$$

Where, $\lambda_i = V_{is}^* V_{ib}$

- Wilson Coefficient for $B \rightarrow X_s l^+ l^-$, are related to functions like $C_0(x_i)$, top quark is dominant $x_t = \frac{m_t^2}{M_W^2}$.

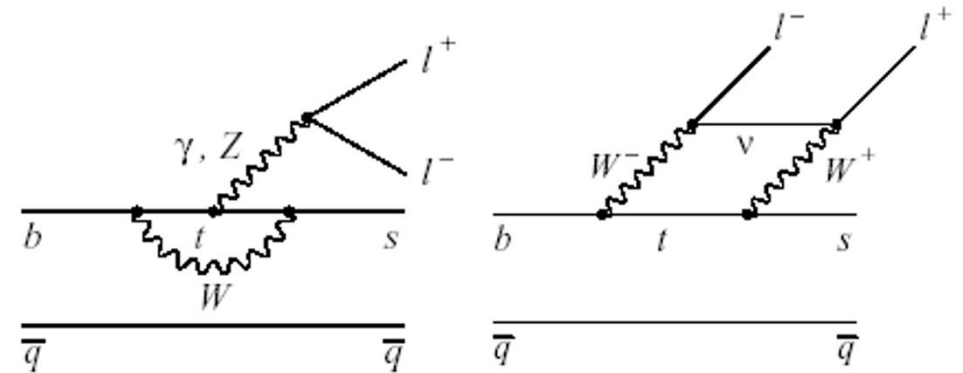
- $C_7 = -\frac{1}{2} D'_0(x_i)$

- $C_9 = \frac{(Y_0(x_i) - 4\sin^2 \theta_W Z_0(x_i))}{\sin^2 \theta_W}$

- $C_{10} = -\frac{Y_0(x_i)}{\sin^2 \theta_W}$

$Y_0(x_i) = C_0(x_i) - B_0(x_i)$

$Z_0(x_i) = C_0(x_i) - 1/4 D_0(x_i)$



PHYSICS BEYOND STANDARD MODEL

■ VECTOR LIKE QUARKS

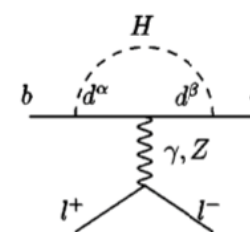
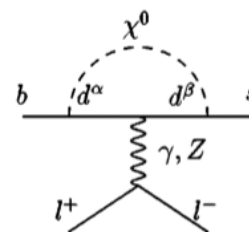
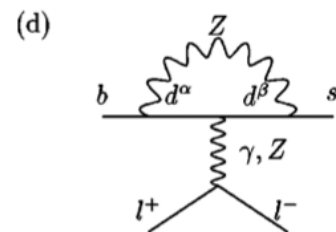
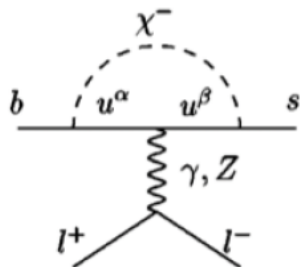
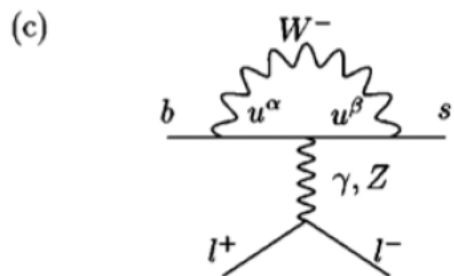
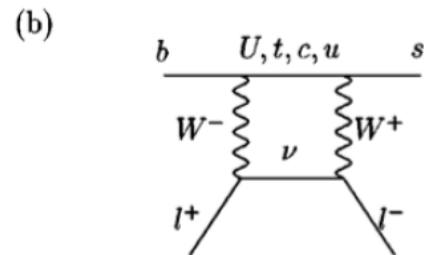
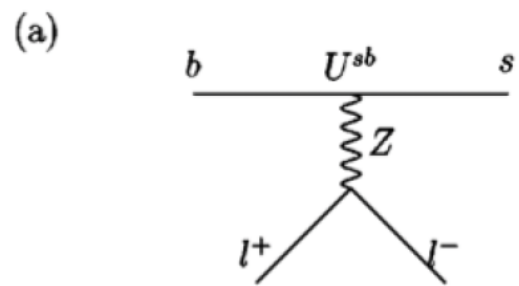
One New Physics Scenario is augmenting the Standard Model with additional down-type Vector Like Quarks, which leads to a non-unitary extended quark mixing matrix.

- VLQ-- A spin 1/2 fermion, color triplet (fundamental rep of SU(3)) and have higher masses than the Standard Model quarks, which makes them more difficult to detect at detectors.
- The same SM quantum numbers for L and R chiralities, and they are SU(2) singlet, leading to a non-unitary CKM matrix with a new parameter.

- $U^{\alpha\beta} = \sum_{i=u,c,t} A^{\alpha i} A^{\beta i*} \neq 0, \text{ For } \alpha \neq \beta$

$U^{\alpha\beta}$ would signal new physics and the presence of FCNC at the tree level, which can substantially modify the predictions of SM for the FCNC processes.

RARE B-DECAYS IN VQM



RARE B-DECAYS IN VQM

- Vector-like quark (VLQ) models significantly alter the decay $B \rightarrow K v \bar{v}$ through non unitarity of CKM matrix and penguin diagram contributions, modifying the effective Wilson coefficient C_L .

$$\mathcal{H}_{eff} = \frac{G_F}{\sqrt{2}} \sum_i V_{CKM}^i (C_L O_L + C_R O_R)$$

where $O_L = \frac{e^2}{16\pi^2} \gamma_\mu \bar{s} (\gamma_\mu P_L) b \bar{v} (1 - \gamma_5) v$ and $O_R = \frac{e^2}{16\pi^2} \gamma_\mu \bar{s} (\gamma_\mu P_R) b \bar{v} (1 - \gamma_5) v$

- Using the results coming from effective Hamiltonian, while considering extra generation of quark (VLQ), we have calculated the effective vertices for the one-loop level calculations of, $B \rightarrow K v \bar{v}$.
- Branching Ratio $B \rightarrow K v \bar{v}$, including the additional diagrams (tree-level and Higgs loops) using form factors from LCSR,
- $f(k) = \frac{0.162}{1 - SB(\frac{M_B}{5.41})^2} + \frac{0.173}{(1 - SB(\frac{M_B}{5.41})^2)^2}$, $\lambda = SB^2 + (\frac{m_k}{M_B})^4 + 1 - 2 \left(SB(\frac{m_k}{M_B})^2 + (\frac{m_k}{M_B})^2 + SB \right)$
- SB varies from [0,0.82]; we get the Total branching ratio by integrating over SB,

$$BR(B \rightarrow K v \bar{v}) = \frac{G_F^2 \alpha^2 M_B^2}{256\pi^2 \sin^4(\theta_W)} X'^2 \tau_B |V_{tb} V_{ts}^*|^2 \int \lambda^{3/2} f^2(k) dSB$$

- Here X' contains the New Physics parameter U_{sb} ,

$$X' = X_{SM} + \frac{U_{sb}}{V_{ts}^8 V_{tb}} \left\{ \begin{array}{l} \frac{\pi}{\alpha} \sin^2 \theta_W + \frac{1}{48} \frac{M_D^2}{M_W^2} \sin^2 \theta_W \left(\left(\frac{-2}{\epsilon} - \frac{1}{2} + \frac{x_1^2 \log(x_1)}{(1-x_1)^2} + \frac{x_1}{(1-x_1)} \right) + \left(\frac{-2}{\epsilon} - \frac{1}{2} + \frac{x_2^2 \log(x_2)}{(1-x_2)^2} + \frac{x_2}{(1-x_2)} \right) \right) \\ + \left(\frac{-1}{2} + \frac{1}{3} \sin^2 \theta_W \right) \frac{M_D^2}{M_W^2} \left(\left(\frac{1}{\epsilon} + \frac{3}{4} - \frac{x_1^2 \log(x_1)}{2(1-x_1)^2} - \frac{1}{2(1-x_1)} \right) + \left(\frac{1}{\epsilon} + \frac{3}{4} - \frac{x_2^2 \log(x_2)}{2(1-x_2)^2} - \frac{1}{2(1-x_2)} \right) \right) \end{array} \right\}$$

NEW PHYSICS PARAMETERS

- For numerical results we first constraint the phase space of the New Physics parameter by using $B_s \rightarrow \mu^+ \mu^-$ and $B \rightarrow X_s \mu^+ \mu^-$.
- Modified Branching Ratio: $BR^{NP}(B_s \rightarrow \mu^+ \mu^-) = BR^{SM} \left| 1 + \frac{C_{10}^{NP}}{C_{10}^{SM}} \right|^2$, with New Physics Parameters r_{sb} and θ_{sb} ,
- $r_{sb} = \left| \frac{U_{sb}}{V_{tb}V_{ts}^*} \right|, \theta_{sb} = \text{arg} \left| \frac{U_{sb}}{V_{tb}V_{ts}^*} \right|$
- Using the C_{10}^{NP} ,
- $$C_{10}^{NP} = C_{10}^{SM} - \frac{U_{sb}}{V_{ts}^8 V_{tb}} \left\{ \begin{array}{l} \frac{\pi}{\alpha} + \frac{1}{48} \frac{M_D^2}{M_W^2} \left(\left(\frac{-2}{\epsilon} - \frac{1}{2} + \frac{x_1^2 \log(x_1)}{(1-x_1)^2} + \frac{x_1}{(1-x_1)} \right) + \left(\frac{-2}{\epsilon} - \frac{1}{2} + \frac{x_2^2 \log(x_2)}{(1-x_2)^2} + \frac{x_2}{(1-x_2)} \right) \right) \\ + \left(\frac{-1}{2} + \frac{1}{3} \sin^2 \theta_W \right) \frac{M_D^2}{M_W^2} \left(\left(\frac{1}{\epsilon} + \frac{3}{4} - \frac{x_1^2 \log(x_1)}{2(1-x_1)^2} - \frac{1}{2(1-x_1)} \right) + \left(\frac{1}{\epsilon} + \frac{3}{4} - \frac{x_2^2 \log(x_2)}{2(1-x_2)^2} - \frac{1}{2(1-x_2)} \right) \right) \end{array} \right\}$$

CONSTRAINTS ON NEW PHYSICS PARAMETERS

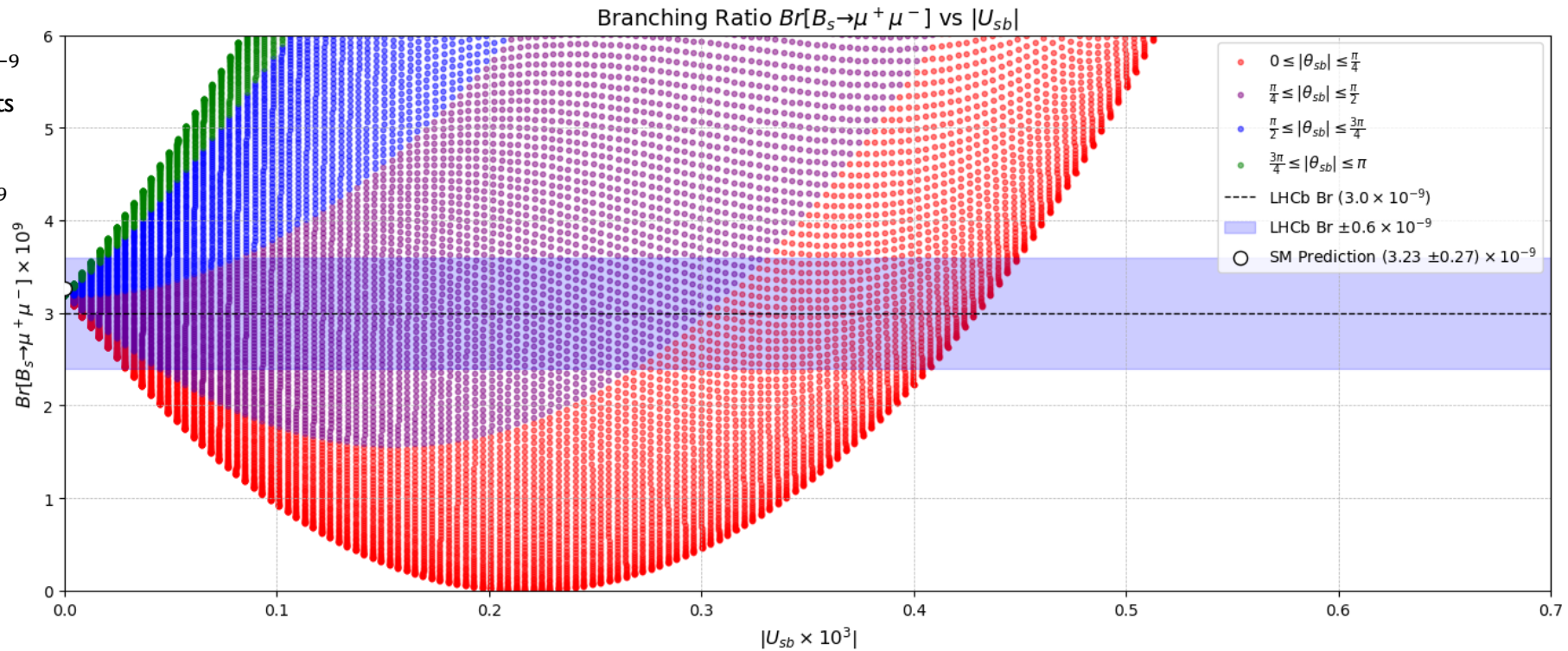
The Standard Model

$$BR(Bs \rightarrow \mu^+ \mu^-) = (3.23 \pm 0.27) \times 10^{-9}$$

The experimental results from LHCb

$$BR(Bs \rightarrow \mu^+ \mu^-) = (3.0 \pm 0.6) \times 10^{-9}$$

$$U_{sb} = |U_{sb}| e^{i\theta_{sb}}$$



BRANCHING RATIO ENHANCEMENT

The Standard Model

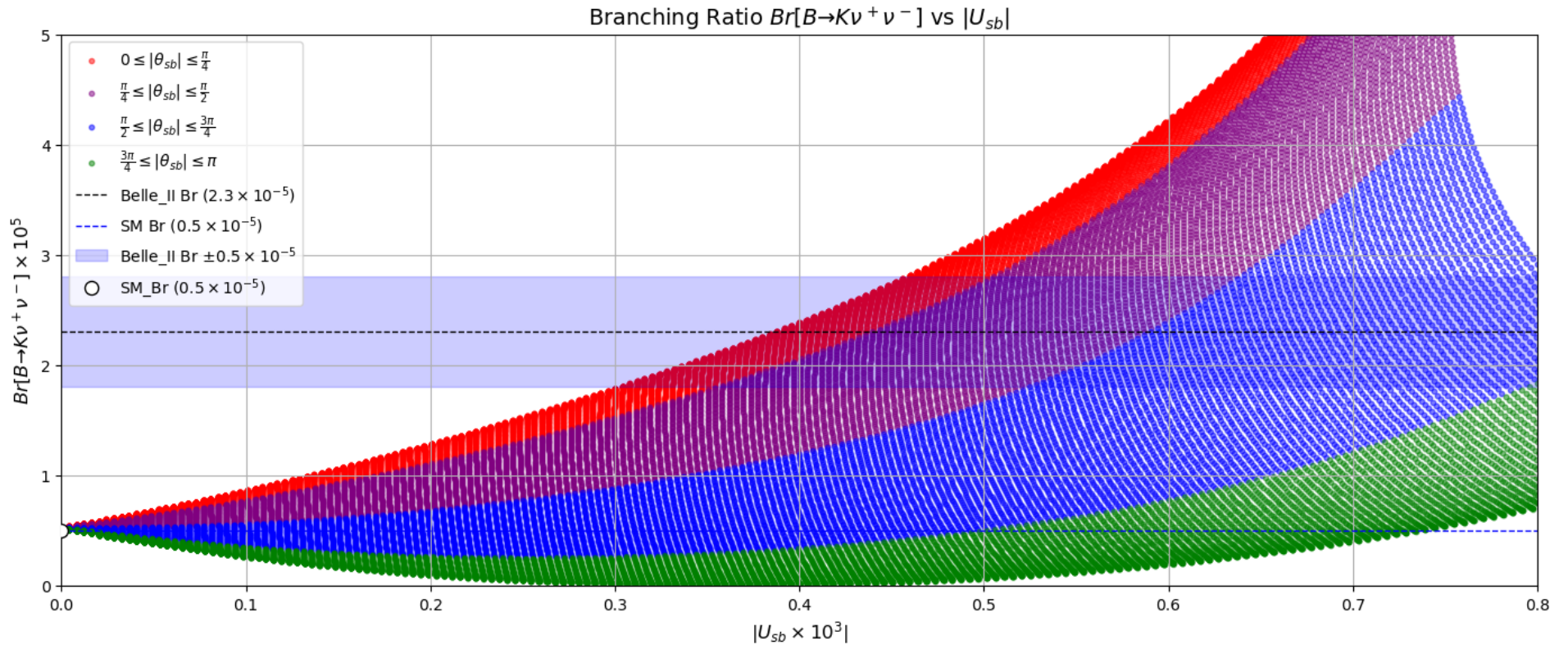
$$BR(B \rightarrow K \nu \nu) = (0.5) \times 10^{-5}$$

Whereas the experimental results from Belle-II

$$BR(B \rightarrow K \nu \nu) = (2.3 \pm 0.7) \times 10^{-5}$$

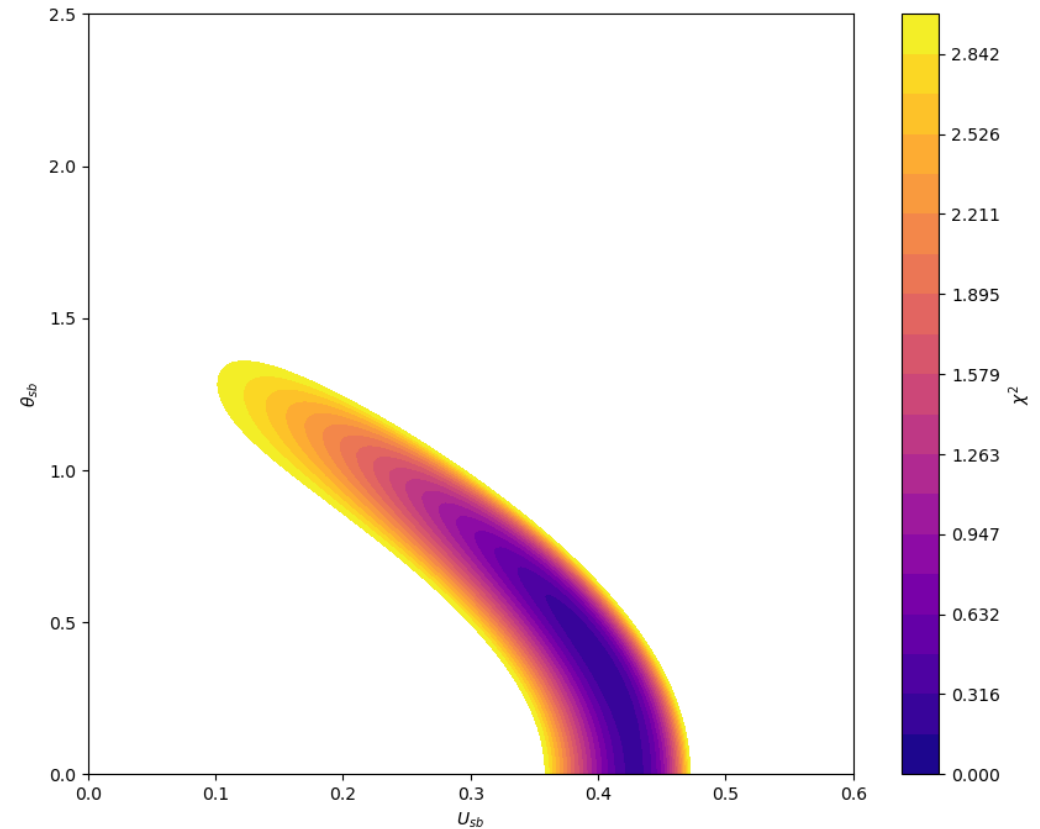
Which lies 2.7σ above Standard Model.

Addition of Vector like quarks has enhanced the Branching ratio $BR(B \rightarrow K \nu \nu)$.



CHI-SQUARED ANALYSIS

The Numerical Evaluation and χ^2 plots gives significant enhancement in the Branching ratio of $B \rightarrow K\nu\bar{\nu}$ indicating that Vector Like Quark Model is promising New Physics candidate Beyond Standard Model.



CONCLUSION

- Rare B decays continue to be valuable probes of physics beyond the SM.
- The presence of VLQ has expanded the phase space of $Bs \rightarrow \mu^+ \mu^-$ for $M_D < 1.5$ TeV.
- One cannot neglect the effect when the VLQ mass is much heavier than the EW scale. When $M_D/M_W \sim 10$, may expect about 10% corrections to the Wilson coefficients.
- Numerical results validate theoretical expectations and VLQs provide viable explanations for observed tensions in $B \rightarrow K\nu\bar{\nu}$, large enhancement is possible which can explain the B-Anomalies.
- This model can modify angular observables, and other characteristics of the rare B-decay processes.
- Future data from LHCb and Belle-II will further test these models

REFERENCES

1. M. R. Ahmady, M. Nagashima and A. Sugamoto, "Inclusive dileptonic rare B decays with an extra generation of vector - like quarks," Phys. Rev. D 64, 054011 (2001), [arXiv:hep-ph/0105049 [hep-ph]]
2. A. K. Alok and S. Gangal, " $b \rightarrow s$ Decays in a model with Z-mediated flavor changing neutral current," Phys. Rev. D, 114009 (2012), doi:10.1103/PhysRevD.86.114009, [arXiv:1209.1987 [hep-ph]]
3. A. J. Buras, "Weak Hamiltonian, CP violation and rare decays," <https://arxiv.org/abs/hep-ph/9806471>
4. K.G. Wilson, Phys. Rev. 179 (1969) 1499. Wilson, K. G., Zimmermann, W. (1972). Comm. Math. Phys. 24, 87.
5. T. Morozumi, Y. Shimizu, S. Takahashi and H. Umeeda, "Effective theory analysis for vector-like quark model," PTEP 2018, no.4, 043B10 (2018) doi:10.1093/ptep/pty042 <https://arxiv.org/pdf/1801.05268>
6. F. Abudinén et al. [Belle-II], "Search for $B^+ \rightarrow K^+ \nu \bar{\nu}$ Decays Using an Inclusive Tagging Method at Belle II," Phys. Rev. Lett. 127, no.18, 181802 (2021) doi:10.1103/PhysRevLett.127.181802 <https://arxiv.org/abs/2104.12624>

Thank You!